

Jet physics

LECTURE PLAN

① COLLIDER PHENOMENOLOGY

- COLLIDING PARTICLES
- PARTON-MODEL FOR THE DRELL-YAN PROCESS
- BREIT-WIGNER & NWA

② QUANTUM CHROMO DYNAMICS

- A REVIEW OF QCD
- RADIATIVE CORRECTIONS to DY
- DGLAP EVOLUTION

③ RESUMMATION

- SOFT-COLLINEAR FACTORISATION,IRC SAFETY
- THE TRANSVERSE MOMENTUM OF THE Z BOSON

④ JET PHYSICS

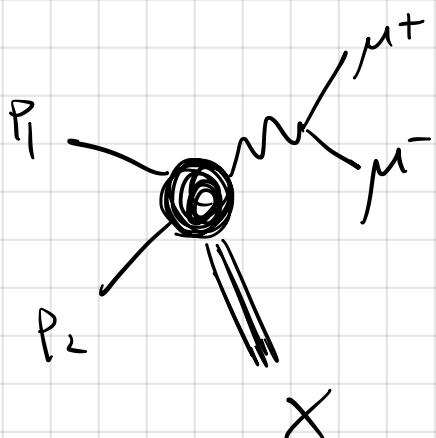
- WHY SETS?
- JET DEFINITIONS

⑤ JET SUBSTRUCTURE

- GROOMING and TAGGING
- MACHINE LEARNING (briefly)

AN INTRODUCTION TO SETS

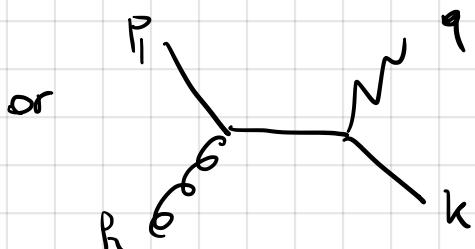
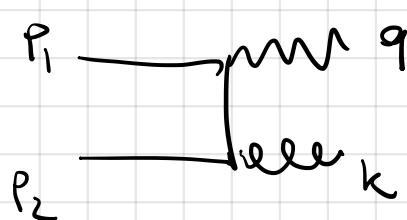
- In the past lecture we've seen that we can study QCD radiation by looking at $\pm q_T$



- we would like to study X more directly.

We expect X to be at high energy a collection of partons, that fragment into hadrons (mostly pions)

- What is the perturbative description of X ?
- Does it make sense? ie Can we take $O(\text{parton}) \simeq O(\text{hadrons})$
- Let's try. At $O(\alpha_s)$ this is pretty straightforward:



- X is either a quark or a gluon.
- its kinematic distributions are strictly related to the ones of the Z boson.

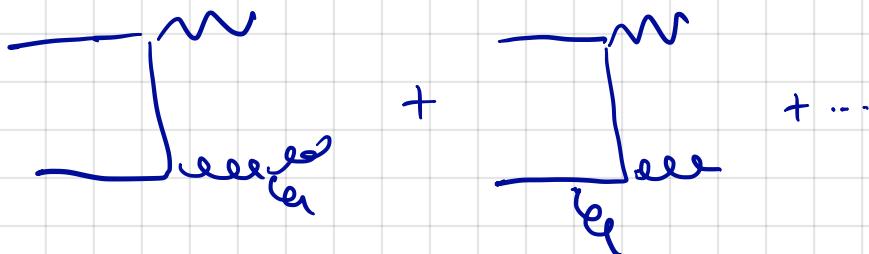
• At $\mathcal{O}(\alpha_s^2)$ we have

real emissions : 2 partons

virtual corrections: 1 parton + 1 loop

- Can we compute the x-section for $2+2$ partons?
(yes, I know we cannot measure partons, if we can compute it, we could relate it to a hadron-level obs.)

eq. $Z + q + q$

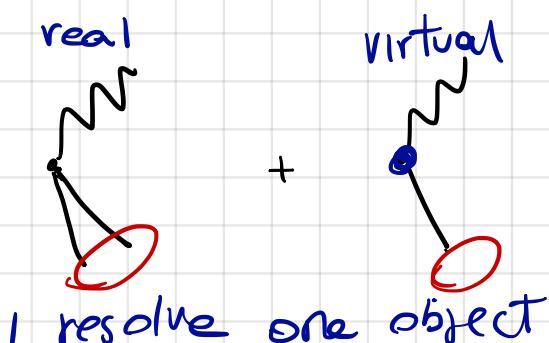


- we expect ISR coll. sing to be absorbed by PDFs and FSR to cancel against ... VIRTUAL corrections - but these do not contribute to $Z+q+q$.

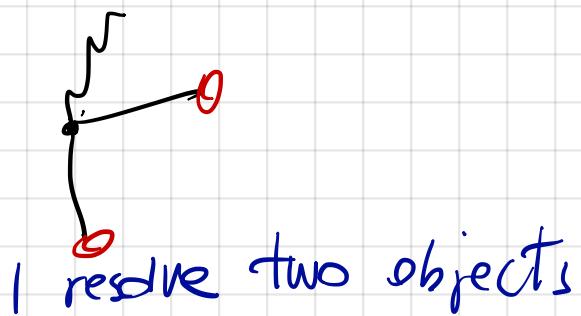
so, we CANNOT compute the cross-section to produce

$Z+2$ partons in pert. theory : it diverges!

- We need to be a little more inclusive.



or



- If I have two hard emissions away from sing. limits, I resolve two objects
- If the two emissions are near a sing. conf., I treat them as one object, together with the virtual corrections and I resolve one object.
- . These "objects" are called **JETS** and are the closest thing to the concept of partons ... but useful!

. Why are they called jets?

remember that in QCD emissions are enhanced at small angles: $\propto \frac{d\sigma}{d\Omega} \propto p(\tau)$



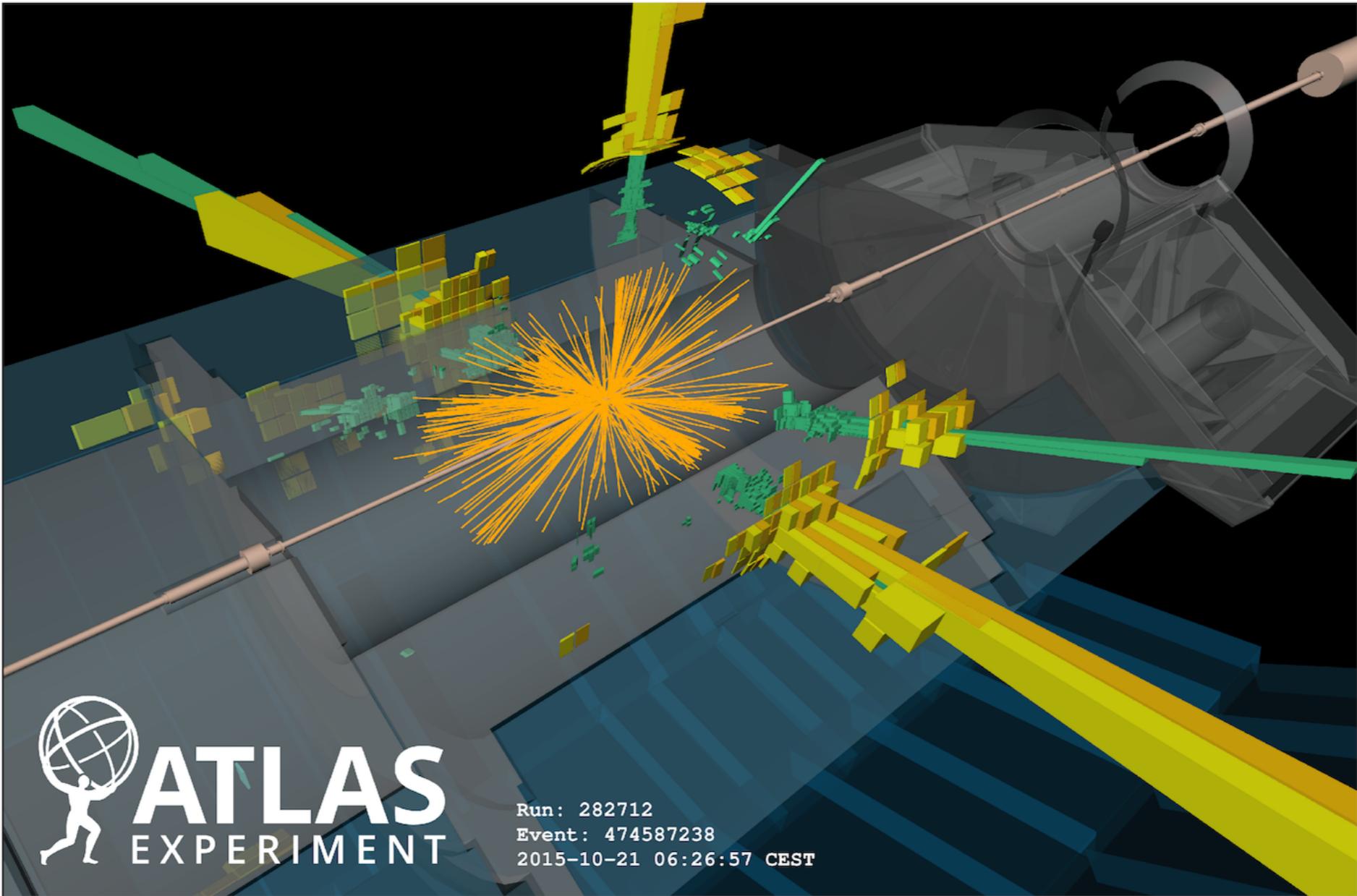
→ radiation is collimated along hard directions

→ partons eventually hadronize but we can still talk about jets.

→ jet formation is an experimental evidence of QCD!

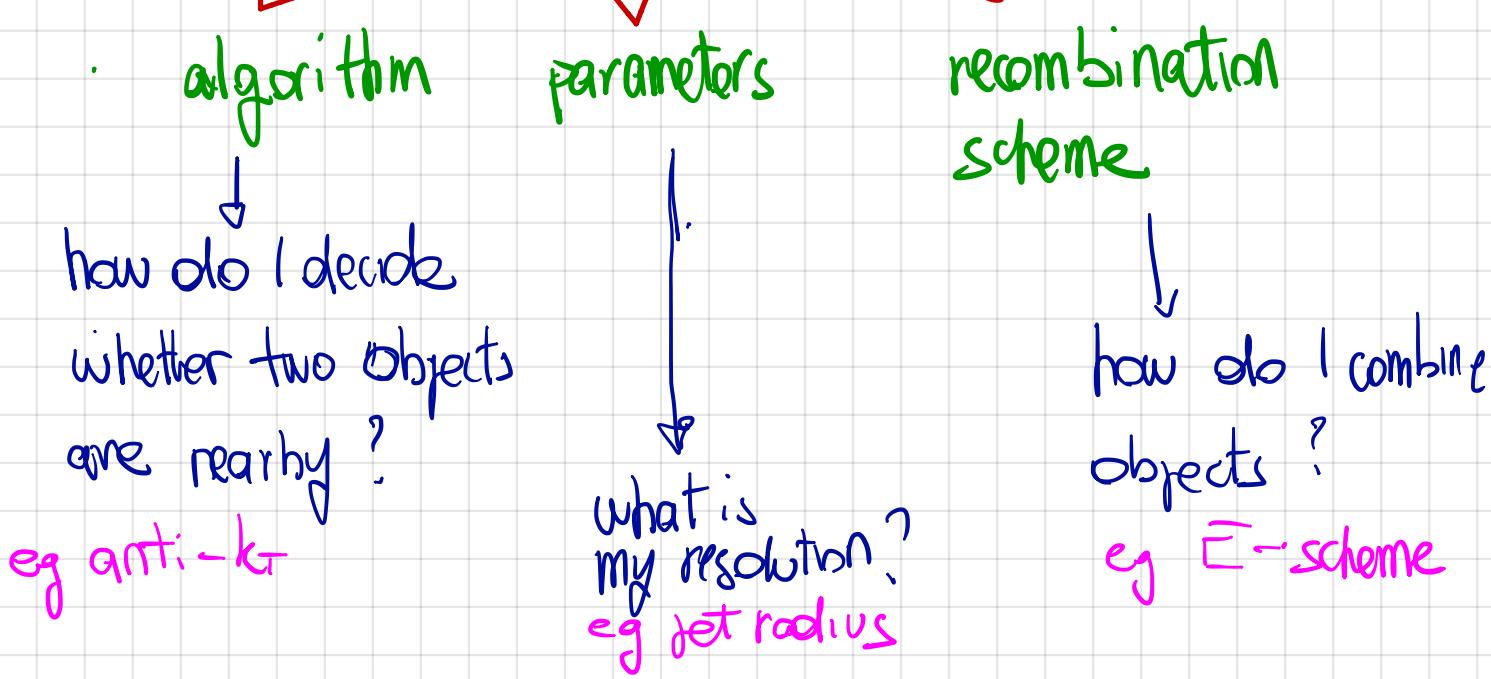
→ jets are at the very boundary between theory and experiment.

jets for experimentalists



- * high-energy collisions often result in collimated sprays of particles

JET DEFINITION



object = a particle or something built from particles
sometimes called pseudoparticle.

JET DEFINITIONS should make sense for both theorists and exp.

. we should be able to run it on a few partons or $O(10^3)$ particles ... or on calo cells!

EXP: fast and easy to calibrate

THEO: guess what! IIRC safety!

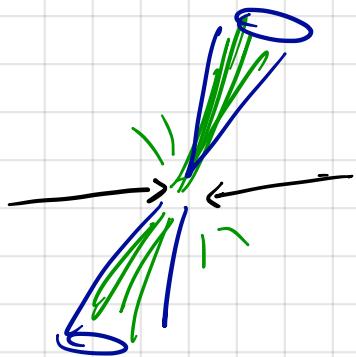
Snowmass accord (1990s)

- ① simple to implement in exp. analysis
- ② simple to implement in th. analysis
- ③ defined at any order in PT
- ④ yield finite $\times\text{-sec}$ at any order in PT
- ⑤ yield $\times\text{-sec}$ \sim insensitive to hadronisation

Jets used at the Tevatron in the 1990s early 2000s were not safe beyond NLO.

FIRST DEFINITION OF A SET Sterman-Weinberg (1977)

$e^+e^- \rightarrow 2 \text{ jets}$: all but a fraction Σ of the energy is within two cones of opening angle δ .



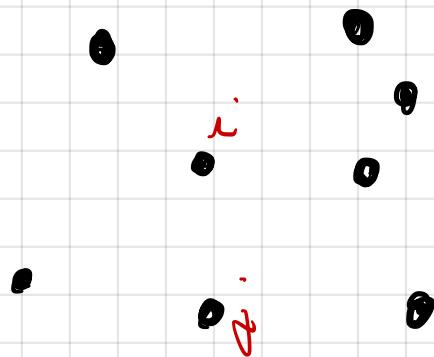
- IRC safe \rightarrow can be computed as a function of the two resolution parameters δ, Σ .

it's an example of a cone algorithm.

Nowadays, CLUSTERING ALGORITHMS are MORE POPULAR

• BOTTOM-UP approach:

① - start with a list of particles



② compute all mutual distances d_{ij} and distances from the beam d_{Bi} (can be an external parameter)

③ find the minimum of all $\{d_{ij}\}$ and $\{d_{Bi}\}$

- if the min is $d_{ij} \rightarrow$ recombine $i+j$

- if the min is $d_{Bi} \rightarrow$ call i a jet and remove it

④ GO TO ①

{list of particles} \rightarrow {list of jets}.

every jet has { 4-momentum
axis
list of constituents
clustering tree}

valuable information
about jet formation
and QCD
dynamics.

A popular family of jet clustering algorithm is the generalised k_T family

$$d_{ij} = \min\left(k_{T_i}^{2p}, k_{T_j}^{2p}\right) \frac{(y_i - y_j)^2 + (\phi_i - \phi_j)^2}{R^2}$$

$p=0$ C/A algorithm: purely geometric

$p=1$ k_T (Durham) algorithm: faithful to each sing. structure

$p=-1$ anti- k_T algorithm: grows jets around hard lines.

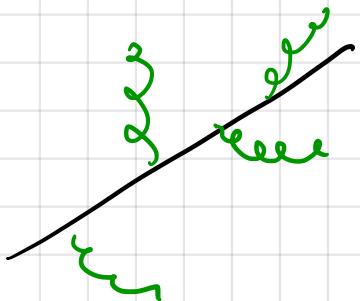
Ex Show that for a jet of just 2 particles, any of the above algorithms clusters the two particles together if $\Delta_{ij} = \sqrt{(y_i - y_j)^2 + (\phi_i - \phi_j)^2} < R \rightsquigarrow$ jet radius.

for $n \gg 3$ particles, the algorithms behave very differently

C/A: purely geometric, particles at small angles are clustered first, the clustering tree is angular-ordered.

k_T : $k_T \frac{\Delta^2}{R^2} \simeq \frac{(k_T N)^2}{R^2}$ particles at small relative trans. momentum one cluster first

C/A \neq k_T "invert" the QCD fragmentation process.



anti- k_T is counter-intuitive: two soft particles are always very far apart: jets grow around hard seeds.

Anti- k_T is the STANDARD for LHC physics

BUT WHY?

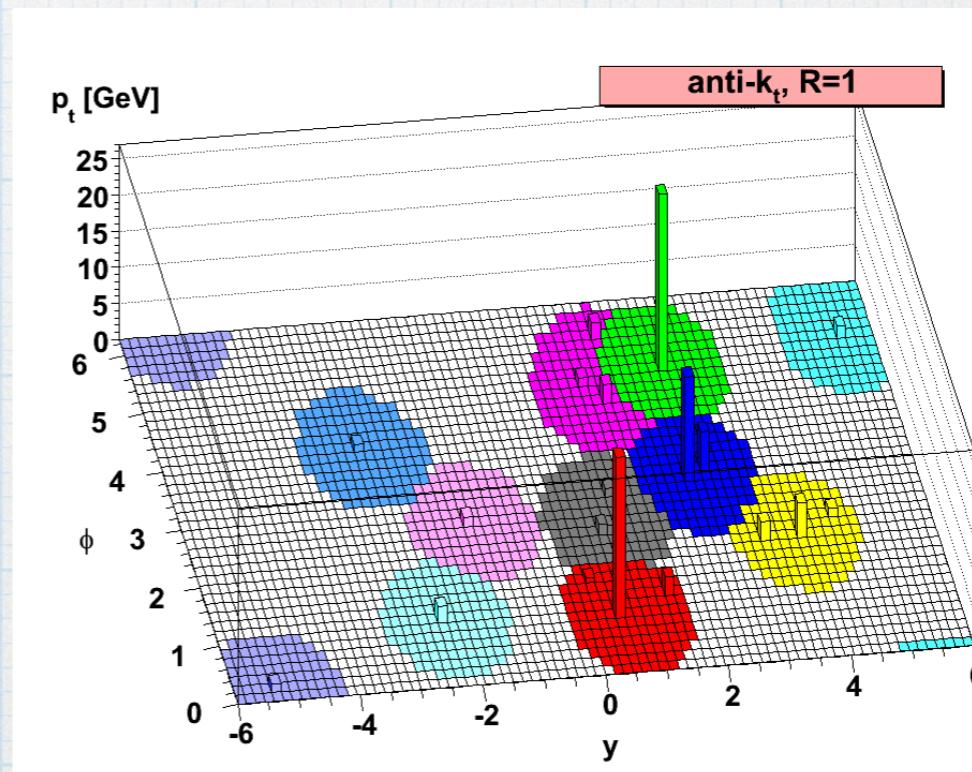
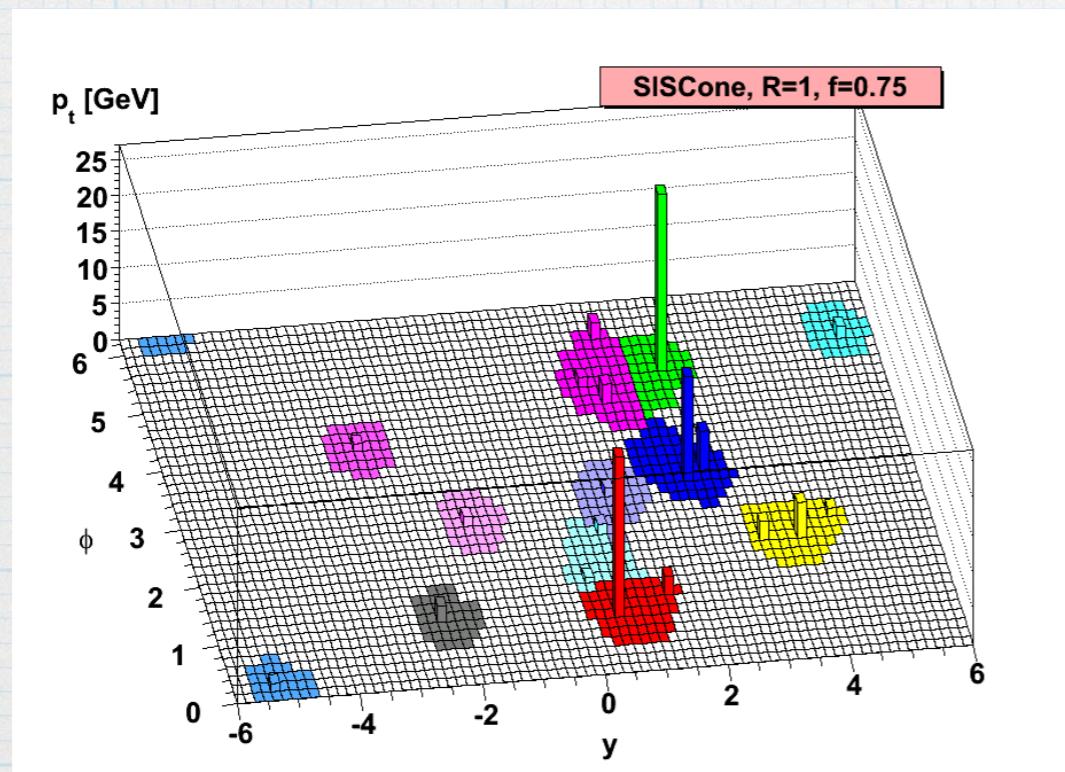
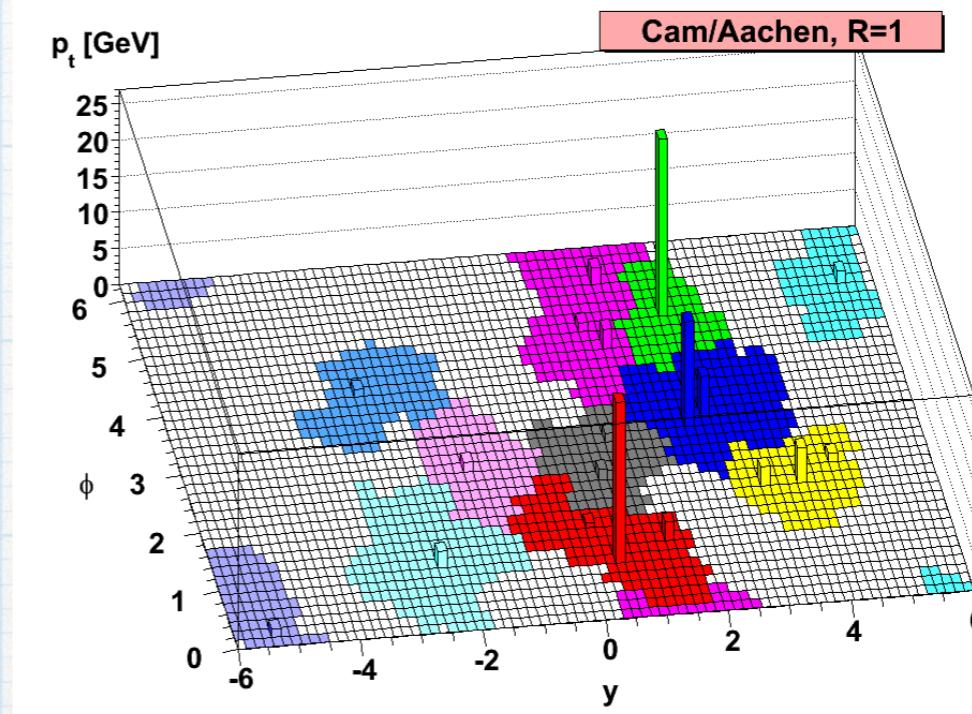
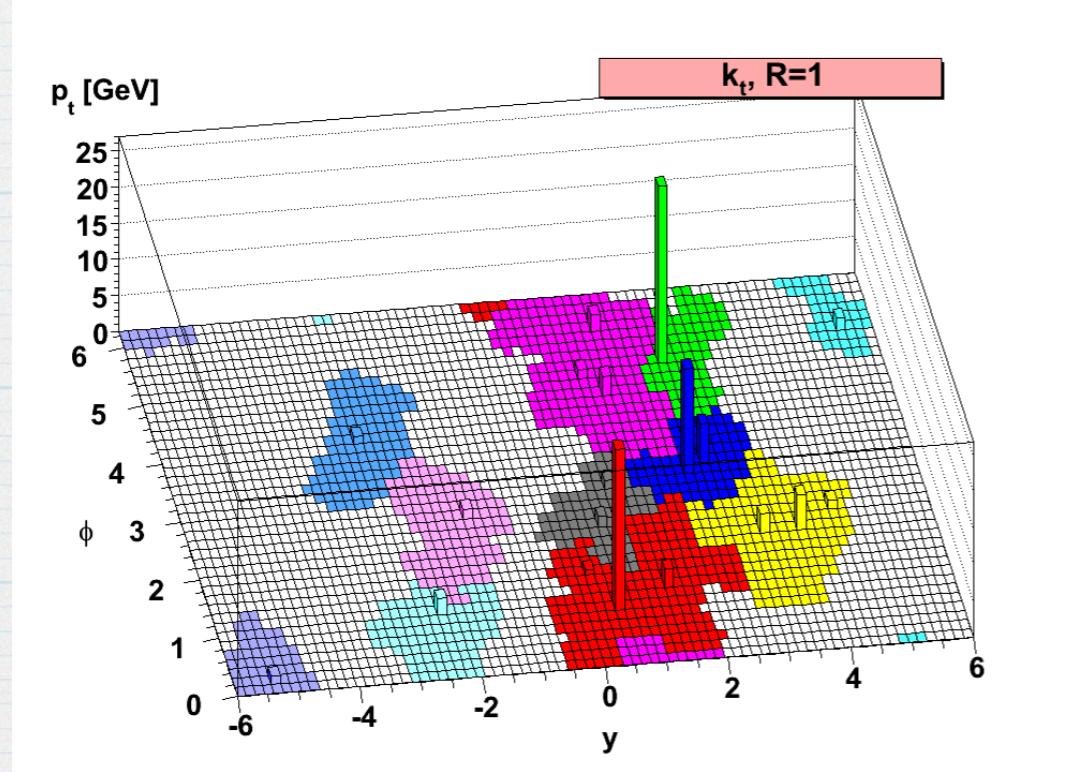
- We've seen that hadron colliders are messy environment.
- Effects that we have neglected because "suppressed"

e.g. $\left(\frac{\Lambda_{\text{QCD}}}{q}\right)^2$ in collinear factorisation, can give non-negligible corrections

- MULTIPLE-PARTON-INTERACTIONS

- PILE-UP (remember 25 collisions per bunch crossing + out-of-time pile-up)

comparing them all



- So now back to α_s by powers.
- We can now talk about cross-sections and distributions for $Z + \text{jet}$, which are finite order by order in α_s .
- We can also ask for more jets:

$Z + 2 \text{ jets}$, (at least two, or just two)
 starts at $\mathcal{O}(\alpha_s \cdot \alpha_s) = \mathcal{O}(\alpha_s^2)$

$Z + 3 \text{ jets}$ starts at $\mathcal{O}(\alpha_s^3)$

• Thus, we can explore processes which are rarer and rarer, going down the staircase plot.

BUT, HOW IS THIS DONE IN PRACTICE?

we compute
observables
with partonic
jets

$\text{NLO}, \text{REN}, \text{COM}$

UNFOLDING

PARTICLE
LEVEL ("TRUTH")
JETS, i.e. jets made
of $\pi^\pm, \eta^\pm, K^\pm, \dots$

experimenters
measure jets
using detectors
(topoclusters, p_T^{jet})

MEANINGFUL COMPARISONS