Extra Higgs bosons in SUSY and beyond

based on 1505.05488 with F. Sala and A. Tesi and 1304.3670 ,1307.4937 with R. Barbieri, K. Kannike, F. Sala and A. Tesi

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GGI - Firenze, 7.9.2015

Intent and motivation

- One or more Higgs bosons?
 May the extra Higgs bosons be the lightest new particles?
- Identify a few most natural, motivated SUSY scenarios, in light of present and future experimental searches
- Sketch a search strategy for the extra scalar states
 - 1. Precision measurements of the couplings of the 125 GeV (standard-like) Higgs boson h_{LHC}
 - 2. Direct searches: $pp \rightarrow h_{LHC} + X$ $\downarrow \rightarrow decay products$

An "almost natural" SUSY spectrum



- Light top squarks: most strongly coupled to the Higgs boson
- Light gluino: affects the stop mass, and Higgs at two loops
- Light higgsinos: experimentally not very constrained

Where do we stand?

• A measure of fine-tuning: $\delta m_h^2 = M_{\rm NP}^2 < \Delta \cdot m_h^2$



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Higgs mass in the MSSM

 $m_h^2 < m_{hh}^2 = m_Z^2 c_{2\beta}^2 + \Delta_t^2$ Δ_t is the top-stop contribution to m_h



MSSM

• A second scalar lighter than 350 GeV is excluded (except a small window)



• Whole parameter space up to ~ 1 TeV will be tested by Higgs fit @ LHC14

MSSM



Higgs mass in the NMSSM

$W \supset \lambda SH_u H_d$

- Extra contribution to the tree-level Higgs mass $m_{hh}^2 = m_Z^2 c_{2\beta}^2 + \Delta_t^2 + \lambda^2 v^2 s_{2\beta}^2 \Rightarrow$ allows for lighter stops
- \bullet Alleviates fine-tuning in v for $\lambda\gtrsim 1 {\rm and}$ moderate $\,\tan\beta$



Assumptions

- General NMSSM: no specific singlet potential
- No CP violation in the Higgs sector
- No SUSY loops or invisible decays, e.g. $h_1 \rightarrow \chi \chi$
- Only loop contribution (from top-stop) $\Delta_t \sim 75$ GeV
- Naturalness: light stops, gluinos, Higgsinos; $\mu A_t \lesssim \langle m_{\tilde{t}}^2 \rangle$
- Description in terms of physical parameters

Higgs sector of a general NMSSM

CP-even states: $\mathcal{H} = (H, h, S)^T = R_{\delta}^{12} R_{\gamma}^{23} R_{\sigma}^{13} (h_3, h_1, h_2)^T \equiv R \mathcal{H}_{phys}$ Mass matrix:

$$\begin{split} \mathcal{M} &= R \cdot \operatorname{diag} \begin{pmatrix} m_{h_3}, m_{h_1}, m_{h_2} \end{pmatrix} \cdot R^T \\ &= \begin{pmatrix} m_A^2 + s_{2\beta}^2 (m_Z^2 - \lambda^2 v^2) + \frac{\Delta_t^2}{t_\beta^2} & \frac{s_{4\beta}}{2} (m_Z^2 - \lambda^2 v^2) - \frac{\Delta_t^2}{t_\beta^2} \\ \frac{s_{4\beta}}{2} (m_Z^2 - \lambda^2 v^2) - \frac{\Delta_t^2}{t_\beta^2} & m_Z^2 c_{2\beta}^2 + \lambda^2 v^2 s_{2\beta}^2 + \Delta_t^2 \\ \lambda v M_1 & \lambda v M_2 \\ \end{bmatrix} \\ &\xrightarrow{\mathbf{X} v M_1} \\ \mathbf{X} v M_2 \\ \mathbf{X} v$$

 $m_A^2 = m_{H^\pm}^2 - m_W^2 + \lambda^2 v^2$ (not the physical pseudoscalar mass)

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Decoupling limits: $m_A \to \infty$ or $M_3 \to \infty$

Modified Higgs couplings



Two limiting cases

S decoupled (both MSSM and NMSSM)

$$h = c_{\beta}H_d + s_{\beta}H_u \quad h_1 \equiv h_{LHC}$$

$$\begin{pmatrix} h \\ \hline h \\ \hline H \\ \hline h_3 \end{pmatrix}$$

(unlikely: H^{\pm} too light)





Singlet decoupled: h₃ production and decays

• Small values of λ : h_3 decays mainly into fermions ~ MSSM



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General case: 3-state mixing

6 independent parameters, $\delta, \gamma, \sigma \neq 0$

Not all combinations of $m_{h_1}, m_{h_2}, m_{h_3}, m_{H^{\pm}}$ and of $\lambda, \tan \beta, \Delta_t$ are viable

 $m_{h_3} = 750 \text{ GeV}, \lambda = 1.4, \Delta_t = 75 \text{ GeV}$



Higgs-singlet mixing: main features

$$\begin{split} \mathsf{SM} + 1 \text{ real singlet:} & H = (i\pi^+, \frac{v+h^0+\pi^0}{\sqrt{2}}), \qquad S = v_S + s^0. \\ \mathsf{Mass eigenstates:} & h = h^0 \cos \gamma + s^0 \sin \gamma, \ \phi = s^0 \cos \gamma - h^0 \sin \gamma. \end{split}$$

The phenomenology mainly depends on only 3 parameters:

$$\begin{split} \mu_h &= c_{\gamma}^2 \times \mu_{\rm SM}, \\ \mu_{\phi \to VV,ff} &= s_{\gamma}^2 \times \mu_{\rm SM}(m_{\phi}) \times (1 - \text{BR}_{\phi \to hh}), \\ \mu_{\phi \to hh} &= s_{\gamma}^2 \times \sigma_{\rm SM}(m_{\phi}) \times \text{BR}_{\phi \to hh}, \end{split}$$

 ϕ is like a heavy SM Higgs, with narrow width $+ \ hh$ channel

$$\sin^2 \gamma = rac{M_{hh}^2 - m_h^2}{m_{\phi}^2 - m_h^2}, \qquad M_{hh}^2 \propto v^2$$
 depends only on EW physics

Decays of $\boldsymbol{\varphi}$

At high mass the equivalence theorem relates the decay widths

$$\Gamma_{\phi \to ZZ} = \Gamma_{\phi \to hh} = \frac{1}{2} \Gamma_{\phi \to WW} \simeq \frac{1}{4}, \qquad m_{\phi} \gg m_h$$

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The triple couplings depend on the details of the potential

 $V = \mu_H^2 |H|^2 + \lambda_H |H|^4 + \lambda_{HS} |H|^2 S^2 + a_H |H|^2 S + \mu_S^2 S^2 + a_S S^3 + \lambda_S S^4$

7 parameters =
$$\underline{m_{\phi}, M_{hh}, v_s, \lambda_{HS}, \lambda_S} + m_h$$
, v
5 free parameters

The dependence on λ_{HS} , λ_S is very weak: v_s is the only relevant additional parameter that determines $BR_{\phi \to hh}$ and the h^3 coupling

$$BR_{\phi \to hh} = \frac{1}{4} - \frac{3}{4} \frac{v}{v_s} \frac{\sqrt{M_{hh}^2 - m_h^2}}{m_\phi} + \mathcal{O}(v^2/m_\phi^2)$$
$$g_{hhh} = g_{hhh}^{SM} \left(1 + \frac{2}{3} \frac{v}{v_s} \frac{\sqrt{M_{hh}^2 - m_h^2}}{m_\phi} \left(\frac{M_{hh}^2}{m_h^2} - 1 \right) + \mathcal{O}(v^2/m_\phi^2) \right)$$

Higgs couplings



Very large modifications of the triple Higgs coupling are possible: in principle observable at the LHC

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Higgs couplings: projections for the future

[Snowmass '13]

1σ reach in	s_{γ}^{2*}	$\left 1 - \frac{g_{hhh}}{g_{hhh}^{\rm SM}}\right $
LHC8	0.2	_
LHC14	0.08-0.12	—
HL-LHC	$4-8 \times 10^{-2}$	0.5
HE-LHC	—	0.2
FCC-hh	_	0.08
ILC	2×10^{-2}	0.21-0.83
ILC-up	4×10^{-3}	0.13-0.46
CLIC	$2-3 \times 10^{-3}$	0.1-0.21
CEPC	2×10^{-3}	—
FCC-ee	1×10^{-3}	—

* projections on most precise coupling

The result of the Higgs fit is approximated well by the precision on g_{hVV}



Higgs couplings



Region relevant for an e⁺e⁻ collider

Direct searches

 ϕ is like a heavy SM Higgs boson: $\phi \to VV$ dominant decay mode



Already more sensitive than Higgs couplings at low masses!

Direct searches

 ϕ is like a heavy SM Higgs boson $+~\phi \rightarrow hh$ decay width



Other decay channels can also be relevant:

► $hh \rightarrow 2b \, 2\gamma$ dominates only at low $m_{\phi} \lesssim 400$ GeV [1406.5053] [CMS-HIG-13-032]

▶
$$hh \rightarrow 2b 2\tau$$
, $hh \rightarrow 4\tau$, $hh \rightarrow 2b 2W$
[No et al. '13], [Kotwal et al. '15], [Martin-Lozano et al. '15]

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➡ rescale 8 TeV LHC data with the parton luminosity of the bkg

[see also Salam, Weiler '14 and Thamm, Torre, Wulzer '15]



The limit on the cross-section is mainly determined by the number of background events around the resonance peak

This method is subject to a number of rather strong assumptions!

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Extrapolation of the limits

• # of background events:

$$B \propto L \cdot \sum_{i,j} \int d\hat{s} \frac{d\mathcal{L}_{ij}}{d\hat{s}} (\sqrt{\hat{s}}, \sqrt{s}) \cdot \hat{\sigma}_{ij}(\hat{s}) \approx L \cdot \frac{\Delta \hat{s}}{m} \cdot \sum_{i,j} c_{ij} \frac{d\mathcal{L}_{ij}}{d\hat{s}}$$
parton luminosity
parton luminosity
$$\hat{\sigma}_{ij} \sim c_{ij}/\hat{s} \text{ partonic cross-section}$$

$$ij \rightarrow h_2$$

• # of signal events: $S = \sigma \cdot L$



Extrapolation of the limits

Some check of our assumptions...



 The excluded cross-sections scale as (parton luminosity)^{1/2}

Below a certain mass the SM thresholds become relevant: we do not extrapolate the exclusions beyond that point.

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 The excluded cross-sections scale as (parton luminosity)^{1/2}

Below a certain mass the SM thresholds become relevant: we do not extrapolate the exclusions beyond that point.

 Our extrapolations are consistent – within a factor of O(1) – with several other studies at 13, 14, 33 TeV...

> Brownson et al. '13 Gouzevich et al. '13









Direct searches always dominate for lower masses (< 1 TeV)

Generic singlet: direct searches @ LHC



Considering both $\phi \to VV$ and $\phi \to hh$ the combined reach does not strongly depend on $BR_{\phi \to hh}$

Generic singlet: direct searches @ FCC



At high masses $\phi \to VV$ is always dominant (BR $_{\phi \to hh} \sim 1/4$)

Generic singlet: summary of bounds



Back to the NMSSM

The results for the generic singlet-Higgs are translated to the NMSSM:



 $M_{hh} = m_Z^2 \cos^2 2\beta + v^2 \lambda^2 \sin^2 2\beta + \Delta^2$

Already w/ 100 fb⁻¹ direct searches more powerful than Higgs fit @ HL

Back to the NMSSM

The results for the generic singlet-Higgs are translated to the NMSSM:



 $M_{hh} = m_Z^2 \cos^2 2\beta + v^2 \lambda^2 \sin^2 2\beta + \Delta^2$

Direct reach @ 100 TeV comparable with sensitivity of FCC-ee

What if h_{LHC} is not the lightest one?

- Still room for a singlet-like state lighter than 125 GeV, compatibly with LEP.
- Regions of parameter space difficult to probe... $\mu_{h_2} = \sin^2 \gamma \times \mu_h^{SM}$



What if h_{LHC} is not the lightest one?

- Still room for a singlet-like state lighter than 125 GeV
- Signal strengths are modified in the 3-state mixing case
 - Example: $h_2 \to \gamma \gamma ~(m_{h_3} = 500 \,\text{GeV}, s_{\sigma}^2 = 10^{-3})$

Badziak et al. '13 Barbieri, B, Kannike, S, T '13 Ellwanger et al. '14 King et al. '14 Jeong et al. '14



CP-odd states

- Two pseudoscalar states A, A_S that mix. Their mass matrix contains additional parameters...
- The singlet-like state can be light: discovery challenging Example: [King et al. 1408.1120] Scale-invariant NMSSM $0.6 \le \lambda \le 0.7, \qquad -0.3 \le \kappa \le 0.3,$ $1.5 \le \tan \beta \le 2.5, \quad 100 \,\text{GeV} \le |\mu_{\text{eff}}| \le 185 \,\text{GeV}$



Beyond SUSY: "neutral naturalness"

- Insisting with naturalness, the s-particles cannot be pushed to too high masses (even in the NMSSM)... Where are they?
- Twin Higgs: consider the SM + a "twin" copy SM':
 - Higgs potential SO(8) invariant + Z_2 symmetry SM \leftrightarrow SM'
 - ► The Higgs is a Goldstone boson of SO(8)/SO(7)
 - The Higgs mass is protected from radiative corrections, without coloured states at the weak scale; all other particles are heavy or very weakly coupled

$$\begin{split} V &= \lambda (\Phi^2 - f_0^2)^2 + \delta V & \text{explicitly breaks G in order to} \\ \Phi &= (h, S) & \text{generate Higgs mass and potential} & \begin{cases} \langle h^2 \rangle = v^2 \\ \langle \Phi^2 \rangle = f^2 \\ \delta V &= m^2 h^2 + \kappa h^4 \end{cases} \end{split}$$

▶ 8 d.o.f.: 1 light Higgs + 1 "radial mode" + 6 eaten Goldstones

Chacko et al. '04 Barbieri et al. '05

Twin Higgs

- There is at least one singlet state σ with mass $m_\sigma^2 pprox \lambda f^2$
- Higgs-singlet mixing: exactly the same situation as before!

$$\sin^2 \gamma = \frac{M_{hh}^2 - m_h^2}{m_\sigma^2 - m_h^2} \qquad \qquad M_{hh}^2 = (m_\sigma^2 + m_h^2) \frac{v^2}{f^2}$$

• The model is fully determined by 2 parameters: m_{σ} , f (and m_h , v)



Summary & conclusions

- Simplified NMSSM scenarios provide "almost natural" new physics cases with extra scalars that can be studied at the LHC
- **Higgs signal strengths:** strong bound in MSSM and NMSSM w/ singlet decoupled: almost whole parameter space covered by LHC14
- Direct searches: already the strongest constraint in NMSSM w/ doublet decoupled; significant improvement expected: already with 100 fb⁻¹ sensitivity comparable to Higgs couplings with 3000 fb⁻¹.
- Triple Higgs: large deviations from SM possible, unlike in MSSM
- Looking for singlets is easy and motivated by many natural models, in SUSY and beyond!
- A state lighter than 125 GeV is still allowed: discovery challenging

Backup

Electroweak Precision Tests

Relevant contribution from loops of the new Higgses? $NO \checkmark$

• H decoupled: couplings scale as $\sin^2 \gamma \ (\cos^2 \gamma)$



• S decoupled: larger effects possible in general, but limits on the mixing angle $\delta \simeq 0 \Rightarrow$ no new constraint



General solutions for the mixing angles

$$\begin{split} s_{\gamma}^{2} &= \frac{\det M^{2} + m_{h_{1}}^{2}(m_{h_{1}}^{2} - \operatorname{tr} M^{2})}{(m_{h_{1}}^{2} - m_{h_{2}}^{2})(m_{h_{1}}^{2} - m_{h_{3}}^{2})}, \\ s_{\sigma}^{2} &= \frac{m_{h_{2}}^{2} - m_{h_{1}}^{2}}{m_{h_{2}}^{2} - m_{h_{3}}^{2}} \frac{\det M^{2} + m_{h_{3}}^{2}(m_{h_{3}}^{2} - \operatorname{tr} M^{2})}{\det M^{2} - m_{h_{2}}^{2}m_{h_{3}}^{2} + m_{h_{1}}^{2}(m_{h_{2}}^{2} + m_{h_{3}}^{2} - \operatorname{tr} M^{2})}, \\ \sin 2\alpha &= \left(\pm 2|s_{\gamma}s_{\sigma}|\sqrt{1 - s_{\sigma}^{2}}\sqrt{1 - \sin^{2}2\xi}(m_{h_{3}}^{2} - m_{h_{2}}^{2}) + \left[m_{h_{3}}^{2} - m_{h_{2}}^{2}s_{\gamma}^{2} + s_{\sigma}^{2}(1 + s_{\gamma}^{2})(m_{h_{2}}^{2} - m_{h_{3}}^{2}) - (1 - s_{\gamma}^{2})m_{h_{1}}^{2}\right]\sin 2\xi \right) \\ &+ \left[m_{h_{3}}^{2} - m_{h_{2}}^{2}s_{\gamma}^{2} + s_{\sigma}^{2}(1 + s_{\gamma}^{2})(m_{h_{2}}^{2} - m_{h_{3}}^{2}) - (1 - s_{\gamma}^{2})m_{h_{1}}^{2}\right]\sin 2\xi \right) \\ &\times \left(\left[m_{h_{3}}^{2} - m_{h_{1}}^{2} + s_{\gamma}^{2}(m_{h_{1}}^{2} - m_{h_{2}}^{2})\right]^{2} + (m_{h_{3}}^{2} - m_{h_{2}}^{2})(1 - s_{\gamma}^{2})s_{\sigma}^{2} \right) \\ &\times \left[2m_{h_{1}}^{2}(1 + s_{\gamma}^{2}) - 2(m_{h_{3}}^{2} + s_{\gamma}^{2}m_{h_{2}}^{2}) + s_{\sigma}^{2}(m_{h_{3}}^{2} - m_{h_{2}}^{2})(1 - s_{\gamma}^{2})\right] \right)^{-1/2} \end{split}$$

where M is the 2x2 submatrix of \mathcal{M} in the 1-2 sector, and $\boldsymbol{\xi}$ its mixing angle (contains the dependence on $\boldsymbol{\lambda}$ and Δ_{t})