Structure formation

Standard lore: after photons decouple from baryons, perturbations overdensities continue to grow under gravity, eventually collapsing into virialized structures "(old" (non-velativistic) DM - small clumps form first, accrete to form larger

structures, "cosmic web"

"Hot" (relativistic) DM- free-streaming erases early small-scale structure, largest structures form first, then fragment - clusters

Neutrinos are HDM, so cannot be 100% (or large fraction) of DM. Limits on subdomment HDM (Archidiaceno et al M3), neutrinos (3 fermions) Zmvco.27 Warm DM- DM has non-negligible free-streaming length during structure formation, erases structure on v small scales, albeit not on scales lage enough to prevent galaxies from forming (an constrain by matter power spectrum max 6.67eV)

HDM should be at most O(1%)

The matter power spectrum Define S(F) = P(F)-P - factional density fluctuations Fourier transform:  $S(\vec{k}) = \frac{1}{(2\pi)^3} \int S(\vec{x}) e^{-i\vec{k}\cdot\vec{x}} d^3\vec{x}$ Power spectrum: P(k) = < 18(k) 12) - describes former in density enhancements at a given scale -SDSS galaxies k = comoving incose distance scale - corresponds to comoving scale ylyman-or forest of original mode that formed neffect of wom a given structure, not physical CMB Size of collapsed structure today k[Mpc]. (thermally compled to SM) while relationstic Warm DM induces cutoff at RFS ~ 5 Mpc-1 Hlozeke et al 12 crude estimate ( Tx) ( Tx) Simulation gives 50% suppression, of matter power at kiz ~ 6.5 h (mwom) !!! (-20m) -0.17 Vid et al 1306.2314 Strongest constraints on WDM come from "Lyman-ox forest" - distant quasas emit radiation, absorbed by clouds of hydrogen - can map matter overdensities at intermediate redshifts. Probes matter power spectrum at Z~2-6, scales as small as kn 10h/Mpc. Viel et al 1702. 01764, mx 25,3 keV

What could DM be? - Last time, briefly discussed BH OM - This time, consider possibility that DM represents 1 or more new particles Note no SM particles work- only neutral, stable particle is neutrino, & it is HDM (from last time: DM should be cold, stable & not interact too strongly) Statisting - Drit and the abcolutely - What is DM mass? - # Is it absolutely stable? If not, what is its lifetime? - How do we explain observed abundance (~Sx greater than baryonic matter)? DM mass scales: TeV Gev Mer PeV ev kev 1 3 generally new simple thermal window 10-21 eV non-thermal, generally nonthermal or if Hurma not pointlike relic" predictive window thermal = was once in thermal contact with SM (or at least attent) Regard DM as 10-21 eV-meV DM-SM interactions determine velic particle, can be regard DM as absorbed or abundance oscillating field, scattered on search for continuous tagets wave signals

Another kind of CMB limit: neff bounds Nucleosynthesis, CMB set constraints on the number of effective relativistiz degrees of freedom - affects energy density of radiation field, modifies the ABBRITHING Universe's expansion rate Pradiation = P8 + (3+ ANV) PV = P8 (1+ = (+) 4/3 neff)  $Neff = 3 \left[ \frac{11}{4} \left( \frac{Tv}{T} \right)^3 \right]^{4/3} \frac{4Nv}{1+3} \qquad \text{If neutrinos}$ If neutrino-photon decoupling is instantaneous, as discussed L> late-time ratio, last week, & etc become non-velativistic well after after neutrino decoupling decoupling, then TX= (+) 3TV at late times, In full calculation, (neff)SM = 3.046. From Planck (2015), (neff)observed = 3.15=0.23. neff = 3+ DNV -> Can constrain light DM directly - temperature of the universe at BBN B-1 MeV, if DM or something to which it couples is the tight, can be m tension w/ neff limits: Aneff # < 1 for BBN (1103.1261) Furthermore, even if DM is substantially colder than SM (allowating neff limits as the contribution to p scales as T+ for a relativistic species), DM decay annihilation that produces SM photons OR neutrinos after neutrino decoupling can change IV, also modifying neff. (See Berlin & Blinov 17 for a covert.) => Thermal DM is challenging below ~ MeV temperatures. At ~keV temperatures, matter limits

Consider evelution of DM number density in carly universe  
No annihilation: 
$$\frac{d}{dt}(na^3) = 0$$
  
 $\Rightarrow a^3 \frac{dn}{dt} + 3a^3 n \frac{da}{dt} = 0$   
 $\Rightarrow a^3 \frac{dn}{dt} + 3a^3 n \frac{da}{dt} = 0$   
 $\Rightarrow \frac{dn}{dt} + 3\frac{a}{n} n = 0$   
(M)  
With annihilation:  $\frac{dn}{dt} + 3Hn = -\frac{m^2}{2}(\sigma v)x2 + (n-independent from annihilation rote, DM production production 2 particles verwed production production  $\frac{2}{particles}$  verwed processes)  
In equilibrium, LHS=0,  $n = neq \Rightarrow = \langle \sigma v \rangle neq^2$   
 $\Rightarrow \frac{dn}{dt} + 3Hn = -\langle \sigma v \rangle [n^2 - neq^2]$   
Equilibrium density neq set by Beltzmann distribution  $\frac{1}{neq} - \frac{1}{neq} - \frac{1}{neq}$$ 

When 
$$\langle \sigma v r \rightarrow 0$$
, in evolves as  $\frac{1}{43}$   
When  $\langle \sigma v r \rangle$  is large, fires in exponentially close to neg  
Crossover when  $\langle \sigma v r n^2 - ttn$  i.e.  $n \langle \sigma v r - tt - v \rangle$  forese out  
inverse timescale  
timescale for expansion  
For full solution, solve Boltzmann equation including changing  
degrees of freedom, etc.  
But as an approximation, OK to define:  $Tf = temperature$  when  $n \langle \sigma v \rangle = H$   
 $xf = \frac{m_X}{Tf}$   
Materine glassing is comoving density at late times  
 $= (m_X)$  freeze-out = comoving density at freeze-out  
 $= (m_X)$  freeze-out = comoving equilibrium density at  
 $First$  case; bot reliz, freeze-out while relationic  $\int_{0}^{2T} \frac{1}{2} \sqrt{\frac{1}{2}} \sqrt{\frac{1}{2}} \frac{1}{2} \sqrt{\frac{1}{2}} \sqrt{\frac{1}{2}} \frac{1}{2} \sqrt{\frac{1}{2}} \frac{1}{2} \sqrt{\frac{1}{2}} \sqrt{\frac{1}{2}} \frac{1}{2} \sqrt{\frac{1}{2}} \sqrt{\frac{1}{2}} \sqrt{\frac{1}{2}} \frac{1}{2} \sqrt{\frac{1}{2}} \sqrt{\frac$ 

Second case: cold velic, freeze-out when non-velativistic At preezeout, H~ (mx T) 3/2 em/T Kov7 In radiation-dominated epoch, H2xpxT4 => TXJH xt-1/2 Write H= H(man) x-2, DC= m H(m) => H(m) 2cf -2~ (mx?) 3/2 2cf -3/2 e-2cf 2007 => e-xf = xf-1/2 Apprex solution  $\left(\frac{m\chi^{3}\langle\sigma\nu\rangle}{H(m)}\right)$  xf ~ ln  $\left(\frac{m\chi^{3}\langle\sigma\nu\rangle}{H(m)}\right)$ Note: only log dependence on mass, pasea A # density of DM the freezeart n~ mx x=3/2 e=x+~ H(m)xf=2/Kov7 ] both then scale ( ~ as is ignoring Note: # density of photons at freezeout entropy dumps ny~ Tp3~ mx3 =)  $\frac{n_X}{n_X} \sim \left[\frac{H(m_X)}{m_X}\right] \times \left(\frac{\chi f}{m_X}\right) \times \frac{1}{\sqrt{\sigma \sqrt{2}}} \int \frac{m_X n_X}{m_X} \int \frac{h(m_X)}{m_X} \frac{h(m_X)}{m_X} \frac{h(m_X)}{m_X} \int \frac{h(m_X)}{m_X} \frac{h(m_X)}{m_$ dependent of max

Thus late-time DM mass density. We hence 
$$\Omega_{c}$$
, has only log  
dependence on mass, mostly just  $\frac{1}{100} \leq \frac{1}{100}$ .  
To get number, note  $H(m_{\chi}) \sim \frac{m_{\chi}^2}{m_{PL}^2}$   
 $\Rightarrow \frac{m_{\chi}m_{\chi}}{m_{\chi}} \sim \frac{\chi f}{\zeta \sigma \sqrt{2}} \frac{1}{m_{PL}}$   
DM mass density  $\sim \frac{56}{20} \chi$  bargon mass density  $\sim \frac{5}{6} \text{ GeV} \chi$  bargon number  
 $\sim 5 \times m_{\chi} \times 5 \times 10^{-10} \text{ GeV}$   
 $m_{\chi} \sim 10^{19} \text{ GeV}$  bargon/phaten ratio  
To match data, we want  
 $\Rightarrow \frac{m_{\chi}m_{\chi}}{m_{\chi}} \sim \frac{2}{20} 3 \times 10^{-9} \text{ GeV} \sim \frac{2}{5} \times 10^{-19} \text{ GeV}^{-1}$   
 $\Rightarrow (\sigma \sqrt{2} \sim 2 f. \frac{3}{20} \times 10^{-9} \text{ GeV}^{-2}$   
 $= 10^{19} \text{ GeV} \sim 10^{10.5} \text{ GeV}^{-2}$   
 $= 10^{10.5} \text{ GeV}^{-2} \frac{10^{-19} \text{ GeV}^{-2}}{m_{\chi}} = 10^{2} \text{ guantity}$   
 $\Rightarrow (\sigma \sqrt{2} \sim 2 f. \frac{3}{20} \times 10^{-10.5} \text{ GeV}^{-2} \text{ GeV}^{-1} = \frac{10^{2} \text{ GeV}^{-1}}{m_{\chi}^{-2}} = \frac{10^{2} \text{ GeV}^{-1}}{m_{\chi}^{-2}} = \frac{10^{2} \text{ GeV}^{-2}}{m_{\chi}^{-2}} = \frac{10^{2} \text{ GeV}^{-1}}{m_{\chi}^{-2}} = \frac{10^{2} \text{ GeV}^{-1}}{m_{\chi}^{-2}} = \frac{10^{2} \text{ GeV}^{-2}}{m_{\chi}^{-2}} = \frac{10^{2} \text{ GeV}^{-1}}{m_{\chi}^{-2}} = \frac{10^{2} \text{ GeV}^{-1}}{m_{\chi}^{-1}} = \frac{10^{2} \text{ GeV}^{-1}}{m_{\chi}^{-1}}} = \frac{10^{2} \text{ GeV}^{-1}}{m_{\chi}^{-1}} = \frac{10^{2} \text{ GeV}^{-1}}{m_{\chi}^{-1}} = \frac{10^{2} \text{ GeV}^{-1}}{m_{\chi}^{-1}} = \frac{10^{2} \text{ GeV}^{-1}}{m_{$ 

Substituting this back in gives  

$$Corributing this back in gives
 $Corributing this back in gives
 $Corributing the careful calculation gives Corributing cm2 (15, nearly independent
of mass - "thermal relic cosis section".
We can write this in an even simpler way (that generalizes casily to
intoday annihilation with 172).
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As before, diff + 3 Hn = -Corributing (that generalizes casily to
intoday annihilation with 172).
As before, diff + 3 Hn = -Corributing (that generalizes casily to
interproduce of matter readiction equality, Tay, point prad (ignority bayons),
i.e. No max Tay - to But n ~ NP x (Tay) if Tay < Tr
(i.e. freezee at happens during readiction domination) - governed by
expansion.
So we can write inf mx ~ Tay Tf = nf ~ Tay mx2, taking TP ~ mmx
(setting xP ~ I)
Since during rediction domination Hr. The we have
 $Tay ~ (corr) NP - Corributing Corributing to have an interproduce to have have
 $Tay ~ (corrible GeV, mrc ~ 10^{19} GeV), so
Tay ~ (corrible GeV, mrc ~ 10^{19} GeV), so
(conductors finds mx2) = (corrible GeV) ~ (10^{-2})^2 Suggests TeV mass scale for
an under the first (1007-1010 mx2 100 TeV for
perturbicitive x.$$$$$$

Natural scale thus lines up with electroweak masses + couplings - suggestive, but basic mechanism works for - MeV-100 TeV DM. Can be realized in SUSY models, where DIM is lightest neutralino (wmo/higgsmo/bino admixture) - couples to \$55 SM via W12/Higgs, mass scale can be naturally 100s of GeV to TeVs DM stabilized by R-party: lightest R-odd particle (superpartner) cannot decay. e. a pure who DM has correct xsec for mx-3 TeV "higgsino " " " for mx ~ I TeV. (Note: freezeout can be more complicated in full SUSY model as other particles near-degenerate with DM may be involved.) Variations: - Velacity-dependent (ov) - p-wave (x v2) or sommerfield-enhanced (at or a tiz) - Coantibilation multiple species inholiced - Forbidden/ impeded DM - annihilation to kenematically forbidden state - SIMPS/n-body annihilation - more than 2-body processes important - Amiliation into dark sector, not SM directly - Scattering w/ SM decoupes before annihilation, ELDERS - Freeze-M - never reaches complete equilibrium, DM-SM interactions. Liete create abundance, don't deplet it

#### Dark Matter Lecture 2: Theoretical Models

#### Tracy Slatyer

ICTP Summer School on Cosmology Trieste 6 June 2016

# Goals (Lecture 2)

- Describe characteristics needed for a dark matter particle, and their implications:
  - Stabilization
  - Relic density
- Outline and explain the cosmology and key properties of the following scenarios:
  - Weakly Interacting Massive Particles (WIMPs)
  - Axions

# Recap from Lecture I

- The distribution and gravitational effects of dark matter can be a powerful probe of dark-matter properties and interactions, independent of any interaction with the known particles.
- We know that dark matter is:
  - Still around today, i.e. stable on timescales ~age of the universe (rotation curves)
  - "Collisionless" electrically neutral and interactions are fairly weak (Bullet Cluster)
  - "Cold" / slightly warm small free-streaming length in epoch of structure formation (matter power spectrum, Lyman-alpha forest)
- No particle in the Standard Model of particle physics (the "SM") matches these properties.

# Beyond the SM

- Photons, leptons, hadrons and W bosons shine too brightly / are charged.
- Z and Higgs bosons are neutral but short-lived.
- Neutrinos are neutral and stable, but too light. They would be hot dark matter - cannot comprise all DM.

#### ELEMENTARY PARTICLES





# Huge range of possibilities



# Stability

- One mystery is why dark matter is stable especially if it is heavy enough to be "cold" in the early universe
- Sets stringent limits on DM-SM interactions:
  - Easiest route: impose some kind of symmetry to prevent DM from decaying
  - Simplest example is a new kind of "parity" - Z<sub>2</sub> discrete symmetry, forces coupling to SM fields to involve pairs of DM particles.
  - Many more examples!



# The dark matter abundance

 Any DM model must explain the abundance of dark matter at the epoch of last scattering, precisely measured (from the CMB) to be:

 $\Omega_c h^2 = 0.1186 \pm 0.0020$   $h = H_0 / (100 \text{km/s/Mpc}) = 0.6781 \pm 0.0092$ 

Q:THERMAL OR NON-THERMAL?

Was the dark matter in thermal equilibrium with the Standard Model during the radiation-dominated epoch? THERMAL NON-THERMAL

Explain how the early abundance of dark matter was depleted -Asymmetric: small asymmetry between dark matter and antiparticle sets final abundance -Symmetric: interactions set final abundance Explain how the required amount of dark matter was produced
-Initial condition from reheating?
-Misalignment mechanism
-Phase transition

-Thermal parent - interactions with state in thermal equilibrium determine its abundance Weakly Interacting Massive Particles (WIMPs)

#### Thermal abundance

- Suppose dark matter:
  - can annihilate to Standard Model particles
  - was at some point kept in thermal equilibrium with the Standard Model by annihilation



#### Thermal freezeout

 In the early universe, let the DM particle be thermally coupled to the SM. Can annihilate to SM particles, or SM particles can collide and produce it.

 $\chi\chi\leftrightarrow \mathrm{SM}\,\mathrm{SM}$  (1)

 Temperature(universe) < particle mass => can still annihilate, but can't be produced.

 $\chi \chi \to \text{SMSM}$   $\chi \chi \nleftrightarrow \text{SMSM}$ (2)

 Abundance falls exponentially, cut off when timescale for annihilation ~ Hubble time. The *comoving* dark matter density then <u>freezes out</u>.



So (known) late-time density is set by annihilation rate.

 $\langle \sigma v \rangle \sim 3 \times 10^{-26} \mathrm{cm}^3/\mathrm{s} \sim \pi \alpha^2 / (100 \,\mathrm{GeV})^2$  (3)

#### Outline of calculation

- Ingredients: annihilation rate for identical particles given by annihilations / dt / dV =  $n^2 \langle \sigma v \rangle / 2$
- Boltzmann equation:

$$\frac{dn}{dt} + 3Hn = -\langle \sigma v \rangle \left[ n^2 - n_{\rm eq}^2 \right]$$

• Equilibrium density (Boltzmann distribution):

$$n_{\rm eq} = g \left(\frac{mT}{2\pi}\right)^{3/2} e^{-m/T}$$

• Temperature of universe (assume radiation domination):  $H^2 \propto \rho \propto T^4 \Rightarrow T \propto \sqrt{H} \propto t^{-1/2}$ 

#### Estimating freezeout

- For precision solution, can solve this differential equation numerically
- But we can get a simple estimate of important quantities analytically.
  - Freezeout occurs when timescale for expansion ~ timescale for collision:  $H \sim n \langle \sigma v \rangle$
  - Up to freezeout, n~n<sub>eq</sub>, so we require  $H \sim g(mT/2\pi)^{3/2} e^{-m/T} \langle \sigma v \rangle$
- Defining x=m/T, we have  $H(m)x^{-2} = g(m^2/2\pi)^{3/2}x^{-3/2}e^{-x}\langle\sigma v\rangle^{3/2}$

• Transcendental equation  $e^{-x} = x^{-1/2}/C$  has approximate solution

$$x \sim \ln C \sim \ln \left( g (m^2/2\pi)^{3/2} \langle \sigma v \rangle / H(m) \right)$$

note: only depends on m and cross section logarithmically

# Estimating freezeout II

• Abundance at freeze-out:

 $n \sim g(m^2/2\pi)^{3/2} x^{-3/2} e^{-x} \sim H(m) x_f^{-2}/\langle \sigma v \rangle$ 

• For comparison, photon abundance at freezeout:

$$n_{\gamma} \sim T^3 \sim m^3 / x_f^3 \Rightarrow n / n_{\gamma} \sim \left(H(m) / m^2\right) \left(x_f / m\right) / \langle \sigma v \rangle$$

To match measurements of DM mass density from CMB (comparable to critical density and baryon density), DM number density ~9 orders of magnitude below photon number density if m<sub>DM</sub> = m<sub>proton</sub>. At higher DM mass, number density must be lower (keeping mass density = mass x number density fixed).

$$H(m) \sim m^2/m_{\rm Pl} \Rightarrow 10^{-9} {\rm GeV} m_{\rm Pl} \sim x_f/\langle \sigma v \rangle \Rightarrow \langle \sigma v \rangle \sim x_f 10^{-10} {\rm GeV}^{-2}$$

 Taking x<sub>f</sub> ~ I as a first approximation (since x<sub>f</sub> is a log quantity, can't be too large) gives us a first estimate for cross section.

#### Cross section & mass scale

- Let us estimate  $\langle \sigma v \rangle \sim \alpha^2/m^2, \, \alpha \sim 10^{-2}$
- Then from first estimate for cross section, natural mass scale is m~1000 GeV.
- Plug this back into formula for x<sub>f</sub>; we find x<sub>f</sub>~25.  $x_f \sim \ln \left( g/(2\pi)^{3/2} m m_{\rm Pl} \langle \sigma v \rangle \right)$
- This gives us a better cross section estimate:  $\langle \sigma v \rangle \sim 2 \times 10^{-9} \text{GeV}^{-2} \approx 2 \times 10^{-26} \text{cm}^3/\text{s}$
- Corresponds to mass scale of a few hundred GeV, details depending on coupling and prefactors.

#### The WIMP miracle

- In a thermal scenario, weak-scale annihilation cross section naturally yields the observed abundance of dark matter.
- Suggestive of new physics not too far above the weak scale.
- Stable WIMPs automatically occur in many scenarios for physics beyond the Standard Model, in particular in supersymmetry.
- However, simplest scenarios are challenged by lack of detection on other fronts; often need some extra ingredient to get the correct abundance.



# Supersymmetry (SUSY)

- Most famous dark matter candidate is the Lightest Supersymmetric Particle (LSP).
- In supersymmetric theories, every particle has a <u>superpartner</u>.
- Fermions have boson superpartners and vice versa.
- These additional particles cancel what would otherwise be very large predicted contributions to the Higgs mass - motivated independently of DM.
- For an in-depth introduction to SUSY, see e.g. Martin hep-ph/9709356.

Particle Fever D.E. Kaplan







# Supersymmetry (II)

- In <u>unbroken</u> supersymmetry, particles and superpartners have same mass and closely related interactions.
- This symmetry must be broken as clearly superpartners do not have mass equal to their (known) counterparts!
- But if we break it "softly", while masses are separated, interactions remain fixed by supersymmetry.
- SUSY theories also inherit huge structure from the Standard Model.
- Consequently many quantities in SUSY theories can be calculated from just the masses of the superpartners.



Example of interactions related by supersymmetry - taken from talk by Tim Tait, August '15

# R-parity

- These SUSY interactions naively imply some peculiar behavior!
- For example, they could make protons decay quickly:



- This is pretty clearly not observed (experimental limit: lifetime >10 years).
- Usual approach is to impose a symmetry called R-parity, so the superpartners can only couple in pairs to the ordinary particles.
  - Superpartners have R-parity = I
  - Ordinary particles have R-parity = +1
  - Product of R-parities before and after an interaction must be conserved

#### The LSP

- But then lightest particle with R-parity odd (i.e. = -1) cannot decay
  - can't produce any other particles with R-parity I (kinematically forbidden)
  - can't decay just to SM particles (violates R-parity)
- Avoiding proton decay gives us a stable DM candidate!
- Furthermore, any R-parity-odd particles in the early universe must eventually produce stable R-parity-odd particles by decays.
- But does the LSP satisfy other requirements for DM?

#### The LSP as dark matter

- First question: is it neutral?
- SUSY models in general have many parameters and the model of supersymmetry breaking matters.
- For a given model, we can compute the spectrum of superpartners, identify the lightest particle, and check its properties.



#### Neutralino dark matter

- Neutral fermionic superpartners = superpartners of the neutral gauge bosons
  - Higgsino = superpartner of the Higgs(es)
  - Wino = corresponds to electrically neutral gauge boson of electroweak SU(2) gauge group (there is also a "chargino" which corresponds to the charged components)
  - Bino = corresponds to gauge boson of the electroweak U(I) gauge group
- In general the physical states (of definite mass) correspond to mixtures of these - details depend on the model
- The lowest-mass such admixture determines the interactions of the DM candidate

# The problem with binos

- A common (not universal) situation is for the LSP to behave mostly like a bino (with small wino/higgsino components)
  - Interactions with SM then mostly involve the scalar partners of the fermions ("sfermions")
  - Main annihilation channels for binos produce SM fermions, via interactions with sfermions.
  - But these annihilations are <u>suppressed</u> by m<sub>f</sub><sup>2</sup>/m<sub>DM</sub><sup>2</sup> smaller than "typical" weak-scale cross section.
- Low annihilation cross sections mean there is typically <u>too much</u> <u>dark matter</u> in the late universe - WIMP miracle doesn't hold up, despite weak-scale masses, due to parametric suppression.

# Relic density from SUSY

- Four standard ways to fix this problem in mSUGRA, simplified example SUSY model:
  - "bulk region" make sfermions light (larger annihilation cross sections)
  - "focus point" reduce bino fraction so other, unsuppressed annihilation modes dominate
  - "funnel region" annihilation through Higgs, near twice mass of DM, gives alternative, unsuppressed decay mode
  - "coannihilation region" DM is not the only particle involved in freeze-out, need to include interactions with other neardegenerate particles



#### Credit to Tim Tait for these slides



#### Hunting the WIMP



- Beyond motivations from SUSY and thermal freezeout, WIMPs are popular candidates because they have many observable signatures.
- Indirect detection: look for SM particles electrons/positrons, photons, neutrinos, protons/antiprotons produced in WIMP collisions or decay, with sensitive telescopes.
- Direct detection: look for nuclear recoils from WIMPs hitting SM particles with sensitive underground detectors.
- Colliders: produce DM particles in high-energy collisions and look for missing energy (e.g. at the LHC), or search for new light dark-sector particles.

#### Axion dark matter

# The strong CP problem

 The Standard Model Lagrangian, describing all known particle interactions, in principle should have a term of the form:

$$\mathcal{L}_{\theta} = \frac{\theta}{16\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu} \quad \text{gluon field strength}$$

- A term like this can be generated by CP violation elsewhere in the Standard Model, in the terms describing the quarks - no reason for it to vanish.
- But this term induces a neutron electric dipole moment:  $d_n = 5.2 \times 10^{-16} \mathrm{e\,cm}$
- Experimentally, we know that:  $d_n < 3 \times 10^{-26} \mathrm{e\,cm} \qquad \Rightarrow \theta \lesssim 10^{-10}$
- Why is this value so small?

# The axion proposal

- Replace the parameter  $\theta$  by a dynamical field, call it (by convention)  $a/f_a$  where a is the field and  $1/f_a$  a coupling.
- Now we just need to explain why a would evolve toward a very small value.
- But the energy stored in this field depends on the value of a potential energy changes as a evolves.
- We can work out this effective potential (I won't give the calculation here - see e.g. Dine's TASI lectures hep-ph/0011376 for much more detail on the strong CP problem) and find:

$$V(a) = -m_{\pi}^{2} f_{\pi}^{2} \frac{\sqrt{m_{u} m_{d}}}{m_{u} + m_{d}} \cos(a/f_{a})$$

pion decay constant  $m_\pi pprox 135 {
m MeV}$  pion mass

 $f_{\pi} \approx 93 \mathrm{MeV}$ 

#### The axion potential

- Field should evolve toward small values of this potential.
- Minima occur at a/f<sub>a</sub> = 2nπ; let's look at n=0.
- The potential is parabolic coefficient of  $a^2$  term gives axion mass.



$$V(a) = m_{\pi}^{2} f_{\pi}^{2} \frac{\sqrt{m_{u}m_{d}}}{m_{u} + m_{d}} + \frac{1}{2} a^{2} \left(\frac{f_{\pi}}{f_{a}}\right)^{2} m_{\pi}^{2} \frac{\sqrt{m_{u}m_{d}}}{m_{u} + m_{d}} + \mathcal{O}(a^{4})$$
$$m_{a} = \frac{f_{\pi}m_{\pi}}{f_{a}} \left(\frac{m_{u}m_{d}}{(m_{u} + m_{d})^{2}}\right)^{1/4} \approx 0.6 \text{meV}\left(\frac{10^{10}\text{GeV}}{f_{a}}\right)$$

# Axion properties

- Axion coupling to Standard Model fields is controlled by the coupling f<sub>a</sub>, although exact couplings depend on details of model.
  - "DFSZ axion" axion couples to photons, gluons, leptons, quarks
  - "KSVZ axion / hadronic axion" axion couples to photons and gluons, but at lowest order no coupling to leptons or light quarks
- Axion mass is inversely proportional to their coupling to Standard Model fields - weakly coupled axions can be <u>very</u> light.
- One might think this makes them poor DM candidates too hot?

#### Thermal axions

- Coupling for axions can be very weak
  - In contrast to WIMPs, question is not "when did they fall out of equilibrium" but "were they ever in equilibrium"?
- Axions produced in early universe by interactions of photons, pions
- Axions can also decay and are produced singly, not in pairs (no symmetry keeping them stable)
  - Need to check lifetime is >> age of universe
  - Solve Boltzmann equation including decay + all production processes

# Thermal axions as hot dark matter

- Timescale for decay to photons is approximately given by: τ ~ 10<sup>24</sup>s (<sup>m<sub>A</sub></sup>/<sub>eV</sub>)<sup>-5</sup>

   Age of universe ~ 10<sup>10</sup> yr ~ π x 10<sup>17</sup> s => for axions to be
- Age of universe ~ 10<sup>10</sup> yr ~ π x 10<sup>17</sup> s => for axions to be around today, must be lighter than ~20 eV (unless decay suppressed in specific model)
  - Side note: at axion masses between about 20 eV and 300 keV, the photons from this process would disrupt nucleosynthesis!
- Solving Boltzmann equation, axions could attain thermal equilibrium if  $m_a > 10^{-3} 10^{-2} \text{ eV}$
- In this case, very roughly, fraction of critical density in axions:  $\Omega_{axions} \sim O\left(\frac{m_a}{100 eV}\right)$ hot dark matter - needs to be small fraction of total DM  $m_a < I eV$  is OK

# Non-thermal axions as cold dark matter

- But what if axions never equilibrate with SM?
- Sufficiently cold, light axions behave like a classical scalar field, evolving in axion potential - not individual particles
  - Q: How does the field evolve?
  - A: If initially displaced from minimum of potential (by some "misalignment angle"), must "roll" toward that minimum





# An evolving scalar field

 $\frac{d^2a}{dt^2} + 3H\frac{da}{dt} + m_a^2 a = 0$  equations of motion for scalar field in FRW note here a = axion field, not scale factor describes shape of potential near minimum

- For  $m_a << H$ , approximate solution with da/dt = 0 field does not evolve
- For m<sub>a</sub> > H, field begins to oscillate in potential like simple harmonic oscillator with H-dependent friction term ("Hubble friction"). For large t solution has approximate form:

 $a(t) = \Theta_0 f(t) \cos(m_a t) \qquad \mbox{f(t) slowly varying compared to oscillations} \\ \mbox{misalignment angle}$ 

- Solving for f(t) we find that in both radiation and matter-dominated epochs,
   f(t) scales like I/(scale factor)<sup>3/2</sup>.
- Energy density stored in axion field falls off like f(t)<sup>2</sup> ~ I/(scale factor)<sup>3</sup>. Same behavior as matter can act as cold dark matter.

# Axion relic density

- Careful relic density calculation requires solving equation of motion including temperature dependence of axion mass, QCD phase transition, etc.
- Fraction of critical density:  $\Omega_{\text{axions}} \approx \Omega_{\text{DM}} \Theta_0^2 \left(\frac{f_a}{5 \times 10^{11} \text{GeV}}\right)^{1.184}$
- Lighter axions = higher  $f_a$  = more weakly coupled = larger relic density
- Relic density can always be suppressed by small initial misalignment angle
- But misalignment angle cannot be much larger than 1 axions must have  $f_a$  of order 10<sup>11</sup> GeV or higher ( $m_a \sim 0.1$  meV or smaller) to be all the DM.

#### Axions and inflation

#### • What value should we expect the misalignment angle to take?

- If axions are produced / misalignment angle is set only <u>after</u> inflation, i.e. H<sub>I</sub> >> f<sub>a</sub>, different patches of cosmos likely have different misalignment angles - take average of random sample
- If misalignment angle is set (in patches) <u>before</u> inflation, each such patch gets blown up at inflation everywhere in our Hubble volume should have same angle
  - "anthropic axion"?

#### Baer '15 (1510.07501)



 $H_I$  = Hubble scale of inflation

There are stringent constraints on scenarios where axion is all the DM and the energy scale of inflation is high - see Hertzberg, Tegmark & Wilczek '08

Learning about inflation may tell us about axions! (or vice versa)

# Searching for axions

- Main observable property of axions (except possibly for gravitational effects) is their coupling to the photon
- Axions can convert <u>into</u> photons in the presence of a magnetic field
- Axions interact much more weakly than photons - can carry energy through regions where photons would be absorbed
  - Can induce strong B-field, look for signs of axion production
  - Or study astrophysical systems where photon absorption is high

axion-photon interaction in presence of magnetic field

$$G_{a\gamma\gamma}aF^{\mu\nu}\tilde{F}_{\mu\nu} = G_{a\gamma\gamma}a\vec{E}\cdot\vec{E}$$



# Summary

- We have discussed the basic properties and cosmology of two major categories of DM models
  - Weakly Interacting Massive Particles (WIMPs)
  - axions
- These furnish examples of non-thermal vs thermal production of the observed relic density
- Very different mass scales (<meV vs GeV-TeV)
- Very different couplings to known particles + detection methods (to be discussed in more depth in later lectures)
- These are not all-encompassing examples! There are (many) models which don't fit into either category - but these two broad scenarios are most popular, and give a sense of the scope of possibilities.