

M. Chanowitz  
LBNL


# What is the precision electroweak data trying to tell us?

Workshop on indirect searches for  
new physics at the time of LHC  
Galileo Institute for Theoretical Physics  
Firenze, March 2010

More precisely: what is the combination of the PEW data **and** the LEP II limit on  $m_H$  trying to tell us?

Canonical: SM fit is great, Higgs boson is light — could be...

But SM fit has a  $3.2\sigma$  problem, which suggests NP *whether  $3.2\sigma$  problem is genuine or not*:

**If** due to systematic error (e.g., theoretical), fit predicts  $m_H$  much too light  NP with  $T > 0$  to raise  $m_H$

Many NP models with custodial SU(2) breaking can then fit PEW data much better than usual SM fit.

Bonus: increased  $m_H$  alleviates little hierarchy fine-tuning problem that is generic for light Higgs.

Canonical view might be correct, but the non-canonical interpretation is also worth considering.

# Topics

SM fit: implications of  $A_{LR} - A_{FB}^b$  anomaly

- interpretations of the anomaly
- Higgs mass predictions

New Physics with  $SU(2)_{\text{Custodial}}$  breaking

- generic
- examples:  $Z'$ , fourth family

# SM Fit

Fits alla EWWG:

- $m_Z, m_t, \Delta\alpha_5, \alpha_S, m_H$   $\longrightarrow$   $O_{Z\text{-Pole}} + m_W + \dots$
- Zfitter with 2 loop  $x_W, m_W$
- biggest experimental correlations
- $\Delta\alpha_5$  from BES (Burkhart-Pietrzyk)  
(omit  $\Gamma_W$  – 2.5% error, not part per mil)

Diminished  $CL(\chi^2) = 0.14$ , primarily from  $3.2\sigma$  difference between  $x_W(A_{LR})$  vs.  $x_W(A_{FB}^b)$

Very slight tension with LEP II:

$$m_H = 89 \text{ GeV}$$

$$CL(m_H > 114 \text{ GeV}) = 0.23$$

	Experiment	SM Fit	Pull
$A_{LR}$	0.1513 (21)	0.1480	<b>1.6</b>
$A_{FB}^l$	0.01714 (95)	0.01644	0.7
$A_{e,\tau}$	0.1465 (32)	0.1480	-0.5
$A_{FB}^b$	0.0992 (16)	0.1038	<b>-2.9</b>
$A_{FB}^c$	0.0707 (35)	0.0742	-1.0
$Q_{FB}$	0.23240 (120)	0.23139	1.0
$m_W$	80.399 (23)	80.378	0.9
$\Gamma_Z$	2495.2 (23)	2495.7	-0.2
$R_l$	20.767 (25)	20.739	1.1
$\sigma_h$	41.540 (37)	41.481	-1.6
$R_b$	0.21629 (66)	0.21582	0.7
$R_c$	0.1721 (30)	0.1722	-0.04
$A_b$	0.923 (20)	0.935	-0.6
$A_c$	0.670 (27)	0.668	0.07
$m_t$	173.1 (1.3)	173.3	0.1
$\Delta\alpha_5(m_Z^2)$	0.02758 (35)	0.02768	0.3
$\alpha_S(m_Z)$		0.118	
$\chi^2/\text{dof}$		17.3/12	
$CL(\chi^2)$		<b>0.14</b>	
$m_H$		<b>89</b>	
$CL(m_H > 114)$		<b>0.23</b>	
$m_H(95\%)$		<b>151</b>	

$\mathbf{x}_W^{\ell, \text{eff}}$  : most important observable for  $m_H$  fit

$\mathbf{A}_{\text{LR}} \quad \mathbf{0.23098} \quad (26)$ $\mathbf{A}_{\text{FB}}^{\ell} \quad \mathbf{0.23099} \quad (53)$ $\mathbf{A}_{e,\tau} \quad \mathbf{0.23159} \quad (41)$	}	$\mathbf{x}^{\ell}[\mathbf{A}_L] = \mathbf{0.23113} \quad (21)$ $\chi^2/N = 1.6/2 \quad \text{CL} = 0.44$	}	$\mathbf{0.23153} \quad (16)$ $\mathbf{3.2\sigma}$
$\mathbf{A}_{\text{FB}}^b \quad \mathbf{0.23221} \quad (29)$ $\mathbf{A}_{\text{FB}}^c \quad \mathbf{0.23220} \quad (81)$ $\mathbf{Q}_{\text{FB}} \quad \mathbf{0.23240} \quad (120)$	}	$\mathbf{x}^{\ell}[\mathbf{A}_H] = \mathbf{0.23222} \quad (27)$ $\chi^2/N = 0.02/2 \quad \text{CL} = 0.99$	}	$\mathbf{CL} = \mathbf{0.0014}$

Dominated by  $\mathbf{x}[\mathbf{A}_{\text{LR}}] \oplus \mathbf{x}[\mathbf{A}_{\text{FB}}^b] = \mathbf{0.23153} \quad (19)$   
 $\mathbf{3.2\sigma} \quad \mathbf{CL} = \mathbf{0.0016}$

Combining all six:  $\chi^2/N = 11.8/5 \quad \text{CL} = 0.037$

# $A_{FB}^b$ , $A_b$ , $x_W^{\ell, \text{eff}}$ & all that...

$$A_{FB}^b = 3/4 \cdot A_e A_b \qquad A_f = \frac{g_{fL}^2 - g_{fR}^2}{g_{fL}^2 + g_{fR}^2}$$

**SM:**  $g_{fL} = t_{3L,f} - q_f x_W^{f, \text{eff}} \qquad g_{fR} = -q_f x_W^{f, \text{eff}}$

$A_b^{(SM)} = 0.935 \pm 0.0005 \implies$  Negligible sensitivity to  $m_H$ ,  $m_t$

Sensitivity to  $x_W$  &  $m_H$  resides in  $A_\ell$  (because  $A_\ell \propto 1/4 - x_W$ )

SM fit assumes  $A_b^{(SM)}$ :  $A_\ell = 4A_{FB}^b / 3A_b^{(SM)} \implies x_W^{\ell, \text{eff}}$

$A_b$  measured **directly**:  $A_{FBLR}^b \implies A_b = 0.923 (20)$  } Agrees with SM

or **indirectly** from  $A_{FB}^b$  using  $A_\ell$  from  $A_{LR}$ ,  $A_{FB}^\ell$ ,  $A_{e,\tau}$ :

$$A_b = 4A_{FB}^b / 3 A_\ell = 0.881 (17) \quad \left\{ \begin{array}{l} 3.2\sigma \text{ from SM} \\ 1.6 \sigma \text{ from } A_{FBLR}^b \end{array} \right.$$

$$A_b[\text{direct}] \oplus A_b[\text{indirect}] = 0.899 (13) \quad \left\{ \begin{array}{l} 2.8\sigma \text{ from SM} \end{array} \right.$$

$\implies$  Evidence for NP in  $Zbb$  interaction is equivocal.

# Three generic options...

$A_{\text{FB}}^b - A_{\text{LR}}$  anomaly could be

- Statistical fluctuation
- New physics
- Underestimated systematic error

Briefly consider each:

# Statistical Fluctuation

*Significance depends on how question is framed.*

- Global CL's fairly reflect likelihood that **any** of a set of measurements might fluctuate to become an outlier:

E.g.,  $\chi^2/N = 17.3/12 \rightarrow \mathbf{CL = 0.14}$

Cf., Probability of at least one  $\geq 2.86\sigma$  outlier ( $A_{FB}^b$ ) among 12 independent measurements:  $\mathbf{P = 0.05}$

- IF we ask for the consistency of the measurements that determine  $m_H$ , the answer is

$\chi^2, N = 14.2, 7$

$\mathbf{CL = 0.05}$

$\left\{ \text{Omits } \sigma_H, R_{b,c}, A_{b,c} \right.$

- IF we ask for the consistency of the two highest precision asymmetry measurements that determine  $m_H$ , the answer is the nominal CL for  $3.2\sigma$ ,  $\mathbf{P = 0.0014}$

Most conservative assessment: there is an O(10%) problem.



# New Physics in $A_b$ ? — the $R_b$ constraint

1998± :  $3\sigma$   $R_b$  anomaly understood as systematic error.

Today:  $R_b[\text{expt}] / R_b[\text{SM}] = 1.003 (3)$

$$\longrightarrow \delta g_{bL}^2 + \delta g_{bR}^2 \sim 0.0005 (5)$$

$A_{\text{FB}}^b$  anomaly:  $A_b[A_{\text{FB}}^b] / A_b[\text{SM}] = 0.942 (18)$

$$\longrightarrow \delta g_{bL}^2 - \delta g_{bR}^2 \sim -0.009 (3)$$

$$\longrightarrow \delta g_{bL} / g_{bL}^{\text{SM}} \approx -0.005 / -0.42 \approx 0.01$$

$$\delta g_{bR} / g_{bR}^{\text{SM}} \approx 0.03 / 0.08 \approx \mathbf{0.4} \quad \mathbf{HUGE}$$

Huge  $\delta g_{bR}$  probably requires tree level NP, hard to find in plausible extensions of the SM but not impossible:

e.g., **b-Q** mixing (Choudury-Tait-Wagner, Morrissey-Wagner)  
 or **Z-Z'** mixing (He-Valencia, Djouadi-Moreau-Richard)

# Systematic uncertainty

$$\mathbf{x}_W(\mathbf{A}_{LR}, \mathbf{A}_{FB}^{\ell}, \mathbf{A}_{e,\tau}) : \quad \chi^2/N = 1.6/2 \quad \text{CL} = 0.44$$

3 very different techniques

Common systematic errors very unlikely

$$\mathbf{x}_W(\mathbf{A}_{FB}^b, \mathbf{A}_{FB}^c, \mathbf{Q}_{FB}) : \quad \chi^2/N = 0.02/2 \quad \text{CL} = 0.99$$

Challenging and complex measurements and analysis

Many shared systematic issues, e.g.,

- 14 parameter heavy flavor fit
- Disentangling  $b \rightarrow e^-, \bar{c} \rightarrow e^-, \bar{b} \rightarrow \bar{c} \rightarrow e^-$
- QCD and hadronization

although quoted error for  $A_{FB}^b$  is predominantly statistical

# 14 parameter Heavy Flavor fit

$x_W( A_{FB}^b, A_{FB}^c, Q_{FB} )$  are very tightly clustered:  
 $\chi^2/N = 0.02/2 \quad CL = 0.99$

$A_{FB}^b, A_{FB}^c$  extracted from 14 parameter HF fit,  
 $\chi^2/N = 53/91 \quad CL = \mathbf{0.9995}$

suggests possibility of imperfectly understood systematics

EWVG: systematic errors too conservative?

Suppose all HF fit sys errors  $\rightarrow 0$

$\longrightarrow \chi^2/N = 92/91 \quad CL = \mathbf{0.45}$

**But:**  $CL \{ x[A_{LR}] \oplus x[A_{FB}^b] \} = \mathbf{0.0016} \quad \longrightarrow \mathbf{0.0007}$

$CL \{ x_W^{\ell, \text{eff}} \} = \mathbf{0.04} \quad \longrightarrow \mathbf{0.02}$

$CL \{ SM \} = \mathbf{0.14} \quad \longrightarrow \mathbf{0.03}$

*Stat. errors  
only for  
 $A_{FB}^{b,c},$   
 $A_{b,c}, R_{b,c}$*

## b and c quark identification

$b \rightarrow e^-$  and  $\bar{c} \rightarrow e^-$  are backgrounds for one another:  
 $b \longleftrightarrow \bar{c}$  mistags are consistent with signs of  
both the  $A_{\text{FB}}^b$  and  $A_{\text{FB}}^c$  anomalies.

Mistags due to primary charm,  $Z \rightarrow \bar{c}c$ , and secondary charm,  $\bar{b} \rightarrow \bar{c} \rightarrow e^-$

Mistags are highly leveraged in  $A_{\text{FB}}^b$ : 1% mistag for primary charm would shift  $A_{\text{FB}}^b$  by  $+1\sigma$

Cuts specific to the  $A_{\text{FB}}^b$  measurement (which favor high thrust) might affect the mistag rate relative to the rate in the  $R_b$  measurement.

➔ To understand the mistag rate in the  $A_{\text{FB}}^b$  measurement, it could be interesting to extract  $R_b$  with  $A_{\text{FB}}^b$  analysis cuts and compare with expectation.

# QCD and hadronization

- QCD corrections (1 + 2 loop) are large:

$$\Delta_{\text{QCD}} \sim 3 \Delta_{\text{EXPT}}$$

Altarelli-Lampe,  
Catani-Seymour,  
Ravindran-  
van Neerven

- Hadronization contributes to systematic uncertainty
  - hadronic thrust axis differs from partonic
  - event selection and analysis cuts favoring high thrust introduce a bias in event topologies which diminishes QCD correction by an amount that cannot be precisely determined. For  $B \rightarrow \ell + X$ ,  
bias correction  $\sim 1/2 \Delta_{\text{QCD}} \sim \Delta_{\text{EXPT}}$  (from JETSET)

Most  
important }

EWVG estimate, based on comparing diff JETSET tunes:

$$\text{QCD/hadronization error} \sim 1/4 \Delta_{\text{EXPT}}$$

but uncertainty of the uncertainty estimate is difficult to quantify

# Systematic error: summary

- $x^\ell[A_L]: A_{LR}, A_{FB}^\ell, A_{e,\tau}$        $\chi^2/N = 1.6/2$      $CL = 0.44$ 
    - relatively simple & clean experimentally
    - no QCD or hadronic Monte Carlo corrections
    - 3 very different techniques: common sys error very unlikely
  - $x^\ell[A_H]: A_{FB}^b, A_{FB}^c, Q_{FB}$        $\chi^2/N = 0.02/2$      $CL = 0.99$ 
    - experimentally challenging: flavor tag & charge
    - big QCD corr'ns with detector-dependent bias, estimated with hadronic Monte Carlo + detector simulation.
- ➔ Unique, correlated experimental & theoretical systematics which may be difficult to quantify

If  $A_{FB}^b, A_{FB}^c, Q_{FB}$  have underestimated sys. error,  $x_W^\ell$  is most reliably obtained from  $A_{LR}, A_{FB}^\ell, A_{e,\tau}$

# Consequences of underestimated systematic error

Without excluding the possibility of statistical fluctuation or new physics, we explore the implications of underestimated systematic error as the explanation of the anomaly.

Assume  $A_{FB}^b$ ,  $A_{FB}^c$ ,  $Q_{FB}$  have underestimated systematic errors and remove from fit.

➡ SM fit improves

**CL: 0.14 → 0.77**

but tension with LEP II increases:

**$m_H$ : 89 → 61**

**CL( $m_H > 114$ ): 0.23 → 0.03**

**$m_H(95\%)$ : < 151 → < 105**

	Experiment	SM Fit	Pull
$A_{LR}$	0.1513 (21)	0.1498	0.7
$A_{FB}^l$	0.01714 (95)	0.01684	0.3
$A_{e,\tau}$	0.1465 (32)	0.1498	-1.0
$m_W$	80.399 (23)	80.400	-0.001
$\Gamma_Z$	2495.2 (23)	2496.4	-0.5
$R_l$	20.767 (25)	20.743	1.0
$\sigma_h$	41.540 (37)	41.480	-1.6
$R_b$	0.21629 (66)	0.21581	0.7
$R_c$	0.1721 (30)	0.1724	-0.05
$A_b$	0.923 (20)	0.935	-0.6
$A_c$	0.670 (27)	0.669	0.03
$m_t$	173.1 (1.3)	173.3	0.1
$\Delta\alpha_5(m_Z^2)$	0.02758 (35)	0.02754	0.1
$\alpha_S(m_Z)$		0.118	
$\chi^2/\text{dof}$		5.7/9	
CL( $\chi^2$ )		<b>0.77</b>	
$m_H$		<b>61</b>	
CL( $m_H > 114$ )		<b>0.03</b>	
$m_H(95\%)$		<b>105</b>	

# Consequences of underestimated systematic error

Without excluding the possibility of statistical fluctuation or new physics, we explore the implications of underestimated systematic error as the explanation of the anomaly.

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$m_H$ : 89 → 61

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$m_H(95\%)$ : < 151 → < 105

$\delta m_t^{\text{EXPT}} \times 2$

→ 61

→ 0.05

→ < 114



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**$m_H(95\%)$ : < 151 → < 105**

$\Delta\alpha_5$  from Hagiwara et al.:

$$\Delta\alpha_5 = 0.02760 (15)$$

→ 58

→ 0.017

→ < 97

# Dissecting the Higgs mass prediction

The  $m_H$  prediction in the SM fit, with  $CL(17.3,11) = 0.14$ ,

$$m_H = 89 \text{ GeV}, \quad < 151 \text{ GeV (95\%)}$$

is dominated by three observables,  $A_{LR}$ ,  $A_{FB}^b$ ,  $m_W$  (+  $m_t$ ,  $\Delta\alpha_5$ )

$$m_H = 89 \text{ GeV}, \quad < 156 \text{ GeV (95\%)}$$

with a poor fit,  $CL(11.6,2) = 0.003$ , casting doubt on reliability of the SM  $m_H$  prediction, regardless of the anomaly's origin.

Separately:

$$A_{LR}: \quad m_H = 37 \text{ GeV}, \quad < 110 \text{ GeV (95\%)}$$

$$m_W: \quad m_H = 61 \text{ GeV}, \quad < 126 \text{ GeV (95\%)}$$

$$A_{FB}^b: \quad m_H = 187 \text{ GeV}, \quad 187 < m_H < 1+ \text{ TeV}$$

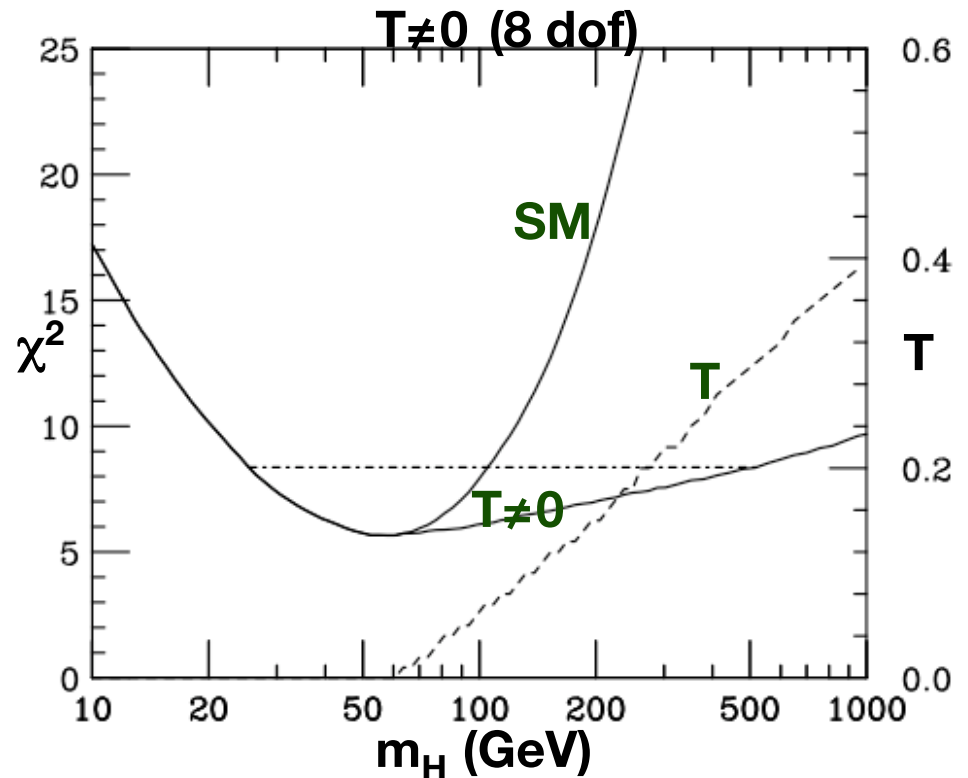
$A_{LR} - m_W$  alliance explains why  $A_{FB}^b$  has biggest pull in SM fit

# New Physics with Custodial SU(2) breaking

NP with  $SU(2)_{\text{Custodial}}$  breaking can raise  $m_H$  while preserving good  $\chi^2$  fit.

Dash-dotted line denotes sym 90% confidence interval:

SM:  $m_H < 105$  95%  
T  $\neq$  0:  $m_H < 520$  95%



At  $m_H = 520$  GeV, oblique NP fit has  $CL(8.4,8) = 0.40$

But not really so easy: oblique NP typically comes with other corrections ( $S \neq 0$  or non-oblique effects) that can degrade the fit.

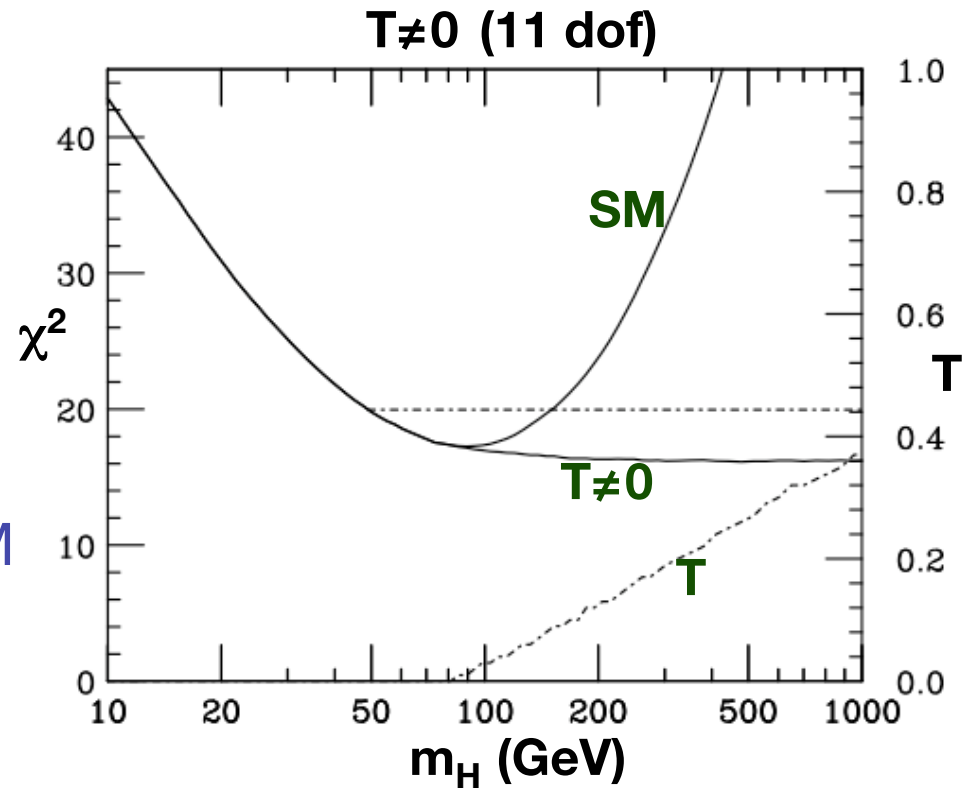
# T≠0 fit to full data set

Fit to full data set, including hadronic asymmetries, has very flat  $\chi^2$  for large  $m_H$

Dash-dotted line denotes sym 90% confidence interval for SM

SM:  $m_H < 151$  95%

T ≠ 0:  $m_H < 1+ \text{TeV}$



CL of oblique fit at large  $m_H$  is  $\sim \text{CL}(16.2, 11) = 0.13$ , similar to SM fit with  $\text{CL}(17.3, 12) = 0.14$

# Example 1: a fourth family

If a 4'th family is discovered the consequences would be at least as profound as those which emerged from the discovery of the 3'rd family, including the possibility of a role in EWSB.

Contrary to popular urban legend, a 4'th family can be consistent with PEW data.  
(Only please tell me why  $m_\nu > m_Z/2 \dots$ )

He *et al.* 2001  
Novikov *et al.* 2002  
Tait *et al.* 2007

Mass splitting in 4'th family quark and lepton doublets provides  $SU(2)_{\text{Custodial}}$  breaking,  $T > 0$ , which raises  $m_H$  and can remove tension with LEP II bound for data set without  $A_{\text{FB}}^b$ ,  $A_{\text{FB}}^c$ ,  $Q_{\text{FB}}$ , as first shown by Novikov *et al.*

Mixing between 3'rd and 4'th families of order  $\theta_{\text{Cabibbo}}$  is allowed and can further increase  $m_H$  prediction.

MC. 2009

# Setup

Choose  $m_{b'} = m_{t'} - 55 \text{ GeV}$

$$\left\{ \begin{array}{l} \text{PEW fits require} \\ |m_{t'} - m_{b'}| \sim 45\text{--}75 \text{ GeV} \end{array} \right.$$

$$m_{\nu_4} = 100 \quad m_{l_4} = 145$$

Little effect on fit

CDF:  $m_T > 311, \quad m_B > 338$

Assume predominantly 3-4 mixing,  $s_{34} = \sin\theta_{34}$

$$T_4 = \frac{1}{8\pi x_W(1-x_W)} \left\{ 3 \left[ F_{t'b'} + s_{34}^2 (F_{t'b} + F_{tb'} - F_{tb} - F_{t'b'}) \right] + F_{l_4\nu_4} \right\}$$

$$F_{12} = \frac{x_1 + x_2}{2} - \frac{x_1 x_2}{x_1 - x_2} \ln \frac{x_1}{x_2} \quad x_i = m_i^2 / m_Z^2$$

Include other non-decoupling effects:  $S_4$  and  $Z_{bb}$

# Results: reduced data set

Example:  $m_T = 500$  GeV

Resolves tension with LEP II

$$\theta_{34} = 0:$$

$$m_H = 89$$

$$\text{CL}(m_H > 114) = 0.28$$

$$\text{CL}(\chi^2) = 0.36$$

At 95% CL limit for  $\theta_{34}$ ,

$$s_{34} = 0.11$$

$$m_H = 280$$

$$\text{CL}(m_H > 114) = 1.0$$

$$\text{CL}(\chi^2) = 0.13$$

	Experiment	SM	Pull	SM <sub>4</sub>	Pull	$s_{34}$ [95%]	Pull
$A_{LR}$	0.1513 (21)	0.1503	0.5	0.1483	1.4	0.1474	1.8
$A_{FB}^l$	0.01714 (95)	0.01694	0.2	0.1649	0.7	0.01630	0.9
$A_{e\tau}$	0.1465 (32)	0.1503	-1.2	0.1483	-0.6	0.1474	-0.3
$m_W$	80.398 (25)	80.403	0.03	80.423	-1.0	80.425	-1.1
$\Gamma_Z$	2495.2 (23)	2496.0	-0.3	2498.5	-1.4	2499.2	-1.7
$R_\ell$	20.767 (25)	20.741	1.0	20.729	1.5	20.725	1.7
$\sigma_h$	41.540 (37)	41.482	1.6	41.489	1.4	41.491	1.3
$R_b$	0.21629 (66)	0.21584	0.7	0.21586	0.6	0.2157	1.0
$R_c$	0.1721 (30)	0.1722	-0.04	0.1722	-0.03	0.1722	-0.05
$A_b$	0.923 (20)	0.935	-0.6	0.935	-0.6	0.935	-0.6
$A_c$	0.670 (27)	0.669	0.03	0.668	0.06	0.668	0.08
$m_t$	172.6 (1.4)	172.3	0.2	172.3	0.2	172.3	0.2
$\Delta\alpha_S(m_Z)$	0.02758 (35)	0.02754	0.1	0.02747	0.3	0.2732	0.7
$\alpha_S(m_Z)$		0.1174		0.1162		0.1168	
$m_\nu$				500		500	
$s_{34}$				0.0		0.11	
$T_4$				0.20		0.35	
$S_4$				0.15		0.15	
$x_\nu$				0.0		0.00028	
$m_H$		50		89		280	
$\text{CL}(m_H > 114)$		0.03		0.28		1.0	
$m_H(95\%)$		105		174		480	
$\chi^2/\text{dof}$		5.6/9		9.8/9		13.7/9	
$\text{CL}(\chi^2)$		0.78		0.36		0.13	

Table 5: Global fits for the data set without the hadronic asymmetry measurements: the SM, the 4 family SM with  $m_\nu = 500$  GeV and  $s_{34} = 0$ , and again with  $s_{34}$  at the 95% confidence level.

# Results: full data set

$$m_T = 500 \text{ GeV}$$

Resolves (slight) tension with LEP II

$$\theta_{34} = 0:$$

$$m_H = 139$$

$$\text{CL}(m_H > 114) = 0.67$$

$$\text{CL}(\chi^2) = 0.15$$

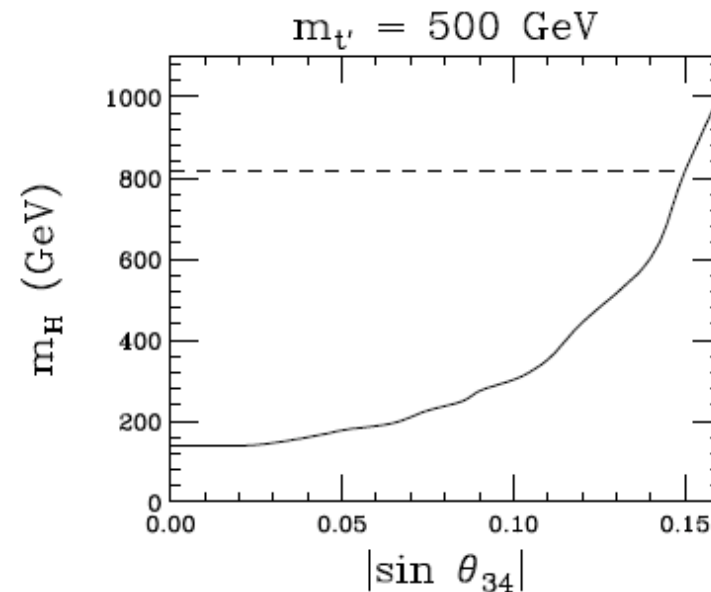
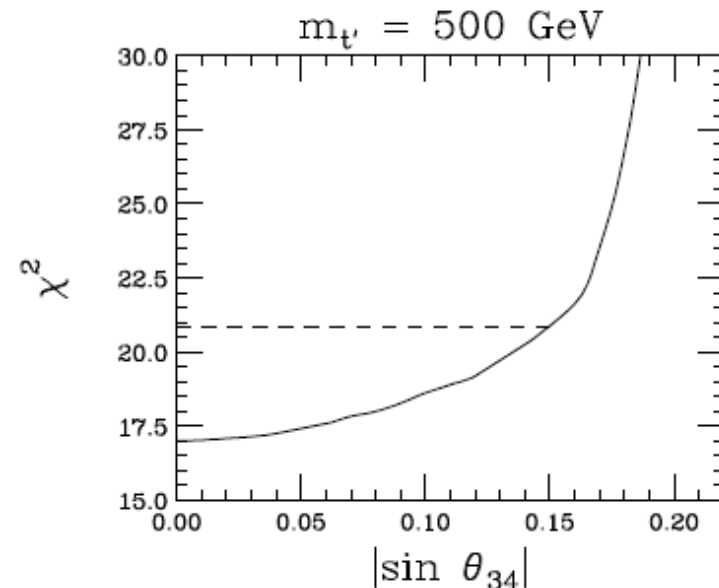
At 95% CL limit for  $\theta_{34}$ ,

$$s_{34} = 0.15$$

$$m_H = 1000+$$

$$\text{CL}(m_H > 114) = 1.0$$

$$\text{CL}(\chi^2) = 0.05$$





# Summary: $m_T = 300 \longrightarrow 1000$ GeV

$m_\nu$	$T_4$	$m_H(\text{GeV})$	$ s_{34}^{(1)} $	$ s_{34}^{(2)}  \pm \Delta_{tB}^{(2)}$	$ c_{34}^{(2)} $
300	0.46	760	0.32	$0.35 \pm 0.001$	0.94
326	0.47	760	0.28	$0.30 \pm 0.002$	0.95
389	0.48	760	0.21	$0.23 \pm 0.004$	0.97
400	0.47	800	0.20	$0.22 \pm 0.005$	0.98
500	0.48	810	0.15	$0.17 \pm 0.007$	0.99
600	0.48	800	0.12	$0.14 \pm 0.010$	0.99
654	0.48	820	0.11	$0.13 \pm 0.013$	0.99
1000	0.49	820	0.07	$0.11 \pm 0.10$	0.99

All data

$m_\nu$	$T_4$	$m_H(\text{GeV})$	$ s_{34}^{(1)} $	$ s_{34}^{(2)}  \pm \Delta_{tB}^{(2)}$	$ c_{34}^{(2)} $
300	0.35	300	0.25	$0.26 \pm 0.0008$	0.97
326	0.35	280	0.21	$0.22 \pm 0.0010$	0.98
389	0.35	270	0.16	$0.17 \pm 0.0016$	0.99
400	0.35	290	0.15	$0.16 \pm 0.0016$	0.99
500	0.35	270	0.11	$0.12 \pm 0.0027$	0.99
600	0.35	290	0.087	$0.095 \pm 0.0033$	0.995
654	0.35	280	0.078	$0.086 \pm 0.0035$	0.996
1000	0.35	270	0.048	$0.059 \pm 0.007$	0.998

Without  $A_{FB}^b$ ,  $A_{FB}^c$ ,  $Q_{FB}$

$T_4$  and  $m_H$  at 95% CL upper limits on  $\theta_{34}$

Fits at  $\theta_{34} = 0$  for all  $m_T$  are similar to fits for  $m_T = 500$  GeV

$s_{34}^{(2)}/s_{34}^{(1)}$  indicates reliability of perturbation theory, showing breakdown at  $m_T = 1$  TeV, especially for “all data” fit.

$\pm \Delta_{tB}^{(2)}$  indicates reliability of two loop results (which are not completely known)

## Example 2: anomaly-free Z'

Consider U(1) extensions of the SM which are anomaly-free without extending fermion sector beyond known quarks & leptons

$$\longrightarrow Q_X = \cos\theta_X \frac{Y}{2} + \sin\theta_X \frac{B-L}{2}$$

MC Ellis Gaillard  
Appelquist *et al.*

Z - Z' mixing decreases  $m_Z$ , equivalent to  $T > 0$

$$\alpha T_X = -\frac{\delta m_Z^2}{m_Z^2} = \frac{r^2 \cos^2 \theta_X}{\hat{m}_{Z'}^2}$$

$$r = \frac{g_{Z'}}{g_Z}$$

Z - Z' mixing angle:  $\theta_M = \frac{r \cos \theta_X}{\hat{m}_{Z'}}$

$$\hat{m}_{Z'} = \frac{m_{Z'}}{m_Z}$$

Zff couplings are then modified by Z' admixture,

$$\mathcal{L}_f = g_Z \left(1 + \frac{\alpha T_X}{2}\right) g_f' \bar{f} Z f \quad g_f' = g_f + r \theta_M q_X^f$$

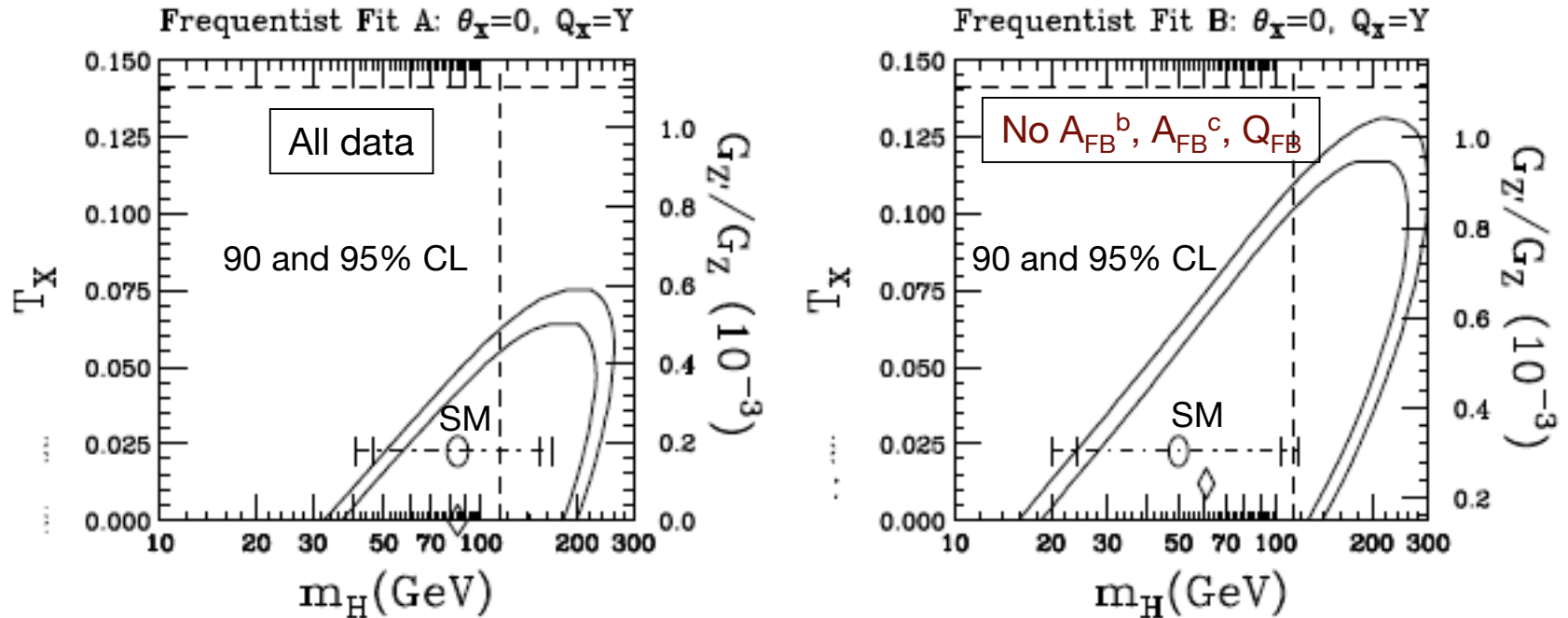
while  $x_W$  and  $m_W$  are corrected by  $T_X$

# Z' fits

Example:  $\theta_X = 0, Q_X = Y/2$

arXiv:0806.0890  
for survey of all  $\theta_X$

– occurs in many BSM models, e.g., little Higgs



• Horizontal dashed line: upper limit from LEP II contact interactions [Carena et al.](#)

• Right axis:  $G_{Z'}/G_Z = g_{Z'}^2/g_Z^2 \cdot m_Z^2/m_{Z'}^2$

$m_H$  reach to 300 GeV at 95% CL (little change in central value – diamond)

E.g., for  $g_{Z'} = g_Z, m_{Z'} \approx 2 - 5$  TeV, probably within reach of LHC

# What about NuTeV?

## SM fits with NuTeV

A) With  $A_{FB}^b$ ,  $A_{FB}^c$

$$m_H = 94$$

$$CL(m_H > 114) = 0.33$$

$$CL(\chi^2) = 0.02$$

B) Without  $A_{FB}^b$ ,  $A_{FB}^c$

$$m_H = 64$$

$$CL(m_H > 114) = 0.07$$

$$CL(\chi^2) = 0.12$$

➡ Tension with LEP II  
moderated but not  
eliminated

	Experiment	A	Pull	B	Pull
$A_{LR}$	0.1513 (21)	0.1476	1.8	0.1494	0.9
$A_{FB}^l$	0.01714 (95)	0.01634	0.8	0.1674	0.4
$A_{e,\tau}$	0.1465 (32)	0.1476	-0.3	0.1494	-0.9
$A_{FB}^b$	0.0992 (16)	0.1035	-2.7		
$A_{FB}^c$	0.0707 (35)	0.0739	-0.9		
$m_W$	80.398 (25)	80.369	1.2	80.391	0.3
$\Gamma_Z$	2495.2 (23)	2495.7	0.2	2496.1	-0.4
$R_l$	20.767 (25)	20.743	1.0	20.743	1.0
$\sigma_h$	41.540 (37)	41.477	1.7	41.479	1.7
$R_b$	0.21629 (66)	0.21586	0.7	0.21584	0.7
$R_c$	0.1721 (30)	0.1722	-0.04	0.1722	-0.04
$A_b$	0.923 (20)	0.935	-0.6	0.935	-0.6
$A_c$	0.670 (27)	0.668	0.07	0.669	0.04
$g_L^2$	0.30005 (137)	0.30396	-2.9	0.30423	-3.1
$g_R^2$	0.03076 (11)	0.03009	0.6	0.03004	0.7
$x_W(ee)$	0.23339 (140)	0.23145	1.4	0.23122	1.55
$x_W(Cs)$	0.22939 (190)	0.23145	-1.1	0.23122	-1.0
$m_t$	172.6 (1.4)	172.3	0.2	172.3	0.2
$\Delta\alpha_5(m_Z)$	0.02758 (35)	0.02768	-0.3	0.02754	0.1
$\alpha_S(m_Z)$		0.1186		0.118	
$m_H$		94		64	
$CL(m_H > 114)$		0.33		0.07	
$m_H(95\%)$		172		124	
$\chi^2/\text{dof}$		28.4/15		19.0/13	
$CL(\chi^2)$		0.02		0.12	

Table 1: SM fits with (A) and without (B)  $A_{FB}^b$  and  $A_{FB}^c$ .

# Z' fits: NuTeV

arXiv:0903.2497

- Status unclear:  $3\sigma \rightarrow 2\sigma$  from  $\bar{s}s$  sea asymmetry measurement?
- Z' models raise  $m_H$  central value and 95% limit in fits with NuTeV

For fits without

$A_{FB}^b, A_{FB}^c, Q_{FB}$ :

- $m_H$  central value increases by factor  $\sim 2$

- $\chi^2$  decreases and in some cases  $CL(\chi^2)$  improves modestly

Model	$T_X$	$\chi^2$	$CL(\chi^2)$	$m_H$	$CL(m_H > 114)$	$m_H^{95\%}(\text{Freq.})$
SM		19.0	0.12	64	0.07	124
$\theta_X = 0$	0.052	17.9	0.12	120	0.56	215
$\theta_X = \pi/12$	0.052	17.4	0.14	126	0.58	224
$\theta_X = \pi/6$	0.048	16.9	0.15	126	0.59	223
$\theta_X = \pi/4$	0.046	16.5	0.17	126	0.60	230
$\theta_X = \pi/3$	0.037	16.1	0.19	126	0.60	223

Original (NO  $A_{FB}^b, A_{FB}^c, Q_{FB}$ )

Model	$T_X$	$\chi^2$	$CL(\chi^2)$	$m_H$	$CL(m_H > 114)$	$m_H^{95\%}(\text{Freq.})$
SM		14.3	0.35	58	0.06	118
$\theta_X = 0$	0.043	13.7	0.32	104	0.42	189
$\theta_X = \pi/12$	0.044	13.3	0.35	109	0.42	197
$\theta_X = \pi/6$	0.043	13.0	0.37	114	0.50	203
$\theta_X = \pi/4$	0.039	12.7	0.39	114	0.50	202
$\theta_X = \pi/3$	0.033	12.4	0.42	109	0.45	201

Revised per  $\bar{s}s$  sea asymmetry measurement  
(NO  $A_{FB}^b, A_{FB}^c, Q_{FB}$ )

# Conclusion

More than one way to read the PEW oracle bones:

- data may favor a light Higgs boson ...
- or maybe it presages NP with custodial SU(2) breaking

PEW data provides important constraints on NP today and will continue to be important to interpret discoveries at LHC

- e.g., discovery of a  $Z'$  and measurement of its parameters would imply a prediction for  $m_H$  from the PEW fit
- discrepancies between LHC observations and the PEW fit could imply additional, still unobserved NP
- interplay of LHC and PEW data can help us to formulate next steps after LHC has run at initial design parameters

To realize the potential of PEW probes, a next generation Z factory could be an important facility, perhaps at the front end of a future LC.