

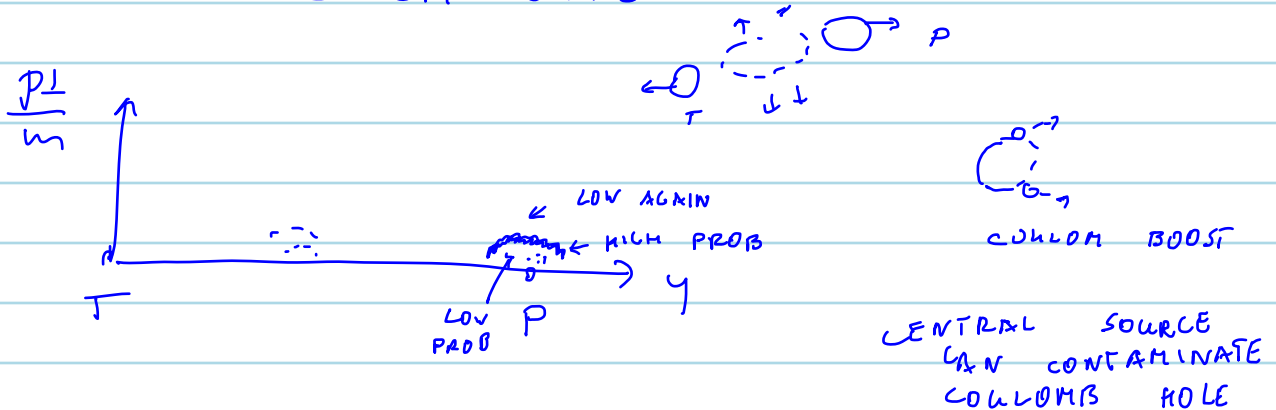
CORRELATIONS

SINGLE - PARTICLE OBSERVABLES

SO-FAR - SINGLE - PARTICLE DISTRIBUTIONS YIELDS

MUTUAL

? INFLUENCE OF EMITTED PARTICLES ON EACH OTHER



CORRELATION FUNCTION

$$C(\vec{u}_1, \vec{u}_2) = \frac{P_2(\vec{u}_1, \vec{u}_2)}{P_1(\vec{u}_1) \cdot P(\vec{u}_2)}$$

IF EMISSION UNCORRELATED $P_2(\vec{u}_1, \vec{u}_2) = P_1(\vec{u}_1) \cdot P_2(\vec{u}_2)$

$C(\vec{u}_1, \vec{u}_2) = 1$

$C \rightarrow 1$ WHEN $|\vec{u}_1 - \vec{u}_2|$ LARGE

V. OFTEN DEVIATIONS FROM 1 OCCUR WHEN $|\vec{u}_1 - \vec{u}_2| \rightarrow 0$

$C(v_{red})$

GLASMACHER

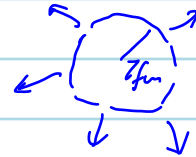
Ar + Au

AT 50 MeV/nucl

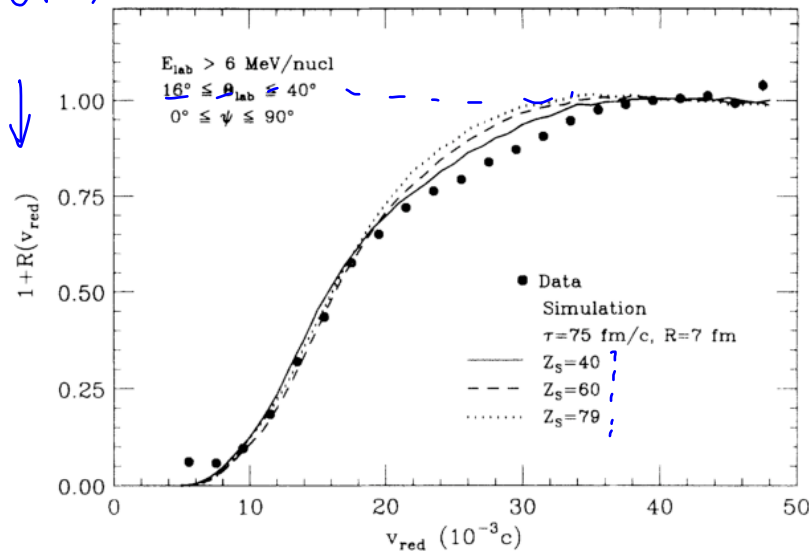
$4 \leq Z_{frag} \leq 9$

INTERMEDIATE

MASS FRAGMENTS



ISOTROPIC
EMISSION



$$e^{-t/\tau}$$

$$P(\vec{u}_1, \vec{u}_2) = \int d^3 r_1^s d^3 r_2^s d^3 u_1^s d^3 u_2^s$$

$$P_{\text{SOURCE}}(r_1^s, r_2^s, u_1^s, u_2^s)$$

$$\text{TRANSF}(r_1^s, r_2^s, u_1^s, u_2^s \rightarrow \vec{u}_1, \vec{u}_2)$$

CLASSICAL EQ OF MOTION

? ONLY INFLUENCE OF 2 FRAGMENTS

TRANSF ACCOUNTED FOR BY SCHRÖDINGER EQ. IF ONLY IMPACT OF ONE FRAGMENT OR ANOTHER THEN 2-BODY SCHR. EQ. BUT EFFECTIVELY 1-BODY

$$\text{IF } P_{\text{emission}}(u_1^s, u_2^s) \approx P_{\text{emission}}(V)$$

$$V \approx u_1^s \approx u_2^s$$

$$P(\vec{u}_1, \vec{u}_2) = \int d^3r_1 \int d^3r_2 P_{\text{emission}}(r_1^s, r_2^s, V)$$

← INFO. ON SPATIAL EXTENT OF REACTION

DATA →

$$|\Psi_{\vec{u}_1, \vec{u}_2}(\vec{r}_1^s, \vec{r}_2^s)|^2$$

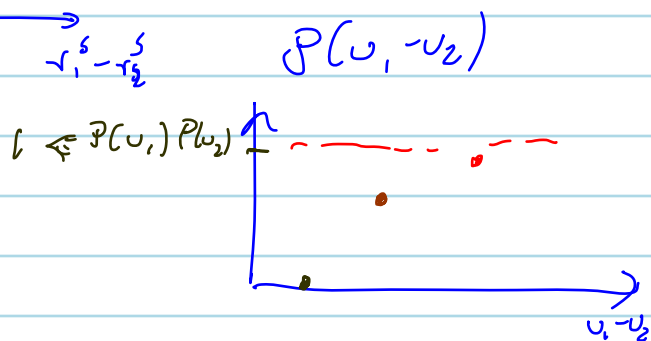
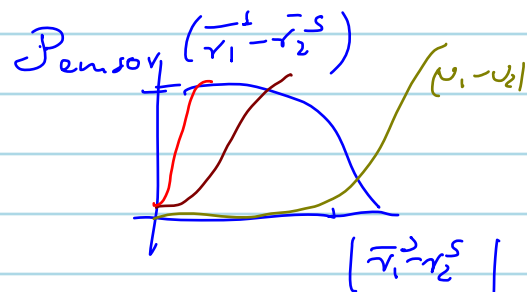
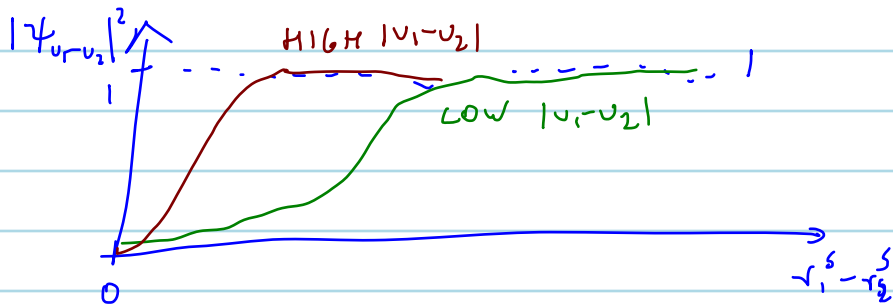
← YOU KNOW HOW TO CALCULATE

AT LARGE

$$|\vec{u}_1 - \vec{u}_2| \quad |\Psi|^2 \approx 1$$

↑ SCATTERING WAVE FUNCTION

E.C. COLUMB REPULSION



GAIN IN TRANSITION

FROM CLASSICAL TO QUANTAL

DESCRIPTION: ABILITY TO ACCOUNT

PROPERLY FOR STRONG INTERACTIONS,

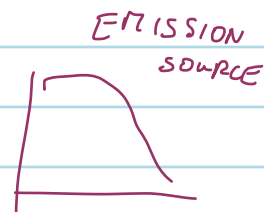
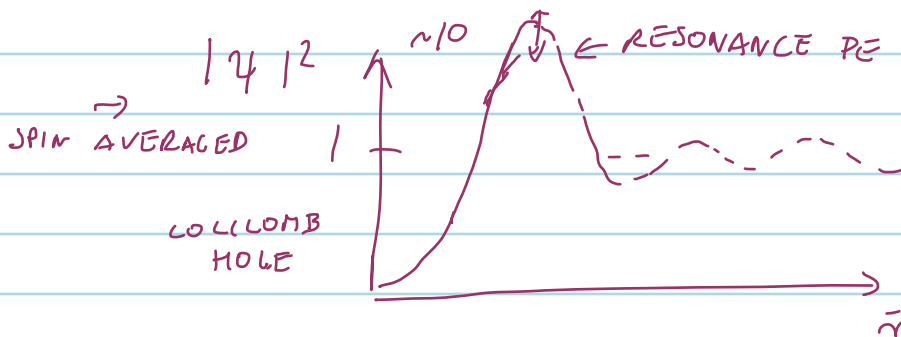
RESONANCE PHENOMENA ETC

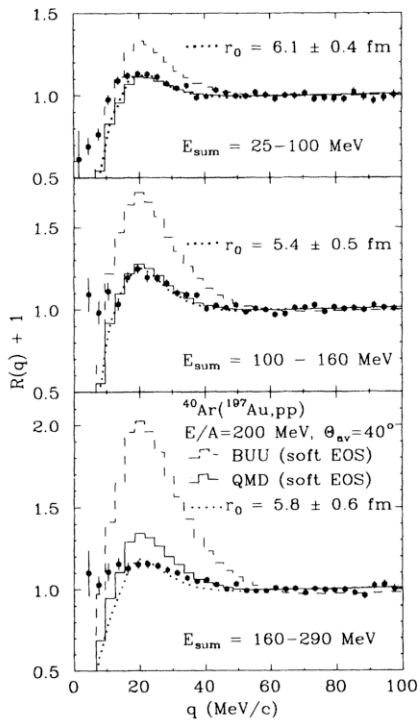
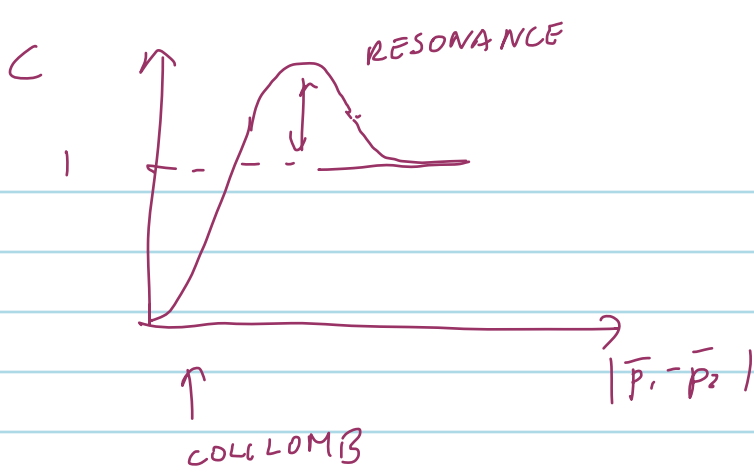
2 CORRELATIONS OF PROTONS WITH EACH OTHER:

- COLUMB REPULSION

- STRONG ATTRACTION W/ RESONANCE

- INTERFERENCE





KUNDE

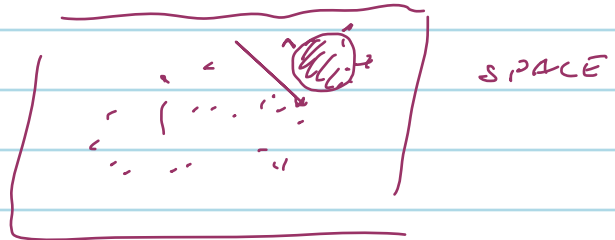
$A_5 + A_5$ 200 MeV/nucl

POINTS DATA

$$P_{em}(r_i^s) \propto \exp\left(-\frac{r_i^{s^2}}{r_0^2}\right)$$

GAUSSIAN EMISSION

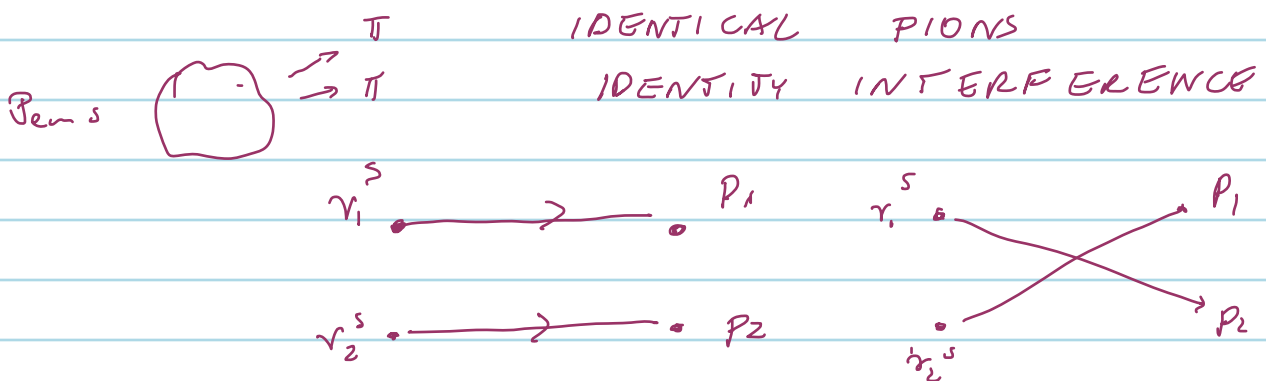
SHAPE FOR EACH PROTON



↑ ANALYSIS MISSES BACKGROUND!

EASY CASE OF CORRELATION

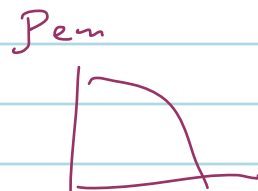
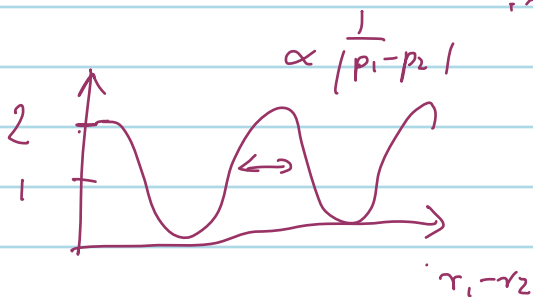
INTERFERENCE IN π EMISSION



$$\begin{aligned}
|\Psi_{\vec{p}_1, \vec{p}_2}(\vec{r}_1^s, \vec{r}_2^s)|^2 &= \left| \frac{1}{\sqrt{2}} \left(e^{i\vec{p}_1 \cdot \vec{r}_1^s} e^{i\vec{p}_2 \cdot \vec{r}_2^s} + e^{i\vec{p}_2 \cdot \vec{r}_1^s} e^{i\vec{p}_1 \cdot \vec{r}_2^s} \right) \right|^2 \\
&= \frac{1}{2} \left(1 + 1 + e^{i\vec{p}_1 \cdot \vec{r}_1^s} e^{i\vec{p}_2 \cdot \vec{r}_2^s} + e^{-i\vec{p}_2 \cdot \vec{r}_1^s} e^{-i\vec{p}_1 \cdot \vec{r}_2^s} \right. \\
&\quad \left. + e^{i\vec{p}_2 \cdot \vec{r}_1^s} e^{i\vec{p}_1 \cdot \vec{r}_2^s} + e^{-i\vec{p}_1 \cdot \vec{r}_1^s} e^{-i\vec{p}_2 \cdot \vec{r}_2^s} \right) \\
&= \frac{1}{2} \left(2 + e^{i\vec{p}_1 \cdot (\vec{r}_1^s - \vec{r}_2^s) - i\vec{p}_2 \cdot (\vec{r}_1^s - \vec{r}_2^s)} + e^{i\vec{p}_2 \cdot (\vec{r}_1 - \vec{r}_2) - i\vec{p}_1 \cdot (\vec{r}_1 - \vec{r}_2)} \right) \\
&= \frac{1}{2} \left(2 + e^{i(\vec{p}_1 - \vec{p}_2) \cdot (\vec{r}_1 - \vec{r}_2)} + e^{-i(\vec{p}_1 - \vec{p}_2) \cdot (\vec{r}_1 - \vec{r}_2)} \right) \\
&= 1 + 2 \cos \left((\vec{p}_1 - \vec{p}_2) \cdot (\vec{r}_1 - \vec{r}_2) \right)
\end{aligned}$$

$$P(\vec{p}_1, \vec{p}_2) = \int d^3 r_1 d^3 r_2 P_{em}(\vec{r}_1, \vec{r}_2)$$

$$\left(1 + \cos \left((\vec{p}_1 - \vec{p}_2) \cdot (\vec{r}_1 - \vec{r}_2) \right) \right)$$



$$d^3 r_1 d^3 r_2 = d^3 (\vec{r}_1 - \vec{r}_2) d^3 \left(\frac{\vec{r}_1 + \vec{r}_2}{2} \right)$$

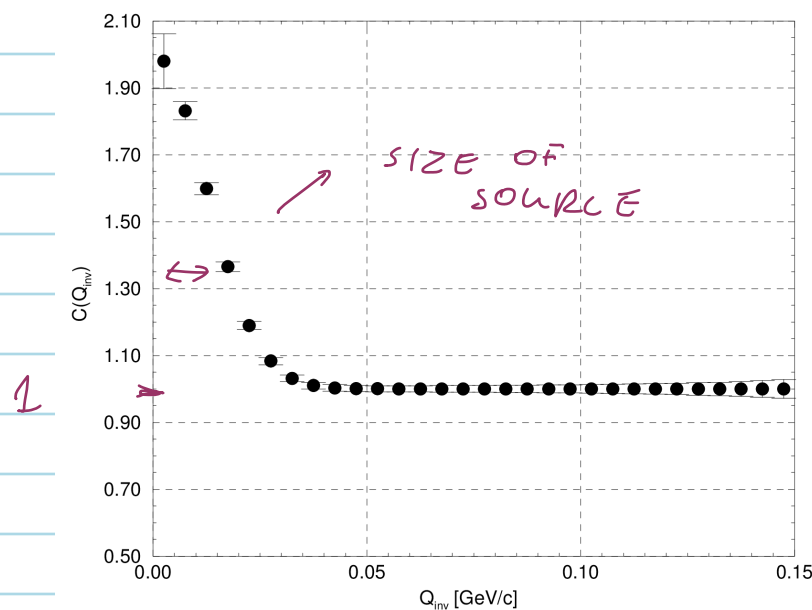
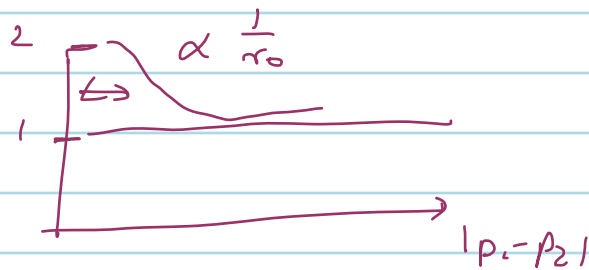
$$P(p_1, p_2) = \int d^3(r_1 - r_2) P_{em}(\bar{r}_1 - \bar{r}_2) \left(1 + \cos\left(\frac{(\vec{p}_1 - \vec{p}_2) \cdot (\bar{r}_1 - \bar{r}_2)}{r_0}\right) \right)$$

$$P_{em}(\bar{r}_1) \propto \exp\left(-\frac{r_1^2}{r_0^2}\right)$$

$$\int d^3\left(\frac{r_1 + r_2}{2}\right) P_{em}(\bar{r}_1) P_{em}(\bar{r}_2) \propto \exp\left(-\frac{(r_1 - r_2)^2}{2r_0^2}\right)$$

$$P(p_1, p_2) \propto \int d^3(r_1 - r_2) \exp\left(-\frac{(r_1 - r_2)^2}{2r_0^2}\right) \left(1 + \cos\left(\frac{(\vec{p}_1 - \vec{p}_2) \cdot (\bar{r}_1 - \bar{r}_2)}{r_0}\right) \right)$$

$$P(p_1, p_2) \propto 1 + \exp\left(-\frac{(\vec{p}_1 - \vec{p}_2)^2 r_0^2}{2}\right)$$



MORE COMPACT SOURCES
YIELD
STRONGER
CORRELATIONS
AT SMALL
RELATIVE
VELOCITIES

→ WAY TO
DETERMINE
SIZE OF
THE EMISSION ZONE

AZIMUTHAL OR REACTION-PLANE CORRELATIONS

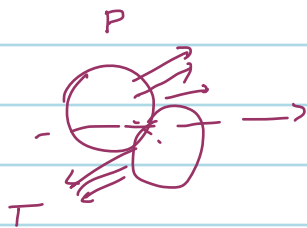
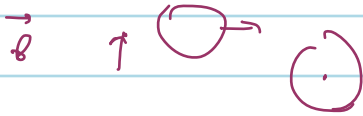


REACTION PLANE

B

\vec{Q}

HAS AZIMUTHAL DIRECTION



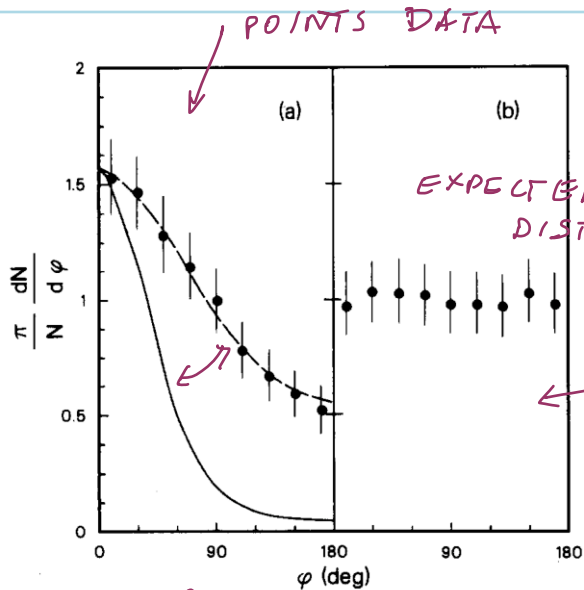
$$\vec{Q}^\perp = \sum_{y \rightarrow y_{cm}} \vec{p}_\perp^v - \sum_{y \leftarrow y_{cm}} \vec{p}_\perp^v$$

? LOOK FOR ORIENTATION OF REACTION PLANE?

ANY SIGNIFICANCE TO \vec{Q}^\perp

MANY PICLES

TAKE EVENT & SPLIT INTO 2: I & II
 \vec{Q}_I^\perp \vec{Q}_{II}^\perp



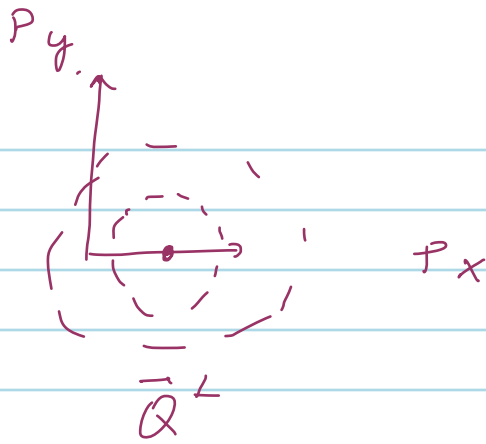
Ar + KCl SEMICENTRAL EVENTS

1.8 GeV/u

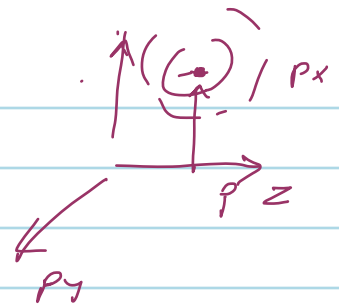
FROM EVENT MIXING

$$\vec{Q} = \vec{Q}_I + \vec{Q}_{II}$$

\vec{Q}_I \vec{Q}_{II} DISTRIBUTION IN RELATIVE AZIMUTHAL ANGLE

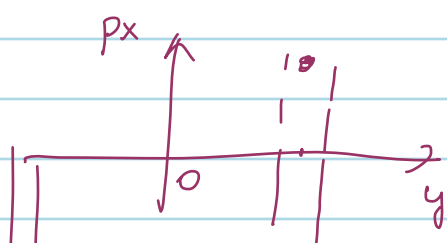


FORWARD y



ESTIMATES DIRECTION OF REACTION PLANE

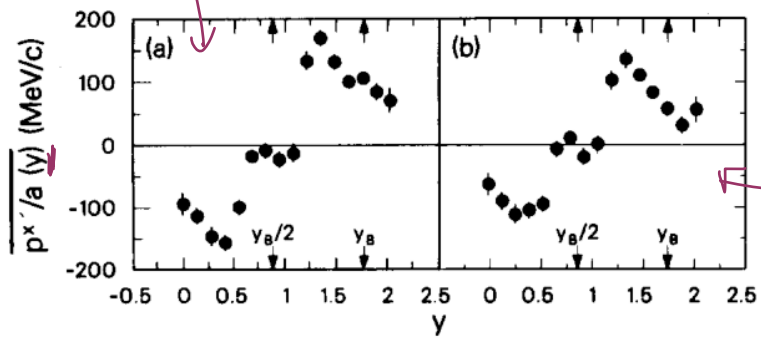
$$\langle p^x(y) \rangle = \vec{p}^\perp \cdot \frac{\vec{Q}^\perp}{|\vec{Q}^\perp|}$$



$$\langle p^x(y) \rangle = \vec{p}^\perp \cdot \frac{\vec{Q}^\perp}{|\vec{Q}^\perp|}$$

Ar + KCl
1.8 GeV/u

DATA



MIXED EVENTS

$$w_\nu = \pm 1$$

AUTOCORRELATION!

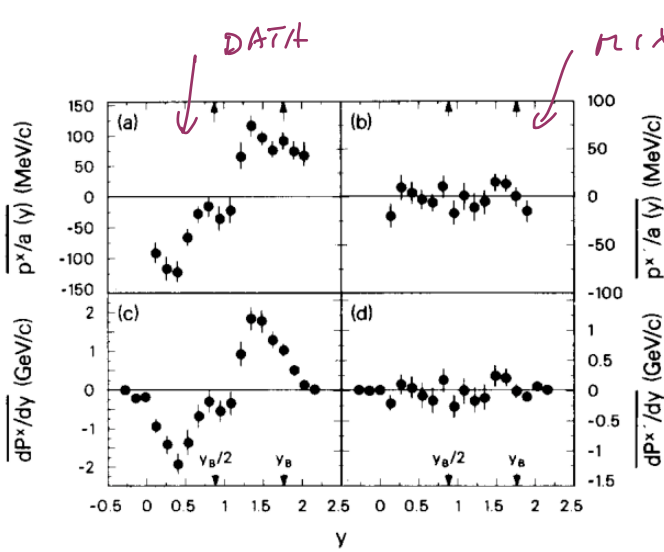
$$\left\langle \vec{p}_\mu^\perp \cdot \frac{\sum_\nu w_\nu \vec{p}_\nu^\perp}{\left| \sum_\nu w_\nu \vec{p}_\nu^\perp \right|} \right\rangle$$

$$= \left\langle \vec{p}_\mu^\perp \cdot \frac{w_\mu \vec{p}_\mu^\perp}{\left| \sum_\nu w_\nu \vec{p}_\nu^\perp \right|} \right\rangle + \left\langle \vec{p}_\mu^\perp \cdot \frac{\sum_{\nu \neq \mu} w_\nu \vec{p}_\nu^\perp}{\left| \sum_\nu w_\nu \vec{p}_\nu^\perp \right|} \right\rangle$$

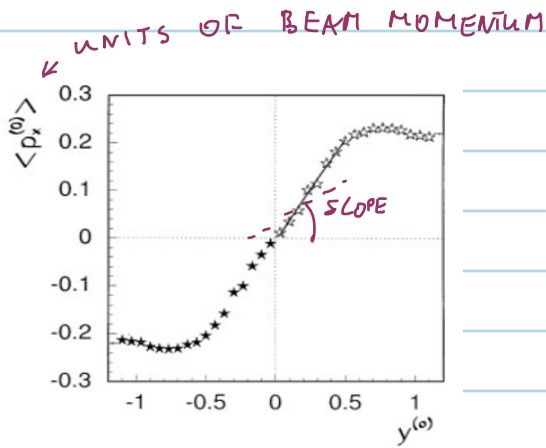
$$= w_\mu \left\langle \frac{p_\mu^2}{\left| \sum_\nu w_\nu \vec{p}_\nu^\perp \right|^2} \right\rangle \approx 0 = \text{SOMETHING POSITIVE} \cdot w_\mu$$

$$\vec{Q}_\mu^\perp = \sum_{\nu \neq \mu} w_\nu \vec{p}_\nu^\perp$$

$w_\nu = \pm 1$ DEPENDING ON y_ν



$\vec{Q} \perp$
 DOES NOT
 POINT EXACTLY
 ALONG THE
 REACTION
 PLANE
 REDUCING ON
 AVERAGE THE
 MAGNITUDE OF \vec{p}^x



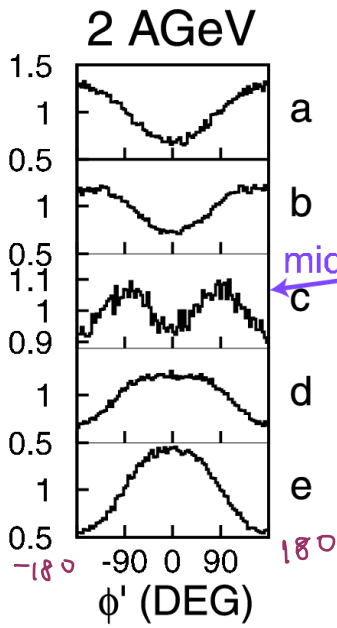
FOP1

Au + Au

$$F = \frac{d\langle p^x \rangle}{dy}$$

SLOPE

UNITS OF
 BEAM RAPIDITY



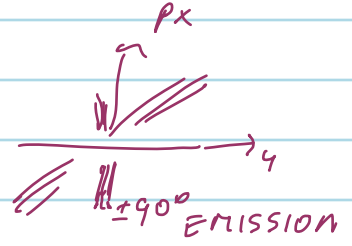
$v_1 < 0$

$v_2 < 0$

$v_1 > 0$

$v_n(p_L)$

← TARGET RAPIDITY REGION



← PROJECTILE RAP

REGION

$$\langle \cos n\phi \rangle = v_n$$