Open-source software tools in quantum science

Quantum (circuit) simulation with QuTiP and quantum error mitigation with Mitiq

Galileo Galilei Institute – Summer School on Quantum Computing and Sensing – June 29th 2021

Nathan Shammah nathan@unitary.fund



Creating a quantum technology ecosystem faster, better, and to benefit everyone.



Open-source software tools in quantum science: Part 1 Make your code count: Leveraging open-source tools in quantum technology

Galileo Galilei Institute – Summer School on Quantum Computing and Sensing – June 22nd, 2021

Nathan Shammah nathan@unitary.fund



Creating a quantum technology ecosystem faster, better, and to benefit everyone.



Open-source software tools in quantum science: Seminar 1 Make your code count

A Guide to building your open-source scientific computing project in Python.

SUPPORTED BY UNITARY FUND

A cheatsheet to develop a scientific open-source library from scratch.

0: Open 1: Code 2: Develop 3: Test 4: Pack 5: Document



Shahnawaz Ahmed Chalmers, Sweden (RIKEN, Japan)

6: Distribute 7: Publish 8: Host

Open, Code, Develop



Test, Pack, Document





Read the Docs







https://github.com/nathanshammah/make-your-code-count

Outline

- About Unitary Fund
 - Community activities
 - In-house research

- QuTiP
 - QuTiP overview
 - New features & updates

- Mitiq
 - About quantum error mitigation
 - Mitiq overview





Non-profit helping create a quantum technology ecosystem faster, better, and to benefit everyone.





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https://unitary.fund/

Unitary Fund Team



Will Zeng, PhD President. Head of Quantum Research at Goldman Sachs Fmr. product/sw lead at Rigetti.



Nathan Shammah, PhD

CTO. Lead developer at QuTiP. Visiting scientist at RIKEN. PhD in guantum physics from Univ. of Southampton.



Sarah Kaiser, PhD

Community Manager. Co-founder of Q# Community, Microsoft MVP, activist for open source and diversity in quantum. UWaterloo PhD in quantum computing.

Andrea Mari, PhD

> 40 peer reviewed scientific publications. Contributor to Pennylane. Fmr. researcher at Xanadu, Univ. of Postdam PhD in guantum information.



Ryan LaRose

NASA Fellowship PhD student at University of Michigan. Fmr at Alphabet X. Wrote first paper benchmarking guantum software packages.

Dan Strano

Full stack web engineer. Lead developer on the grack guantum simulator.

Advisory Board

15 volunteer experts in quantum systems & software from:



Community

60+ grantees 21 countries



Vincent Russo, PhD

Post-quantum security developer at ISARA. Lead dev on togito quantum info package. PhD from UWaterloo.

Full-time

Part-time

6

Unitary Fund Programs

Microgrant Program

Small microgrants => big impact

>\$100k

Granted to date

Unitary Labs

- Open source research team
- Targeting impactful and open niches that aren't monetizable by companies

47 grants in 21 countries;

10+ publications; 30+ libraries with 1167 stars, 50+ contributors and ~6k commits Helped 12 folks get into quantum tech full time

2 new startups, 1 new non-profit

from giskit import QuantumCircuit
from mitig import mitigate executor

circ _ unrung import mitigate_executor(gs)
circ = QuantumCircuit(1, 1)
for __ in range(120): circ.x(0)
circ.measure(0, 0)

expectation = qskt_noisy_sim(circ)
print(f"Error is {1 - expectation:.{3}}")

Mitig: Error mitigating quantum compiler

Error is 0.0582

Built on Original Research:

Digital Zero Noise Extrapolation for Quantum Error Mitigation: https://arxiv.org/abs/2005.10921

Mitiq: A software package for error mitigation on noisy quantum computers: https://arxiv.org/abs/2009.04417 QuTiP: Quantum Toolbox in Python

Unitary Fund is setting up governance and fiscal sponsorship for a critical open source quantum technology package



30k annual downloads, >2500 citations



downloads 152k total



QuTiP: The Quantum Physics Simulator

The Quantum Toolbox in Python





Full Power of Python Classes



The QObj class

The Quantum Toolbox in Python

- State and operators are declared as QObj
 - Qubit



 $|\psi\rangle = \frac{1}{\sqrt{(2)}} \left(|0\rangle + |1\rangle\right) \qquad \underset{\text{Quantum object: dims = [[2], [1]], shape = (2, 1), type = ket}{\Rightarrow}$

$$\left(\begin{array}{c} 1.0\\ 0.0 \end{array}\right)$$





• Operator
>> d = destroy(2)
Quantum object: dims = [[2], [2]],
shape = (2, 2), type = oper,
isherm = False

$$\begin{pmatrix} 0.0 & 1.0 \\ 0.0 & 0.0 \end{pmatrix}$$

https://github.com/nathanshammah/interactive-notebooks

States, operators, tensor spaces, density matrix

The Quantum Toolbox in Python

$$\begin{split} H &= \frac{\sigma_z}{2} & \implies \texttt{from qutip import } * \\ &> \texttt{H} = \texttt{sigmaz}()/2 \\ &a, a^{\dagger} & \implies \texttt{a} = \texttt{destroy}(2) \\ &|\psi\rangle &= \frac{1}{\sqrt{(2)}} \left(|0\rangle + |1\rangle\right) & \implies \texttt{psi1} = \texttt{basis}(2, \ 0) \\ &> \texttt{psi2} = \texttt{basis}(2, \ 1) \\ &> \texttt{psi} = (\texttt{psi1} + \texttt{psi2})/1.414 \\ &\sigma_z \otimes \sigma_x & \implies \texttt{tensor}(\texttt{rhol}, \texttt{rho2}) \\ &> \texttt{tensor}(\texttt{sigmaz}(), \texttt{sigmax}()) \\ &\rho & \implies \texttt{rho} = \texttt{ket2dm}(\texttt{psi}) \\ &> \texttt{op} = \texttt{vector_to_operator}(\texttt{rhol}) \end{split}$$

https://github.com/nathanshammah/interactive-notebooks

What does a Schrödinger Cat looks like

The Quantum Toolbox in Python



Cavity Quantum Electrodynamics (Cavity QED)

Using the **Quantum Toolbox in Python to study physics**



A. F. Kockum, A. Miranowicz, S. De Liberato, S. Savasta & Franco Nori, Nature Reviews Physics, 1 19 (2019)

Numerical Solvers at a glance



The Quantum Toolbox in Python

The **Result** class stores the expectation values of the operators passed to the solver.

Simple Example: A driven, damped single mode cavity.

Solvers:

- `mesolve`: Lindblad master equations
- `mcsolve`: Monte-Carlo trajectory
- `Floquet_modes`: Floquet theory
- **bloch_redfield:** Bloch-Redfield master equation
- ssesolve`: Stochastic Schrödinger equation
- `smesolve`: Stochastic master equations

```
result_ref = mesolve(H, rho0, times, c_ops, e_ops)
plot_expectation_values(result_ref, y_labels = "E[a'a], ...,)
```



Monte Carlo Quantum Trajectories

Photon counting statistics with `mcsolve`

"quantum jump"
$$\frac{d}{dt}\rho = -\frac{i}{\hbar}[H,\rho] + \gamma \left(\frac{L\rho L^{\dagger}}{L\rho L^{\dagger}} - \frac{1}{2}L^{\dagger}L\rho - \frac{1}{2}\rho L^{\dagger}L\right)$$

continuous decay

A. **Effective Hamiltonian**: shrinking the state

$$H_{\rm eff} = H_{\rm sys} - \frac{i\hbar}{2}L^{\dagger}L$$

B. Quantum jump:

$$\left|\psi(t+\delta t)\right\rangle = \frac{L\left|\psi(t)\right\rangle}{\left\langle\psi(t)\left|L^{+}L\right|\psi(t)\right\rangle^{1/2}}$$

- 1. Generale random number, r.
- 2. Is *r* > norm(psi)?
 - I. Yes: keep integrating (A)
 - II. No: apply jump and renormalize

Stochastic solvers

ł

Stochastic master equation: Continuous weak measurements with: `smesolve`

continuous weak measurements

- / >

Heterodyne Detection

$$d\rho(t) = -i[H, \rho(t)]dt + \gamma \mathscr{D}[a]\rho(t)dt + \frac{1}{\sqrt{2}}dW_{1}(t)\sqrt{\gamma}\mathscr{H}[a]\rho(t) + \frac{1}{\sqrt{2}}dW_{2}(t)\sqrt{\gamma}\mathscr{H}[-ia]\rho(t)$$

$$\mathscr{D}[A]\rho = A\rho A^{\dagger} - \frac{1}{2}\left(\rho A^{\dagger}A + A^{\dagger}A\rho\right) \quad \text{Lindblad term}$$

$$\mathscr{H}[A]\rho = A\rho + \rho A^{\dagger} - \text{Tr}\left[A\rho + \rho A^{\dagger}\right]\rho \quad \text{Nonlinear term}$$

result = smesolve(H, rho0, times, [], c_ops, e_ops, method='heterodyne')

```
method = `heterodyne'
method = `homodyne'
method = `photocurrent'
```

QuTiP: Numerical Stochastic Solvers



The Quantum Toolbox in Python



solution = ssesolve([H, c_ops = c_ops , fock(N), tlist, sc_op_td, e_op, **kwargs)

- = `ssesolve`: Stochastic Schrödinger equation result = ssesolve(H, rho0, times, [], c_ops, e_ops)
- `smesolve`: Stochastic master equations result

result = smesolve(H, rho0, times, [], c ops, e ops)





50x faster Time-dependent jumps

Stochastic Master Equations `smesolve`



More general More integration methods Benchmarked solvers

Contributing to QuTiP – Tutorials

The Quantum Toolbox in Python



Recent addition: Cat vs coherent states in a Kerr resonator and the role of measurement

Homodyne

Another possible way to monitor a quantum-optical system is through homodyne detection, a widely-used experimental technique which allows to access the field quadratures [5-6]. To implement this kind of measurement, the cavity output field is mixed to the coherent field of a reference laser through a beam splitter (here assumed of perfect transmittance). Then, the mixed fields are probed via (perfect) photodectors, whose measures are described by new jump operators. We stress that both the coherent and the cavity fields are measured simultaneously.

In the ideal limit $\beta_{1,2} \rightarrow \infty$, the system evolves diffusively according to a homodyne stochastic Schr\"odinger equation. Using the ssesolve function with option "method='homodyne'", one can simulate the trajectory.

Dr. Fabrizio Minganti (RIKEN) \rightarrow EPFL List=np.linspace(0,8000,800)



sol_hom=ssesolve(H, fock(20,0), tlist, c_ops, [a.dag()*a, (a+a.dag())/2, -1.j*(a-a.dag())/2, parit





Contributing to QuTiP – Tutorials

The Quantum Toolbox in Python

Pull Request: Optical Quantum State tomography with MaxLikelihood

Shahnawaz Ahmed (Chalmers)



Counting photons: measuring the photon number operator $\ln \left| \left\langle n \right| \right|$

The expectation value of the photon number operator can be obtained easily from a state written in the fock basis - it is simply the diagonal elements of the density matrix, $|p_n|^2$. Here, we displace the initial state with various values of the displacement, β_i and then we can measure the photon number statistics by simply reading the diagonal elements of the displaced density matrix ρ' .

 $\rho' = D(\beta_i)\rho D^{\dagger}(\beta_i)$



QuTiP recent additions (2018-2019)

qutip.scattering

Model nonlinear photon scattering in multiple waveguides

How photons scatter into the waveguide when the system is driven with some excitation field



K.A. Fischer, *et.al.* (2017), Quantum **2**, 69 (2018) **Code**: Ben Bartlett. Github: bencbartlett

qutip.piqs

Efficiently model local dissipation Collective dissipation vs. Local dissipation

vs. Coherent coupling



N. Shammah *et al.*, Phys Rev A **98**, 063815 (2018) **Code**: Nathan Shammah and Shahnawaz Ahmed

qutip.nonmarkov

The environment has a memory Non-Markovian dynamics Hierarchical Equations of Motion (HEOM).



A. Fruchtman, *et al.*, Sci. Rep. **6**, 28204 (2016) N. Lambert *et al.*, Nature Comm. **10**, 3721 (2019)

Code: Shahnawaz Ahmed and Neill Lambert

QuTiP: Visualize a qubit

The Quantum Toolbox in Python



qutip.org/tutorials

github.com/qutip

launch binder

Take a snapshot



1.Introduction_to_qutip.ipynb https://github.com/nathanshammah/interactive-notebooks

QuTiP: The Quantum Toolbox in Python

About QuTiP



QuTiP is a free and open source library for efficient simulation of a wide variety of quantum systems.

Field-specific intuitive framework

The mathematics of quantum mechanics

- Complex number matrices
- Non-commutative algebras
- Operators and superoperators
- Intuitive Python classes: QObj Results

Advanced mathematical techniques

- Noisy Dynamics: Master equation solvers
- Correlation functions (quantum regression formula)
- Modularity: Permutational invariant quantum solver

Hierarchical equations of motion Waveguide photon scattering Topological quantum circuits

Efficient numerical calculations

- Fast complex-complex matrix-vector multiplication with SSE3 intrinsics.
- Multiprocessing: Enhanced parallel performance with OPENMP
- Sparse Matrices: Fast CSR (Compressed Sparse Row) matrix class.
- Up to 100x improvement: in CSR adjoint & transpose

More info at http://gutip.org/

in Hermitian verification, Krönecker product in partial trace calculation

QuTiP: Project Governance

Admin Team



Alex Pitchford Aberystwyth University Main focus: Quantum optimal control, solvers.



Nathan Shammah RIKEN Main focus: Symmetrical models.

education and outreach.



Eric Giguère Université de Sherbrooke Main focus: Stochastic solvers, coc



Shahnawaz Ahmed Chalmers

Main focus: Machine learning, Nor Markovian dynamics.



Neill Lambert

RIKEN Main focus: Non-Markovian dynamics, counting statistics.



Jake Lishman Imperial College London Main focus: Core data model and linear algebra.



Boxi Li Forschungszentrum Juelich

Main focus: Quantum control, Ouantum device simulation.



Simon Cross RIKEN

Main focus: Quantum control. machine learning, general maintenance.



Supporting Organizations

QuTiP is currently supported by these organizations:









OuTiP is proud to be affiliated to:





The development of QuTiP was partially supported by the following organizations:





Board: Daniel Burgarth, Anton Frisk Kockum, Robert Johansson, Franco Nori, Will Zeng

https://github.com/qutip/governance

QuTiP: Empowering scientific research

The Quantum Toolbox in Python

Experimental Research

arXiv:1806.04682v1 [quant-ph] 12 Jun 2018

High-fidelity control and entanglement

of Rydberg atom qubits



arXiv:1903.05672 [quant-ph] 13 Mar 2019

Phonon-mediated quantum state transfer

and remote qubit entanglement



QuTiP: Impact and Recent Updates

- Over **13,000 downloads per month** from **PyPI** the Python Index Package only (pip install qutip) and **more than 350,000 overall** from the Conda Forge channel by Anaconda (conda install qutip).
- As of June 2021, **7076 commits**, in over **13 version releases** by over **96 contributors**.
- The two QuTiP papers have over 1500 citations (Google Scholar).
- -
- The QuTiP admin team is now formed of eight maintainers meeting monthly.
- Three ongoing Google Summer of Code projects:
 - 1. QuTiP-CuPy: GPU integration (Felipe).
 - 2. QuTiP-**Tensorflow** data back-end (Asier).
 - 3. Universal decomposition of quantum gates (Purva).



Cavity Quantum Electrodynamics (Cavity QED)

Using the Quantum Toolbox in Python to study physics. Things are scaling up



Image Credit: A. F. Kockum, A. Miranowicz, S. De Liberato, S. Savasta & Franco Nori, Nature Reviews Physics, 1 19 (2019)

Solving a many-qubit dynamics

Closed vs. Open dynamics

Schrödinger Equation

$$i\hbar \frac{d}{dt} |\psi\rangle = H |\psi\rangle$$

Master Equation

$$i\hbar \frac{d}{dt}\rho = [H, \rho] +$$
Noise

	Schrödinger Equation	Lindblad Master Equation		
Probability	Conserved	Conserved		
Evolution	Unitary, $H = H^{\dagger}$	Non-Unitary		
Time reversal	Preserved	Broken		
Features	Closed system	Open system: noise and dissipation		
Scaling with N qubits	2^N			

Exploiting permutational symmetry

Numerically solving the dynamics of many qubits



Efficiently studying out-of-equilibrium systems

What's going on





Efficiently model local dissipation Collective dissipation vs. Local dissipation vs. Coherent coupling

import qutip.piqs piqs.readthedocs.io gutip.org/tutorials#pigs

N. Shammah *et al.*, *Phys Rev A* 98, 063815 (2018)

Code: Nathan Shammah and Shahnawaz Ahmed

piqs QuTiP library

QuTiP library Now a qutip module QuTiP-based quantum optimal control library

krotov

matsubara

A qutip plugin for non-Markovian dynamics

QuTiP ecosystem: Like AstroPy, but for Quantum

Engineering Quantum Optimal Control

What's going on

Examples %

krotov.readthedocs.io

render on nbviewer 🚱 launch binder

- Optimization of a State-to-State Transfer in a Two-Level-System
- Optimization of a state-to-state transfer in a lambda system with RWA
- Optimization of a dissipative state-to-state transfer in a Lambda system
- Optimization of Dissipative Qubit Reset
- Optimization of an X-Gate for a Transmon Qubit
- Optimization of a Dissipative Quantum Gate
- Optimization towards a Perfect Entangler

Population evolutions for a gate (iSWAP)



piqs

QuTiP library Now a qutip module

krotov QuTiP-based c

QuTiP-based quantum optimal control library

A qutip plugin for non-Markovian dvnamics

matsubara



Krotov: A Python implementation of Krotov's method for quantum optimal controlM. H. Goerz et al., SciPost Phys. 7, 080 (2019)

> QuTiP ecosystem: Like AstroPy, but for Quantum

QuTiP plugin: The environment is watching

What's going on

matsubara.readthedocs.io

matsubara Search docs Introduction Installation Matsubara correlation Positivity constrained fitting

- Hierarchical Eq. of Motion (HEOM)
- Pseudomodes
- Reaction Coordinate (RC)
- Pure dephasing
- Virtual photon population
- **API Documentation**

References

Docs » Matsubara: a QuTiP plugin

C Edit on GitHub

Matsubara: a QuTiP plugin

A QuTiP plugin to study the spin-boson model in the Ultra-Strong Coupling limit at zero temperature. We provide the code to reproduce the results in [LACN19].

- Introduction
- Installation
- Matsubara correlation
- Positivity constrained fitting
- Hierarchical Eq. of Motion (HEOM)
- Pseudomodes
- Reaction Coordinate (RC)
- Pure dephasing
- Virtual photon population
- API Documentation
- matsubara heom
- matsubara.correlation
- References

pigs

QuTiP library Now a qutip module

krotov

QuTiP-based quantum optimal control library

A qutip plugin for non-Markovian dynamics

matsubara



0.020 RC Model ground state HEOM (Matsubara) (b)a) Psuedomodes (Matsubara) latsubard RC (Matsubara) ₹0.010 ation Manno Indo,005 0.000 50 150 200 100 $t(1/\omega_0)$

Comparison of open system models

Virtual excitations in the ultra-strongly-coupled spin-boson model: physical results from unphysical modes N. Lambert, S. Ahmed, M. Cirio, and F. Nori Nature Communications 10, 3721 (2019)

Quantum circuit simulation with qutip-qip

Installation: pip install qutip-qip

Documentation: qutip-qip.readthedocs.io

from qutip_qip.circuit import QubitCircuit from qutip_qip.operations import Gate # create the quantum circuit qc = QubitCircuit(2, num_cbits=1) qc.add_gate("CNOT", controls=0, targets=1) qc.add_gate("SNOT", targets=1) qc.add_gate("ISWAP", targets=[0,1]) qc.add_measurement("M0", targets=1, classical_store=0) # plot the quantum circuit qc.png



LaTeX rendering powered by QCircuit

Pulse-level noisy quantum circuits with qutip-qip



ise-level noisy quantum circuits with qu



(a) an example of quantum circuit



- Single-qubit rotation around an axis Ω^{α}_{i} $\alpha = x, y, z$ (color blue and orange)
- Coupling strength (color green) q_i
- $\Omega_{i}^{\mathrm{cr}k}$ The cross-resonance effective interaction (color green)
 - Ω_0^x and an $\Gamma_{\rm c}$ $\Gamma_{\rm c}$ Ω_1^x Ω_0^z Ω_1^z

Realistic and flexible simulation of noisy quantum processors.

- Reproducing experimental results on _ crosstalk noise in an ion-based processor.
- Demonstrating the simulation of noisy quantum circuits on different hardware platforms with various native gate sets.
- Multiple types of model processors and _ noise models and solvers in QuTiP can be simulated.
 - Integration with OpenQASM standard.

(b) Spin chain model

(c) Superconducting qubits model

(d) Optimal control model

Pulse-level noisy quantum circuits with QuTiP, B. Li, S. Ahmed, S. Saraogi, N. Lambert, F. Nori, A. Pitchford, N. Shammah, arXiv:2105.09902



Pulse-level noisy quantum circuits with qutip-qip



Pulse-level noisy quantum circuits with QuTiP, B. Li, S. Ahmed, S. Saraogi, N. Lambert, F. Nori, A. Pitchford, N. Shammah, arXiv:2105.09902

Pulse-level noisy quantum circuits with qutip-qip



Random noise in the pulse intensity

Pulse wobbling

Despite single-qubit decoherence, Processor can also simulate coherent control noise. For general types of noise, one can define a noise object and add it to the processor. An example of predefined noise is the random amplitude noise, where random value is added to the pulse every dt. loc and scale are key word arguments for the random number generator np.random.normal.

Pulse-level noisy quantum circuits with QuTiP, B. Li, S. Ahmed, S. Saraogi, N. Lambert, F. Nori, A. Pitchford, N. Shammah, arXiv:2105.09902

Overview of Mitiq



- Scope: providing a toolkit to easily apply different error mitigation techniques
- Compatible with many existing quantum software libraries: Cirq, Qiskit, PyQuil, Braket.
- Structurally designed to be **backend independent**.



Mitiq uses the best practices of scientific software development

White paper https://arxiv.org/abs/2009.04417

\$ pip install mitiq

https://github.com/unitaryfund/mitiq (version 0.9.1)

Documentation

https://mitiq.readthedocs.io

DevelopmentTestingMarch-September 202098% of lines		Continuous Integration		Research	Documentation	
		98% of lines	Github Actions		T. Giurgica-Tiron <i>et al.</i> , arXiv:2005.10921	Tutorials for any back-end
Releasing:	GitHub PyPI	TestPyPI	OS:	Linux (ubuntu) Mac Windows	R. LaRose <i>et al.,</i> arXiv:2009.04417	Sphinx.Doctest: >80 tests



Mitiq: Open development

Weekly Engineering Meeting: Community Call

Streamed at 12pm-12:40pm EDT at discord.unitary.fund



Over **20 external contributors** on GitHub, also thanks to the **UnitaryHACK** hackathon (May 14th – 30th, 2021)



🎉 Accepted Pull Requests 🎉

unitaryfund/mitiq:

- andre-a-alves HACKED [UnitaryHACK] ZNE-PEC uniformity
- maxtremblay HACKED [UnitaryHACK] Improve conversion from braket to cirq
- Yash-10 HACKED Warning for short programs [unitaryHACK]

Over **19 developers** beyond Unitary Fund! More than **10,000 downloads** from the Python Package Index. 40

Ideal quantum circuits

Ideal Von Neumann master equation: $\partial_t \rho = -i[K(t),\rho]$ \uparrow noiseless Hamiltonian



[1] K. Temme, S. Bravyi, and J. M. Gambetta, "Error Mitigation for Short Depth Quantum Circuits," Physical Review Letters,. 119, 180509,(2017).



Ideal quantum circuits... on noisy computers

Ideal Von Neumann master equation: $\partial_t \rho = -i[K(t),\rho]$

noiseless Hamiltonian



[1] K. Temme, S. Bravyi, and J. M. Gambetta, "Error Mitigation for Short Depth Quantum Circuits," Physical Review Letters,. 119, 180509,(2017).



Typical workflow in quantum software



Mitiq: a thin layer between the user and the backend





Mitiq: a thin layer between the user and the backend





Mitiq code tree (simplified)





Zero-noise extrapolation workflow with Mitiq





Noisy quantum evolution

noise scale factor [dimensionless real number]



Noiseless evolution: $\lambda = 0$

Hardware dynamics: $\lambda = 1$

= 1

[1] K. Temme, S. Bravyi, and J. M. Gambetta, "Error Mitigation for Short Depth Quantum Circuits," Physical Review Letters,. 119, 180509,(2017).



Noisy quantum evolution

noise scale factor [dimensionless real number]



Noiseless evolution: $\lambda = 0$ **Hardware** dynamics: $\lambda = 1$

Increase noise: $\lambda = 2$

[1] K. Temme, S. Bravyi, and J. M. Gambetta, "Error Mitigation for Short Depth Quantum Circuits," Physical Review Letters,. 119, 180509,(2017).



Zero-noise extrapolation (ZNE): increasing noise... and back



Noise scaling [1]

noise scale factor [dimensionless real number]



Experimentally:



[1] K. Temme, S. Bravyi, and J. M. Gambetta, "Error Mitigation for Short Depth Quantum Circuits," Physical Review Letters, **119**, 180509,(017).

[2] A. Kandala, K. Temme, A.D. Córcoles, A. Mezzacapo, J.M. Chow, and J.M. Gambetta, "Error mitigation extends the computational reach of a noisy quantum processor" Nature **567**, 491 (2019)



Zero-noise extrapolation

Two main requirements:

- Noise scaling: Some means of increasing (scaling) noise.
- **Inference method**: a model that one can *fit* to the measured data to *extrapolate* to the zero-noise limit.



K. Temme, S. Bravyi, and J. M. Gambetta, "Error Mitigation for Short Depth Quantum Circuits," Physical Review Letters, vol. 119, p. 180509, 11 2017. T. Giurgica-Tiron, Y. Hindy, R. LaRose, A. Mari, W. J. Zeng, *Digital zero noise extrapolation for quantum error mitigation*, 2020 IEEE International Conference on Computing and Engineering (QCE) (2020).

Single-qubit depth d = 200 randomized benchmarking circuit on IBMQ Armonk

Analog and digital noise scaling methods



K. Temme, S. Bravyi, and J. M. Gambetta, "Error Mitigation for Short Depth Quantum Circuits," Physical Review Letters, vol. 119, p. 180509, 11 2017. T. Giurgica-Tiron, Y. Hindy, R. LaRose, A. Mari, W. J. Zeng, *Digital zero noise extrapolation for quantum error mitigation*, 2020 IEEE International Conference on United Public Computing and Engineering (QCE) (2020). Example: noise scaling by global folding with Mitiq

```
>>> import cirq
>>> from mitig.zne.scaling import fold global
# Get a circuit to fold
>>> greg = cirq.LineQubit.range(2)
>>> circ = cirq.Circuit(cirq.ops.H.on(qreg[0]), cirq.ops.CNOT.on(qreg[0], qreg[1]))
>>> print("Original circuit:", circ, sep="\n")
Original circuit:
0: ___H___@___
                                           \lambda = 3
# Fold the circuit
>>> folded = fold_global(circ, scale_factor=3.)
>>> print("Folded circuit:", folded, sep="\n")
Folded circuit:
1: _____X____X_____
```



Example: using different extrapolation methods in Mitiq with **Factories**

		Class	Extrapolation Method
		LinearFactory	Extrapolation with a linear fit.
		RichardsonFactory	Richardson extrapolation.
mitia zno informa		PolyFactory	Extrapolation with a polynomial fit.
miterq.zne.interence	,e	ExpFactory	Extrapolation with an exponential fit.
•		PolyExpFactory	Similar to ExpFactory but the exponent
			can be a non-linear polynomial.
		AdaExpFactory	Similar to ExpFactory but the noise
			scale factors are adaptively chosen.

Experiment (2-qubit RB circuit): IBM Q London **Rigetti Aspen-8** (a) (b) 1.4 1.4🛧 Linear Linear Richardson Richardson 1.2 1.2 Quadratic Quadratic Exponential Exponential (00|0|00) 1.0 1.0 ¢ 0.8 0.8 0.6 0.6 ★ R. LaRose, A. Mari, P. J. Karalekas, N. Shammah, W. J. Zeng, 0.40.4 "Mitig: A software package for error mitigation on noisy 0.2 0.2 quantum computers", arXiv:2009.04417 (2020). 0 2 3 5 6 0 2 3 5 Noise scaling λ_i Noise scaling λ_i



Probabilistic Error Cancellation

Typical step of many quantum algorithms: estimating expectation values.

Ideal quantum circuit $~{\cal U}={\cal G}_t\circ\ldots{\cal G}_2\circ{\cal G}_1~~$ Ideal gates (local unitary operations)

Ideal expectation value Observable Initial state $\langle A \rangle_{\rm ideal} = {\rm tr}[A {\cal U}(\rho_0)],$

Unfortunately, we cannot apply an ideal gate with a NISQ device, but... we can **represent** it as a linear combination of noisy gates!

Replacing
$$\mathcal{G}_{i} = \sum_{\alpha} \eta_{i,\alpha} \mathcal{O}_{i,\alpha}$$
, we get: $\langle A \rangle_{ideal} = \sum_{\vec{\alpha}} \eta_{\vec{\alpha}} \langle A_{\vec{\alpha}} \rangle_{noisy}$
Quasi-probability Implementable noisy gates We can express the ideal result as a linear combination of noisy results! One estimates the sum by probabilistically sampling and measuring only a subset of all the terms.

K. Temme, S. Bravyi, and J. M. Gambetta, "Error Mitigation for Short Depth Quantum Circuits," Physical Review Letters, vol. 119, p. 180509, 11 2017. 56

Probabilistic Error Cancellation workflow with Mitiq





Probabilistic Error Cancellation with Mitiq

Define the circuit of interest

```
from cirq import X, H, CNOT
seed = np.random.RandomState(0)
q0, q1 = LineQubit.range(2)
ideal_circuit = Circuit(X(q0), H(q1), CNOT(q0, q1))
ideal_circuit
```

```
0: —X—@—
|
1: —H—X—
```

Define an executor (a black box function to get noisy expectation values)

```
from cirq import DensityMatrixSimulator
SIMULATOR = DensityMatrixSimulator()
def noisy_executor(circ: Circuit) -> float:
    """Simulates a circuit with depolarizing noise and returns the expectation value
    of the projector on the ground state |00...><00...|.
    """
    circuit = circ.with_noise(depolarize(BASE_NOISE))
    rho = SIMULATOR.simulate(circuit).final_density_matrix
    projector = np.zeros(rho.shape)
    projector[0, 0] = 1.0
    expectation = np.real(np.trace(rho @ projector))
    return expectation</pre>
```



Probabilistic Error Cancellation with Mitiq

Using the mitiq.pec.representations sub-module:





Probabilistic Error Cancellation with Mitiq

Beyond expectation values: analysis of raw data





Thank you!

discord.unitary.fund

nathan@unitary.fund

