

Hyperons, Hypernuclei & Neutron Stars

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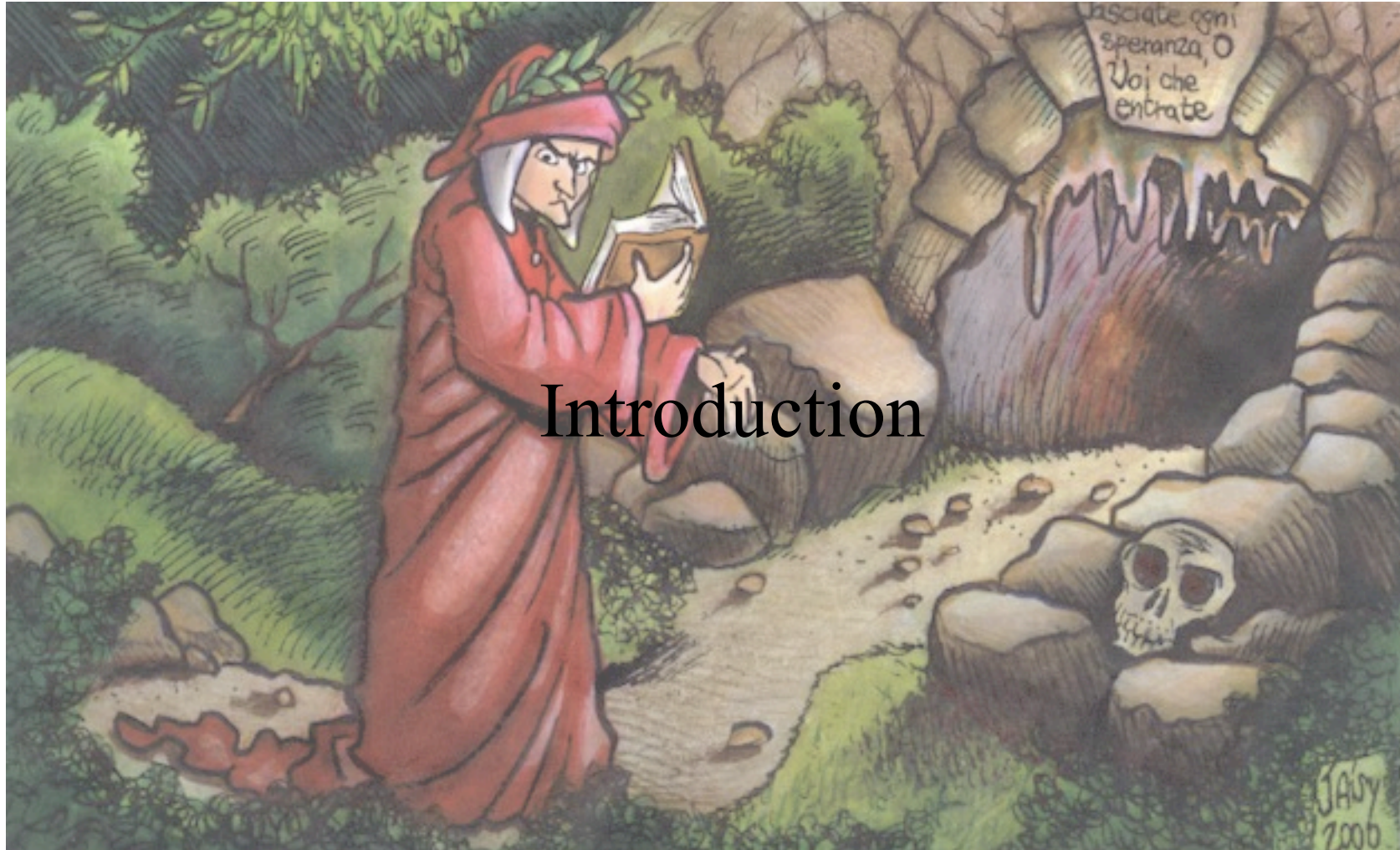


Galileo Galilei Institute for Theoretical Physics
Firenze (Italia), March 10th-14th 2014

Road Map for a Strange Trip



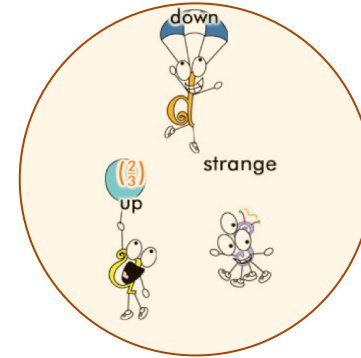
- ✧ Hypernuclei & Hypernuclear Physics
- ✧ YN & YY Interactions
- ✧ EoS of Hypernuclear Matter
- ✧ Role of Hyperons on Neutron Stars



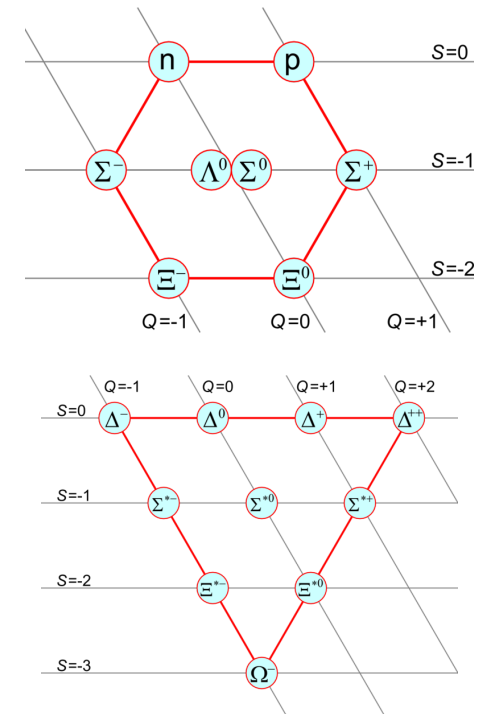
Introduction

What is a hyperon ?

✧ A **hyperon** is a baryon made of one , two or three **strange quarks**

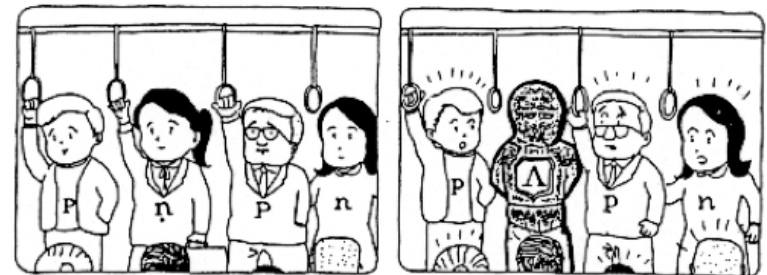


Hyperon	Quarks	I(J ^P)	Mass (MeV)
Λ	uds	0(1/2 ⁺)	1115
Σ^+	uus	1(1/2 ⁺)	1189
Σ^0	uds	1(1/2 ⁺)	1193
Σ^-	dds	1(1/2 ⁺)	1197
Ξ^0	uss	1/2(1/2 ⁺)	1315
Ξ^-	dss	1/2(1/2 ⁺)	1321
Ω^-	sss	0(3/2 ⁺)	1672



What is a hypernucleus ?

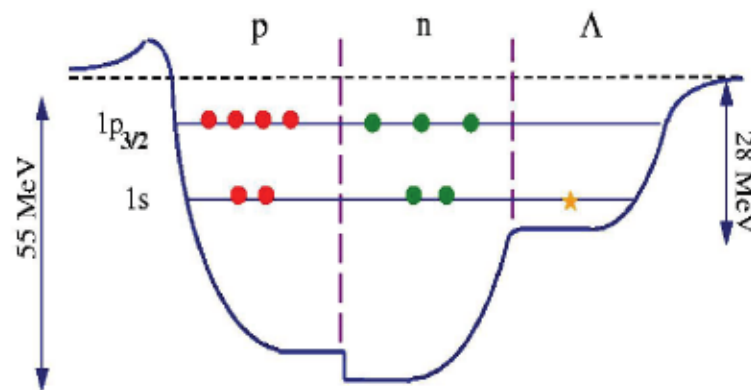
- ✧ A hypernucleus is a bound system of nucleons with one or more strange baryons (Λ , Σ , Ξ , Ω^- hyperons).



Ordinary nucleus

With a strange particle

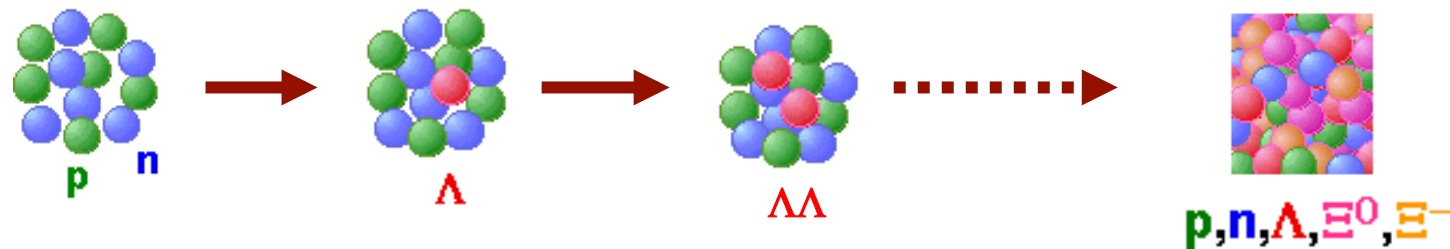
H. Bando, PARITY 1, 54 (1986)



Simple s.p. model of ${}_{\Lambda}^{12}\text{C}$

- ✧ In a simple single-particle model: protons, neutrons and hyperons are considered distinguishable particles placed in independent effective potential wells in which Pauli exclusion principle is applied.

- ✧ Since hyperons are distinguishable from nucleons, they are privileged probes to explore states deep inside the nucleus, extending our knowledge of conventional to flavored nuclear physics.



- ✧ Hyperons can change the nuclear structure. For instance the glue-like role of the Λ hyperon can facilitate the existence of neutron-rich hypernuclei, being a more suitable framework to study matter with extreme n/p ratios as compared to ordinary nuclei.
- ✧ A hypernucleus is a “laboratory” to study hyperon-nucleon (YN) and hyperon-hyperon (YY) interactions.

A simple model of hypernuclei: Hyperon-Nucleus effective potential

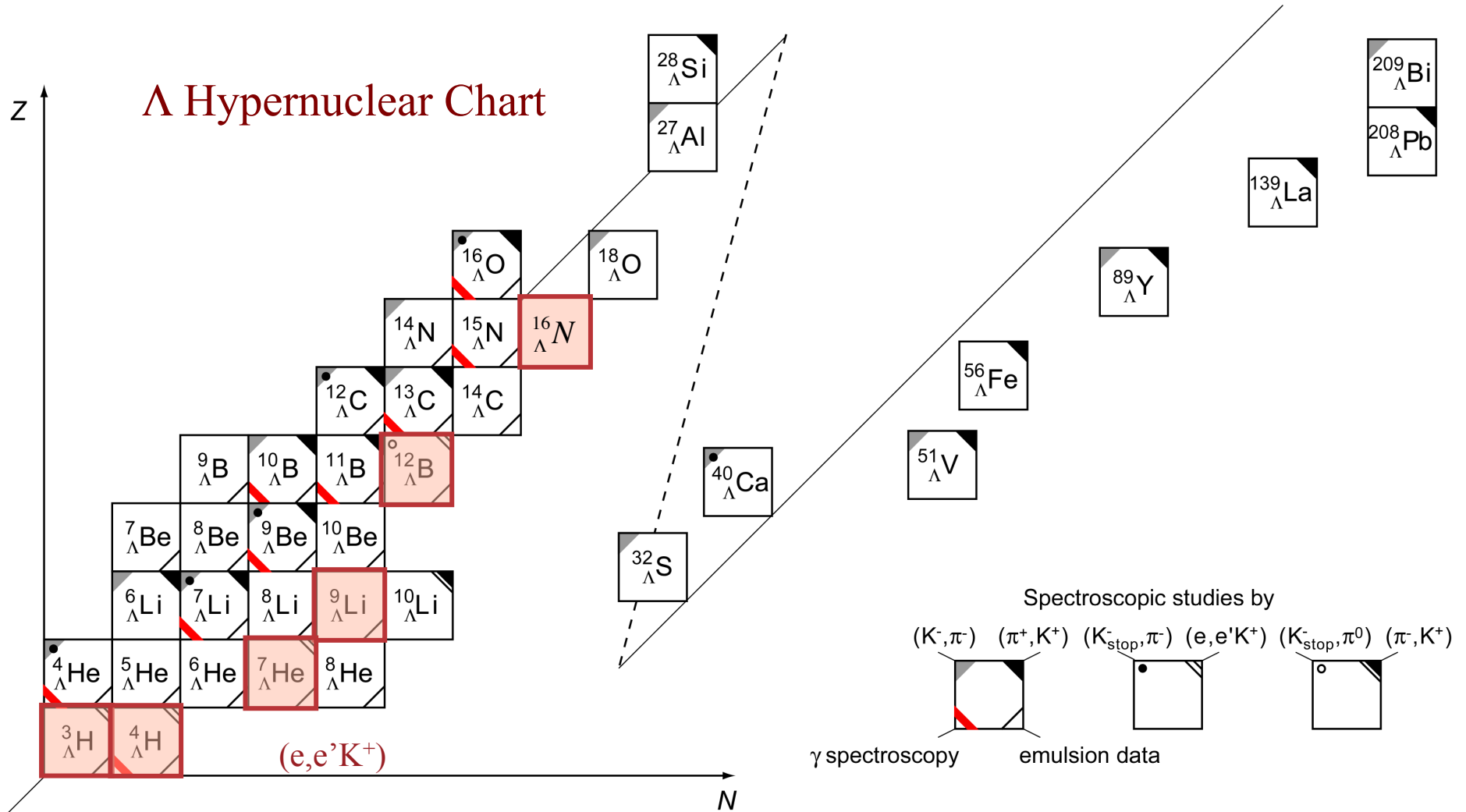
Hypernucleus = Ordinary Nuclear Core + Hyperon in a
s.p. state of a hyperon-nucleus effective potential
derived from hyperon-nucleon interaction

$$V_{\Lambda N}^{eff}(r) = V_0(r) + V_S(r)(\vec{S}_N \cdot \vec{S}_\Lambda) + V_T(r)S_{12} + V_{ls}(r)(\vec{L} \times \vec{S}^+) + V_{als}(r)(\vec{L} \times \vec{S}^-)$$

The diagram illustrates the decomposition of the hyperon-nucleon interaction potential $V_{\Lambda N}^{eff}(r)$ into five terms, each with a corresponding physical interpretation indicated by an arrow:

- $V_0(r)$: central
- $V_S(r)(\vec{S}_N \cdot \vec{S}_\Lambda)$: spin-spin
- $V_T(r)S_{12}$: tensor
- $V_{ls}(r)(\vec{L} \times \vec{S}^+)$: symmetric spin-orbit
- $V_{als}(r)(\vec{L} \times \vec{S}^-)$: antisymmetric spin-orbit (zero in NN due to Pauli principle)

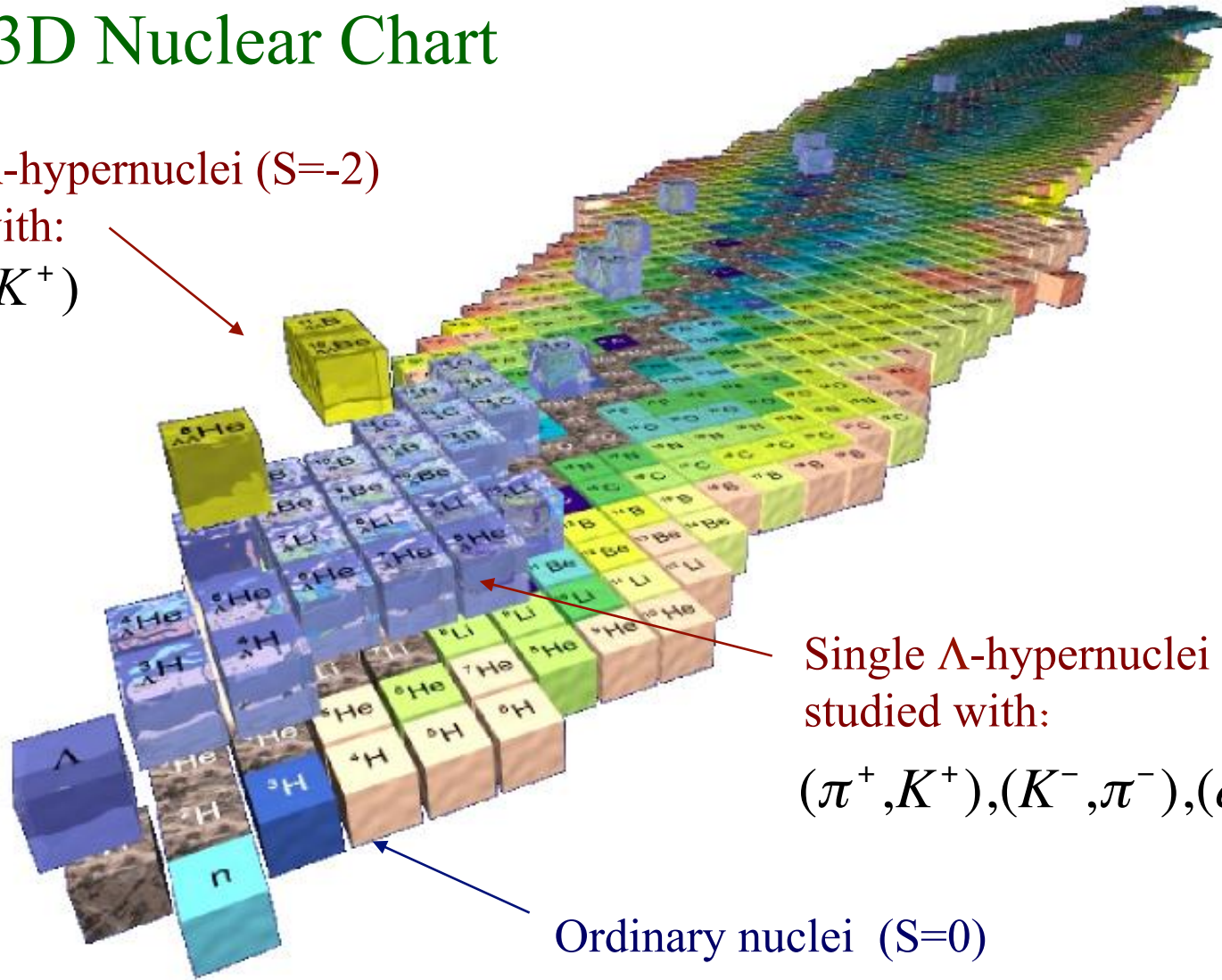
Present status of Λ Hypernuclear Spectroscopy



O. Hashimoto and H. Tamura, Prog. Part. Nucl. Phys. 57, 564 (2006)

The 3D Nuclear Chart

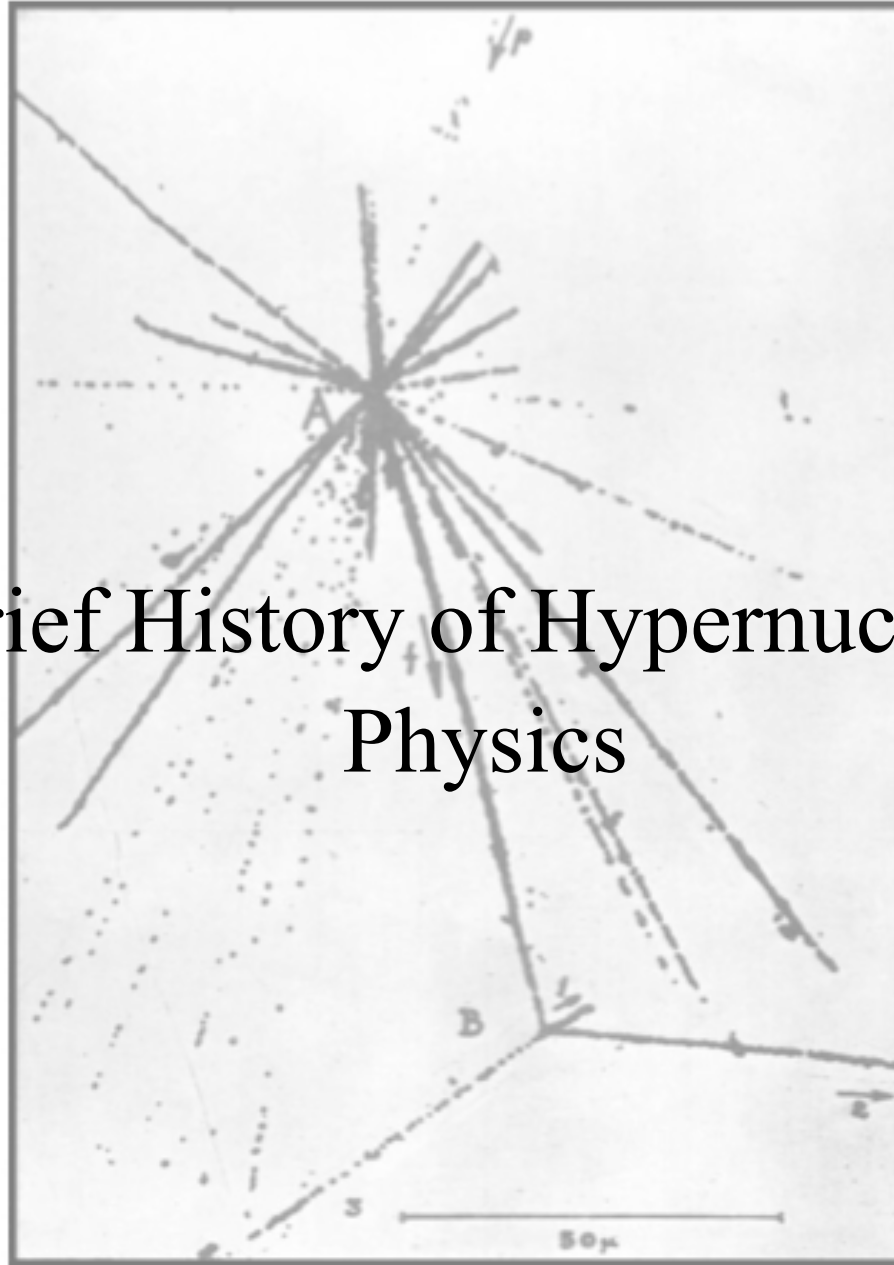
Double Λ -hypernuclei ($S=-2$)
studied with:
 (K^-, K^+)



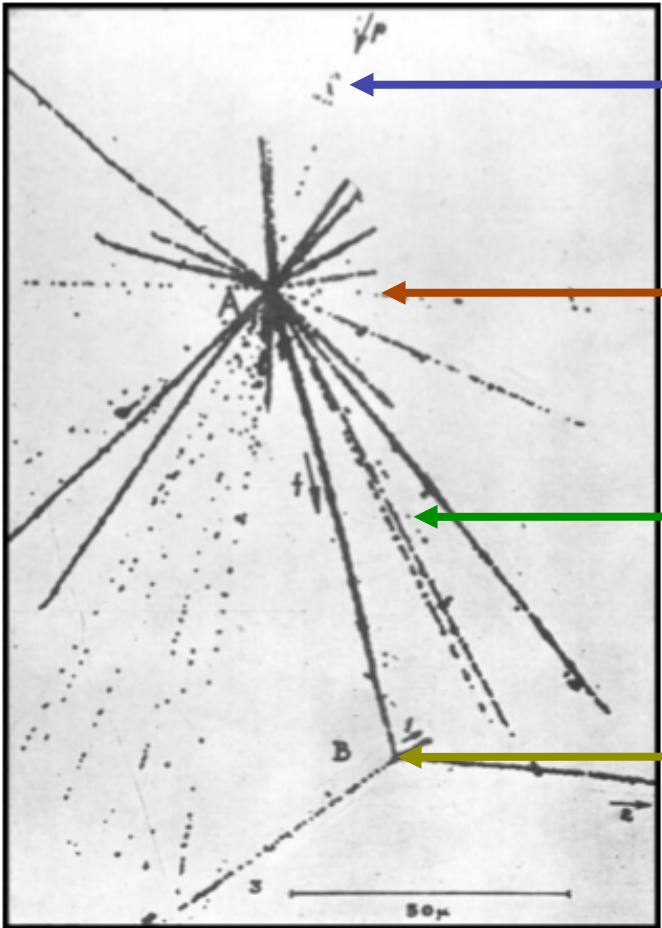
Single Λ -hypernuclei ($S=-1$)
studied with:
 $(\pi^+, K^+), (K^-, \pi^-), (e, e' K^+)$

Ordinary nuclei ($S=0$)

Brief History of Hypernuclear Physics



First hypernuclear event observed in a nuclear emulsion by Marian Danysz and Jerzy Pniewski in 1952



Incoming high energy cosmic ray (proton)

Collision with the nucleus

Nuclear fragments that eventually stop in the emulsion

One fragment containing a hyperon disintegrates weakly

To commemorate the discovery of Danysz and Pniewski a postcard was issued by the Polish Post in May 1993



(200.000 postcards, postcard price 2000 zł, stamp 1500 zł)

A few years earlier, in 1989, the postmark designed on the basis of the first hypernucleus observation was used for the 20th International Physics Olympiad at the Warsaw post office number 64





Historical Overview

1953 → 1970 : hypernuclear identification with visualizing techniques emulsions, bubble chambers

1962 : first double Λ hypernucleus discovered in a nuclear emulsion irradiated by a beam of K^- mesons at CERN

1970 → Now : Spectrometers at accelerators:

CERN (up to 1980)

BNL : (K^- , π^-) and (π^+ , K^+) production methods

KEK : (K^- , π^-) and (π^+ , K^+) production methods

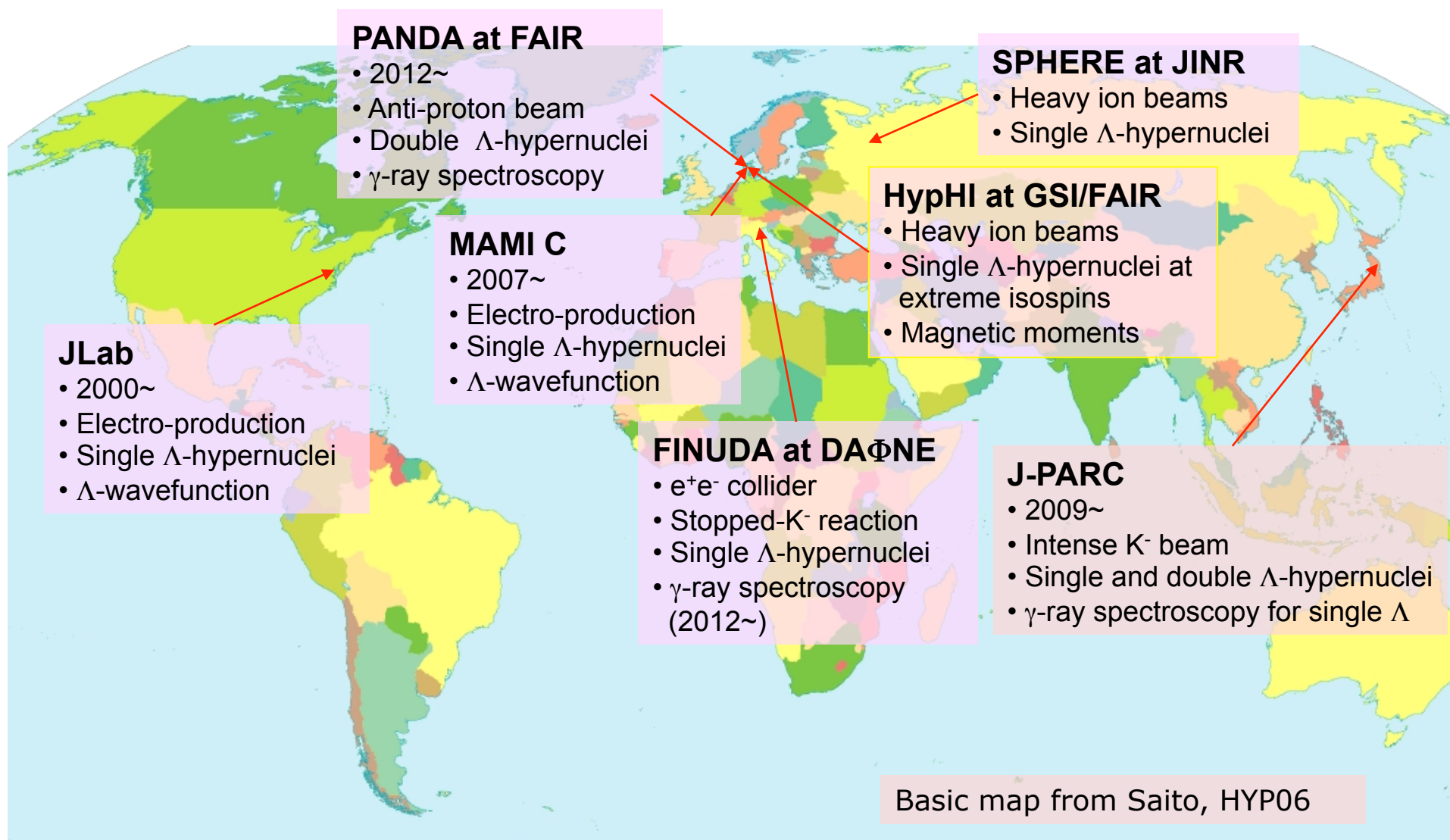
After 2000 : Stopped kaons at DAΦNE (FINUDA) : (K^-_{stop} , π^-)

The new electromagnetic way :

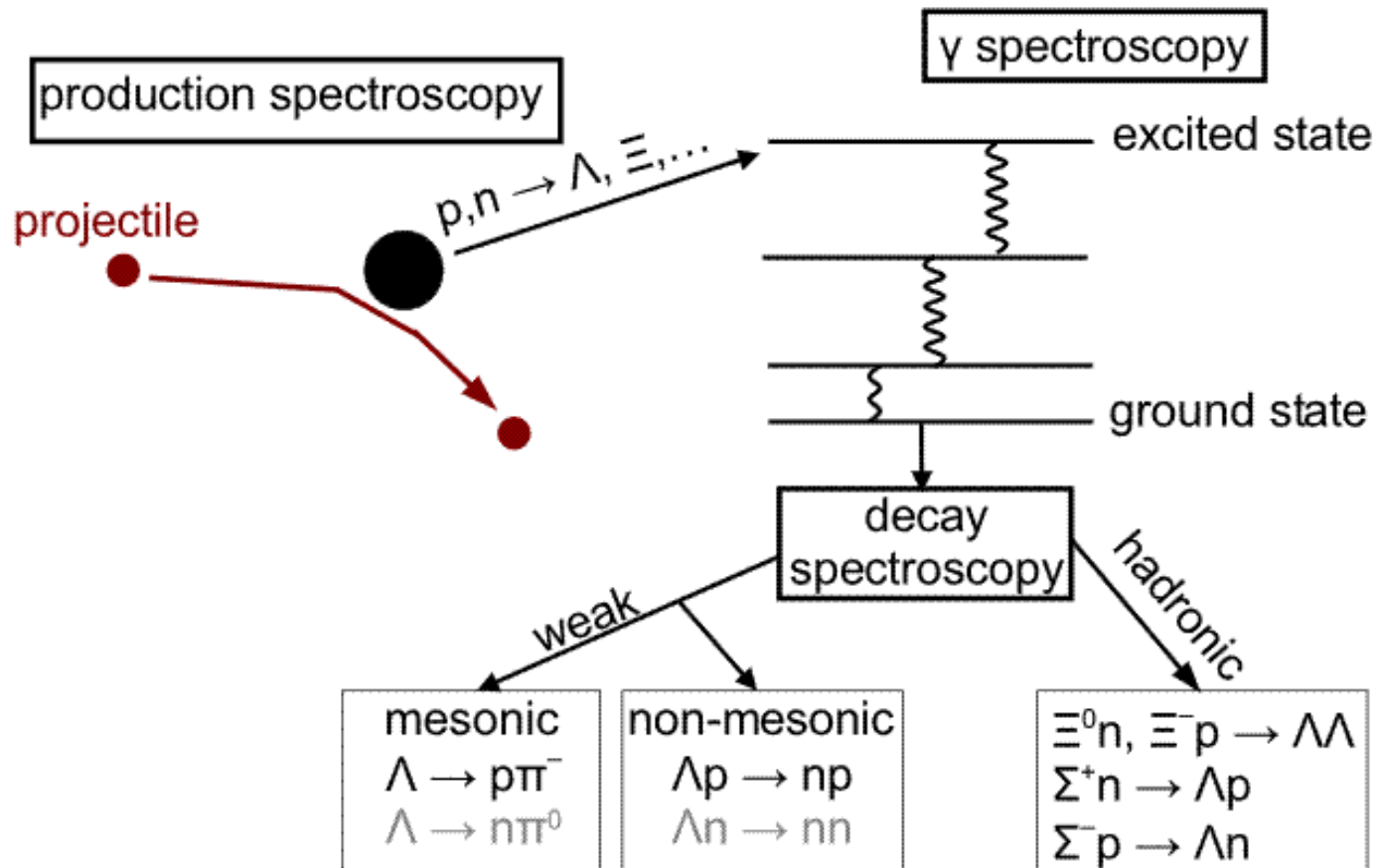
HYPERNUCLEAR production with

ELECTRON BEAM ($e, e'K^+$) at JLAB & MAMI-C

International Hypernuclear Network

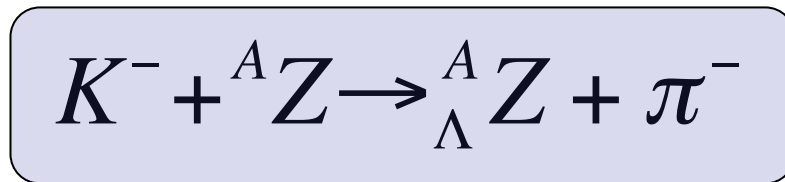


Hypernuclei: from the cradle to the grave

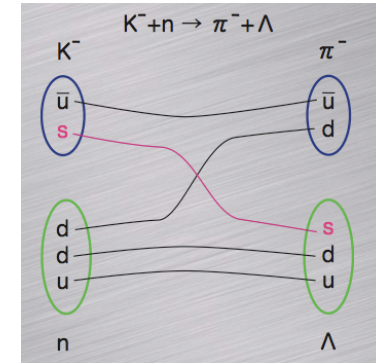


Production of Λ hypernuclei can occur by ...

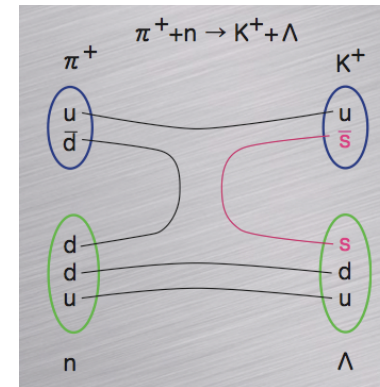
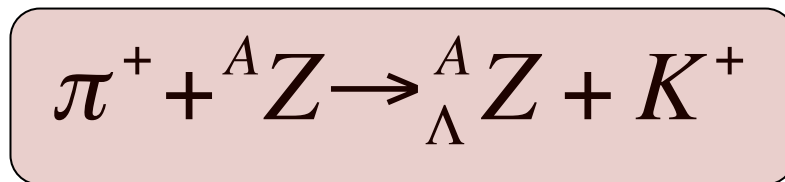
- ✧ Strangeness exchange: (BNL, KEK, JPARC)
(replace a u or d quark with an s quark)



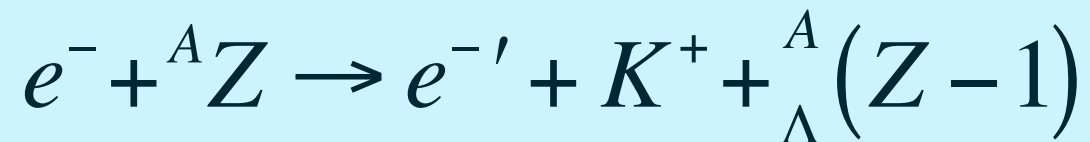
Where the K^- in-flight or stopped



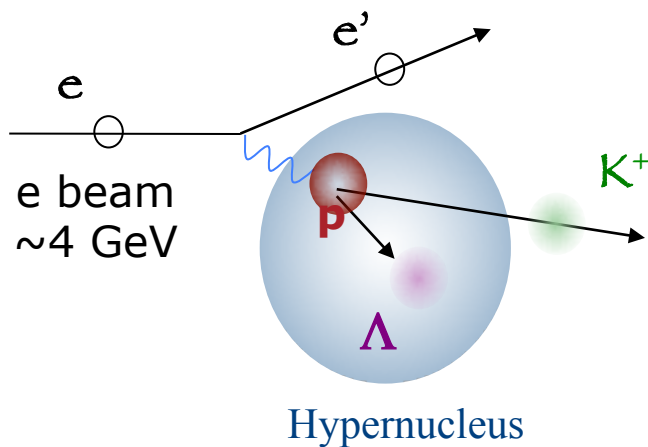
- ✧ Associated production: (BNL, KEK, GSI)
(produces an $s\bar{s}$ pair)



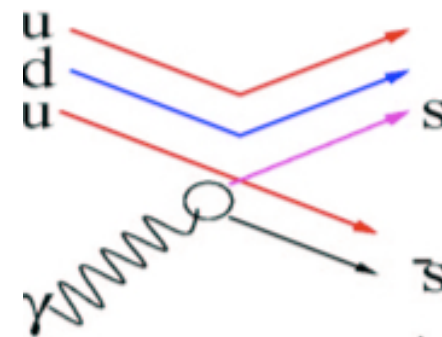
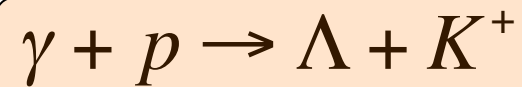
✧ Electroproduction: (JLAB, MAMI-C)



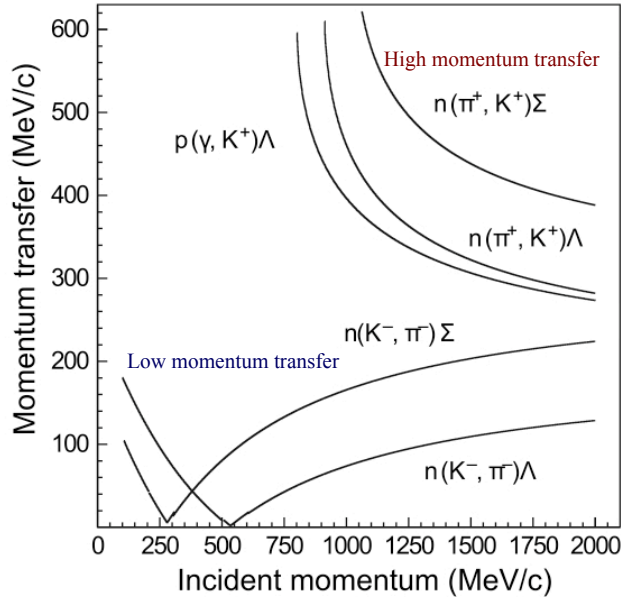
${}^A Z(e, e' K) {}^A(Z-1)_{\Lambda}$



elementary process



Production kinematics

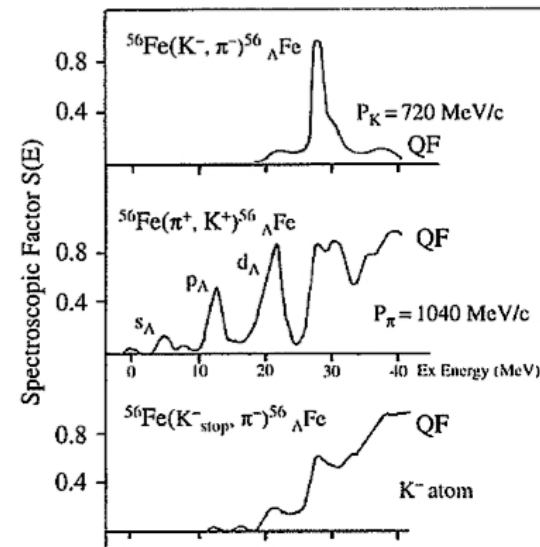


✧ $n(K^-, \pi^-)\Lambda$

- ✓ Low momentum transfer \rightarrow hyperon has large probability of being bound.
- ✓ Attenuation of (K^-, π^-) reaction in matter (resonance states). Interaction with outer shell neutrons replacing it with a Λ in the same shell.

✧ $n(\pi^+, K^+)\Lambda, p(\gamma, K^+)\Lambda$

- ✓ High momentum transfer \rightarrow hyperon has large probability of escaping the nucleus.
- ✓ Longer π^+ and K^+ mean free path \rightarrow interaction with interior nucleons, significant angular momentum transfer.

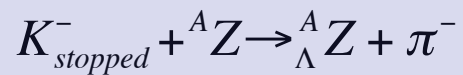


Measurement of hypernuclear masses

$$M_{\Lambda Z} - M_{AZ} = B_{AZ} - B_{\Lambda Z} + M_{\Lambda} - M_N$$

✧ Stopped K⁻ reaction

(K⁻_{stopped}, π⁻)

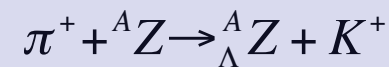
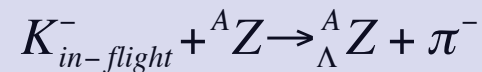


$$M_{\Lambda Z} = \sqrt{(E_{\pi} - M_K - M_{AZ})^2 - p_{\pi}^2}$$

Need only π⁻ outgoing momentum →
One Spectrometer

✧ In-flight reactions

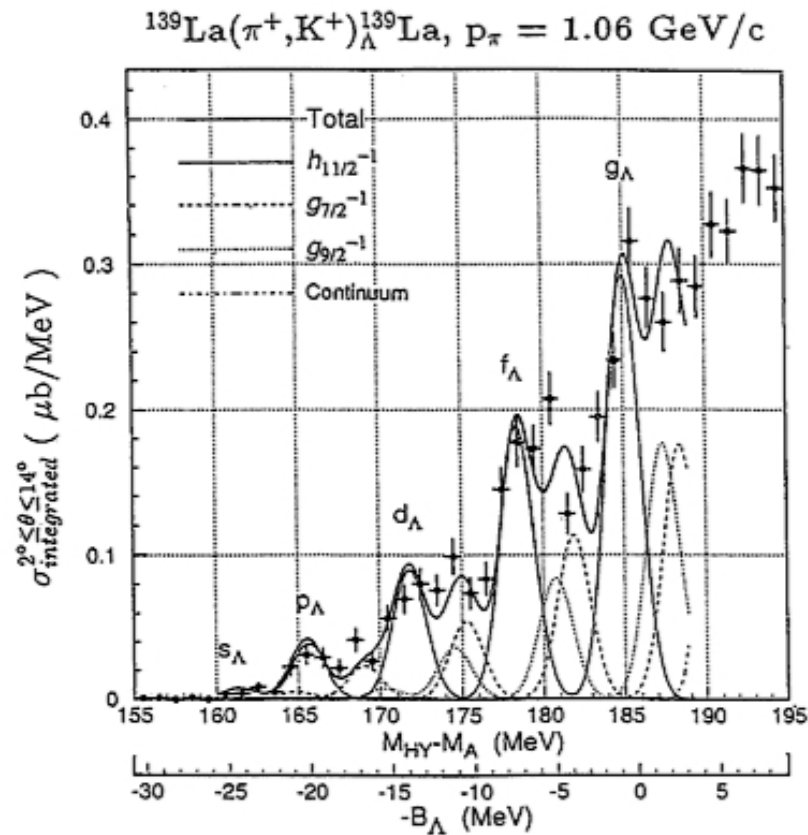
(K⁻_{in-flight}, π⁻) (π⁺, K⁺)



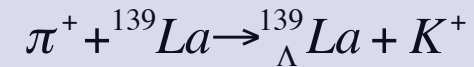
$$M_{\Lambda Z} = \sqrt{(E_{\pi} - E_K - M_{AZ})^2 - (\vec{p}_{\pi} - \vec{p}_K)^2}$$

Need incident & outgoing momenta →
Two Spectrometers

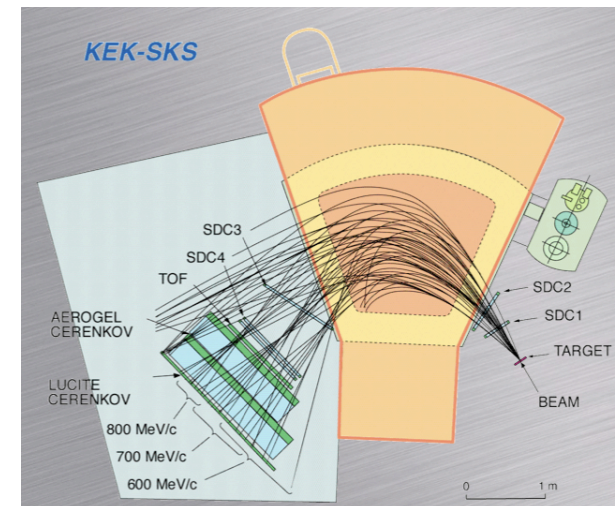
Example: spectrum for a (π^+, K^+) on a heavy target



T. Hasegawa et al., Phys. Rev. C 53, 1210 (1996)



- ✓ Energy resolution: 2.5 MeV
- ✓ Clear shell structure
- ✓ Obtained with a typical magnetic spectrometer for the detection of K^+



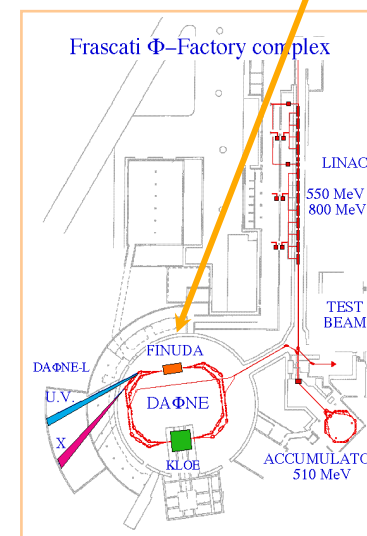
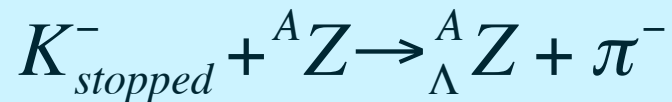
The FINUDA experiment @ DAΦNE (Frascati)

DAΦNE: Double Annular e^+e^-
Φ-factory for Nice Experiments

e^+e^- collider dedicated to the production
of Φ resonance

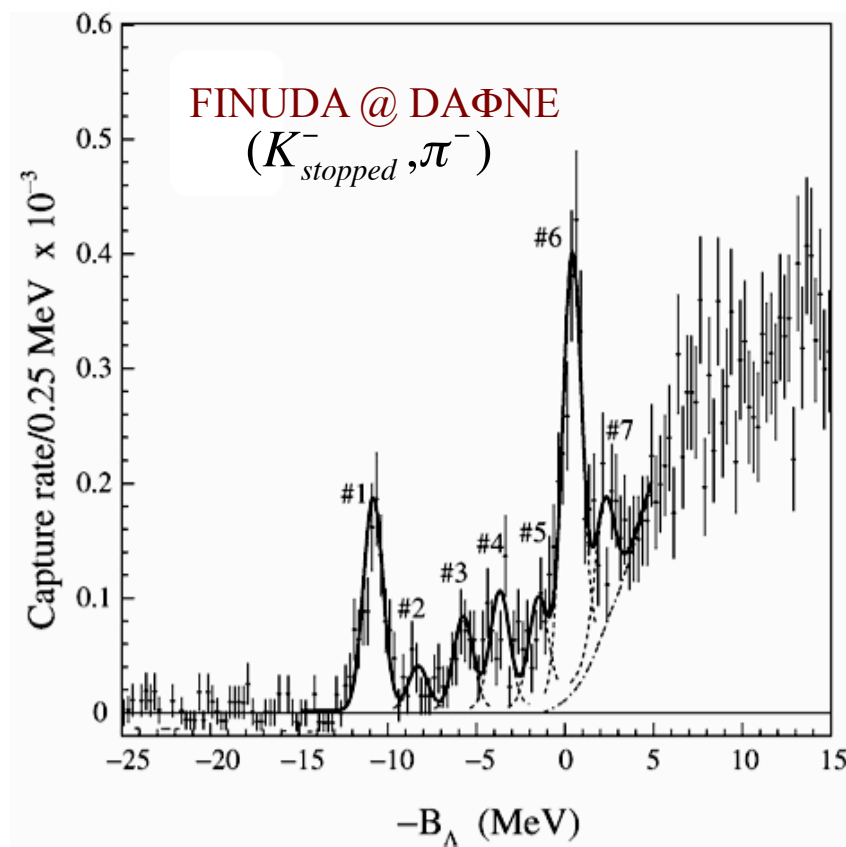
FINUDA: FISica NUcleare at DAΦNE

produce hypernuclei by stopping negative kaon
originating from Φ decay in nuclear target

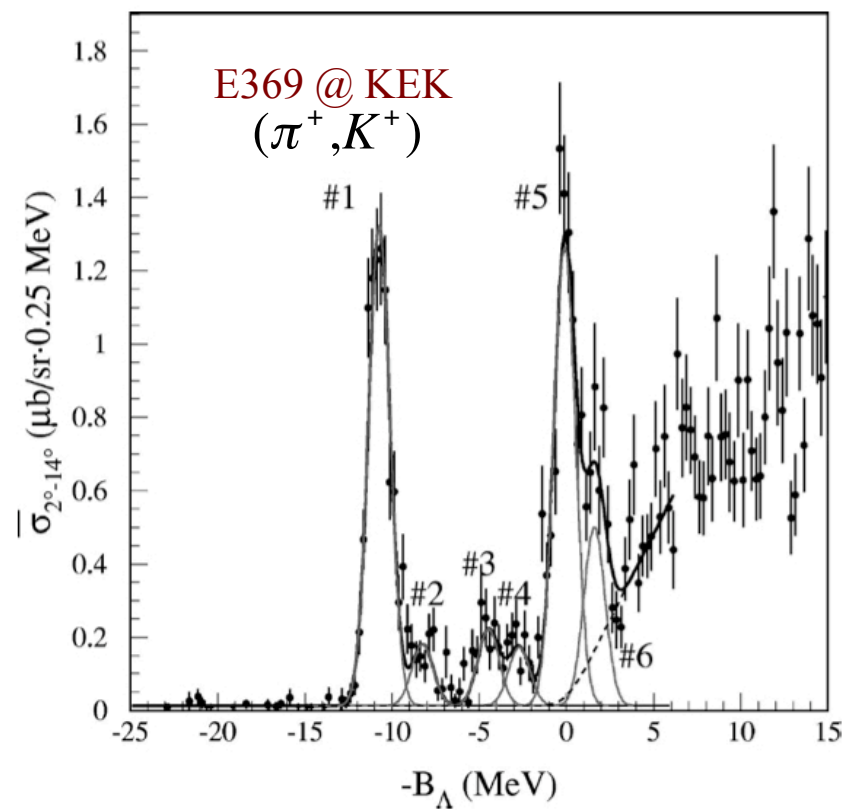


FINUDA results on $^{12}_{\Lambda}\text{C}$

Very good agreement between FINUDA results
& E368 @ KEK ones



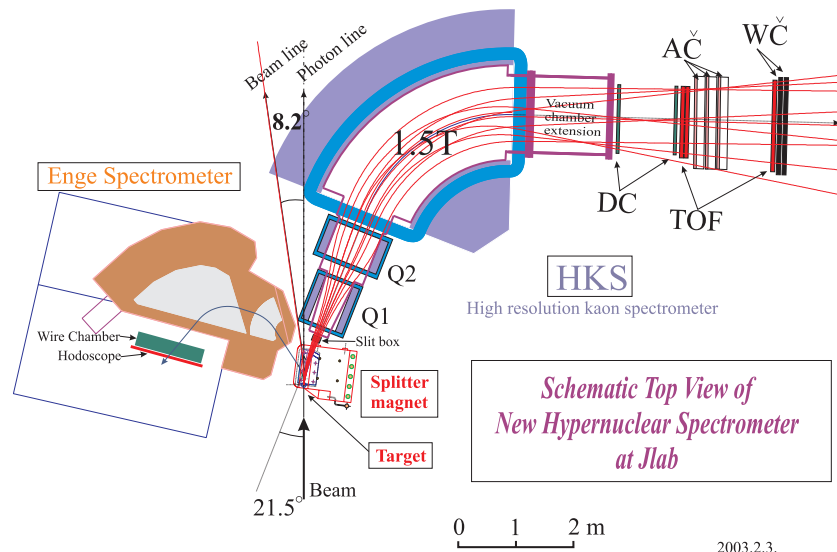
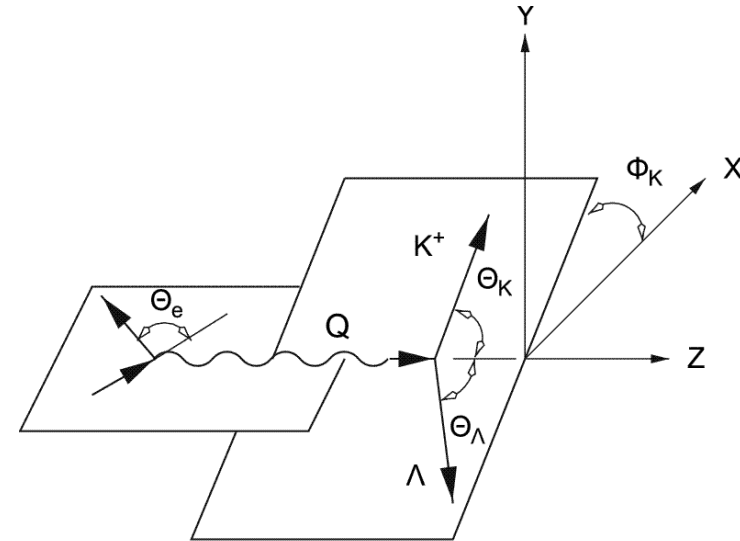
M. Agnello et al., Phys. Lett. B 622, 35 (2005)



H. Hotchi et al., Phys. Rev. C 64, 044302 (2001)

The $(e, e'K^+)$ reaction

- ✧ Relatively new (JLAB, MAMI-C).
- ✧ Excellent energy resolution of energy spectrum.
- ✧ Although the cross section is 10^{-2} smaller than that of (π^+, K^+) this is compensated by larger beam intensity.

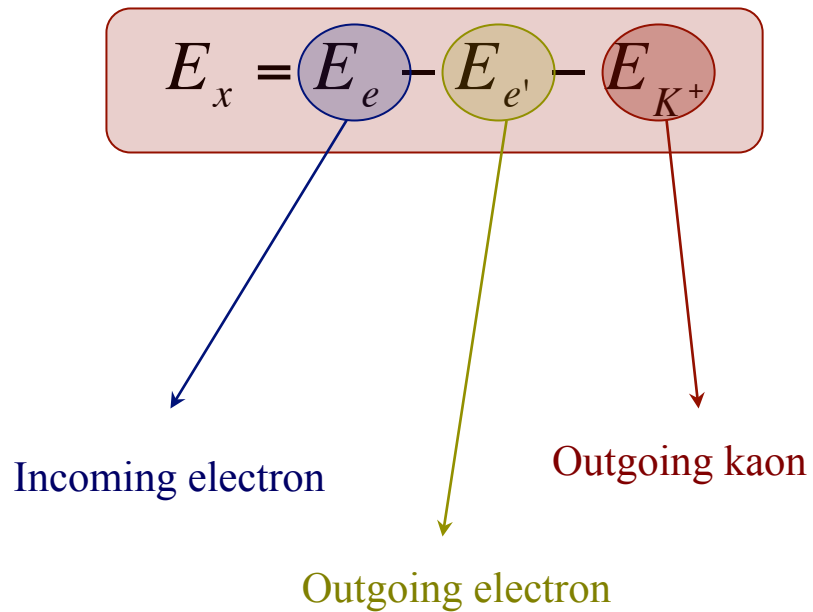


The experimental geometry requires two spectrometers to detect:

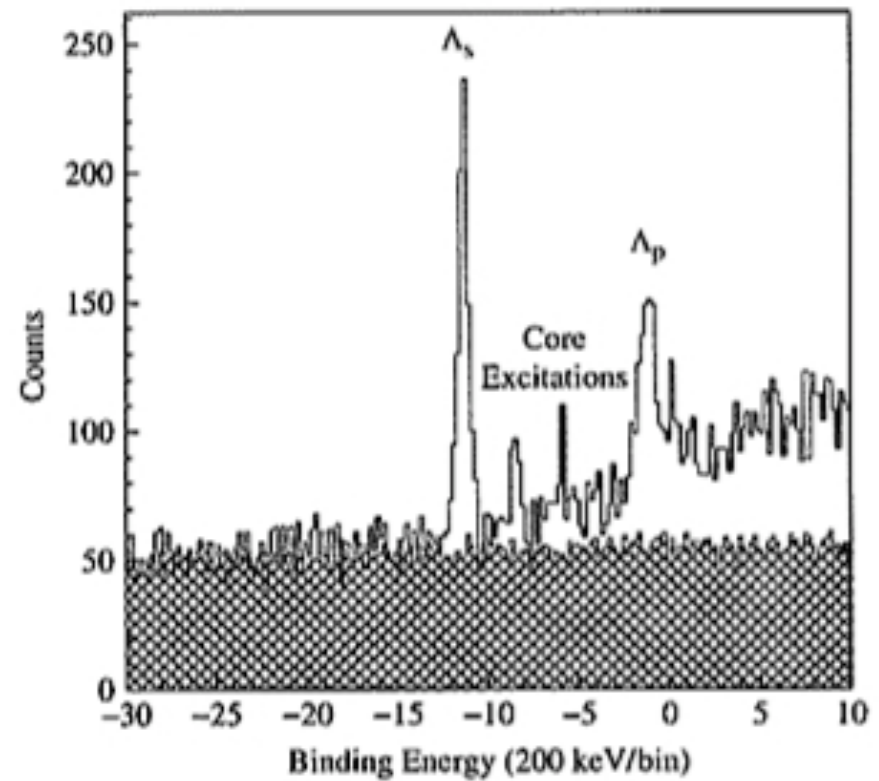
- ✓ the scattered electrons which defines the virtual photons
- ✓ the kaons

Hypernuclear spectrum from the (e,e'K⁺) reaction

Energy left inside the nucleus
(related to the excitation energy)

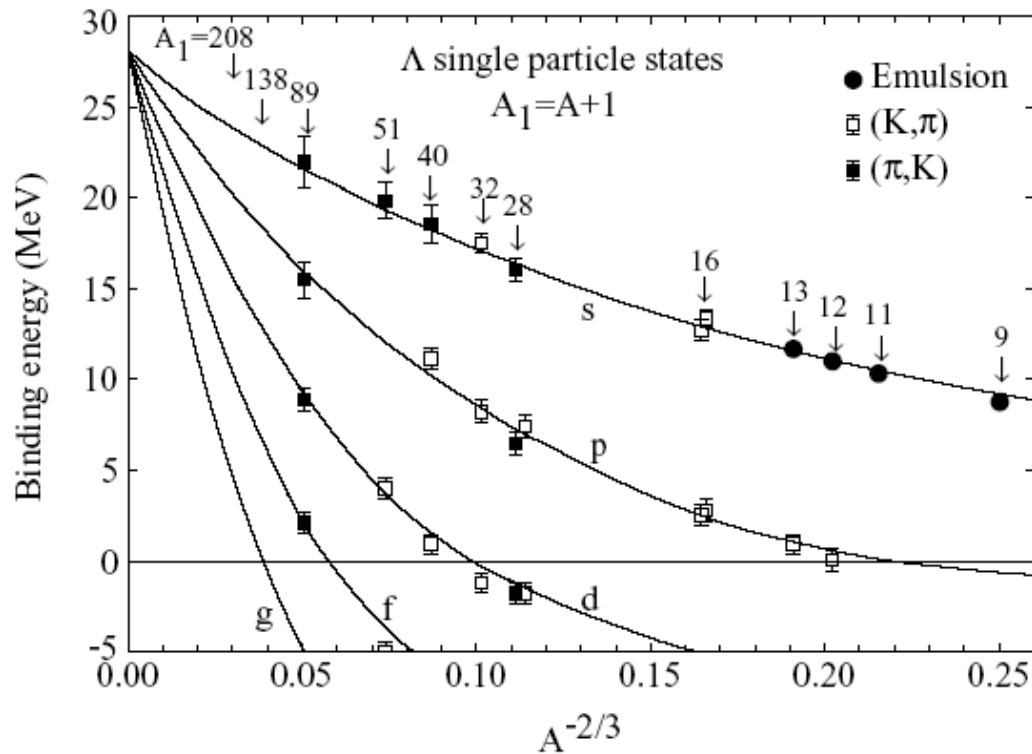


$^{12}\text{C}(e,e'K^+)^{12}_\Lambda\text{B}$ spectrum

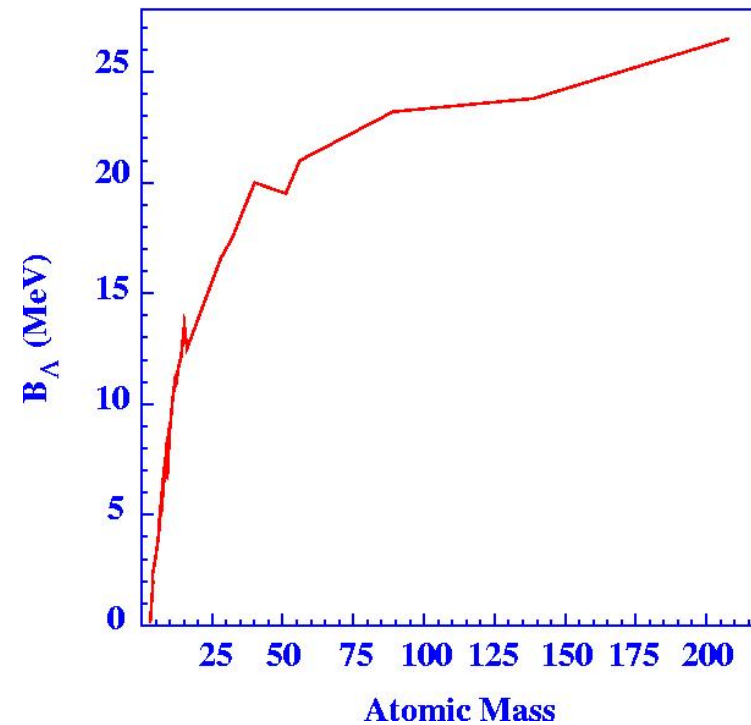


In summary ...

The Λ single particle states



Hypernuclear binding energies

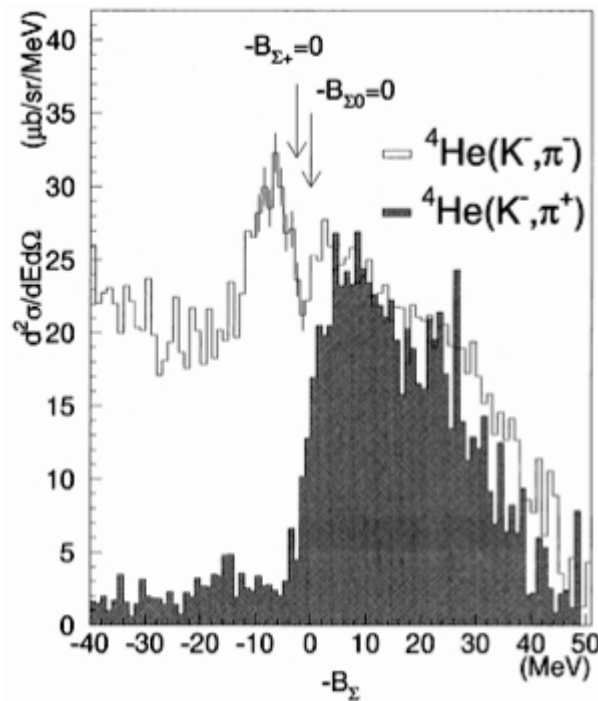


Hypernuclear binding energies show saturation as ordinary nuclei

Production of Σ hypernuclei

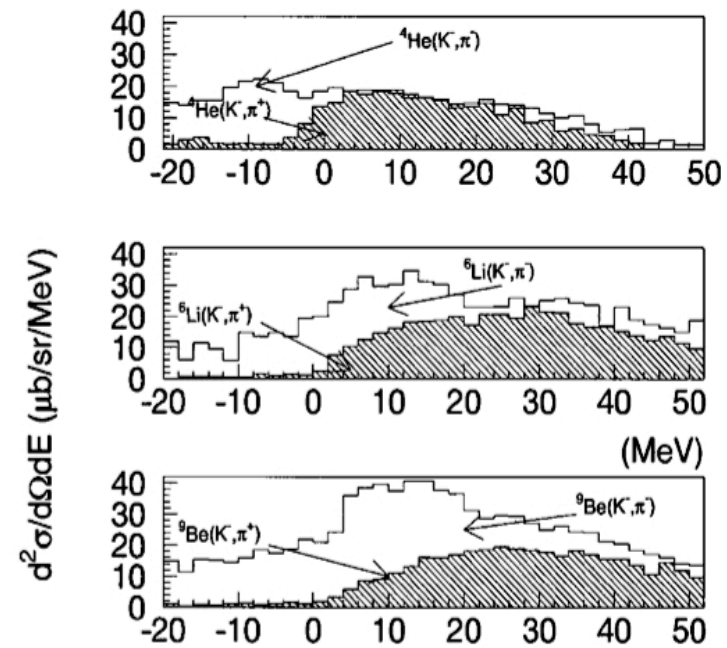
Production mechanisms similar to the ones considered for Λ hypernuclei like, e.g., strangeness exchange (K^-, π^\pm)

$^4_\Sigma\text{He}$ bound state
 $E \sim 4 \text{ MeV}, \Gamma \sim 7 \text{ MeV}$



T. Nagae et al., Phys. Rev. Lett. 80, 1605 (1998)

Σ hypernuclear states in
 p-shell hypernuclei



S. Bart et al., Phys. Rev. Lett. 83, 5238 (1998)

What do we know about double Λ hypernuclei ?

Not so much

	$B_{\Lambda\Lambda}$ (MeV)	$\Delta B_{\Lambda\Lambda}$ (MeV)		
${}_{\Lambda\Lambda}^6\text{He}$	10.9 ± 0.5	4.7 ± 0.6	Prowse	(1966)
${}_{\Lambda\Lambda}^6\text{He}$	$7.25 \pm 0.19^{+0.18}_{-0.11}$	$1.01 \pm 0.20^{+0.18}_{-0.11}$	KEK-E373	(2001)
${}_{\Lambda\Lambda}^{10}\text{Be}$	17.7 ± 0.4	4.3 ± 0.4	Danyasz	(1963)
${}_{\Lambda\Lambda}^{10}\text{Be}$	8.5 ± 0.7	-4.9 ± 0.7	KEK-E176	(1991)
${}_{\Lambda\Lambda}^{13}\text{B}$	27.6 ± 0.7	4.8 ± 0.7	KEK-E176	(1991)
${}_{\Lambda\Lambda}^{10}\text{Be}$	$12.33^{+0.35}_{-0.21}$		KEK-E373	(2001, unpublished)

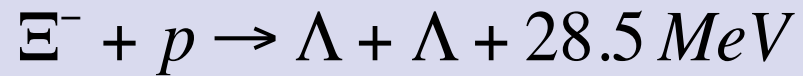
Nagara event
same event

$$B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^AZ) = B_{\Lambda}({}_{\Lambda\Lambda}^AZ) + B_{\Lambda}({}_{\Lambda}^{A-1}Z)$$

$$\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^AZ) = B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^AZ) - 2B_{\Lambda}({}_{\Lambda}^{A-1}Z) = B_{\Lambda}({}_{\Lambda\Lambda}^AZ) - B_{\Lambda}({}_{\Lambda}^{A-1}Z)$$

The production of double Λ hypernuclei

✧ Ξ^- conversion in two Λ 's:

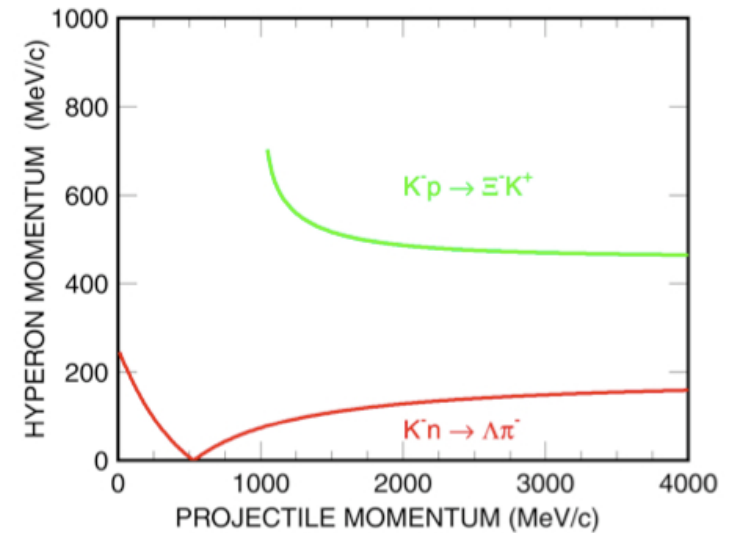
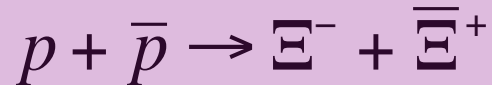


■ Ξ^- production:

✓ (K^-, K^+) reaction (BNL, KEK)

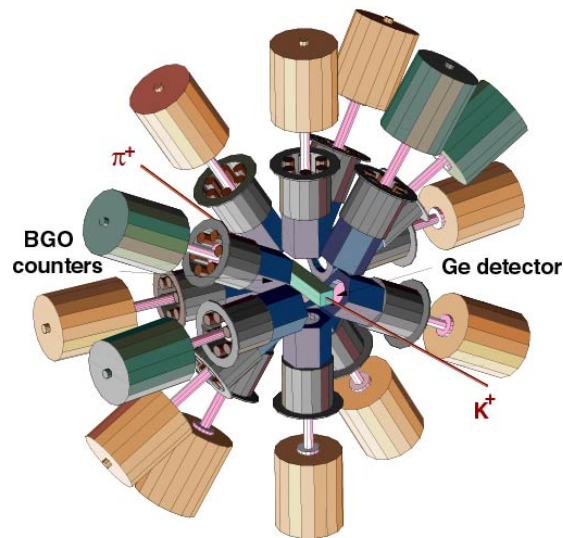


✓ Antiproton production (PANDA@FAIR)

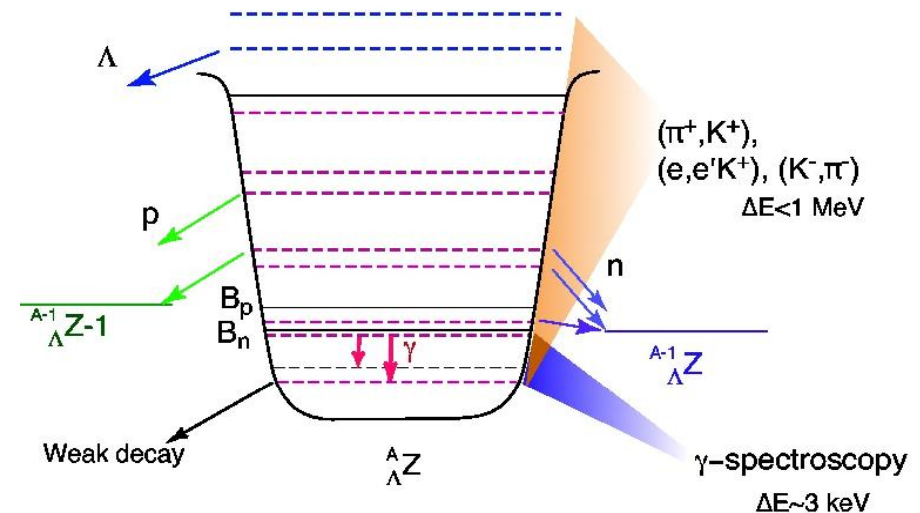


Hypernuclear γ -ray spectroscopy

- Produced hypernuclei can be in an excited state.
- Energy released by emission of neutrons or protons or γ -ray when hyperon moves to lower states.

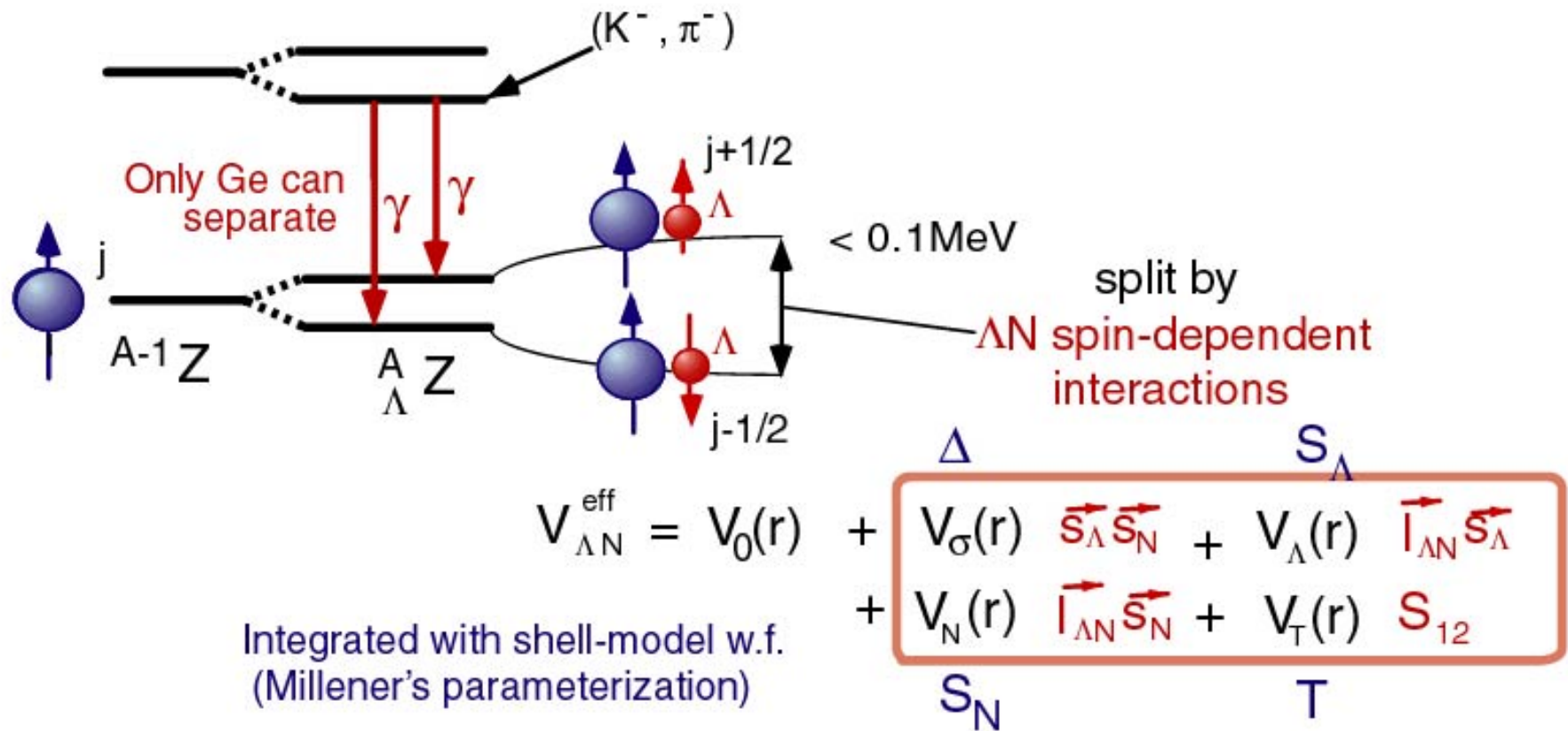


Hyperball



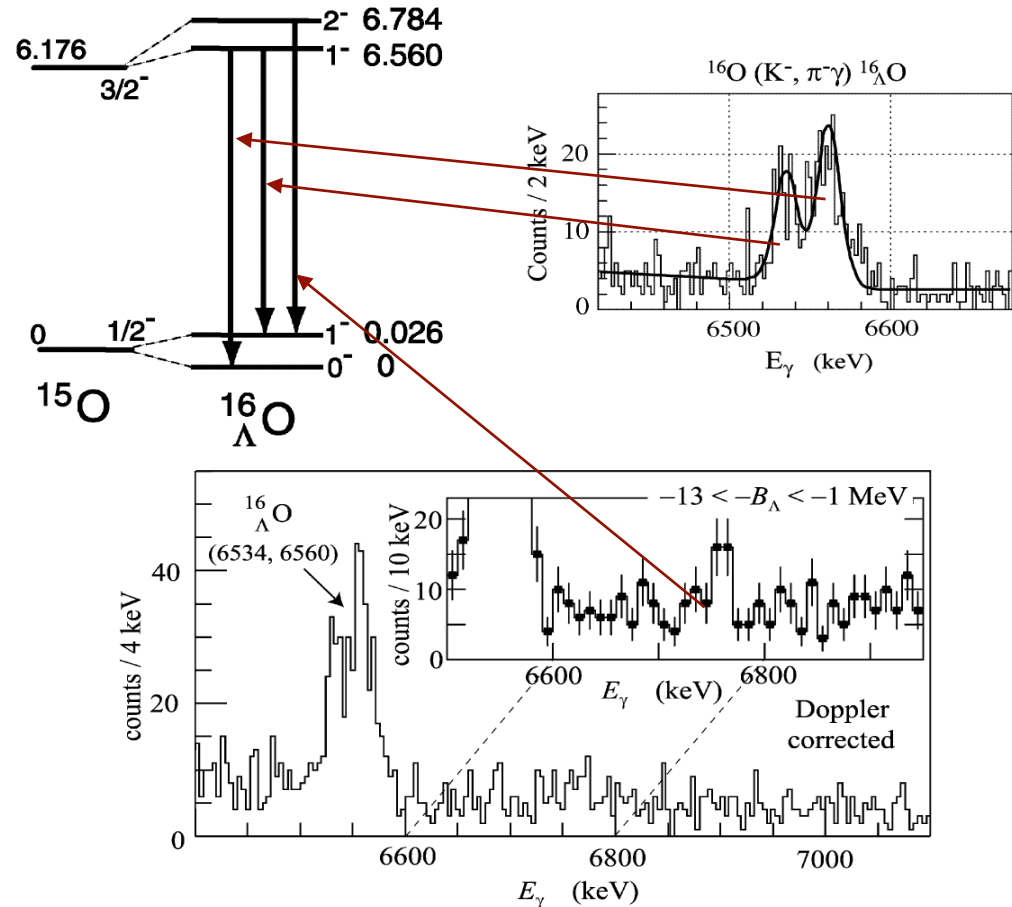
- Excellent resolution with Ge (NaI) detectors.
- Λ depth potential in nucleus $\sim 30 \text{ MeV}$
 \rightarrow observation of γ -rays limited to low excitation region.
- γ -ray transition measures only energy difference between two states.

Hypernuclear fine structure & the spin-dependent ΛN interaction



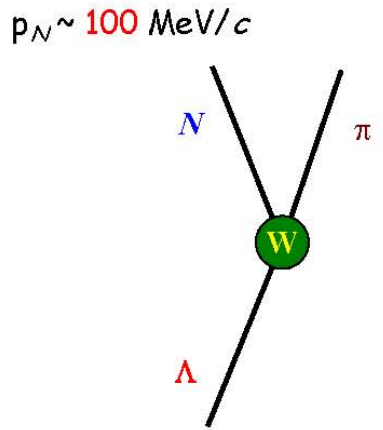
γ -ray spectrum of $^{16}_{\Lambda}\text{O}$

- ✧ Observed twin peaks demonstrate hypernuclear fine structure for $^{16}_{\Lambda}\text{O}$ ($1^- \rightarrow 1^-, 0^-$) transitions.
- ✧ Small spacing in twin peaks caused by spin-dependent ΛN interaction.
- ✧ Recent analysis revealed another transition at 6758 keV corresponding to $^{16}_{\Lambda}\text{O}$ ($2^- \rightarrow 0^-$).



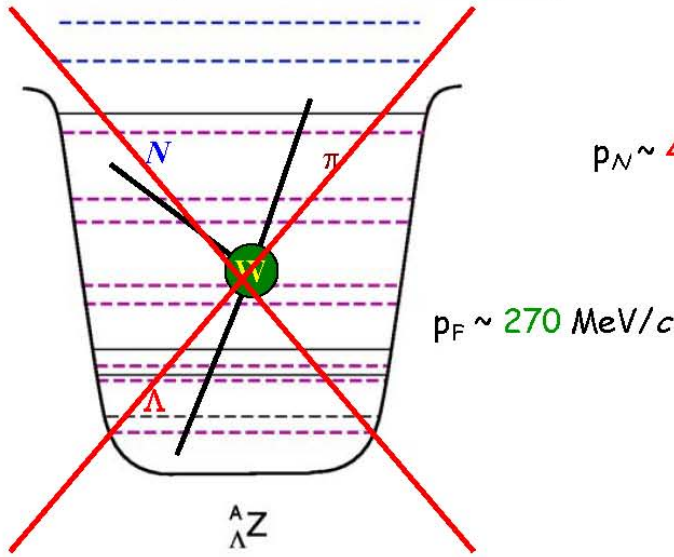
The Weak Decay of Λ hypernuclei

free Λ decay



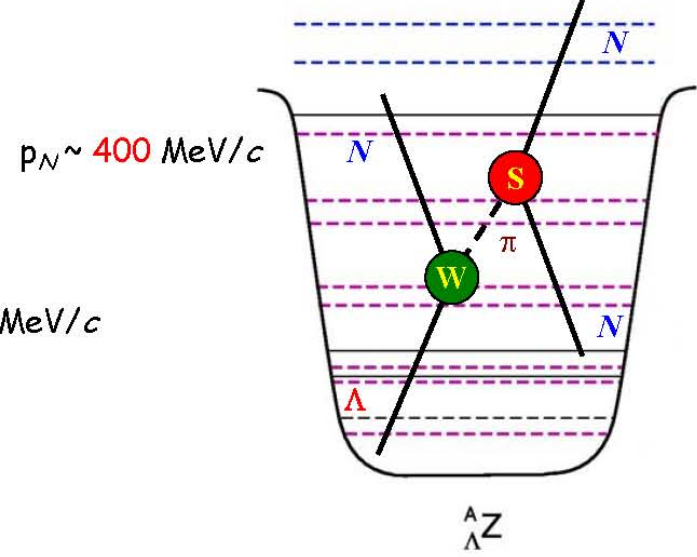
$\Lambda \rightarrow n + \pi^0 + 41 \text{ MeV} \text{ (36\%)}$
 $\Lambda \rightarrow p + \pi^- + 38 \text{ MeV} \text{ (64\%)}$
 $\tau_\Lambda = 263 \text{ ps}$

hypernucleus
mesonic decay



suppressed by
Pauli blocking

hypernucleus
non-mesonic decay



$\Lambda + n \rightarrow n + n + 176 \text{ MeV}$
 $\Lambda + p \rightarrow n + p + 176 \text{ MeV}$

Decay observables

$$\Gamma \sim \Gamma_{\Lambda}^{free} = 3.8 \times 10^9 \text{ s}^{-1}$$

Hypernuclear lifetimes-Decay Rates

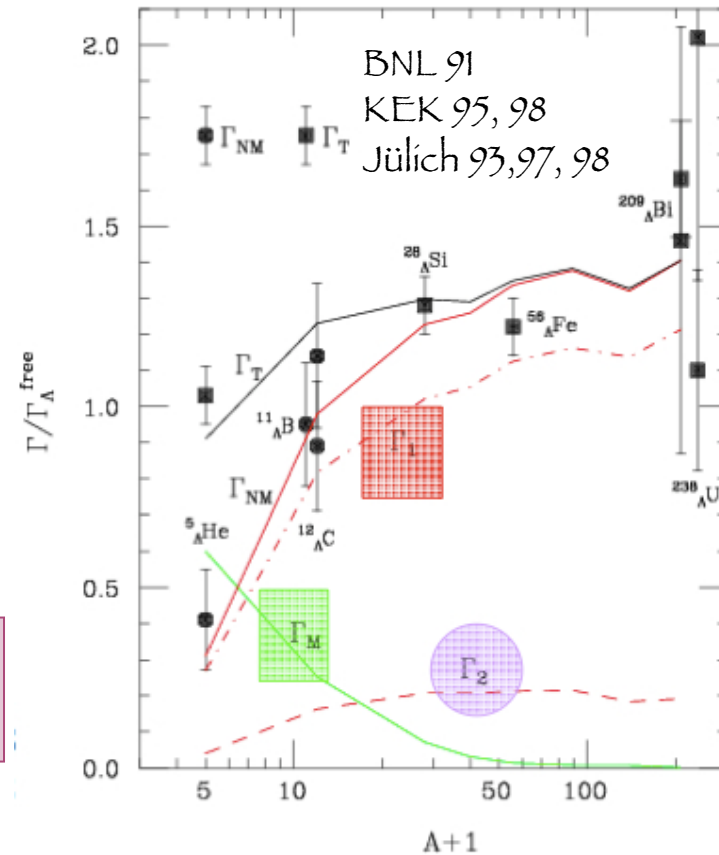
$$\Gamma = \Gamma_M + \Gamma_{NM} + \Gamma_{2N}$$

$$= \Gamma_{\pi^0} + \Gamma_{\pi^-} + \Gamma_n + \Gamma_p + \Gamma_{np}$$

$\Lambda \rightarrow N\pi$
 $p_N \sim 100 \text{ MeV}$

$\Lambda N \rightarrow NN$
 $p_N \sim 420 \text{ MeV}$

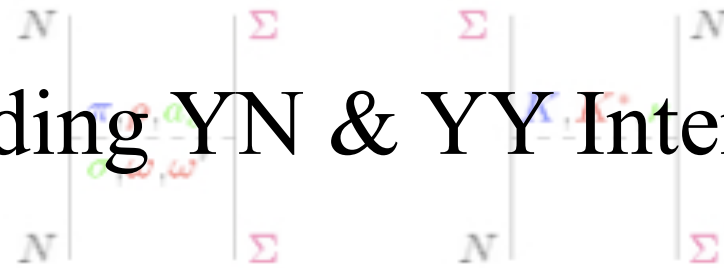
$\Lambda NN \rightarrow NNN$
 $p_N \sim 340 \text{ MeV}$



W. M. Alberico et al., Phys. Rev. C 61, 044314 (2000)

(well reproduced by theoretical models)

Building YN & YY Interactions



The YN & YY Interactions

- ✧ Study of the role of strangeness in low and medium energy nuclear physics.
- ✧ Test of $SU(3)_{\text{flavor}}$ symmetry.
- ✧ Input for Hypernuclear Physics & Astrophysics (Neutron Stars).

But due to:

- ✓ difficulties of preparation of hyperon beams.
- ✓ no hyperon targets available.
- YN: Only about 35 data points, all from the 1960's
- 10 new data points, from KEK-PS E251 collaboration (2000)
- YY: No scattering data at all

(cf. > 4000 NN data for $E_{\text{lab}} < 350$ MeV)

YN meson-exchange models

Strategy: start from a NN model & impose $SU(3)_{\text{flavor}}$ constraints

$$L = g_M \Gamma_M (\bar{\Psi}_B \Psi_B) \phi_M$$

✧ scalar: σ, δ

$$\Gamma_s = 1$$

✧ pseudoscalar: π, K, η

$$\Gamma_{ps} = i\gamma^5$$

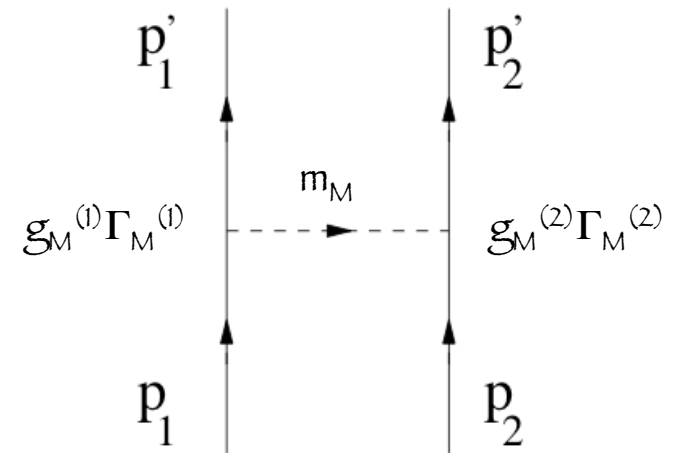
✧ vector: ρ, K, ω, ϕ

$$\Gamma_v = \gamma^\mu, \quad \Gamma_T = \sigma^{\mu\nu}$$

$$\langle p'_1 p'_2 | V_M | p_1 p_2 \rangle = \bar{u}(p'_1) g_M^{(1)} \Gamma_M^{(1)} u(p_1) \frac{P_M}{(p_1 - p'_1)^2 - m_M^2} \bar{u}(p'_2) g_M^{(2)} \Gamma_M^{(2)} u(p_2)$$



$$V(r) = V_0(r) + V_S(r)(\vec{\sigma}_1 \cdot \vec{\sigma}_2) + V_T(r)S_{12} + V_{ls}(r)(\vec{L} \times \vec{S}^+) + V_{als}(r)(\vec{L} \times \vec{S}^-)$$



The Nijmegen & Jülich models

Nijmegen

(Nagels, Rijken, de Swart, Maessen)

- ✧ Based on Nijmegen NN potential.
- ✧ Momentum & Configuration Space.
- ✧ Exchange of nonets of pseudo-scalar, vector and scalar.
- ✧ Strange vertices related by SU(3) symmetry with NN vertices.
- ✧ Gaussian Form Factors:

$$F_M(k^2) = e^{-\frac{k^2}{2\Lambda_M^2}}$$

Jülich

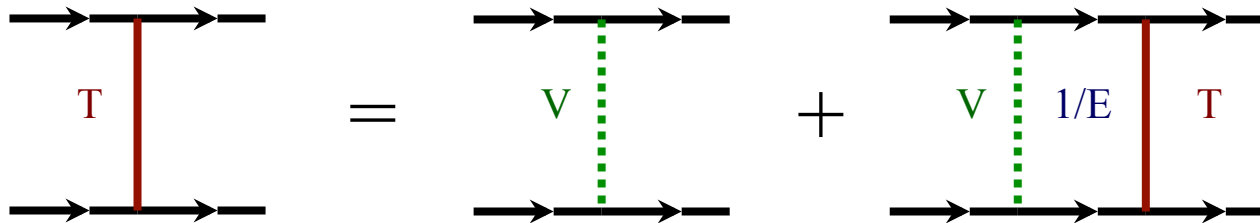
(Holzenkamp, Reube, Holinde, Speth, Haidenbauer, Meissner, Melnitchouck)

- ✧ Based on Bonn NN potential.
- ✧ Momentum Space & Full energy-dependence & non-locality structure.
- ✧ higher-order processes involving π - and ρ -exchange (correlated 2π -exchange) besides single meson exchange.
- ✧ Strange vertices related by SU(6) = SU(3)_{flavor} x SU(2)_{spin} symmetry with NN vertices.
- ✧ Dipolar Form Factors:

$$F_M(k^2) = \left(\frac{\Lambda_M^2 - m_M^2}{\Lambda_M^2 - k^2} \right)^2$$

Scattering amplitudes

Scattering amplitudes describing the hyperon-nucleon scattering are obtained by solving the **Lipmann-Schwinger equation**

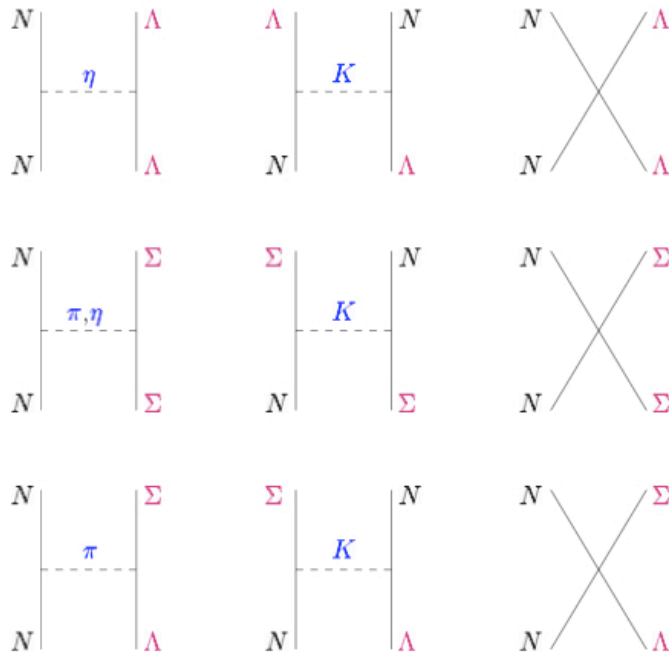


$$T = V + V \frac{1}{E} T$$

Chiral Effective Field Theory for YN

Strategy: start from a **chiral effective lagrangian** in a way similar to the NN case

Leading order (LO)



✧ Contact terms

$$L_1 = C_i^1 \langle \bar{B}_a \bar{B}_b (\Gamma_i B)_b (\Gamma_i B)_a \rangle$$

$$L_2 = C_i^2 \langle \bar{B}_a (\Gamma_i B)_a \bar{B}_b (\Gamma_i B)_b \rangle$$

$$L_3 = C_i^3 \langle \bar{B}_a (\Gamma_i B)_a \rangle \langle \bar{B}_b (\Gamma_i B)_b \rangle$$



$$V^{B_1 B_2 \rightarrow B_3 B_4} = C_S^{B_1 B_2 \rightarrow B_3 B_4} + C_T^{B_1 B_2 \rightarrow B_3 B_4} \vec{\sigma}_1 \cdot \vec{\sigma}_2$$

✧ One-pseudoscalar meson exchange

$$L = \left\langle i \bar{B} \gamma^\mu D_\mu B - M_0 \bar{B} B + \frac{D}{2} \bar{B} \gamma^\mu \gamma_5 \{u_\mu, B\} + \frac{F}{2} \bar{B} \gamma^\mu \gamma_5 [u_\mu, B] \right\rangle$$



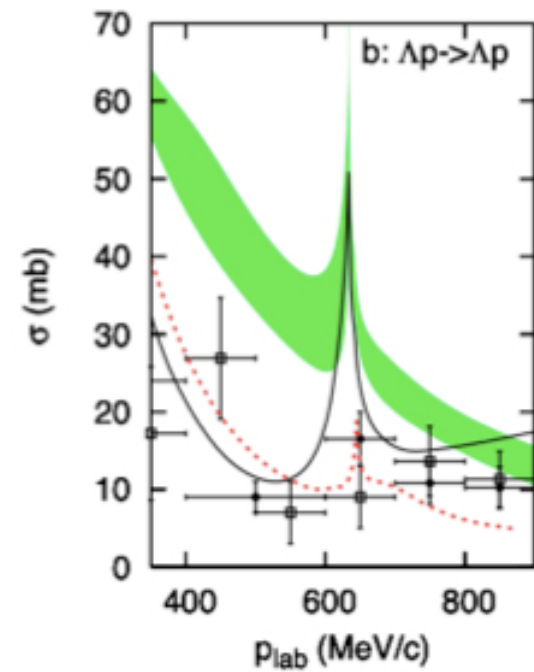
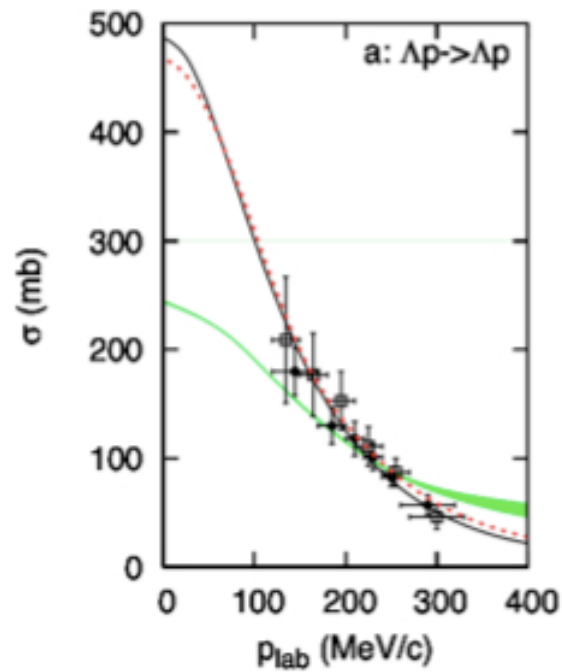
$$V^{B_1 B_2 \rightarrow B_3 B_4} = -f_{B_1 B_2 M} f_{B_3 B_4 M} \frac{(\vec{\sigma}_1 \cdot \vec{k})(\vec{\sigma}_2 \cdot \vec{k})}{k^2 + m_M^2}$$

- ✧ Lippmann-Schwinger equation cut-off with the regularized

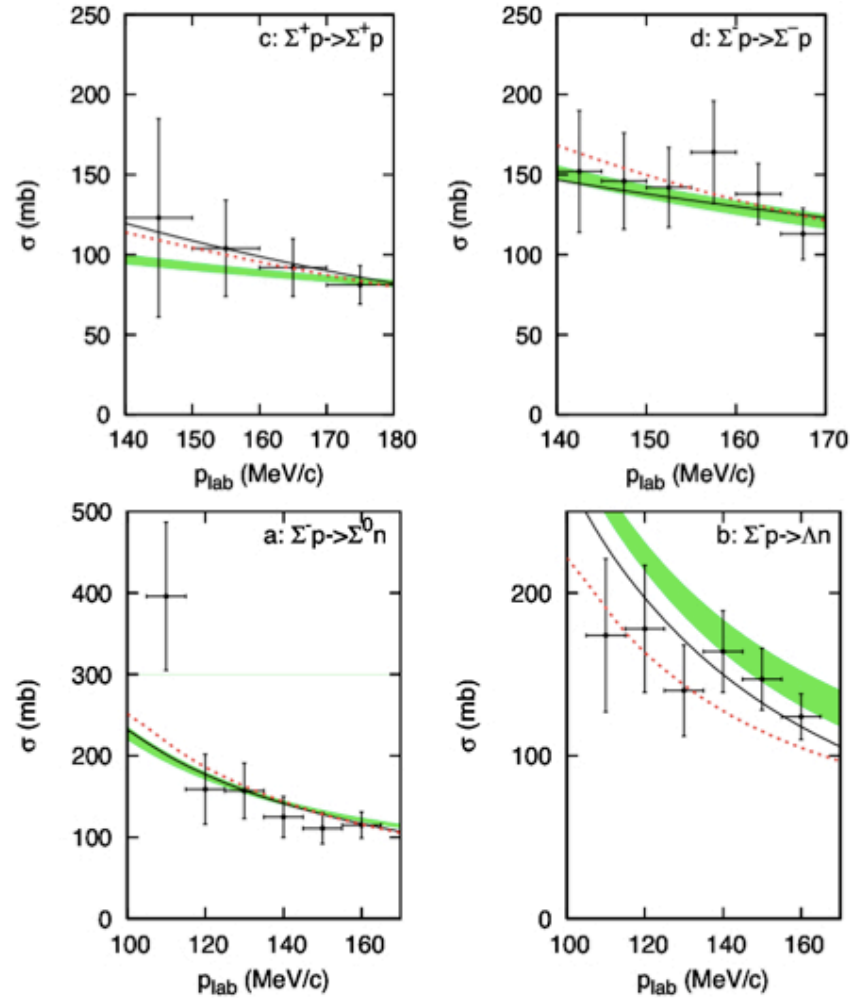
$$F(p, p', \Lambda) = e^{-\frac{(p^4 + p'^4)}{\Lambda^4}}$$

Cutoff dependence:
 $\Lambda \approx 550-700$ MeV

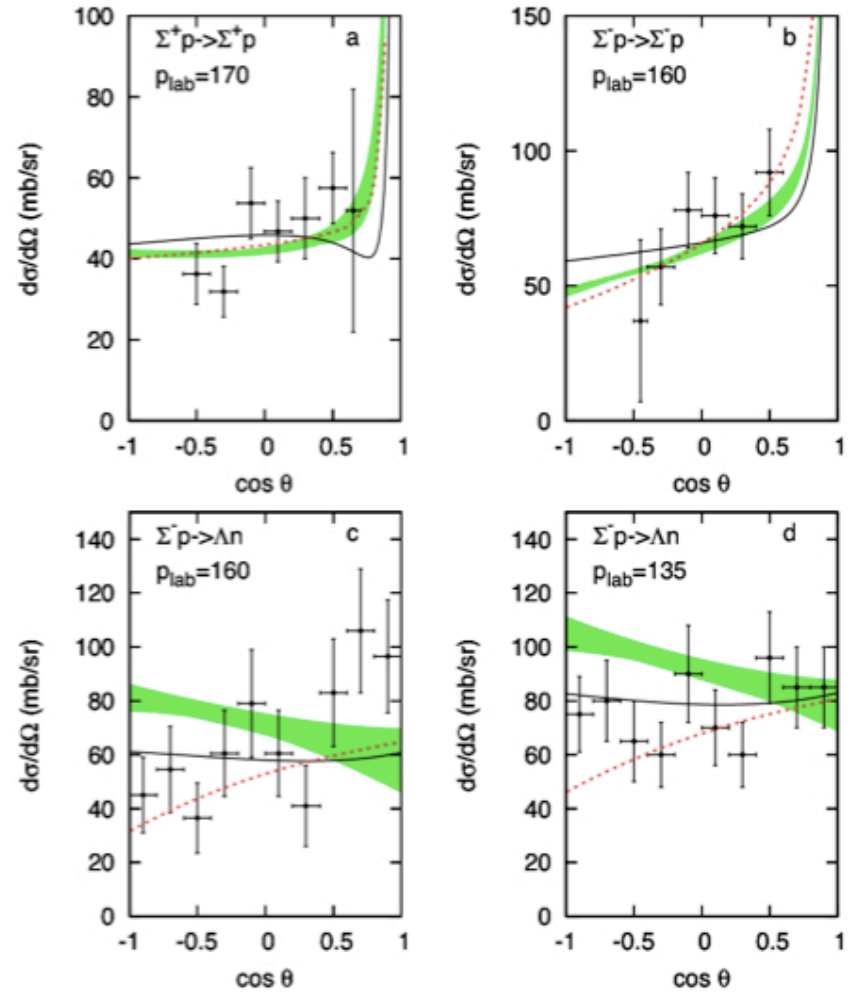
YN data rather
 well described



Total cross YN sections



Differential YN cross sections



NPA 779, 224 (2006)

Green band: EFT

Solid: NSC97f

Dashed: Jülich04

Light hypernuclei properties

✧ Hypertriton (${}^3\text{H}_\Lambda$) binding energy cutoff independent

$\Lambda=550$	$\Lambda=600$	$\Lambda=650$	$\Lambda=700$	Jülich04	NSC97f	Expt.
-2.35	-2.34	-2.34	-2.36	-2.27	-2.30	-2.354(50)

Deuteron B(${}^2\text{H}$): -2.224 MeV

✧ A=4 doublet: ${}^4\text{H}_\Lambda$ - ${}^4\text{He}_\Lambda$

${}^4\text{H}_\Lambda$	$\Lambda=550$	$\Lambda=600$	$\Lambda=650$	$\Lambda=700$	Jülich04	NSC97f	Expt.
$E_{\text{sep}}(0^+)$	2.63	2.46	2.36	2.38	1.87	1.60	2.04
$E_{\text{sep}}(1^+)$	1.85	1.51	1.23	1.04	2.34	0.54	1.00
ΔE_{sep}	0.78	0.95	1.13	1.34	-0.48	0.99	1.04

CSB- 0^+	0.01	0.02	0.02	0.03	-0.01	0.10	0.35
CSB- 1^+	-0.01	-0.01	-0.01	-0.01		-0.01	0.24

(All units are given in MeV)

Low-momentum YN interaction

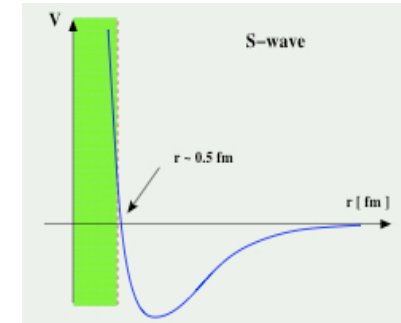
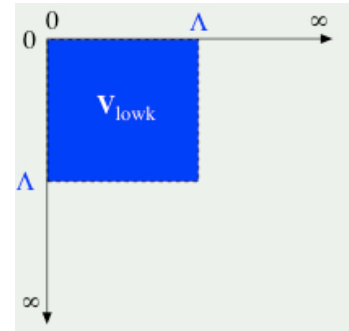
Idea: start from a realistic YN interaction & integrate out the high-momentum components in the same way as as been done for NN.



$V_{\text{low } k}$

- ✓ phase shift equivalent
- ✓ energy independent
- ✓ softer (no hard core)
- ✓ hermitian

B. -J. Schaefer et al., Phys. Rev. C 73, 011001 (2006)



Lippmann-Schwinger Equation

$$T(k',k;E_k) = V_{\text{low } k}(k',k) + \frac{2}{\pi} P \int_0^\Lambda dq q^2 V_{\text{low } k}(k',q) \frac{1}{E_k - H_0(q)} T(q,k;E_k)$$

Conditions

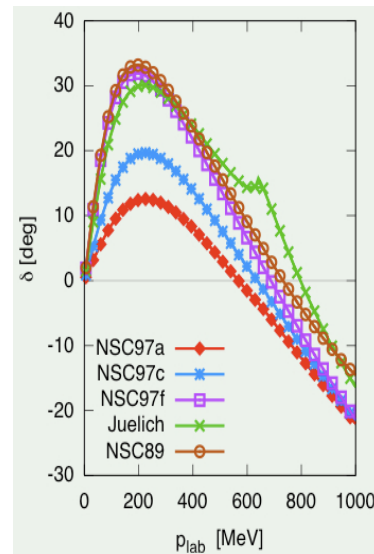
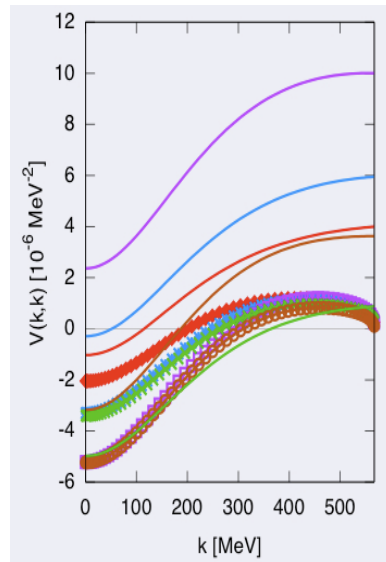
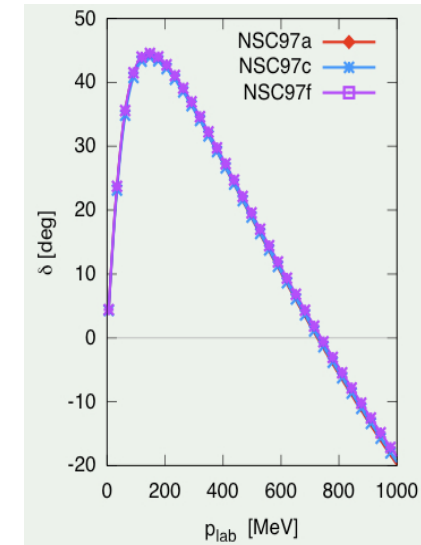
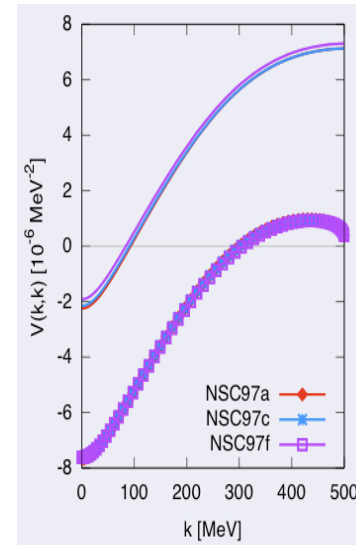
$$\frac{dT_\Lambda}{d\Lambda} = 0; \quad V_{\text{low } k} = \Lambda \quad \Lambda \rightarrow \infty : V_{\text{low } k} = V_{\text{bare}}$$

Renormalization Group Flow Equation

$$\frac{d}{d\Lambda} V_{\text{low } k}(k',k) = -\frac{2}{\pi} \frac{V_{\text{low } k}(k',\Lambda) T(\Lambda,k;\Lambda^2)}{E_k - H_0(\Lambda)}$$

1S_0 ($I=3/2$) matrix elements
and phase-shift for $\Sigma N \rightarrow \Sigma N$

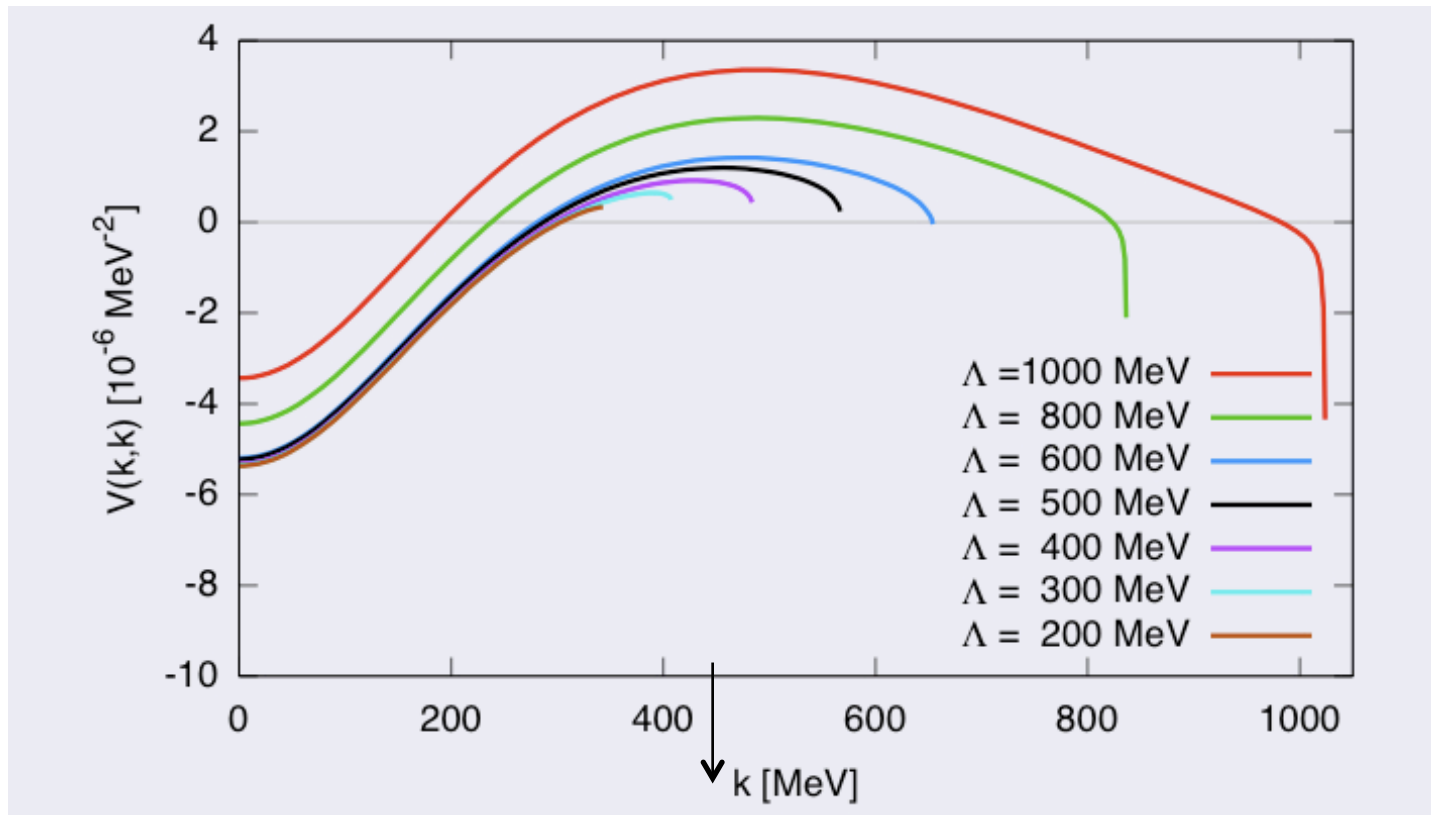
$\Lambda \approx 500$ MeV



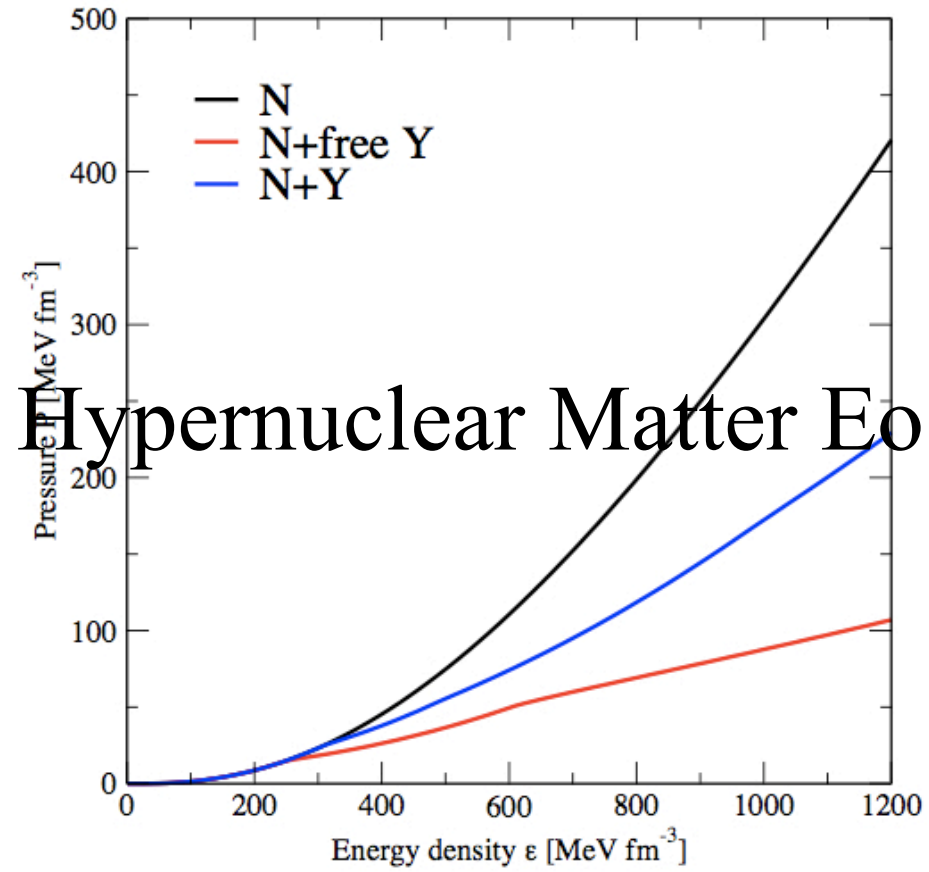
1S_0 ($I=1/2$) matrix elements
and phase-shift for $\Lambda N \rightarrow \Lambda N$

$\Lambda \approx 500$ MeV

Cut-off dependence



1S_0 ($I=1/2$) matrix elements for $\Lambda N \rightarrow \Lambda N$ (NSC97f)



Approaches to Hypernuclear Matter EoS

The Hypernuclear Matter EoS has been considered
by many authors using



Phenomenological approaches

Based on effective density-dependent interactions with parameters adjusted to reproduce nuclear and hypernuclear observables and compact star properties (e.g., Skyrme, RMF, ...)



Microscopic approaches

Based on realistic two-body baryon-baryon interactions that describe scattering data in free space. To obtain the EoS one has to “solve” the complicated many-body problem (e.g., BHF, DBHF, $V_{\text{low } k}$, ...)

Brueckner Theory for Hyperonic Matter

Consider a system of A fermions described by

$$H = \sum_{i=1}^A K_i + \sum_{i<j}^A V_{ij} \quad \longrightarrow \quad \text{Ground State} \quad H|\psi\rangle = E|\psi\rangle$$

UNSOLVABLE !!!

✧ Idea: introduce an auxiliary s. p. potential U_i

$$H = \underbrace{\sum_{i=1}^A (K_i + U_i)}_{H_0 \text{ unperturbed}} + \underbrace{\sum_{i<j}^A V_{ij} - \sum_{i=1}^A U_i}_{H_1 \text{ perturbation}}$$

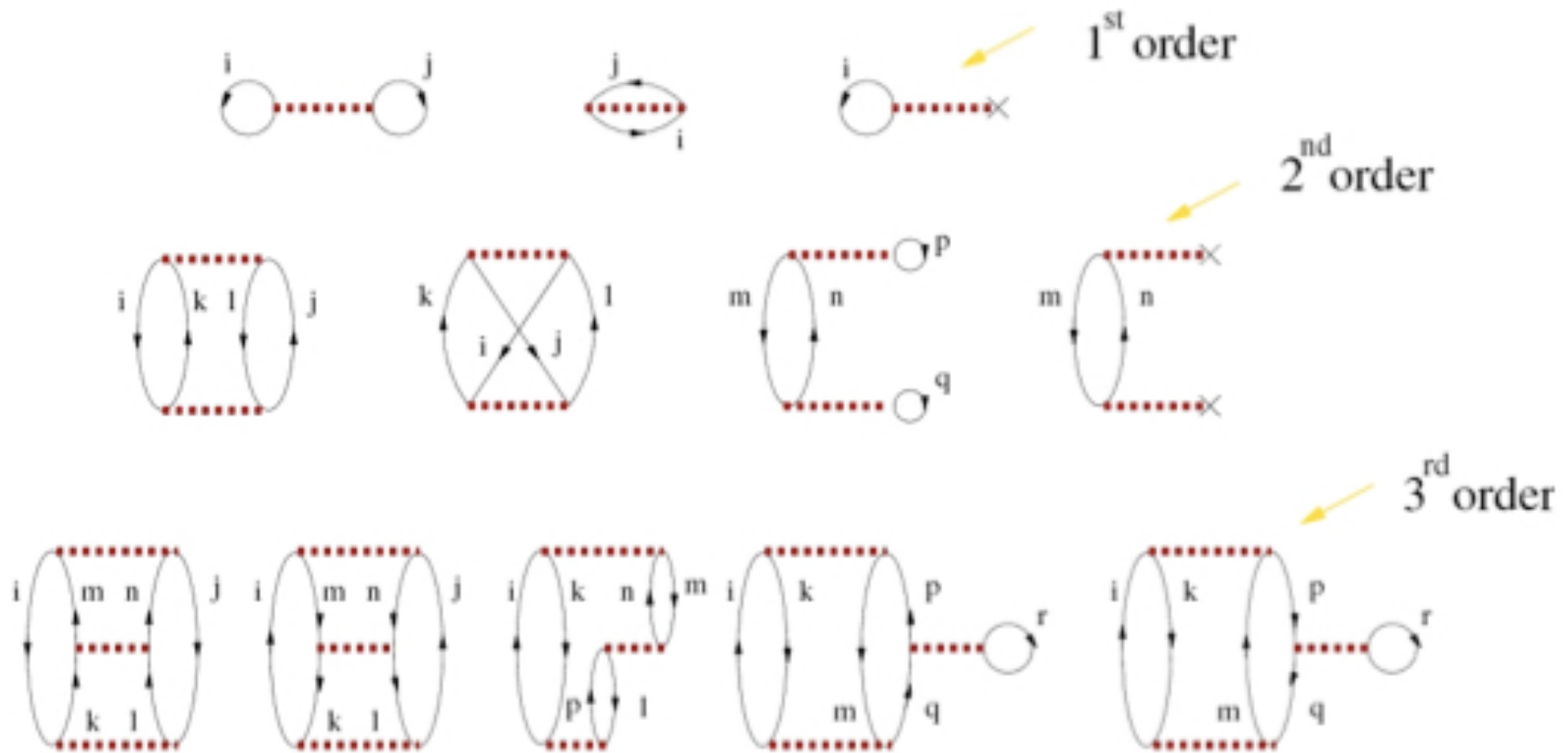
$$E = E_0 + \Delta E$$

$$H_0 |\phi_0\rangle = E_0 |\phi_0\rangle$$

$\Delta E \longrightarrow$ perturbation theory

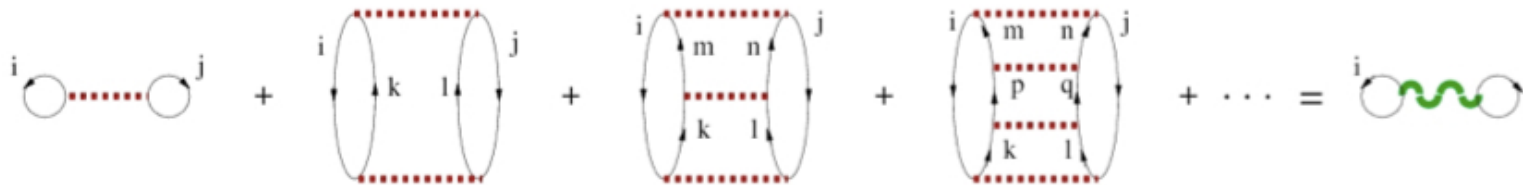
✧ Goldstone Expansion
(only linked diagrams)

$$\Delta E = \langle \phi_0 | H_1 \sum_{n=0}^{\infty} \left[\frac{1 - |\phi_0\rangle\langle\phi_0|}{E_0 - H_0} H_1 \right]^n | \phi_0 \rangle_l$$



✧ Brueckner's reaction matrix (G-matrix)

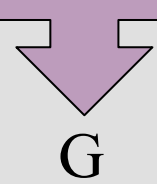
- ✓ Partial summation of the set of **pp ladder diagrams**



- ✓ G-matrix obtained by solving the **Bethe-Goldstone equation**

$$G = V + V \frac{Q}{\omega - H_0 + i\eta} V + V \frac{Q}{\omega - H_0 + i\eta} V \frac{Q}{\omega - H_0 + i\eta} V + \dots$$

$$= V + V \frac{Q}{\omega - H_0 + i\eta} \left[V + V \frac{Q}{\omega - H_0 + i\eta} V + V \frac{Q}{\omega - H_0 + i\eta} V \frac{Q}{\omega - H_0 + i\eta} V + \dots \right]$$



G

Then:

$$G = V + V \frac{Q}{\omega - H_0 + i\eta} G$$

Note that the **Bethe-Goldstone equation** is formally identical to the **Lippmann-Schwinger equation** describing the scattering of two particles in free space

$$T = V + V \frac{1}{\omega - K + i\eta} T$$



The G-matrix describes the scattering of two particles in the presence of a surrounding medium

✧ Medium Effects

➤ Pauli blocking of intermediate states

The Pauli operator Q prevents the scattering to any occupied state, limiting the phase space of intermediate states



➤ Dressing of intermediate particles

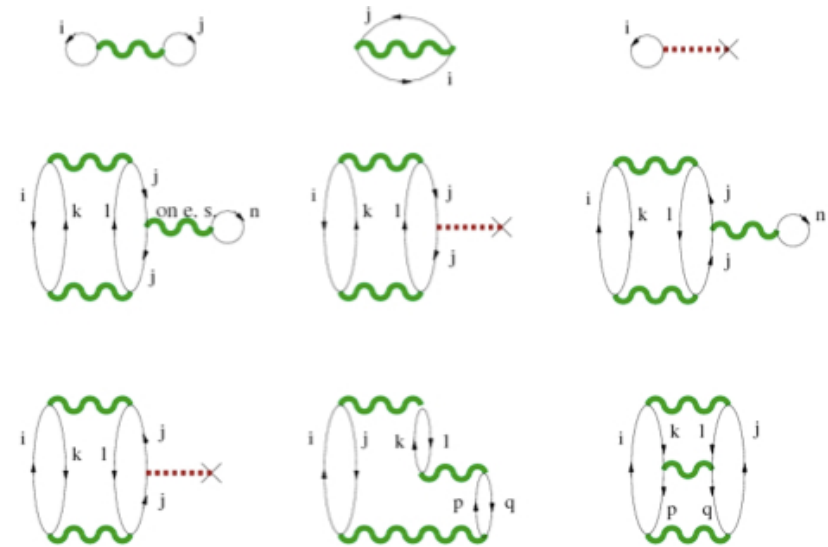
The s.p. spectrum is modified by U which represents the average potential “felt” by a particle due to the presence of the medium



✧ Hole-line expansion & the BHF approximation

Goldstone expansion in terms of G

➡ Brueckner-Goldstone expansion

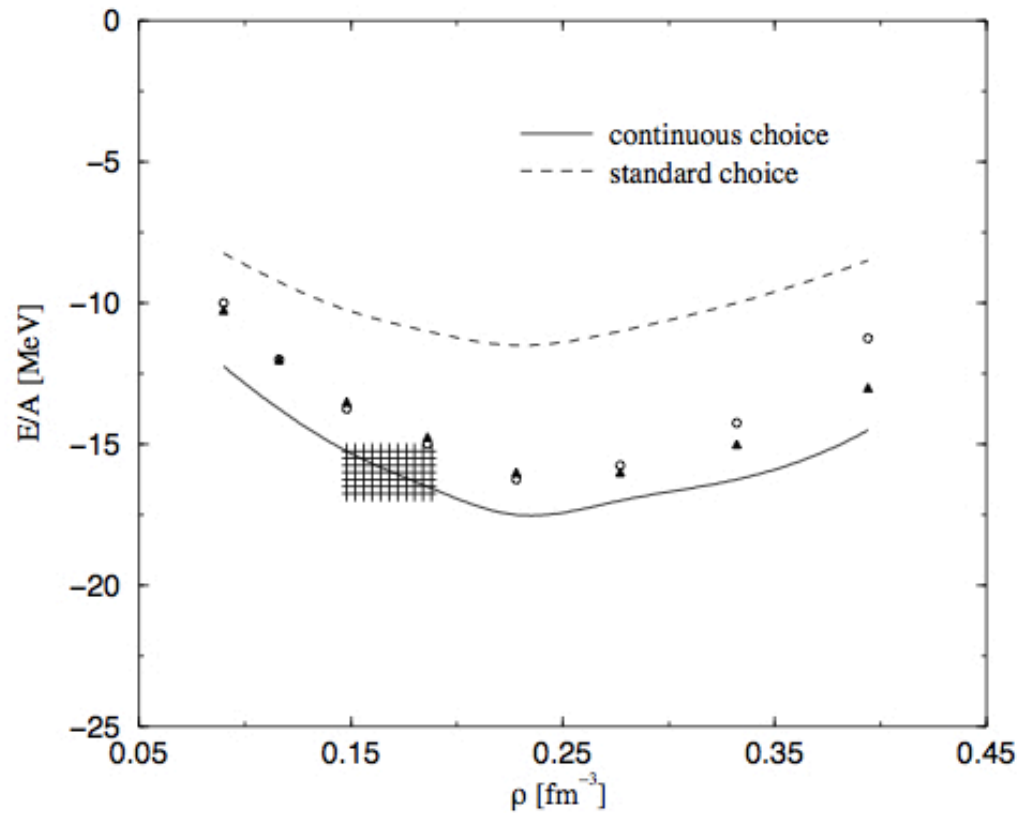


Grouping by number of hole lines ($c/r_0 < 1$) ➡ hole-line or Brueckner-Bethe-Goldstone expansion. Leading term: BHF approximation

$$E_{BHF} = \sum_{i \leq A} \langle \alpha_i | K | \alpha_i \rangle + \frac{1}{2} \text{Re} \left[\sum_{i, j \leq A} \langle \alpha_i \alpha_j | G(\omega) | \alpha_i \alpha_j \rangle \right]$$

Convergence of the hole-line expansion

Depends on the choice of the auxiliary potential



➤ Standard or Gap Choice

- $k < k_F$

$$U_B(k) = \sum_{B'} \sum_{k' \leq k_{F_{B'}}} \langle \vec{k}\vec{k}' | G(\omega = E_B(k) + E_{B'}(k')) | \vec{k}\vec{k}' \rangle$$

- $k > k_F$

$$U_B(k) = 0$$

➤ Continuous Choice

$$U_B(k) = \sum_{B'} \sum_{k' \leq k_{F_{B'}}} \langle \vec{k}\vec{k}' | G(\omega = E_B(k) + E_{B'}(k')) | \vec{k}\vec{k}' \rangle$$

H. Q. Song et al., PRL 81, 1584 (1998)

✧ Extended BHF approach: Hyperonic Matter

➤ **Bethe-Goldstone equation (coupled channels)**

- $$G(\omega)_{B_1 B_2; B_3 B_4} = V_{B_1 B_2; B_3 B_4} + \sum_{B_i B_j} V_{B_1 B_2; B_j B_k} \frac{Q_{B_i B_j}}{\omega - E_{B_i} - E_{B_j} + i\eta} G(\omega)_{B_j B_k; B_3 B_4}$$
- $$E_B(k) = \frac{\hbar^2 k^2}{2m_B} + \text{Re}[U_B(k)] + m_B$$
- $$U_B(k) = \sum_{B'} \sum_{k' \leq k_{FB'}} \langle \vec{k} \vec{k}' | G(\omega = E_B(k) + E_{B'}(k')) | \vec{k} \vec{k}' \rangle$$

➤ **Energy per particle**

- $$\frac{E}{A}(\rho, \beta) = \frac{1}{A} \sum_B \sum_{k \leq k_{FB}} \left(\frac{\hbar^2 k^2}{2m_B} + \frac{1}{2} \text{Re}[U_B(\vec{k})] + m_B \right)$$



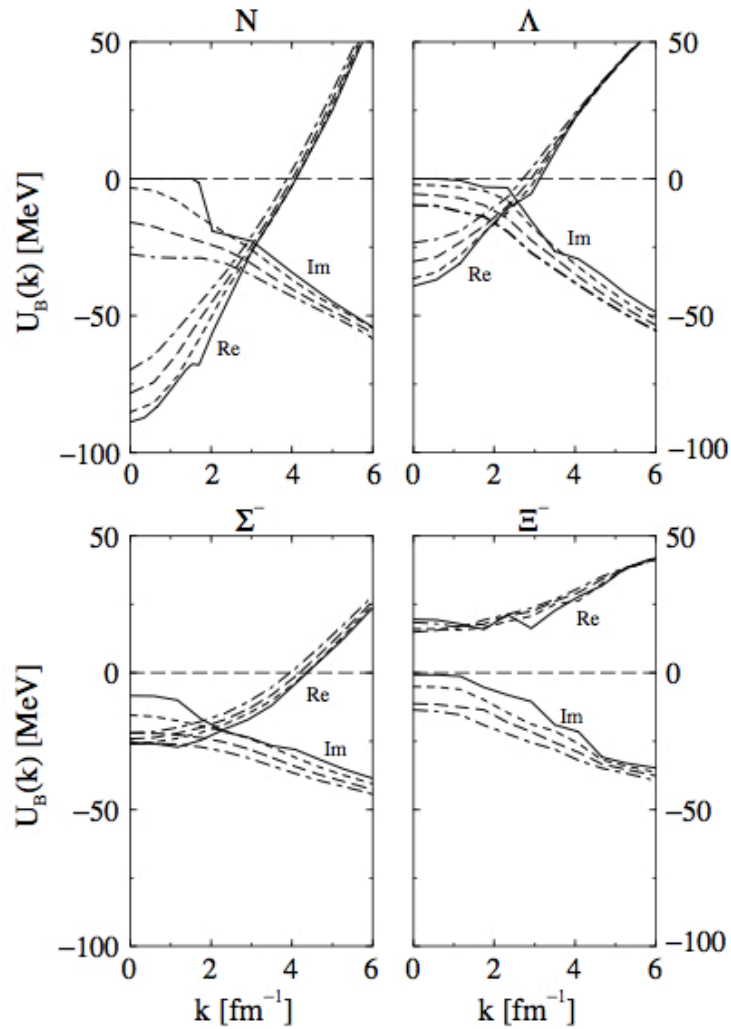
Infinite summation of **two-hole line** diagrams

✧ Coupled Channels

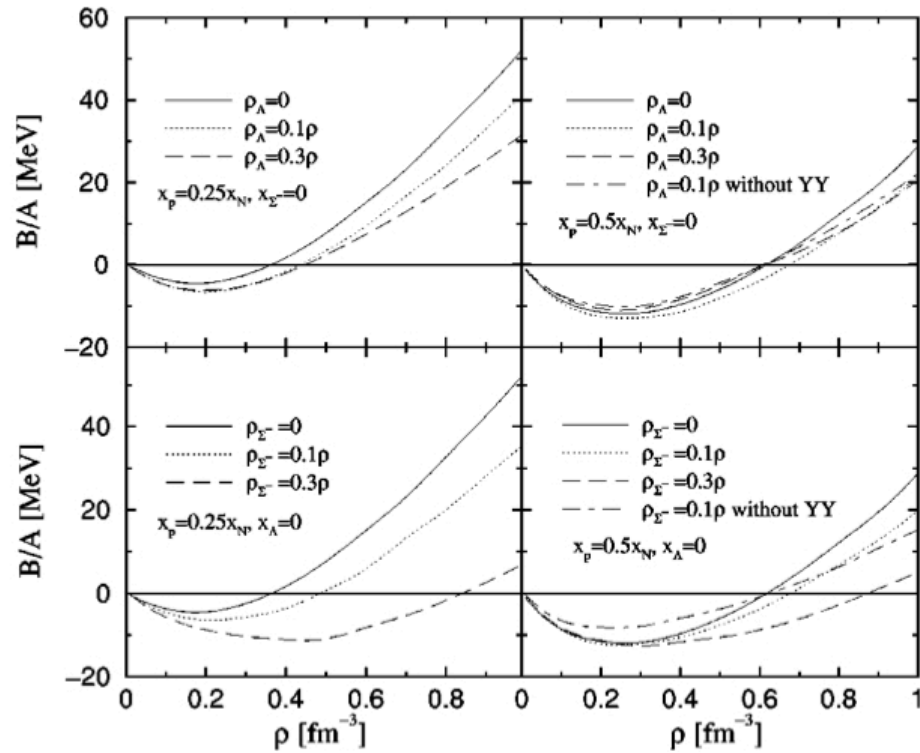
	S = 0	S = -1	S = -2	S = -3	S = -4
I = 0	(NN → NN)		$\begin{pmatrix} \Lambda\Lambda \rightarrow \Lambda\Lambda & \Lambda\Lambda \rightarrow \Xi N & \Lambda\Lambda \rightarrow \Sigma\Sigma \\ \Xi N \rightarrow \Lambda\Lambda & \Xi N \rightarrow \Xi N & \Xi N \rightarrow \Sigma\Sigma \\ \Sigma\Sigma \rightarrow \Lambda\Lambda & \Sigma\Sigma \rightarrow \Xi N & \Sigma\Sigma \rightarrow \Sigma\Sigma \end{pmatrix}$		(ΞΞ → ΞΞ)
I = 1/2		$\begin{pmatrix} \Lambda N \rightarrow \Lambda N & \Lambda N \rightarrow \Sigma N \\ \Sigma N \rightarrow \Lambda N & \Sigma N \rightarrow \Sigma N \end{pmatrix}$		$\begin{pmatrix} \Lambda\Xi \rightarrow \Lambda\Xi & \Lambda\Xi \rightarrow \Sigma\Xi \\ \Sigma\Xi \rightarrow \Lambda\Xi & \Sigma\Xi \rightarrow \Sigma\Xi \end{pmatrix}$	
I = 1	(NN → NN)		$\begin{pmatrix} \Xi N \rightarrow \Xi N & \Xi N \rightarrow \Lambda\Sigma & \Xi N \rightarrow \Sigma\Sigma \\ \Lambda\Sigma \rightarrow \Xi N & \Lambda\Sigma \rightarrow \Lambda\Sigma & \Lambda\Sigma \rightarrow \Sigma\Sigma \\ \Sigma\Sigma \rightarrow \Xi N & \Sigma\Sigma \rightarrow \Lambda\Sigma & \Sigma\Sigma \rightarrow \Sigma\Sigma \end{pmatrix}$		(ΞΞ → ΞΞ)
I = 3/2		(ΣN → ΣN)		(ΣΞ → ΣΞ)	
I = 2			(ΣΣ → ΣΣ)		

Hyperons in Nuclear Matter

s.p. potentials



binding energy



BHF calculation with **NSC97**



Hyperons & Neutron Star Properties

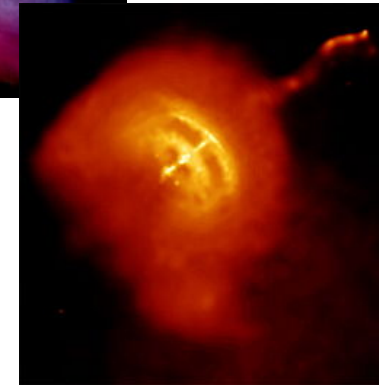
Some known facts about Neutron Stars

- Mass: $M \sim 1 - 2 M_{\odot}$
- Radius: $R \sim 10 - 12 \text{ km}$ (or less ?)
- Density: $\rho \sim 10^{14} - 10^{15} \text{ g/cm}^3$

$$\rho_{\text{universe}} \sim 10^{-30} \text{ g/cm}^3$$

$$\rho_{\text{sun}} \sim 1.4 \text{ g/cm}^3$$

$$\rho_{\text{earth}} \sim 5.5 \text{ g/cm}^3$$



- Firenze

$$M_{\text{Firenze}} \sim (3.65 \times 10^5) \times 75 \text{ kg}$$

$$\sim 1.37 \times 10^{-23} M_{\odot}$$

$$A_{\text{Firenze}} \sim 102 \text{ km}^2, \quad H_{\text{Fiorentini}} \sim 1.75 \text{ m}$$

$$\pi R_{\text{NS}}^2 \sim 300 \text{ km}^2$$

$$\rho_{\text{Fiorentini}} \sim 1.55 \times 10^{-4} \text{ g/cm}^3$$

- Baryonic number: $N_b \sim 10^{57}$ (“giant (hyper)nuclei”)
- Magnetic field: $B \sim 10^{8...16} \text{ G}$ ($10^{4...12} \text{ T}$)

$0.3 - 0.5 \text{ G}$



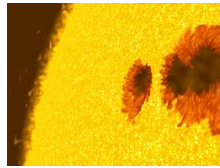
Earth

$10^3 - 10^4 \text{ G}$



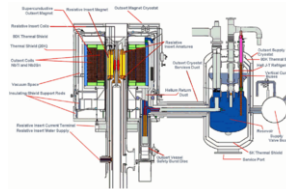
Magnet

10^5 G



Sunspots

$4.5 \times 10^5 \text{ G}$



Largest continuous field in lab. (FSU, USA)

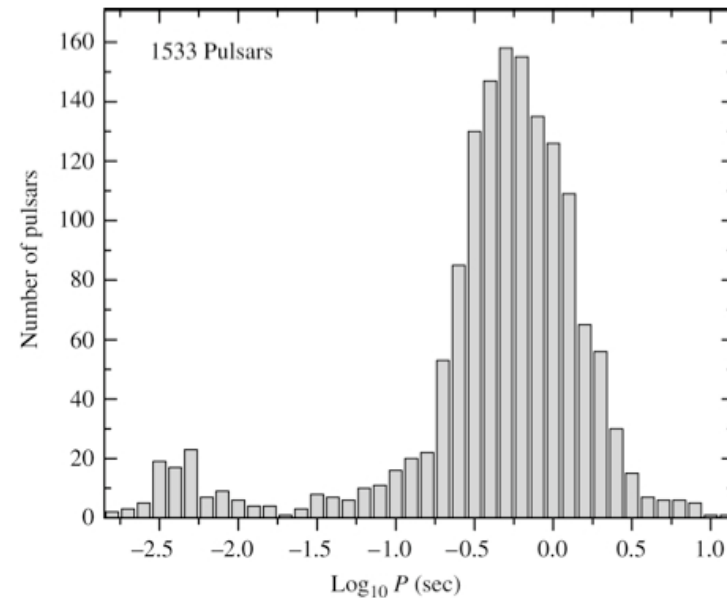
$2.8 \times 10^7 \text{ G}$



Largest magnetic pulse in lab. (Russia)

- Electric field: $E \sim 10^{18} \text{ V/cm}$
- Temperature: $T \sim 10^{6...11} \text{ K}$
- Rotational period distribution
 → two types of pulsars:

- pulsars with $P \sim \text{s}$
- pulsars with $P \sim \text{ms}$

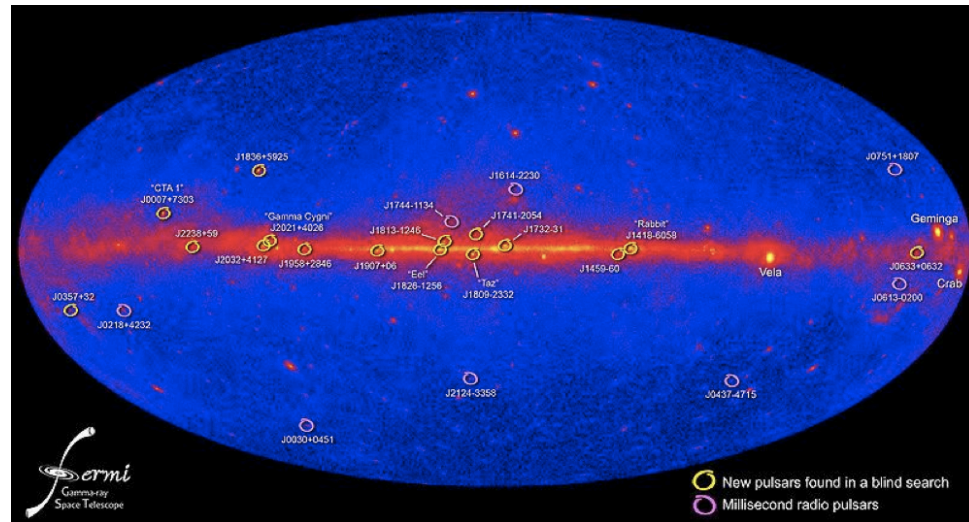


Shortest rotational period PSR in Terzan 5: $P_{\text{J1748-2446ad}} = 1.39 \text{ ms}$

Most NS are observed as pulsars. Nowadays more than 2000 pulsars are known

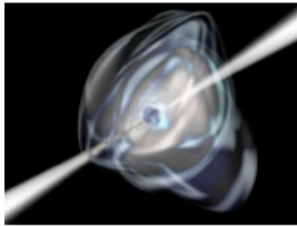
Observables

- Period (P , dP/dt)
- Masses
- Luminosity
- Temperature
- Magnetic Field
- Gravitational Waves (future)

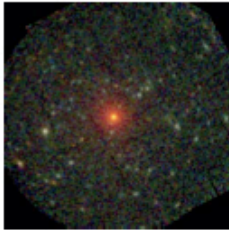


http://www.phys.ncku.edu.tw/~astrolab/mirrors/apod_e/ap090709.html

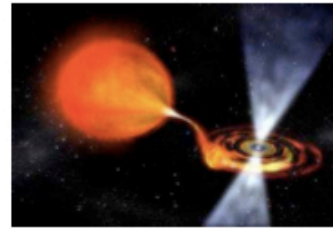
The 1001 Astrophysical Faces of Neutron Stars



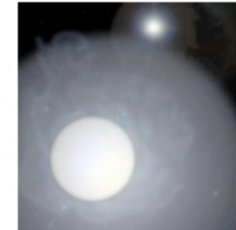
Anomalous X-ray Pulsars



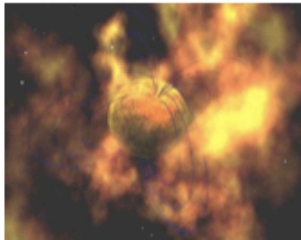
*dim isolated
neutron stars*



X-ray binaries



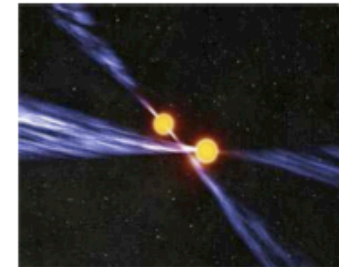
bursting pulsars



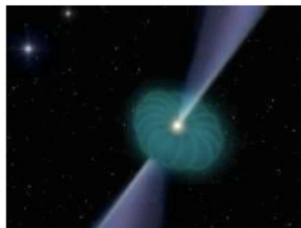
Soft Gamma Repeaters



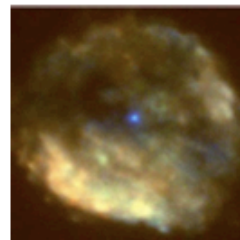
pulsars



binary pulsars



Rotating Radio Transients



Compact Central Objects



planets around pulsar

Observation of Neutron Stars

X- and γ -ray telescopes



Chandra

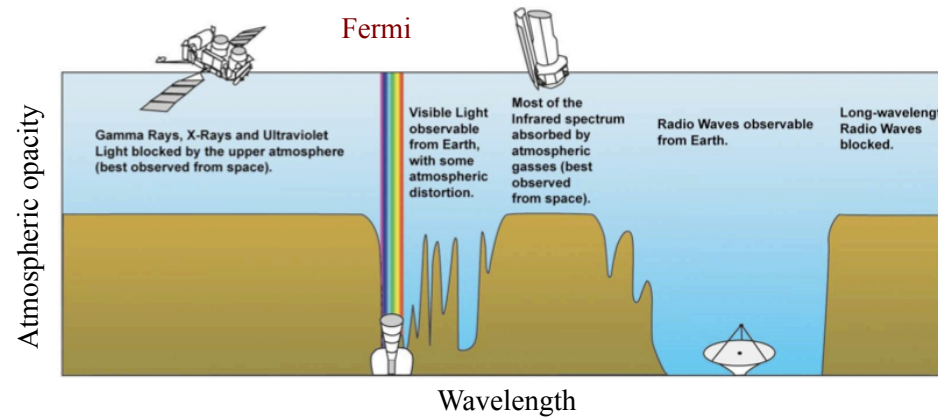


Fermi

Space telescopes



HST (Hubble)



Optical telescopes



VLT (Atacama, Chile)



Arecibo (Puerto Rico): 305 m



Green Banks (USA): 100 m



Nançay (France): 94 m

How to Measure Neutron Star Masses

Use Doppler variations in spin period to measure orbital velocity changes along the line-of-sight

- 5 Keplerian parameters can normally be determined:

$P, a \sin i, \epsilon, T_0$ & ω

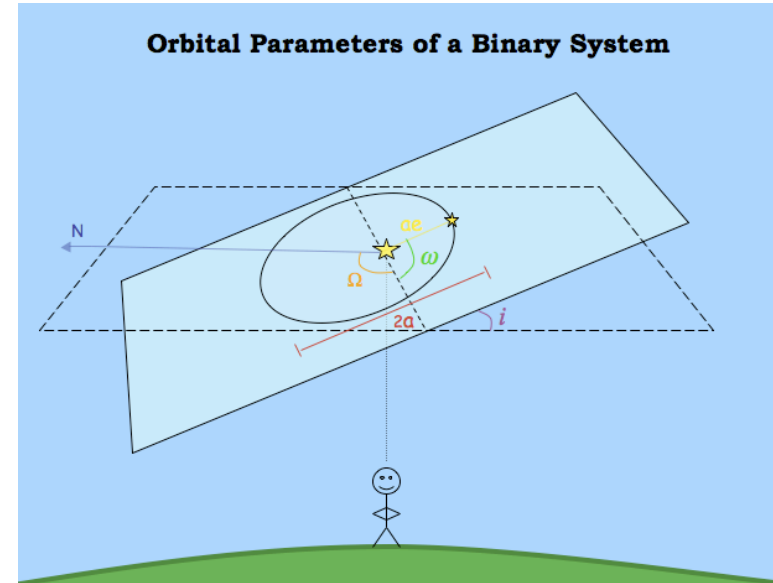
- 3 unknowns: M_1, M_2, i

Kepler's 3rd law

$$\frac{G(M_1 + M_2)}{a^3} = \left(\frac{2\pi}{P}\right)^2 \rightarrow$$

$$f(M_1, M_2, i) \equiv \frac{(M_2 \sin i)^3}{(M_1 + M_2)^2} = \frac{Pv^3}{2\pi G}$$

mass function



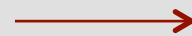
In few cases small deviations from Keplerian orbit due to GR effects can be detected

Measure of at least 2 post-Keplerian parameters



High precision NS mass determination

$$\dot{\omega} = 3T_{\otimes}^{2/3} \left(\frac{P_b}{2\pi} \right)^{-5/3} \frac{1}{1-\varepsilon} (M_p + M_c)^{2/3}$$



Periastron precession

$$\gamma = T_{\otimes}^{2/3} \left(\frac{P_b}{2\pi} \right)^{1/3} \varepsilon \frac{M_c (M_p + 2M_c)}{(M_p + M_c)^{4/3}}$$



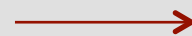
Time dilation and grav. redshift

$$r = T_{\otimes} M_c$$



Shapiro delay “range”

$$s = \sin i = T_{\otimes}^{-1/3} \left(\frac{P_b}{2\pi} \right)^{-2/3} x \frac{(M_p + M_c)^{2/3}}{M_c}$$



Shapiro delay “shape”

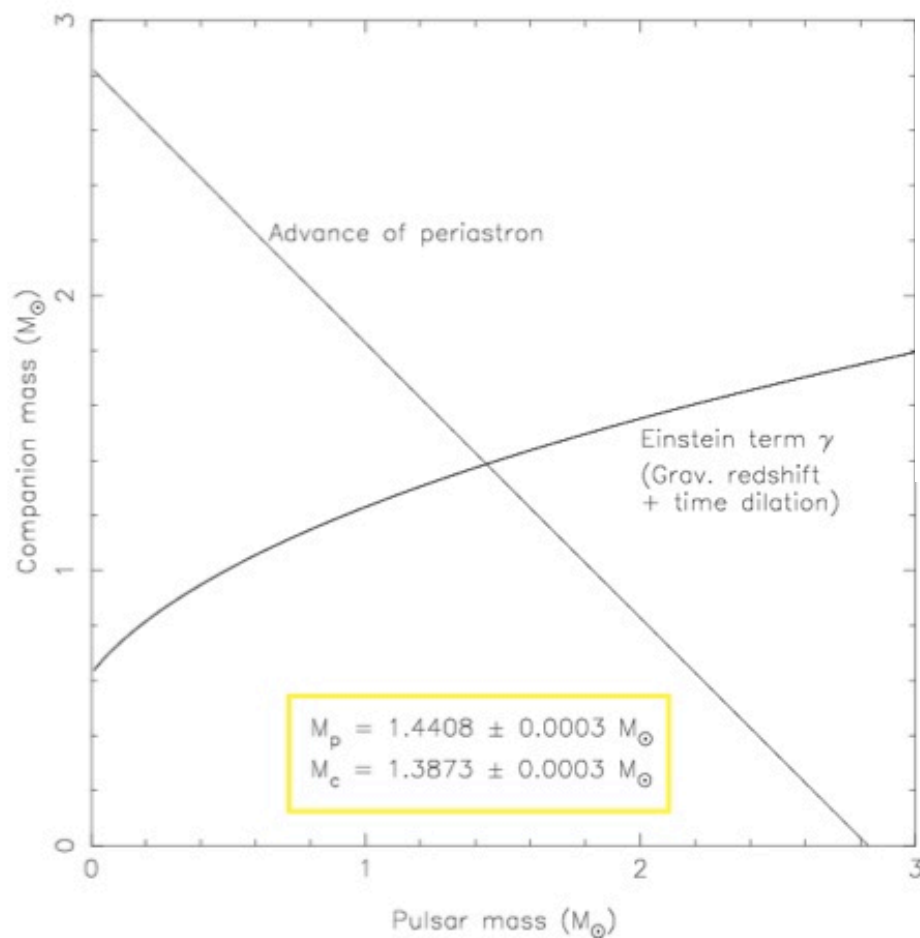
$$\dot{P}_b = -\frac{192\pi}{5} T_{\otimes}^{5/3} \left(\frac{P_b}{2\pi} \right)^{-5/3} f(\varepsilon) \frac{M_p M_c}{(M_p + M_c)^{1/3}}$$



Orbit decay due to GW emission



An example: the mass of the Hulse-Taylor pulsar (PSR J1913+16)

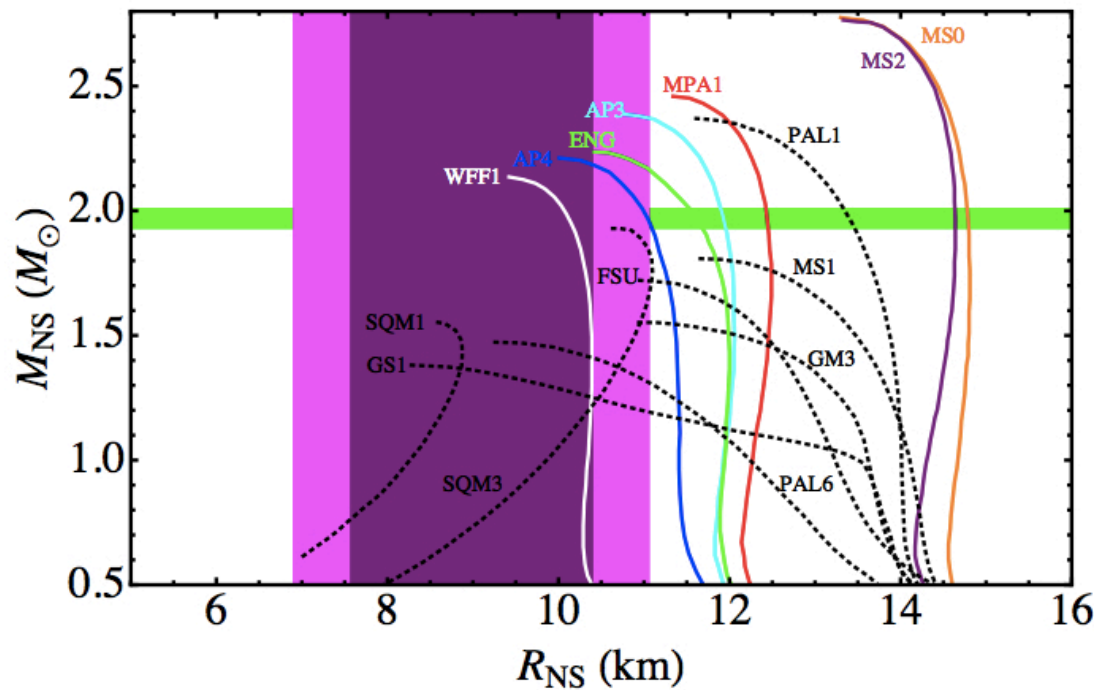


Parameter	Value
Orbital period P_b (d)	0.322997462727(5)
Projected semi-major axis x (s)	2.341774(1)
<u>Eccentricity e</u>	<u>0.6171338(4)</u>
Longitude of periastron ω (deg)	226.57518(4)
Epoch of periastron T_0 (MJD)	46443.99588317(3)
Advance of periastron $\dot{\omega}$ (deg yr $^{-1}$)	4.226607(7)
Gravitational redshift γ (ms)	4.294(1)
Orbital period derivative $(\dot{P}_b)^{\text{obs}}$ (10^{-12})	-2.4211(14)



Neutron Star Radii Measurements

Not much to say after the excellent seminar by Sebastien Guillot yesterday



Analysis of thermal spectrum of 5 quiescent LMXB in globular clusters, assuming that all NS have the same radius

$$R = 9.1^{+1.3}_{-1.5} \text{ km}$$

Guillot et al., 2013:

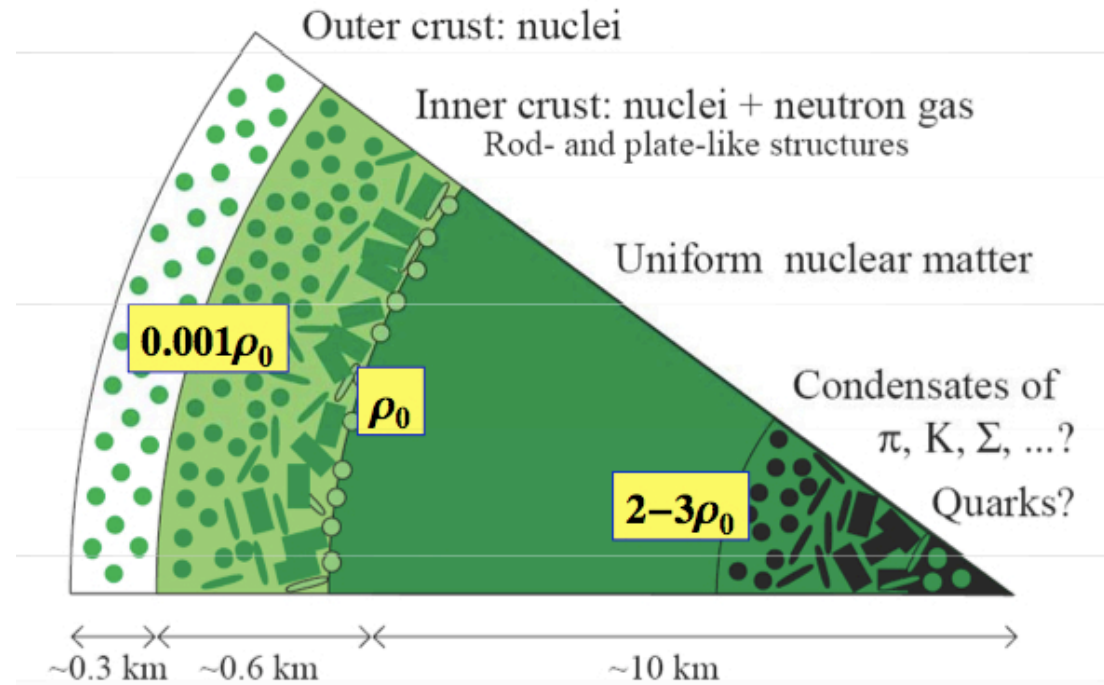
Anatomy of a Neutron Star

Equilibrium composition
determined by

- ✓ Charge neutrality

$$\sum_i q_i \rho_i = 0$$

- ✓ Equilibrium with respect to weak interacting processes



$$\begin{array}{l}
 b_1 \rightarrow b_2 + l + \bar{\nu}_l \\
 b_2 + l \rightarrow b_1 + \nu_l
 \end{array}
 \longrightarrow
 \mu_i = b_i \mu_n - q_i (\mu_e - \mu_{\nu_e}), \quad \mu_i = \frac{\partial \varepsilon}{\partial \rho_i}$$

Hyperons in Neutron Stars

Hyperons in NS considered by many authors since the pioneering work of Ambartsumyan & Saakyan (1960)



Phenomenological approaches

- ✧ **Relativistic Mean Field Models:** Glendenning 1985; Knorren et al. 1995; Shaffner-Bielich & Mishustin 1996, Bonano & Sedrakian 2012, ...
- ✧ **Non-relativistic potential model:** Balberg & Gal 1997
- ✧ **Quark-meson coupling model:** Pal et al. 1999, ...
- ✧ **Chiral Effective Lagrangians:** Hanauske et al., 2000
- ✧ **Density dependent hadron field models:** Hofmann, Keil & Lenske 2001



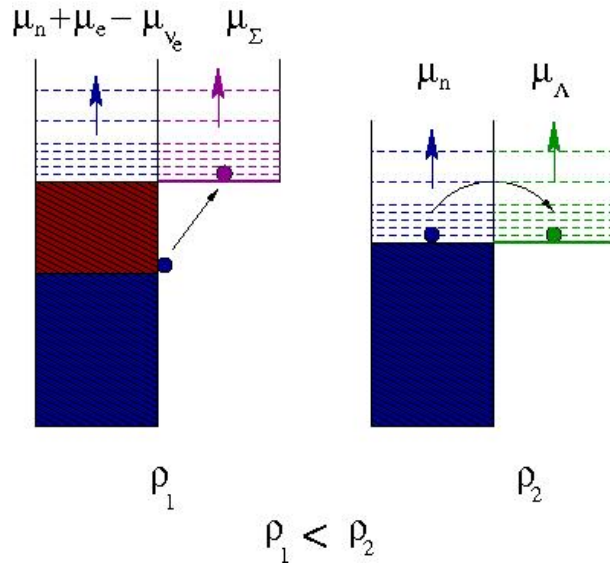
Microscopic approaches

- ✧ **Brueckner-Hartree-Fock theory:** Baldo et al. 2000; I. V. et al. 2000, Schulze et al. 2006, I.V. et al. 2011, Burgio et al. 2011, Schulze & Rijken 2011
- ✧ **$V_{\text{low } k}$:** Djapo, Schaefer & Wambach, 2010



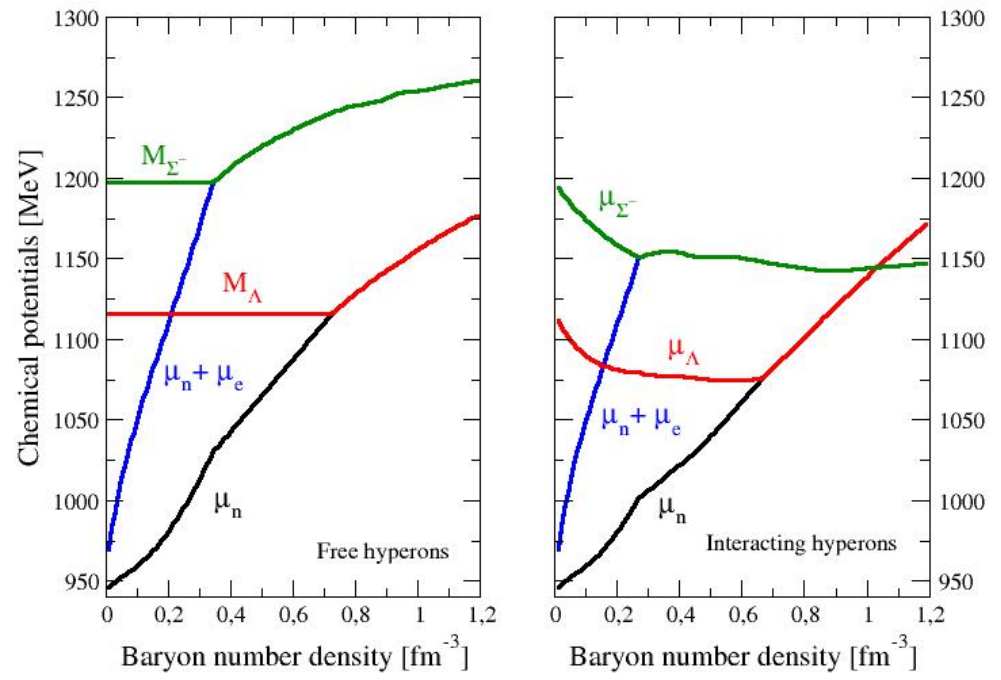
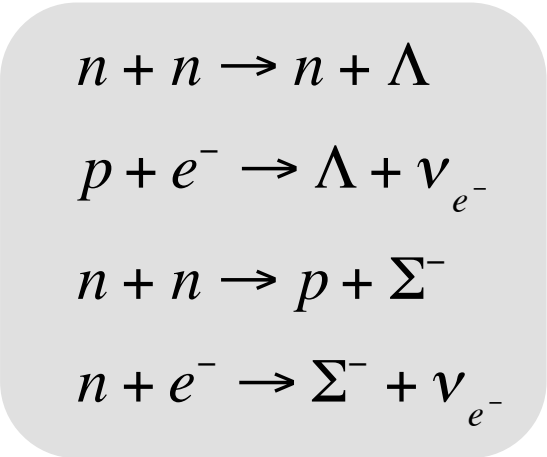
Sorry if I missed somebody

Hyperons are expected to appear in the core of neutron stars at $\rho \sim (2-3)\rho_0$ when μ_N is large enough to make the conversion of N into Y energetically favorable.



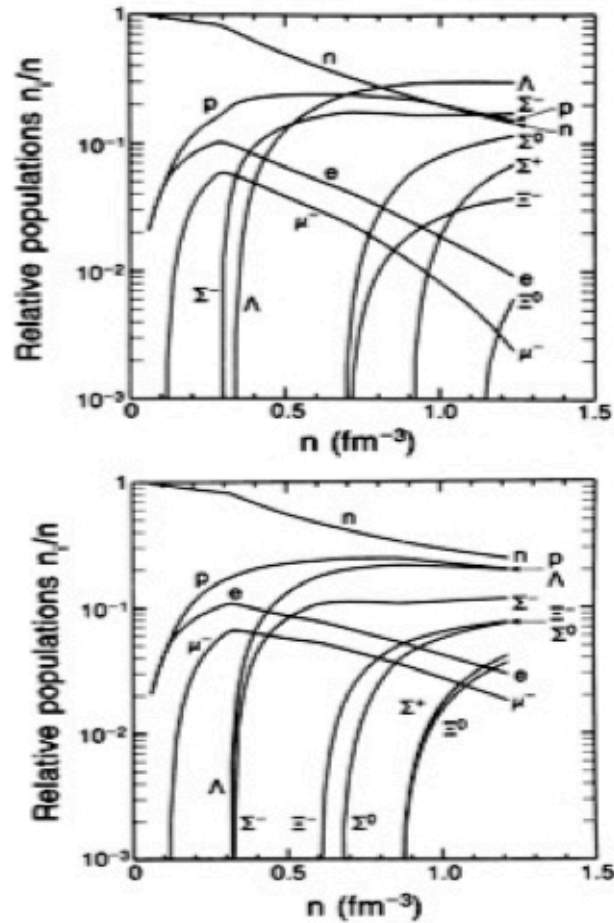
$$\mu_{\Sigma^-} = \mu_n + \mu_{e^-} - \mu_{\nu_{e^-}}$$

$$\mu_{\Lambda} = \mu_n$$

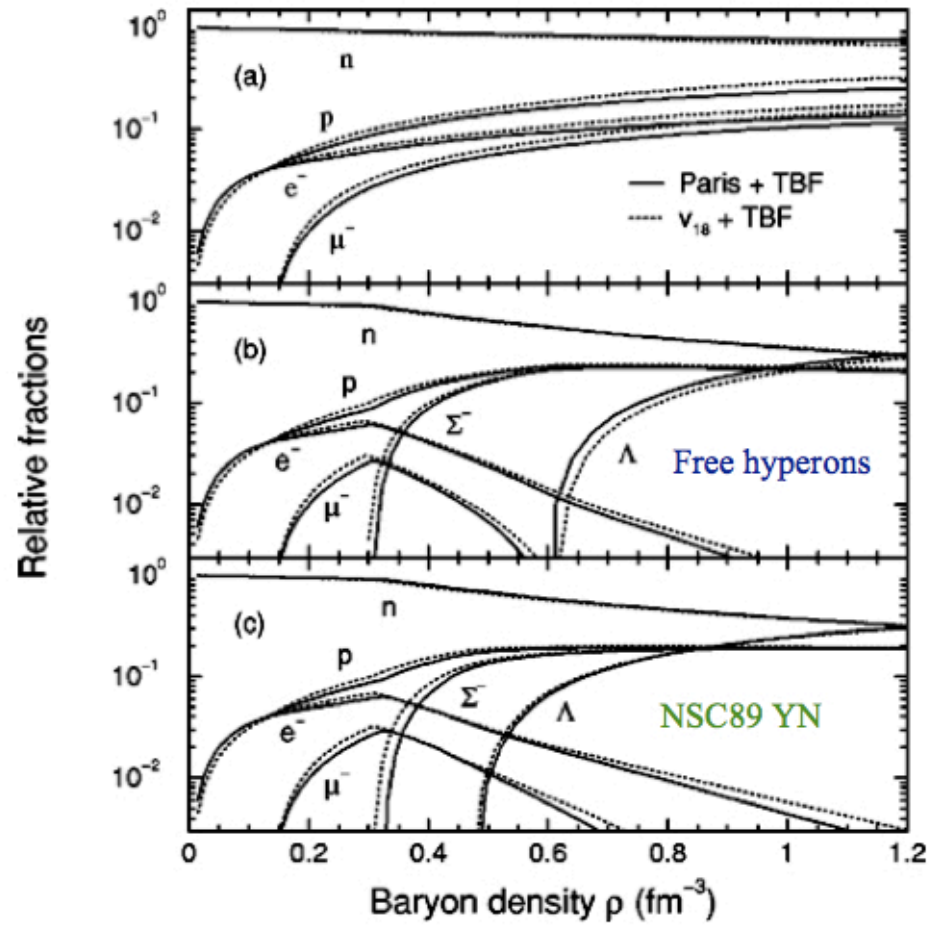


Neutron Star Matter Composition

RMFT



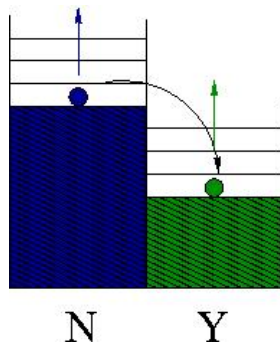
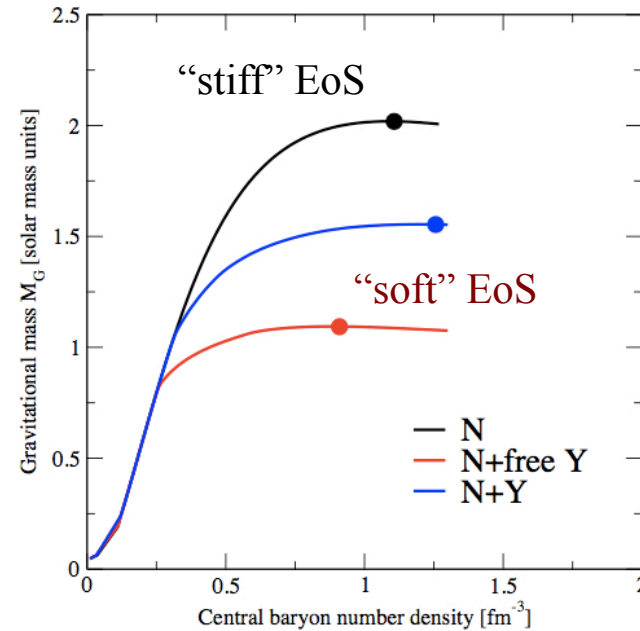
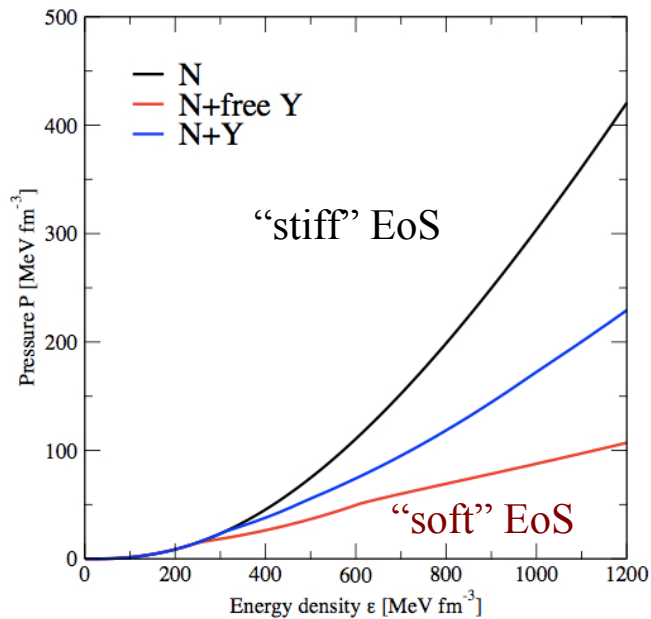
BHF



N. K. Glendenning, APJ 293, 470 (1985)

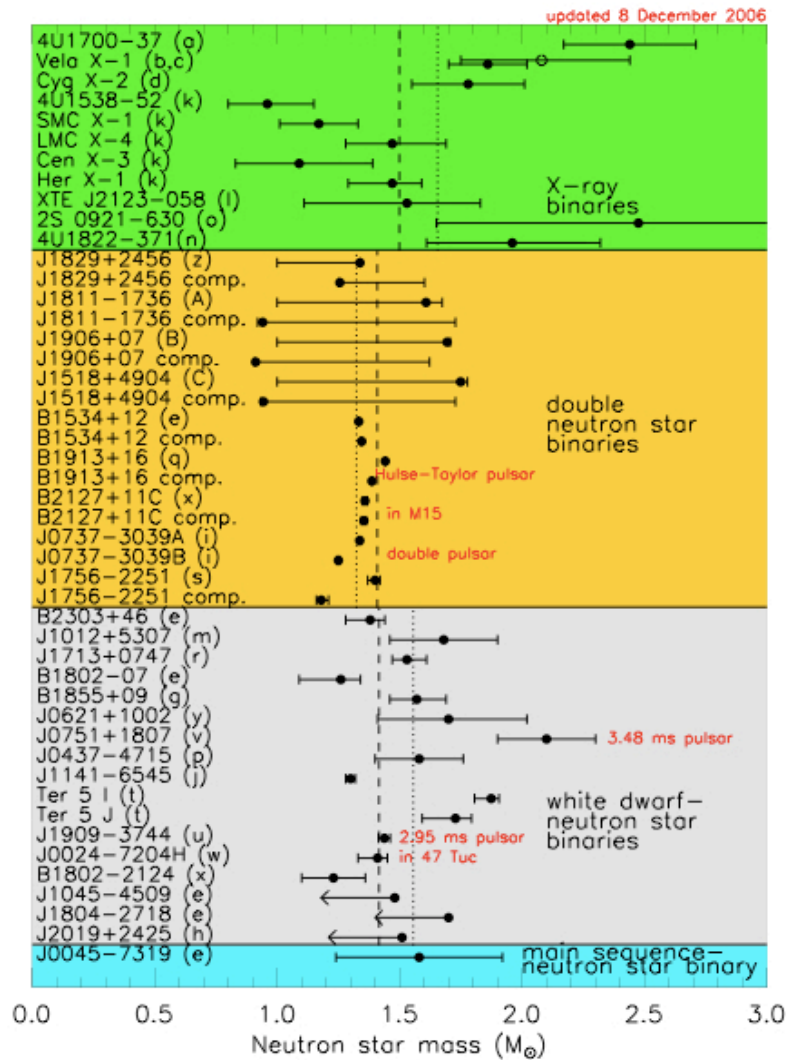
M. Baldo et al., PRC 61, 055801 (2000)

Effect of Hyperons in the EoS and Mass of Neutron Stars

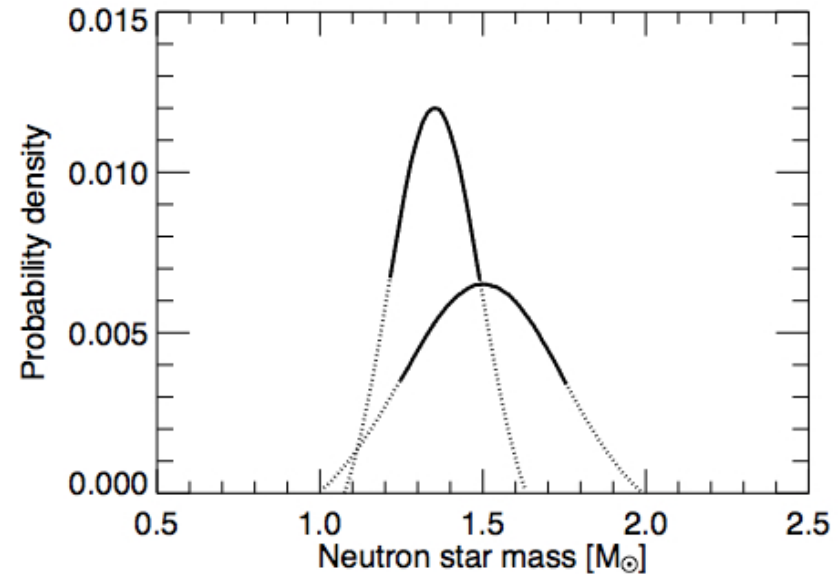


Relieve of Fermi pressure due to the appearance of hyperons →
EoS softer → reduction of the mass

Measured Neutron Star Masses (up to ~ 2006-2008)



(Lattimer & Prakash 2007)

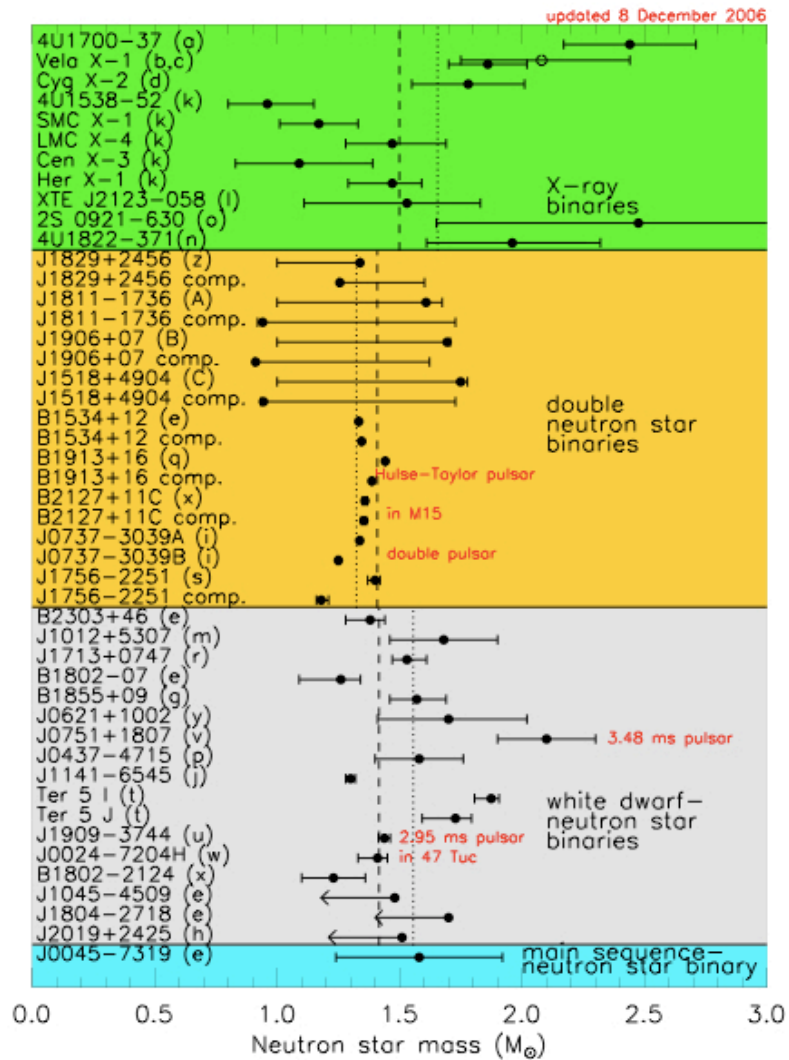


up to ~ 2006-2008 any valid
 EoS should predict

$$M_{\max} [EoS] > 1.4 - 1.5 M_{\odot}$$

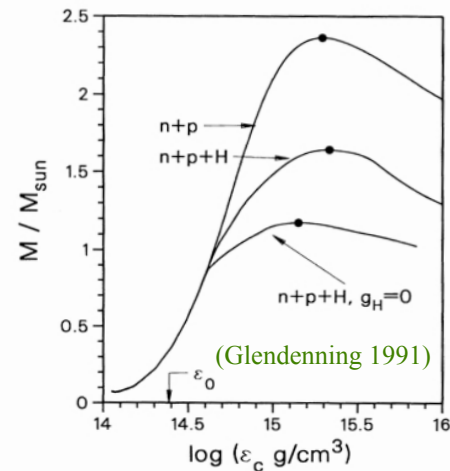
Hyperons in NS

(up to ~ 2006-2008)

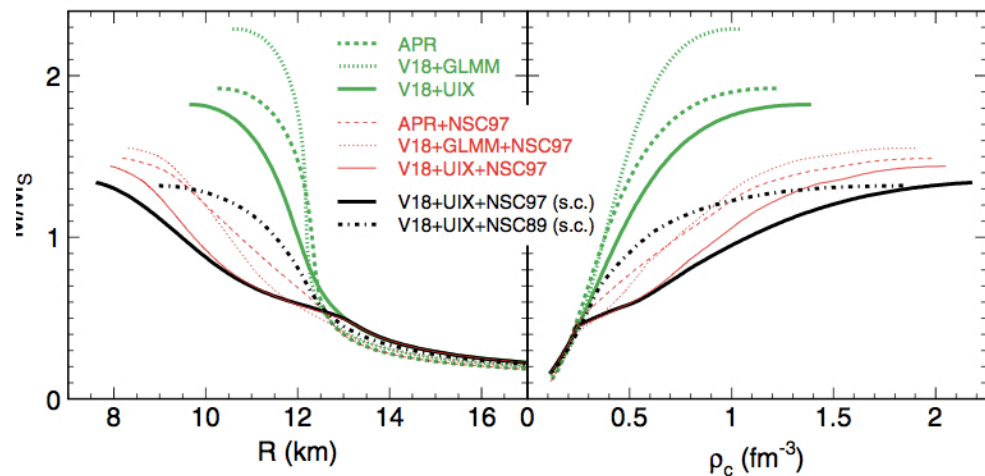


(Lattimer & Prakash 2007)

Phenomenological:
 M_{\max} compatible with 1.4-1.5 M_{\odot}



Microscopic : $M_{\max} < 1.4-1.5 M_{\odot}$



(Schulze, Polls, Ramos & IV 2006)

Recent measurements of high masses → life of hyperons more difficult

Eccentric Binary Millisecond Pulsars

Paulo C. C. Freire

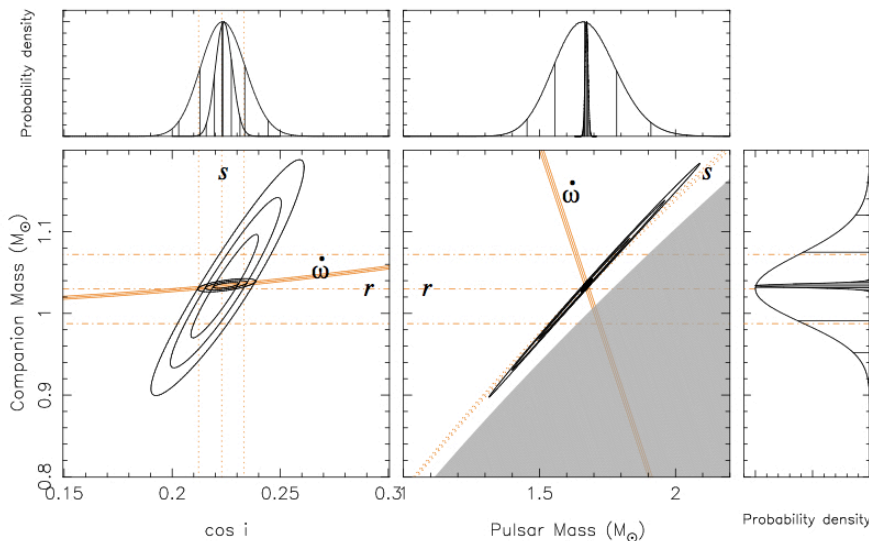
*Arecibo Observatory, HC 3 Box 53995, Arecibo PR 00612, USA
West Virginia University, PO Box 6315, Morgantown WV 26505, USA*

Abstract. In this paper we review recent discovery of millisecond pulsars (MSPs) in eccentric binary systems. Timing these MSPs we were able to estimate (and in one case precisely measure) their masses. These results suggest that, as a class, MSPs have a much wider range of masses (1.3 to $> 2M_{\odot}$) than the normal and mildly recycled pulsars found in double neutron star (DNS) systems ($1.25 < M_p < 1.44M_{\odot}$). This is very likely to be due to the prolonged accretion episode that is thought to be required to form a MSP. The likely existence of massive MSPs makes them a powerful probe for understanding the behavior of matter at densities larger than that of the atomic nucleus; in particular, the precise measurement of the mass of PSR J1903+0327 ($1.67 \pm 0.01M_{\odot}$) excludes several "soft" equations of state for dense matter.

Keywords: Neutron Stars, Pulsars, Binary Pulsars, General Relativity, Nuclear Equation of State

PACS: 97.60.Gb; 97.60.Jd; 97.80.Fk; 95.30.Sf; 26.60; 91.60.Fe

The precise measurement of the mass of PSR J1903+0328 ($1.67 \pm 0.01 M_{\text{sun}}$) excludes several "soft" EoS for dense matter



- ✓ binary system (P=95.17 d)
- ✓ high eccentricity ($\epsilon=0.437$)
- ✓ companion mass: $\sim 1M_{\odot}$
- ✓ pulsar mass: $M = 1.67 \pm 0.11M_{\odot}$

Two-solar mass neutron star measured

LETTER

Nature 464, 1081 (2010)

doi:10.1038/nature09466

A two-solar-mass neutron star measured using Shapiro delay

P. B. Demorest¹, T. Pennucci², S. M. Ransom¹, M. S. E. Roberts³ & J. W. T. Hessels^{4,5}

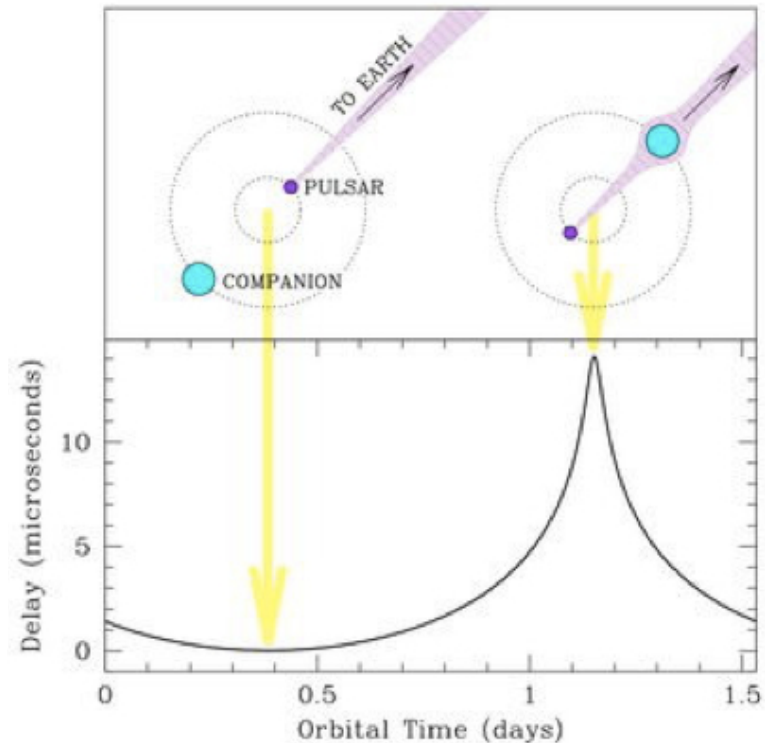
Neutron stars are composed of the densest form of matter known to exist in our Universe, the composition and properties of which are still theoretically uncertain. Measurements of the masses or radii of these objects can strongly constrain the neutron star matter equation of state and rule out theoretical models of their composition^{1,2}. The observed range of neutron star masses, however, has hitherto been too narrow to rule out many predictions of 'exotic' non-nucleonic components³⁻⁶. The Shapiro delay is a general-relativistic increase in light travel time through the curved space-time near a massive body⁷. For highly inclined (nearly edge-on) binary millisecond radio pulsar systems, this effect allows us to infer the masses of both the neutron star and its binary companion to high precision^{8,9}. Here we present radio timing observations of the binary millisecond pulsar J1614-2230^{10,11} that show a strong Shapiro delay signature. We calculate the pulsar mass to be $(1.97 \pm 0.04)M_{\odot}$, which rules out almost all currently proposed²⁻⁵ hyperon or boson condensate equations of state (M_{\odot} , solar mass). Quark matter can support a star this massive only if the quarks are strongly interacting and are therefore not 'free' quarks¹².

long-term data set, parameter covariance and dispersion measure variation can be found in Supplementary Information.

As shown in Fig. 1, the Shapiro delay was detected in our data with extremely high significance, and must be included to model the arrival times of the radio pulses correctly. However, estimating parameter values and uncertainties can be difficult owing to the high covariance between many orbital timing model terms¹⁴. Furthermore, the χ^2 surfaces for the Shapiro-derived companion mass (M_2) and inclination angle (i) are often significantly curved or otherwise non-Gaussian¹⁵. To obtain robust error estimates, we used a Markov chain Monte Carlo (MCMC) approach to explore the post-fit χ^2 space and derive posterior probability distributions for all timing model parameters (Fig. 2). Our final results for the model

Table 1 | Physical parameters for PSR J1614-2230

Parameter	Value
Ecliptic longitude (λ)	245.78827556(5) ^o
Ecliptic latitude (β)	-1.256744(2) ^o
Proper motion in λ	9.79(7) mas yr ⁻¹
Proper motion in β	-30(3) mas yr ⁻¹
Parallax	0.5(6) mas



Binary millisecond pulsar PSR J1614+2230
Shapiro delay signature

$$\Delta t = -\frac{2GM}{c^3} \log(1 - \vec{R} \cdot \vec{R}')$$

The mass $1.97 \pm 0.04 M_{\text{sun}}$ of the pulsar PSR J1614+2230 rules out almost all currently proposed hyperon or boson condensate EoS. Quark matter can support such a massive star only if quarks are strongly interacting (not "free quarks")

On April 26th 2013 the discovery of the most massive (up to now) pulsar (PSR J0348+0432) was made public

Science 26 April 2013:
Vol. 340 no. 6131
DOI: 10.1126/science.1233232

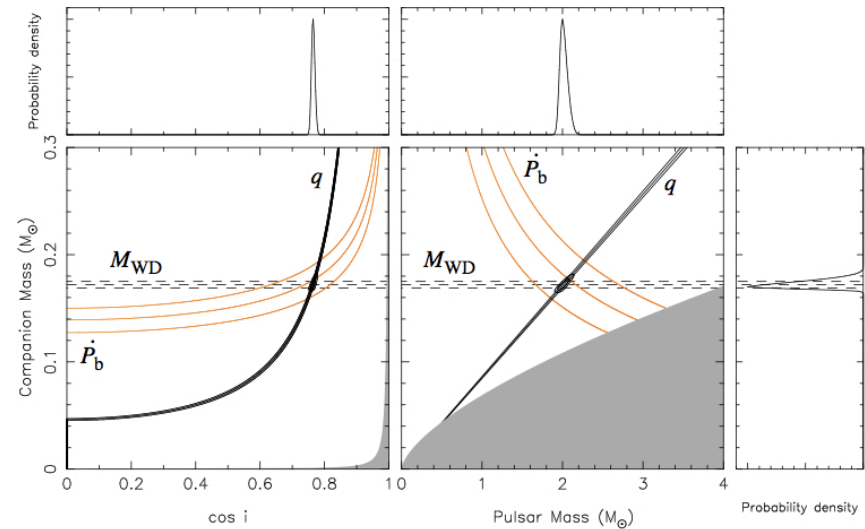
A Massive Pulsar in a Compact Relativistic Binary

John Antoniadis^{1,2}, Paulo C. C. Freire³, Norbert Wex⁴, Thomas M. Tauris^{2,3}, Ryan S. Lynch³, Marten H. van Kerkwijk⁴, Michael Kramer^{1,5}, Cees Bassa⁶, Vik S. Dhillon⁶, Thomas Driebe⁷, Jason W. T. Hessels^{8,9}, Victoria M. Kaspi³, Vladislav I. Kondratiev^{8,10}, Norbert Langer², Thomas R. Marsh¹¹, Maura A. McLaughlin¹², Timothy T. Pennucci¹³, Scott M. Ransom¹⁴, Ingrid H. Stairs¹⁵, Joeri van Leeuwen^{8,9}, Joris P. W. Verbiest¹, David G. Whelan¹³

Author Affiliations
Corresponding author. E-mail: jantonadis@mpifr-bonn.mpg.de

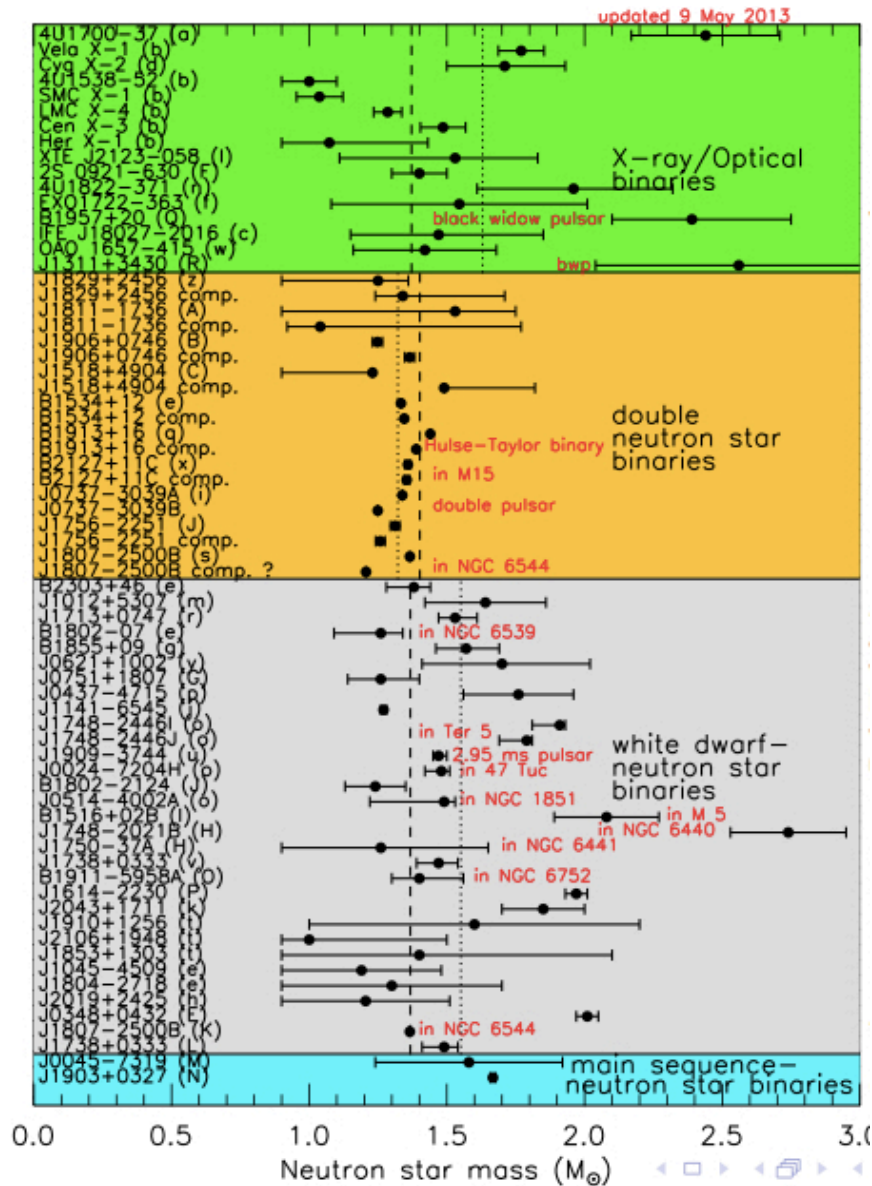
ABSTRACT STRUCTURED ABSTRACT EDITOR'S SUMMARY

Many physically motivated extensions to general relativity (GR) predict substantial deviations in the properties of spacetime surrounding massive neutron stars. We report the measurement of a 2.01 ± 0.04 solar mass (M_{\odot}) pulsar in a 2.46-hour orbit with a $0.172 \pm 0.003 M_{\odot}$ white dwarf. The high pulsar mass and the compact orbit make this system a sensitive laboratory of a previously untested strong-field gravity regime. Thus far, the observed orbital decay agrees with GR, supporting its validity even for the extreme conditions present in the system. The resulting constraints on deviations support the use of GR-based templates for ground-based gravitational wave detectors. Additionally, the system strengthens recent constraints on the properties of dense matter and provides insight to binary stellar astrophysics and pulsar recycling.



- ✓ binary system (P=2.46 h)
- ✓ very low eccentricity
- ✓ companion mass: $0.172 \pm 0.003 M_{\odot}$
- ✓ pulsar mass: $M = 2.01 \pm 0.04 M_{\odot}$

Measured Neutron Star Masses (2014)



Observation of $\sim 2 M_{\text{sun}}$ neutron stars



Dense matter EoS stiff enough is required such that

$$M_{\text{max}} [EoS] > 2M_{\odot}$$

Can strangeness (hyperons, kaons, quarks) still be present in the interior of neutron stars in view of this constraint?

The Hyperon Puzzle



“Hyperons → “soft (or too soft) EoS” not compatible (mainly in microscopic approaches) with measured (high) masses. However, the presence of hyperons in the NS interior seems to be unavoidable.”



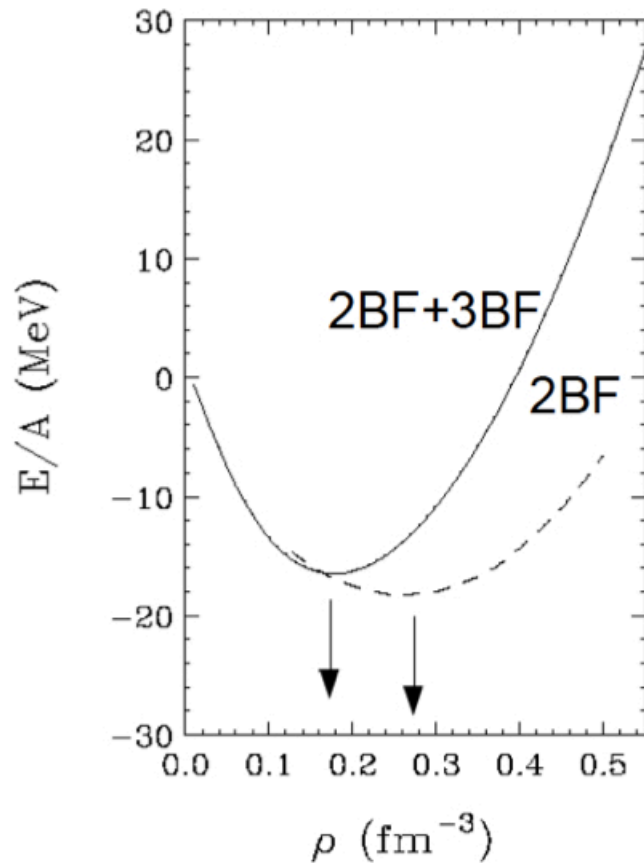
- ✓ can YN & YY interactions still solve it ?
- ✓ or perhaps hyperonic three-body forces ?
- ✓ what about quark matter ?

Solution I: Hyperonic Three Body Forces

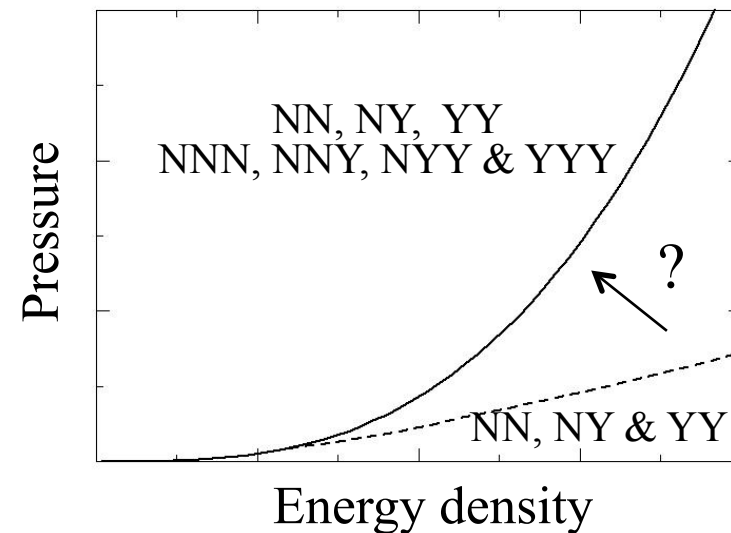
Natural solution based on: **Importance of NNN force in Nuclear Physics**

(Considered by several authors: Chalk, Gal, Usmani, Bodmer, Takatsuka, Loiseau, Nogami, Bahaduri, IV)

NNN Force

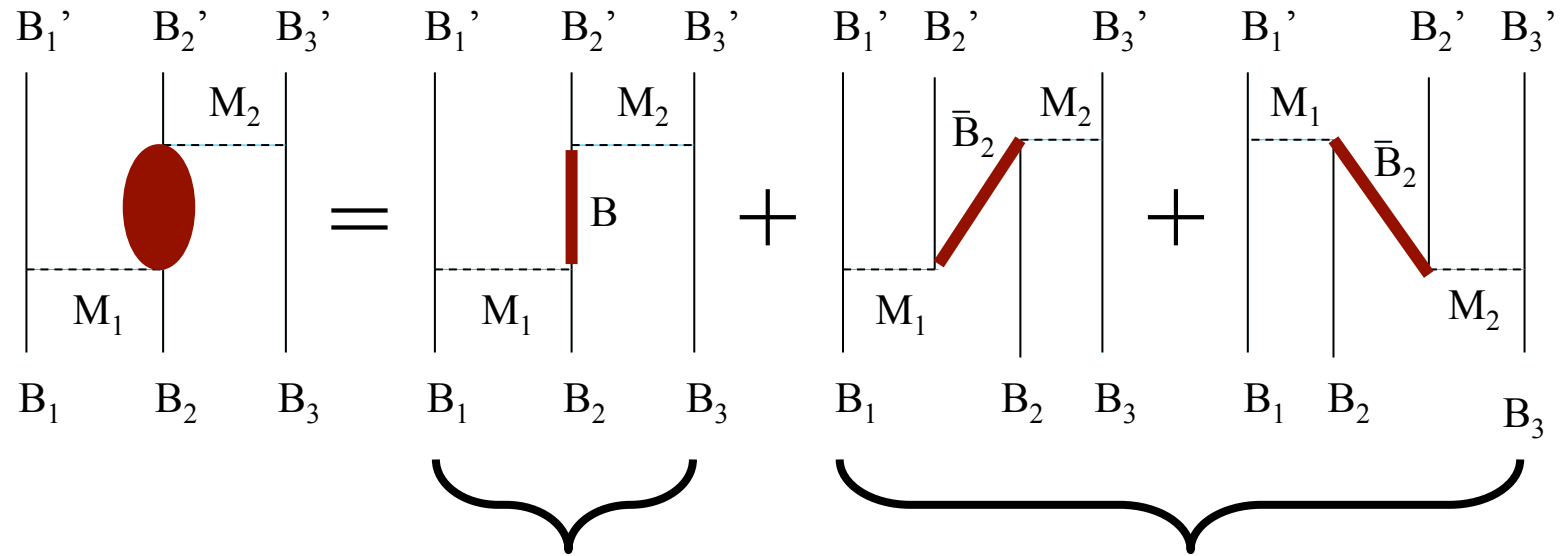


NNY, NYY & YYY Forces



Can hyperonic TBF provide enough repulsion at high densities to reach $2M_{\odot}$?

Two-meson exchange Hyperonic TBF



B_i, B_i' : N, Λ, Σ

B - excitation

Z - diagram

M_i : $\pi, K, \rho, K^*, \sigma, \omega$

B : $N, \Lambda, \Sigma, \Delta, N^*, \Sigma^*$

\bar{B}_2 : $\bar{N}, \bar{\Lambda}, \bar{\Sigma}$

Vertices: consistent with YN and YY

Repulsion at high densities due to Z -diagram as in NNN



Example: the NN Λ force

- $\pi\pi$ contribution

$$V_{NN\Lambda}^{\Sigma, \Sigma^*}(\vec{r}_{N_1\Lambda}, \vec{r}_{N_2\Lambda}) = -C_{NN\Lambda}^{\Sigma, \Sigma^*} \{X_{N_1\Lambda}(\vec{r}_{N_1\Lambda}), X_{N_2\Lambda}(\vec{r}_{N_2\Lambda})\} \vec{\tau}_{N_1} \cdot \vec{\tau}_{N_2}$$

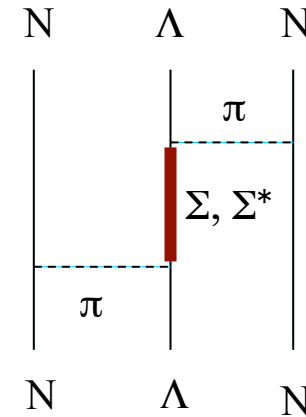
with

$$X_{ij}(\vec{x}) = \vec{\sigma}_i \cdot \vec{\sigma}_j Y(x) + S_{ij}(\hat{x}) T(x)$$

$$Y(x) = \frac{\partial^2 Z}{\partial x^2} + \frac{2}{x} \frac{\partial Z}{\partial x}$$

$$T(x) = \frac{\partial^2 Z}{\partial x^2} - \frac{1}{x} \frac{\partial Z}{\partial x}$$

$$Z(x) = \frac{4}{m_\pi} \int \frac{d\vec{k}}{(2\pi)^3} \frac{e^{-i\vec{k}\cdot\vec{x}}}{k^2 + m_\pi^2} F_{NN\pi}(k^2) F_{\Lambda(\Sigma, \Sigma^*)\pi}(k^2)$$



$$C_{NN\Lambda}^{\Sigma} = -\frac{1}{9} \frac{g_{NN\pi}^2 g_{\Lambda\Sigma\pi}^2}{16\pi^2} \frac{m_\pi^2}{m_\Sigma - m_\Lambda}$$

$$C_{NN\Lambda}^{\Sigma^*} = \frac{2}{27} \frac{g_{NN\pi}^2 f_{\Lambda\Sigma^*\pi}^2}{16\pi^2} \frac{m_\pi^2}{m_{\Sigma^*} - m_\Lambda}$$

$$\left(C_{NN\Lambda}^{\Lambda} = \frac{2}{81} \frac{g_{NN\pi}^2 f_{\Lambda\Lambda\pi}^2}{16\pi^2} \frac{m_\pi^2}{m_\Lambda - m_\Lambda}, C_{NN\Lambda}^{\Sigma} \sim 0.185 \right)$$



- KK contribution

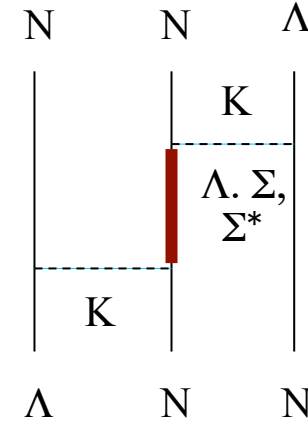
$$V_{NN\Lambda}^{\Lambda}(\vec{r}_{N_1\Lambda}, \vec{r}_{N_2\Lambda}) = -C_{NN\Lambda}^{\Lambda} \left\{ X_{N_1\Lambda}(\vec{r}_{N_1\Lambda}), X_{N_2\Lambda}(\vec{r}_{N_2\Lambda}) \right\}$$

$$V_{NN\Lambda}^{\Sigma}(\vec{r}_{N_1\Lambda}, \vec{r}_{N_2\Lambda}) = -C_{NN\Lambda}^{\Sigma} \left(\left\{ \vec{\rho}_{\Lambda_1} \cdot \vec{\tau}_{N_2}, \vec{\tau}_{N_2} \cdot \vec{\rho}_{\Lambda_2} \right\} \right. \\ \left. + \left[\vec{\rho}_{\Lambda_1} \cdot \vec{\tau}_{N_2}, \vec{\tau}_{N_2} \cdot \vec{\rho}_{\Lambda_2} \right] \right) \left\{ X_{N_1\Lambda}(\vec{r}_{N_1\Lambda}), X_{N_2\Lambda}(\vec{r}_{N_2\Lambda}) \right\}$$

$$V_{NN\Lambda}^{\Sigma^*}(\vec{r}_{N_1\Lambda}, \vec{r}_{N_2\Lambda}) = -C_{NN\Lambda}^{\Sigma^*} \left(\left\{ \vec{\rho}_{\Lambda_1} \cdot \vec{\tau}_{N_2}, \vec{\tau}_{N_2} \cdot \vec{\rho}_{\Lambda_2} \right\} \right. \\ \left. + \frac{1}{2} \left[\vec{\rho}_{\Lambda_1} \cdot \vec{\tau}_{N_2}, \vec{\tau}_{N_2} \cdot \vec{\rho}_{\Lambda_2} \right] \right) \left\{ X_{N_1\Lambda}(\vec{r}_{N_1\Lambda}), X_{N_2\Lambda}(\vec{r}_{N_2\Lambda}) \right\}$$

with

$$Z(x) = \frac{4}{m_K} \int \frac{d\vec{k}}{(2\pi)^3} \frac{e^{-i\vec{k}\cdot\vec{x}}}{k^2 + m_K^2} F_{N\Lambda K}(k^2) F_{N(\Sigma, \Sigma^*)K}(k^2)$$



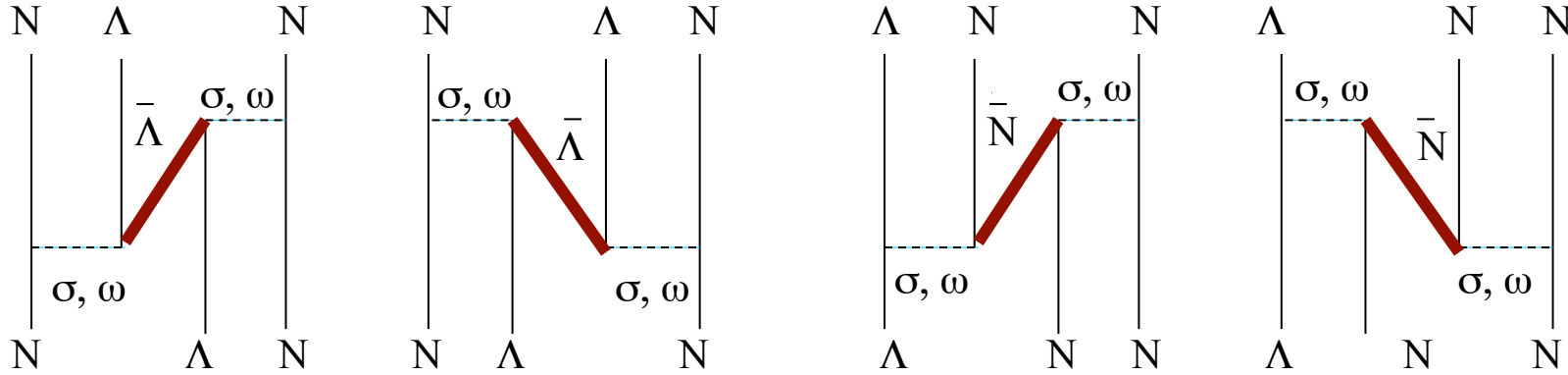
$$C_{NN\Lambda}^{\Lambda} = -\frac{1}{9} \frac{g_{N\Lambda K}^4}{16\pi^2} \frac{m_{\pi}^2}{m_{\Lambda} - m_N} \left(\frac{m_K}{m_{\pi}} \right)^4$$

$$C_{NN\Lambda}^{\Sigma} = -\frac{1}{18} \frac{g_{N\Lambda K}^2 g_{N\Sigma K}^2}{16\pi^2} \frac{m_{\pi}^2}{m_{\Sigma} - m_N} \left(\frac{m_K}{m_{\pi}} \right)^4$$

$$C_{NN\Lambda}^{\Sigma^*} = \frac{1}{27} \frac{g_{N\Lambda K}^2 f_{N\Sigma^* K}^2}{16\pi^2} \frac{m_{\pi}^2}{m_{\Sigma^*} - m_N} \left(\frac{m_K}{m_{\pi}} \right)^4$$



■ $\sigma\sigma$, $\omega\omega$ and $\sigma\omega$ contributions



For instance $\sigma\sigma$ looks like:

$$V_{N\bar{\Lambda}N}^{\bar{\Lambda}} = C_{N\bar{\Lambda}N}^{\bar{\Lambda}} \delta(\mathbf{r}'_1 - \mathbf{r}_1) \delta(\mathbf{r}'_2 - \mathbf{r}_2) \{ -4Z(r_{13})Z(r_{32}) \nabla_{\mathbf{r}'_3}^2 - 4Z'(r_{13})Z(r_{32}) \hat{\mathbf{r}}_{13} \cdot \nabla_{\mathbf{r}'_3} - 4Z(r_{13})Z'(r_{32}) \hat{\mathbf{r}}_{32} \cdot \nabla_{\mathbf{r}'_3} - [Y(r_{13})Z(r_{32}) + Z(r_{13})Y(r_{32})] - \hat{\mathbf{r}}_{13} \cdot \hat{\mathbf{r}}_{32} Z'(r_{13})Z'(r_{32}) - 2i[Z'(r_{13})Z(r_{32}) \boldsymbol{\sigma}_3 \cdot \hat{\mathbf{r}}_{13} \wedge \nabla_{\mathbf{r}'_3} + Z'(r_{32})Z(r_{13}) \boldsymbol{\sigma}_3 \cdot \hat{\mathbf{r}}_{32} \wedge \nabla_{\mathbf{r}'_3}] \} \delta(\mathbf{r}'_3 - \mathbf{r}_3)$$

$$V_{\bar{\Lambda}NN}^{\bar{N}} = C_{\bar{\Lambda}NN}^{\bar{N}} \delta(\mathbf{r}'_1 - \mathbf{r}_1) \delta(\mathbf{r}'_2 - \mathbf{r}_2) \{ -4Z_1(r_{13})Z_2(r_{32}) \nabla_{\mathbf{r}'_3}^2 - 4Z'_1(r_{13})Z_2(r_{32}) \hat{\mathbf{r}}_{13} \cdot \nabla_{\mathbf{r}'_3} - 4Z_1(r_{13})Z'_2(r_{32}) \hat{\mathbf{r}}_{32} \cdot \nabla_{\mathbf{r}'_3} - [Y_1(r_{13})Z_2(r_{32}) + Z_1(r_{13})Y_2(r_{32})] - \hat{\mathbf{r}}_{13} \cdot \hat{\mathbf{r}}_{32} Z'_1(r_{13})Z'_2(r_{32}) - 2i[Z'_1(r_{13})Z_2(r_{32}) \boldsymbol{\sigma}_3 \cdot \hat{\mathbf{r}}_{13} \wedge \nabla_{\mathbf{r}'_3} + Z'_2(r_{32})Z_1(r_{13}) \boldsymbol{\sigma}_3 \cdot \hat{\mathbf{r}}_{32} \wedge \nabla_{\mathbf{r}'_3}] \} \delta(\mathbf{r}'_3 - \mathbf{r}_3),$$



But that's only the beginning of the story
there are

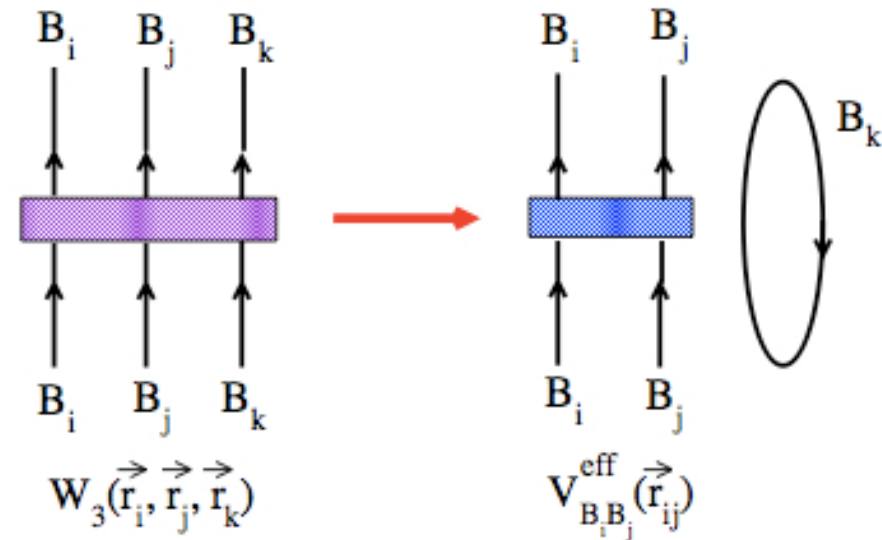
MANY MANY MANY more forces & contributions

....



Three-Body Forces within the BHF approach

TBF can be introduced in our BHF approach by adding effective density-dependent two body forces to the baryon-baryon interactions V when solving the Bethe-Goldstone equation

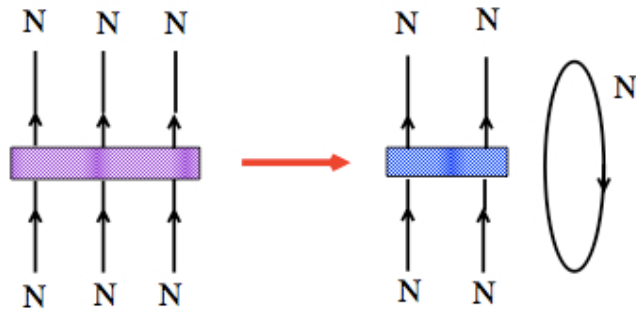


$$W_{B_i B_j}(\vec{r}_{ij}) = \int W_3(\vec{r}_i, \vec{r}_j, \vec{r}_k) n(\vec{r}_i, \vec{r}_j, \vec{r}_k) d^3 \vec{r}_k$$

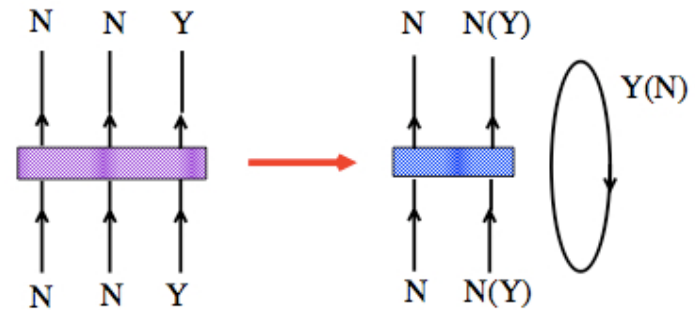
$W_3(\vec{r}_i, \vec{r}_j, \vec{r}_k)$: genuine TBF $n(\vec{r}_i, \vec{r}_j, \vec{r}_k)$: three-body correlation function

From the genuine NNN,NNY, NYY and YYY TBF ...

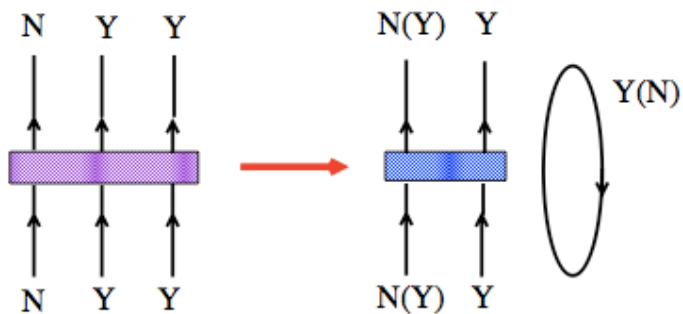
NNN → NN



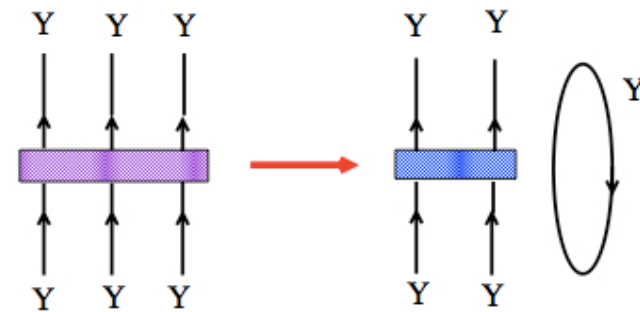
NNY → NN, NY



NYY → NY, YY



YYY → YY



Effective density-dependent 2BF from NNY

- $\pi\pi$ contribution

$$W_{NN}^B(\vec{r}) = -C_{NNY}^B \rho_Y \left[V_{\sigma}^{\pi\pi}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{\pi\pi}(\vec{r}) S_{12}(\hat{r}) \right] \vec{\tau}_1 \cdot \vec{\tau}_2$$

$$(B=\Lambda, \Sigma, \Sigma^* \quad Y=\Lambda, \Sigma)$$

$$W_{N\Sigma}^{\Delta}(\vec{r}) = -C_{NN\Sigma}^{\Delta} \rho_N \left[V_{\sigma}^{\pi\pi}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{\pi\pi}(\vec{r}) S_{12}(\hat{r}) \right] \vec{\tau}_1 \cdot \vec{I}_2$$

$$W_{N\Sigma \rightarrow N\Lambda}^{\Delta}(\vec{r}) = -C_{NN\Sigma \rightarrow NN\Lambda}^{\Delta} \rho_N \left[V_{\sigma}^{\pi\pi}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{\pi\pi}(\vec{r}) S_{12}(\hat{r}) \right] \vec{\tau}_1 \cdot \vec{\rho}_2$$



- KK contribution

$$W_{N\Lambda}^{\Lambda}(\vec{r}) = -C_{NN\Lambda}^{\Lambda} \rho_N \left[V_{\sigma}^{KK}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{KK}(\vec{r}) S_{12}(\hat{r}) \right]$$

$$W_{N\Lambda}^{\Sigma, \Sigma^*}(\vec{r}) = -C_{NN\Lambda}^{\Sigma, \Sigma^*} \rho_N \left[V_{\sigma}^{KK}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{KK}(\vec{r}) S_{12}(\hat{r}) \right] \vec{\tau}_1 \cdot \vec{\rho}_2$$

$$W_{N\Sigma}^{\Lambda, \Sigma}(\vec{r}) = -C_{NN\Sigma}^{\Lambda, \Sigma} \rho_N \left[V_{\sigma}^{KK}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{KK}(\vec{r}) S_{12}(\hat{r}) \right] \vec{\tau}_1 \cdot \vec{\tau}_2$$

$$W_{N\Sigma}^{\Sigma^*}(\vec{r}) = -C_{NN\Sigma}^{\Sigma^*} \rho_N \left[V_{\sigma}^{KK}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{KK}(\vec{r}) S_{12}(\hat{r}) \right] \vec{\tau}_1 \cdot \vec{\rho}_2$$

$$W_{N\Sigma \rightarrow N\Lambda}^{\Lambda, \Sigma, \Sigma^*}(\vec{r}) = -C_{NN\Sigma \rightarrow NN\Lambda}^{\Lambda, \Sigma, \Sigma^*} \rho_N \left[V_{\sigma}^{KK}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{KK}(\vec{r}) S_{12}(\hat{r}) \right] \vec{\tau}_1 \cdot \vec{\rho}_2$$



- $\sigma\sigma$ contribution

$$W_{NN}^{\bar{\Lambda}}(\vec{r}) = C_{NN\Lambda}^{\bar{\Lambda}} \left[\rho_N V_{c_1}^{\sigma\sigma}(\vec{r}) + \rho_N^{5/3} V_{c_2}^{\sigma\sigma}(\vec{r}) \right]$$

$$W_{N\Lambda}^{\bar{N}}(\vec{r}) = C_{NN\Lambda}^{\bar{N}} \left[\rho_\Lambda V_{c_1}^{\sigma\sigma}(\vec{r}) + \rho_\Lambda^{5/3} V_{c_2}^{\sigma\sigma}(\vec{r}) \right]$$

$$W_{N\Sigma}^{\bar{N}}(\vec{r}) = C_{NN\Sigma}^{\bar{N}} \left[\rho_\Sigma V_{c_1}^{\sigma\sigma}(\vec{r}) + \rho_\Sigma^{5/3} V_{c_2}^{\sigma\sigma}(\vec{r}) \right]$$

- $\omega\omega$ contribution

$$W_{NN}^{\bar{\Lambda}}(\vec{r}) = C_{NN\Lambda}^{\bar{\Lambda}} \rho_\Lambda \left[V_c^{\omega\omega}(\vec{r}) + V_\sigma^{\omega\omega}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{\omega\omega}(\vec{r}) S_{12}(\hat{r}) \right]$$

$$W_{N\Lambda}^{\bar{N}}(\vec{r}) = C_{NN\Lambda}^{\bar{N}} \rho_N \left[V_c^{\omega\omega}(\vec{r}) + V_\sigma^{\omega\omega}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{\omega\omega}(\vec{r}) S_{12}(\hat{r}) \right]$$

$$W_{N\Lambda}^{\bar{N}}(\vec{r}) = C_{NN\Lambda}^{\bar{N}} \rho_N \left[V_c^{\omega\omega}(\vec{r}) + V_\sigma^{\omega\omega}(\vec{r}) \vec{\sigma}_1 \cdot \vec{\sigma}_2 + V_T^{\omega\omega}(\vec{r}) S_{12}(\hat{r}) \right]$$



- $\sigma\omega$ contribution

$$W_{NN}^{\bar{\Lambda}}(\vec{r}) = C_{NN\Lambda}^{\bar{\Lambda}} \rho_N V_c^{\sigma\omega}(\vec{r})$$

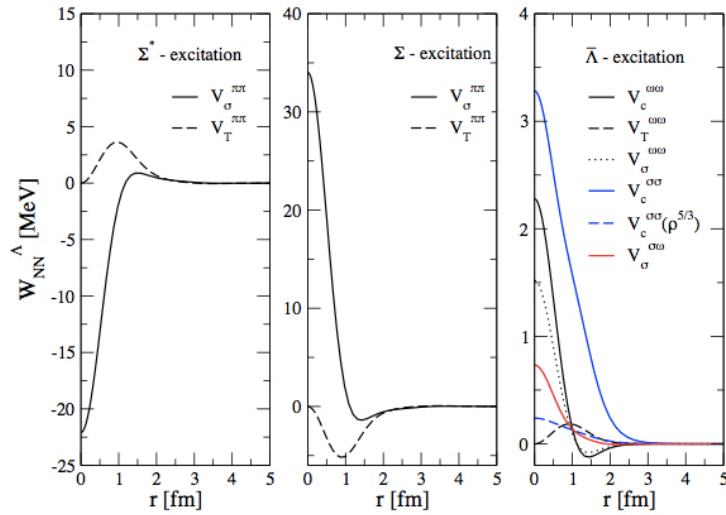
$$W_{N\Lambda}^{\bar{N}}(\vec{r}) = C_{NN\Lambda}^{\bar{N}} \rho_\Lambda V_c^{\sigma\omega}(\vec{r})$$

$$W_{N\Sigma}^{\bar{N}}(\vec{r}) = C_{NN\Sigma}^{\bar{N}} \rho_\Sigma V_c^{\sigma\sigma}(\vec{r})$$

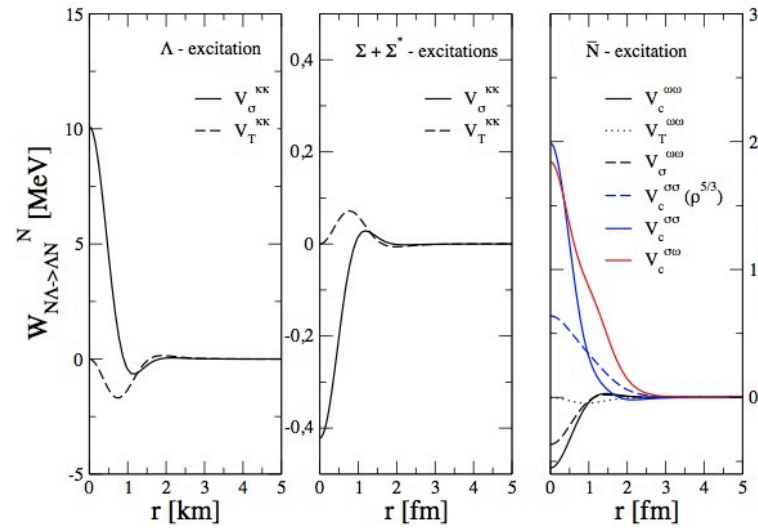
and so on and so forth



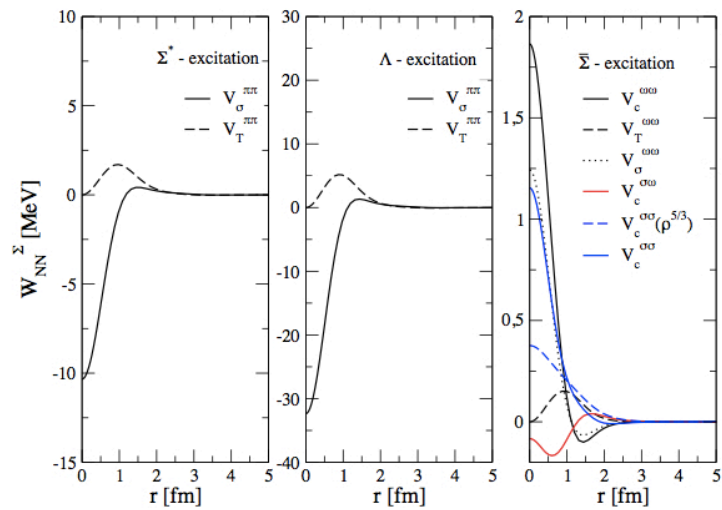
■ $W_{NN}^{\Lambda}(r)$



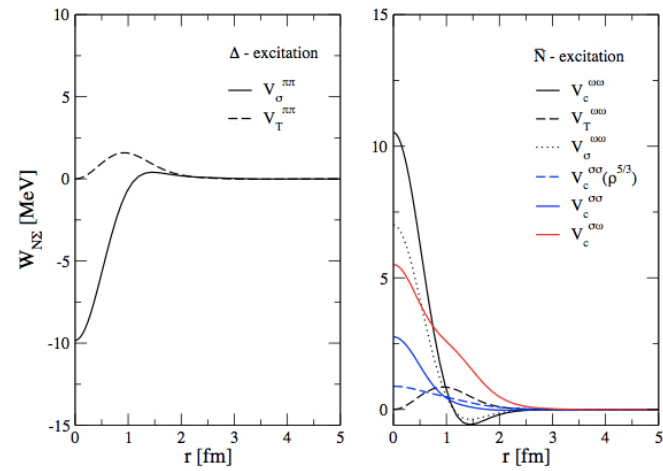
■ $W_{\Lambda N}^N(r)$



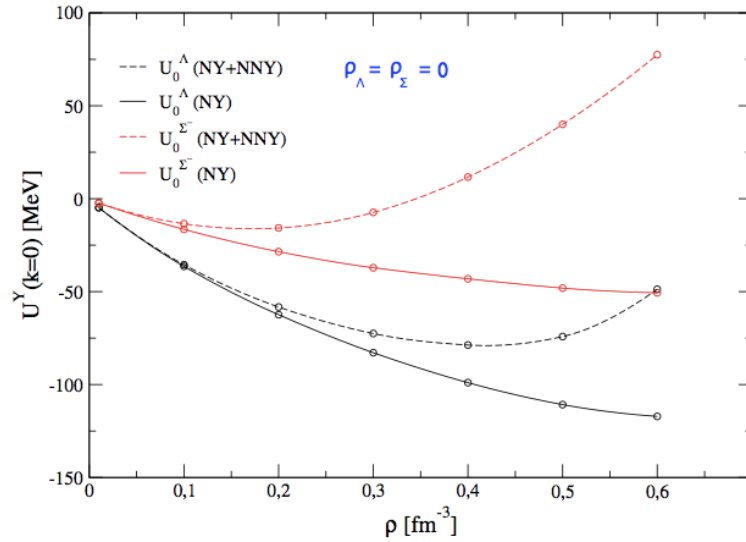
■ $W_{NN}^{\Sigma}(r)$



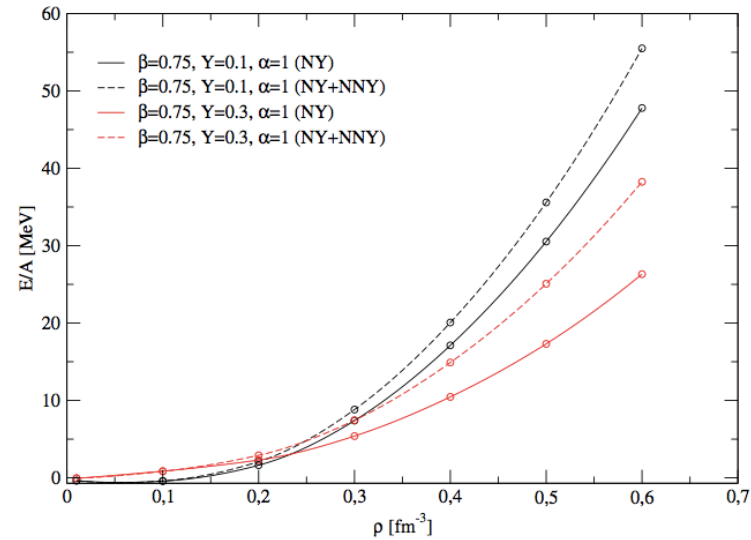
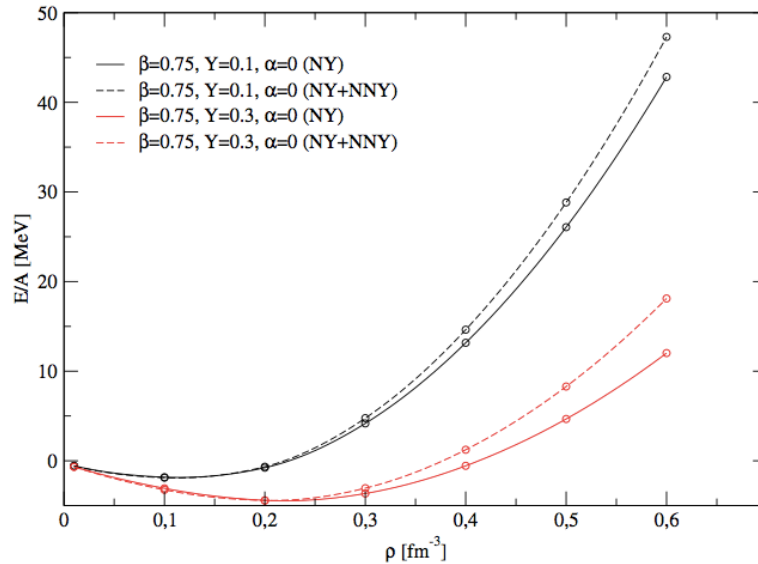
■ $W_{\Sigma N}^N(r)$



Effect of TBF on Mean Field & E/A



- ✓ Only NNY considered (preliminar)
- ✓ Repulsion at high densities due to Z-diagram contribution as in NNN



Work is in progress, but we can still estimate the effect of hyperonic TBF in NS

- 1-. Construct the hyperonic matter EoS within the BHF at 2 body level (Av18 NN + NSC89 YN)
- 2-. Add simple phenomenological density-dependent contact terms that mimic the effect of TBF.

Density-dependent contact terms: (Balberg & Gal 1997)

Potential of a baryon B_y in a sea of baryons B_x of density ρ_x

Folding $V_y(\rho_x)$ with ρ_x , $V_x(\rho_y)$ with ρ_y and combining with weight factors ρ_x/ρ and ρ_y/ρ

$$V_y(\rho_x) = a_{xy}\rho_x + b_{xy}\rho_x^{\gamma_{xy}}$$

$$\varepsilon_{xy}(\rho_x, \rho_y) = a_{xy}\rho_x\rho_y + b_{xy}\rho_x\rho_y \left(\frac{\rho_x^{\gamma_{xy}} + \rho_y^{\gamma_{xy}}}{\rho_x + \rho_y} \right)$$

attraction

repulsion

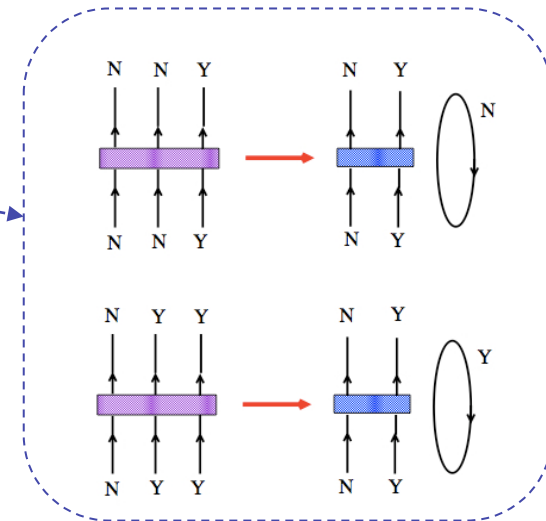
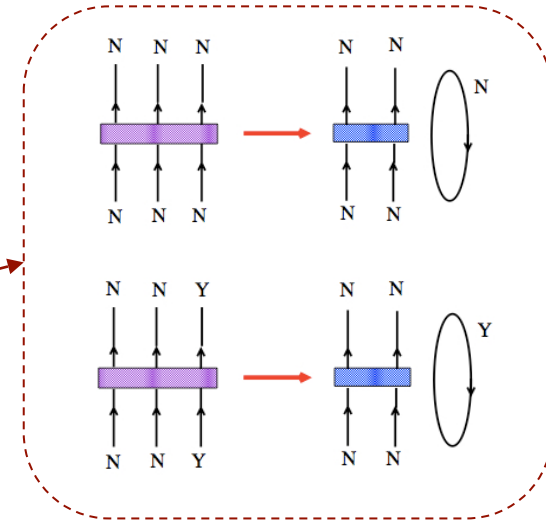
larger than 1

Then, we have ...

$$\varepsilon_{CT} = a_{NN}\rho_N^2 + b_{NN}\rho_N^{\gamma_{NN}}$$

$$+ a_{\Lambda N}\rho_\Lambda\rho_N + b_{\Lambda N}\rho_\Lambda\rho_N\left(\frac{\rho_\Lambda^{\gamma_{\Lambda N}} + \rho_N^{\gamma_{\Lambda N}}}{\rho_\Lambda + \rho_N}\right)$$

$$+ a_{\Sigma N}\rho_\Sigma\rho_N + b_{\Sigma N}\rho_\Sigma\rho_N\left(\frac{\rho_\Sigma^{\gamma_{\Sigma N}} + \rho_N^{\gamma_{\Sigma N}}}{\rho_\Sigma + \rho_N}\right)$$



$$\rho_N = \rho_n + \rho_p, \quad \rho_\Sigma = \rho_{\Sigma^-} + \rho_{\Sigma^0} + \rho_{\Sigma^+}$$

NYN → NY and YYY → YY
not included for consistency

The parameters a_{NN} , b_{NN} and γ_{NN}
 fitted to reproduce $\rho_0=0.16 \text{ fm}^{-3}$,
 $E/A=-16 \text{ MeV}$ and $K = 211-285 \text{ MeV}$

γ_{NN}	a_{NN} [MeV fm ³]	b_{NN} [MeV fm ^{3γ_{NN}}]	K_∞ [MeV]
2	-33.44	213.02	211
2.5	-22.08	355.03	236
3	-16.40	665.68	260
3.5	-12.99	1331.36	285

For simplicity, we take $a_{\Lambda N}=a_{\Sigma N}$, $b_{\Lambda N}=b_{\Sigma N}$ and $\gamma_{\Lambda N}=\gamma_{\Sigma N}$ with

$$a_{\Lambda N} = xa_{NN}, \quad b_{\Lambda N} = xb_{NN}, \quad x = 0, \frac{1}{3}, \frac{2}{3}, 1$$

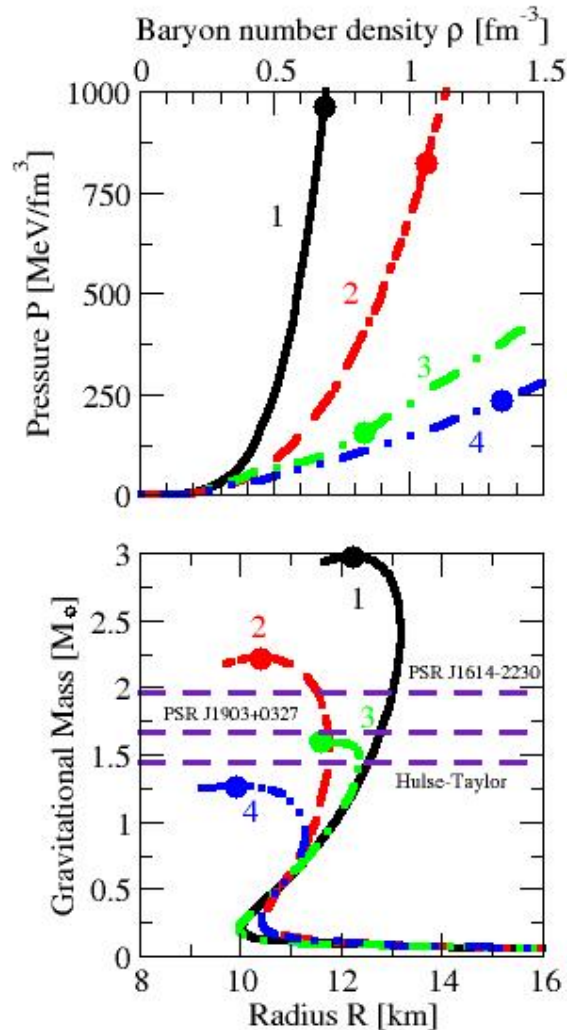
to explore different strength
of the hyperonic TBF

$\gamma_{\Lambda N}$ is obtained using the value of
-28 MeV for the binding energy
of a Λ in nuclear matter

$$\left(\frac{B}{A}\right)_\Lambda = 28 \text{ MeV} = -U_\Lambda(k=0) - a_{YN}\rho_0 - b_{YN}\rho_0^{\gamma_{YN}}$$

$$U_\Lambda(k=0) = -30.8 \text{ MeV}$$

Effect of hyperonic TBF on M_{\max}



γ_{NN}	x	γ_{YN}	Maximum Mass
2	0	-	1.27 (2.22)
	1/3	1.49	1.33
	2/3	1.69	1.38
2.5	1	1.77	1.41
	0	-	1.29 (2.46)
	1/3	1.84	1.38
3	2/3	2.08	1.44
	1	2.19	1.48
	0	-	1.34 (2.72)
3.5	1/3	2.23	1.45
	2/3	2.49	1.50
	1	2.62	1.54
3.5	0	-	1.38 (2.97)
	1/3	2.63	1.51
	2/3	2.91	1.56
	1	3.05	1.60

Hyperonic TBFs seem not to be the full solution of the “Hyperon Puzzle”, although they probably contribute to its solution

$$1.27 < M_{\max} < 1.6M_{\odot}$$

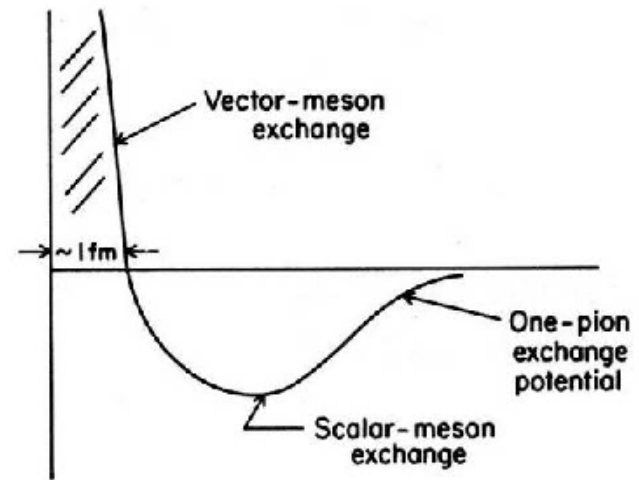


Solution II: YY vector meson repulsion

(explored in the context of RMF models)

General Feature:

Exchange of scalar mesons generates attraction (softening), but the exchange of vector mesons generates repulsion (stiffening)



Add vector mesons with hidden strangeness (ϕ) **coupled to hyperons** yielding a strong repulsive contribution at high densities

$M_{\max} > 2M_{\odot}$, but **smaller population of hyperons**



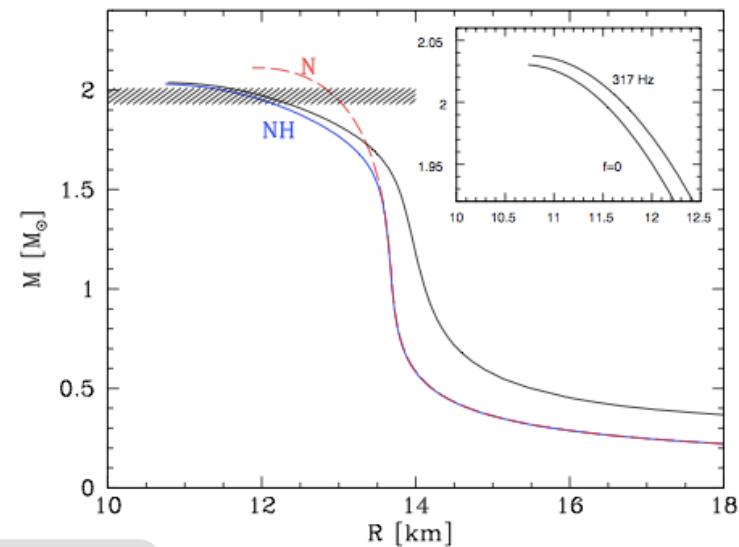
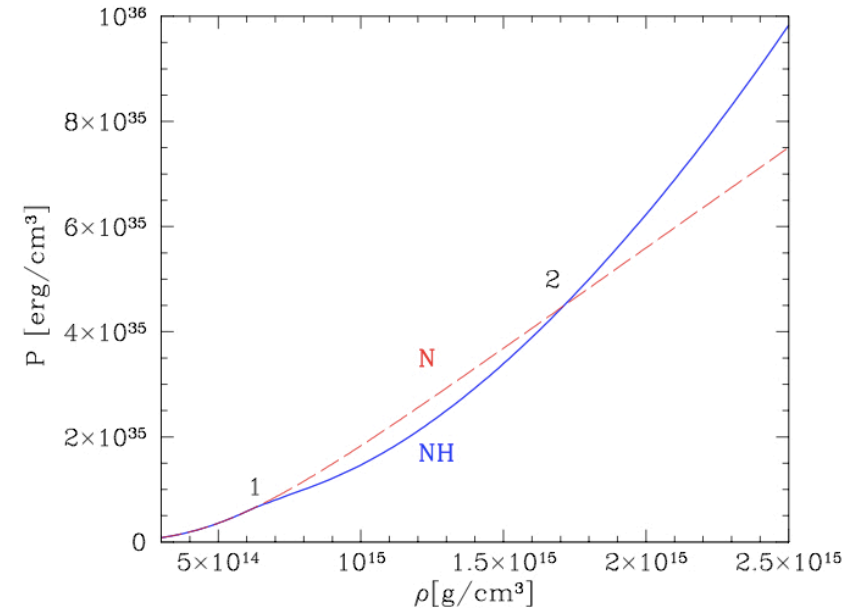
Dexhamer & Schramm (2008), Bednarek et al, (2012), Weissenborn et al., (2012)

■ Non-linear RMF

- ✓ $\sigma^2, \sigma^3, \sigma^4$ terms
- ✓ $\rho^2, \rho^4, \omega^2, \omega^4$ terms
- ✓ “hidden strangeness” mesons: σ^*, ϕ
($\sigma^{*2}, \phi^2, \phi^4$)
- ✓ cross terms: $\omega^2\rho^2, \phi^2\omega^2, \phi^2\rho^2$
- ✓ g_{YV} couplings fixed by SU(6)
- ✓ g_{YS} couplings adjusted by fitting $U_B^{(B)}$
($U_\Lambda^{(N)}=-28, U_\Sigma^{(N)}=+30, U_\Xi^{(N)}=-18$ MeV)
($U_\Xi^{(\Xi)}=U_\Lambda^{(\Xi)}=2U_\Lambda^{(\Lambda)}, U_\Lambda^{(\Lambda)}=-5$ MeV)

- Hyperonic EoS stiffer than the nucleonic one at $\rho > 5\rho_0$ due to the **quartic terms** involving ϕ meson

$M_{\max} > 2M_\odot$ but if $E^{NY}(n_b) > E^N(n_b) \Rightarrow \text{instability}$



Bednarek et al., (2012)

■ Non-linear RMF

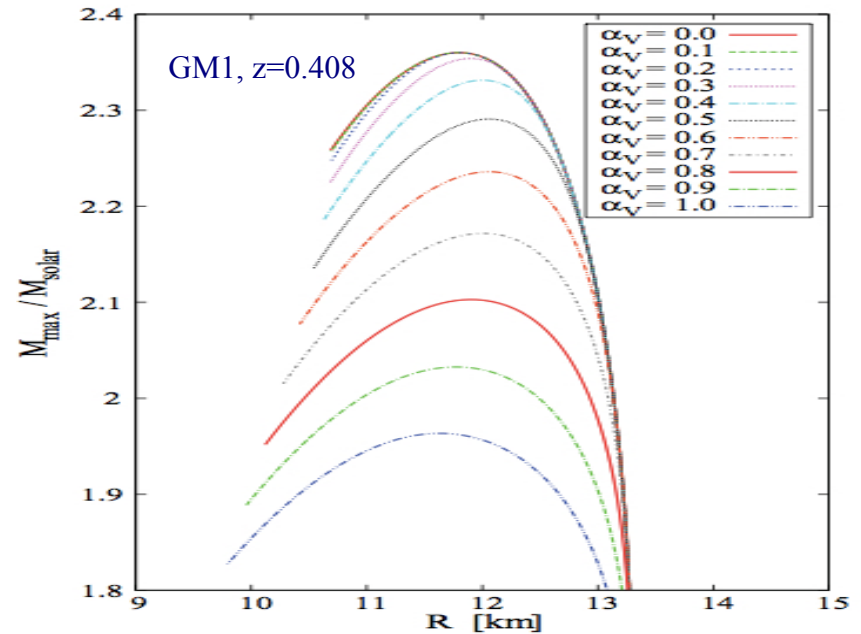
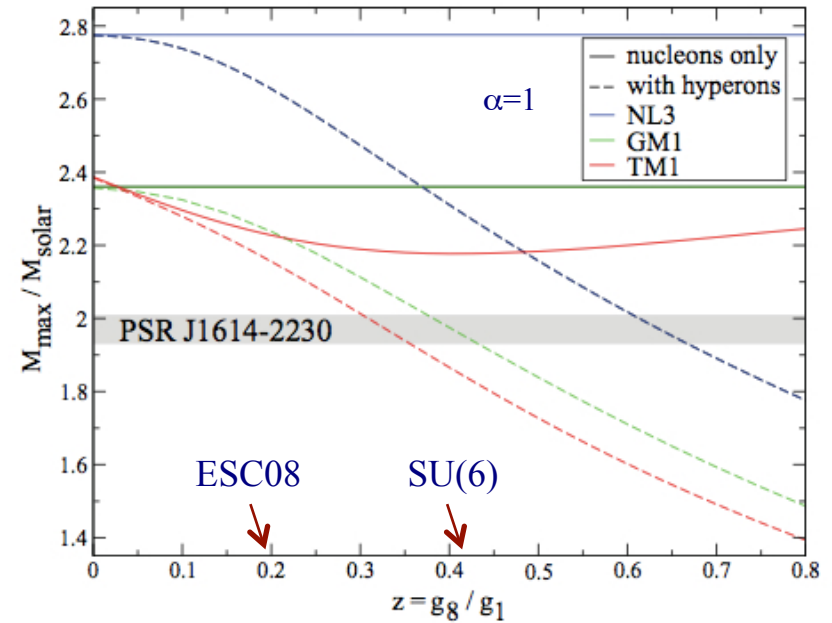
- ✓ $\sigma^2, \sigma^3, \sigma^4$ terms
- ✓ $\rho^2, \omega^2, \omega^4$ terms
- ✓ “hidden strangeness” mesons: σ^*, ϕ
(σ^{*2}, ϕ^2)
- ✓ g_{YV} couplings: from SU(6) to SU(3)
vary $z=g_8/g_1$ & $\alpha=F/(F+D)$
- ✓ g_{YS} couplings adjusted by fitting $U_B^{(N)}$
($U_\Lambda^{(N)}=-30, U_\Sigma^{(N)}=+30, U_\Xi^{(N)}=-28$ MeV)

- Stiffest EoS when including ϕ & σ^* is omitted for $z=0$ & $\alpha=0$

$$M_{\max} > 2M_\odot$$

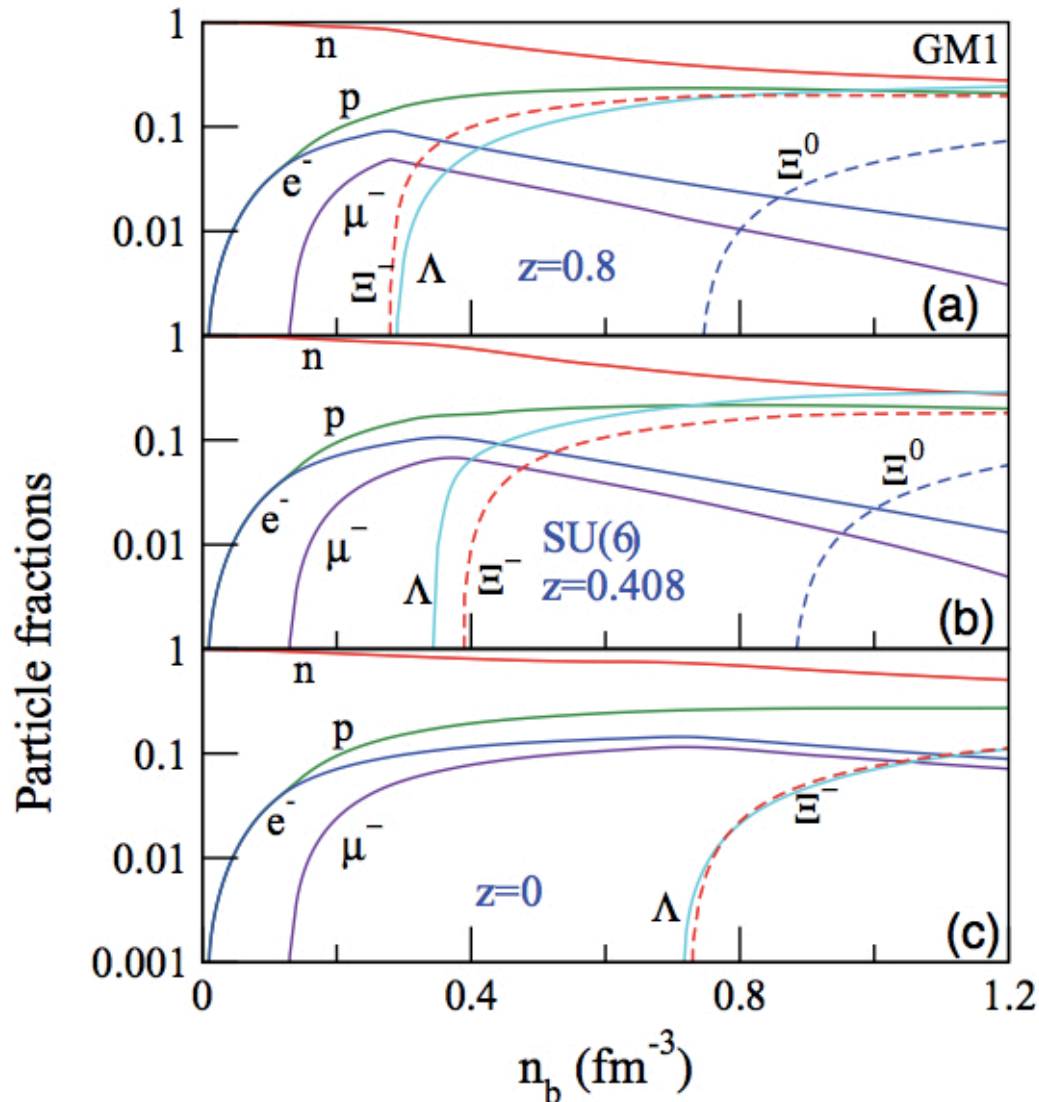
but

$$z = 0 \Rightarrow g_{N\rho} = 0$$



Weissenborn et al., (2012)

Particle Cocktail



Moving from SU(6) to SU(3):

- Hyperon thresholds moved to very high densities
- Small hyperon fraction

The problem seems to be solved (?) because there is **not much strangeness**



Solution III: Quark Matter Core

General Feature:

Some authors have suggested that the hyperon core in neutron stars could be replaced by a cores of uds quark mater. Massive neutron stars could actually be hybrid stars with a stiff quark matter core

To yield $M_{\max} > 2M_{\odot}$ Quark Matter should have:

- significant overall quark repulsion \longrightarrow stiff EoS
- strong attraction in a channel \longrightarrow strong color superconductivity



Ozel et al., (2010), Weissenborn et al., (2011), Klaehn et al., (2011), Bonano & Sedrakian (2012), Lastowiecki et al., (2012), Zdunik & Haensel (2012)

Recent General Analysis by Zdunik & Haensel

Based on:

Simple linear EoS is a rather precise analytic representation of modern quark EoS in a phase 2SC, CFL.

$$P(\varepsilon) = a(\varepsilon - \varepsilon^*), \quad \mu(P) = \frac{\varepsilon^*}{n^*} \left(1 + \frac{1+a}{a} \frac{P}{\varepsilon^*} \right)^{\frac{a}{1+a}}$$

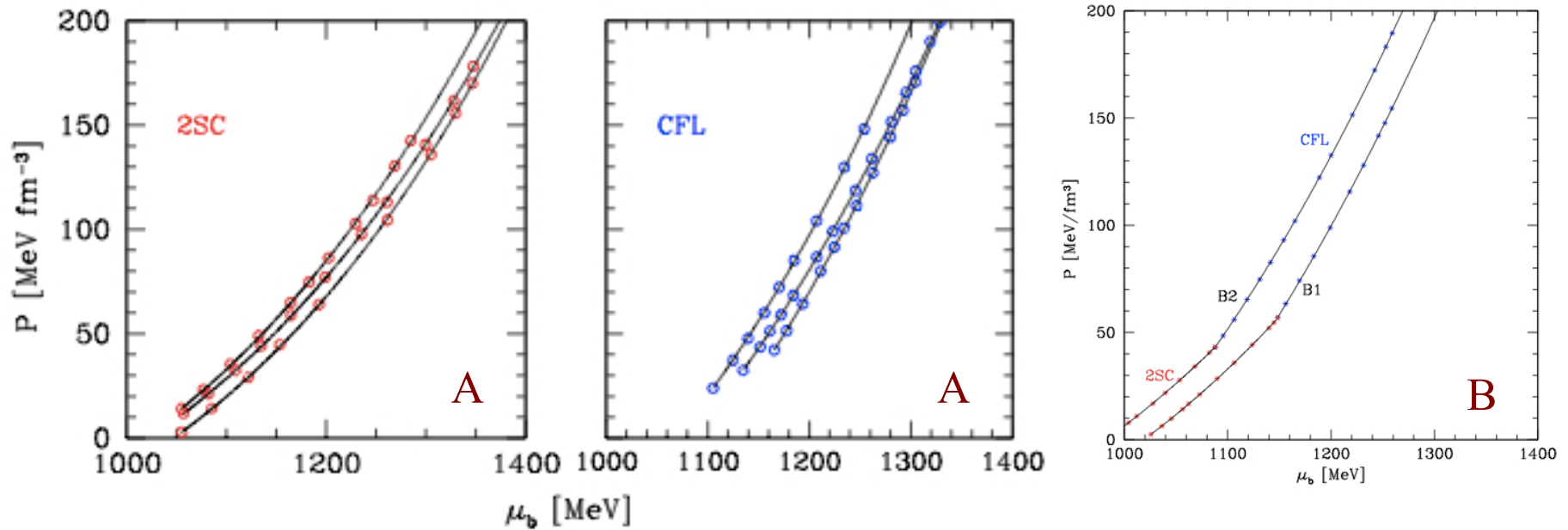
$$n(P) = n^* \left(1 + \frac{1+a}{a} \frac{P}{\varepsilon^*} \right)$$

3 parameters:

- a : squared of v_{sound}
- ε^* : energ. dens. at $P=0$
- n^* : num. dens. at $P=0$



Fitting 2SC & CFL quark matter EoS



Numerical calculations based on:
Nambu-Jona-Lasinio+Color Superconductivity

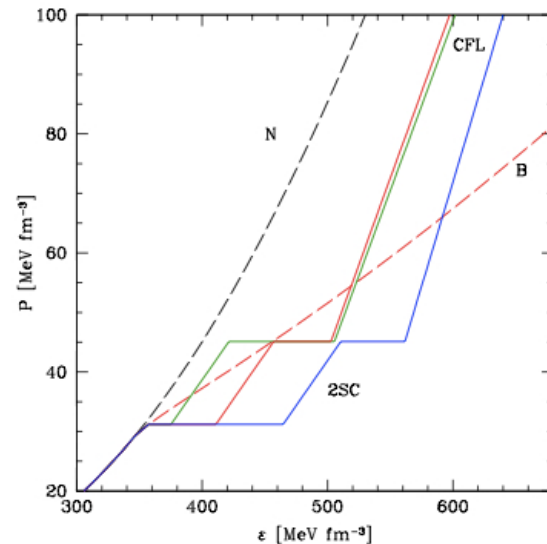
- A. Agrawal (2010)
- B. Blaschke et al., (2010)



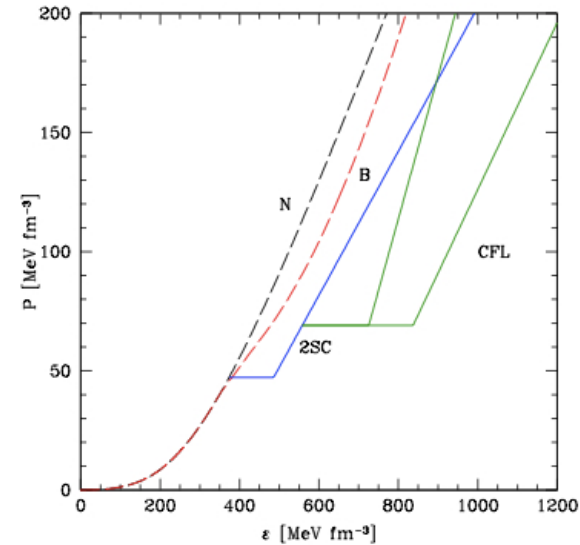
Zdnunik & Haensel (2012)

From Hadrons to Quarks

match to a soft hadron EoS



match to a stiff hadron EoS



They simulate the sequence:

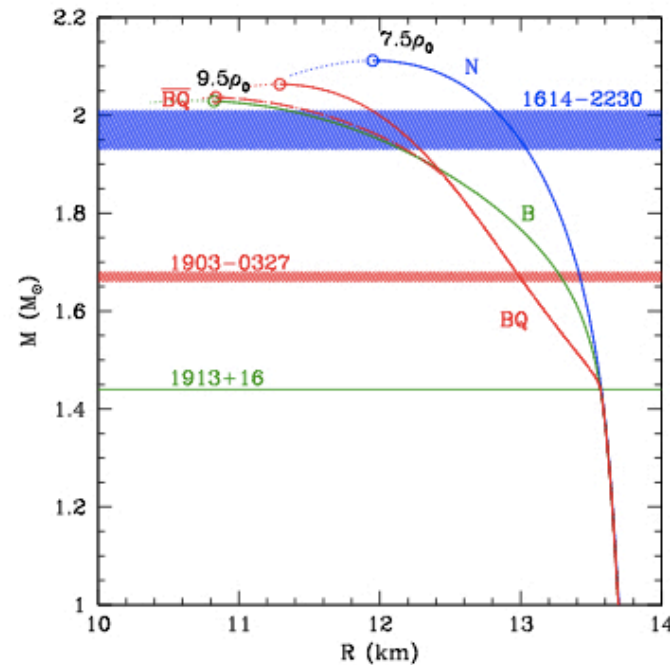
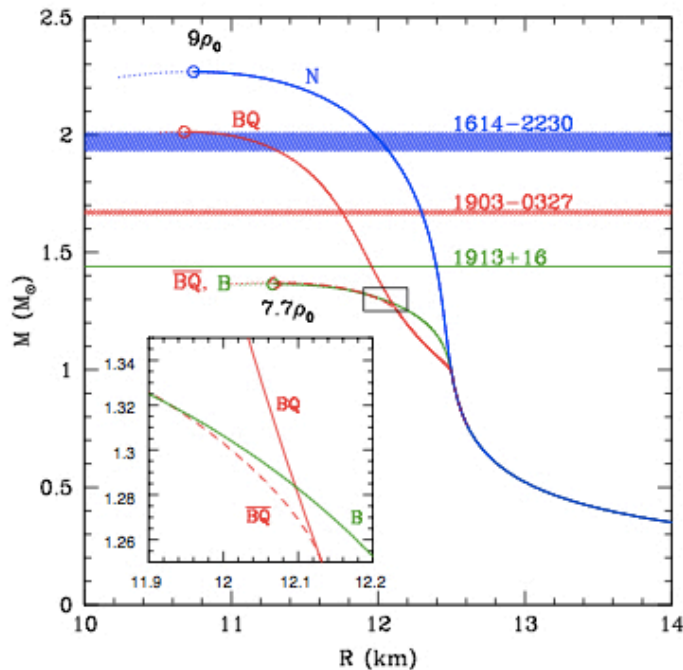
Hadron phase \rightarrow 2SC phase \rightarrow CFL phase

$$P_i = P^{(B)}(\epsilon_1^i) = P^{(Q)}(\epsilon_2^i), \quad \mu^{(B)}(P_i) = \mu^{(Q)}(P_i), \quad \lambda_i = \frac{\epsilon_2^i}{\epsilon_1^i} > 1$$



Zdnunik & Haensel (2012)

Stability of QM core and M_{\max}



$M_{\max} > 2M_{\odot}$ requires:

- BQ transition must be rather low $\sim 2\rho_0$ - $3\rho_0$
- Density jumps λ_i should not be too large (< 1.2)
- $v_{\text{sound}} \sim 0.8$ - 0.9 if $2.2 - 2.4M_{\odot}$ is observed
- Stiffening EoS $\rightarrow \mu_b$ increases
- If $\mu_b^Q(P) > \mu_b^H(P) \rightarrow$ instability (reconfinement)



Question is **so open** that ...

Hyperons-NS-2012

A task force meeting-November 21-24, 2012

Copernicus Astronomical Center

Warsaw, Poland

Organizers: M. Bejger, P. Haensel, J.
Schaffner-Bielich & L. Zdunik



A photograph of the Frankfurt skyline, featuring several tall skyscrapers and the Main River in the foreground with a bridge and a boat. The text is overlaid on the image.

**EMMI Rapid Reaction Task Force
Quark Matter in Compact Stars
7-10 October 2013 FIAS
Frankfurt, Germany**

Chairs: J. Schaffner-Bielich & S. Schramm



Hyperon Stars at Birth

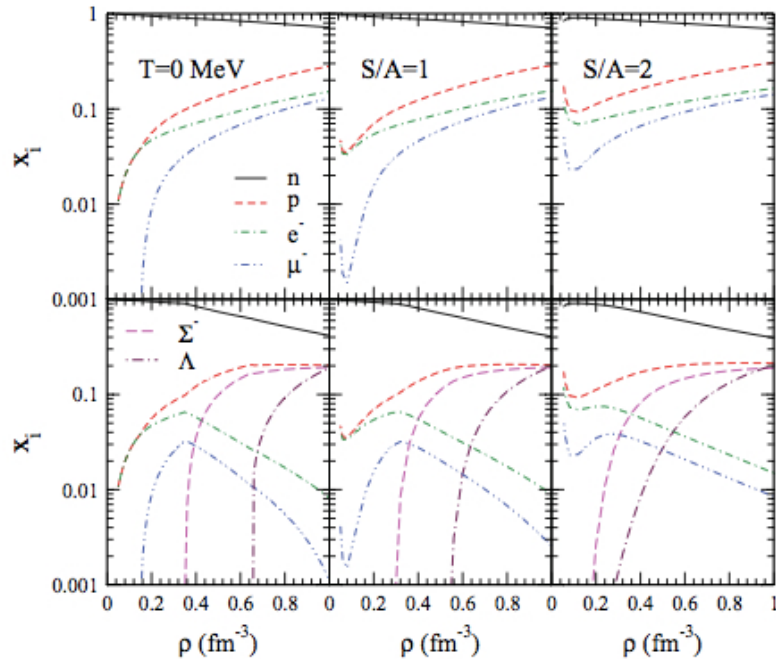
David Lloyd Glover

Proto-Neutron Stars: Composition

■ Neutrino free

$$\mu_\nu = 0$$

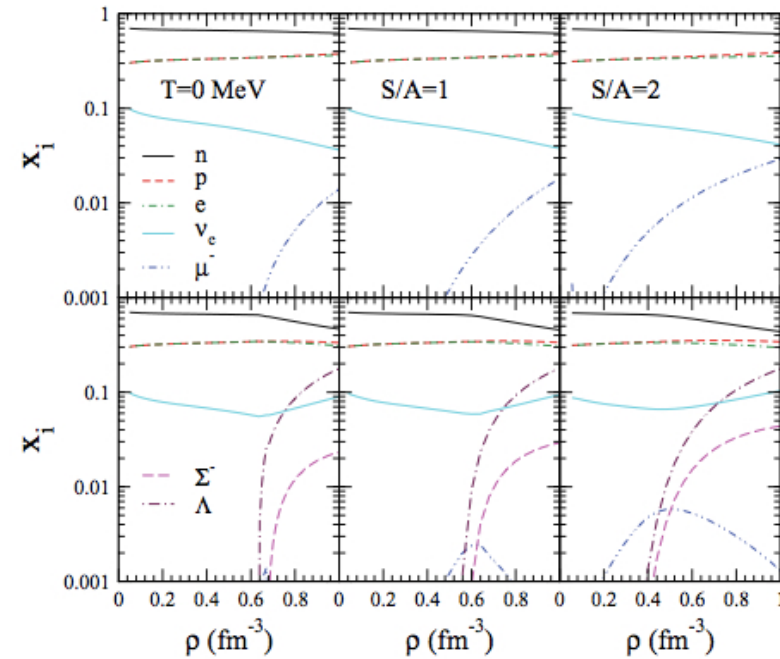
(Burgio & Schulze 2011)



■ Neutrino trapped

$$\mu_\nu \neq 0$$

(Burgio & Schulze 2011)



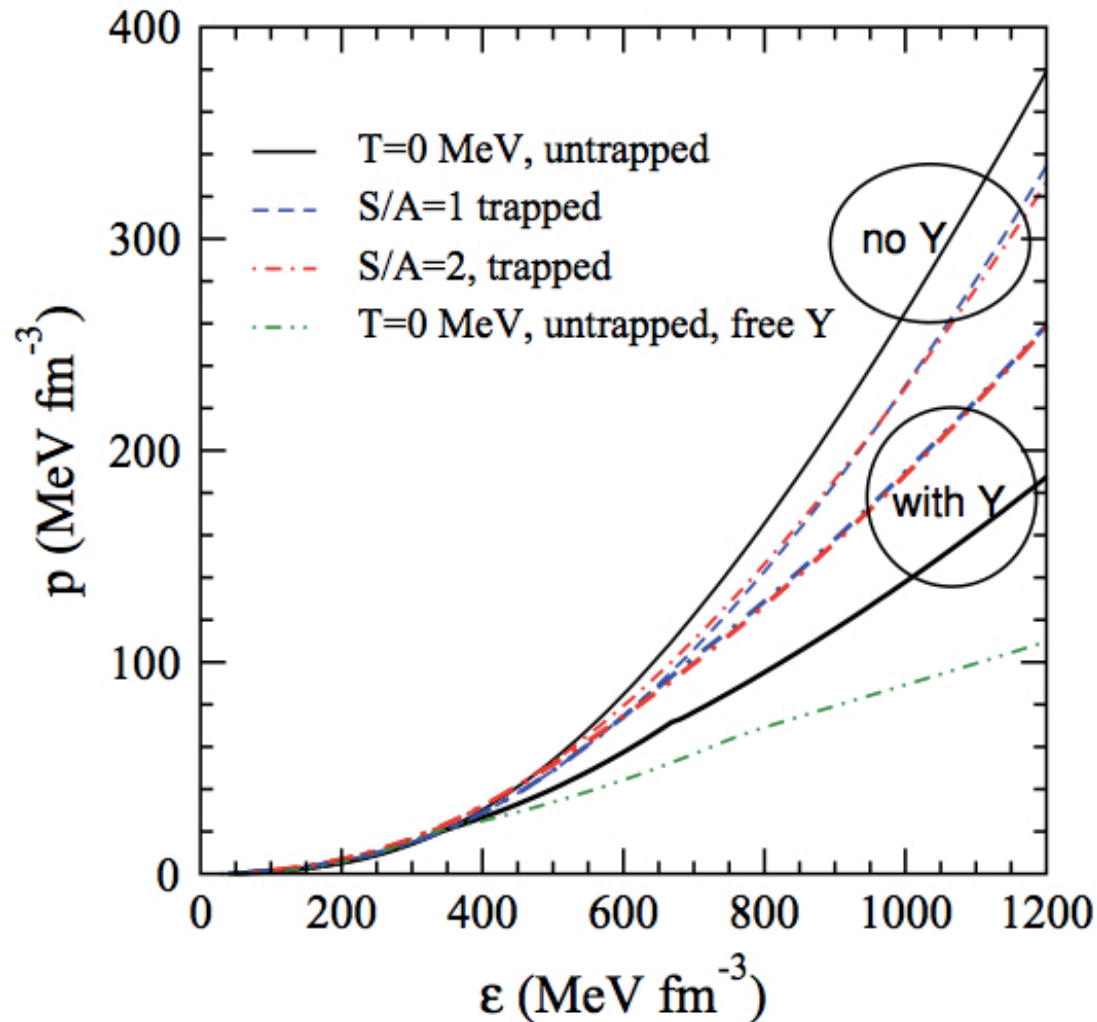
Neutrino trapped



- ✓ Large proton fraction
- ✓ Small number of muons
- ✓ Onset of $\Sigma^-(\Lambda)$ shifted to higher (lower) density
- ✓ Hyperon fraction lower in n-trapped matter

Proto-Neutron Stars: EoS

(Burgio & Schulze 2011)



■ Nucleonic matter

✧ ν -trapping + temperature
→ softer EoS

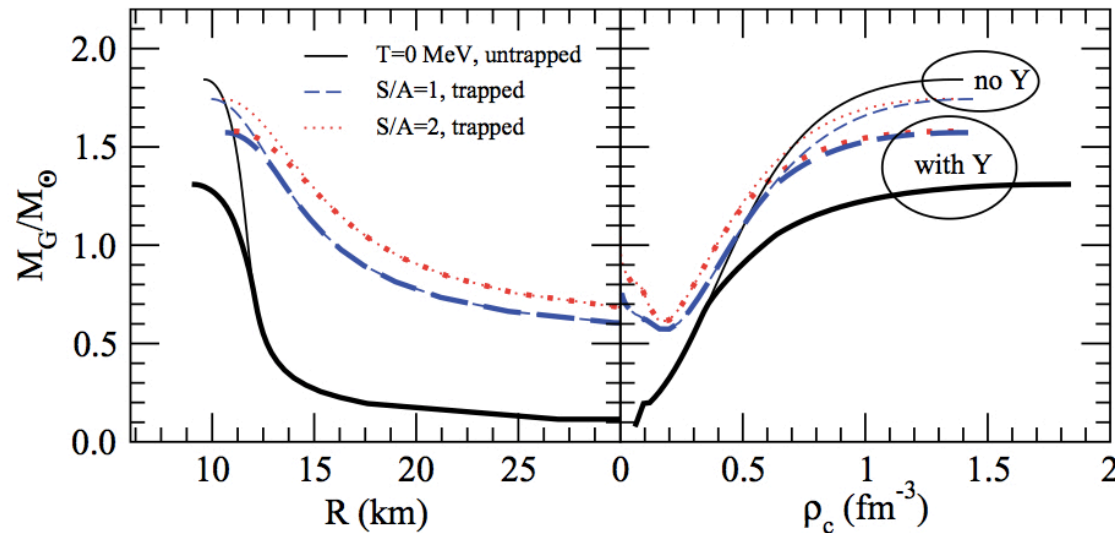
■ Hyperonic matter

✧ ν -trapping + temperature
→ stiffer EoS

✧ More hyperon softening
in ν -untrapped matter
(larger hyperon fraction)

Proto-Neutron Stars: Structure

(Burgio & Schulze 2011)



Hyperonic matter

ν -trapping + T:
increase of M_{max}

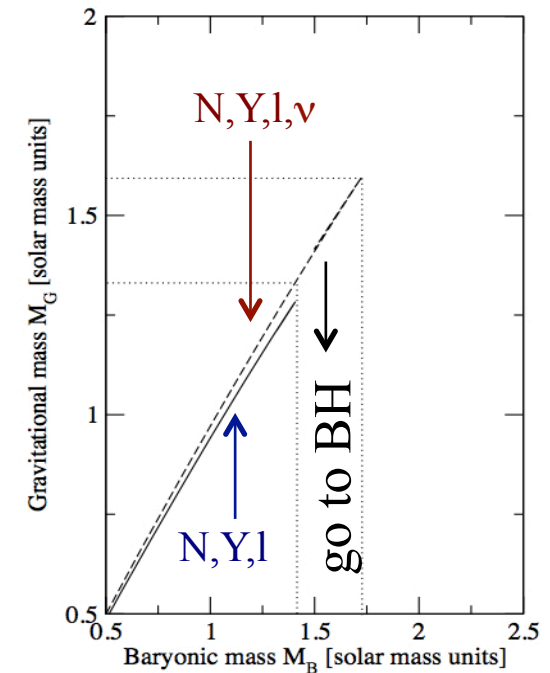


delayed formation
of a low mass BH

Nucleonic matter

ν -trapping + T:
reduction of M_{max}

(IV et al. 2003)





Hyperons & Neutron Star Cooling

Neutron Star Cooling in a Nutshell

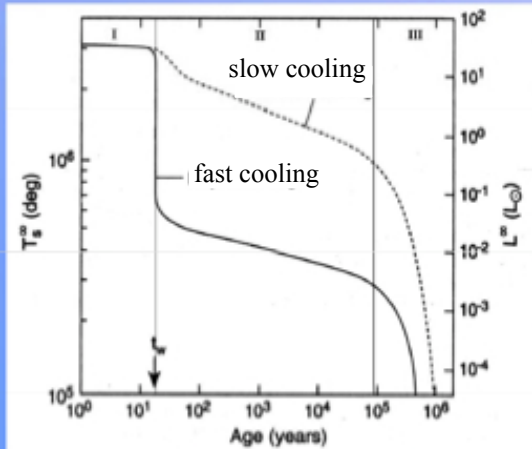
Two cooling regimes

Slow

Low NS mass

Fast

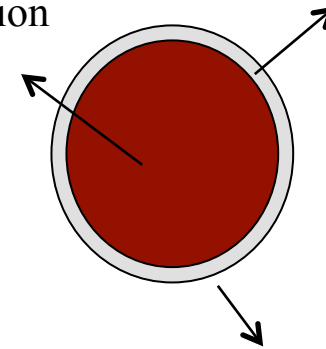
High NS mass



- I. Core relaxation epoch
- II. Neutrino cooling epoch
- III. Photon cooling epoch

Core cools by
neutrino emission

Crust cools by
conduction



Surface photon emission
dominates at $t > 10^6$ yrs

$$\frac{dE_{th}}{dt} = C_v \frac{dT}{dt} = -L_\gamma - L_\nu + H$$

- ✓ C_v : specific heat
- ✓ L_γ : photon luminosity
- ✓ L_ν : neutrino luminosity
- ✓ H : “heating”

Neutrino Emission

Name	Process	Emissivity	
Direct URCA	$n \rightarrow p + l + \bar{\nu}_l$ $p + l \rightarrow n + \nu_l$	$\sim T^6$	Fast
Modified URCA	$N + n \rightarrow N + p + l + \bar{\nu}_l$ $N + p + l \rightarrow N + n + \nu_l$	$\sim T^8$	Slow
Bremsstrahlung	$N + N \rightarrow N + N + \nu + \bar{\nu}$	$\sim T^8$	Slow
Cooper pair formation	$n + n \rightarrow [nn] + \nu + \bar{\nu}$ $p + p \rightarrow [pp] + \nu + \bar{\nu}$	$\sim T^7$	Medium

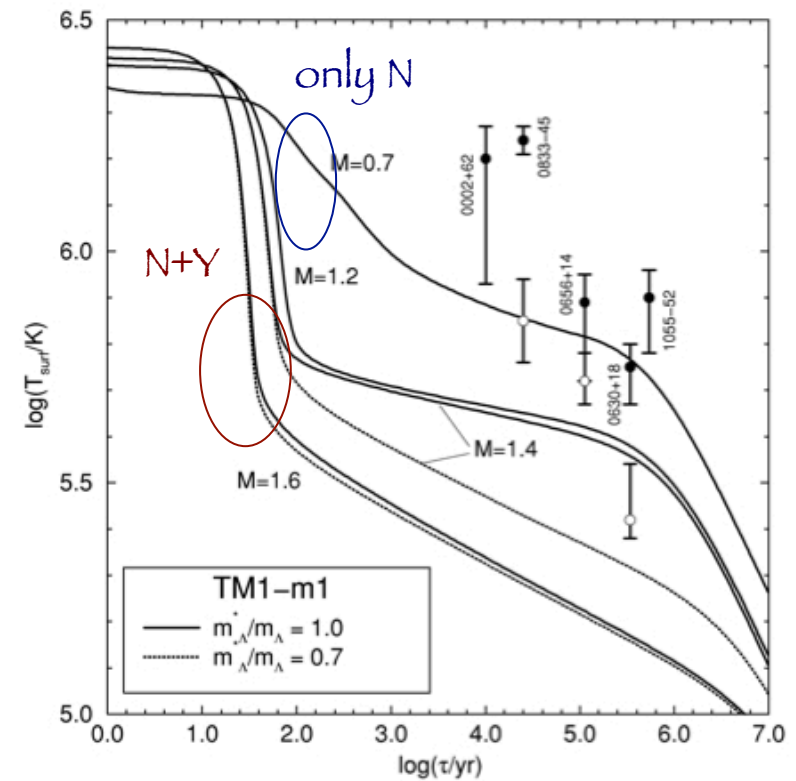
Hyperonic DURCA processes possible
 as soon as hyperons appear
 (nucleonic DURCA requires $x_p > 11-15\%$)

➔ Additional
 Fast Cooling
 Processes

Process	R
$\Lambda \rightarrow p + l + \bar{\nu}_l$	0.0394
$\Sigma^- \rightarrow n + l + \bar{\nu}_l$	0.0125
$\Sigma^- \rightarrow \Lambda + l + \bar{\nu}_l$	0.2055
$\Sigma^- \rightarrow \Sigma^0 + l + \bar{\nu}_l$	0.6052
$\Xi^- \rightarrow \Lambda + l + \bar{\nu}_l$	0.0175
$\Xi^- \rightarrow \Sigma^0 + l + \bar{\nu}_l$	0.0282
$\Xi^0 \rightarrow \Sigma^+ + l + \bar{\nu}_l$	0.0564
$\Xi^- \rightarrow \Xi^0 + l + \bar{\nu}_l$	0.2218

+ partner reactions generating neutrinos,
 Hyperonic MURCA, ...

(Schaab, Shaffner-Bielich & Balberg 1998)

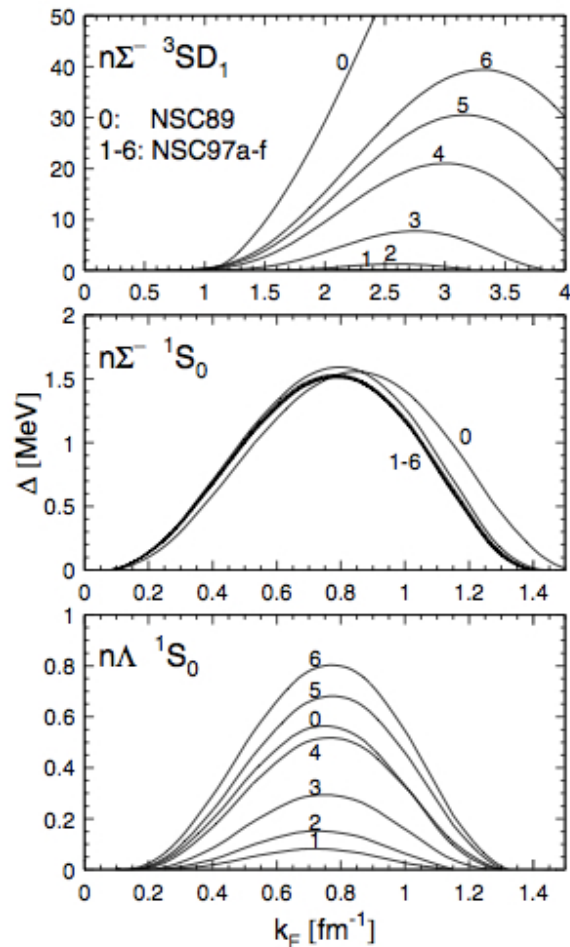


R: relative emissivity w.r.t. nucleonic DURCA

Pairing Gap \longrightarrow suppression of C_v & ϵ by

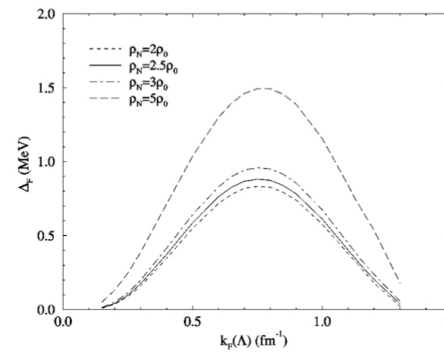
$$\sim e^{(-\Delta/k_B T)}$$

■ 1S_0 , 3SD_1 ΣN & 1S_0 ΛN gap

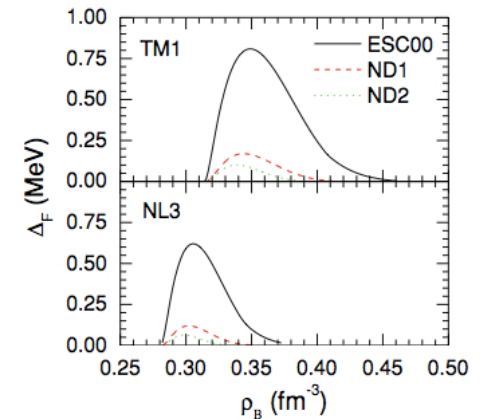


(Zhou, Schulze, Pan & Draayer 2005)

■ 1S_0 $\Lambda\Lambda$ gap

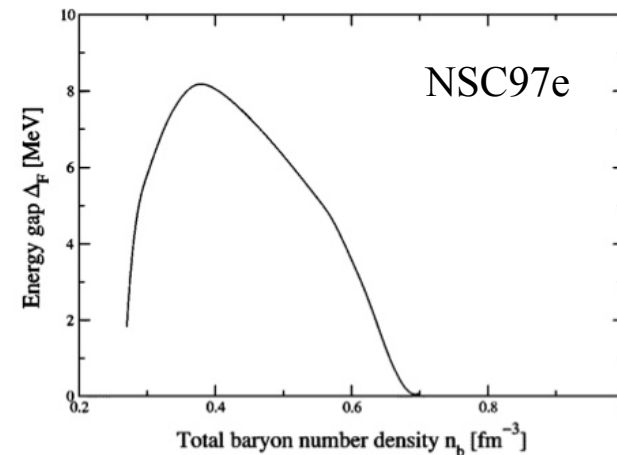


(Balberg & Barnea 1998)



(Wang & Shen 2010)

■ 1S_0 $\Sigma\Sigma$ gap



(IV & Tolós 2004)

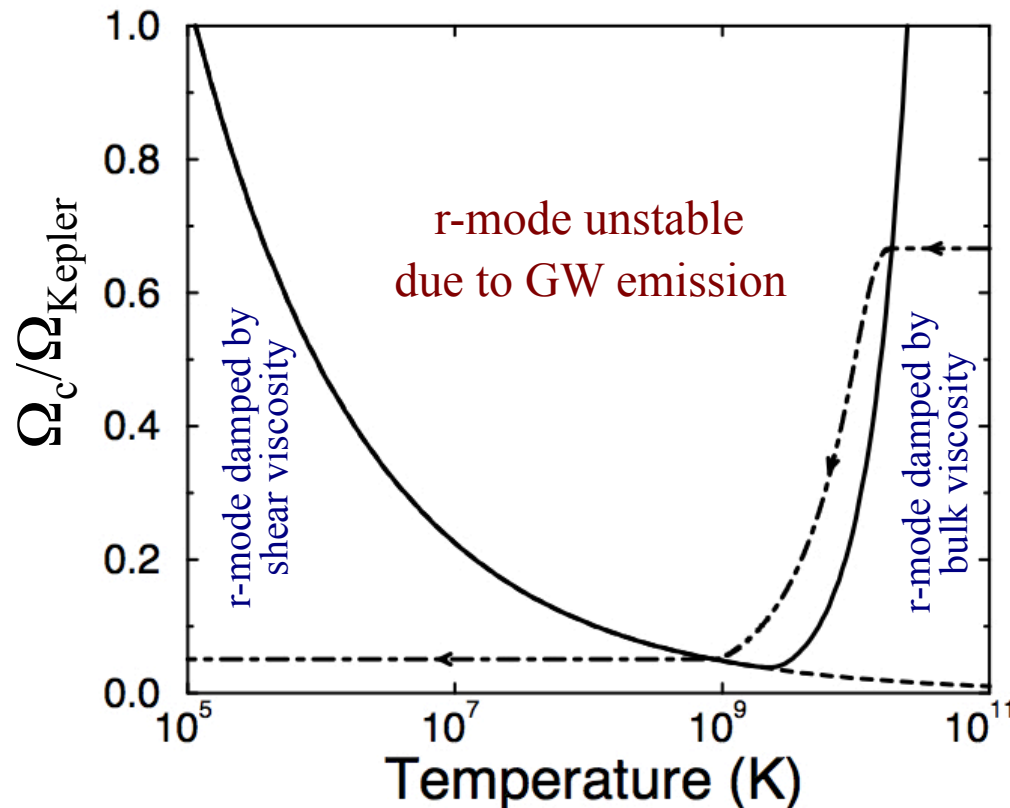
The background of the slide is a reproduction of the Japanese woodblock print 'The Great Wave off Kanagawa' by Katsushika Hokusai. It depicts a massive, curling blue wave with white foam, threatening three small boats on the sea. In the distance, the snow-capped Mount Fuji is visible under a pale, hazy sky. The text is overlaid on the central part of the image.

**Hyperons & the R-mode
instability of Neutron Stars**

The R-mode Instability

Ω_{Kepler} : Absolute Upper Limit
of Rot. Freq.

Instabilities prevent NS
to reach Ω_{Kepler}



R-mode Instability : toroidal mode
of oscillation

- ✓ restoring force: Coriolis
- ✓ emission of GW in hot & rapidly rotating NS (CFS mechanism)

- GW makes the mode unstable
- Viscosity stabilizes the mode

$$A \propto A_0 e^{-i\omega(\Omega)t - t/\tau(\Omega, T)}$$

$$\frac{1}{\tau(\Omega, T)} = -\frac{1}{\tau_{\text{GW}}(\Omega)} + \frac{1}{\tau_{\text{Viscosity}}(\Omega, T)}$$

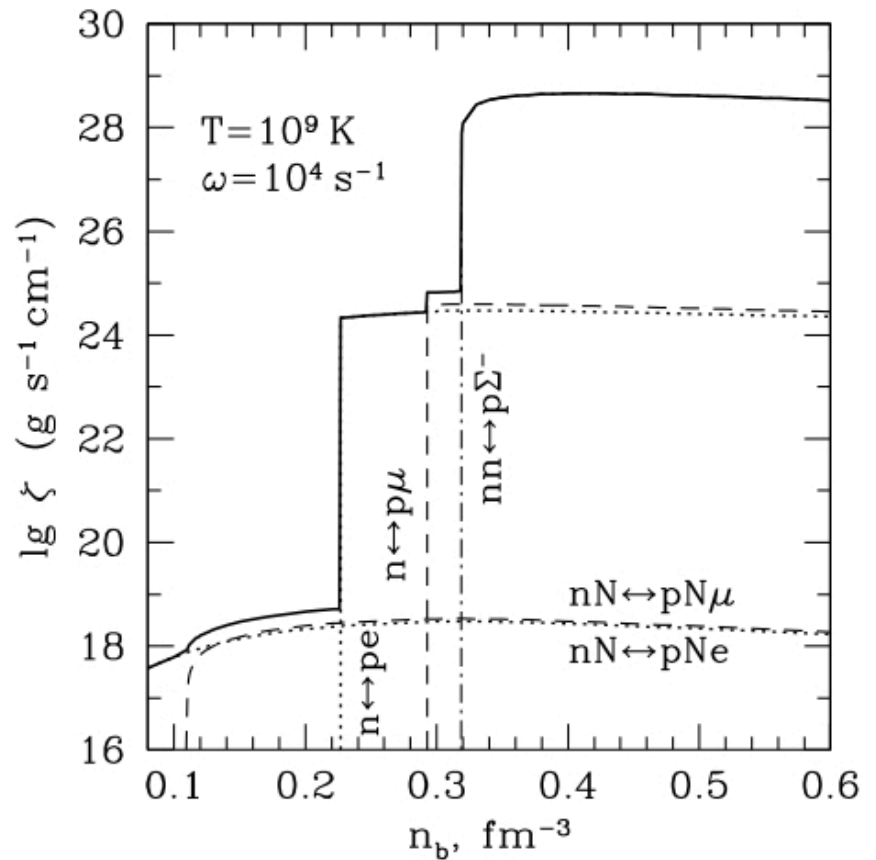
Hyperon Bulk Viscosity ξ_Y

(Lindblom et al. 2002, Haensel et al 2002, van Dalen et al. 2002, Chatterjee et al. 2008, Gusakov et al. 2008, Shina et al. 2009, Jha et al. 2010,...)

Sources of ξ_Y :

non-leptonic weak reactions	$N + N \leftrightarrow N + Y$ $N + Y \leftrightarrow Y + Y$
Direct & Modified URCA	$Y \rightarrow B + l + \bar{\nu}_l$ $B' + Y \rightarrow B' + B + l + \bar{\nu}_l$
strong reactions	$N + Y \leftrightarrow N + Y$ $N + \Xi \leftrightarrow Y + Y$ $Y + Y \leftrightarrow Y + Y$

(Haensel, Levenfish & Yakovlev 2002)



Reaction Rates & ξ_Y reduced by
Hyperon Superfluidity

Critical Angular Velocity of Neutron Stars

- r-mode amplitude: $A \propto A_o e^{-i\omega(\Omega)t - t/\tau(\Omega)}$

$$\frac{1}{\tau(\Omega, T)} = -\frac{1}{\tau_{GW}(\Omega)} + \frac{1}{\tau_{\xi}(\Omega, T)} + \frac{1}{\tau_{\eta}(T)}$$

→ $\frac{1}{\tau(\Omega_c, T)} = 0$ r-mode instability region

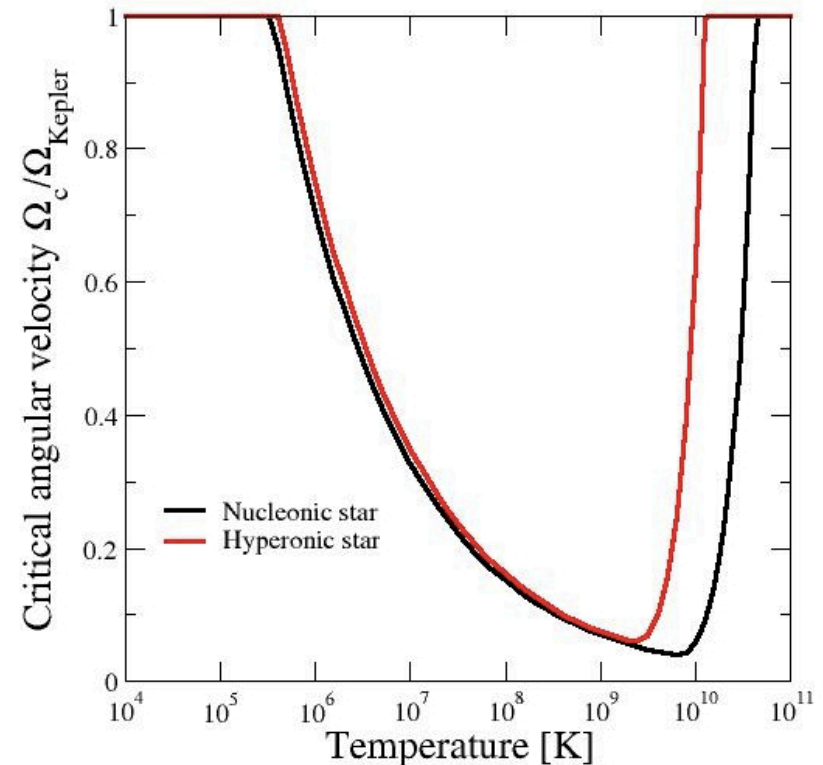
$\Omega < \Omega_c$ stable

$\Omega > \Omega_c$ unstable



As expected:
smaller r-mode instability region
due to hyperons

(I.V. & C. Albertus in preparation)



BHF: NN (Av18)+NY (NSC89)
($M=1.27M_{\odot}$)

Take away message



Strangeness adds a new dimension to nuclear physics & astrophysics which gives us the opportunity to study fundamental interactions from an enlarged perspective

- You for your time & attention
- The organizers for their invitation
- The sponsors for their support

