Gluino Pair Production at the LHC

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• Supersymmetry as a candidate for new physics

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- possible detection at the LHC



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[Harrison and Smith '83; Dawson, Eichten and Quigg '85; Haber and Kane '85]

• investigation of $\tilde{g}\tilde{g}$ - bound states [Keung and Khare '84; Kühn and Ono '84; Goldman and Haber '85]

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 [Hagiwara and Yokoya '09]
- complete NLO analysis of the differential cross section at threshold

[Kauth, Kühn, Marquard and Steinhauser '10] (in preparation)

- properties of gluinos
- interact only strong
- spin- $\frac{1}{2}$ particles
- no mixing

- adjoint $SU_C(3)$ representation
- Majorana fermions
- $-m_{\tilde{g}}>308\,{
 m GeV}\,[\,{
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• $2\Gamma_{\tilde{g}}$, level spacing $\Delta M = |E_1 - E_2|$ and annihilation width Γ_{gg} (SDECAY [Mühlleitner, Djouadi and Mambrini '05])



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◦ class A ($2\Gamma_{\tilde{g}} < \Gamma_{gg}$) $\longrightarrow \tilde{g}\tilde{g}$ bound states [Kauth, Kühn, Marquard and Steinhauser '09] ◦ class B ($\Gamma_{gg} < 2\Gamma_{\tilde{g}} < \Delta M$) and class C ($\Delta M < 2\Gamma_{\tilde{g}}$) \longrightarrow bound-state effects

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colour representation

 $8 \otimes 8 = 1_s \oplus 8_s \oplus 8_a \oplus 10_a \oplus \overline{10}_a \oplus 27_s$









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dominant processes

• modification of the QCD potential $V_C^{[Y]}$

$$V_C^{[Y]} = -\frac{4\pi\alpha_s(\mu_r)C^{[Y]}}{\vec{q}^{\,2}} \left[1 + \frac{\alpha_s(\mu_r)}{4\pi} \left(\beta_0 \ln \frac{\mu_r^2}{\vec{q}^{\,2}} + a_1 \right) \right]$$

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modification of the QCD potential $V_C^{[Y]}$

dominant processes $Y \parallel C^{[Y]}$

 $\begin{array}{c|c} Y & C^{[Y]} \\ \hline 1 & C_A \\ \hline 8 & \frac{C_A}{2} \\ \hline 10 & 0 \\ \hline 27 & -\frac{C_A}{3} \end{array}$

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• modification of the QCD potential $V_C^{[Y]}$

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Schrödinger equation

$$\left\{2m_{\tilde{g}} + \left[\frac{(-i\nabla)^2}{m_{\tilde{g}}} + V_C^{[Y]}\left(\vec{r}\right)\right] - (M + i\Gamma_{\tilde{g}})\right\}G^{[Y]}(\vec{r}; M + i\Gamma_{\tilde{g}}) = \delta^3(\vec{r})$$

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Green's function

 $\frac{1}{m_{\tilde{g}}^2}G^{[Y]}(0;M+i\Gamma_{\tilde{g}}) = G_{\text{free}} + \frac{C^{[Y]}\alpha_s(\mu_r)}{4\pi} \left[G_{\text{LO}} + \frac{\alpha_s(\mu_r)}{4\pi}G_{\text{NLO}} + \dots\right]$

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and the scale
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SPS4

 $m_{\tilde{g}} = 734.11 \,\mathrm{GeV}$ $2\Gamma_{\tilde{g}} = 3.48 \,\mathrm{GeV}$

Green's function $\frac{1}{m_{\tilde{g}}^2}G^{[Y]}(0;M+i\Gamma_{\tilde{g}}) = G_{\text{free}} + \frac{C^{[Y]}\alpha_s(\mu_r)}{4\pi} \left[G_{\text{LO}} + \frac{\alpha_s(\mu_r)}{4\pi} G_{\text{NLO}} + \ldots \right]$ $\mu_r = \mu_s \equiv \left| C^{[Y]} \right| m_{\tilde{q}} \, \alpha_s(\mu_s)$ and the scale 0.5 SPS4 $m_{\tilde{q}} = 734.11 \, \text{GeV}$ 0.4 8, NLO $2\Gamma_{\tilde{q}}=3.48\,\mathrm{GeV}$ 27. NLO m { G(0,M+i $\Gamma_{\tilde{g}}$) } / $m_{\tilde{g}}^2$ 0.3 0.2 0.1 0 1430 1440 1450 1460 1420 1470 1480 M [GeV]

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$$\begin{split} & LO \text{ result - I} \\ & = \sum_{i,j} \int_{\frac{M^2}{S}}^{1} d\tau \left[\frac{d\mathcal{L}_{ij}}{d\tau} \right] (\tau, \mu_f^2) \ M \frac{d\hat{\sigma}_{ij \to T^{[X]}}}{dM} (\hat{s}, M^2, \mu_r^2) \frac{1}{m_{\tilde{g}}^2} \mathsf{Im} \left\{ G^{[X]}(0; M + i\Gamma_{\tilde{g}}) \right\} \end{split}$$

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LO result - II



• NLO part of the Green's function from $q\overline{q}$ case

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NLO calculation - II

- conversion to dimensional reduction
 - [Martin and Vaughn '93]



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- real $2 \rightarrow 3$ corrections







$$m_{\tilde{g}} = 734.11 \,\mathrm{GeV}$$

 $\Gamma_{\tilde{g}} = 3.48 \,\mathrm{GeV}$
 $m_{\tilde{q}} = 546.52 \,\mathrm{GeV}$

NLO result - I



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• (N)LO Green's function

$$\circ ||C^{[Y]}|| m_{\tilde{g}} \alpha_s(\mu_s) = \mu_s \quad \leftrightarrow \quad \mu_h = 2m_{\tilde{g}}$$

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Thank you for your attention!