

# *A More Natural Higgs Sector at LHC*

Lawrence Hall

UC Berkeley

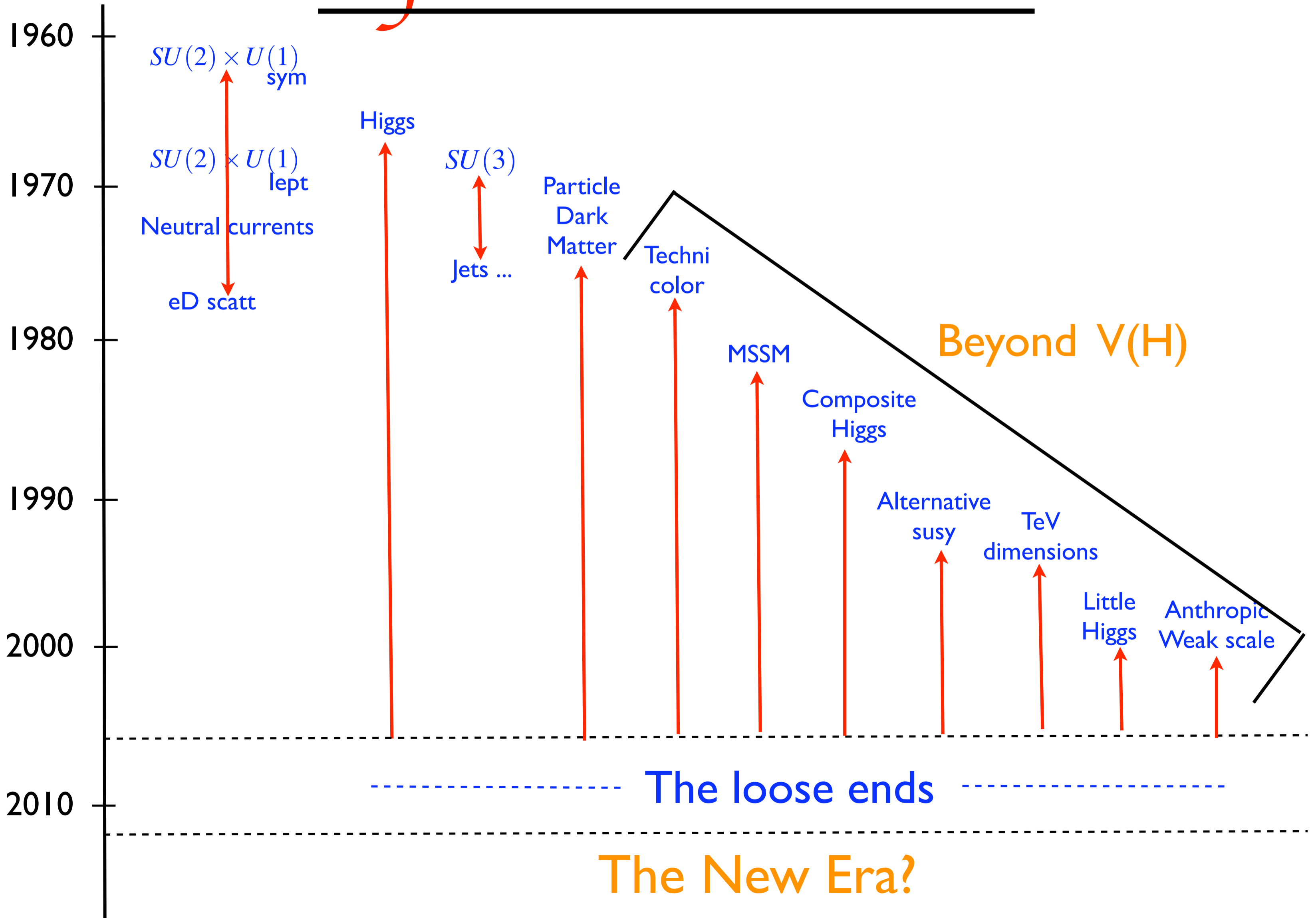
Based on

R. Barbieri, T. Gregoire and L.J.H., hep-ph/0509242

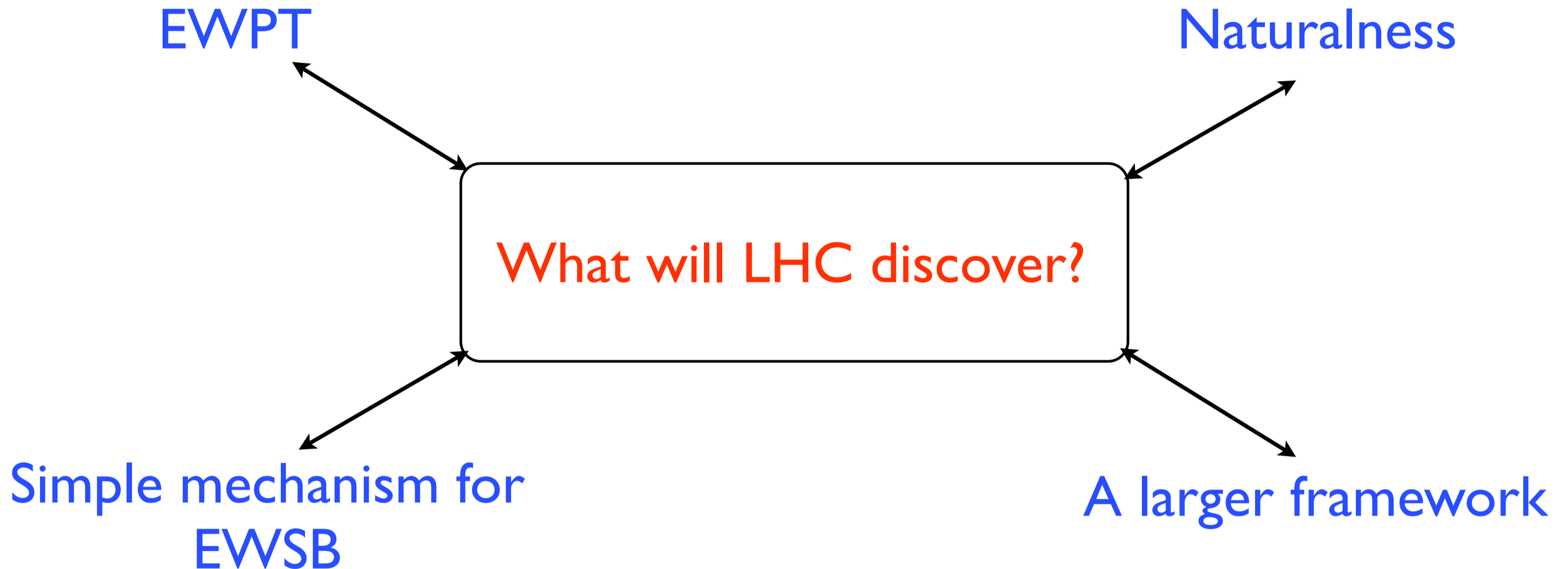
R. Barbieri and L.J.H., hep-ph/0510243

R. Barbieri, S. Rychkov and L.J.H., hep-ph/0603188

# After the SM ... ?



# Four Signposts



Supersymmetry is very successful on all four,  
and hard to beat on any one!

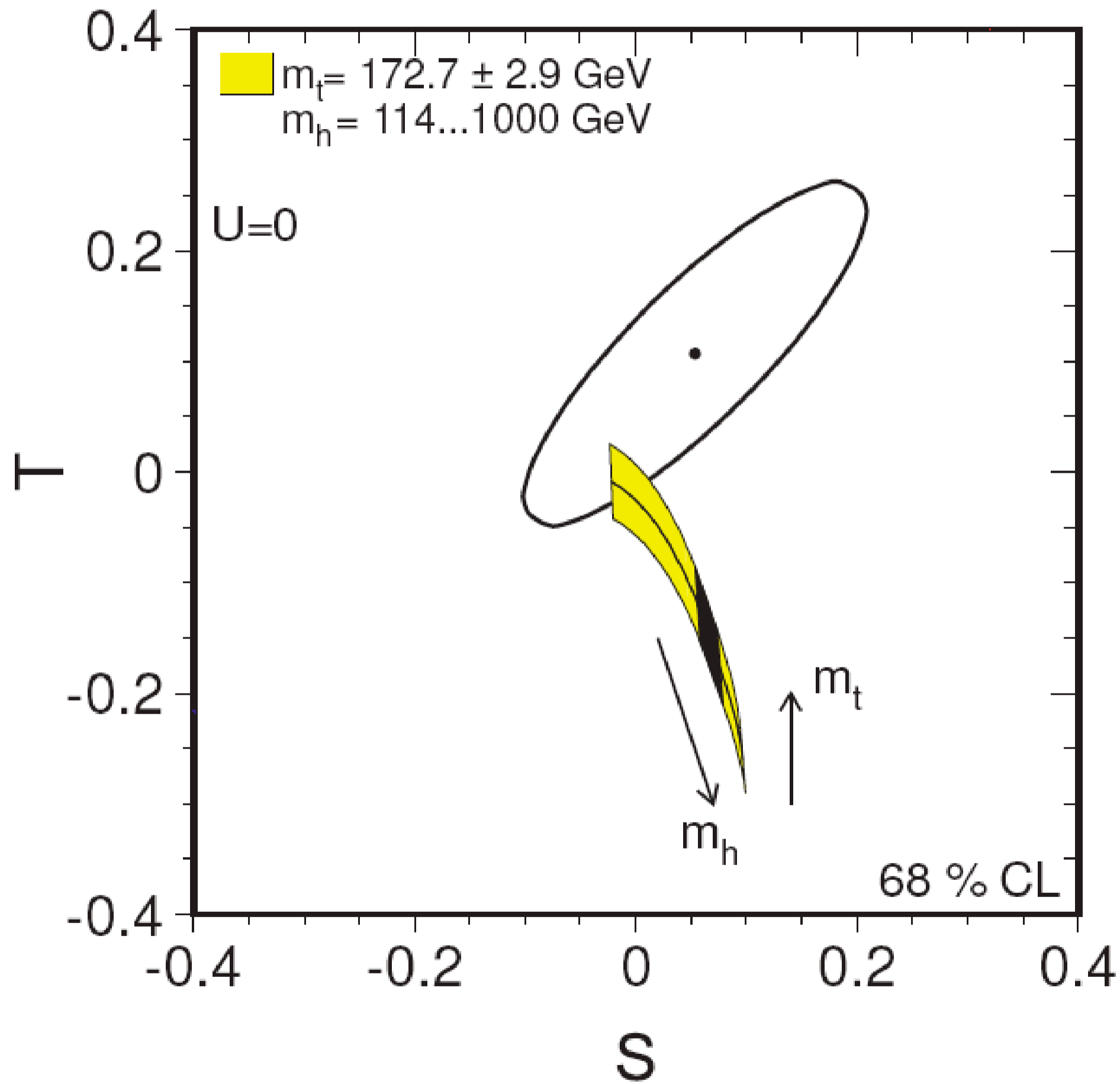
**But:**

- superpartners
- exotic flavor/CP
- light Higgs
- p decay

**If not susy: What?**

Ultra Bottom Up approach: EWPT & Naturalness

# EWPT and SM



SM Higgs  
is light!

Especially as TeVatron Run II finds  
a lower top mass.

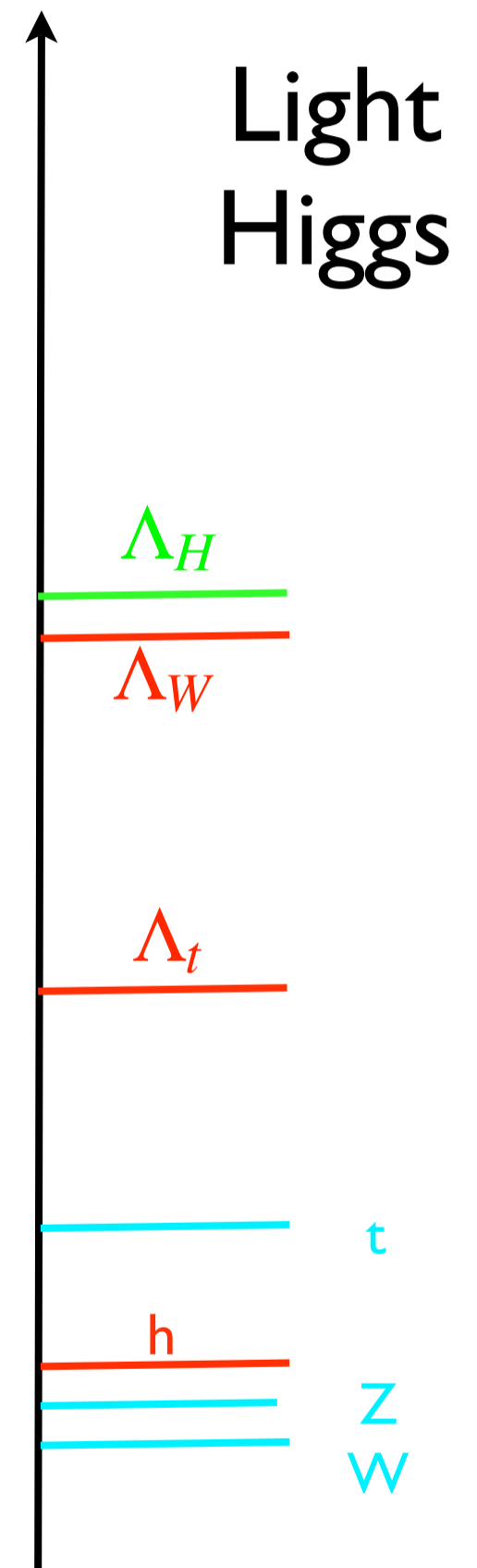
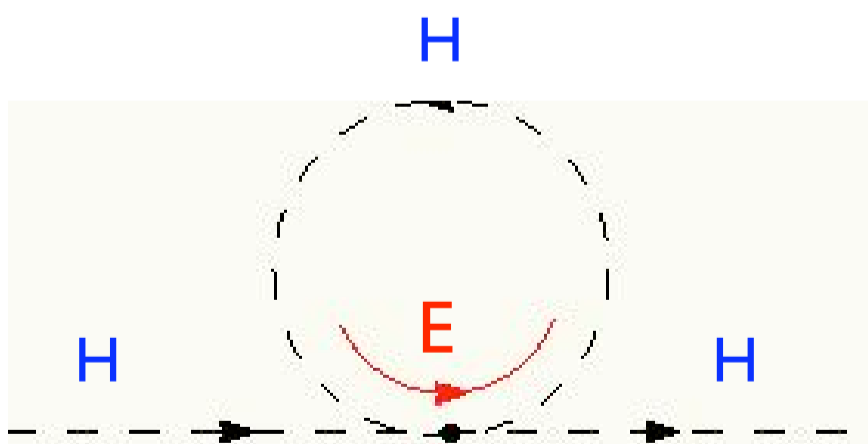
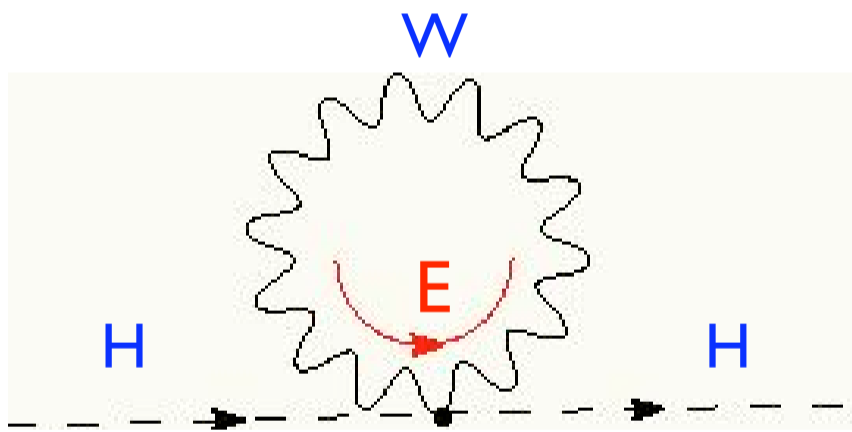
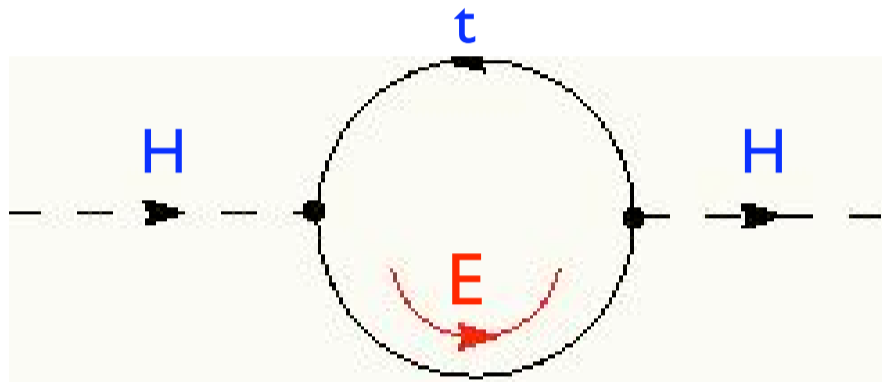
# Light SM Higgs $\longrightarrow$ Low SM Cutoff

$$\underline{E_{max} \longrightarrow \Lambda_{t,W,H}}$$

$$\Lambda_t = 400 \text{ GeV} \left( \frac{m_h}{115 \text{ GeV}} \right) D_t^{1/2}$$

$$\Lambda_W = 1.1 \text{ TeV} \left( \frac{m_h}{115 \text{ GeV}} \right) D_W^{1/2}$$

$$\Lambda_H = 1.3 \text{ TeV} D_H^{1/2}$$



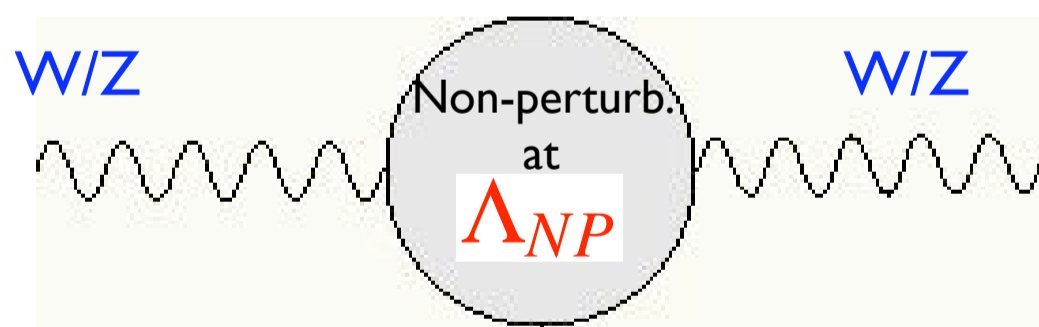
We expect to find “canceling” physics at  $\Lambda_{t,W,H}$

# TeV Scale Non-Perturbative Physics

No susy  $\longrightarrow$  non-perturbative physics at the TeV scale

(eg technicolor, composite Higgs, KK EWSB, BC EWSB, ...)

Expectations from EWPT for  $\Lambda_{NP}$



$$\Lambda_{NP} \geq 5-10 \text{ TeV}$$

$$(S, T) = (S, T)_{SM} \left( 1 + \frac{16\pi^2 v^2}{\Lambda_{NP}^2} \right)$$

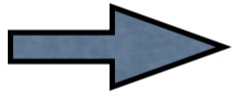
Contribution from light Higgs works well!

# The Little Hierarchy Problem

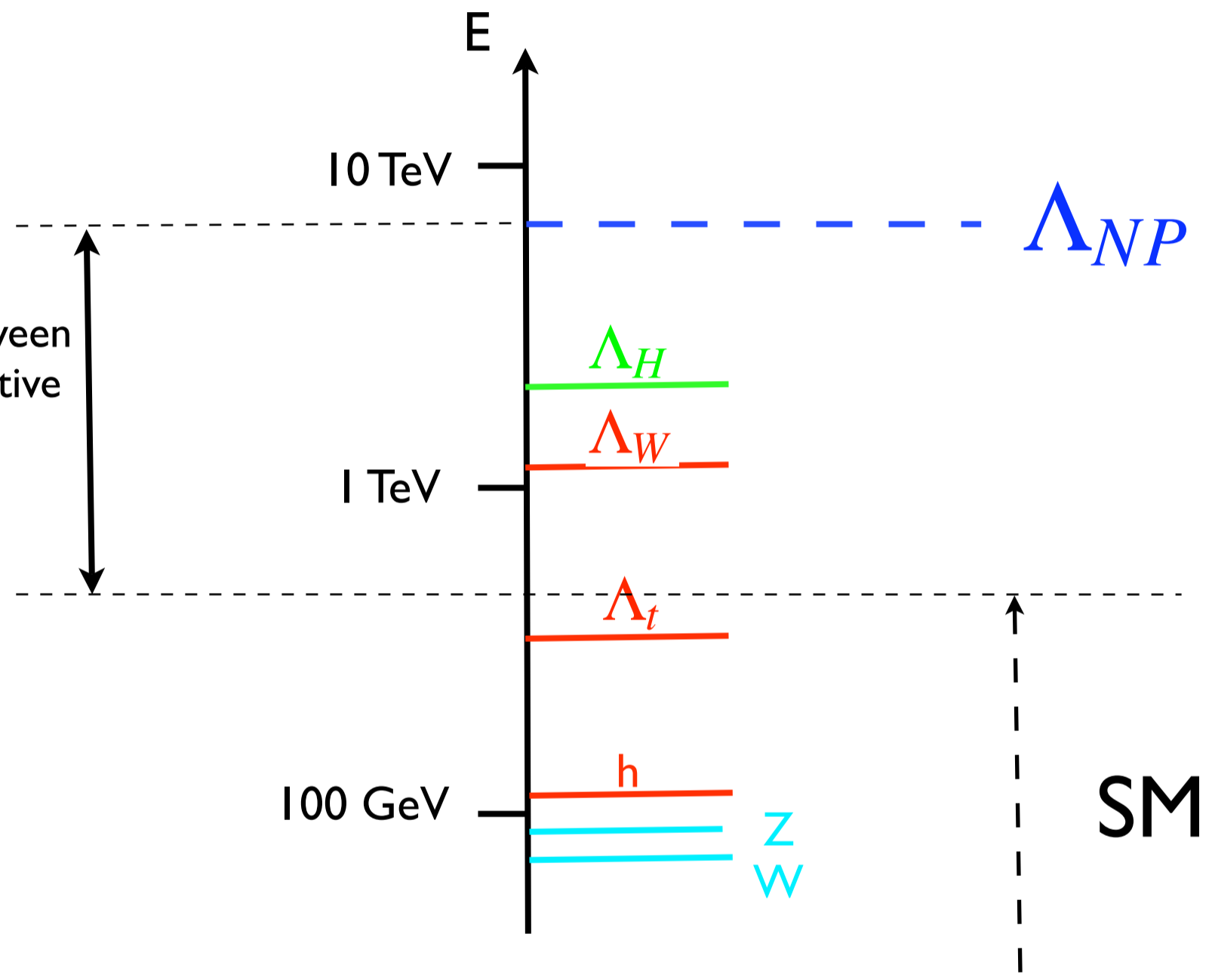
Barbieri, Strumia hep-ph/0007265

Applies to theories with low  $\Lambda_{NP}$

An energy interval of a factor of 10 between “cancellation” physics and non-perturbative physics.



1% fine-tune



In non-susy theories, what is the perturbative “cancellation” physics?



- How does it delay strong interactions?
- Does it satisfy EWPT?
- What are LHC signals?

# Beautiful Ideas for EWSB that have LHP

## Technicolor

The first and best BSM idea for EWSB

Strong interactions at TeV scale, but perturbative to Planck scale

## Supersymmetric SM in 5D

Boundary Conditions break supersymmetry at TeV scale

Higgs mass calculable

## Higgsless

EWSB directly by boundary conditions in extra dimensions

**LHP Hard to Solve**

Perhaps susy is right after all!

Little Higgs: considerable new physics; partial progress



# Improved Naturalness

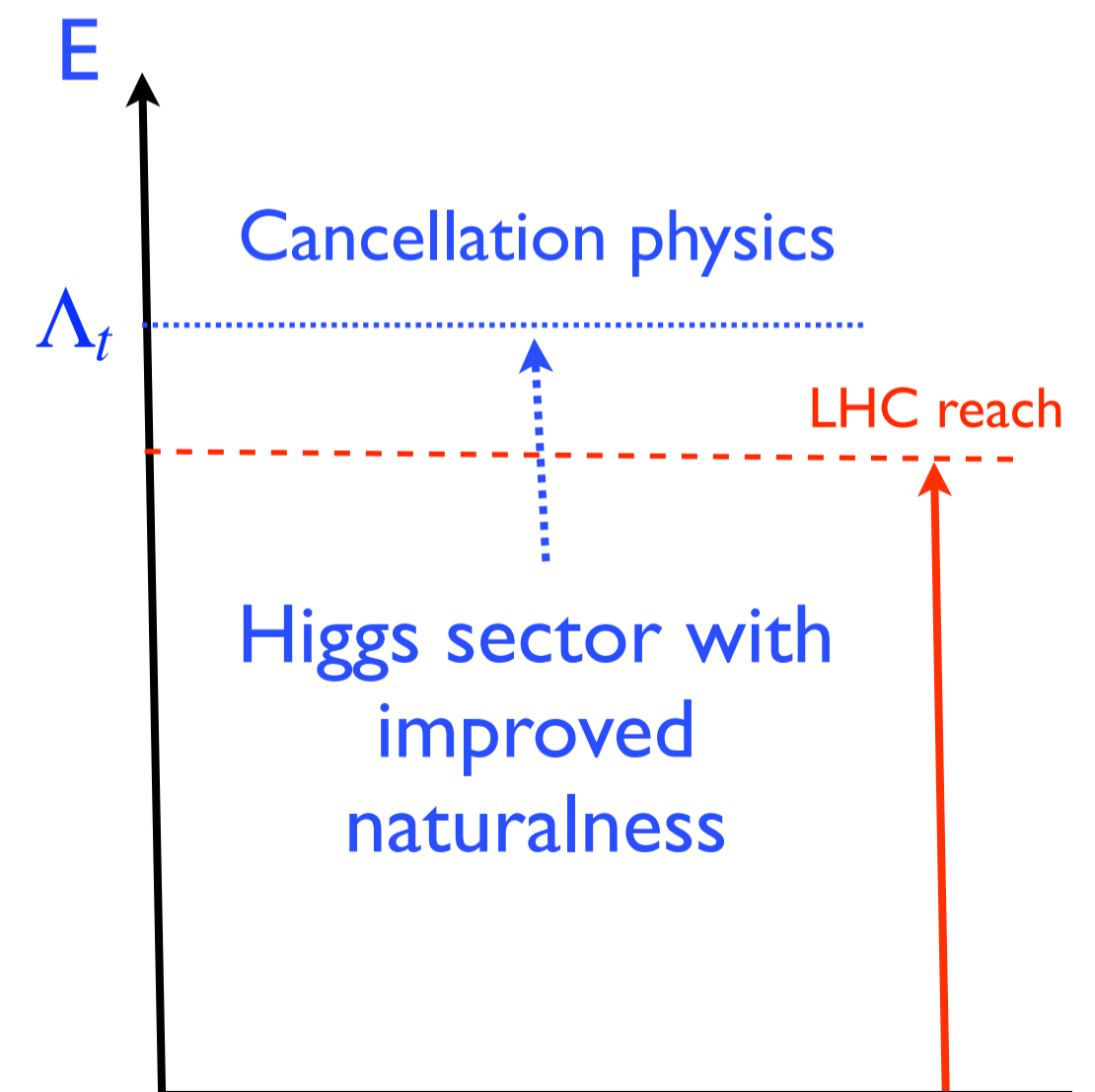
Seek simple Higgs sector that

- 1) agrees with all data (especially EWPT)
- 2) is completely natural up to 1.5 TeV

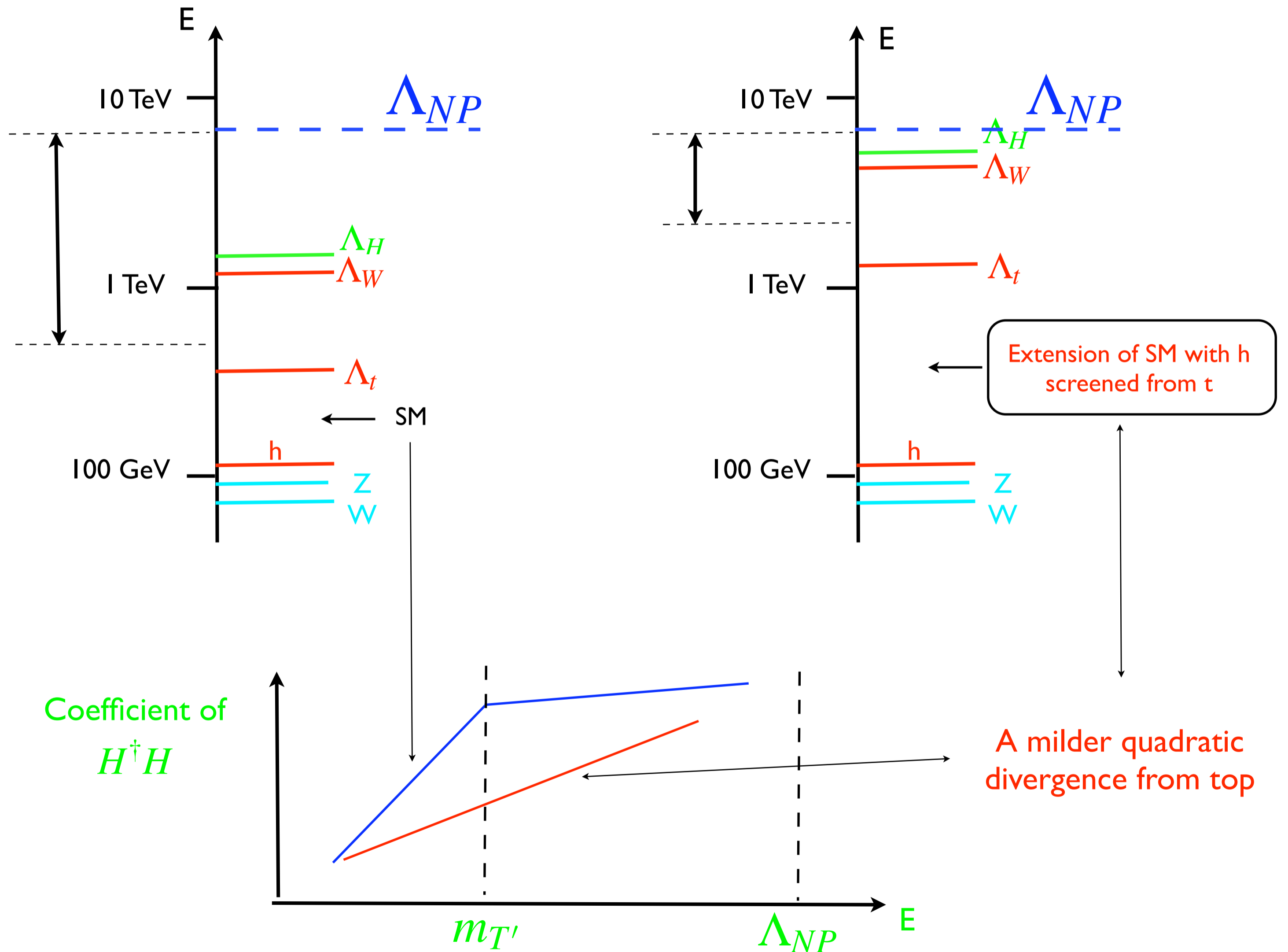
ie

cutoff is factor 3 higher  
 fine tuning is a factor 10 less } than SM with light Higgs

A modest “ultra bottom up” approach,  
with crucial consequences for the LHC



# Improving Naturalness: a Light Higgs



# Two scalars: one heavy, one light

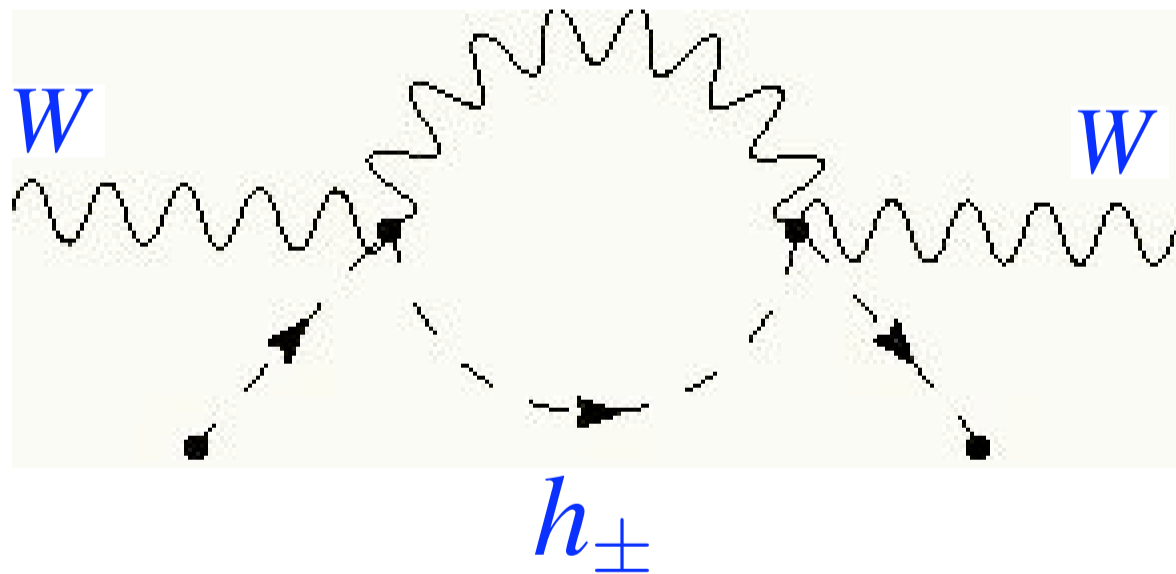
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$h_{1,2}$  mix to  $h_{\pm}$

Top couples to  $h_2$  which mainly  $h_+$  so

$$\Lambda_t \propto m_+$$

For EWPT, contribution to T from



$$\ln m_h \rightarrow \frac{v_1^2}{v^2} \ln m_- + \frac{v_2^2}{v^2} \ln m_+$$

$$m_+ < m_- \left( \frac{m_{EWPT}}{m_-} \right)^{1+v_1^2/v_2^2}$$

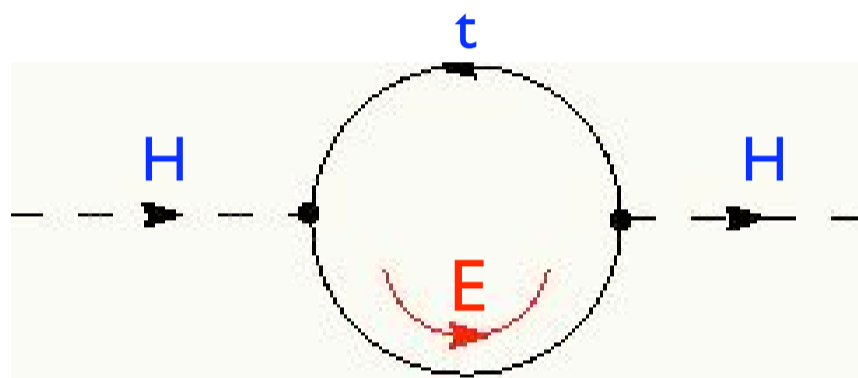
Two models  $\begin{cases} \text{Mirror world} \\ \text{Usual 2 Higgs doublet} \end{cases}$

R. Barbieri, T. Gregoire and LjH, hep-ph/0509242

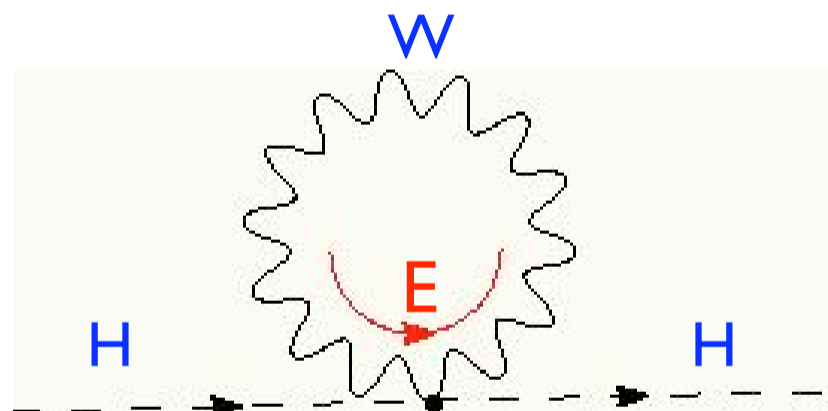
R. Barbieri and LjH, hep-ph/0510243

# Improving Naturalness with a Heavy Higgs

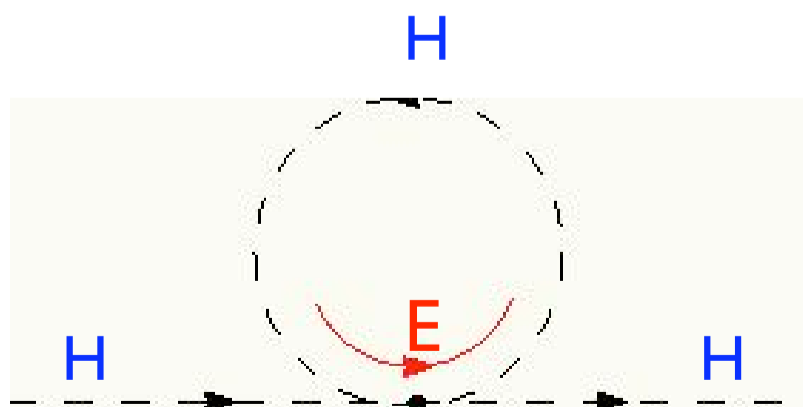
Recall SM:



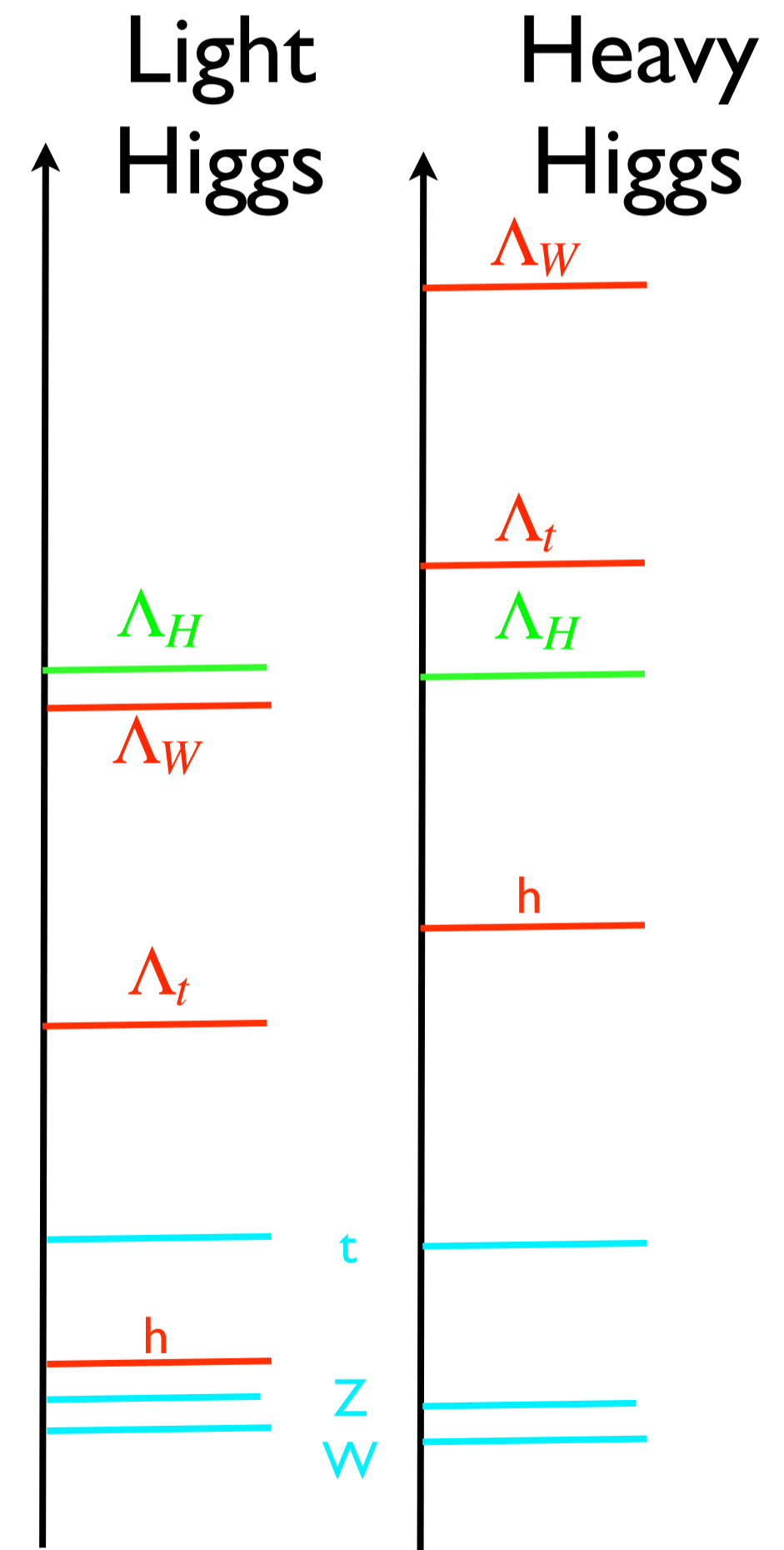
$$\Lambda_t = 400 \text{ GeV} \left( \frac{m_h}{115 \text{ GeV}} \right) D_t^{1/2}$$



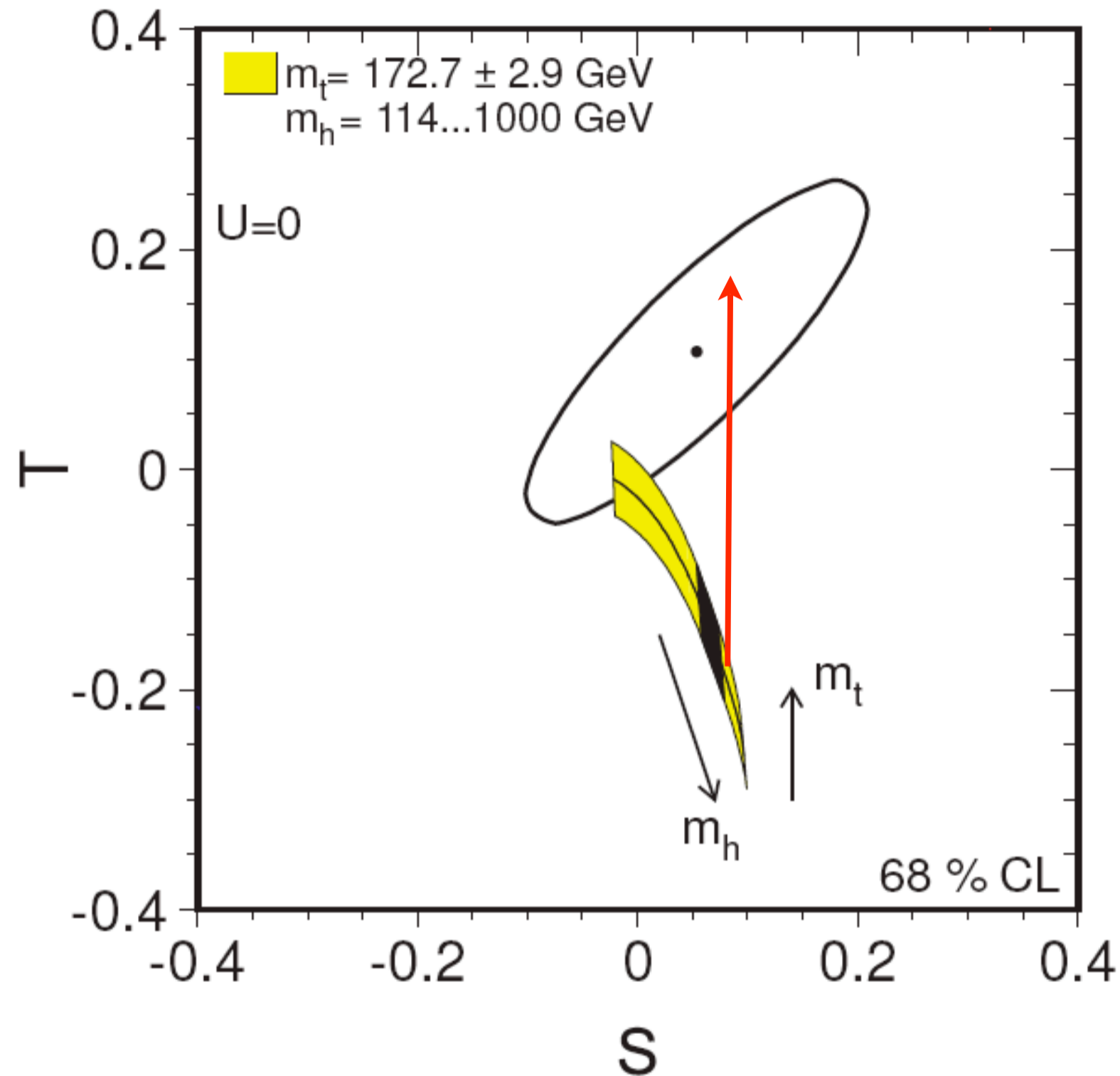
$$\Lambda_W = 1.1 \text{ TeV} \left( \frac{m_h}{115 \text{ GeV}} \right) D_W^{1/2}$$



$$\Lambda_H = 1.3 \text{ TeV} D_H^{1/2}$$



# A Heavy SM Higgs and EWPT



Heavy Higgs with positive  
 $\Delta T$

No fine tuning!!!

Origin of  $\Delta T$  (Peskin, Wells hep-ph/0101342)

SM + heavy triplet scalars

New gauge interaction

2 Higgs Doublets - both with vevs

- but often get trouble from 4 fermion operators

$$\Lambda_{H_i} = 1.3 \text{ TeV} (\cos \beta, \sin \beta)$$

# 2 $HDM$ in an Alternative Phase

Barbieri, Hall, Rychkov, hep-ph/0603188

$$V = -\mu_1^2 H_1^\dagger H_1 + \mu_2^2 H_2^\dagger H_2 + \text{quartics}$$

For natural flavor conservation impose

$$H_2 \rightarrow -H_2$$

Only  $H_1$  couples to matter



$$H_2 = \begin{pmatrix} H^+ \\ H + iA \end{pmatrix}$$

is "inert"



$$v_2 = 0$$

This is not the usual phase in the fine-tuned limit of

$$v_2 \ll v_1$$

1.  $H_1 = \begin{pmatrix} 0 \\ v + h \end{pmatrix}$  similar to SM Higgs
2.  $H_2$  mass splittings lead to  $\Delta T > 0$
3.  $H_2 \rightarrow -H_2$  is exact, and not spontaneously broken

Lightest Inert Particle (**LIP**) is stable and could be Dark Matter

# SM-like Doublet + Inert Doublet

## Higgs sector

$$H_1 = \begin{pmatrix} 0 \\ v+h \end{pmatrix}$$

Couples to fermions and is much like SM doublet; h heavy

$$\Lambda_t = 1.5 \text{ TeV} \left( \frac{m_h}{400 \text{ GeV}} \right) D_t^{1/2}$$

$$\Lambda_H = 1.3 \text{ TeV} D_H^{1/2}$$

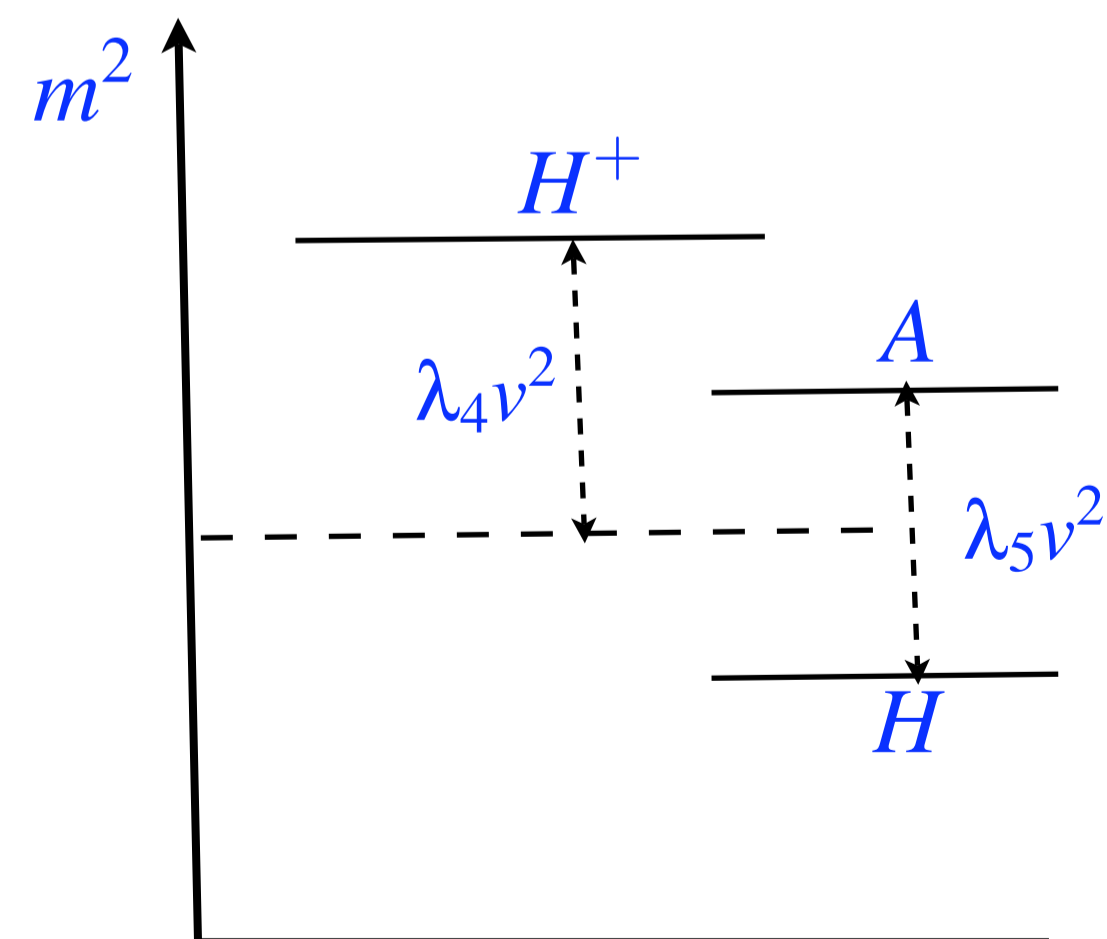
Perturbative up to 2 TeV

## Inert sector

$$H_2 = \begin{pmatrix} H^+ \\ H + iA \end{pmatrix}$$

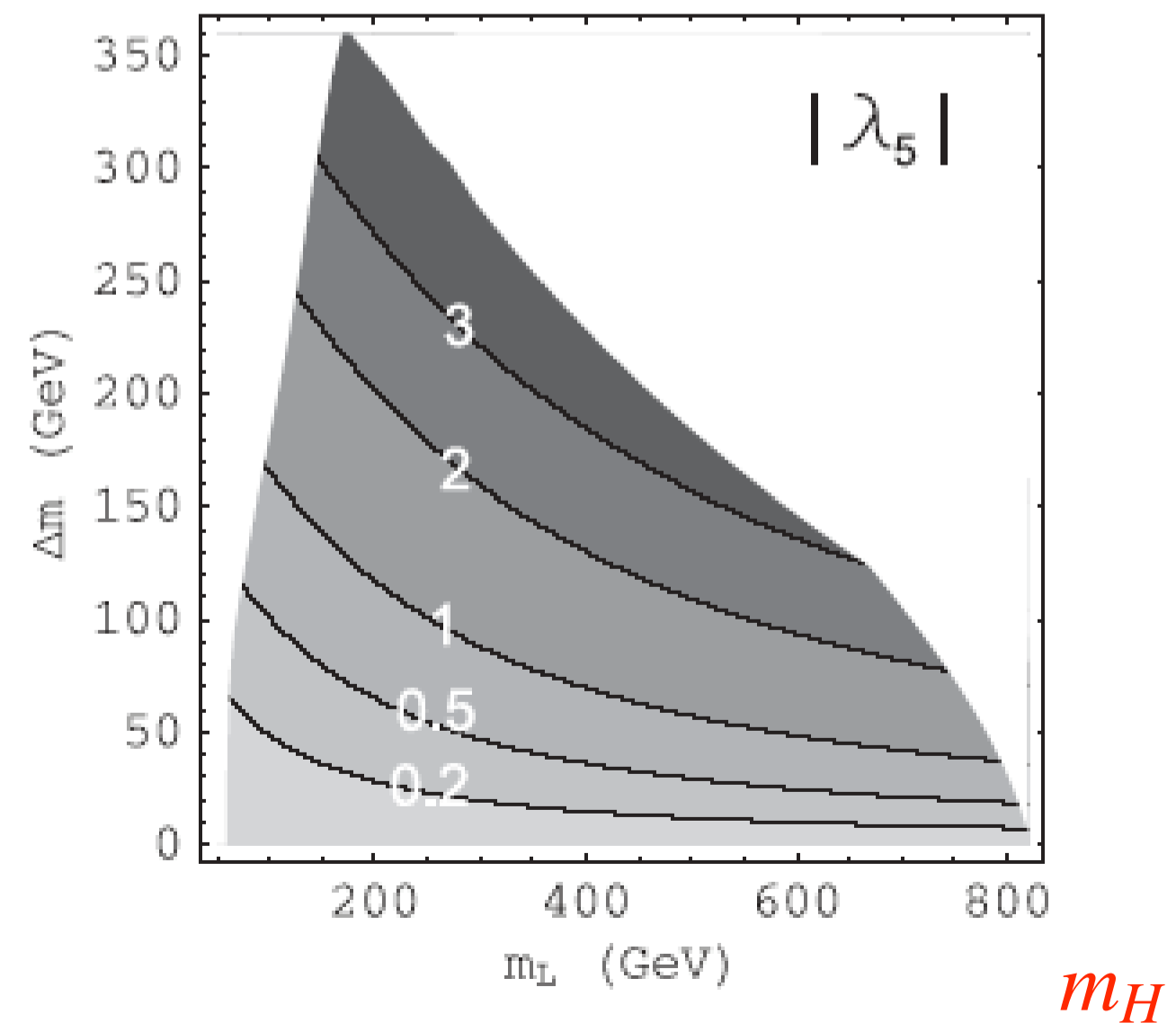
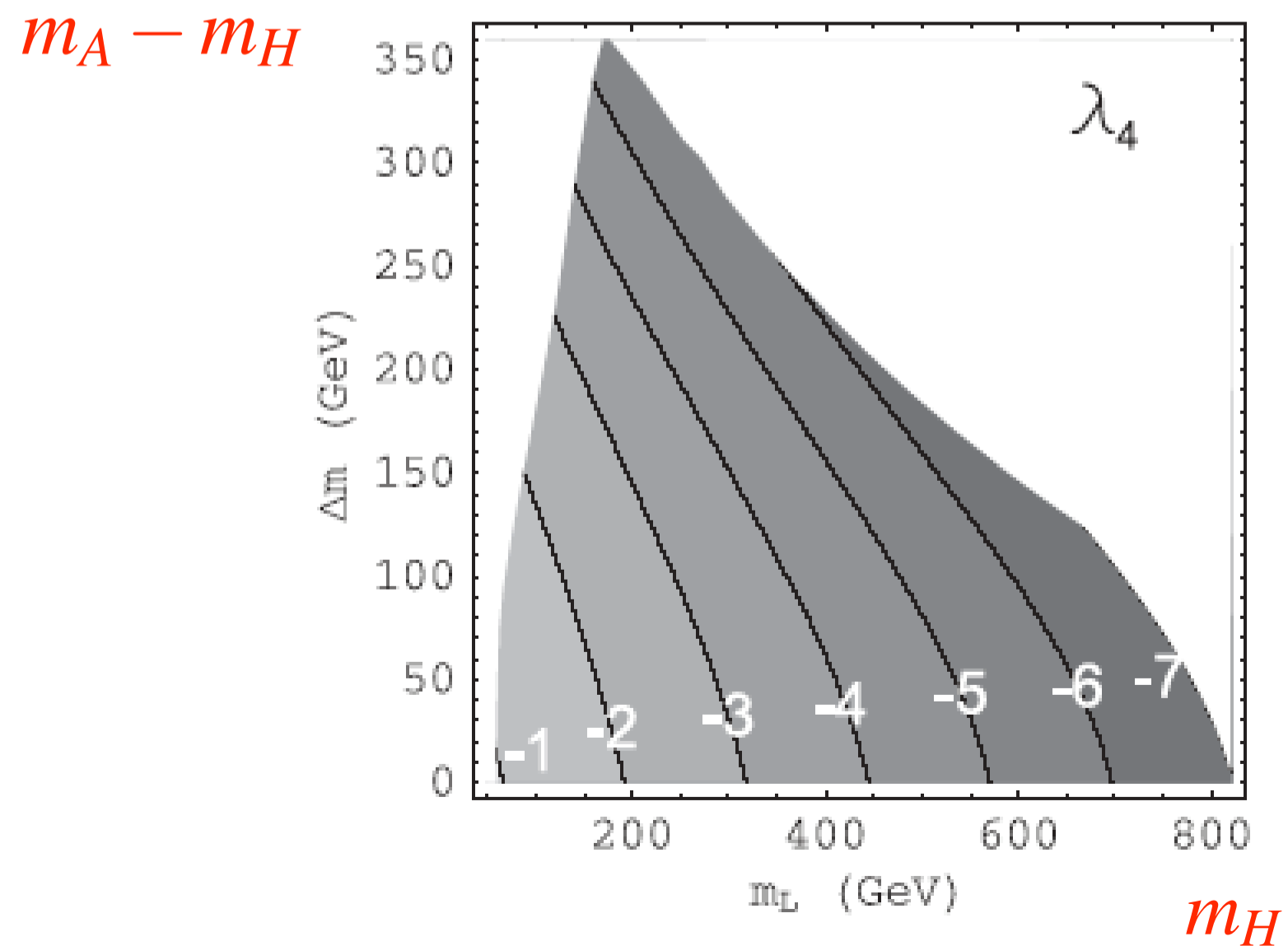
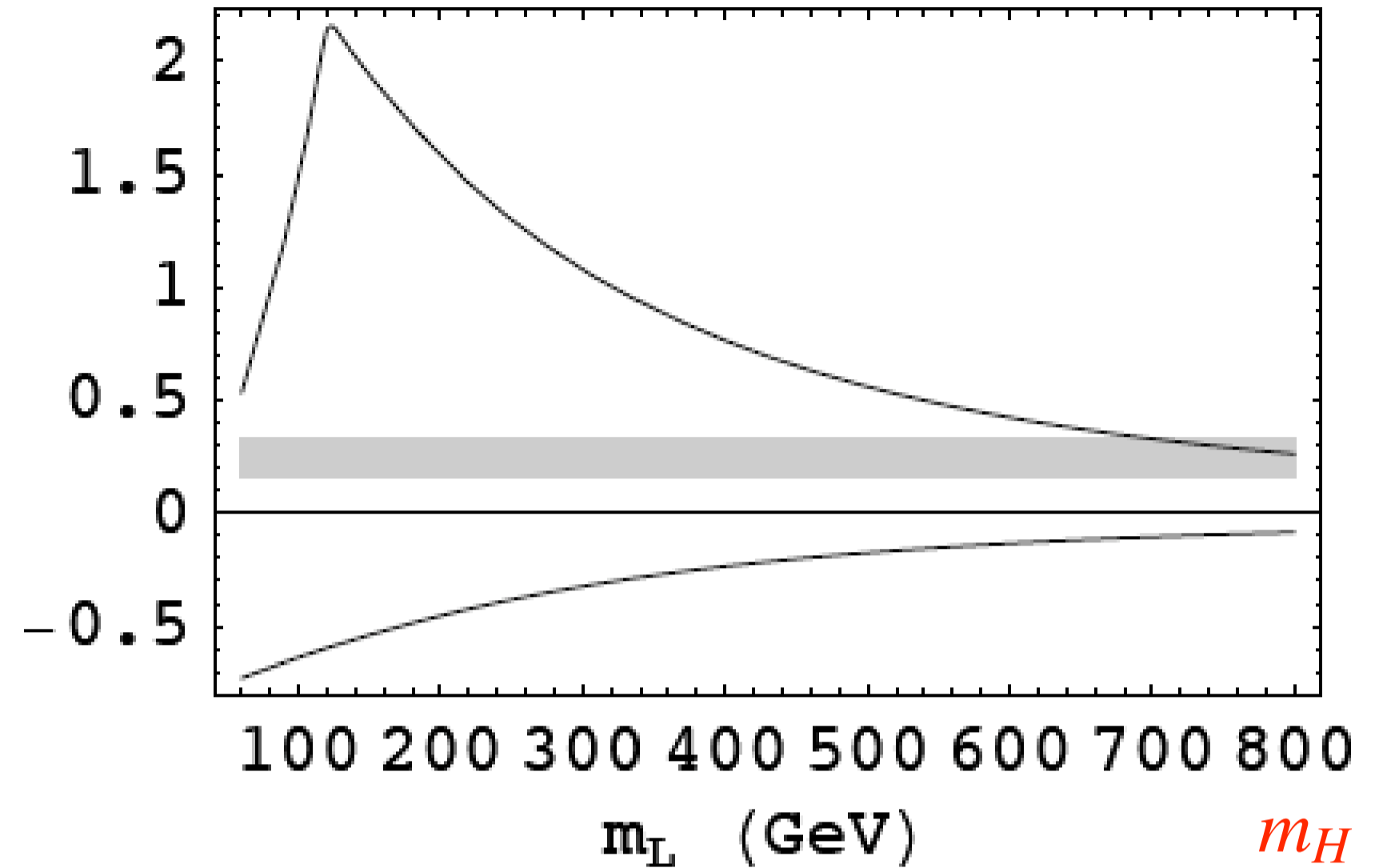
Custodial breaking masses for  $\Delta T$

$$(m_{H^+} - m_A)(m_{H^+} - m_H) \approx (120 \text{ GeV})^2$$



Ranges for:

$\Delta T, m_H, m_A - m_H$





# LTP Dark Matter

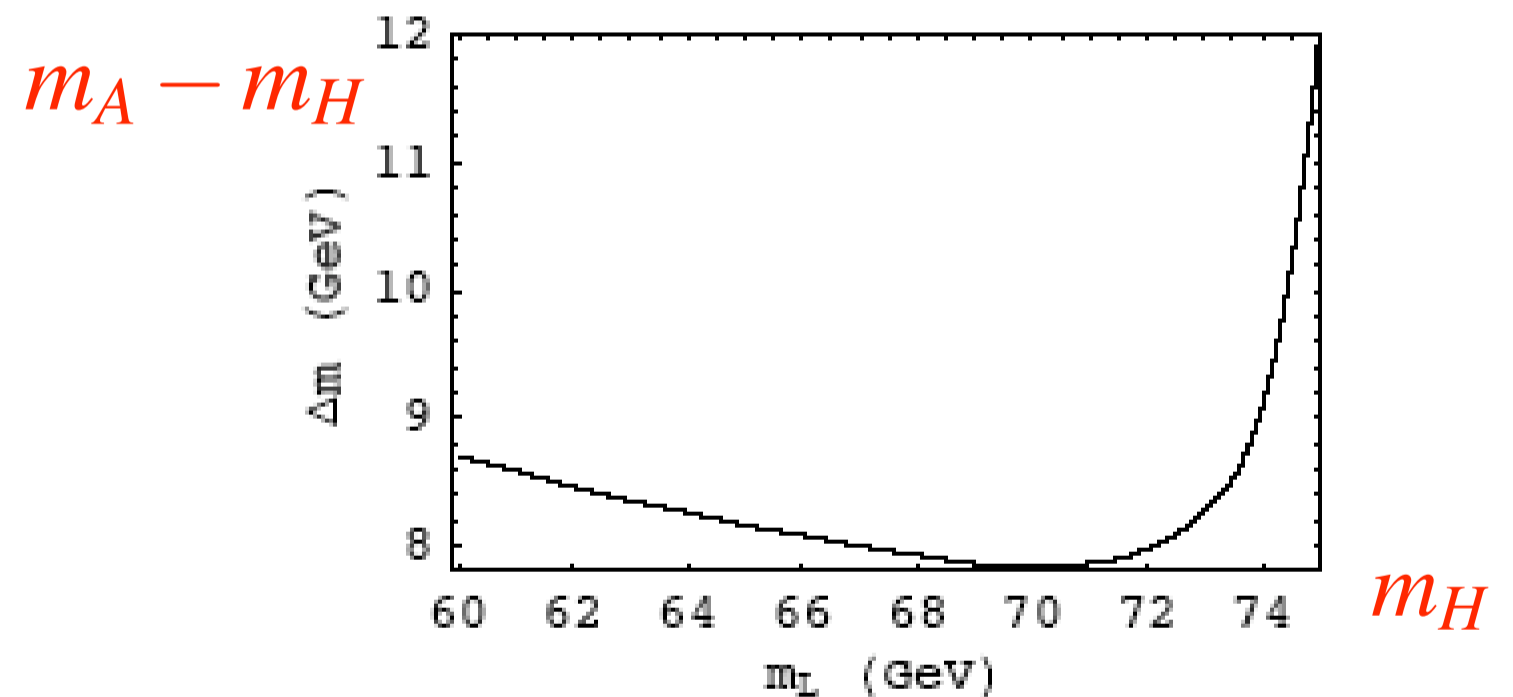
$m_H > m_W$

$HH \rightarrow W^+W^-$  Depletes H to a small fraction of the observed Dark Matter

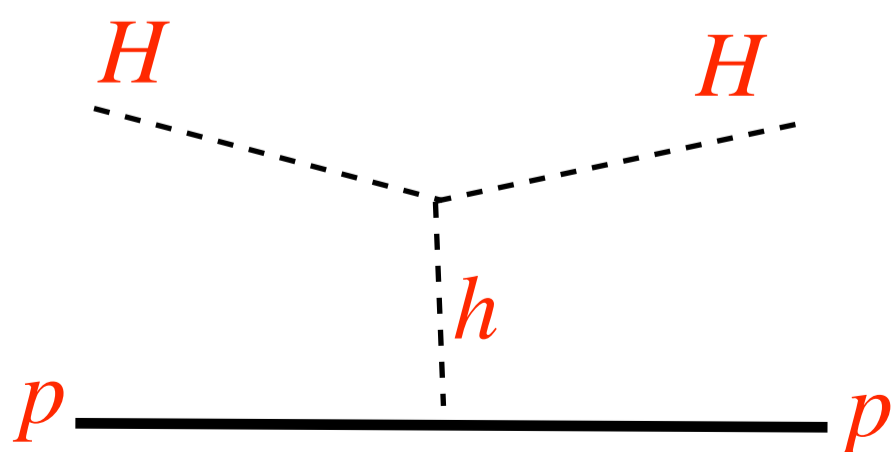
$m_H < m_W$

If A and H degenerate, then  $AH \rightarrow Z^* \rightarrow \bar{f}f$  over-depletes by about a factor 10

AH co-annihilation gives observed Dark Matter if:



Direct detection



$$\sigma(Hp \rightarrow Hp) \approx 2 \times 10^{-9} \text{ pb} \left( \frac{70 \text{ GeV}}{m_H} \right)^2 \left( \frac{500 \text{ GeV}}{m_h} \right)^2 \left( \frac{\lambda_H}{0.5} \right)^2$$

About 2 orders of magnitude below the present Ge limit from CDMS

# LHC Signals of the Inert Doublet

Pair Production of inert particles:

$$pp \rightarrow AH, H^+H^-, AH^+, HH^+$$

followed by cascade decays:

$$H^+ \rightarrow W^+(A, H) \quad A \rightarrow Z^*H$$

Events with leptons, jets, missing transverse energy

## Tri-leptons in Dark Matter region

$$pp \rightarrow W^* \rightarrow AH^+ \rightarrow (H, Z^*) + (W^+H)$$

with  $Z^*$  and  $W$  decaying to leptons

$$\sigma \approx (0.25 \text{ pb})(0.015) \approx 3.5 \text{ fb}$$

Pythia      lept. BR

with  $\Delta m_{l+l^-} < 10 \text{ GeV}$

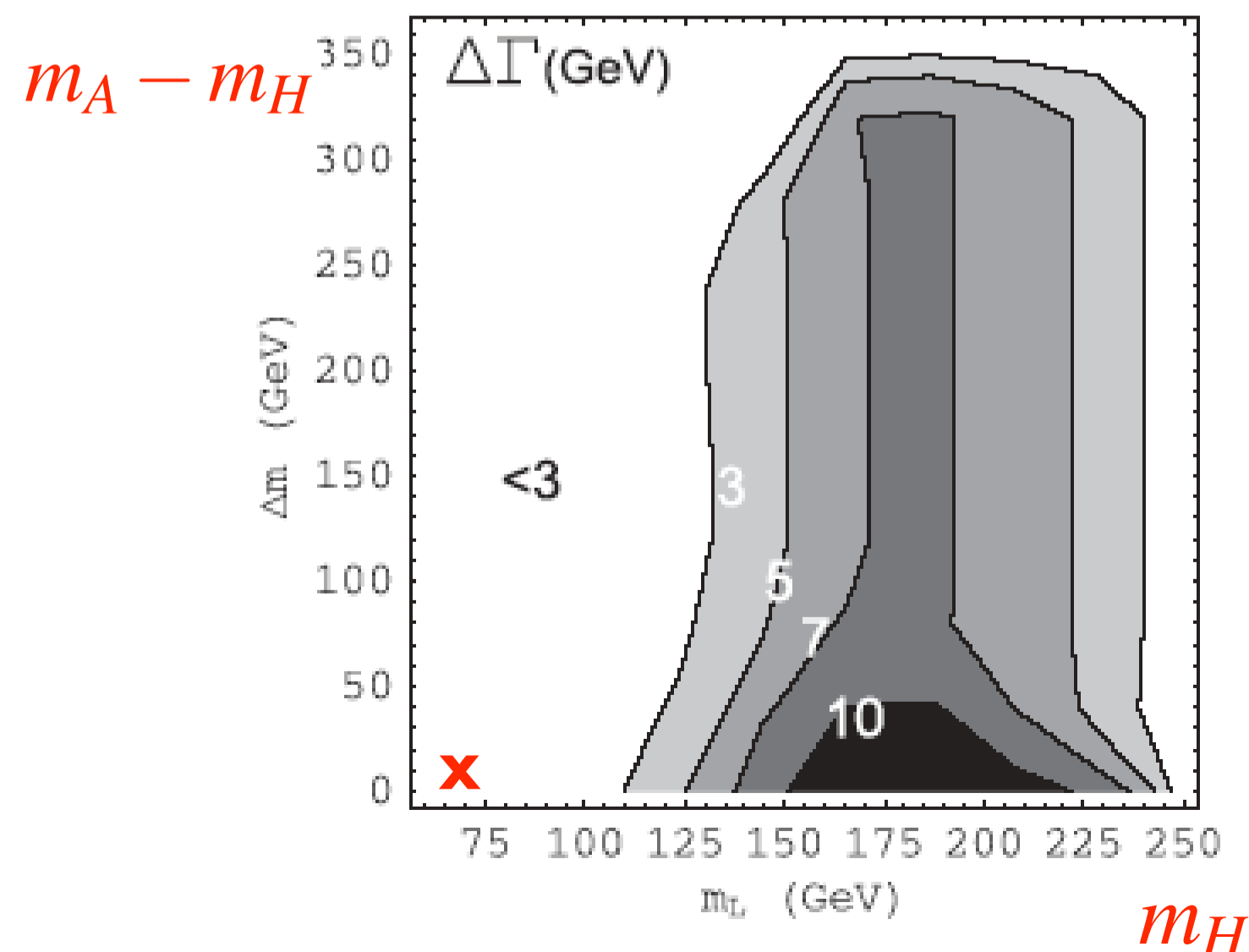
Background  $\sigma_{WZ} \approx 20 \text{ fb}$

Signal may be detected with  $30 \text{ fb}^{-1}$

but other backgrounds  $\bar{t}t, W\gamma^*$

## Increase in h width

$$h \rightarrow AA, HH, H^+H^-$$



# Conclusions

Suppose no susy at the weak scale: use naturalness and EWPT as guides

## 1) Alternative Higgs sectors, natural up to 1.5 TeV

Little Hierarchy Problem ameliorated, but not solved

eg:

$$H_1 = \begin{pmatrix} 0 \\ v+h \end{pmatrix}$$

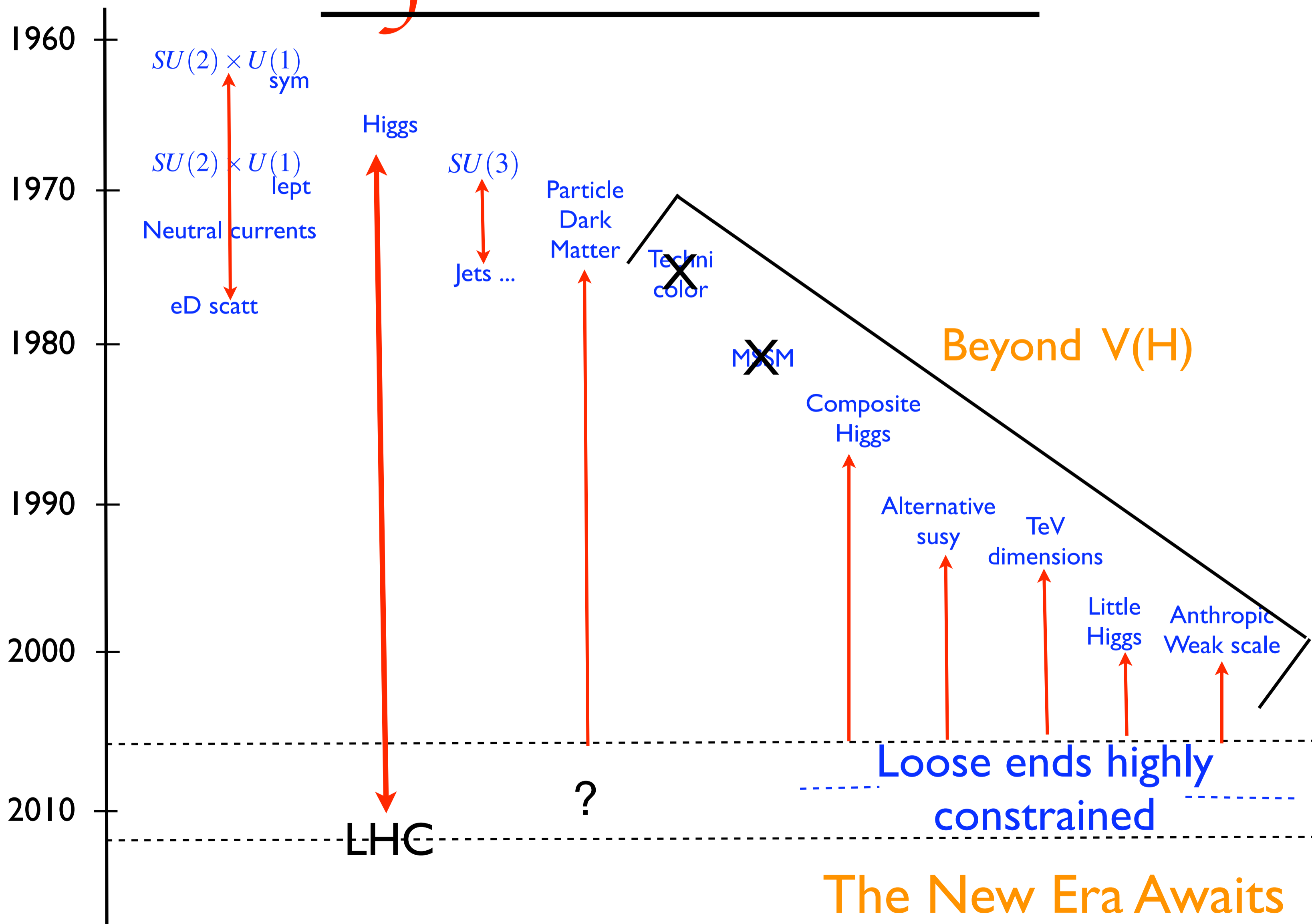
SM-like Higgs for EWSB

$$H_2 = \begin{pmatrix} H^+ \\ H+iA \end{pmatrix}$$

Inert Doublet for EWPT and for DM

2) The cancellation physics may be out of the reach of LHC, which will probe the alternative Higgs sector.

# After the SM ... ?



# *Is DM Region Excluded by LEP2*

# Outline

Going 1 step beyond the SM

(I) Little Hierarchy Problem and “Improved Naturalness”

(II) Light Higgs

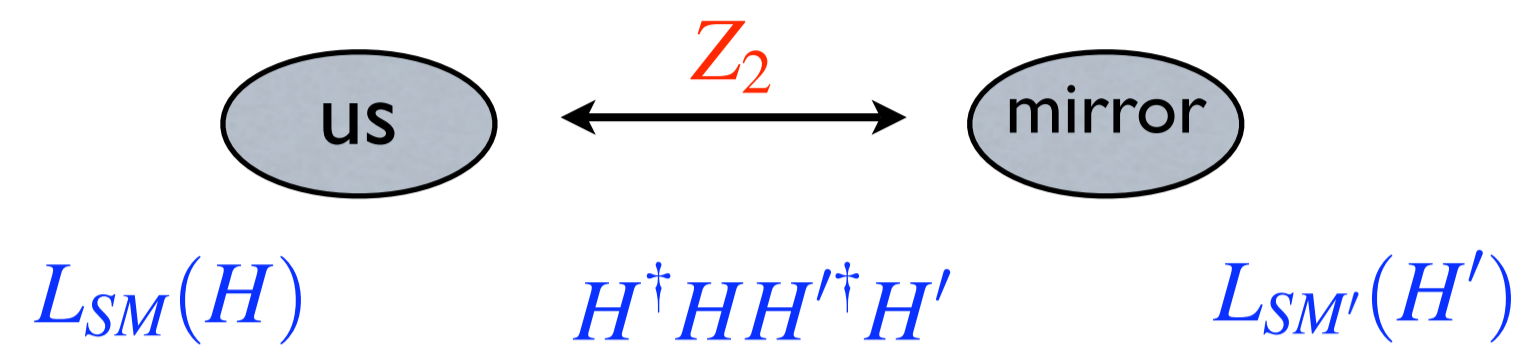
- using Twin Higgs
- using 2 HDM

(III) Heavy Higgs

- Inert Doublet Model

# A) Twin Higgs

Chacko, Goh, Harnik hep-ph/0506256



## Approx SU(4)

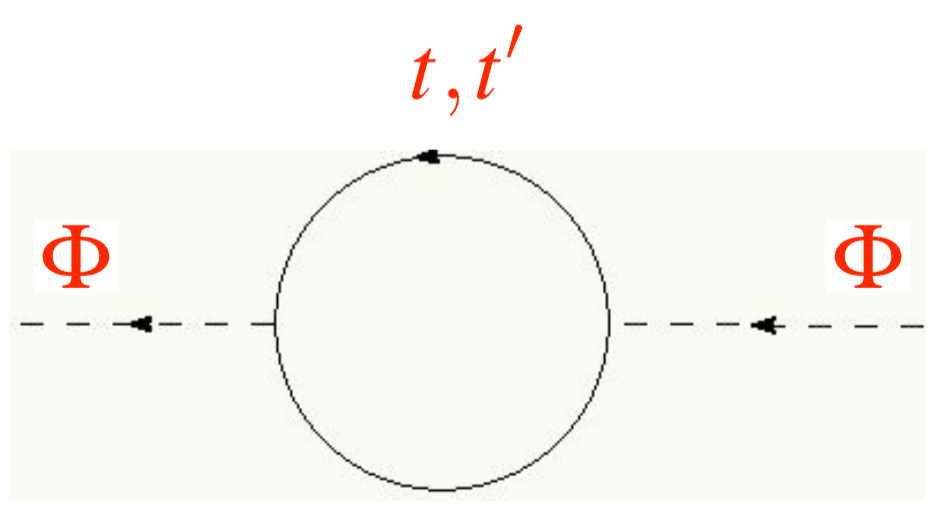
$$\Phi = \begin{pmatrix} H \\ H' \end{pmatrix}$$

$$V = -\mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2$$

$$\langle \Phi \rangle = \begin{pmatrix} 0 \\ 0 \\ 0 \\ f \end{pmatrix}$$

$$f^2 = \frac{\mu^2}{2\lambda}$$

H is a Goldstone Boson



does not contribute to  $V(H)$

# Bottom Up Analysis

Barbieri, Gregoire, Hall hep-ph/0509242

Radiative quartics don't respect SU(4), hence add

$$\Delta V = \delta \left[ (H^\dagger H)^2 + (H'^\dagger H')^2 \right]$$

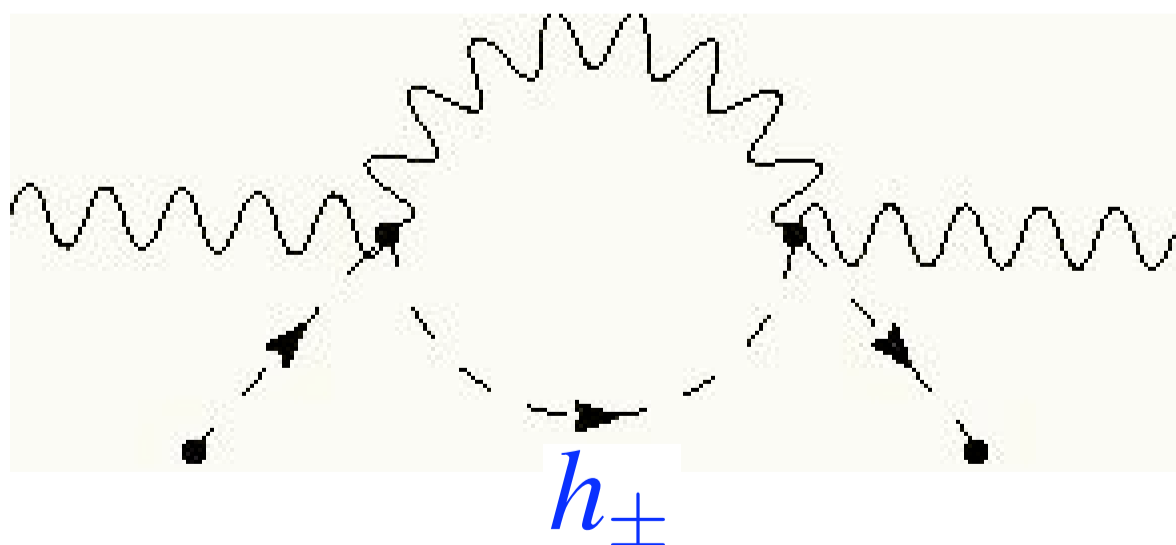
Aligns vacuum to  $H = H' = \begin{pmatrix} 0 \\ v \end{pmatrix}$

so that Higgs mass eigenstates are

$$h_+ = \frac{h+h'}{\sqrt{2}} \quad m_+^2 = 2\mu^2$$

$$h_- = \frac{h-h'}{\sqrt{2}} \quad m_-^2 = \mu^2 \frac{\delta}{\lambda}$$

Make  $\mu^2$  large and  $\frac{\delta}{\lambda}$  small? **No: EWPT!**



$$\ln m_h \rightarrow \frac{1}{2} \ln m_+ + \frac{1}{2} \ln m_-$$

Only a modest improvement



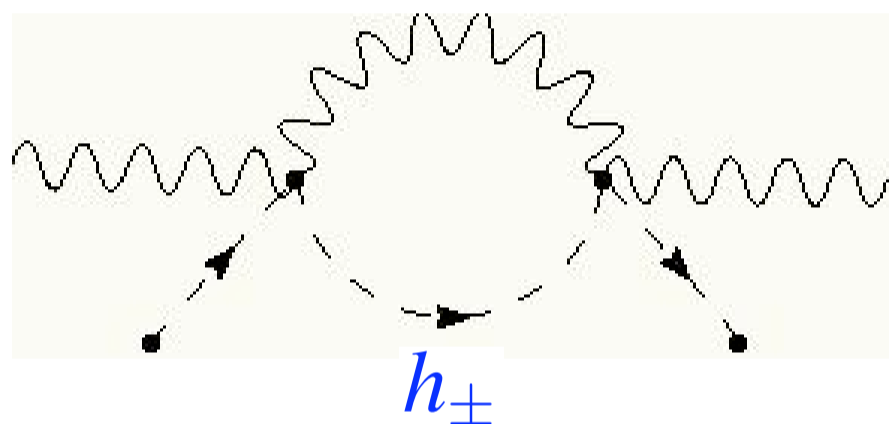
# Unequal vevs

Add  $Z_2$  breaking

$$\Delta V = m^2 (H^\dagger H - H'^\dagger H')$$

$$\frac{v'}{v} = \frac{\cos \theta}{\sin \theta}$$

(but large ratio is still a fine tune)



$$h = \cos \theta h_- + \sin \theta h_+ \text{ so } \ln m_h \rightarrow \cos^2 \theta \ln m_- + \sin^2 \theta \ln m_+$$

$$m_+ < m_- \left( \frac{m_{EWPT}}{m_-} \right)^{1+v'^2/v^2}$$

For example:  $\frac{v'}{v} = 1.5$ ,  $m_- = 120 \text{ GeV}$ ,  $m_{EWPT} = 180 \text{ GeV}$ ,  $m_+ = 450 \text{ GeV}$

allowing

$$\Lambda_t = 1.5 \text{ TeV}$$

$$\Lambda_H = 1.4 \text{ TeV}$$

# Twin Higgs: LHC Signals

$h_-$

$$\Gamma_{prod} = \cos^2 \theta \Gamma_{SM}(m_-)$$

$$BR(h_- \rightarrow X) = \cos^2 \theta BR_{SM}(h \rightarrow X)$$

All event rates of light Higgs are reduced relative to SM by

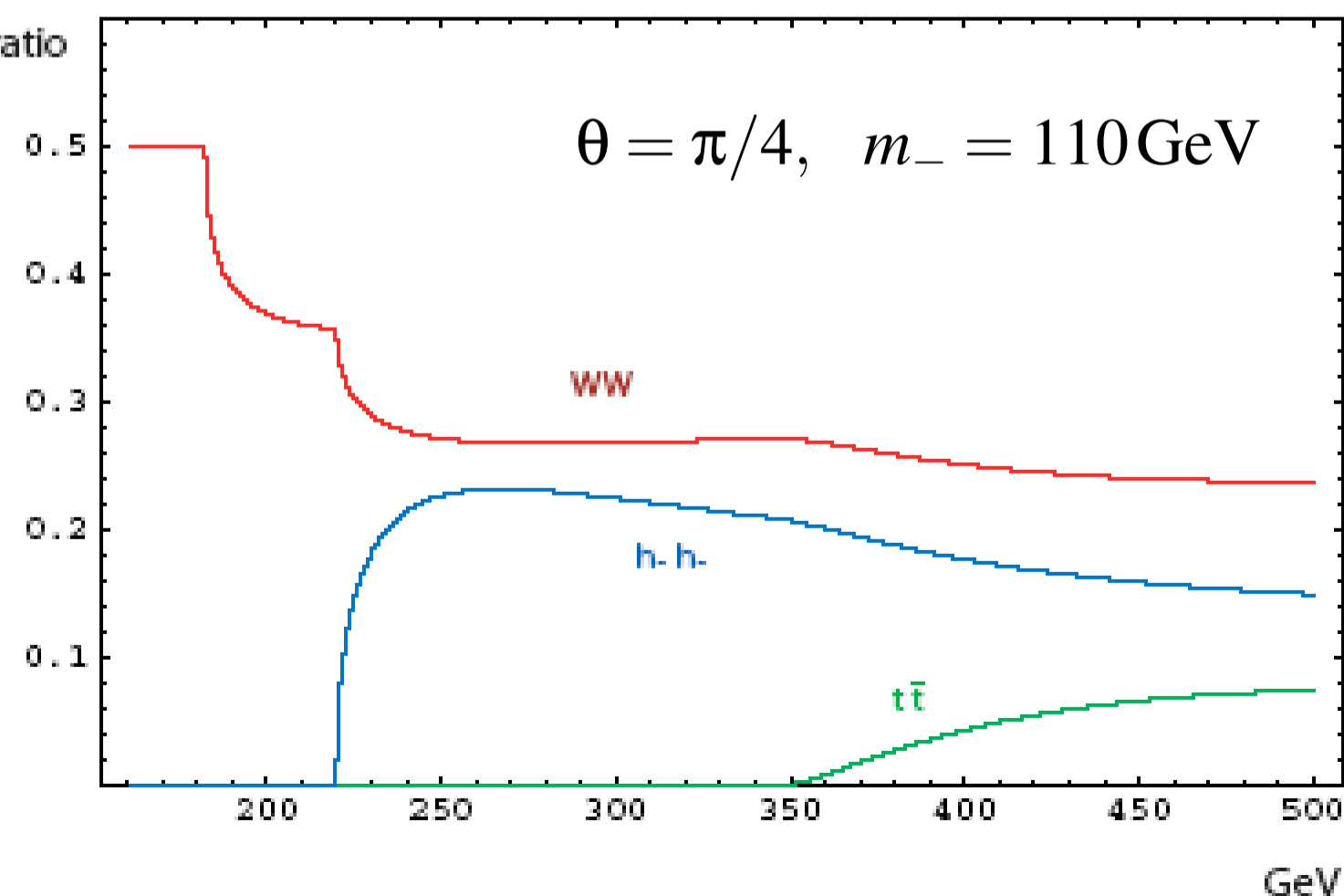
$$\cos^4 \theta \quad (0.48 \text{ for } \frac{v'}{v} = 1.5)$$

$h_+$

$$\Gamma_{prod} = \sin^2 \theta \Gamma_{SM}(m_+)$$

Will be first discovery at LHC; a precise measurement of the signal event rates will provide evidence for the mirror sector.

$h_+$  Branching ratio



# B) General 2 Higgs Doublet Model

Barbieri, Hall hep-ph/0510243

Impose a discrete symmetry for natural flavor conservation; most general potential is

$$V = -\mu_1^2 H_1^\dagger H_1 - \mu_2^2 H_2^\dagger H_2 + \lambda_1 (H_1^\dagger H_1)^2 + \lambda_2 (H_2^\dagger H_2)^2 + \lambda_3 H_1^\dagger H_1 H_2^\dagger H_2 + \lambda_4 H_1^\dagger H_2 H_2^\dagger H_1 + \frac{\lambda_5}{2} [(H_1^\dagger H_2)^2 + h.c.]$$

Neutral Higgs mass matrix

$$(h_1 \ h_2) \begin{pmatrix} 4\lambda_1 v_1^2 & 2\delta v_1 v_2 \\ 2\delta v_1 v_2 & 4\lambda_2 v_2^2 \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}$$

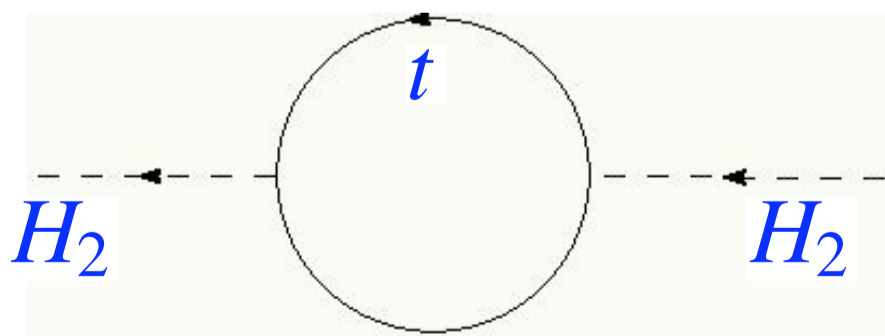
Naturalness

$$\delta = \lambda_3 + \lambda_4 + \lambda_5$$

$H_2$  couples to top

$\lambda_2$  largest, so  $h_+ \sim h_2$

$$m_+^2 \approx 4\lambda_2 v_2^2$$



$$\Lambda_t \propto m_+$$

# Problems

1) Distributing the vev hurts

$$\Lambda_{H_i} = 1.3 \text{ TeV} (\cos \beta, \sin \beta)$$

2) To increase

$$\Lambda_t \begin{cases} \sin \beta \text{ small} \\ m_{EWPT} \text{ large} \end{cases}$$

Conflict

TeVatron Run II

3)  $\Lambda_t$  from  $m_-^2 \longrightarrow m_{H^+}$  relatively low

Since top Yukawa increased,  $Z\bar{b}b, b \rightarrow s\gamma$

Only a factor 2 increase in natural cutoff compared to SM

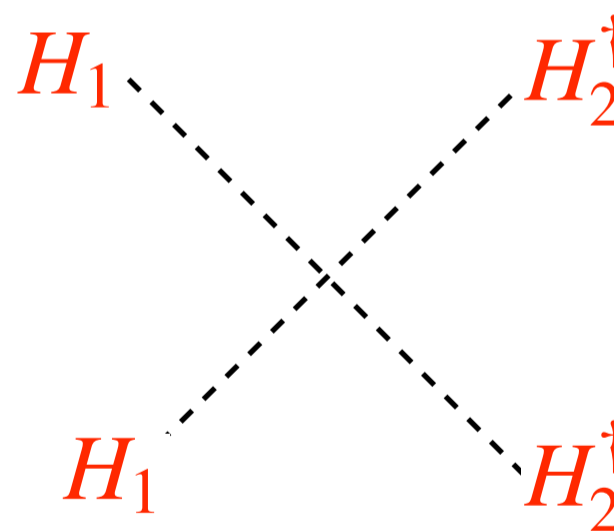
# The “Charged” 2 HDM

Suppose the quartics are dominated by  $\lambda_5$

$$V = \mu_1^2 H_1^\dagger H_1 + \mu_2^2 H_2^\dagger H_2 - \mu^2 (H_1^\dagger H_2 + h.c.) + \frac{\lambda_5}{2} [(H_1^\dagger H_2)^2 + h.c.]$$

A local minimum with  $\frac{v_1}{v_2} = \frac{\mu_2}{\mu_1}$

Cannot close quartic into loop!



$$\Lambda_H \approx 10 \text{ TeV !}$$

## Problem

Tunnel to runaway vacuum:  $H_1 = \begin{pmatrix} 0 \\ v_1 \end{pmatrix}$   $H_2 = \begin{pmatrix} 0 \\ iv_2 \end{pmatrix}$

# 2-Higgs Doublets: An Alternative Phase

Work in progress with R. Barbieri and V. Rychkov

$$\begin{array}{ll} H_2 \rightarrow -H_2 & \longrightarrow \\ \mu_1^2 < 0, \mu_2^2 > 0 & \longrightarrow \end{array} \quad \begin{array}{l} V = \mu_1^2 H_1^\dagger H_1 + \mu_2^2 H_1^\dagger H_1 + \dots \\ v_2 = 0 \end{array} \quad H_2 \text{ Inert}$$

$$H_1 = \begin{pmatrix} 0 \\ v + H \end{pmatrix}$$

Couples to fermions and is much like SM doublet; H heavy

$$H_2 = \begin{pmatrix} H^+ \\ h + iA \end{pmatrix}$$

Custodial breaking masses for  $\Delta T$

$$(m_{H^+} - m_A)(m_{H^+} - m_h) \approx (120 \text{ GeV})^2$$

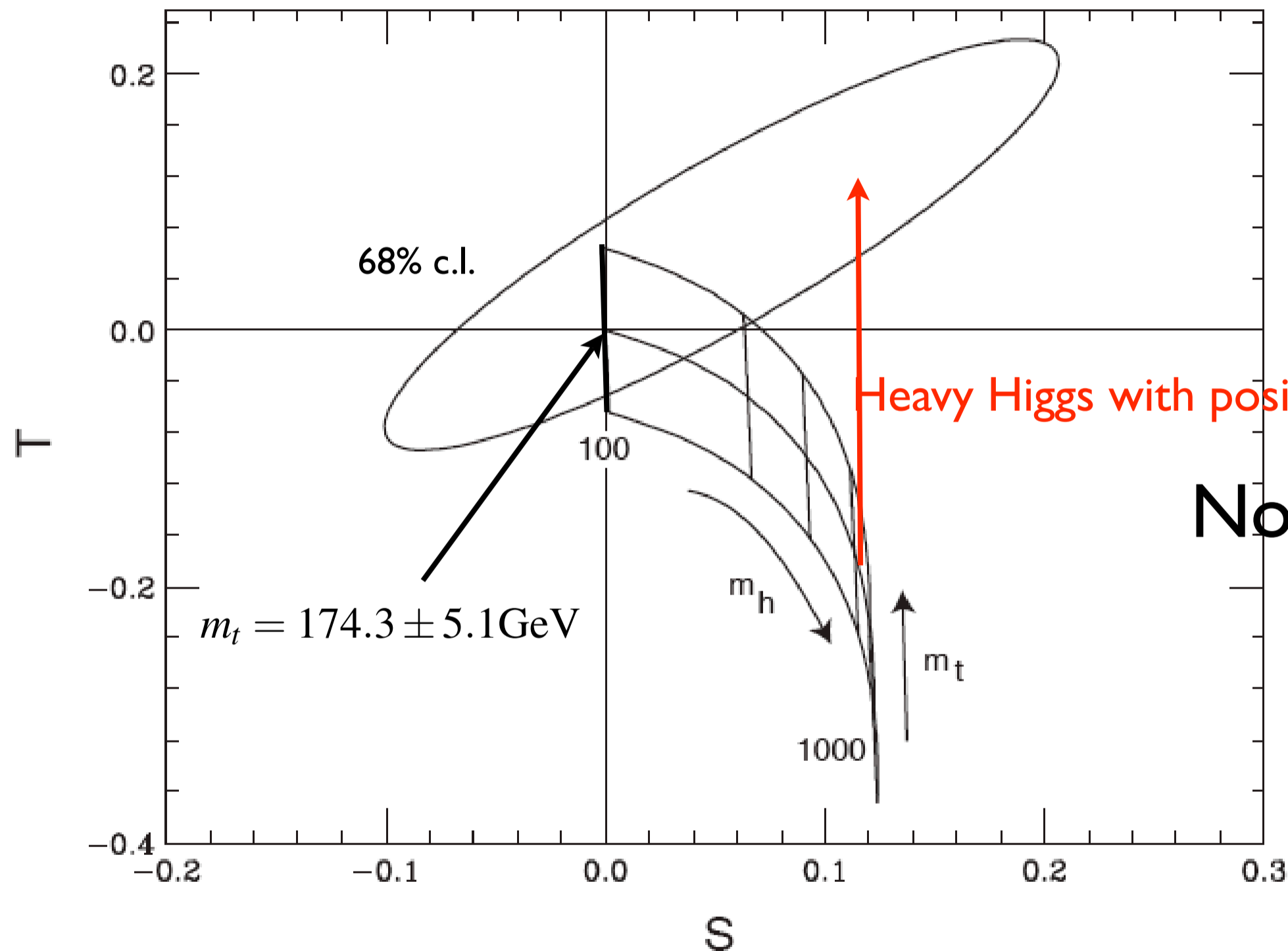
$\Lambda_t$  increased to 1.5 TeV  $D_t^{1/2}$

LHC signals could be just those of  $H^+, h, A$

Lightest of  $h, A$  is stable and could be DM

# A Heavy SM Higgs and EWPT

Peskin, Wells hep-ph/0101342



## Origin of $\Delta T$

SM + heavy triplet scalars

New gauge interaction

2 Higgs Doublets - both Higgs heavy

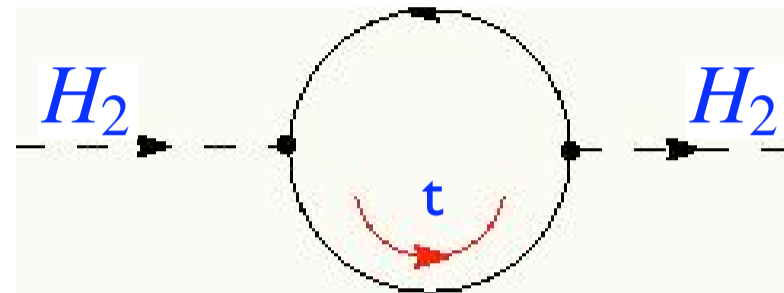
- but often get trouble from 4 fermion operators

$$\Lambda_{H_i} = 1.3 \text{ TeV} (\sin \beta, \cos \beta)$$

# 1 Heavy Higgs and 1 Light Higgs

$(H_2, t)$

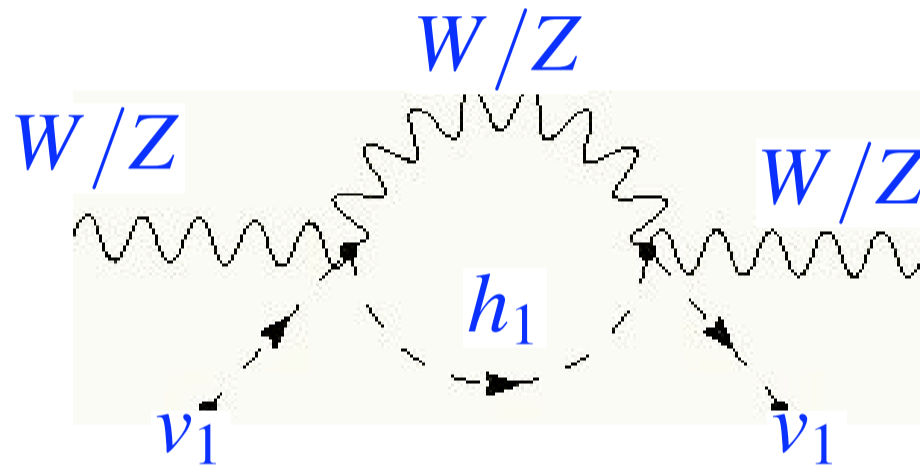
Top couples to a heavy Higgs



$$\Lambda_t \approx 2 \text{ TeV} \left( \frac{m_{H_2}}{600 \text{ GeV}} \right) \sin \beta D_t^{1/2}$$

$(h_1, W)$

Light Higgs dominates EWPT



$$\frac{g^4}{16\pi^2} v_1^2 \ln \frac{m_{h_1}}{M_W}$$

What is EWPT limit on  $m_{H_2}$  ?

$$m_{H_2} < m_{h_1} \left( \frac{m_{max}}{m_{h_1}} \right)^{\frac{1}{\sin^2 \beta}}$$

“Cancellation” physics may be out of LHC reach. Discover 2 Higgs with:

$$\tan \beta \approx 0.8-1$$

$$m_{h_1} \approx 115-150 \text{ GeV}$$

$$\alpha \leq 0.3$$

$$m_{H_2} \approx 500-800 \text{ GeV}$$

Low top mass?



# 2 Higgs Doublets

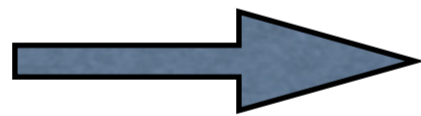
Most general model with a discrete symmetry for natural flavor conservation

$$V = \mu_1^2 H_1^\dagger H_1 + \mu_2^2 H_2^\dagger H_2$$

$$+ \lambda_1 (H_1^\dagger H_1)^2 + \lambda_2 (H_2^\dagger H_2)^2 + \lambda_3 H_1^\dagger H_1 H_2^\dagger H_2 + \lambda_4 H_1^\dagger H_2 H_2^\dagger H_1 + \lambda_5 [(H_1^\dagger H_2)^2 + h.c.]$$

Standard Phase

$$\mu_{1,2}^2 < 0$$



$$v_{1,2} \neq 0$$

# Mass Constraints from T

