

Soft Stuff, Heavy Ions and Event Generators IV



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Outline of Lectures

- ▶ Lecture I: Basics of Monte Carlo methods, the event generator strategy, matrix elements, LO/NLO, ...
- ▶ Lecture II: Parton showers, initial/final state, (matching/merging), hadronization, decays. ...
- ▶ Lecture III: Minimum bias, multi-parton interactions, pile-up, summary of general purpose event generators, ...
- ▶ Lecture IV: Protons vs. heavy ions, Glauber calculations, initial/final-state interactions, ...

Buckley et al. (MCnet collaboration), *Phys. Rep.* **504** (2011) 145.



Outline of Lecture IV

The Glauber formalism

- Distributing nucleons in a nuclei
- Interactions between nucleons
- The importance of fluctuations
- The standard Glauber implementations

The Initial State

- Color Glass Condensate
- The DIPSY model

The Final State

- Quark-Gluon Plasma
- Wounded Nucleons

Heavy Ions in PYTHIA8

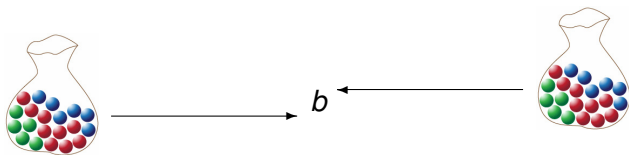
- Angantyr
- Comparison to data

String Interactions



The Glauber formalism

- ▶ How do we model the geometrical distribution of nucleons in colliding nuclei?
- ▶ How do we determine which nucleon interacts with which nucleon?
- ▶ How do they interact?



Distributing nucleons in a nuclei

There are advanced models for the shell-structure of nuclei — we will not be that advanced.

Assume a simple density of nucleons based on the (spherically symmetric) Woods–Saxon potential

$$\rho(r) = \frac{\rho_0(1 + wr^2/R^2)}{1 + \exp((r - R)/a)}$$

R is the radius of the nucleus

a is the *skin width*

w can give a varying density but is typically = 0



For a nucleus (Z, A), we simply generate A nucleon positions randomly according to

$$P(\vec{r}_i) = \rho(r_i) d^3\vec{r}_i$$

The Woods–Saxon parameters are tuned to measurements of (low energy) charge distributions assuming some charge distribution of each nucleon (proton).

We normally assume iso-spin invariance ($p \approx n$).

There are absolutely no correlations between the nucleons.

What happens if two nucleons end up in the same place?



We can get some correlations if we assume that nucleons have a **hard core**, R_h , and require $\Delta r_{ij} > 2R_h$

If you generate a nucleon which is too close to a previously generated nucleon you could either

- ▶ generate a new position for the last one (efficient, but may give a bias)
- ▶ throw away everything and start over (inefficient, unbiased)



There are many implementations of this, and most experiments have their own. Typical parameters for $A > 16$ are (from the GLISSANDO program):

R (fm)	a	w	R_h
$(1.120A^{1/3} - 0.860A^{-1/3})$	0.540	0	0
$(1.100A^{1/3} - 0.656A^{-1/3})$	0.459	0	0.45

[nucl-th/0710.5731, nucl-th/1310.5475]



We can estimate the AA cross section assuming the nuclei are like black disks,

$$\sigma^{AA} = \int_{-\infty}^{\infty} d^2\vec{b} \frac{d\sigma^{AA}(b)}{d^2\vec{b}} = 4\pi R^2$$

where

$$\frac{d\sigma^{AA}(b)}{d^2\vec{b}} = \begin{cases} 1 & : \quad b < 2R \\ 0 & : \quad b > 2R \end{cases}$$



We can also look at the positions of the individual nucleons:

$$\frac{d\sigma^{AA}(b)}{d^2\vec{b}} = 1 - \prod_{i,j} \int d^2\vec{r}_i d^2\vec{r}_j \left(1 - \frac{d\sigma^{NN}(b_{ij})}{d^2\vec{b}} \right) \rho(\vec{r}_i) \rho(\vec{r}_j)$$

where $b_{ij} = \left| \vec{b} + \vec{r}_i - \vec{r}_j \right|$.

But we have to think about which cross section we are talking about. Total? Non-diffractive? Inelastic?



Interactions between nucleons

Let's assume that a projectile with some kind of internal structure interacts with a structureless target. The projectile can have different mass-eigenstates, Ψ_i , and these can be different from the eigenstates of the (diffractive) interaction, Φ_k .

$$\Psi_i = \sum_k c_{ik} \Phi_k \quad \text{with} \quad \Psi_0 = \Psi_{in}.$$

With an elastic amplitude T_k for each interaction eigenstate we get the elastic cross section for the incoming state

$$\frac{d\sigma_{el}(b)}{d^2\vec{b}} = |\langle \Psi_0 | T | \Psi_0 \rangle|^2 = \left(\sum_k |c_{0k}|^2 T_k \right)^2 = \langle T \rangle^2.$$



For a completely black target and projectile, we know from the optical theorem that the elastic cross section is the same as the absorptive cross section and

$$\sigma_{el} = \sigma_{abs} = \sigma_{tot}/2$$

but with substructure and fluctuations we have also diffractive scattering with the amplitude

$$\langle \Psi_i | T | \Psi_0 \rangle = \sum_k c_{ik} T_k c_{0k}^*$$

and

$$\frac{d\sigma_{diff}(b)}{d^2\vec{b}} = \sum_i \langle \Psi_0 | T | \Psi_i \rangle \langle \Psi_i | T | \Psi_0 \rangle = \langle T^2 \rangle.$$



The importance of fluctuations

We see now that diffractive excitation to higher mass eigenstates is given by the fluctuations

$$\frac{d\sigma_{\text{dex}}(b)}{d^2\vec{b}} = \frac{d\sigma_{\text{diff}}(b)}{d^2\vec{b}} - \frac{d\sigma_{\text{el}}(b)}{d^2\vec{b}} = \langle T^2(b) \rangle - \langle T(b) \rangle^2$$

When looking at AA interactions we may assume that the state of each nucleon is frozen during the interaction according to the eikonal approximation.

We also assume the elastic nucleon scattering amplitude is purely imaginary and $T(b) \equiv -iA(b)$ giving $0 \leq T \leq 1$ from unitarity.



We can now also write down the total and absorptive (aka. non-diffractive) cross section, and we can look at the situation where both the projectile and target nucleon has a sub-structure:

$$\frac{d\sigma_{\text{tot}}^{\text{NN}}(b)}{d^2\vec{b}} = 2\langle T(b) \rangle$$

$$\frac{d\sigma_{\text{abs}}^{\text{NN}}(b)}{d^2\vec{b}} = 2\langle T(b) \rangle - \langle T^2(b) \rangle$$

$$\frac{d\sigma_{\text{el}}^{\text{NN}}(b)}{d^2\vec{b}} = \langle T(b) \rangle^2$$

$$\frac{d\sigma_{\text{dex}}^{\text{NN}}(b)}{d^2\vec{b}} = \langle T^2(b) \rangle - \langle T(b) \rangle^2$$



We can also divide the diffractive excitation depending on whether the target or projective nucleon is excited.

$$\frac{d\sigma_{Dp}^{NN}(b)}{d^2\vec{b}} = \langle\langle T(b)\rangle_t^2\rangle_p - \langle\langle T(b)\rangle_t\rangle_p^2$$

$$\frac{d\sigma_{Dt}^{NN}(b)}{d^2\vec{b}} = \langle\langle T(b)\rangle_t^2\rangle_p - \langle\langle T(b)\rangle_p\rangle_t^2$$

$$\frac{d\sigma_{DD}^{NN}(b)}{d^2\vec{b}} = \langle\langle T(b)^2\rangle_t\rangle_p - \langle\langle T(b)\rangle_p^2\rangle_t - \langle\langle T(b)\rangle_t^2\rangle_p + \langle\langle T(b)\rangle_t\rangle_p^2$$



We note in particular that the probability of a target nucleon being **wounded** is given by

$$\begin{aligned}
 \frac{d\sigma_{\text{Wt}}^{\text{NN}}(b)}{d^2\vec{b}} &= \frac{d\sigma_{\text{abs}}^{\text{NN}}(b)}{d^2\vec{b}} + \frac{d\sigma_{\text{DD}}^{\text{NN}}(b)}{d^2\vec{b}} + \frac{d\sigma_{\text{Dt}}^{\text{NN}}(b)}{d^2\vec{b}} \\
 &= \frac{d\sigma_{\text{tot}}^{\text{NN}}(b)}{d^2\vec{b}} - \frac{d\sigma_{\text{el}}^{\text{NN}}(b)}{d^2\vec{b}} - \frac{d\sigma_{\text{Dp}}^{\text{NN}}(b)}{d^2\vec{b}} \\
 &= 2\langle T(b) \rangle_{tp} - \langle \langle T(b) \rangle_t^2 \rangle_p
 \end{aligned}$$

and thus only depends on the fluctuations in the projectile, but only on average properties of the target itself.



The standard (naive) Glauber implementation

Estimate the distribution in number of participants in a pA or AA collision.

- ▶ Distribute the nucleons randomly according to Woods–Saxon
- ▶ Monte-Carlo the b -distributions (typically in a square with side $\sim 4R$).
- ▶ Count the number of nucleons in the target that is within a distance $d = \sqrt{\sigma/2\pi}$ from any of the projectile nucleons. (Gives you N_{coll} and N_{part} .)

Normally no fluctuations, but includes diffractively wounded nucleons by using $\sigma = \sigma_{\text{abs}}^{\text{NN}} + \sigma_{\text{dex}}^{\text{NN}} = \sigma_{\text{tot}}^{\text{NN}} - \sigma_{\text{el}}^{\text{NN}}$.



A more sophisticated Glauber implementation

Assume a fluctuating NN cross section

$$P(\sigma) = \rho \frac{\sigma}{\sigma + \sigma_0} \exp \left\{ -\frac{(\sigma/\sigma_0 - 1)^2}{\Omega^2} \right\}$$

with

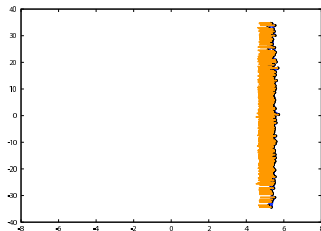
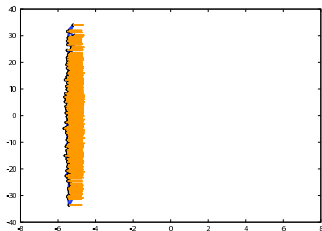
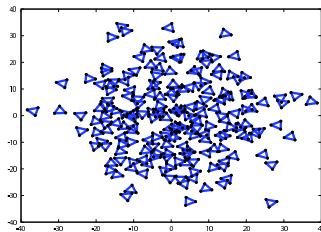
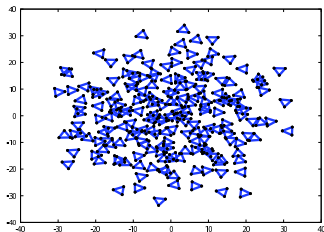
$$T(b, \sigma) \propto \exp \left(-cb^2/\sigma \right).$$

For pA this gives a longer tail out to a large number of wounded nucleons.

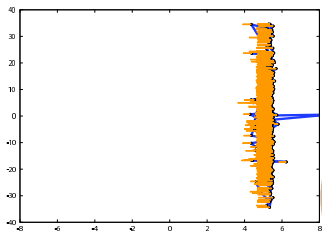
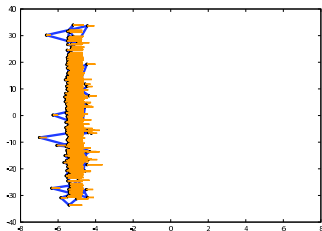
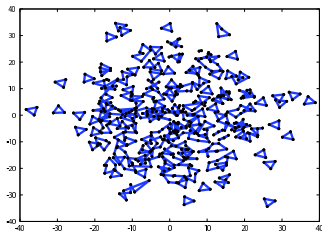
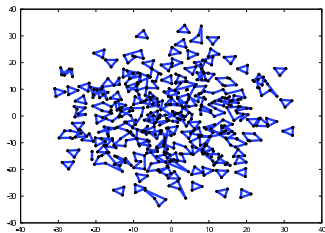
[Strikman et al. hep-ph/1301.0728]



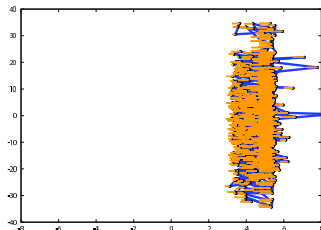
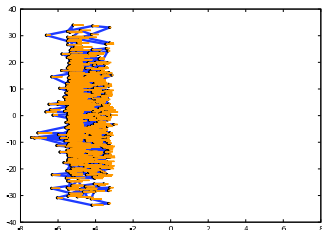
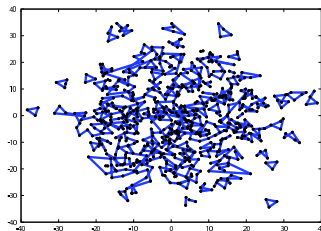
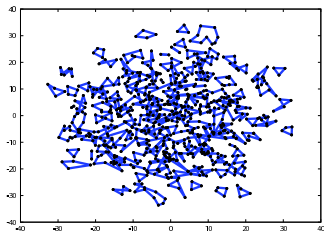
Sample Au-Au event



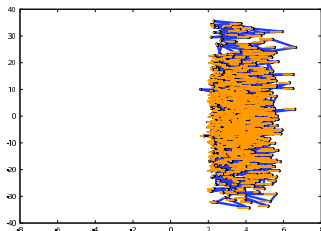
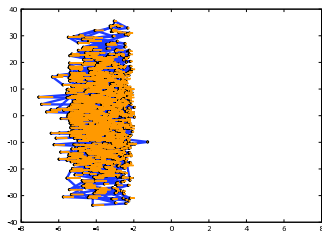
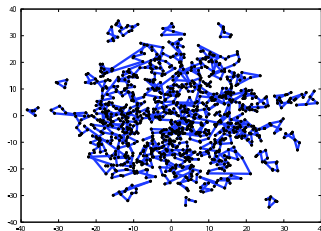
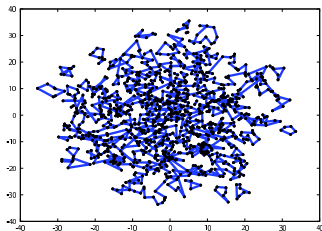
Sample Au-Au event



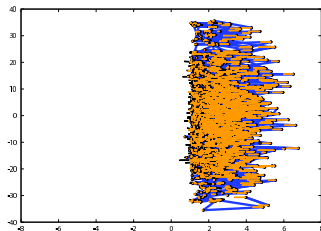
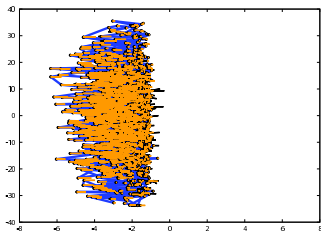
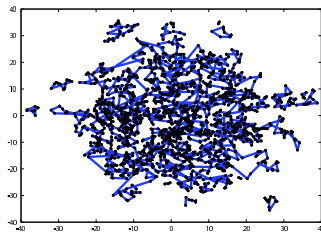
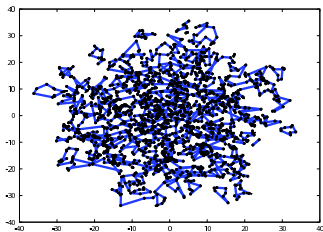
Sample Au-Au event



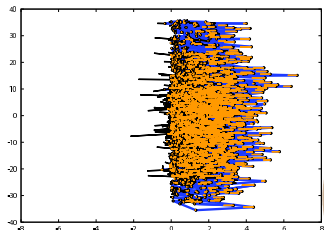
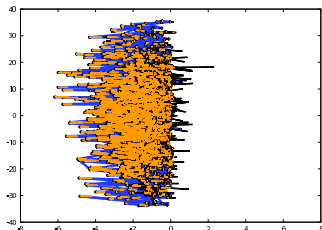
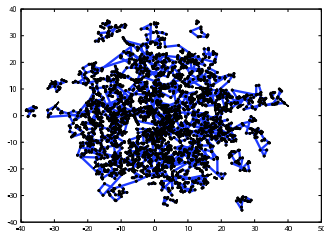
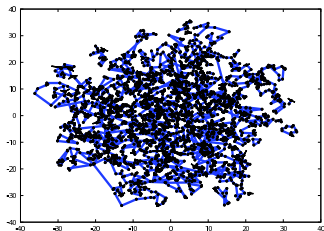
Sample Au-Au event



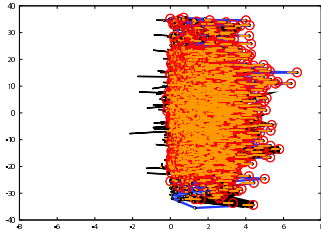
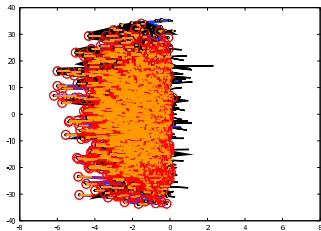
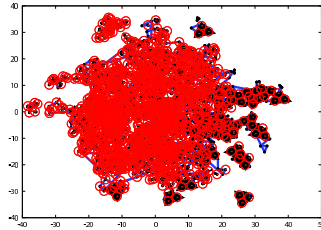
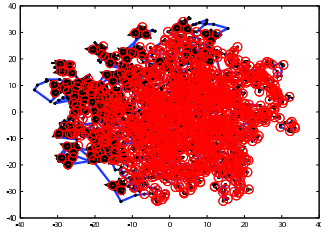
Sample Au-Au event



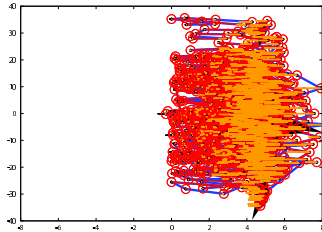
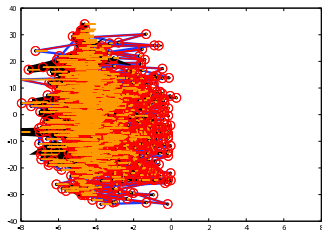
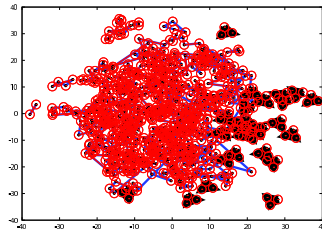
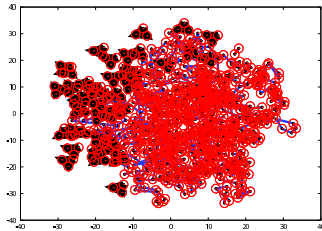
Sample Au-Au event



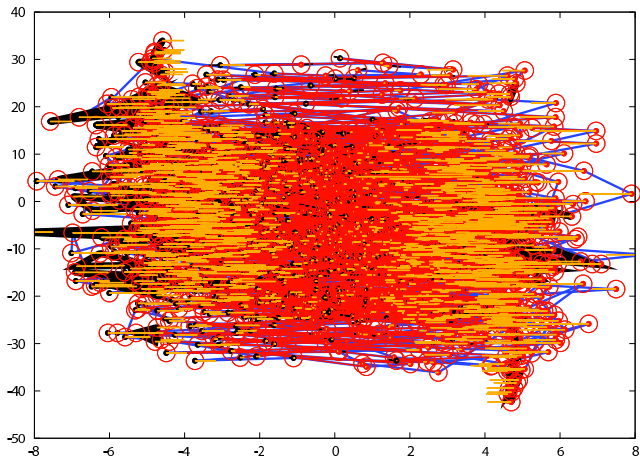
Sample Au-Au event



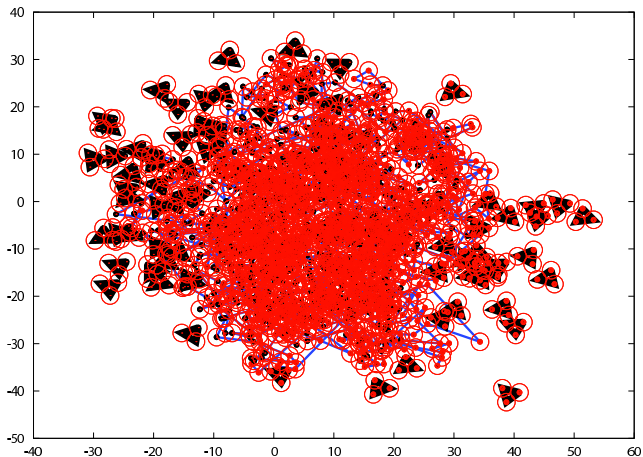
Sample Au-Au event



Sample Au-Au event



Sample Au-Au event



Color Glass Condensate (CGC)

A mean-field statistical approach to the density of gluons.

- ▶ Color: It's American, and yes, it's QCD
- ▶ Glass: Solid on short timescales, amorphous on long.
- ▶ Condensate: There are a lot of gluons.

Includes **Saturation** of gluons.

In standard DGLAP the gluon density increases rapidly with decreasing x . Also in BFKL. Somewhere it has to stop,
 $g + g \rightarrow g = \text{Saturation}$

$$Q_{\text{sat}} = Q_0^2 \left(\frac{x}{x_0} \right)^\lambda$$



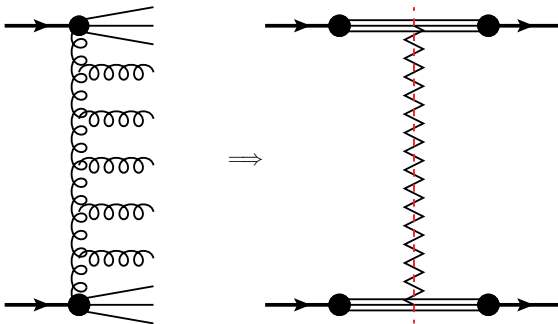
CGC starts with an initial gluon density at some $x \sim 0.01$, and evolves it to smaller x using a (non-linear) renormalization group equation (JIMWLK \sim BFKL + Saturation)

The initial density is folded with the nucleon distribution in b .

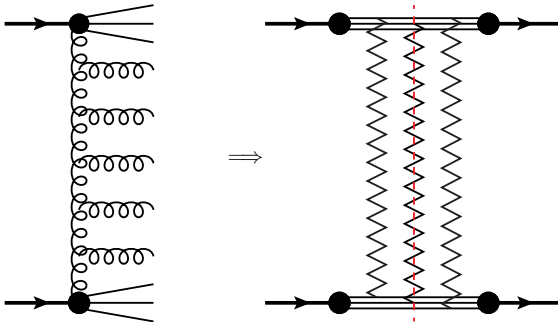
IP-Glasma model is similar but uses DGLAP + Saturation.



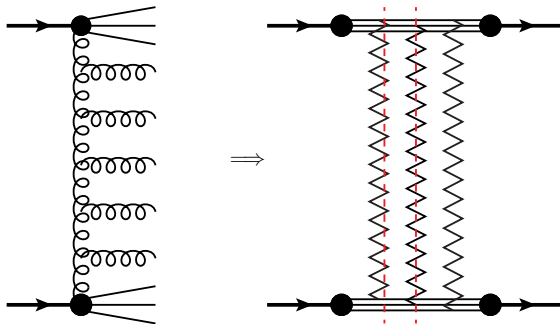
The Cut Pomeron picture



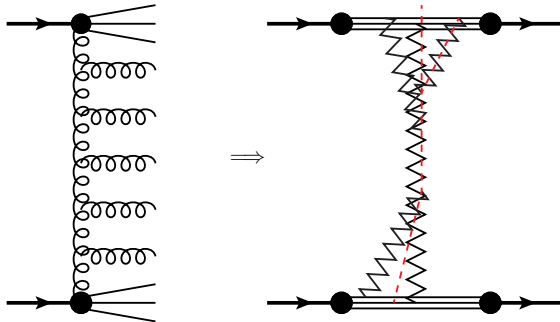
The Cut Pomeron picture



The Cut Pomeron picture



The Cut Pomeron picture

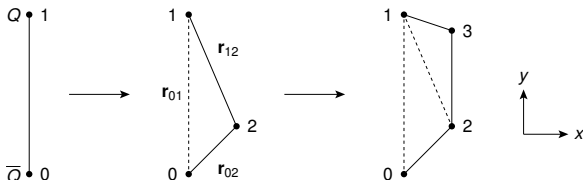


Each cut pomeron will give rise to a string (or two) spanned between two colliding nucleons, or between a nucleon and another Pomeron.



The DIPSY model

More or less same ingredients as the CGC, but generating each gluon explicitly using the (mueller) dipole model.



- ▶ Mueller's formulation of BFKL
- ▶
$$\frac{dP}{dy} = \frac{\bar{\alpha}}{2\pi} d^2 r_2 \frac{r_{01}^2}{r_{02}^2 r_{12}^2}$$
- ▶ Dipoles in impact parameter space, evolved in rapidity
- ▶ Builds up virtual Fock-states of the proton



The interaction

Dipole–dipole interaction:

- ▶ $F = \sum_{ij} f_{ij} \quad f_{(12)(34)} \propto \alpha_s^2 \ln^2 \left(\frac{r_{13} r_{24}}{r_{14} r_{23}} \right)$
- ▶ Unitarize to get saturation effects $T = 1 - e^{-F}$

Saturation in the evolution with the **Swing** model

- ▶ Colour reconnection
- ▶ Two dipoles with the same colour may reconnect.
- ▶ Does not reduce the number of dipoles, but smaller dipoles are favoured, and these have weaker interactions.
- ▶ Also reconnections between different nucleons in a nuclei.

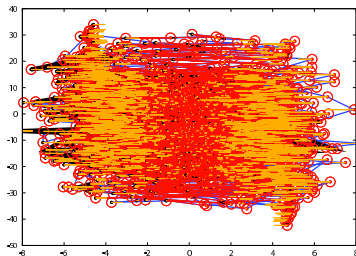
Models all kinds of fluctuations and correlations.



Questions!



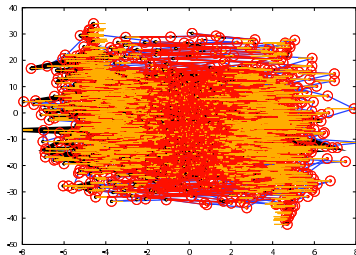
The Final State



Model each gluon/dipole individually?



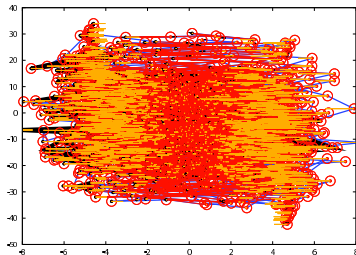
The Final State



Model each gluon/dipole individually?
Or give up and use statistical methods?



The Final State



- Model each gluon/dipole individually?
- Or give up and use statistical methods?
- Or both?



Quark-Gluon Plasma

Construct the the energy momentum density and the flavour flow vector for all point in space at an initial proper time $\tau = \tau_0$:

$$T^{\mu\nu}(x) = \sum_i \frac{\delta p_i^\mu \delta p_i^\nu}{\delta p_i^0} g(x - x_i)$$

$$N_q^\mu(x) = \sum_i \frac{\delta p_i^\mu}{\delta p_i^0} q_i g(x - x_i)$$

- ▶ $q_i = u, d, s$
- ▶ δp is the momentum of the parton (or string segment)
- ▶ $g(x)$ is a smoothing kernel with some assumed width



Relativistic hydrodynamics

The individual flavour flow is a conserved current

$$\partial_\nu N_q^\nu = 0$$

So is the energy–momentum tensor

$$\partial_\nu T^{\mu\nu} = 0$$

Typically divide up in small cells, get the velocity vector u^ν in the restframe of each cell (comoving frame) and evolve.

but we have four only equations for $T^{\mu\nu}$ so we need to have extra assumptions.



Ideal fluid

In the comoving frame:

- ▶ $T^{00} = \varepsilon$: energy density
- ▶ $T^{0i} = 0$: no energy flow
- ▶ $T^{i0} = 0$: no momentum
- ▶ $T^{ij} = \delta_{ij}p$: isotropic pressure

But it is also possible to include viscous effects...



Freezeout = Hadronisation and Rescattering

After the evolution we convert $T^{\mu\nu}$ and N_q^μ back into particles (Hadrons). This happens at some given hypersurface.

There is still a fairly high density of hadrons, and we expect some rescattering:

$$h_1 + h_2 \rightarrow h' \quad \text{or} \quad h_1 + h_2 \rightarrow h'_1 + h'_2$$



Freezeout = Hadronisation and Rescattering

After the evolution we convert $T^{\mu\nu}$ and N_q^μ back into particles (Hadrons). This happens at some given hypersurface.

Sorry, I don't understand this enough myself

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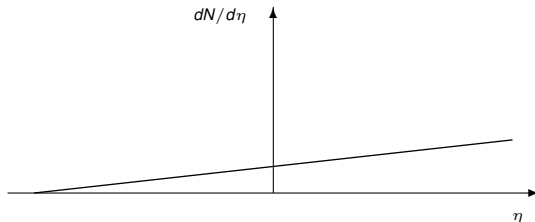
c.f. the model in PYTHIA



The Wounded Nucleon model

A simple model by Białaś and Czyż, implemented in Fritiof

Each wounded nucleon contributes with hadrons according to a function $F(\eta)$. Fitted to data, and approximately looks like



$$\frac{dN}{d\eta} = F(\eta)$$

(single wounded nucleon)

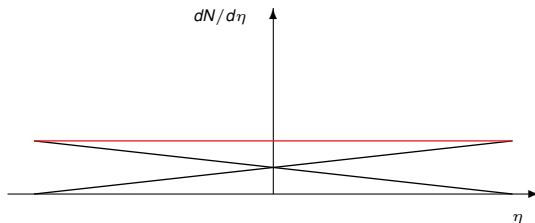
[Nucl.Phys.B111(1976)461, J.Phys.G35(2008)044053, Nucl.Phys.B281(1987)289.]



The Wounded Nucleon model

A simple model by Białaś and Czyż, implemented in Fritiof

Each wounded nucleon contributes with hadrons according to a function $F(\eta)$. Fitted to data, and approximately looks like



$$\frac{dN}{d\eta} = F(\eta) + F(-\eta) \quad (\text{pp})$$

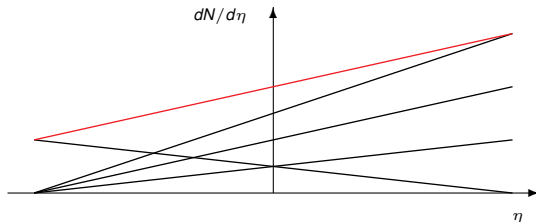
[Nucl.Phys.B111(1976)461, J.Phys.G35(2008)044053, Nucl.Phys.B281(1987)289.]



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$$\frac{dN}{d\eta} = w_t F(\eta) + F(-\eta) \quad (\text{pA})$$

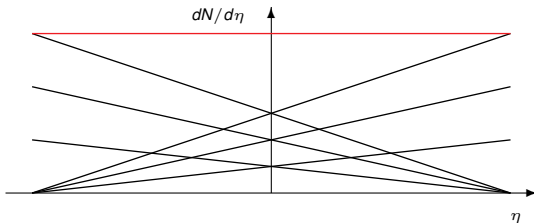
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$$\frac{dN}{d\eta} = w_t F(\eta) + w_p F(-\eta) \quad (AA)$$

[Nucl.Phys.B111(1976)461, J.Phys.G35(2008)044053, Nucl.Phys.B281(1987)289.]



In Fritiof this was modelled by stretching out a string from each wounded nucleon with an invariant mass distributed as dm_X/m_X , which reproduces $F(\eta) \propto \eta - \eta_0$.

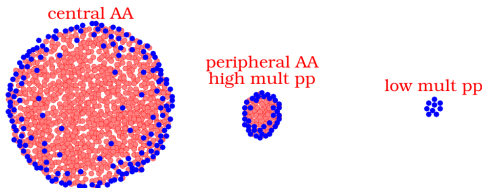
Note that there are no collective effects here. But nevertheless Fritiof reproduced most data: No conclusive evidence for QGP until the late nineties.



Core – Corona

The EPOS generator uses a *Core–Corona* model:

- ▶ Start with the Pomeron picture.
- ▶ Create strings
- ▶ Divide up:
 - ▶ Core: If the density of strings is high, chop them up and use relativistic hydrodynamics.
 - ▶ Corona: For lower densities, allow for hard interactions and perturbative ISR/FSR/MPI evolution



HIJING

(one of the standard HI generators)

- ▶ Inspired by Fritiof
- ▶ Hard scatterings with nuclear PDFs + Shadowing
- ▶ Soft radiation with ARIADNE
- ▶ String fragmentation



AMPT

(Another standard HI generator with collective effects)

- ▶ Same initial state as HIJING
- ▶ String melting
 - ▶ String fragmentation
 - ▶ Convert back to $q\bar{q}$
 - ▶ Evolve in time with elastic scattering
 - ▶ Nearest neighbour recombination into hadrons
- ▶ Hadron rescattering



Heavy Ions in PYTHIA8: Angantyr



- ▶ Glauber model with advanced fluctuation treatment
- ▶ Divides NN interactions into absorptive, single or double diffractive.
- ▶ Also differentiates absorptive interactions:
 - ▶ Primary: is modelled as a PYTHIA non-diffractive pp event.
 - ▶ Secondary: an interaction with a nucleon that has already had an interaction with another. Modelled as a (modified) diffractive excitation event (with dm_X/m_X as in Fritiof).
- ▶ All sub-events generated on parton level and merged together into a consistent pA or AA event and then hadronised.

(No string interactions yet.)

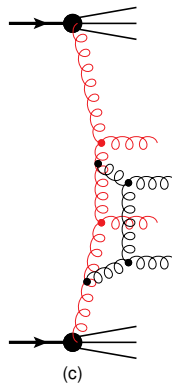
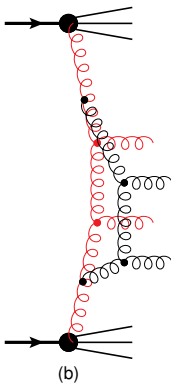
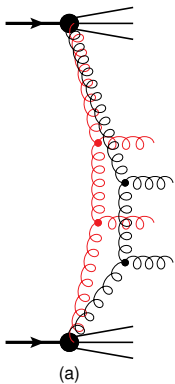


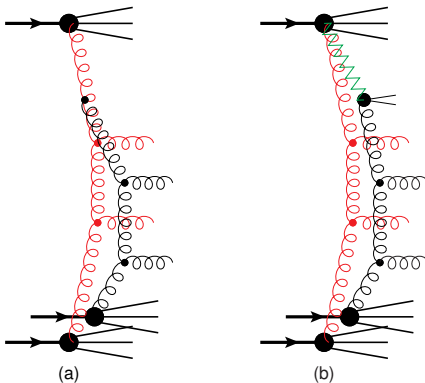
Heavy Ions in PYTHIA8: Angantyr

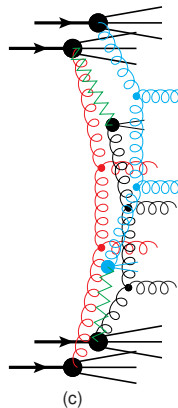
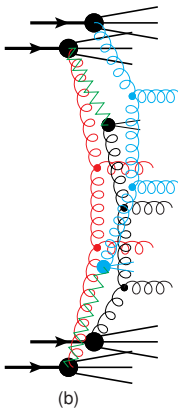
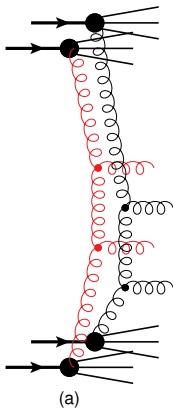


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(No string interactions yet.)









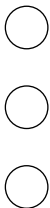
projectile



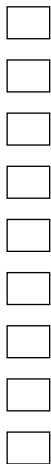
target



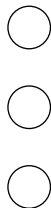
projectile



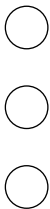
collisions



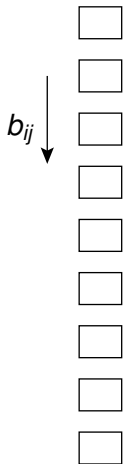
target



projectile



collisions



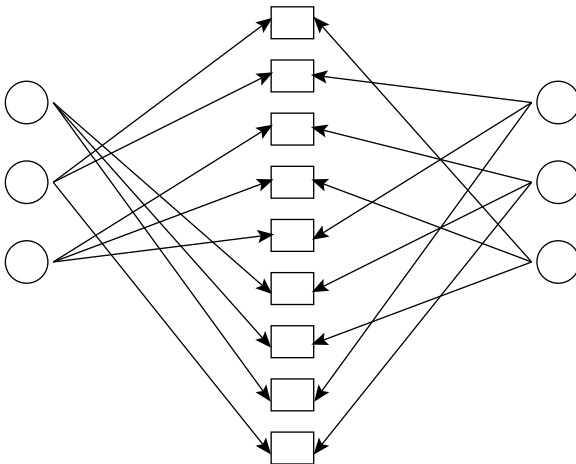
target



projectile

collisions

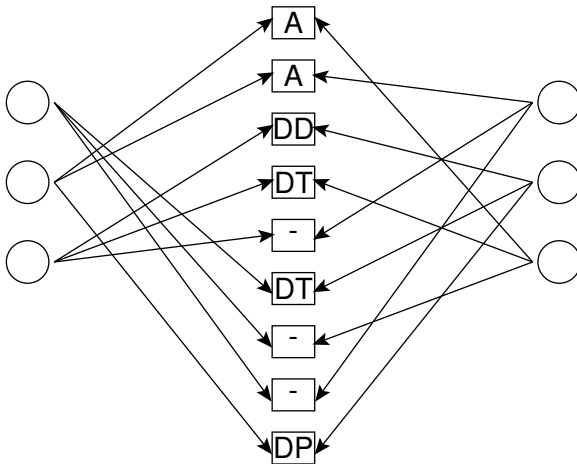
target



projectile

collisions

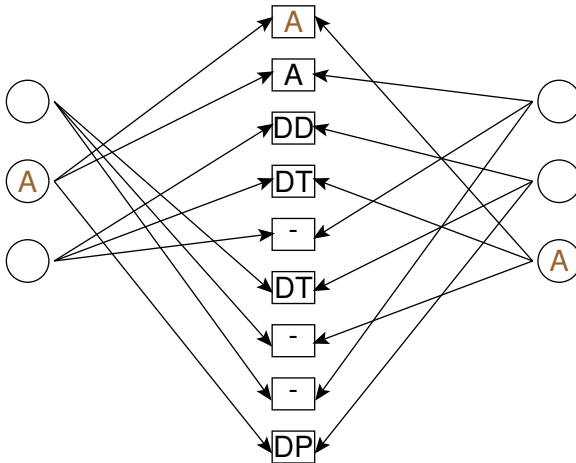
target



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collisions

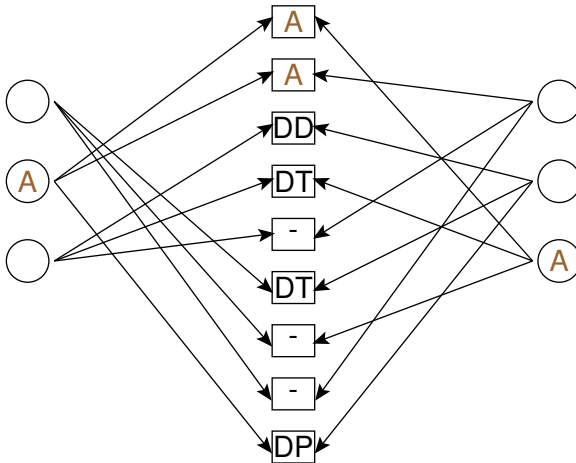
target



projectile

collisions

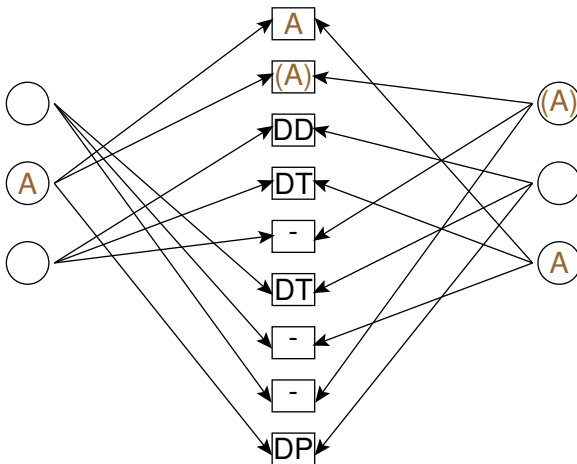
target



projectile

collisions

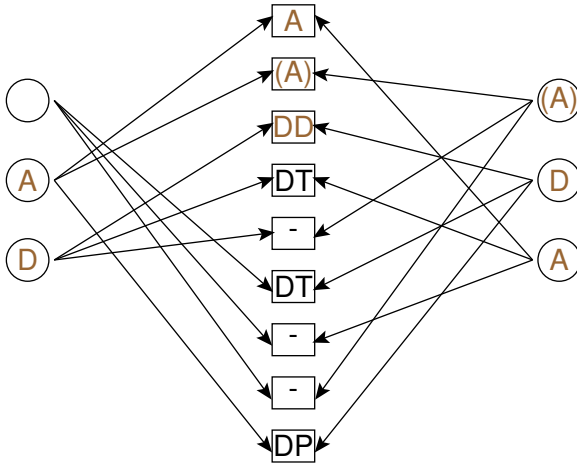
target



projectile

collisions

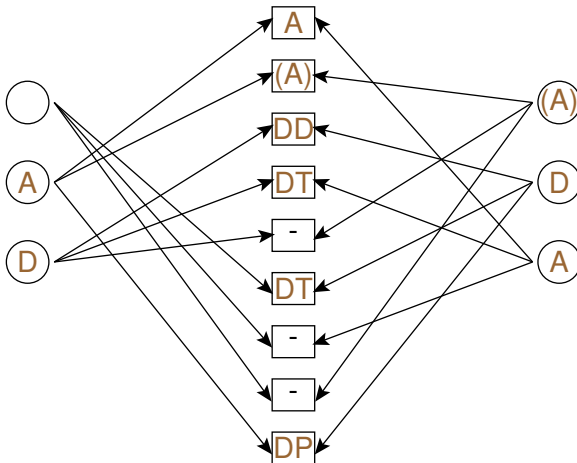
target



projectile

collisions

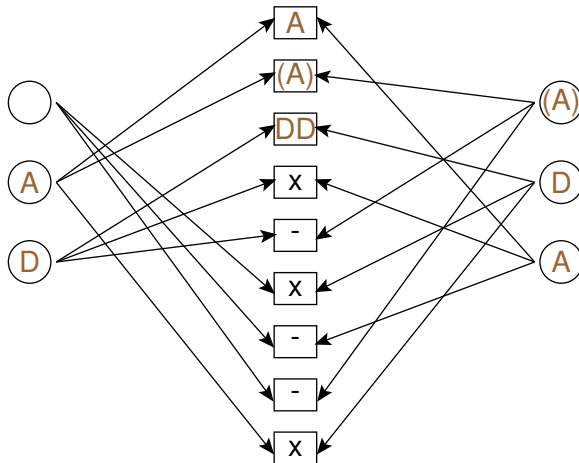
target



projectile

sub-events

target



Signal processes

Not only min-bias. Rather than just generating non-diffractive events, The first absorptive sub-event can be generated using any hard process in PYTHIA8, giving the final event a weight $N_A \sigma_{hard} / \sigma_{ND}$.



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(not perfect yet)



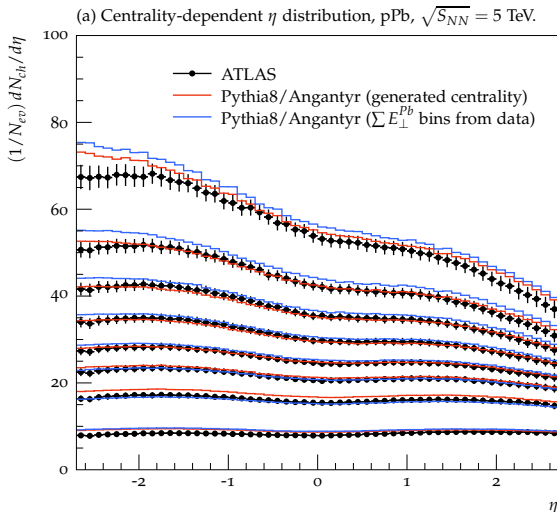
Comparison to data

Several parameters in addition to the pp PYTHIA8 ones.

- ▶ Nucleon distributions can in principle be measured independently.
- ▶ NN cross section fluctuations are fitted to (semi-) inclusive pp cross sections (total, non-diffractive, single and double diffractive, elastic, and elastic slope) for given $\sqrt{s_{NN}}$.
- ▶ Diffractive parameters for secondary absorptive collisions, “tuned” to non-diffractive pp PYTHIA.
- ▶ M_X distribution: $dM_X^2/M_X^{2(1+\epsilon)}$, could be tuned (to pA), but we choose $\epsilon = 0$.
- ▶ Few other choices concerning energy momentum conservation which do not have large impact.



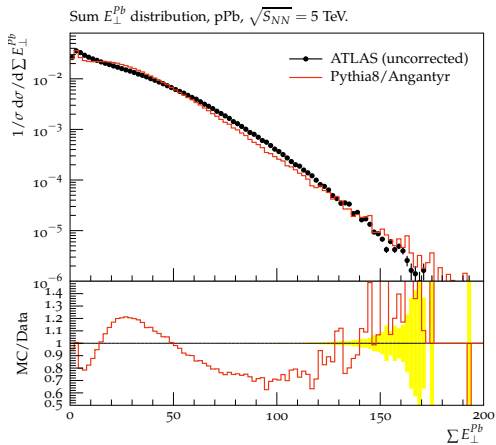
Eta distribution in pPb



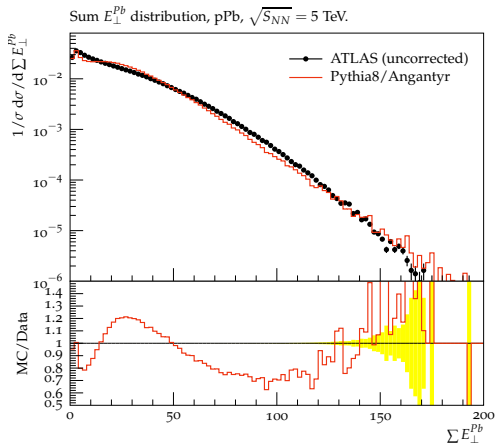
[arXiv:1508.00848]



Centrality in pPb



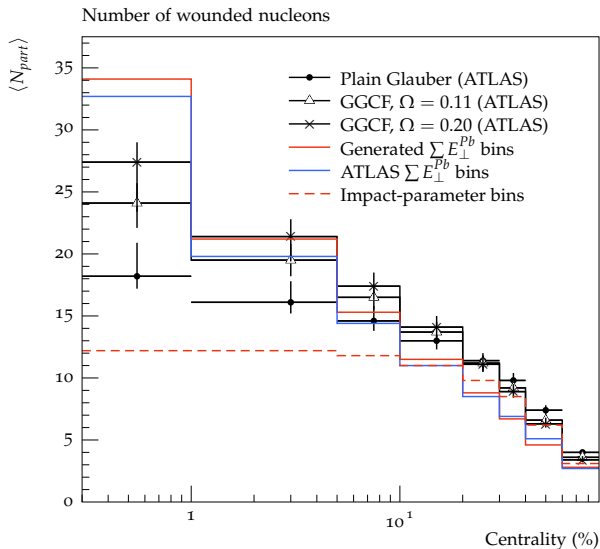
Centrality in pPb



What was actually measured in the previous slide is a correlation between the η -distribution and the forward activity.

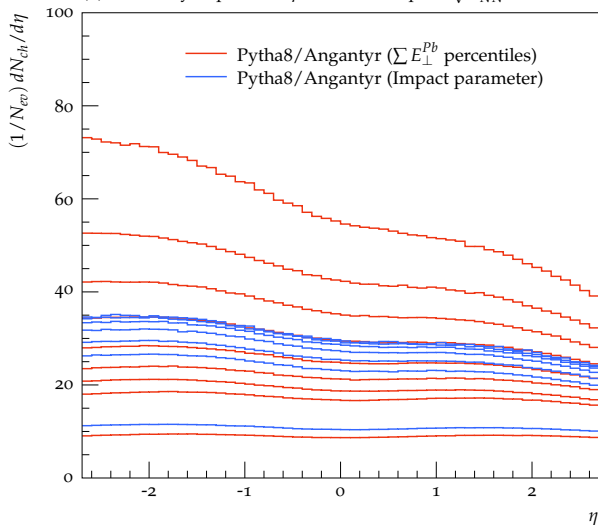


p-Pb number of participants

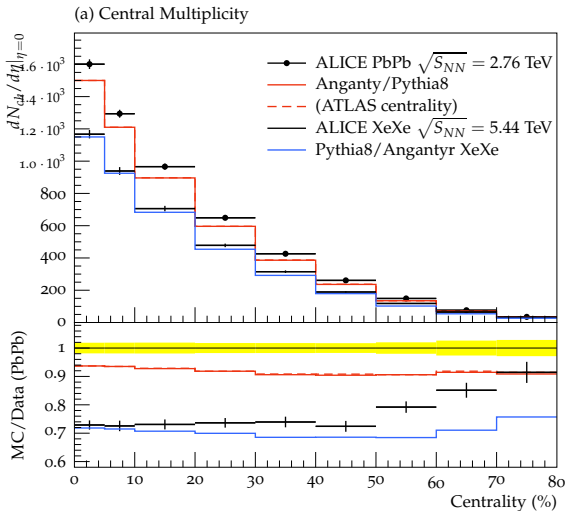


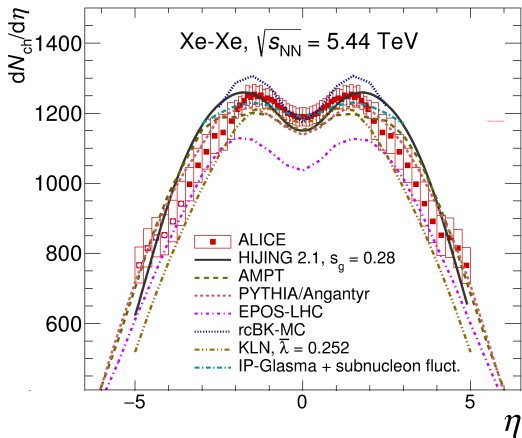
p-Pb η -distribution

(b) Centrality-dependent η distribution, pPb, $\sqrt{s_{NN}} = 5$ TeV.



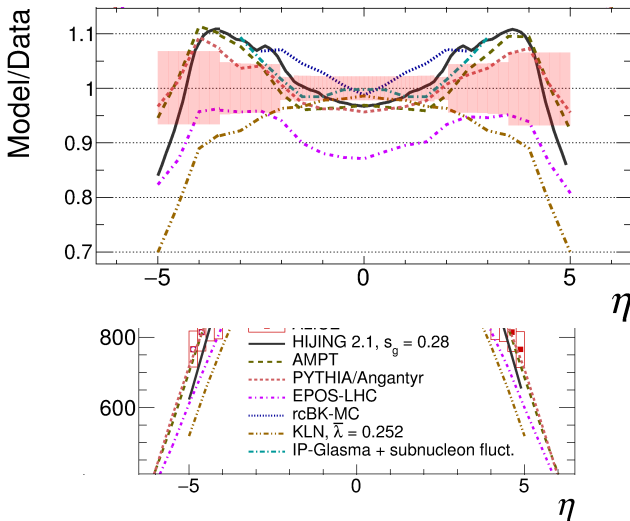
Central multiplicity in PbPb





[arXiv:1805.04432]

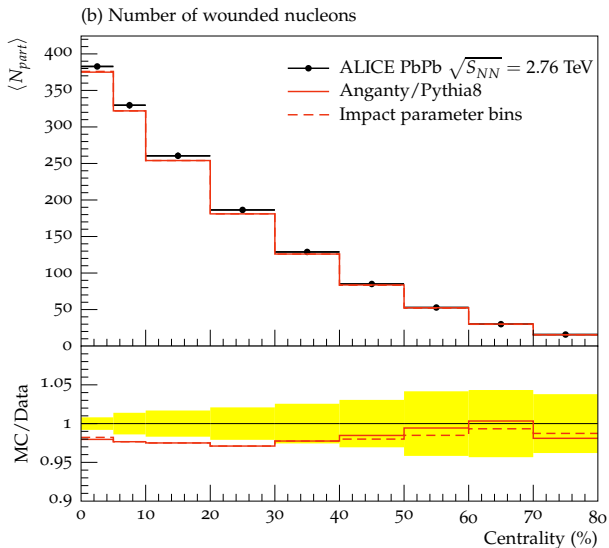




[arXiv:1805.04432]



Pb–Pb number of participants



Go generate yourself!

```
pythia.readString("Beams:idA = 1000822080");  
pythia.readString("Beams:idB = 1000822080");  
pythia.readString("Beams:eCM = 2760.0");
```



String fragmentation

Formally based on one-dimensional, massless, relativistic strings.

- ▶ $V(r) \propto r$ gives a constant string tension
 $\kappa \sim 1 \text{ GeV/fm}$
- ▶ The string breaks by $q\bar{q}$ pairs tunnelling out of the vacuum
 $P \propto \exp(-\pi(m_q^2 + k_{\perp}^2)/\kappa)$
- ▶ Strings are stretched between a quark and an anti-quark with gluons in between acting as kinks.
- ▶ Hadrons are chopped off from the ends with the Lund symmetric fragmentation function

$$f(z) \propto \frac{(1-z)^a}{z} e^{-bm_{\perp}^2/z}$$



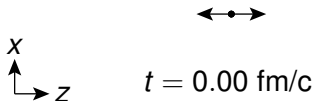
But strings are not one-dimensional. We can estimate both the tension and the radius of a QCD string on the lattice:

$$R = 0.25 - 1.0 \text{ fm.}$$



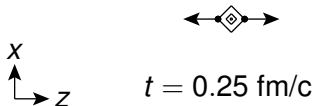
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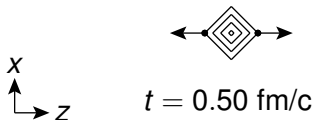
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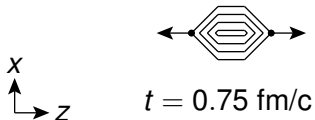
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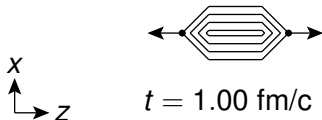
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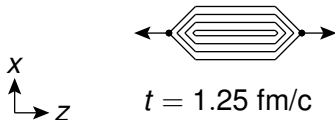
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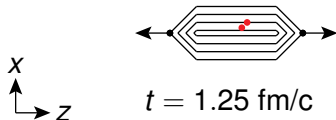
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String Interactions: GLEIPNIR (X₁MIC₂IR)

- ▶ Overlapping anti-parallel strings may attenuate each other.
- ▶ Overlapping strings may repel each other
- ▶ Overlapping strings will have an increased string tension, making it easier to produce eg. strange hadrons.



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[work in progress: H. Shah, T Lundberg]



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String Shoving \Rightarrow ridges and flow
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[arXiv:1710.09725, arXiv:2010.07595]



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Rope Hadronisation \Rightarrow strangeness enhancement

[work in progress: H. Shah, T Lundberg]

[arXiv:1710.09725, arXiv:2010.07595]

[arXiv:1412.6259, arXiv:2202.12783, arXiv:2205.11170]



String repulsion: Shoving

The string endpoints (quarks and gluons) carry longitudinal momentum, but the string itself cannot.

The shoving between parallel strings gives a transverse push according to

$$\frac{dp_{\perp}}{dt dz} = \frac{g_{\kappa} \delta_{\perp}(t)}{R^2} \exp\left(-\frac{\delta_{\perp}^2(t)}{4R^2}\right).$$

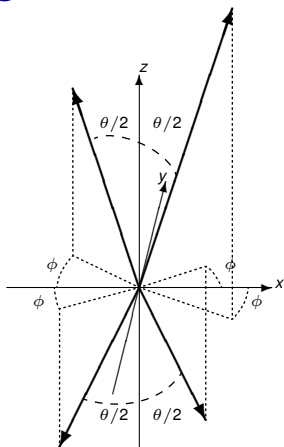
This push must be parallel to both string pieces.

There is no frame where two random string pieces are parallel.

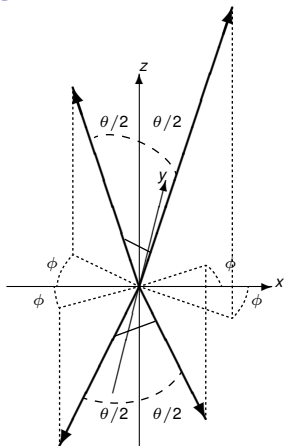
But there is always a frame where they lie in parallel planes at any given time.



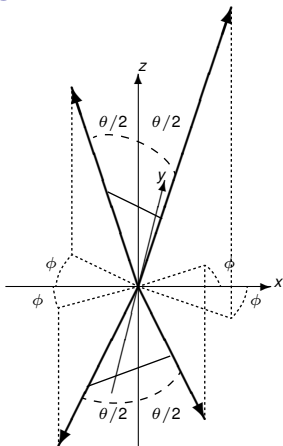
The parallel string frame



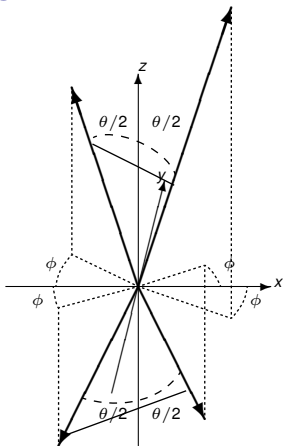
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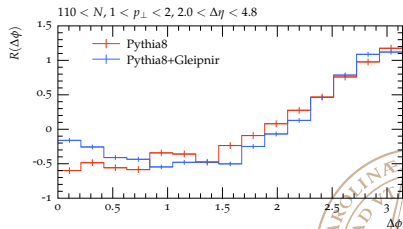
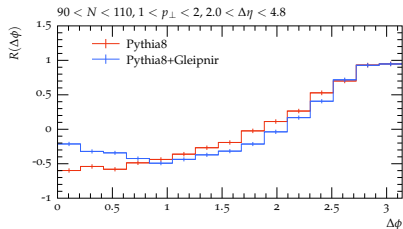
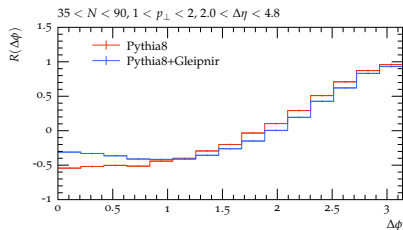
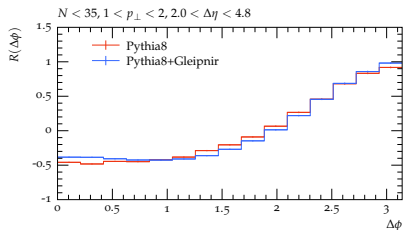
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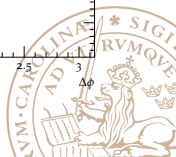
- ▶ Use (simplified) space-time information of all partons.
- ▶ Transform to parallel frame for every pair of string pieces.
- ▶ Calculate and collect small nudges, ordered in time.
- ▶ Apply the nudges to the produced primary hadrons (both position and momenta).

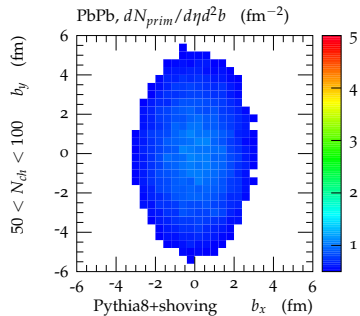
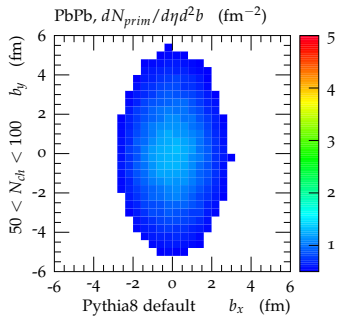


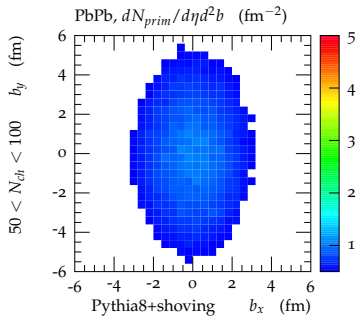
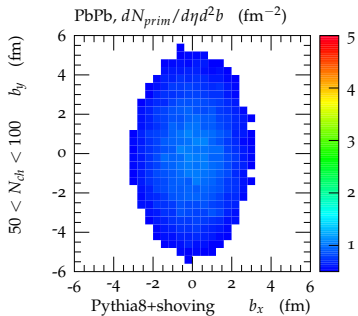
We have a ridge!



[arXiv:1009.4122]







Rope hadronisation

Overlapping strings will give a higher string tension.

From lattice calculations $\kappa \propto C_2$.

In a rope with p parallel and q anti-parallel, completely overlapping strings we have

$$\kappa_{\{p,q\}} = \frac{1}{4} (p^2 + pq + q^2 + 3p + 3q) \kappa_{\{1,0\}}$$

The relative probability to produce a strange quark in a break-up, compared to a light quark is

$$P \propto \exp(\pi(m_s^2 - m_d^2)/\kappa_{\text{eff}}),$$

where $\kappa_{\text{eff}} = \kappa_{\{p,q\}} - \kappa_{\{p-1,q\}}$

is the *reduction* of the string tension.



- ▶ Strings are not parallel \Rightarrow the parallel frame
- ▶ Strings are not completely overlapping

$$\begin{aligned}\mathcal{I}(\delta_y, \delta_z, \phi) &= \int d^2\rho \mathbf{E}_1(\rho) \cdot \mathbf{E}_2(\rho) \\ &= 2\pi E_0^2 R^2 \frac{\cos \phi}{\cos \frac{\phi}{2}} \exp\left(-\frac{\delta_y^2 \cos \frac{\phi}{2} + \delta_z^2}{4R^2}\right).\end{aligned}$$

- ▶ Again use pairwise interactions, and sum up (fractional) p and q .
- ▶ Adjust the hadronisation parameters in PYTHIA8 in each break-up.



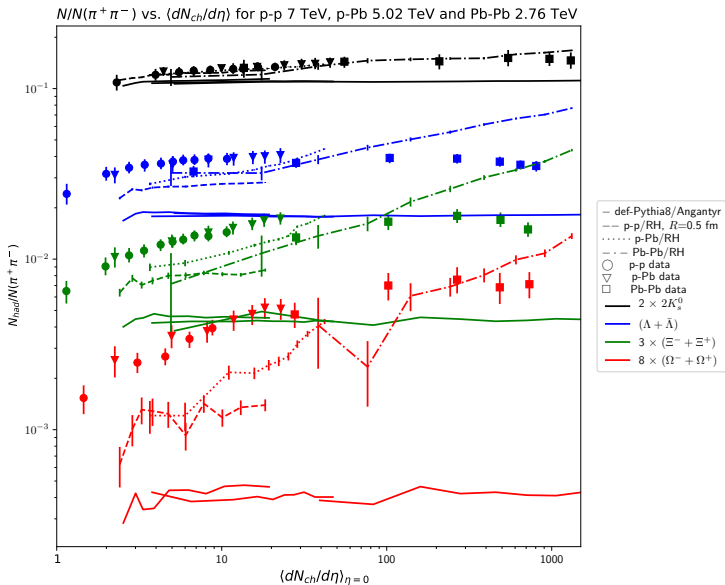
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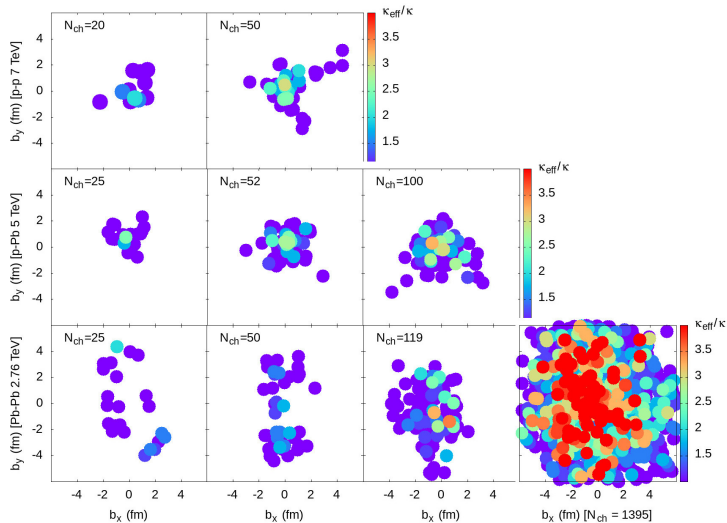
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- ▶ Again use pairwise interactions, and sum up (fractional) p and q .
- ▶ Adjust the hadronisation parameters in PYTHIA8 in each break-up.
(A bit messy, especially for baryons)

[arXiv:2201.06316]





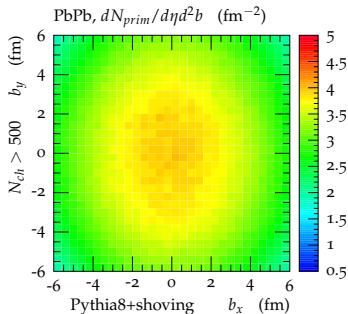
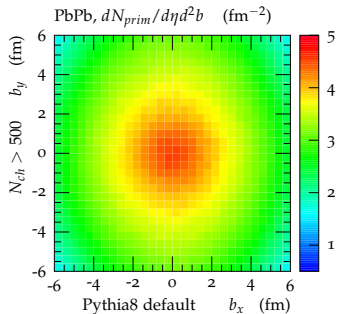


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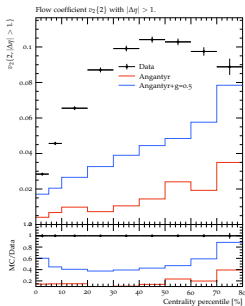
And then there is an interplay with Hadronic rescattering

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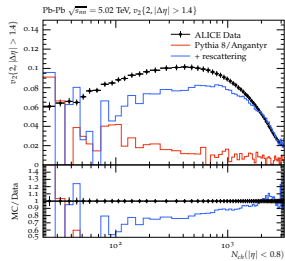
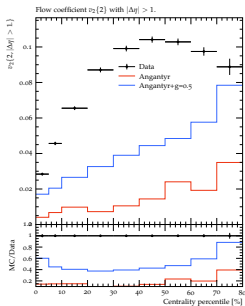


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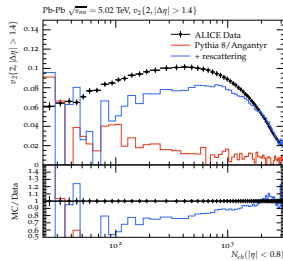
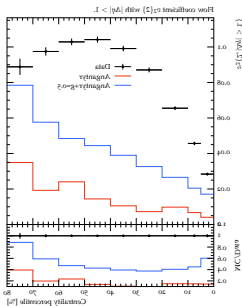
[arXiv:2103.09665]

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Summary

- ▶ Heavy-Ion collisions are messy
- ▶ Not just overlaid NN collisions
- ▶ Initial state effects (saturation, fluctuations, ...)
- ▶ Final state effects (QGP, hydrodynamics, string interactions, flow, jet-quenching, rescattering, ...)

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Tutorial this afternoon:

<http://home.thep.lu.se/~leif/misc/angantyr-tutorial.tgz>

Final Comments

By tradition HI and HEP have been separate communities

- ▶ LHC brought them together
- ▶ There are collective effects in pp
- ▶ There are jets in AA
- ▶ We can (and need to) learn from each other

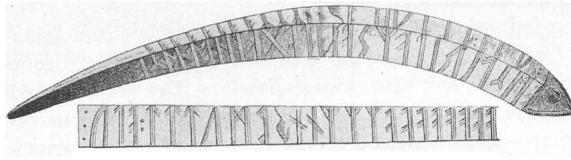
Questions!

Outline of Lectures

- ▶ Lecture I: Basics of Monte Carlo methods, the event generator strategy, matrix elements, LO/NLO, . . .
- ▶ Lecture II: Parton showers, initial/final state, (matching/merging), hadronization, decays. . . .
- ▶ Lecture III: Minimum bias, multi-parton interactions, pile-up, summary of general purpose event generators, . . .
- ▶ Lecture IV: Protons vs. heavy ions, Glauber calculations, initial/final-state interactions, . . .

Buckley et al. (MCnet collaboration), *Phys. Rep.* **504** (2011) 145.

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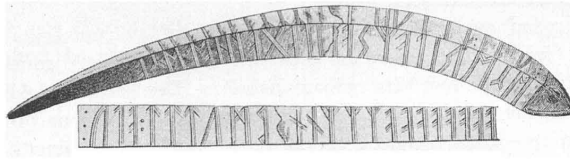
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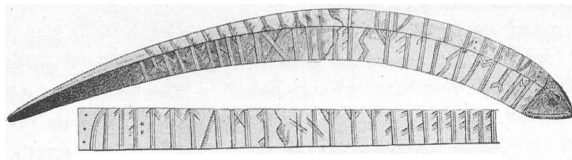
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EK	ERILAR	SAWILAGAR	HATEKA
I	the rune master	magic	is my name