

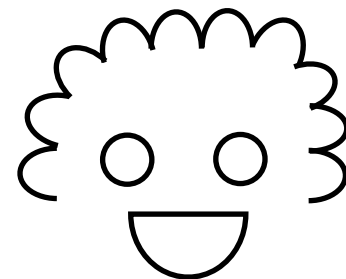
# Hyperbolic-like Encounters of Binary Black Holes with the numerical relativity code SpEC

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Albert Einstein Institute  
Potsdam

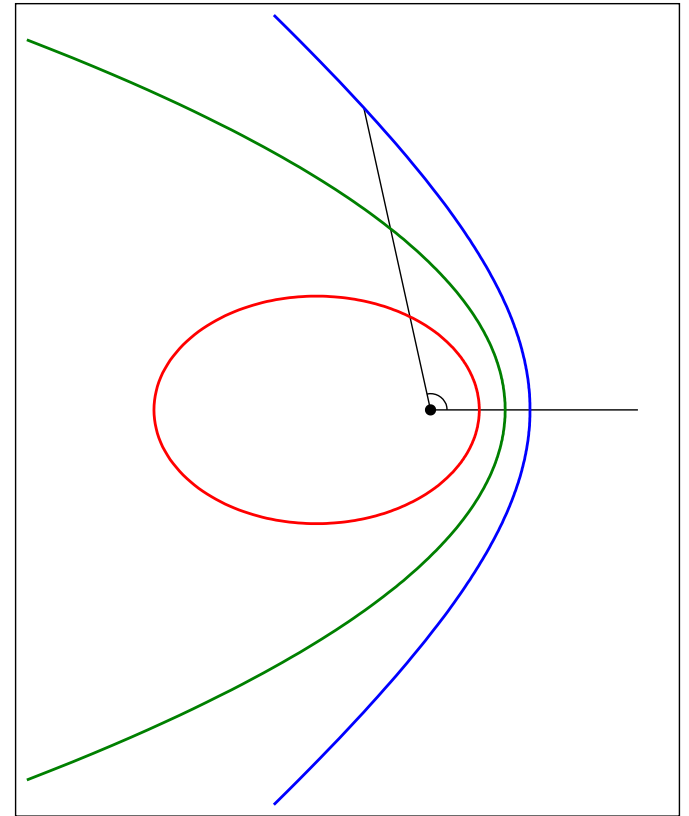


# Hyperbolic-like Encounters

Hyperbolic-like orbit  
= initially unbound orbit

$$E_{\text{orb}}(t = 0) > 0$$

Orbital parameters change  
due to gravitational wave  
emission



[https://en.wikipedia.org/wiki/File:Kepler\\_orbits.svg](https://en.wikipedia.org/wiki/File:Kepler_orbits.svg)

# Motivation

Hyperbolic-like encounters are astrophysically rare events

Mostly expected near the center of galaxies

Validation/Calibration of post-Newtonian and effective-one-body predictions [Damour - PRD 081503 (2014), Nagar - PRD 064013 (2021)]

# Setup

## Spectral Einstein Code (SpEC)

<https://www.black-holes.org/code/SpEC.html> [CQG 36, 195006 (2019)]

Evolve spacetime with  
Generalized Harmonic Gauge (GHG) system

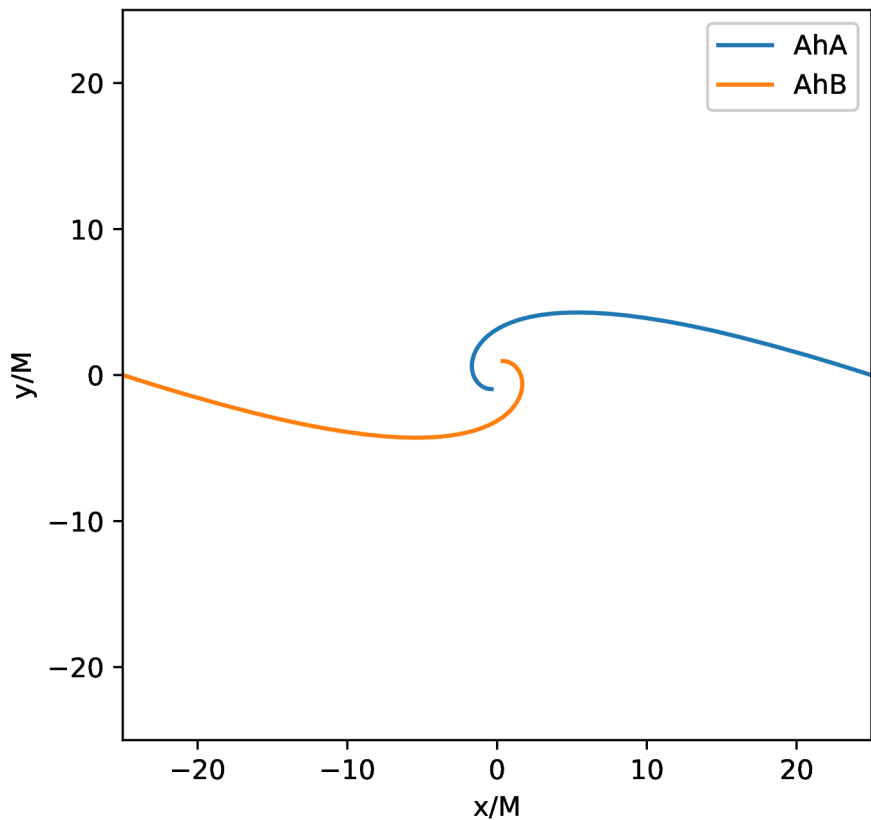
Damped Harmonic Gauge

Equal mass binary:  $m_A = m_B = 0.5M$

No spin

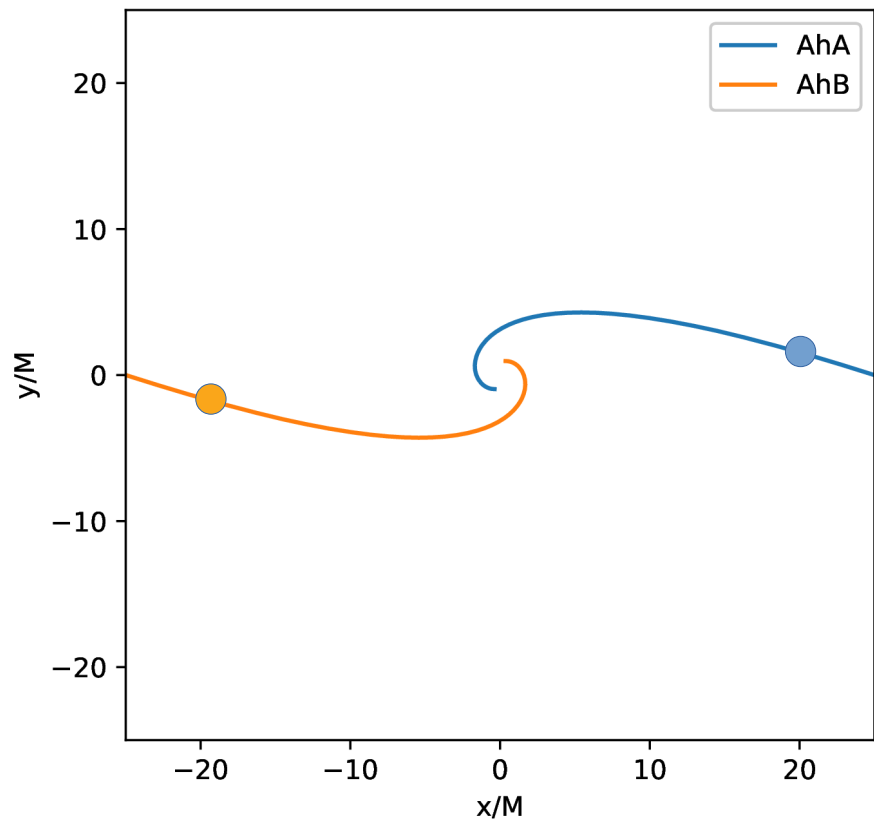
$$E_{\text{orb}} = 0.00052 M$$

$$J_{\text{orb}} = 0.85 M^2$$



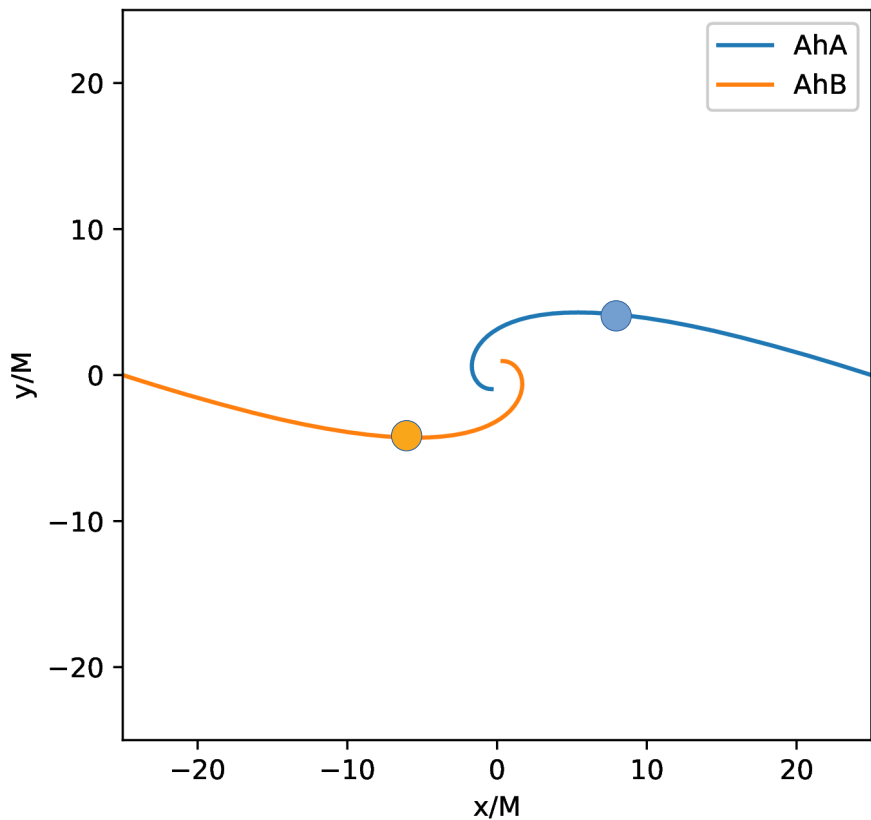
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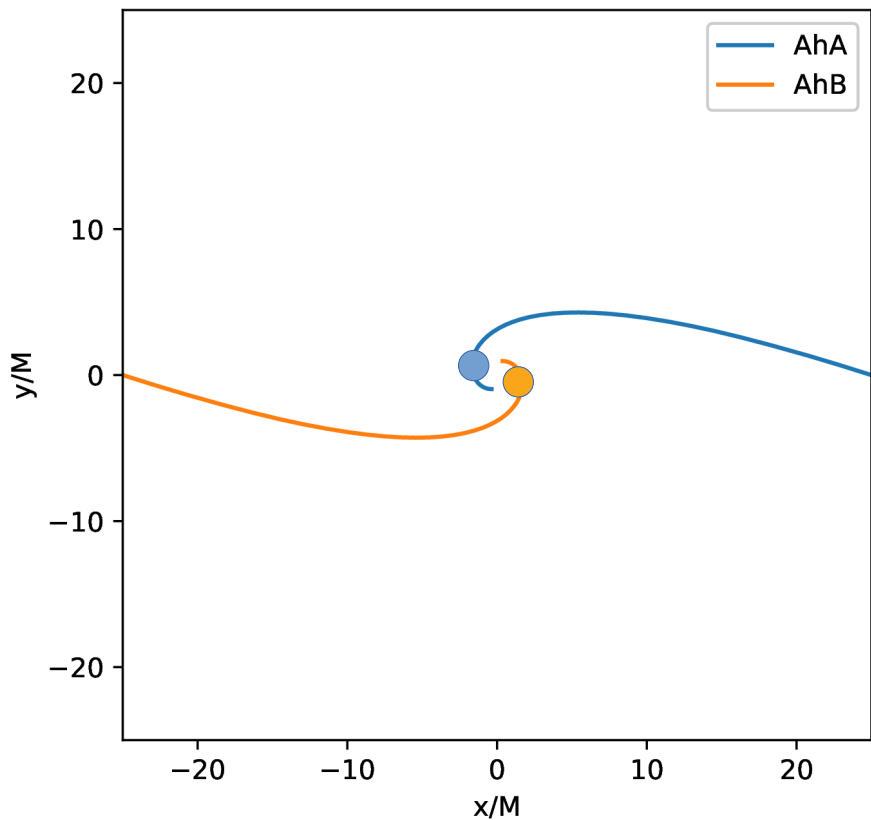
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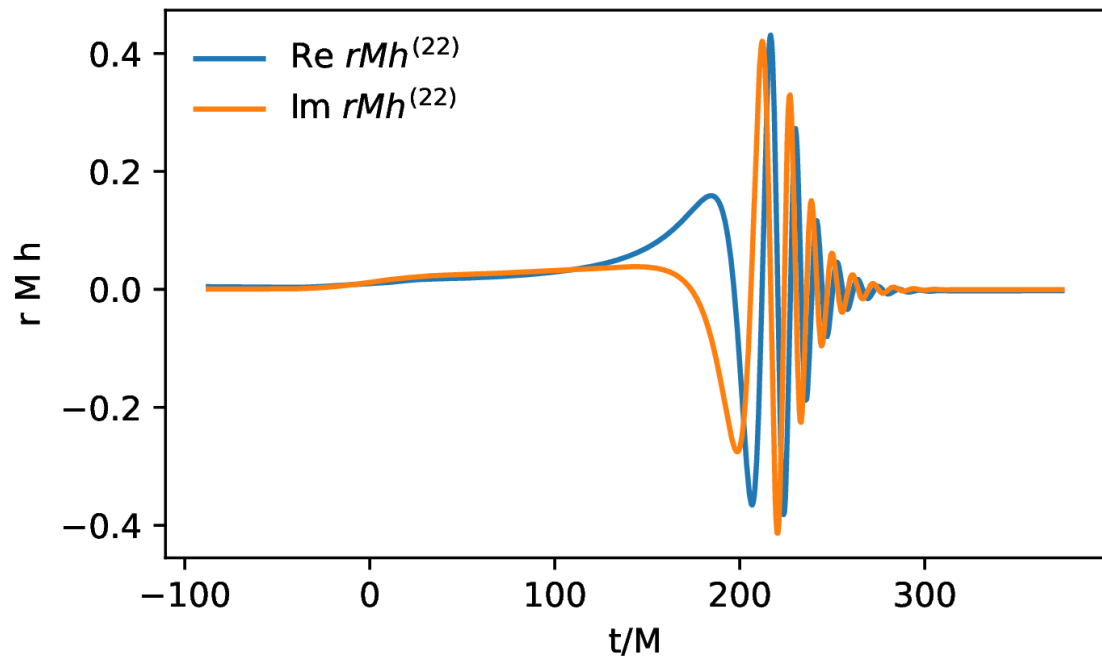
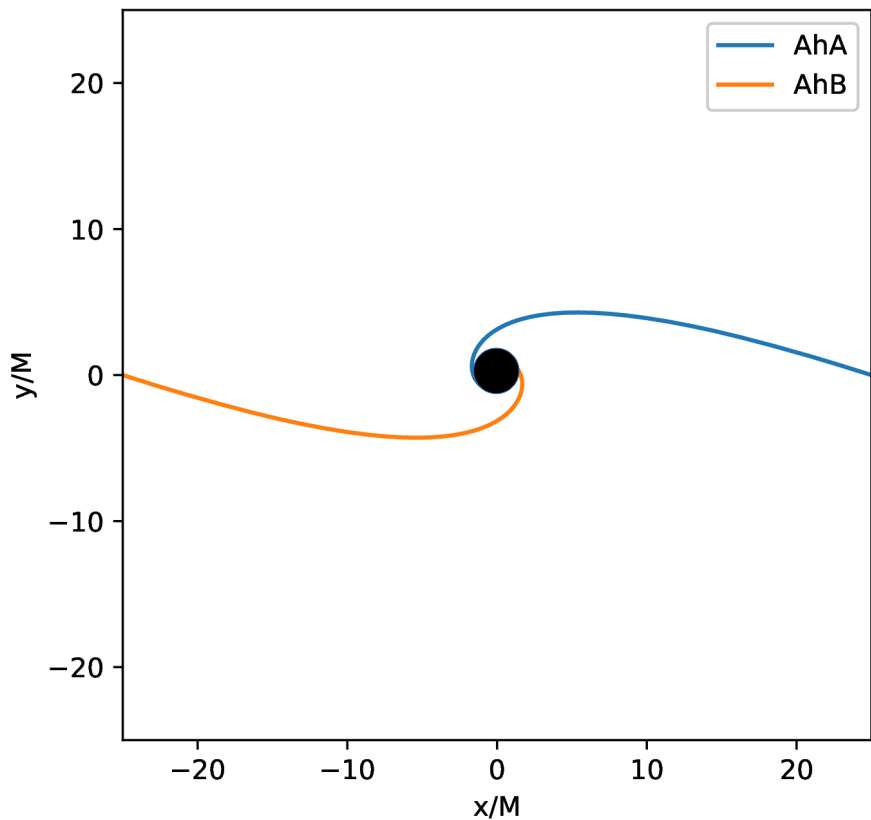
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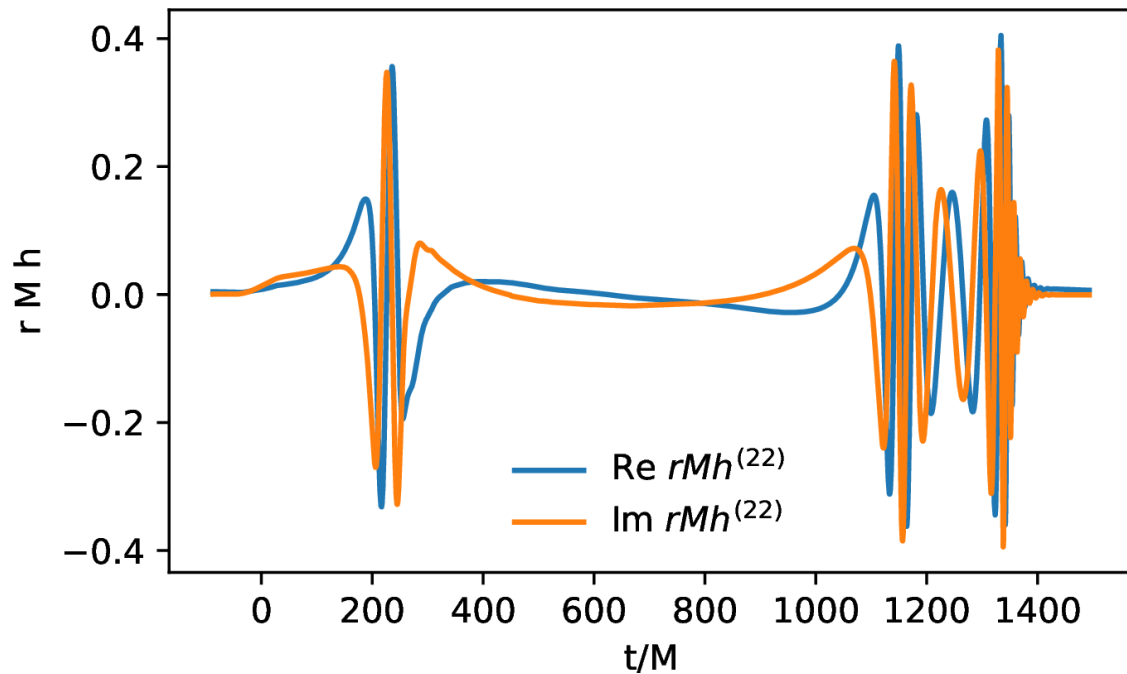
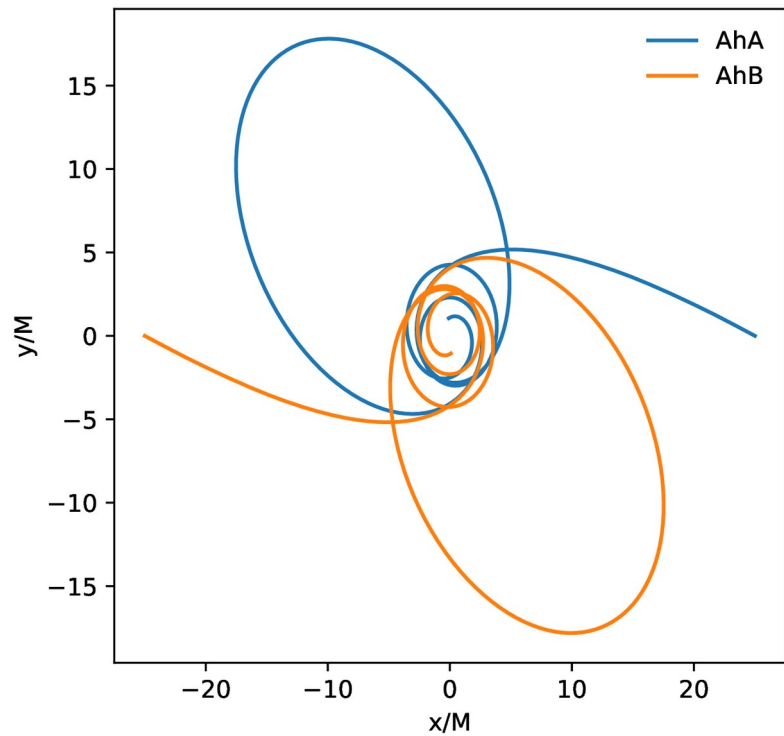
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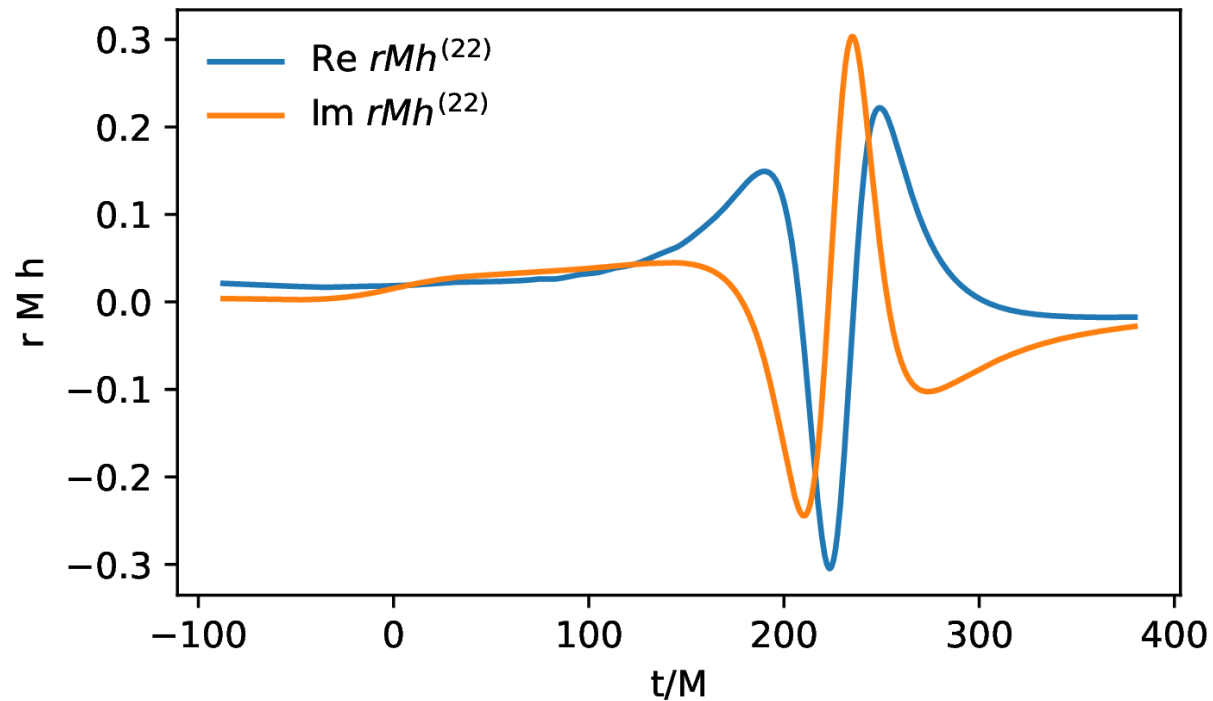
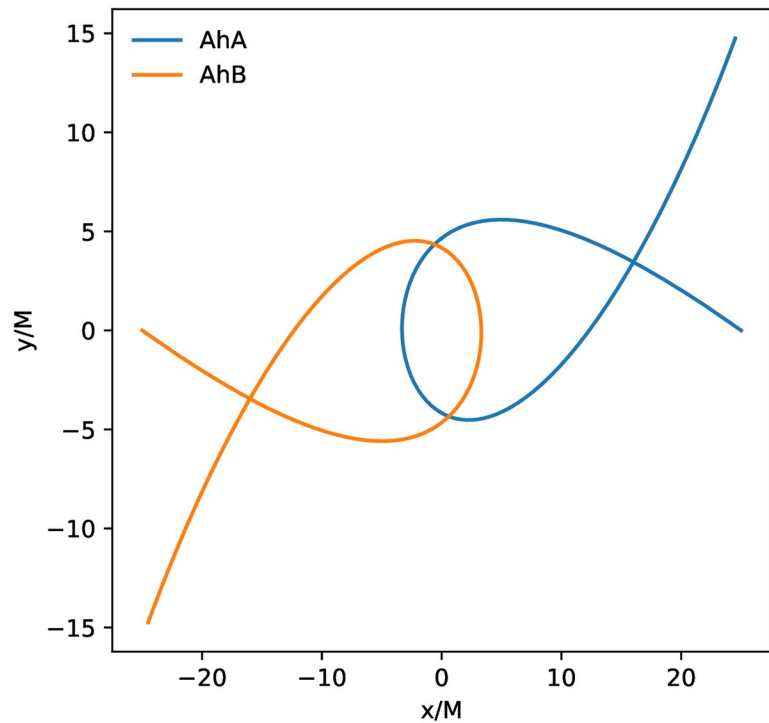
$$E_{\text{orb}} = 0.00052 M$$

$$J_{\text{orb}} = 1.007 M^2$$



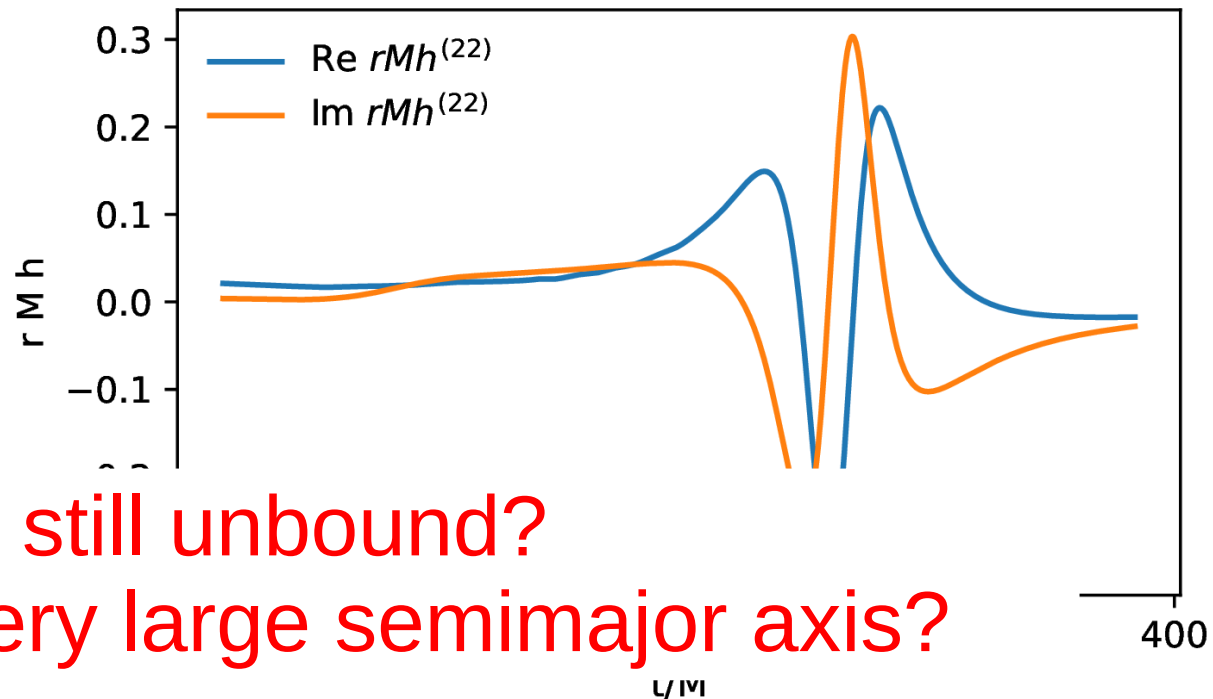
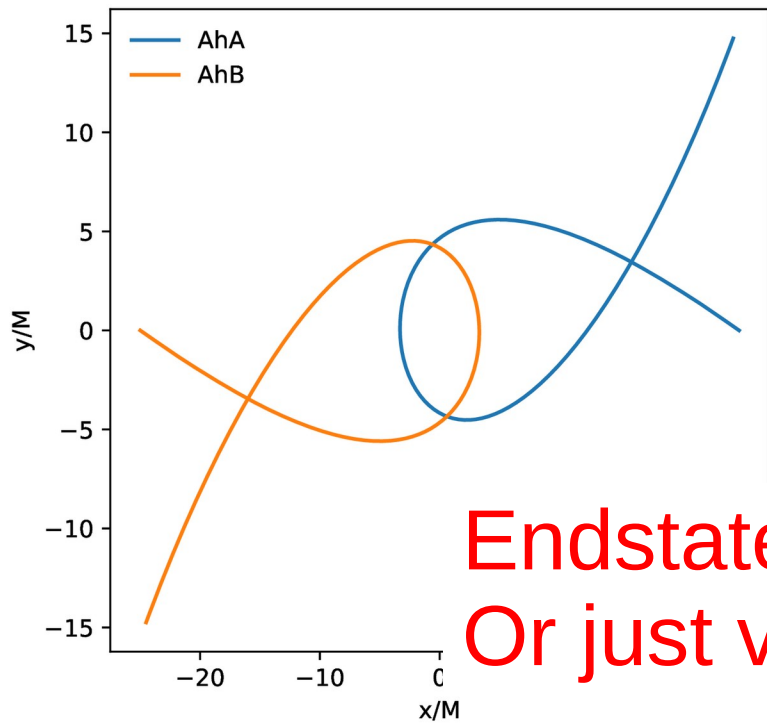
$$E_{\text{orb}} = 0.00052 M$$

$$J_{\text{orb}} = 1.076 M^2$$



$$E_{\text{orb}} = 0.00052 M$$

$$J_{\text{orb}} = 1.076 M^2$$



Endstate still unbound?  
Or just very large semimajor axis?

# Computation of Orbital Energy

Coevolve harmonic coordinates  $X^\mu$

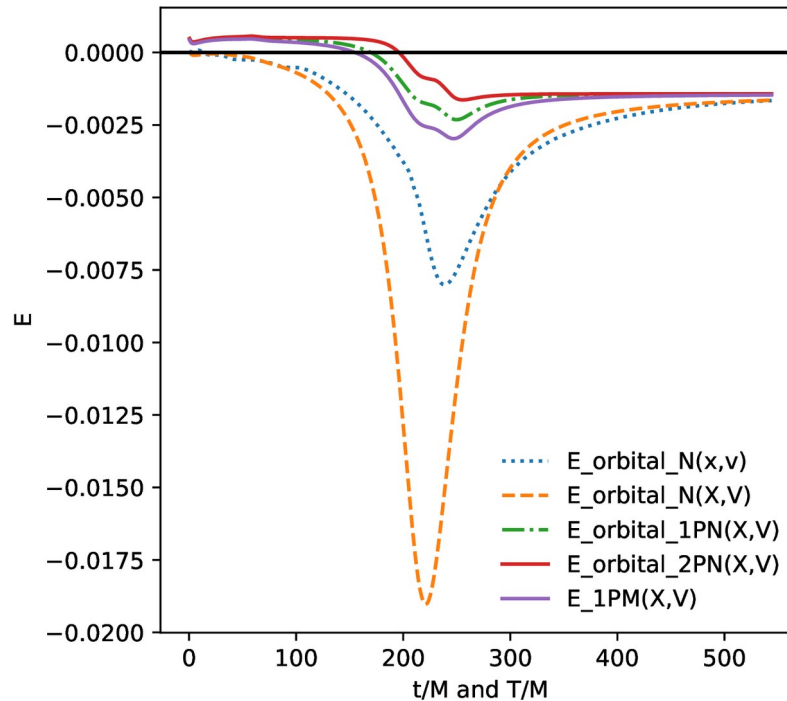
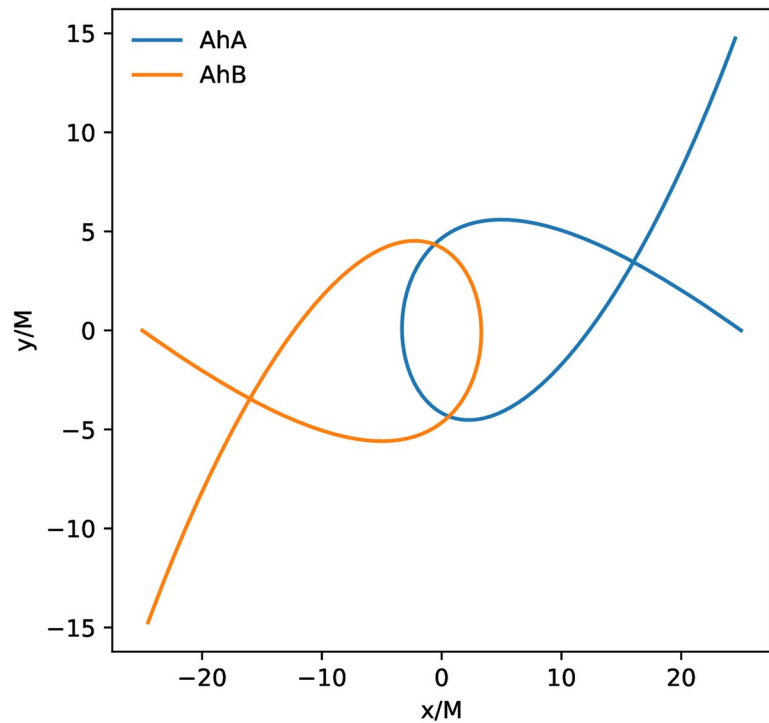
[Prayush Kumar]

Use PN expressions for orbits in harmonic coordinates [Memmesheimer - PRD 104011 (2004)]

$$\rightarrow E_{\text{orb}}(X^\mu, V^\mu) \quad J_{\text{orb}}(X^\mu, V^\mu)$$

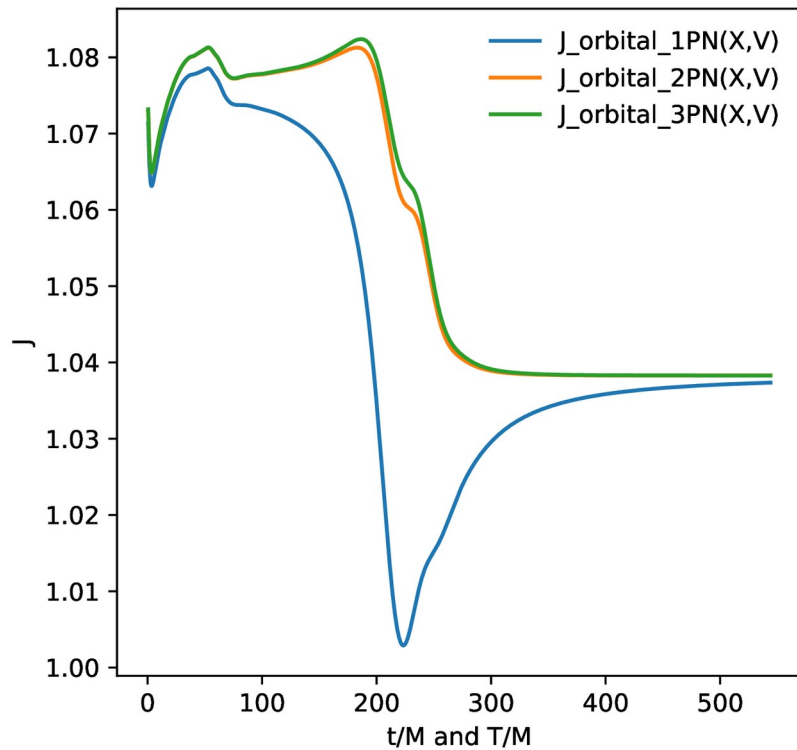
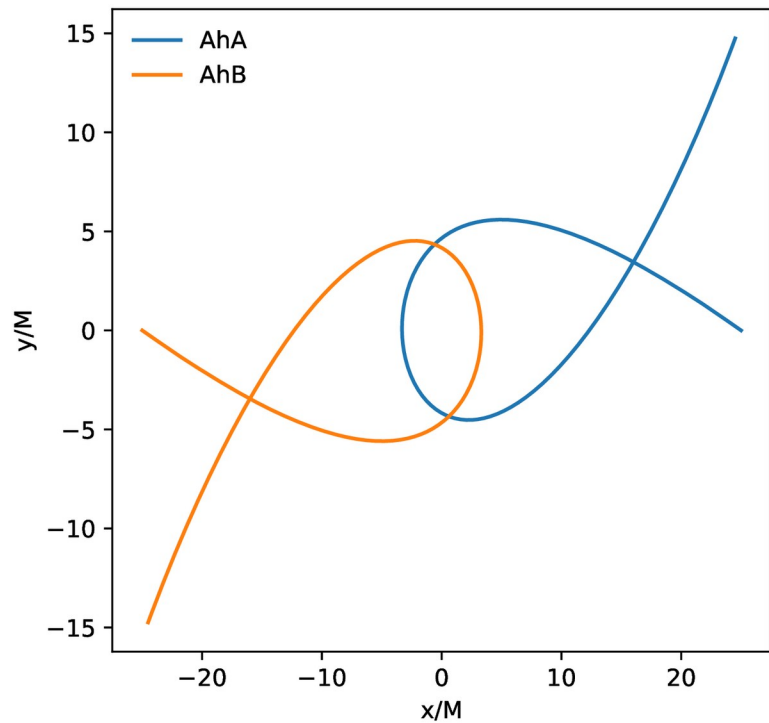
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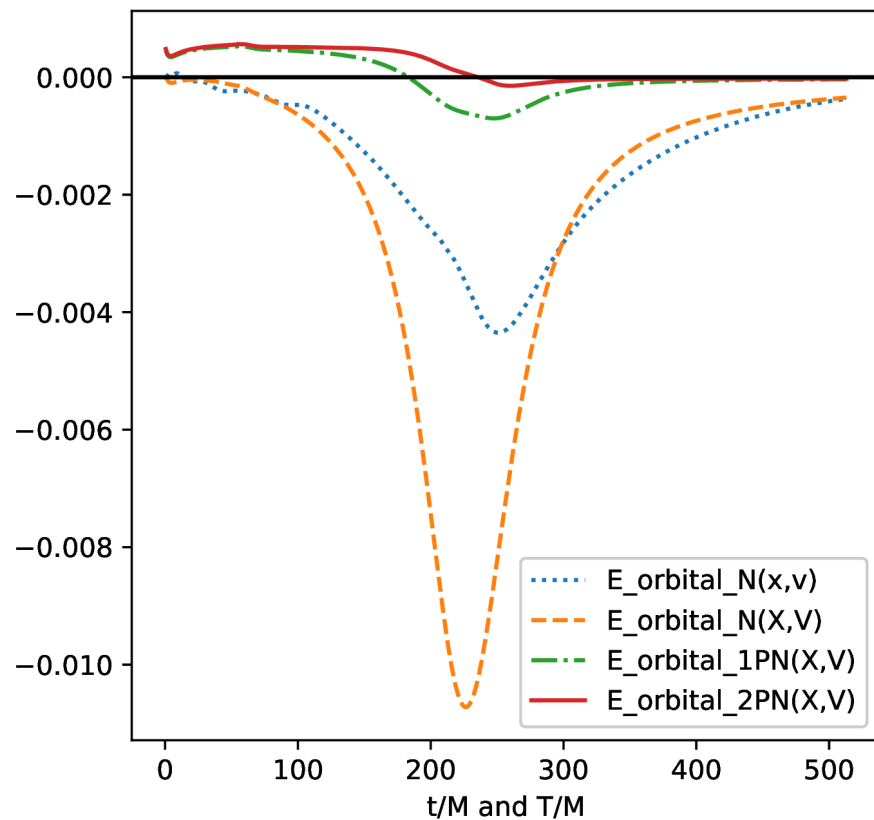
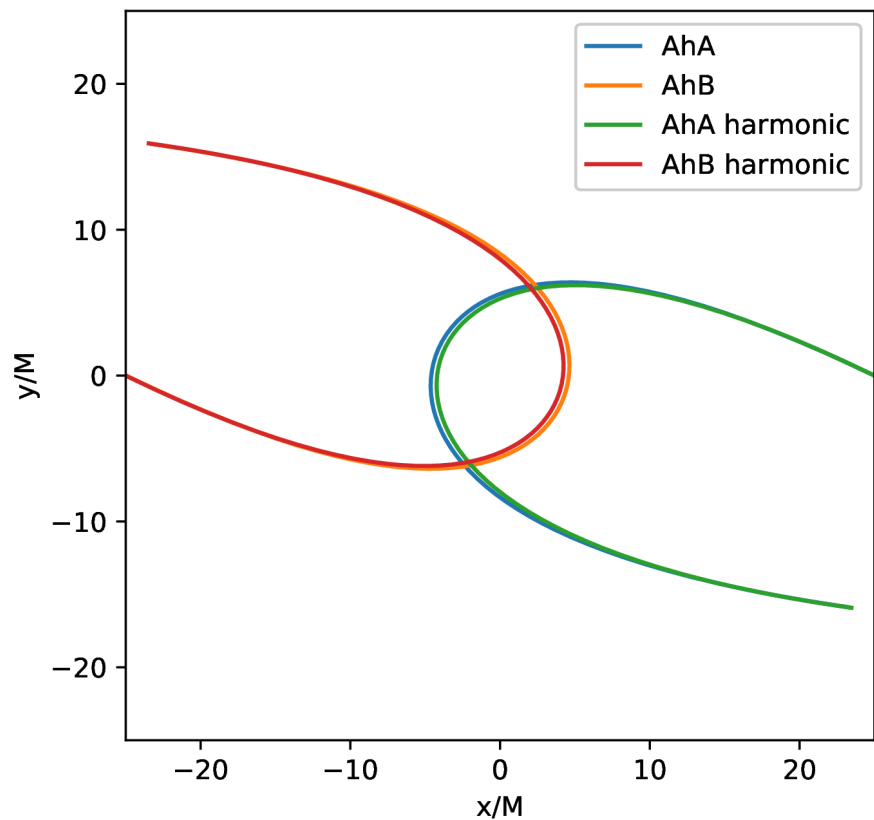
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$$J_{\text{orb}} = 1.076 M^2$$



$$E_{\text{orb}} = 0.00052 M$$

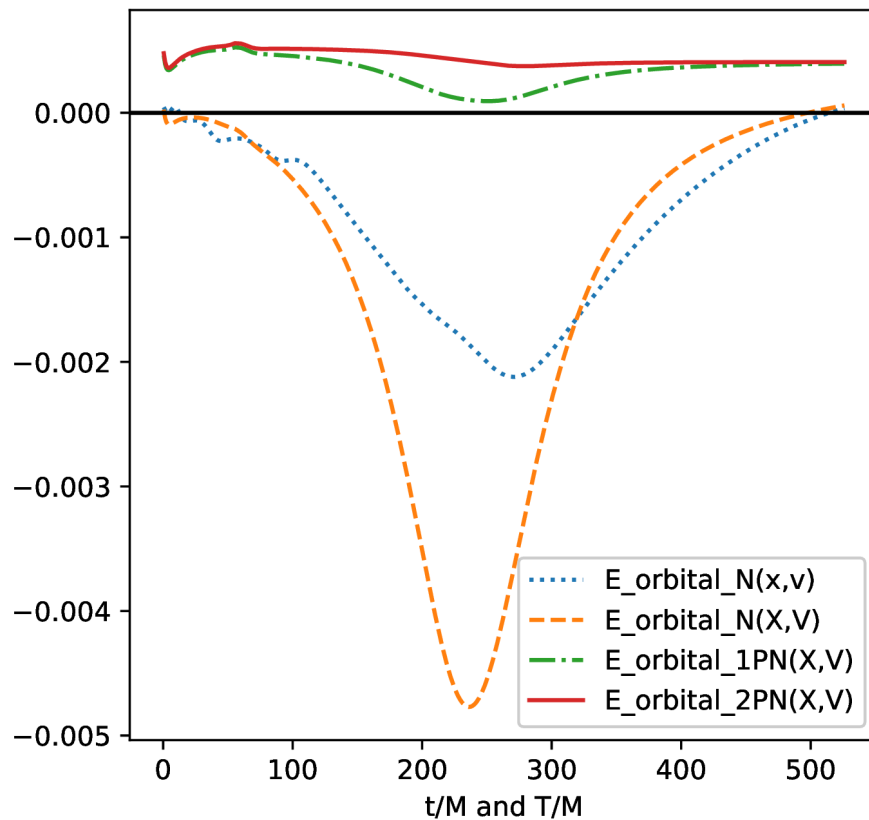
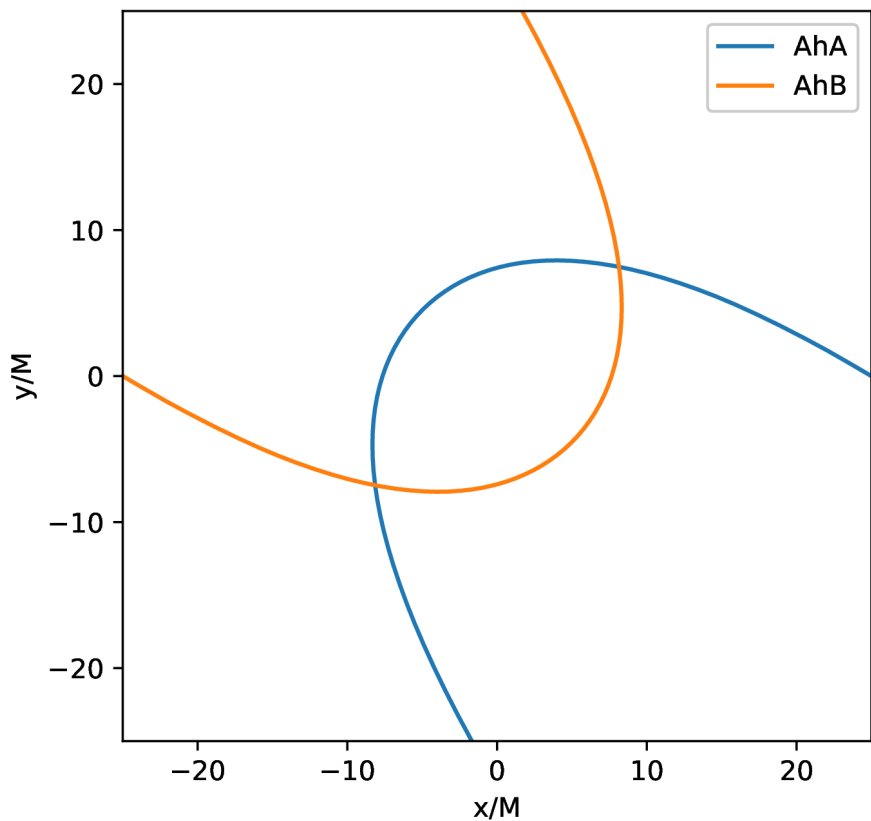
$$J_{\text{orb}} = 1.204 M^2$$





$$E_{\text{orb}} = 0.00052 M$$

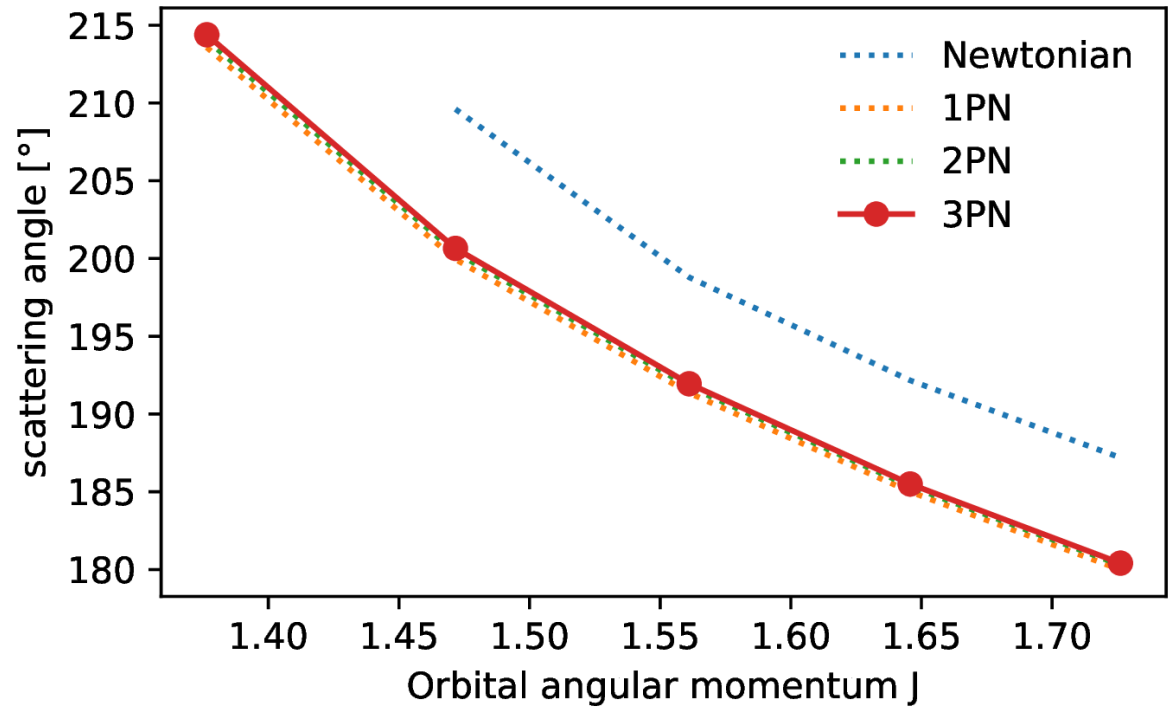
$$J_{\text{orb}} = 1.425 M^2$$



# Scattering Angle: $E_{\text{orb}} = 0.000157 M$

Extrapolate orbit to  $t=\pm\infty$

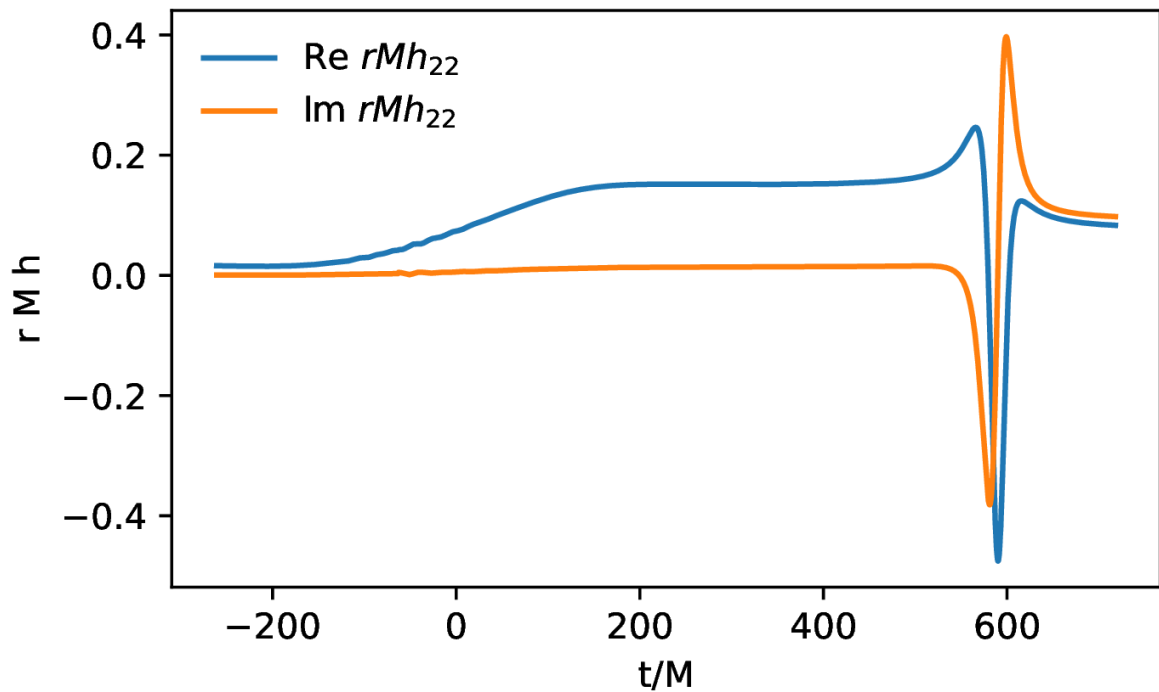
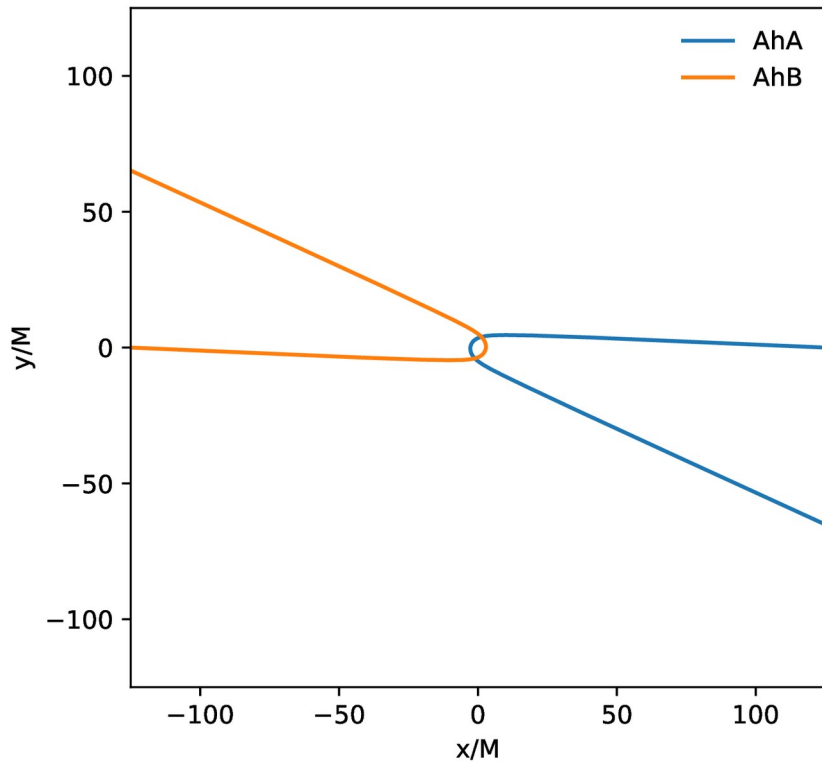
# \$  
%  
&' \$\$ \$ ! ( )  
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Towards Higher Energies

$$E_{\text{orb}} = 0.0226 M$$

$$J_{\text{orb}} = 1.145 M^2$$



# Scattering Angle: $E_{\text{orb}} = 0.0226 M$

## Damour NR

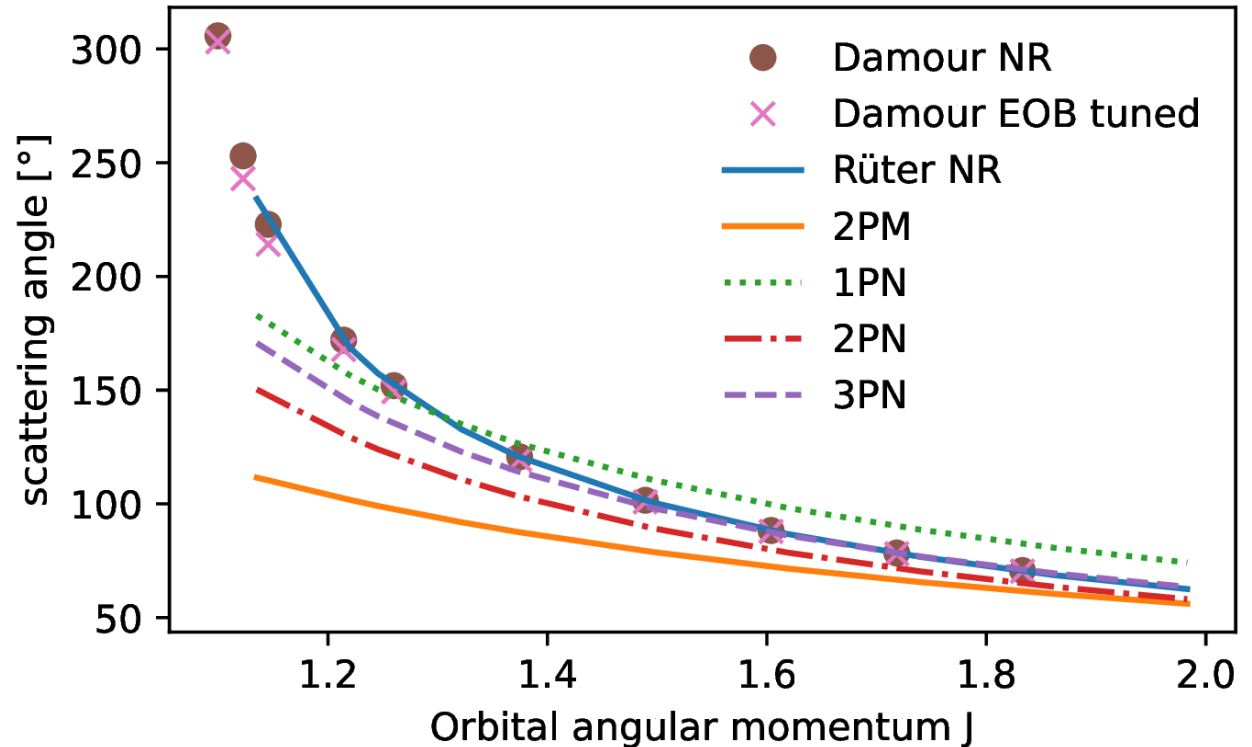
Damour - PRD 89,  
081503 (2014)

## Damour EOB tuned

Nagar - PRD 103,  
064013 (2021)

## PN

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! ( - . /



# Challenges when simulating hyperbolic-like encounters

# Challenges

## Coordinates

Use defined coordinates

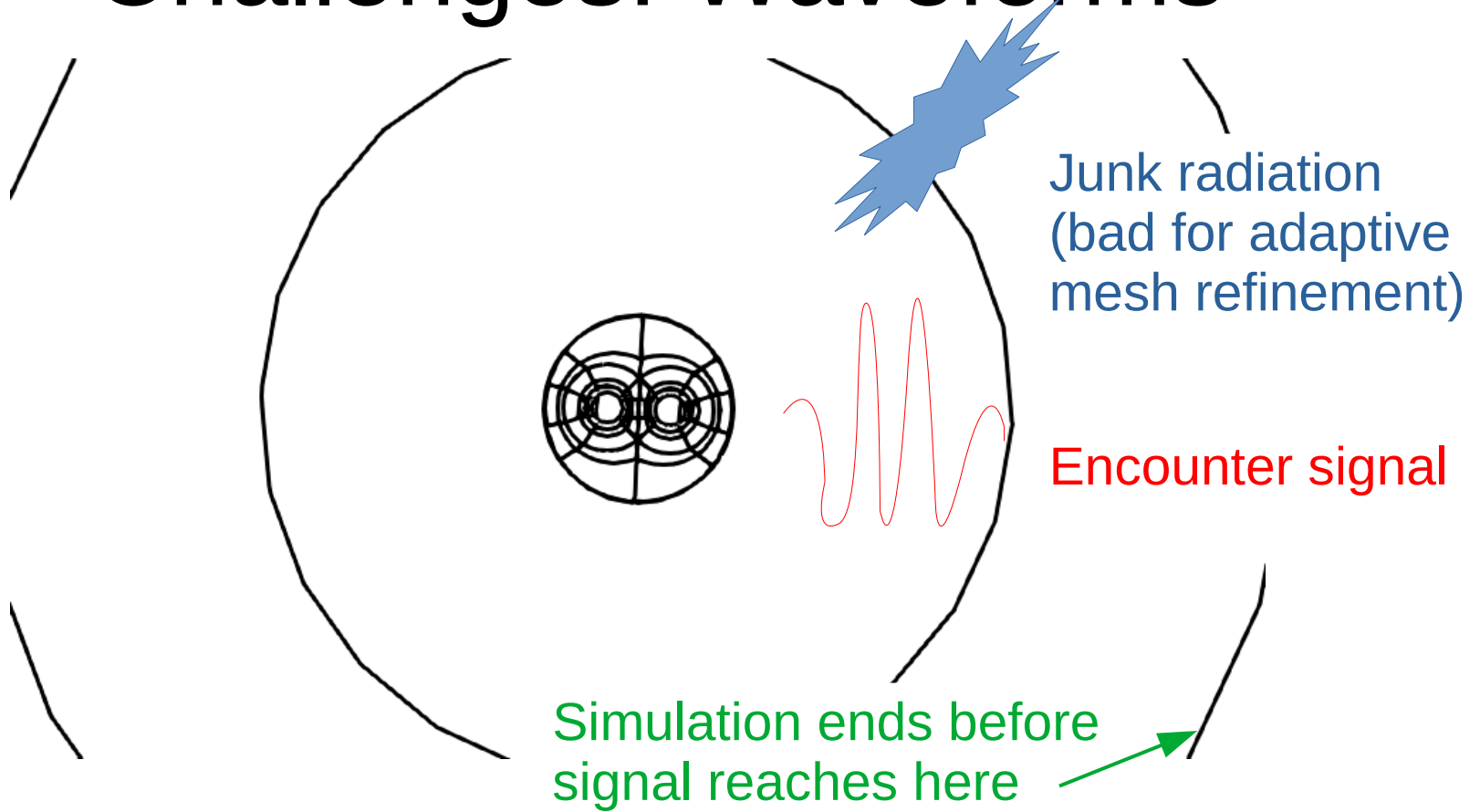
→ coevolve harmonic coordinates

Choose suitable gauge

Keep the coordinate maps well-defined

→ control system must react very fast

# Challenges: Waveforms





# Challenges: initial data

Junk radiation

→ superposed harmonic Kerr initial data

High velocities

→ initial data problem becomes harder

# Conclusion

Accurate waveforms for hyperbolic encounters and captures

Use coevolved harmonic coordinates to analyze orbital parameters  $E$ ,  $J$ ,  $\chi$

Future: configurations with spin