



Short-range tests of gravity and the Casimir effect

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<http://www.lkb.ens.fr/Vacuum>



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EU Framework 6 project
NEST (New Emerging Science & Technology)



Motivation : Tests of the Newtonian law

New hypothetical forces

(cf. G.Veneziano's and G. Tino's talk)

Generic representation :
Yukawa + Newtonian
potential

$$V(r) = V_N(r) + V_Y(r)$$

$$V_N(r) = -G_N \frac{M_1 M_2}{r}$$

$$V_Y(r) = V_N(r) \alpha \exp(-r/\lambda)$$

$$F(r) = F_N(r) + F_Y(r)$$

$$F_N(r) = -G_N \frac{M_1 M_2}{r^2}$$

$$F_Y(r) = F_N(r) \alpha \left(1 + \frac{r}{\lambda} \right) \exp(-r/\lambda)$$

Modification of
Newtonian law between
pointlike masses

How to test the Newtonian law ?

Measurements give constraints in the plane (λ, α)

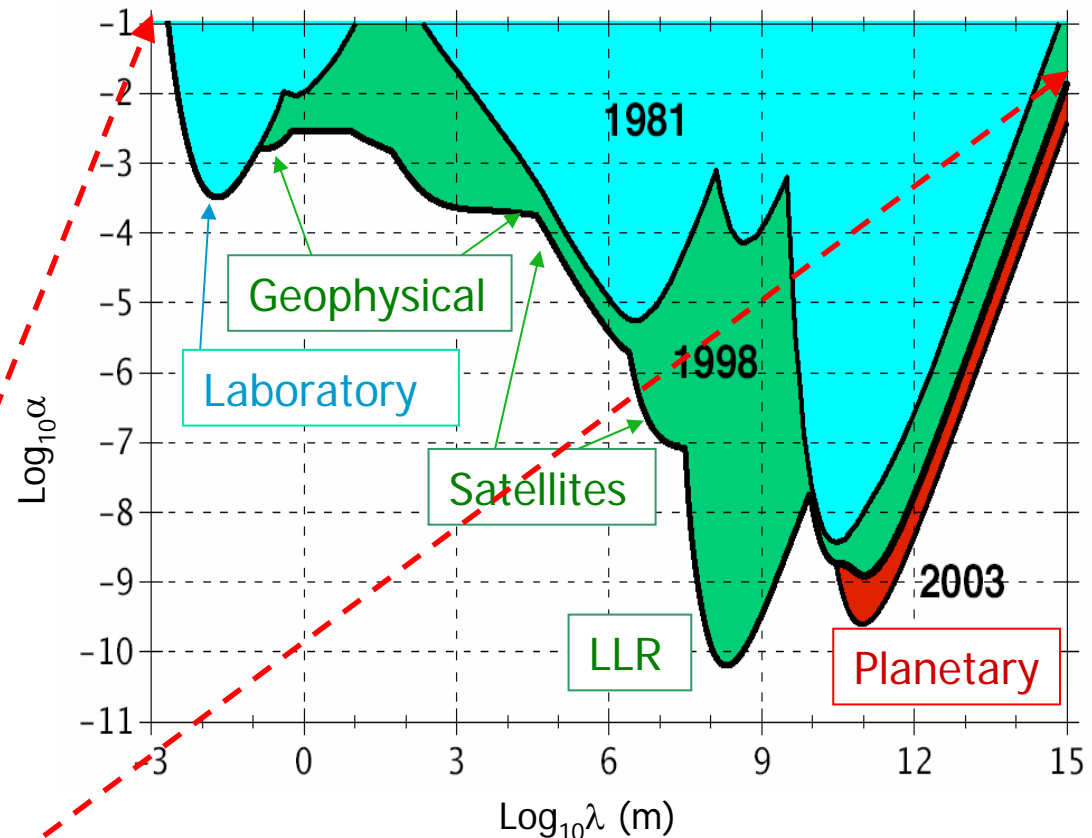
Open window at short distances...

$$\lambda < 10^{-3} \text{ m}$$

and at long distances

$$\lambda > 10^{16} \text{ m}$$

(cf. Marc Jaekel's talk)



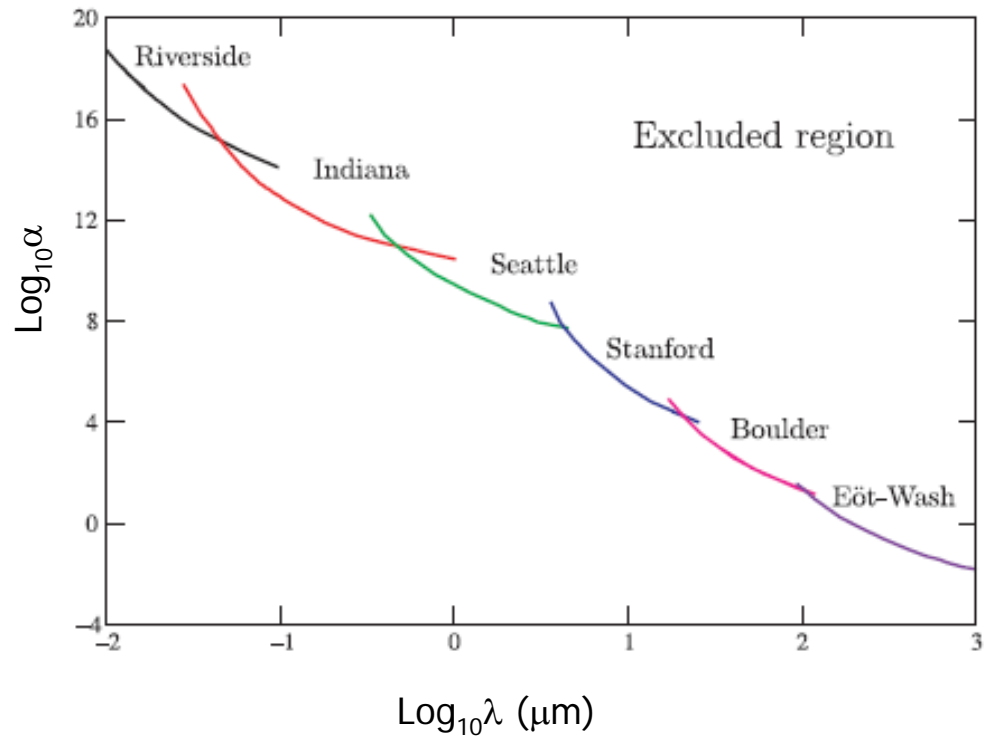
Courtesy : J. Coy, E. Fischbach, R. Hellings, C. Talmadge, and E. M. Standish (2003)

Test at short distances

- Gravity measurements at millimetric distances

$$\frac{GM_1M_2}{r} (1 + \alpha e(-r/\lambda))$$

- $\lambda \leq 30\mu\text{m}$: comparison between experimental results and theoretical predictions of the Casimir force



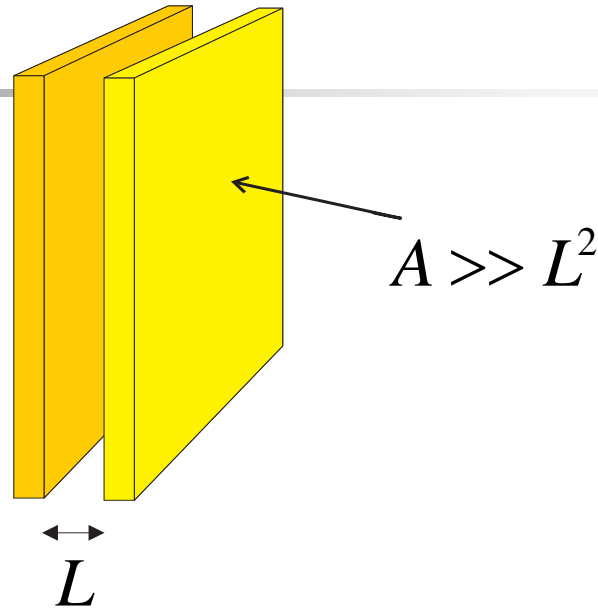
Casimir 1948

$$F_{\text{Cas}} = \frac{\hbar c \pi^2}{240 L^4} A$$

$$E_{\text{Cas}} = -\frac{\hbar c \pi^2}{720 L^3} A$$

■ Assumptions

- plane parallel mirrors
- perfect reflection
- zero temperature
- perfectly flat surfaces



- Order of magnitude of the Casimir pressure

$$L = 1 \mu\text{m} \rightarrow \frac{F_{\text{Cas}}}{A} \approx 10^{-3} \text{ Pa}$$

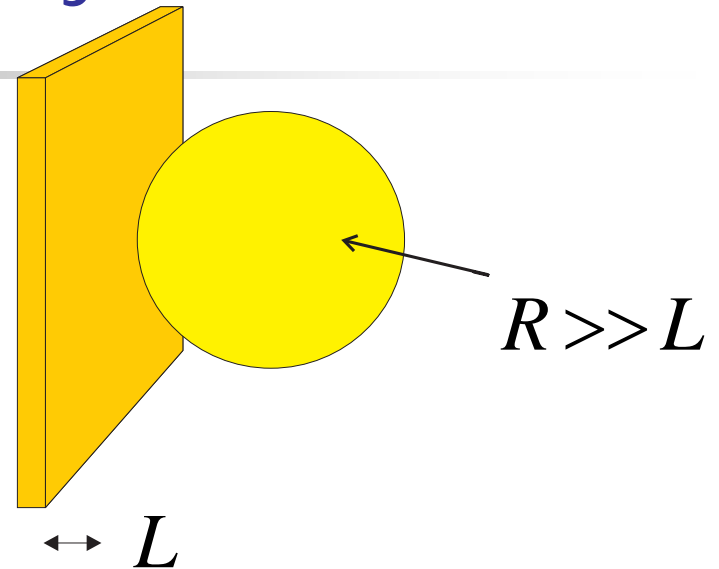
Plane-sphere geometry

- Proximity force approximation (PFA)

contributions of surface elements are added up independently

$$F_{PS} = \int d^2x \frac{F_{PP}(x)}{A}$$

$$F_{PS} = 2\pi R E_{PP}$$



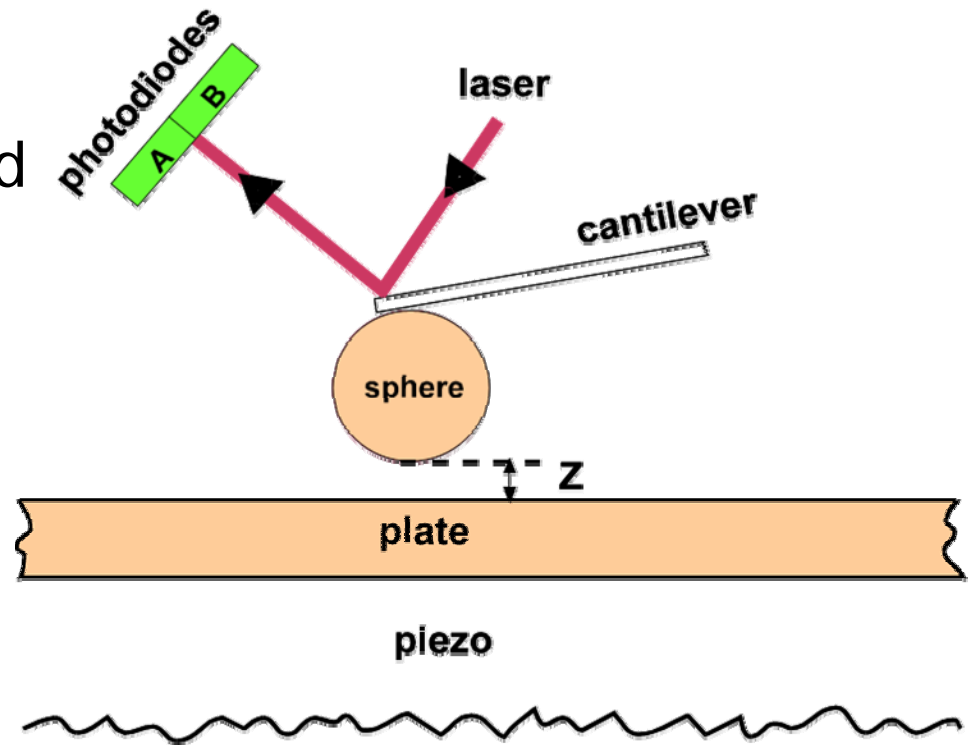
- BUT
- Casimir forces are not additive
- Approximation is valid for $R \gg L$

Mohideen et al. (Riverside)

Atomic force microscope (AFM)

- Plane-sphere geometry
- Sphere and plane covered with Au
- Distances 60-900nm
- Optical readout
- Experimental accuracy
~1% @ short distances

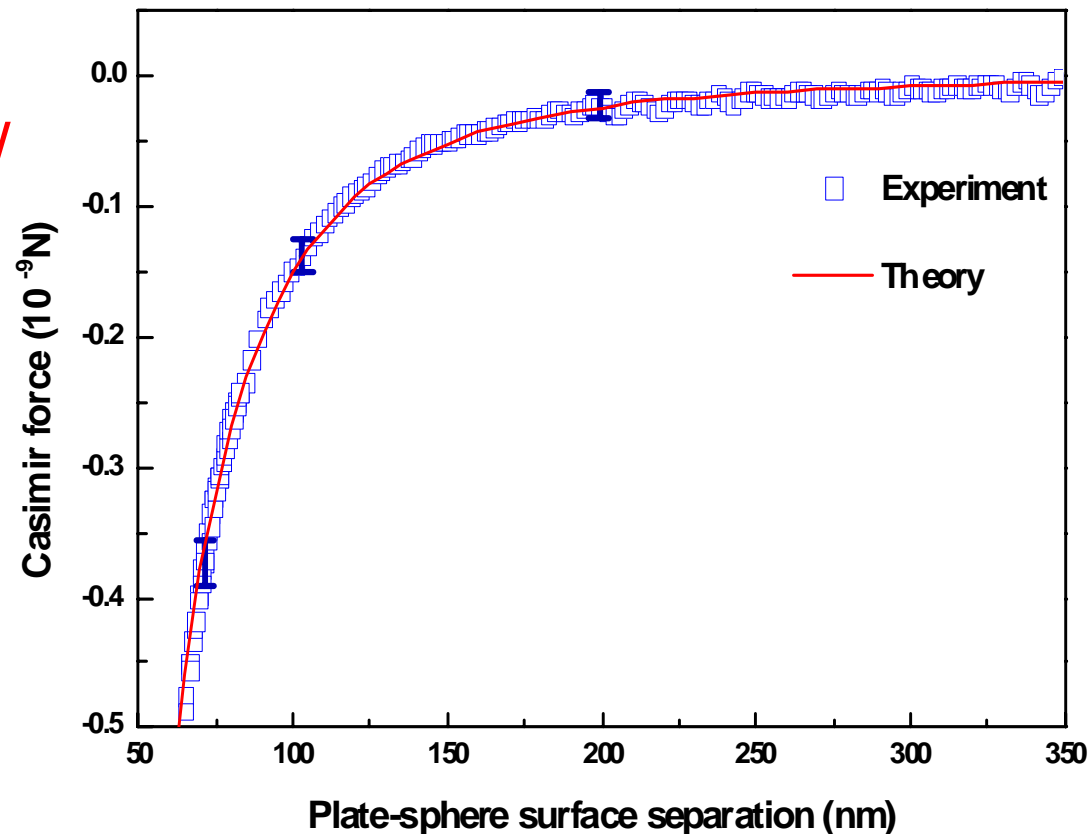
Courtesy U. Mohideen



Theory - experiment comparison

Agreement at $\sim\%$ level after having accounted for

- Plane-sphere geometry
- Imperfect reflection
- Room temperature (correction $< 1\%$)
- Surface roughness



Fischbach et al. (Purdue University)

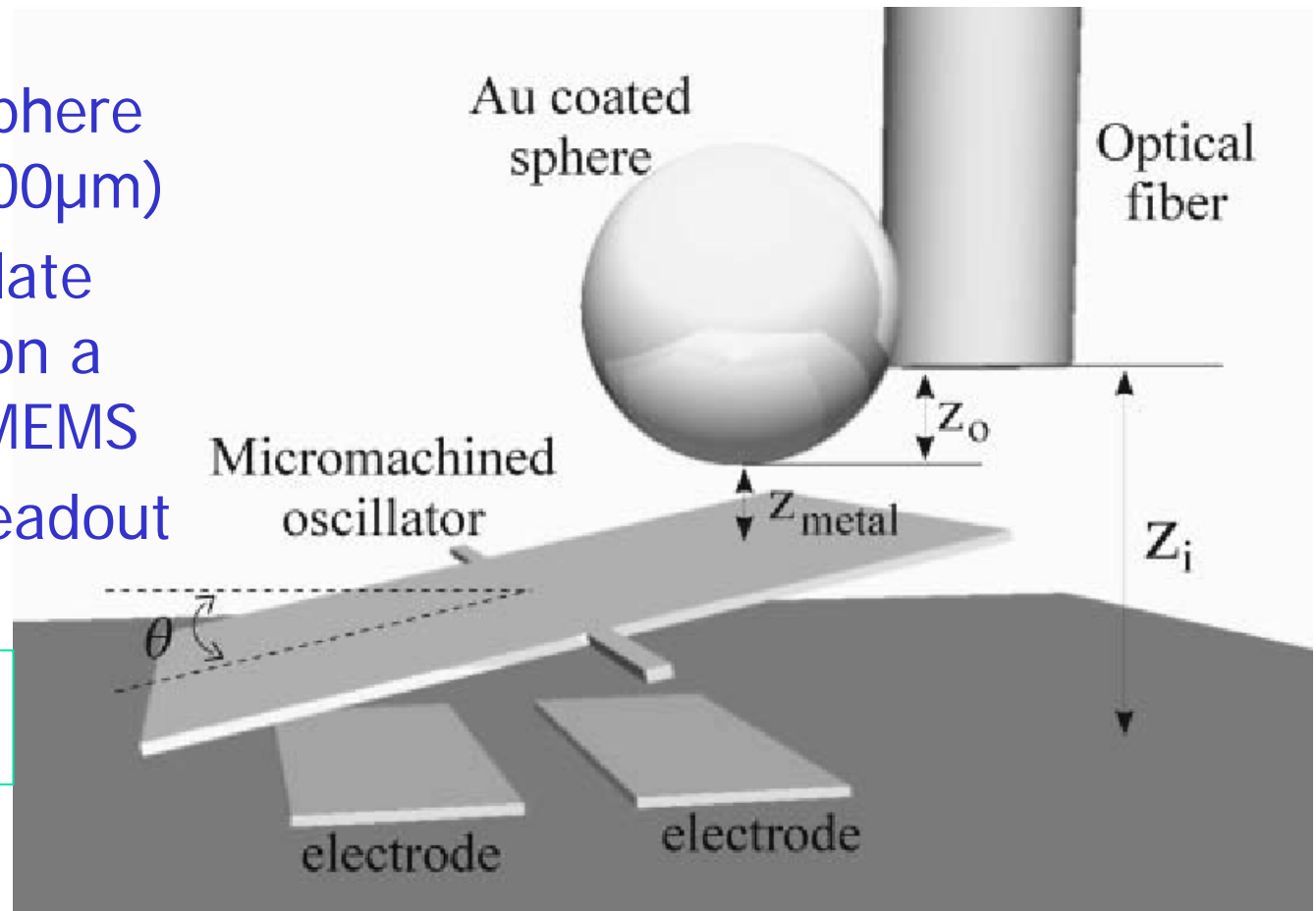
Au-coated sphere
($R=100-600\mu\text{m}$)

Cu-coated plate
mounted on a
torsional MEMS

Capacitive readout

Static or dynamic
measurements

$L=260-1200\text{nm}$



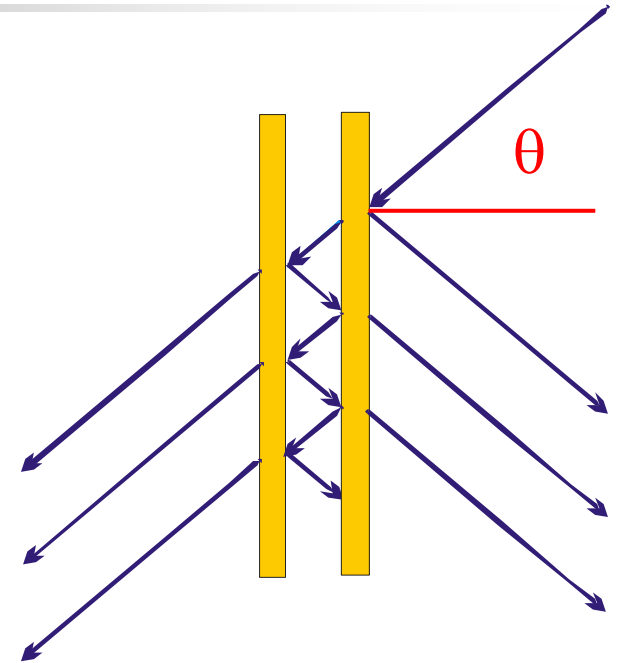
Origin of the Casimir Force

Vacuum radiation pressure

- outside the cavity : $\frac{\hbar\omega}{2} \cos^2\theta$
- inside the cavity : $\frac{\hbar\omega}{2} \cos^2\theta \times g(\omega)$

Spectral mode density :

$$g_k^p(\omega) = \frac{1 - \left| r_1^p(\omega) r_2^p(\omega) e^{2ik_z L} \right|^2}{\left| 1 - r_1^p(\omega) r_2^p(\omega) e^{2ik_z L} \right|^2}$$

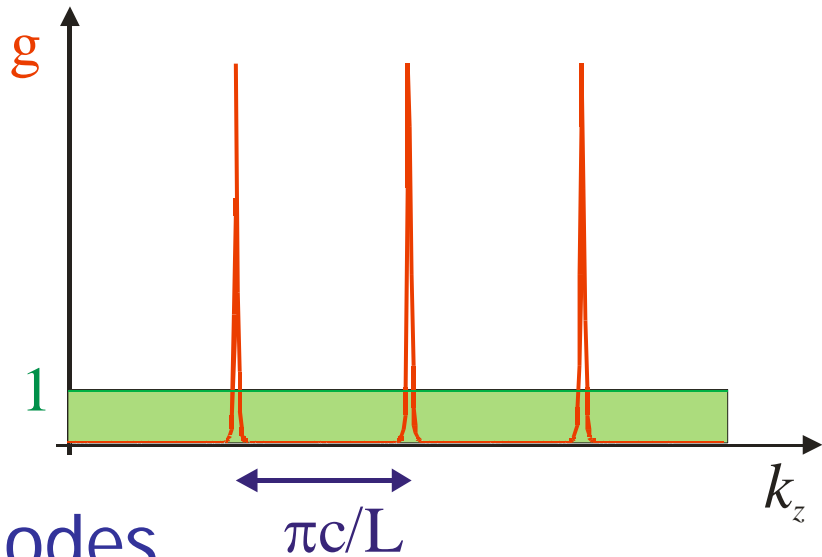


$$k_z = \frac{\omega}{c} \cos\theta$$

longitudinal wave vector

Mode density and Casimir force

- Cavity resonances
- Casimir force = integral over all field modes



$$F = A \sum_p \int \frac{d^2k}{4\pi^2} \int_0^\infty \frac{dk_z}{2\pi} \hbar \omega \cos^2 \Theta (1 - g_k^p(\omega)); \quad p = \text{TE, TM}$$

C. Genet, A. Lambrecht & S. Reynaud, Phys. Rev. A67 043811 (2003)

The force between metallic mirrors

■ Plasma model

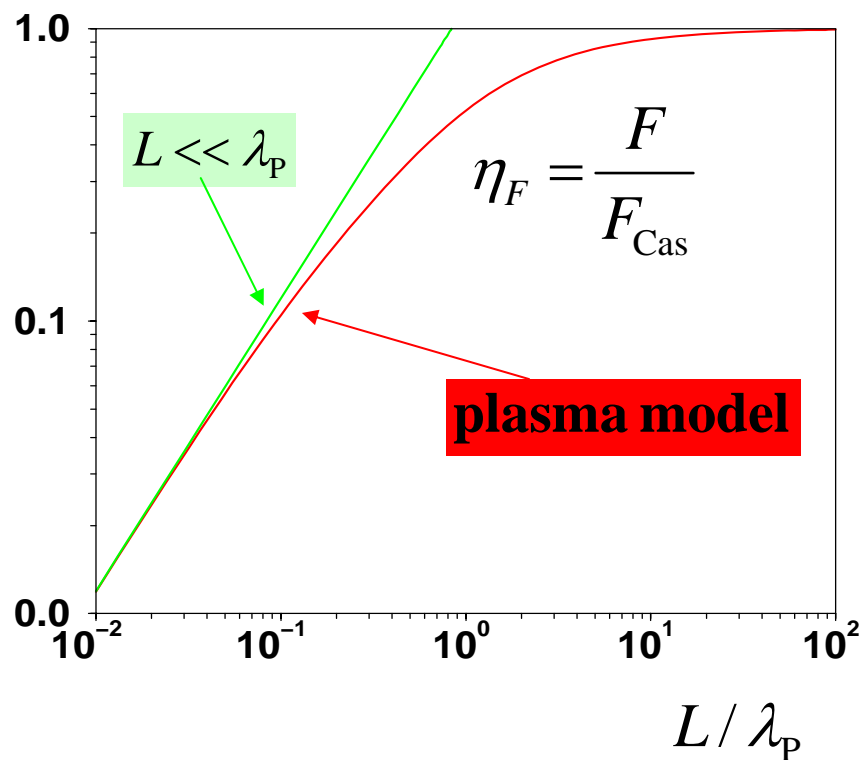
$$\varepsilon(\omega) = 1 - \frac{\omega_P^2}{\omega^2} \quad \omega_P = \frac{2\pi c}{\lambda_P}$$

Au: $\lambda_P \sim 137\text{nm}$

■ Reduction of the force

$$L \leq \lambda_P$$

$$F = \frac{\alpha L}{\lambda_P} F_{\text{Cas}} \propto \frac{1}{\lambda_P L^3}$$



Temperature correction

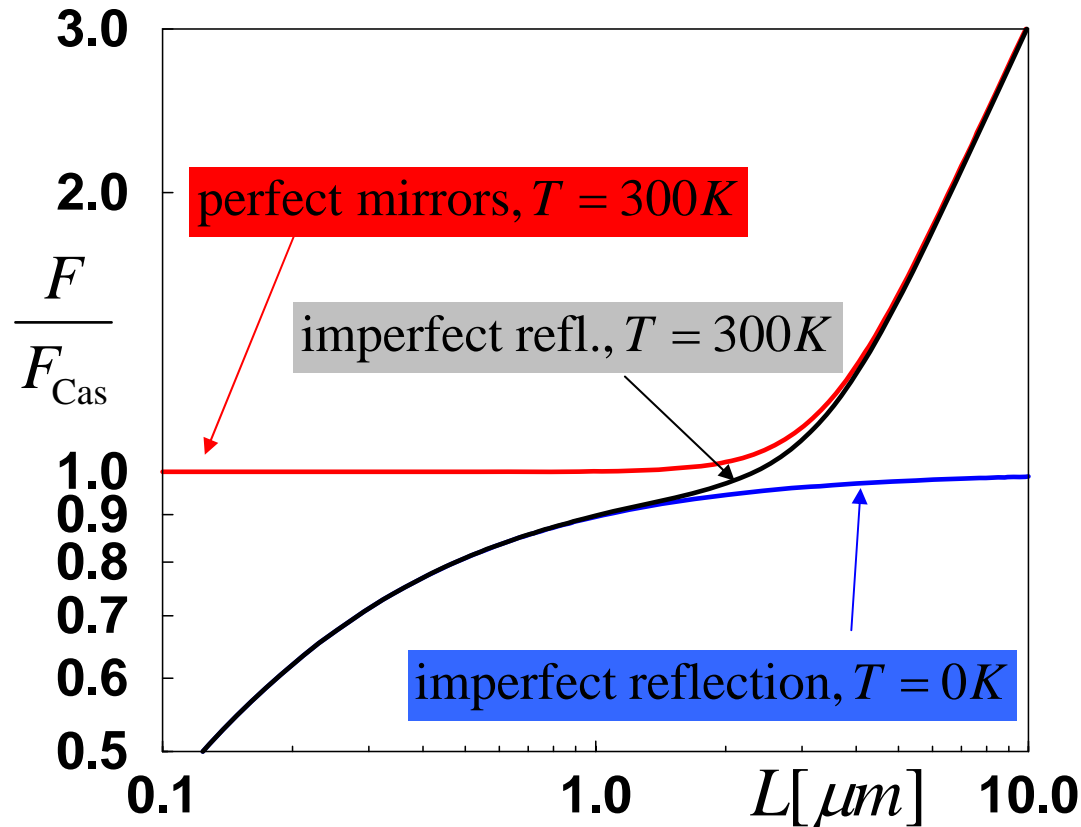
- Vacuum and thermal fluctuations in TD equilibrium

$$\frac{\hbar\omega}{2} + \frac{\hbar\omega}{e^{\hbar\omega/k_B T} - 1}$$

- $T=300\text{K}$

$$\lambda_T = \frac{\hbar c}{kT} \approx 7\ \mu\text{m}$$

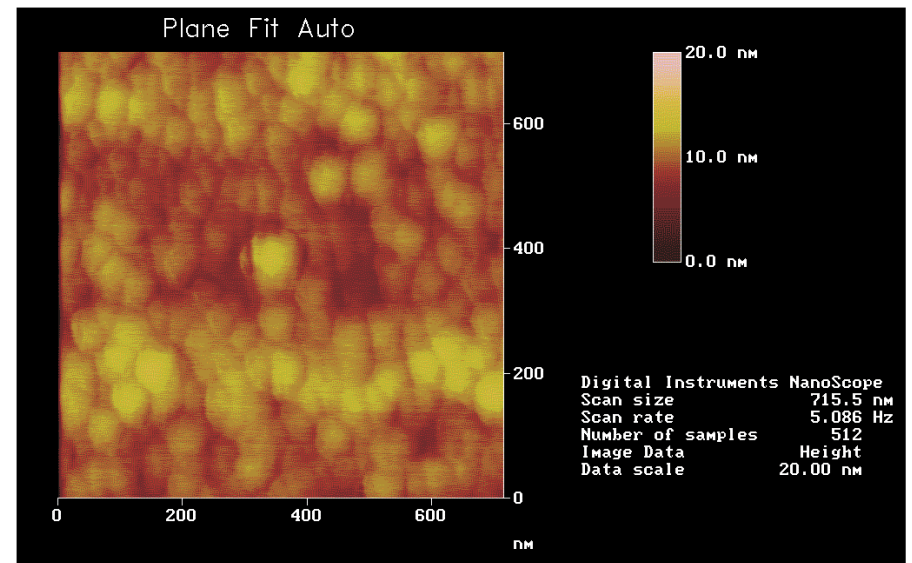
- Important at long distances



Surface state

- Surface roughness:
PFA and specular reflection
- Characteristic lengthscale $\lambda_c \gg L$

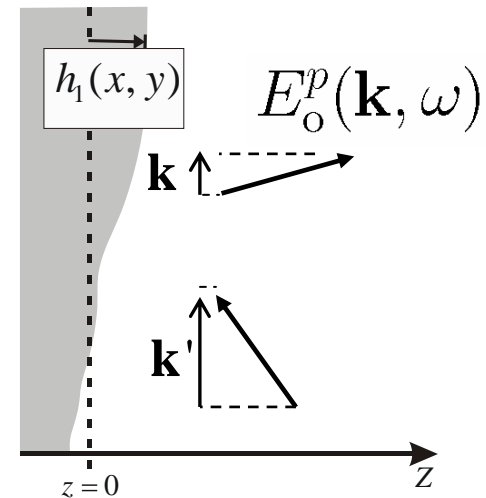
Courtesy U. Mohideen



P. Maia Neto, A. Lambrecht & S. Reynaud, EPL (2003) & (2005)

Surface state

- Non specular reflection: mixes wavevectors and polarizations
- Surface roughness correction: important at short distances and intertwined with finite reflectivity correction
- Violation of PFA measurable in lateral Casimir force



P. Maia Neto, A. Lambrecht & S. Reynaud, PRA 72, 012115 (2005)

R. Rodrigues, P. Maia Neto, A. Lambrecht & S. Reynaud, PRL. 96, 100402 (2006)



State of the art

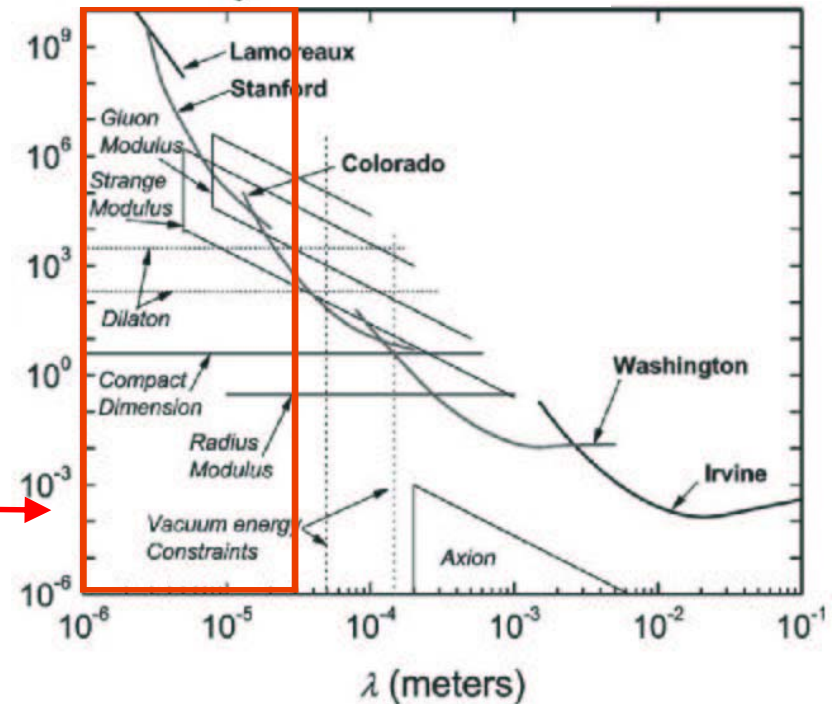
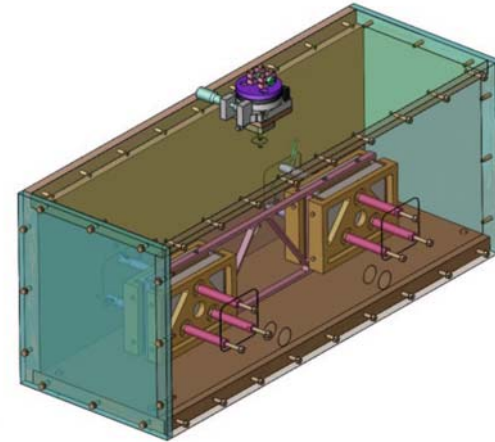
- The Casimir force is now measured with an experimental accuracy $\sim 1\%$
- Theory and experiment agree at the same level in the distance range $100\text{ nm} < L < 500\text{ nm}$
- Going beyond the 1% level

- Discussions are still going on for non zero T
- No experiments at distances $> 1\text{ }\mu\text{m}$
- New trends : NEMS, repulsive Casimir forces beyond PFA : lateral Casimir force
Casimir-Polder forces (BEC),
non-thermal-equilibrium effects
(cf. Mauro Antezza's talk),...

New Casimir force measurement

- Experiment with Valery Nesvizhevsky (ILL, Grenoble)
 - High precision torsion balance
 - Very high quality mirrors
 - Very good control of parallelism

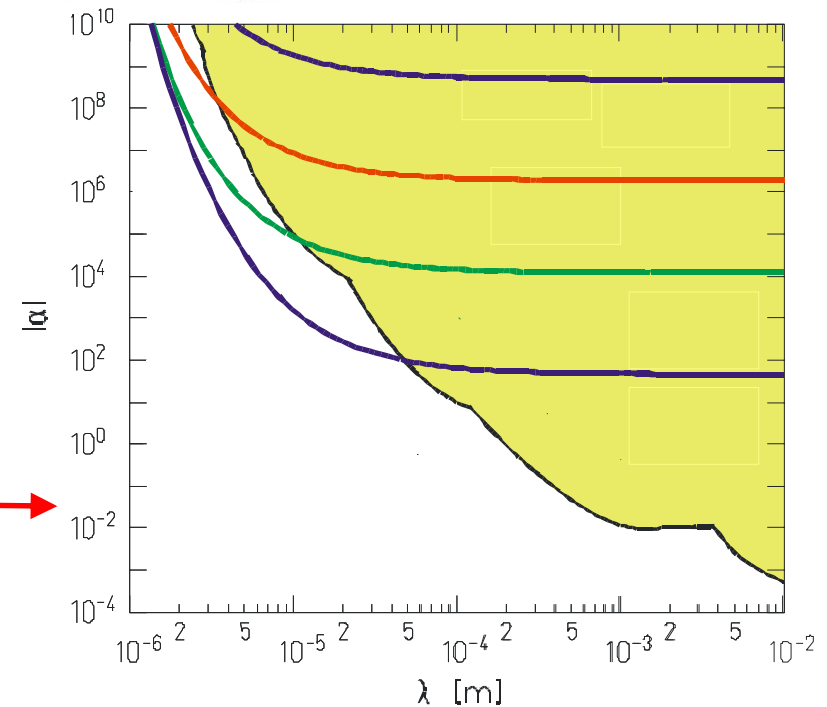
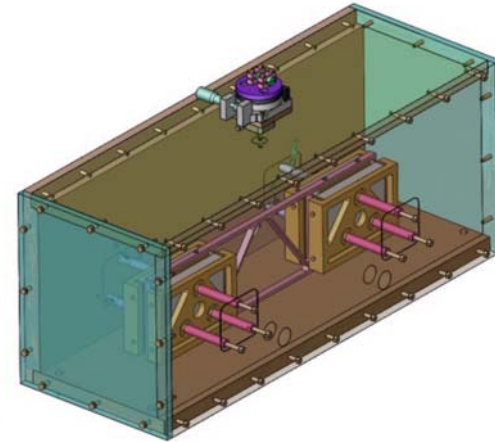
- Advantage in window around $10\mu\text{m}$ where a variety of models can be ruled out or confirmed



New Casimir force measurement

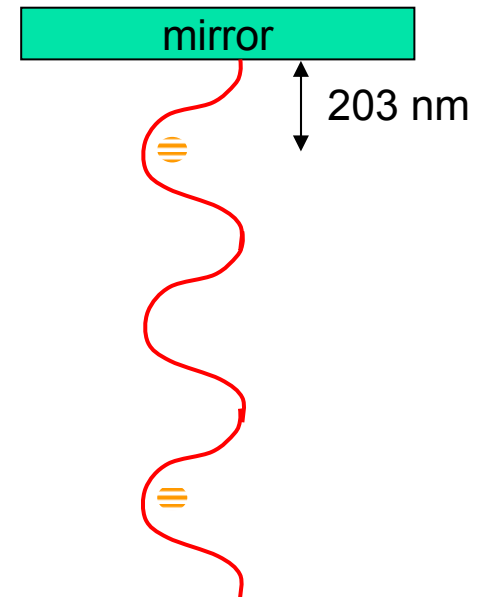
- Experiment with Valery Nesvizhevsky (ILL, Grenoble)
 - High precision torsion balance
 - Very high quality mirrors
 - Very good control of parallelism

- Expected new constraints for
 - 0.1 μm
 - 1 μm
 - 3 μm
 - 10 μm thickness of Au layer



Casimir Polder Force Using Cold Atoms in an Optical Lattice

- Atomic interferometer: coherent superposition between atomic states at different lattice sites
- Measuring the atom-surface interaction potential :
 - Casimir Polder interaction
 - Search for new interactions : improvement by 2 to 4 orders of magnitude



Systèmes de Référence Temps-Espace



SYRTE

P. Wolf, P. Lemonde, A. Lambrecht, S. Bize, A. Landragin, A. Clairon,
Proc. IEEE Freq. Control Symposium (2006); ArXiv:physics/0608021



Casimir Team



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