

Status of the Muon $g-2$

Michel Davier (LAL – Orsay)

- the muon magnetic anomaly
- revisited τ spectral functions: Belle + updated corrections
- ee spectral functions after KLOE and BaBar
- combination of all ee data
- discussion and perspectives



Lepton Magnetic Anomaly: from Dirac to QED

$$\vec{\mu} = g \frac{e}{2m} \vec{s},$$

$$a = (g - 2)/2$$

Dirac (1928) $g_e=2$ $a_e=0$

anomaly discovered:

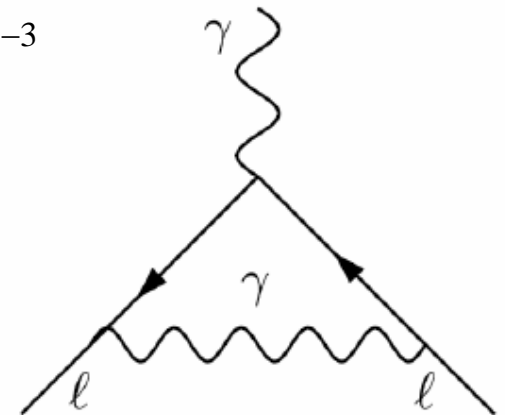
Kusch-Foley (1948) $a_e = (1.19 \pm 0.05) 10^{-3}$

and explained by $O(\alpha)$ QED contribution:

Schwinger (1948) $a_e = \alpha/2\pi = 1.16 10^{-3}$

first triumph of QED

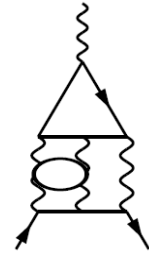
$\Rightarrow a_e$ sensitive to quantum fluctuations of fields



More Quantum Fluctuations

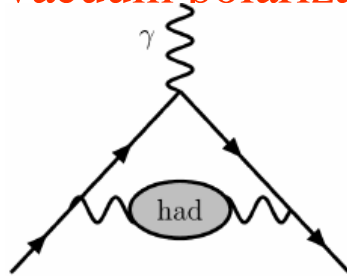
$$a = a^{\text{QED}} + a^{\text{had}} + a^{\text{weak}} + ? a^{\text{new physics ?}}$$

QED up to $O(\alpha^4)$, α^5 in progress (Kinoshita et al.)

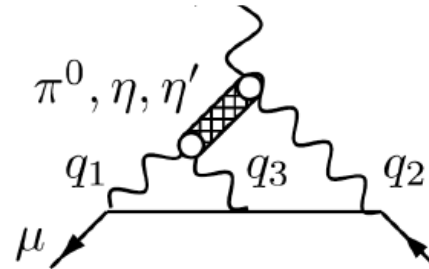


Hadrons

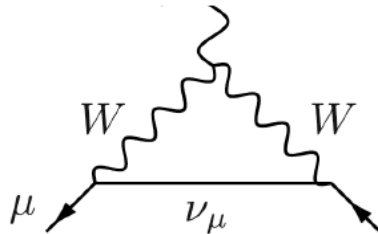
vacuum polarization



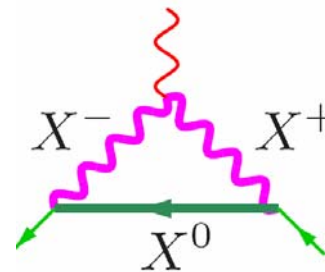
light-by-light (models)



Electroweak



new physics at high mass scale



$$\delta a_e \propto \frac{m_e^2}{M^2}$$

$\Rightarrow a_\mu$ much more sensitive to high scales

Hadronic Vacuum Polarization and Muon $(g-2)_\mu$

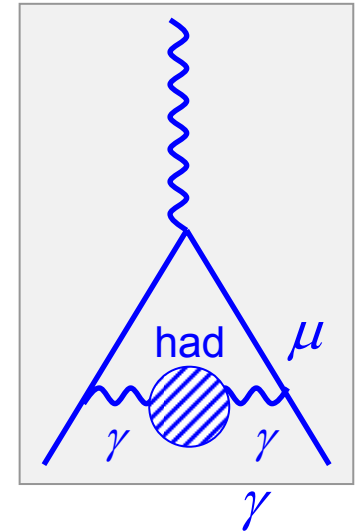
Dominant uncertainty from lowest-order HVP piece

Cannot be calculated from QCD (low mass scale), but one can use experimental data on $e^+e^- \rightarrow \text{hadrons}$ cross section (Bouchiat-Michel 1961)

$$\text{Born: } \sigma^{(0)}(s) = \sigma(s)(\alpha / \alpha(s))^2$$

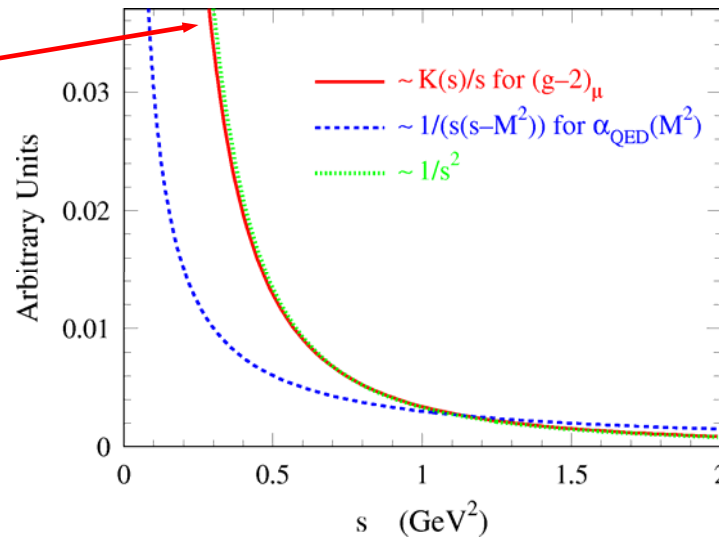
$$12\pi \text{Im}\Pi_\gamma(s) = \frac{\sigma^0[e^+e^- \rightarrow \text{hadrons}(\gamma)]}{\sigma_{pt}} \equiv R(s)$$

$$\text{Im}[\text{Diagram}] \propto |\text{Diagram hadrons}|^2$$



$$a_\mu^{\text{had}} = \frac{\alpha^2}{3\pi^2} \int_{4m_\pi^2}^{\infty} ds \frac{K(s)}{s} R(s)$$

Dispersion relation



The E-821 a_μ Measurement at BNL Updated

a_μ measured from a ratio of frequencies

$$\omega_a = \omega_{\text{precession}} - \omega_{\text{cyclotron}} \quad \omega_{\text{precession}} = \omega_L + \omega_T \quad \omega_a = a_\mu \frac{eB}{m_\mu}$$

$$a_\mu = \frac{\omega_a}{\omega_L - \omega_a} = \frac{\omega_a/\tilde{\omega}_p}{\omega_L/\tilde{\omega}_p - \omega_a/\tilde{\omega}_p} = \frac{\mathcal{R}}{\lambda - \mathcal{R}}$$

$\lambda = \omega_L/\omega_p = \mu_\mu/\mu_p$ from muonium hyperfine splitting

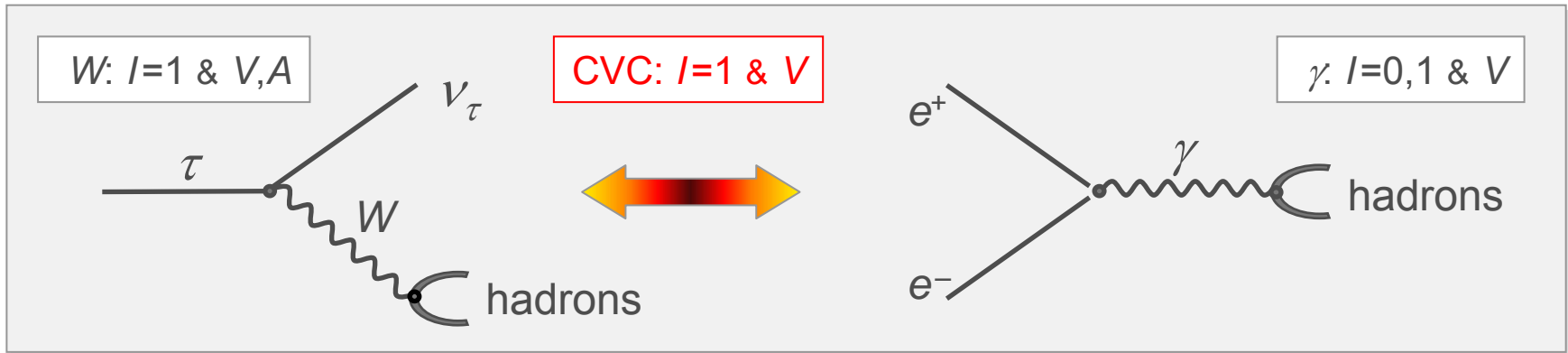
value used by E-821 3.18334539(10)

new value 3.183345137(85) [Mohr et al., RMP 80 \(2008\) 633](#)

\Rightarrow change in a_μ ($+0.92 \cdot 10^{-10}$)
(review in RPP2009 ([Höcker-Marciano](#)))

$a_\mu^{\text{exp}} = (11\,659\,208.9 \pm 5.4 \pm 3.3) \cdot 10^{-10}$ updated
(± 6.3) (0.54 ppm)

The Role of τ Data through CVC – SU(2)



Hadronic physics factorizes (**spectral Functions**)

$$\sigma^{(I=1)}[e^+e^- \rightarrow \pi^+\pi^-] = \frac{4\pi\alpha^2}{s} \nu[\tau^- \rightarrow \pi^-\pi^0\nu_\tau]$$

$$\nu[\tau^- \rightarrow \pi^-\pi^0\nu_\tau] \propto \underbrace{\frac{\text{BR}[\tau^- \rightarrow \pi^-\pi^0\nu_\tau]}{\text{BR}[\tau^- \rightarrow e^-\bar{\nu}_e\nu_\tau]}}_{\text{branching fractions}} \underbrace{\frac{1}{N_{\pi\pi^0}} \frac{dN_{\pi\pi^0}}{ds}}_{\text{mass spectrum}} \underbrace{\frac{m_\tau^2}{(1-s/m_\tau^2)^2 (1+s/m_\tau^2)}}_{\text{kinematic factor (PS)}}$$

R. Alemany, MD, A. Höcker, EPJC 1998

SU(2) Breaking

Corrections for SU(2) breaking applied to τ data for dominant $\pi^-\pi^+$ contrib.:

■ Electroweak radiative corrections:

- ▶ dominant contribution from short distance correction S_{EW}
- ▶ subleading corrections (small)
- ▶ long distance radiative correction $G_{EM}(s)$

Marciano-Sirlin' 88

Braaten-Li' 90

Cirigliano-Ecker-Neufeld' 02
Lopez Castro et al.' 06

■ Charged/neutral mass splitting:

- ▶ $m_{\pi^-} \neq m_{\pi^0}$ leads to phase space (cross sec.) and width (FF) corrections
- ▶ ρ - ω mixing (EM $\omega \rightarrow \pi^-\pi^+$ decay) corrected using FF model
- ▶ $m_{\rho^-} \neq m_{\rho^0}$ *** and $\Gamma_{\rho^-} \neq \Gamma_{\rho^0}$ ***

Alemany-Davier-Höcker' 97, Czyż-Kühn' 01

Flores-Baez-Lopez Castro' 08
Davier et al.'09

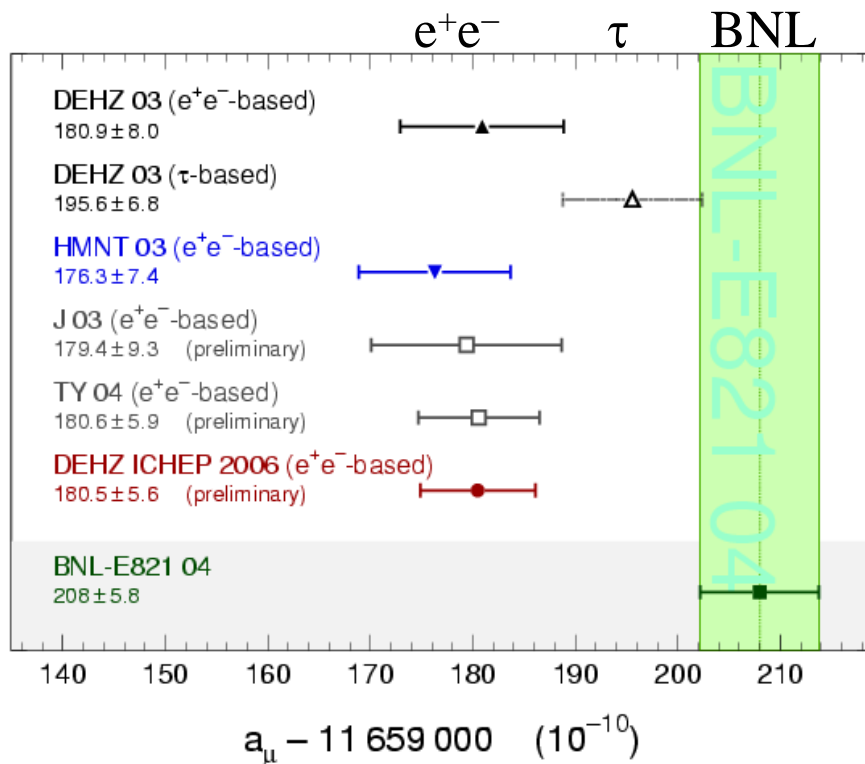
■ Electromagnetic decays: $\rho \rightarrow \pi\pi\gamma$ ***, $\rho \rightarrow \pi\gamma$, $\rho \rightarrow \eta\gamma$, $\rho \rightarrow l^+l^-$

■ Quark mass difference $m_u \neq m_d$ (negligible)

Situation at ICHEP'06 / 08

$$a_{\mu}^{\text{had}} [\text{ee}] = (690.9 \pm 4.4) \times 10^{-10}$$

$$a_{\mu} [\text{ee}] = (11\,659\,180.5 \pm 4.4_{\text{had}} \pm 3.5_{\text{LBL}} \pm 0.2_{\text{QED+EW}}) \times 10^{-10}$$



Hadronic HO $-(9.8 \pm 0.1) \times 10^{-10}$

Hadronic LBL $+(12.0 \pm 3.5) \times 10^{-10}$

Electroweak $(15.4 \pm 0.2) \times 10^{-10}$

QED $(11\,658\,471.9 \pm 0.1) \times 10^{-10}$

Knecht-Nyffeler (2002), Melnikov-Vainhstein (2003)

Davier-Marciano (2004)

Kinoshita-Nio (2006)

Observed Difference with BNL using e^+e^- :

$$a_{\mu} [\text{exp}] - a_{\mu} [\text{SM}] = (27.5 \pm 8.4) \times 10^{-10}$$

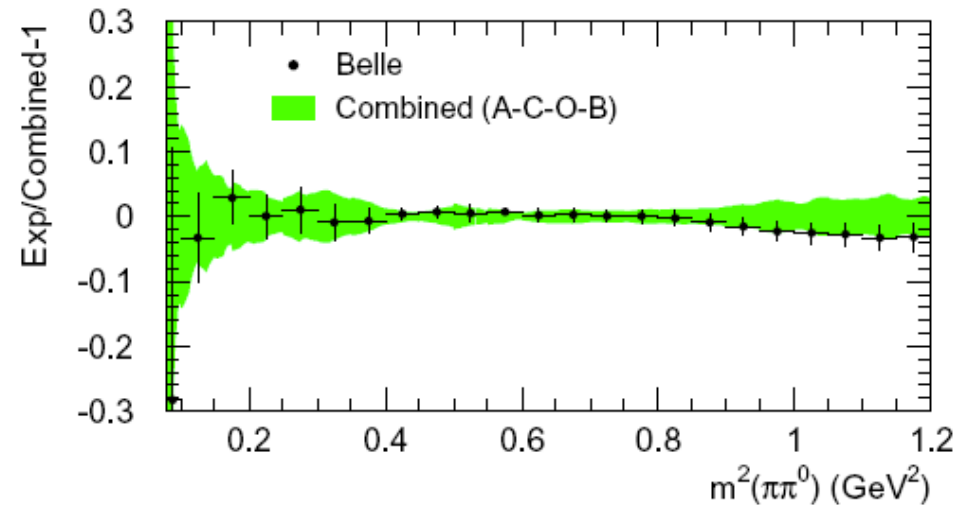
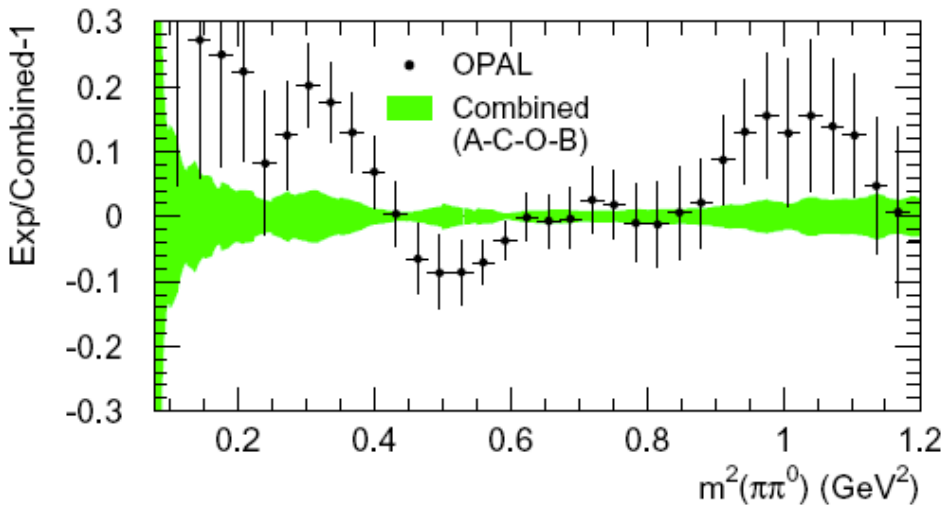
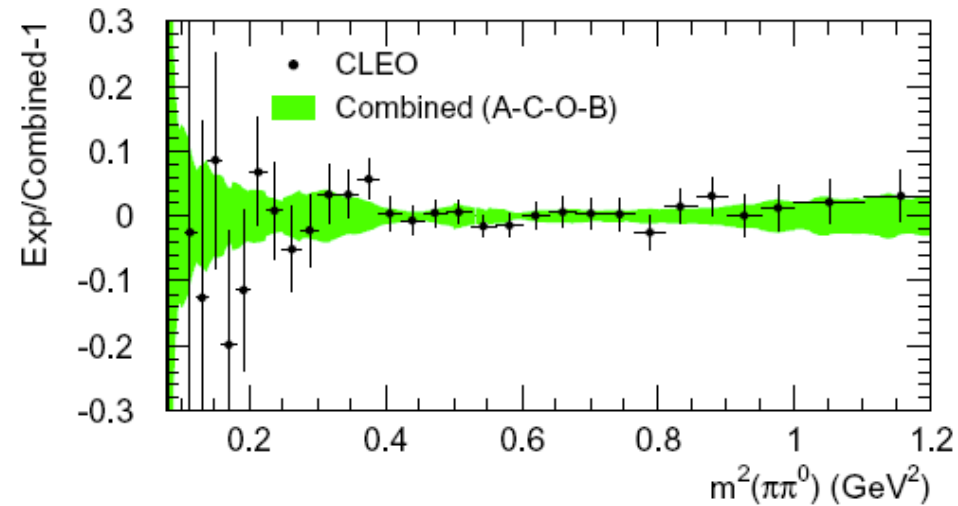
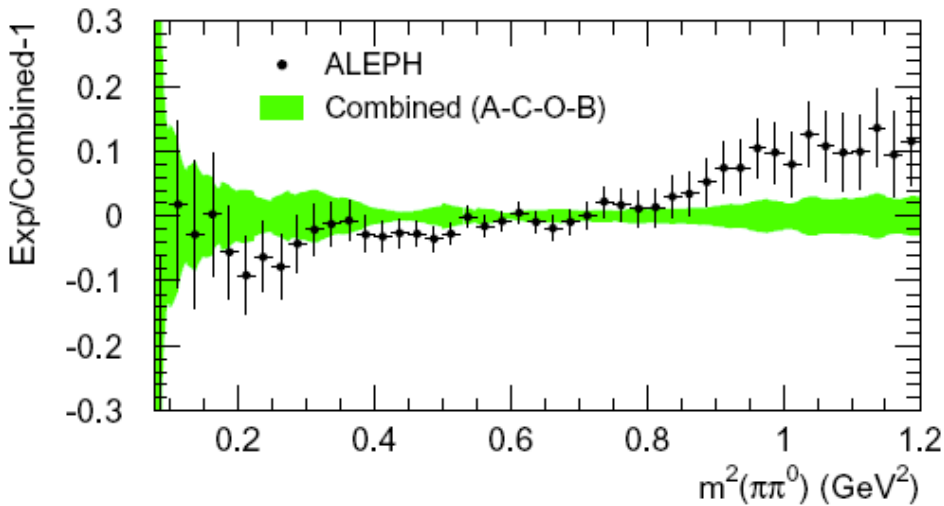
➔ 3.3 „standard deviations“

But estimate using τ data consistent with E-821 !

Most recent data and analyses

- $\tau \rightarrow \pi \pi^0 \nu_\tau$ data from Belle [PRD 78 \(2008\) 072006](#)
- $e^+ e^- \rightarrow \pi^+ \pi^-$ data
 - KLOE [PLB 670 \(2009\) 285](#)
 - BaBar [arXiv:0908.3589v1 \(PRL\)](#)
- updated τ -based analysis [arXiv:0906.5443v3 \(EPJC\)](#)
[MD, A. Hoecker, G. Lopez Castro, B. Malaescu, X.H.Mo, G. Toledo Sanchez, P. Wang, C.Z. Yuan, Z. Zhang](#)
- updated ee-based analysis [arXiv:0908.4300v2 \(EPJC\)](#)
[MD, A. Hoecker, B. Malaescu, C.Z. Yuan, Z. Zhang](#)

Revisited Analysis using τ Data: including Belle



Test of the spectral function shapes from different experiments: WA BR used

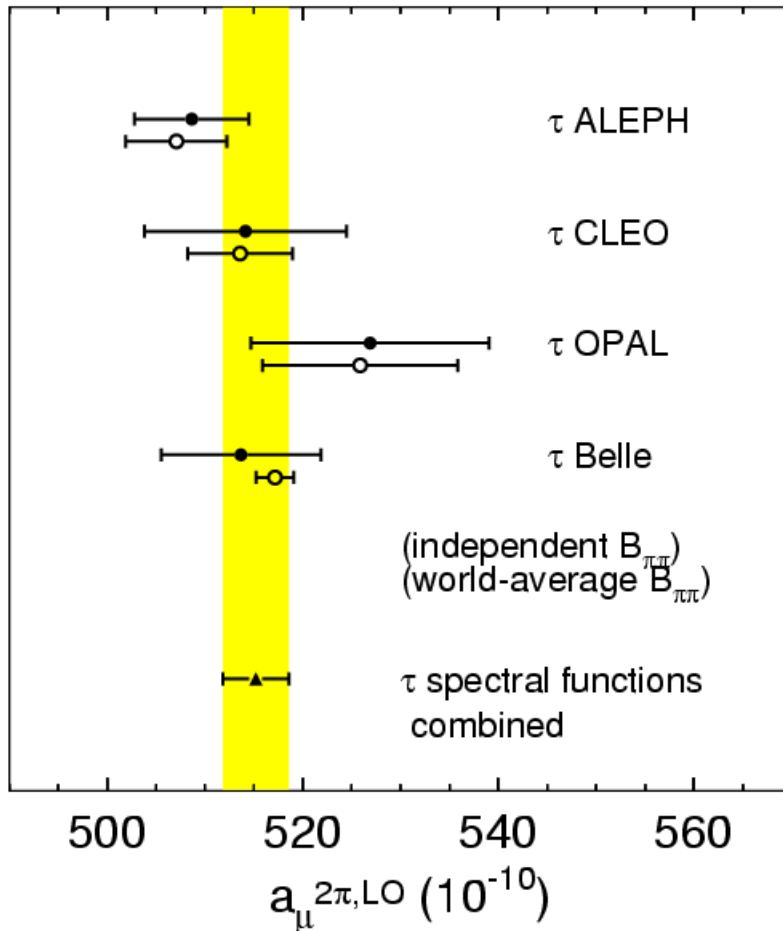
Revisited Analysis τ Data: new IB corrections

Source	$\Delta a_\mu^{\text{had,LO}}[\pi\pi, \tau] (10^{-10})$	
	GS model	KS model
S_{EW}	-12.21 ± 0.15	
G_{EM}	-1.92 ± 0.90	
FSR	$+4.67 \pm 0.47$	
ρ - ω interference	$+2.80 \pm 0.19$	$+2.80 \pm 0.15$
$m_{\pi^\pm} - m_{\pi^0}$ effect on σ	-7.88	
$m_{\pi^\pm} - m_{\pi^0}$ effect on Γ_ρ	$+4.09$	$+4.02$
$m_{\rho^\pm} - m_{\rho_{\text{bare}}^0}$	$0.20^{+0.27}_{-0.19}$	$0.11^{+0.19}_{-0.11}$
$\pi\pi\gamma$, electrom. decays	-5.91 ± 0.59	-6.39 ± 0.64
Total	-16.07 ± 1.22	-16.70 ± 1.23
	-16.07 ± 1.85	

disagreement with
Maltman-Wolfe
arXiv:0908.2391

← large change
since DEHZ (2003)

Consistency of τ Data: Dispersion Integrals



- using BR from each experiment makes results independent from each other
- consistent results (disagreement with Benayoun et al. arXiv:09075603v1)
- using WA BR checks consistency for the spectral function shapes

- WA BR + combined spectral function \Rightarrow

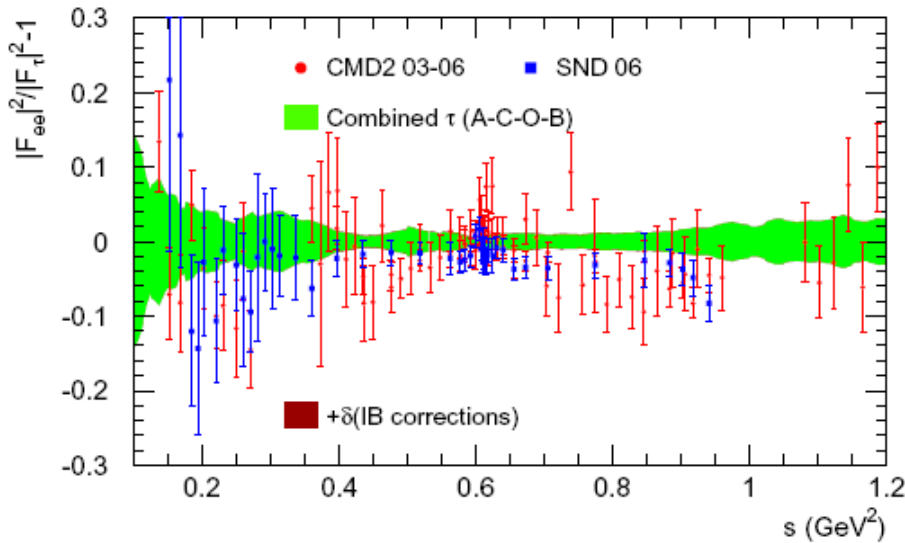
$$a_{\mu}^{2\pi,LO} = (515.2 \pm 2.0_{\text{exp}} \pm 0.9_{B_e} \pm 2.1_{B_{\pi\pi}} \pm 1.6_{IB}) 10^{-10}$$

- 0.7% precision

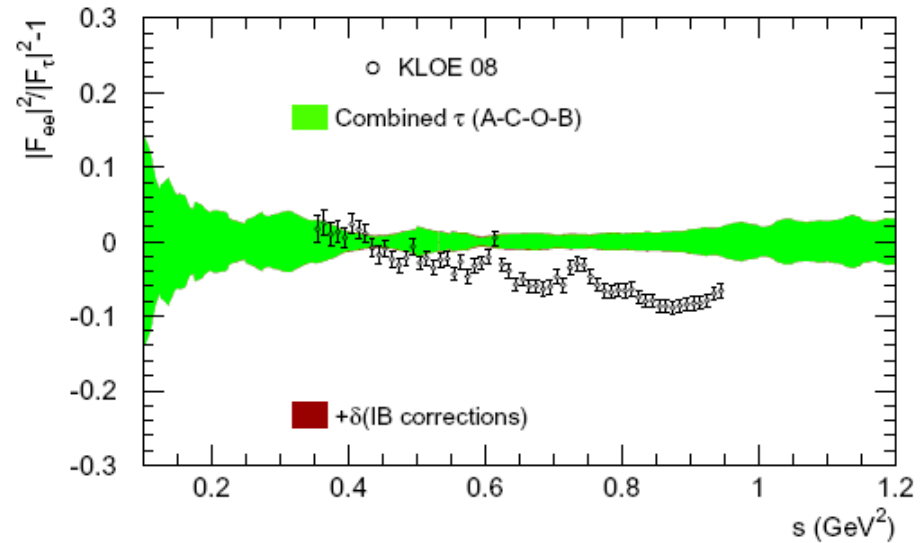
Comparison of ee and τ Data Revisited (1)

Relative comparison of IB-corrected τ and ee spectral functions (τ green band)

CMD-2, SND

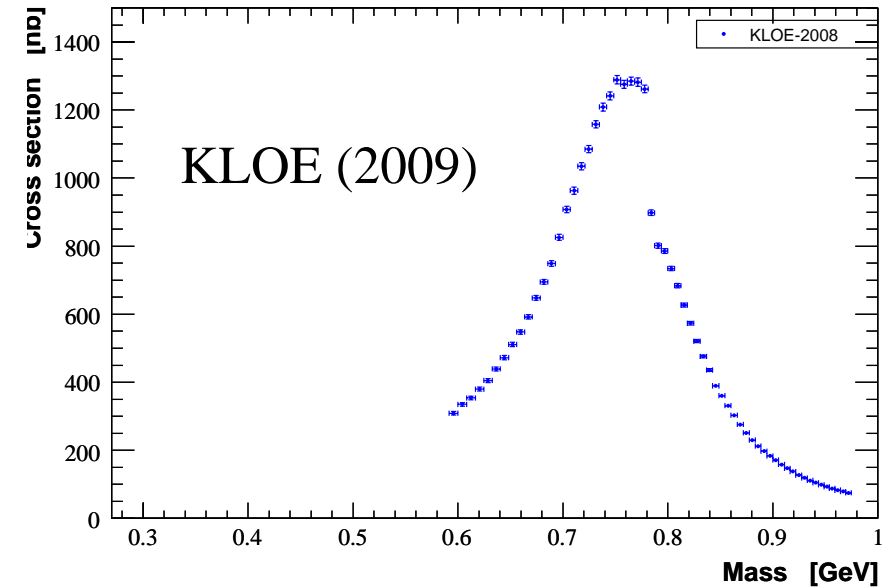
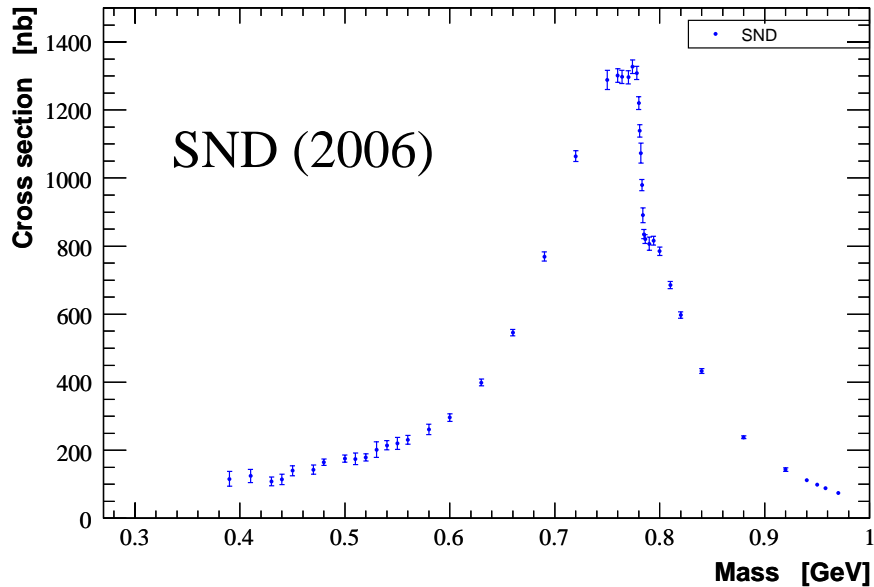
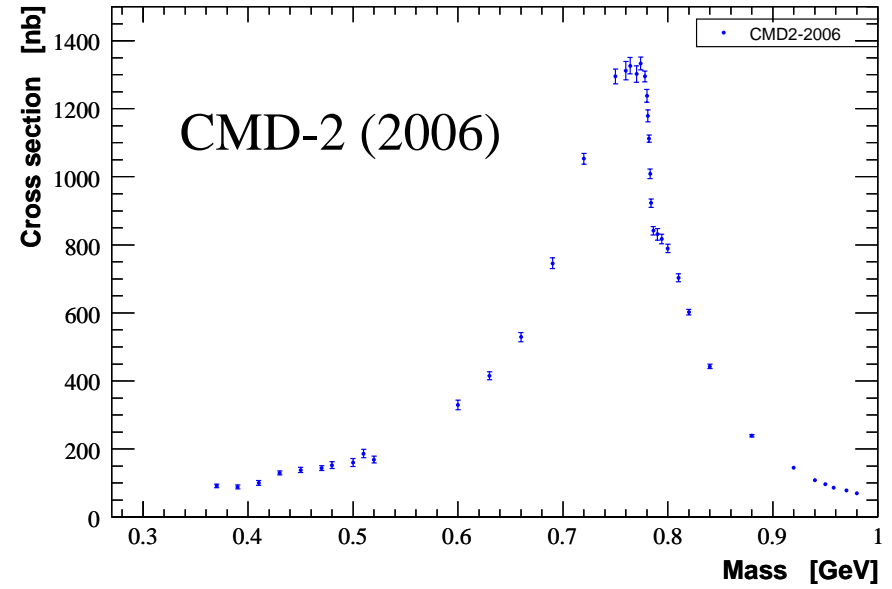
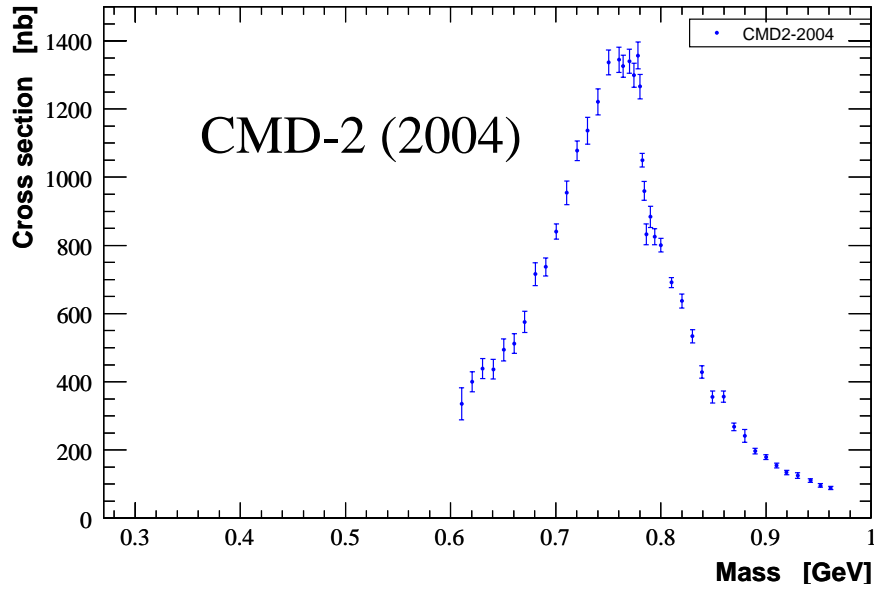


KLOE



- \Rightarrow better agreement than before with CMD2-SND
- \Rightarrow strong disagreement with KLOE : slope...

Data on $e^+e^- \rightarrow \text{hadrons}$

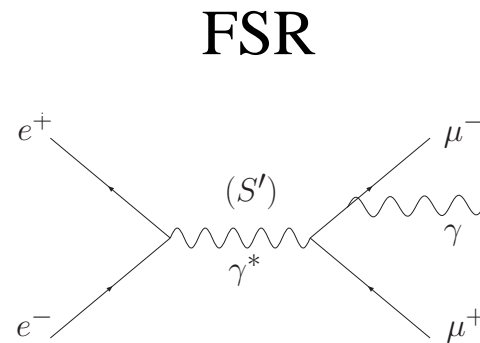
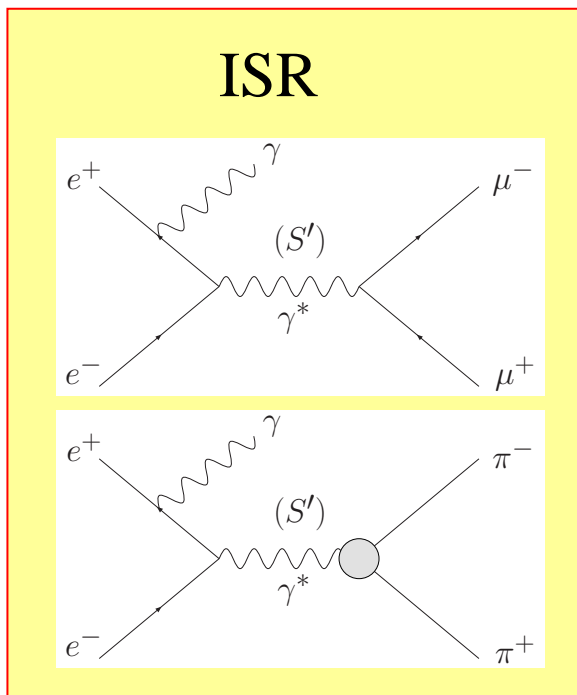


The BaBar Analysis

$e^+ e^- \rightarrow \mu^+ \mu^- \gamma (\gamma)$ and $\pi^+ \pi^- \gamma (\gamma)$ measured simultaneously

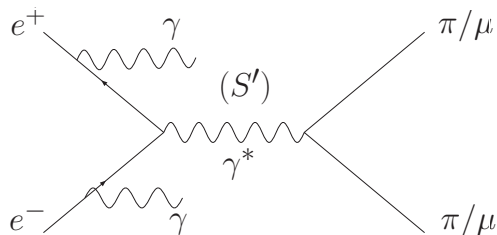
$$x = 2E_{\gamma}^*/\sqrt{s}$$

$$s' = s(1 - x)$$

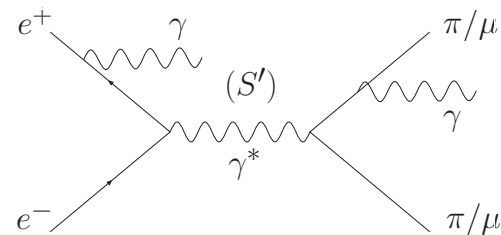


LO FSR negligible for $\pi\pi$
at $s \sim (10.6 \text{ GeV})^2$

ISR + add. ISR

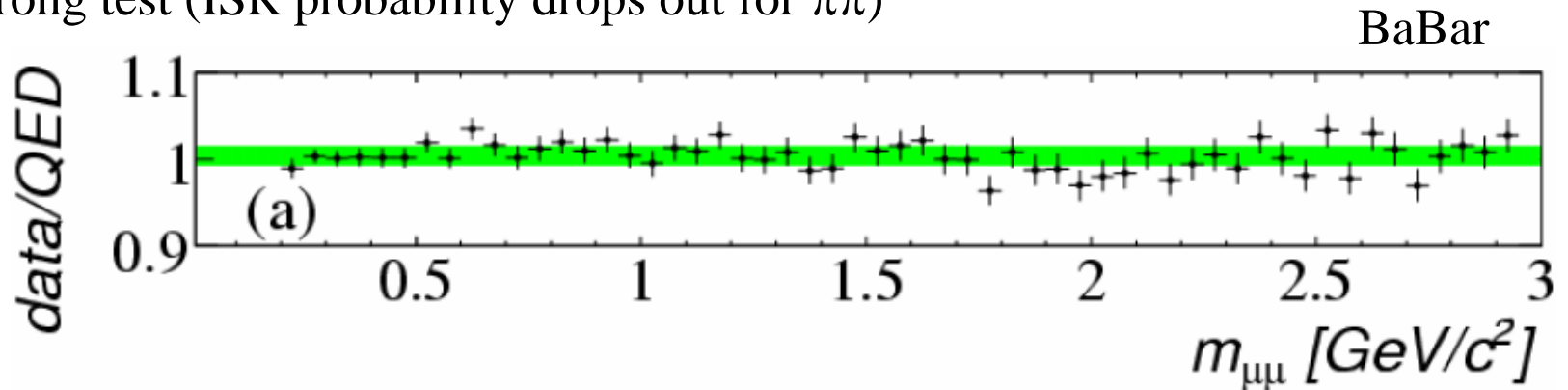


ISR + add. FSR



QED Test with $\mu\mu\gamma$ sample

- absolute comparison of $\mu\mu$ mass spectra in data and in simulation
- simulation corrected for data/MC efficiencies
- AfkQed corrected for incomplete NLO using Phokhara
- strong test (ISR probability drops out for $\pi\pi$)



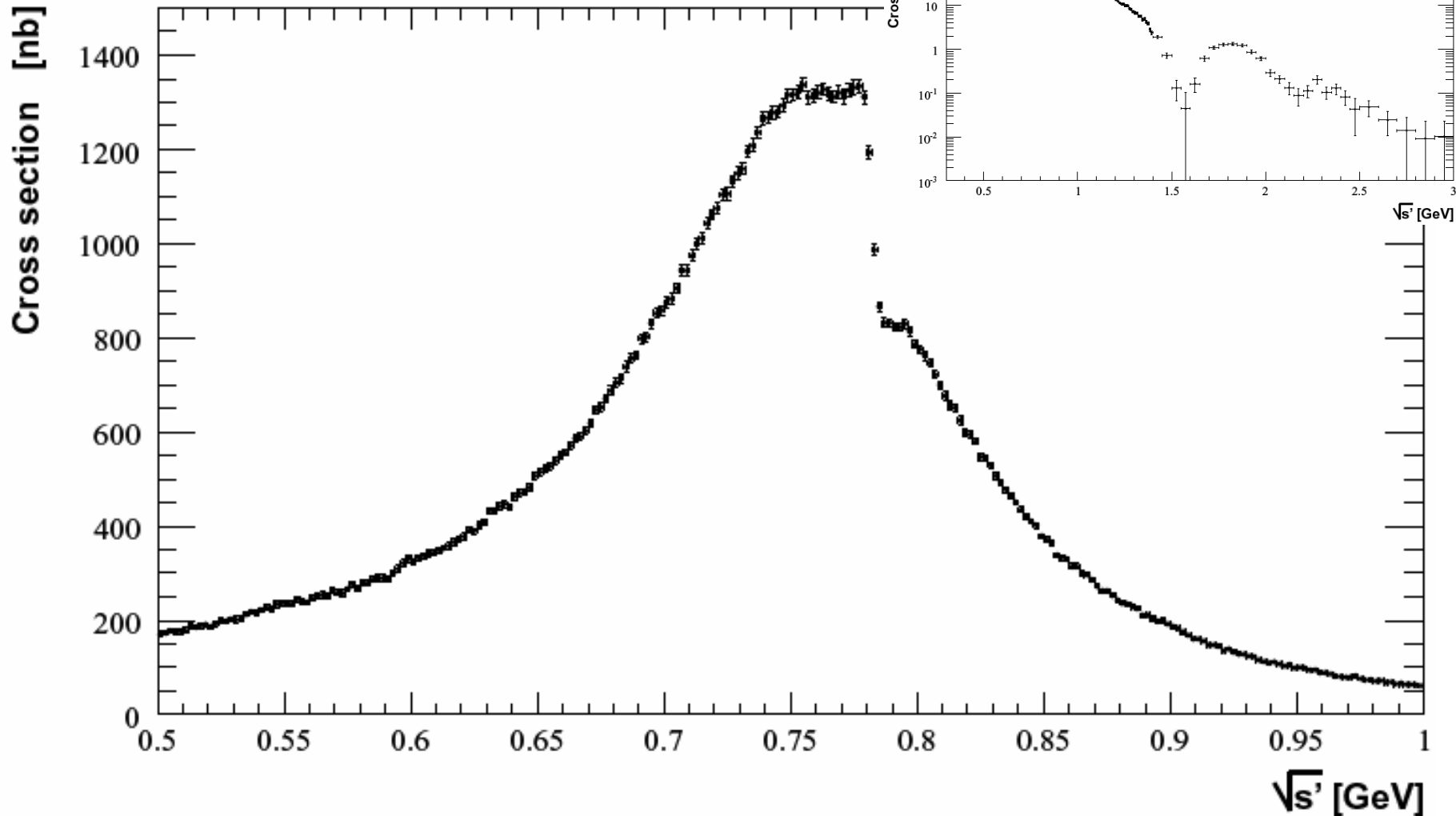
$$\frac{\sigma_{\mu\mu\gamma(\gamma)}^{data}}{\sigma_{\mu\mu\gamma(\gamma)}^{NLO\ QED}} = 1 + (4.0 \pm 1.9 \pm 5.5 \pm 9.4) 10^{-3} \quad (0.2 - 3\ \text{GeV})$$

ISR γ efficiency 3.4 syst.
trig/track/PID 4.0

BaBar ee luminosity

Data on $e^+e^- \rightarrow \text{hadrons}$ (2)

BaBar (PRL Dec 2009)



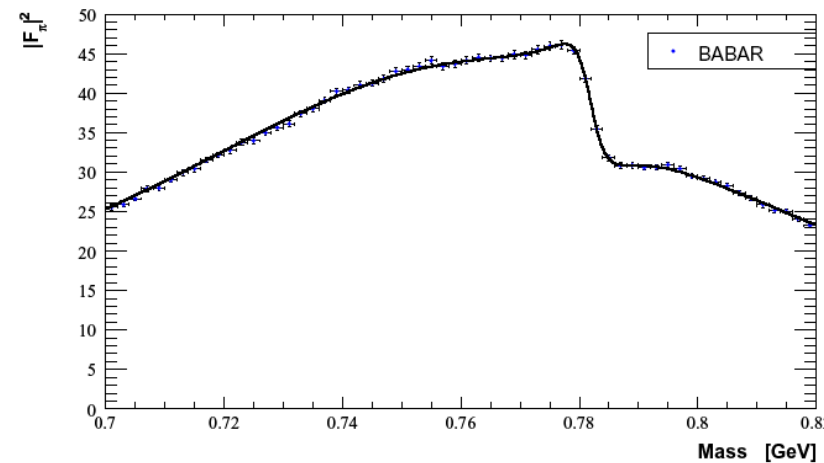
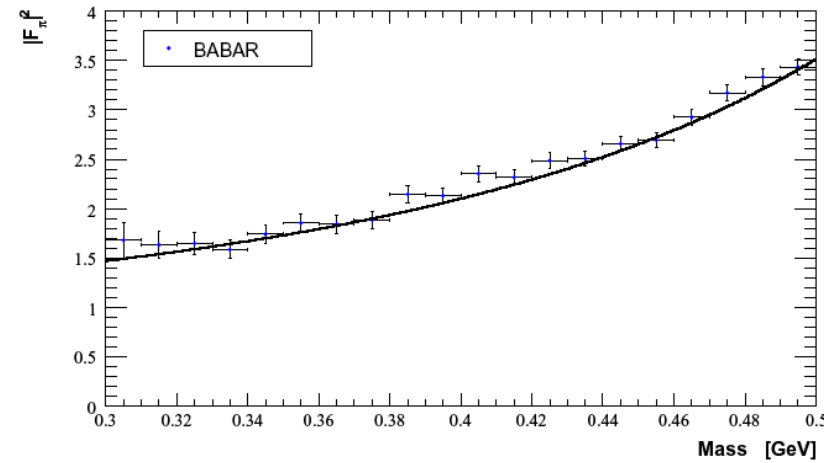
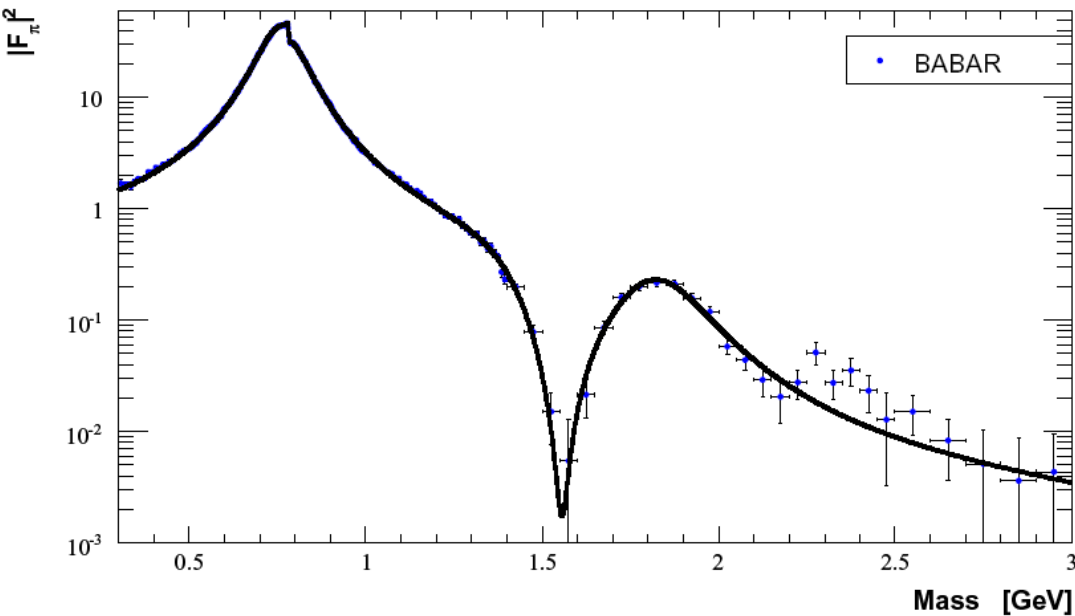
VDM Fit of the BaBar Pion Form Factor

$$F_\pi(s) = \frac{BW_\rho^{GS}(s, m_\rho, \Gamma_\rho) \frac{1 + \alpha BW_\omega^{KS}(s, m_\omega, \Gamma_\omega)}{1 + \alpha} + \beta BW_{\rho'}^{GS}(s, m_{\rho'}, \Gamma_{\rho'}) + \gamma BW_{\rho''}^{GS}(s, m_{\rho''}, \Gamma_{\rho''})}{1 + \beta + \gamma}$$

$$|F_\pi|^2(s') = \frac{3s'}{\pi\alpha^2(0)\beta_\pi^3} \sigma_{\pi\pi}(s')$$

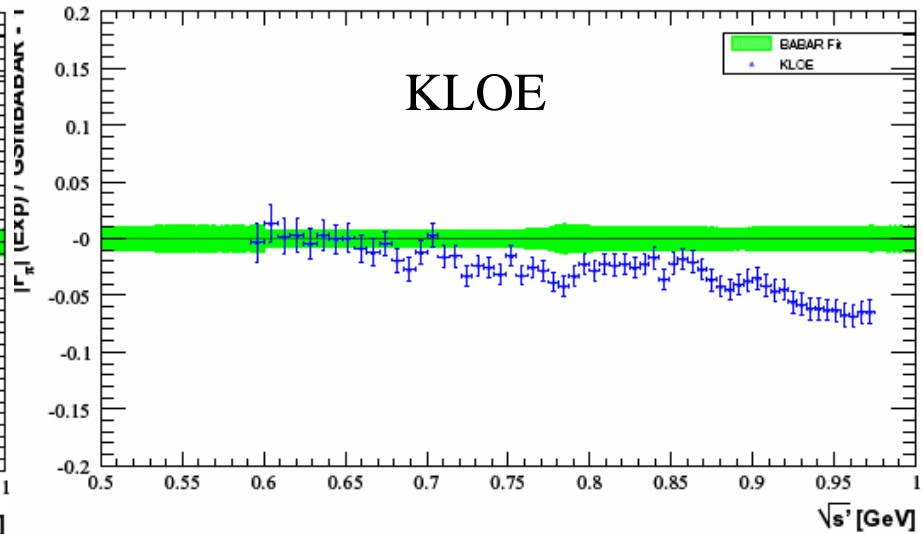
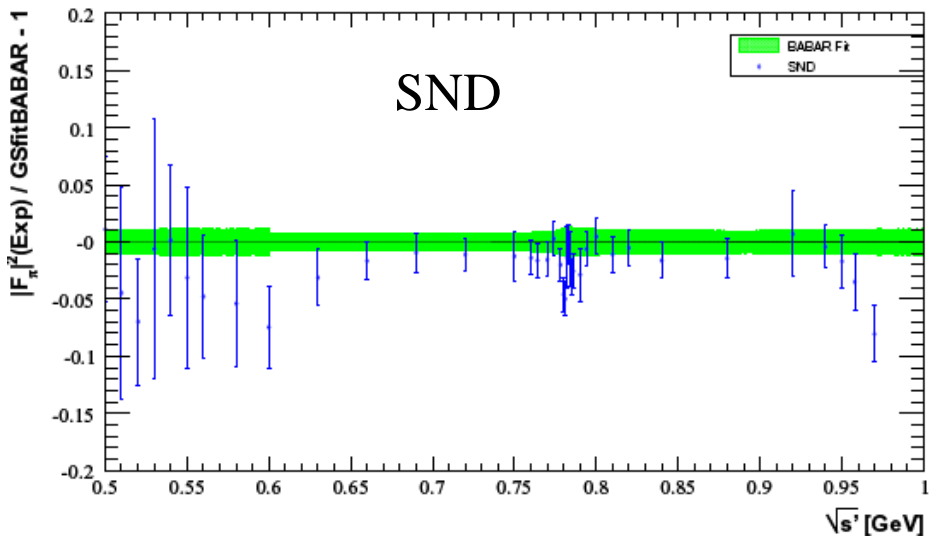
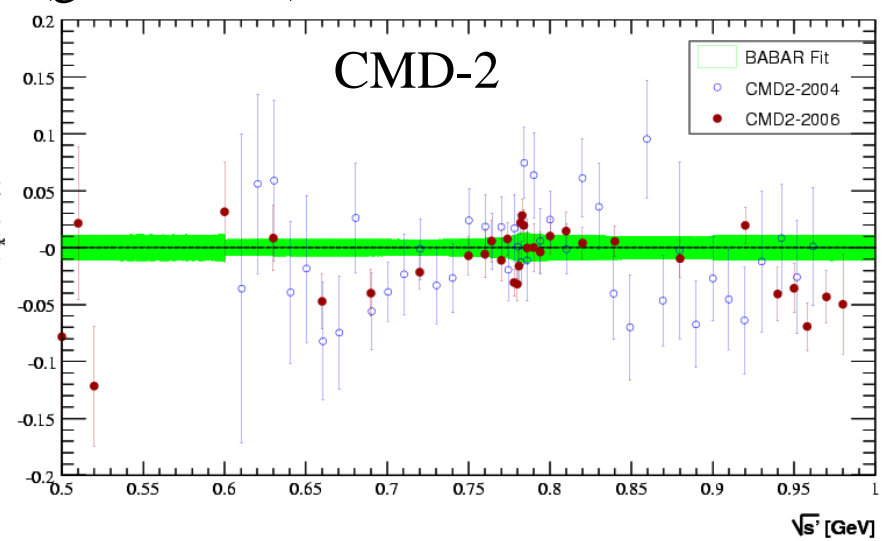
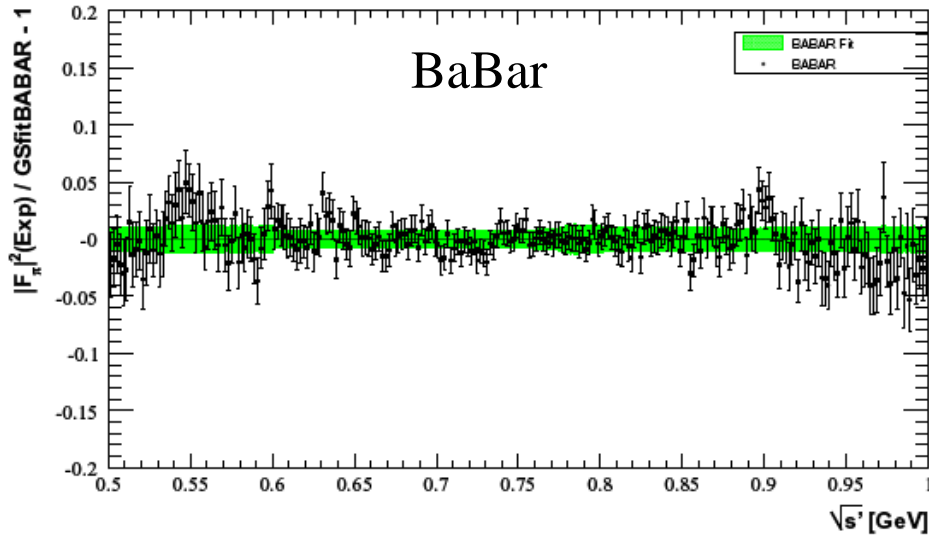
$$\sigma_{\pi\pi}(s') = \frac{\sigma_{\pi\pi(\gamma)}^0(s')}{1 + \frac{\alpha}{\pi}\eta(s')} \left(\frac{\alpha(s')}{\alpha(0)} \right)^2$$

add. FSR α Running (VP)

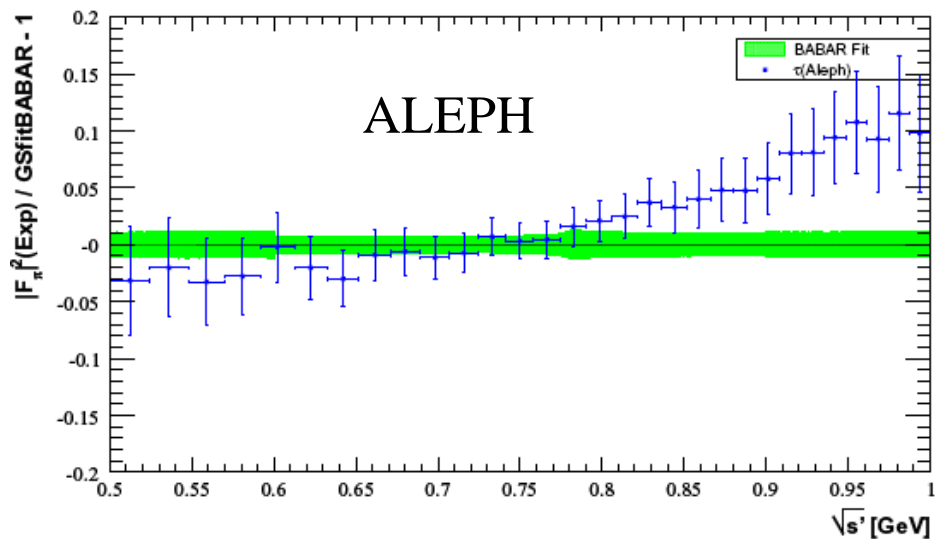


BaBar vs. other ee data (0.5-1.0 GeV)

direct relative comparison of cross sections with BaBar fit (stat + syst errors included)
(green band)



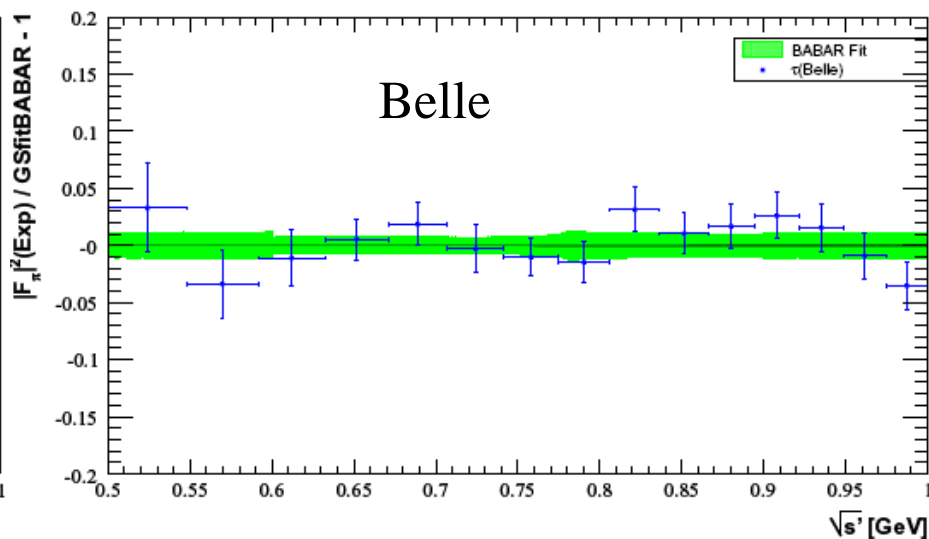
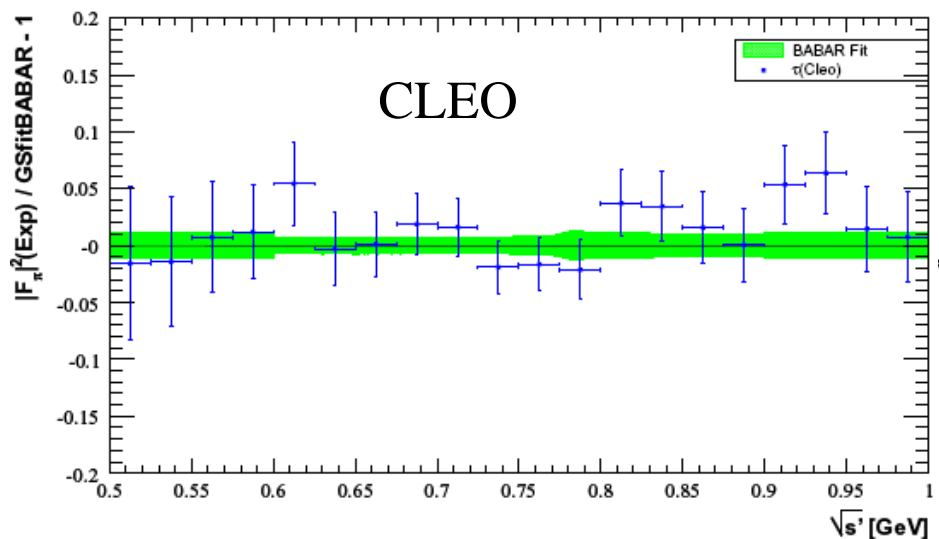
BaBar vs. IB-corrected τ data (0.5-1.0 GeV)



relative comparison w.r.t. BaBar of isospin-breaking corrected τ spectral functions

IB corrections: radiative corr., π masses, ρ - ω interference, ρ masses/widths

each τ data normalized to its own BR

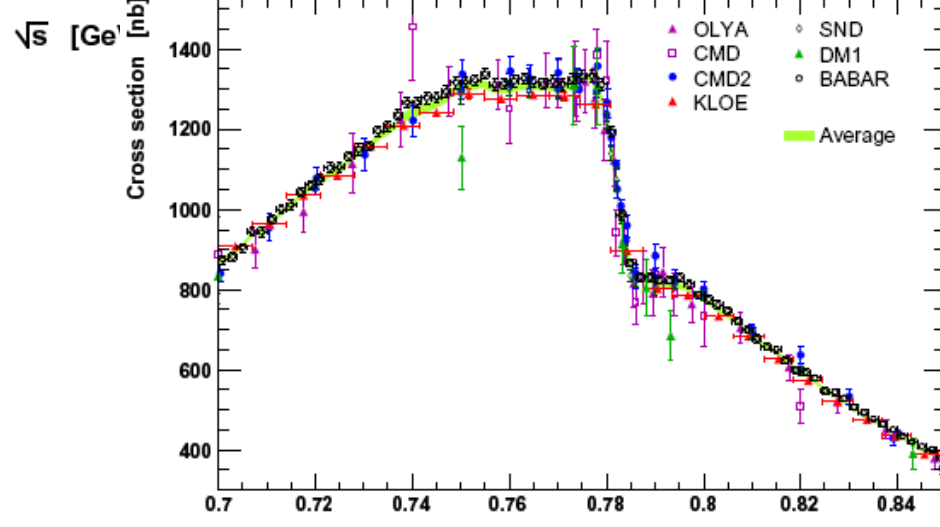
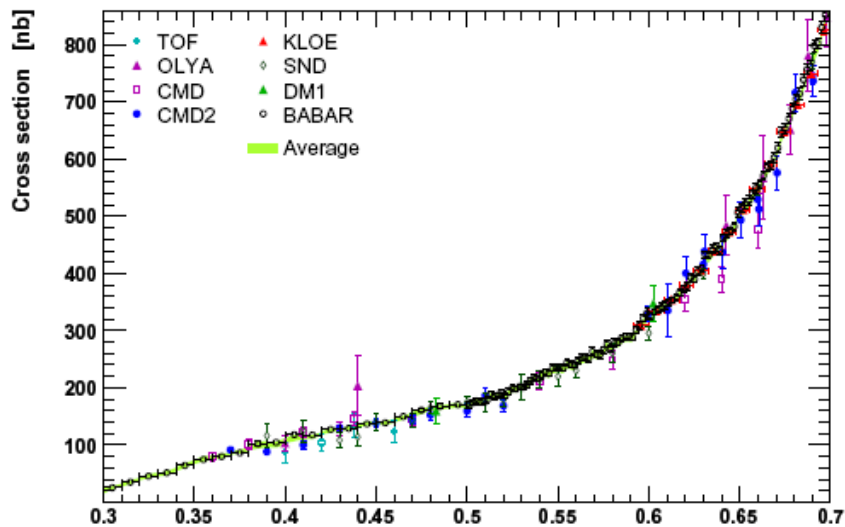
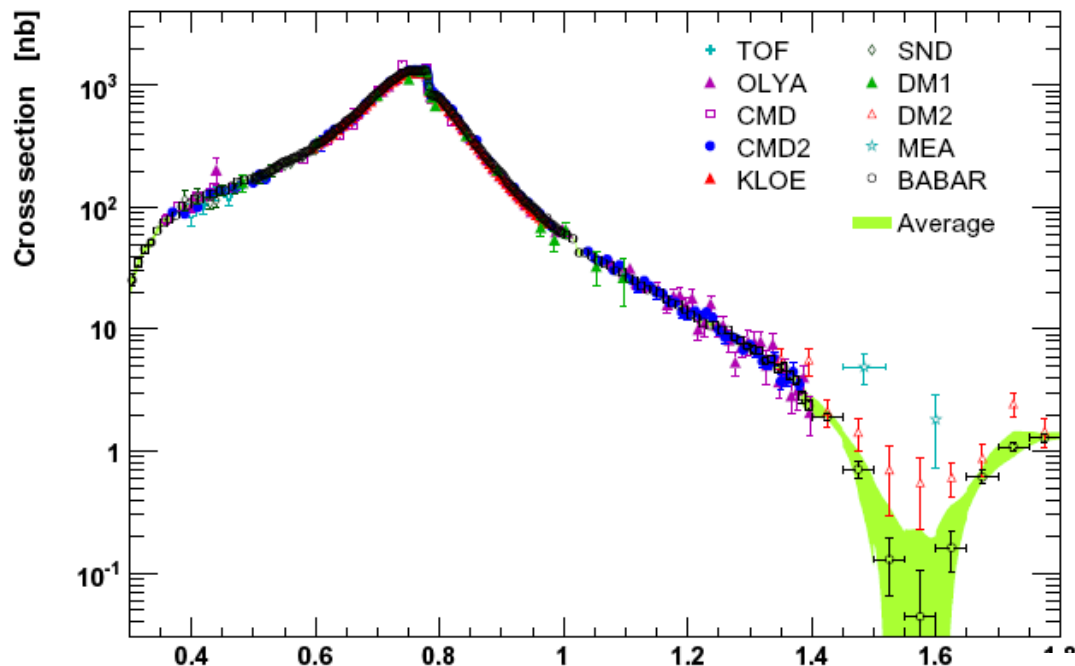


Combination of all e^+e^- Data

arXiv: 0908.4300 (EPJC)

MD-Höcker-Malaescu-Yuan-Zhang

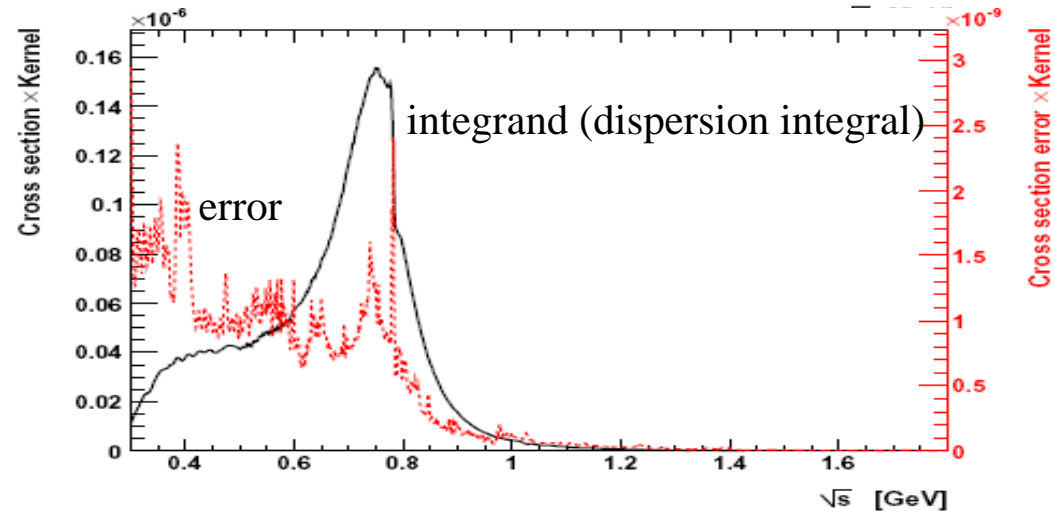
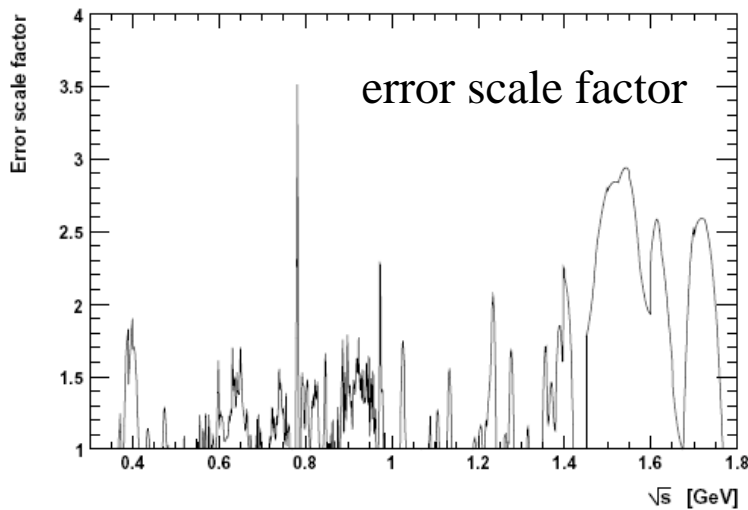
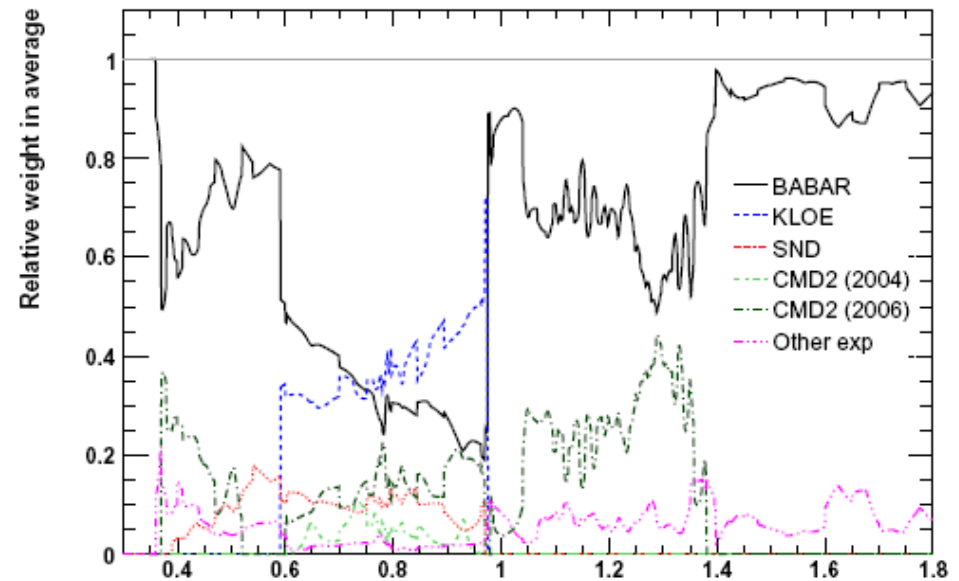
Improved procedure and software (HVPTools) for combining cross section data with arbitrary point spacing/binning



Obtaining the average cross section

- local weighted average performed
- full covariance matrices
- local χ^2 used for error rescaling
- average dominated by BaBar and KLOE, BaBar covering full range

relative weights



Computing $a_{\mu}^{\pi\pi}$ [$2m_{\pi}$, 1.8 GeV]

Energy range (GeV)	Experiment	$a_{\mu}^{\text{had,LO}}[\pi\pi]$ (10^{-10})
$2m_{\pi\pm} - 0.3$	Combined e^+e^- (fit)	0.55 ± 0.01
0.30 – 0.63	Combined e^+e^-	$132.6 \pm 0.8 \pm 1.0$ (1.3 _{tot})
0.63 – 0.958	CMD2 03	$361.8 \pm 2.4 \pm 2.1$ (3.2 _{tot})
	CMD2 06	$360.2 \pm 1.8 \pm 2.8$ (3.3 _{tot})
	SND 06	$360.7 \pm 1.4 \pm 4.7$ (4.9 _{tot})
	KLOE 08	$356.8 \pm 0.4 \pm 3.1$ (3.1 _{tot})
	BABAR 09	$365.2 \pm 1.9 \pm 1.9$ (2.7 _{tot})
	Combined e^+e^-	$360.8 \pm 0.9 \pm 1.8$ (2.0 _{tot})
0.958 – 1.8	Combined e^+e^-	$14.4 \pm 0.1 \pm 0.1$ (0.2 _{tot})
Total	Combined e^+e^-	$508.4 \pm 1.3 \pm 2.6$ (2.9 _{tot})
Total	Combined τ [1]	$515.2 \pm 2.0_{\text{exp}} \pm 2.2_B \pm 1.6_{\text{IB}}$ (3.4 _{tot})

Pre-BaBar combined ee	503.5 ± 3.5
BaBar	514.1 ± 3.8
Combined ee	508.4 ± 2.9
Combined τ	$515.2 \pm 3.0 \pm 1.6$ (3.4)

($\times 10^{-10}$)

Other hadronic contributions

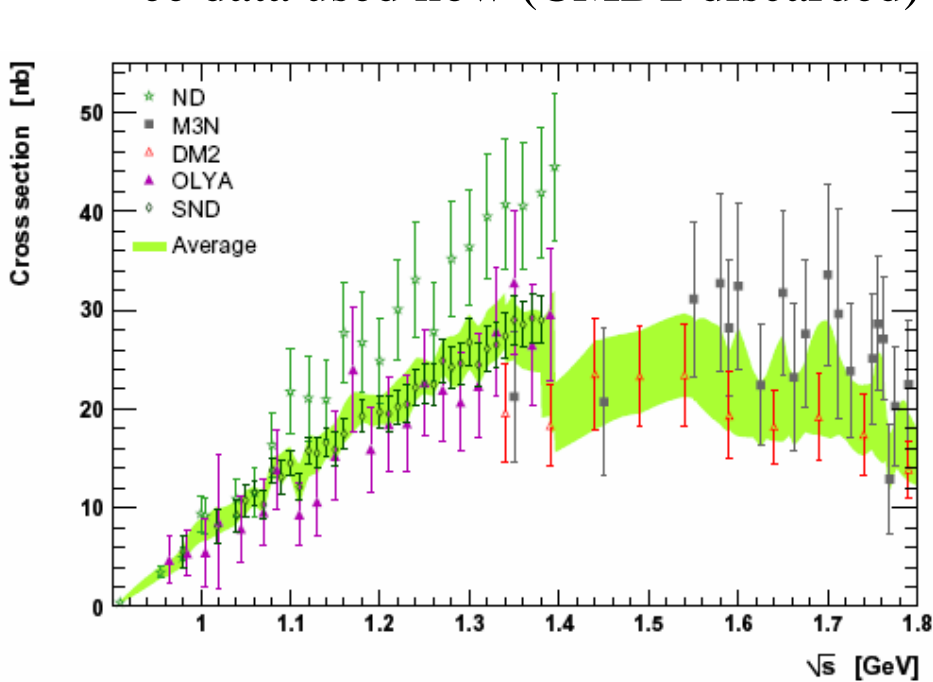
from MD-Eidelman-Höcker-Zhang NP Proc. Suppl. 169 (2007) 288

Modes	Energy [GeV]	e^+e^-	τ
$\pi^+\pi^-2\pi^0$	$2m_\pi - 1.8$	$16.8 \pm 1.3 \pm 0.2_{\text{rad}}$	$21.4 \pm 1.3 \pm 0.6_{\text{SU}(2)}$
$2\pi^+2\pi^-$ (+BaBar)	$2m_\pi - 1.8$	$13.1 \pm 0.4 \pm 0.0_{\text{rad}}$	$12.3 \pm 1.0 \pm 0.4_{\text{SU}(2)}$
ω (782)	0.3 – 0.81	$38.0 \pm 1.0 \pm 0.3_{\text{rad}}$	–
ϕ (1020)	1.0 – 1.055	$35.7 \pm 0.8 \pm 0.2_{\text{rad}}$	–
Other excl. (+BaBar)	$2m_\pi - 1.8$	$24.3 \pm 1.3 \pm 0.2_{\text{rad}}$	–
$J/\psi, \psi(2S)$	3.08 – 3.11	$7.4 \pm 0.4 \pm 0.0_{\text{rad}}$	–
R [QCD]	1.8 – 3.7	$33.9 \pm 0.5_{\text{theo}}$	–
R [data]	3.7 – 5.0	$7.2 \pm 0.3 \pm 0.0_{\text{rad}}$	–
R [QCD]	5.0 – ∞	$9.9 \pm 0.2_{\text{theo}}$	–

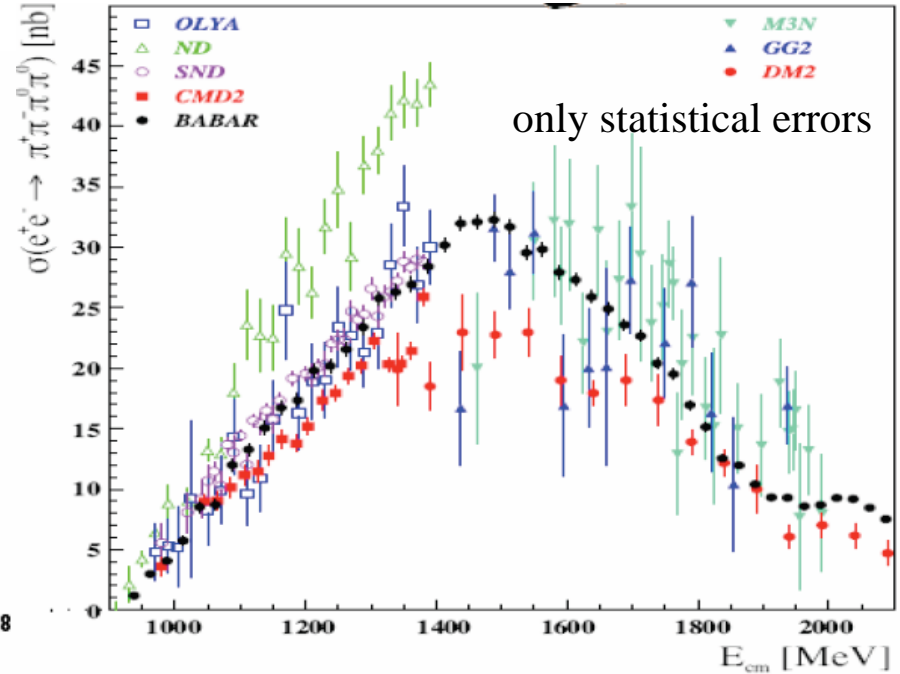
\Rightarrow another large long-standing discrepancy in the $\pi^+\pi^-2\pi^0$ channel !

The Problematic $2\pi 2\pi^0$ Contribution

ee data used now (CMD2 discarded)

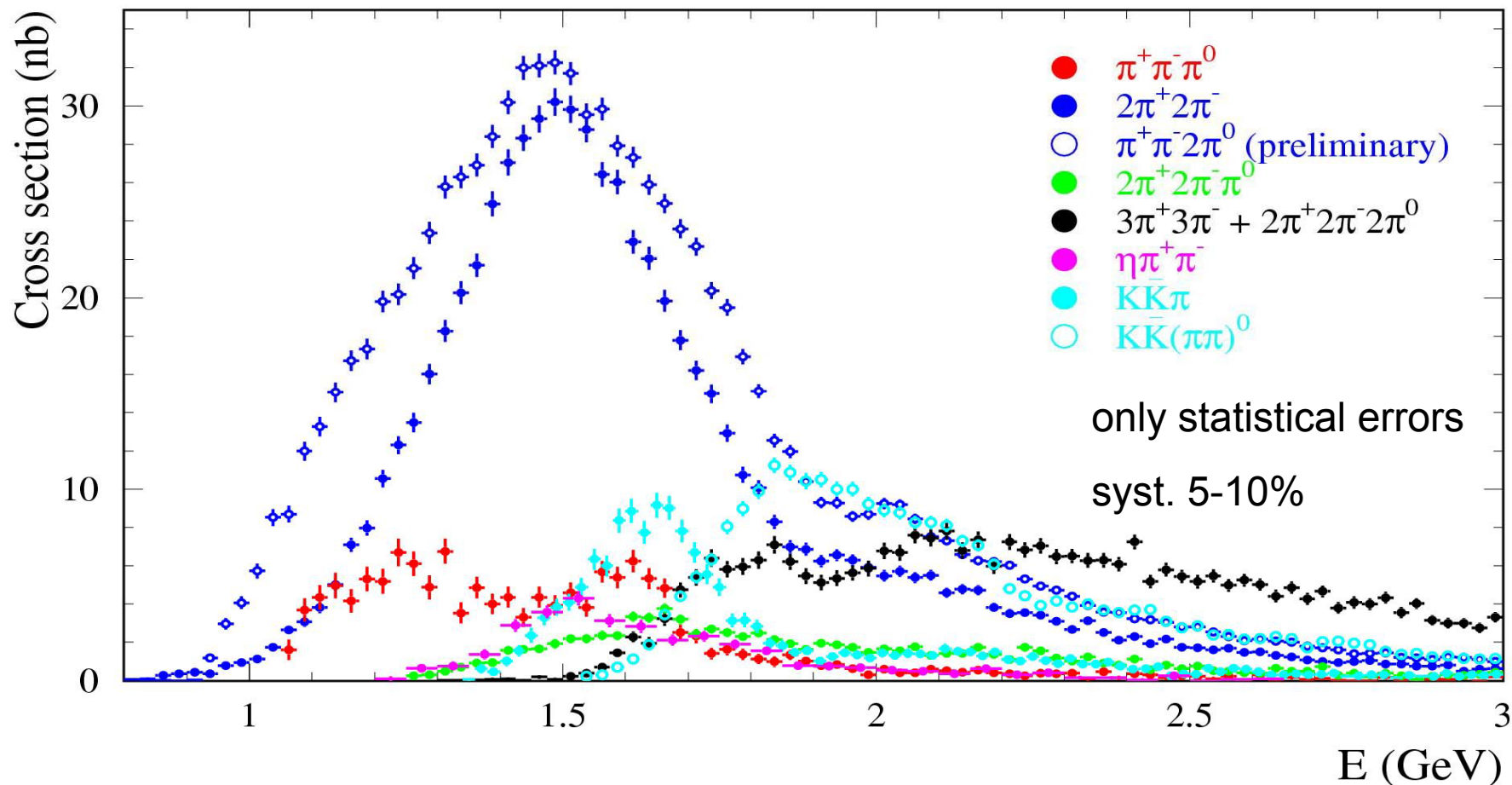


preliminary BaBar data:
A. Petzold, EPS-HEP (2007)



old contribution	16.8 ± 1.3	
update	17.6 ± 1.7	probably still underestimated (BaBar prelim.)
τ	21.4 ± 1.4	

BaBar Multi-hadronic Results



Still more channels under analysis: K^+K^- , $K\bar{K}\pi\pi$ with K^0

Where are we?

- including BaBar 2π results in the e^+e^- combination + estimate of hadronic LBL contribution (Prades-de Rafael-Vainhstein, 2009) yields

$$a_\mu^{\text{SM}}[e^+e^-] = (11\,659\,183.4 \pm 4.1 \pm 2.6 \pm 0.2) 10^{-10}$$

HVP LBL EW (± 4.9)

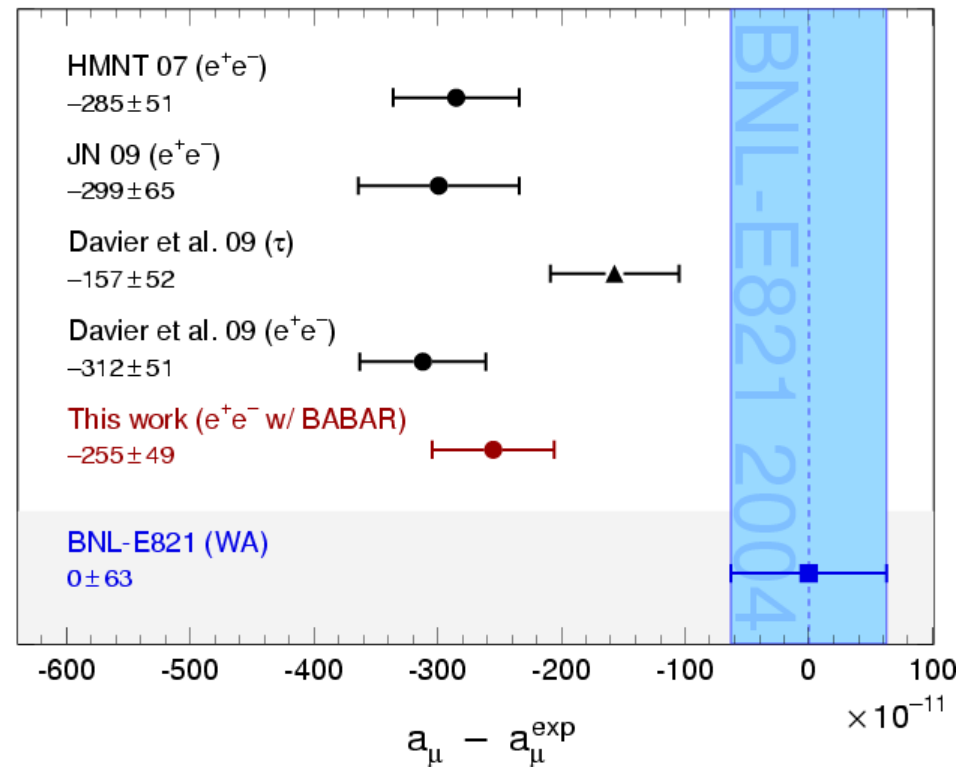
- E-821 updated result

$$11\,659\,208.9 \pm 6.3$$

- deviation (ee) 25.5 ± 8.0
(3.2σ)

- updated τ analysis
+Belle +revisited IB corrections

- deviation (τ) 15.7 ± 8.2
(1.9σ)



Discussion

- BaBar 2π data complete and the most accurate, but expected gain in precision not fully realized because of discrepancy with KLOE
- however, **previous τ/ee disagreement strongly reduced (resolved?)**
2.9 σ (2006) \rightarrow 2.4 σ (τ update) \rightarrow 1.5 σ (including BaBar)
- a range of values for the deviation from the SM can be obtained, depending on the 2π data used:

BaBar	2.4 σ	
all ee	3.2 σ	\leftarrow
all ee - BaBar	3.7 σ	
all ee - KLOE	2.9 σ	
τ	1.9 σ	

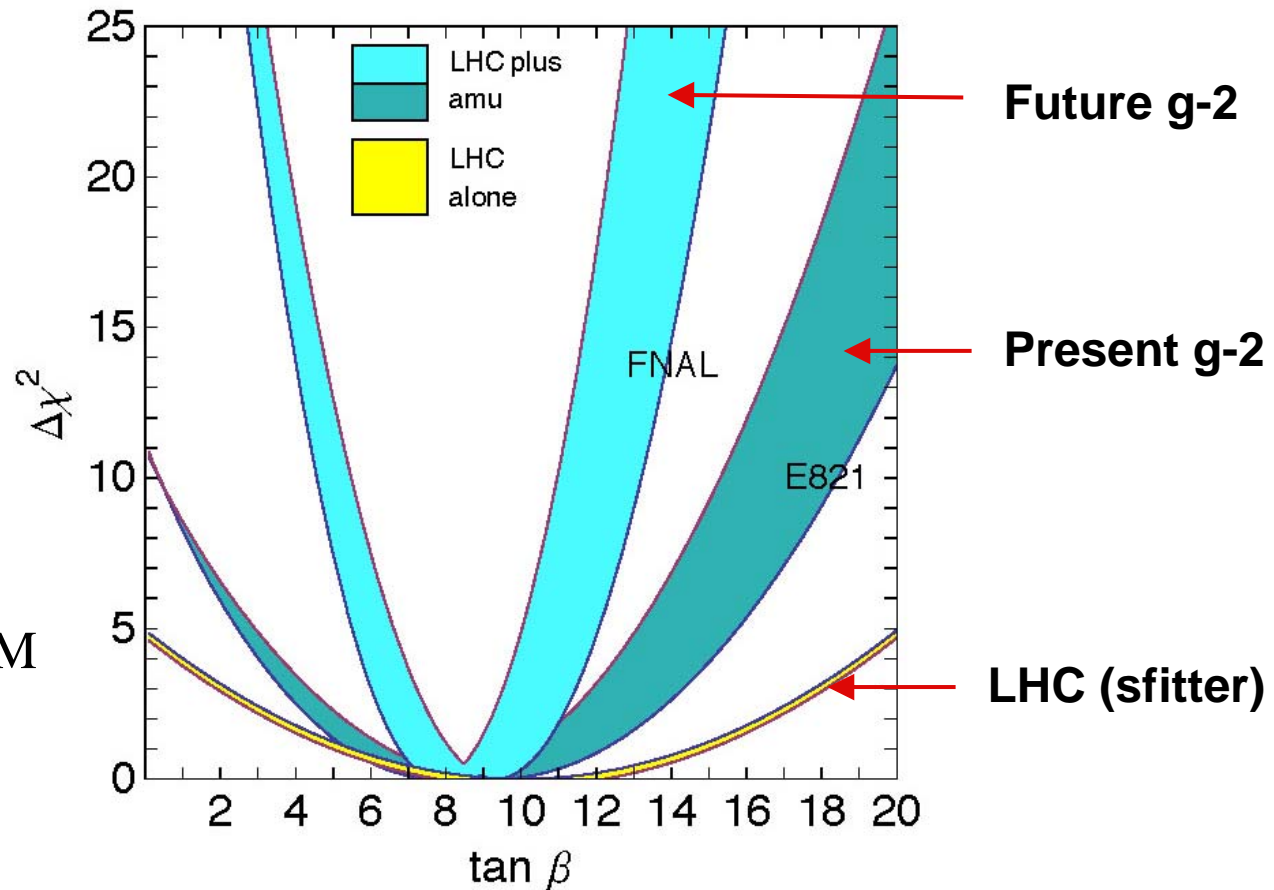
- all approaches yield a deviation, but SM test limited by systematic effects not accounted for in the experimental analyses (ee) and/or the corrections to τ data
- at the moment some evidence for a deviation ($\sim 3\sigma$), but **not sufficient to establish a contribution from new physics (NP)**
- however if NP is found at LHC, this deviation **will constraint the NP phenomenology**

Impact on new physics : ex. SUSY

LHC: direct search for SUSY partners

difficult to measure couplings and disentangle between models (ILC)

$g-2$ measurement + theory prediction: sensitivity to couplings



taking one MSSM
parameter point
(D. Stöckinger)

Perspectives

- **first priority is a clarification of the BaBar- τ / KLOE discrepancy:**
 - origin of the ‘slope’ (was very pronounced with the 2004 KLOE results, reduced now with the 2008 results)
 - normalization difference on ρ peak (most direct effect on a_μ)
 - Novosibirsk results in-between and not precise enough
- further checks of the KLOE results are possible: as method is based on MC simulation for ISR and additional ISR/ISR probabilities \Rightarrow **long-awaited test with $\mu\mu\gamma$ analysis**
- contribution from multi-hadronic channels will continue to be updated with more results forthcoming from BaBar, **particularly $2\pi 2\pi^0$**
- new precise data expected from VEPP-2000 in Novosibirsk
- experimental error of E-821 direct a_μ measurement is a limitation, already now \Rightarrow **new projects necessary**
 - proposal accepted in Fermilab (financed?): improve accuracy by a factor 4
 - project at JPARC

Backup Slides

Comparison of ee and τ Data Revisited (2)

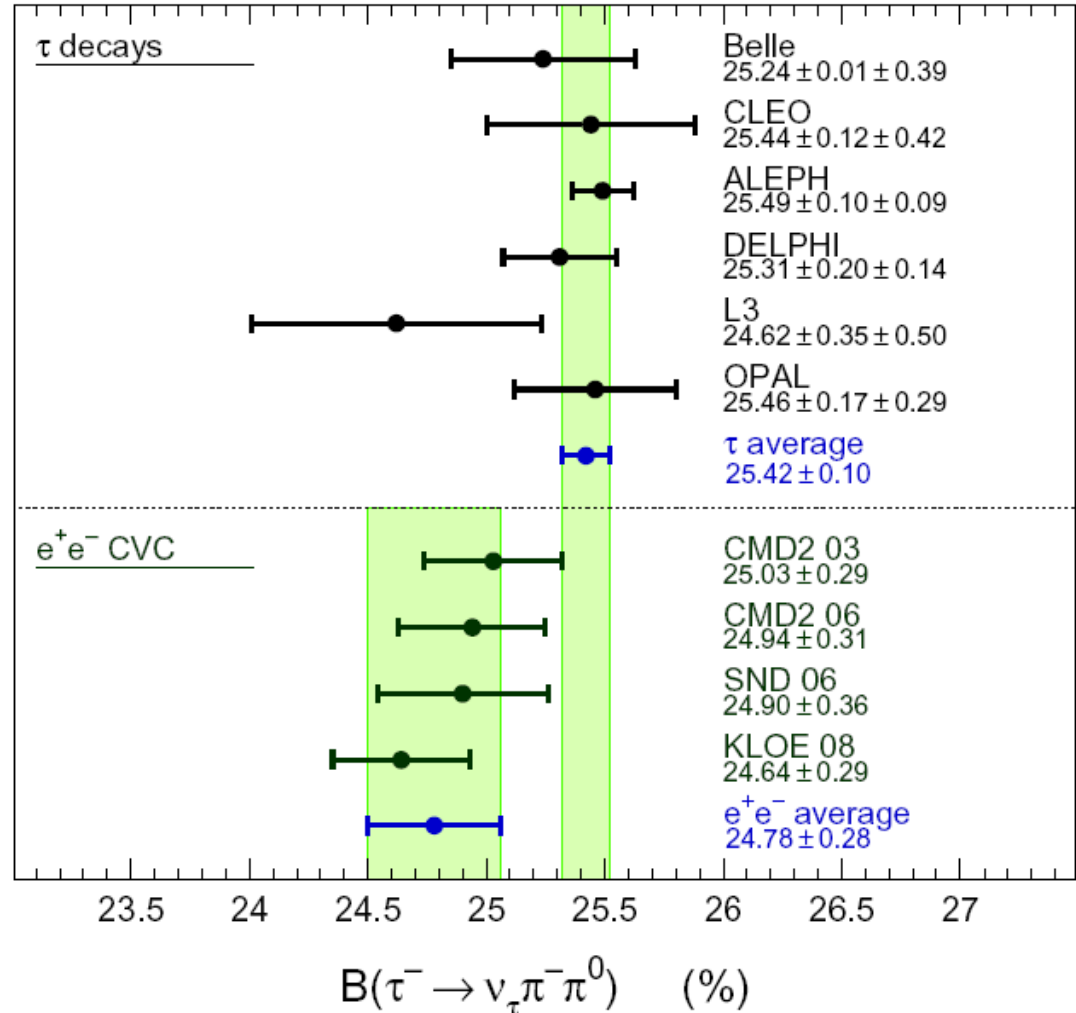
Global test of spectral functions:
prediction of τ BR using ee data

\Rightarrow apply to $\pi\pi^0$ channel

IB corrections applied to ee data
this time

$$\mathcal{B}_X^{\text{CVC}} = \frac{3 \mathcal{B}_e |V_{ud}|^2}{2 \pi \alpha^2 m_\tau^2} \int_{s_{\min}}^{m_\tau^2} ds s \sigma_{X^0} \left(1 - \frac{s}{m_\tau^2}\right)^2 \left(1 + \frac{2s}{m_\tau^2}\right)$$

- data from CMD2-SND overconsistent ?
- fair agreement CMD2-SND with τ
- larger disagreement with KLOE



Obtaining the $\pi\pi(\gamma)$ cross section

$$\frac{dN_{\pi\pi\gamma(\gamma)}}{d\sqrt{s'}} = \frac{dL_{ISR}^{eff}}{d\sqrt{s'}} \epsilon_{\pi\pi\gamma(\gamma)}(\sqrt{s'}) \sigma_{\pi\pi(\gamma)}^0(\sqrt{s'})$$

Unfolded spectrum

Acceptance from MC + data/MC corrections

Effective ISR luminosity from $\mu\mu\gamma(\gamma)$ analysis (similar equation + QED)

$\pi\pi$ mass spectrum unfolded (Malaescu arXiv:0907-3791) for detector response

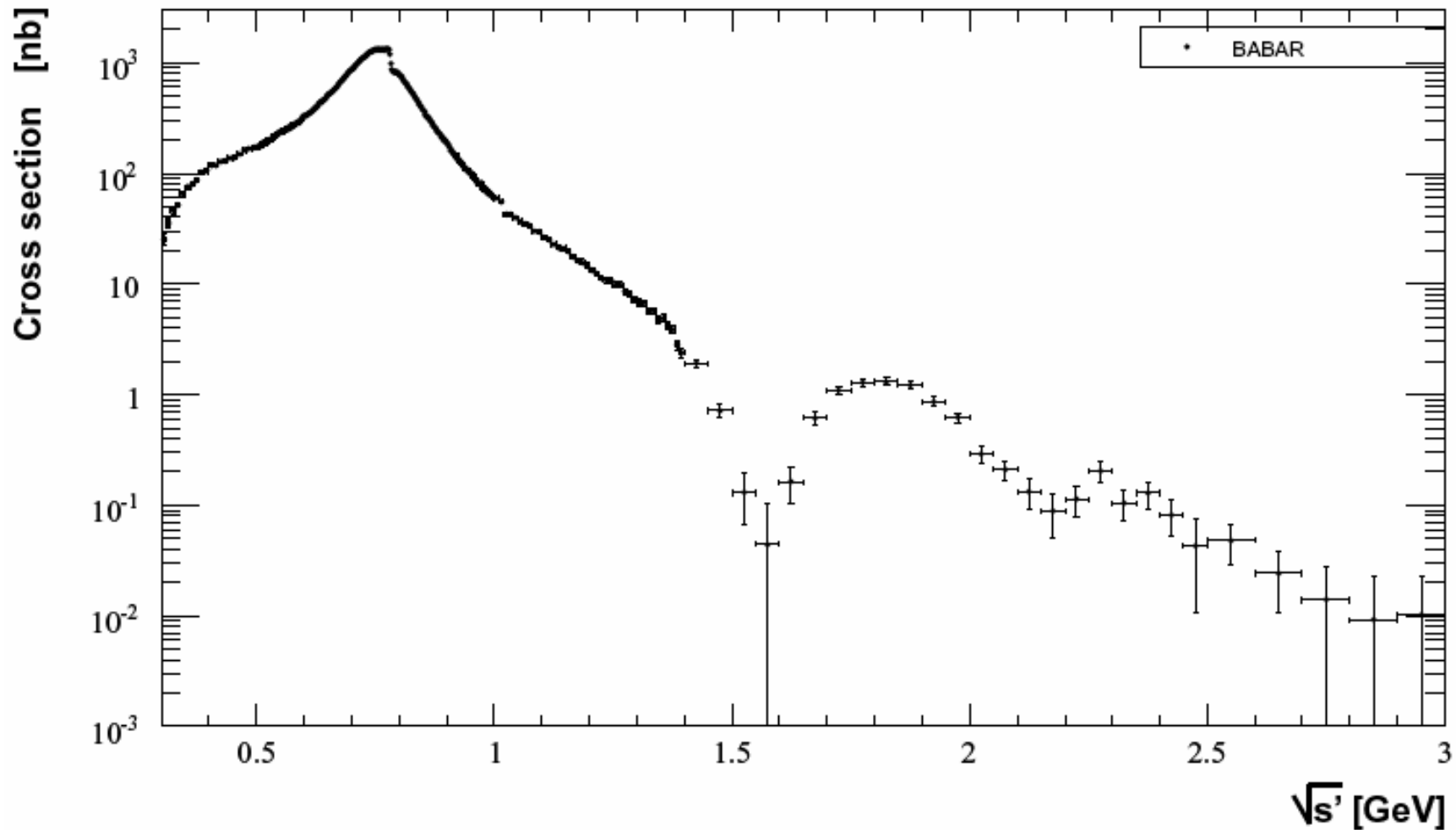
Additional ISR almost cancels in the procedure ($\pi\pi\gamma(\gamma)$ / $\mu\mu\gamma(\gamma)$ ratio)

Correction $(2.5 \pm 1.0) 10^{-3} \Rightarrow \pi\pi$ cross section does not rely on accurate description of NLO in the MC generator

ISR luminosity from $\mu\mu\gamma$ in 50-MeV energy intervals
(small compared to variation of efficiency corrections)

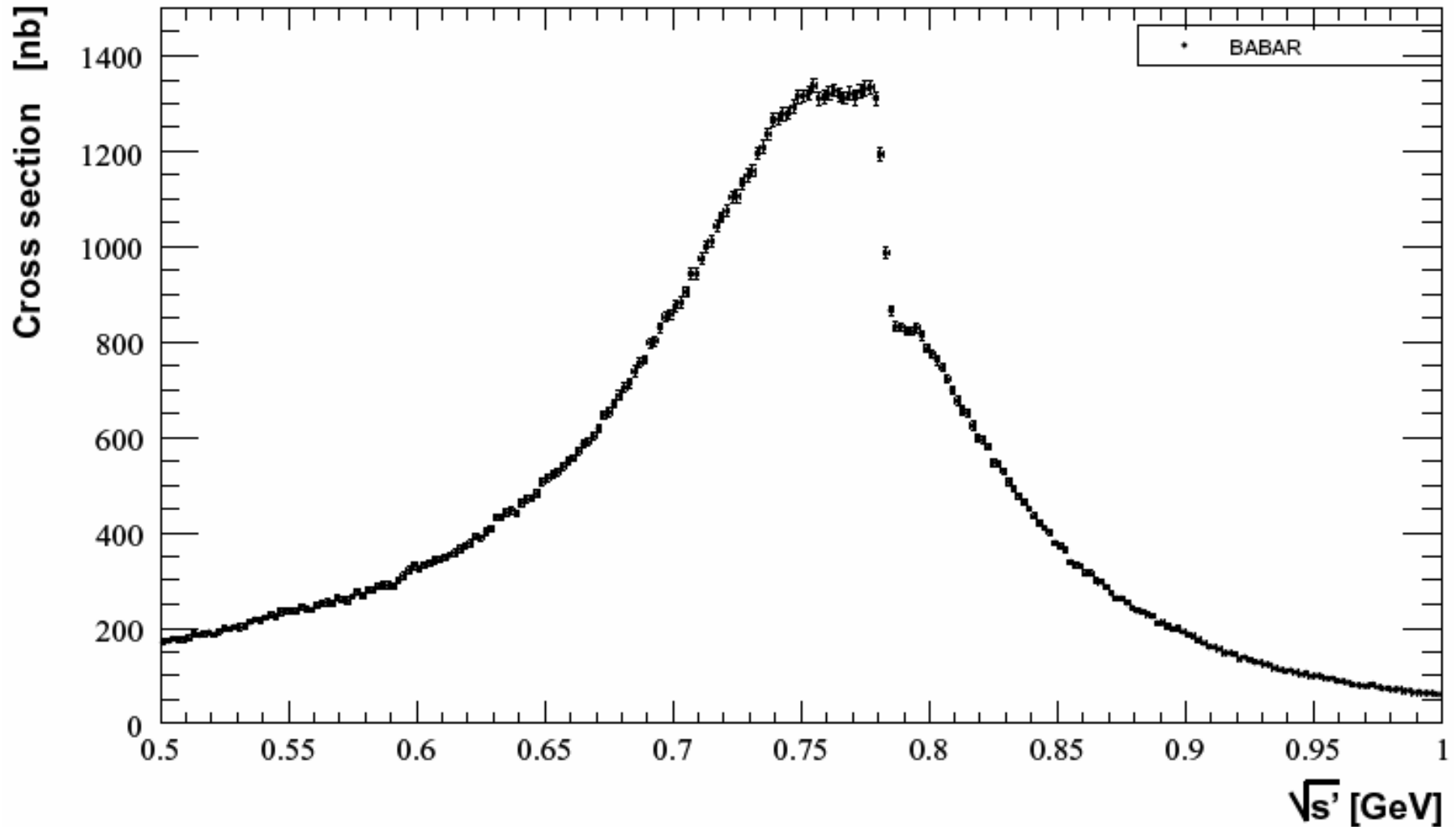
BaBar results (arXiv:0908.3589)

$e^+ e^- \rightarrow \pi^+ \pi^- (\gamma)$ bare (no VP) cross section diagonal errors stat+syst

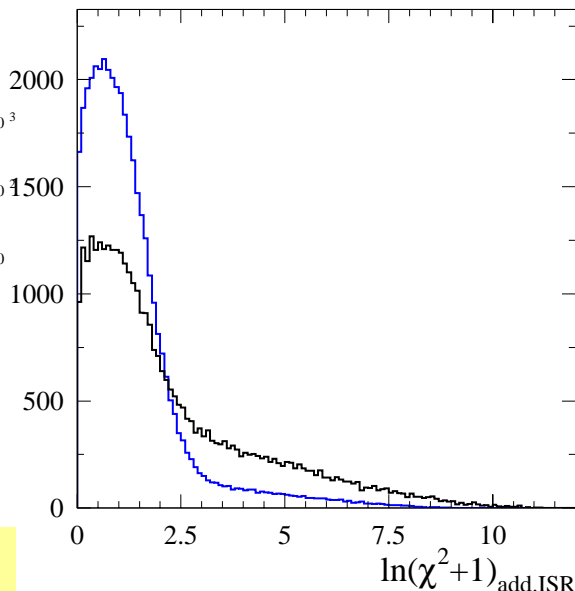
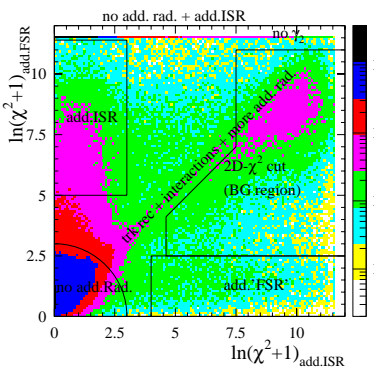


BaBar results in ρ region

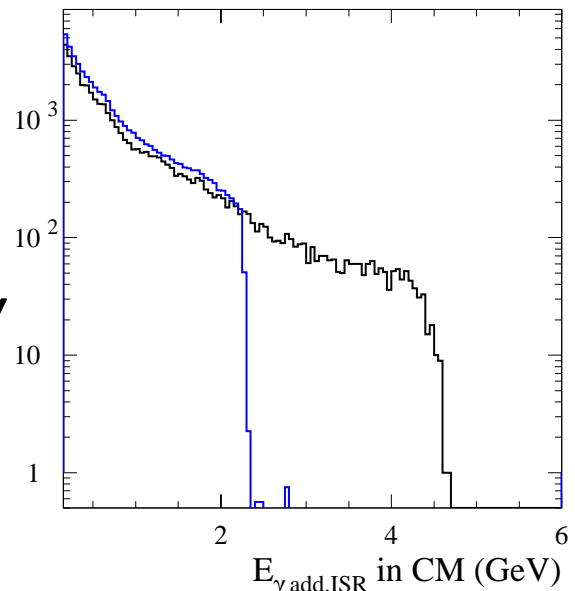
2-MeV energy intervals



Additional ISR

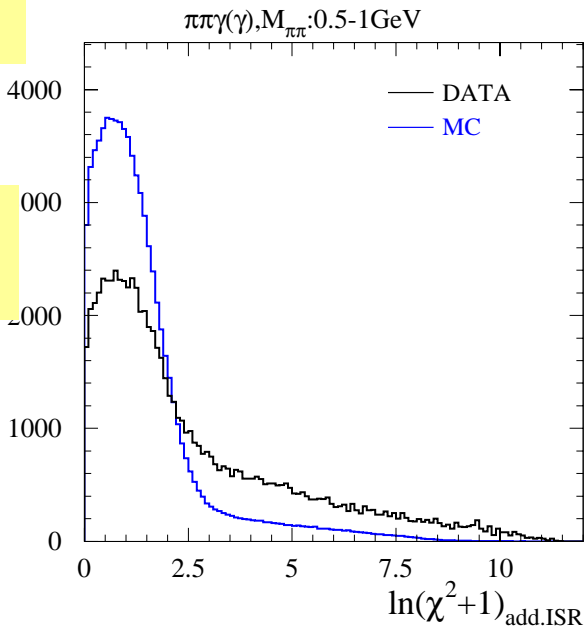


$\mu\mu\gamma\gamma$

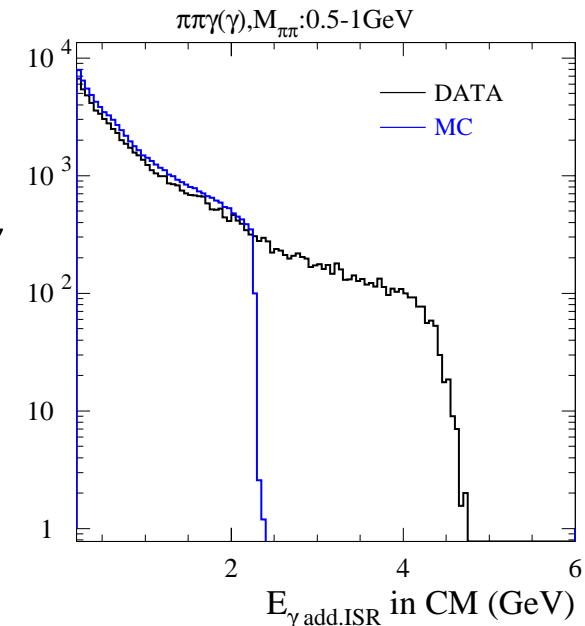


Angular distribution of add. ISR /beams!

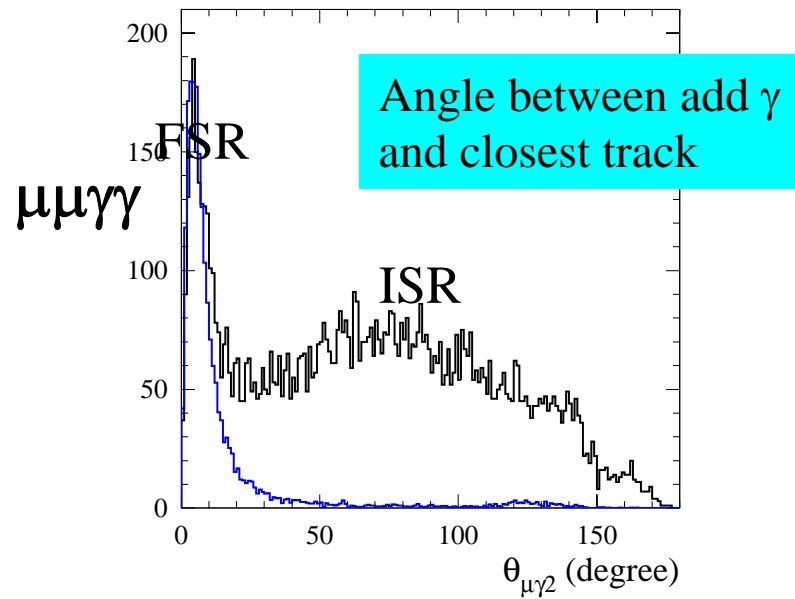
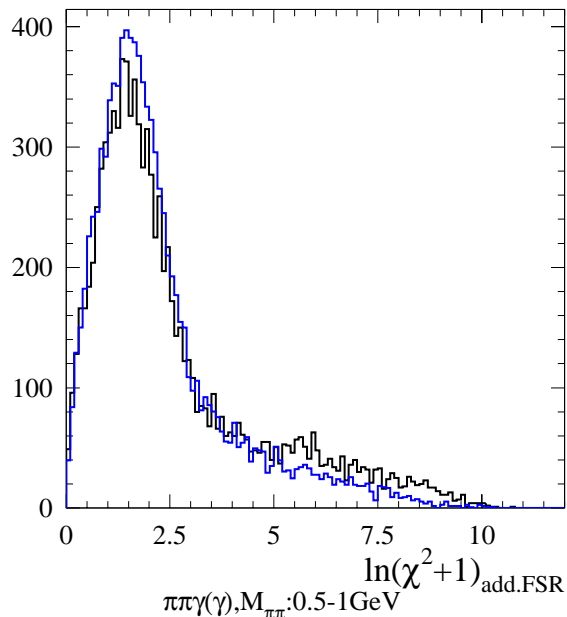
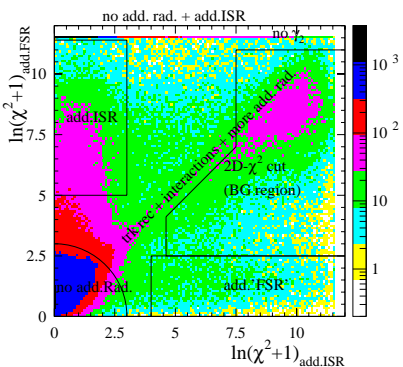
Energy cut-off for add. ISR in AfkQed



$\pi\pi\gamma\gamma$



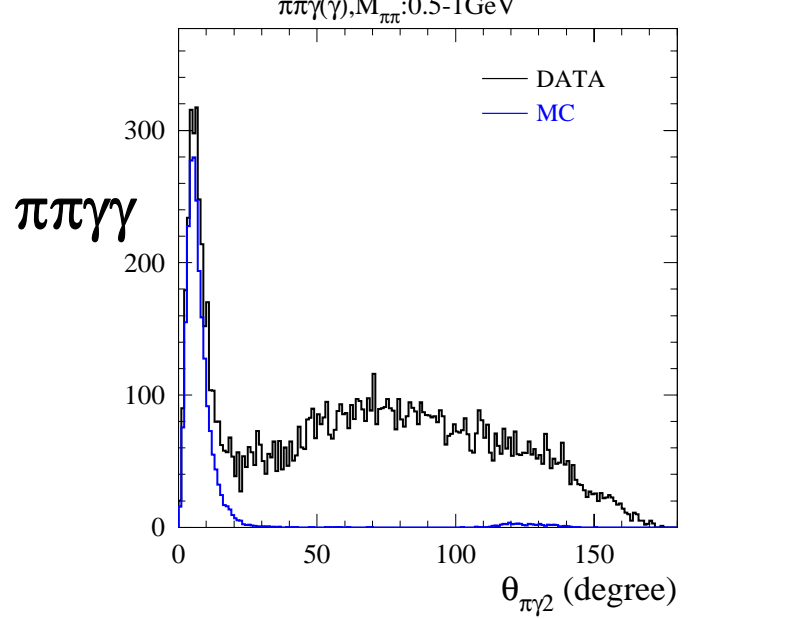
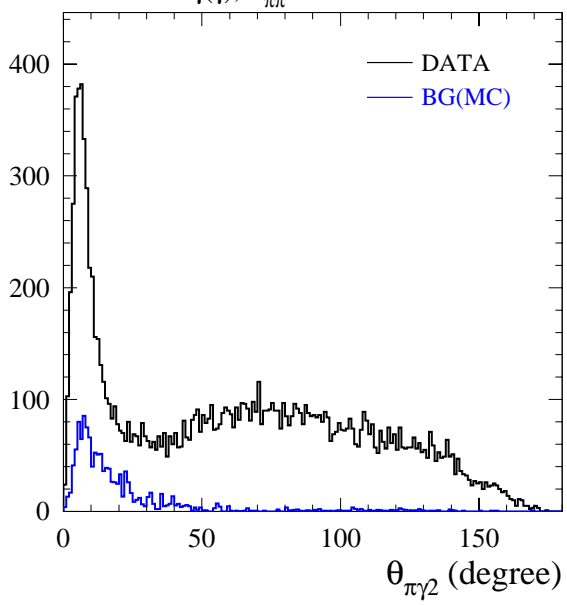
Additional FSR



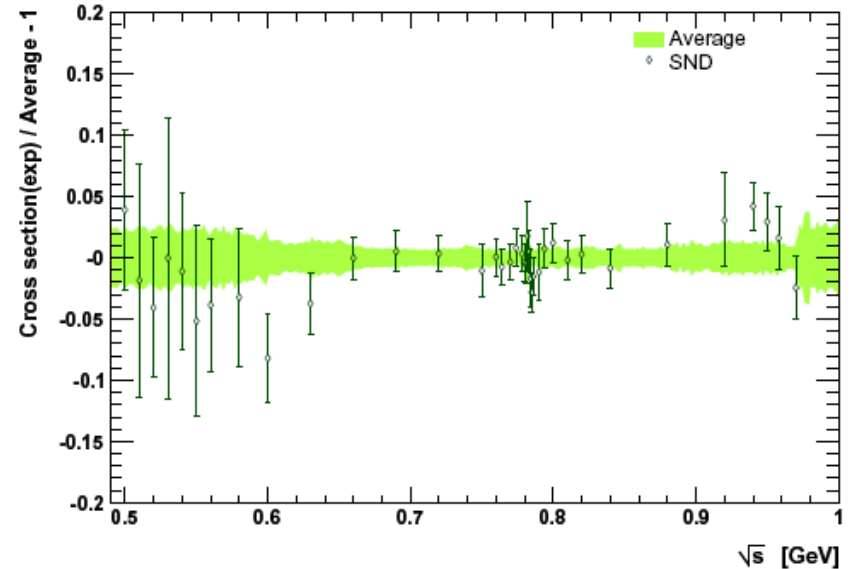
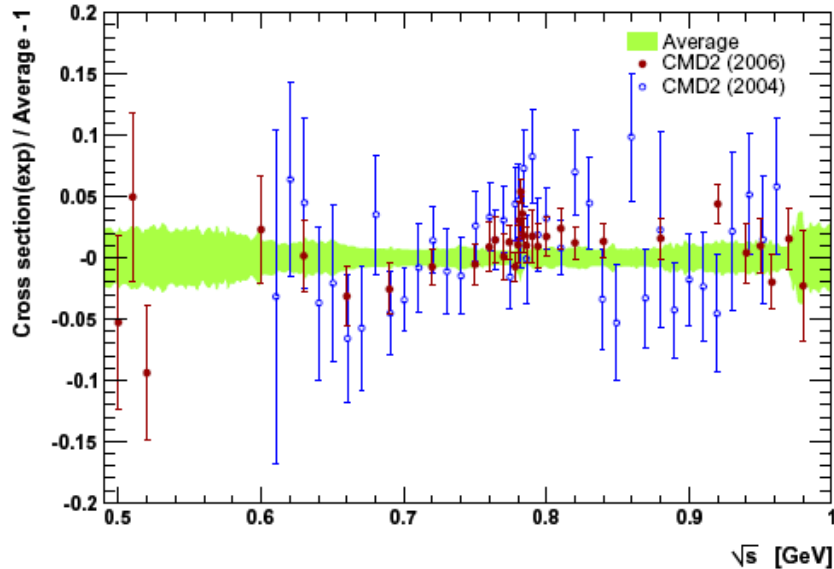
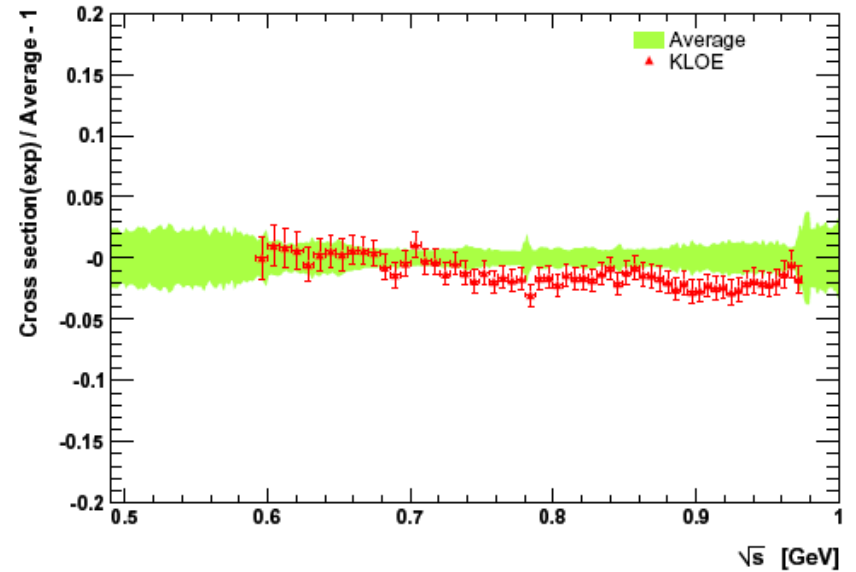
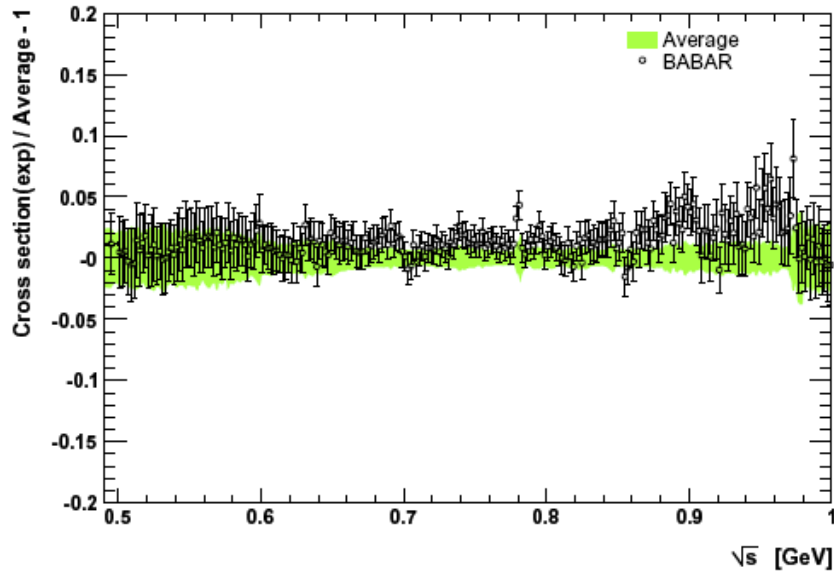
Large-angle add.ISR
in data \neq AfkQed

Evidence for FSR
data \sim AfkQed

data/MC
 $\mu\mu$ 0.96 ± 0.06
 $\pi\pi$ 1.21 ± 0.05



Consistency of Experiments with Average



Computing $a_\mu^{\pi\pi}$

$$a_\mu^{\pi\pi(\gamma),LO} = \frac{1}{4\pi^3} \int_{4m_\pi^2}^{\infty} ds K(s) \sigma_{\pi\pi(\gamma)}^0(s),$$

where $K(s)$ is the QED kernel,

$$K(s) = x^2 \left(1 - \frac{x^2}{2}\right) + (1+x)^2 \left(1 + \frac{1}{x^2}\right) \left[\ln(1+x) - x + \frac{x^2}{2} \right] + x^2 \frac{1+x}{1-x} \ln x,$$

with $x = (1 - \beta_\mu)/(1 + \beta_\mu)$ and $\beta_\mu = (1 - 4m_\mu^2/s)^{1/2}$.

$m_{\pi\pi}$ range (GeV)	$a_\mu^{\pi\pi(\gamma),LO}$ BABAR
0.28–0.30	$0.55 \pm 0.01 \pm 0.01$
0.30–0.50	$57.62 \pm 0.63 \pm 0.55$
0.50–1.00	$445.94 \pm 2.10 \pm 2.51$
1.00–1.80	$9.97 \pm 0.10 \pm 0.09$
0.28–1.80	$514.09 \pm 2.22 \pm 3.11$

($\times 10^{-10}$)

0.7% precision

0.28–1.8 (GeV)

BABAR

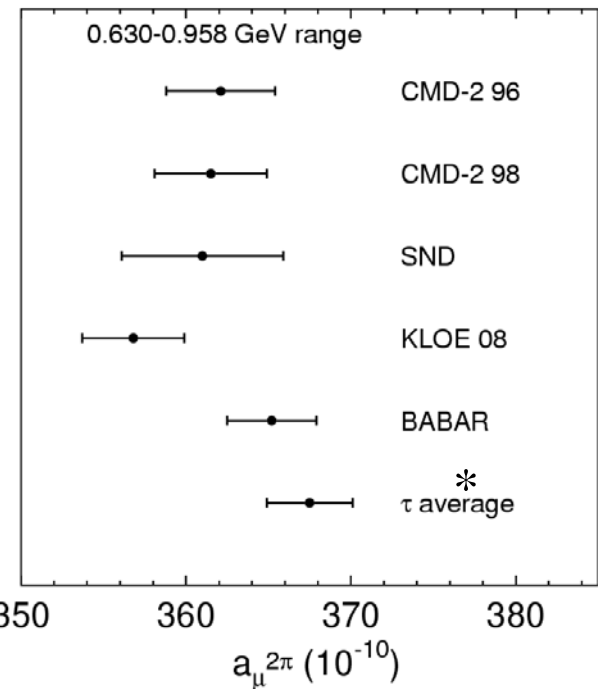
514.1 ± 3.8

previous e^+e^- combined

503.5 ± 3.5 *

τ combined

515.2 ± 3.5 *



* arXiv:0906-5443 MD et al.