

# SUSY@ILC

**Abdelhak DJOUADI**  
**(LPT Orsay/Next Southampton)**

- 1. Probing SUSY**
- 2. Precision SUSY measurements at the ILC**
- 3. Determining the SUSY Lagrangian**
- 4. Summary**

**From the physics chapter of the ILC Reference Design Report:  
“Physics at the ILC”, August 2007.**

# 1. Introduction: motivations for low-energy SUSY

If SUSY is to solve some of the most severe problems of the SM:

**We need light SUSY particles:  $M_S \lesssim 1 \text{ TeV}$ .**

- The hierarchy problem: radiative corrections to the Higgs masses

$$\Delta M_H^2 = \frac{\lambda_f^2 N_f}{4\pi^2} \left[ (m_f^2 - M_S^2) \log\left(\frac{\Lambda}{M_S}\right) + 3m_f^2 \log\left(\frac{M_S}{m_f}\right) \right] + \mathcal{O}\left(\frac{1}{\Lambda^2}\right)$$

- The unification problem: the slopes of the  $\alpha_i$  SM gauge couplings need to be fixed early enough to meet at  $M_{\text{GUT}} \sim 2 \times 10^{16} \text{ GeV}$ .
- The dark matter problem: the electrically neutral, weakly interacting, stable LSP should have a mass  $\lesssim \mathcal{O}(1 \text{ TeV})$  for  $\Omega h^2$  to match WMAP.

**In this case, sparticles are accessible at future machines.**

- We expect great discoveries at the LHC.
- We will have a great deal of exciting physics to do at the ILC.

# 1. Introduction: SUSY models

**Focus mainly on the Minimal Supersymmetric Standard Model (MSSM):**

- minimal gauge group:  $SU(3) \times SU(2) \times U(1)$ ,
- minimal particle content: 3 fermion families and 2  $\Phi$  doublets,
- $R = (-1)^{(2s+L+3B)}$  parity is conserved,
- minimal set of terms (masses, couplings) breaking “softly” SUSY.

To reduce the number of the (too many in general) free parameters:

- impose phenomenological constraints:  $\mathcal{O}(20)$  free parameters,
- unified models,  $\mathcal{O}(5)$  parameters (mSUGRA:  $m_0, m_{\frac{1}{2}}, A_0, \tan \beta, \epsilon_\mu$ ),

**In this talk, I will concentrate on the MSSM with gravity mediated breaking.**

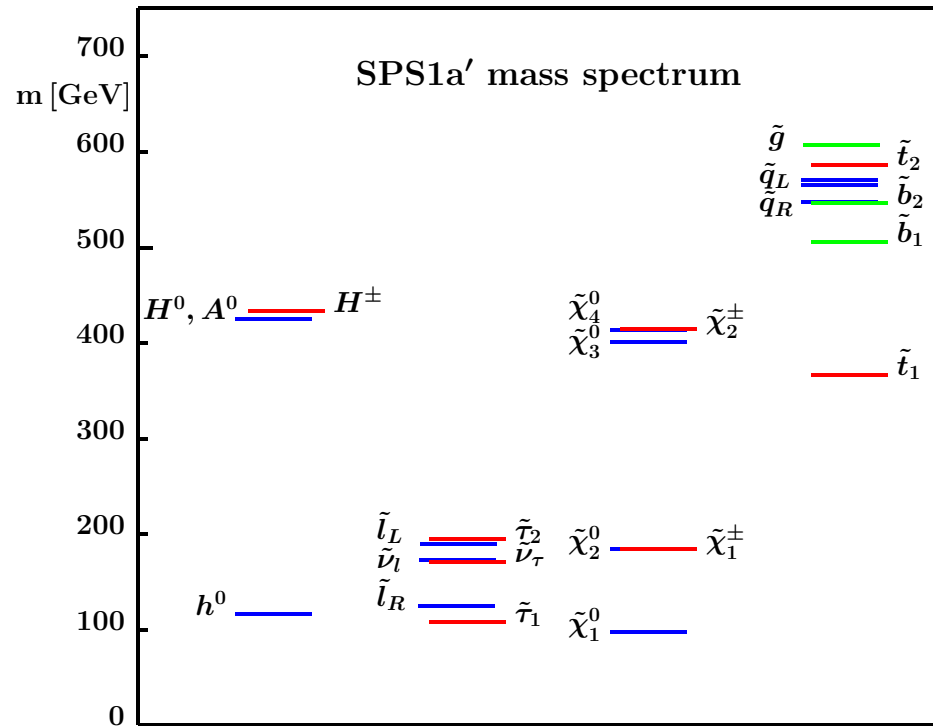
But, one should not forget that:

- other possibilities are models with GMSB/AMSB....
- the impact of relaxing some MSSM basic assumptions can be large
- other scenarios are possible (strings, right-handed neutrinos,...)

**There is a need for model independent analyses...**

# 1. Introduction: example of SUSY spectrum

SPS1a':  $m_{1/2} = 250\text{GeV}$ ,  $m_0 = 70\text{GeV}$ ,  $A_0 = -300\text{GeV}$ ,  $\tan\beta = 10$ ,  $\mu >$



| $\tilde{p}/\text{mass}$ | $\chi_1^0$ | $\chi_2^0$ | $\chi_1^\pm$ | $\tilde{e}_1$ | $\tilde{e}_2$ | $\tilde{\nu}_e$ | $\tilde{\tau}_1$ | $\tilde{\tau}_2$ | $\tilde{\nu}_\tau$ | $\tilde{t}_1$ | $\tilde{b}_1$ |
|-------------------------|------------|------------|--------------|---------------|---------------|-----------------|------------------|------------------|--------------------|---------------|---------------|
| <b>SPS1a'</b>           | 98         | 184        | 184          | 125           | 190           | 172             | 108              | 195              | 170                | 366           | 506           |
| <b>SPS1a</b>            | 96         | 177        | 176          | 143           | 202           | 186             | 133              | 206              | 185                | 379           | 492           |

# 1. Introduction: probing SUSY

All these particles will be produced at the LHC (direct/cascades)...

These particles can also be produced directly at the ILC...

**But producing these new states is not the whole story! We need to:**

- measure the masses and mixings of the newly produced particles, their decay widths, branching ratios, production cross sections, etc...;
- verify that there are indeed superpartners and, thus, determine their spin and parity, gauge quantum numbers and their couplings;
- reconstruct the low-energy soft-SUSY breaking parameters with the smallest number of assumptions (model independent way);
- ultimately, unravel the fundamental SUSY breaking mechanism and shed light on the physics at the very high energy scale.
- make the connection to cosmology and predict the relic density.

**To achieve this goal, a combination of LHC and ILC is mandatory!**

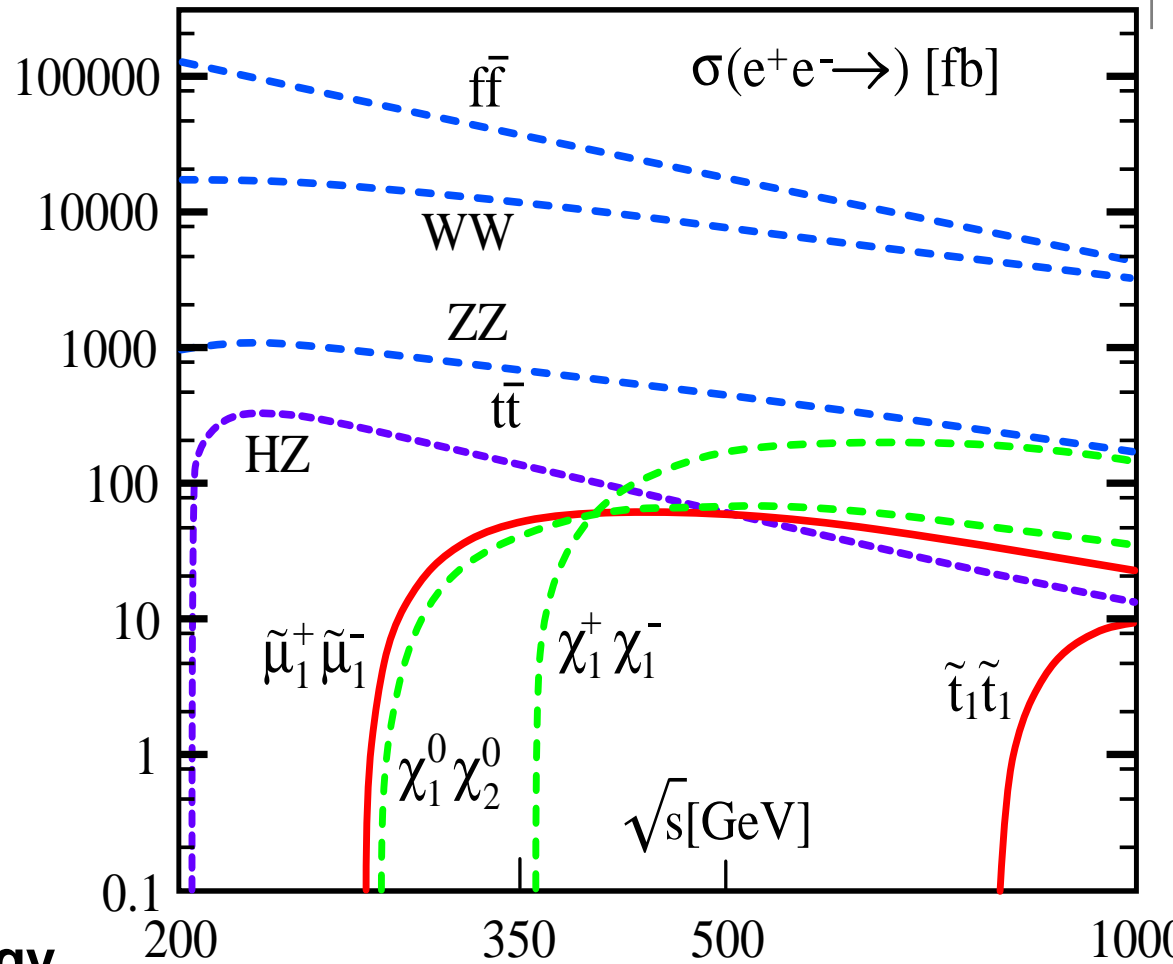
# 1. Introduction: the role of the ILC

## At the LHC:

- copious  $\tilde{q}/\tilde{g}$  production
- $\tilde{\ell}/\chi$  from cascades
- complicated topologies
- very large backgrounds
- difficult environment.

## At the ILC:

- direct  $\tilde{\ell}/\chi$  production
- large production rates
- good signal to bkg ratios
- very clean environment
- possibility of tuning energy
- initial beam polarization
- more collider options...



## 2. Precision SUSY measurements: the $\chi$ sector

- **Charginos:** mixtures of the charged higgsinos and gauginos

$$\tilde{W}^\pm, \tilde{h}_{2/1}^\pm \longrightarrow \chi_{1,2}^\pm$$

The general chargino mass matrix, in terms of  $M_2$ ,  $\mu$  and  $\tan \beta$ , is

$$\mathcal{M}_C = \begin{bmatrix} M_2 & \sqrt{2}M_W s_\beta \\ \sqrt{2}M_W c_\beta & \mu \end{bmatrix}, \quad s_\beta \equiv \sin \beta \text{ etc}$$

- **Neutralinos:** mixtures of the neutral higgsinos and gauginos

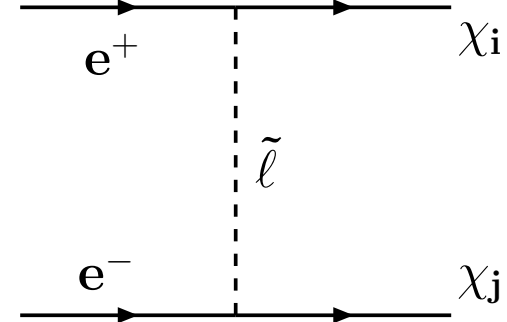
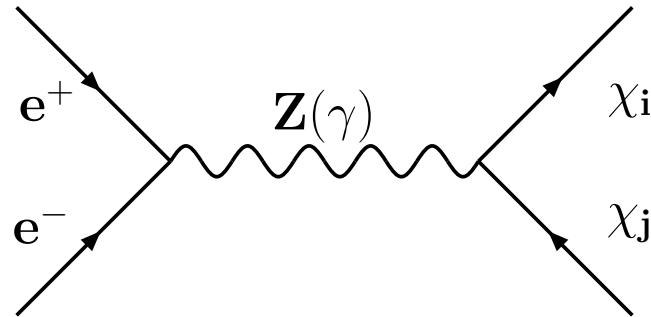
$$\tilde{B}, \tilde{W}_3, \tilde{H}_1^0, \tilde{H}_2^0 \longrightarrow \chi_{1,2,3,4}^0$$

The 4x4 mass matrix depends on  $\mu$ ,  $M_2$ ,  $\tan \beta$ ,  $M_1$ ; given by:

$$\mathcal{M}_N = \begin{bmatrix} M_1 & 0 & -M_Z s_W c_\beta & M_Z s_W s_\beta \\ 0 & M_2 & M_Z c_W c_\beta & -M_Z c_W s_\beta \\ -M_Z s_W c_\beta & M_Z c_W c_\beta & 0 & -\mu \\ M_Z s_W s_\beta & -M_Z c_W s_\beta & -\mu & 0 \end{bmatrix}$$

## 2. Precision SUSY measurements: the $\chi$ sector

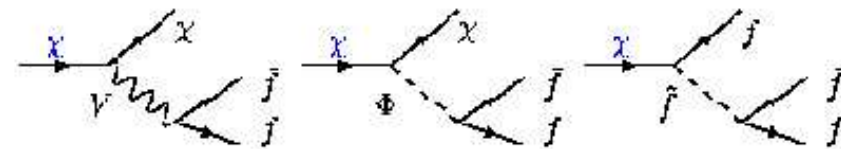
$\chi$  production:



- $e^+e^- \rightarrow \chi_i^\pm \chi_j^\pm$ :  $s$ -channel  $\gamma$ ,  $Z$  and  $t$ -channel  $\tilde{\nu}_e$ ; large  $\sigma$  for  $i=j$
- $e^+e^- \rightarrow \chi_i^0 \chi_j^0$ :  $s$ -channel  $Z$  and  $t$ -channel  $\tilde{e}$ ;  $\sigma = \mathcal{O}(10 \text{ fb})$ .
- $e^\pm$  beam polarization selects various production channels
- cross section for  $\chi^\pm$  rises steeply near threshold,  $\sigma \propto \beta$
- cross sections for  $\chi^0$  rise less steeply in general,  $\sigma \propto \beta^3$

$\chi$  decays:

- in general  $\chi_i \rightarrow V \chi_j, \Phi \chi_j, f \bar{f}$
- possibility of cascade decays
- signature:  $\cancel{E}_T$  from escaping  $\chi_1^0$

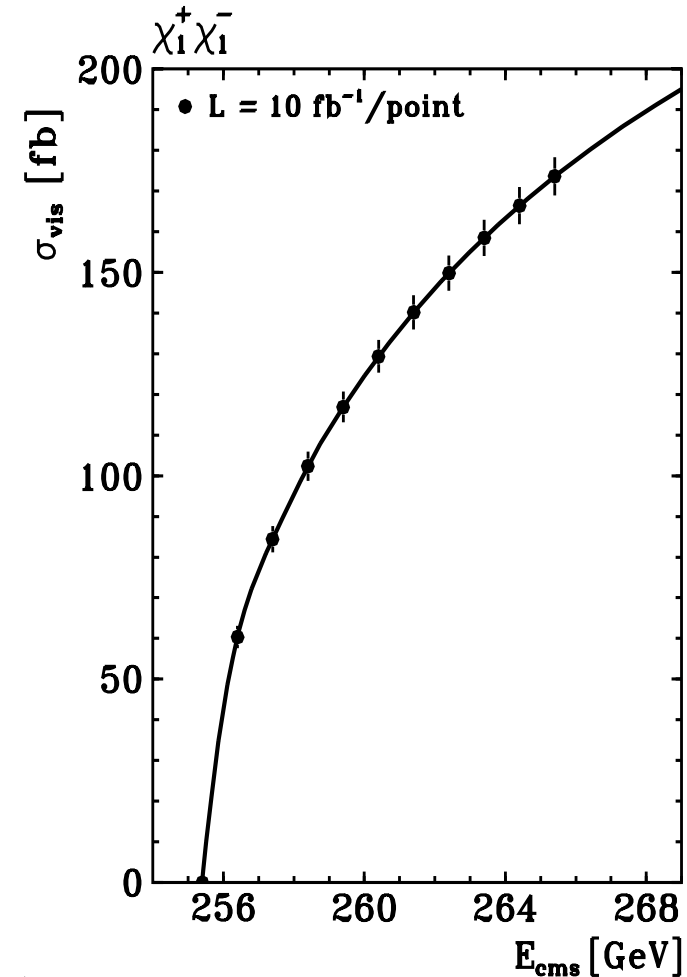




## 2. Precision SUSY measurements: the $\chi$ sector

### Measurement of $\chi^\pm/\chi^0$ masses:

- from a threshold scan,  $\Delta m_{\chi_1^\pm} \sim 50$  MeV for  $m_{\chi_1^\pm} \sim 200$  GeV as steep rise  $\sigma \propto \beta$ .
- $\Delta m_{\chi_1^\pm} \sim 0.1\%$  in continuum from dijet mass in  $e^+e^- \rightarrow \chi_1^+\chi_1^- \rightarrow \ell^\pm \nu q\bar{q}' \chi_1^0\chi_1^0$
- from dijet mass,  $m_{\chi_1^0}$  determination with precision  $\Delta(m_{\chi_1^\pm} - m_{\chi_1^0}) = \mathcal{O}(50)$  MeV.
- for small  $m_{\chi_1^\pm} - m_{\chi_1^0}$ , use  $e^+e^- \rightarrow \chi_1^+\chi_1^-\gamma$  to measure both  $m_{\chi_1^\pm}/m_{\chi_1^0}$  from spectra.
- $e^+e^- \rightarrow \chi_2^0\chi_1^0 \rightarrow \ell^+\ell^-\chi_1^0\chi_1^0$  allows an accuracy  $\Delta(m_{\chi_2^0} - m_{\chi_1^0}) = \mathcal{O}(0.1\%)$



## 2. Precision SUSY measurements: the $\chi$ sector

### Determination of spin:

- idea from excitation curve and angular distribution from production,
- sure with angular distributions of polarized  $\chi$  decays with  $e_{\text{pol}}^{\pm}$ .

### Determination of Majorana nature of neutralinos:

- guess from  $\beta^3$  threshold behavior of  $\sigma(e^+e^- \rightarrow \chi_i^0 \chi_j^0)$ ,
- $e^-e^- \rightarrow \tilde{e}^-\tilde{e}^-$  occurs only because Majorana  $\chi^0$  exchange.

### Verification of the SUSY identity of gauge/Yukawa couplings:

- production cross sections for  $\chi^0, \chi^{\pm} \propto \hat{g}(e\tilde{e}\chi^0), \hat{g}(e\tilde{\nu}\chi^{\pm})$ ,
- combining with  $\tilde{\ell}$  production,  $\Delta\tilde{g} = 0.7\%$  and  $\Delta\tilde{g}' = 0.2\%$

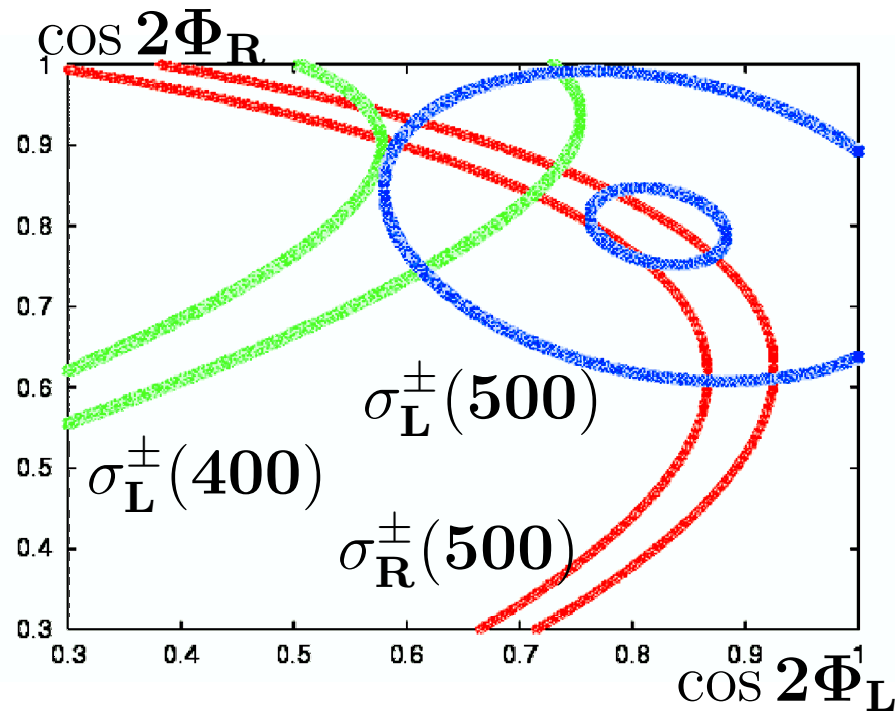
### Determination of the chargino/neutralino mixing angles:

- $\sigma(e^+e^- \rightarrow \chi_i^+ \chi_j^-)$  is binomial in the  $\chi^{\pm}$  mixing angles  $\cos 2\phi_{L,R}$   
→ determined in a model independent way using polarized  $e^{\pm}$  beams

(neutralino mixing from  $\chi^0$  production/decay, see Jan Kalinowski).

## 2. Precision SUSY measurements: the $\chi$ sector

**SPS1a:**  $c_{2\phi_L} = [0.62, 0.72]$ ,  $c_{2\phi_R} = [0.87, 0.91]$  at 95% CL at  $\sqrt{s} = \frac{1}{2}$  TeV



- **CPC:**  $e^+e^- \rightarrow \chi_i^+ \chi_j^-$  alone allows to determine basic parameters;
- sneutrinos can be probed up to masses of 10 TeV with polarization.
- **CPV:**  $e^+e^- \rightarrow \chi_i^0 \chi_j^0$  would be needed (with direct probe of CPV).

## 2. Precision SUSY measurements: the $\tilde{f}$ sector

Sfermion system described by  $\tan \beta$ ,  $\mu$  and 3 param. for each species:

$m_{\tilde{f}_L}$ ,  $m_{\tilde{f}_R}$  and  $A_f$ . For 3d generation, mixing  $\propto m_f$  to be included.

$$\mathcal{M}_{\tilde{f}}^2 = \begin{pmatrix} m_f^2 + m_{\tilde{f}_L}^2 + (I_f^{3L} - e_f s_W^2) M_Z^2 c_{2\beta} & m_f A_f - \mu (\tan \beta)^{-2I_f^{3L}} \\ m_f A_f - \mu (\tan \beta)^{-2I_f^{3L}} & m_f^2 + m_{\tilde{f}_R}^2 + e_f s_W^2 M_Z^2 c_{2\beta} \end{pmatrix}$$

They are diagonalized by  $2 \times 2$  rotation matrices of angle  $\theta_f$ , which turn the current eigenstates  $\tilde{f}_L, \tilde{f}_R$  into the mass eigenstates  $\tilde{f}_1, \tilde{f}_2$ .

$$m_{\tilde{f}_{1,2}}^2 = m_f^2 + \frac{1}{2} \left[ m_{LL}^2 + m_{RR}^2 \mp \sqrt{(m_{LL}^2 - m_{RR}^2)^2 + 4m_f^2 X_f^2} \right]$$

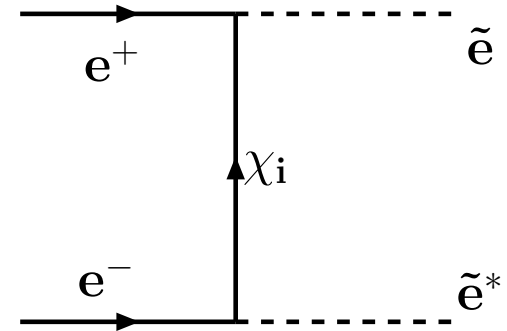
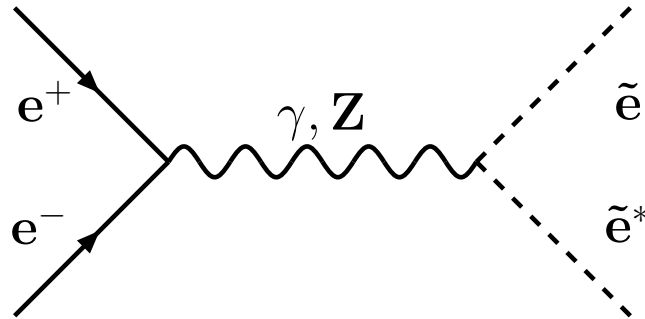
**Note:** mixing very strong in stop sector,  $X_t = A_t - \mu \cot \beta$  and

generates mass splitting between  $\tilde{t}_1, \tilde{t}_2$ , leading to light  $\tilde{t}_1$ ;

mixing in sbottom/stau sectors also for large  $X_{b,\tau} = A_{b,\tau} - \mu \tan \beta$ .

## 2. Precision SUSY measurements: the $\tilde{l}$ sector

$\tilde{l}$  production:



- $e^+e^- \rightarrow \tilde{\mu}^+\tilde{\mu}^-/\tilde{\tau}^+\tilde{\tau}^-/\tilde{\nu}_{\mu,\tau}\tilde{\nu}_{\mu,\tau}$ : s-channel  $\gamma, Z$  exchange;
- $e^+e^- \rightarrow \tilde{e}^+\tilde{e}^-$ : s-channel  $\gamma, Z$  and t-channel  $\chi^0$  exchange;
- $e^+e^- \rightarrow \tilde{\nu}_e\tilde{\nu}_e$ : s-channel  $Z$  and t-channel  $\chi^\pm$  exchange;

Again, in this case:

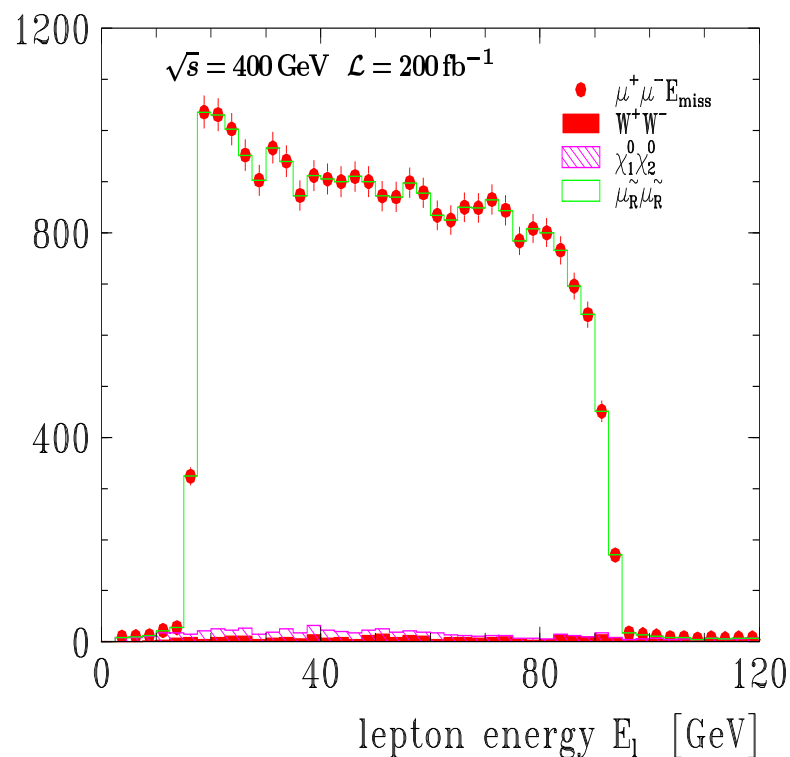
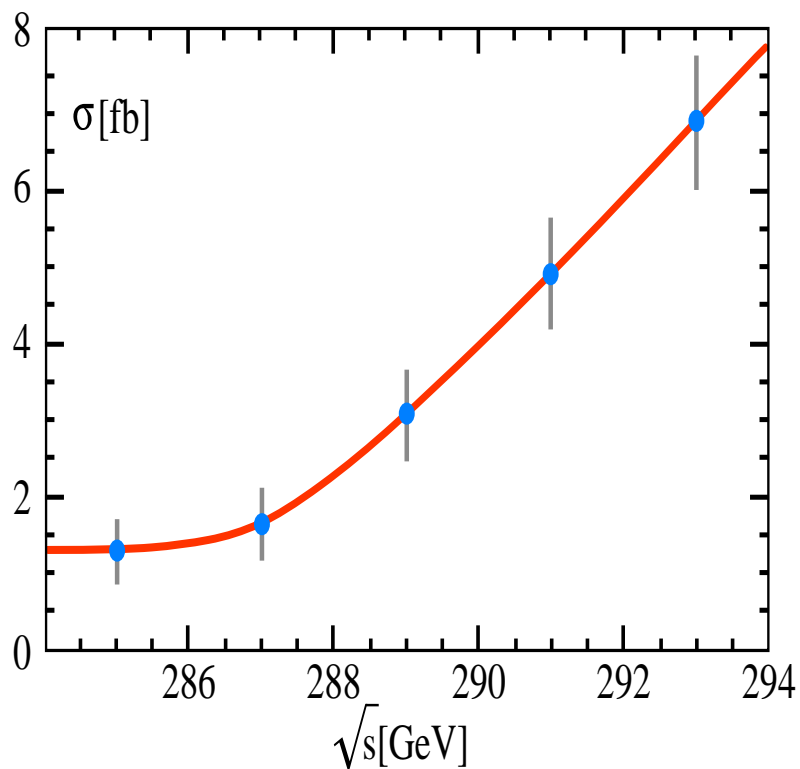
- $e^\pm$  beam polarization selects various channels/chiralities for  $\tilde{e}, \tilde{\nu}_e$ ;
- $\tilde{e}_{L/R}$  production in  $e_{L/R}^-e_{L/R}^-$  collisions;
- cross sections for  $\tilde{e}, \tilde{\nu}_e$  rise steeply near threshold,  $\sigma \propto \beta$ ,
- cross sections for 2d/3d generation rise less steeply,  $\sigma \propto \beta^3$ .

**Slepton decays:** in general  $\tilde{l} \rightarrow l\chi_1^0$  with possible cascades.

## 2. Precision SUSY measurements: the $\tilde{\ell}$ sector

**Slepton mass measurement from threshold scan and in continuum:**

- polarized  $e^+e^-$ :  $\Delta m_{\tilde{e}_R} = 0.2 \text{ GeV}$  and  $\Delta \Gamma_{\tilde{e}_R} = 0.25 \text{ GeV}$ ;
- improvement by 4 using  $e^-e^-$  but 2 times worse for  $\tilde{\mu}$  in  $e^+e^-$ ;
- from  $E_\ell$  spectra in  $\tilde{\ell} \rightarrow \ell \chi_1^0$  decays, 0.1% precision for  $m_{\tilde{\ell}}$  and  $m_{\chi_1^0}$ ;
- $\tilde{\nu}_e$  more involved,  $m_{\tilde{\nu}}$  at 1% from  $e^+e^- \rightarrow \tilde{\nu}_e \tilde{\nu}_e \rightarrow \nu_e \chi_1^0 e^\pm \chi_1^\mp$



## 2. Precision SUSY measurements: the $\tilde{\ell}$ sector

**Slepton spin determination:** conceptually very simple in  $e^+e^-$ :

- hint from the P-wave onset of the excitation curve (not sufficient),
- the  $\sin^2\theta$  behavior of the cross section (for  $\tilde{e}$ , near threshold).

**Coupling determination:** check of the SUSY identity  $g_{\text{gauge}} = \tilde{g}_{\text{Yukawa}}$ :

- from  $\tilde{e}$  and  $\tilde{\nu}_e$  production cross sections (t-channel contributions),
- also in  $\chi^\pm$  and  $\chi^0$  production (works also for heavy  $\tilde{\ell}$ ).

**In the case of  $\tilde{\tau}$ :**  $\tilde{\tau}$  mixing and final state  $\tau$  slightly complicate pattern:

- mass determination as above for  $\tilde{\mu}$  but accuracy  $\sim 3$  times worse,
- complication ( $\gamma\gamma$  bkg) when  $\tilde{\tau}_1$  almost degenerate with the LSP  $\chi_1^0$ ,
- mixing  $\theta_{\tilde{\tau}}$  measurable from  $\sigma(e^+e^- \rightarrow \tilde{\tau}_1\tilde{\tau}_1)$  with  $\neq$  beam polarization,
- polarization of  $\tau$ -lepton measurable and helps for model discrimination,
- $\mu$ ,  $A_\tau$  and  $\tan\beta$  can be determined from  $\sigma(\tilde{\tau}\tilde{\tau})$  and  $\tau$  polarization
- $H, A \rightarrow \tilde{\tau}_1\tilde{\tau}_2$  decays give extra information ( $A_\tau$  measurement)...

## 2. Precision SUSY measurements: the $\tilde{Q}$ sector

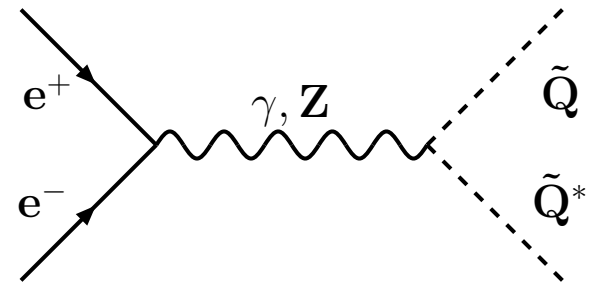
Third generation  $\tilde{Q} = \tilde{t}_1, \tilde{b}_1$ : possibly lightest squarks due to mixing.

- In particular,  $\tilde{t}_1$  is in general the lightest squark (RGE+mixing).
- Light stops needed in models with electroweak baryogenesis.
- Light stops are very difficult to detect at the LHC (large  $tt$  bkg).

$\tilde{Q}$  production at ILC:

$e^+e^- \rightarrow \tilde{t}_1\tilde{t}_1$  and  $\tilde{b}_1\tilde{b}_1$ :

via s-channel  $\gamma, Z$  exchange



$\tilde{t}_1$  decays:

- if heavy, two-body  $\tilde{t}_1 \rightarrow t\chi_1^0, b\chi_1^+$ ,
- otherwise multi-body decays,
- or loop induced  $\tilde{t}_1 \rightarrow c\chi_1^0$  decays.

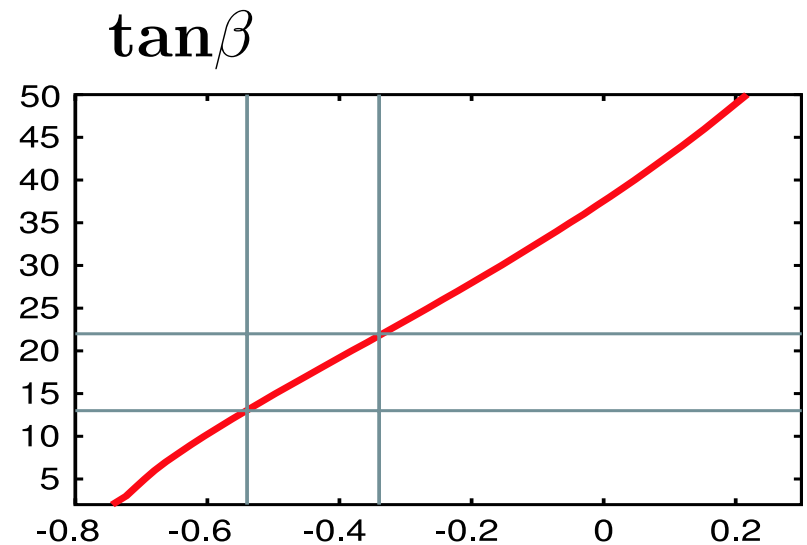
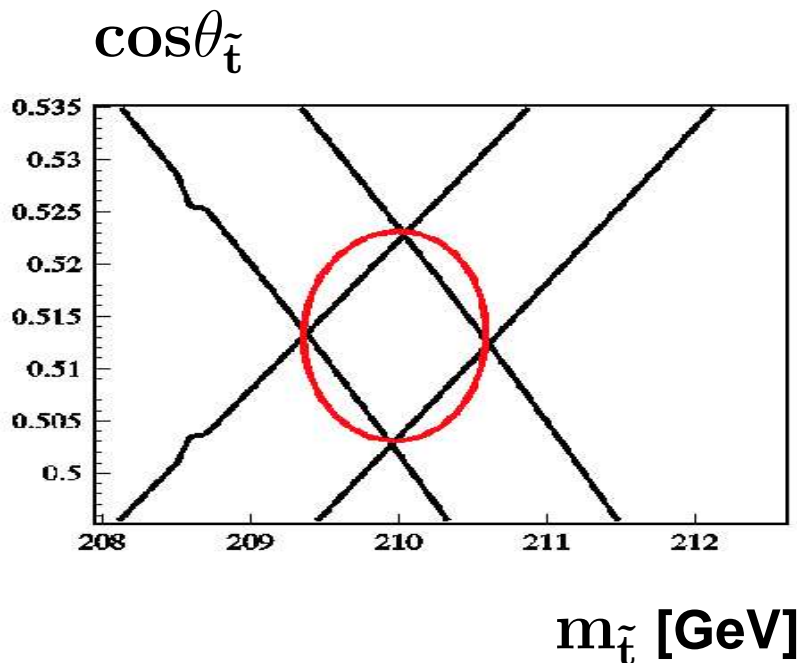




## 2. Precision SUSY measurements: the $\tilde{Q}$ sector

Phenomenology of  $\tilde{t}_1$  and  $\tilde{b}_1$  at the ILC similar to that of  $\tilde{\tau}_1$ :

- Masses and mixing obtained from production with polarized beams, ex: study of  $\sigma(e_R^- e_L^+, e_L^- e_R^+ \rightarrow \tilde{t}_1 \tilde{t}_1)$  for  $\tilde{t}_1 \rightarrow b\chi_1^\pm, c\chi_1^0$  at 500 GeV.
- Top quark polarization in  $\tilde{t}_1, \tilde{b}_1$  decays provides crucial information ex: top polarization in  $e_L^+ e_R^- \rightarrow \tilde{b}_1 \tilde{b}_1 \rightarrow t\chi_1^- + \bar{t}\chi_1^+$  at  $\sqrt{s} = 1$  TeV.



## 2. Precision SUSY measurements: summary

From analyses at ILC with  $\sqrt{s} = 0.5\text{--}1$  TeV and  $10\text{--}1000$  fb $^{-1}$  luminosity:

|                   | $m$ [GeV]    | $\Delta m$  | Comments  |
|-------------------|--------------|-------------|---|
| $\chi_{1\pm}^\pm$ | <b>183.7</b> | <b>0.55</b> | simulation threshold scan, $100$ fb $^{-1}$   |
| $\chi_{2\pm}^\pm$ | <b>415.4</b> | <b>3</b>    | estimate $\chi_{1\pm}^\pm \chi_{2\mp}^\mp$ , spectra $\chi_{2\pm}^\pm \rightarrow Z \chi_{1\pm}^\pm, W \chi_{1\pm}^0$ |
| $\chi_{1\pm}^0$   | <b>97.7</b>  | <b>0.05</b> | combination of all methods  |
| $\chi_{2\pm}^0$   | <b>183.9</b> | <b>1.2</b>  | simulation threshold scan $\chi_{2\pm}^0 \chi_{2\pm}^0$ , $100$ fb $^{-1}$  |
| $\chi_3^0$        | <b>400.5</b> | <b>3–5</b>  | spectra $\chi_3^0 \rightarrow Z \chi_{1,2}^0, \chi_{2,4}^0 \chi_3^0$ , <b>750 GeV</b> , $\gtrsim 1$ ab $^{-1}$        |
| $\chi_4^0$        | <b>413.9</b> | <b>3–5</b>  | spectra $\chi_4^0 \rightarrow W \chi_{1\pm}^\pm, \chi_{2,3}^0 \chi_4^0$ , <b>750 GeV</b> , $\gtrsim 1$ ab $^{-1}$     |
| $\tilde{e}_R$     | <b>125.3</b> | <b>0.05</b> | $e^- e^-$ threshold scan, $10$ fb $^{-1}$   |
| $\tilde{e}_L$     | <b>189.9</b> | <b>0.18</b> | $e^- e^-$ threshold scan $20$ fb $^{-1}$  |
| $\tilde{\nu}_e$   | <b>172.5</b> | <b>1.2</b>  | simulation energy spectrum, <b>500 GeV</b> , $500$ fb $^{-1}$   |
| $\tilde{\mu}_R$   | <b>125.3</b> | <b>0.2</b>  | simulation energy spectrum, <b>400 GeV</b> , $200$ fb $^{-1}$   |
| $\tilde{\mu}_L$   | <b>189.9</b> | <b>0.5</b>  | estimate threshold scan, $100$ fb $^{-1}$   |
| $\tilde{\tau}_1$  | <b>107.9</b> | <b>0.24</b> | simulation energy spectra, <b>400 GeV</b> , $200$ fb $^{-1}$  |
| $\tilde{\tau}_2$  | <b>194.9</b> | <b>1.1</b>  | estimate threshold scan, $60$ fb $^{-1}$  |
| $\tilde{t}_1$     | <b>366.5</b> | <b>1.9</b>  | estimate b-jet spectrum, $m_{\min}(\tilde{t}_1)$ , <b>1TeV</b> , $1$ ab $^{-1}$                                       |

### 3. Determination of the SUSY parameters:

Once  $m_i, \sigma, P_i$  are measured, determine the low-energy SUSY parameters from inversion of the mass and cross section formulae:

• **Chargino/neutralino system:** see Jan Kalinowski

$$M_1 = \sqrt{\sum_i m_{\chi_i^0}^2 - M_2^2 - \mu^2 - 2M_Z^2}, \quad M_2 = M_W \sqrt{\Sigma - \Delta [c_{2\phi_R} + c_{2\phi_L}]}$$

$$|\mu| = M_W \sqrt{\Sigma + \Delta [c_{2\phi_R} + c_{2\phi_L}]}, \quad \tan \beta = \sqrt{(1 + \Delta') / (1 - \Delta')}$$

$$\text{with } \Delta = \frac{m_{\tilde{\chi}_2^\pm}^2 - m_{\tilde{\chi}_1^\pm}^2}{4M_W^2}, \quad \Delta' = \Delta (c_{2\phi_R} - c_{2\phi_L}), \quad \Sigma = \frac{m_{\tilde{\chi}_2^\pm}^2 + m_{\tilde{\chi}_1^\pm}^2}{2M_W^2} - 1.$$

• **Sfermion system:** see Barbara Mele

$$m_{\tilde{f}_{L,R}}^2 = M_{\tilde{f}_{L,R}}^2 + M_Z^2 \cos 2\beta (I_{L,R}^3 - Q_f \sin^2 \theta_W) + m_f^2$$

$$A_f - \mu (\tan \beta)^{-2I_f^3} = (m_{\tilde{f}_1}^2 - m_{\tilde{f}_2}^2) / (2m_f) \cdot \sin 2\theta_{\tilde{f}}$$

• **Higgs system:** see e.g. Marco Battaglia

$$\text{Precise } M_h \text{ measurement: } M_h^2 = M_Z^2 |\cos 2\beta|^2 + \frac{3g^2}{2\pi^2} \frac{m_t^4}{M_W^2} \log \frac{m_t^2}{m_t^2}$$

**Also:**  $e^+e^- \rightarrow t\bar{t}\Phi, b\bar{b}\Phi, \chi\chi\Phi, \tau\tau \rightarrow \Phi, \Phi \rightarrow \tilde{\tau}_1\tilde{\tau}_2, \Phi \rightarrow \chi\chi, \dots$

### 3. Determination of SUSY parameters: summary

In reality, life is more complicated than the tree-level results above:

complete analysis with sophisticated programs: **Sfittino**, **Sfitter**, ...

|                      | $\Delta$ LHC | $\Delta$ ILC | $\Delta$ LHC+ILC | SPS1a  | $\Delta$ LHC+ILC | SPS1a' |
|----------------------|--------------|--------------|------------------|--------|------------------|--------|
| $\tan \beta$         | $\pm 9.1$    | $\pm 0.3$    | $\pm 0.2$        | 10     | $\pm 0.3$        | 10     |
| $\mu$                | $\pm 7.3$    | $\pm 2.3$    | $\pm 1.0$        | 344.3  | $\pm 1.1$        | 396    |
| $M_A$                | <b>fixed</b> | $\pm 0.9$    | $\pm 0.8$        | 399.1  | $\pm 0.8$        | 372    |
| $A_t$                | $\pm 91$     | $\pm 2.7$    | $\pm 3.3$        | -504.9 | $\pm 24.6$       | -565   |
| $M_1$                | $\pm 5.3$    | $\pm 0.1$    | $\pm 0.1$        | 102.2  | $\pm 0.1$        | 103.3  |
| $M_2$                | $\pm 7.3$    | $\pm 0.7$    | $\pm 0.2$        | 191.8  | $\pm 0.1$        | 193.2  |
| $M_3$                | $\pm 15$     | <b>fixed</b> | $\pm 11$         | 589.4  | $\pm 7.8$        | 571.7  |
| $M_{\tilde{\tau}_L}$ | <b>fixed</b> | $\pm 1.2$    | $\pm 1.1$        | 197.8  | $\pm 1.2$        | 179.3  |
| $M_{\tilde{e}_L}$    | $\pm 5.1$    | $\pm 0.2$    | $\pm 0.2$        | 198.7  | $\pm 0.18$       | 181.0  |
| $M_{\tilde{e}_R}$    | $\pm 5.0$    | $\pm 0.05$   | $\pm 0.05$       | 138.2  | $\pm 0.2$        | 115.7  |
| $M_{\tilde{Q}_{3L}}$ | $\pm 110$    | $\pm 4.4$    | $\pm 39$         | 501.3  | $\pm 4.9$        | 471.4  |
| $M_{\tilde{Q}_{1L}}$ | $\pm 13$     | <b>fixed</b> | $\pm 6.5$        | 553.7  | $\pm 5.2$        | 525.8  |
| $M_{\tilde{d}_R}$    | $\pm 20$     | <b>fixed</b> | $\pm 15$         | 529.3  | $\pm 17.3$       | 505.7  |

### 3. Determination of SUSY parameters

Once the low-energy SUSY parameters have been obtained, try to determine the SUSY parameters at the very high scale ( $M_{GUT}, M_P$ ):

- pin-down the model/SUSY-breaking (mSUGRA, AMSB, GMSB, ..),
- determine the few fundamental unified parameters of the model.

Example of mSUGRA, using all previous measurements at LHC/ILC:

|             | SPS1a       | LHC        | ILC        | LHC+ILC    | SPS1a'      | LHC+ILC    |
|-------------|-------------|------------|------------|------------|-------------|------------|
| $m_0$       | <b>100</b>  | $\pm 4.0$  | $\pm 0.09$ | $\pm 0.08$ | <b>70</b>   | <b>0.2</b> |
| $m_{1/2}$   | <b>250</b>  | $\pm 1.8$  | $\pm 0.13$ | $\pm 0.11$ | <b>250</b>  | <b>0.2</b> |
| $\tan\beta$ | <b>10</b>   | $\pm 1.3$  | $\pm 0.14$ | $\pm 0.14$ | <b>10</b>   | <b>0.3</b> |
| $A_0$       | <b>-100</b> | $\pm 31.8$ | $\pm 4.43$ | $\pm 4.13$ | <b>-300</b> | <b>13</b>  |

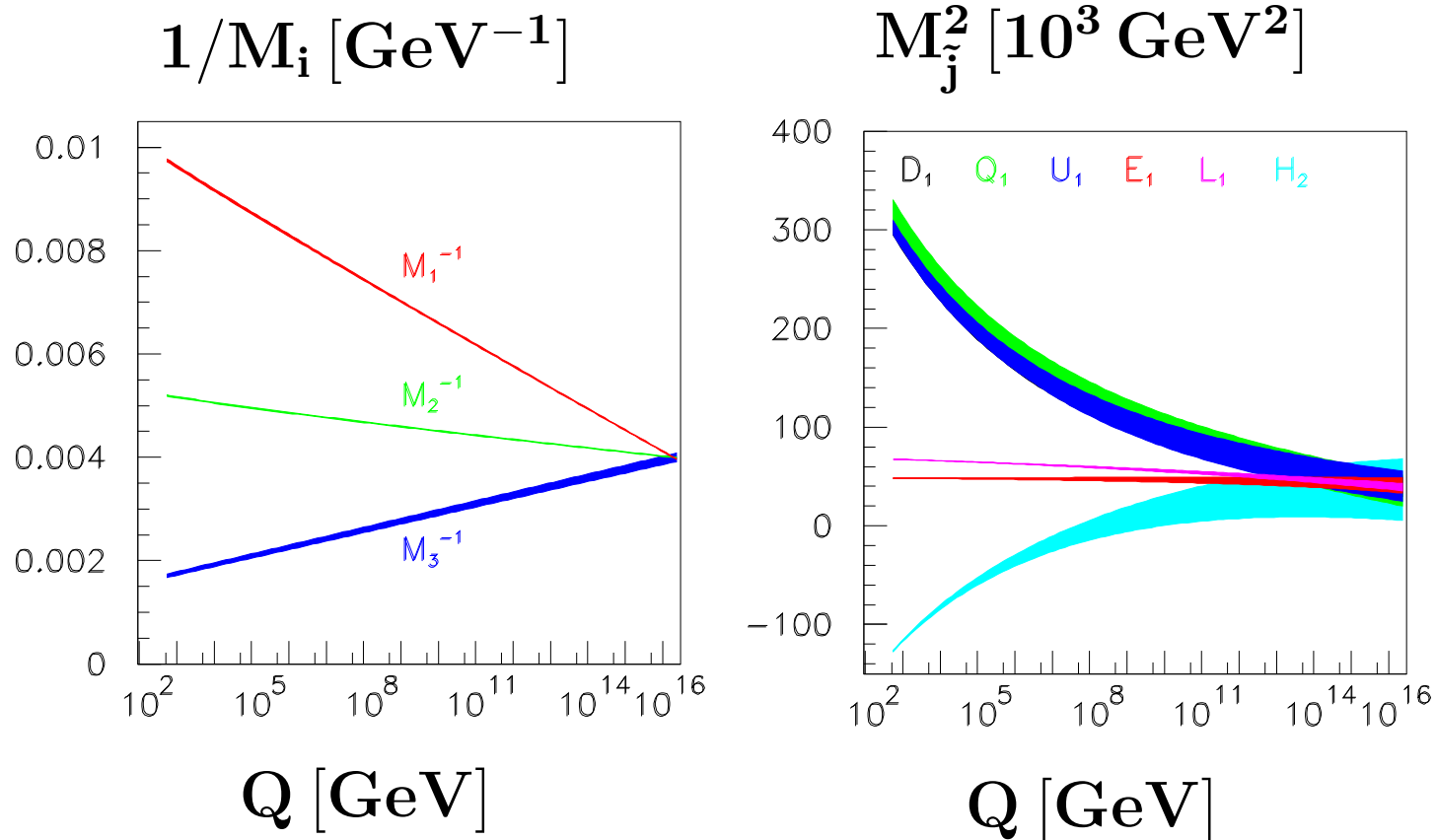
The same type of analysis in other breaking schemes/other models.

To be absolutely sure: only with model dependent analyses at ILC!

### 3. Determination of SUSY parameters:

One can check the fundamental assumptions at high (GUT) scale.

For example: gaugino and scalar mass unification in mSUGRA....



Also, check that one is in accord with cosmology (see G. Bélanger):

use precise determination of SUSY parameters to predict  $\Omega h^2$ .

## 4. Summary

**If SUSY is the solution to the SM pbs: SUSY particles should be light.**

**Colored and non-colored sparticles observable (very?) soon at LHC.**

**The ILC will be needed as it will provide crucial additional information:**

- **very clean environment, large production rates with low backgrounds,**
- **tunable energy to perform threshold scans and increase rates,**
- **beam polarization which allow to select various channels,**
- **additional options ( $e^-e^-$ ,  $\gamma\gamma$ ,  $e\gamma$ ) for complementary studies,**  
⇒ **high-precision analyses and a true probe of SUSY phenomena.**

**Only coherent/combined analyses of LHC+ILC data will allow for:**

- **better/model independent reconstruction of low energy SUSY parameters**
- **connect weak-scale SUSY with more fundamental physics at GUT scale,**
- **provide input to predict the LSP density and connection with cosmology**

**Here: gave illustration of ILC “performance” in mSUGRA-type MSSM.**

**Many interesting analyses/physics can also be done in other scenarios!**