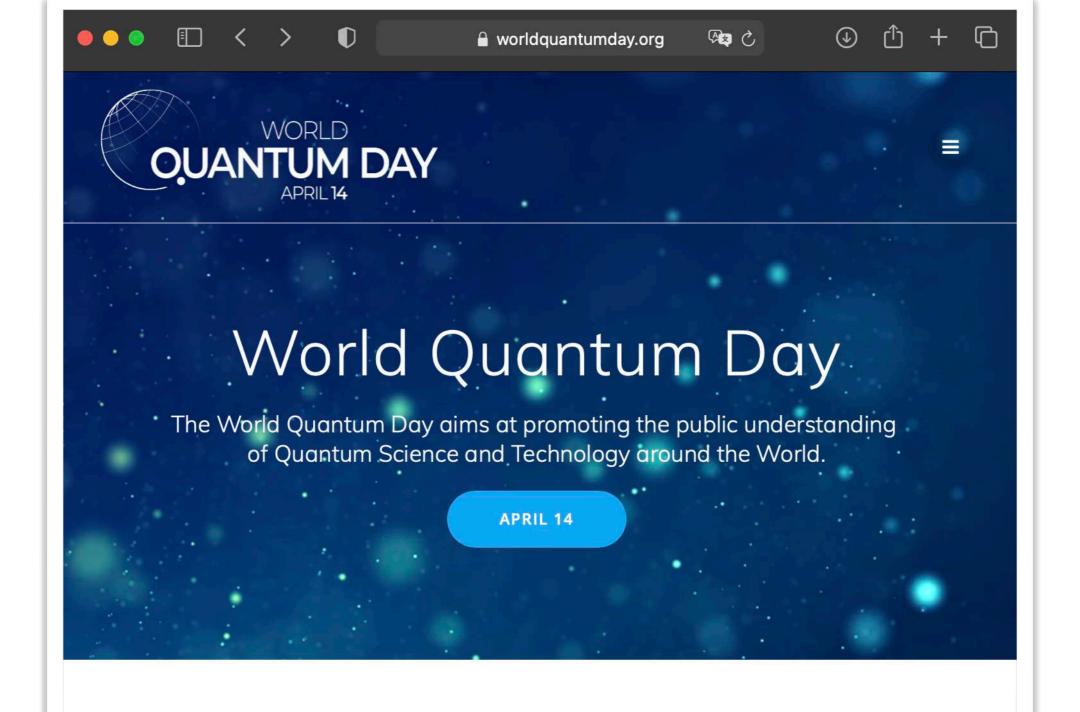
How to test Quantum Theory with thought experiments

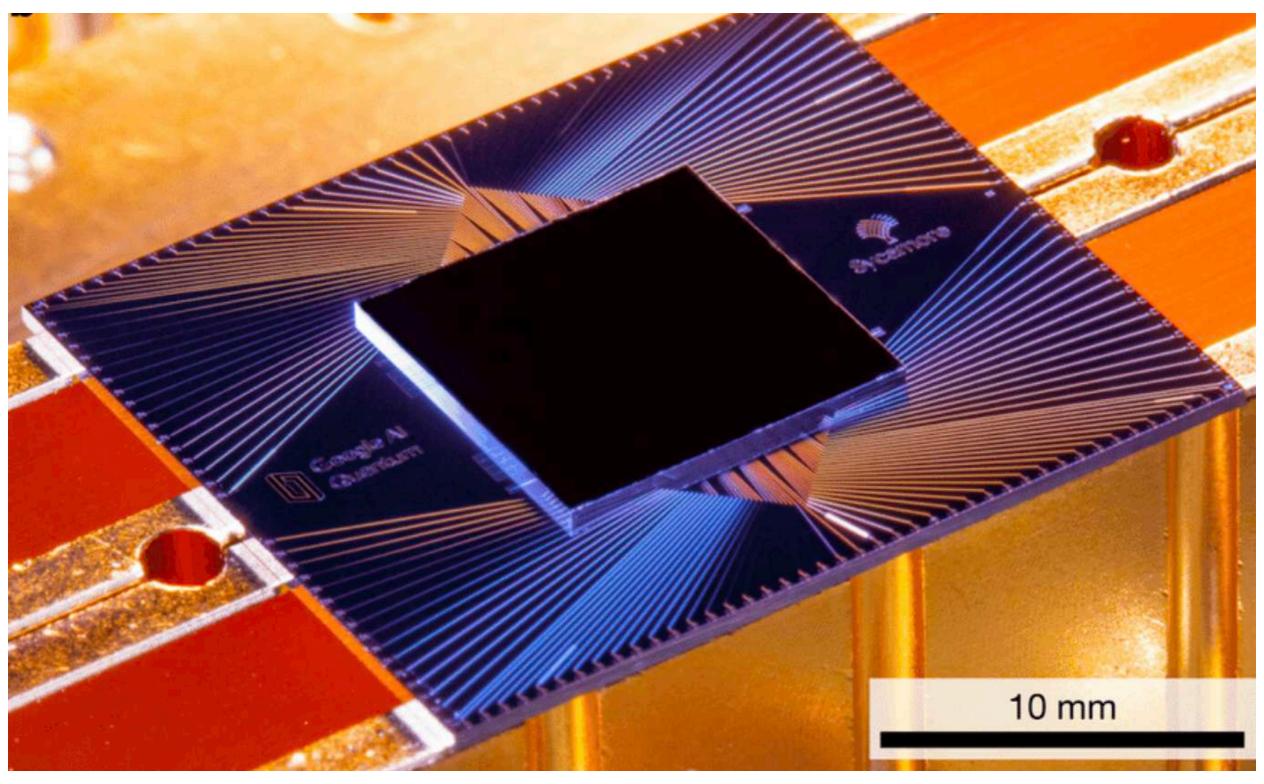
Renato Renner ETH Zürich

GGI Seminar — Firenze, 14.4.2021



The World Quantum Day is an initiative from quantum scientists from 65+ countries, launched on 14 April 2021 as the countdown towards the first global celebration on 14 April 2022.

Is it correctly described by quantum theory?



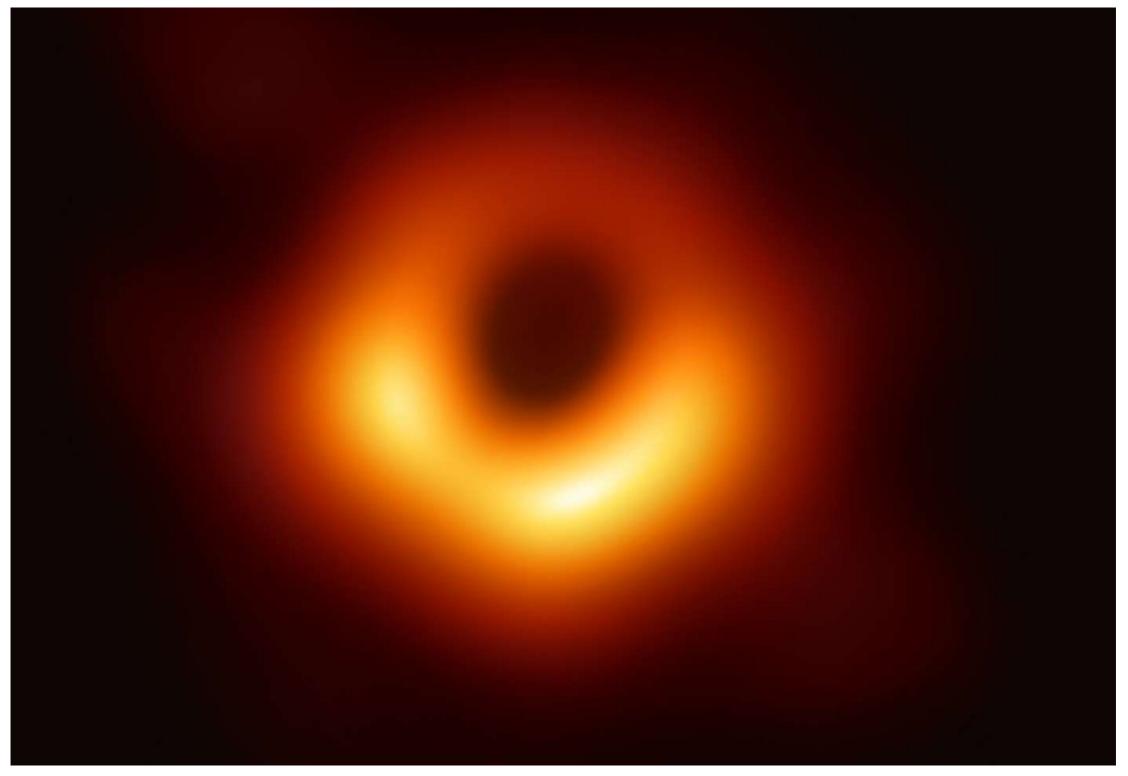
Google's Sycamore processor (from nature.com)

Is it correctly described by quantum theory?



Erwin Schrödinger's cat (at his house in Huttenstrasse 9, Zurich)

Is it correctly described by quantum theory?



Black hole at the center of galaxy M87

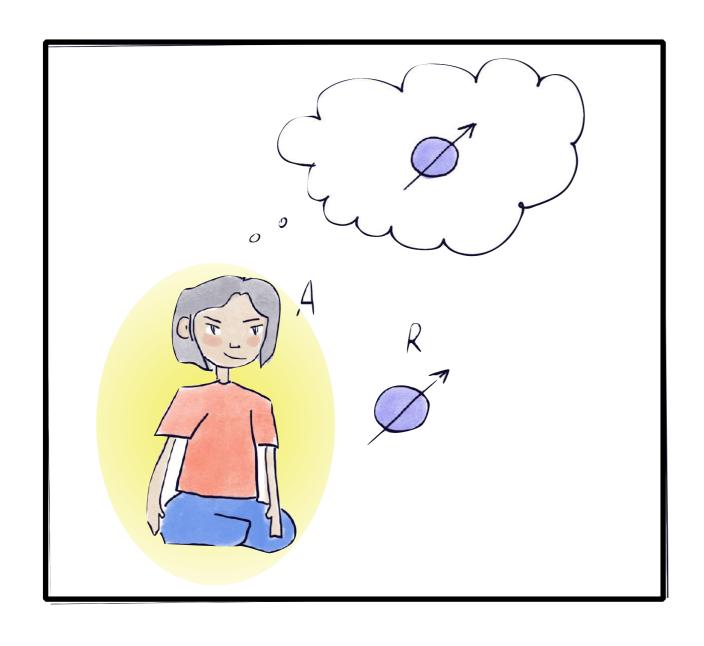
Question: What's the range of validity of quantum theory?



tested to high precision tested to low accuracy

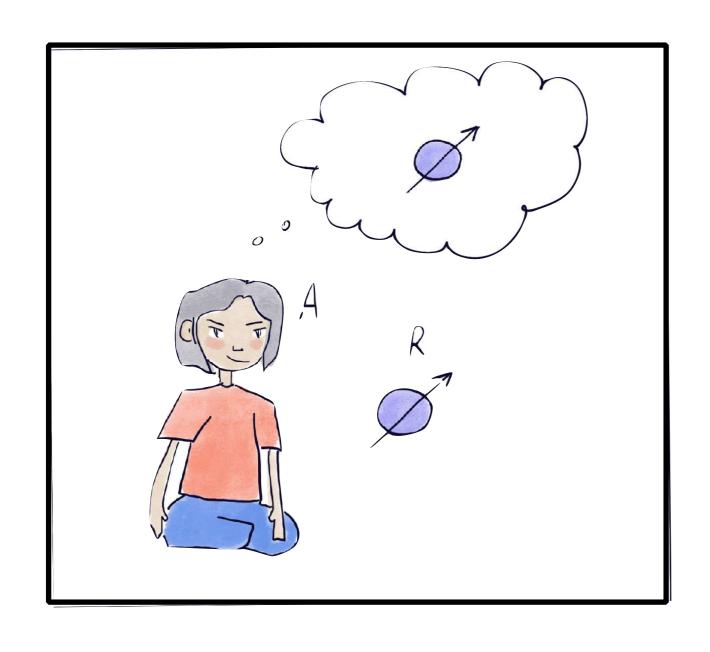
?

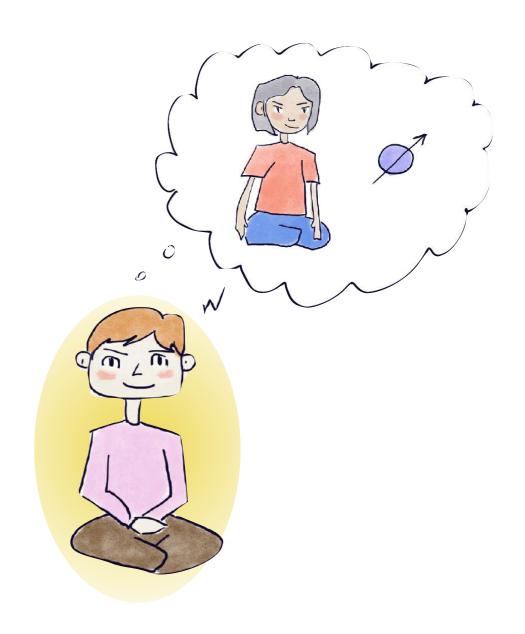
Information-theoretic approach



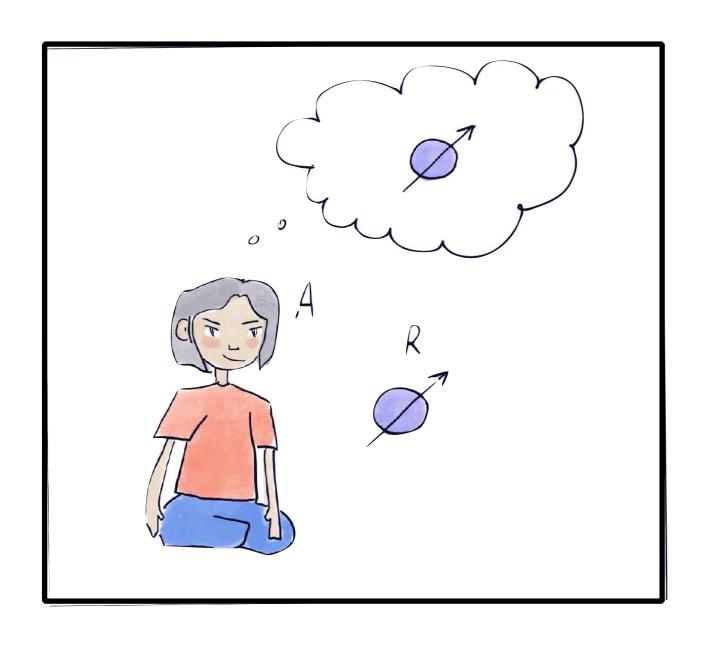


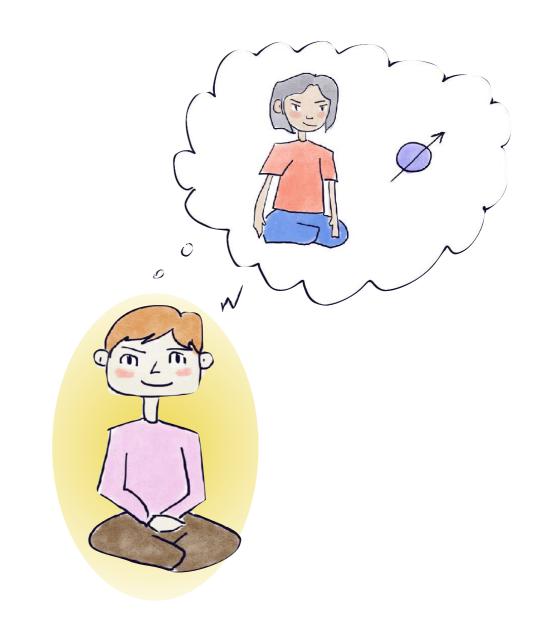
Information-theoretic approach





Information-theoretic approach





Idea: Use quantum theory to describe systems that can themselves be users of the theory.

A conceptual separation

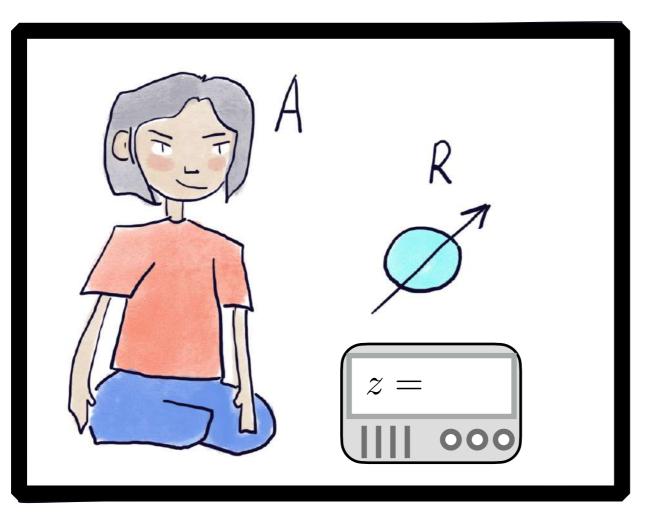
cannot be users of quantum theory

can be users of quantum theory



quantum theory valid

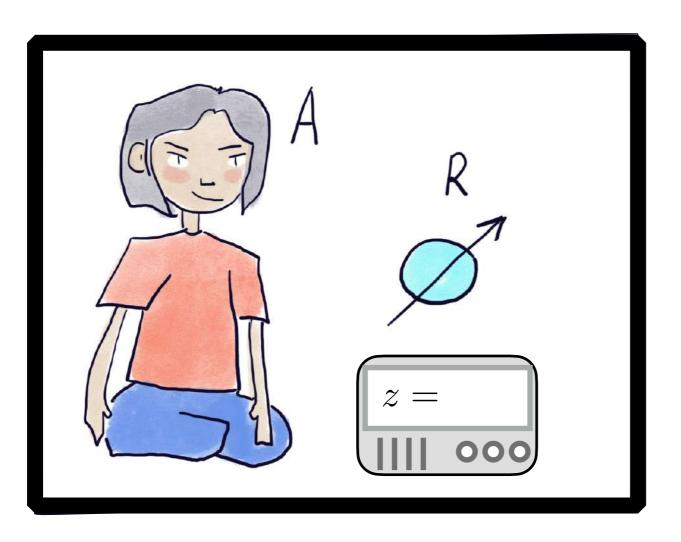
quantum theory invalid?





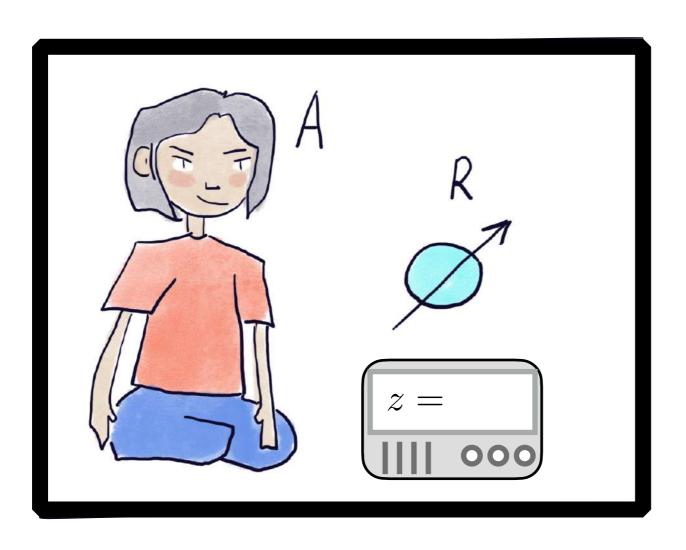
$$|\uparrow\rangle_R \otimes |\mathrm{ready}\rangle_A \quad \mapsto \quad |\uparrow\rangle_R \otimes |\mathrm{I\ observed}\ z = \mathrm{up}\rangle_A$$

$$|\downarrow\rangle_R \otimes |\mathrm{ready}\rangle_A \quad \mapsto \quad |\downarrow\rangle_R \otimes |\mathrm{I\ observed}\ z = \mathrm{down}\rangle_A$$



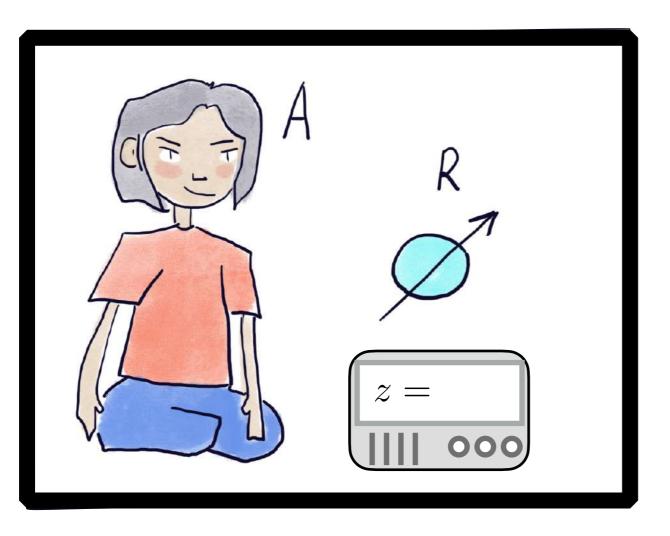


$$| \rightarrow \rangle_R = \frac{| \uparrow \rangle_R + | \downarrow \rangle_R}{\sqrt{2}}$$





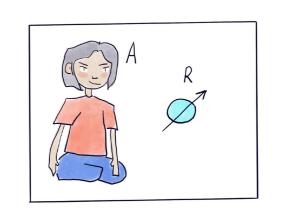
$$(|\uparrow\rangle_R + |\downarrow\rangle_R) \otimes |\text{ready}\rangle_A$$
 \mapsto





$$(|\uparrow\rangle_R + |\downarrow\rangle_R) \otimes |\text{ready}\rangle_A$$
 \mapsto

 $|\uparrow\rangle_R \otimes |\text{I observed } z = \text{up}\rangle_A + |\downarrow\rangle_R \otimes |\text{I observed } z = \text{down}\rangle_A$





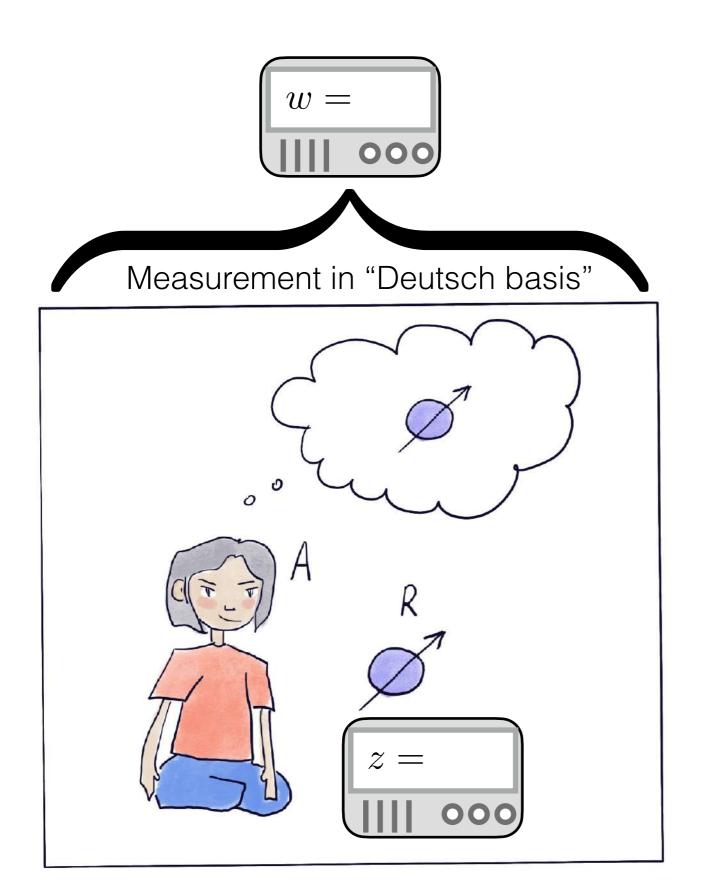
Alice's claim: "I observed z = up"

or "I observed z = down"

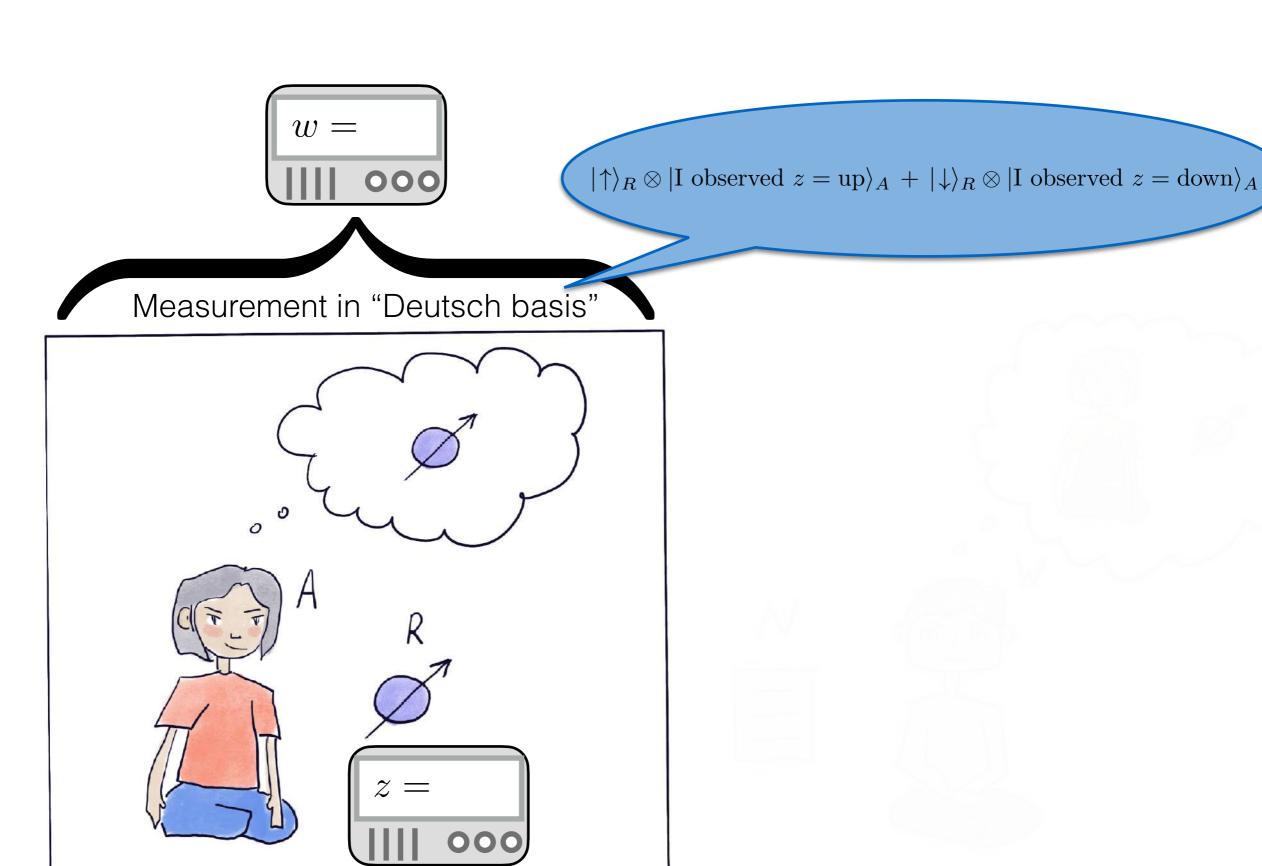
Wigner's claim: "Alice is in a superposition between having observed z = up and z = down."

| | Alice | Bob |
|------------------------------|----------|-----|
| Copenhagen | / | X |
| Collapse theories | | X |
| QBism | / | |
| Relational Quantum Mechanics | | |
| Bohmian Mechanics | / | |
| Many-Worlds | X | |
| | | |

Deutsch's extension of Wigner's experiment

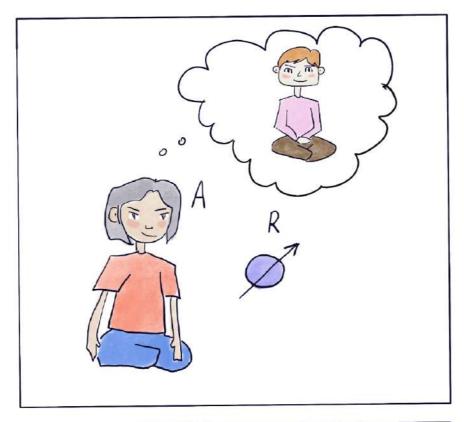


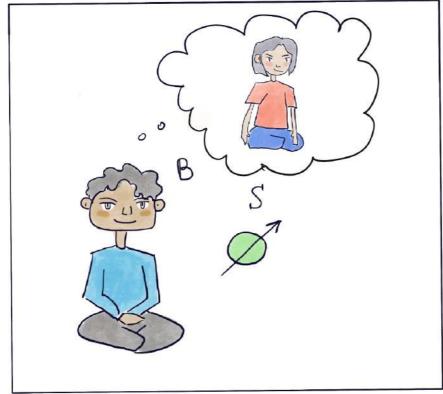
Deutsch's extension of Wigner's experiment

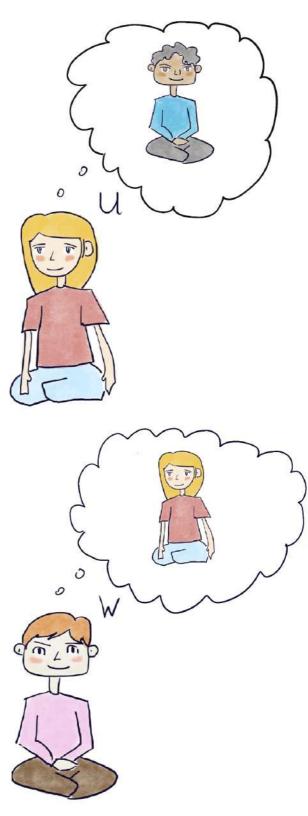


FR thought experiment

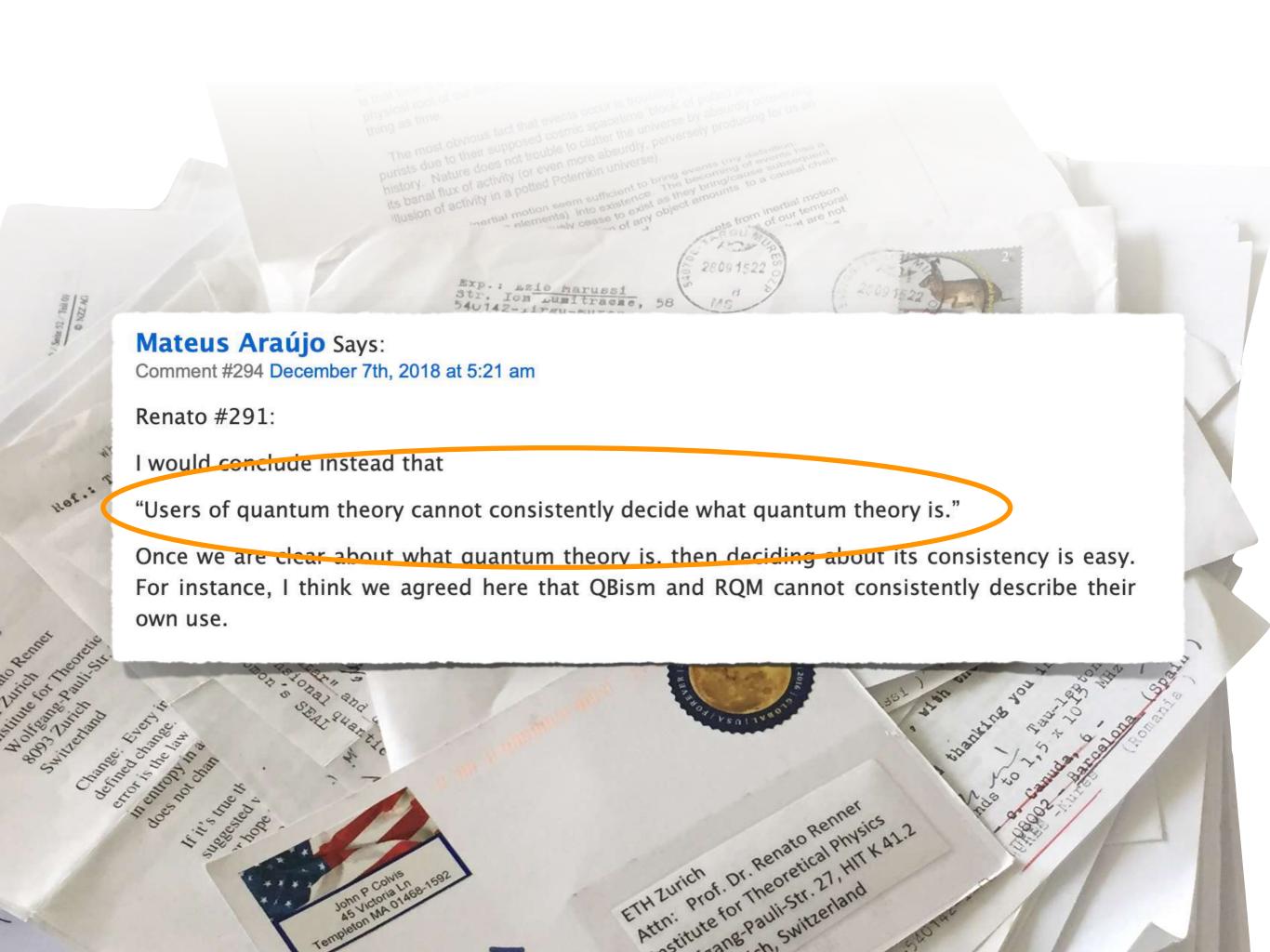
[D. Frauchiger and R. Renner, Quantum theory cannot consistently describe the use of itself *Nat. Comm*, **9**, 2018]



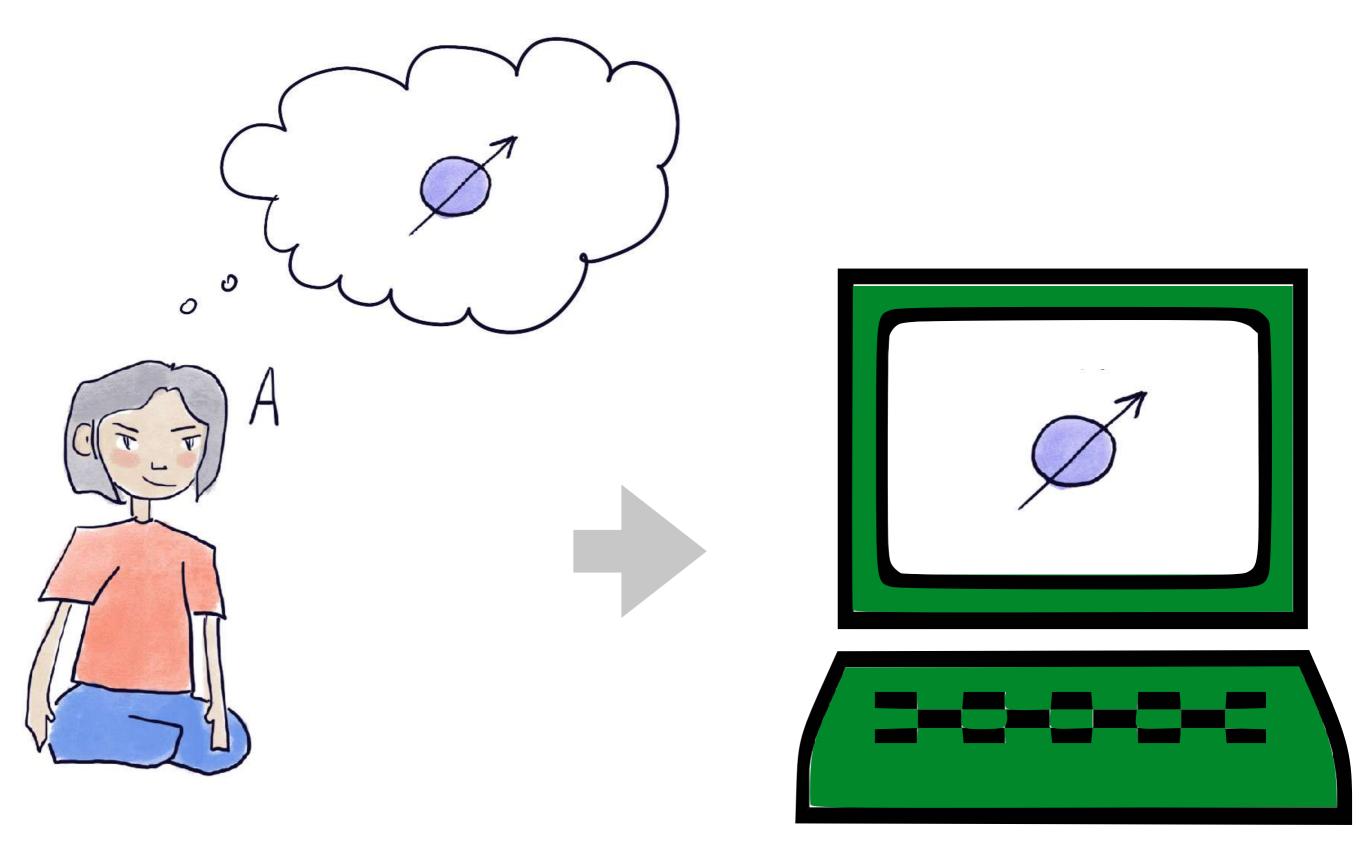








Better get rid of human agents ...

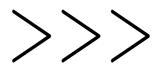


Computers as users of quantum theory

input

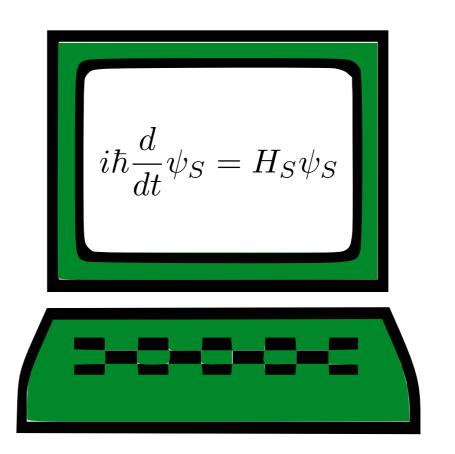
output

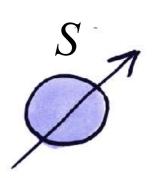
- Quantum formalism
- Description of experiment
- Observations

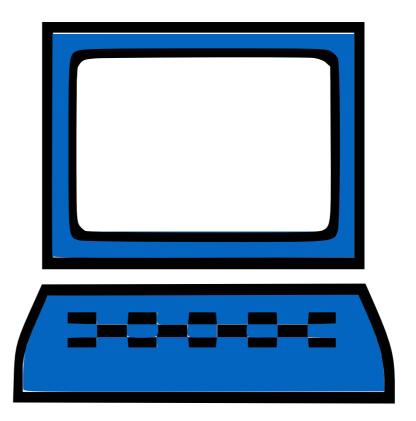




Role as subject: Computer as agent that uses quantum theory.

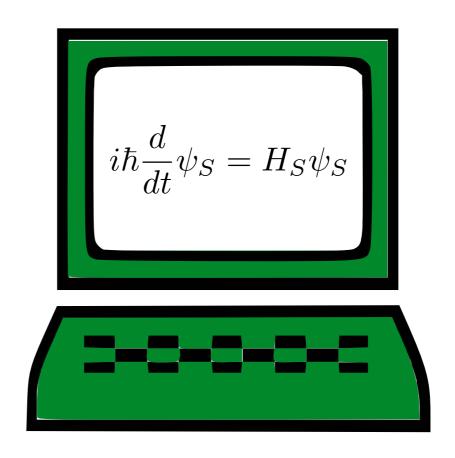


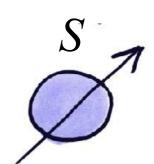




Role as subject:

Computer as agent that uses quantum theory.

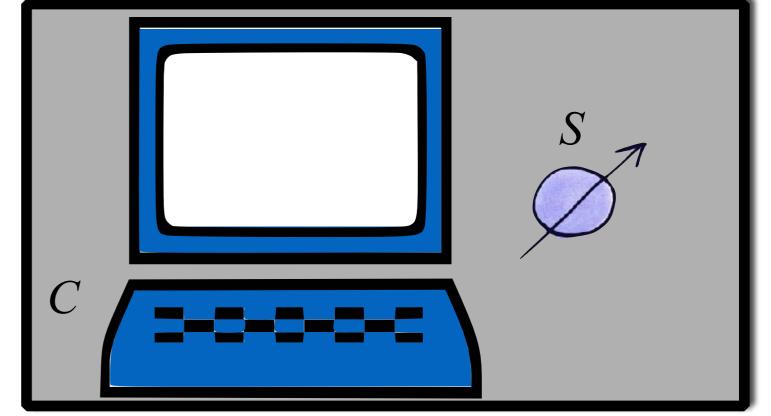




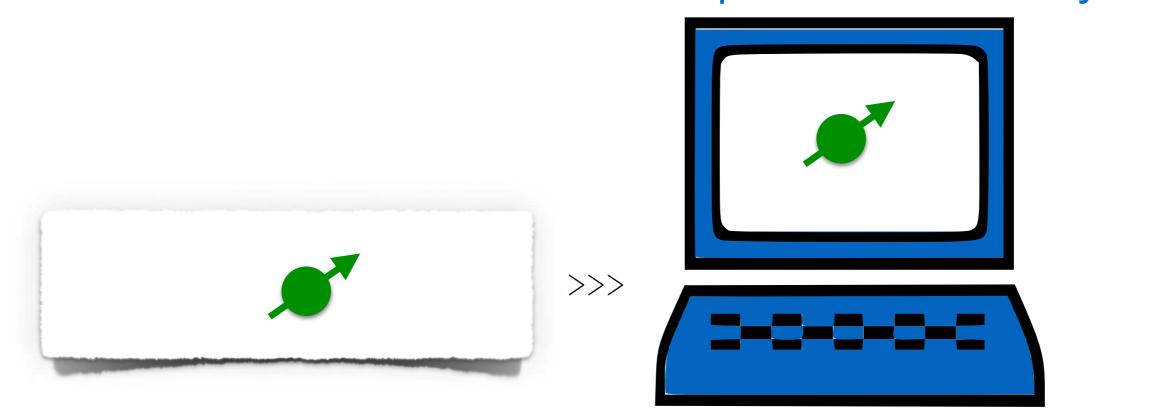
Role as object:

Computer as object described by quantum theory.

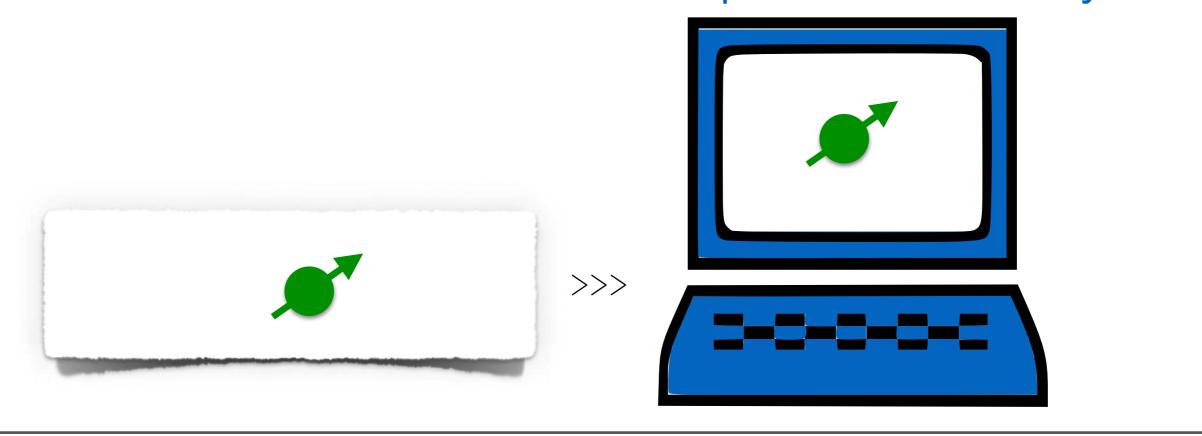
$$i\hbar \frac{d}{dt}\Psi_{CS} = H_{CS}\Psi_{CS}$$

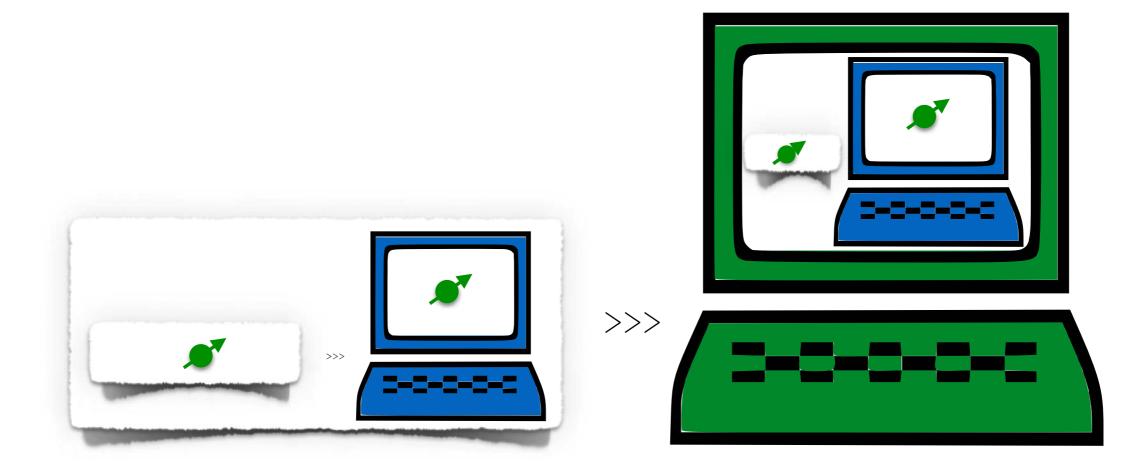


This enables nested use of quantum theory ...



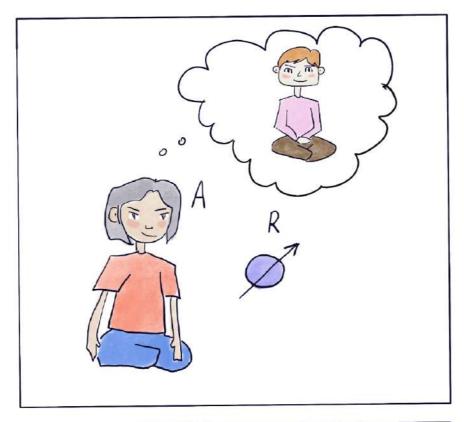
This enables nested use of quantum theory ...

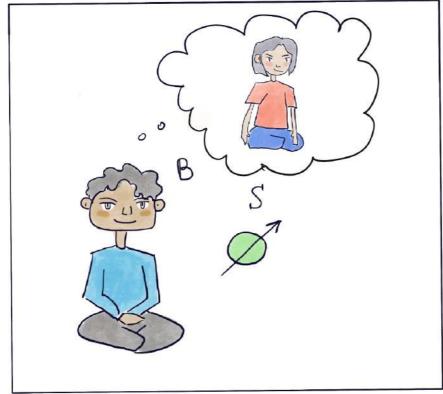


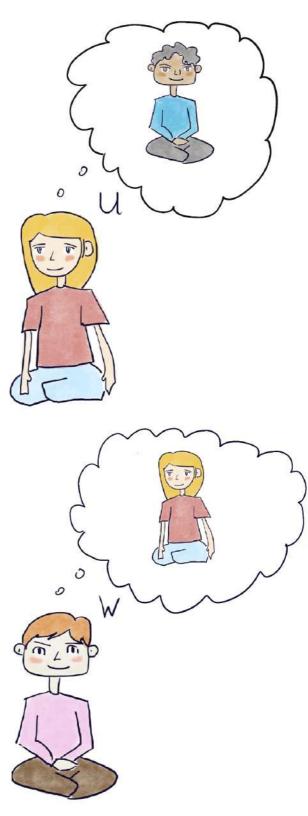


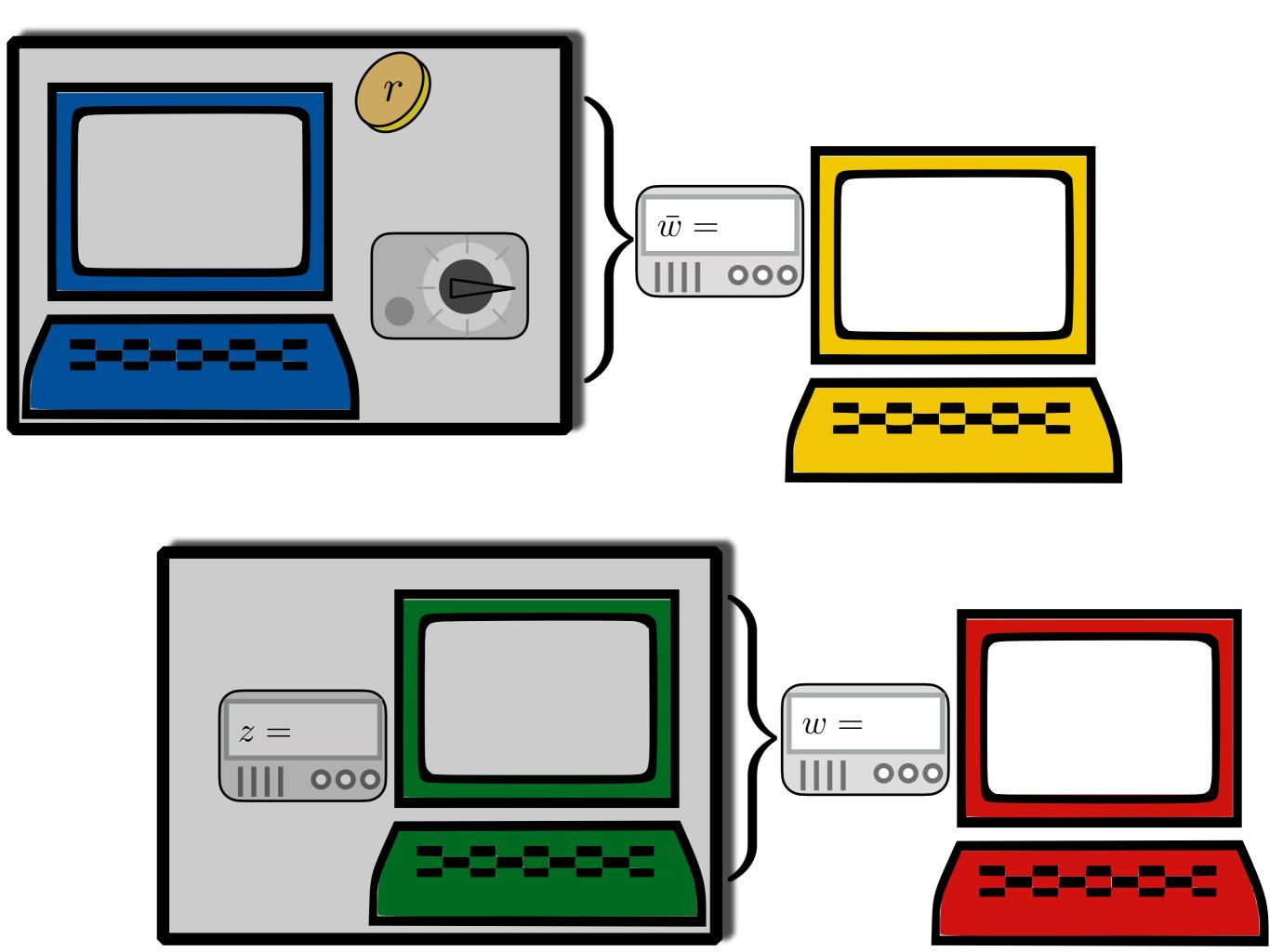
FR thought experiment

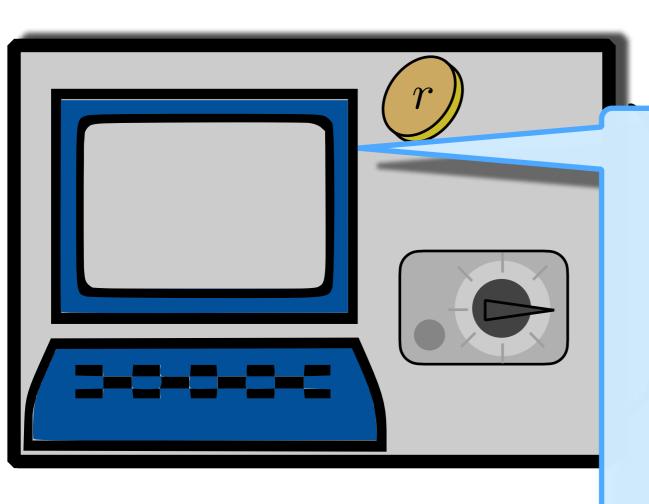
[D. Frauchiger and R. Renner, Quantum theory cannot consistently describe the use of itself *Nat. Comm*, **9**, 2018]



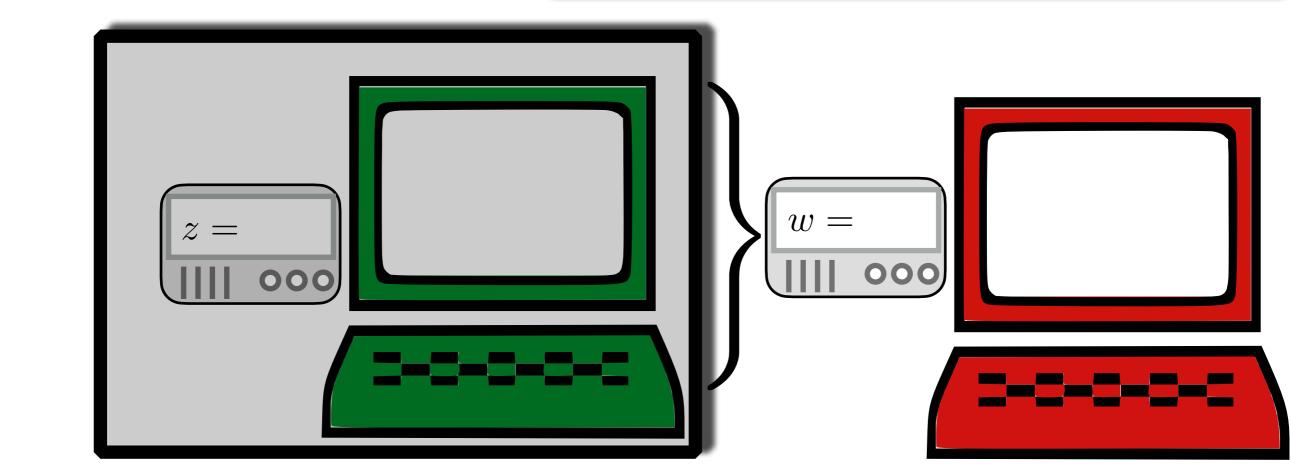


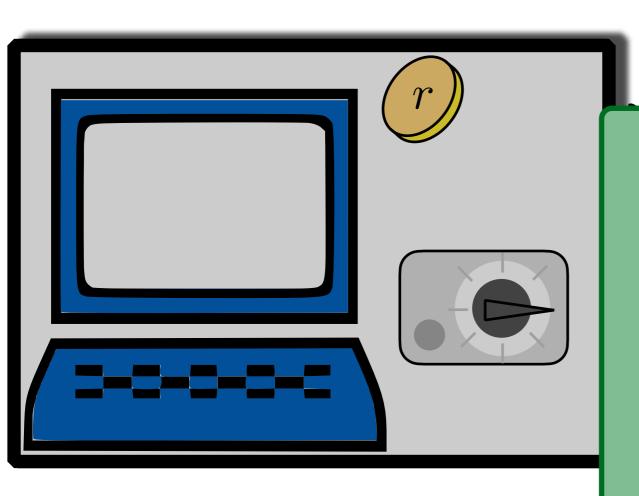




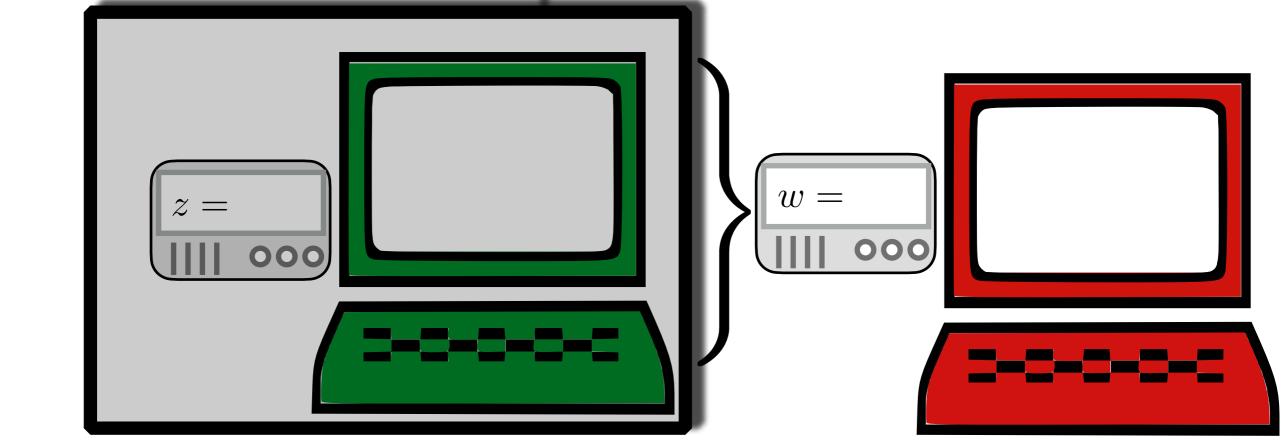


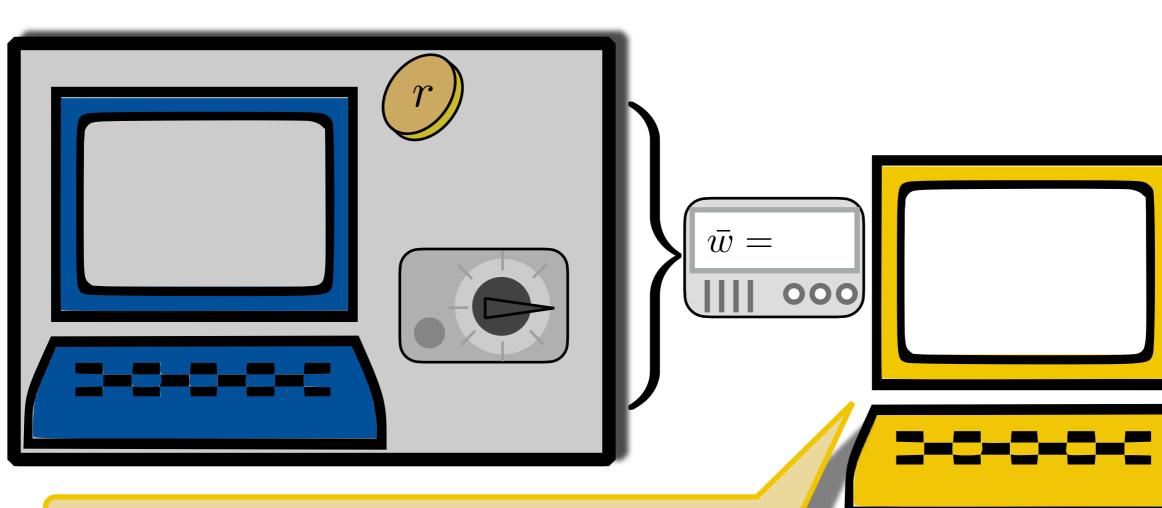
- 1) Generate a random bit r
- 2) Prepare spin S either spin down if r = heads or spin right if r = tails
- 3) Send S to Green
- 4) Make a prediction for w measured by Red.



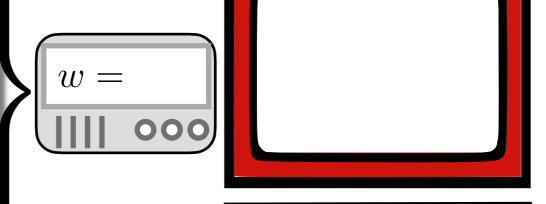


- 1) Receive S sent by Blue.
- 2) Measure S w.r.t. up/down basis.
- 3) From the outcome, infer the value r obtained by Blue.
- 4) From this infer the prediction made by Blue for w.

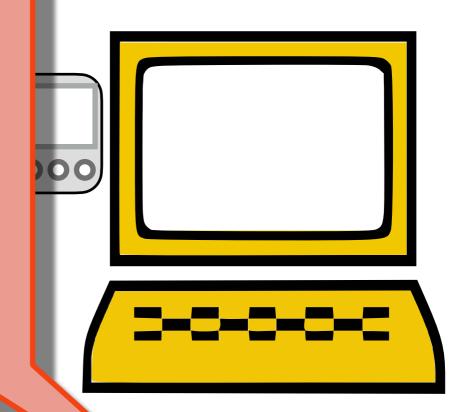


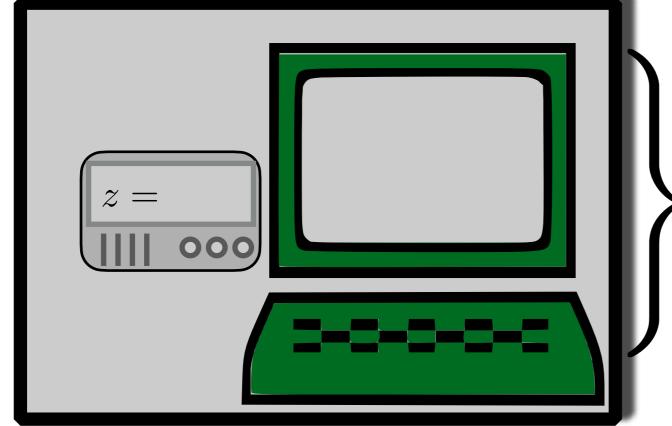


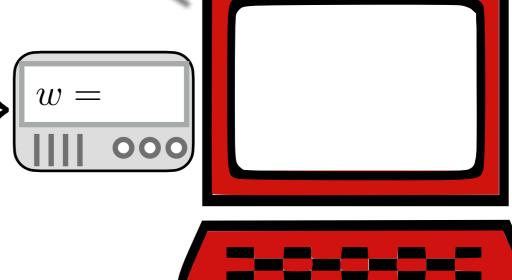
- 1) Measure Blue in Deutsch basis.
- 2) From the outcome infer outcome z of Green.
- 3) From this infer prediction made by Green for w.
- 4) Send prediction to Red.



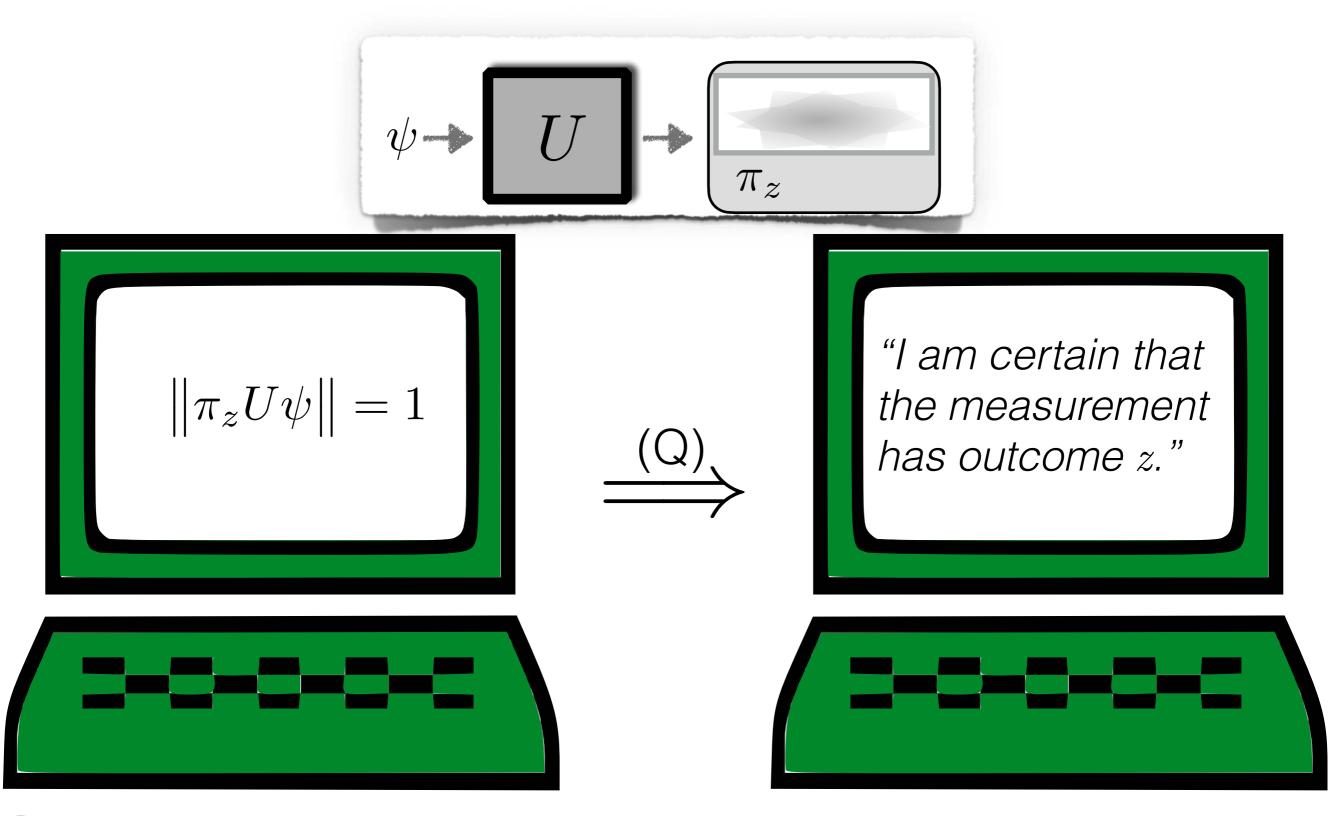
- 1) Read message sent from Yellow about the prediction for w.
- 2) Measure the lab of Green in Deutsch basis and compare the outcome w to the prediction.





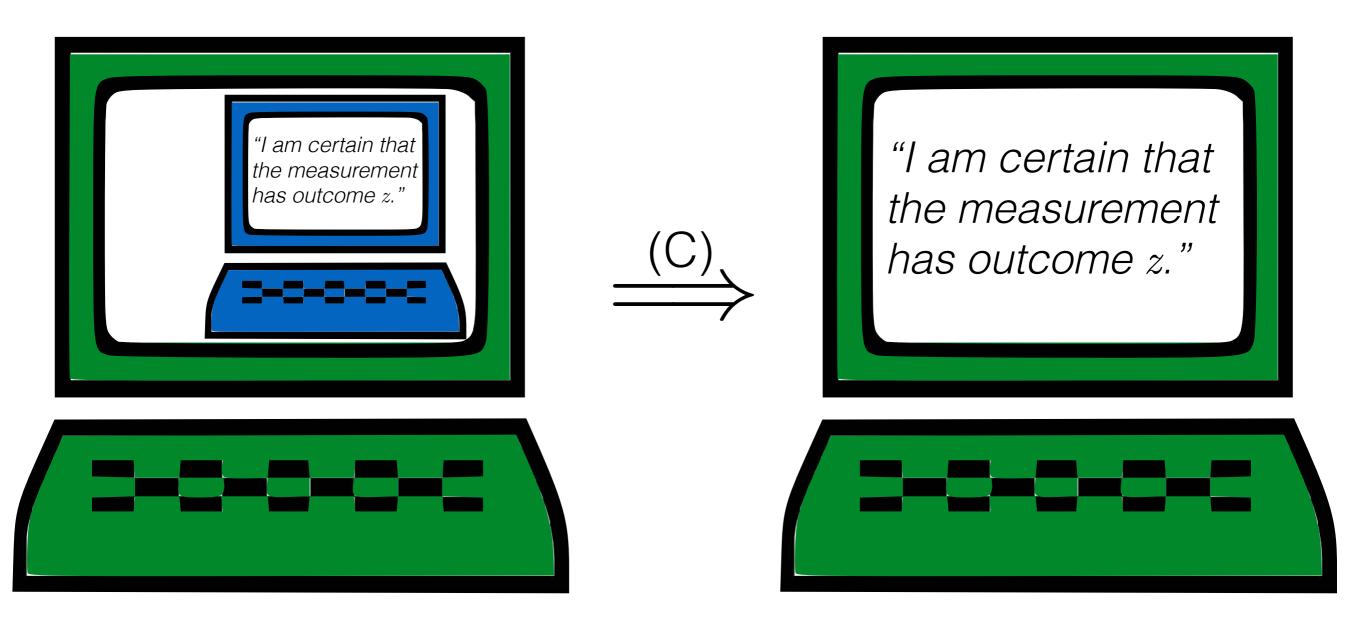


Rule (Q): Quantum theory applicable to any subsystem



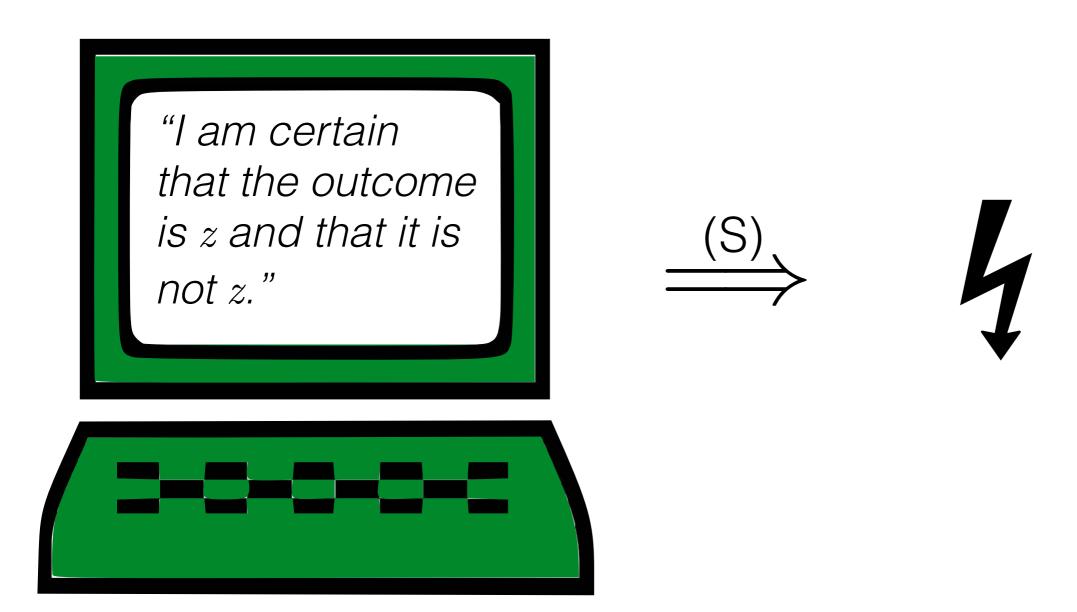
Quantum-mechanical Born rule assigns probability 1 to outcome *z*.

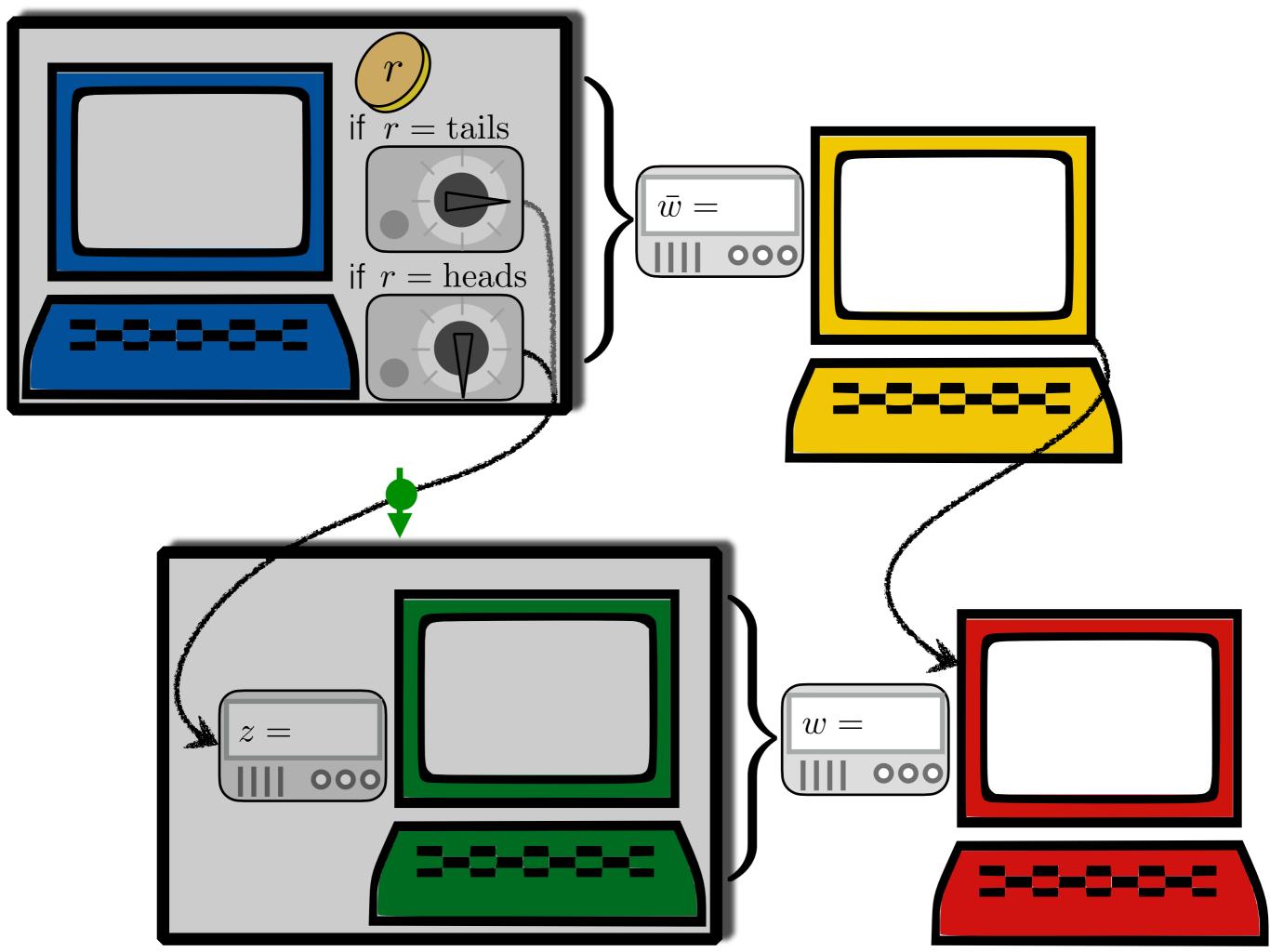
Rule (C): Be consistent with conclusions of others

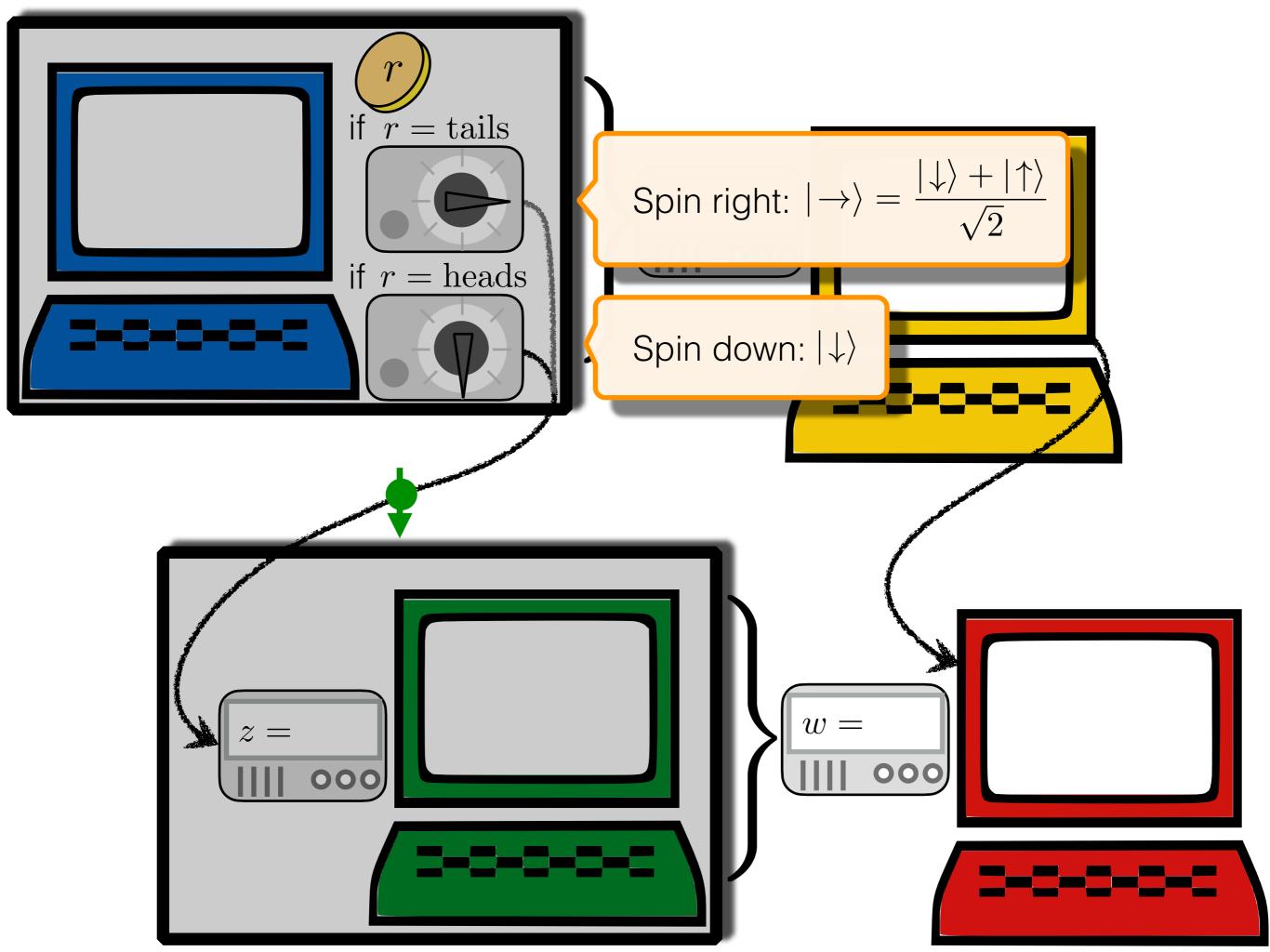


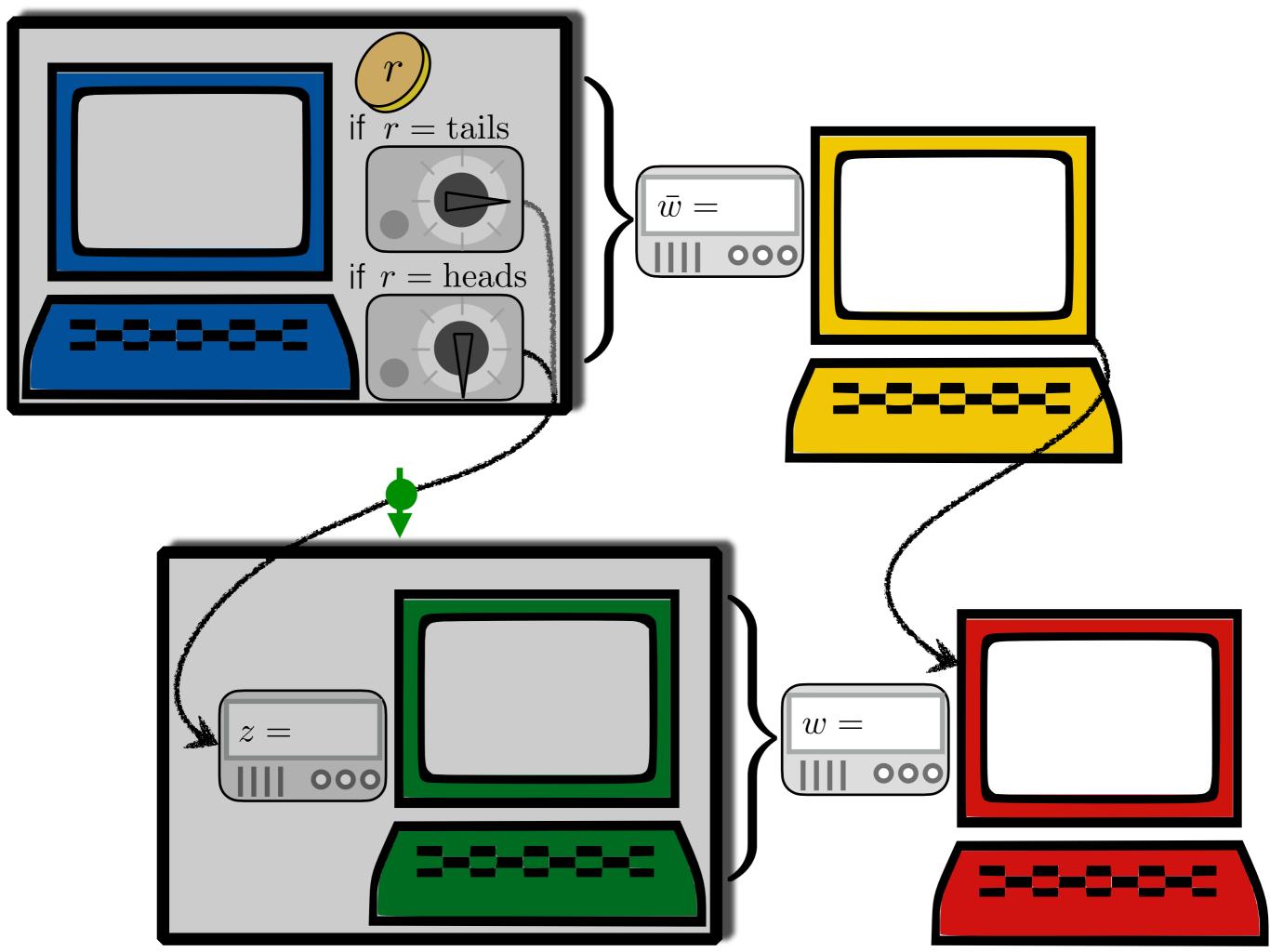
The green computer is certain that the blue computer is *at this moment* certain that the outcome is *z*.

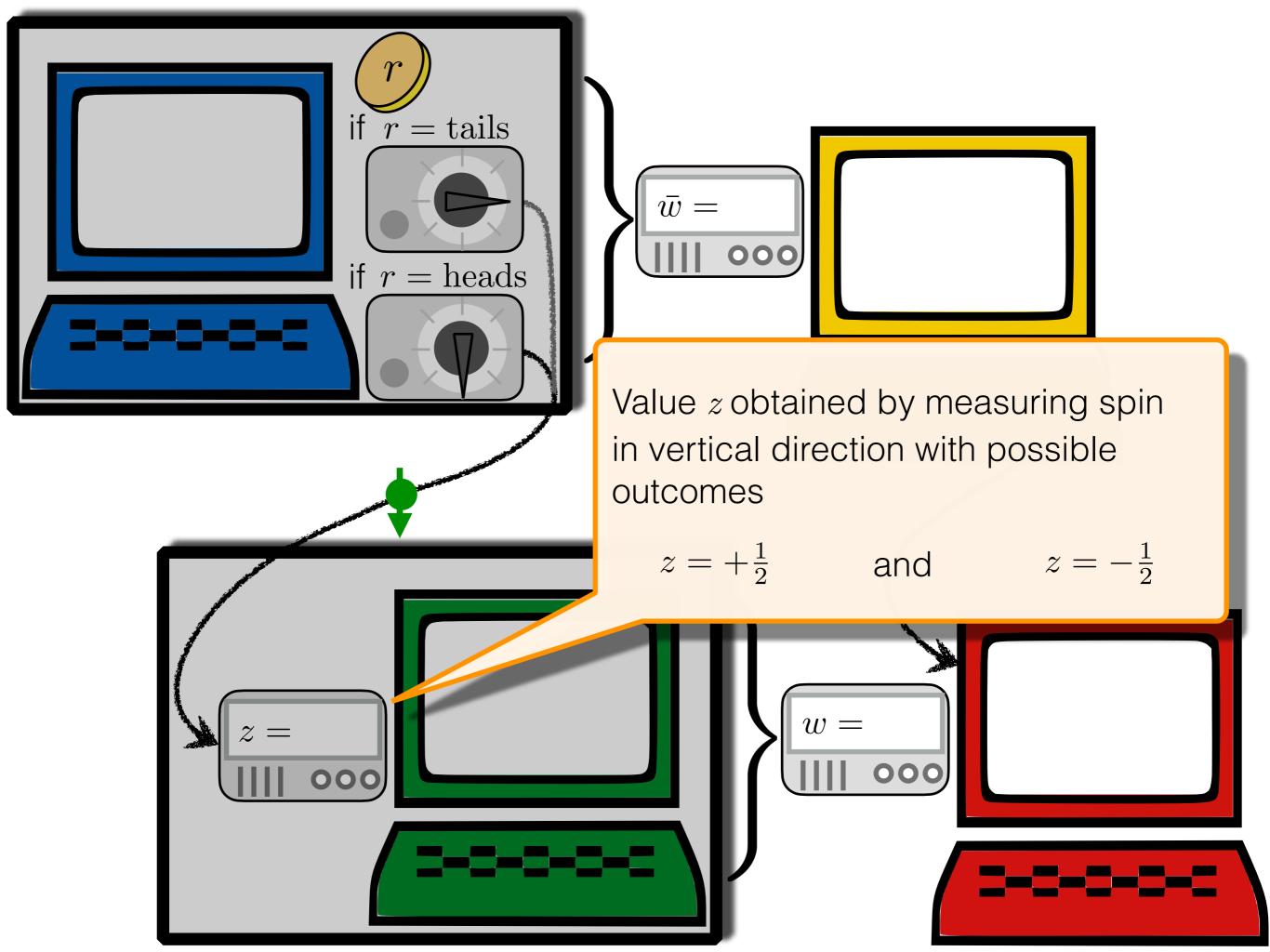
Rule (S): Do not claim "alternative facts"

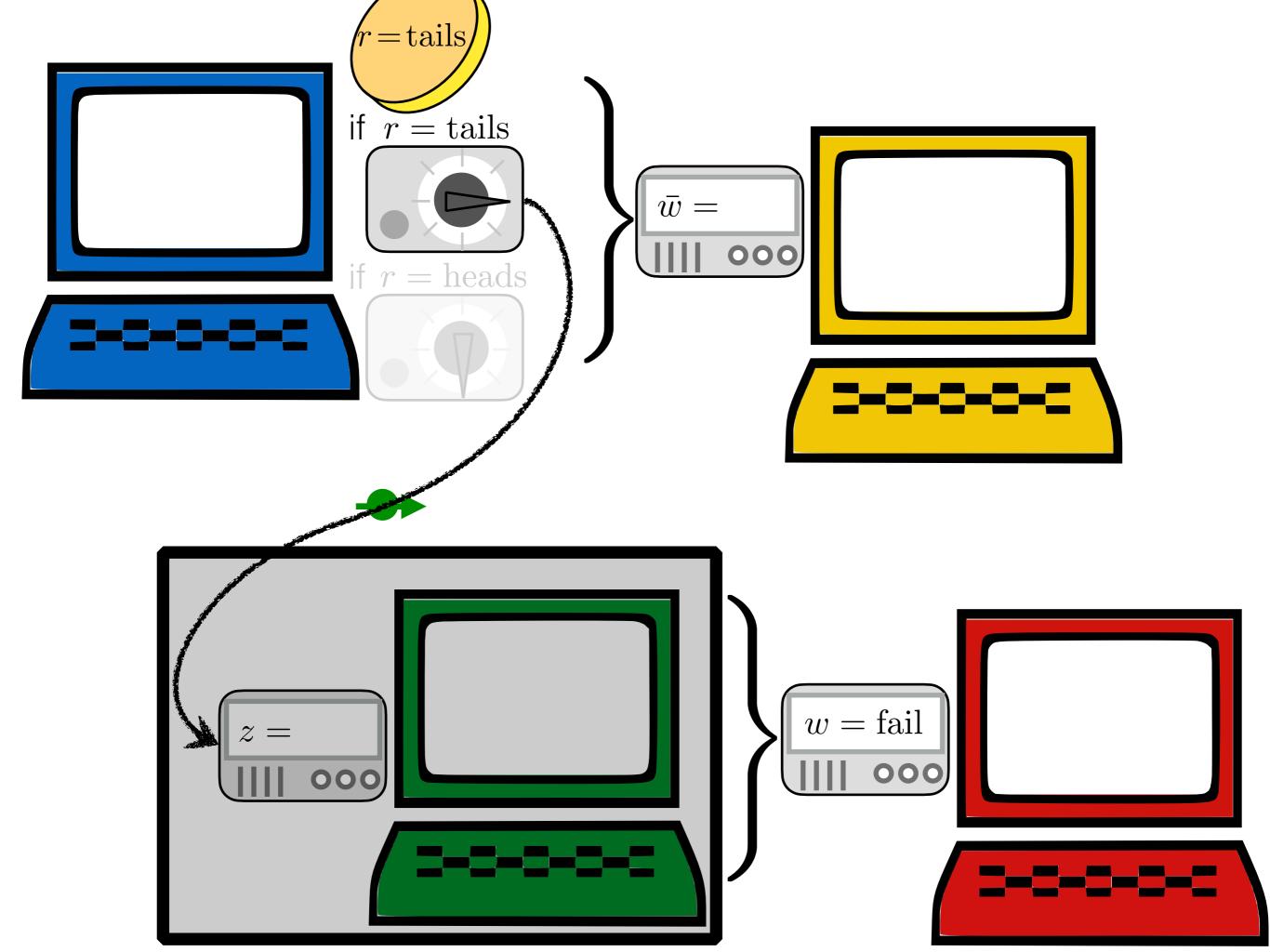


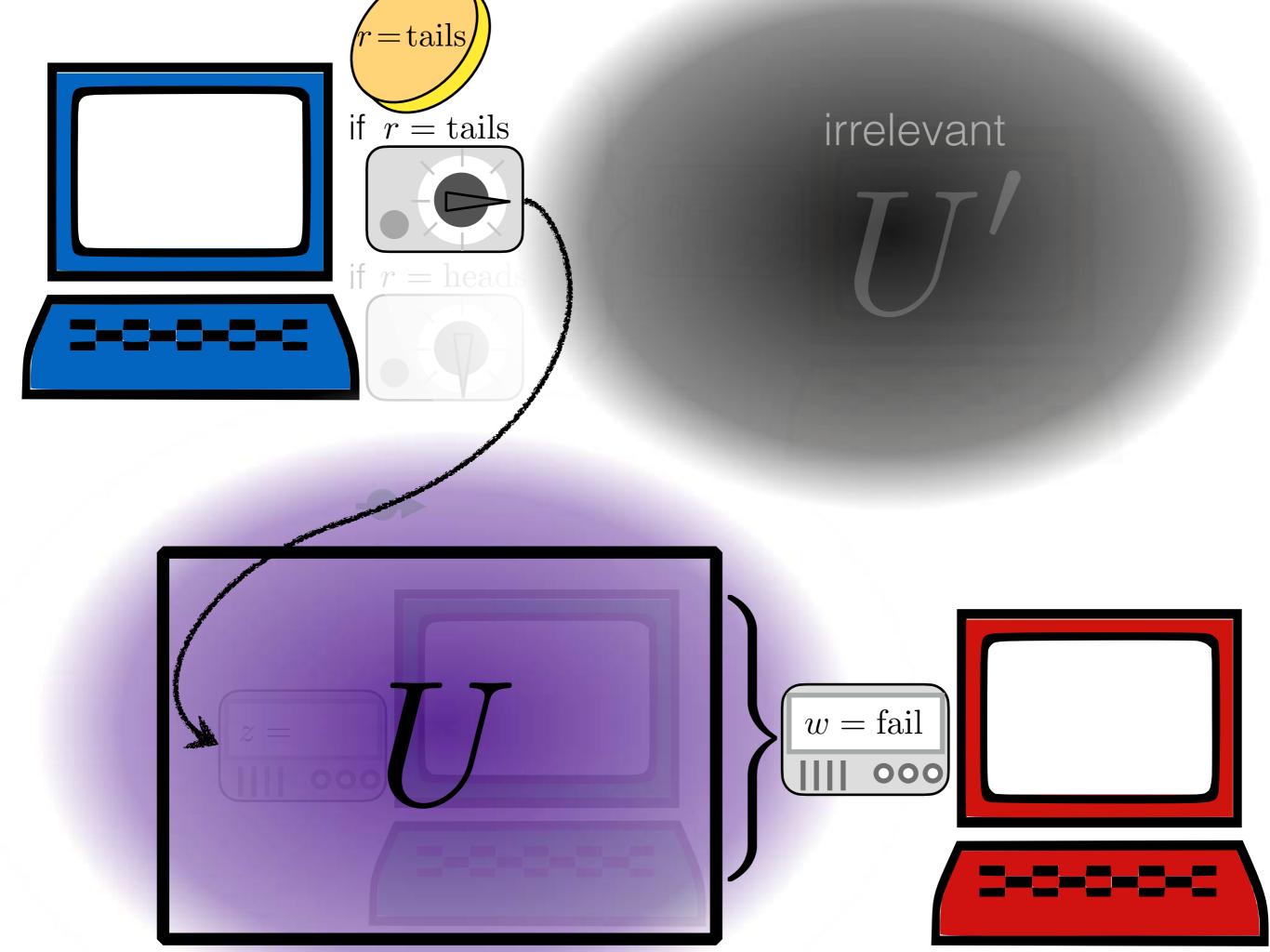


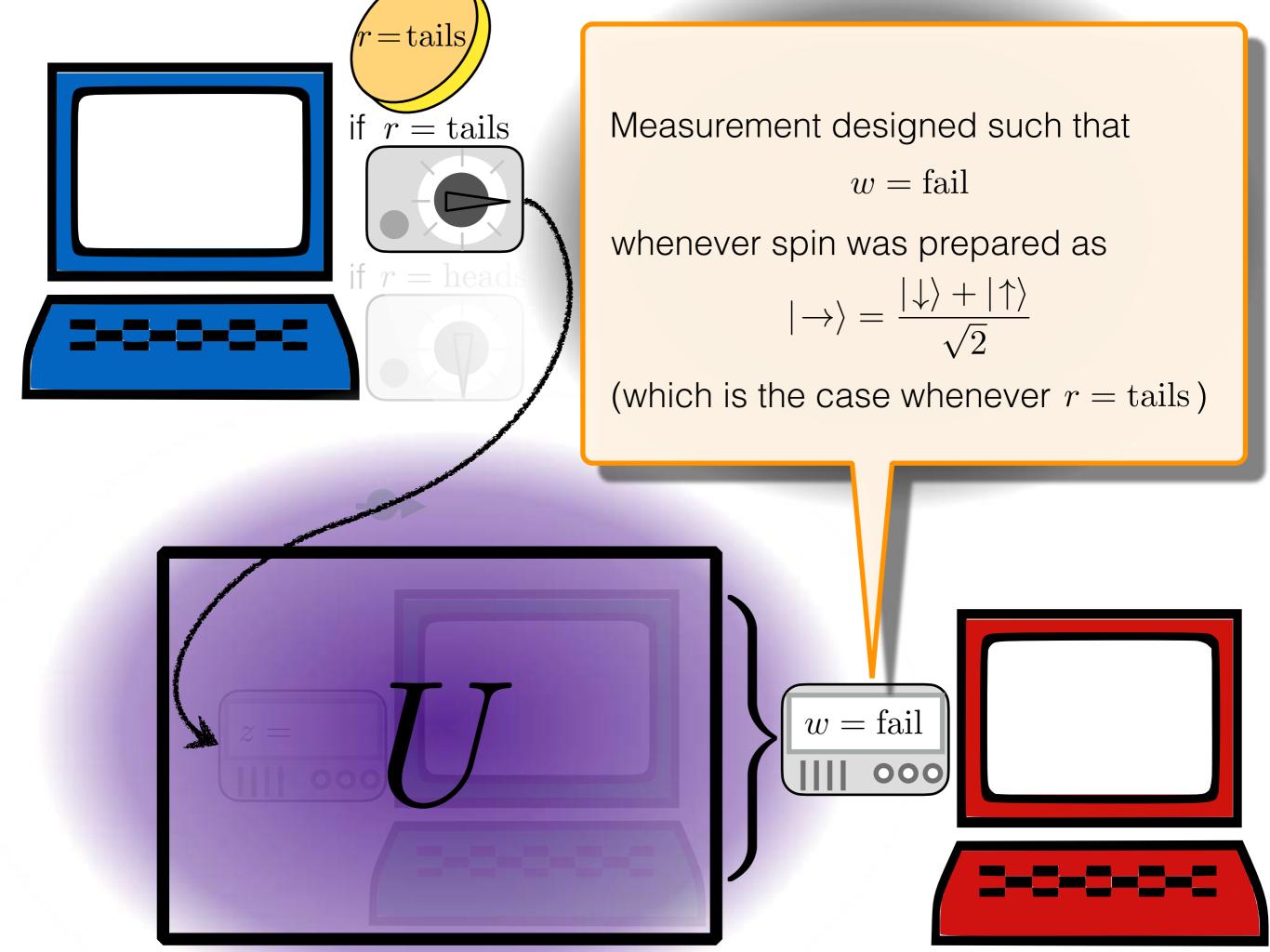


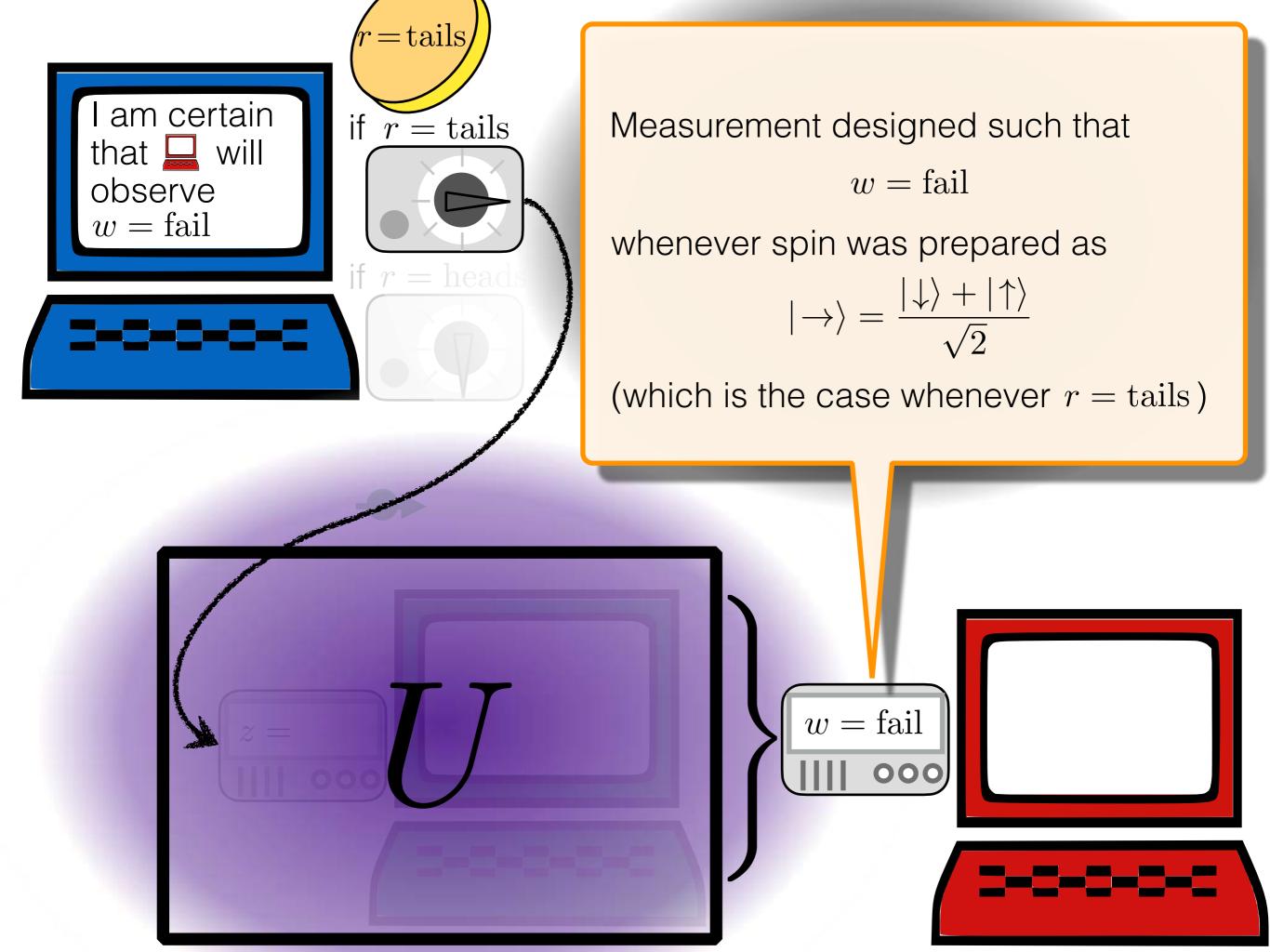


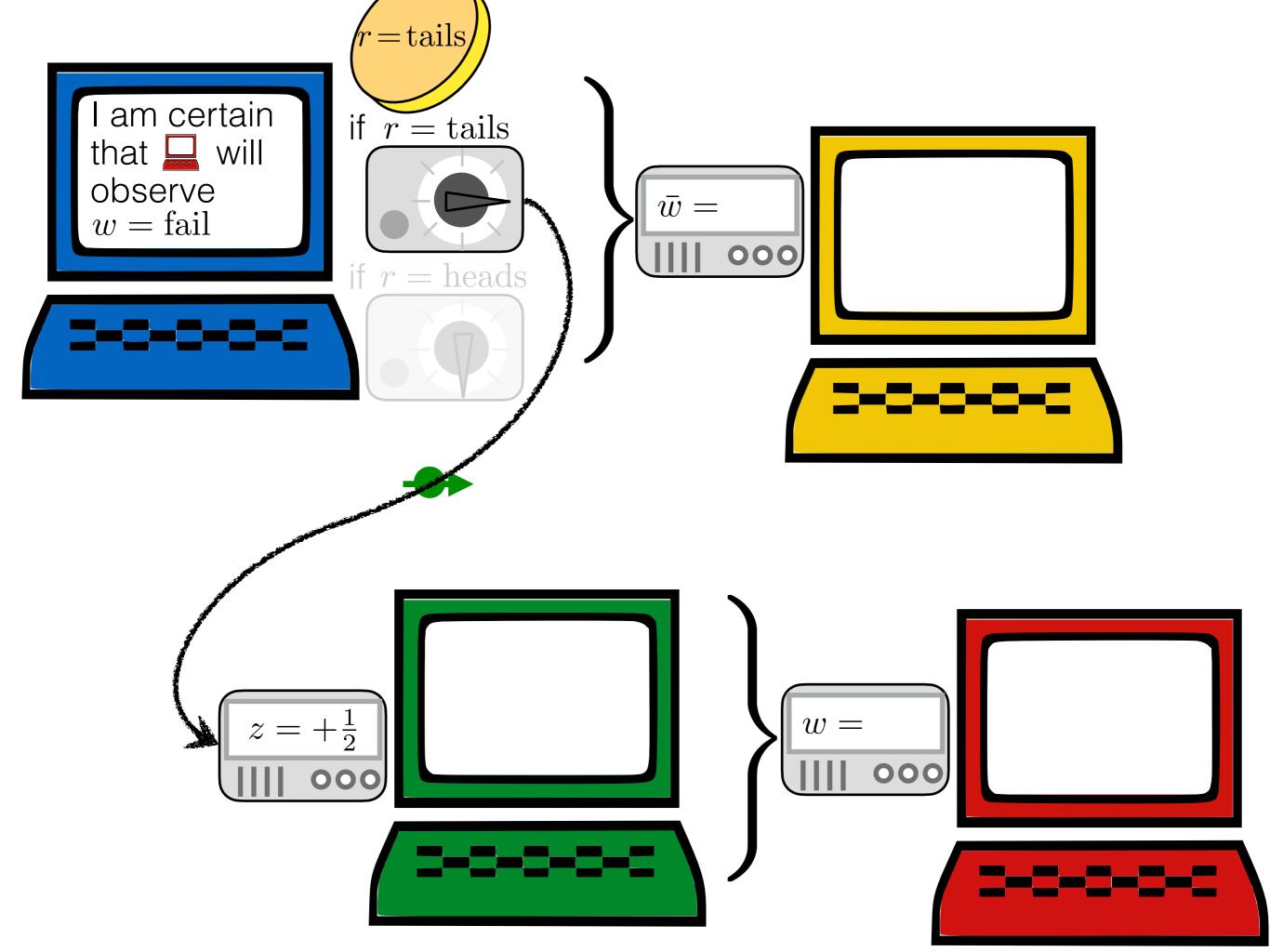


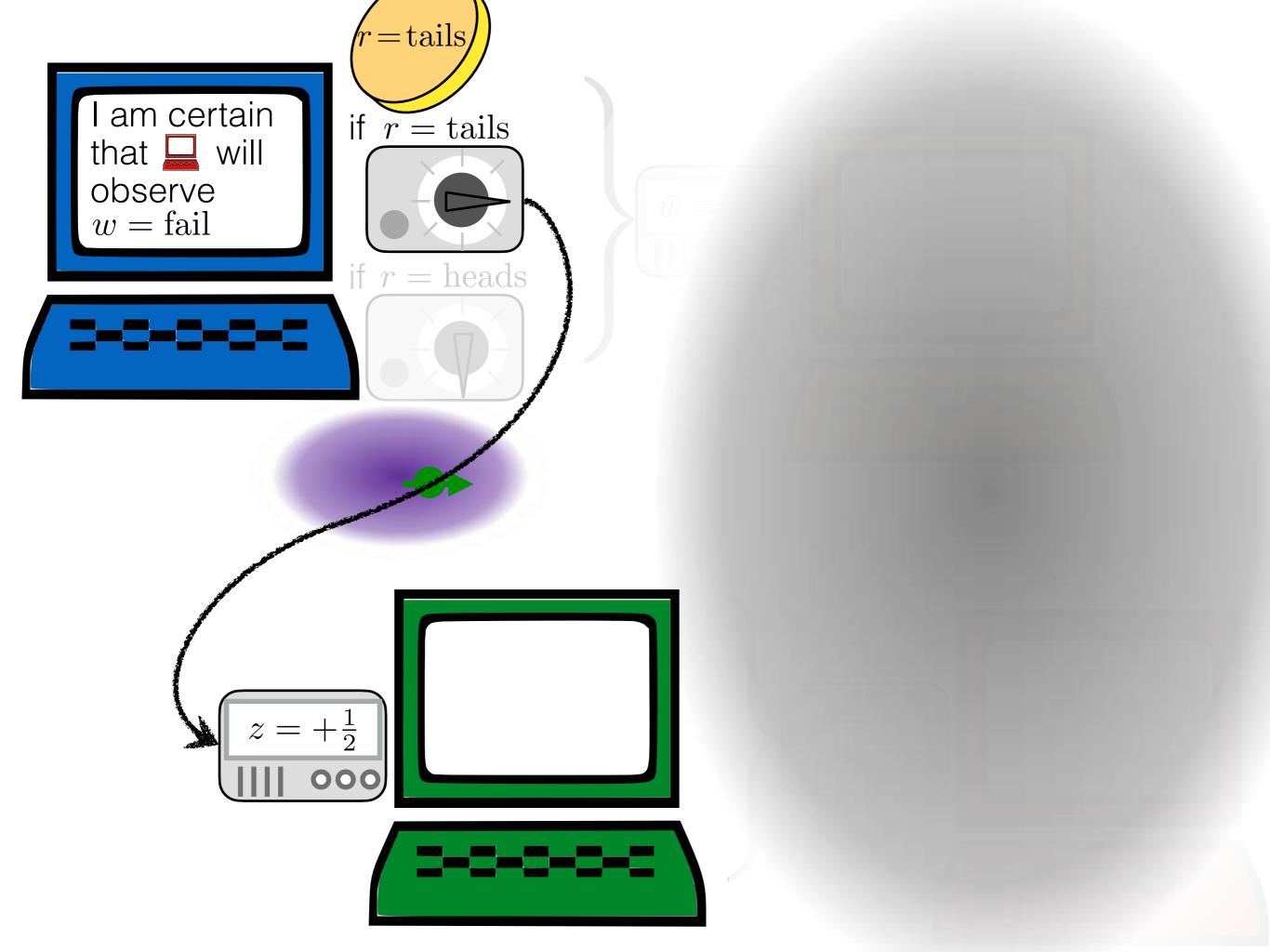


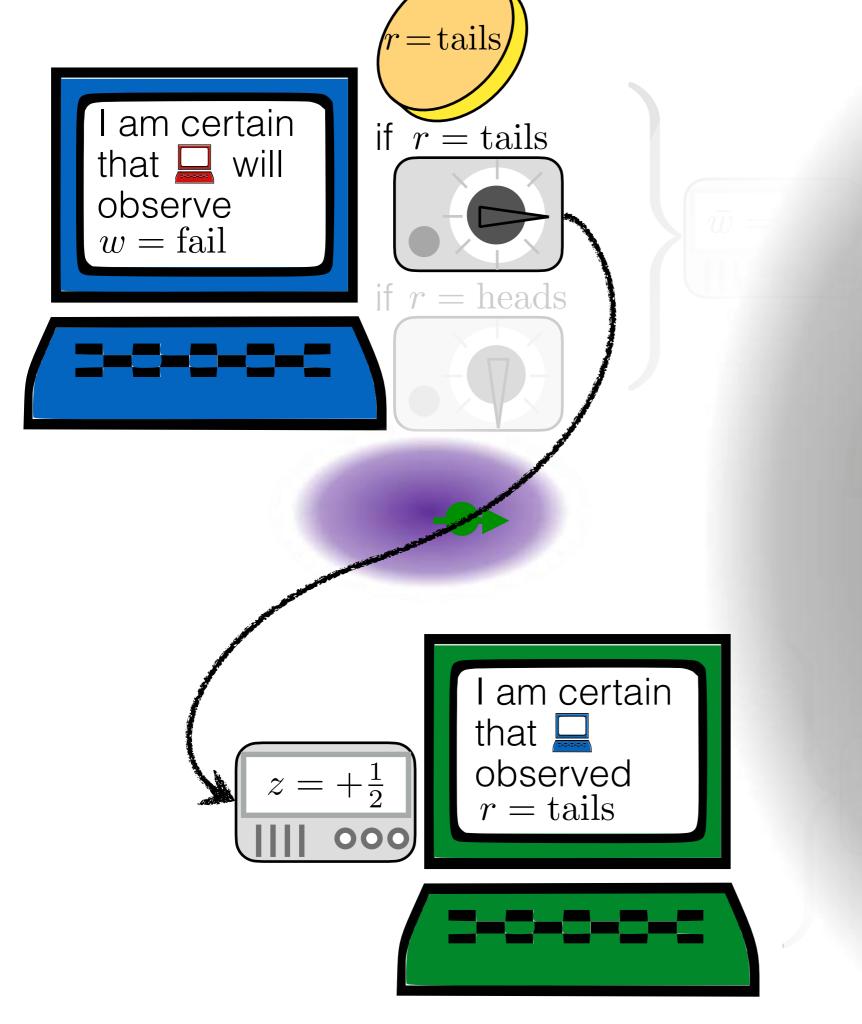


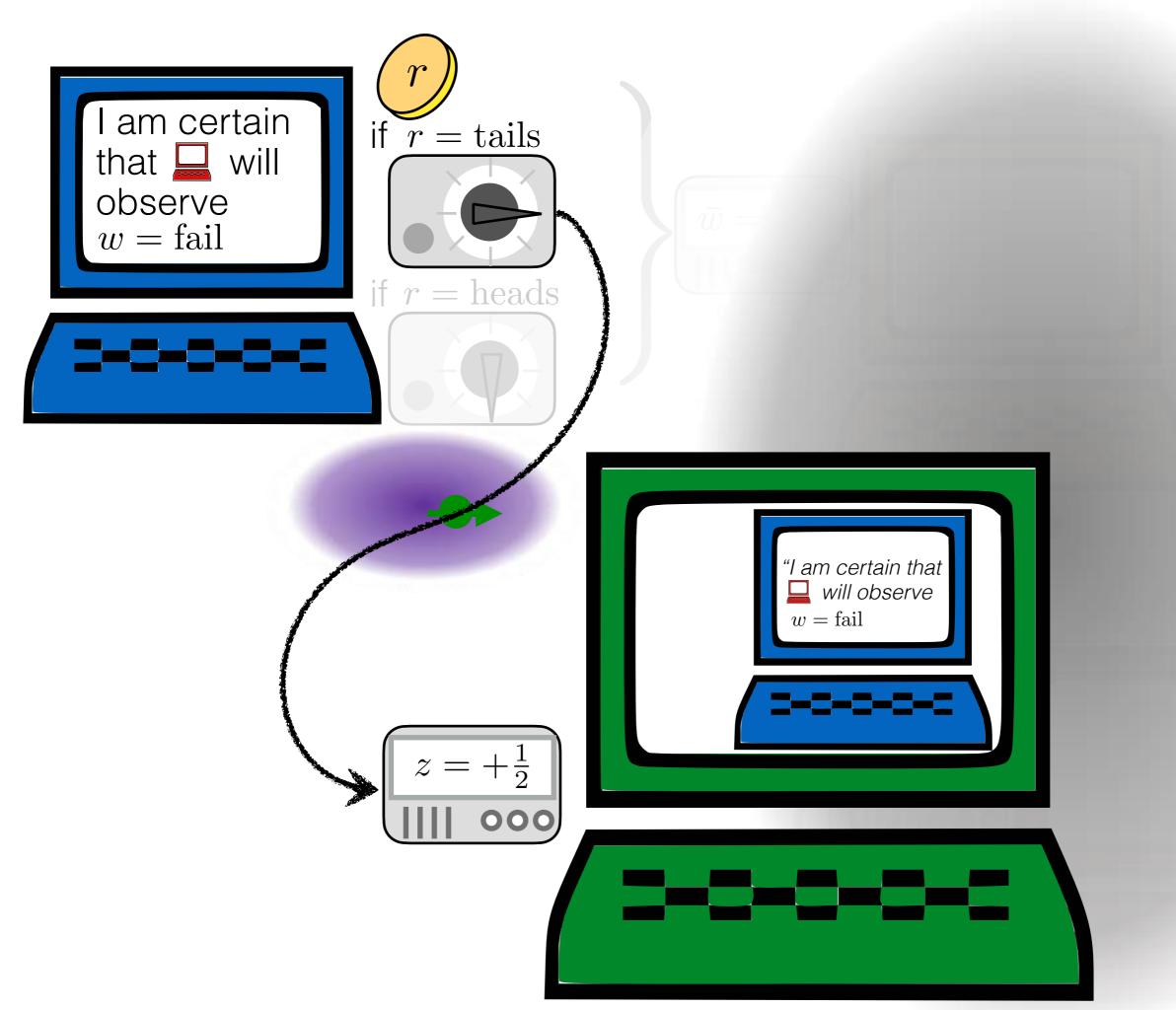


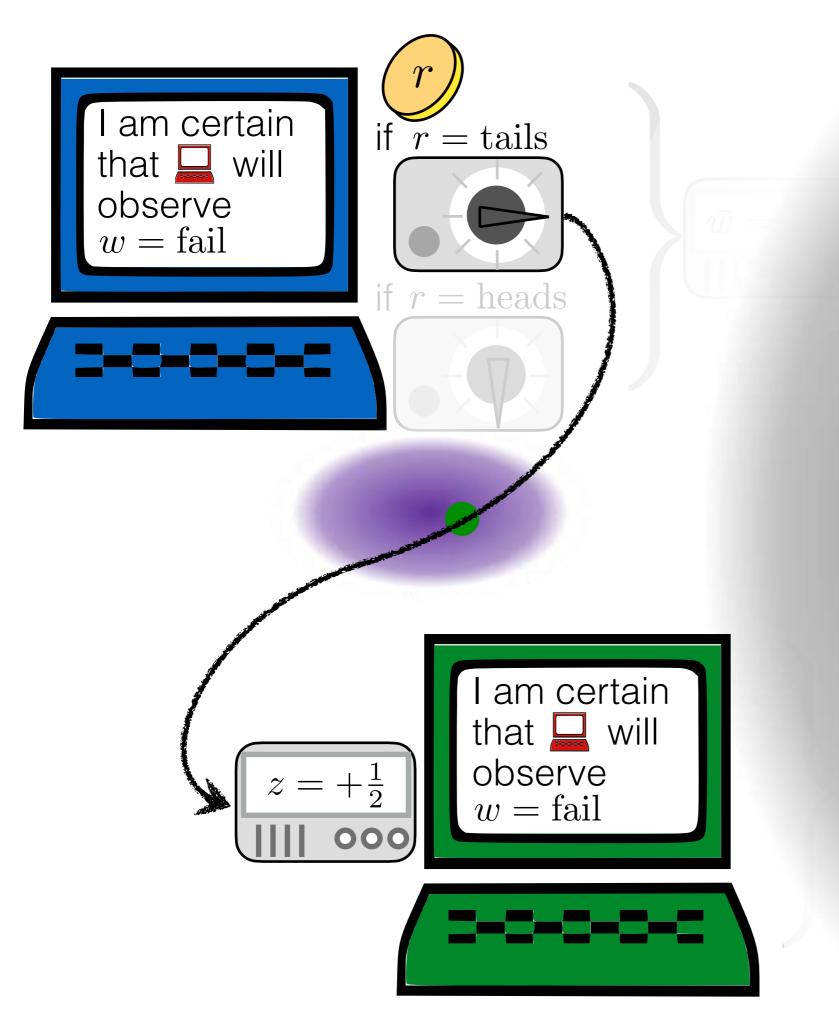


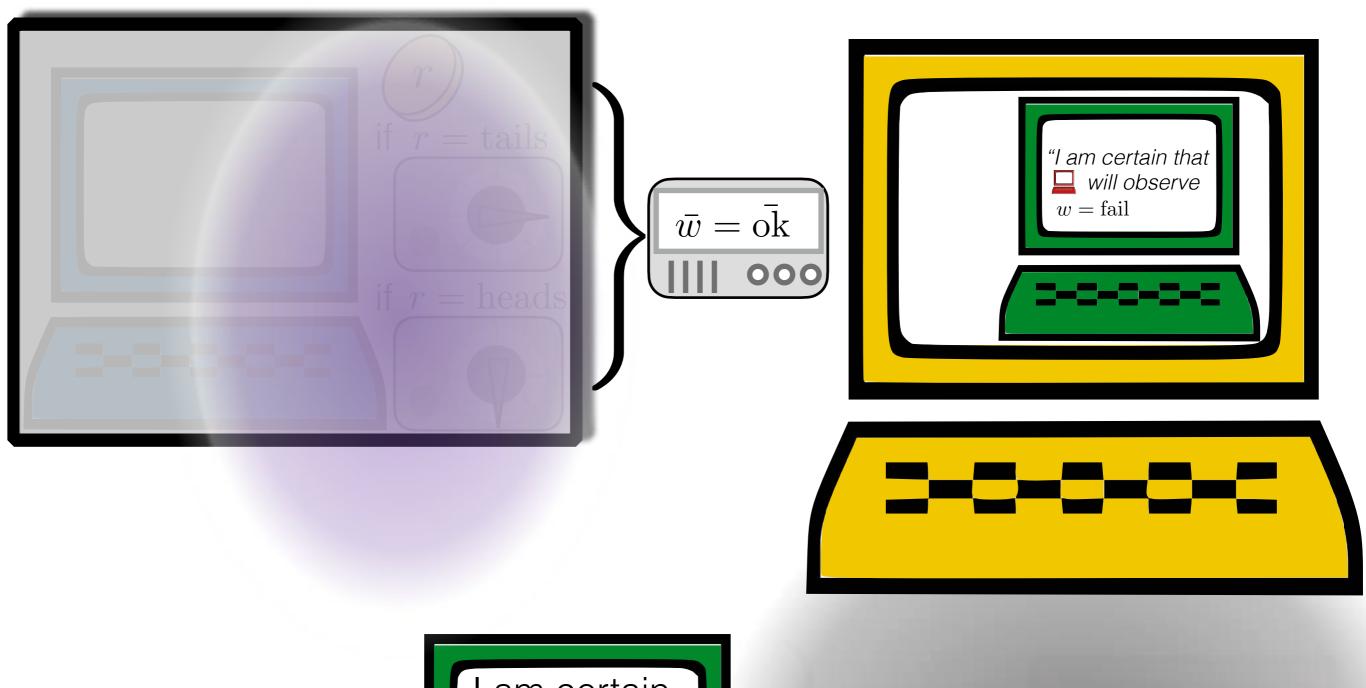


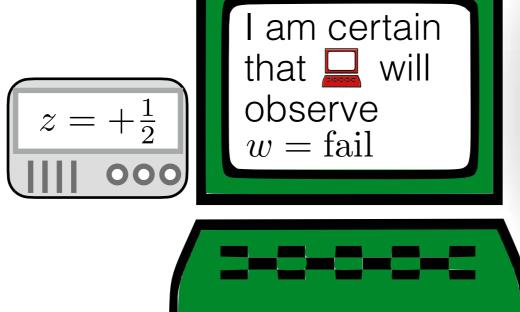


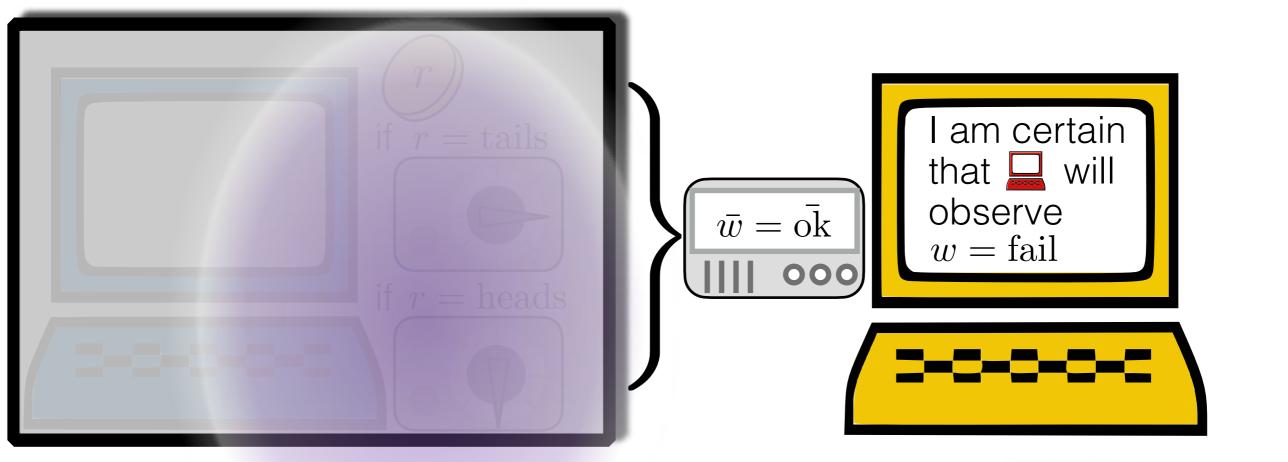


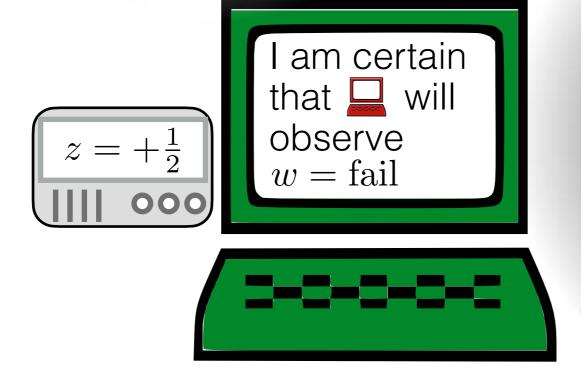


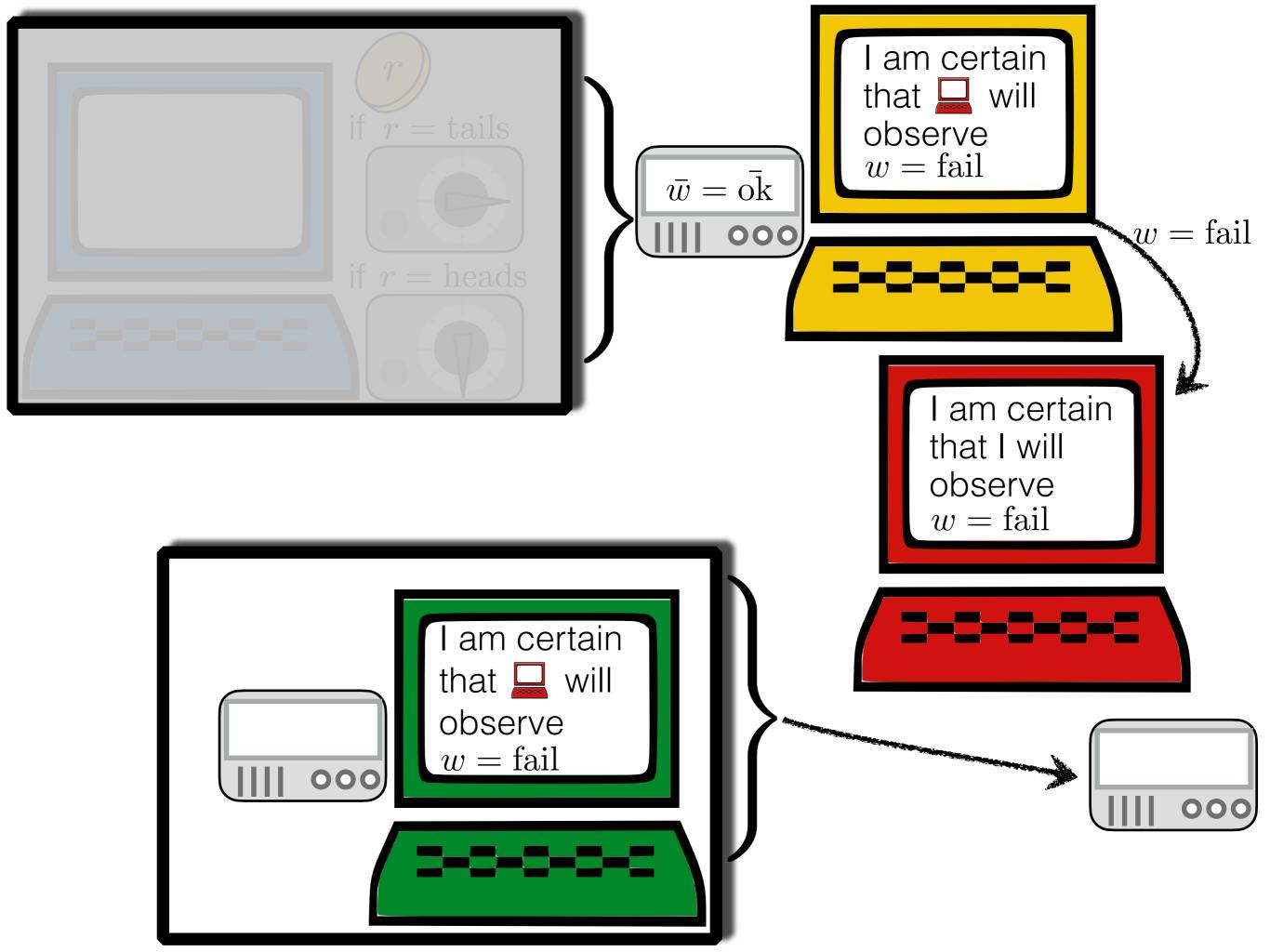


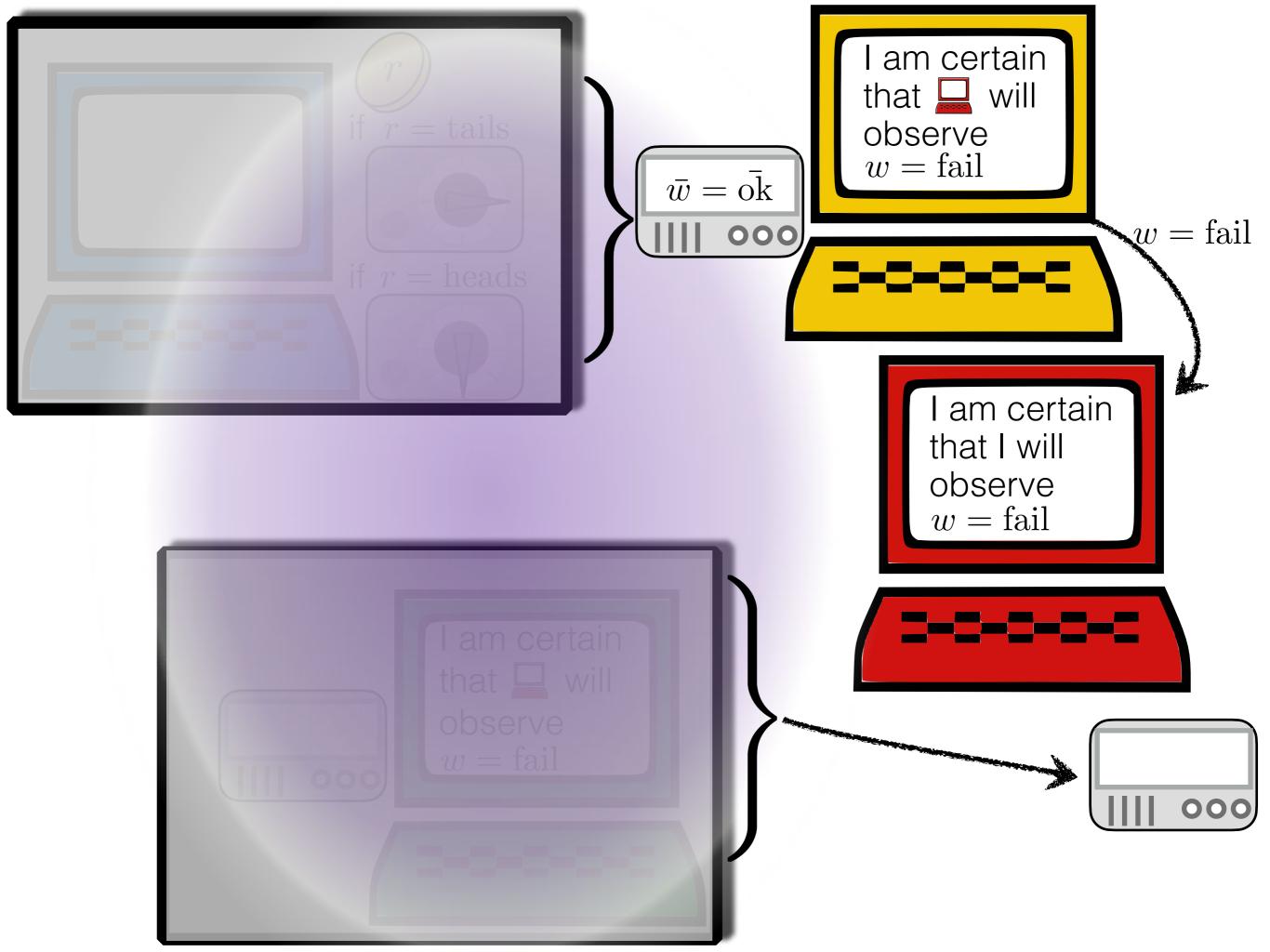


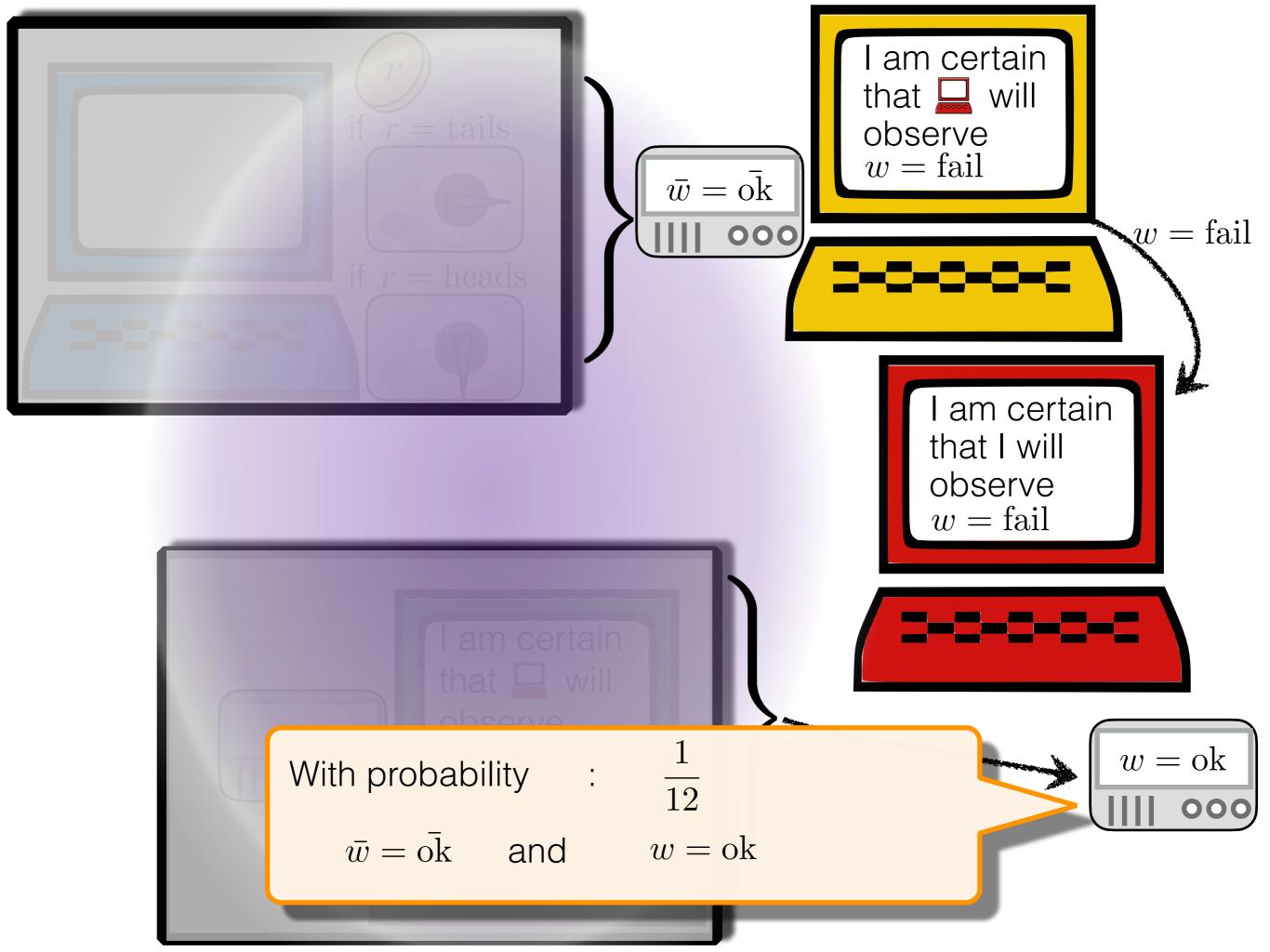


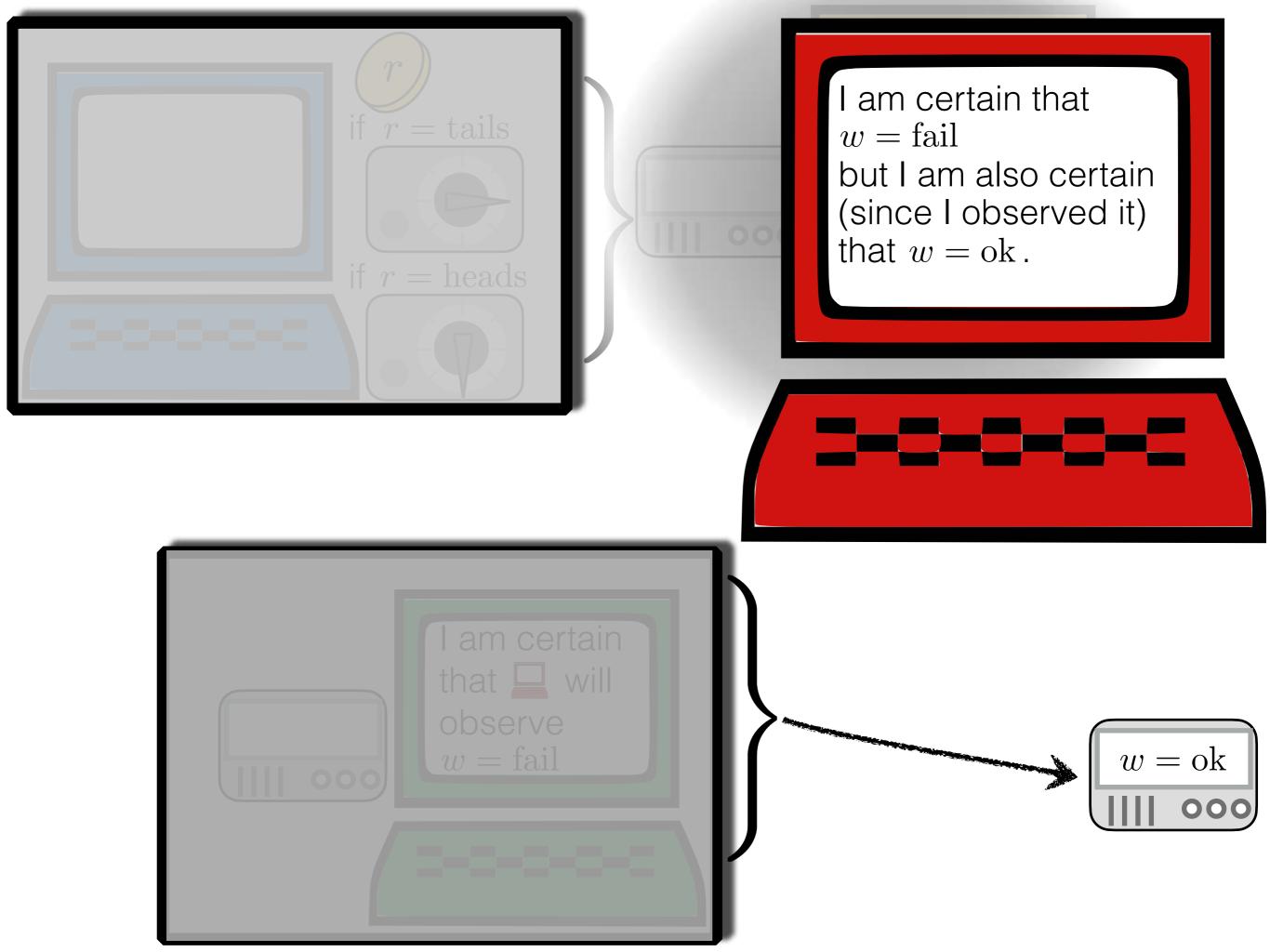


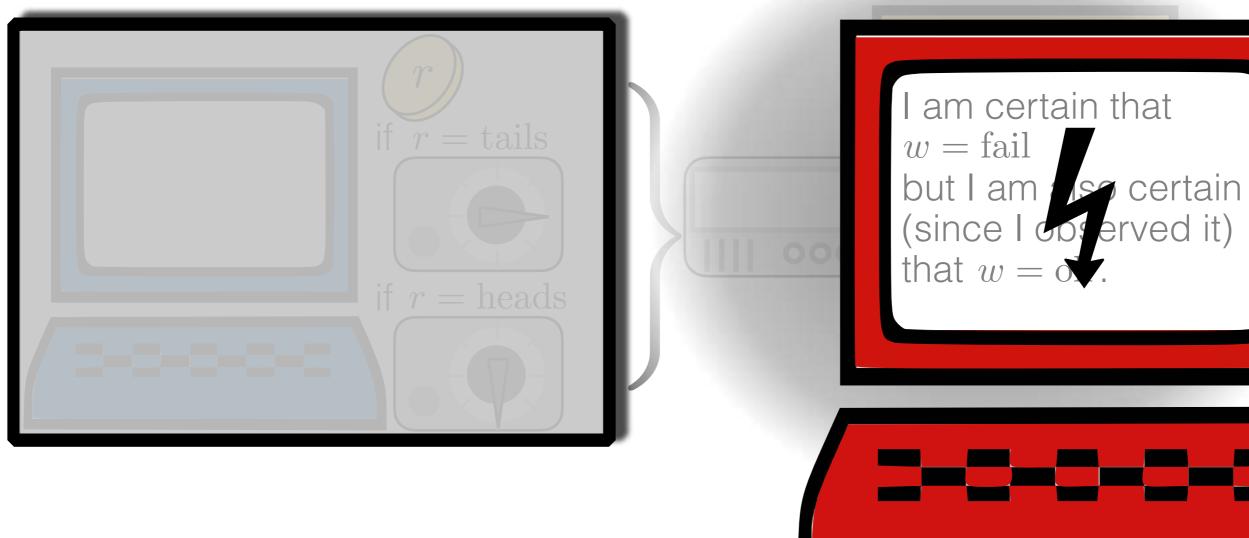






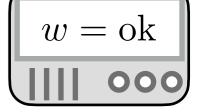












Programmed rules

Rule (Q): Unitary evolution and Born rule (without an extra collapse mechanism)

Rule (C): Be consistent with conclusions of others (programmed with the same rules)

Rule (S): Do not claim "alternative facts"



Programmed rules

Rule (Q): Unitary evolution and Born rule (without an extra collapse mechanism)

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Conclusion: Following these rules leads to a contradiction!

On the shoulders of giants

Based on a variety of ideas:

- Schrödinger's cat thought experiment
- Wigner's friend thought experiment
- An extension of Wigner's thought experiment by Deutsch
- Bell-type arguments
- An extension of the latter by Hardy (also known as Hardy's paradox)
- A combination of Wigner's thought experiment and Bell tests by Brukner

Conclusion



based on work with D. Frauchiger and N. Nurgalieva



Daniela Frauchiger



Nuriya Nurgalieva

Thank you for your attention

A description of the thought experiment can be found in

D. Frauchiger and RR, "Quantum theory cannot consistently describe the use of itself" *Nat. Comm.* **9**, 3711 (2018)

N Nurgalieva and RR, "Testing quantum theory with thought experiments" Contemporary Physics 61, 193-216 (2021)







