

# **SO(10) model, Flavor Violation and the Recent D0 Result**

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# Outline

**A Minimal SO(10) Model**

**Proton decay**

**Fermion masses, mixings and predictions**

**Lepton Flavor Violation**

**Gauge coupling unification**

**$B_s - \bar{B}_s$  and the recent D0 result**

**Conclusion**

# The Model...

The Yukawa superpotential involves the couplings of 16-dimensional matter spinors :

**All SM fields+  $\nu_R$**

$$W_Y = 1/2 h_{ij} \psi_i \psi_j H + 1/2 f_{ij} \psi_i \psi_j \bar{\Delta} + 1/2 h'_{ij} \psi_i \psi_j D.$$

$\psi_i$  ( $i$  denotes a generation index)

with 10 (**H**),  $\overline{126}$  ( $\Delta$ ), and 120 (**D**) dim. Higgs fields:

**$h$  and  $f$  are symmetric matrices and  $h'$  is an anti-symmetric matrix due to the  $SO(10)$  symmetry.**

The Higgs doublet fields not only exist in **H**,  $\Delta$ , **D**, but also in other Higgs fields (e.g., **210**) which are needed in the model.

# The Model...

**SO(10) gets broken  
by the following  
Higgs Fields:**

**210, 45, 54, 126,  $\overline{126}$ ,**

**SO(10)**

**SU(5)**

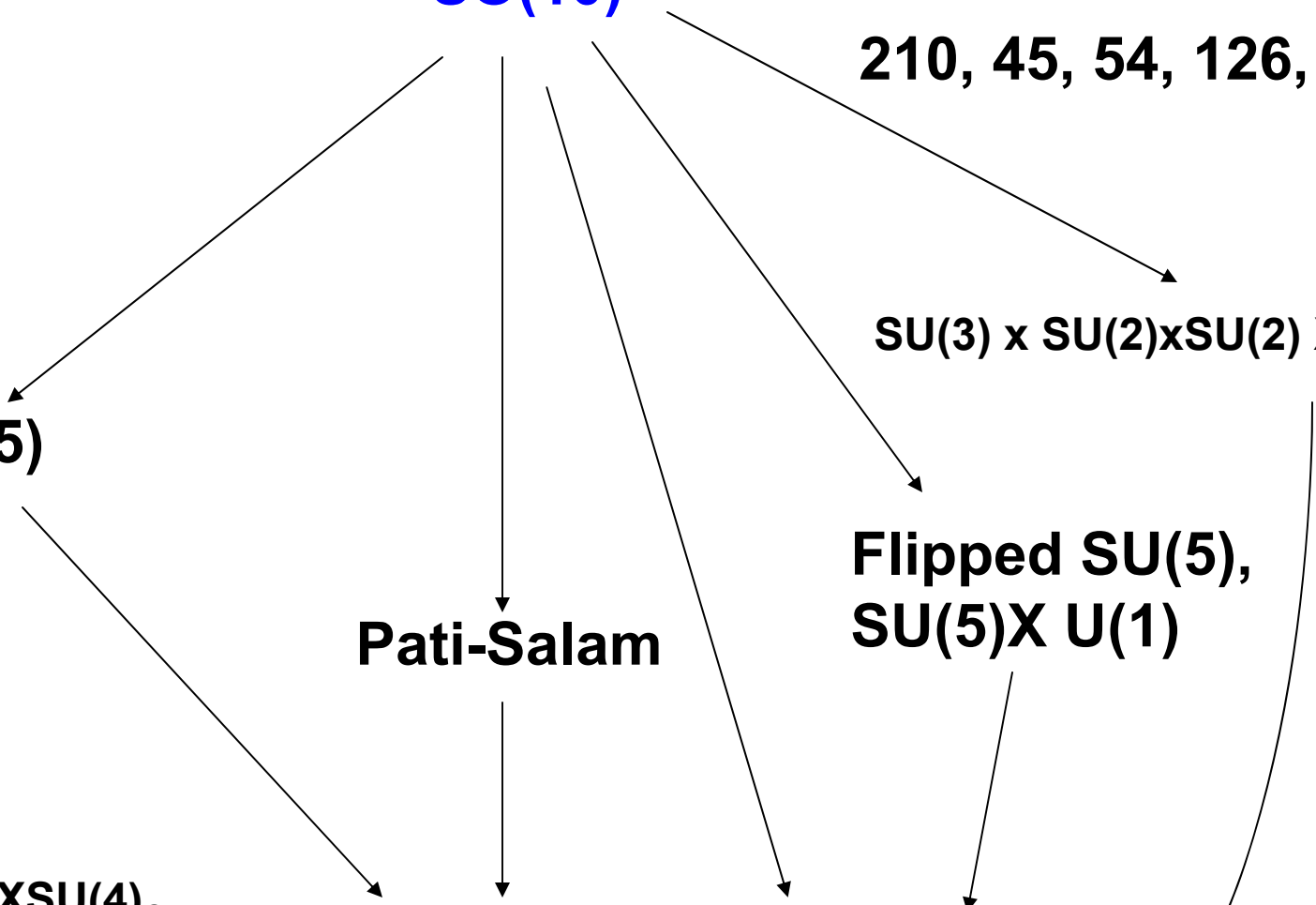
**SU(3) x SU(2)xSU(2) X U(1)**

**Pati-Salam**

**Flipped SU(5),  
SU(5)X U(1)**

**Pati-Salam:  
SU(2)<sub>L</sub>xSU(2)<sub>R</sub>XSU(4)<sub>C</sub>**

**SM (SU(3) x SU(2) X U(1))**



# The Model...

**210 Higgs multiplet ( $\phi$ ):** is employed to break the  $SO(10)$  symmetry

**$\overline{126}$  Higgs multiplet ( $\overline{\Delta}$ ):** introduced as a vector-like pair and this field also contains a Higgs doublet.

The VEV of this pair reduces the rank of  $SO(10)$  group, keep supersymmetry unbroken down to the weak scale.

Altogether, we have **six** pairs of Higgs doublets:

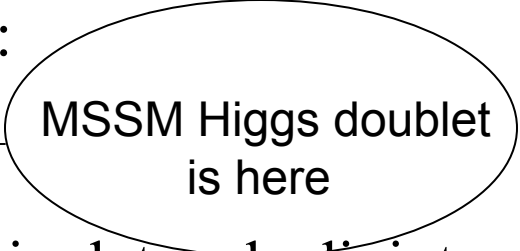
$$\phi_d = (\mathbf{H}^{10}_d, \mathbf{D}^1_d, \mathbf{D}^2_d, \overline{\Delta}_d, \Delta_d, \phi_d),$$

$$\phi_u = (\mathbf{H}^{10}_u, \mathbf{D}^1_u, \mathbf{D}^2_u, \Delta_u, \overline{\Delta}_u, \phi_u),$$

where superscripts 1, 2 of  $\mathbf{D}_{u,d}$  stand for  $SU(4)$  singlet and adjoint pieces under the  $G_{422} = SU(4) \times SU(2) \times SU(2)$  decomposition.

**The mass term of the Higgs doublets :**  $(\phi_d)_a (\mathbf{M}_D)_{ab} (\phi_u)_b,$

The lightest Higgs pair (MSSM doublets) has masses of the order of the weak scale.



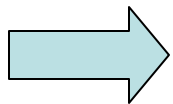
MSSM Higgs doublet  
is here

# The Model...

The Yukawa interaction includes mass terms of the quark and lepton fields as follows (**using 10+120+126-Higgs fields**):-

$$\begin{aligned}
 W^{\text{mass}}_Y = & hH^{10}_d (qd^c + \ell e^c) + hH^{10}_u (qu^c + \ell v^c) + \\
 & 1/\sqrt{3} f \Delta_d (qd^c - 3\ell e^c) + 1/\sqrt{3} f \Delta_u (qu^c - 3\ell v^c) + \sqrt{2} f v^c v^c \Delta_R + \\
 & \sqrt{2} f \ell \ell \Delta_L + h'D^1_d (qd^c + \ell e^c) + h'D^1_u (qu^c + \ell v^c) + \\
 & 1/\sqrt{3} h'D^2_d (qd^c - 3\ell e^c) - 1/\sqrt{3} h'D^2_u (qu^c - 3\ell v^c),
 \end{aligned}$$

where  $q, u^c, d^c, \ell, e^c, v^c$  are the quark and lepton fields for the standard model, which are all unified into one spinor representation of  $SO(10)$ .



$$\begin{aligned}
 Y_u &= h + r_2 f + r_3 h' \\
 Y_d &= r_1 (h + f + h') \\
 Y_e &= r_1 (h - 3f + c_e h') \\
 Y_\nu &= h - 3r_2 f + c_\nu h'
 \end{aligned}$$

**$r_{1,2,3}$  : Higgs mixing**

# The Model...

Imposing that the Lagrangian is invariant under a CP conjugation, the Yukawa couplings,  $h_{ij}$ ,  $f_{ij}$  and  $h'_{ij}$  and all masses and couplings in the Higgs superpotential are all real.

The mixing of the lightest Higgs doublets with the Higgs doublets present in **120** involves a pure imaginary coefficient which will make the fermion masses **hermitian** in this model

Very interesting property!

**Solves the EDM problems of SUSY models**

# Neutrino Mass

The VEVs of the fields

$\Delta_R : (1, 1, 3)$  and  $\Delta_L : (1, 3, 1)$  give neutrino Majorana masses.

**Seesaw: EW scale<sup>2</sup>/GUT scale  $\sim$  eV**

The light neutrino mass is obtained as

$$\mathbf{m}_\nu^{\text{light}} = \mathbf{M}_L - \mathbf{M}_\nu^D \mathbf{M}_R^{-1} (\mathbf{M}_\nu^D)^T$$

Type I: Minkowski'77;  
Yanagida'79,  
Gellman, Ramond, Slansky  
'79; Glashow'79;  
Mohapatra, Senjanovic'80

where  $\mathbf{M}_\nu^D = Y_h \langle H_u \rangle$ ,  $\mathbf{M}_L = 2\sqrt{2}f \langle \Delta_L \rangle$ ,  $\mathbf{M}_R = 2\sqrt{2}f \langle \Delta_R \rangle$ .

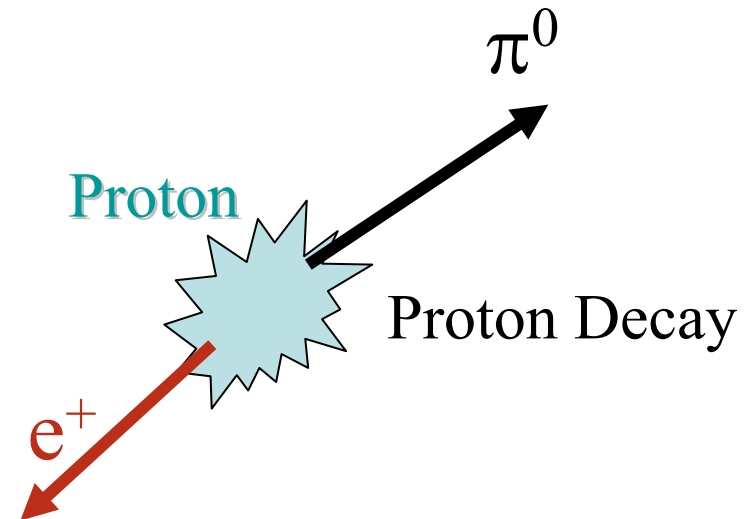
Pure type II:  $\mathbf{M}_L$  (In this talk)

Lazarides, Shafi, Wetterich,81,  
Mohapatra, Senjanovic,81



# Proton Decay

- Generic prediction of most Grand Unified Theories
- Lifetime  $> 10^{33}$  yr!



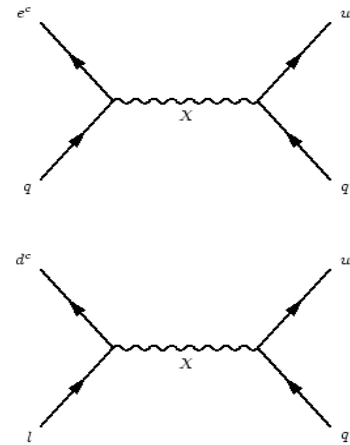
# Nucleon decay

- Reach of partial lifetime
  - $p \rightarrow e^+ \pi^0$  up to  $\sim 10^{35}$  yrs with  $\sim$  Mton water Cherenkov (present SK limit:  $5.4 \times 10^{33}$  yrs)
  - $p \rightarrow \nu K^+$  up to  $\sim$  a few  $\times 10^{34}$  yrs with  $\sim$  100 kton liq. Ar and  $\sim$  50 kton liq. scintillator (present SK limit:  $2.0 \times 10^{33}$  yrs)
- There is a lot of life in proton decay
- It is possible to suppress the decay rate, but in many cases proton decay is just around the corner: keep looking !
- Next step is significant!

# Proton Decay

- The amplitudes mediated by GUT bosons (dimension 6 operators) become small

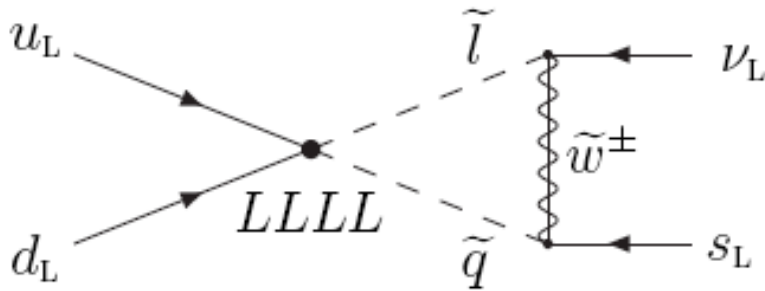
$$\frac{qqql}{\Lambda^2} \quad \frac{d^c d^c u^c e^c}{\Lambda^2} \quad \frac{e^c u^c qq}{\Lambda^2} \quad \frac{d^c u^c ql}{\Lambda^2}$$



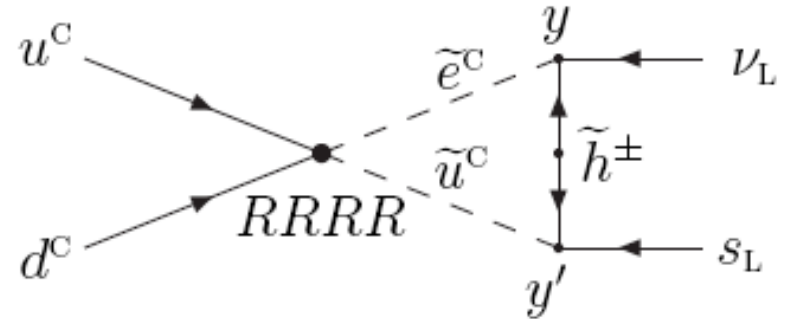
Dimension 6 proton decay mediated by the X boson  $(3, 2)_{-\frac{5}{6}}$  in  $SU(5)$  GUT.

$\Lambda$  is the cutoff scale for the Standard Model:  $M_{\text{GUT}}$

- processes mediated by the *triplet higgsino* emerge (dimension 5 operators)



(a)



(b)

$$\text{Amp} = \lambda_u \lambda_d \frac{1}{M_{H3}} \frac{1}{M_{\text{SUSY}}} \frac{\alpha_s}{2\pi}$$

$M_{H3}$ : Mass of colored Higgsino  $\sim M_{\text{GUT}}$

# Proton decay Summary for SO(10)

Models of SO(10); Mohapatra et al, Raby et al, Pati and Babu,  
Senjanovic et al, Okada et al, Nath et al

**SO(10) allows only small  $\tan\beta$  ( $< 3$ ) and  
very large values of SUSY masses**

**Small  $\tan\beta$  is not preferred by Higgs mass and  
large values of SUSY masses also mean problem!**

**Situation is as bad as in SU(5)**

# Proton Decay in SO(10) Model

The proton decay is mediated by the colored Higgs triplets:

$$\varphi_T + \varphi_{\bar{T}} : ((3, 1, -1/3) + \text{c.c.}) \text{ (CL operator);}$$

$$\varphi_C + \varphi_{\bar{C}} : ((3, 1, -4/3) + \text{c.c.}) \text{ (CR operator);}$$

These Higgs triplets appear in:

**10+120+126+126+210** multiplets.

We generate both LLLL (CL) and RRRR (CR) operators:

$$-\mathbf{W5} = \mathbf{C}^{ijkl}_L \mathbf{q}_k \mathbf{q}_l \mathbf{q}_i \mathbf{\ell}_j + \mathbf{C}^{ijkl}_R \mathbf{e}^c_k \mathbf{u}^c_l \mathbf{u}^c_i \mathbf{d}^c_j$$

**These operators are obtained by integrating out the triplet Higgs fields,**

$\varphi_T = (\mathbf{H}_T, \mathbf{D}_T, \mathbf{D}'_T, \mathbf{\Delta}_T, \overline{\mathbf{\Delta}}_T, \overline{\mathbf{\Delta}}'_T, \mathbf{\phi}_T)$  The fields with “ $\bar{\phantom{x}}$ ” are **decuplet**, and the others are **sextet or 15-plet** under SU(4) decomposition.

$$\varphi_C = (\mathbf{D}_C, \overline{\mathbf{\Delta}}_C).$$

# Proton Decay...

$$W_{\text{trip}}^{\text{Y}} = hH_{\bar{T}} (q\bar{\ell} + u^c d^c) + hH_T (1/2qq + e^c u^c) + f\bar{\Delta}_{\bar{T}} (q\bar{\ell} - u^c d^c) + \dots$$

Same  $h$ ,  $f$  and  $h'$  which appear in the Yukawa couplings

$$C_{\text{L}}^{\text{ijkl}} = c h_{ij} h_{kl} + x_1 f_{ij} f_{kl} + x_2 h_{ij} f_{kl} + x_3 f_{ij} h_{kl} + x_4 h'_{ij} h_{kl} + x_5 h'_{ij} f_{kl},$$

$$C_{\text{R}}^{\text{ijkl}} = c h_{ij} h_{kl} + y_1 f_{ij} f_{kl} + y_2 h_{ij} f_{kl} + y_3 f_{ij} h_{kl} + y_4 h'_{ij} h_{kl} + \dots$$

$c = (M_T^{-1})_{11}$ , and the other coefficients  $x_i, y_i$  are also given by the components of  $M_T^{-1}$ .

The proton decay amplitude:

$A = \alpha_2 \beta_p / (4\pi M_T m_{\text{SUSY}}) A_x$ , where

$$A_x = c A_{hh} + x_1 A_{ff} + x_2 A_{hf} + x_3 A_{fh} + x_4 A_{h'h} + x_5 A_{h'f} + \dots$$

# Proton Decay (1<sup>st</sup> solution) ...

The current nucleon decay bounds,

$$|A_{p \rightarrow K\bar{\nu}}| \leq 10^{-8}, \quad |A_{n \rightarrow \pi\bar{\nu}}| \leq 2 \cdot 10^{-8} \text{ and}$$

$|A_{n \rightarrow K\bar{\nu}}| \leq 5 \cdot 10^{-8}$  for colored Higgsino mass is  $2 \cdot 10^{16}$  GeV,  
and squark and wino masses : 1 TeV and 250 GeV

**One way to suppress the decay amplitude is by demanding cancellation among different terms.**

In order to achieve that, **we need a cancellation among  $h$ ,  $f$  and  $h'$**  to have small couplings

However, we also need cancellation among the same set of couplings to generate the large mass hierarchy among the quark masses, i.e.,

$$Y_u = h + r_2 f + r_3 h'$$

$$Y_d = r_1 (h + f + h')$$

$$Y_e = r_1 (h - 3f + c_e h')$$

$$Y_\nu = h - 3r_2 f + c_\nu h'$$

## Understanding the solutions:

**h, f, h' combine together to produce the fermion masses**

**We need small numbers in this combination to reproduce the first generation fermion masses**

**Two ways: (1) Big h element+ Big f element + Big h' element  
= Small element  
(2) small h element+ small f element + small  
h' element = Small element**

**Small elements are preferred to solve proton decay problem!**

**If the couplings are small then the amplitudes are small**



# Proton Decay...

To suppress  $A_{hh}$ , the elements  $h_{11}$  and  $h_{22}$  (in  $h$ -diagonal basis) are needed to be suppressed rather than the up- and charm-quark Yukawa couplings, respectively. As a result, we need Yukawa texture to be  $\bar{\mathbf{h}} \simeq \text{diag}(\sim 0, \sim 0, \mathbf{O}(1))$ .

Once  $h$  is fixed, the other matrices  $f$  and  $h'$  are almost determined as

$$\bar{\mathbf{f}} = \begin{pmatrix} \sim \mathbf{0} & \sim \mathbf{0} & \lambda^3 \\ \sim \mathbf{0} & \lambda^2 & \lambda^2 \\ \lambda^3 & \lambda^2 & \lambda^2 \end{pmatrix} \quad \bar{\mathbf{h}}' = -i \begin{pmatrix} \mathbf{0} & \lambda^3 & \lambda^3 \\ -\lambda^3 & \mathbf{0} & \lambda^2 \\ -\lambda^3 & -\lambda^2 & \mathbf{0} \end{pmatrix}$$

where  $\lambda \sim 0.2$ .

$$\begin{aligned} Y_u &= h + r_2 f + r_3 h' \\ Y_d &= r_1 (h + f + h') \\ Y_e &= r_1 (h - 3f + c_e h') \\ Y_\nu &= h - 3r_2 f + c_\nu h' \end{aligned}$$

# Proton Decay...

One example for numerical fit for  
 $\tan \beta(M_Z) = 50, \bar{h} = \text{diag}(0, 0, 0.638),$

$$\bar{f} = \begin{pmatrix} \sim 0 & \mathbf{0.0044} & \mathbf{0.00208} \\ \mathbf{0.0044} & \mathbf{0.00945} & \mathbf{0.0101} \\ \mathbf{0.00208} & \mathbf{0.0101} & \mathbf{0.0071} \end{pmatrix} \quad \bar{h}' = i \begin{pmatrix} 0 & -\mathbf{0.0022} & \mathbf{0.00046} \\ \mathbf{0.0022} & 0 & \mathbf{0.0181} \\ -\mathbf{0.00046} & -\mathbf{0.0181} & 0 \end{pmatrix}$$

$$r_1 = 0.966, r_2 = 0.135, r_3 = 0, |c_e| = 0.987.$$

[ SU(5) like vacuum]

$r_2 \neq 0$  to produce  
correct charm mass

The coefficients,  $x_i, y_i$ , involve the colored Higgs mixings,  
which can be suppressed by our choice of the vacuum  
expectation values and the Higgs couplings.

The  $A_{hh}$  for  $p \rightarrow K \bar{\nu}_\mu$  mode is  $\sim 2 \cdot 10^{-11}$ .

B.D.,Y. Mimura, R. Mohapatra, Phys.Rev.Lett.94:091804,05;  
Phys.Rev.D72:075009,2005.

# The Model Predictions

**The number of parameters in the models is 17  
3 (h), 6(f), 3(h') and 5 Higgs parameters ( $r_{1,2,3}, c_e, c_\nu$ ).**

Explanation of the proton decay fix some parameters.

We choose  $\bar{h}_{11,22} = 0$  and  $r_3 = 0$ .

Since we will be working pure type II seesaw, i.e.,  $M_\nu = f v_L$ ,  $c_\nu$  is redundant in fitting fermion masses and mixings. This reduces the number of parameters to **13**.

**13 input parameters: up-type quark masses, charged lepton masses, the CKM angles and the phase, the ratio of the squared of neutrino mass differences ( $m_{\text{sol}}^2/m_{\text{A}}^2$ ), and the bi-maximal mixings as input parameters.**

**The down-type quark masses,  $U_{e3}$  and  $\delta_{\text{MNSP}}$  etc are the predictions of this model.**

# Strange Quark Mass

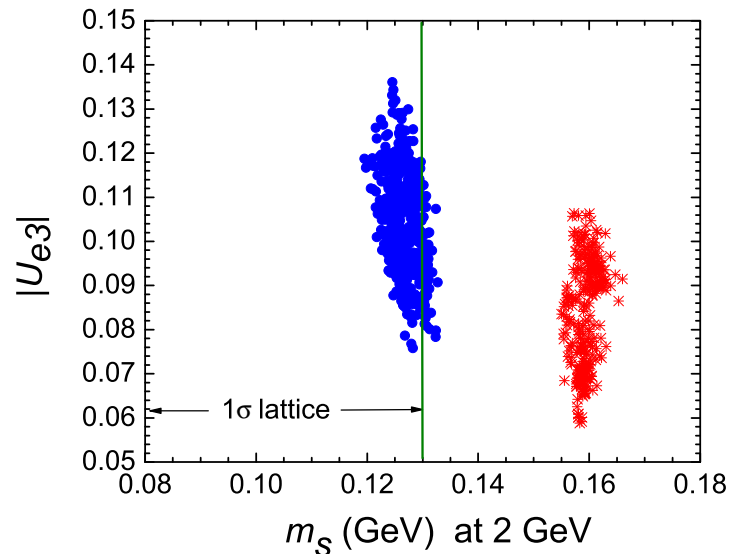
The predicted value of strange quark mass has two separate regions, roughly  $m_s \sim 1/3 m_\mu (1 \pm O(\lambda^2))$ .

The negative sign corresponds to a strange quark mass:

$$m_s(\mu = 2\text{GeV}) = 120 - 130 \text{ MeV}.$$

lattice derived value,  $m_s(\mu = 2\text{GeV}) = (105 \pm 25) \text{ MeV}$

The positive signature gives the following value of the strange quark mass,  $m_s(\mu = 2\text{GeV}) = 155 - 165 \text{ MeV}$



$$m_s/m_d = 17-18, 19-20.5$$

$$[18.9 \pm 0.8, \text{Leutwyler'00}]$$

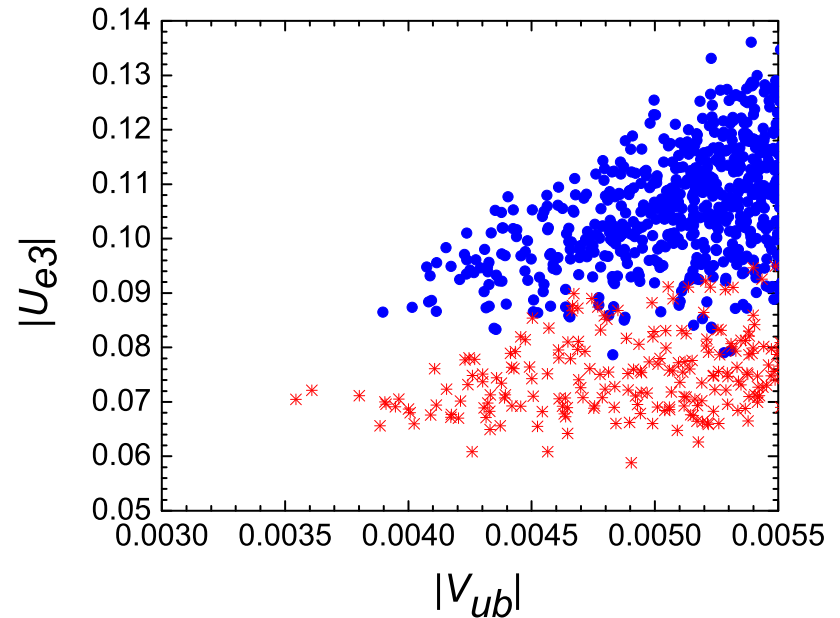
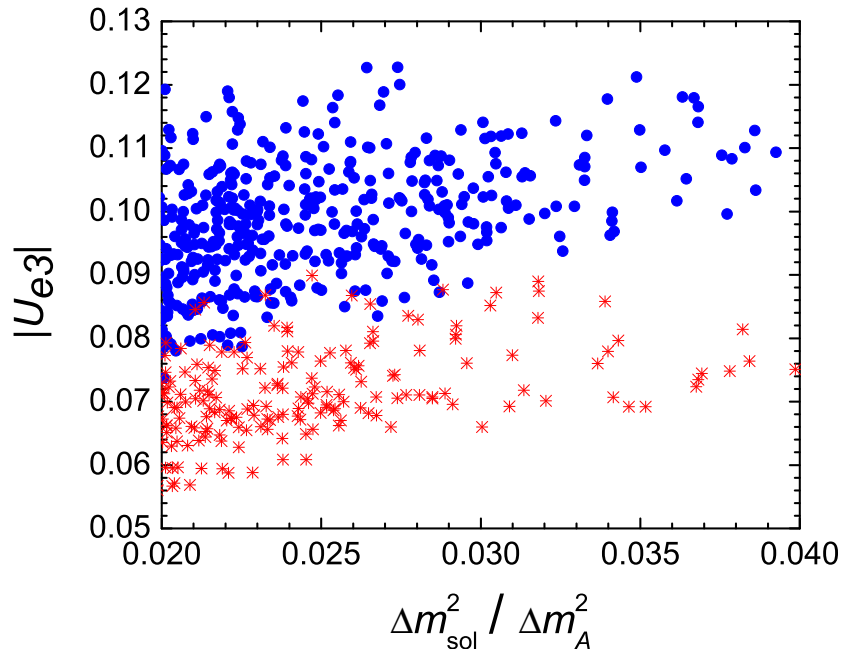
$$|U_{e3}|$$

We get the following approximate relation for  $U_{e3}$ :

$$|U_{e3}|^2 \approx \tan^2 \theta_{\text{sol}} / (1 - \tan^4 \theta_{\text{sol}}) \Delta m_{\text{sol}}^2 / \Delta m_{\text{A}}^2$$

We also have the following relation since  $U_{e3}$  is related to the ratio :

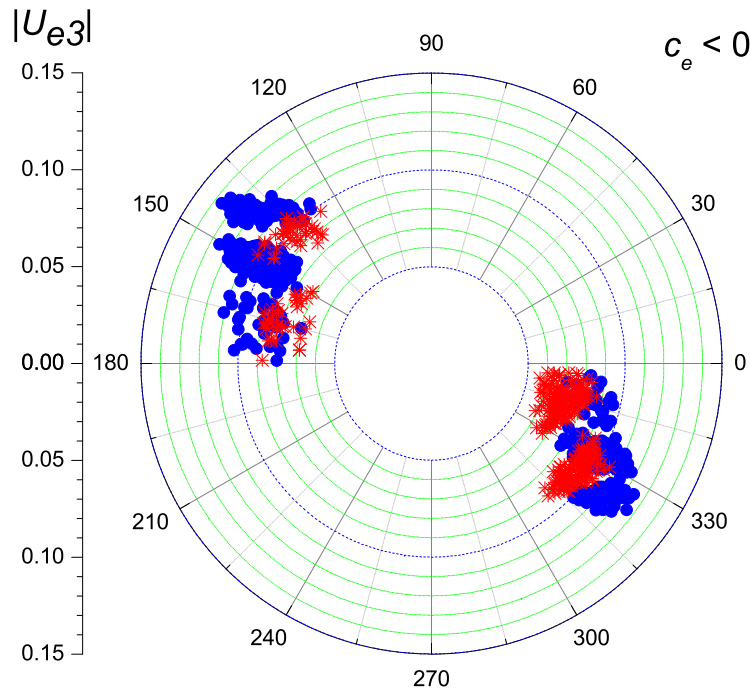
$$|U_{e3}| \approx 1/\sqrt{2} |V_{ub}/V_{cb}|$$



# MNSP Phase

The MNSP phase is given by the approximate expression:

$$\sin \delta_{\text{MNSP}} \sim 1/\sqrt{2} \sin \theta_{12}^e \sin \theta_{13}^v \sin(\tan^{-1} c_e \bar{h}'_{12} / (3 \bar{f}_{12}))$$



**B.D.,Y. Mimura, R. Mohapatra,  
Phys.Rev.Lett.94:091804,05;  
Phys.Rev.D72:075009,2005.**

# Gauge Coupling Unification

The minimal  $SO(10)$  model is ruled out  
When gauge coupling unification is required.

S. Bertolini et al, Phys.Rev.D73:115012,2006.

Fermion mass hierarchies plus the  $SO(10)$  breaking vacuum causes problem to gauge coupling unification

The minimal  $SO(10)$  superpotential is used, i.e.,  
210, 10 and 126 [K. Babu, R. Mohapatra, Phys.Rev.Lett.70:2845,1993]

Proton decay also applies strong constraint

**Soln.: Extension is needed, extra 120, 10 etc.**

# **Gauge Coupling Unification...**

**We can solve this puzzle using 120 or even with an additional 10' Higgs extension**

**The SO(10) symmetry breaks at around  $10^{17-18}$  GeV**

**We also need the colored Higgs masses to be at the string scale for successful unification**

**This automatically solves proton decay problem.**



# Gauge Coupling Unification...

The strategy is to find the lighter multiplets to keep the gauge coupling unification at the string scale

The lighter multiplets which can move the gauge coupling unification to  $10^{17-18}$  GeV are the followings:  
(8,1,0); (8,2,1/2)+cc; (6,1,1/3)+cc; (6,2,-1/6)+cc [210,126+126]

The colored Higgs masses are of the string scale → proton decay is suppressed.

The new multiplets can be around  $10^{15-16}$  GeV and the unification scale is the string scale → Flavor violation due to the majorana couplings [when the fields from 126+ $\overline{126}$  are light].

Dutta, Mimura and Mohapatra, Phys.Rev.Lett.100:181801,2008.

# Gauge Coupling Unification and Proton Decay

Proton decay amplitudes are reduced, since the Cutoff scale are high

$$\lambda_u \lambda_d \frac{1}{M_{Hc}} \frac{1}{M_{SUSY}} \alpha_s / 2 \pi$$

$M_{H3}$  becomes large

The unification of the three gauge couplings provides two independent relations on the particle mass spectrum below the symmetry breaking scale

Hisano, Murayama and Yanagida'93

$$\begin{aligned}
 & -2\alpha_3^{-1}(m_Z) + 3\alpha_2^{-1}(m_Z) - \alpha_1^{-1}(m_Z) \\
 &= \frac{1}{2\pi} \left( \frac{12}{5} \ln \frac{M_{Hc}}{m_Z} + \sum_I N_A^I \ln \frac{M_I}{\Lambda} - 2 \ln \frac{m_{SUSY}}{m_Z} \right), \\
 & -2\alpha_3^{-1}(m_Z) - 3\alpha_2^{-1}(m_Z) + 5\alpha_1^{-1}(m_Z) \\
 &= \frac{1}{2\pi} \left( 12 \ln \frac{M_X^2 \Lambda}{m_Z^3} + \sum_I N_B^I \ln \frac{M_I}{\Lambda} + 8 \ln \frac{m_{SUSY}}{m_Z} \right),
 \end{aligned}$$

$$N_A^I = 2T^3(\varphi^I) - 3T^2(\varphi^I) + T^1(\varphi^I) \text{ and } N_B^I = 2T^3(\varphi^I) + 3T^2(\varphi^I) - 5T^1(\varphi^I)$$

# Proton Decay...

**Case 1: no  $\phi$ 's;  $M_{\text{HC}} \sim 10^{15}$  GeV: bad for proton decay**

**SU(5) got ruled out...**

**Case 2: with  $\phi$ 's;  $M_{\text{HC}}$  can be large (using positive  $N^{\text{ls}}$ ):  
good for proton decay**

**We rescue SO(10)...**

# How general are these solutions?

## Can we rescue any SO(10)?

**Yes, we can! Provided we have the following multiplets around  $10^{16}$  GeV**

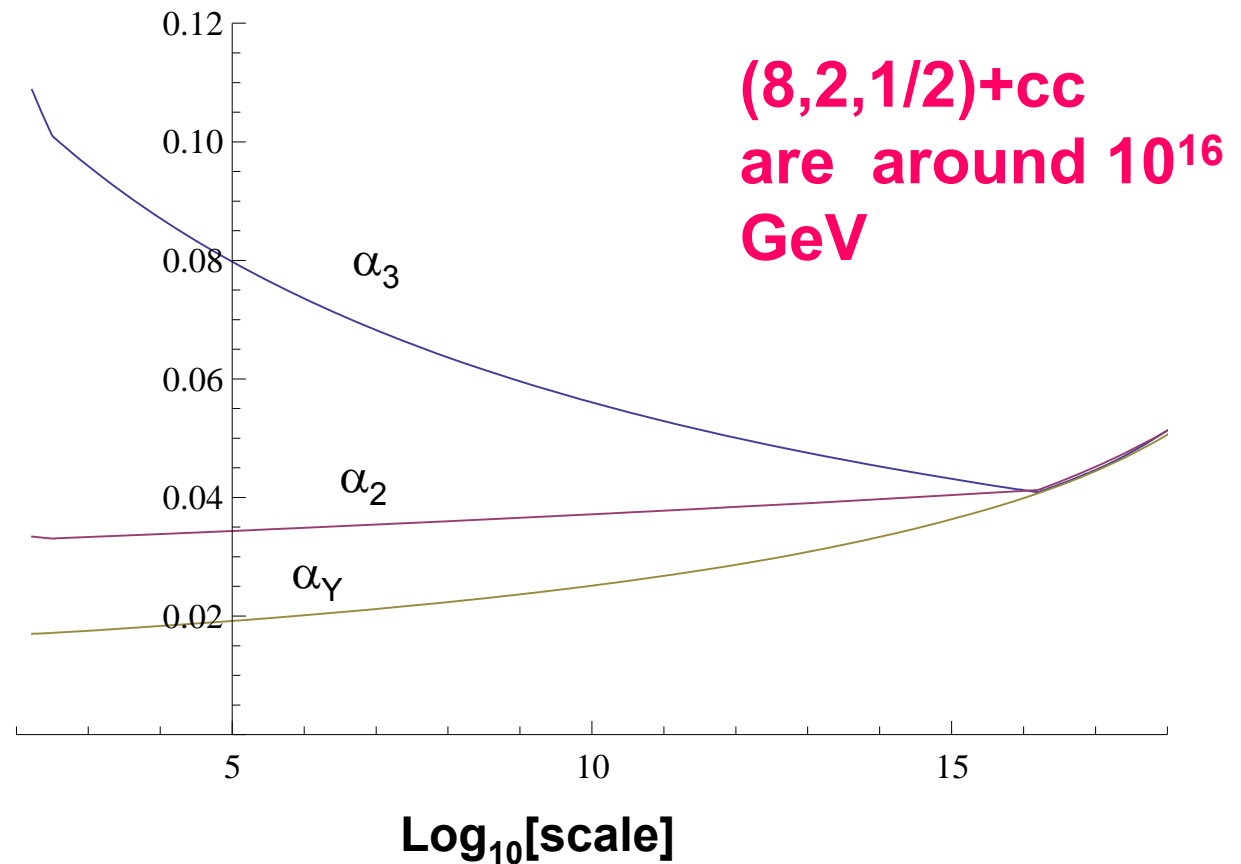
TABLE II: List of the fields whose  $N_A$  and  $N_B$  are both positive. The definitions of  $N_A$  and  $N_B$  are given in the text.

	$N_A$	$N_B$	SO(10)	SU(5)
$(\mathbf{8}, \mathbf{2}, 1/2) + c.c.$	$\frac{24}{5}$	24	$\mathbf{126} + \overline{\mathbf{126}}, \mathbf{120}$	$\mathbf{45}, \mathbf{50}$
$(\mathbf{6}, \mathbf{1}, 1/3) + c.c.$	$\frac{54}{5}$	6	$\mathbf{126} + \overline{\mathbf{126}}, \mathbf{120}$	$\mathbf{45}$
$(\mathbf{6}, \mathbf{2}, -1/6) + c.c.$	$\frac{12}{5}$	36	$\mathbf{210}$	$\mathbf{40}$
$(\mathbf{8}, \mathbf{1}, 0)$	6	6	$\mathbf{210}, \mathbf{45}, \mathbf{54}$	$\mathbf{24}, \mathbf{75}$

**Only these four fields can rescue SO(10)**

# Gauge Coupling Unification...

## The Unification



# Status of Proton Decay in the new scenario

Since the colored Higgs fields can be heavier than  $10^{17}$  GeV and the current nucleon decay bounds can be satisfied.

If  $\tan \beta$  is large enough  $>20$ , the proton decay via dimension five operator (such as  $p \rightarrow K^{\bar{v}}$ ) can be observable in the megaton class detector.

However, the proton decay via the dimension six operator (such as  $p \rightarrow \pi e$ ) may not be observed

# Flavor violations:

If  $(8, 2, 1/2)$  and/or  $(6, 1, 1/3)$  is much lighter than the  $SO(10)$  breaking scale, a sizable flavor violation can be generated since those fields originate from 126 or 120 which couple to fermions

The couplings can be written as

$$f_{qu} \bar{q} u^c \phi(8, 2, 1/2) + f_{qd} \bar{q} d^c \phi(8, 2, -1/2) + f_{qq} \bar{q} q \phi(6, 1, -1/3) + f_{u^c d^c} \bar{u}^c d^c \phi(6, 1, 1/3)$$

If  $(8, 2, 1/2)$  field is light, it can generate off-diagonal elements for both left- and right handed squark mass matrices  $[f_{23} \sim f_{33}]$

If the light  $(\bar{6}, 1, -1/3)$  field comes from 126, it can generate off-diagonal elements only for left-handed squarks.

*If both left- and right-handed squark mass matrices have sizable off-diagonal elements, the meson mixing via box diagram is enhanced and thus, it can have impact on  $D^+ D^-$ ,  $B_s^+ B_s^-$  mixings etc*

However,  $f_{16 \cdot 16} H_{126}$  coupling has a source of large mixings.

The coupling includes the Majorana couplings :  $f_L L L \Delta_L + f_R L^c L^c \Delta_R$

$$m_{\tilde{Q}}^2 \simeq m_{\tilde{Q}}^2 \simeq m_{\tilde{U}^c}^2 \simeq m_{\tilde{D}^c}^2$$

$$m_{\tilde{Q}}^2 \simeq m_0^2 \left( \mathbf{1} - \kappa U \begin{pmatrix} k_1 & & \\ & k_2 & \\ & & 1 \end{pmatrix} U^\dagger \right)$$

Threshold parameter :  $\kappa \simeq \frac{(f_{33}^{\text{diag}})^2}{8\pi^2} \left( 3 + \frac{A_0^2}{m_0^2} \right) \ln \frac{M_*}{M_{\text{GUT}}}$

$$f = U f^{\text{diag}} U^T$$

$M_*$ : String/Planck scale

$$m_{\tilde{D}^c}^2 \Big|_{23} = -\frac{1}{2} m_0^2 \kappa \sin 2\theta_{23} e^{i\alpha} \qquad k_2 \simeq \frac{\Delta m_{\text{sol}}^2}{\Delta m_{\text{atm}}^2}$$

Both left- and right-squarks have sizable FCNC effects!

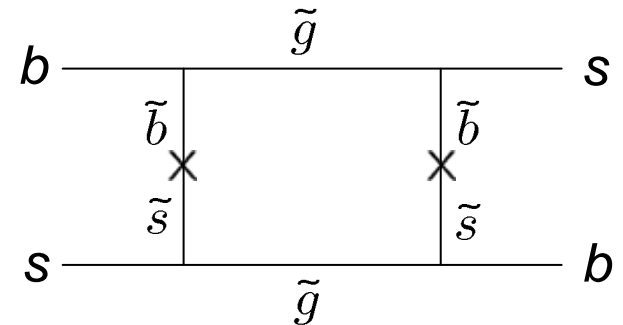


# SUSY contributions in $B$ - $\bar{B}$ mixings

$$M_{12} = \langle B | H | \bar{B} \rangle$$

$$\Delta M = 2|M_{12}|$$

The gluino box diagram dominates.



Mass insertion approximation:

$$\frac{M_{12}^{\text{SUSY}}}{M_{12}^{\text{SM}}} \simeq a[(\delta_{LL}^d)_{32}^2 + (\delta_{RR}^d)_{32}^2] - b(\delta_{LL}^d)_{32}(\delta_{RR}^d)_{32} + \dots$$

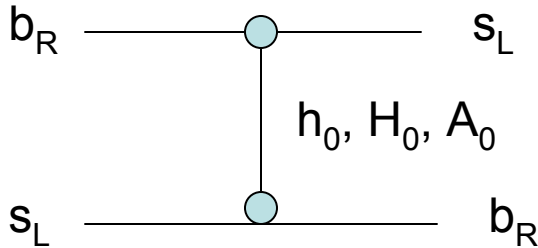
$a \sim O(1), b \sim O(100)$  for  $m_{\text{SUSY}} \sim 1 \text{ TeV}$

(Randall-Su; Ball-Khalil-Kou)

$$\delta_{LL,RR}^d = (M_{\tilde{d}}^2)_{LL,RR} / \tilde{m}^2 \quad \tilde{m} : \text{average squark mass}$$

$$(\tilde{d}_L, \tilde{d}_R) \begin{pmatrix} (M_{\tilde{d}}^2)_{LL} & (M_{\tilde{d}}^2)_{LR} \\ (M_{\tilde{d}}^2)_{RL} & (M_{\tilde{d}}^2)_{RR} \end{pmatrix} \begin{pmatrix} \tilde{d}_L^\dagger \\ \tilde{d}_R^\dagger \end{pmatrix} \quad \begin{aligned} (M_{\tilde{d}}^2)_{LL} &= m_{\tilde{Q}}^2 + \dots \\ (M_{\tilde{d}}^2)_{RR} &= (m_{\tilde{D}^c}^2)^\top + \dots \end{aligned}$$

# Large $\tan\beta$



Double penguin diagram can have large Contribution

[Hamzaoui, Pospelov and Toharia;  
Buras, Chankowski, Rosiek and Slawianowska]

This diagram's contribution ( $\sim \kappa^2 \tan^4\beta / M_A^4$ )

Both SU(5) and SO(10) get contribution from this diagram

Chargino and gluino mediated penguins contribute

➔ Similar single penguin diagrams contribute to  $\text{Br}[B_s \rightarrow \mu\mu]$   
( $\sim \kappa^2 \tan^6\beta / M_A^4$ )

Large  $B_s$  phase induces larger  $B_s \rightarrow \mu\mu$  process even for  $\tan\beta \sim 20$   
for universal boundary condition

# New Physics Contribution in the Mixing

Accurate measurement of mass difference  
is consistent with SM.

$$\Delta M_s = 17.77 \pm 0.10 \pm 0.07 \text{ ps}^{-1}$$

[Tevatron]

One may think that large SUSY contribution is not allowed.

However, experimental result of  $\Delta M_s = 2|M_{12}(B_s)|$   
does not constrain size of SUSY contribution  $|M_{12}^{\text{SUSY}}|$  much.

$$M_{12} = M_{12}^{\text{SM}} + M_{12}^{\text{SUSY}}$$

$\equiv \Delta_{12}^{\text{NP}}$

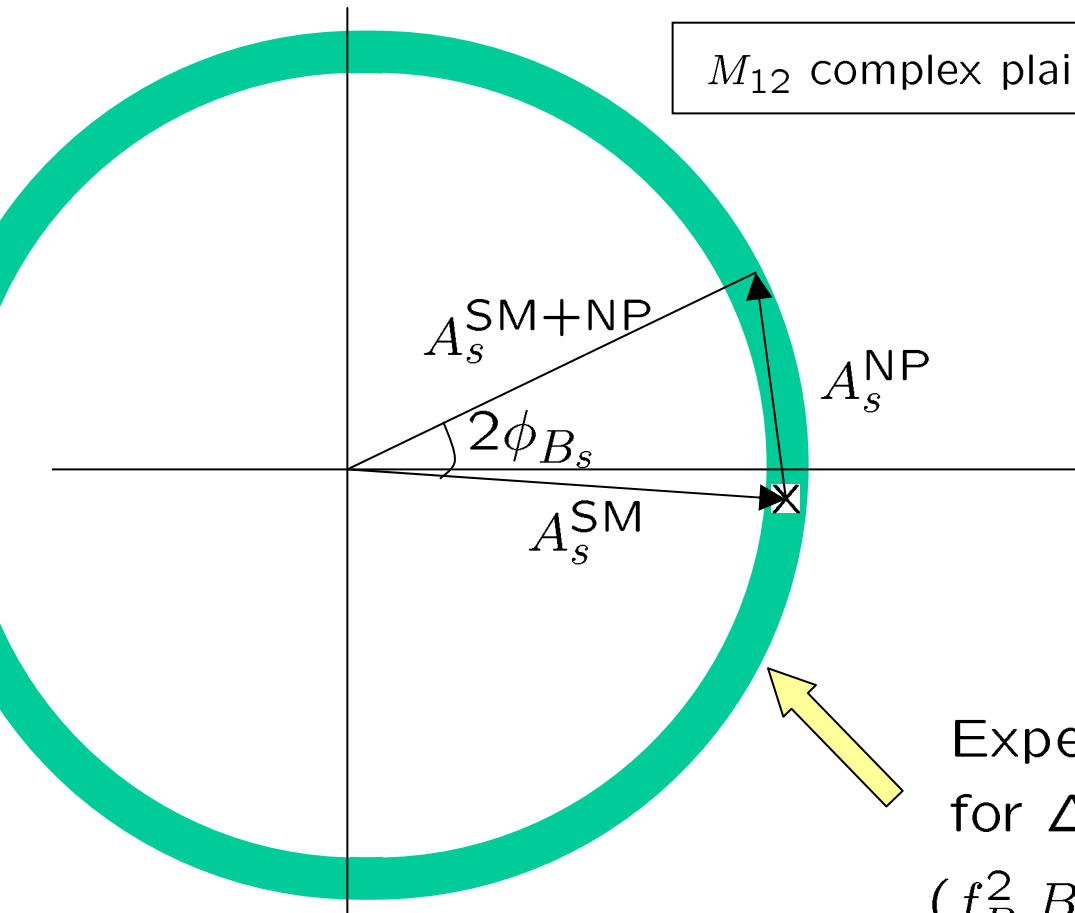
arg  $M_{12}^{\text{SUSY}}$  is free in the model

Due to free phases in the Yukawa coupling

➔ There is room for a sizable SUSY contribution.

**What is this large SUSY contribution?**

$M_{12}$  complex plain



When  $A_s^{\text{SM}} \simeq A_s^{\text{SM}+\text{NP}}$ ,

$$\sin \phi_{B_s} \simeq \frac{1}{2} \frac{A_s^{\text{NP}}}{A_s^{\text{SM}}}$$

Experimental bound  
for  $\Delta M_s$

( $f_{B_s}^2 B_{B_s}$  ambiguity from lattice)

$$\frac{M_{12}^{\text{full}}}{M_{12}^{\text{SM}}} = \frac{A_s^{\text{SM}} e^{-2i\beta_s} + A_s^{\text{NP}} e^{2i(\phi_s^{\text{NP}} - \beta_s)}}{A_s^{\text{SM}} e^{-2i\beta_s}} \equiv C_{B_s} e^{2i\phi_{B_s}}$$

# SU(5) GUT

Down quarks ( $D^c$ ) and lepton doublet ( $L$ ) are unified in  $\bar{5}$ .

$Q, U^c, E^c : \mathbf{10}$       Right-handed neutrino :  $N^c$

$$W_Y = Y_u \mathbf{10} \cdot \mathbf{10} H_5 + Y_d \mathbf{10} \cdot \bar{\mathbf{5}} H_{\bar{5}} + Y_\nu \bar{\mathbf{5}} N^c H_5$$

Both RH down-squarks and LH sleptons can have FCNC effects.

(Moroi, Akama-Kiyo-Komine-Moroi, Baek-Goto-Okada-Okumura, ...)

# SU(5) GUT...

$$m_5^2 \simeq m_0^2 \left( \mathbf{1} - \kappa U \begin{pmatrix} k_1 & & \\ & k_2 & \\ & & 1 \end{pmatrix} U^\dagger \right)$$

$\propto Y_\nu Y_\nu^\dagger$

$$Y_e = Y_e^{\text{diag}}$$

$$Y_\nu = U Y_\nu^{\text{diag}} U_R^\dagger$$

$$M_N = M_N^{\text{diag}}$$

$$m_5 = m_{\tilde{D}^c} = m_{\tilde{L}}$$

$$k_1, k_2 \ll 1$$

$$m_{10} = m_{\tilde{Q}} = m_{\tilde{U}^c} = m_{\tilde{E}^c}$$

$$\kappa \simeq \frac{(Y_{\nu 33}^{\text{diag}})^2}{8\pi^2} \left( 3 + \frac{A_0^2}{m_0^2} \right) \ln \frac{M_*}{M_{\text{GUT}}}$$

$U$  : unitary mixing matrix

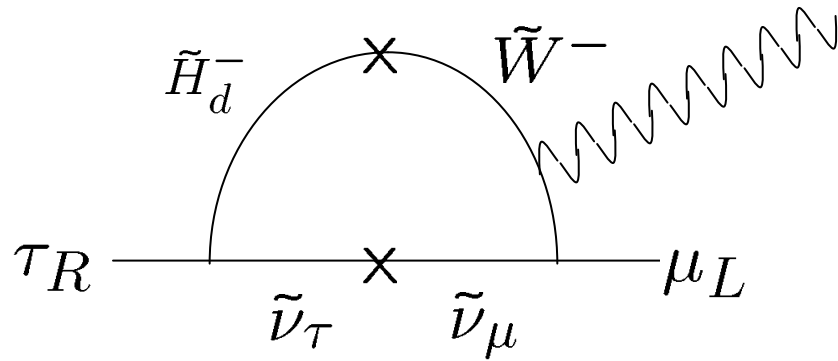
$$(m_5^2)_{23} = -\frac{1}{2} m_0^2 \kappa \sin 2\theta_{23} e^{i\alpha}$$



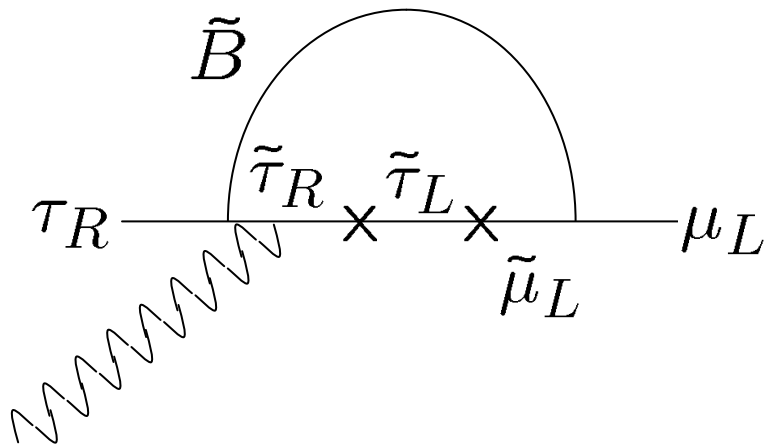
$U$  is the MNS neutrino mixing matrix.

**The flavor violating elements in  $m_5^2$  induces  $B_s$  mixing**

# SU(5) GUT...



$$\propto \kappa \frac{1}{m_5^2} \frac{M_W}{\mu} \tan \beta$$



$$\propto \kappa \frac{1}{m_{10}^2} \frac{\mu \tan \beta m_\tau}{m_5^2}$$

Large  $m_5, m_{10}, \mu$  are needed to suppress  $\tau \rightarrow \mu\gamma$ .



Sparticle spectrum is restricted.



LHC

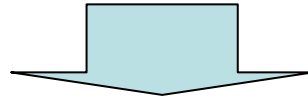
# SO(10) GUT

Both left- and right-squarks have FCNC effects in SO(10).

$$\frac{M_{12}^{\text{SUSY}}}{M_{12}^{\text{SM}}} \simeq a[(\delta_{LL}^d)_{32}^2 + (\delta_{RR}^d)_{32}^2] - b(\delta_{LL}^d)_{32}(\delta_{RR}^d)_{32} + \dots$$

$$a \sim O(1), b \sim O(100) \text{ for } m_{\text{SUSY}} \sim 1 \text{ TeV}$$

---



Flavor violating effects are larger in the box diagram in SO(10).

Only  $\delta_{RR}^d$  is large in SU(5).

**Dutta and Mimura, Phys.Rev.Lett.97:241802,2006.**



# Large Phase of $B_s$ - $\bar{B}_s$ mixing

CP violation in  $B_s \rightarrow J/\psi\phi$  decay ( $b \rightarrow sc\bar{c}$ ).

$$S_{b \rightarrow sc\bar{c}} = \sin \phi_s$$

SM prediction :  $\phi_s = 2\beta_s \simeq 0.04$  (rad) **small!**

$$\beta_s \equiv \arg \left( -\frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*} \right)$$

Measurements :

$$\phi_s(\text{CDF}) = -0.28 \text{ to } -1.29 \quad (2.8 \text{ fb}^{-1}) \quad \text{arXiv:0810.3229}$$

$$\phi_s(\text{D0}) = 0.57^{+0.30}_{-0.24}(\text{stat})^{+0.02}_{-0.07}(\text{syst}) \quad (2.8 \text{ fb}^{-1})$$

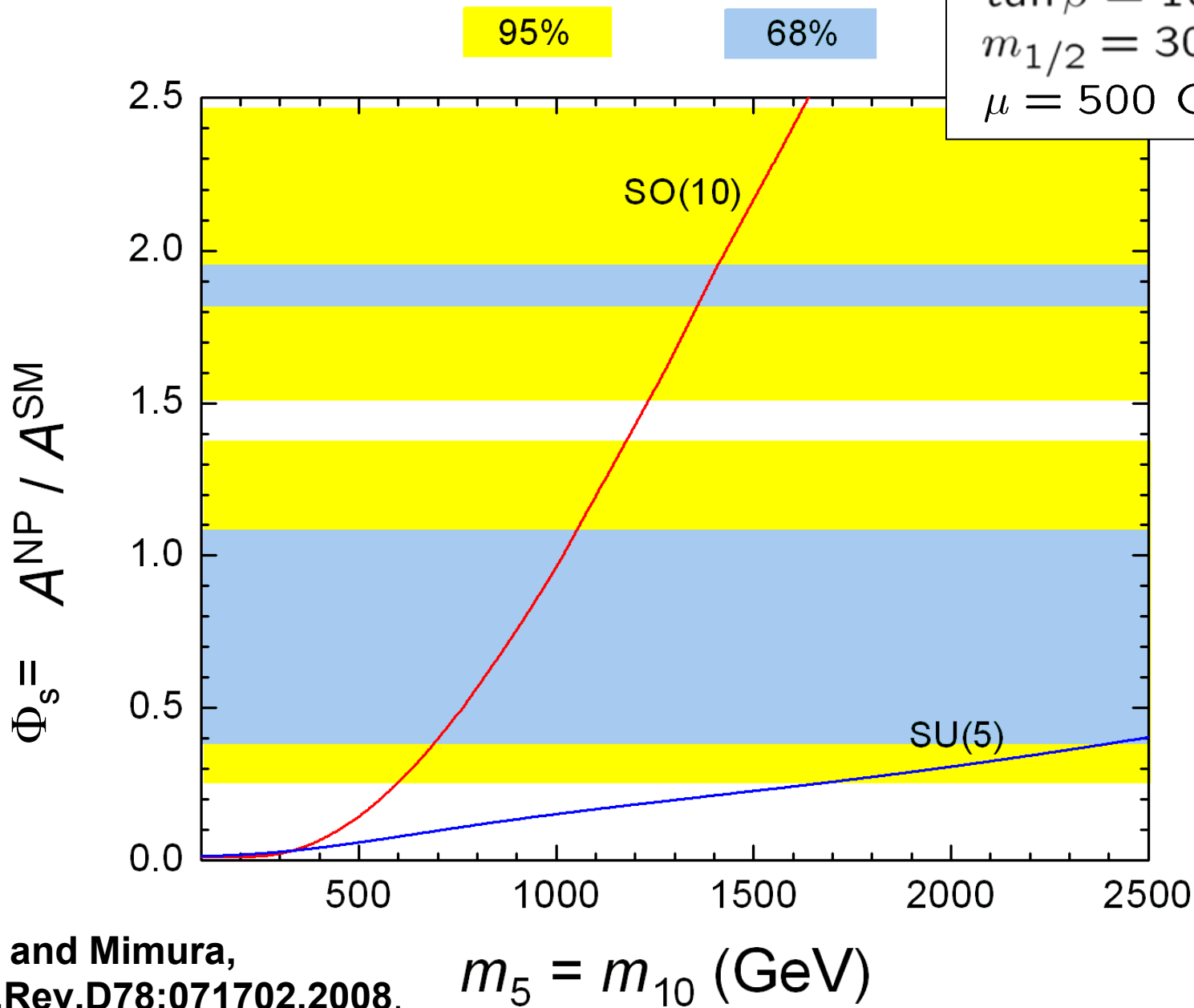
**2.2 sigma deviation from the SM** (arXiv: 0802.2255)

**Combined data analysis by UFit: More than 3 sigma deviation from the SM**

$$\phi_{B_s} = -19.9 \pm 5.6 \text{ (degree)} \quad \text{arXiv:0803.0659}$$

# Large Phase of $B_s - \bar{B}_s$ mixing

$\text{Br}(\tau \rightarrow \mu\gamma) < 4.5 \times 10^{-8}$   
 $\tan\beta = 10$   
 $m_{1/2} = 300 \text{ GeV}$   
 $\mu = 500 \text{ GeV}$



Dutta and Mimura,  
Phys.Rev.D78:071702,2008.

$m_5 = m_{10}$  (GeV)

# Large Phase of $B_s-\bar{B}_s$ mixing : Semileptonic $B \rightarrow X+l$

## New Fermilab results from D0

$$A_{sl}^b = \frac{N_b^{++} - N_b^{--}}{N_b^{++} + N_b^{--}} \quad N_b^{++}, N_b^{--}: \text{number of events containing two } b \text{ hadrons decaying semileptonically}$$

$A_{sl}^b$  : equivalent to the charge asymmetry of semileptonic decays of  $b$  hadrons to wrong charge muons that are induced by oscillation

$$A_{sl}^b = \frac{\Gamma(\bar{B} \rightarrow \mu^+ + X) - \Gamma(B \rightarrow \mu^- + X)}{\Gamma(\bar{B} \rightarrow \mu^+ + X) + \Gamma(B \rightarrow \mu^- + X)} = a_{sl}^b$$

$$A_{sl}^b = (0.506 \pm 0.043)a_{sl}^d + (0.494 \pm 0.043)a_{sl}^s$$

$$a_{sl}^d(SM) = (-4.8_{-1.2}^{+1.0}) \times 10^{-4}$$

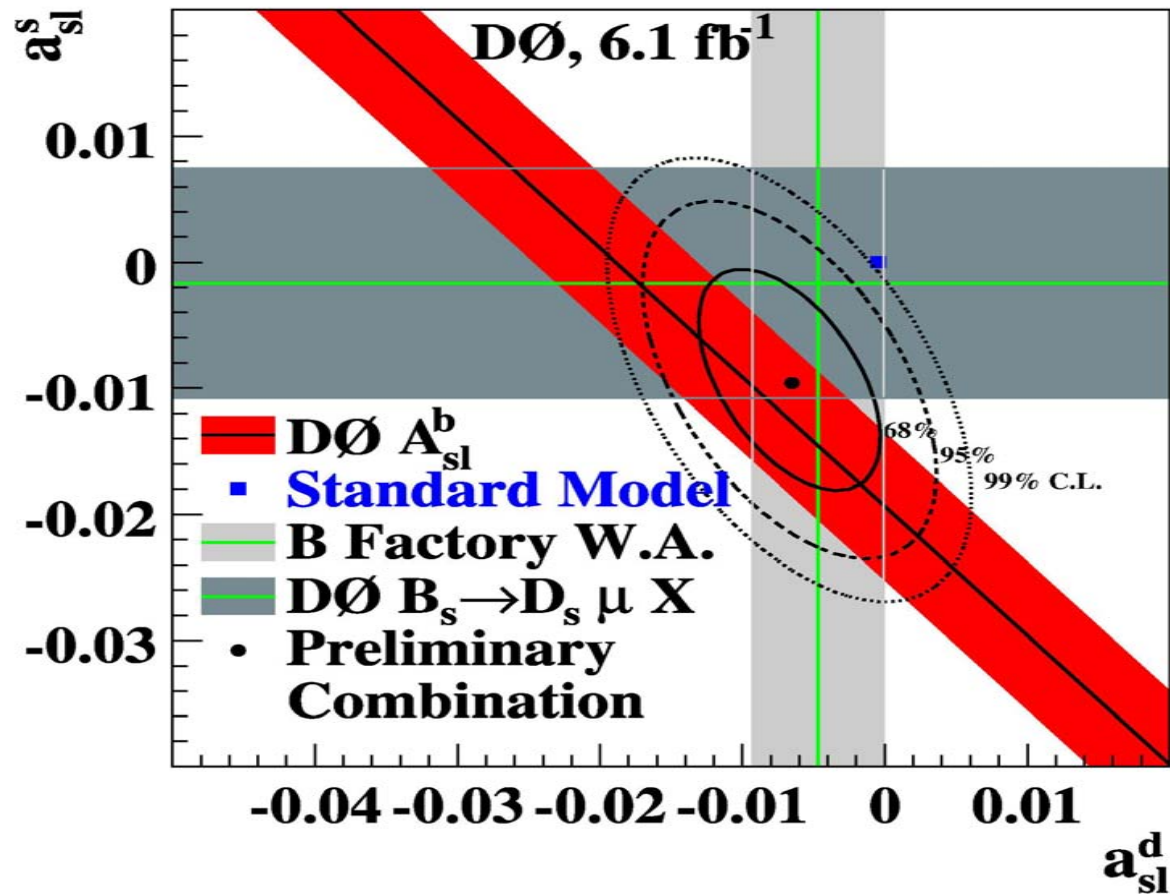
$$a_{sl}^s(SM) = (2.1 \pm 0.6) \times 10^{-5}$$

$$A_{sl}^b(SM) = (-2.3_{-0.6}^{+0.5}) \times 10^{-4}$$

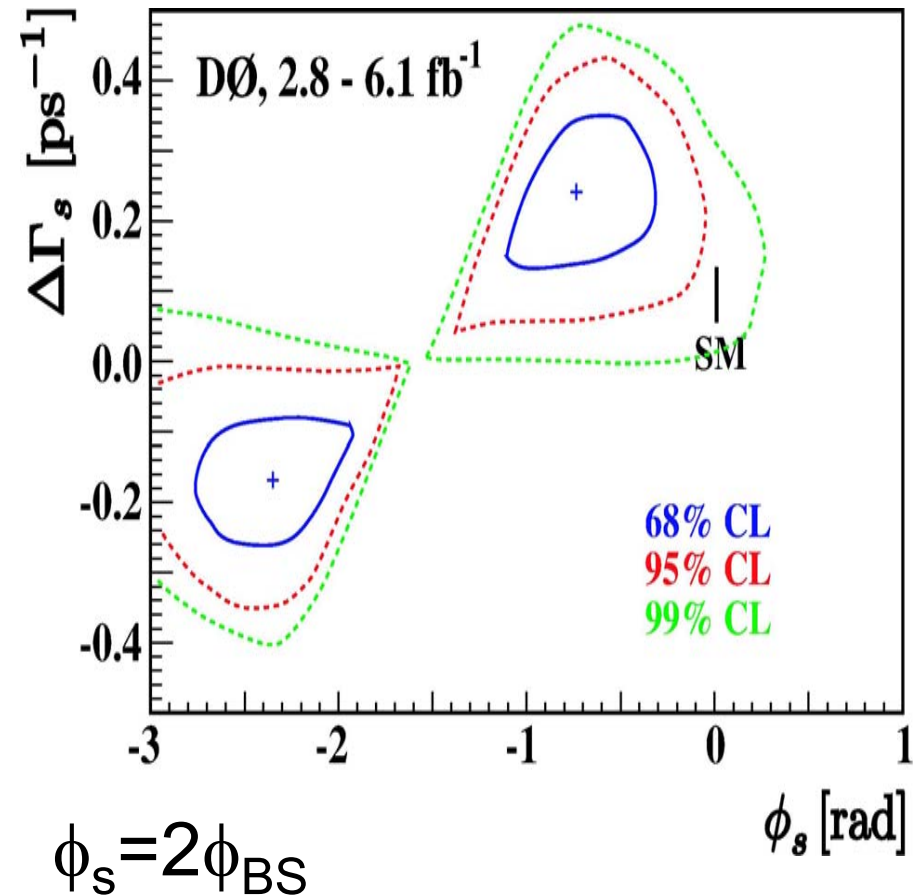
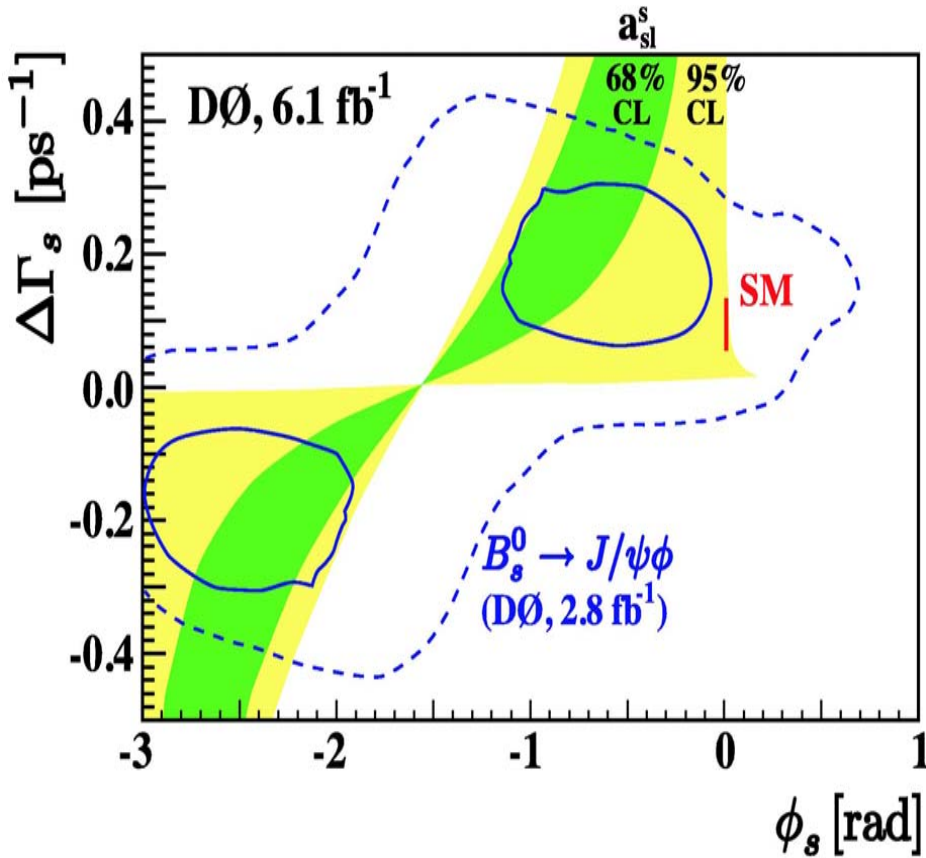
$$a_{sl}^q = \frac{|\Gamma_q^{12}|}{|M_q^{12}|} \sin \phi_q$$

$$A_{sl}^b = -0.00957(stat) \pm 0.00251 \pm 0.00146(syst) : \text{Exptal} \quad : 3.2 \sigma$$

# New Fermilab results from D0...

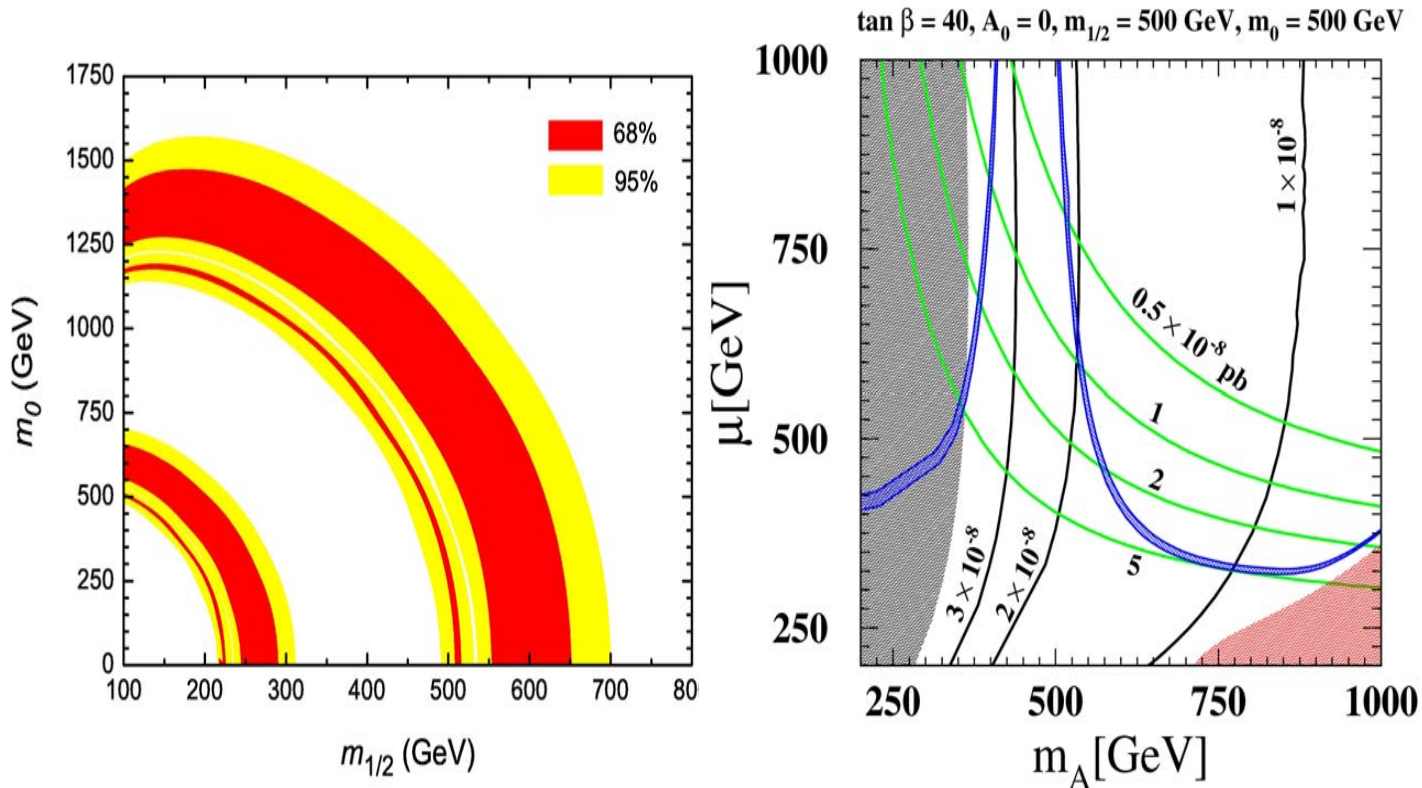


# New Fermilab results from D0...

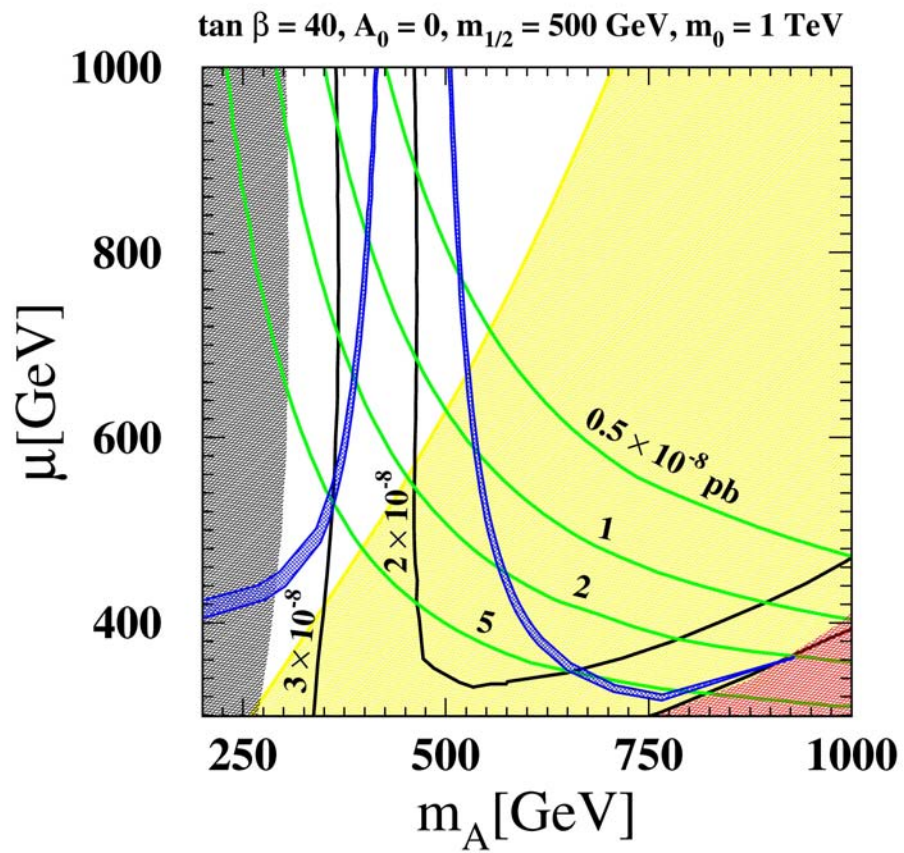


Using the experimental range for  $a_{\text{SL}}^d$

# Effect of Large Phase: e.g., $\phi_{BS} \sim 0.5$



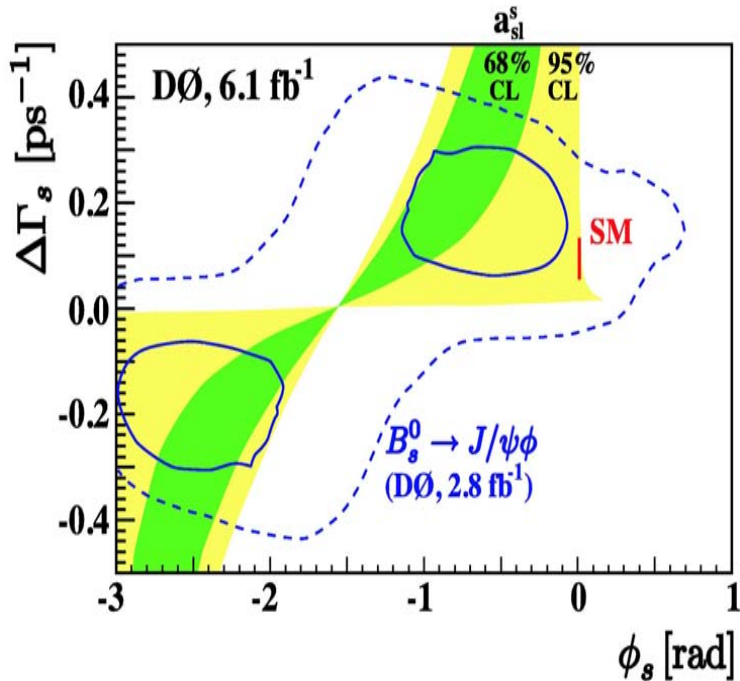
Dutta and Mimura, Phys.Rev.D80:095005,2009.



$\phi_s \sim 0.5$

Dutta and Mimura, Phys.Rev.D80:095005,2009.

# Tension???



In order to obtain the fit, experimental Value is used  $a_{SL}^d : (-4.6 \pm 4.7) \times 10^{-3}$

If we use the theoretical SM value  $(-4.8 \times 10^{-4})$ , within  $1 \sigma$  of  $A_{SL}^b$   $a_{SL}^s$  has to be at least  $-0.012$  or smaller

→  $\sin\phi = -2.5 \pm 1.3$

More than  $1 \sigma$  away from  $|\sin\phi| < 1$

1. New contribution to  $a_{SL}^d$ : But  $\sin 2\beta$  is well measured

$$2. a_{sl}^s = 2 \frac{|\Gamma_s^{12}|}{|\Delta M_s^{SM}|} \frac{\sin\phi_s}{\Delta} \quad \text{Where} \quad \Delta = 0.97 \pm 0.26; \Gamma_s^{12}(SM) = 1/2(0.096 \pm 0.04) ps^{-1}$$

One can consider new physics contribution in  $\Gamma$ : need to compete with CKM favored tree level contribution to  $b \rightarrow c\bar{c}s$



# Conclusion

**We should wait for CDF to confirm this semileptonic asymmetry**



**The existence of deviation in the CP asymmetry measurement of  $B \rightarrow J/\Psi \phi$  from both CDF and D0 has made a good case for new physics**

**SO(10) model has a good chance to explain this**

**We showed an example of an SO(10) model which does not have proton decay problem, explains the masses and mixings of fermions**