



MADFKS

AUTOMATION OF THE FKS SUBTRACTION METHOD

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NEXT-TO-LEADING ORDER

$$\sigma^{\text{NLO}} = \int_{m+1} d^{(d)} \sigma^R + \int_m d^{(d)} \sigma^V + \int_m d^{(4)} \sigma^B$$

‘Real emission’
NLO corrections

‘Virtual’ or ‘one-loop’
NLO corrections

‘Born’ or ‘LO’
contribution

WHY AUTOMATE?

- ☀ To save time

NLO calculations can take a long time. It would be nice to spend this time doing phenomenology instead.

- ☀ To reduce the number of bugs in the calculation

Having a code that does everything automatically will be without bugs once the internal algorithms have been checked properly.*

- ☀ To have all processes within one framework

To learn how to use a new code for each process is not something all our (experimental) colleagues are willing to do.

IR DIVERGENCE

$$\sigma^{\text{NLO}} = \int_{m+1} d^{(d)} \sigma^R + \int_m d^{(d)} \sigma^V + \int_m d^{(4)} \sigma^B$$

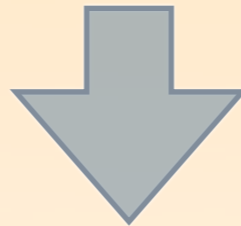
- ✱ Real emission -> IR divergent
- ✱ (UV-renormalized) virtual corrections
-> IR divergent
- ✱ After integration, the sum of all contributions is finite
(for infrared-safe observables)
- ✱ To see this cancellation the integration is done in a non-integer number of dimensions:
Not possible with a Monte-Carlo integration

SUBTRACTION TERMS

$$\sigma^{\text{NLO}} = \int_{m+1} d^{(d)} \sigma^R + \int_m d^{(d)} \sigma^V + \int_m d^{(4)} \sigma^B$$

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$$\sigma^{\text{NLO}} = \int_{m+1} d^{(d)} \sigma^R + \int_m d^{(d)} \sigma^V + \int_m d^{(4)} \sigma^B$$



$$\sigma^{\text{NLO}} = \int_{m+1} \left[d^{(4)} \sigma^R - d^{(4)} \sigma^A \right] + \int_m \left[d^{(4)} \sigma^B + \int_{\text{loop}} d^{(d)} \sigma^V + \int_1 d^{(d)} \sigma^A \right]_{\epsilon=0}$$

- ✿ Include subtraction terms to make real emission and virtual contributions separately finite
- ✿ All can be integrated numerically

MADFKS

*In collaboration with Stefano Frixione, Fabio Maltoni &
Tim Stelzer, arXiv: 0908.4247*

FKS SUBTRACTION

$$\sigma^{\text{NLO}} = \int_{m+1} \left[d^{(4)} \sigma^R - d^{(4)} \sigma^A \right] + \int_m \left[d^{(4)} \sigma^B + \int_{\text{loop}} d^{(d)} \sigma^V + \int_1 d^{(d)} \sigma^A \right]_{\epsilon=0}$$

- ✱ **FKS** subtraction: **F**rixione, **K**unszt & **S**igner 1996.
- ✱ Also known as “residue subtraction”
- ✱ Based on partitioning the phase space such that each partition has at most one soft and/or collinear divergence
- ✱ Use simple plus-distributions to regulate the divergences
- ✱ Are relevant formulae can be found in our *MadFKS* paper, arXiv:0908.4247

FKS -- TECHNICALITIES

- ✿ Naive scaling of the number of subtraction terms is n^2 (as opposed to n^3 of CS dipoles). Can be greatly **reduced by using symmetry** of the matrix elements
 - ✿ Adding additional gluons does not lead to more phase-space partitions
- ✿ In a given phase space partition, **Born amplitudes need be computed only once** for each real-emission event, and can be used for the Born and collinear, soft and soft-collinear counter events (and their remainders)
- ✿ Trivially extended to **BSM physics**. Massive particles have only soft singularity which is independent of the spin

MADFKS

- ✿ Automatic FKS subtraction for QCD within the MadGraph/MadEvent framework
- ✿ Given the $(n+1)$ process, it generates the **real**, all the **subtraction terms** and the **Born** processes
- ✿ **Completely general & all automatic**, using the same user-friendly interface as MadGraph
- ✿ MadFKS works also for any **BSM physics** model implemented in MadGraph, e.g. MSSM
- ✿ Color-linked Borns generated by MadDipole *RE, Gehrmann & Greiner*
- ✿ **MC-ing over helicities possible**; only more efficient for high-multiplicity final states
- ✿ Phase-space generation for the (n) -body is the same as in standard MG. It has been heavily adapted to generate $(n+1)$ -body emission events at the same time

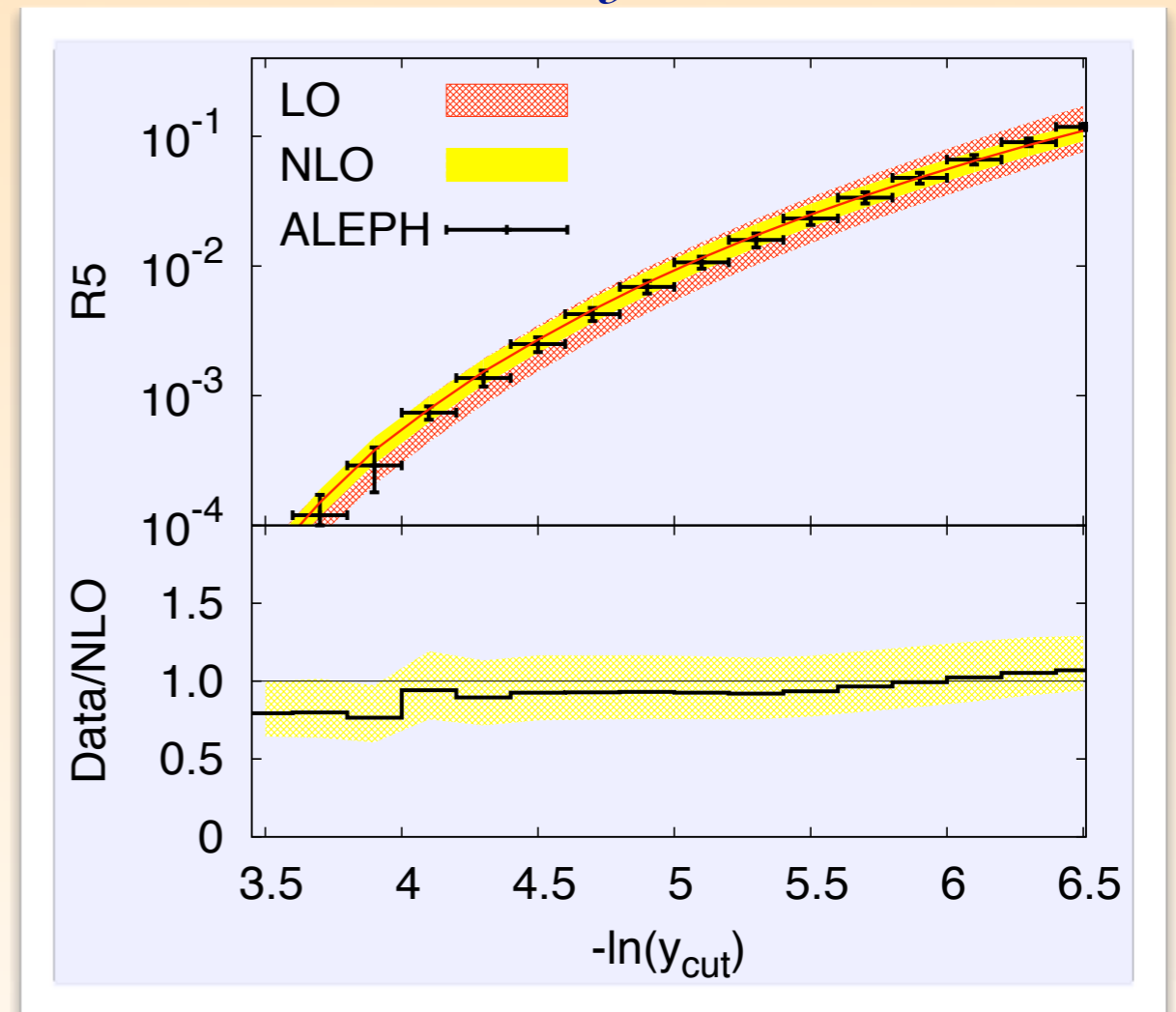
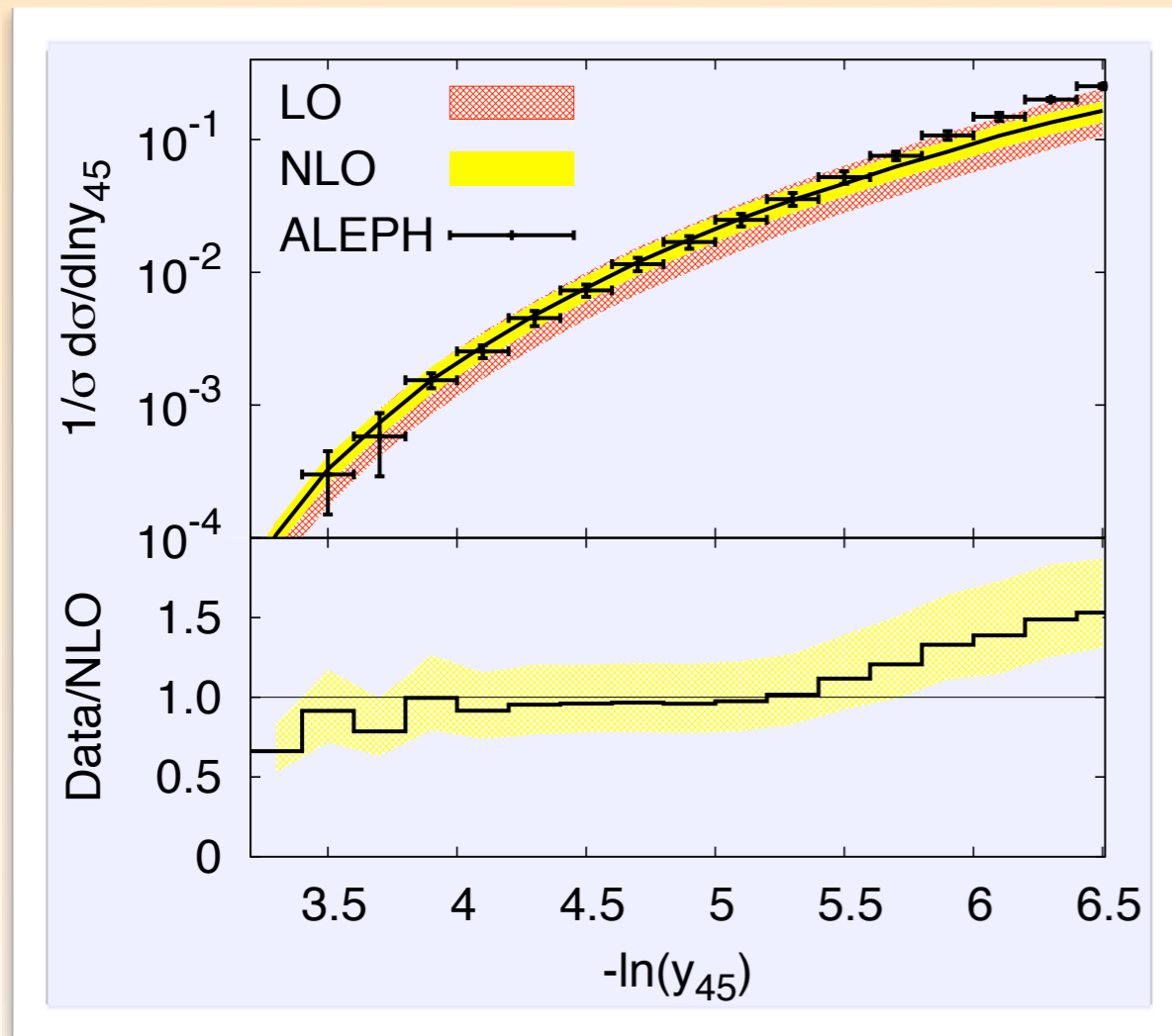
FULL NLO

- ✿ Of course, to get the total NLO results, the finite parts of the virtual corrections should be included as well
- ✿ Interface to link with the virtual corrections following the **Binoth-Les Houches Accord**
 - ✿ Standardized way to link MC codes to one-loop programs
- ✿ We are also working on an interface to CutTools
In collaboration with Hirschi, Garzelli e Pittau

5 JETS AT LEP @ NLO



RE, Frixione, Melnikov, Zanderighi arXiv:1008.5313



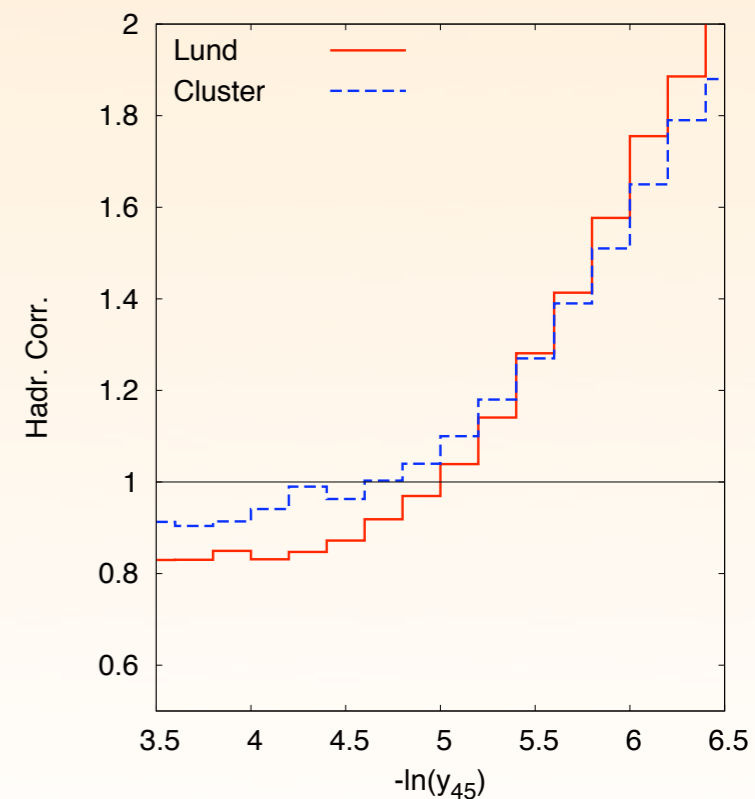
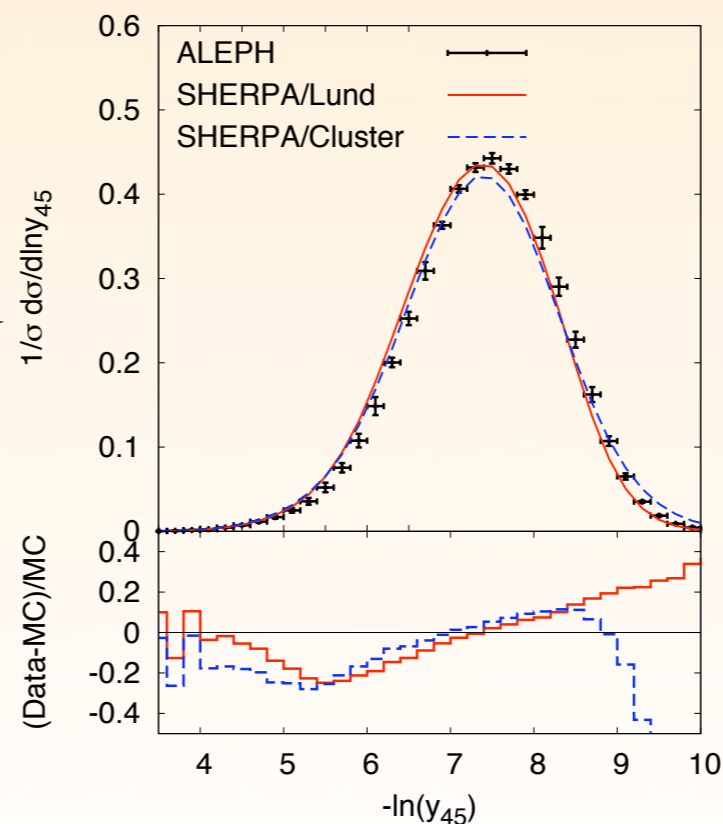
- ✿ Durham jet algorithm
- ✿ Scale dependence: +45% -30% at LO; **±20% at NLO**
- ✿ LO and NLO bands overlap (LO uses $\alpha_s(M_Z)=0.130$)
- ✿ Point-by-point agreement with BlackHat (*Berger et al.*) for the virtuals

HADRONIZATION CORRECTIONS

- Historically, for LEP, hadronization corrections have been estimated by using Ariadne, Herwig & Pythia, which are tuned to data
- However, they are based on $2 \rightarrow 2$ and $2 \rightarrow 3$ matrix elements. Therefore, for these 5 jet observables, they rely strongly on the showers.

- We have estimated the hadronization corrections using Sherpa, with CKKW matching up to 5 hard partons

- Corrections are mild up to $-\ln(y_{45}) \sim 6$



α_s EXTRACTION



	LEP1, hadr. $\sigma_{\text{tot}}^{-1} d\sigma/dy_{45}, R_5$	LEP1, no hadr. $\sigma_{\text{tot}}^{-1} d\sigma/dy_{45}, R_5$
stat.	+0.0002	+0.0002
	-0.0002	-0.0002
syst.	+0.0027	+0.0027
	-0.0029	-0.0029
pert.	+0.0062	+0.0068
	-0.0043	-0.0047
fit range	+0.0014	+0.0005
	-0.0014	-0.0005
hadr.	+0.0012	-
	-0.0012	-
$\alpha_s(M_Z)$	0.1159 ^{+0.0070} _{-0.0055}	0.1163 ^{+0.0073} _{-0.0055}

	LEP2, no hadr. $\sigma_{\text{tot}}^{-1} d\sigma/dy_{45}$	LEP2, no hadr. R_5	LEP2, no hadr. $\sigma_{\text{tot}}^{-1} d\sigma/dy_{45}, R_5$
stat.	+0.0020	+0.0022	+0.0015
	-0.0022	-0.0025	-0.0016
syst.	+0.0008	+0.0012	+0.0008
	-0.0009	-0.0012	-0.0008
pert.	+0.0049	+0.0029	+0.0029
	-0.0034	-0.0020	-0.0020
fit range	+0.0038	+0.0030	+0.0028
	-0.0038	-0.0030	-0.0028
$\alpha_s(M_Z)$	0.1189 ^{+0.0066} _{-0.0057}	0.1120 ^{+0.0050} _{-0.0047}	0.1155 ^{+0.0044} _{-0.0039}

- Statistical uncertainties negligible at LEP1; larger at LEP2
- Systematic and Perturbative uncertainties larger at LEP1 than LEP2, fit range uncertainties are opposite
- Uncertainties from hadronization corrections already negligible at LEP1, not even considered for LEP2
- Correlations between bins and LEP energies taken into account conservatively

$$\alpha_s(M_Z) = 0.1156^{+0.0041}_{-0.0034}$$

α_s EXTRACTION -- CORRELATIONS

- ✱ Statistical uncertainties are uncorrelated between different center-of-mass energies. At a given c.o.m. energy, y_{45} is uncorrelated, while R_5 is assumed to be fully correlated.
- ✱ Systematic uncertainties are assumed to be fully correlated at a given c.o.m. energy and between all LEP2 energies, however completely uncorrelated between LEP1 and LEP2.
- ✱ Perturbative uncertainties are assumed to be fully correlated.
- ✱ Hadronization uncertainties (considered only at LEP1) are assumed to be fully correlated.

COMPARISON WITH OTHER MEASUREMENTS

Observable	$\alpha_s(M_Z)$	Ref.
τ decays	0.1197 ± 0.0016	S. Bethke
Υ decays	0.119 ± 0.0055	N. Brambilla <i>et al.</i>
3 jet observables	0.1224 ± 0.0039	G. Dissertori <i>et al.</i>
jets in DIS	0.1198 ± 0.0032	H1 collaboration
DIS	0.1142 ± 0.0021	J. Blümlein
thrust	0.1135 ± 0.0011	R. Abbate <i>et al.</i>
lattice	0.1183 ± 0.0008	HPQCD collaboration
EW fits	0.1193 ± 0.0028	H. Flacher <i>et al.</i>
world average	0.1184 ± 0.0007	S. Bethke
$e^+e^- \rightarrow$ five jets	0.1156 ± 0.0038	RF, S. Frixione, K. Melnikov & G. Zanderighi

- ✱ Uncertainty competitive with other measurements
- ✱ Slightly smaller than world average, but consistent within uncertainties

VIRTUAL CORRECTIONS

*In collaboration with Valentin Hirschi and
Maria-Vittoria Garzelli e Roberto Pittau*

VIRTUAL CORRECTIONS

- ✱ Interface using the Binoth-LHA is available
- ✱ For more flexibility (e.g. massive particles & BSM) we also started working on generating the virtual corrections ourselves
- ✱ Using the OPP method as implemented in CutTools
Ossola, Papadopoulos & Pittau

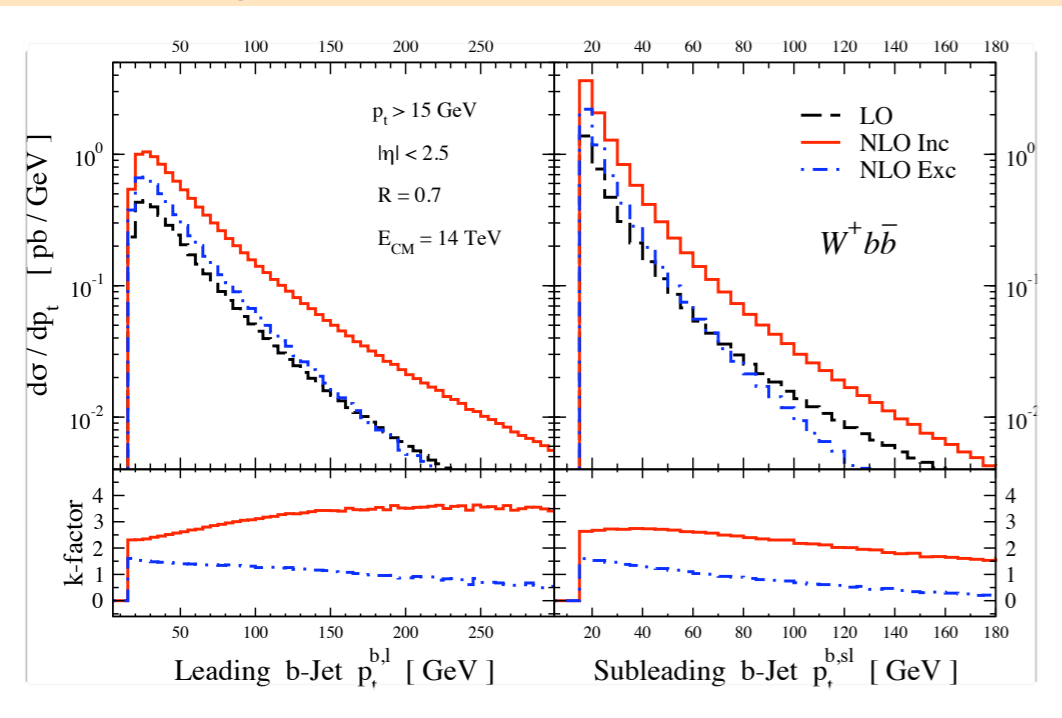
IMPLEMENTATION

- ✱ MadGraph generates the loop diagrams by cutting one of the particles in the loop: simple tree-level diagrams remain
→ Passed to **CutTools**
- ✱ **NLOComp** filters duplicates and sets-up the interference with the Born diagrams: computation of the color factors.
- ✱ Ghosts also needed
- ✱ R2 terms are computed using tree-level Feynman Rules
Draggiotis, Garzelli, Papadopoulos e Pittau
- ✱ Point-by-point agreement found with MCFM (and private codes):
Drell-Yan, 2-jet production, top pair, W/Z+1 jet...
- ✱ Not yet optimized in any way. This will be done only in the MGv5 framework

WBB ASSOCIATED PRODUCTION

- ✱ First new results with **MadFKS+NLOComp/CutTools**
- ✱ $pp \rightarrow W^+ (\rightarrow e^+ \nu_e) b \bar{b}$, with massive b's
- ✱ *Similar calculation by Febres Cordero, Reina e Wackeroth*
- ✱ However, here the W boson decay is included, and stable enough to generate results without cuts on the bottom quarks

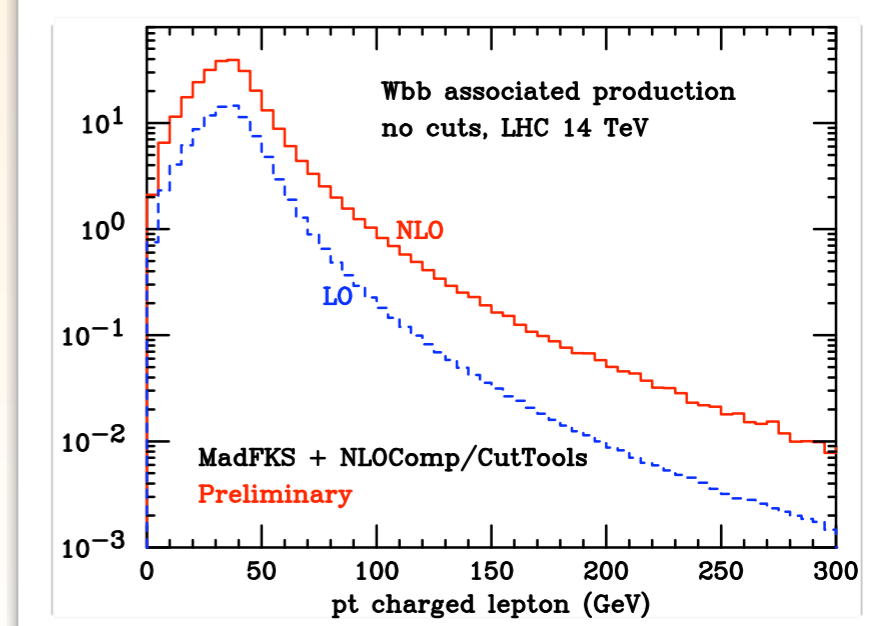
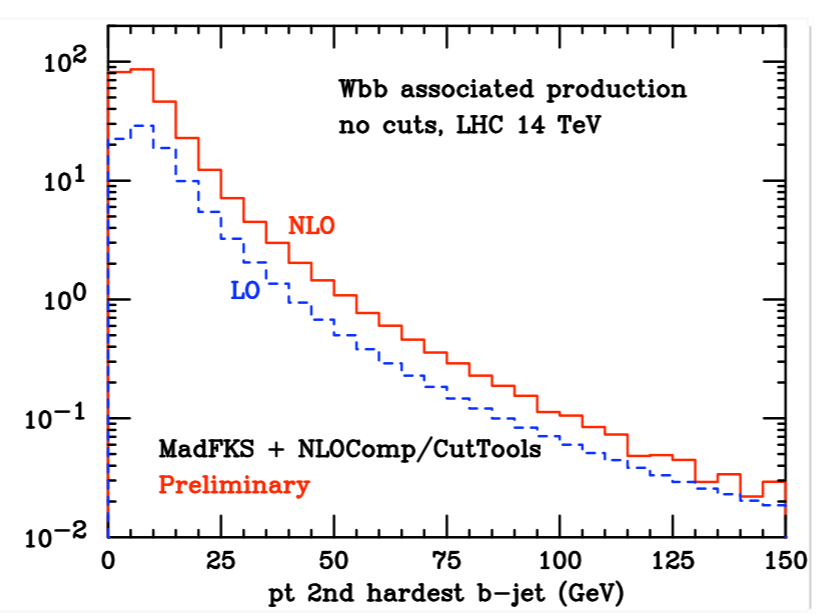
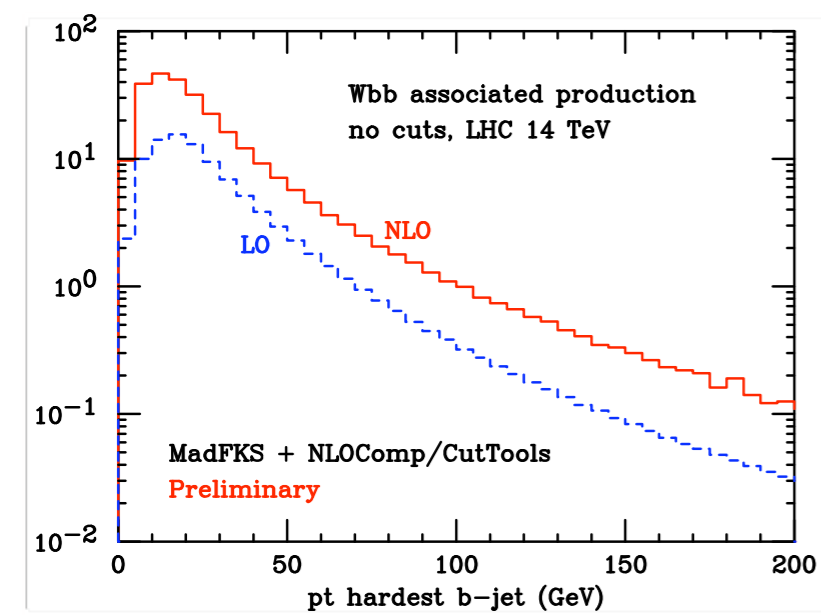
WBB RESULTS



- ☼ Transverse momentum of the hardest and 2nd hardest b-jets regulated by the b quark mass
- ☼ W boson decay included
- ☼ Unfortunately, slight disagreement between calculations when cuts are also applied to our results

work in progress

RF, Frixione, Garzelli, Hirschi, Maltoni e Pittau



MATCHING TO A PARTON SHOWER

In collaboration with Stefano Frixione e Paolo Torrielli

AUTOMATION OF MC@NLO

$$d\sigma_{\text{MC@NLO}}^{(\text{H})} = d\phi_{n+1} \left(\mathcal{M}^{(r)}(\phi_{n+1}) - \mathcal{M}^{(\text{MC})}(\phi_{n+1}) \right)$$

$$d\sigma_{\text{MC@NLO}}^{(\text{S})} = \int_{+1} d\phi_{n+1} \left(\mathcal{M}^{(b+v+rem)}(\phi_n) - \mathcal{M}^{(c.t.)}(\phi_{n+1}) + \mathcal{M}^{(\text{MC})}(\phi_{n+1}) \right)$$

✱ In black: pure NLO, fully tested in MadFKS

✱ In red: already implemented for Herwig 6;

Pythia and Herwig++ are work in progress

✱ FKS is based on a collinear picture, so are the MC counter terms: branching structure is for free

✱ Automatic determination of color partners

✱ Automatic computation of leading-color matrix elements

✱ Works also when MC-ing over helicities

MADFKS MATCHED TO PARTON SHOWER

- ✿ In MadFKS many process fully tested and working
(*e.g. e^+e^- to jets, Drell-Yan, top pair production, ...*)

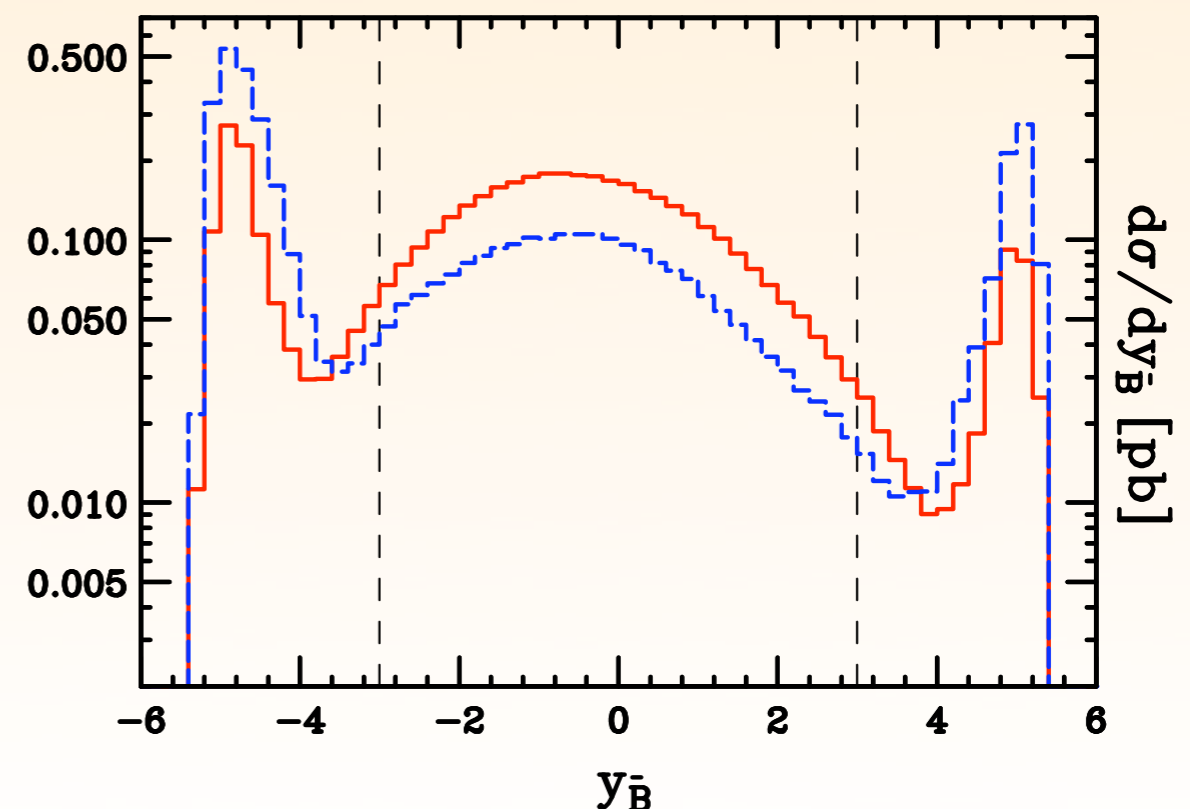
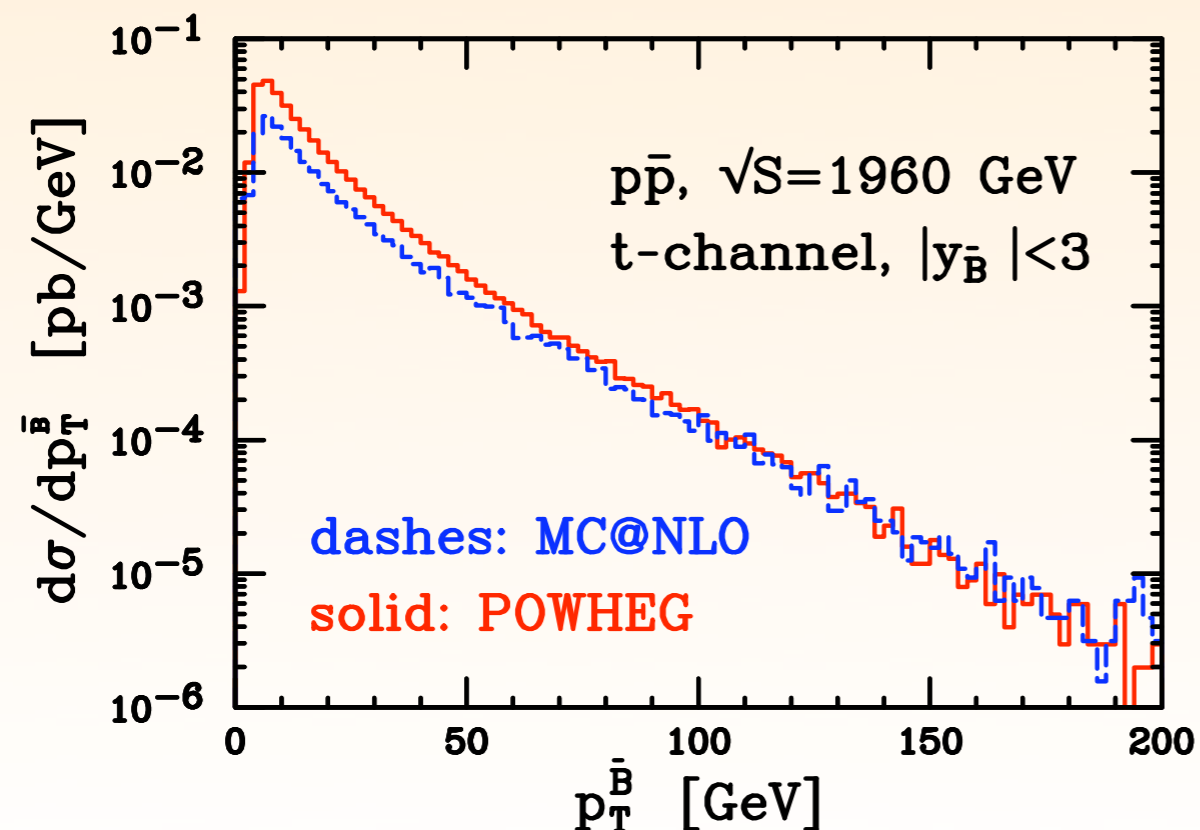
- ✿ New result: t-channel single top production

T-CHANNEL SINGLE TOP

- ☼ Already implemented in MC@NLO and POWHEG

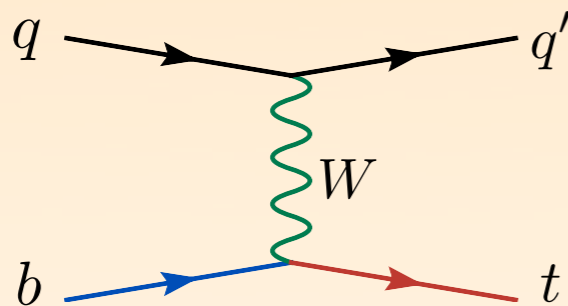
*Frixione, Laenen, Motylinski & Webber (2006);
Alioli, Nason, Oleari & Re (2009)*

- ☼ However, due to the massless initial state b quark in the fixed order calculation, some strange behavior at low p_T and for forward B hadrons

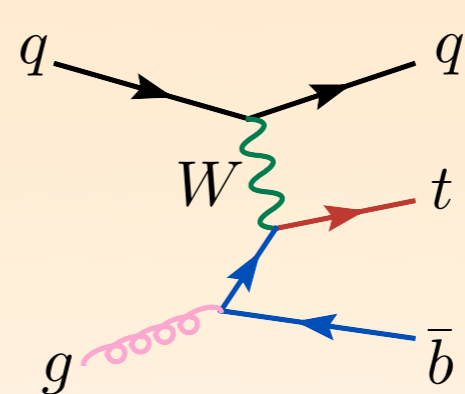


INITIAL STATE B QUARK

- ☼ “Standard” way of looking at this process



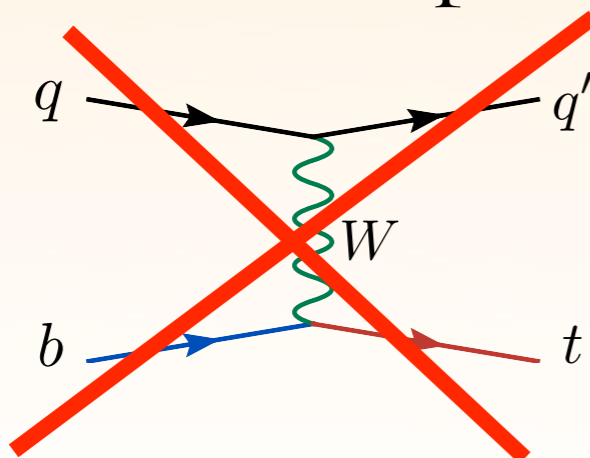
leading order



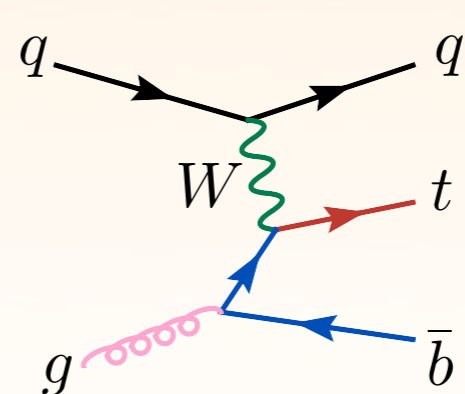
(contribution to) NLO

5-flavor
scheme

- ☼ But there is an equivalent description with no bottom PDF and an explicit gluon splitting to b quark pairs



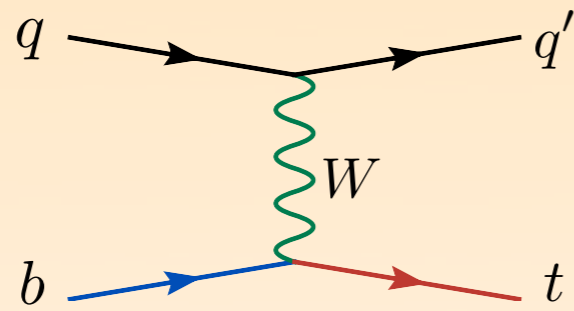
Does not exist



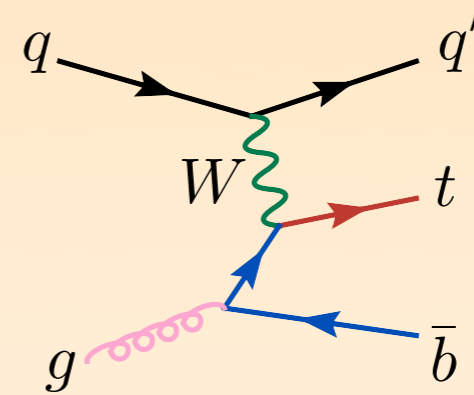
(part of) leading order

4-flavor
scheme

THE TWO SCHEMES



5-flavor scheme: “2 → 2”



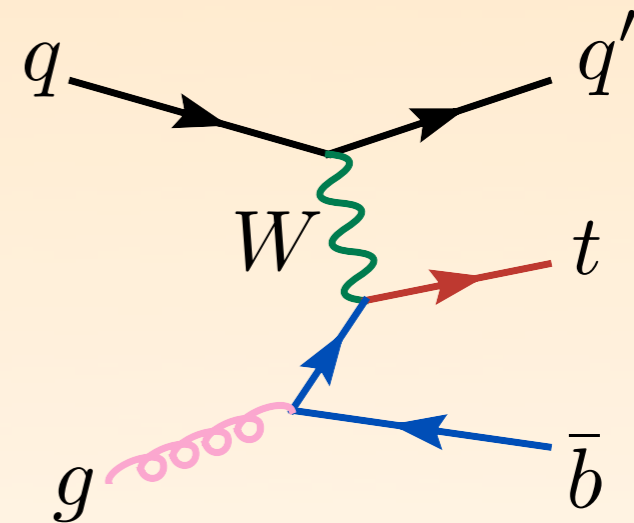
4-flavor scheme: “2 → 3”

- ✿ At all orders both description should agree; otherwise, differ by:
 - ✿ evolution of logarithms in PDF: they are resummed
 - ✿ available phase space
 - ✿ approximation by large logarithm

FOUR-FLAVOR SCHEME

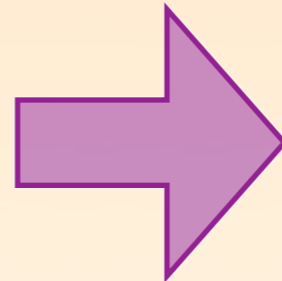
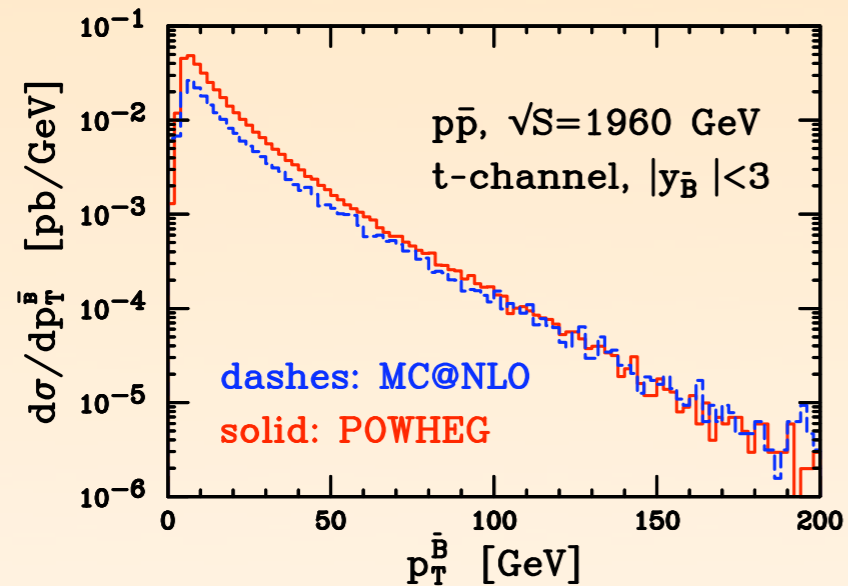
Campbell, RF, Maltoni, Tramontano (2009)

- ✱ Use the 4-flavor ($2 \rightarrow 3$) process as the Born and calculate NLO
- ✱ Much harder calculation due to extra mass and extra parton
- ✱ Spectator b for the first time at NLO
- ✱ Process implemented in the MCFM-v5.7 parton-level NLO code
 - ✱ Starting point for future NLO+PS beginning at ($2 \rightarrow 3$)

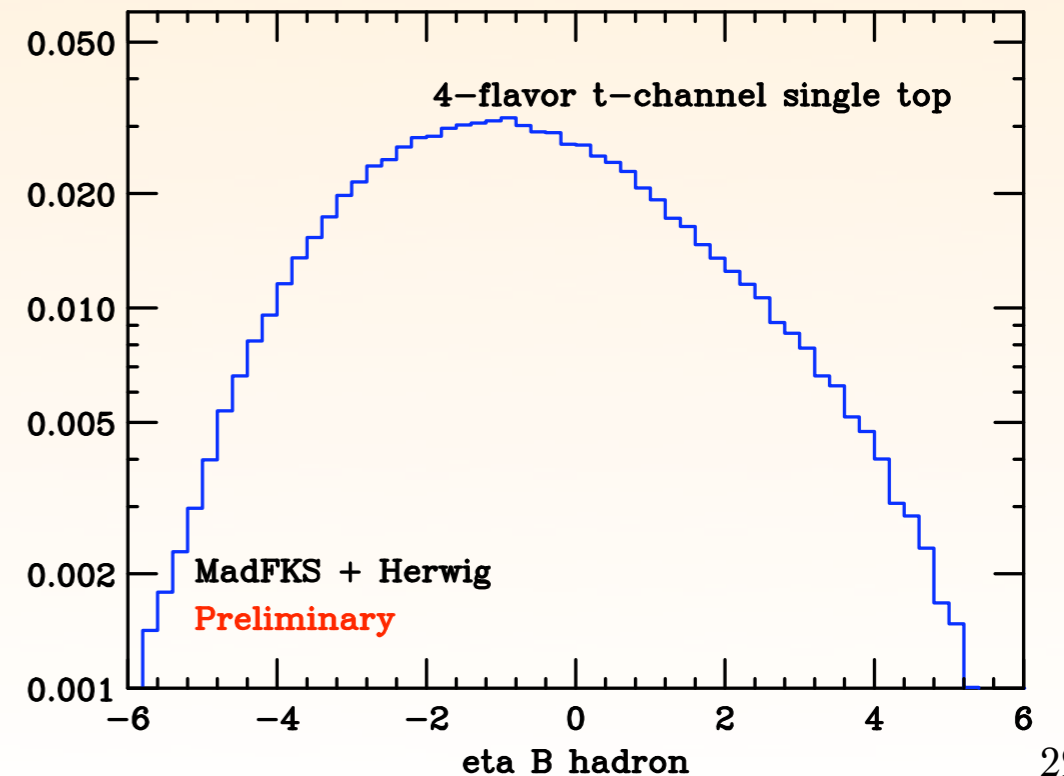
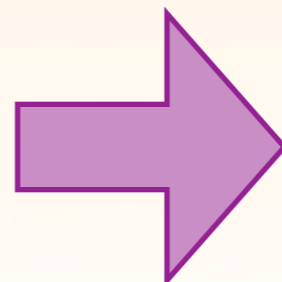
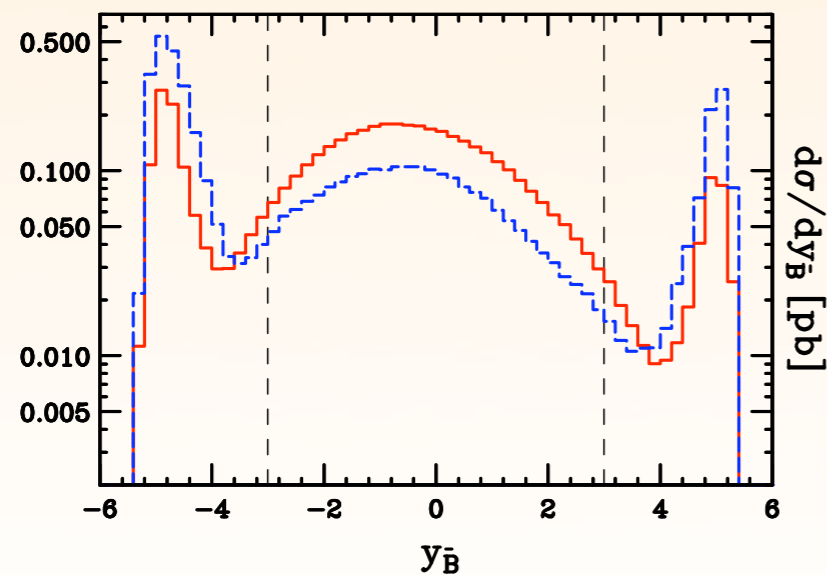
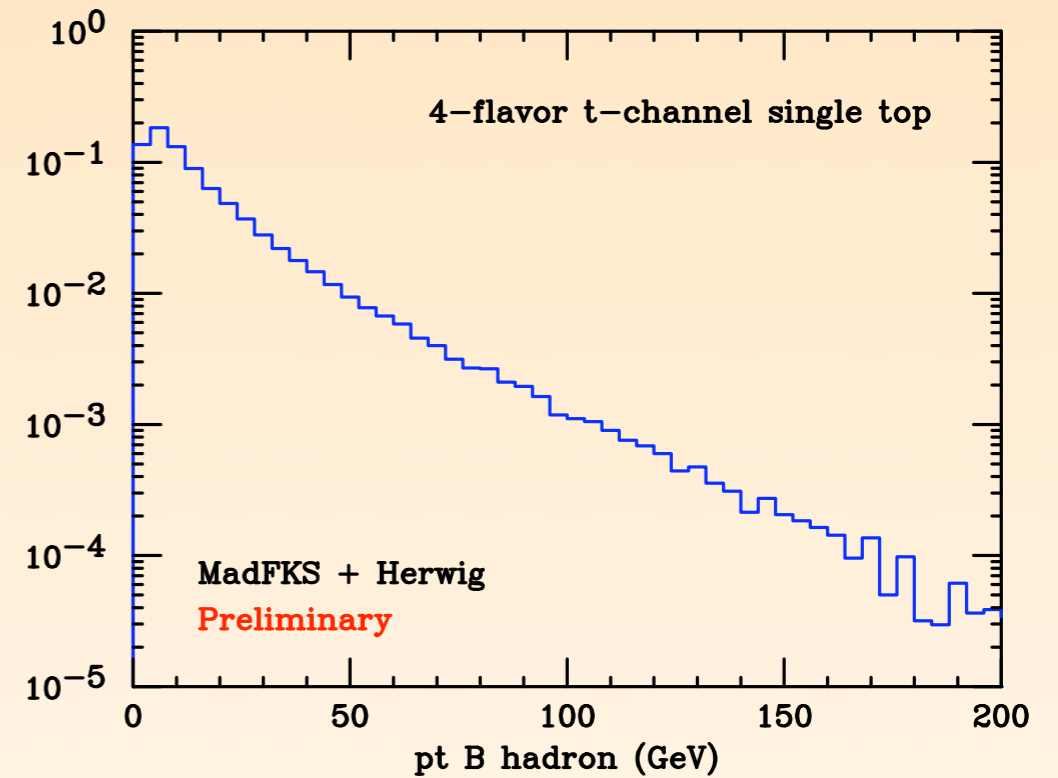


NLO 4 FLAVOR + SHOWER

5-flavor scheme

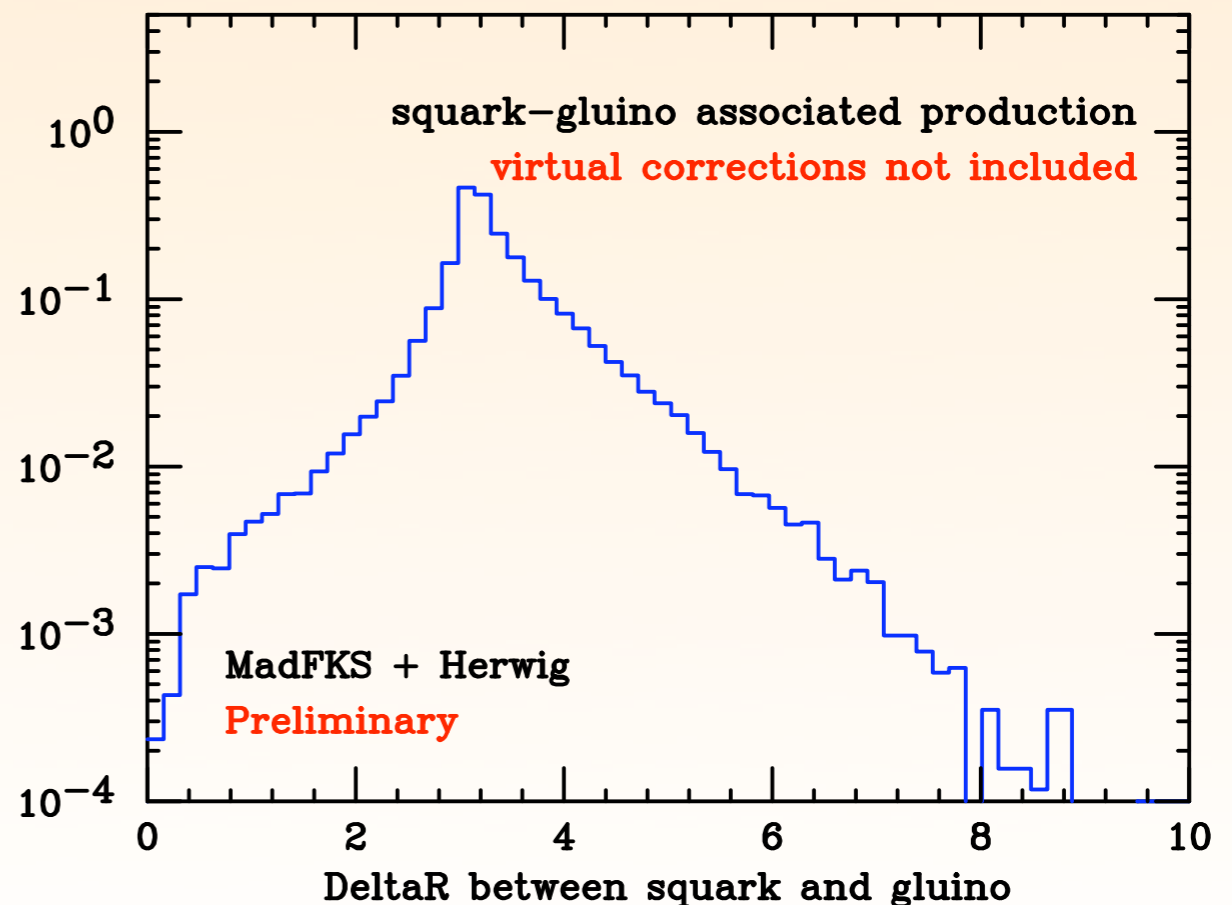
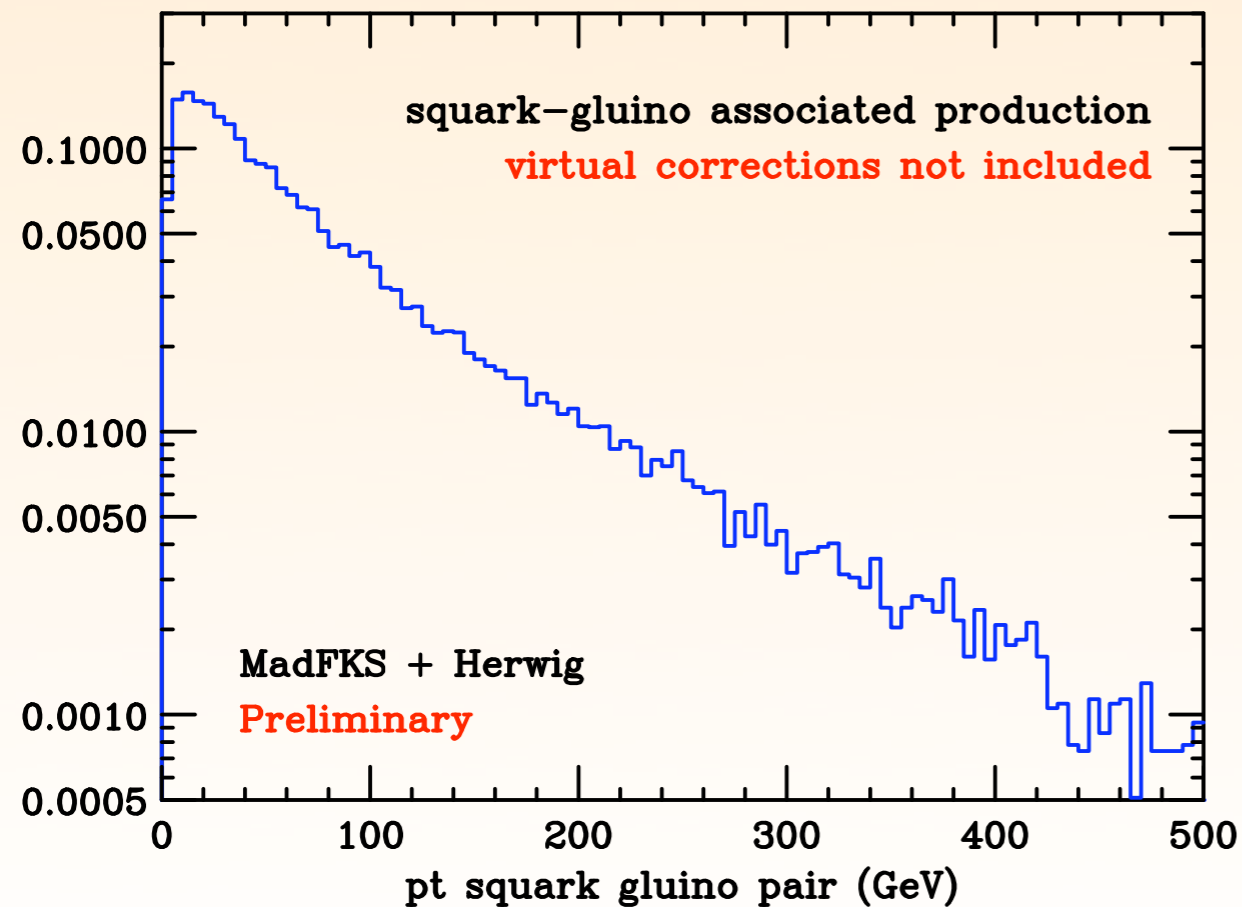
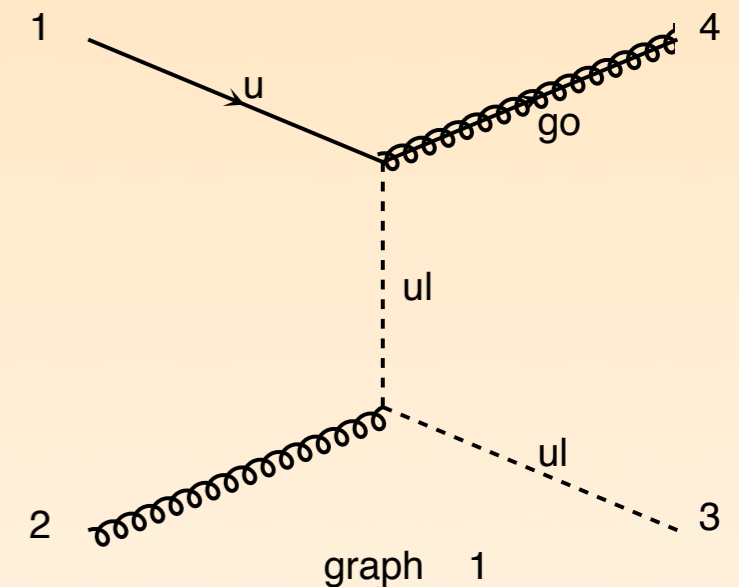


4-flavor scheme



ALSO BSM

- ☼ squark-gluino associated production
- ☼ real emission corrections included, but virtual correction not (yet)



TO CONCLUDE

- ✿ For any QCD NLO computation (SM & BSM) MadFKS takes care of:
 - ✿ Generating the Born, real emission, subtraction terms, phase-space integration and overall management of symmetry factors, subprocess combination etc.
- ✿ Using NLOComp+CutTools and virtual corrections are being automated
- ✿ With the shower subtraction terms, interface to showers to generate automatically unweighted events with NLO precision is working with Herwig and work in progress with Pythia and Herwig++
- ✿ First physics results at NLO are being produced within the MadGraph/MadEvent framework using the MadFKS code