

Electroweak corrections to W/Z+jet production at the LHC

Alexander Mück

in collaboration with

A. Denner (PSI), S. Dittmaier (Freiburg),
T. Kasprzik (Karlsruhe)

HP².3rd

Florence, 14th September 2010

- **W/Z production** at the LHC

- **W/Z+jet** production:

$$pp \rightarrow W/Z + \text{jet} \rightarrow l\nu_l/ll + \text{jet}$$

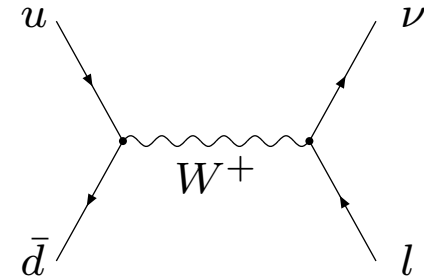
- **motivation** and theoretical **status**
- **Electroweak** and QCD **corrections**
- Numerical **results** for the LHC
- **Conclusions**

W/Z Production at the LHC

Charged-current Drell-Yan:

$$pp \rightarrow W^\pm \rightarrow l^\pm \nu_l$$

- clean signal: **lepton + missing p_T**
- huge cross section: $\sigma_{W^+ \rightarrow \mu^+ \nu_\mu} = 3 \text{ nb}$ (Atlas cuts at 7 TeV)
 \Rightarrow 2 events per minute at LHC right now

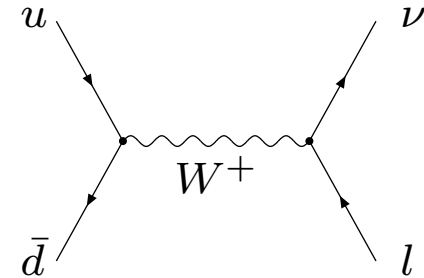


W/Z Production at the LHC

Charged-current Drell-Yan:

$$pp \rightarrow W^\pm \rightarrow l^\pm \nu_l$$

- clean signal: **lepton + missing** p_T
- huge cross section: $\sigma_{W^+ \rightarrow \mu^+ \nu_\mu} = 3 \text{ nb}$ (Atlas cuts at 7 TeV)
- very **useful**: M_W , Γ_W , luminosity, PDFs, calibration

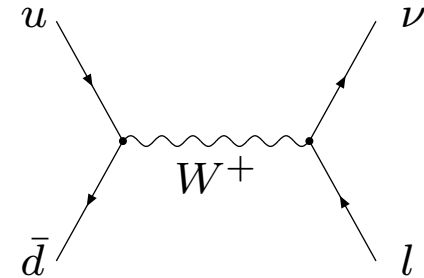


W/Z Production at the LHC

Charged-current Drell-Yan:

$$pp \rightarrow W^\pm \rightarrow l^\pm \nu_l$$

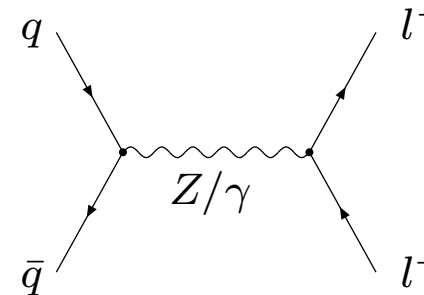
- clean signal: **lepton + missing** p_T
- huge cross section: $\sigma_{W^+ \rightarrow \mu^+ \nu_\mu} = 3 \text{ nb}$ (Atlas cuts at 7 TeV)
- very **useful**: M_W , Γ_W , luminosity, PDFs, calibration



Neutral-current Drell-Yan:

$$pp \rightarrow Z/\gamma \rightarrow l^+ l^-$$

- clean signal: **charged lepton pair**
- huge cross section: $\sigma_{Z \rightarrow \mu^+ \mu^-} = 0.5 \text{ nb}$ (Atlas cuts at 7 TeV)
- very **useful**: calibration, luminosity, PDFs



W/Z Production at the LHC

Theory status:

- **QCD**: NNLO, resummation, parton shower matching
- **EW**: NLO, leading higher order contributions

W/Z Production at the LHC

Theory status:

- **QCD**: NNLO, resummation, parton shower matching
- **EW**: NLO, leading higher order contributions
- combined **EW and QCD** corrections?

W/Z Production at the LHC

Theory status:

- **QCD**: NNLO, resummation, parton shower matching
- **EW**: NLO, leading higher order contributions
- combined **EW and QCD** corrections?

$$d\sigma = d\sigma_{\text{MC@NLO}} + (d\sigma_{\text{EW}}^{\text{HORACE}} - d\sigma_{\text{Born}})_{\text{HERWIG-PS}} \text{ etc.}$$

Balossini et al. [arXiv:0907.0276]

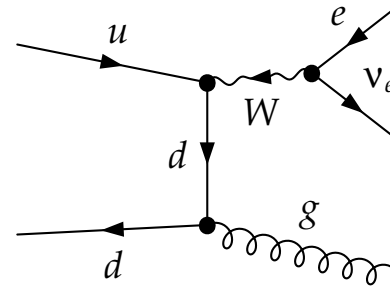
hard QCD radiation + **EW** corrections?

⇒ look at **EW** corrections for **W/Z+jet** production

W/Z+jet production

$$pp \rightarrow l\nu_l/l^+l^- + \text{jet}:$$

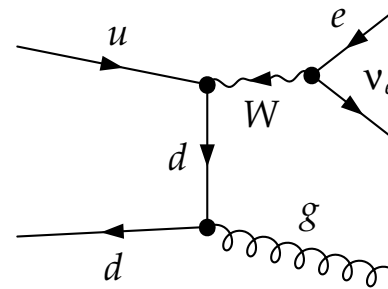
- **large** cross section
($\sim 10\%$ of inclusive sample)
- dominant SM channel for **high p_T leptons**
- precision tests for **jet dynamics**
- W+jet(s) **important background** for many searches
(high p_T lepton, missing energy, jet(s))



W/Z+jet production

$$pp \rightarrow l\nu_l/l^+l^- + \text{jet}:$$

- **large** cross section
($\sim 10\%$ of inclusive sample)
- dominant SM channel for **high p_T leptons**
- precision tests for **jet dynamics**
- W+jet(s) **important background** for many searches



Theoretical status:

- **NLO QCD** corrections known and available

DYRAD: Giele et al. [hep-ph/9302225]

MCFM: Campbell, Ellis [hep-ph/0202176]

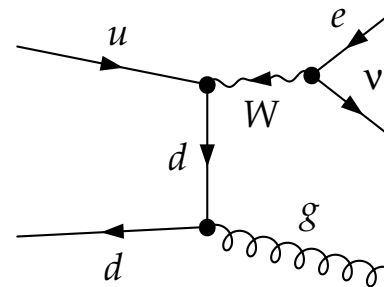
and as part of NNLO single W: Melnikov, Petriello [hep-ph/0609070]

Catani et al. [arXiv:0903.2120]

W/Z+jet production

$$pp \rightarrow l\nu_l/l^+l^- + \text{jet}:$$

- **large** cross section
($\sim 10\%$ of inclusive sample)
- dominant SM channel for **high p_T leptons**
- precision tests for **jet dynamics**
- W+jet(s) **important background** for many searches



Theoretical status:

- **NLO QCD** corrections known and available
- **EW** corrections for **stable (on-shell) W/Z bosons**

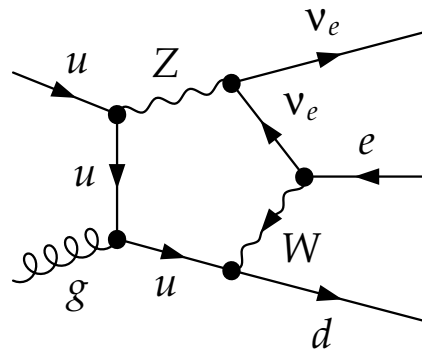
Z+jet: Kühn, Kulesza, Pozzorini, Schulze [hep-ph/0408308], [hep-ph/0507178]

W+jet: Kühn, Kulesza, Pozzorini, Schulze [hep-ph/0703283], [arXiv:0708.0476]
Hollik, Kasprzik, Kniehl [arXiv:0707.2553]

Complete EW corrections calculated

W+jet: Denner, Dittmaier, Kasprzik, AM [arXiv:0906.1656]

Z+jet: internal comparison just finished



+
 $\mathcal{O}(100)$ diagrams for W,
 $\mathcal{O}(200)$ diagrams for Z
per partonic channel

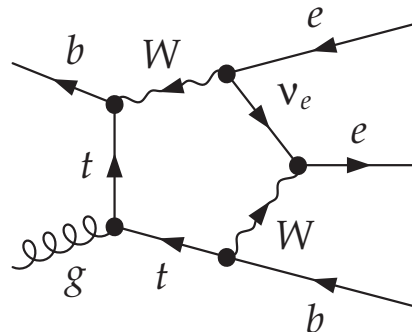
- physical final state
- all off-shell effects included
- part of the $\mathcal{O}(\alpha\alpha_s)$ corrections for incl. W production

EW corrections

Complete EW corrections calculated

W+jet: Denner, Dittmaier, Kasprzik, AM [arXiv:0906.1656]

Z+jet: internal comparison just finished



+
tops in the loop for Z
in bottom initiated
processes

- W/Z+jet very **similar** in general
- **more** partonic channels, diagrams, helicities for **Z+jet**

Complete EW corrections calculated

- **stable reduction** scheme for tensor integrals

Denner, Dittmaier [hep-ph/0509141]

- avoid inverse Gram determinants for pentagon reduction
- expand around vanishing determinants in critical phase-space regions

Complete EW corrections calculated

- **stable reduction** scheme for tensor integrals

Denner, Dittmaier [hep-ph/0509141]

- **complex mass scheme** for resonances

Denner, Dittmaier, Roth, Wieders [hep-ph/0505042]

- use complex W and Z masses everywhere by means of complex renormalization:

$$M_{V,0}^2 = \mu_V^2 + \delta\mu_V^2$$

with: $M_{V,0}^2 =$ bare mass ($V = W, Z$)

$\mu_V^2 =$ ren. complex mass

$\delta\mu_V^2 =$ complex counterterm

- \Rightarrow complex $s_W^2 = 1 - \mu_W^2/\mu_Z^2$

- loop-integrals for complex masses needed

Complete EW corrections calculated

- **stable reduction** scheme for tensor integrals

Denner, Dittmaier [hep-ph/0509141]

- **complex mass scheme** for resonances

Denner, Dittmaier, Roth, Wieders [hep-ph/0505042]

- **dipole subtraction** for infrared divergencies

Catani, Seymour [hep-ph/9605323]

Dittmaier [hep-ph/9904440]

- subtraction formalism also for **non-collinear safe** observables

e.g. for **bare muons** (without lepton–photon recombination)

⇒ muon-mass logarithms extracted analytically

Dittmaier, Kabelschacht, Kasprzik [arXiv:0802.1405]

- phase-space slicing used as a check

non collinear-safe subtract.

- usual subtraction procedure:

$$\int d\Phi_{n+1} |\mathcal{M}|^2 = \int d\Phi_{n+1} (|\mathcal{M}|^2 - |\mathcal{M}_{\text{Sub}}|^2) + \int d\Phi_n \int dk_\gamma |\mathcal{M}_{\text{Sub}}|^2$$

- clever choice of $|\mathcal{M}_{\text{Sub}}|^2$

$\Rightarrow (|\mathcal{M}|^2 - |\mathcal{M}_{\text{Sub}}|^2)$ is integrable

$\Rightarrow \int dk_\gamma |\mathcal{M}_{\text{Sub}}|^2$ can be done analytically

non collinear-safe subtract.

- usual subtraction procedure:

$$\int d\Phi_{n+1} |\mathcal{M}|^2 = \int d\Phi_{n+1} (|\mathcal{M}|^2 - |\mathcal{M}_{\text{Sub}}|^2) + \int d\Phi_n \int dk_\gamma |\mathcal{M}_{\text{Sub}}|^2$$

- $\mathcal{M}_{\text{Sub}} = \sum_f \mathcal{M}_{\text{Sub}}(p_{\text{jet}}, z_f)$ where $z_f \rightarrow p_f^0 / (p_f^0 + p_\gamma^0)$, $p_{\text{jet}} \rightarrow p_f^0 + p_\gamma^0$
for collinear events
- only cuts on p_{jet} , **no cuts on $p_f \Rightarrow$ cuts independent of z_f**
 $\Rightarrow z_f$ integration can be done analytically

non collinear-safe subtract.

- usual subtraction procedure:

$$\int d\Phi_{n+1} |\mathcal{M}|^2 = \int d\Phi_{n+1} (|\mathcal{M}|^2 - |\mathcal{M}_{\text{Sub}}|^2) + \int d\Phi_n \int dk_\gamma |\mathcal{M}_{\text{Sub}}|^2$$

- $\mathcal{M}_{\text{Sub}} = \sum_f \mathcal{M}_{\text{Sub}}(p_{\text{jet}}, z_f)$ where $z_f \rightarrow p_f^0 / (p_f^0 + p_\gamma^0)$, $p_{\text{jet}} \rightarrow p_f^0 + p_\gamma^0$
for collinear events
- only cuts on p_{jet} , **no cuts on $p_f \Rightarrow$ cuts independent of z_f**
 $\Rightarrow z_f$ integration can be done analytically

- **non-collinear safe** implementation:

- no recombination: **cuts on p_f** allowed
- cut on z_f in \mathcal{M}_{Sub} to ensure cancellation of singularities
- **integrate over z_f in dk_γ numerically**

(soft divergence treated via Plus-distribution
in analogy to treatment of initial-state emitters/spectators)

photon–jet recombination

Treat **photon** like another **parton**?

photon–jet recombination

Treat **photon** like another **parton**?

- Yes: Photon–jet **recombination** mandatory for infrared safe observables (poles in $q \rightarrow q\gamma$ splitting)

photon–jet recombination

Treat **photon** like another **parton**?

- Yes: Photon–jet **recombination** mandatory for infrared safe observables (poles in $q \rightarrow q\gamma$ splitting)
- No: a **gluon** in a gluon-photon jet can become **soft** (in accidentally collinear configurations) \Rightarrow **IR singularity**

photon–jet recombination

Treat **photon** like another **parton**?

- Yes: Photon–jet **recombination** mandatory for infrared safe observables (poles in $q \rightarrow q\gamma$ splitting)
- No: a **gluon** in a gluon-photon jet can become **soft** (in accidentally collinear configurations) \Rightarrow **IR singularity**
- soft gluon pole cancelled by **virt. QCD corr.** to **V+photon**

photon–jet recombination

Treat **photon** like another **parton**?

- Yes: Photon–jet **recombination** mandatory for infrared safe observables (poles in $q \rightarrow q\gamma$ splitting)
- No: a **gluon** in a gluon-photon jet can become **soft** (in accidentally collinear configurations) \Rightarrow **IR singularity**
- soft gluon pole cancelled by **virt.** QCD corr. to **V+photon**

The problem: **V+jet** \Leftrightarrow **V+photon**

- do not distinguish (also calculate $V+\gamma$ and its NLO QCD corr.)
- or use a sophisticated isolation Frixione [hep-ph:9801442]
- or **cut on photon energy** fraction z_γ inside a jet

photon–jet recombination

Treat **photon** like another **parton**?

- Yes: Photon–jet **recombination** mandatory for infrared safe observables (poles in $q \rightarrow q\gamma$ splitting)
- No: a **gluon** in a gluon-photon jet can become **soft** (in accidentally collinear configurations) \Rightarrow **IR singularity**
- soft gluon pole cancelled by **virt.** QCD corr. to **V+photon**

The problem: **V+jet** \Leftrightarrow **V+photon**

- do not distinguish (also calculate $V+\gamma$ and its NLO QCD corr.)
- or use a sophisticated isolation Frixione [hep-ph:9801442]
- or **cut on photon energy** fraction z_γ inside a jet

\Rightarrow this is what we want; But: **not infrared safe**

photon–jet recombination

What does z_γ cut imply?

- sensitivity to $q \rightarrow q\gamma$ splitting
- **non-perturbative** corrections to be included

photon–jet recombination

What does z_γ cut imply?

- sensitivity to $q \rightarrow q\gamma$ splitting
- **non-perturbative** corrections to be included
- introduce **quark-to-photon fragmentation function** $D_{q \rightarrow \gamma}(z_\gamma, \mu_F)$
 - measured in hadronic Z decays at LEP ($Z \rightarrow q\bar{q} \rightarrow q\bar{q}\gamma$)
 - using ALEPH fit:

$$D_{q \rightarrow \gamma}(z_\gamma, \mu_F) = \frac{\alpha Q_q^2}{2\pi} P_{q \rightarrow \gamma}(z_\gamma) \left(\ln \frac{m_q^2}{\mu_F^2} + 2 \ln z_\gamma + 1 \right) + D_{q \rightarrow \gamma}^{\text{ALEPH}}(z_\gamma, \mu_F),$$

where

$$D_{q \rightarrow \gamma}^{\text{ALEPH}}(z_\gamma, \mu_F) = \frac{\alpha Q_q^2}{2\pi} \left(P_{q \rightarrow \gamma}(z_\gamma) \ln \frac{\mu_F^2}{(1 - z_\gamma)^2 \mu_0^2} + C \right)$$

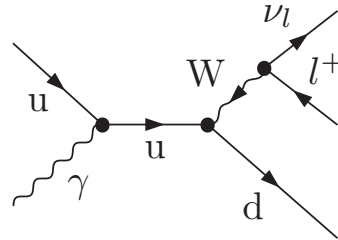
$$P_{q \rightarrow \gamma}(z_\gamma) = \frac{1 + (1 - z_\gamma)^2}{z_\gamma}$$

up to $\mathcal{O}(\alpha^3 \alpha_s)$

- also **full NLO QCD** corrections
 - **variable** (phase-space dependent) **scale** supported

up to $\mathcal{O}(\alpha^3 \alpha_s)$

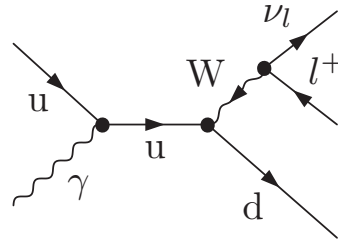
- also **full NLO QCD** corrections
 - **variable** (phase-space dependent) **scale** supported
- **photon-induced** processes



at **NLO QCD**
(phenomenologically irrelevant)

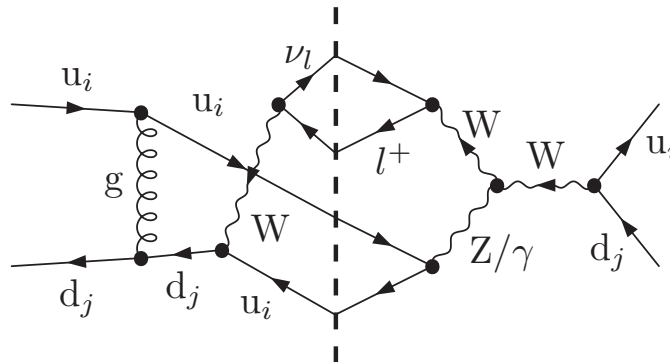
up to $\mathcal{O}(\alpha^3 \alpha_s)$

- also **full NLO QCD** corrections
 - **variable** (phase-space dependent) **scale** supported
- **photon-induced** processes



at **NLO QCD**
(phenomenologically irrelevant)

- **QCD-EW interference terms** in 4-quark processes



(phenomenologically irrelevant,
dropped for Z+jet)

Monte-Carlo programs

two completely **independent calculations**

- in mutual **agreement**

- FeynArts 1.0 [Böhm, Denner, Küblbeck]

in-house Mathematica Routines

loop integral library: DD [Dittmaier]

Vegas integration

- FeynArts 3.2, FormCalc 3.1 [Hahn]

loop integral library: Coli [Denner]

Pole [Meier, AM]

- using Weyl-van der Waerden formalism

Dittmaier [hep-ph/9805445]

- automatic generation of subtraction/slicing terms

- automatic multi-channeling using Lusifer

Dittmaier, Roth [hep-ph/0206070]

basic cuts

- $p_{T,l/\text{miss}/\text{jet}} > 25 \text{ GeV}$
- $|y_{l/\text{jet}}| < 2.5$
- lepton isolation: $R_{l,\text{jet}} > 0.5$
- photon-energy fraction inside jets: $z_\gamma < 0.7$

recombination

- do not recombine photons and muons (bare μ^+)
- photons and electrons: $R_{\gamma,l} < 0.1$ (γ rec.)
- photons and partons: $R_{\gamma,\text{jet}} < 0.5$

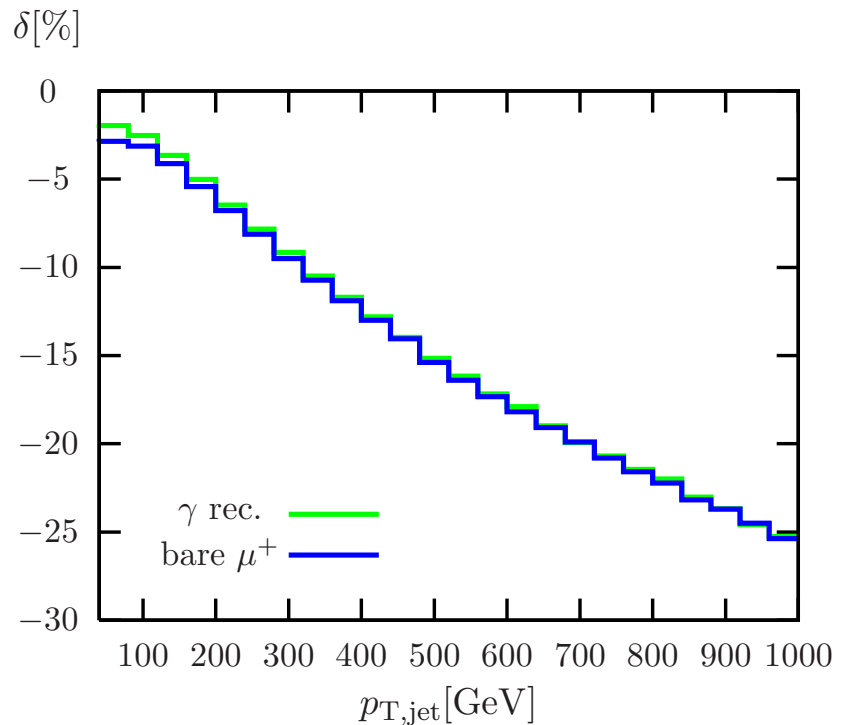
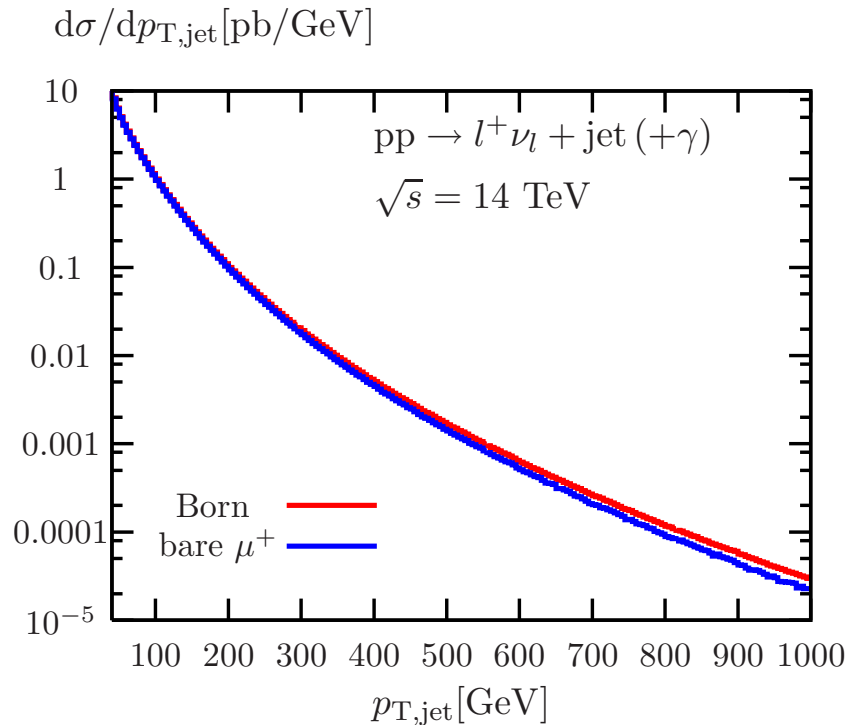
renormalization and factorization scale

- fixed scale ($\mu = M_{W/Z}$)
- variable scale: $\mu = \sqrt{M_{W/Z}^2 + p_T^{\text{had}}}$ (our default choice)

General Remarks

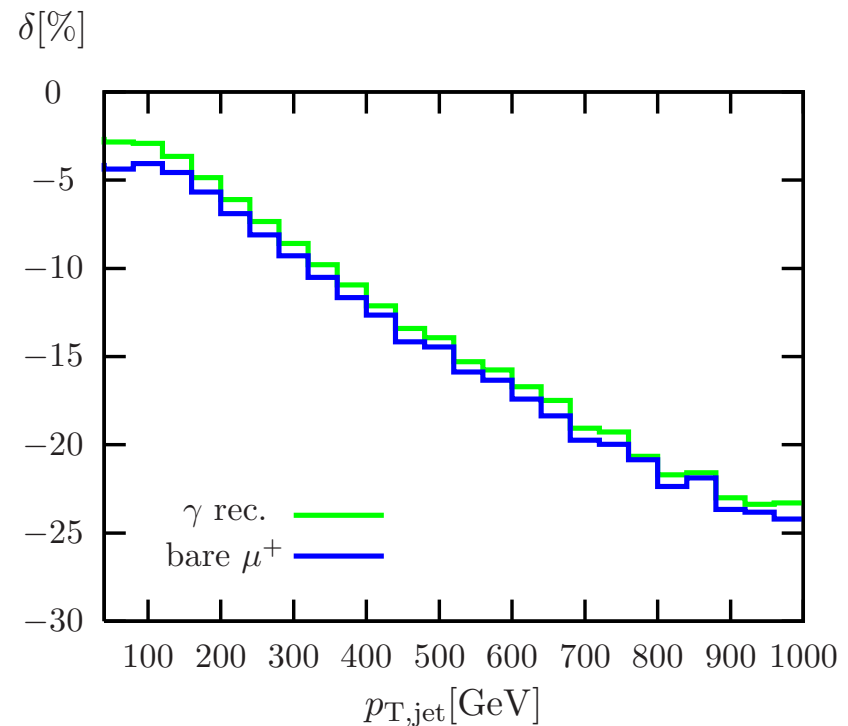
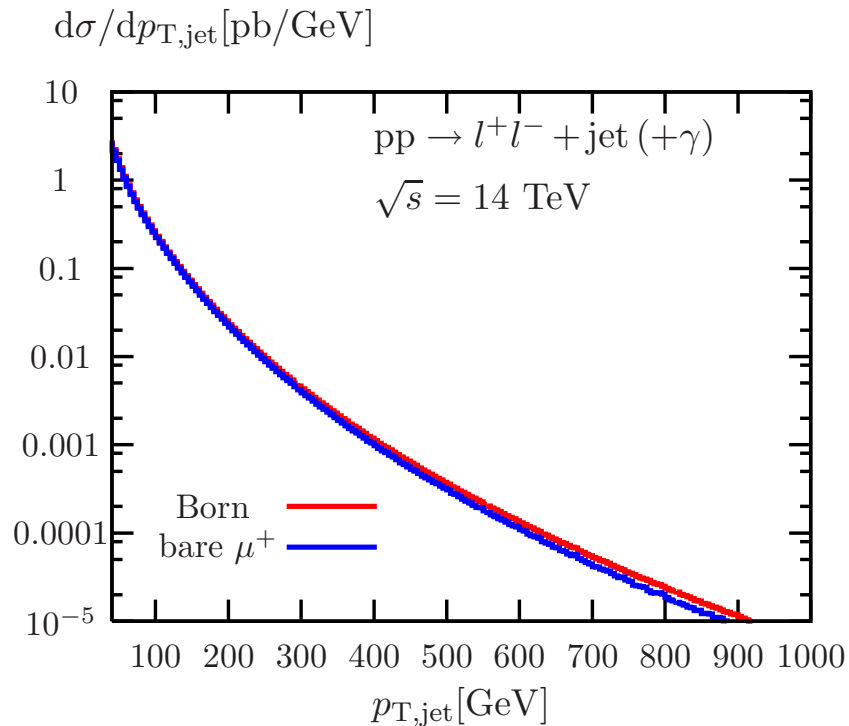
- **PDF** choice:
 - MRST2004QED \Rightarrow modern PDFs
 - almost no dependence of EW corrections on PDFs
- LHC **energy**
 - almost no dependence of EW corrections on energy
 - also Tevatron results very similar

$p_{T,jet}$ distribution for W+jet at the LHC:



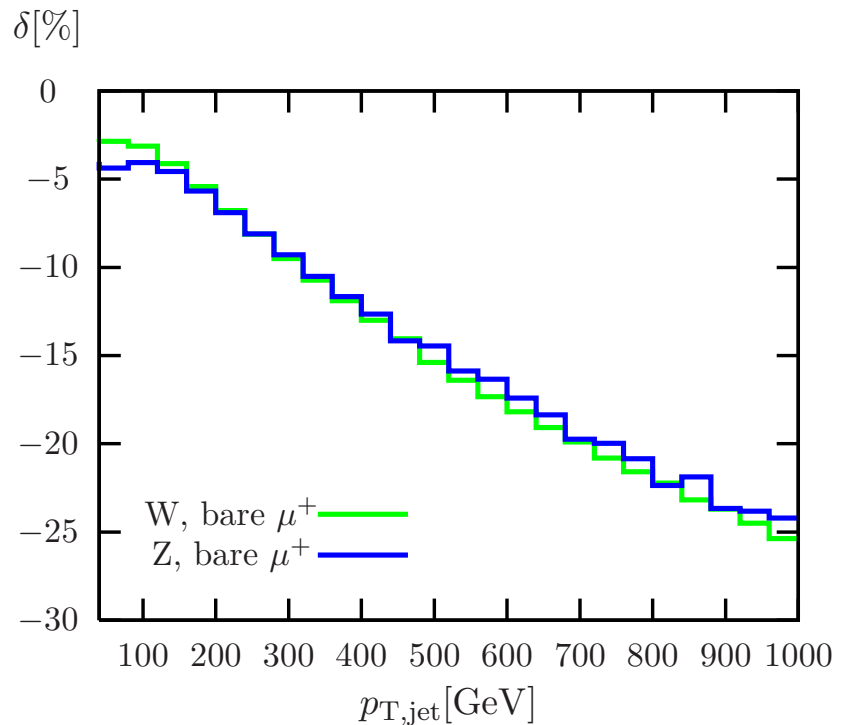
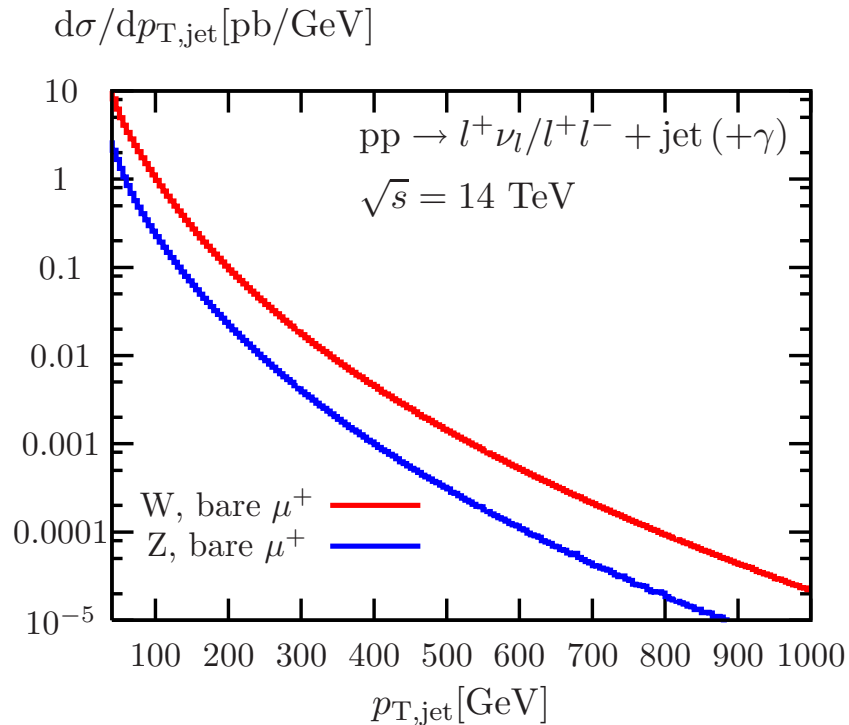
large corrections at large energies (Sudakov logs)
(on-shell W/Z good approximation)

$p_{T,\text{jet}}$ distribution for Z+jet at the LHC:



large corrections at large energies (Sudakov logs)
(on-shell W/Z good approximation)

$p_{T,\text{jet}}$ distribution for W/Z+jet at the LHC:

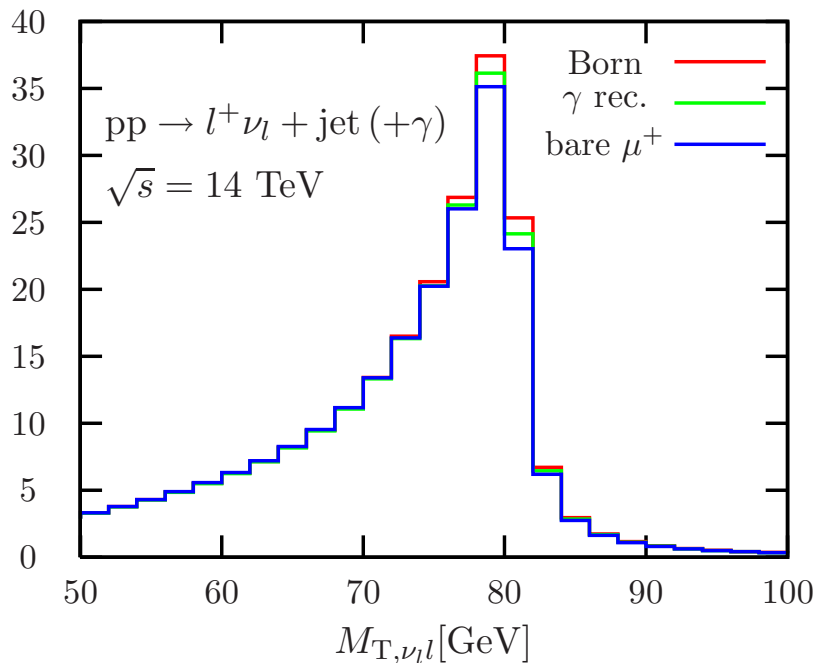


large corrections at large energies (Sudakov logs)
(on-shell W/Z good approximation)

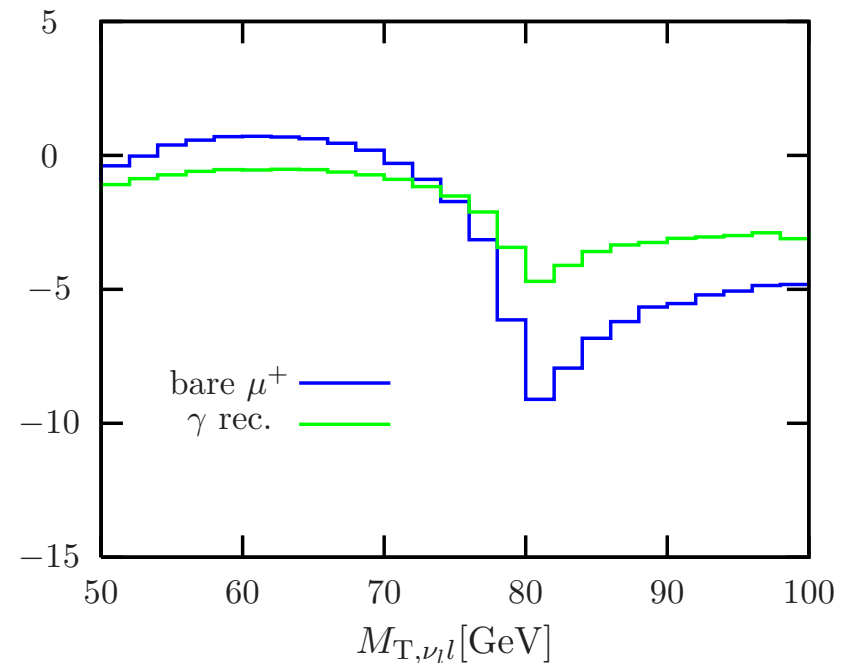
M_T distribution for W+jet at the LHC:
(similar results for the Tevatron)

$$M_{T,l\nu_l} = \sqrt{2 p_{T,l} p_T^{\text{miss}} (1 - \cos \phi_{\nu_l l})}$$

$d\sigma/dM_{T,\nu_l l} [\text{pb/GeV}]$



$\delta[\%]$

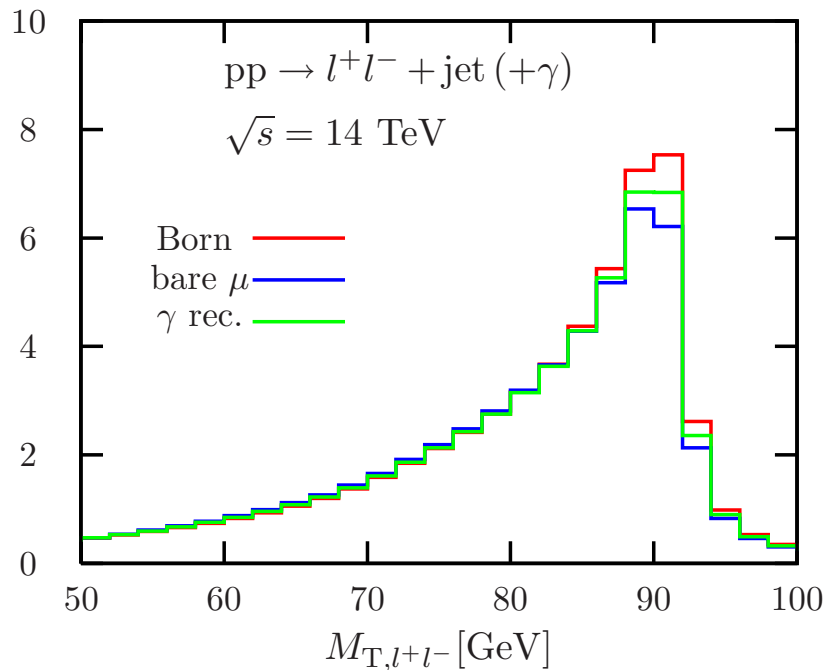


corrections dominated by (collinear) final state radiation

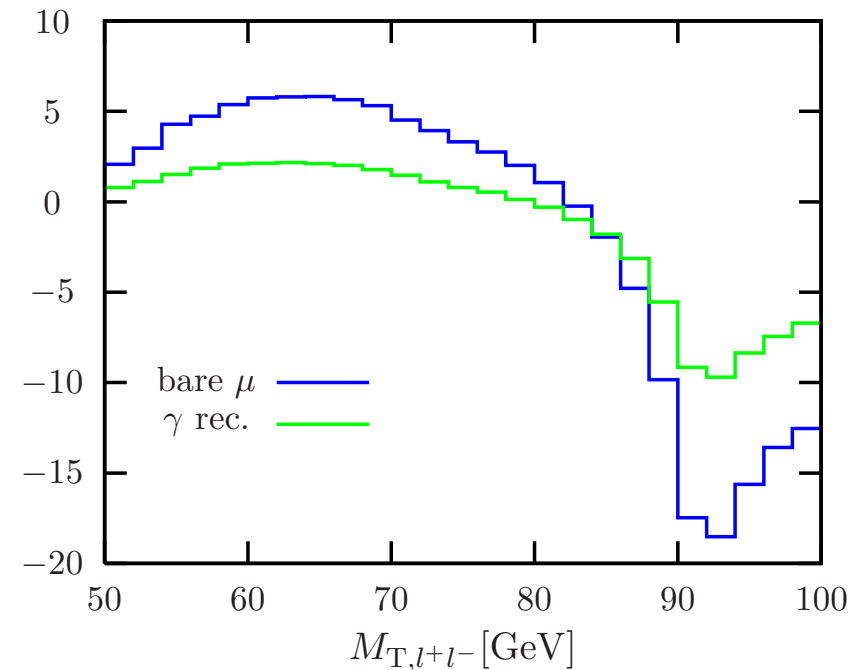
M_T distribution for Z+jet at the LHC:
(similar results for the Tevatron)

$$M_{T,l+l^-} = \sqrt{2 p_{T,l^+} p_{T,l^-} (1 - \cos \phi_{l+l^-})}$$

$d\sigma/dM_{T,l+l^-}$ [pb/GeV]



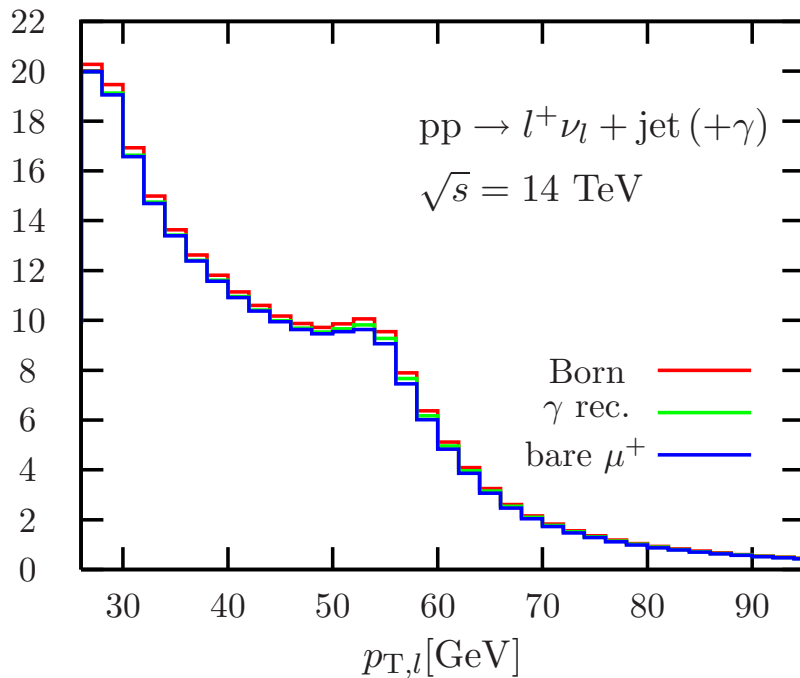
δ [%]



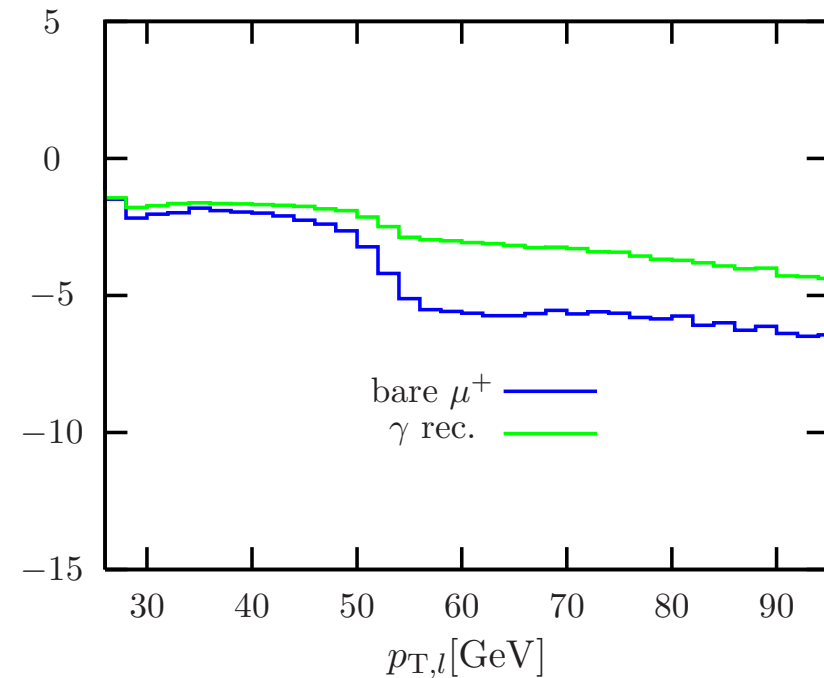
larger correction due to second charged lepton

p_T distribution for W +jet at the LHC:
(similar results for the Tevatron)

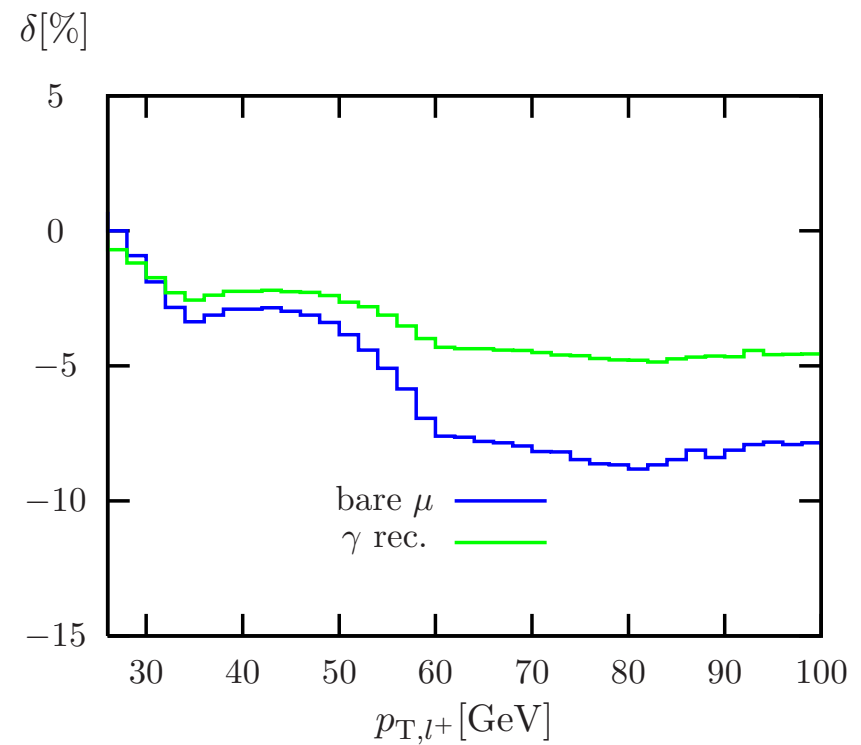
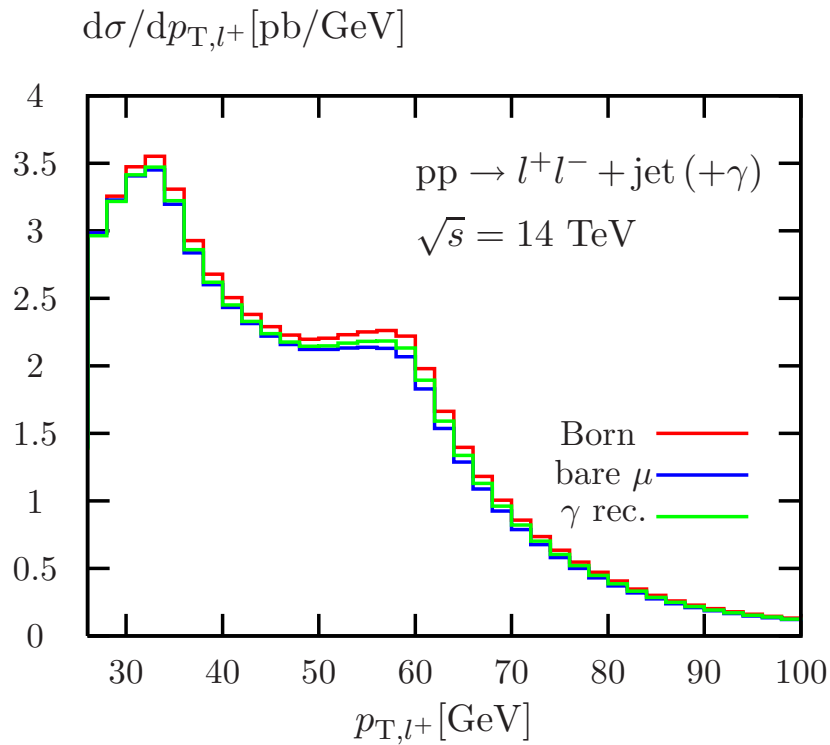
$d\sigma/dp_{T,l}[\text{pb/GeV}]$



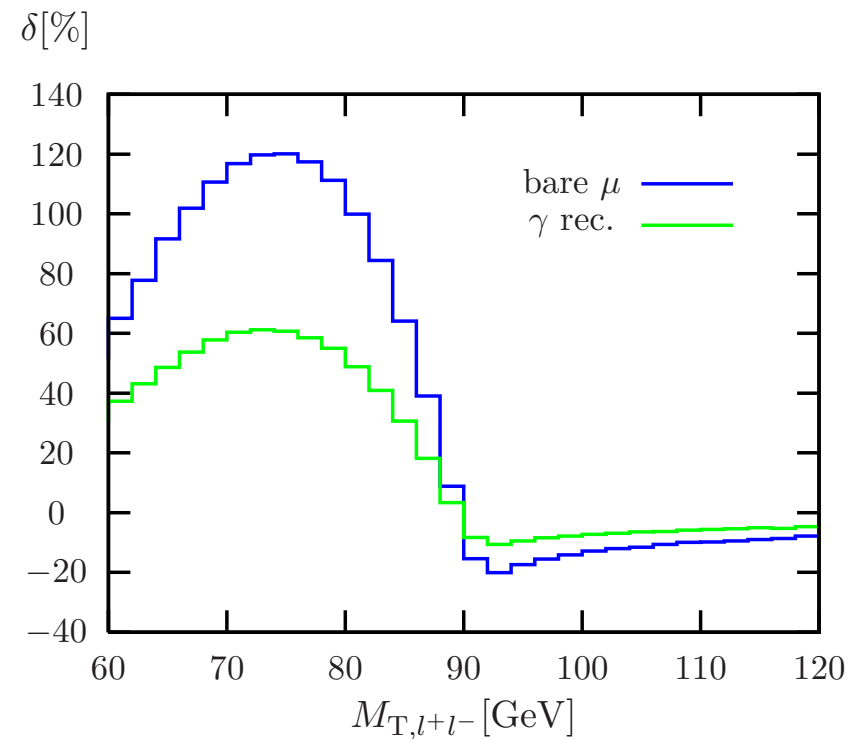
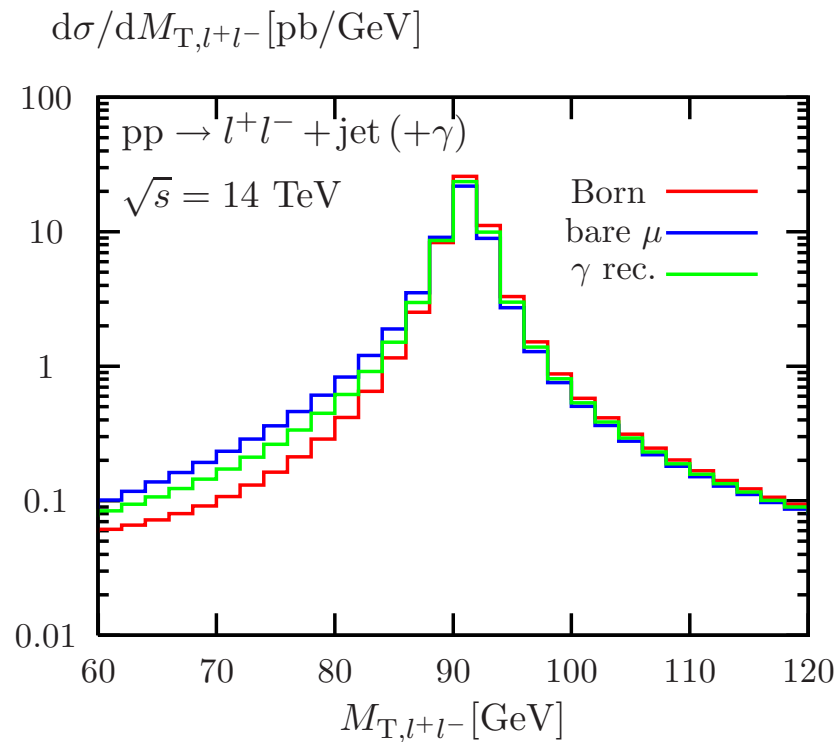
$\delta[\%]$



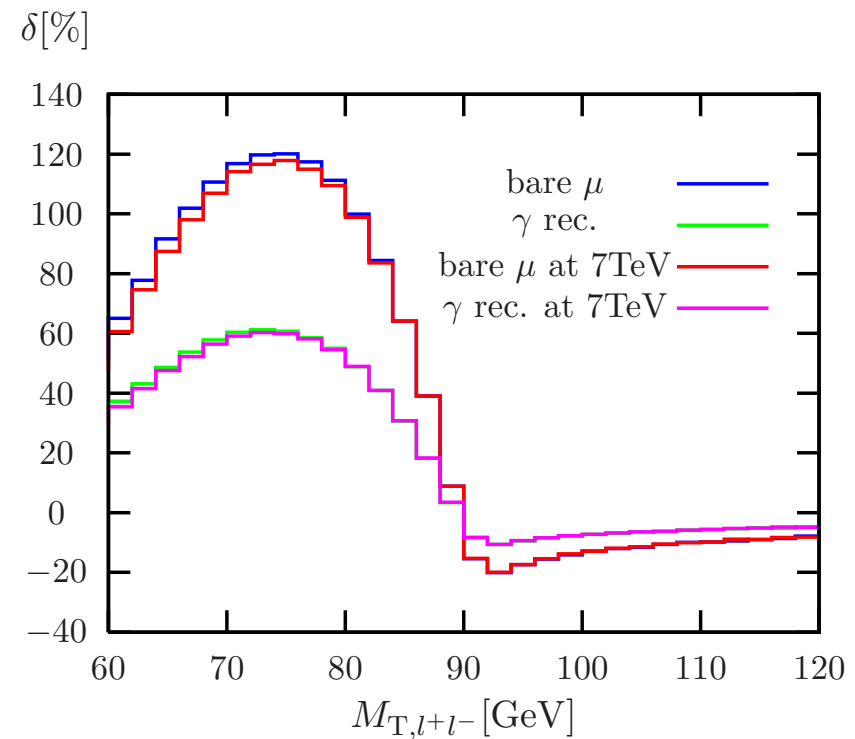
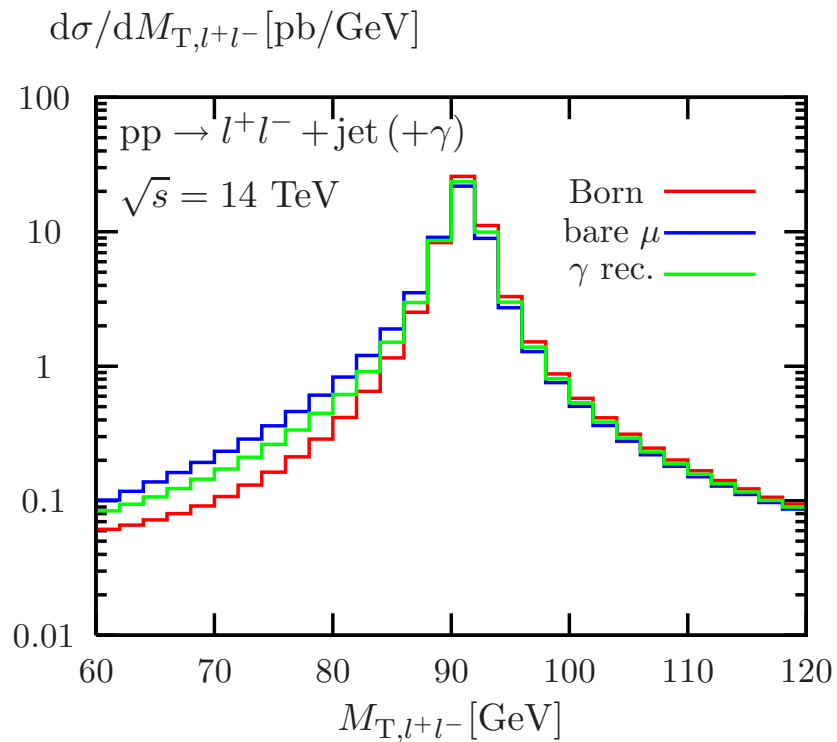
p_T distribution for Z+jet at the LHC:
(similar results for the Tevatron)



Z lineshape in Z+jet events at the LHC:

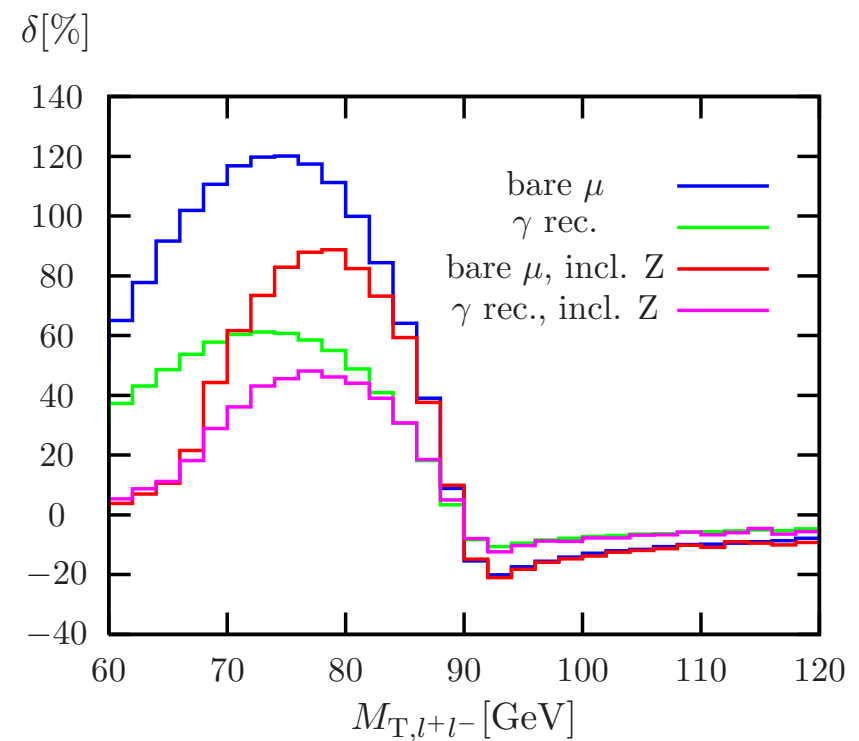
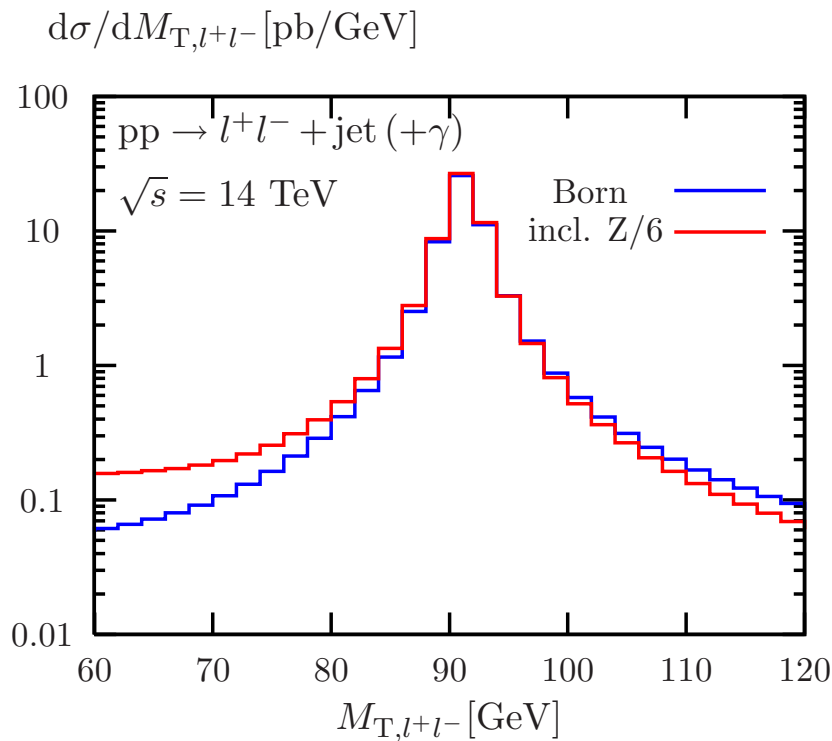


Z lineshape in Z+jet events at the LHC:



corrections hardly differ at 7 TeV

comparison with inclusive Z production:
(incl. Z production: Dittmaier, Huber [arXiv:0911.2329])



lineshape (and corrections) depends on $p_{T,Z}$ in the tails

RWTH Summary

- **W/Z+jet** are SM **benchmark** process
- our calculation
 - **flexible** Monte Carlo programs for **NLO EW+QCD**
 - **physical final state** (all off-shell effects included)
 - for single W, single Z, **W+jet**, **Z+jet**
- EW corrections
 - typically at the **percent level**
 - **larger** corrections in some **distributions**
 - **growing** with **energy** ($\sim -25\%$ at $p_{T,\text{jet}} = 1 \text{ TeV}$)
- outlook
 - more **pheno**, e.g. $W+\text{jet} \leftrightarrow Z+\text{jet}$, incl. $V \leftrightarrow V+\text{jet}$
 - $Z/W+\gamma$, $Z/W+\text{Higgs}$ production

Back-up slides

QCD corrections

$p_{T,\text{jet}}$ distribution for the LHC:

huge NLO QCD corrections:

new kinematical configuration:

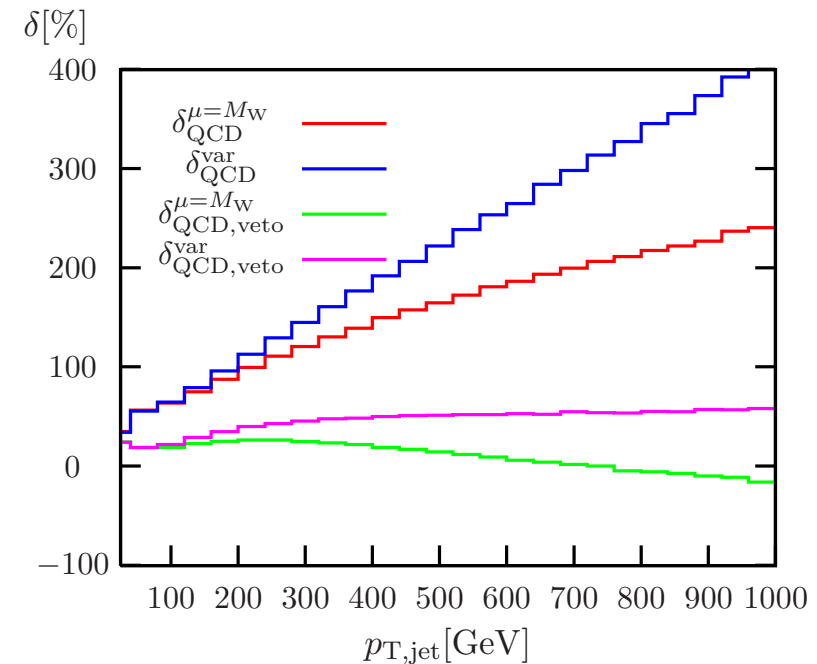
back-to-back jets balance p_T

⇒ 2 jet events with W emission

⇒ no genuine QCD correction
for W+jet

use simple jet veto:

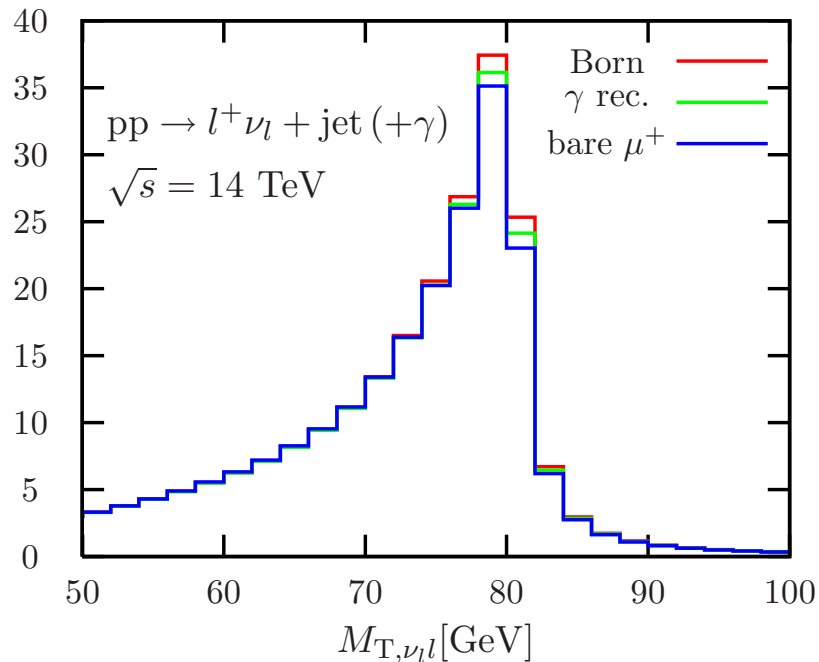
veto second jet with $p_T > \frac{1}{2} p_T^{\text{lead}}$.



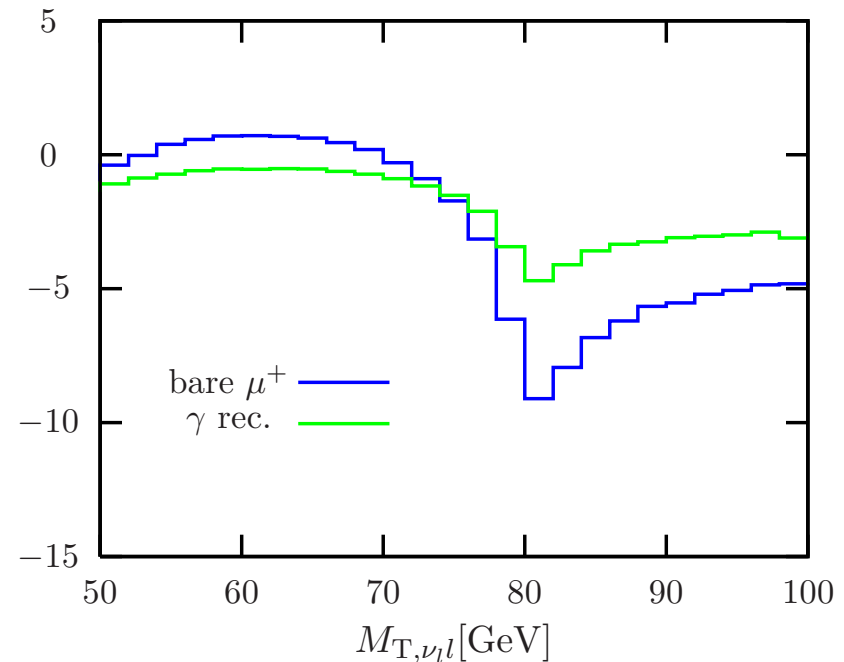
M_T distribution for the LHC:
(similar results for the Tevatron)

$$M_{T,l\nu_l} = \sqrt{2 p_{T,l} p_T^{\text{miss}} (1 - \cos \phi_{\nu_l l})}$$

$d\sigma/dM_{T,\nu_l l} [\text{pb/GeV}]$



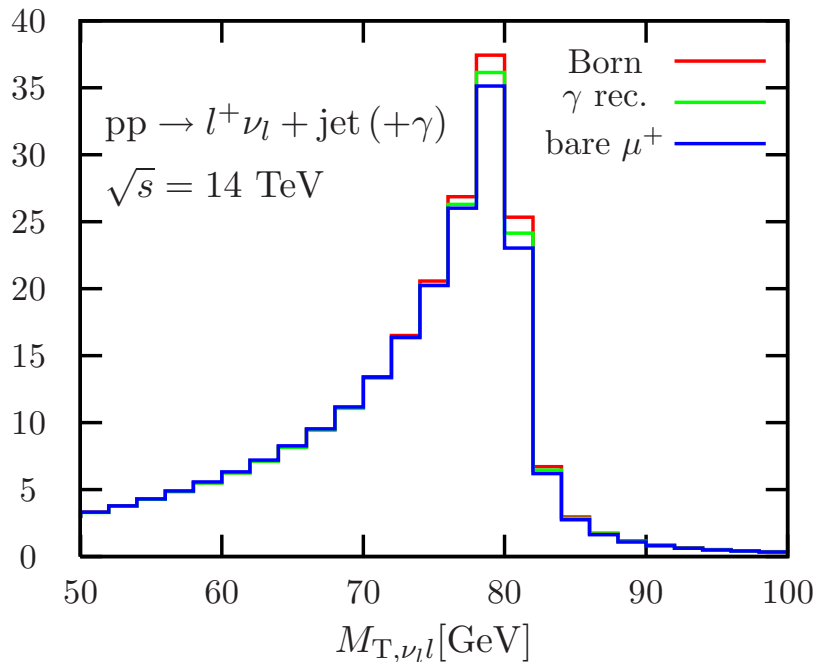
$\delta [\%]$



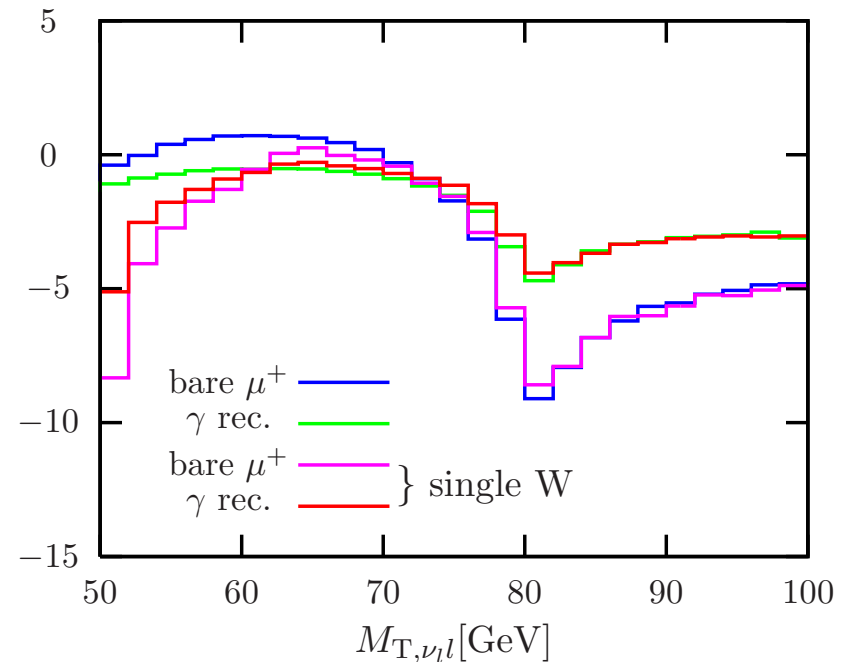
M_T distribution for the LHC:
(similar results for the Tevatron)

$$M_{T,l\nu_l} = \sqrt{2 p_{T,l} p_T^{\text{miss}} (1 - \cos \phi_{\nu_l l})}$$

$d\sigma/dM_{T,\nu_l l} [\text{pb/GeV}]$



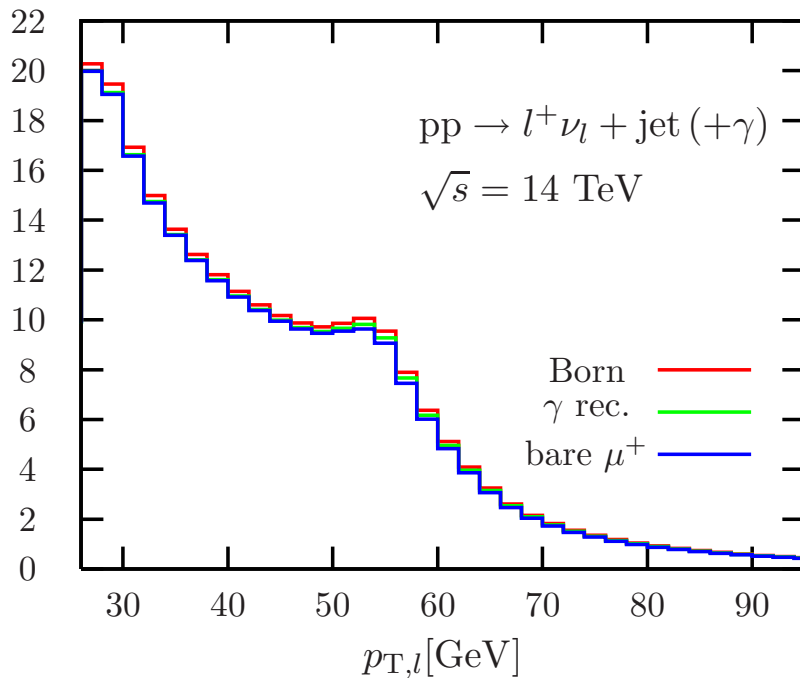
$\delta [\%]$



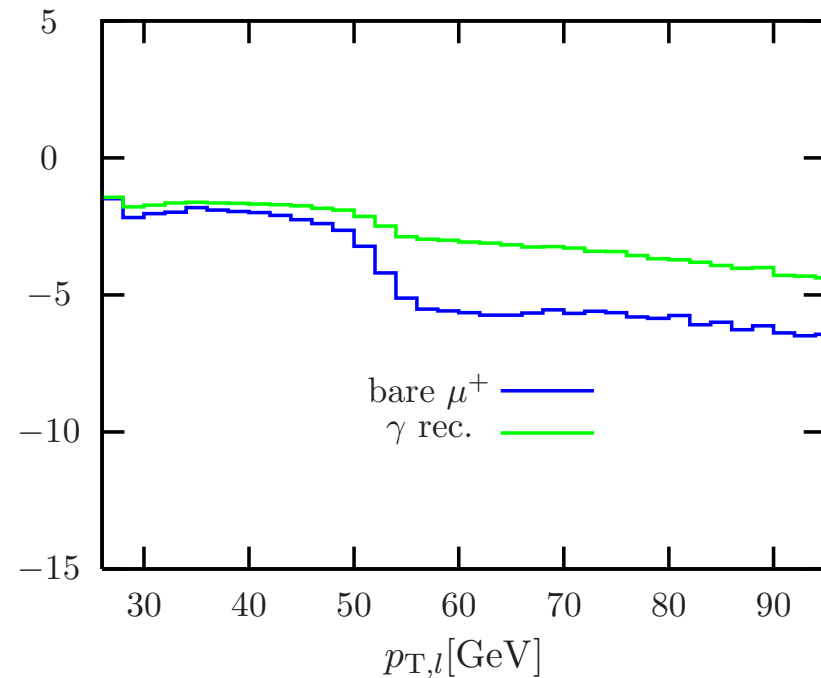
corrections very similar to single W production

p_T distribution for the LHC:
(similar results for the Tevatron)

$d\sigma/dp_{T,l}[\text{pb}/\text{GeV}]$

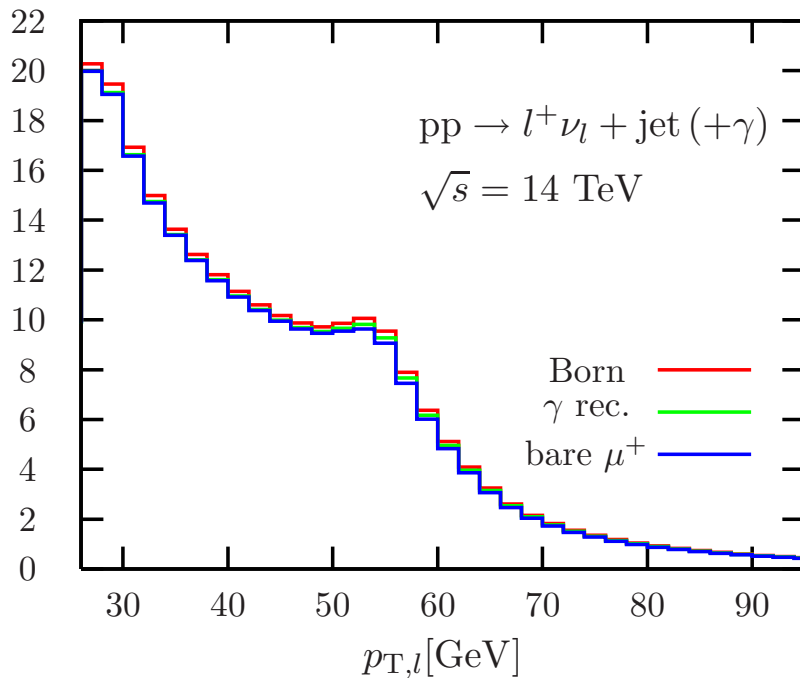


$\delta[\%]$

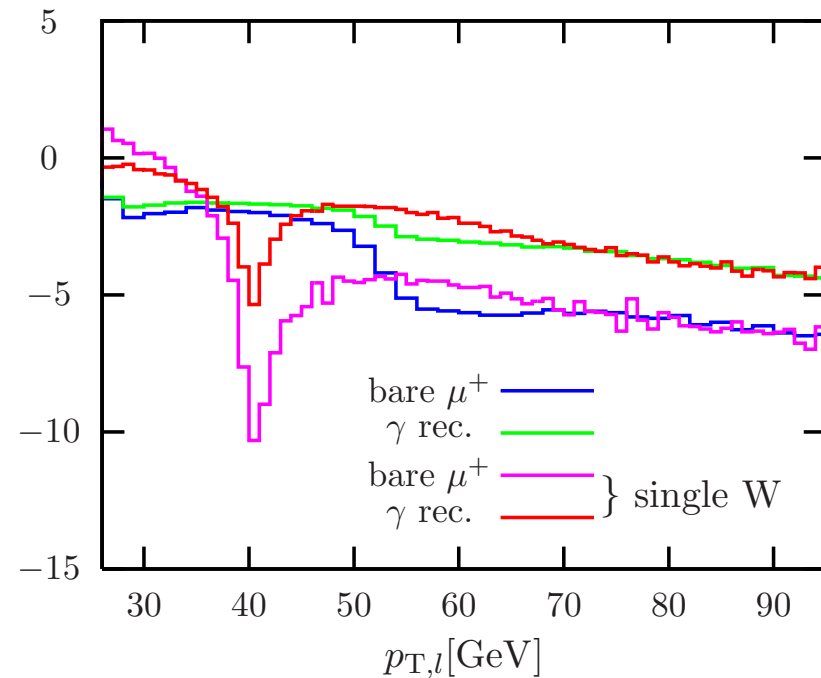


p_T distribution for the LHC:
(similar results for the Tevatron)

$d\sigma/dp_{T,l}[\text{pb/GeV}]$



$\delta[\%]$



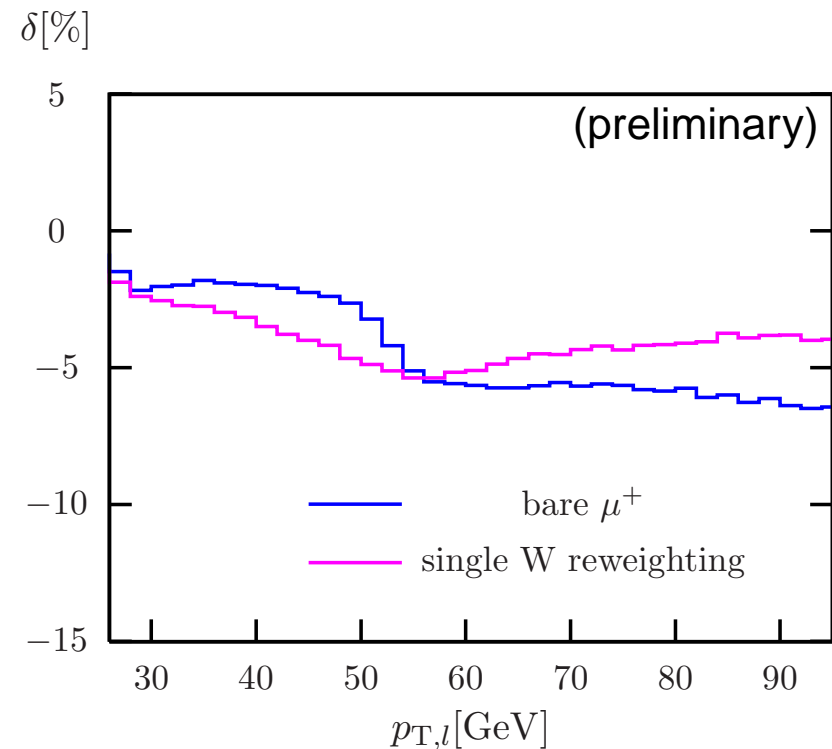
no similarity to single W production

single W vs. W+jet

p_T distribution for the LHC:

single W reweighting:

- **boost** W+jet event to W-boson **rest frame**
- **reweight** event **with EW correction for single W** in rest-frame $p_{T,l}$ bin

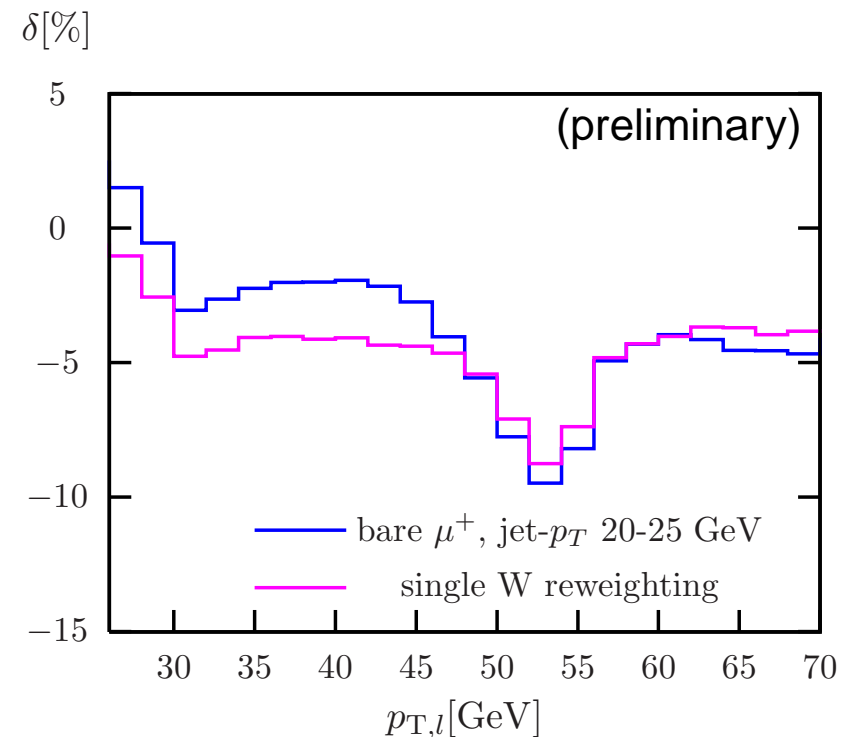


still big differences due to high- p_T jets

single W vs. W+jet

p_T distribution for the LHC:

- only look at jets with
 $p_{T,\text{jet}} = 20 - 25 \text{ GeV}$

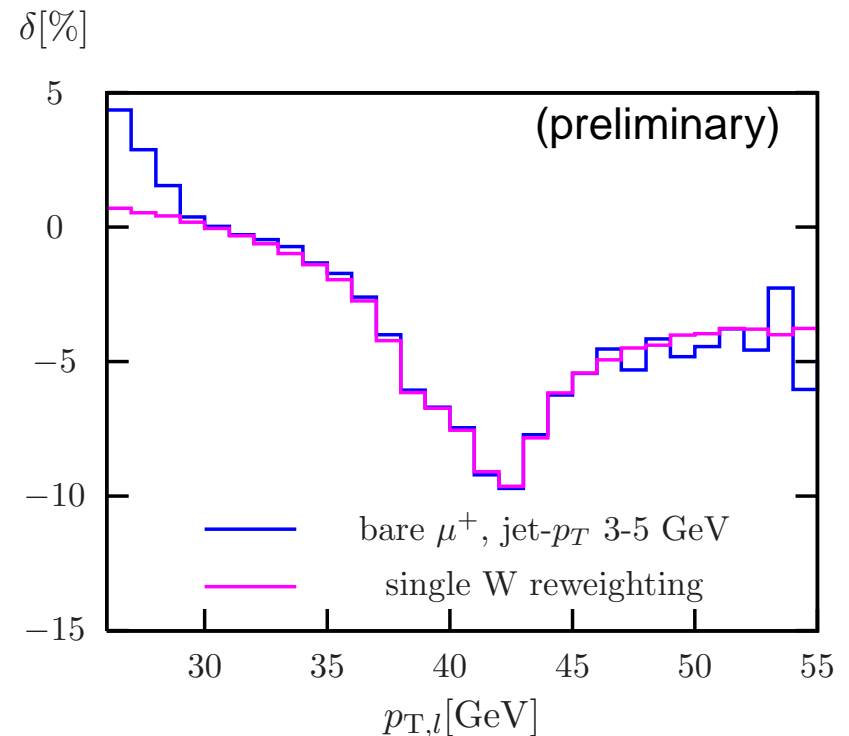


good but not perfect agreement

single W vs. W+jet

p_T distribution for the LHC:

- only look at jets with
 $p_{T,\text{jet}} = 3 - 5 \text{ GeV}$
- cross-section not reliably predicted in this region
- one can still estimate the EW corrections for the limited kinematical region



very good agreement

EW corrections: single W

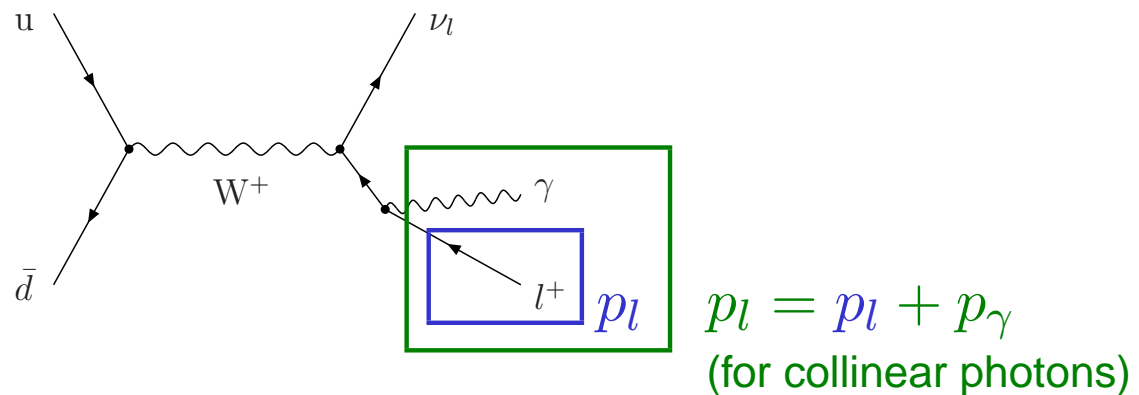
EW corrections **distort shapes**:

- in particular due to **final state photon radiation**
- also for M_T distribution
- strong dependence on lepton-photon **recombination**

EW corrections: single W

EW corrections **distort shapes**:

- in particular due to **final state photon radiation**
- also for M_T distribution
- strong dependence on lepton-photon **recombination**



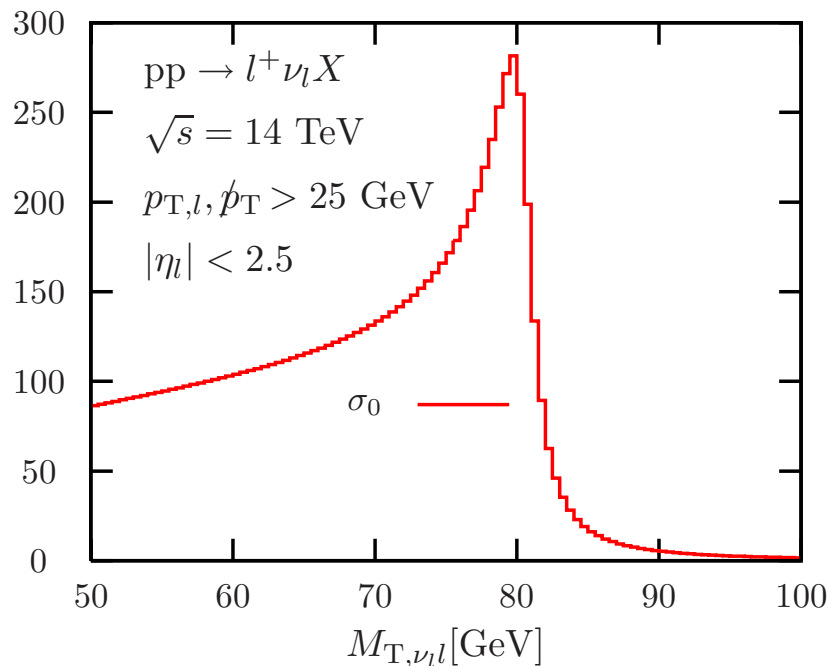
exclusive (bare) leptons (muons): $\alpha \log(M_W^2/M_l^2)$ corrections
 inclusive leptons (electrons): **no large logs** (KLN theorem)

EW corrections: single W

EW corrections **distort shapes**:

- in particular due to **final state photon radiation**
- also for M_T distribution
- strong dependence on lepton-photon **recombination**

$d\sigma/dM_{T,\nu l}[\text{pb/GeV}]$



Brensing, Dittmaier, Krämer, AM [arXiv:0710.3309]

