

# Interference effects for Higgs-mediated $ZZ^*$ jet production

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# Motivation

- \* a large fraction of the cross section for events where the Higgs decays to vector bosons,

$$pp \rightarrow H(\rightarrow VV) + X$$

lies in the high mass tail  $M_{VV} > 2 m_V$

Kauer, Passarino, JHEP 1208, 116 (2012)

- \* this tail is independent of the Higgs boson width  $\Gamma_H$

→ use it to

bound  $\Gamma_H$

Caola, Melnikov, PRD88, 054024 (2013); Campbell et al., JHEP 1404, 060 (2014), PRD89,053011 (2014);

Khachatryan et al. (CMS Collab.), PLB 736, 64 (2014); Tech. Rep. ATLAS-CONF-2014-042.

study the effective gluon-Higgs coupling

Cacciapaglia et al., 1406.1757; Azatov et al., 1406.6338.

# Motivation

why the extra jet?

\* radiation in gluon-fusion Higgs production is large

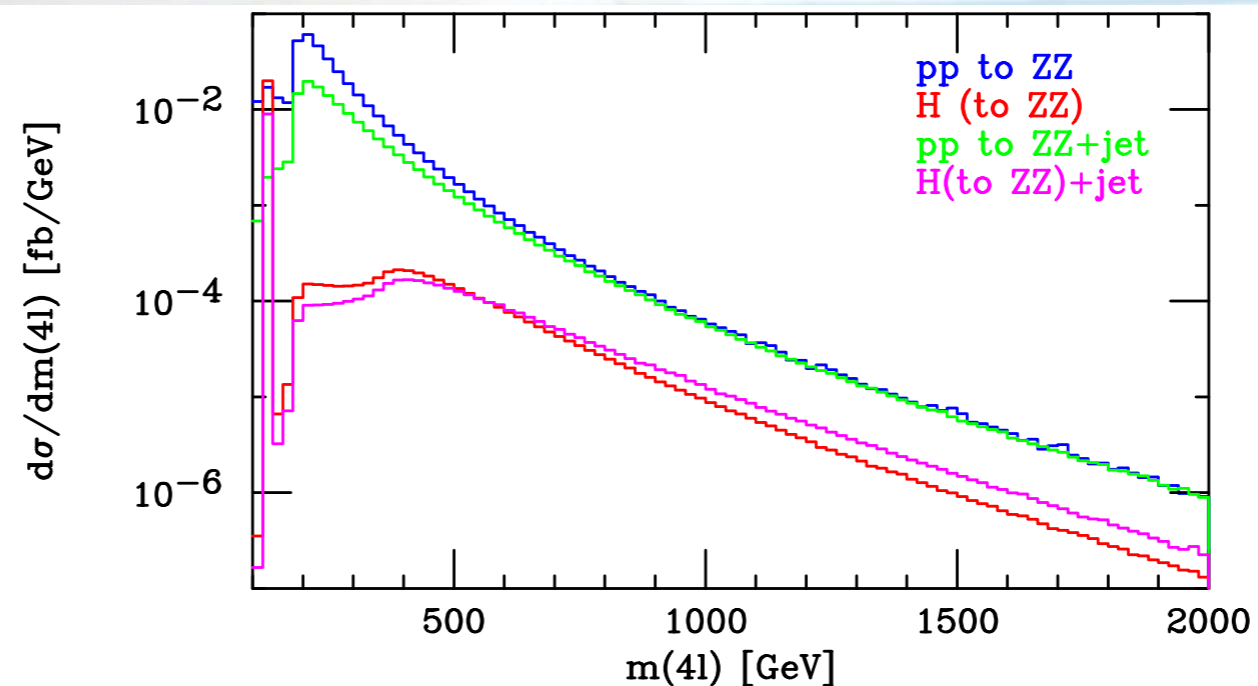
➔ large k-factors in  $gg \rightarrow H$

Dawson, NPB 359, 283 (1991); Djouadi et al., PLB 264, 440 (1991); Graudenz et al., PRL 70, 1372 (1993); ...

➔ large cross section for  $gg \rightarrow H + 1 \text{ jet}$

Ellis et al., NPB297, 221 (1998)

➔ production xsec in  $H + 1 \text{ jet}$  and  $H + 0 \text{ jet}$  comparable



# Motivation

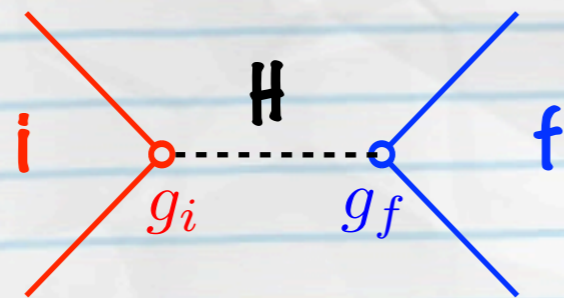
- \* the one-loop amplitudes entering  $ZZ + \text{jet}$  are part of the missing higher-order corrections to inclusive loop-mediated  $Z$  pair production relevant to the Higgs-continuum interference
- \* these corrections are expected to be large  $\rightarrow$  having them under control would allow for a more reliable bound on  $\Gamma_H$  from  $ZZ$  interference
- \* our results are analytical  $\rightarrow$  easier to integrate over singular regions
- \* virtual corrections are still missing ..

# Introduction

## Bounding the Higgs width using interference effects in ZZ

Caola, Melnikov, PRD88, 054024 (2013); Campbell et al., JHEP 1404, 060 (2014), PRD89,053011 (2014);  
Kauer, Passarino, JHEP 1208, 116 (2012)

\* consider an Higgs-mediated process  $i \rightarrow H \rightarrow f$



$$\frac{d\sigma}{dq^2} \sim \frac{g_i^2 g_f^2}{(q^2 - m_H^2)^2 + m_H^2 \Gamma_H^2}$$

→ in the on-shell region  
(integrate around  $q^2 \sim m_H^2$ )

$$\sigma^{peak} \sim \frac{g_i^2 g_f^2}{\Gamma_H}$$

→ in the off-shell region  
(above the resonance,  
 $q^2 \gg m_H^2$ )

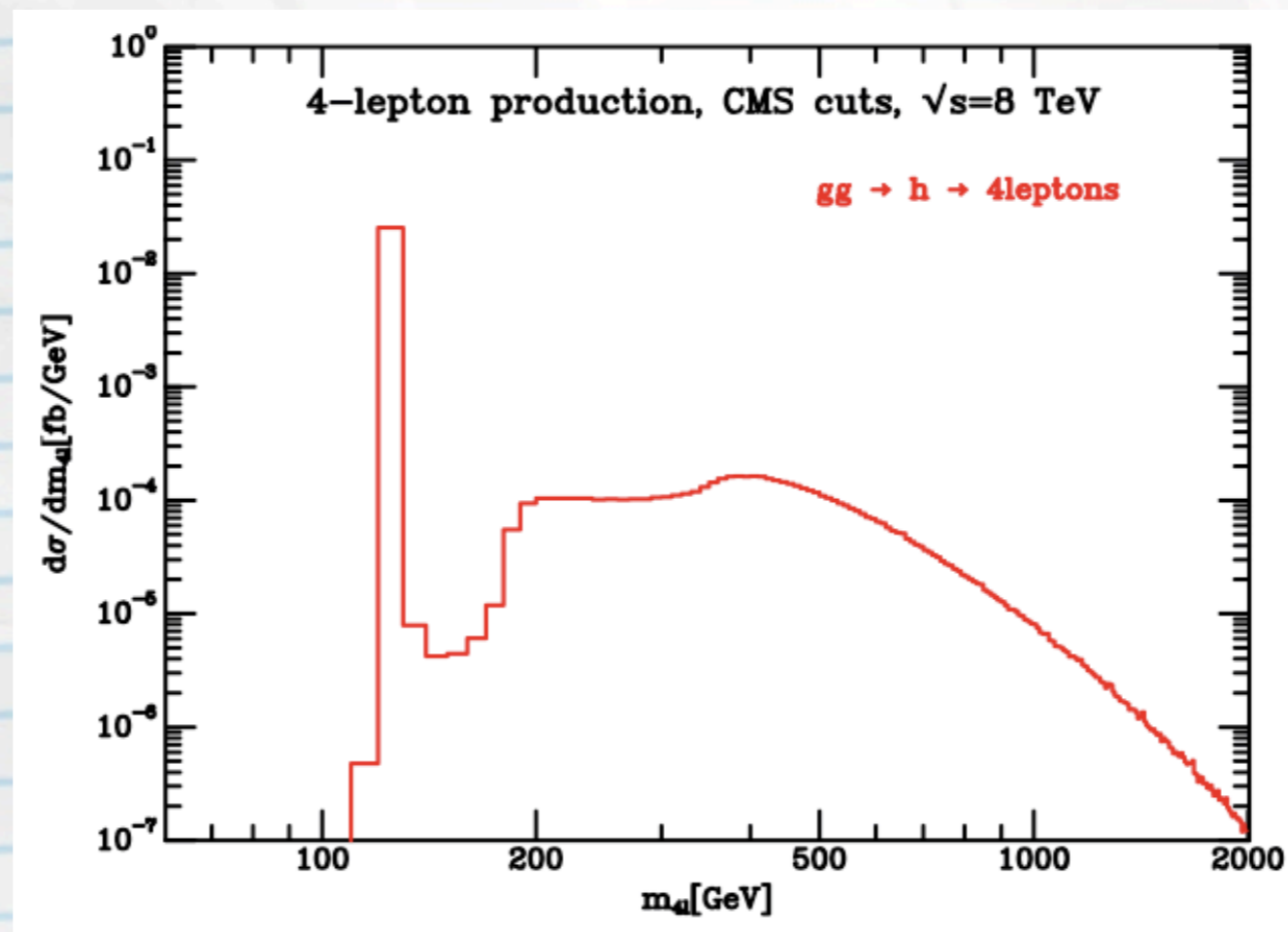
$$\sigma^{tail} \sim g_i^2 g_f^2$$

$$\Gamma_H \propto \frac{\sigma^{tail}}{\sigma^{peak}}$$

# Introduction

- \* for  $pp \rightarrow H \rightarrow ZZ \rightarrow 4l$ , about 15% of the total cross section is in the region with  $m_{4l} > 130$  GeV

Kauer, Passarino

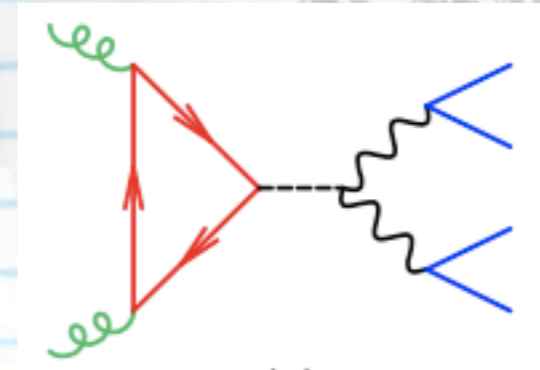


- use current measurements of the  $pp \rightarrow ZZ$  cross section to constrain  $\Gamma_H$

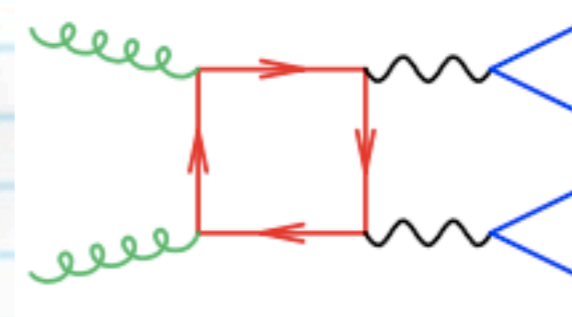
Caola, Melnikov,

# Introduction

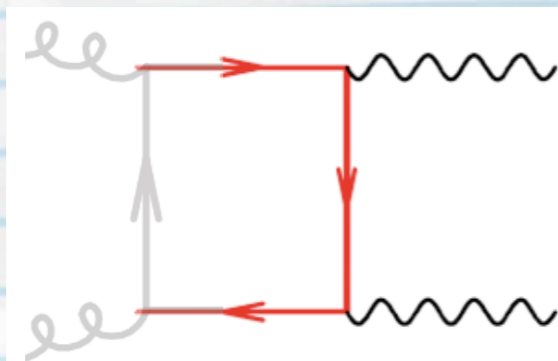
\* look at Higgs-mediated  
Z pair production  
 $gg \rightarrow H \rightarrow ZZ$



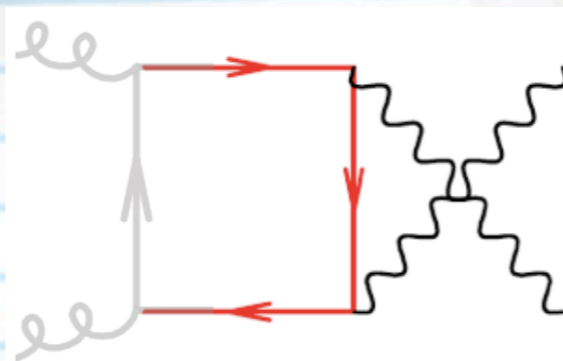
\* interference effects with  
the background process  
 $gg \rightarrow ZZ$



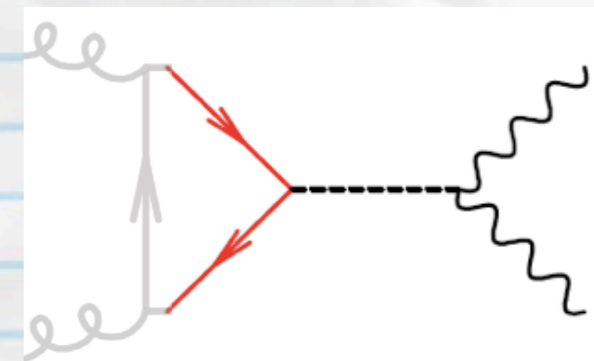
are large in the high invariant mass region due to  
unitarity requirements for the  $t\bar{t} \rightarrow ZZ$  scattering



$$-aE^2 + (d - c)m_t E$$



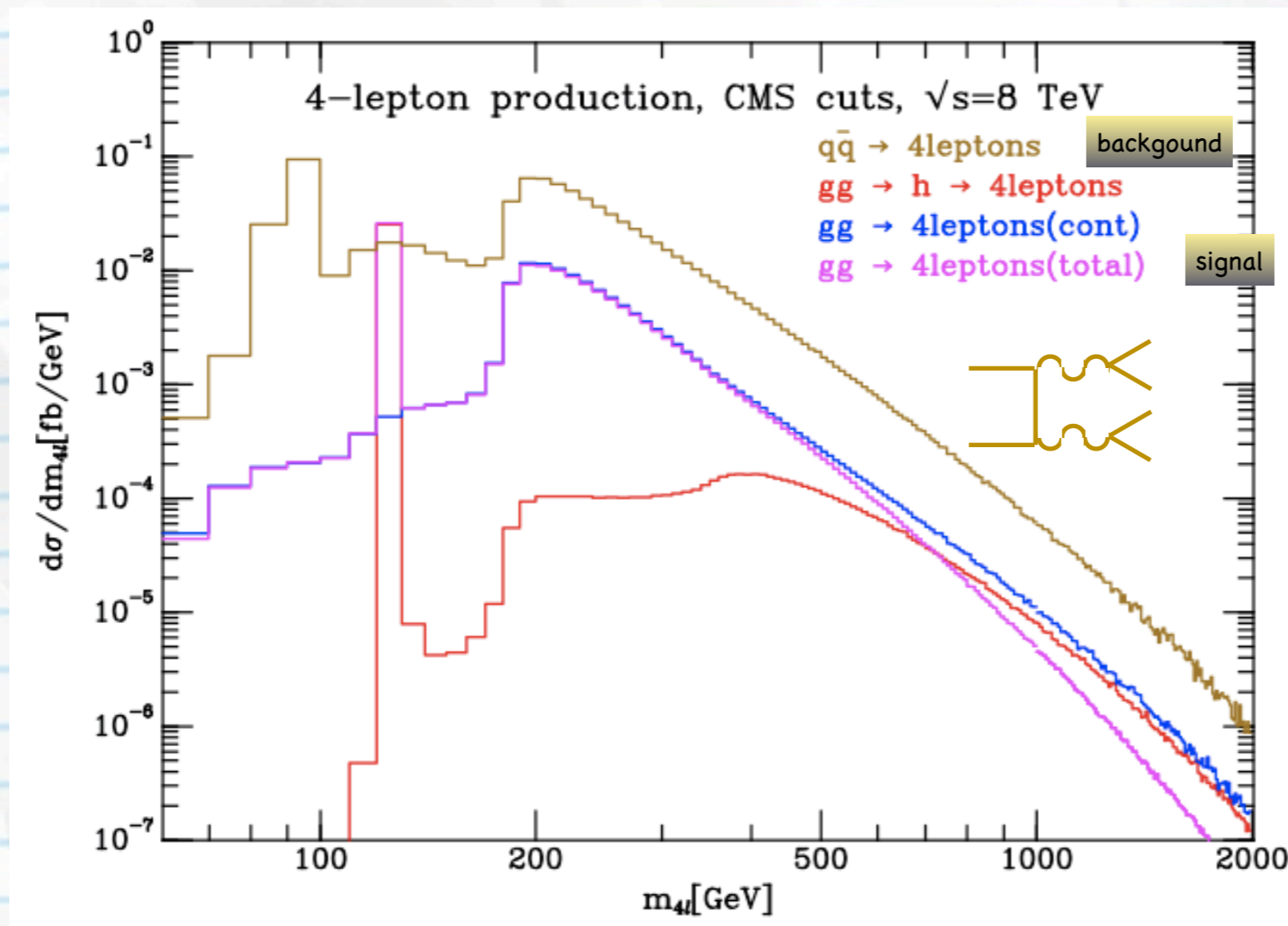
$$aE^2 + (b + c)m_t E$$



$$-(b + d)m_t E$$

# Introduction

- \* this yields large **destructive interference** between  $gg \rightarrow H(-\rightarrow ZZ) \rightarrow 4l$  and  $gg \rightarrow ZZ \rightarrow 4l$



→ the  $qq$  background is 1-2 orders of magnitude larger than the signal

→ situation improves at higher center of mass energies



# Introduction

- \* constraint on the Higgs width: assume that

$$\sigma_H^{peak} = \sigma_H^{peak, SM} \quad , \quad g_{i,f}^{peak} = g_{i,f}^{off}$$

but allow for  $\Gamma_H \neq \Gamma_H^{SM}$  , i.e.,  $g_{i,f} = \alpha g_{i,f}^{SM}$  ,

$$\Gamma_H = \alpha^4 \Gamma_H^{SM} .$$

- \* the ratio of peak and off-peak cross sections at 8TeV yields

$$\frac{\sigma_{off}^{H+I}(m_{4l} > 300 \text{ GeV})}{\sigma_{peak}^H} = 0.098 \left( \frac{\Gamma_H}{\Gamma_H^{SM}} \right) - 0.141 \sqrt{\frac{\Gamma_H}{\Gamma_H^{SM}}}$$

➔  $\Gamma_H \lesssim 25.2 \Gamma_H^{SM}$

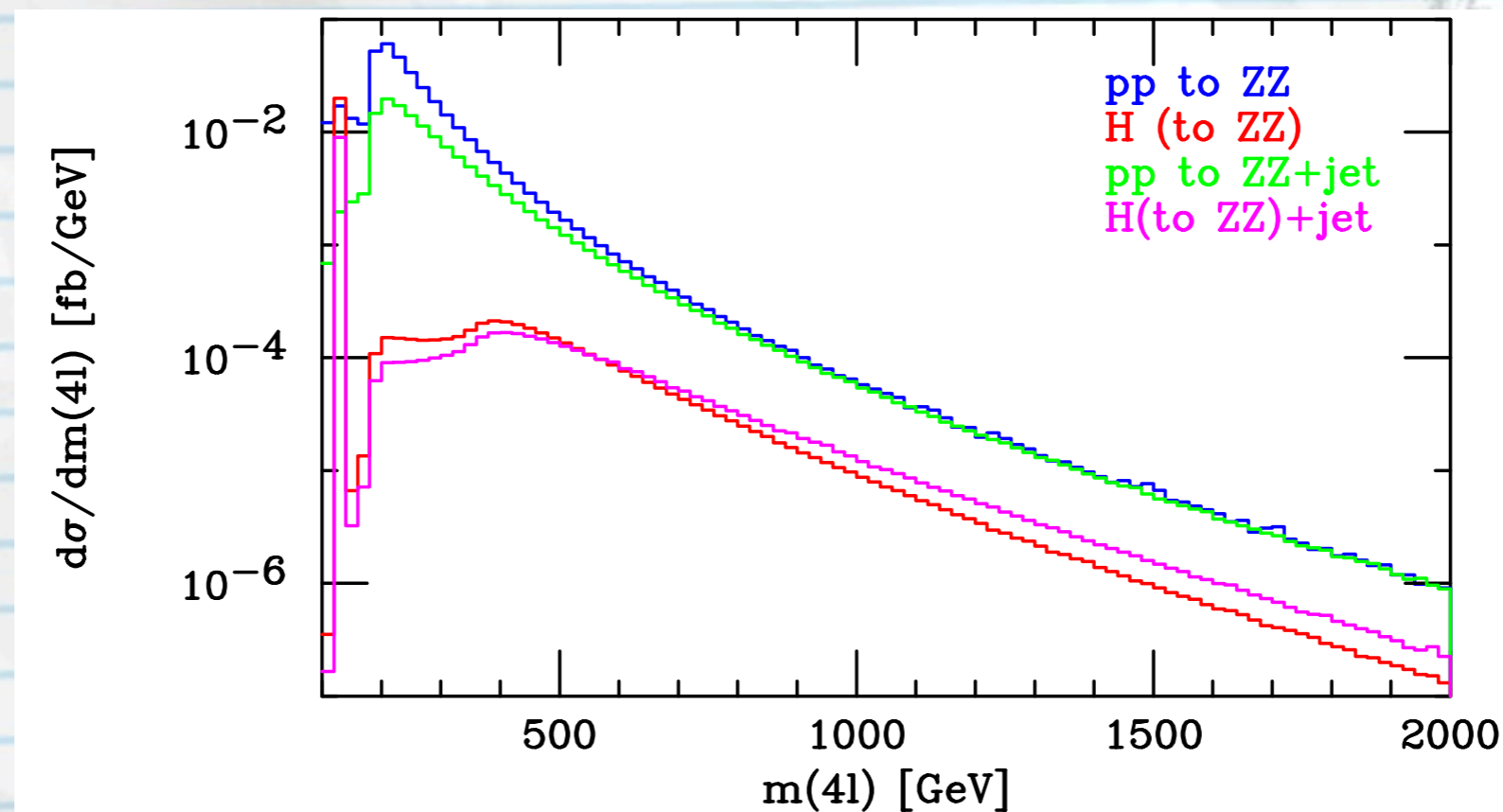
Campbell et al., JHEP 1404, 060 (2014)

$$\Gamma_H < 5.4 \Gamma_H^{SM} \quad (\text{CMS})$$

$$\Gamma_H < (4.8 - 7.7) \Gamma_H^{SM} \quad (\text{ATLAS})$$

# Introduction

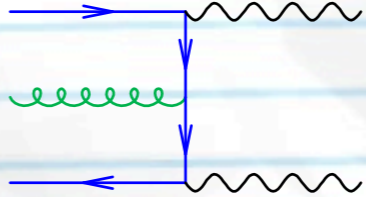
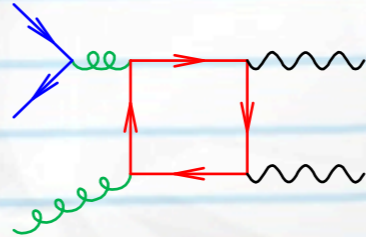
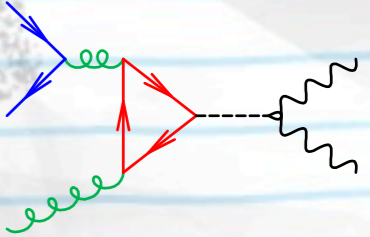
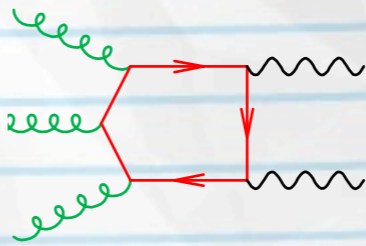
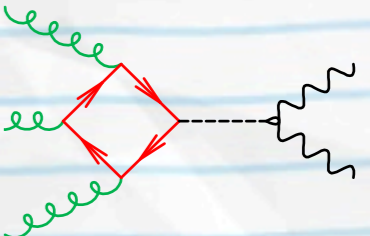
- \* similar ideas for interference effects in  $pp \rightarrow ZZ+1 \text{ jet}$ 
  - in the tail, the ratio of Higgs signal to LO background even (slightly) better than for  $pp \rightarrow ZZ$



# Introduction

- \* similar ideas for interference effects in  $pp \rightarrow ZZ + 1 \text{ jet}$ 
  - in the tail, the ratio of Higgs signal to LO background even better than for  $pp \rightarrow ZZ$ !
  - also in this case the interference between  $pp \rightarrow H(\rightarrow ZZ) + 1 \text{ jet}$  and  $pp \rightarrow ZZ + 1 \text{ jet}$  in the high energy region is large and needs to be taken into account

# Ingredients

order	process	background	signal
$g_w^2 g_s$	$q\bar{q} \rightarrow ZZ + g$ $qg \rightarrow ZZ + q$	$\mathcal{B}_t^{qqg}$ 	
$g_w^2 g_s^3$	$q\bar{q} \rightarrow ZZ + g$ $qg \rightarrow ZZ + q$	$\mathcal{B}_{1l}^{qqg}$ 	$\mathcal{S}_{1l}^{qqg}$ 
	$gg \rightarrow ZZ + g$	$\mathcal{B}_{1l}^{ggg}$ 	$\mathcal{S}_{1l}^{ggg}$ 

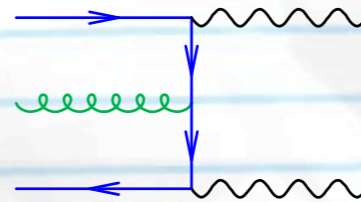
# Ingredients

- \* LO cross section
- \*  $O(g_w^4 g_s^2)$

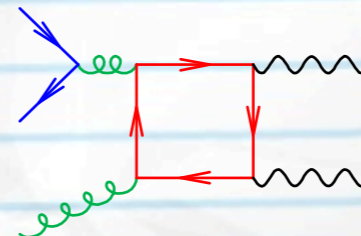
background

signal

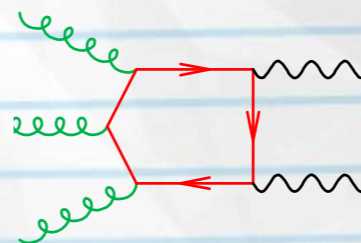
$\mathcal{B}_t^{qqg}$



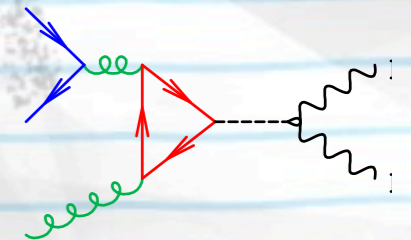
$\mathcal{B}_{1l}^{qqg}$



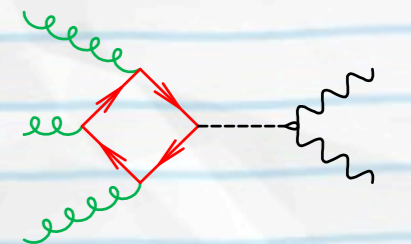
$\mathcal{B}_{1l}^{ggg}$



$\mathcal{S}_{1l}^{qqg}$

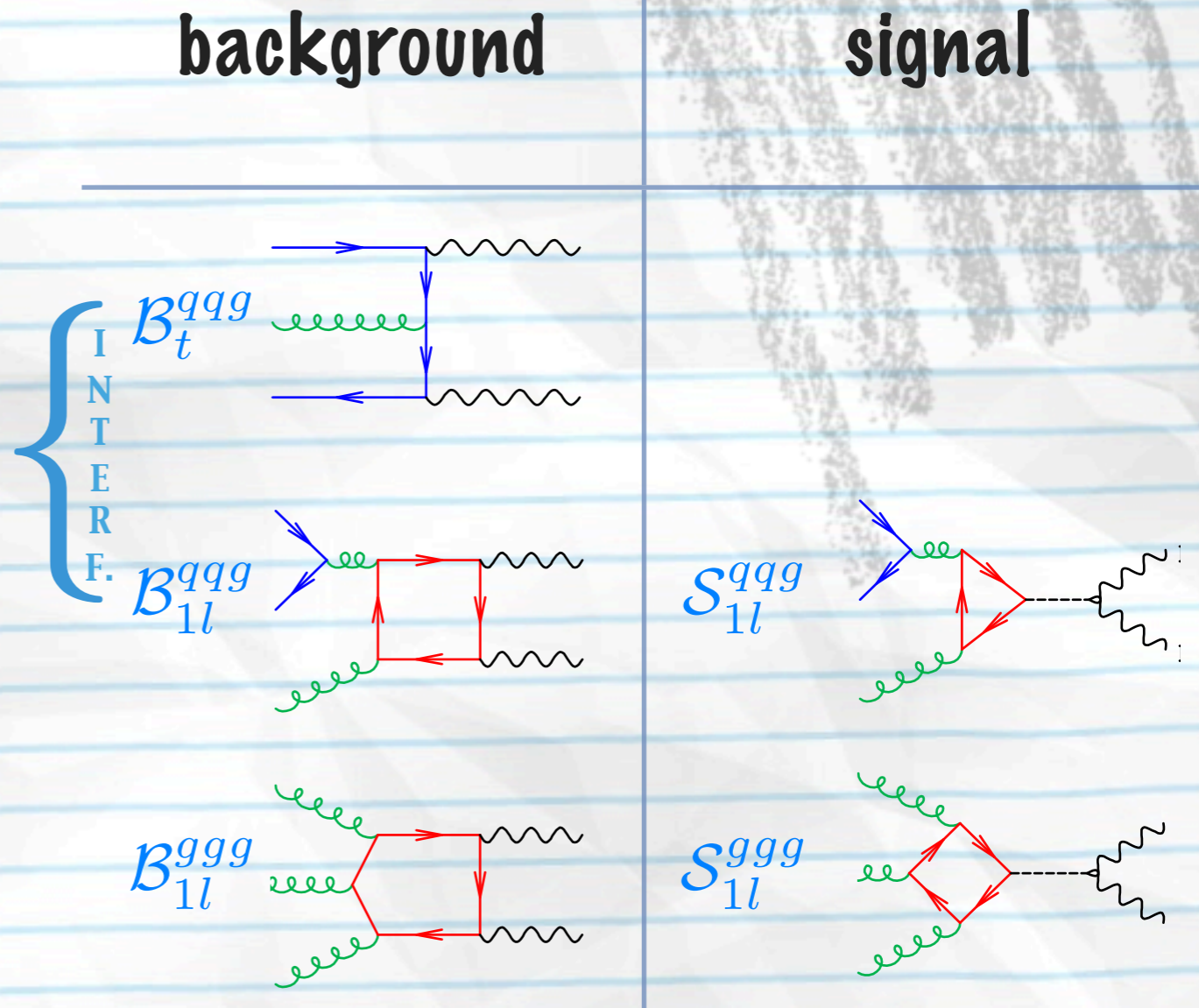


$\mathcal{S}_{1l}^{ggg}$



# Ingredients

- \* NLO effects
  - \*  $O(g_w^4 g_s^4)$
  - \* interference is small both for S and B:  
 $\rightarrow \text{KNLO} \sim 0.98$  Binoth et al., PLB 683, 154 (2010)
- and fermion loops  
yield  $\sim 1\%$  of the contribution  
 $\rightarrow$  for S, expect the same due to unitarity

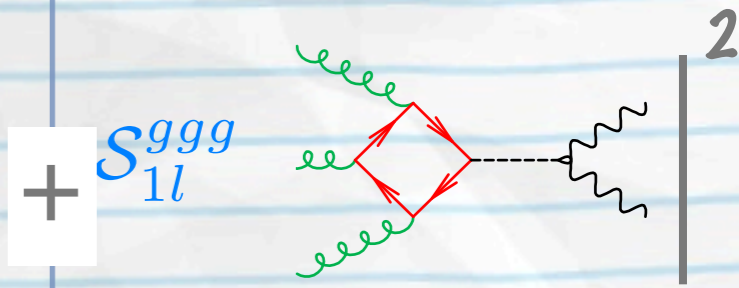
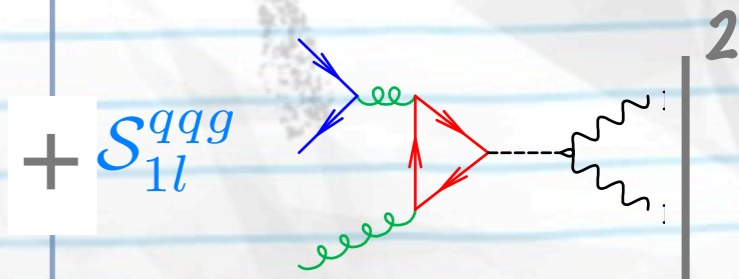
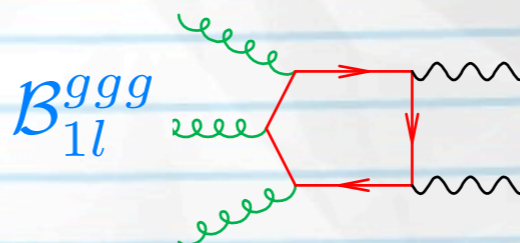
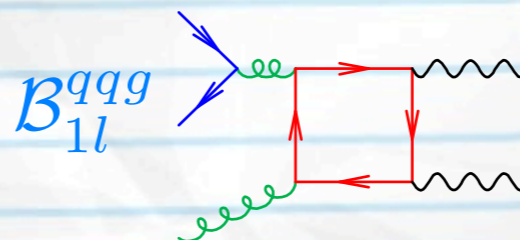
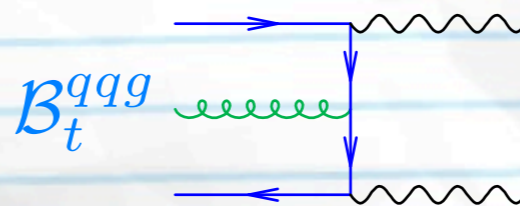


# Ingredients

- \* NNLO effects
  - \*  $O(g_w^4 g_s^6)$
  - \* S-B interference in  $gg \rightarrow ZZg$  is large and negative in the high mass tail
- Campanario et al.,  
JHEP 1306, 069 (2013)
- \* we add the interference in  $qqg \rightarrow ZZ$   
→ 25 - 40% effect

background

signal



+

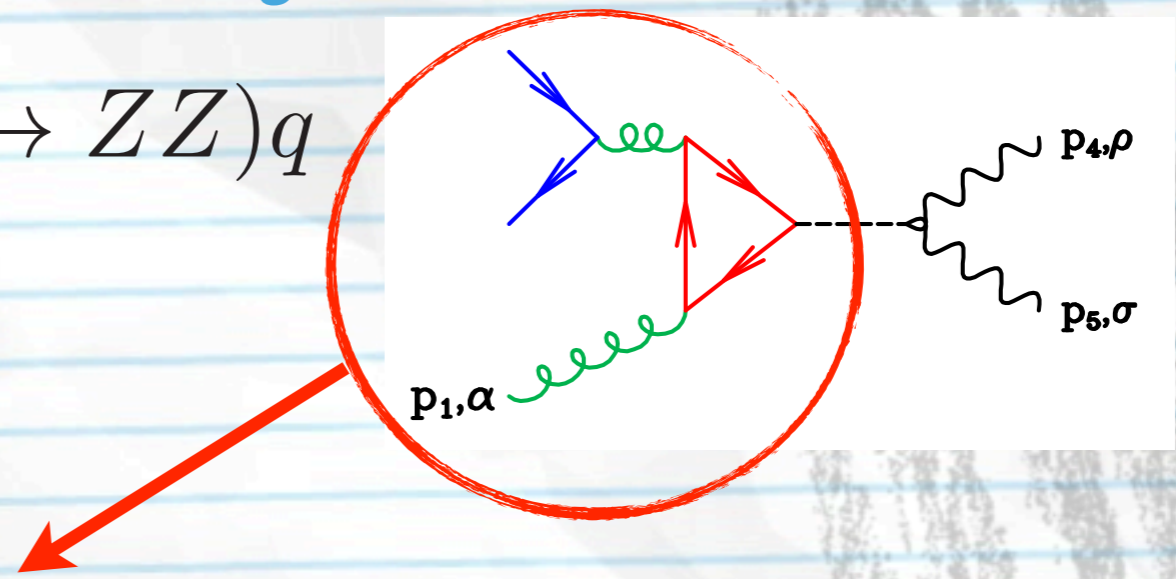
+

2

2

# Example

Amplitude for  $gq \rightarrow H(\rightarrow ZZ)q$



$$-i \frac{g_s^2}{16\pi^2} \frac{g_W}{4m_W} \frac{1}{2} (t^A)_{32} g_s \frac{1}{s_{23}} \bar{u}(p_3) \gamma^\mu u(p_2) \left( g^{\alpha\mu} - \frac{p_1^\mu (p_2^\alpha + p_3^\alpha)}{p_1 \cdot (p_2 + p_3)} \right) F(s_{23}, s_H)$$

scalar loop function for off-shell Higgs production from  $g^*g$

Including also the Higgs decay into ZZ,

$$\mathcal{M}^{\alpha\rho\sigma} = \mathcal{N} \left( g_s (t^A)_{32} \frac{F(s_{23}, s_H)}{s_H - M_H^2} \right) \frac{1}{s_{23}} \bar{u}(p_3) \gamma^\mu u(p_2) \left( g^{\alpha\mu} - \frac{p_1^\mu (p_2^\alpha + p_3^\alpha)}{p_1 \cdot (p_2 + p_3)} \right) g^{\rho\sigma}$$

$$\mathcal{S}_{gq\bar{q}} = \frac{V}{2} g_s^2 |\mathcal{N}|^2 \frac{1}{s_{23}} \frac{(p_1 \cdot p_2^2 + p_1 \cdot p_3^2)}{p_1 \cdot p_{23}^2} \frac{|F(s_{23}, s_{123})|^2}{(s_{123} - M_H^2)^2} \left[ 8 + \left( \frac{s_{123} - 2m_Z^2}{m_Z^2} \right)^2 \right]$$



# Results for $pp \rightarrow ZZ + \text{jet}$

demand

\* one single jet

\*  $|\eta_j| < 3$

,  $p_{T,j} > p_{T,cut}$

\*  $m_{ZZ} > 300 \text{ GeV}$  (high mass tail)

$$|S_{1l}^{ggg}|^2$$

$$|S_{1l}^{qqg}|^2$$

$$S_{1l}^{qqg} \times B_{1l}^{*,qqg}$$

	$p_{T,cut}$ [GeV]	$\sigma_H^{gg}$ [fb]	$\sigma_H^{qq+q\bar{q}}$ [fb]	$\sigma_I^{gg}$ [fb]	$\sigma_I^{qq+q\bar{q}}$ [fb]	$\sigma_I^{\text{tree}}$ [fb]
$\sqrt{s} = 8 \text{ TeV}$	30	0.0212	0.00679	-0.0299	-0.00929	0.00230
	50	0.0124	0.00522	-0.0173	-0.00706	0.00182
	100	0.00467	0.00279	-0.00632	-0.00369	0.00097
	200	0.00104	0.00086	-0.00133	-0.00111	0.00026

$$S_{1l}^{ggg} \times B_{1l}^{*,ggg}$$

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✓  
\* agree with [Campanario et al., JHEP 1306, 069 \(2013\)](#)

✓  
\* strong cancellation as required by unitarity

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- ✓
- \* small, as expected from Dixon et al., PRD 60, 114037 (1999)  
by unitarity arguments

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\*  $m_{ZZ} > 300 \text{ GeV}$  (high mass tail)

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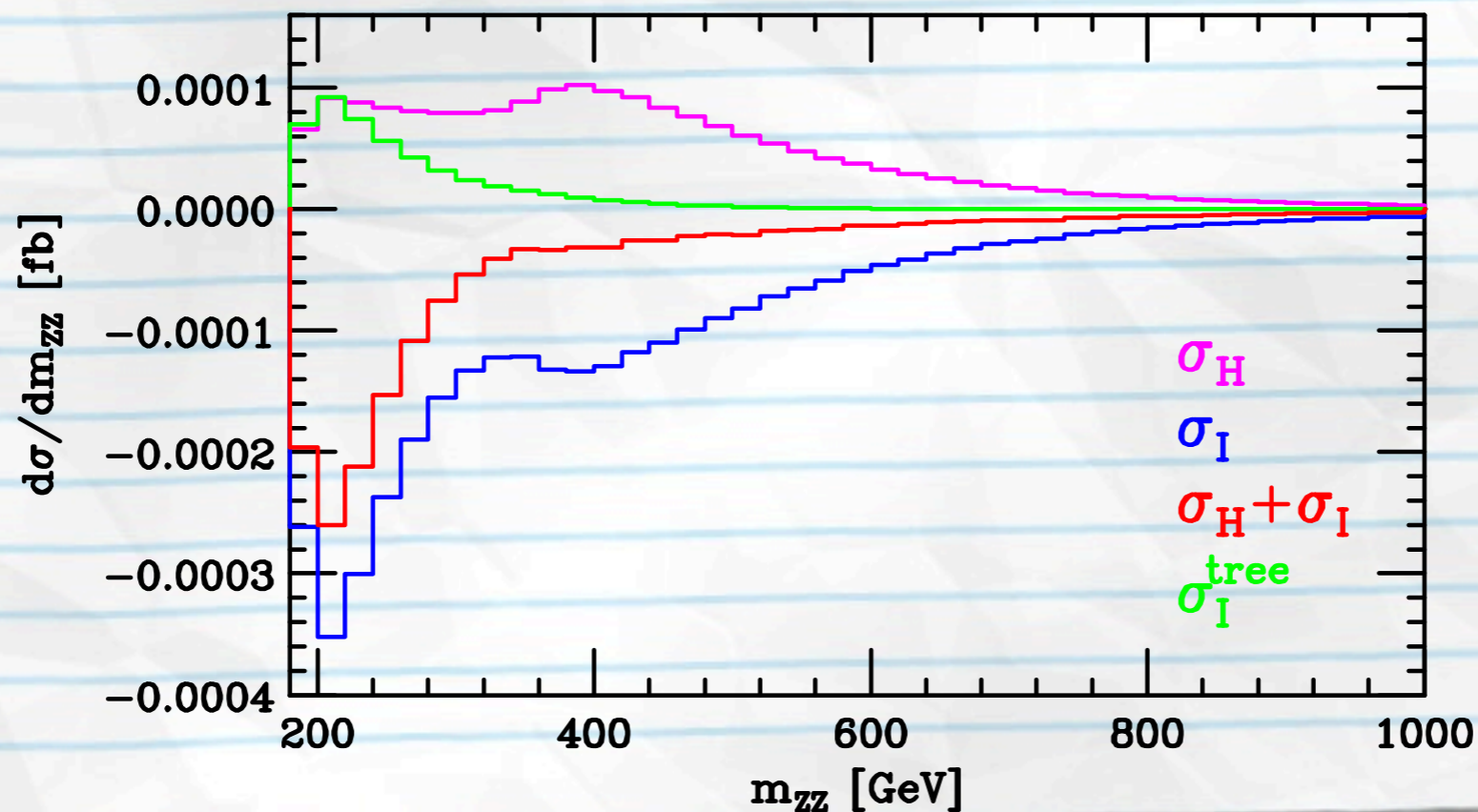
$$\frac{\sigma_H^{qg+q\bar{q}}}{\sigma_H} \sim \frac{\sigma_I^{qg+q\bar{q}}}{\sigma_I} \sim \begin{cases} 25\% & \text{for } p_{T,cut} = 30 \text{ GeV} \\ 50\% & \text{for } p_{T,cut} = 200 \text{ GeV} \end{cases}$$

➔ an harder cut probes regions of large  $x$ , where quark PDFs are relatively more important than gluon PDFs

# Results for $pp \rightarrow ZZ + \text{jet}$

importance of the interference term:

- \* the Higgs-mediated contribution becomes negative
- \* its shape changes
- \* its magnitude is reduced in the high  $p_T$  tail



$p_{T,cut} = 30$  GeV

$\sqrt{s} = 8$  TeV

# Results for $pp \rightarrow ZZ + \text{jet}$

- \* analogous to the ZZ case, the ratio of peak and off-peak cross sections at 8 TeV can be used to bound the Higgs width

$$\frac{\sigma_{off,ZZ+jet}^{H+I}(m_{ZZ} > 300 \text{ GeV})}{\sigma_{peak,ZZ+jet}^H} = 0.02890 \left( \frac{\Gamma_H}{\Gamma_H^{SM}} \right) - 0.0391 \sqrt{\frac{\Gamma_H}{\Gamma_H^{SM}}}$$

- \* in the next run of the LHC, expect about 100 events to be produced in the high mass tail

➔ alternative extraction of the Higgs width

# Conclusions

- \* Higgs width already constrained from interference effects in  $ZZ$  production
- \* similar analysis in the  $ZZ + \text{jet}$  channel is viable: in the high invariant mass tail,
  - the Higgs production cross section in the zero and one jet bins are comparable
  - the ratio of the Higgs signal to the LO background is larger in the one-jet bin than in the zero-jet bin

# Conclusions

- \* we performed a detailed analysis of the high invariant mass tail
  - interference effects between Higgs and QCD ZZ production:  
large and negative as required by unitarity
- \* as in the  $pp \rightarrow ZZ$  case, relate the ratio of peak and off-peak cross sections to the Higgs decay width relative to the Standard Model