

Elliptic Flow Fluctuations with the PHOBOS detector

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PHOBOS Collaboration



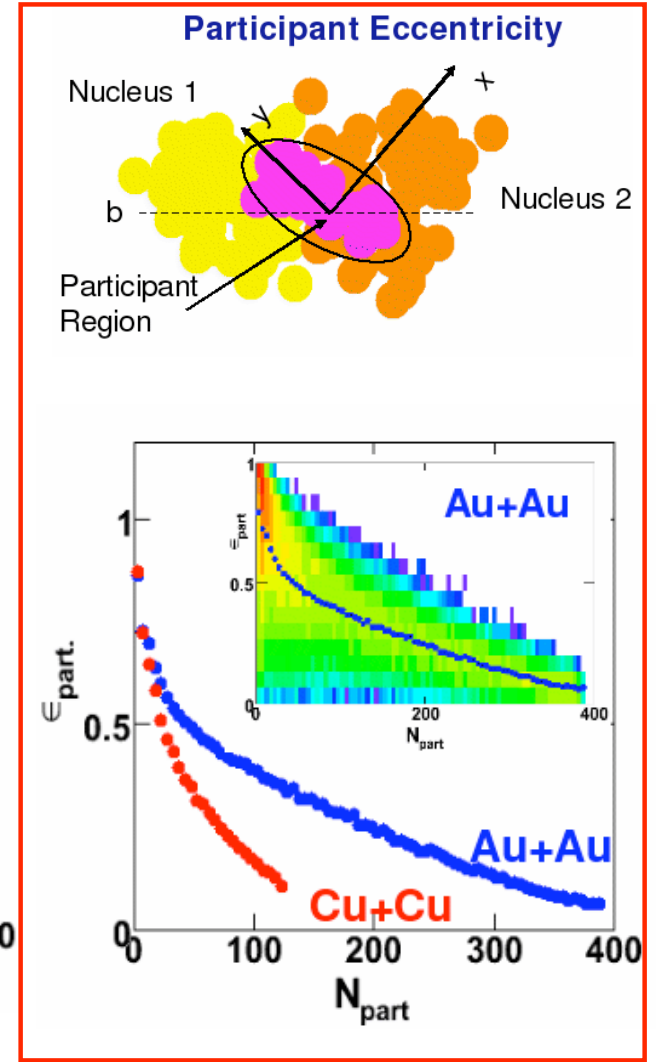
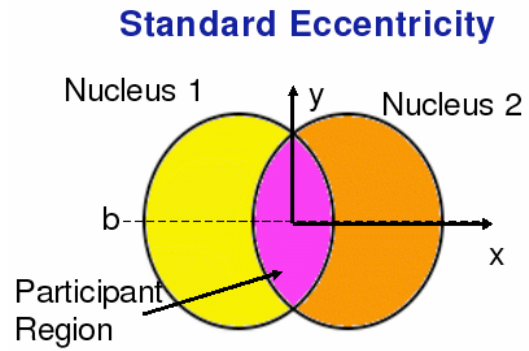
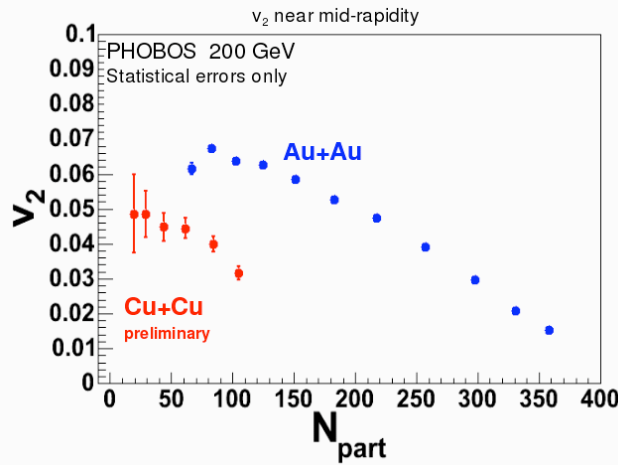
Burak Alver, Birger Back, Mark Baker, Maarten Ballintijn, Donald Barton, Russell Betts, **Richard Bindel**, Wit Busza (Spokesperson), Zhengwei Chai, **Vasundhara Chetluru**, Edmundo García, **Tomasz Gburek**, Kristjan Gulbrandsen, Clive Halliwell, **Joshua Hamblen**, **Ian Harnarine**, Conor Henderson, David Hofman, Richard Hollis, Roman Holynski, Burt Holzman, Aneta Iordanova, Jay Kane, Piotr Kulinich, Chia Ming Kuo, **Wei Li**, Willis Lin, Constantin Loizides, Steven Manly, Alice Mignerey, Gerrit van Nieuwenhuizen, Rachid Nouicer, Andrzej Olszewski, Robert Pak, **Corey Reed**, **Eric Richardson**, Christof Roland, Gunther Roland, **Joe Sagerer**, Iouri Sedykh, Chadd Smith, **Maciej Stankiewicz**, Peter Steinberg, George Stephans, Andrei Sukhanov, **Artur Szostak**, Marguerite Belt Tonjes, Adam Trzupek, **Sergei Vaurynovich**, Robin Verdier, Gábor Veres, **Peter Walters**, **Edward Wenger**, **Donald Wilhelm**, Frank Wolfs, Barbara Wosiek, Krzysztof Wozniak, **Shaun Wyngaardt**, Bolek Wyslouch

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Motivation

High v_2 observed in CuCu can be explained by fluctuations in initial collision region.



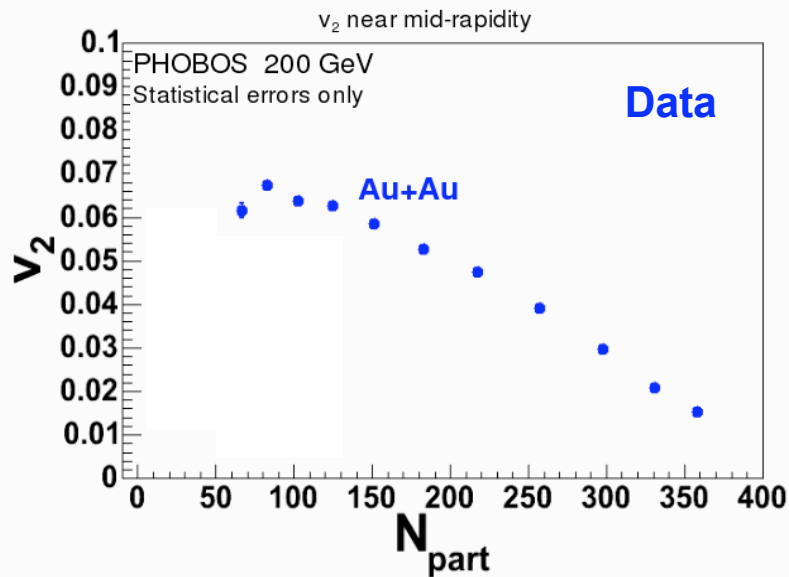
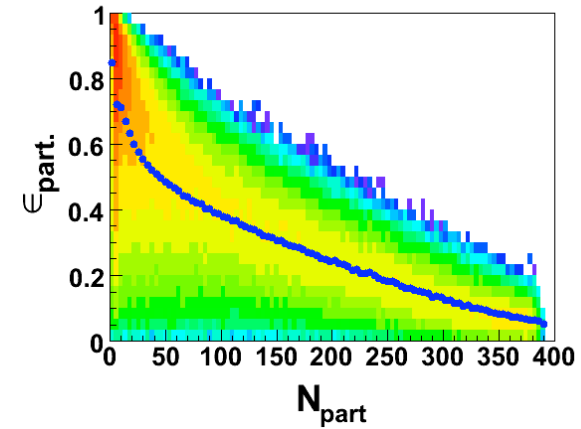
Can we test the Participant Eccentricity Model?

Expected fluctuations

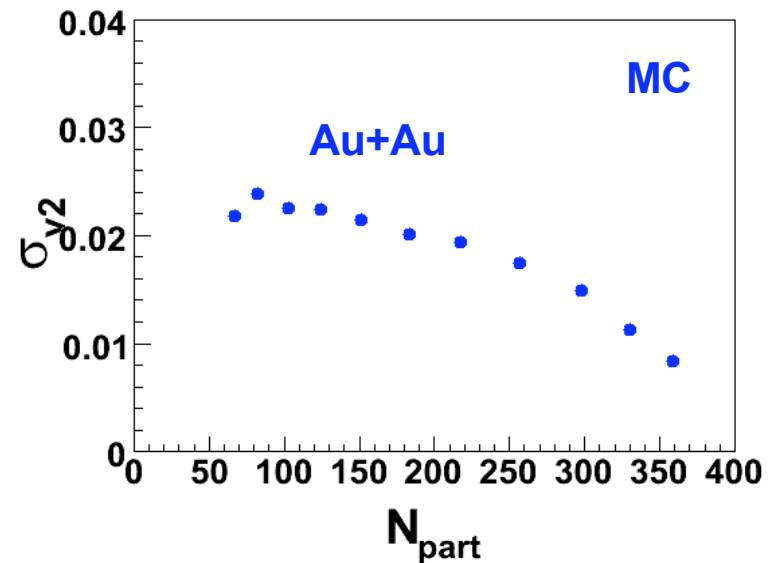
Assuming $v_2 \propto \epsilon_{\text{part}}$, participant eccentricity model predicts

v_2 fluctuations

$$\frac{\sigma_{v_2}}{v_2} = \frac{\sigma_{\epsilon}}{\epsilon}$$



Expected σ_{v_2} from fluctuations in ϵ_{part}



Measuring v_2 Fluctuations

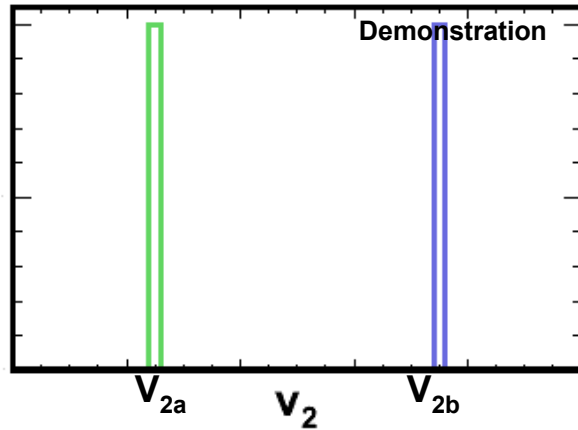
- We have considered 3 different methods
 - 2 particle correlations $\rightarrow \langle v_2^2 \rangle$
 - c.f. S. Voloshin nucl-th/0606022
 - $\sigma_{v_2}^2 = \langle v_2^2 \rangle - \langle v_2 \rangle^2$
 - Do systematic errors cancel?
 - 2 particle correlations $\rightarrow v_2^2$ event by event
 - Mixed event background generation is possible
 - Reduces fit parameters to 1 (no reaction plane)
 - Hard to untangle acceptance effects event by event
 - v_2 event by event
 - This is the method we are pursuing

Measuring v_2 Fluctuations - Today's Talk

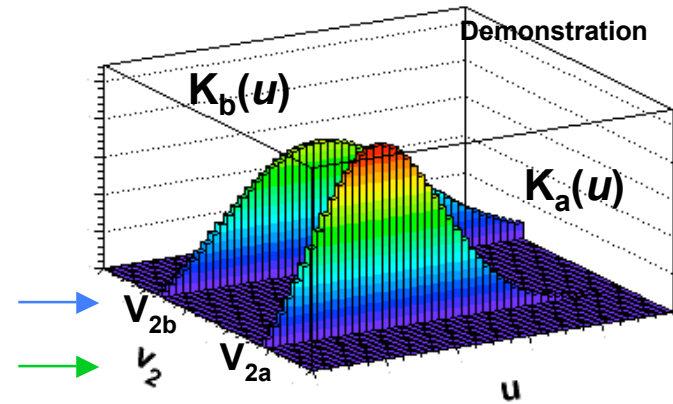
- Measuring v_2 event by event
- Ongoing analysis on 200GeV Au-Au
- Today
 - How we are planning to make the measurement
 - Studies on fully simulated MC events
 - Modified Hijing - Flow
 - Geant

Method Overview - Simplified Example

2 possible v_2 values



Event by Event measurement

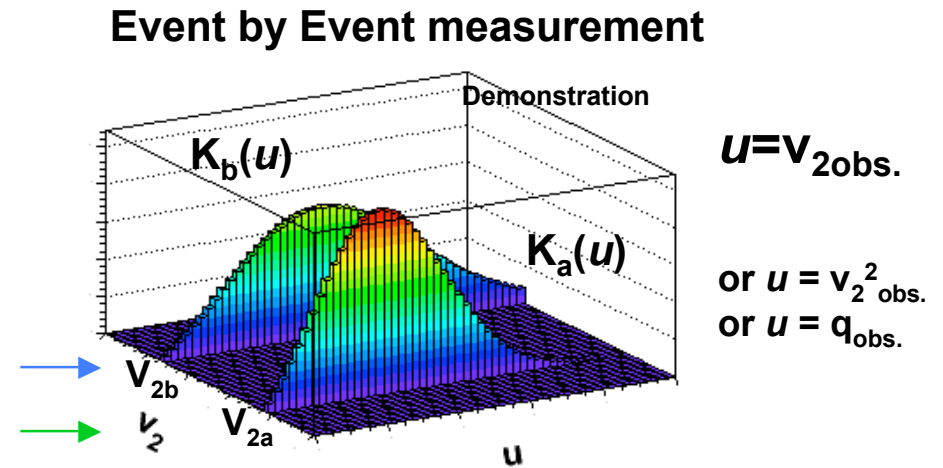
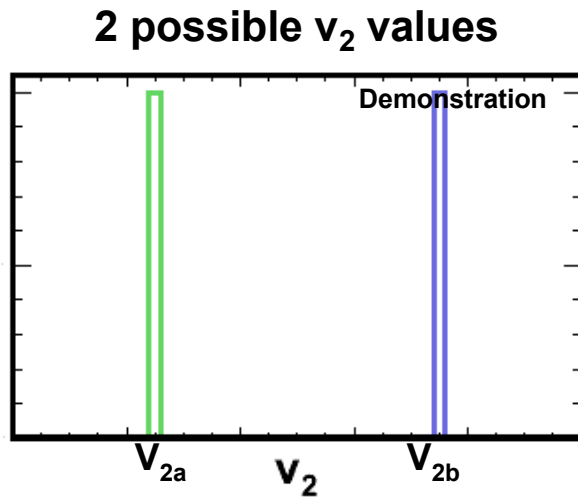


$$u = v_{2\text{obs.}}$$

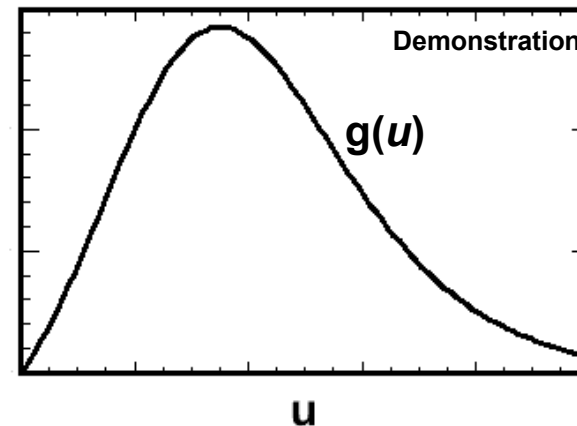
$$\text{or } u = v_{2\text{obs.}}^2$$

$$\text{or } u = q_{\text{obs.}}$$

Method Overview - Simplified Example



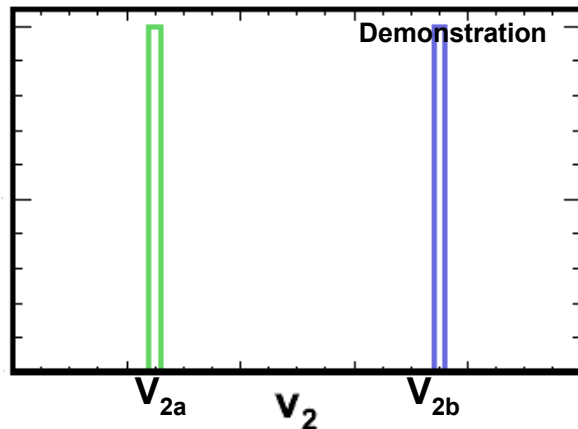
Measured u distribution in a sample



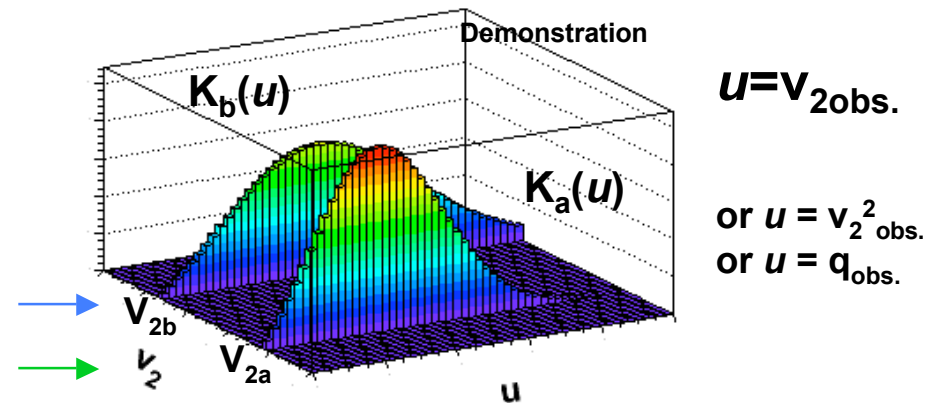
Question: What is the relative abundance of v_{2a} to v_{2b} in the sample?

Method Overview - Simplified Example

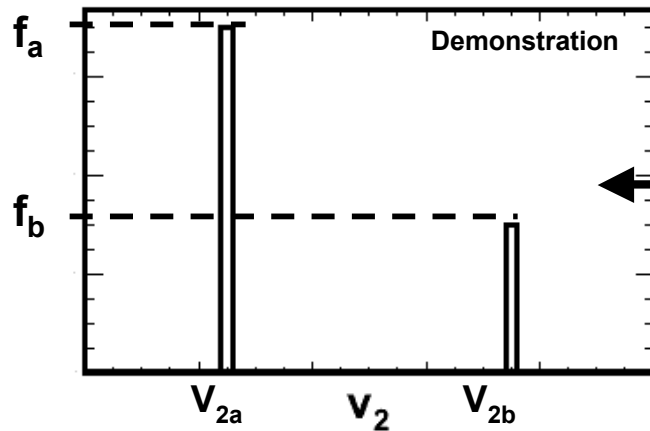
2 possible v_2 values



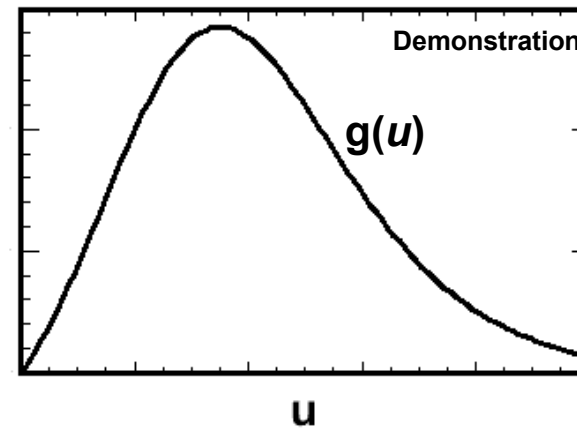
Event by Event measurement



Extracted $v_{2\text{true}}$ distribution from sample



Measured u distribution in a sample



Question: What is the relative abundance of v_{2a} to v_{2b} in the sample?

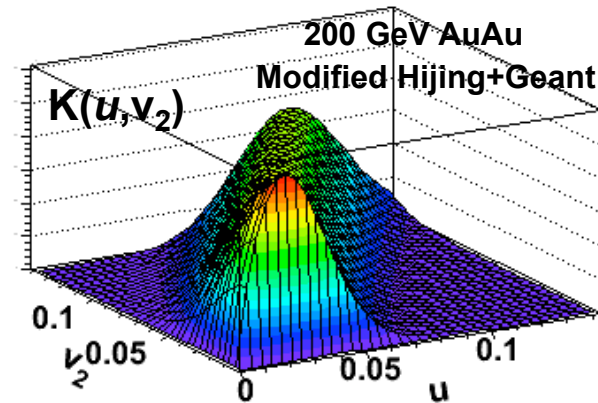
$$g(u) = f_a K_a(u) + f_b K_b(u)$$

Method Overview

In real life v_2 can take a continuum of values

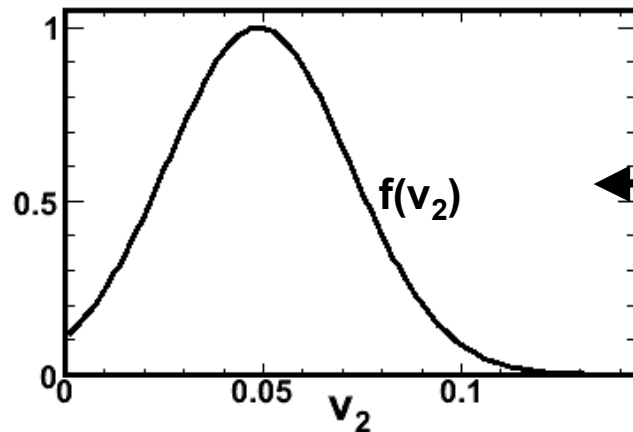
$$g(u) = \int_0^\infty K(u, v_2) f(v_2) dv_2$$

Kernel

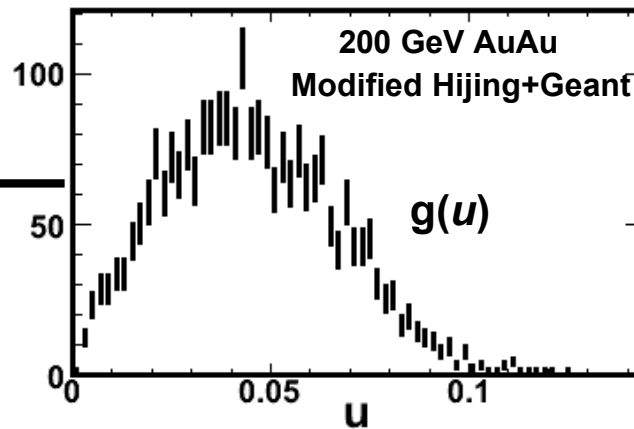


$$u = v_{2\text{obs.}}$$

Extracted $v_{2\text{true}}$ distribution from sample



Measured u distribution in a sample



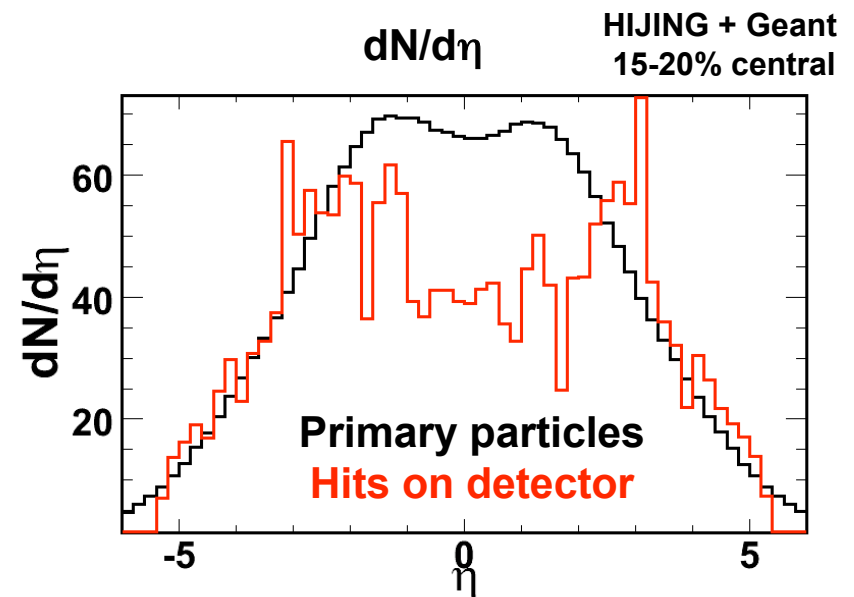
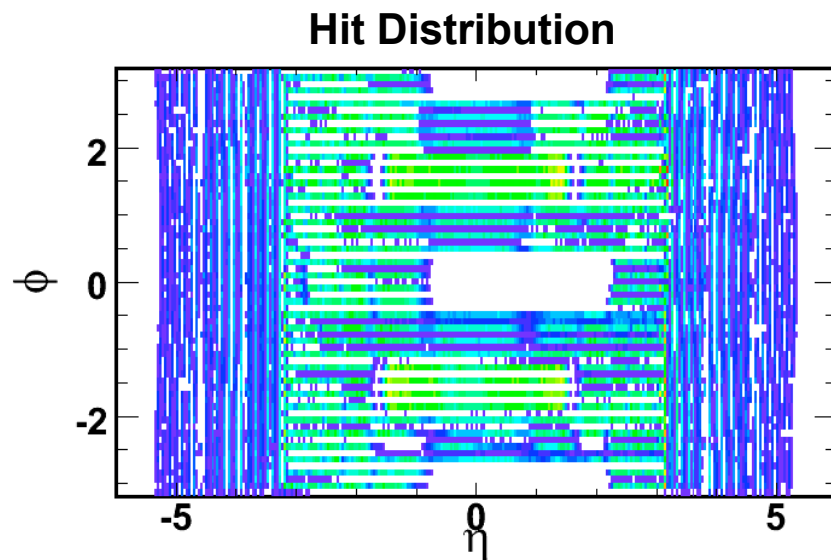
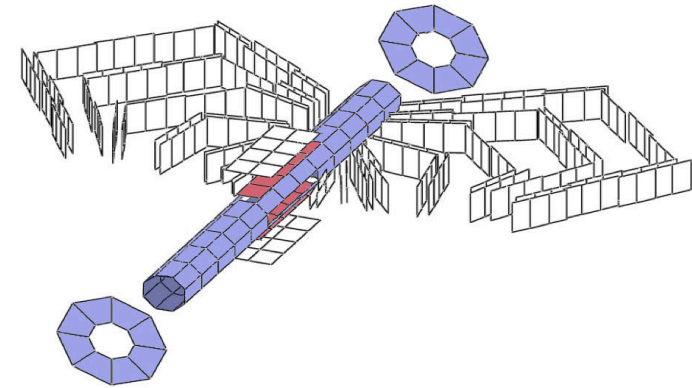
Method Overview

- **3 Tasks**
 - **Measure u event-by-event $g(u)$**
 - **Calculate the kernel $K(u, v_2)$**
 - **Extract dynamical fluctuations $f(v_2)$**

$$g(u) = \int_0^{\infty} K(u, v_2) f(v_2) dv_2$$

PHOBOS Detector

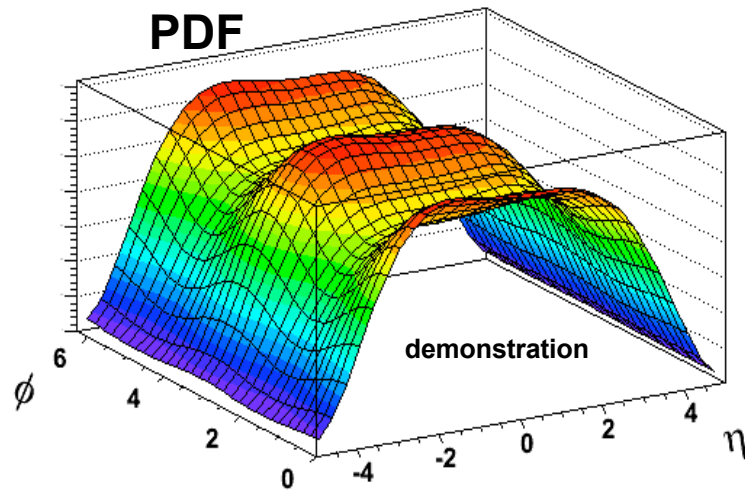
- PHOBOS Multiplicity Array
 - 5.4 < η < 5.4 coverage
 - Holes / granularity differences
- Idea: Use all available information in event to read off single u value



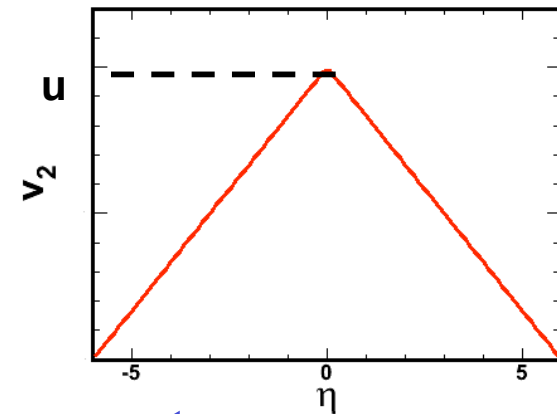
Measuring $u=v_{2\text{obs}}$ Event by Event I

- Probability Distribution Function (PDF) for hit positions:

$$P(\eta, \phi|u, \phi_0) = \underbrace{p(\eta)}_{\substack{\uparrow \\ \text{Probability of hit in } \eta}} \underbrace{[1 + 2v_2(\eta)\cos(2(\phi - \phi_0))]}_{\substack{\uparrow \\ \text{Probability of hit in } \phi}}$$



$$v_2(\eta) = u(1 - |\eta|/6)$$



- Define likelihood of u and ϕ_0 for an event:

$$L(u, \phi_0) = \prod_{i=1}^n P(\eta_i, \phi_i|u, \phi_0)$$

Measuring $u=v_{2\text{obs}}$ Event by Event II

$$L(u, \phi_0) = \prod_{i=1}^n p(\eta_i) [1 + 2u (1 - |\eta_i|/6) \cos(2(\phi_i - \phi_0))]$$

- Maximize likelihood to find “most likely” value of u
- Comparing values of u and ϕ_0
 - In an event, $p(\eta_i)$ is same for all u and ϕ_0 .
 - PDF folded by acceptance must be normalized to the same value for different u and ϕ_0 's

$$s(u, \phi_0 | \eta) = \int A(\eta, \phi) [1 + 2u (1 - |\eta|/6) \cos(2(\phi - \phi_0))] d\phi d\eta$$

Acceptance

Measuring $u=v_{2\text{obs}}$ Event by Event II

$$L(u, \phi_0) = \prod_{i=1}^n p(\eta_i) [1 + 2u (1 - |\eta_i|/6) \cos(2(\phi_i - \phi_0))]$$

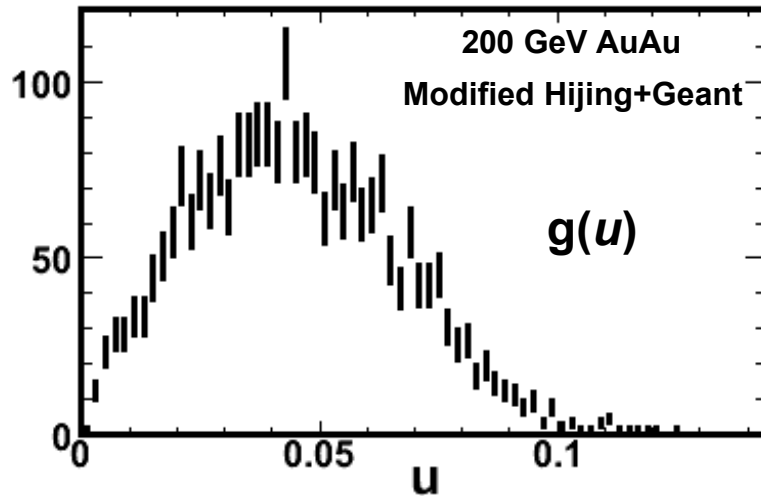
- Maximize likelihood to find “most likely” value of u
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 - In an event, $p(\eta_i)$ is same for all u and ϕ_0 .
 - PDF folded by acceptance must be normalized to the same value for different u and ϕ_0 's

$$s(u, \phi_0 | \eta) = \int \underbrace{A(\eta, \phi)}_{\text{Acceptance}} [1 + 2u (1 - |\eta|/6) \cos(2(\phi - \phi_0))] d\phi d\eta$$

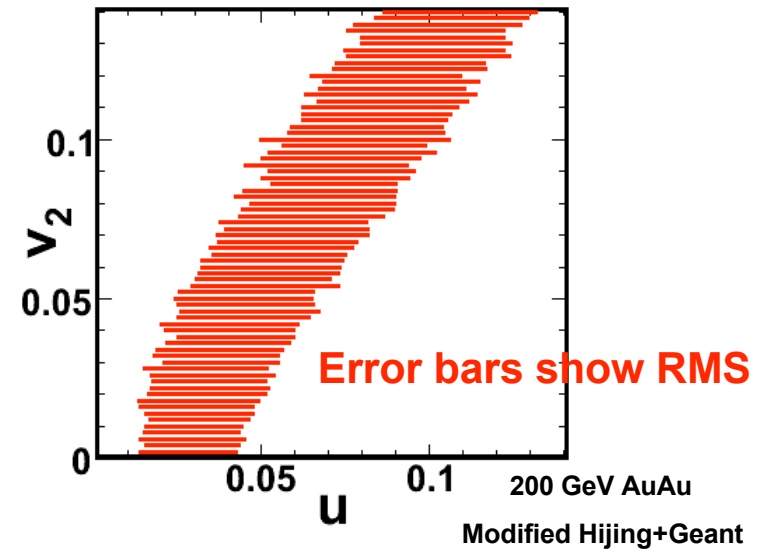
$$L(u, \phi_0) = \prod_{i=1}^n \frac{1}{s(u, \phi_0 | \eta_i)} [1 + 2u (1 - |\eta_i|/6) \cos(2(\phi_i - \phi_0))]$$

Measuring $u=v_{2\text{obs}}$ Event by Event III

Observed u distribution in a sample



Mean and RMS of u in slices of v_2

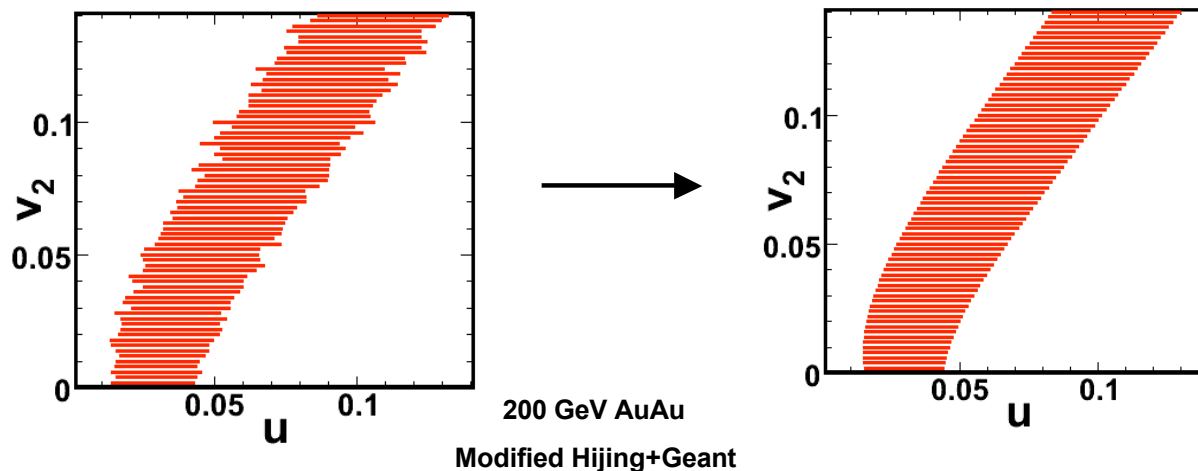


Next Step: Construct the Kernel to unfold $g(u)$

$$g(u) = \int_0^{\infty} K(u, v_2) f(v_2) dv_2$$

Calculating the Kernel I

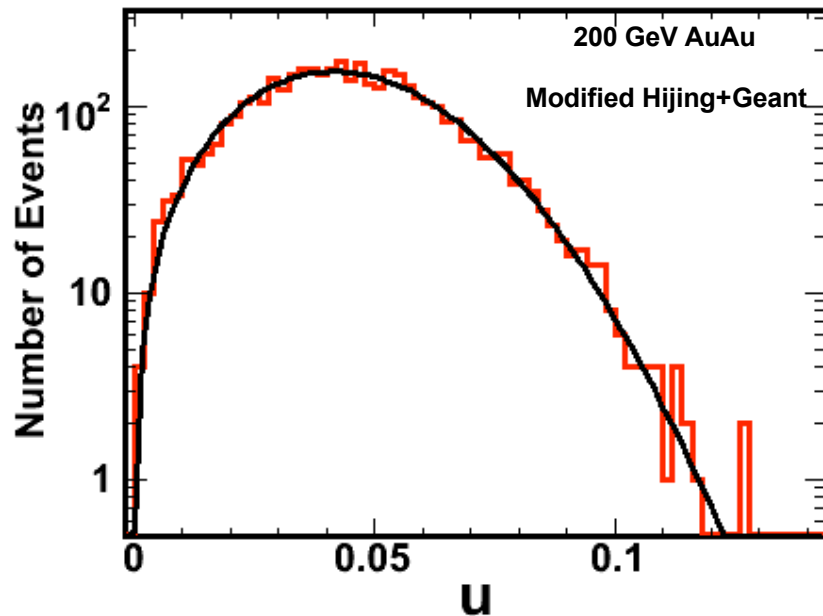
- Simple: Measure u distribution in bins of v_2
- 2 small complications
 - Kernel depends on multiplicity: $K(u, v_2, n)$
 - n = number of hits on the detector
 - Measure u distribution in bins of v_2 and n .
 - Statistics in bins can be combined by fitting smooth functions



Calculating the Kernel II

- In a single bin of v_2 and n

u distribution with for fixed v_2 and n



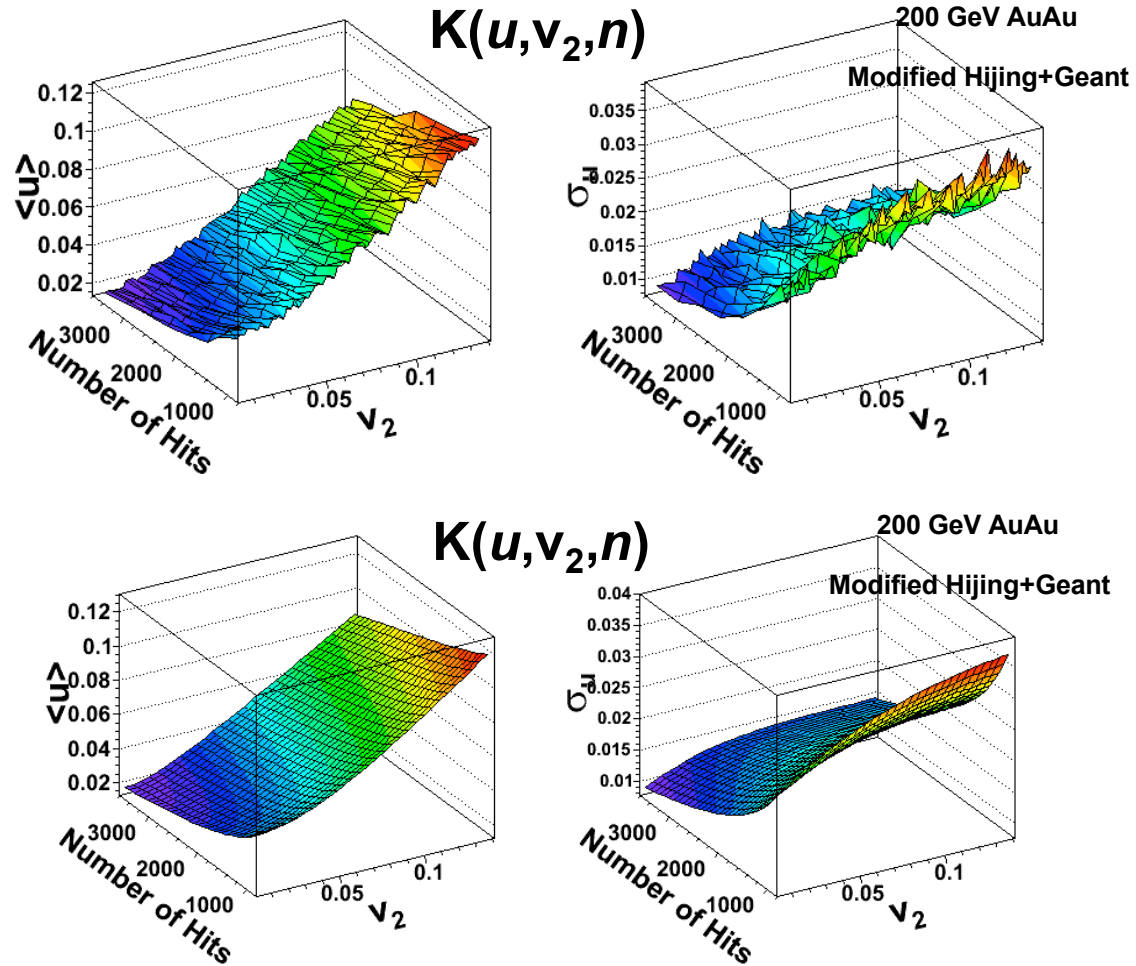
$$K(u)|_{v_2, n} = u \cdot \exp\left(-\frac{u - a^2}{2b^2}\right)$$

$$(a, b) \leftrightarrow (\langle u \rangle, \sigma_u)$$

- Distribution is not Gaussian
- But can be parameterized by $\langle u \rangle$ and σ_u

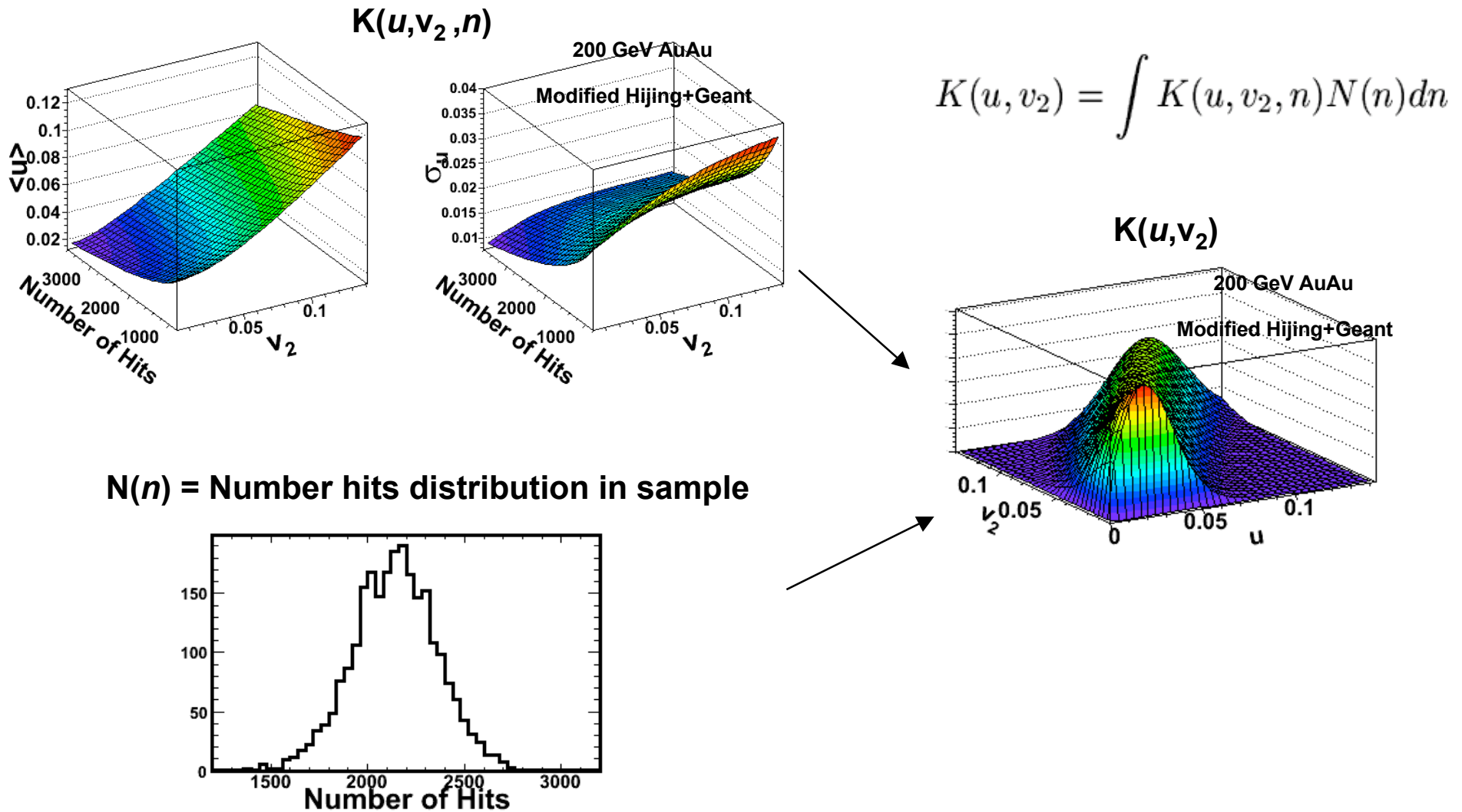
Calculating the Kernel III

- Measure $\langle u \rangle$ and σ_u in bins of v_2 and n
- Fit smooth functions



Calculating the Kernel IV

- Multiplicity dependence can be integrated out



Extracting dynamical fluctuations

$$\underline{g(u)} = \int_0^\infty \underline{K(u, v_2)} \underline{f(v_2)} dv_2$$

known

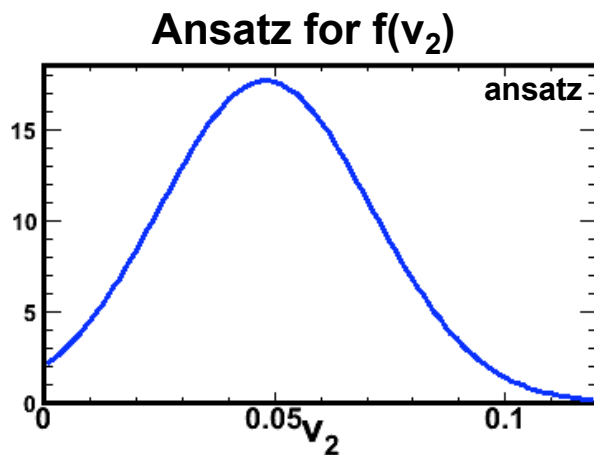
?

Extracting dynamical fluctuations

$$\underline{g(u)} = \int_0^{\infty} \underline{K(u, v_2)} \underline{f(v_2)} dv_2$$

↙↗↑
known ?

Ansatz with two parameters: $f(v_2) = \exp\left(-\frac{(v_2 - \langle v_2 \rangle)^2}{2\sigma_{v_2}^2}\right)$

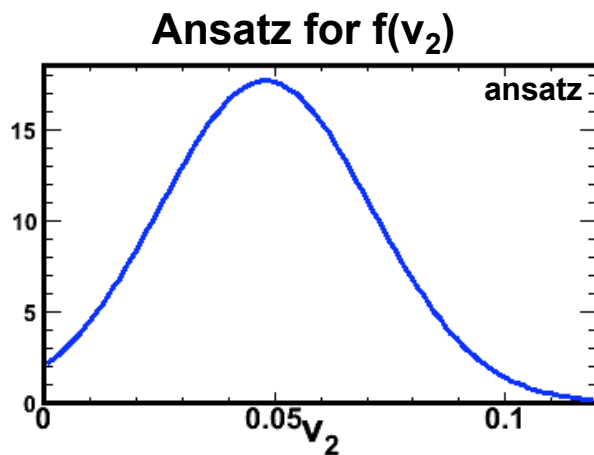


Extracting dynamical fluctuations

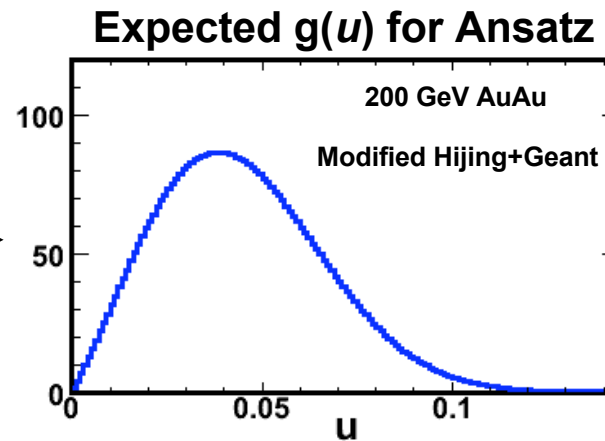
$$\underline{g(u)} = \int_0^\infty \underline{K(u, v_2)} \underline{f(v_2)} dv_2$$

← known ← ?

Ansatz with two parameters: $f(v_2) = \exp\left(-\frac{(v_2 - \langle v_2 \rangle)^2}{2\sigma_{v_2}^2}\right)$



integrate →

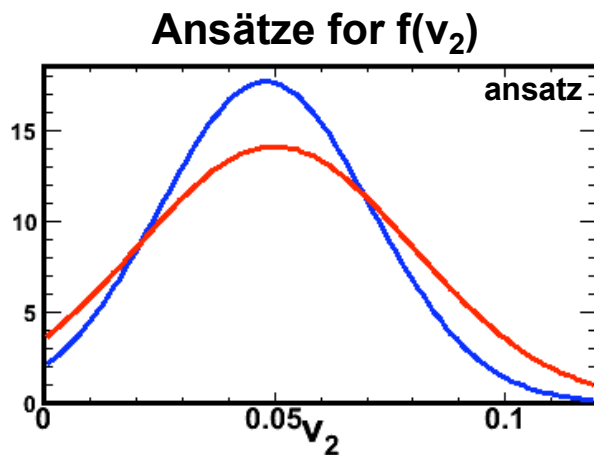


Extracting dynamical fluctuations

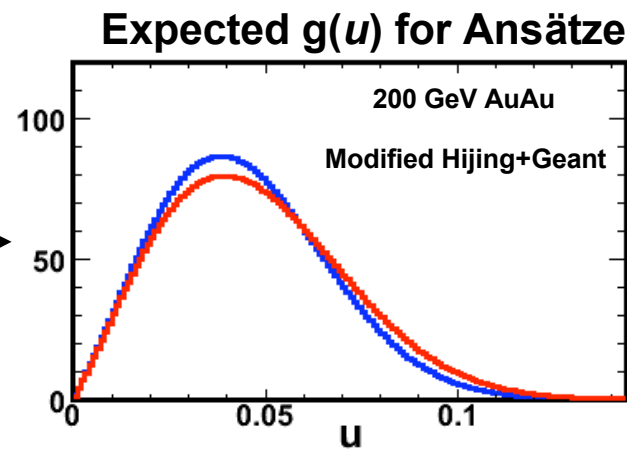
$$\underline{g(u)} = \int_0^\infty \underline{K(u, v_2)} \underline{f(v_2)} dv_2$$

known ?

Ansatz with two parameters: $f(v_2) = \exp\left(-\frac{(v_2 - \langle v_2 \rangle)^2}{2\sigma_{v_2}^2}\right)$



integrate →

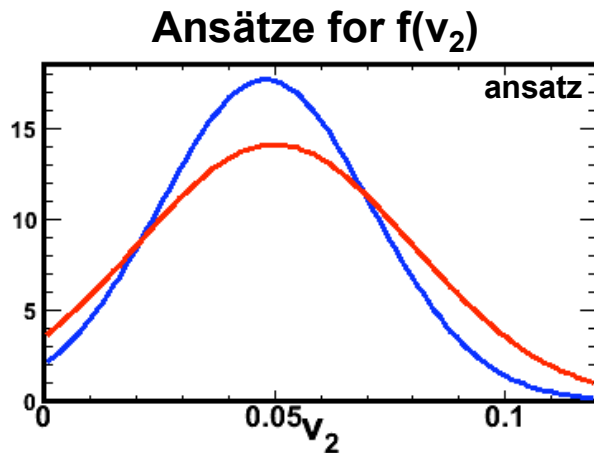


Extracting dynamical fluctuations

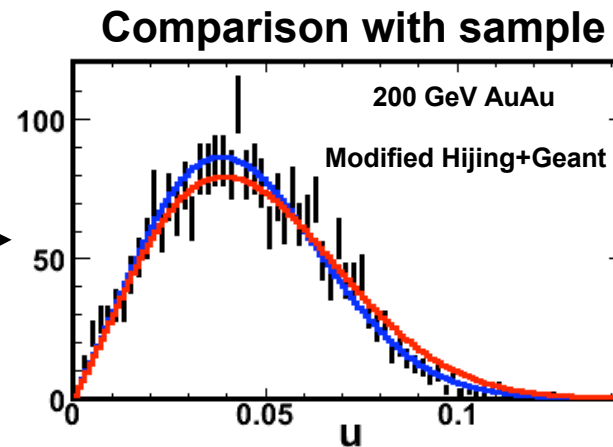
$$\underline{g(u)} = \int_0^\infty \underline{K(u, v_2)} \underline{f(v_2)} dv_2$$

← known ← ?

Ansatz with two parameters: $f(v_2) = \exp\left(-\frac{(v_2 - \langle v_2 \rangle)^2}{2\sigma_{v_2}^2}\right)$



integrate →

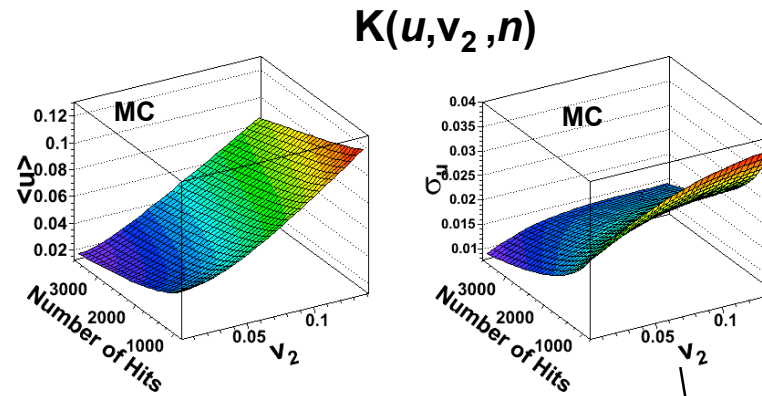


Compare expected $g(u)$ for Ansatz with measurement

Minimum $\chi^2 \rightarrow \langle v_2 \rangle$ and σ_{v_2}

Method Summary

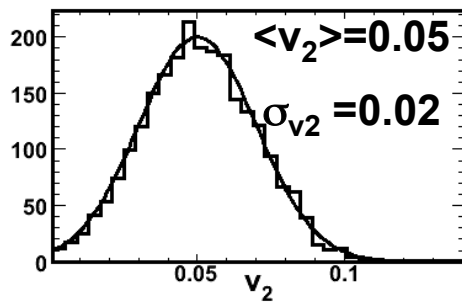
Many MC events \rightarrow



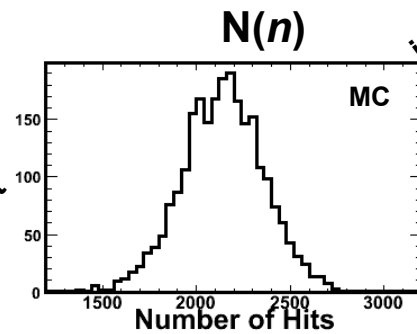
$$K(u, v_2) = \int K(u, v_2, n) N(n) dn$$

A Small Sample

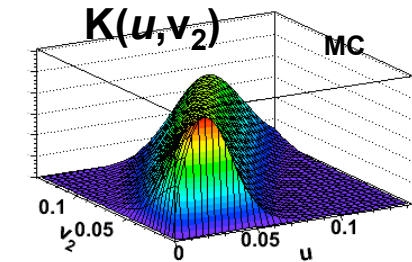
$f_{in}(v_2)$



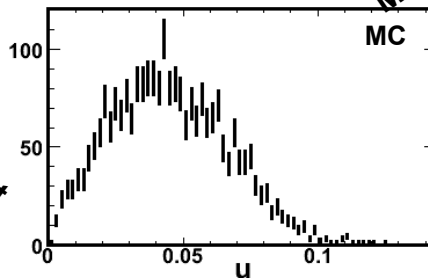
measurement \nearrow



integration \swarrow

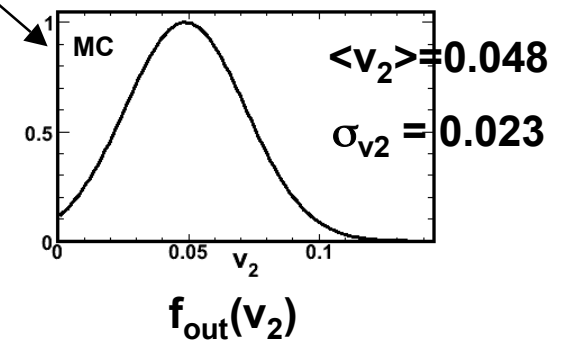


measurement \searrow



Minimize χ^2 in integral \searrow

$$g(u) = \int_0^\infty K(u, v_2) f(v_2) dv_2$$

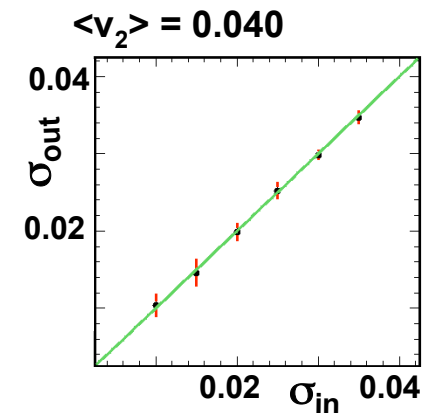
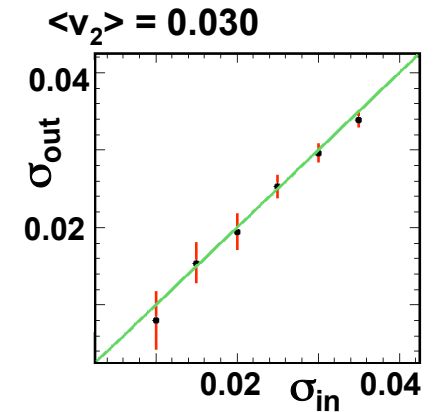
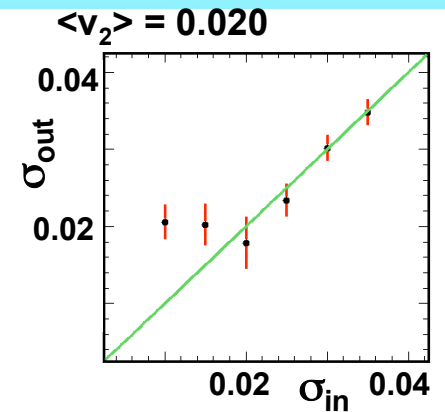
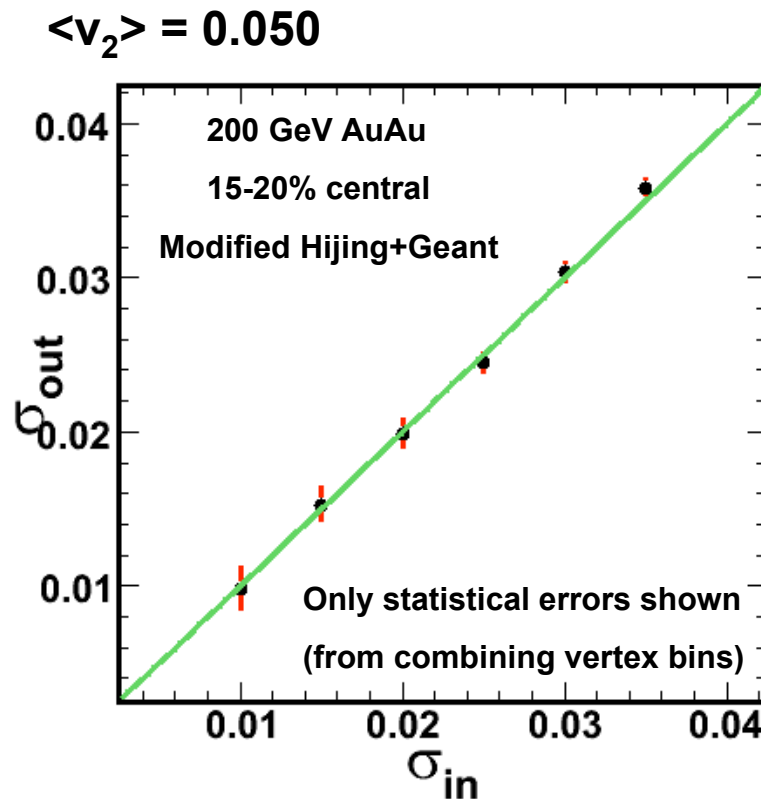


Verification

- **Ran this analysis on Modified Hijing**
 - $v_2(\eta) = v_2(0) \cdot (1-|\eta|/6)$
 - Same as the assumption in our fit
 - $v_2(0)$ given by a **Gaussian distribution in each sample**
 - Same as our Ansatz
 - **Analysis done in 10 collision vertex bins**
 - Final results are averaged
 - **0-40% central events used to construct Kernel**
 - **15-20% central events used as sample**

Verification

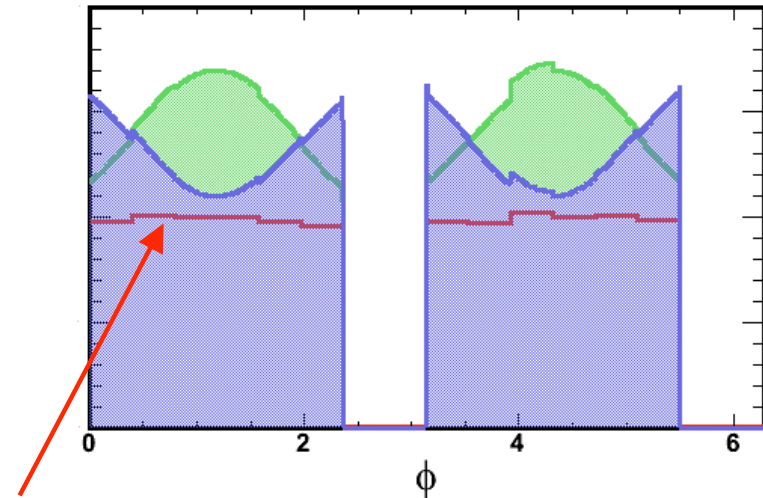
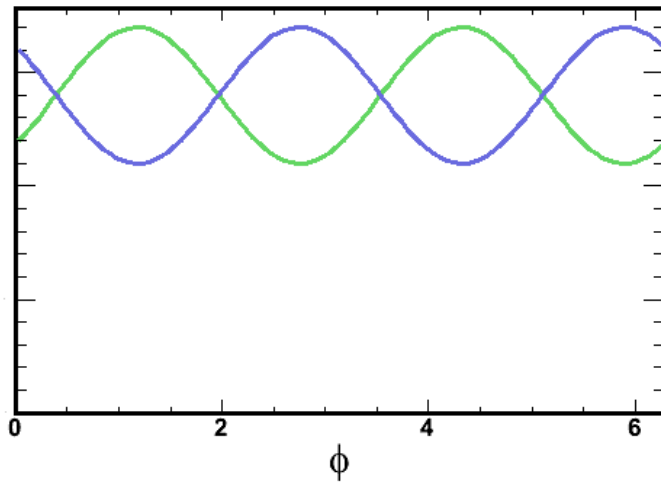
- Ran this analysis on Modified Hijing
 - The input fluctuations are reconstructed successfully



Conclusion / Outlook

- A new method to measure elliptic flow fluctuations is developed.
- Fluctuations in MC simulations are successfully reconstructed.
- Ready to apply the method to extract dynamical fluctuations in DATA.
 - Important part will be to estimate systematic uncertainties due to the MC/DATA differences
 - $dN/d\eta(\eta)$
 - $v_2(\eta)$
 - Non-flow in data
 - Should show up in reaction plane resolutions

Likelihood Fit Normalization

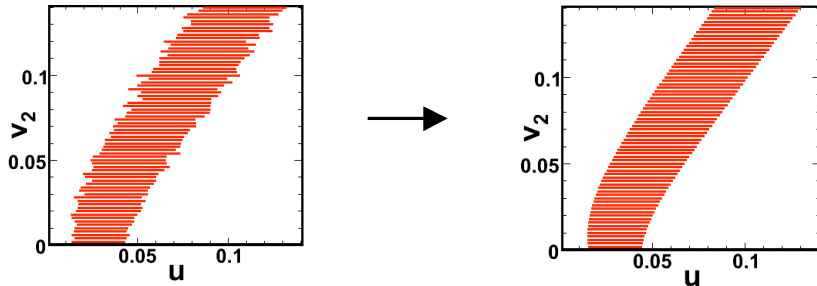


Acceptance

$$s(u, \phi_0 | \eta) = \int A(\eta, \phi) [1 + 2u(1 - |\eta|/6) \cos(2(\phi - \phi_0))] d\phi d\eta$$

$$L(u, \phi_0) = \prod_{i=1}^n \frac{1}{s(u, \phi_0 | \eta_i)} [1 + 2u(1 - |\eta_i|/6) \cos(2(\phi_i - \phi_0))]$$

Calculating the Kernel. Functions observed to fit the Kernel



$$\langle u \rangle (v_2) | n = \sqrt{m_1 \cdot v_2^2 + m_2}$$

$$\sigma_u(v_2) | n = \frac{1}{r_1 + \frac{2}{3} e^{r_2 v_2}}$$

$$\langle u \rangle (v_2, n) = \sqrt{(M_1 n^2 + M_2 n + M_3) \cdot v_2^2 + (M_4 * n + M_5)}$$

$$\sigma_u(v_2, n) = \frac{R_1}{(R_2 \sqrt{n} + 1) \cdot (1 + \frac{2}{3} e^{(R_3 n + R_4) v_2})}$$

