



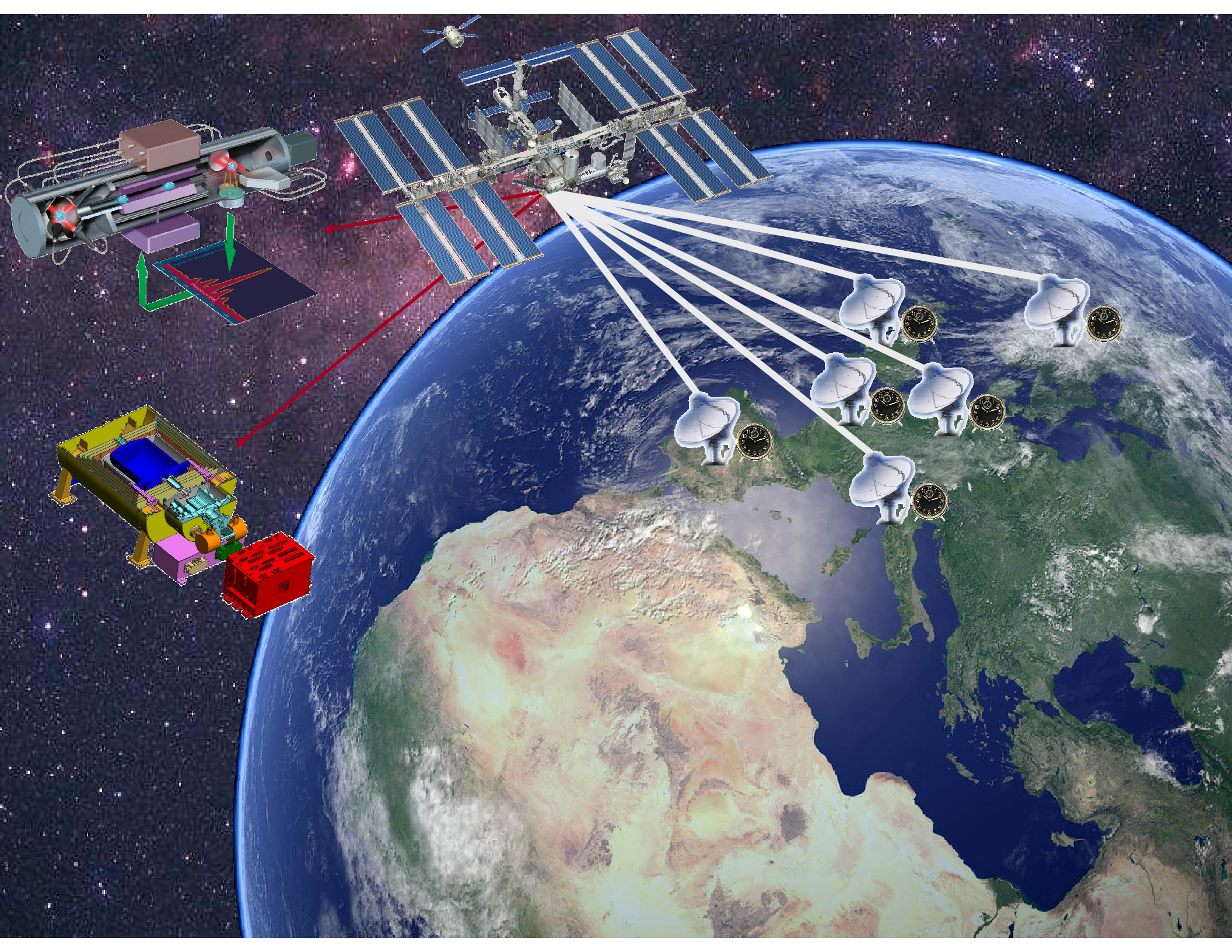
Atomic Clock Ensemble in Space

L. Cacciapuoti

ESA-ESTEC

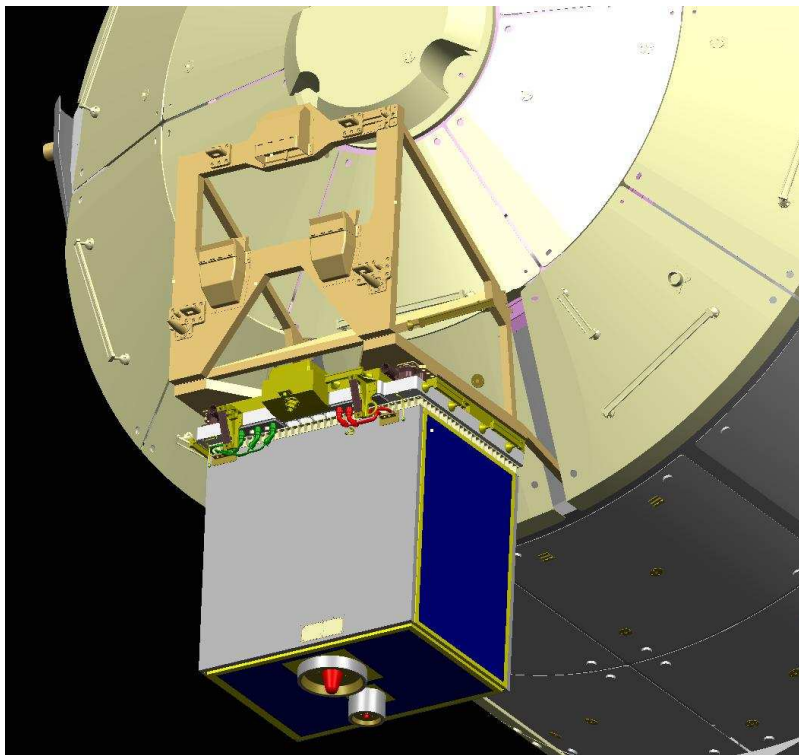
SCI-SA

*International Workshop on
Advances in Precision Tests and Experimental Gravitation in Space
Firenze, 28-30 September 2006*

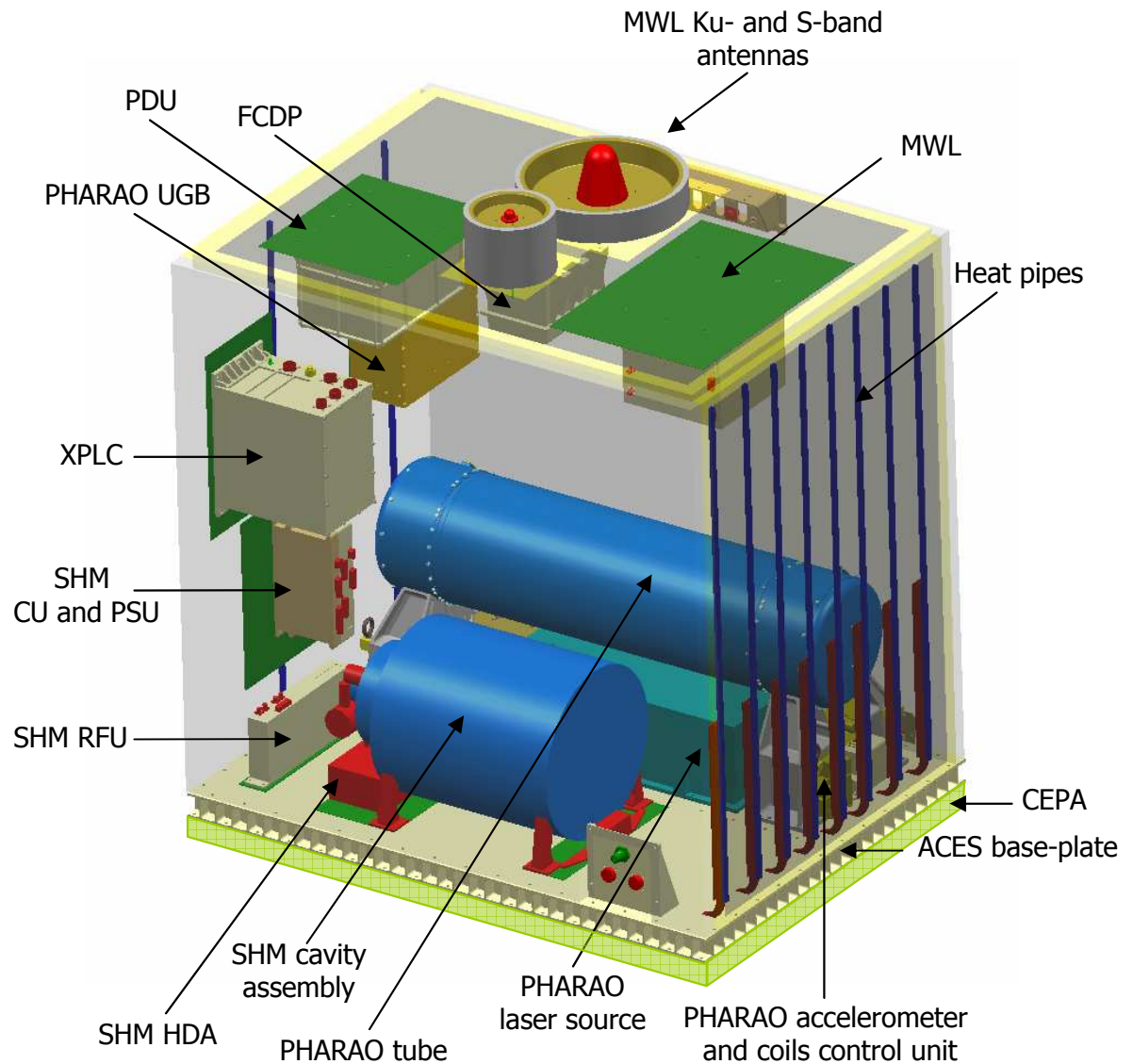


The ACES Payload

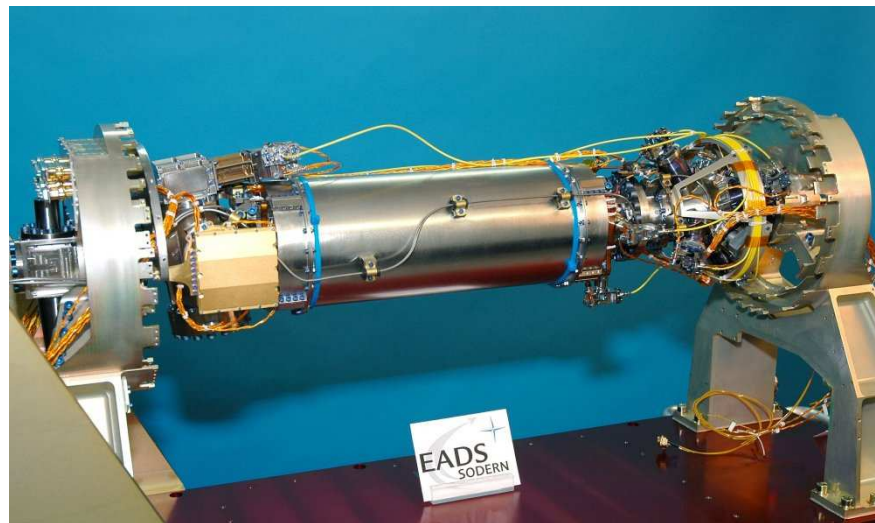
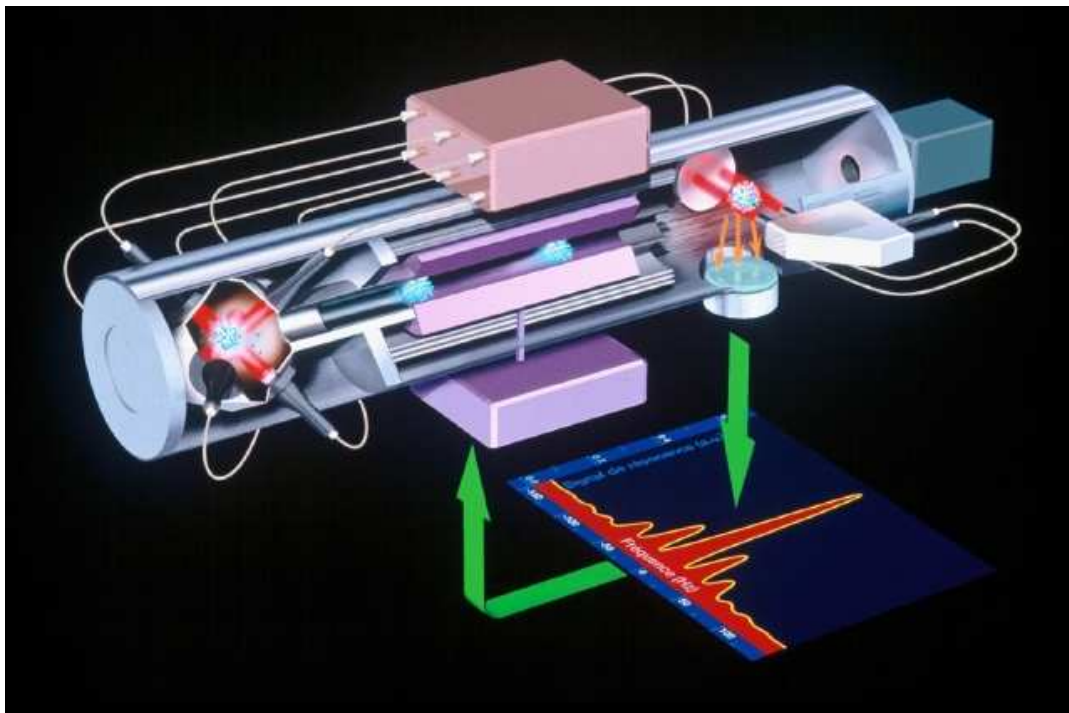
ASTRIUM



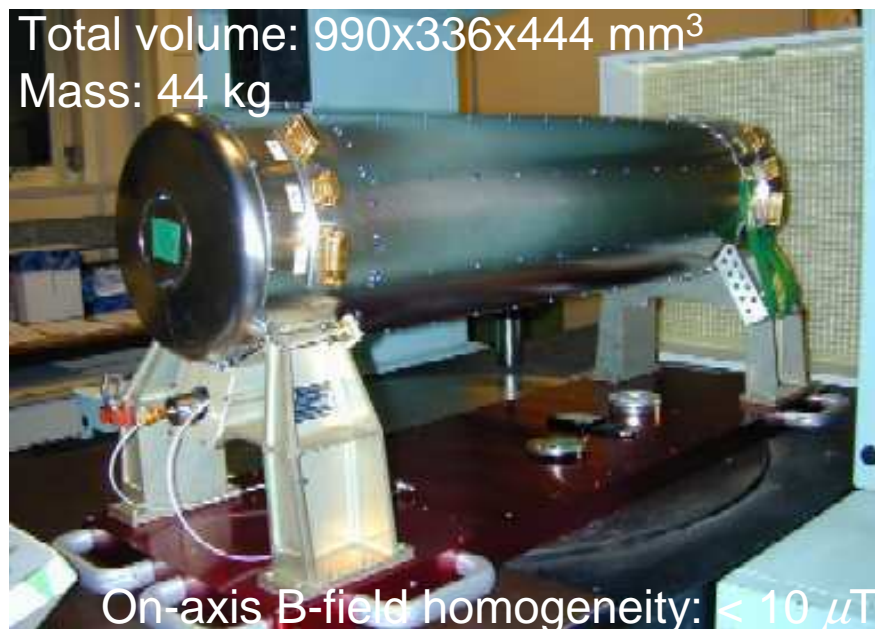
Volume: 1172x867x1246 mm³
 Total mass: 227 kg
 Power: 450 W



PHARAO: A Cold-Atom Clock in μ -gravity



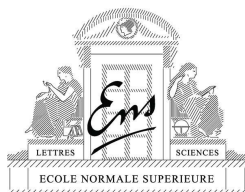
Total volume: 990x336x444 mm³
 Mass: 44 kg



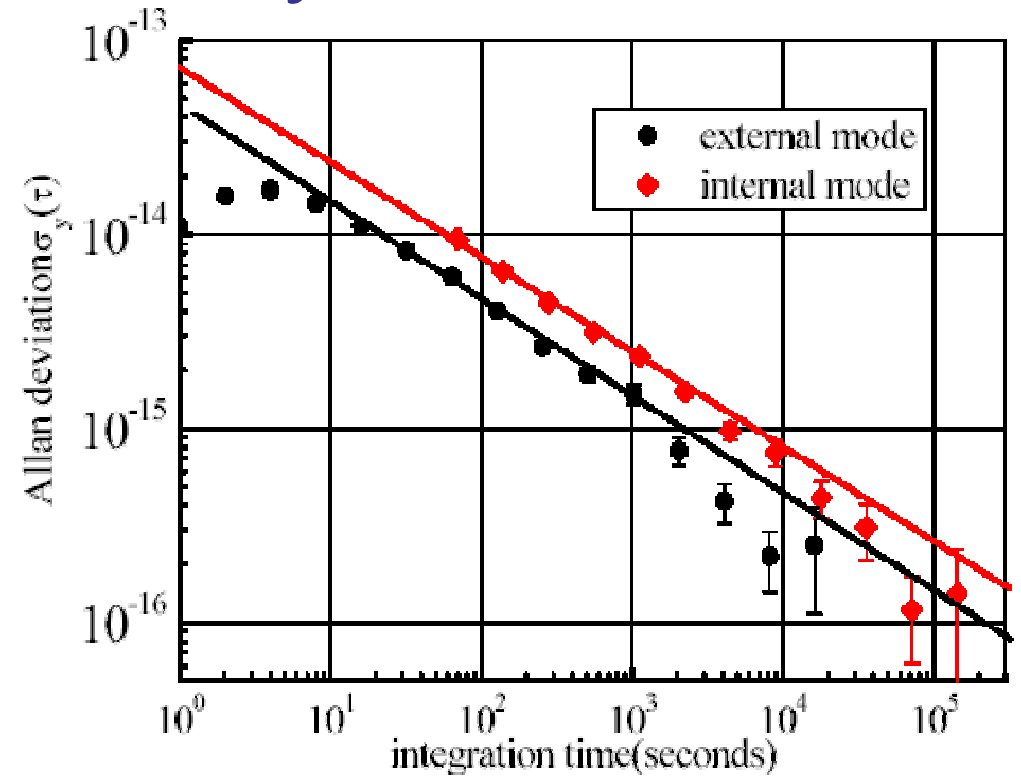
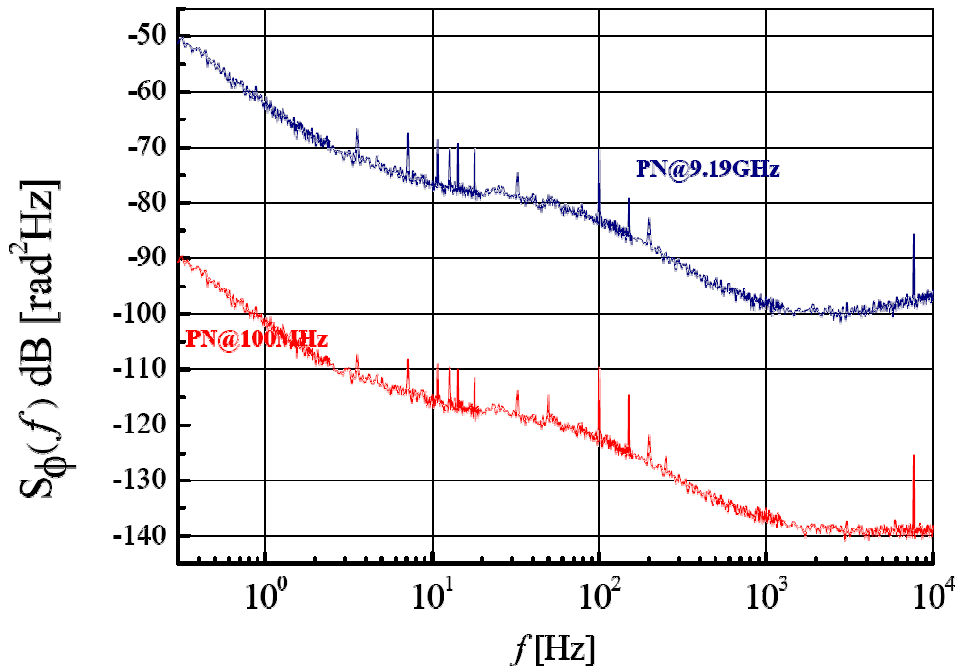
On-axis B-field homogeneity: $< 10 \mu\text{T}$

l'Observatoire de Paris — BNM-SYRTE

Bureau National de Métrologie - Systèmes de Référence Temps-Espace



PHARAO Oscillator and Synthesis Chain



Tested at LNE-SYRTE on the F02 fountain clock

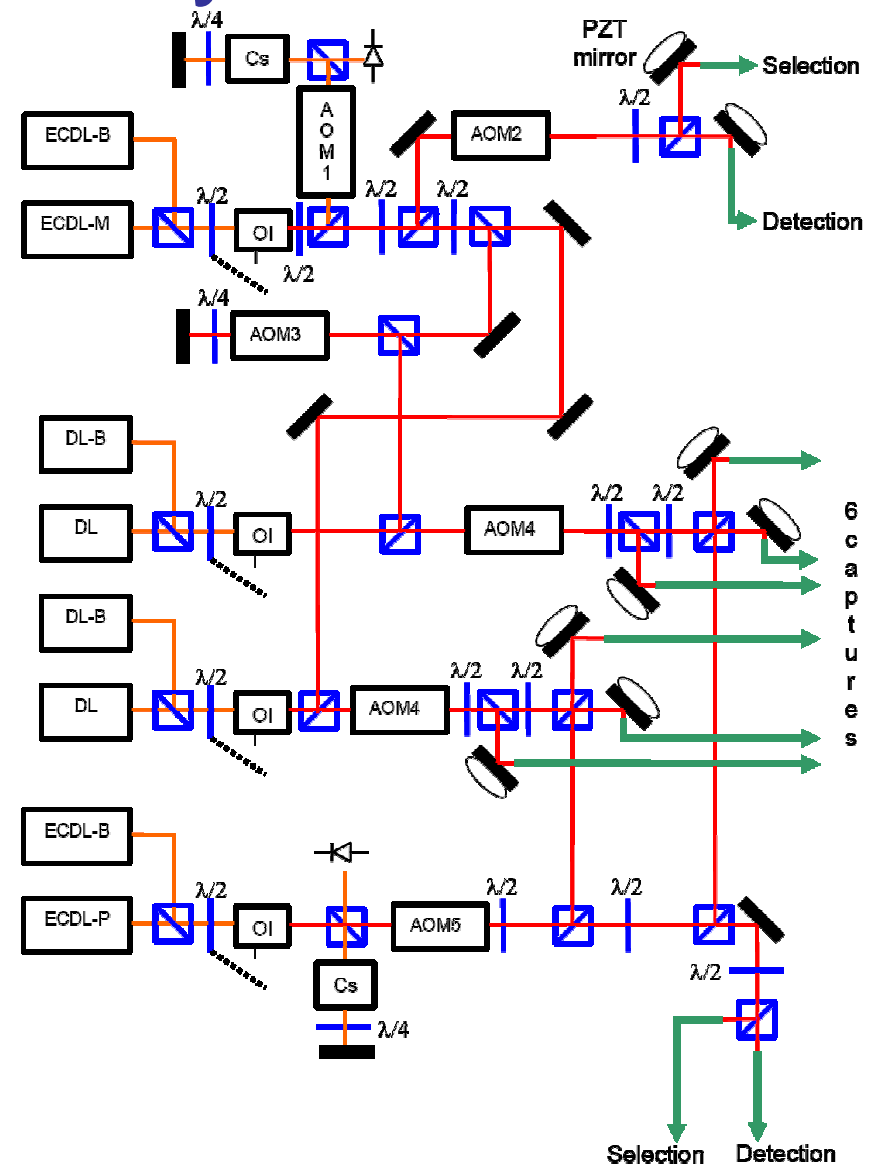
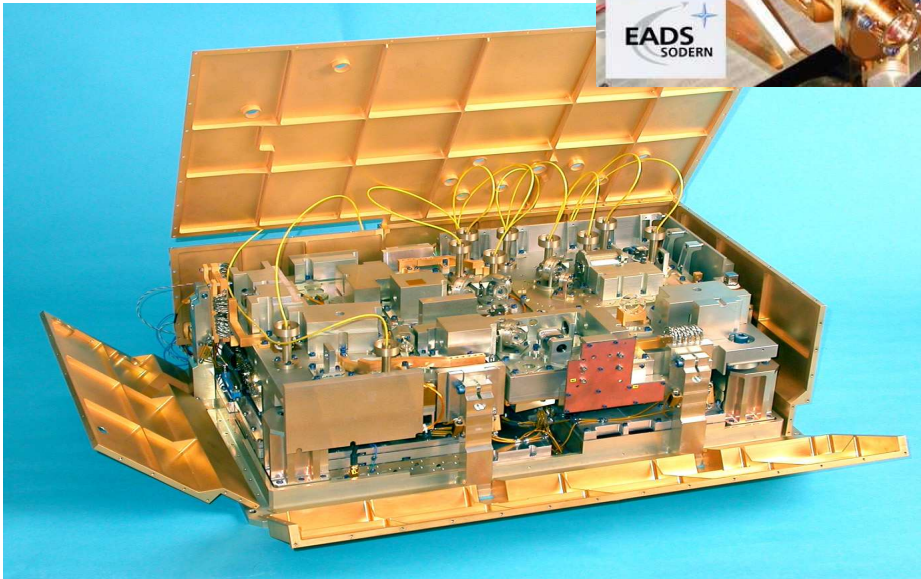
– Fractional frequency instability:
 $7 \cdot 10^{-14} \cdot \tau^{-1/2}$

PHARAO Optical System

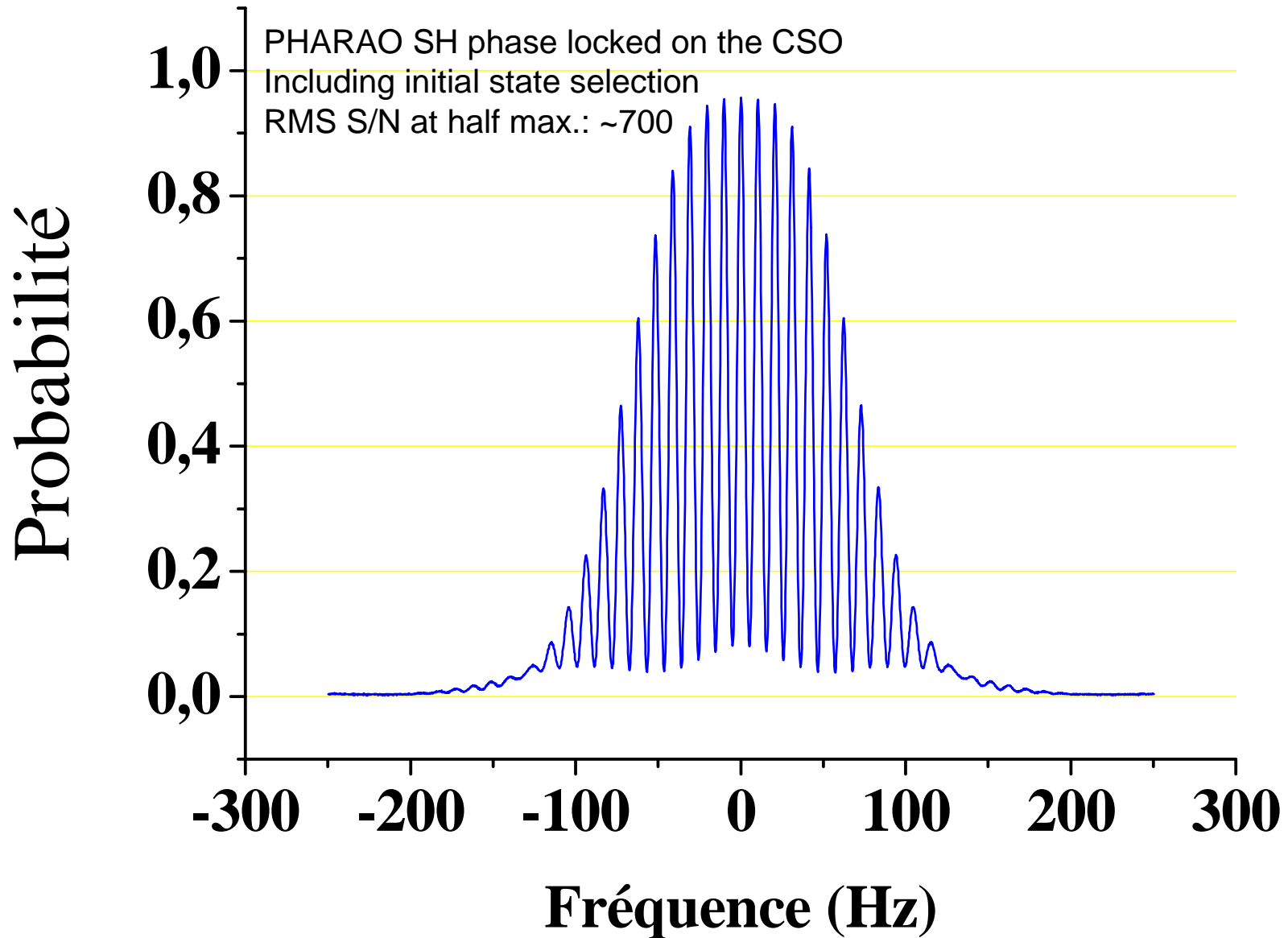
- Dimensions: 530x350x150 mm³
- Mass: 20.054 kg
- Cooling beams: 6 x 17 mW
- Repumper used for cooling, selection, and detection
- Detection system
 - Standing wave (F=4)
 - Pushing beam (F=4)
 - Pumping beam (F=3)
 - Standing wave (F=4)



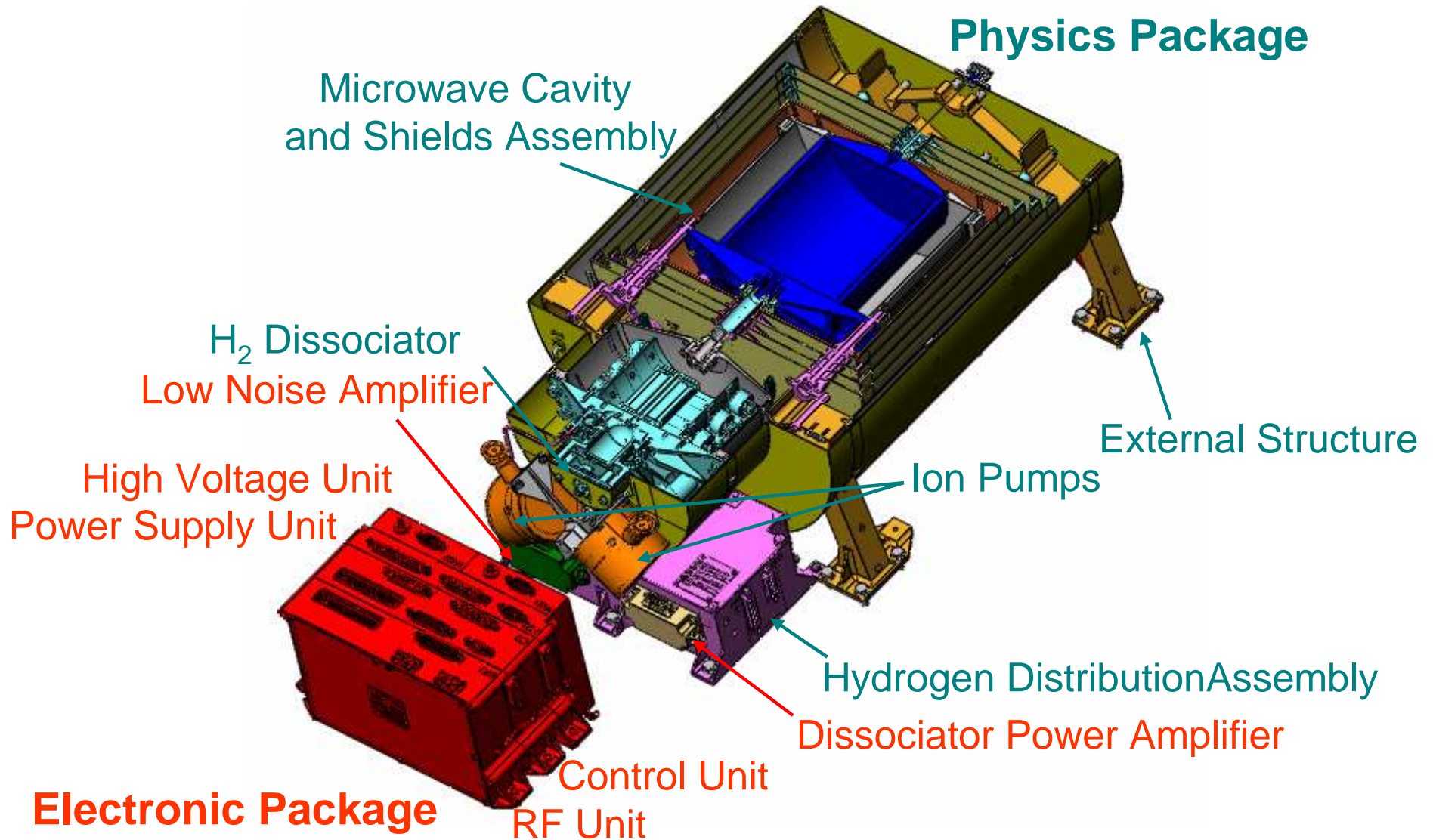
EADS SODERN



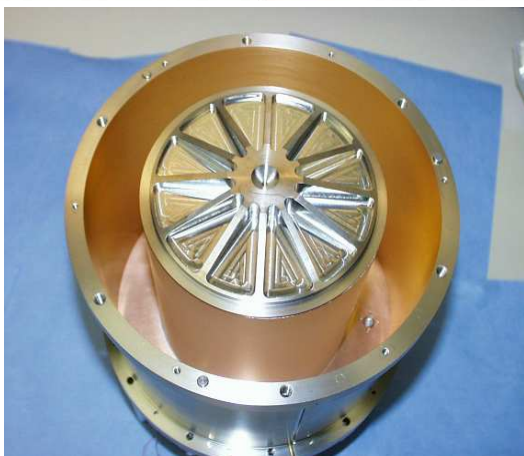
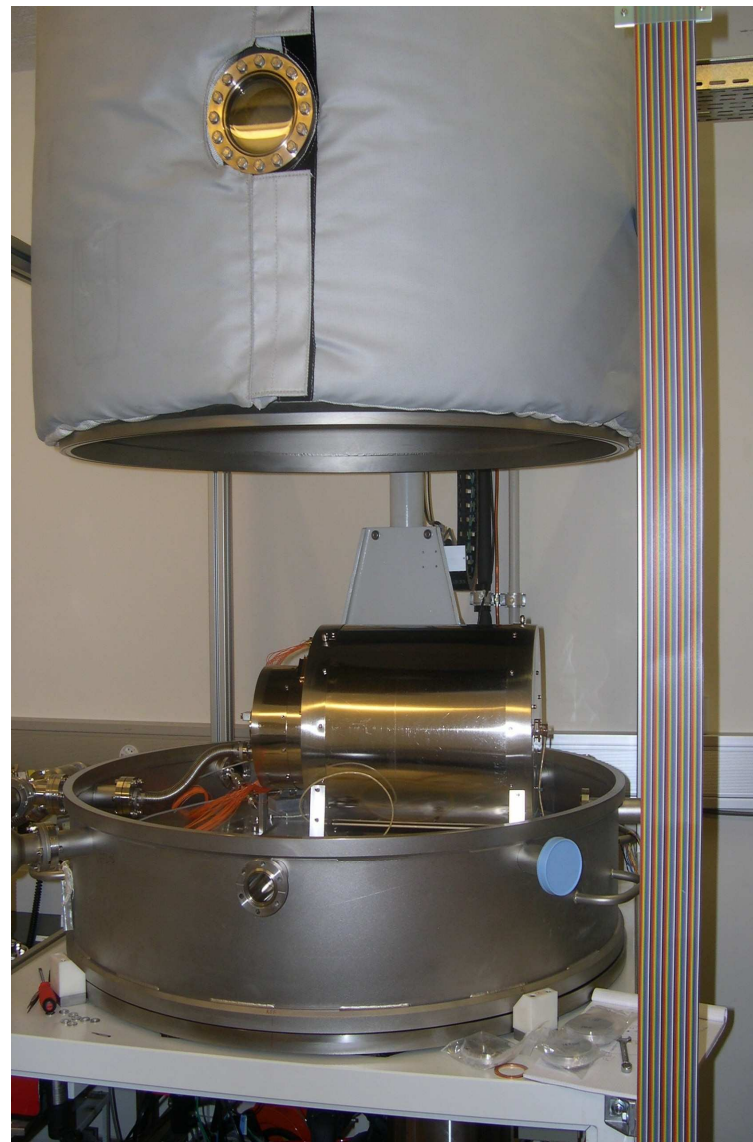
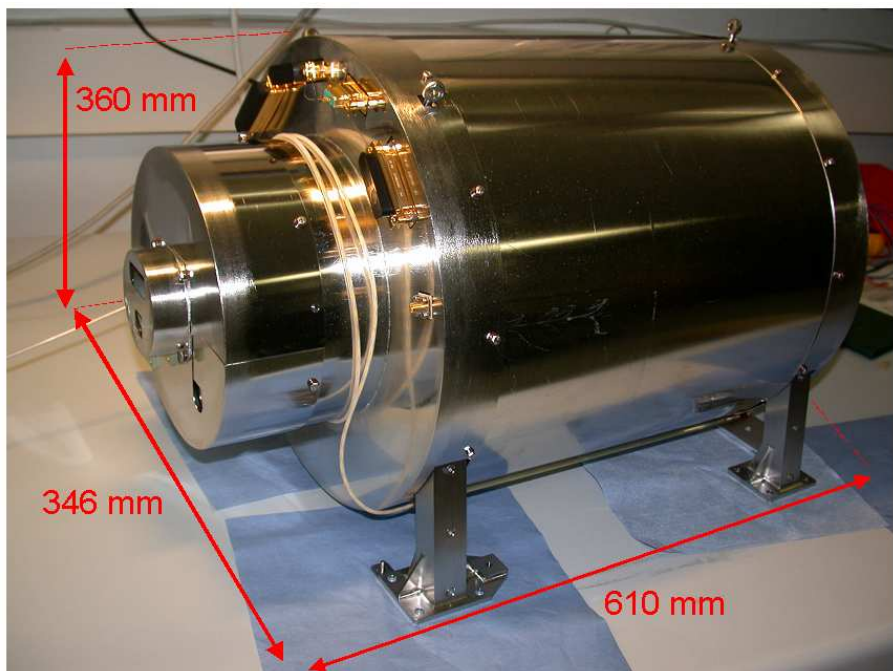
PHARAO Ramsey Fringes



SHM: An Active Maser for Space



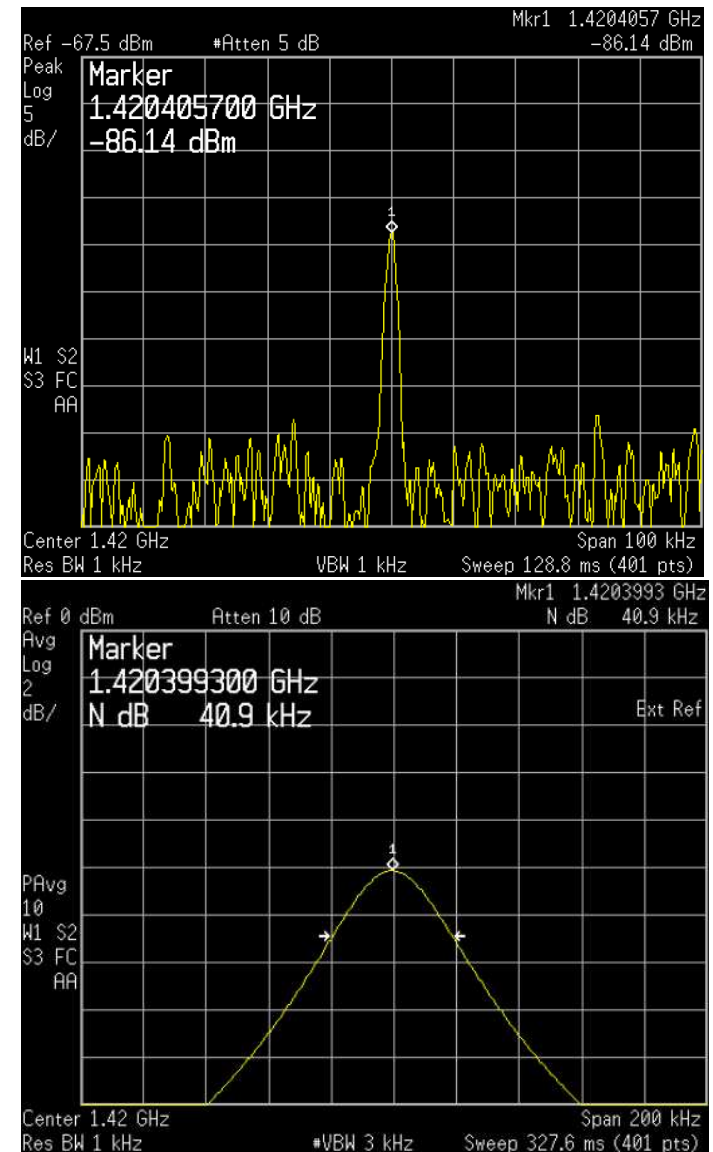
SHM Physics Package



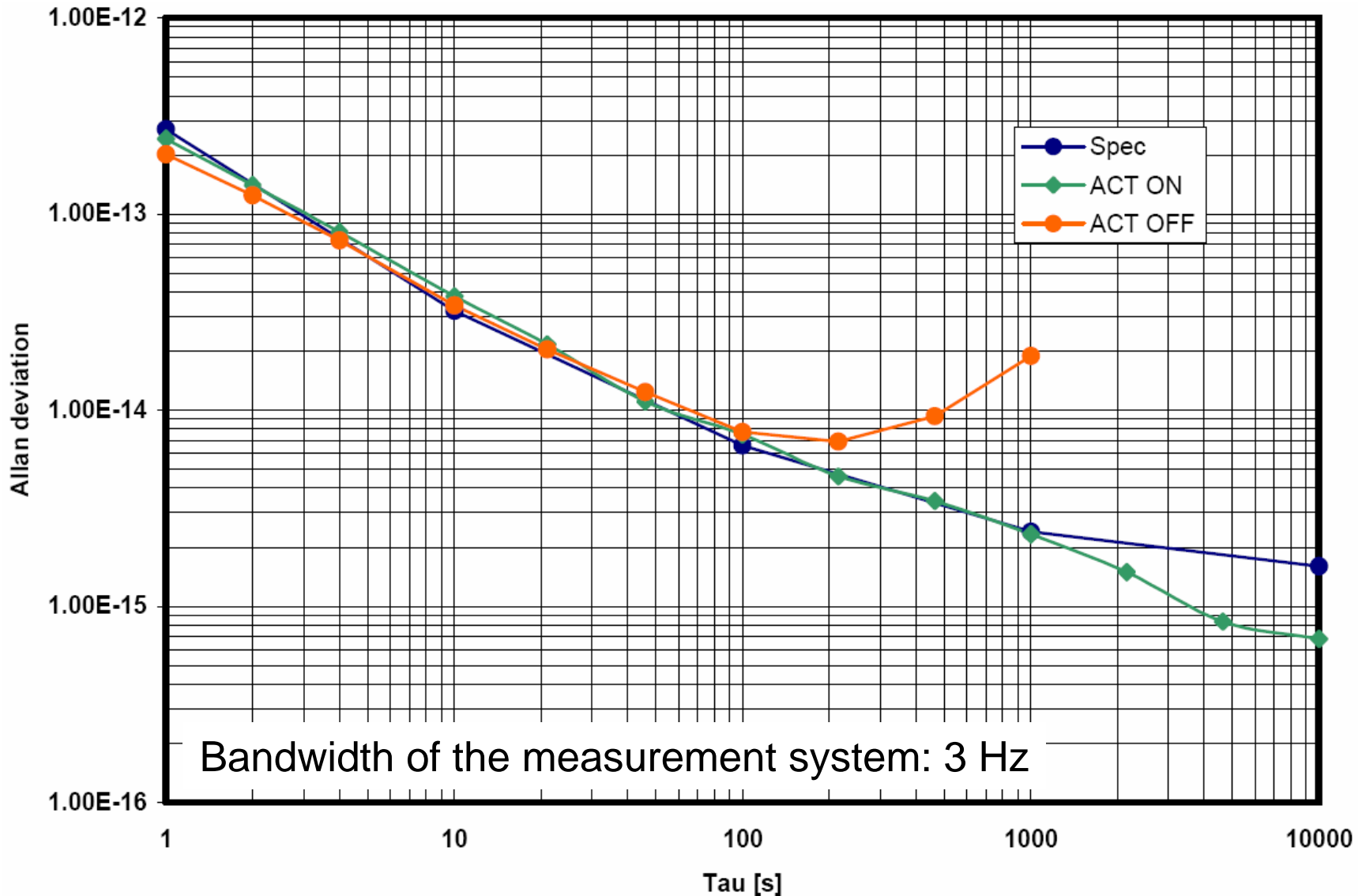
SHM Parameters

Measured Parameters

- Temperature stabilization of the microwave cavity: <math><1\text{mK}</math>
- Active oscillation: power level of -104 dBm (specified: -105 dBm)
- Measurement of the atomic quality factor via the cavity pulling effect: $1.5 \cdot 10^9$ (specified: $1.5 \cdot 10^9$)
- Cavity quality factor: (35487 ± 164) Hz
- Measurement of the spin-exchange tuning point: 8741 Hz
- Characterization of the maser signal vs B-field
- Magnetic shielding factor: $2 \cdot 10^5$



Allan Deviation: Preliminary Results



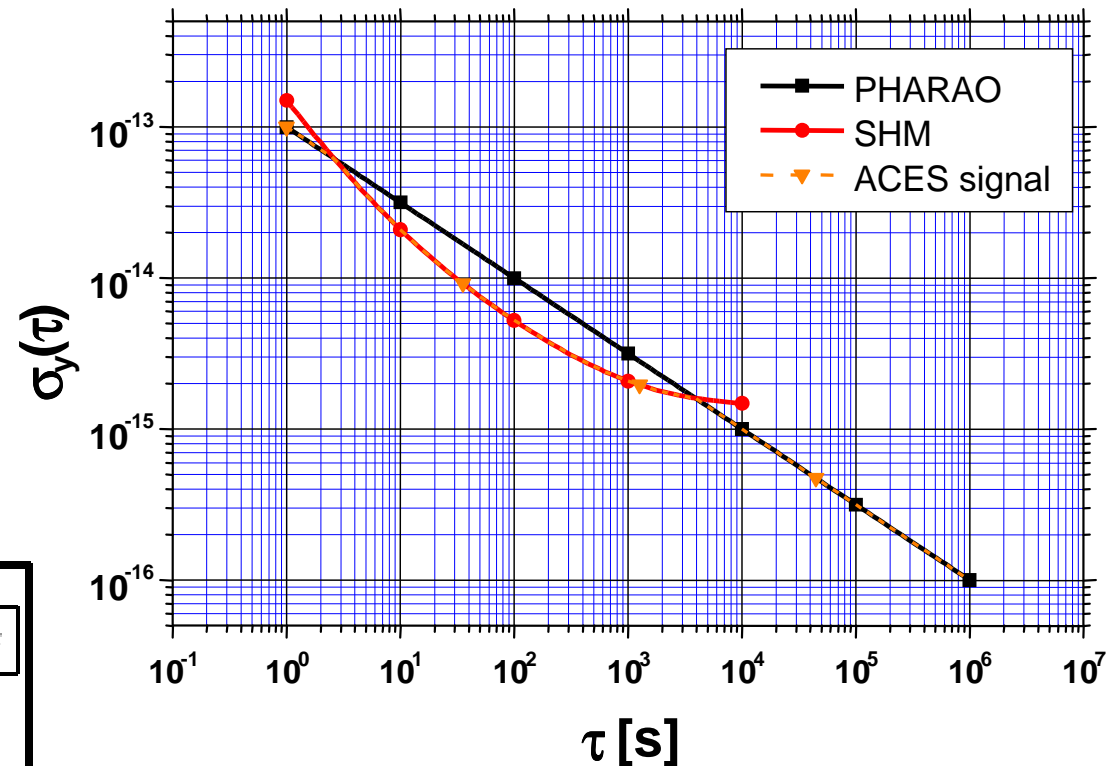
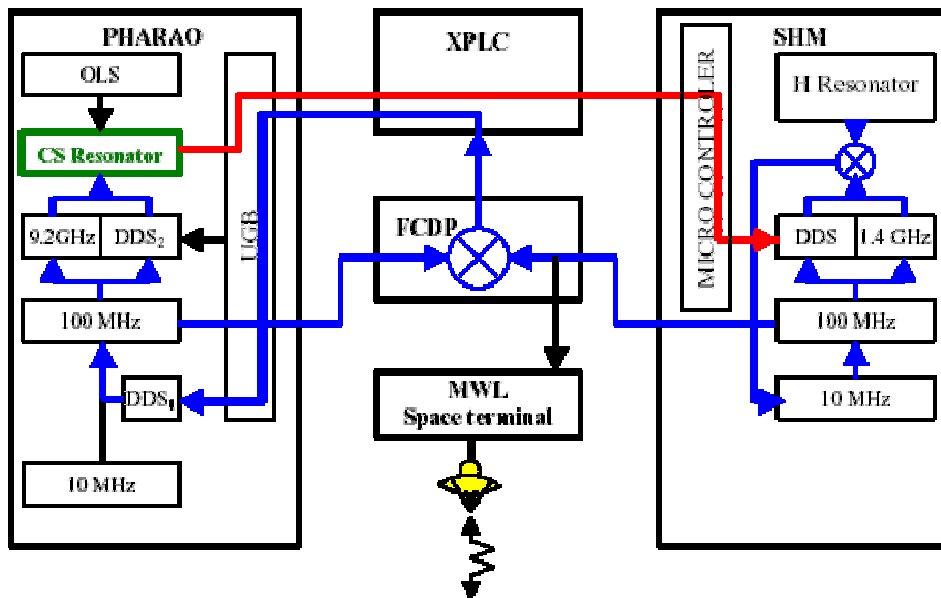
The ACES Clock Signal

Short term servo loop

Locks PHARAO local oscillator to SHM ensuring a better short and mid-term stability

Long term servo loop

Corrects for SHM drifts providing the ACES clock signal with the long-term stability and accuracy PHARAO



Stability of the ACES clock signal:

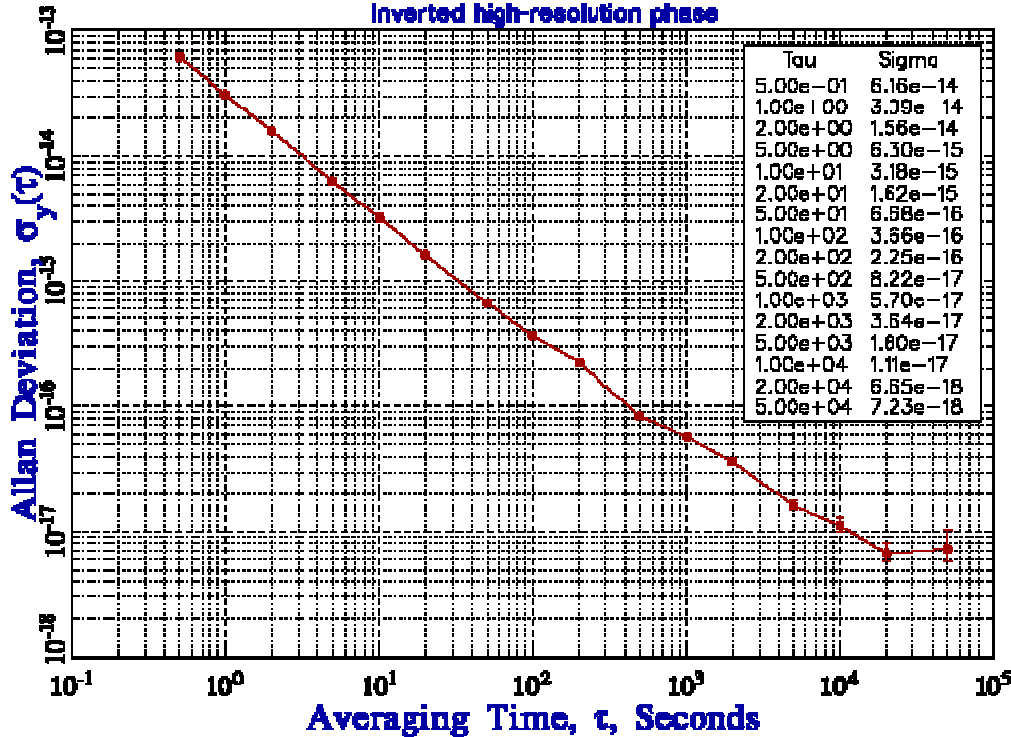
- $3 \cdot 10^{-15}$ at 300 s (ISS pass)
- $3 \cdot 10^{-16}$ at 1 day
- $1 \cdot 10^{-16}$ at 10 days

Accuracy: $\sim 1 \cdot 10^{-16}$

FCDP Engineering Model

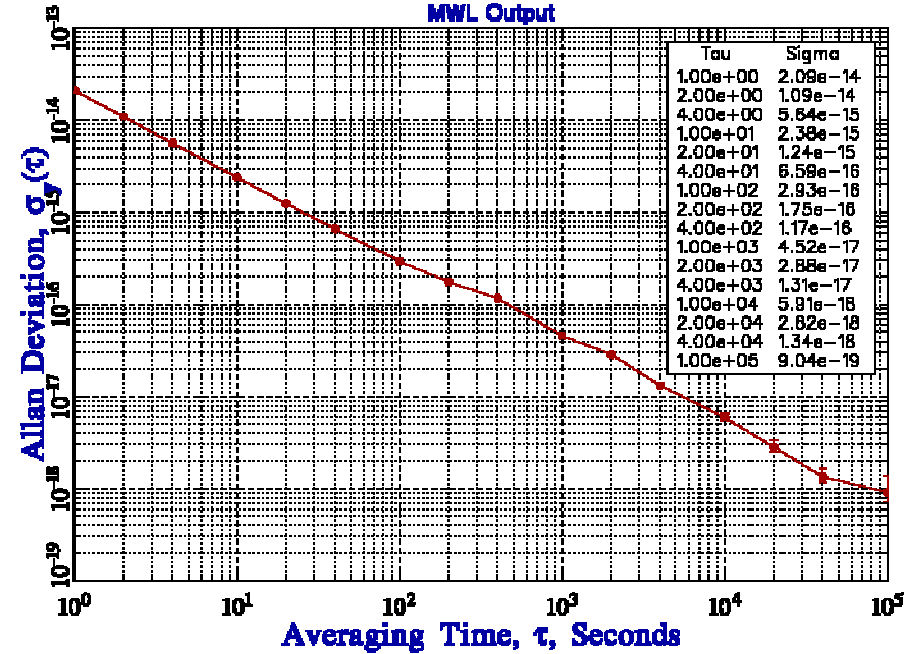
Date: 04/16/03 Time: 17:46:02 Data Points 1 thru 999999 of 999999 Tau=8.0000000e-01 File: phase.dot

FREQUENCY STABILITY Inverted high-resolution phase

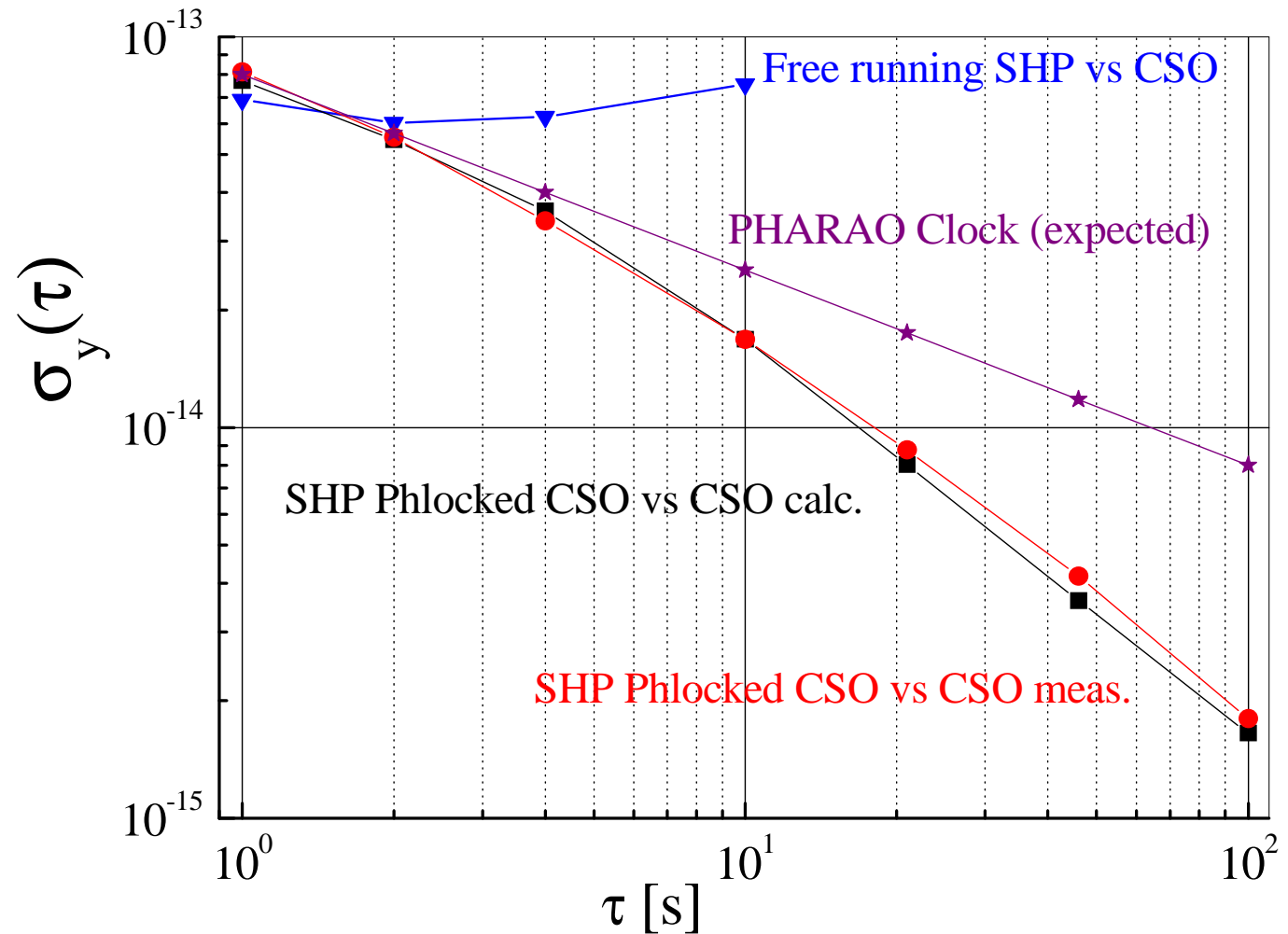
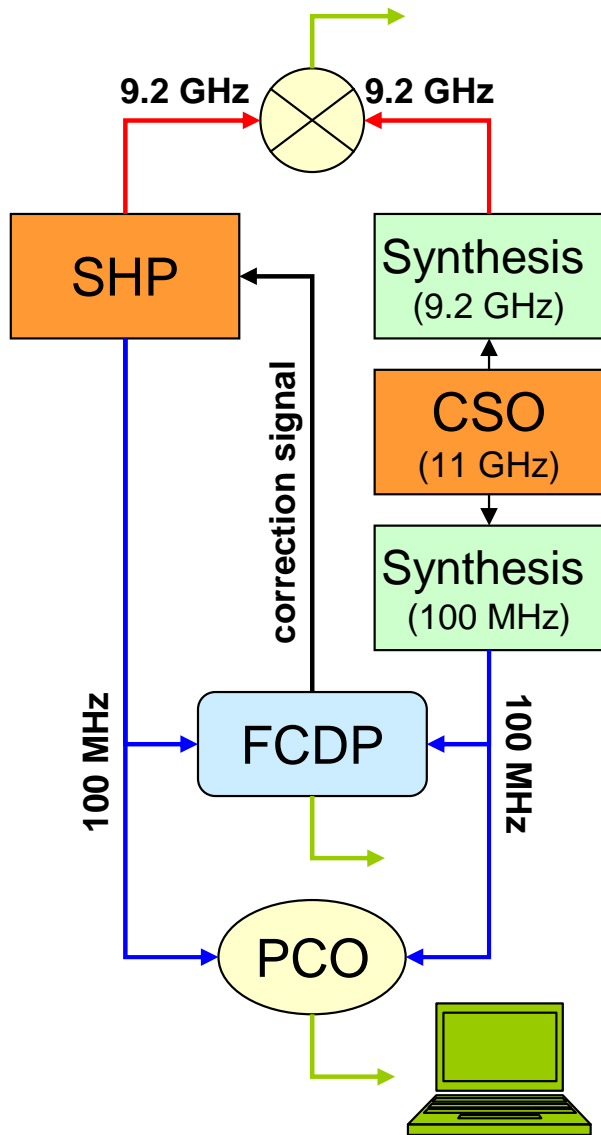


Date: 04/16/03 Time: 12:36:58 Data Points 1 thru 999999 of 999999 Tau=1.0000000e+00 File: phase2.dot

FREQUENCY STABILITY MWL Output



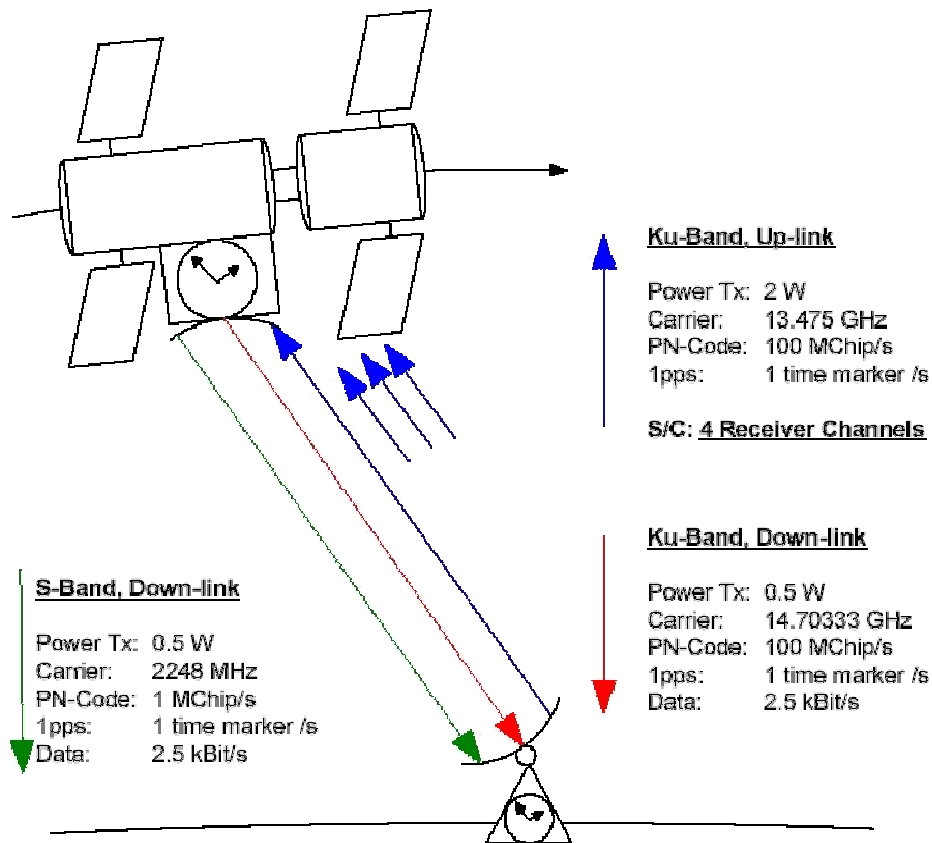
Short-term Servo Loop Test



FCDP-SHP integrated tests performed at CNES

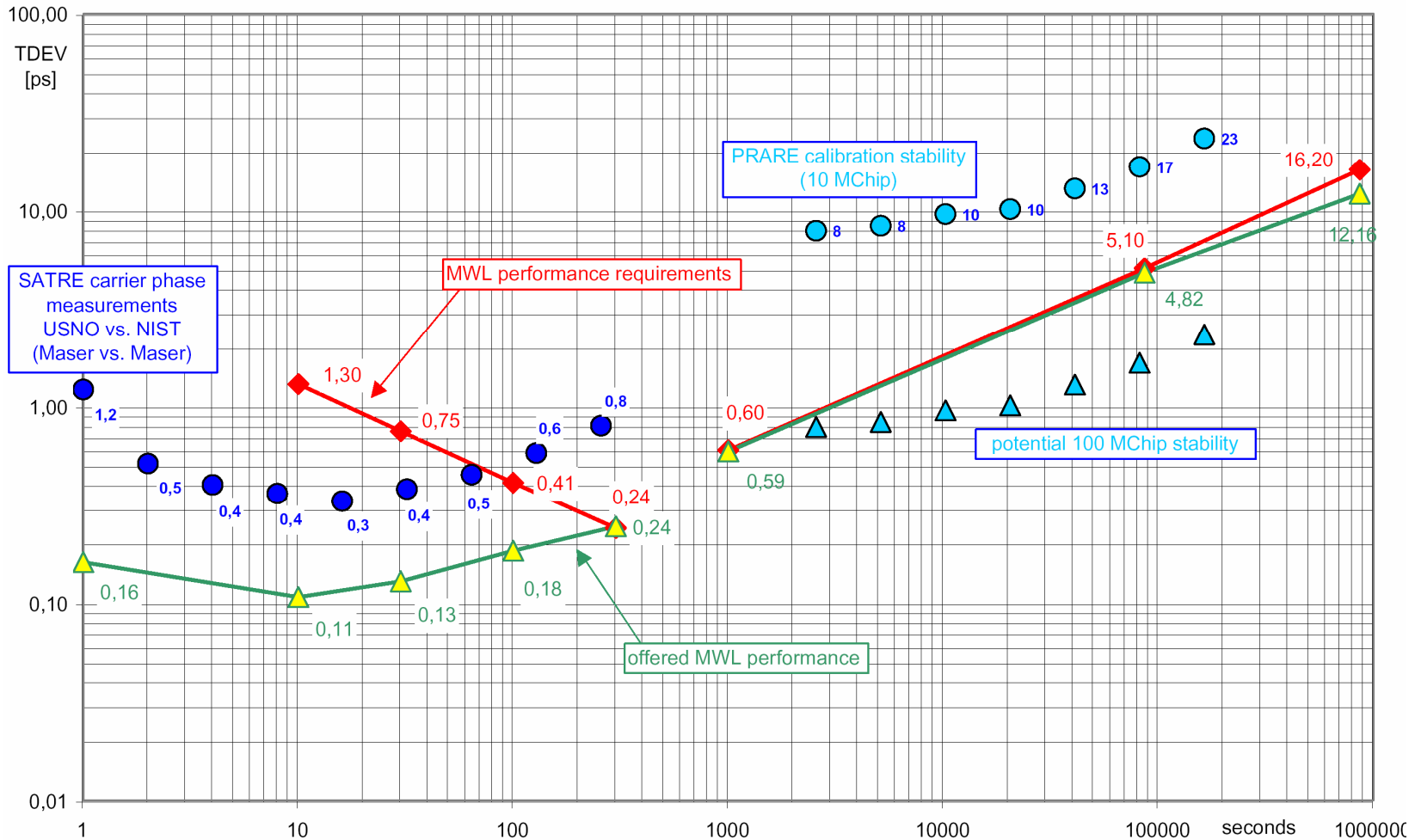


ACES Microwave Link



- **Two-way link:**
 - Removal of the troposphere time delay (8.3-103 ns)
 - Removal of 1st order Doppler effect
 - Removal of instrumental delays and common mode effects
- **Additional down-link in the S-band:**
 - Determination of the ionosphere TEC
 - Correction of the ionosphere time delay (0.3-40 ns in S-band, 6-810 ps in Ku-band)
- **Phase PN code modulation:** Removal of 2π phase ambiguity
- **High chip rate (100 MChip/s) on the code:**
 - Higher resolution
 - Multipath suppression
- **Carrier and code phase measurements (1 per second)**
- **Data link:** 2 kBits/s on the S-band down-link to obtain clock comparison results in real time
- **Up to 4 simultaneous space-to-ground clock comparisons**

ACES MWL Performances



- **Time stability:** 0.3 ps at 300 s, 6 ps at 1 day, 23 ps at 10 days of integration time
- **Accuracy:** absolute calibration at the 100 ps level
- **Clock comparisons:** 10^{-17} regime after 1 day of integration time

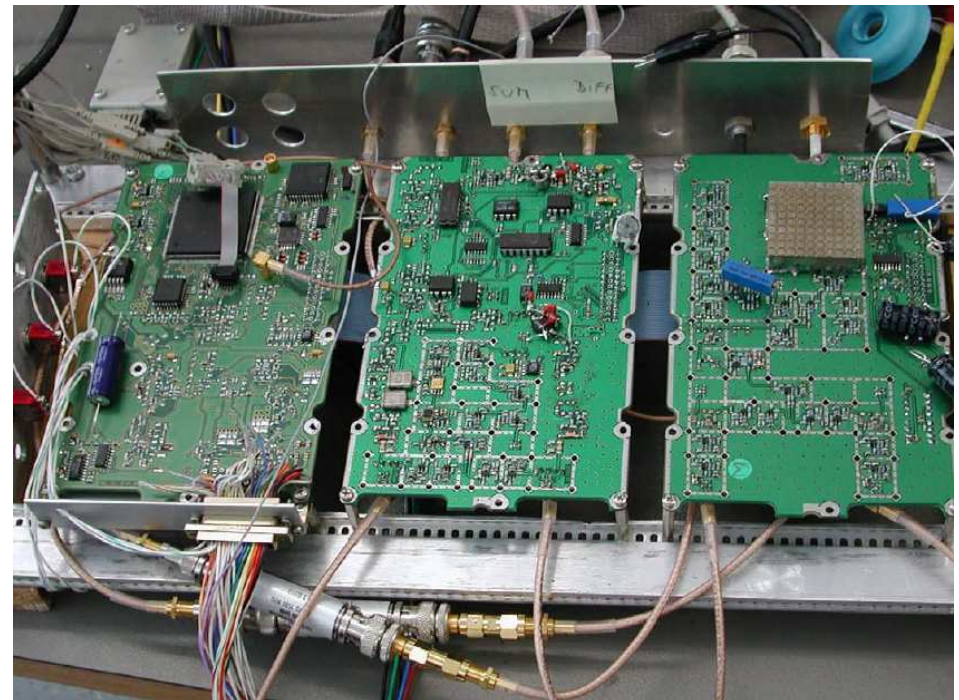
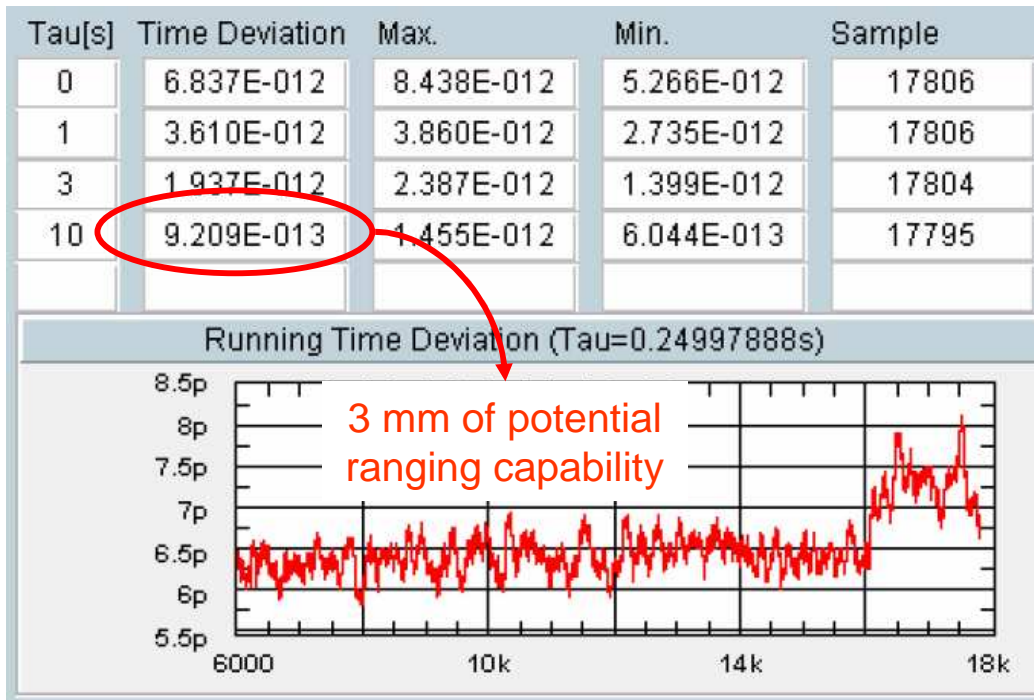
MWL Code/Carrier Phase Measurement

Code phase measurements

- Long-term stability ensured by the built-in test translator, removing thermally induced drifts
- Short-term stability (~300 s) depending on noise performances and reproducibility of each DLL receiver channel after proper calibration
- Four to five times improvement wrt 20 MChip/s commercial products demonstrated

Carrier phase measurements

- Ultimate phase stability for short integration time obtained with carrier phase measurement.
- TDEV evaluated from Ku-band Tx and IF local oscillator of Ku Band Rx: $2.3 \cdot 10^{-13}$ s up to 300 s
- ...still margin for improvement



MWL Antennas

Ku-band antenna

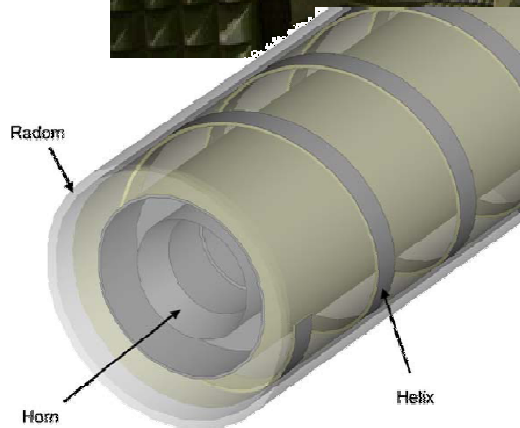
MWL FS antennas



S-band antenna



MWL GT antennas

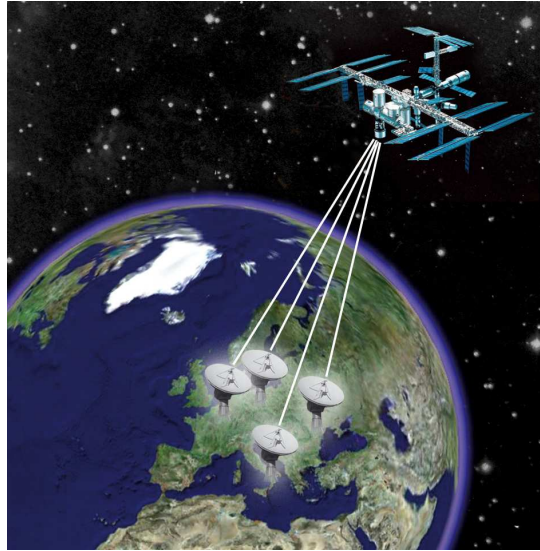


Dual feed system with 60 cm offset reflector

- Horn antenna for the Ku-band
- Helix antenna for the S-band

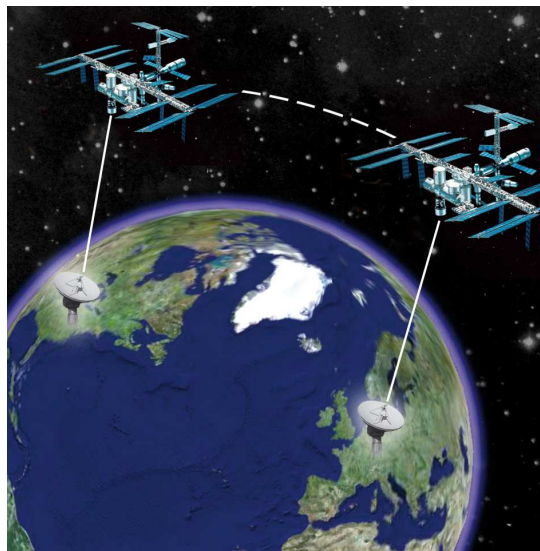
ACES Operational Scenario

- Mission duration: 1.5 years up to 3 years
- ISS orbit parameters:
 - Altitude: ~ 400 km
 - Inclination: ~ 51.6°
 - Period: 90 min
- Link according to orbit characteristics:
 - Link duration: up to 400 seconds
 - Useful ISS passes: at least one per day
- MWL ground terminals
 - Located at ground clock sites
 - Distributed worldwide



Common view comparisons

- Up to 4 simultaneous comparisons of ground clocks
- Uncertainty below 1 ps per ISS pass (~ 300 s)



Non-common view comparisons

- ACES clocks as *fly wheel*
- Uncertainty below 2 ps over 1000 s and 20 ps over 1 day

ACES Mission Objectives I

ACES Mission Objectives	ACES performances	Scientific background and recent results		
<i>Test of a new generation of space clocks</i>				
<i>Cold atoms in micro-gravity</i>	Study of cold atom physics in microgravity	Essential for the development of atomic quantum sensors for space applications (optical clocks, atom interferometers, atom lasers)		
	Frequency instability: $< 3 \cdot 10^{-16}$ at 1 day Inaccuracy: $\sim 10^{-16}$ Short term frequency instability evaluated by direct comparison to SHM. Long term instability and systematic frequency shifts measured by comparison to ultra-stable ground clocks.	PHARAO will be one of the most accurate frequency standards ever built. Recent progress of clocks in the optical domain is making available frequency standards with performances comparable to or better than PHARAO, increasing the scientific return of the ACES mission.		
<i>Test of the space hydrogen maser SHM</i>	Frequency instability: $< 2.1 \cdot 10^{-15}$ at 1000 s $< 1.5 \cdot 10^{-15}$ at 10000 s Medium term frequency instability evaluated by direct comparison to ultra-stable ground clocks. Long term instability determined by on-board comparison to PHARAO in FCDP.	Performances of state-of-the-art masers		
		Maser	$\sigma_y(1000 \text{ s})$	$\sigma_y(10000 \text{ s})$
		GALILEO	$3.2 \cdot 10^{-14}$	$1.0 \cdot 10^{-14}$
EFOS C	$2.0 \cdot 10^{-15}$	$2.0 \cdot 10^{-15}$		

ACES Mission Objectives II

ACES Mission Objectives	ACES performances	Scientific background and recent results			
<i>Stable time and frequency transfer</i>					
<i>Test of the time and frequency link MWL</i>	Time transfer stability: < 0.3 ps at 300 s < 7 ps at 1day < 23 ps at 10 days	At present, no time and frequency transfer link has performances comparable to MWL.			
<i>Time and frequency comparisons between ground clocks</i>	Common view comparisons with an uncertainty level below 1 ps per ISS pass. Non common view comparisons at an uncertainty level of <ul style="list-style-type: none"> - 2 ps for $\tau=1000$ s - 5 ps for $\tau=10000$ s - 20 ps for $\tau=1$ day 	Existing T&F links	Time stability (1day)	Time accuracy (1day)	Frequency accuracy (1day)
		GPS-DB	2 ns	3-10 ns	$4 \cdot 10^{-14}$
		GPS-CV	1 ns	1-5 ns	$2 \cdot 10^{-14}$
		GPS-CP	0.1 ns	1-3 ns	$2 \cdot 10^{-15}$
		TWSTFT	0.1-0.2 ns	1 ns	$2-4 \cdot 10^{-15}$
<i>Absolute synchronization of ground clocks</i>	Absolute synchronization of ground clock time scales with an uncertainty of 100 ps.	These performances will allow time and frequency transfer at an unprecedented level of stability and accuracy. The development of such links is mandatory for space experiments based on high stability frequency standards.			
<i>Contribution to atomic time scales</i>	Comparison of primary frequency standards with accuracy at the 10^{-16} level.				

ACES Mission Objectives III

ACES Mission Objectives	ACES performances	Scientific background and recent results
<i>Fundamental physics tests</i>		
Measurement of the gravitational red shift	Absolute measurement of the gravitational red-shift at an uncertainty level $< 50 \cdot 10^{-6}$ after 300 s and $< 2 \cdot 10^{-6}$ after 10 days.	Space-to-ground clock comparison at the 10^{-16} level, will yield a factor 30 improvement on previous measurements (GPA experiment).
Search for time drifts of fundamental constants	Time variations of the fine structure constant α at a precision level of $\alpha^{-1} \cdot d\alpha / dt < 1 \cdot 10^{-16} \text{ year}^{-1}$	Crossed comparisons of clocks based on different atomic elements to impose strong constraints on the time drifts of α , $m_e / \Lambda_{\text{QCD}}$, and $m_u / \Lambda_{\text{QCD}}$.
Search for violations of special relativity	Search for anisotropies of the speed of light at the level $\delta c / c \sim 10^{-10}$. Measurements relying on the time stability of SHM, PHARAO, MWL, and ground clocks over one ISS pass.	ACES results will improve previous tests based on GPS satellites by at least one order of magnitude.

Relativistic Frequency Transfer

The diagram illustrates relativistic frequency transfer between a satellite and Earth. A satellite with a clock is shown in orbit above Earth, which also has a clock. The background is a blue grid representing spacetime curvature. A table on the right lists relativistic effects and their magnitudes. Below the table, a large white arrow points down to the text 'Precise Orbit Determination'. At the bottom left, a mathematical formula for frequency shift is provided, along with its source.

Relativistic effects	
First order Doppler effect	$2 \cdot 10^{-5}$
Second order Doppler effect	$3 \cdot 10^{-10}$
Gravitational red-shift	$5 \cdot 10^{-11}$
Sagnac effect	$7 \cdot 10^{-13}$

↓

Precise Orbit Determination

$$\frac{\delta f}{f} = \frac{1}{c^2} \left(U_{BA} - \frac{v_{BA}^2}{2} - \vec{R}_{BA} \cdot \vec{a}_B \right) \left(1 - \frac{1}{c} \frac{\vec{R}_{BA} \cdot \vec{v}_{BA}}{R_{BA}} \right) + \frac{R_{BA}}{c^3} (-\vec{v}_A \cdot \vec{a}_B + \vec{R}_{BA} \cdot \vec{b}_B + 2\vec{v}_B \cdot \vec{a}_B - \vec{v}_B \cdot \vec{\nabla} U_B) + O\left(\frac{1}{c^4}\right)$$

L. Blanchet *et al.*, A&A **370**, 320 (2001)

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<i>Search for time drifts of fundamental constants</i>	Time variations of the fine structure constant α at a precision level of $\alpha^{-1} \cdot d\alpha / dt < 1 \cdot 10^{-16} \text{ year}^{-1}$	Crossed comparisons of clocks based on different atomic elements to impose strong constraints on the time drifts of α , m_e / Λ_{QCD} , and m_q / Λ_{QCD} .
<i>Search for violations of special relativity</i>	Search for anisotropies of the speed of light at the level $\delta c / c \sim 10^{-10}$. Measurements relying on the time stability of SHM, PHARAO, MWL, and ground clocks over one ISS pass.	ACES results will improve previous tests based on GPS satellites by at least one order of magnitude.

Time Variations of Fundamental Constants I

Frequency of hyperfine transitions: $\nu_{\text{hfs}}^{(i)} \simeq R_{\infty} c \times \mathcal{A}_{\text{hfs}}^{(i)} \times g^{(i)} \left(\frac{m_e}{m_p} \right) \alpha^2 F_{\text{hfs}}^{(i)}(\alpha)$

Frequency of electronic transitions: $\nu_{\text{elec}}^{(i)} \simeq R_{\infty} c \times \mathcal{A}_{\text{elec}}^{(i)} \times F_{\text{elec}}^{(i)}(\alpha)$

Ratios between atomic frequencies:

$$\frac{\nu_{\text{elec}}^{(ii)}}{\nu_{\text{elec}}^{(i)}} \propto \frac{F_{\text{elec}}^{(ii)}(\alpha)}{F_{\text{elec}}^{(i)}(\alpha)} \quad \frac{\nu_{\text{hfs}}^{(ii)}}{\nu_{\text{elec}}^{(i)}} \propto g^{(ii)} \frac{m_e}{m_p} \alpha^2 \frac{F_{\text{hfs}}^{(ii)}(\alpha)}{F_{\text{elec}}^{(i)}(\alpha)} \quad \frac{\nu_{\text{hfs}}^{(ii)}}{\nu_{\text{hfs}}^{(i)}} \propto \frac{g^{(ii)}}{g^{(i)}} \frac{F_{\text{hfs}}^{(ii)}(\alpha)}{F_{\text{hfs}}^{(i)}(\alpha)}$$

Sensitivity to time variations of fundamental constants:

$$\delta \ln \left(\frac{\nu_{\text{hfs}}^{(i)}}{R_{\infty} c} \right) \simeq \frac{\delta g^{(i)}}{g^{(i)}} + \frac{\delta(m_e/m_p)}{(m_e/m_p)} + \left(2 + \alpha \frac{\partial}{\partial \alpha} \ln F_{\text{hfs}}^{(i)}(\alpha) \right) \times \frac{\delta \alpha}{\alpha}$$

$$\delta \ln \left(\frac{\nu_{\text{elec}}^{(i)}}{R_{\infty} c} \right) \simeq \left(\alpha \frac{\partial}{\partial \alpha} \ln F_{\text{elec}}^{(i)}(\alpha) \right) \times \frac{\delta \alpha}{\alpha}$$

Time Variations of Fundamental Constants II

$g^{(i)}$ and m_p are not “fundamental” constants; they depend on

- QCD mass scale Λ_{QCD}
- Quark mass $m_q = (m_u + m_d)/2$

therefore comparisons of atomic frequency will test the time stability

of the three fundamental constants $\alpha, \frac{m_q}{\Lambda_{\text{QCD}}}, \frac{m_e}{\Lambda_{\text{QCD}}}$

In general
$$\delta \ln \left(\frac{\nu^{(i)}}{R_\infty c} \right) \simeq K_\alpha^{(i)} \times \frac{\delta \alpha}{\alpha} + K_q^{(i)} \times \frac{\delta(m_q/\Lambda_{\text{QCD}})}{(m_q/\Lambda_{\text{QCD}})} + K_e^{(i)} \times \frac{\delta(m_e/\Lambda_{\text{QCD}})}{(m_e/\Lambda_{\text{QCD}})}$$

$$K_\alpha^{(i)} \neq 0, K_q^{(i)} \neq 0, K_e^{(i)} \simeq 1$$

hyperfine transitions

$$K_\alpha^{(i)} \neq 0, K_q^{(i)} \simeq 0, K_e^{(i)} \simeq 0$$

electronic transition

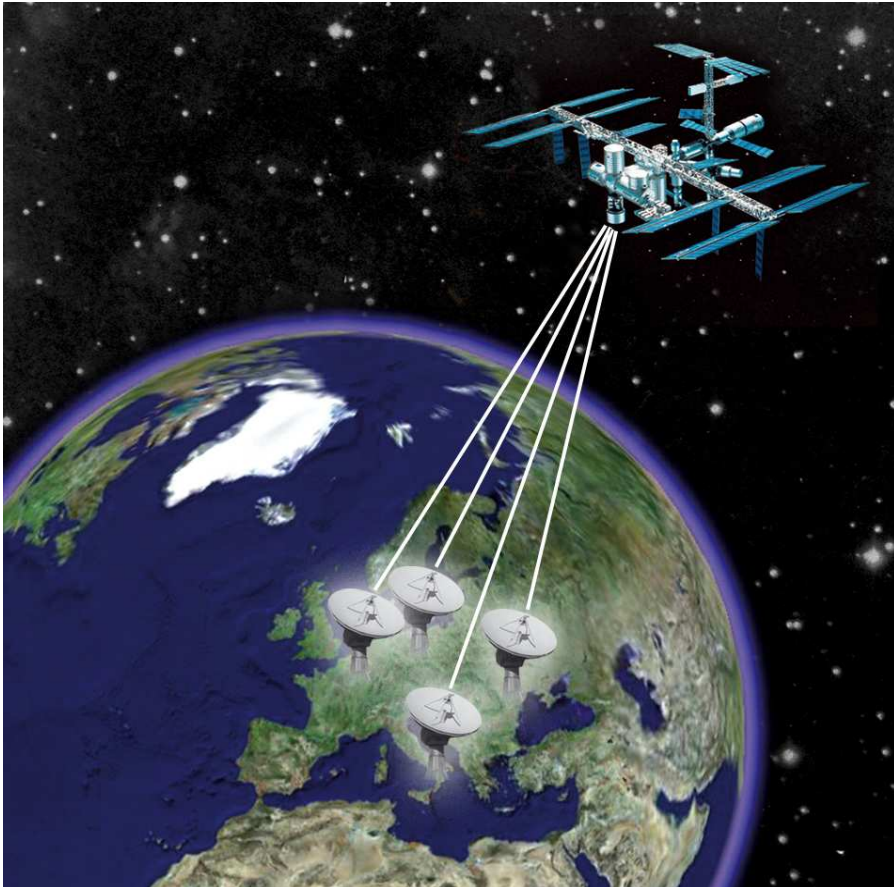
$$K_\alpha^{(i)} \simeq 0, K_q^{(i)} \simeq 0, K_e^{(i)} \simeq 1/2$$

vibrational transitions in molecules

V.V. Flambaum, arxiv:physics/0302015

V.V. Flambaum *et al.*, Phys. Rev. D **69**, 115006 (2004)

Time Variations of Fundamental Constants III



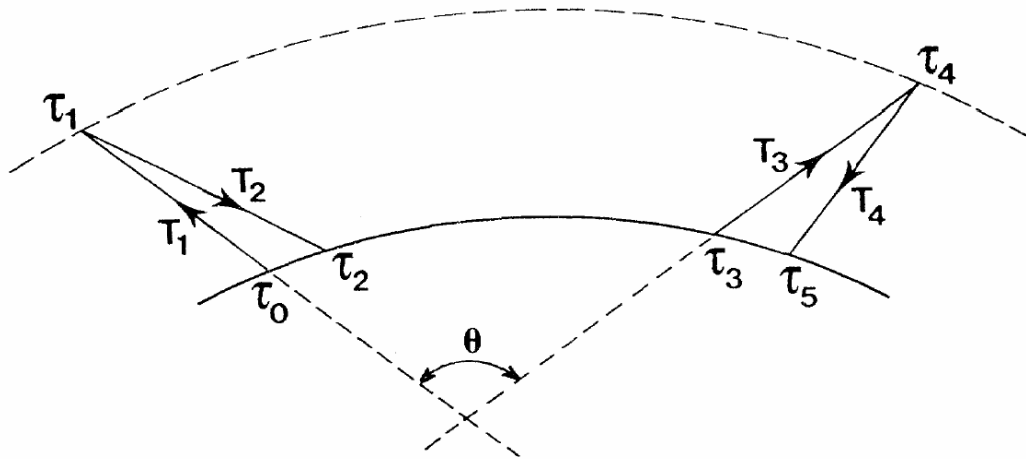
- Worldwide access to the ACES frequency standard
- Common view comparisons up to 4 different clocks based on different atomic transitions to constrain time variations of $\alpha, m_q/\Lambda_{\text{QCD}}, m_e/\Lambda_{\text{QCD}}$
- Non common view comparisons of distant clocks
- Redundancy possible with more than 4 atomic clocks
- Frequency comparisons at the 10^{-16} level possible

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Clock Tests of Special Relativity

- **Kinematic test theories (RMS framework):** Preferred reference frame (CMB) in which light is assumed to propagate isotropically
- **Dynamic test theories (SME framework):** Lorentz transformations violating terms in the Hamiltonian of the system



Measurement principle:

- Exchange of microwave signals between ACES clocks and ground clocks along the ISS orbit
- Difference of measured reception and emission times provides the one-way travel time of the signal plus some unknown constant offset (desynchronization, path asymmetries, propagation delays,...)
- Difference of the up and down travel times sensitive to a non zero value of $\delta c/c$

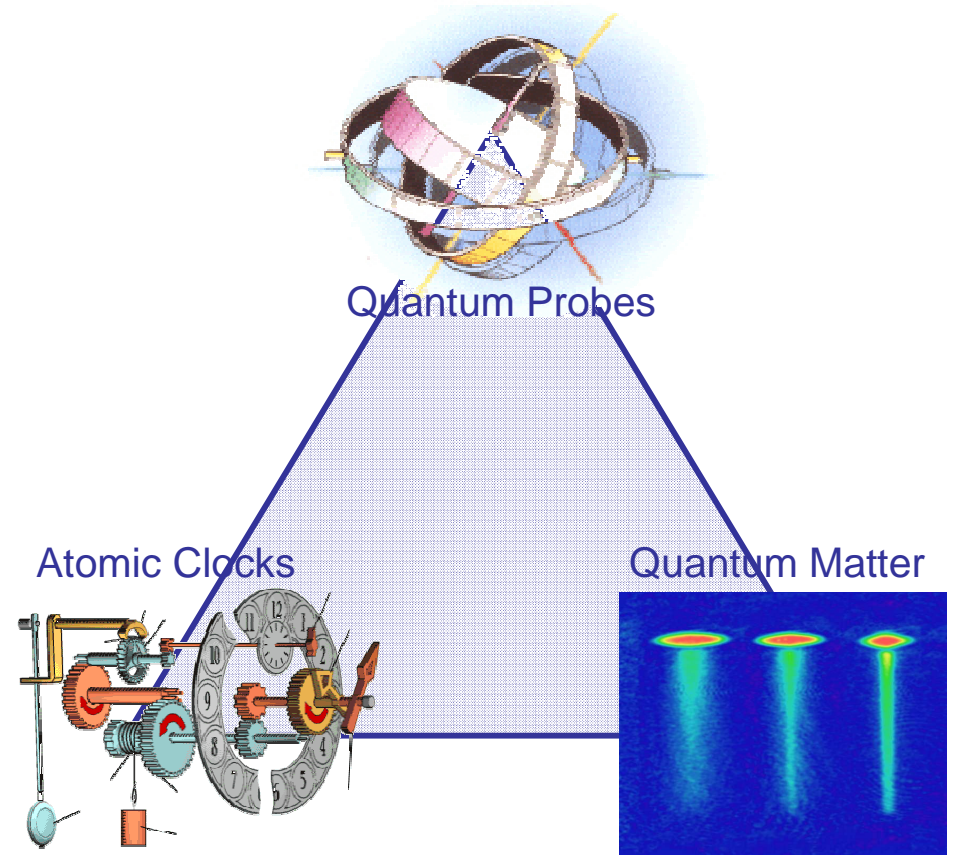
$$T_1 - T_2 = \Delta_s + \Delta_l + 2 \frac{\delta c}{c} T \cos \theta$$

$$(T_1 - T_2) - (T_3 - T_4) + \Delta_a = 2 \frac{\delta c}{c} T (1 - \cos \theta)$$

P. Wolf, PRA **51**, 5016 (1995)

Pioneering Aspects of ACES

- Technology demonstrator for **cold atom based missions**
- First μg **experiments with cold atoms**
- Validation in space of **complex laser systems, UHV equipment, ultra-stable RF electronics...**
- Validation of a **new generation of atomic clocks**
- Demonstration of stable and accurate **time and frequency transfer**
- Long-distance **clock-to-clock comparisons**
- Precursor of **optical clocks**: towards the 10^{-18} stability and accuracy regime



from E. Rasel *et al.*

These results will arrive in time to prepare the next generation of atomic quantum sensors for space

Atomic Quantum Sensors in Space

Atomic Clocks

Fundamental Physics

- Standard Model Extension tests
- Universality of the gravitational red-shift
- Time variations of fundamental constants
- Gravitational red-shift
- Shapiro time delay and $1/c^3$ effects
- Gravitational waves detection

Applications

- Atomic time scales (TAI)
- Time & Frequency metrology
- Deep space navigation
- Doppler tracking
- Synchronization of DSNA
- VLBI
- Time & Frequency transfer
- Gravity mapping
- Planetary exploration

Atom Interferometers

Fundamental Physics

- Weak Equivalence Principle tests
- Measurement of fundamental constants
- Time variations of fundamental constants
- Measurement of the gravito-magnetic effect
- Tests of the Newton's law at short distances
- Gravitational waves detection

Applications

- Inertial navigation
- Earth observation and monitoring
- Geology and vulcanology
- Gravity and gravity-gradient mapping
- Planetary exploration

Degenerate Quantum Gases

Fundamental Physics

- Thermodynamics of the phase transition at ultra-low temperatures
- Collective excitations in the weak trapping regime
- BEC coherence properties in microgravity
- Role of interactions in BEC: dipolar forces and short range interactions
- Dynamics of Bose mixtures in microgravity

Applications

- Atomic sources for atom interferometry
- High-resolution interferometric measurements with dilute coherent matter waves

ASTRIUM

