

Flavor Physics: old problems and recent hopes

Gino Isidori

[*University of Zürich*]

- ▶ Introduction
- ▶ The flavor problem(s)
- ▶ The LFU anomalies
- ▶ EFT considerations on the anomalies
- ▶ Model-building considerations
- ▶ Speculations on UV completions
- ▶ Conclusions



**University of
Zurich** ^{UZH}

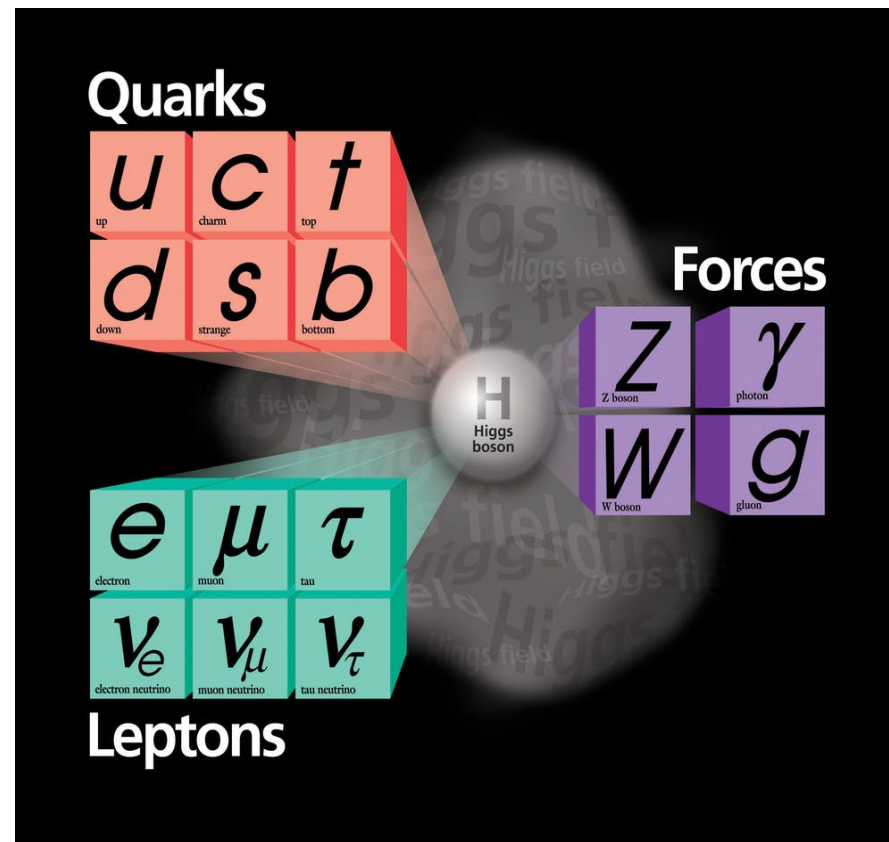


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► Introduction

The Standard Model (**SM**) is a remarkably simple Quantum Field Theory (QFT) that describes well (*almost...*) all microscopic phenomena that we observe in Nature

$$\mathcal{L}_{\text{SM}} = \mathcal{L}_{\text{gauge}}(\psi_i, A_a) + \mathcal{L}_{\text{Higgs}}(H, A_a, \psi_i)$$



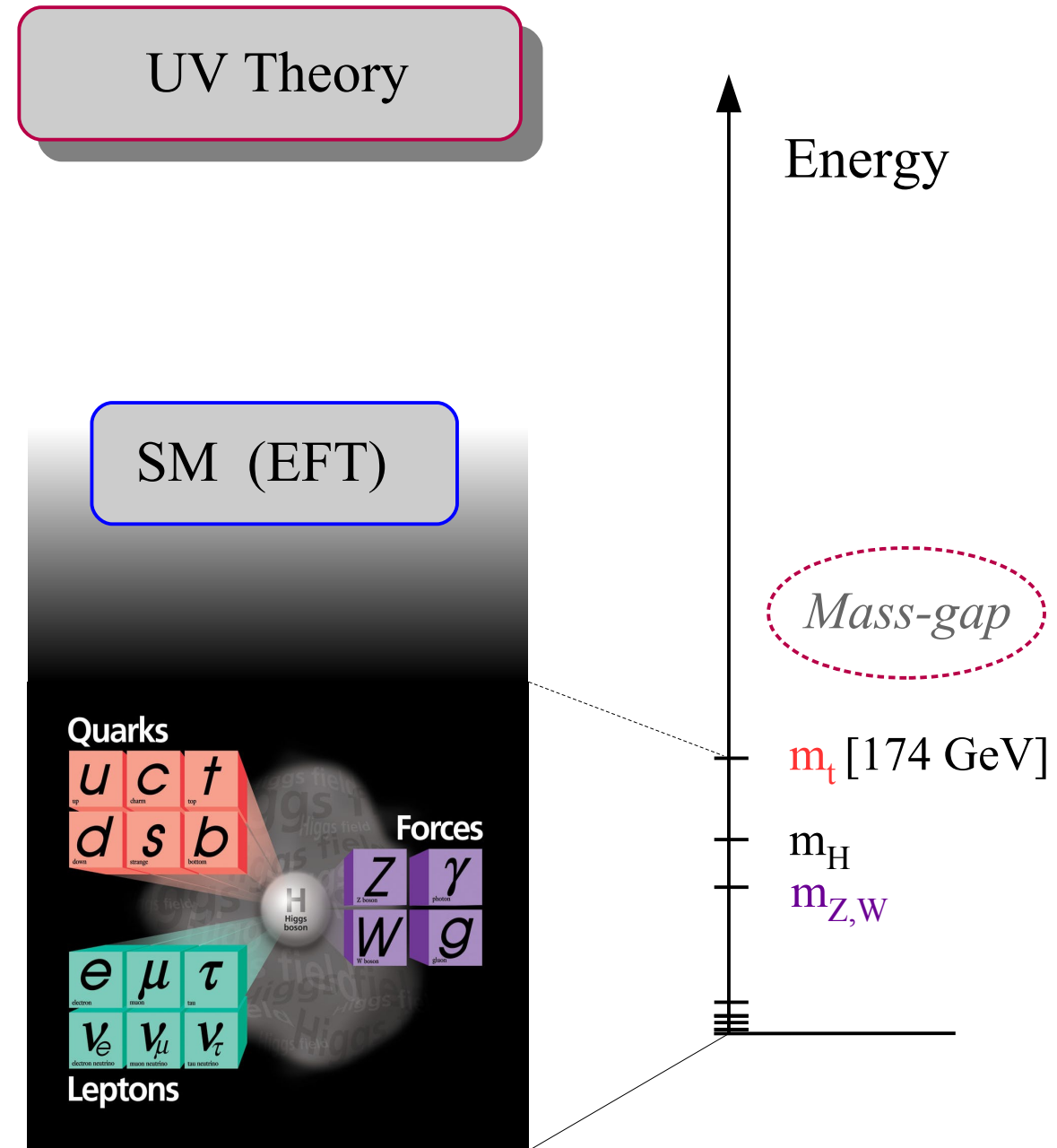
► Introduction

As for any QFT, we believe the SM is only an Effective Field Theory (EFT), i.e. the low energy limit of a more complete theory with more degrees of freedom

$$\mathcal{L}_{\text{SM-EFT}} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Higgs}} + \dots$$

We identified the *long-range* properties of this EFT, but we struggle to understand

- *the nature of short-distance dynamics*
- *why such peculiar structure emerges at low-energies*



► Introduction

Ideally, we would like to probe the UV *directly*, via high-energy experiments



UV Theory

However, for > 30 years this will not be possible....

For the time being, we can only extract *indirect* UV infos exploring the low-energy limit of the EFT.

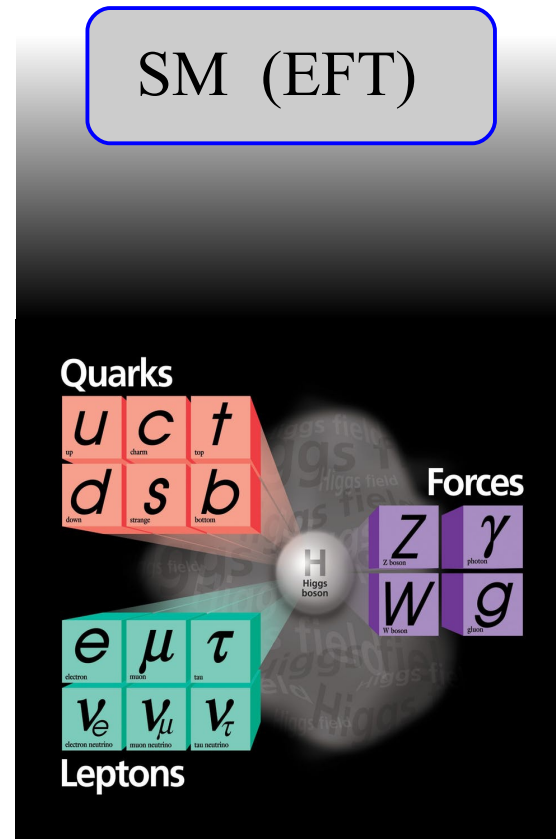


SM (EFT)

Many infos, with 2 clear messages:



- *several tuned (SM) couplings*
- *several accidental (approximate) symmetries*



Energy

Mass-gap

m_t [174 GeV]

m_H

$m_{Z,W}$

► Introduction

A closer look to the “SM-EFT”:

$$\mathcal{L}_{\text{SM-EFT}} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Higgs}} + \sum_{d,i} \frac{c_i^{[d]}}{\Lambda^{d-4}} \mathcal{O}_i^{d \geq 5}$$

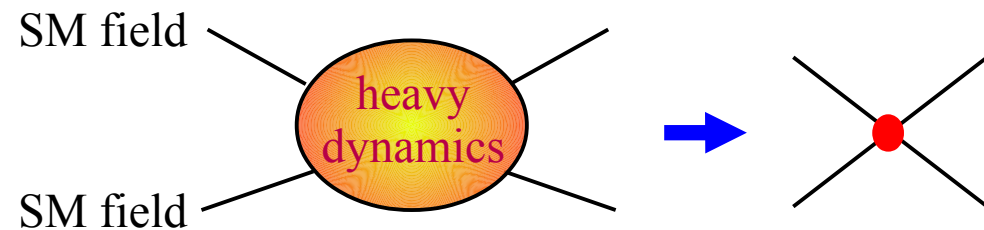
SM (EFT)

Interactions surviving @ large distances
(operators with $d \leq 4$)

Long-range forces
of the SM particles
+
ground state (Higgs)

Local contact interactions
(operators with $d > 4$)

“Remnant” of the heavy
dynamics at low energies



► Introduction

The (indirect) imprints of the UV dynamics manifest themselves in two distinct ways:

$$\mathcal{L}_{\text{SM-EFT}} = \underbrace{\mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Higgs}}}_{\text{qualitative UV imprint}} + \underbrace{\sum_{d,i} \frac{c_i^{[d]}}{\Lambda^{d-4}} \mathcal{O}_i^{d \geq 5}}_{\text{quantitative UV imprint}}$$

Un-natural/tuned values
of **low-energy couplings**

qualitative
UV imprint

Evidence of higher-dim.
operators (\leftrightarrow violations of
accidental symmetries)

quantitative
UV imprint

UV Theory



SM (EFT)

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Un-natural/tuned values
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qualitative
UV imprint

Notable case: *instability of the Higgs mass term under quantum corrections*
[electroweak hierarchy problem]:

$$\text{---} \bullet \text{---} + \text{---} \bigcirc \text{---} \rightarrow m_H^2 \Big|_{\text{Phys}}$$

$m_H^2 \Big|_{\Lambda}$ $\Delta m_H^2 \sim \Lambda^2$

(some) **New Physics**
(coupled at least
to Higgs & top)
in the TeV domain

UV Theory



SM (EFT)

► Introduction

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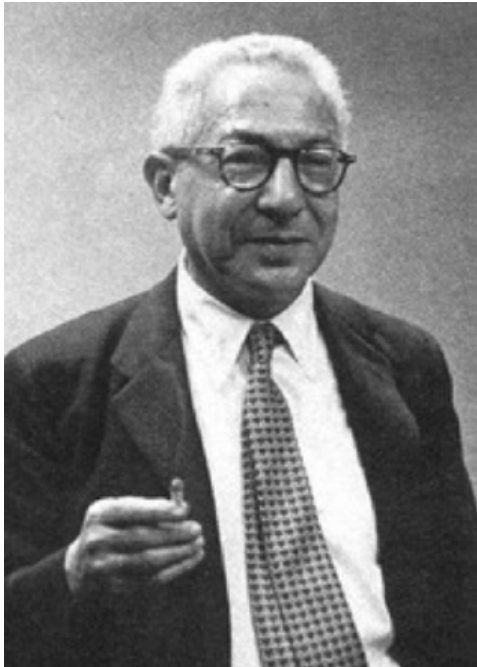


SM (EFT)

Flavour physics

is telling us much more on both these aspects !
(and might tell us even more in the near future...)

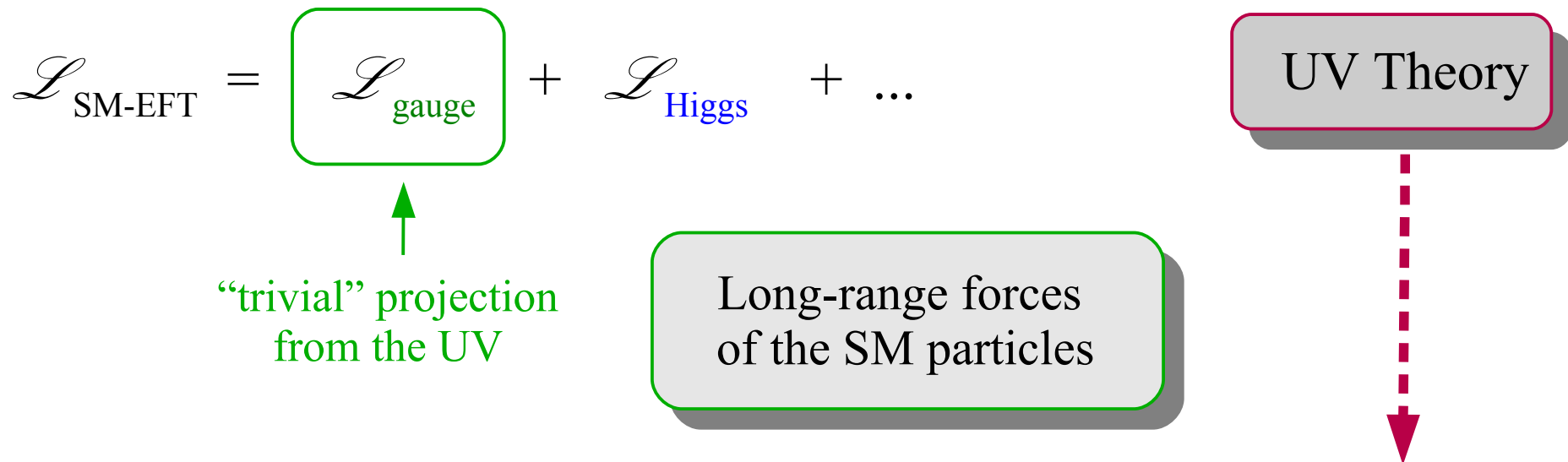
The Flavor Problem(s)



Isidor Issac Rabi
(1898—1988)



► The Flavor Problem(s)

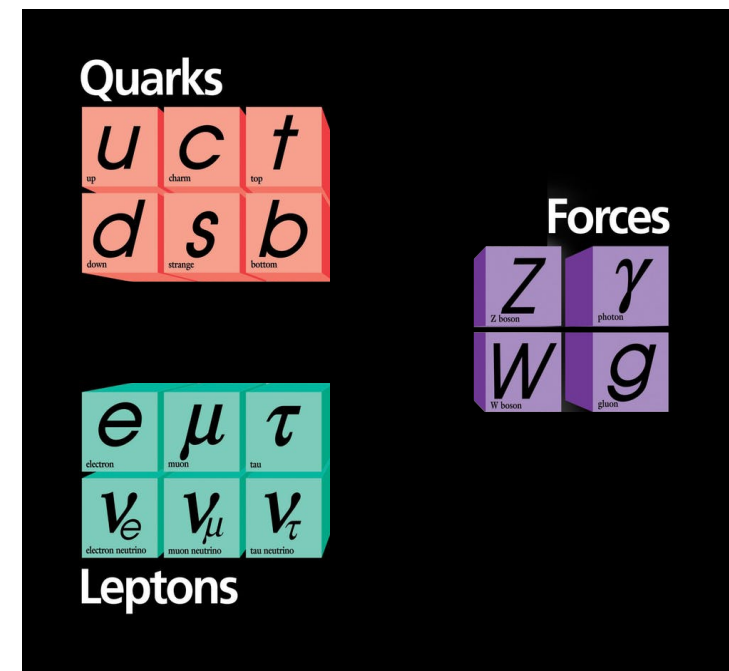


Structure fully dictated by

- Number of light fields
- Their charges under long-range interactions

It contains only “natural” $O(1)$ couplings

Three identical replica of the basic fermion family
 ⇒ huge flavor-degeneracy [$U(3)^5$ symmetry]



► The Flavor Problem(s)

$$\mathcal{L}_{\text{SM-EFT}} = \mathcal{L}_{\text{gauge}} + \boxed{\mathcal{L}_{\text{Higgs}}} + \dots$$

Within the SM, the flavor-degeneracy is broken only by the **Yukawa** interaction:

$$y_{ij} \psi_i \psi_j H \rightarrow m_{ij} \psi_i \psi_j$$

The Yukawa couplings have a peculiar hierarchical structure which does not appear to be accidental:

E.g.:

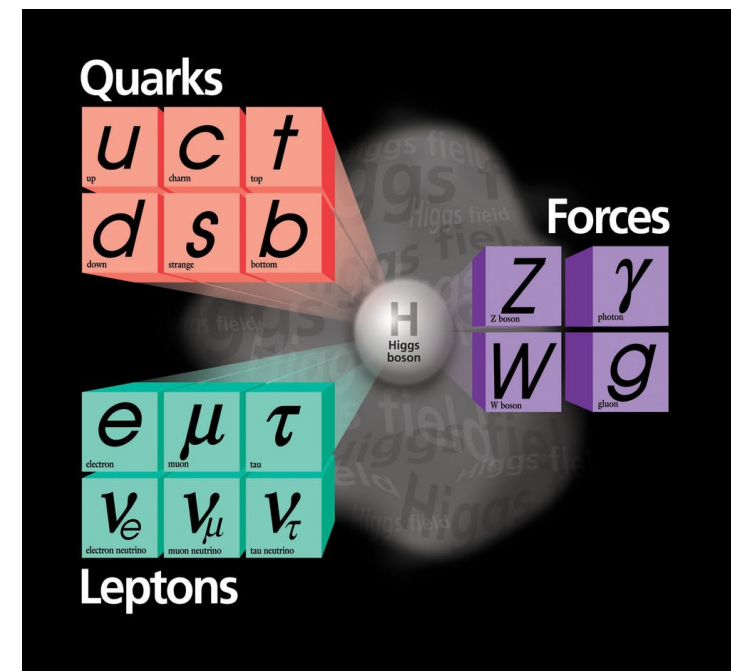
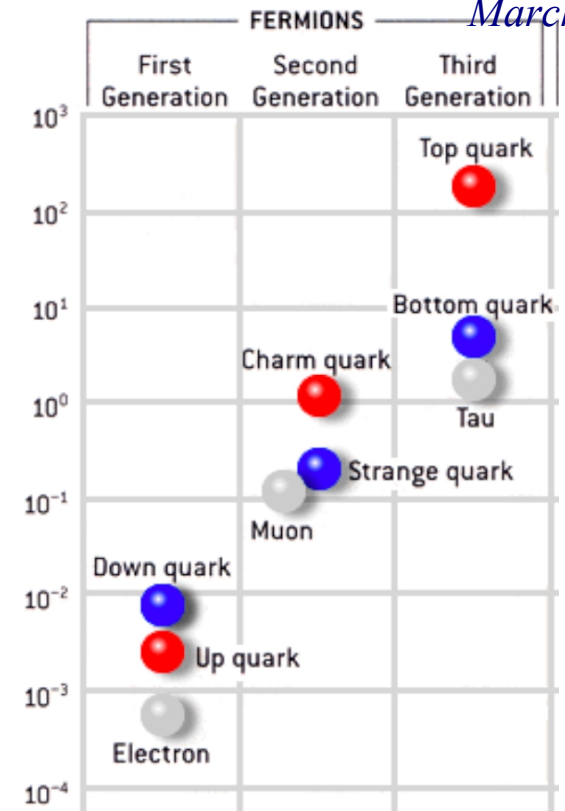
$$Y_U \sim \begin{pmatrix} \text{light} & \text{light} & \text{light} \\ \text{light} & \text{medium} & \text{dark} \\ \text{light} & \text{dark} & \text{black} \end{pmatrix}$$

$V_{ts} \approx 0.04$

$y_c \approx 0.005$

$y_t = \frac{\sqrt{2} m_t}{\langle H \rangle} \approx 1$

The SM Flavor problem



► The Flavor Problem(s)

$$\mathcal{L}_{\text{SM-EFT}} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Higgs}} + \sum_i \frac{1}{\Lambda_i^{d-4}} \mathcal{O}_i^{d \geq 5}$$

Large flavor symmetry

Three identical replica of
the basic fermion family
[$U(3)^5$ symmetry]

Flavor-degeneracy broken
by the Yukawa interaction

$$y_{ij} \psi_L^i \psi_R^j H \rightarrow \mathbf{m}_{ij} \psi_L^i \psi_R^j$$

“Peculiar” breaking structure

Exact & approximate (*accidental* ?) symmetries

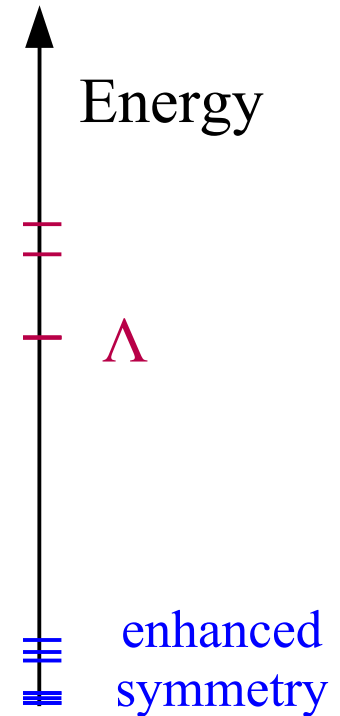
- Eg:
- $U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} =$ (individual) Lepton Flavor [*exact symmetry*]
 - $m_u \approx m_d \approx 0 \rightarrow$ Isospin symmetry [*approximate symmetry*]

► The Flavor Problem(s) [*a brief detour...*]

$$\mathcal{L}_{\text{SM-EFT}} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Higgs}} + \sum_{d,i} \frac{c_i^{[d]}}{\Lambda^{d-4}} \mathcal{O}_i^{d \geq 5}$$

(long-distance interactions) (local contact interact.)

“**Accidental symmetries**” are symmetries which are not fundamental properties of the theory, but emerge accidentally at low energies / large distances → not enough “variables” to describe the violation of the symmetry [*~ multipole expansion*]



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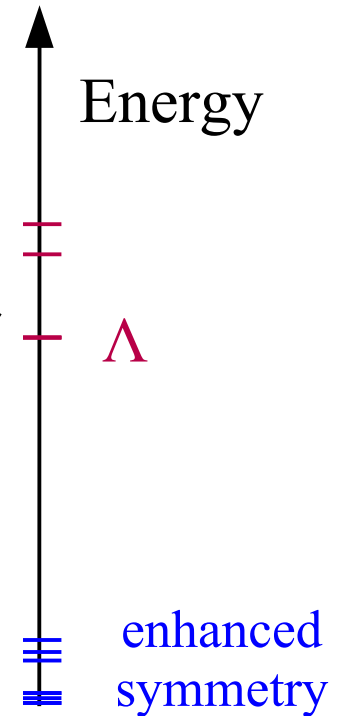
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If a symmetry arises accidentally in the low-energy theory, we expect it to be violated by higher dim. ops

Violations of
accidental symmetries

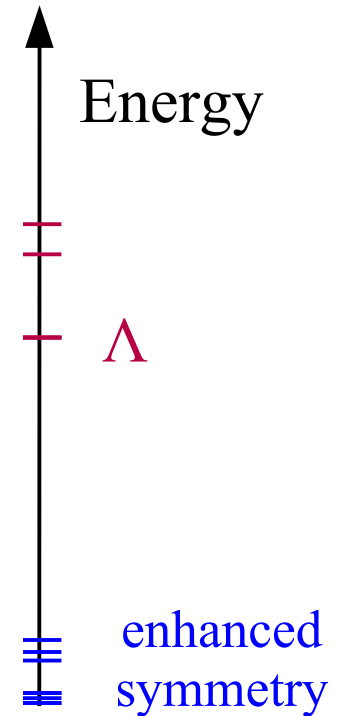


► The Flavor Problem(s) [*a brief detour...*]

$$\mathcal{L}_{\text{SM-EFT}}^{\text{[QCD+QED]-EFT}} = \mathcal{L}_{\text{gauge}} + \cancel{\mathcal{L}_{\text{Higgs}}} + \cancel{\mathcal{L}_{\text{mf}}} + \underbrace{\sum_{d,i} \frac{c_i^{[d]}}{\Lambda^{d-4}} \mathcal{O}_i^{d \geq 5}}_{\text{Violations of accidental symmetries}}$$

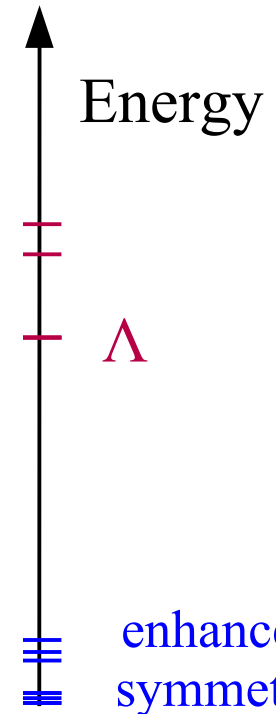
Well-known examples from the past...

Eg: Low-energy theory: QED + QCD
 Accidental symm.: Flavor [U(1)^{n_f}]
 Violated by: Weak interactions → G_F ~ (250 GeV)⁻²



► The Flavor Problem(s) [*a brief detour...*]

$$\mathcal{L}_{\text{SM-EFT}}^{\text{[SM-2]-EFT}} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Higgs}} + \underbrace{\sum_{d,i} \frac{c_i^{[d]}}{\Lambda^{d-4}} \mathcal{O}_i^{d \geq 5}}_{\text{Violations of accidental symmetries}}$$



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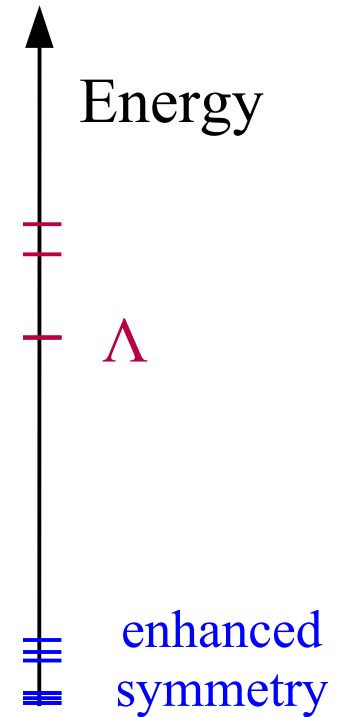
Eg: *Low-energy theory:* SM, 2 generations
Accidental symm.: CP
Violated by: “Super-weak” interaction [L. Wolfenstein]:

$$\frac{e^{i\delta}}{\Lambda^2} (\bar{s} \Gamma d)^2 \quad \frac{1}{\Lambda^2} \sim (10^4 \text{ TeV})^{-2} \sim \frac{(G_F m_t V_{ts} V_{td})^2}{4\pi^2}$$

► The Flavor Problem(s) [*a brief detour...*]

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Well-known examples from the past...



...the violations of **L**epton **F**lavor **U**niversality
recently reported by experiments (B-physics *anomalies*)
belong to this category

► The Flavor Problem(s)

$$\mathcal{L}_{\text{SM-EFT}} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Higgs}} + \sum_{d,i} \frac{c_i^{[d]}}{\Lambda^{d-4}} \mathcal{O}_i^{d \geq 5}$$

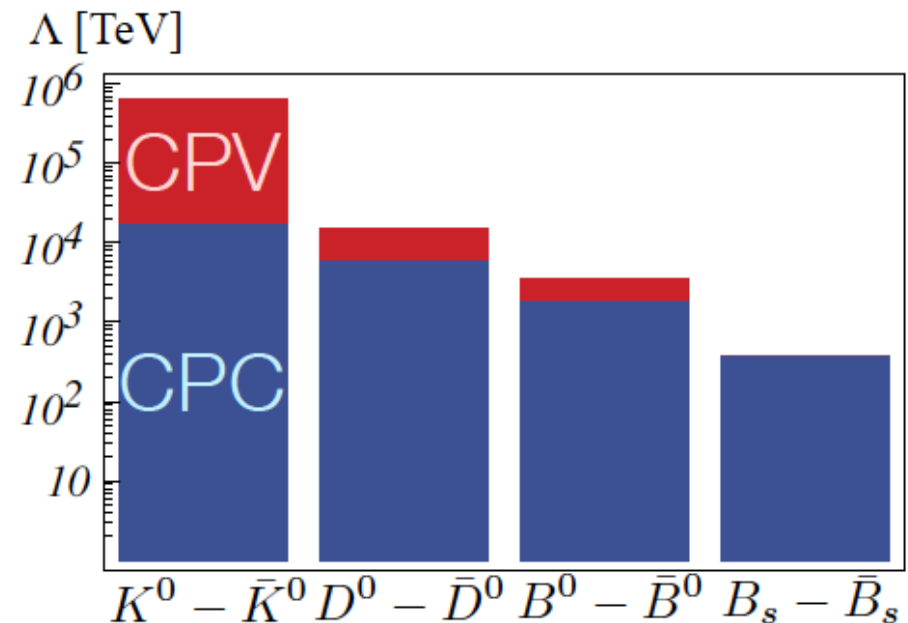
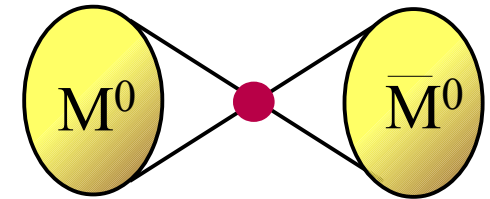
In principle, we could expect many violations of the accidental symmetries from the heavy dynamics \rightarrow *new flavor violating effects*

However, beside the B-physics anomalies we observe none

Stringent bounds on the scale of possible new flavor non-universal interactions

The NP Flavor problem

E.g.: $\frac{1}{\Lambda^2} (\psi_i \psi_j)^2$



► The Flavor Problem(s)

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Flavor-degeneracy:
 $U(3)^5$ symmetry

$U(3)^5$ symmetry
broken by
Yukawa couplings

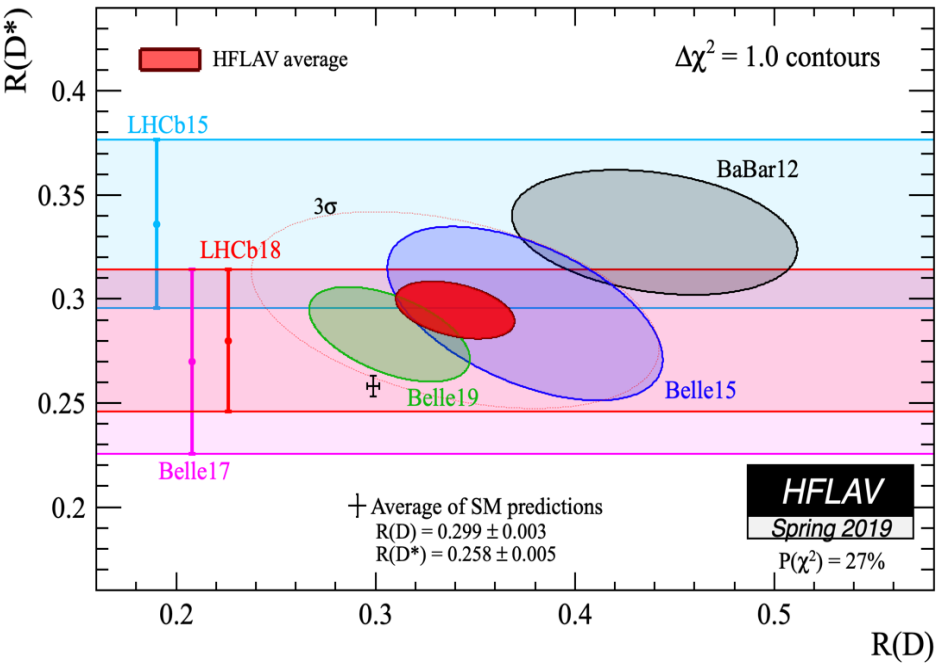
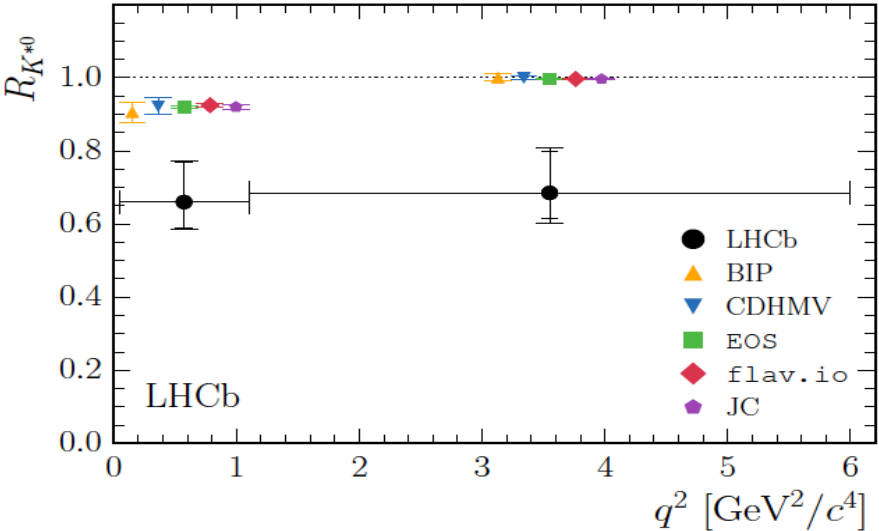
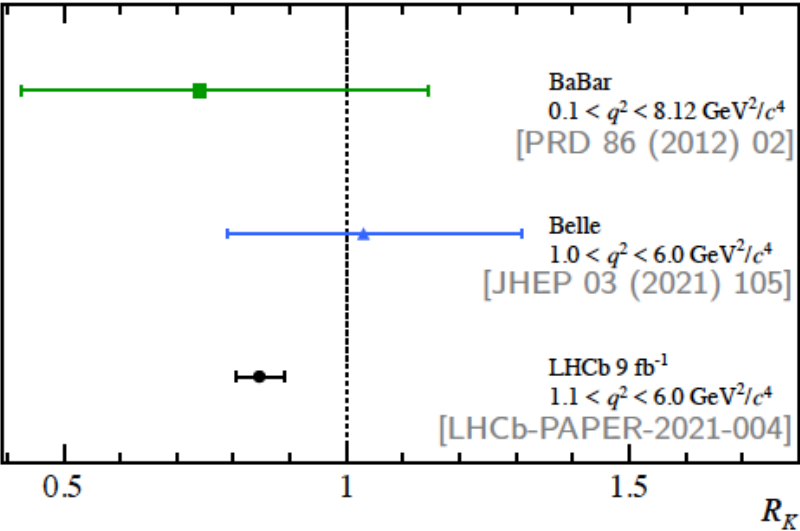
Stringent bounds
on generic
flavor-violating ops.

The big questions in flavor physics:

- Are all the accidental flavor symmetries of the SM broken in the other sectors of the SM-EFT ?
- Can we make sense of the tight NP bounds from flavor-violating processes and still hope to see NP signals somewhere?
And in case where?

Recent data start to provide some answers...

The LFU anomalies



► The LFU anomalies

Since 2013 results in semi-leptonic B decays started to exhibit tensions with the SM predictions connected to a possible violation of **L**epton **F**lavor **U**niversality

More precisely, we seem to observe a different behavior (*beside pure kinematical effects*) of different lepton species in the following processes:

- $b \rightarrow s \, l^+ l^-$ (neutral currents): μ vs. e
- $b \rightarrow c \, l \nu$ (charged currents): τ vs. light leptons (μ, e)

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N.B: **LFU** is an accidental symmetry of the SM Lagrangian in the limit where we neglect the lepton Yukawa couplings.

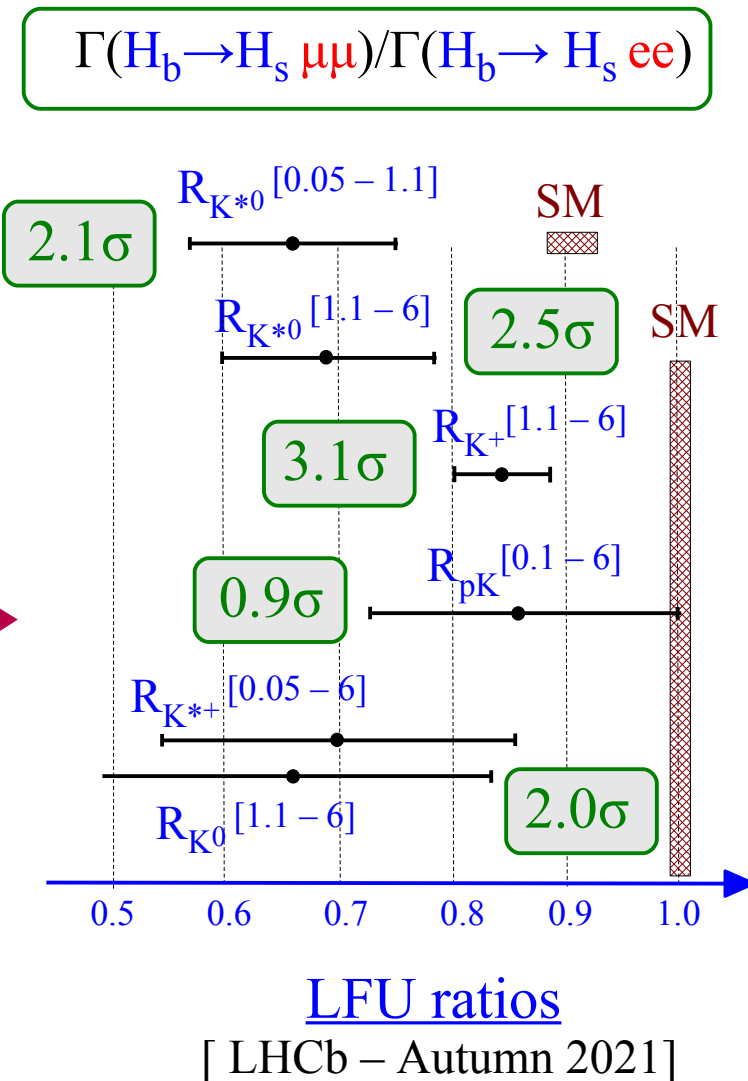
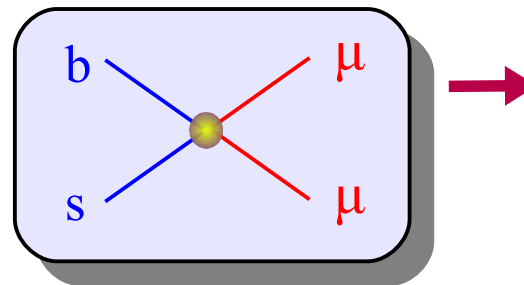
LFU is badly broken in the Yukawa sector: $y_e \sim 3 \times 10^{-6}$, $y_\mu \sim 3 \times 10^{-4}$, $y_\tau \sim 10^{-2}$

but all the lepton Yukawa couplings are small compared to SM gauge couplings, giving rise to the (*approximate*) universality of decay amplitudes which differ only by the different lepton species involved

► The LFU anomalies

- $b \rightarrow s \, l^+ l^-$ (neutral currents): μ vs. e

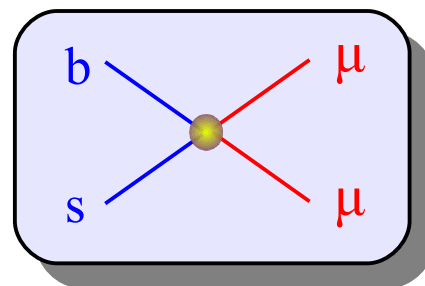
High significance: several observables pointing to the same coherent picture [several new results in 2021]



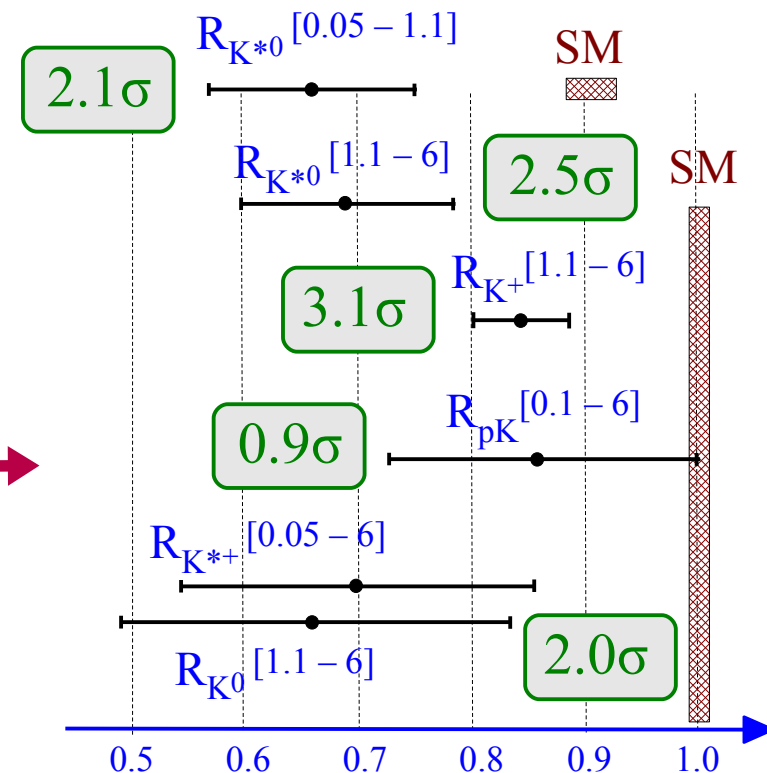
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$$\Gamma(H_b \rightarrow H_s \mu\mu) / \Gamma(H_b \rightarrow H_s ee)$$



$$\text{BR}(B_s \rightarrow \mu\mu)$$

$$\text{BR}_{\text{exp}} = (2.85 \pm 0.32) \times 10^{-9} \quad \text{ATLAS+CMS+LHCb '21}$$

$$\text{BR}_{\text{SM}} = (3.66 \pm 0.14) \times 10^{-9}$$

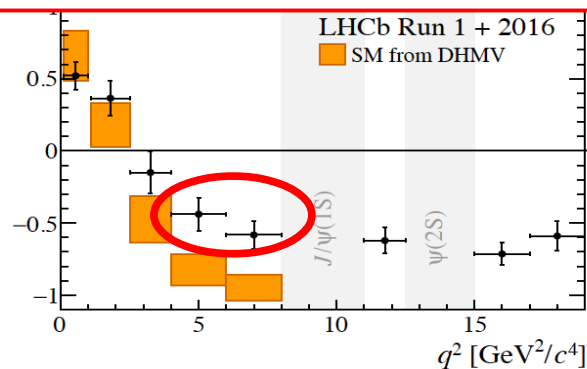
2.3σ

► The LFU anomalies

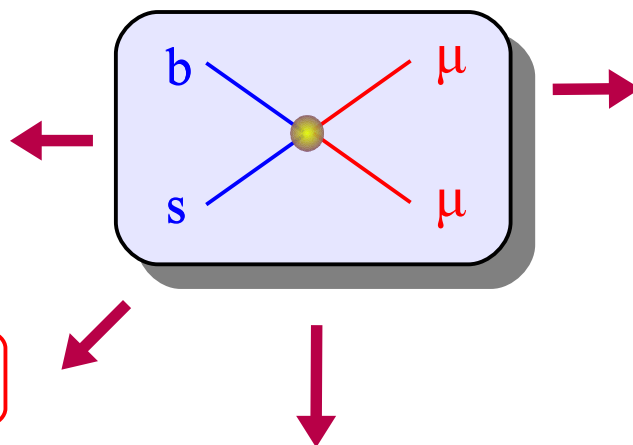
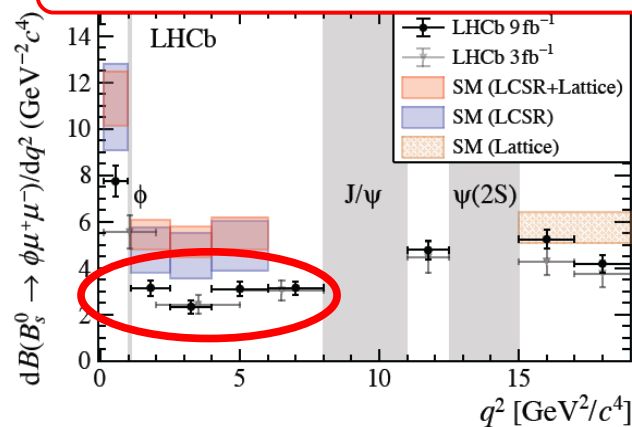
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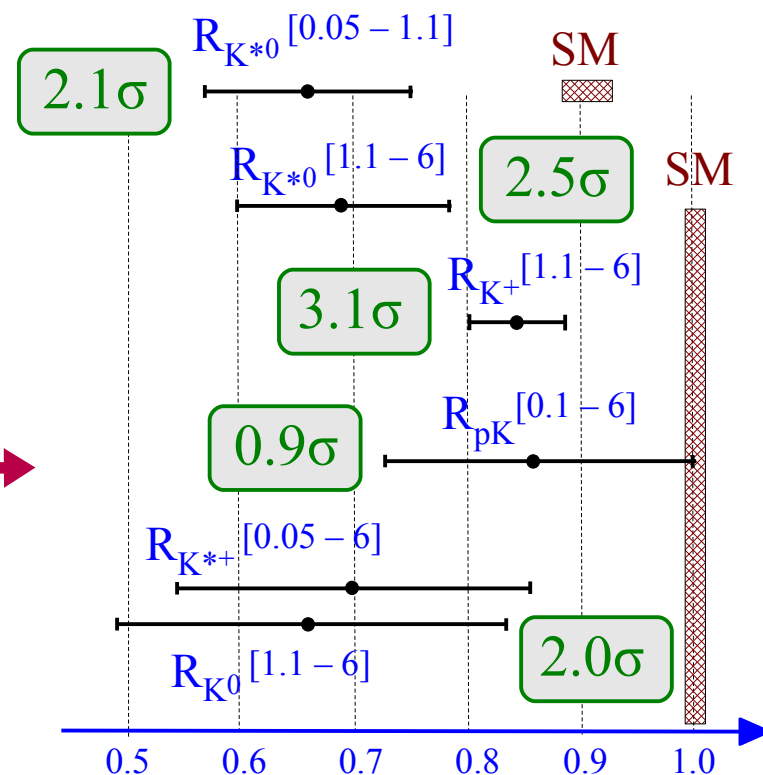
$B \rightarrow K^* \mu\mu$ angular distribution



$B \rightarrow H \mu\mu$ branching ratios



$$\Gamma(H_b \rightarrow H_s \mu\mu) / \Gamma(H_b \rightarrow H_s ee)$$



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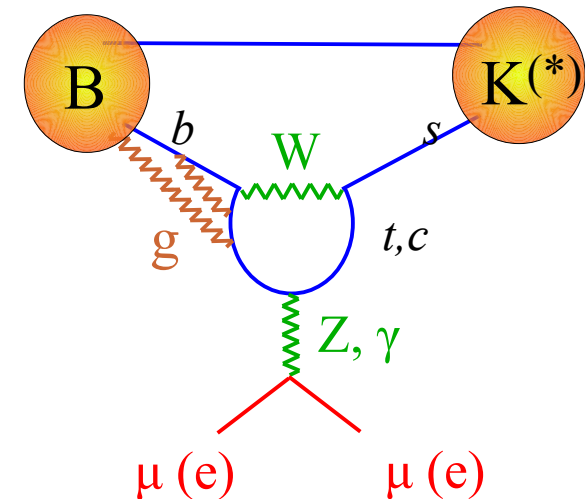
$b \rightarrow s \ell^+ \ell^-$ transitions are forbidden at the tree level within the SM.

Depending on the $q^2 = m^2_{\ell\ell}$ range, they are dominated by

- short distance dynamics
→ *precisely calculable*, more sensitive to NP
- long-distance dynamics
→ *moderate/large theory errors*, small/no sensitivity to NP

N.B: long-distance dynamics is lepton-flavor universal

- cannot generate $C_i^\mu \neq C_i^e$
- does not affect $C_{10}^{\mu,e}$



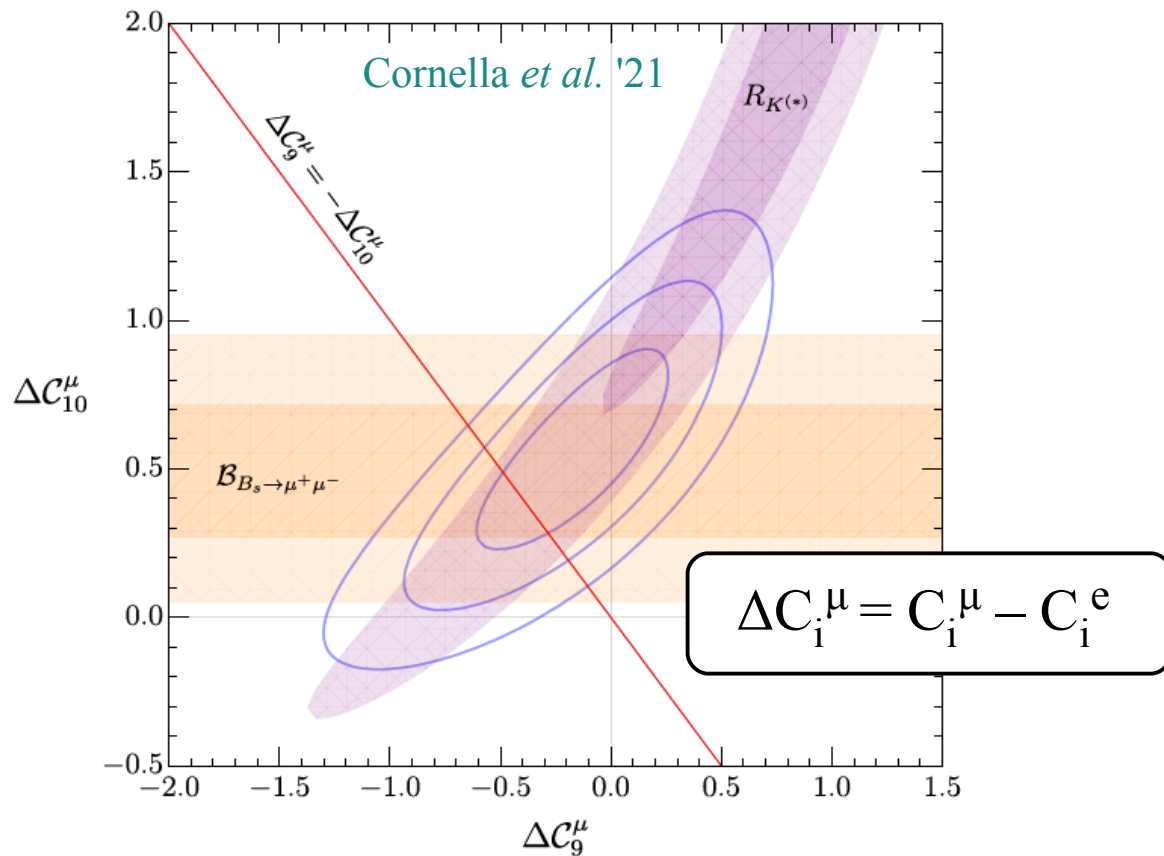
Leading short-distance effective operators:

$$\mathcal{O}_{10}^\ell = (\bar{s}_L \gamma_\mu b_L)(\bar{\ell} \gamma^\mu \gamma_5 \ell)$$

$$\mathcal{O}_9^\ell = (\bar{s}_L \gamma_\mu b_L)(\bar{\ell} \gamma^\mu \ell)$$

► The LFU anomalies

• $b \rightarrow s \ell^+ \ell^-$ (neutral currents): μ vs. e



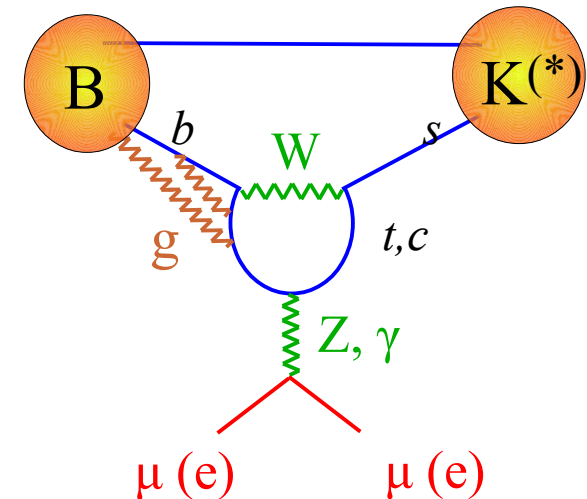
Conservative fit using “clean obs.” only

5.0 σ

significance of NP hypothesis

$\Delta C_9^\mu = -\Delta C_{10}^\mu$ vs. SM

Beyond tree level in SM:



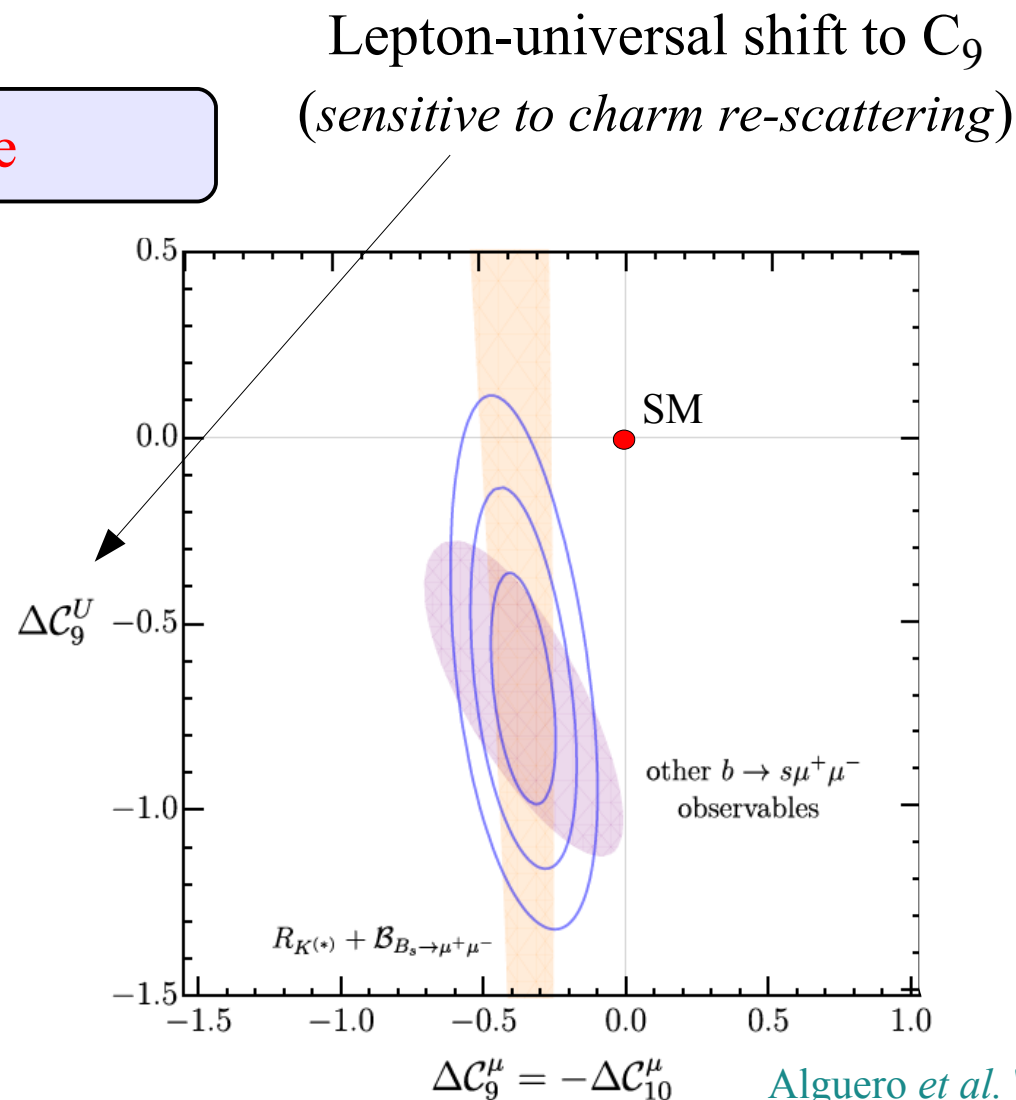
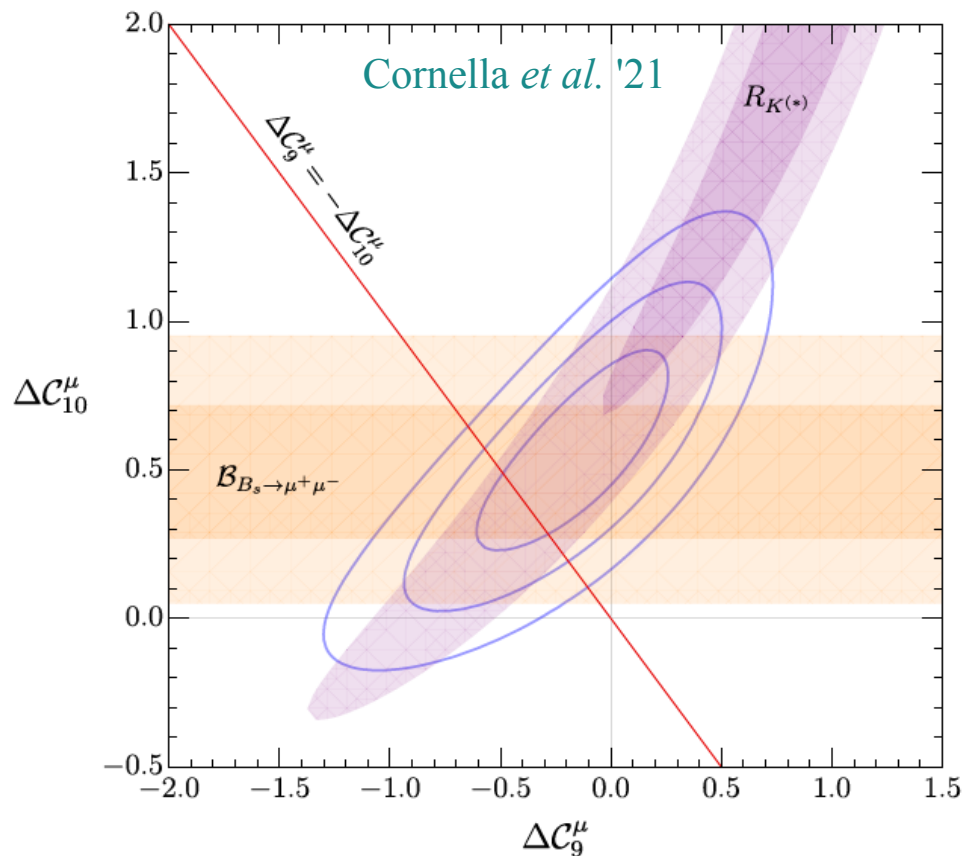
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► The LFU anomalies

• $b \rightarrow s \, l^+ l^-$ (neutral currents): μ vs. e



Conservative fit using “clean obs.” only

$\gg 5\sigma$ best estimate of charm contribution

Alguero et al. '19
Ciuchini et al. '20
Li-Sheng et al. '21
Altmanshofer & Stangl '21

5.0σ

significance of NP hypothesis

$\Delta C_9^\mu = -\Delta C_{10}^\mu$ vs. SM

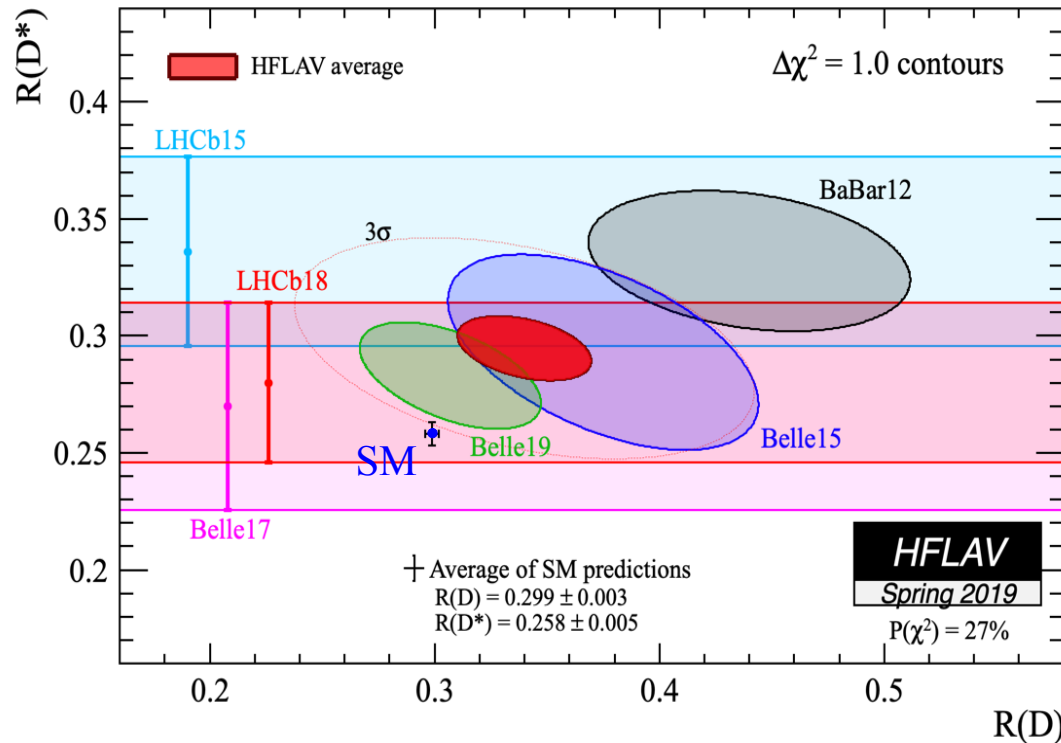
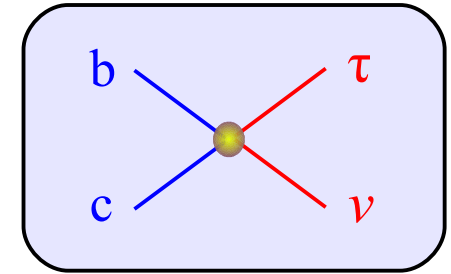
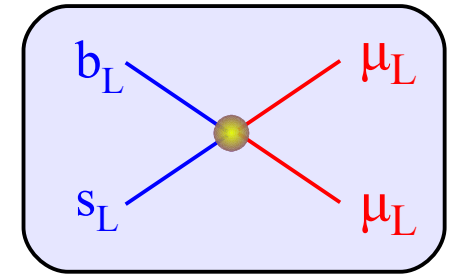
4.3σ global significance of NP
(very conserv. estimate)

GI, Lancierini
Owen, Serra '21

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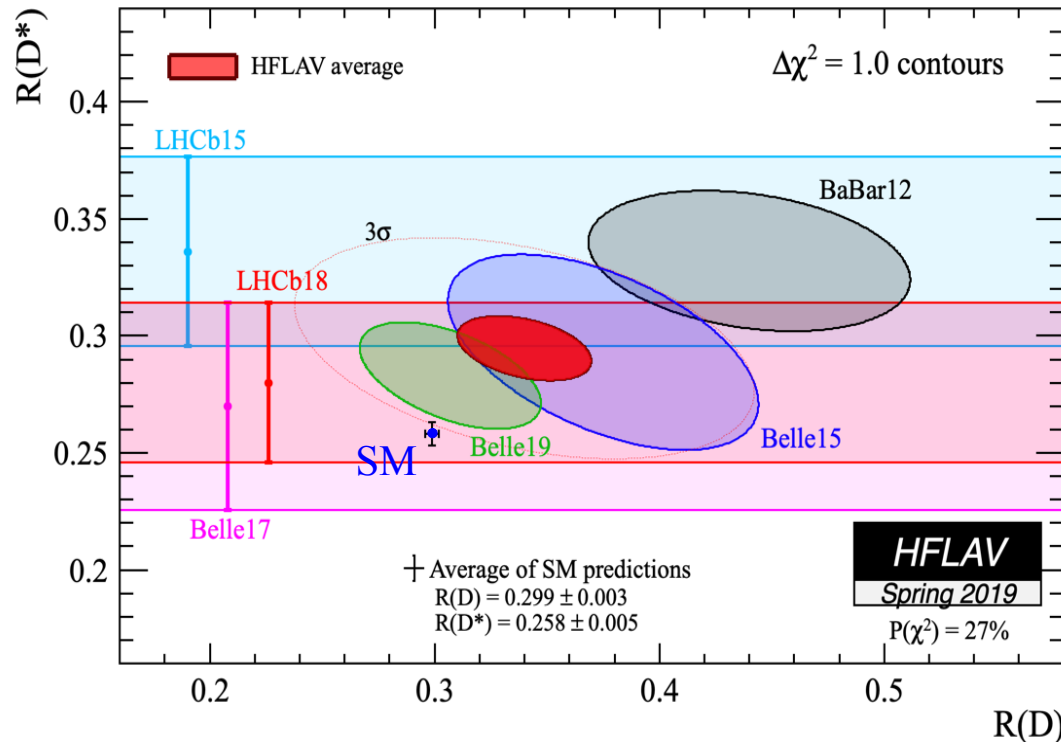
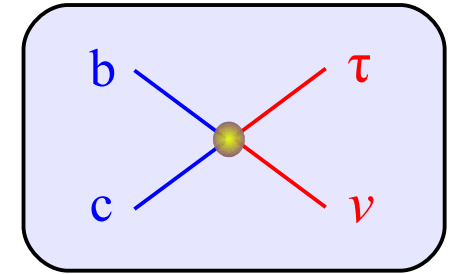
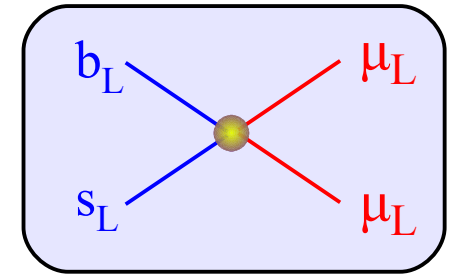
$$R(X) = \frac{\Gamma(B \rightarrow X \, \tau \nu)}{\Gamma(B \rightarrow X \, l \nu)} \quad X = D \text{ or } D^*$$

- Clean SM predictions (*uncertainties cancel in the ratios*)
- Consistent results by 3 different exp.ts: **3.1 σ** excess over SM
- Slower progress

The LFU anomalies

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Not general consensus...

Bordone, Jung, van Dyk '19

$\sim 4\sigma$

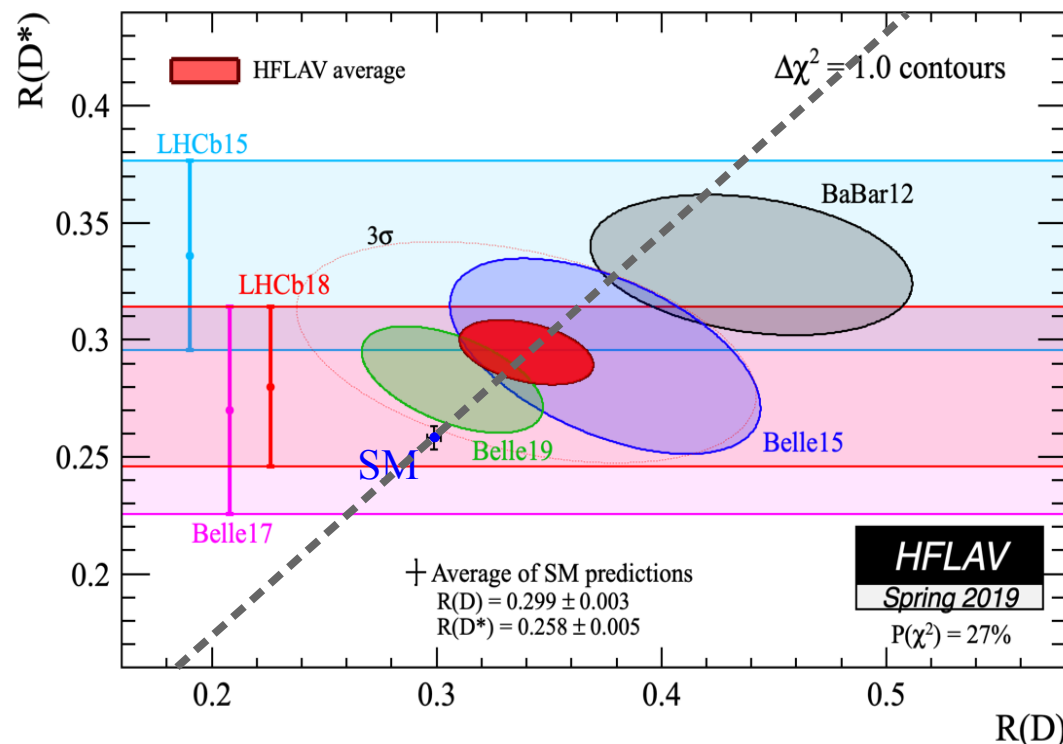
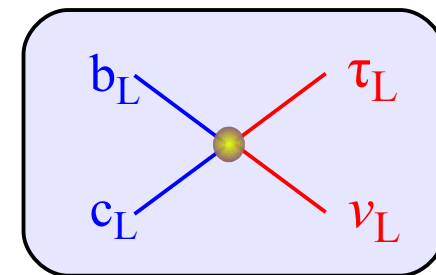
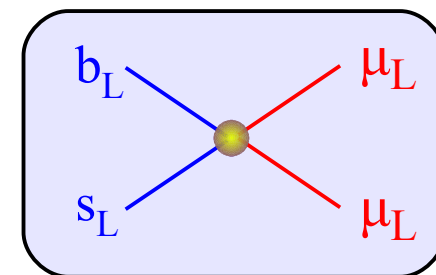
Martinelli, Simula, Vittorio '22

$\sim 2\sigma$

► The LFU anomalies

• $b \rightarrow s \, l^+ l^-$ (neutral currents): μ vs. e

• $b \rightarrow c \, l \nu$ (charged currents): τ vs. light leptons (μ, e)

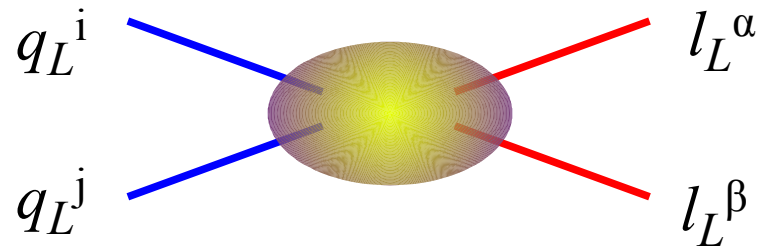


$$R(X) = \frac{\Gamma(B \rightarrow X \, \tau \nu)}{\Gamma(B \rightarrow X \, l \nu)} \quad X = D \text{ or } D^*$$

- Clean SM predictions (*uncertainties cancel in the ratios*)
- Consistent results by 3 different exp.ts: **3.1 σ** excess over SM
- Slower progress

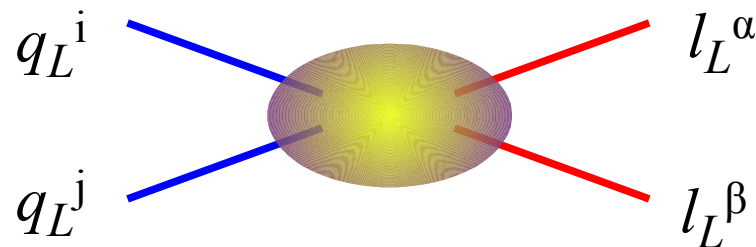
- Large NP effect competing with tree-level SM amplitude
- Left-handed NP amplitude describe well data (*but other options still possible*)

EFT considerations on the LFU anomalies



► EFT considerations

- Anomalies are seen only in semi-leptonic (quark \times lepton) operators
- We definitely need non-vanishing left-handed current-current operators although other contributions are also possible



Bhattacharya *et al.* '14
 Alonso, Grinstein, Camalich '15
 Greljo, GI, Marzocca '15
 (+many others...)

- Large coupl. [*compete with SM tree-level*] in $b(3^{\text{rd}}) \ c(2^{\text{nd}}) \rightarrow \tau(3^{\text{rd}}) \ \nu_\tau(3^{\text{rd}})$
- Small coupl. [*compete with SM loop-level*] in $b(3^{\text{rd}}) \ s(2^{\text{nd}}) \rightarrow \mu(2^{\text{rd}}) \ \mu(2^{\text{rd}})$



$$C_{ij\alpha\beta} = \begin{array}{c} \text{large for} \\ 3^{\text{rd}} \text{ generation} \\ \text{fields} \end{array} + \begin{array}{c} \text{small terms} \\ \text{for } 2^{\text{nd}} \text{ (\& } 1^{\text{st}}) \\ \text{generations} \end{array}$$

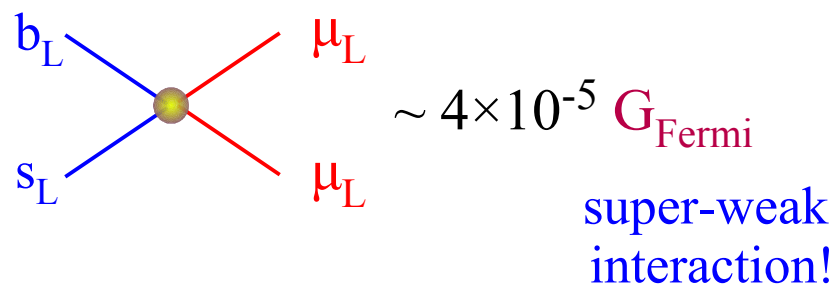


*Link to pattern
 of the Yukawa
 couplings !*

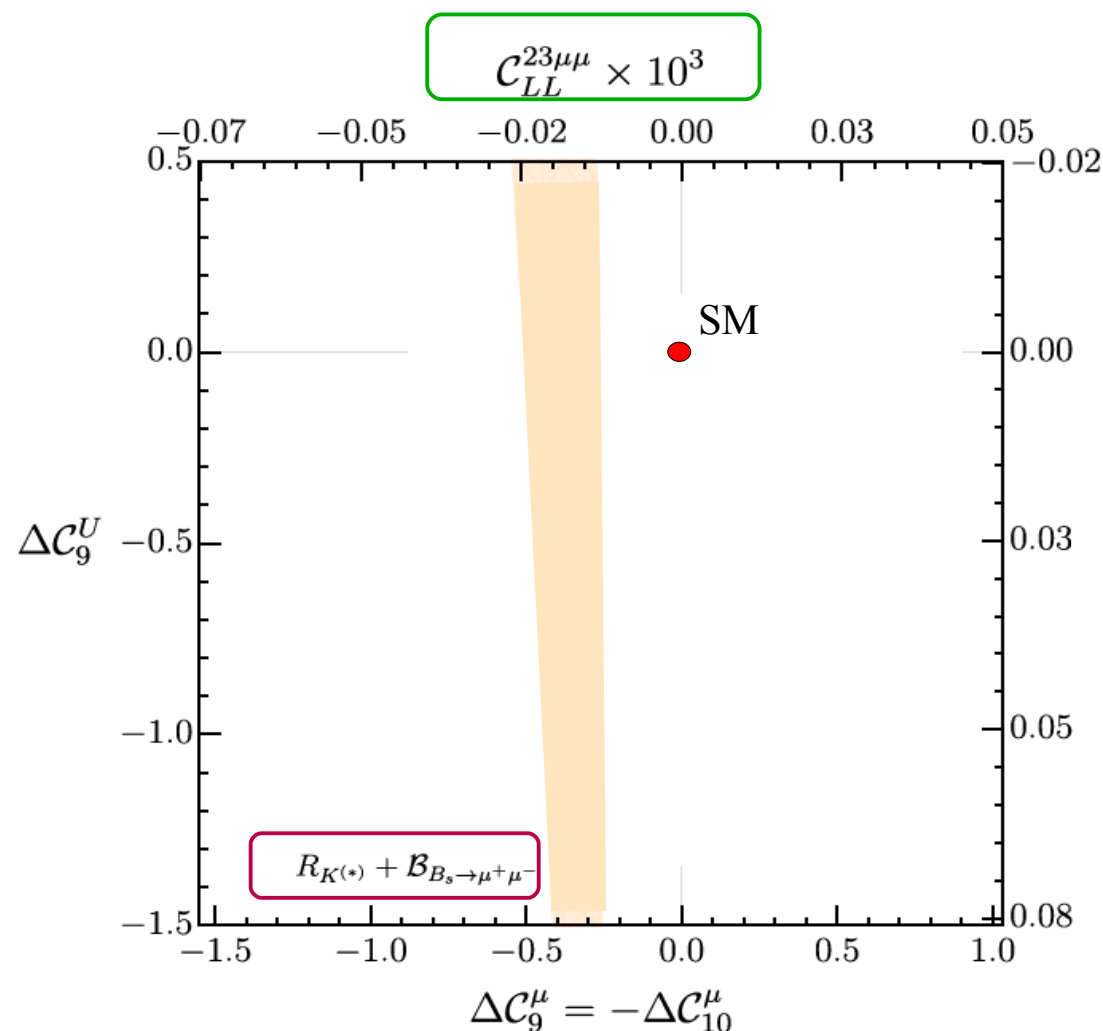
► EFT considerations

Data point to (short-distance) NP effects in operators of the type

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{\ell}_L^\beta \gamma_\mu q_L^j)$$



$$C_{LL}^{23\mu\mu} \rightarrow \Delta C_9^\mu = -\Delta C_{10}^\mu$$

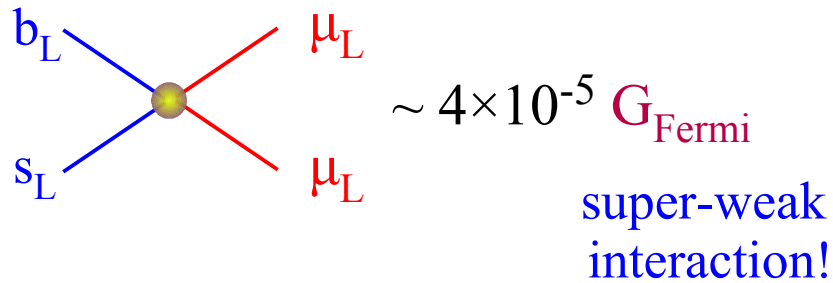


► EFT considerations

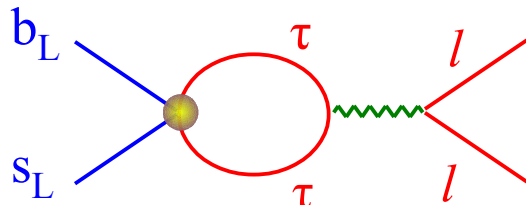
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$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{\ell}_L^\beta \gamma_\mu q_L^j)$$

✓ $\mathcal{O}(10^{-1})$ suppress. for each 2nd gen. l_L

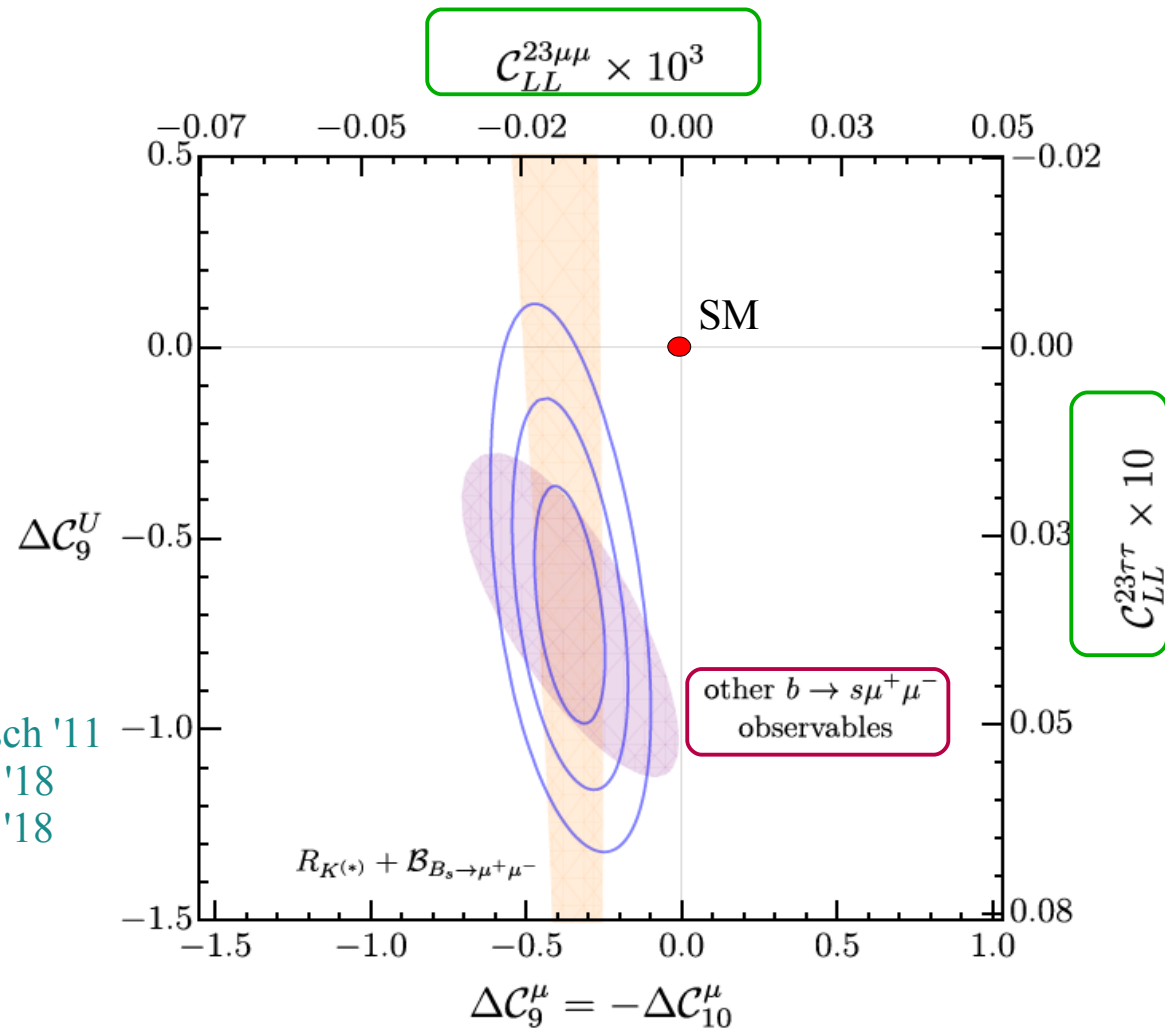


$$C_{LL}^{23\mu\mu} \rightarrow \Delta C_9^\mu = -\Delta C_{10}^\mu$$



$$C_{LL}^{23\tau\tau} \rightarrow \Delta C_9^{\text{Univ}}$$

Bobeth & Haisch '11
Crivellin *et al.* '18
Alguero *et al.* '18

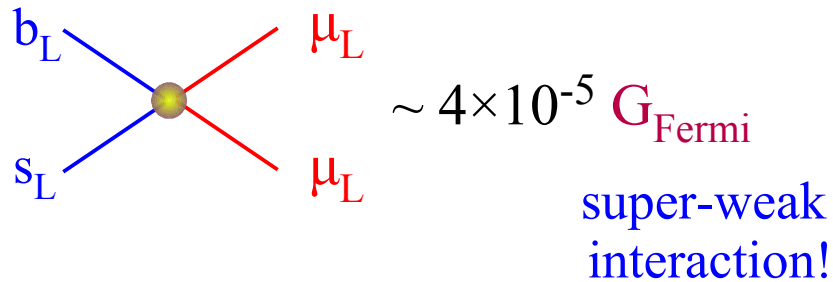


► EFT considerations

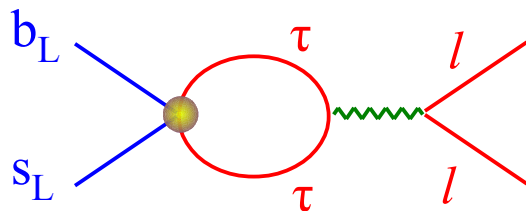
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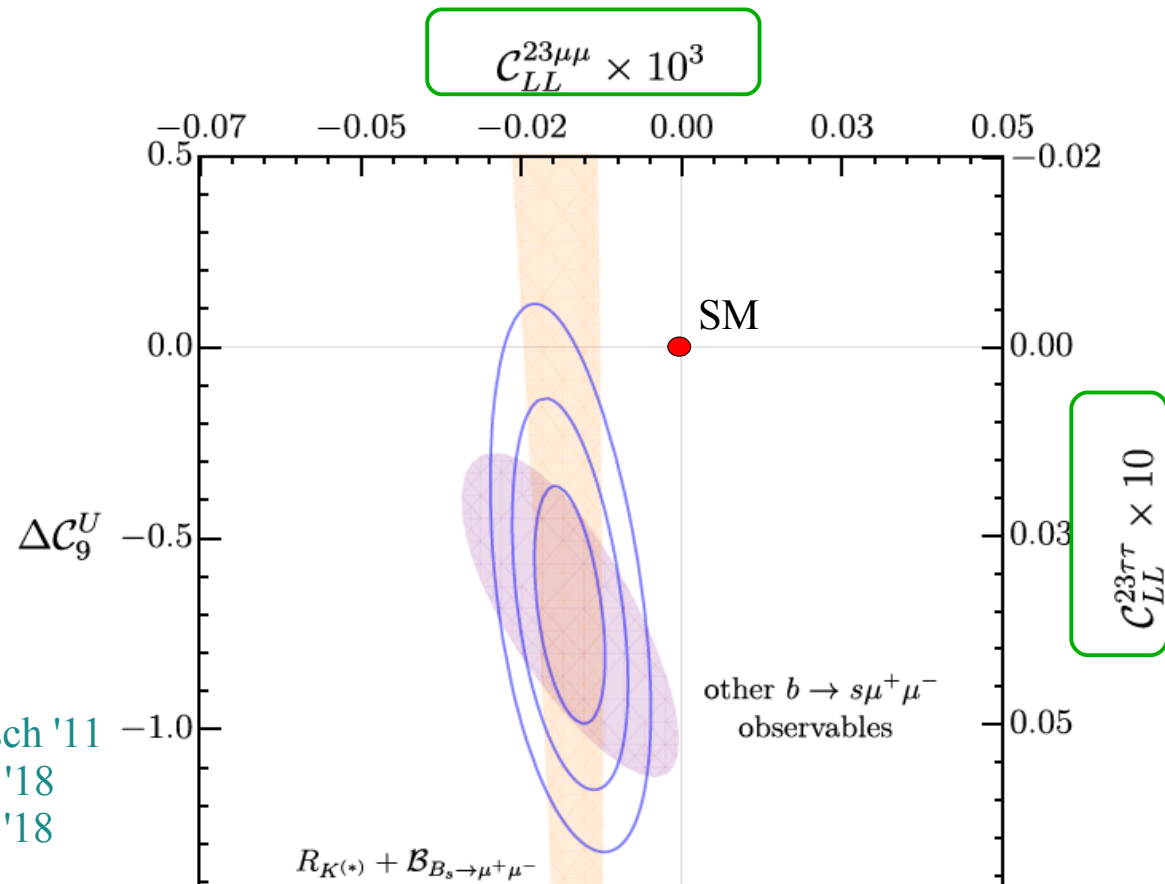
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Bobeth & Haisch '11
Crivellin *et al.* '18
Alguero *et al.* '18

$$C_{LL}^{23\tau\tau} \rightarrow \Delta C_9^{\text{Univ}}$$

Link to CC anomaly



Size (and need) of $C^{23\tau\tau}$ pre-dicted from CC before this effect was observed in NC

Greljo *et al.* '17

► EFT considerations

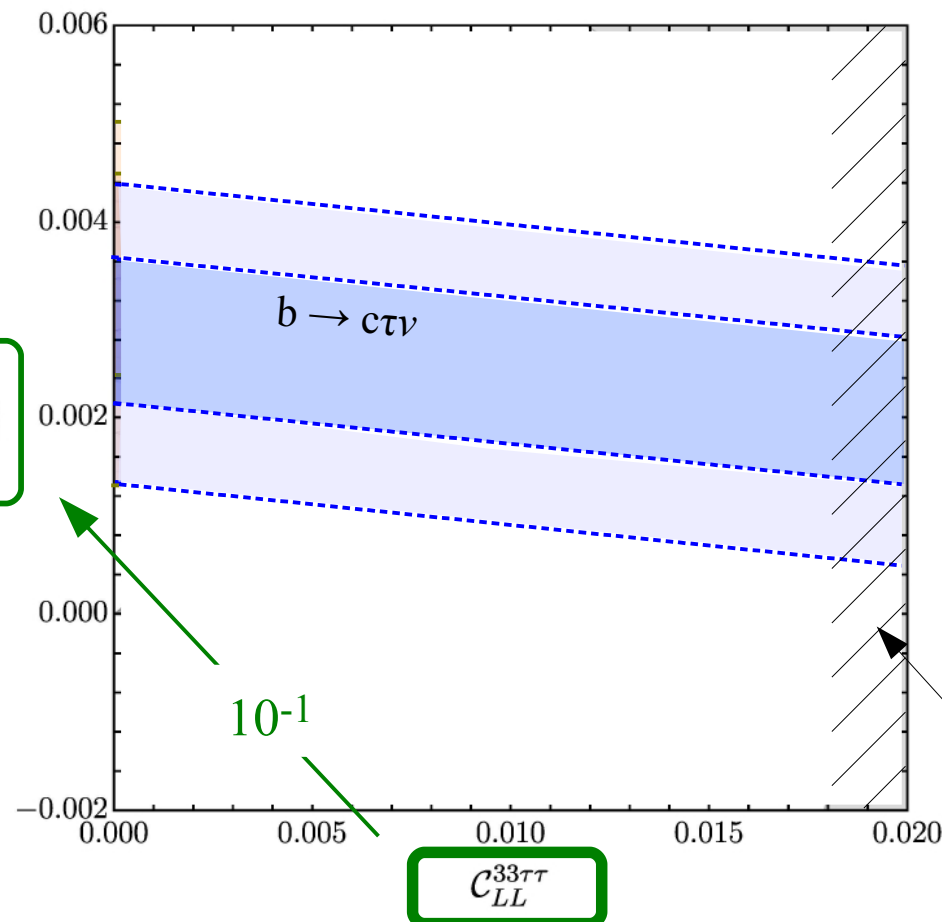
Data point to (short-distance) NP effects in operators of the type

✓ $O(10^{-1})$ suppress. for each 2nd gen. q_L or l_L

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{\ell}_L^\beta \gamma_\mu q_L^j)$$

charged-currents:

$$\frac{V_{cb} \mathcal{C}_{LL}^{33\tau\tau} + V_{cs} \mathcal{C}_{LL}^{23\tau\tau}}{V_{cb}}$$

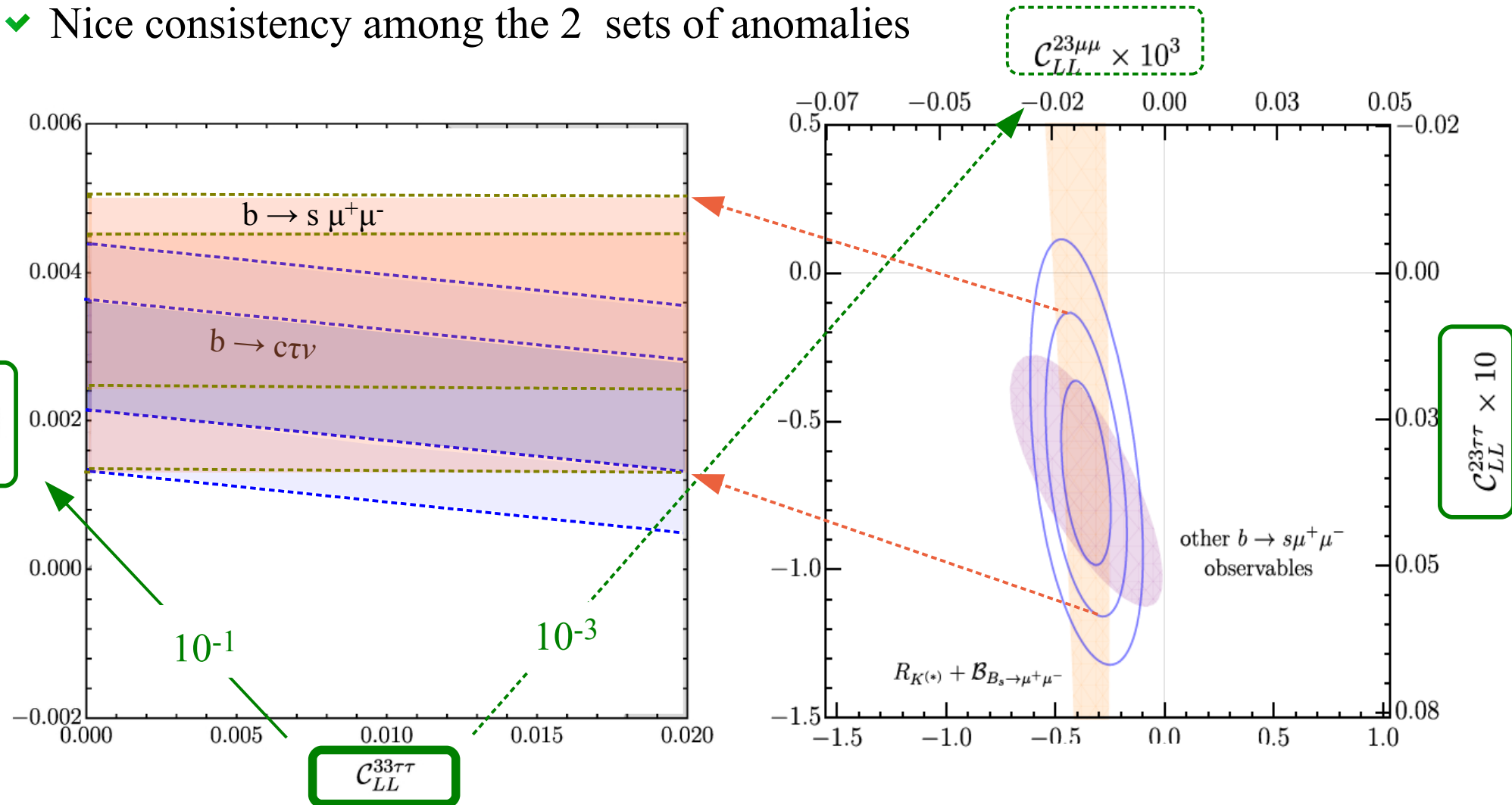


► EFT considerations

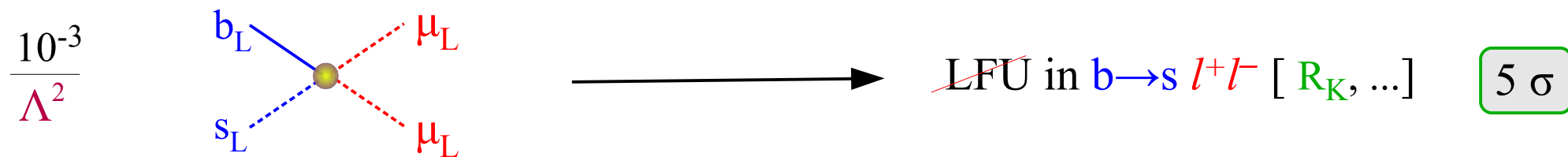
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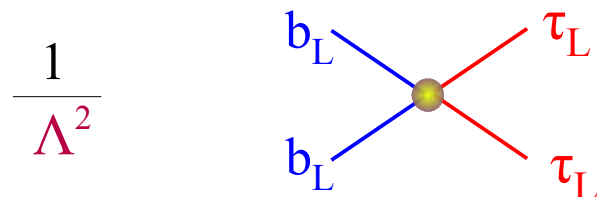
- ✓ $\mathcal{O}(10^{-1})$ suppress. for each 2nd gen. q_L or l_L
- ✓ Nice consistency among the 2 sets of anomalies



► EFT considerations



“*natural*”
flavor
connection

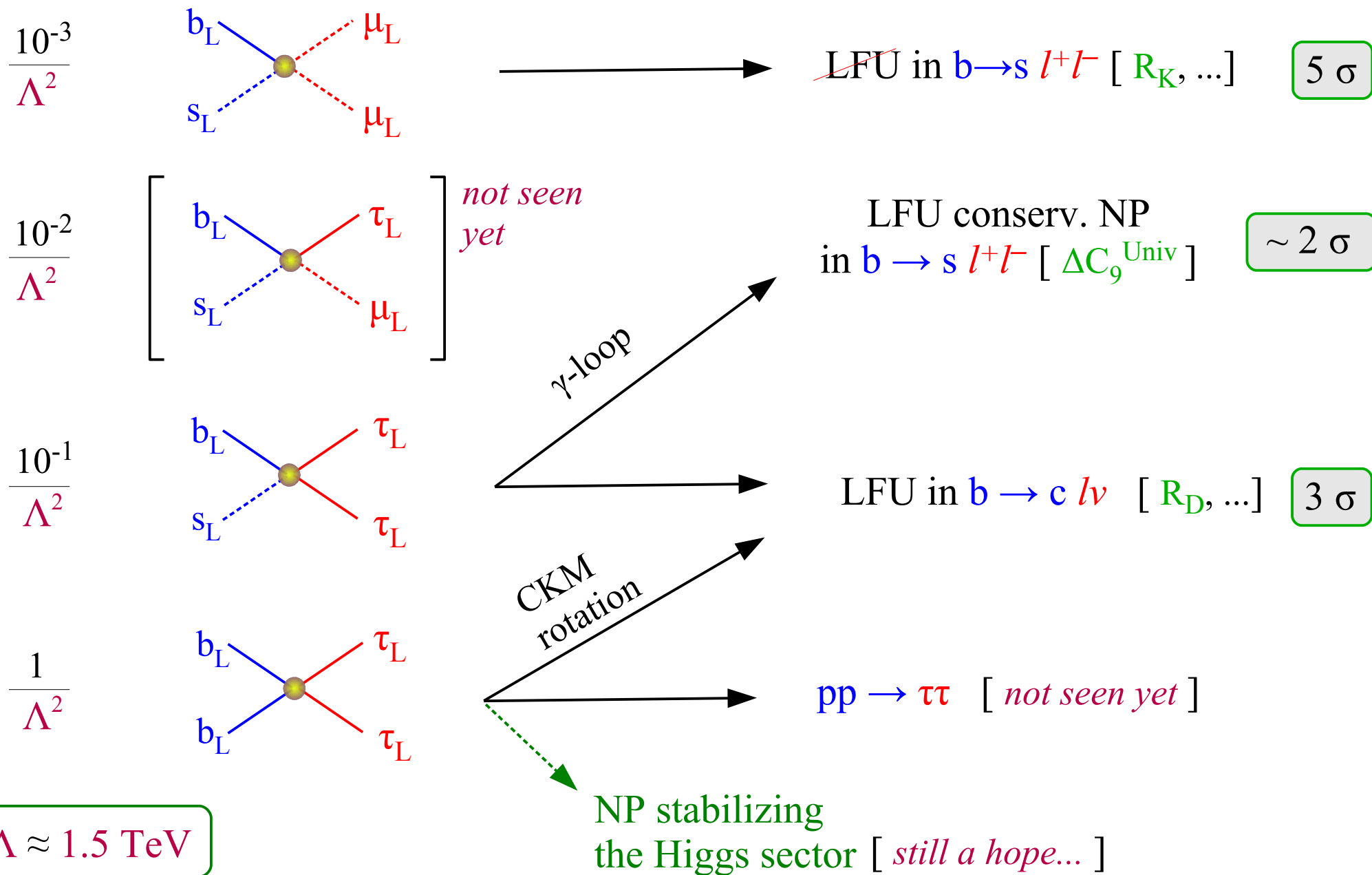


CKM
rotation

LFU in $b \rightarrow c \, l \nu$ [R_D, \dots]

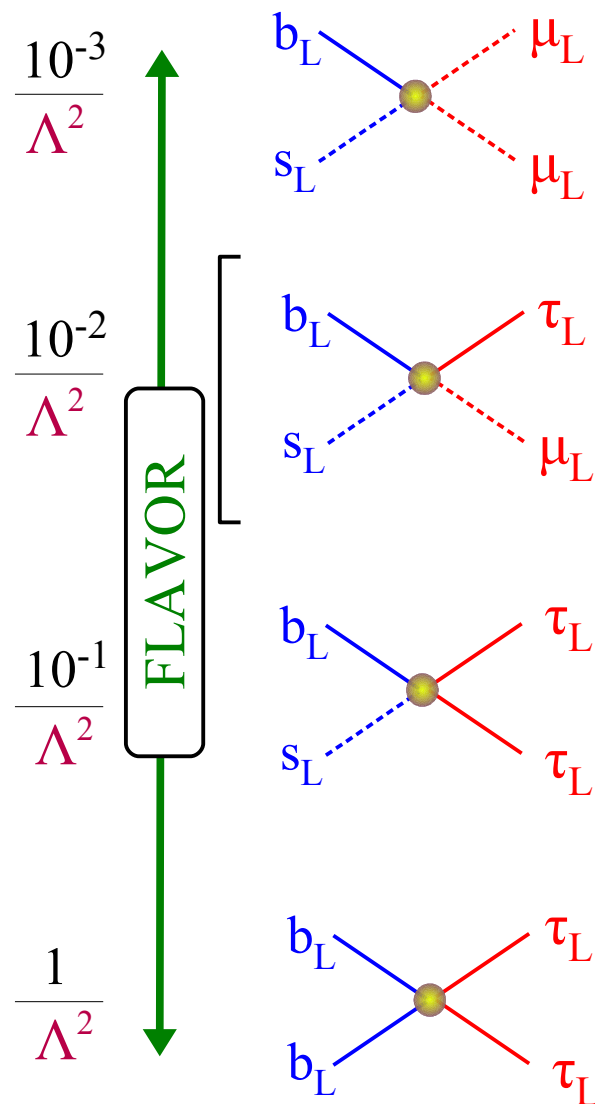
$\Lambda \approx 1.5 \text{ TeV}$

► EFT considerations



► EFT considerations

An exciting “narrow path” connecting old problems and recent anomalies



$\Lambda \approx 1.5 \text{ TeV}$

not seen yet

LFU in $b \rightarrow s \, l^+ l^-$ [R_K, \dots] 5σ

LFU conserv. NP in $b \rightarrow s \, l^+ l^-$ [ΔC_9^{Univ}] $\sim 2 \sigma$

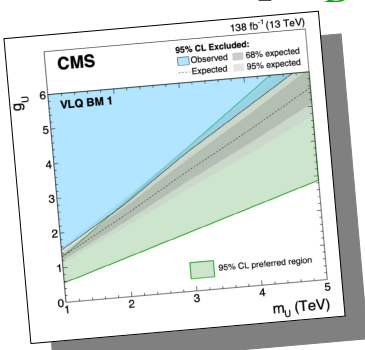
γ -loop

LFU in $b \rightarrow c \, l \nu$ [R_D, \dots] 3σ

CKM rotation

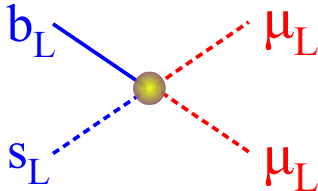
$pp \rightarrow \tau \tau$ $\sim 1 \sigma$

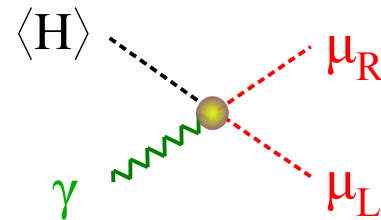
NP stabilizing the Higgs sector



Higgs = pNGB of the new dynamics (\leftrightarrow LQ mass)

► EFT considerations

$$|V_{ts}| \frac{1}{\Lambda^2}$$


$$\frac{e}{16\pi^2} \frac{1}{\Lambda^2}$$


A possible alternative story...

→ ~~LFU~~ in $b \rightarrow s \text{ } l^+ l^-$ [R_K, \dots]

5σ

→ $\Delta a_\mu = (a_\mu^{\text{exp}} - a_\mu^{\text{SM}})$

$\sim 4 \sigma$

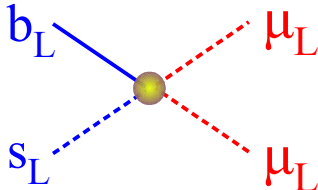
(more controversial...)

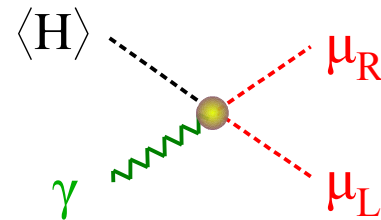
Ignoring the (less convincing) CC anomaly other paths are certainly possible...

$$\Lambda \approx 10 \text{ TeV}$$

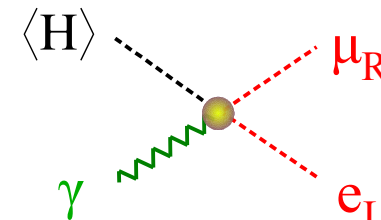
► EFT considerations

A possible alternative story...

$$|V_{ts}| \frac{1}{\Lambda^2}$$


$$\frac{e}{16\pi^2} \frac{1}{\Lambda^2}$$


However...

$$\frac{e}{16\pi^2} \frac{\Theta_{\mu e}}{\Lambda^2}$$


$$|\Theta_{\mu e}| < 2 \times 10^{-5}$$

Possible unified description by means of a new interaction with special role for muons (and maybe tau's)

Greljo, Stangl, Thomsen '21
Baum *et al.* '21
Davighi, '21
Altmannshofer *et al.* '21
+ *many others...*

Tight constraint
involving
several ops

Exact flavor symm.
@ work the lepton
sector

*different behavior
of quarks &
leptons*

$$\Lambda \approx 10 \text{ TeV}$$

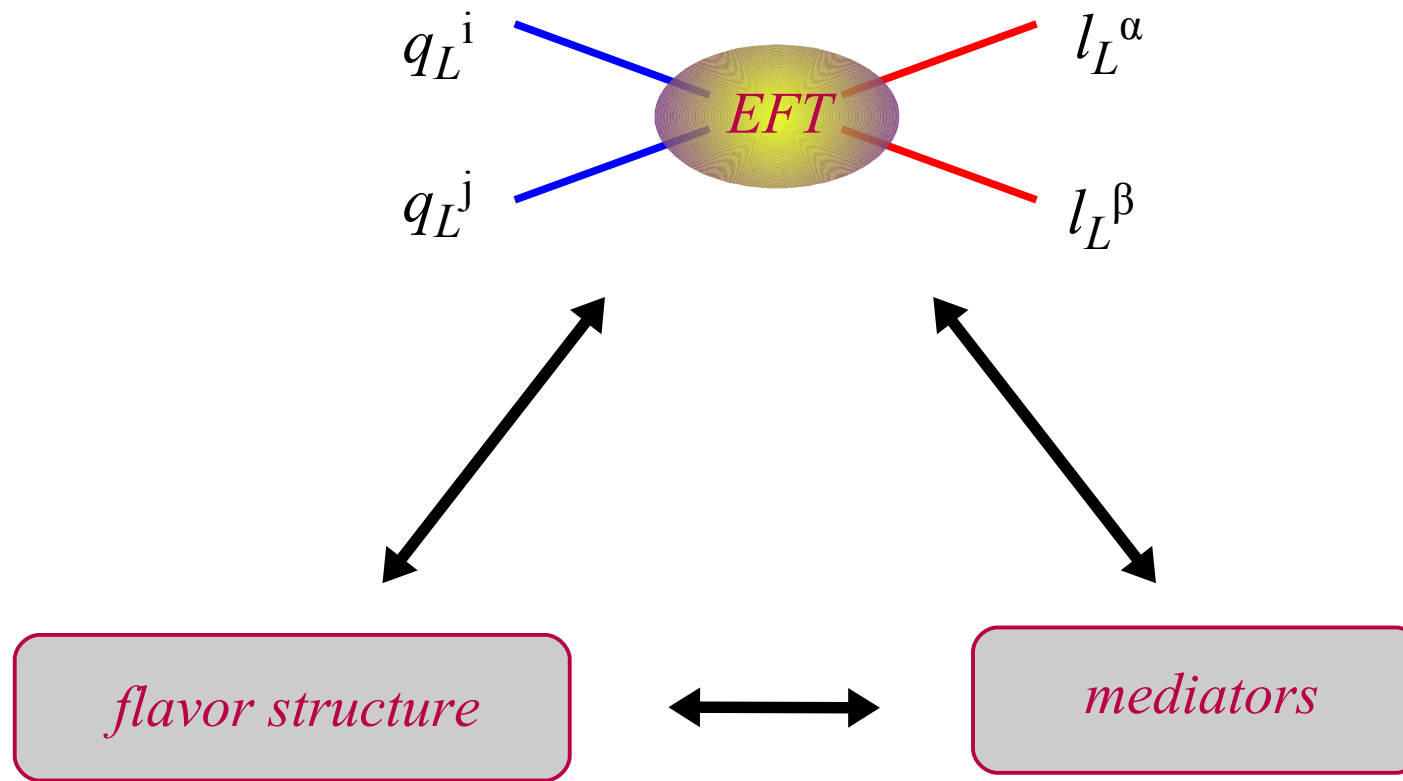
GI, Pages, Wilsch '21

Model-building considerations



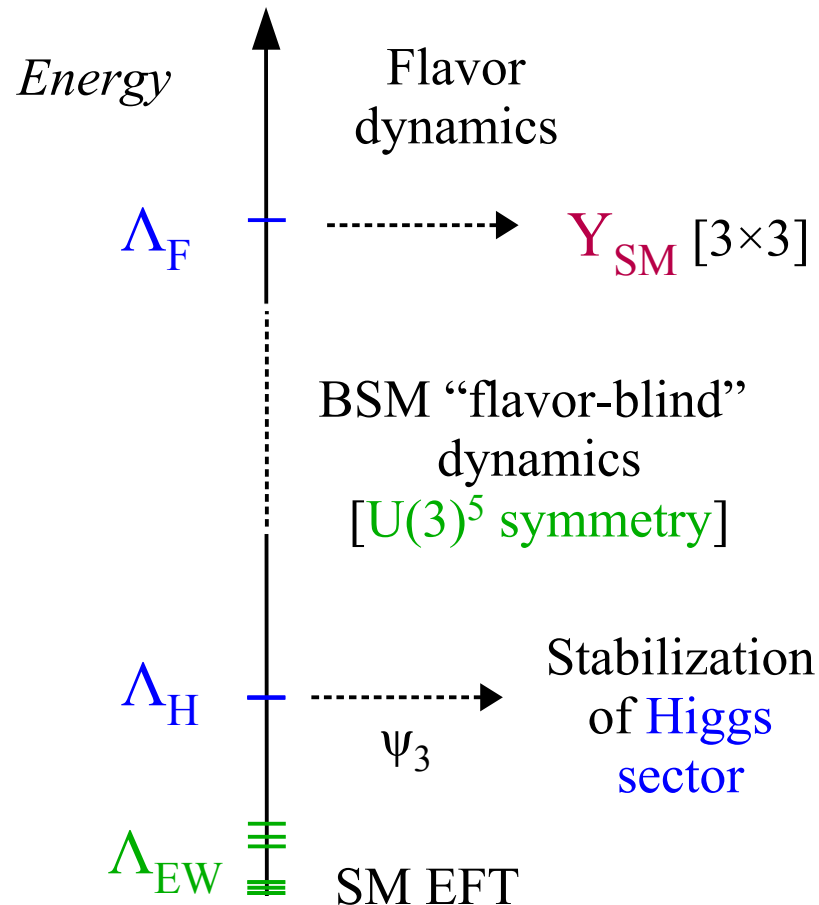
► Model-building considerations

To move from the EFT toward more complete/ambitious models, we need to address two general aspects: the *flavor structure* of the underlying theory, and the nature of the possible *mediators*



► Model-building considerations

The old (Minimal Flavor Violation) paradigm:



Main idea:

- Concentrate on the Higgs hierarchy problem
- Postpone (ignore) the flavor problem

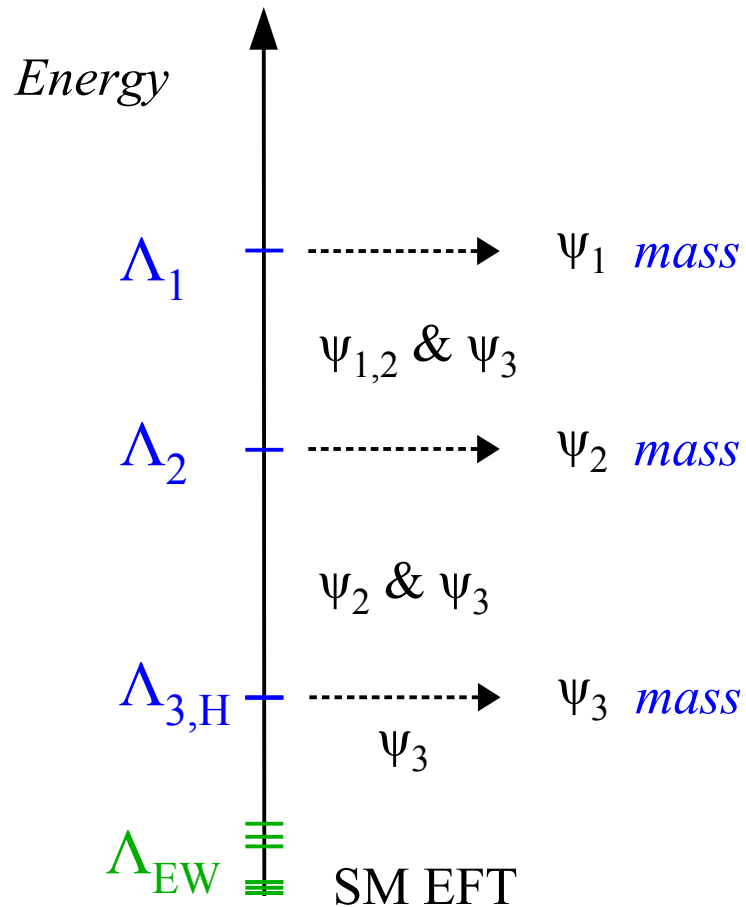


3 gen. = “identical copies”
up to high energies

► Model-building considerations

~~The old (MFV) paradigm~~

Multi-scale picture @ origin of flavor:



Bordone *et al.* '17
 Allwicher, GI, Thomsen '20
 Barbieri '21

Panico & Pomarol '16
 ⋮
 Dvali & Shifman '00

Main idea:

- Flavor **non-universal interactions** already at the **TeV scale**:
- **1st & 2nd gen.** have small masses because they are coupled to **NP at heavier scales**

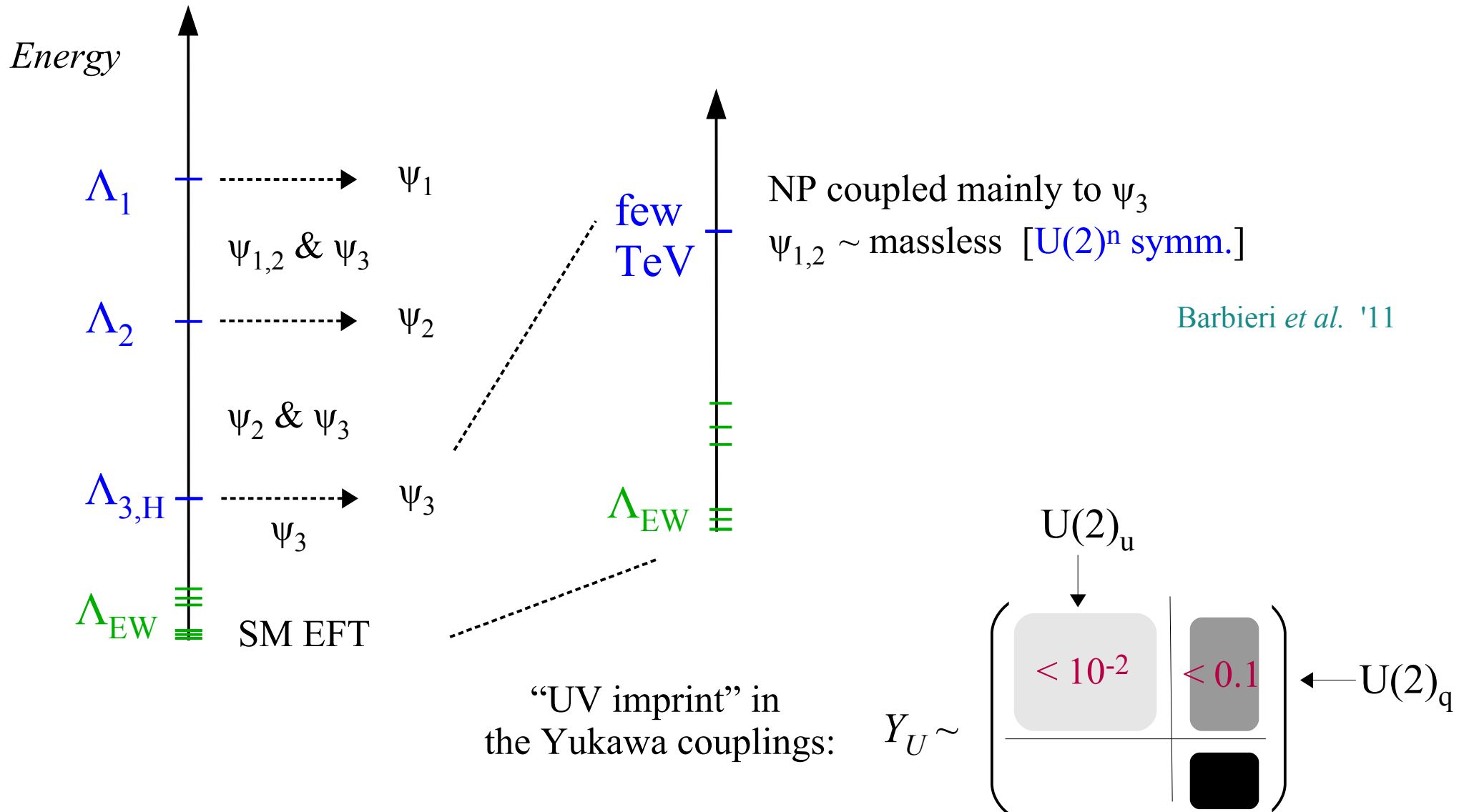


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► Model-building considerations

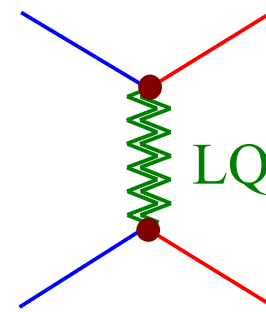
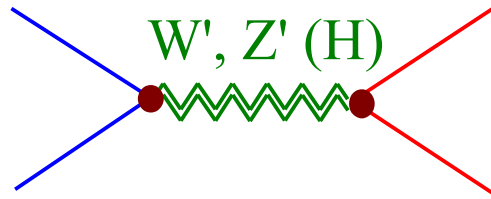
~~The old (MEV) paradigm~~

Multi-scale picture @ origin of flavor:



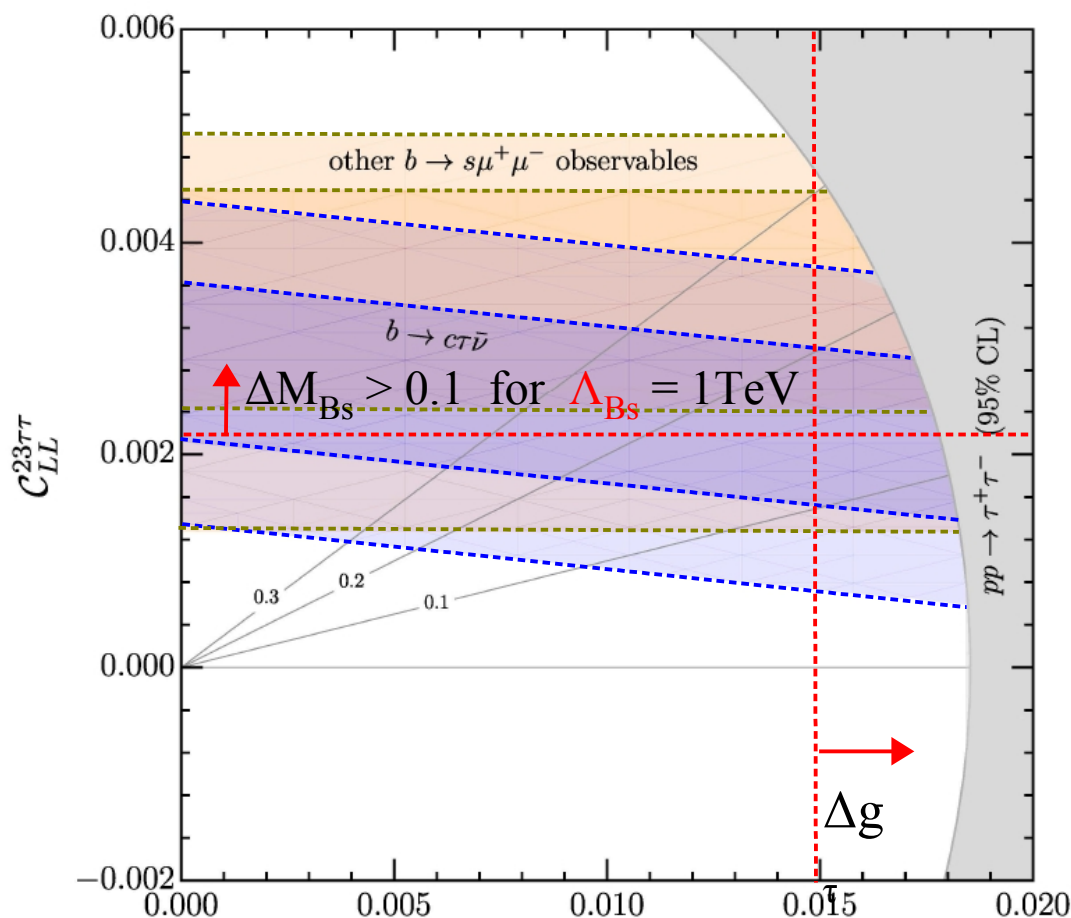
► Model-building considerations

Which mediators can generate the effective operators required for by the EFT fit?
If we restrict the attention to tree-level mediators, not many possibilities...



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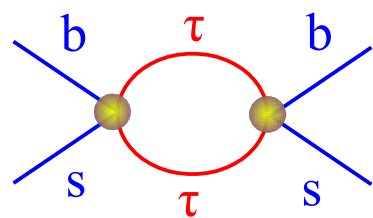


Pattern emerging from data:

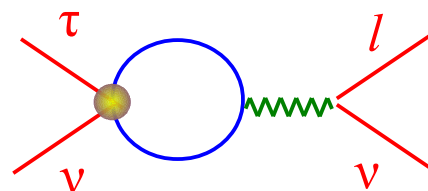
- ✓ $O(10^{-1})$ for each 2nd gen. q_L or l_L
- ✓ Nice consistency among the two sets of anomalies

What we do not see (*seem to call for an additional loop suppression*):

- ✗ Four-quarks ($\Delta F=2$)
- ✗ Four-leptons ($\tau \rightarrow \mu \nu \nu$)
- ✗ Semi-leptonic $O^{(1-3)}$ ($b \rightarrow s \nu \nu$)



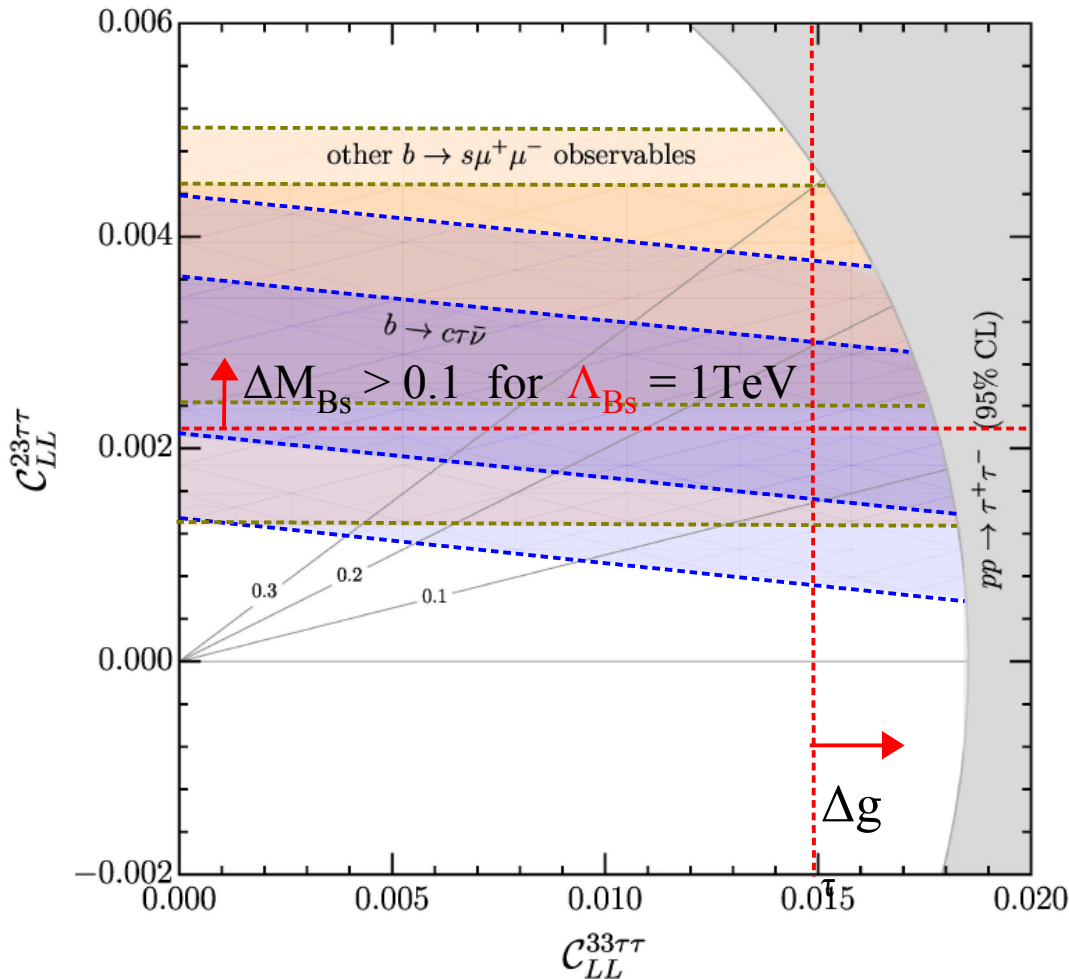
$$\Delta M_{B_s} \sim (C_{LL}^{23\tau\tau})^2 \Lambda_{B_s}^2$$



$$\Delta g_\tau \sim (C_{LL}^{33\tau\tau}) \log(\Lambda/m_t)$$

► Model-building considerations

Which mediators can generate the effective operators required for by the EFT fit?
If we restrict the attention to tree-level mediators, not many possibilities...



Pattern emerging from data:

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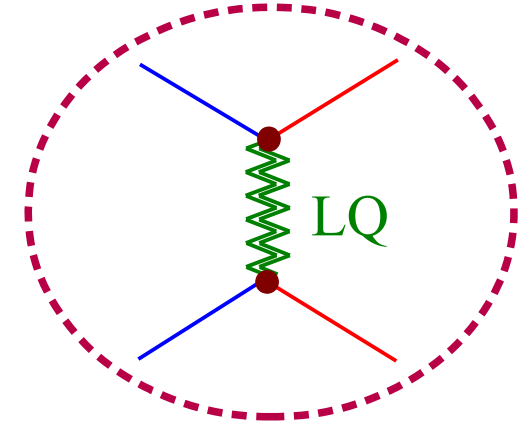
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Leptoquarks

► Model-building considerations

“Renaissance” of LQ models
(*to explain the anomalies, but not only...*):



- Scalar LQ as PNG
Gripaios, '10
Gripaios, Nardecchia, Renner, '14
Marzocca '18
- Scalar LQ from GUTs & ~~R~~ SUSY
Hiller & Schmaltz, '14; Becirevic *et al.* '16,
Fajfer *et al.* '15-'17; Dorsner *et al.* '17;
Crivellin *et al.* '17; Altmannshofer *et al.* '17
Trifinopoulos '18, Becirevic *et al.* '18 + ...
- Vector LQ in GUT gauge models

Assad *et al.* '17
Di Luzio *et al.* '17
Bordone *et al.* '17
Heeck & Teresi '18
+ ...
- Vector LQ as techni-fermion resonances
Barbieri *et al.* '15;
Buttazzo *et al.* '16,
Barbieri, Murphy, Senia, '17 + ...
- LQ as Kaluza-Klein excit.
Megias, Quiros, Salas '17
Megias, Panico, Pujolas, Quiros '17
Blanke, Crivellin, '18 + ...

► Model-building considerations

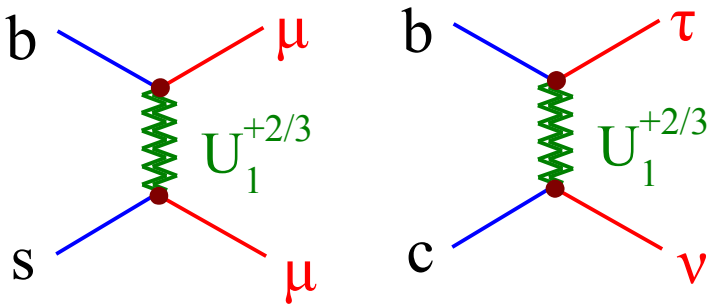
Which LQ explains which anomaly?

	Model	$R_{K(*)}$	$R_{D(*)}$	$R_{K(*)}$ & $R_{D(*)}$
Scalars	$S_1 = (\mathbf{3}, \mathbf{1})_{-1/3}$	✗	✓	✗
	$R_2 = (\mathbf{3}, \mathbf{2})_{7/6}$	✗	✓	✗
	$\tilde{R}_2 = (\mathbf{3}, \mathbf{2})_{1/6}$	✗	✗	✗
	$S_3 = (\mathbf{3}, \mathbf{3})_{-1/3}$	✓	✗	✗
Vector	$U_1 = (\mathbf{3}, \mathbf{1})_{2/3}$	✓	✓	✓
	$U_3 = (\mathbf{3}, \mathbf{3})_{2/3}$	✓	✗	✗

Angelescu, Becirevic, DAF, Sumensari [1808.08179]

Barbieri, GI,
Pattori, Senia '15

- mediator: U_1
- flavor structure: $U(2)^n$
- UV completion: $SU(4)$



LQ of the Pati-Salam
gauge group:

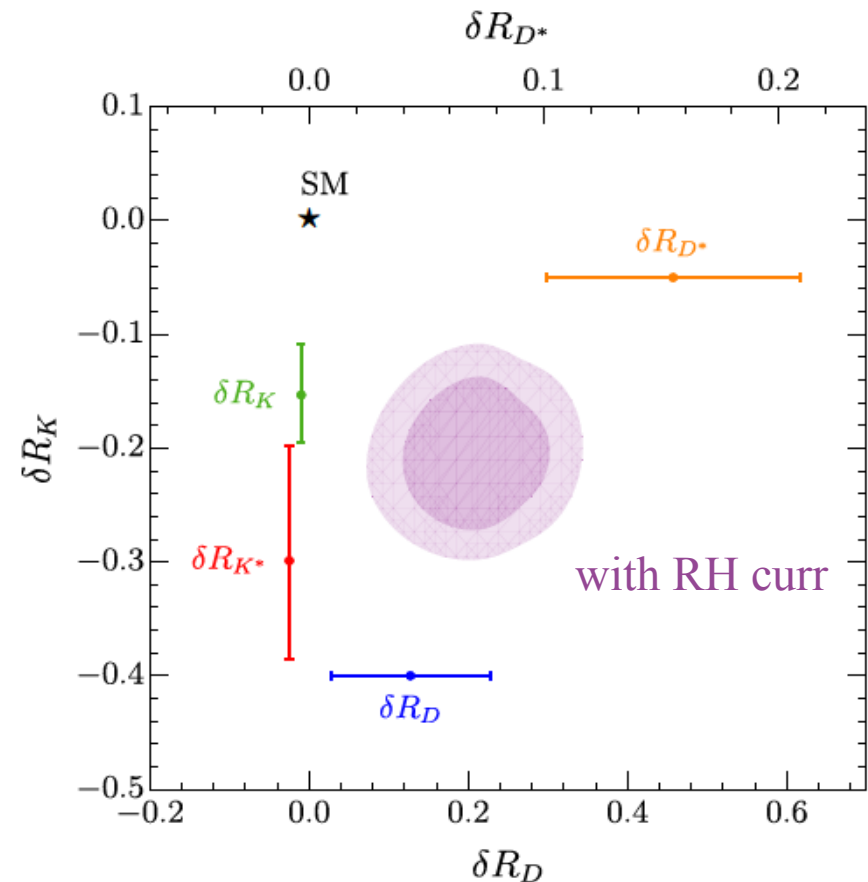
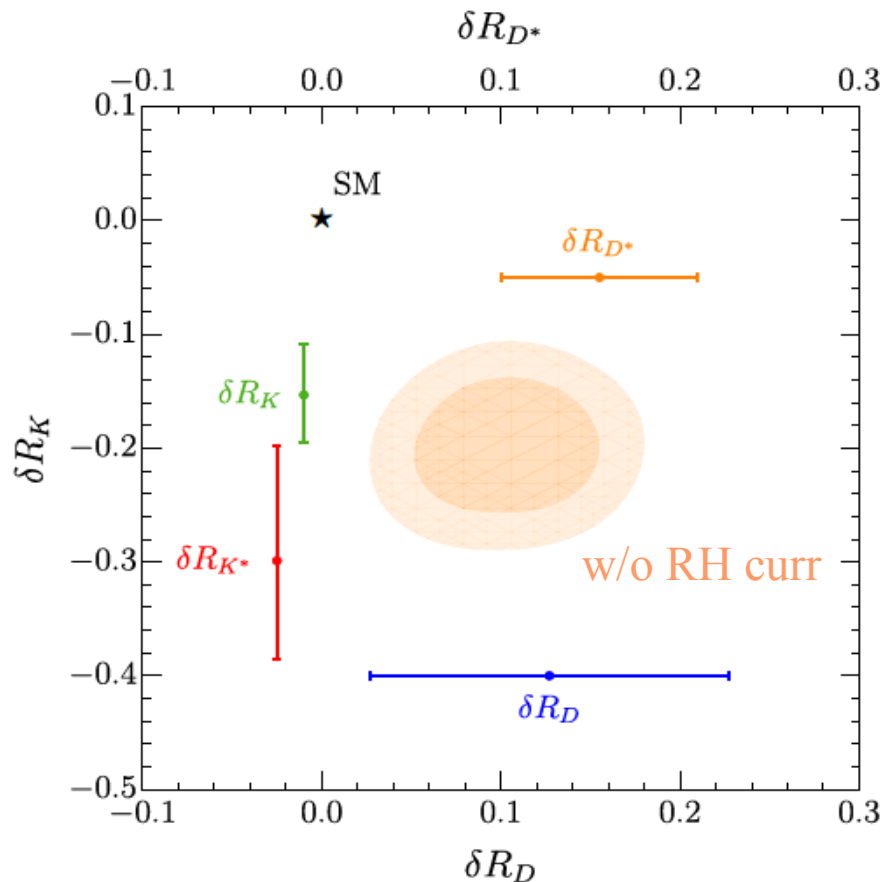
$SU(4) \times SU(2)_L \times SU(2)_R$

Model-building considerations

Considering the U_1 only

$$\mathcal{L} \supset \frac{g_U}{\sqrt{2}} U_1^\mu \left[\beta_{i\alpha}^L (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) - \beta_{i\alpha}^R (\bar{d}_R^i \gamma_\mu e_R^\alpha) \right] + \text{h.c.}$$

→ excellent description of all available low-energy data [*beyond tree-level...*] :



► Model-building considerations

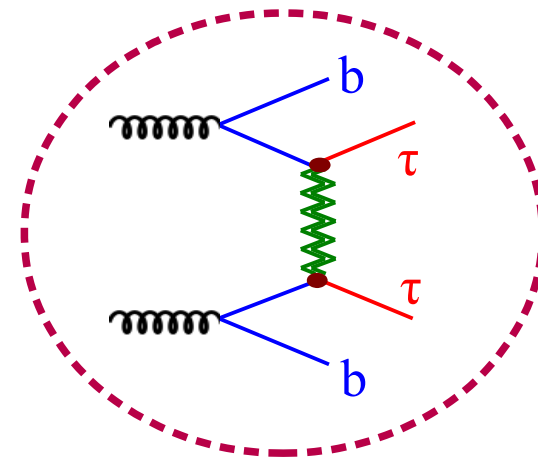
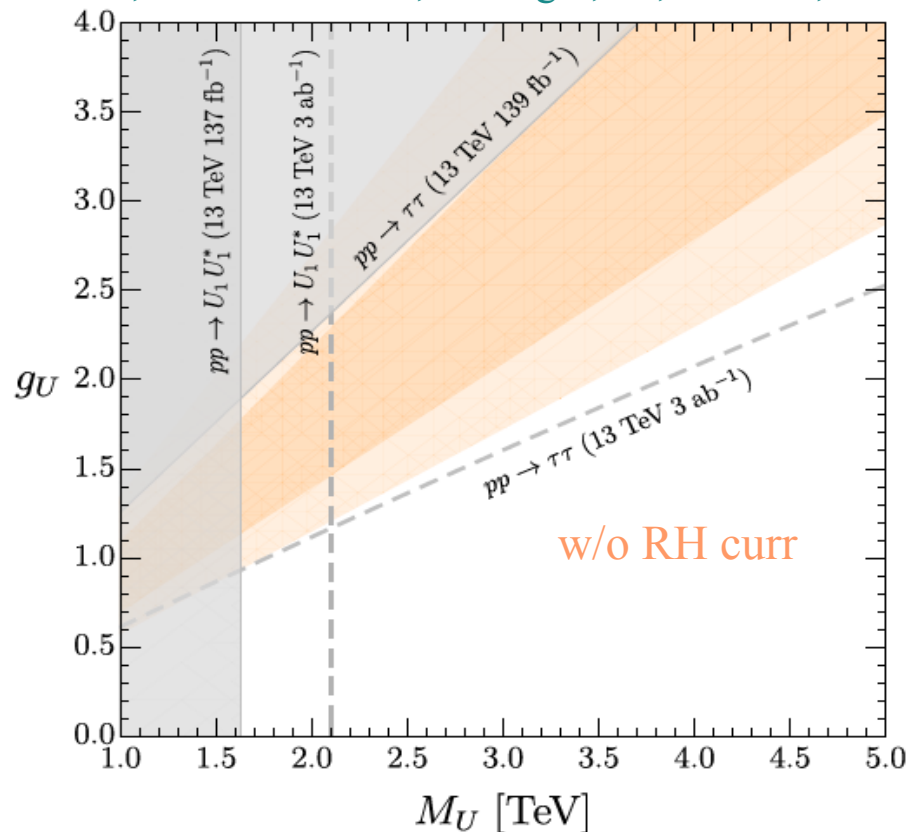
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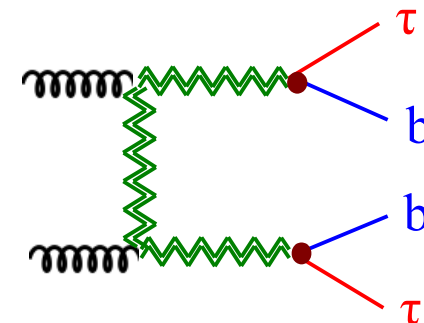
→ excellent description of all available low-energy data

→ consistent with present high-energy data → *signals within the reach of HL-LHC:*

Cornella, Fuentes-Martin, Faroughi, GI, Neubert, '21



Faroughi, Greljo, Kamenik '16



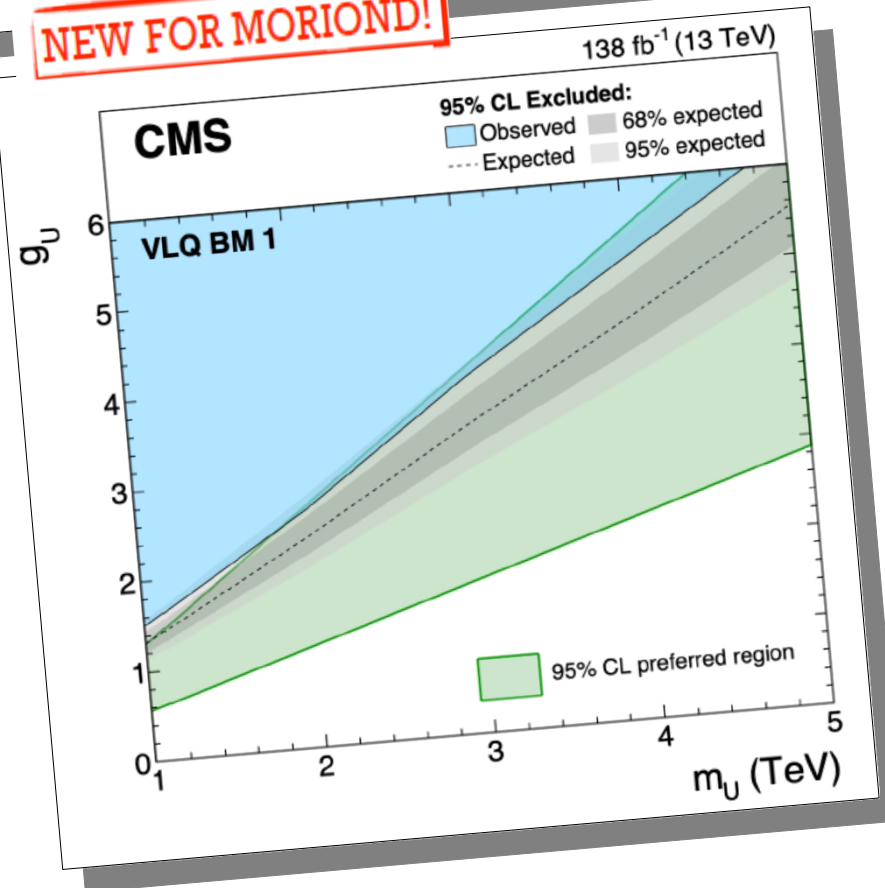
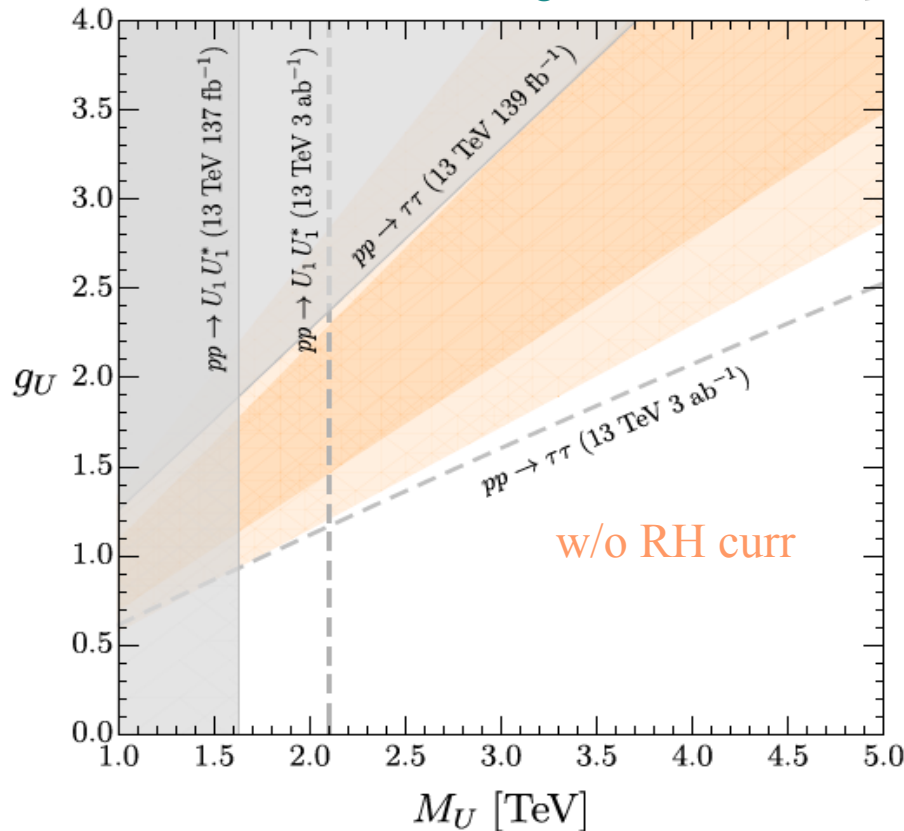
Model-building considerations

Considering the U_1 only

$$\mathcal{L} \supset$$

- excellent description of all available
- consistent with present high-energy

Cornella, Fuentes-Martin, Faroughi, GI, Neubert, Z

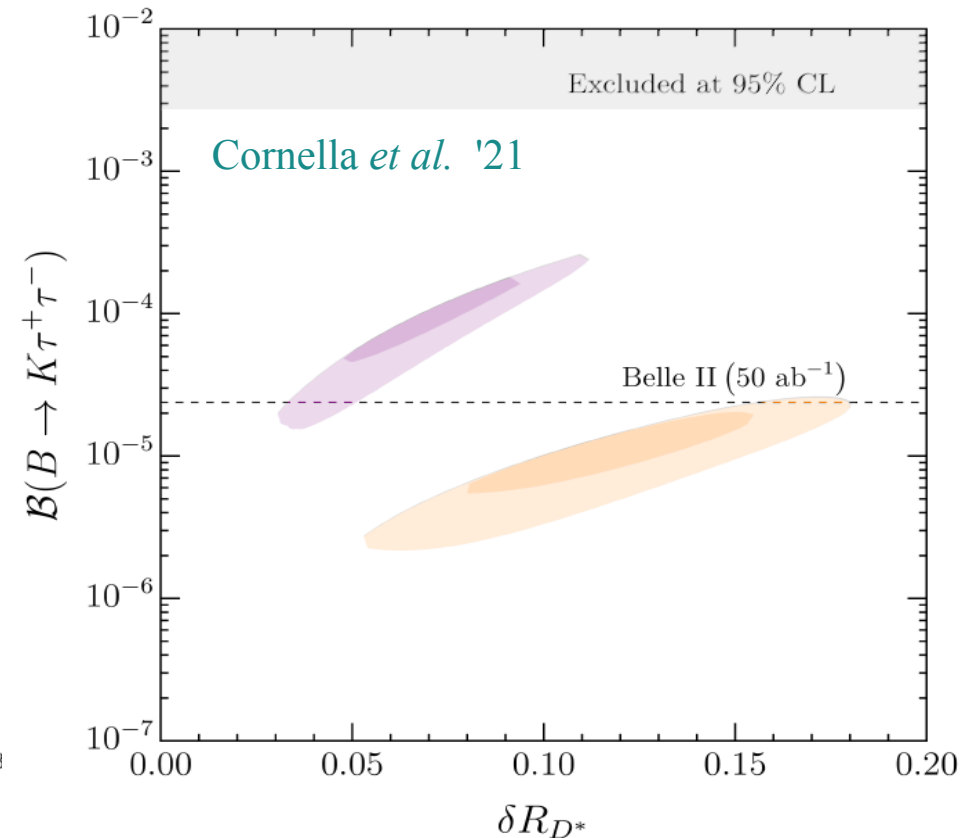
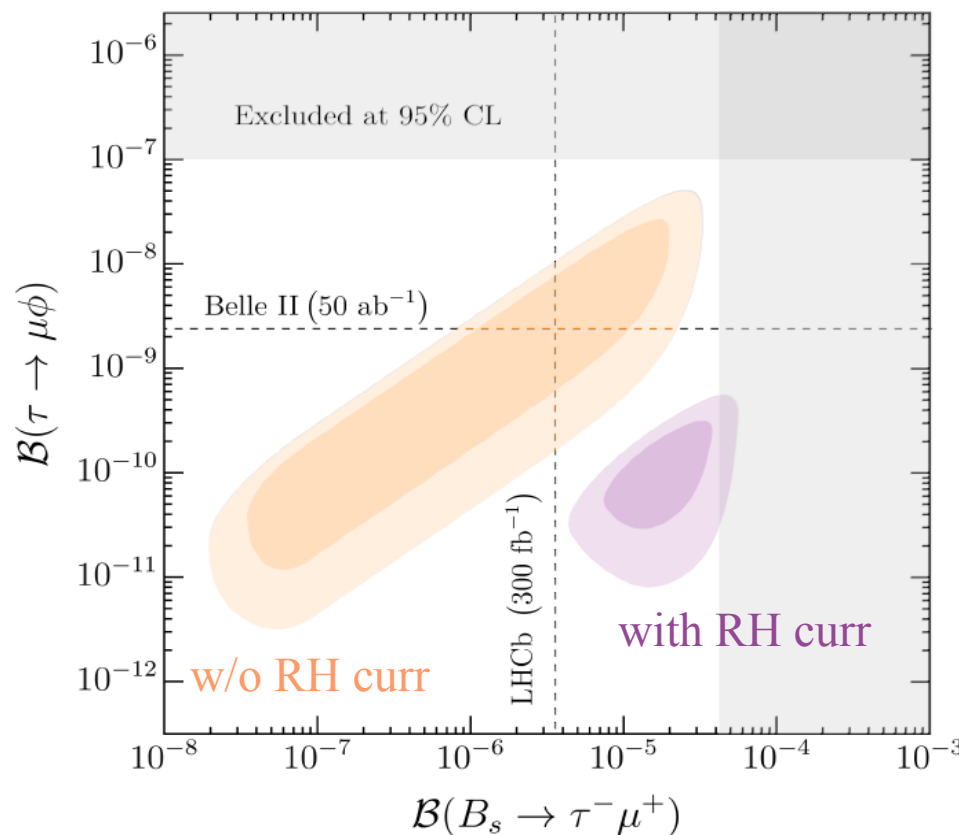


► Model-building considerations

Considering the U_1 only

$$\mathcal{L} \supset \frac{g_U}{\sqrt{2}} U_1^\mu \left[\beta_{i\alpha}^L (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) - \beta_{i\alpha}^R (\bar{d}_R^i \gamma_\mu e_R^\alpha) \right] + \text{h.c.}$$

- excellent description of all available low-energy data
- consistent with present high-energy data → *signals within the reach of HL-LHC*
- *interesting implications also for future low-energy searches:*



Speculations on UV completions



► Speculations on UV completions

First observation: the Pati & Salam group, proposed in the 70's to unify quarks & leptons predicts the only massive LQ that is a good mediator for both anomalies:

Pati-Salam group: $SU(4) \times SU(2)_L \times SU(2)_R$

Fermions in $SU(4)$:

$$\begin{bmatrix} Q_L^\alpha \\ Q_L^\beta \\ Q_L^\gamma \\ L_L \end{bmatrix} \quad \begin{bmatrix} Q_R^\alpha \\ Q_R^\beta \\ Q_R^\gamma \\ L_R \end{bmatrix}$$

Main Pati-Salam idea:
Lepton number as “the 4th color”

The massive LQ [U_1] arise from the breaking $SU(4) \rightarrow SU(3)_C \times U(1)_{B-L}$

$$SU(4) \sim \left[\begin{array}{c|c} SU(3)_C & 0 \\ \hline 0 & 0 \end{array} \right] \quad \left[\begin{array}{c|c} 0 & LQ \\ \hline LQ & \end{array} \right] \quad \left[\begin{array}{c|c} \frac{1}{3} & 0 \\ \hline 0 & -1 \end{array} \right]$$

► Speculations on UV completions

First observation: the Pati & Salam group, proposed in the 70's to unify quarks & leptons predicts the only massive LQ that is a good mediator for both anomalies:

Pati-Salam group: $SU(4) \times SU(2)_L \times SU(2)_R$

Fermions in $SU(4)$:

$$\begin{bmatrix} Q_L^\alpha \\ Q_L^\beta \\ Q_L^\gamma \\ L_L \end{bmatrix} \quad \begin{bmatrix} Q_R^\alpha \\ Q_R^\beta \\ Q_R^\gamma \\ L_R \end{bmatrix}$$

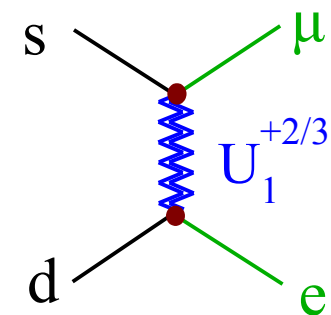
Main Pati-Salam idea:
Lepton number as “the 4th color”

The massive LQ [U_1] arise from the breaking $SU(4) \rightarrow SU(3)_C \times U(1)_{B-L}$

The problem of the “original PS model” are the strong bounds on the LQ couplings to 1st & 2nd generations [e.g. $M > 200 \text{ TeV}$ from $K_L \rightarrow \mu e$]

Attempts to solve this problem simply adding extra fermions or scalars

Calibbi, Crivellin, Li, '17;
Fornal, Gadam, Grinstein, '18
Heeck, Teresi, '18



► Speculations on UV completions

Second observation: we can “protect” the light families charging under SU(4) only the 3rd gen. or, more generally, “separating” the universal SU(3) component

PS group:

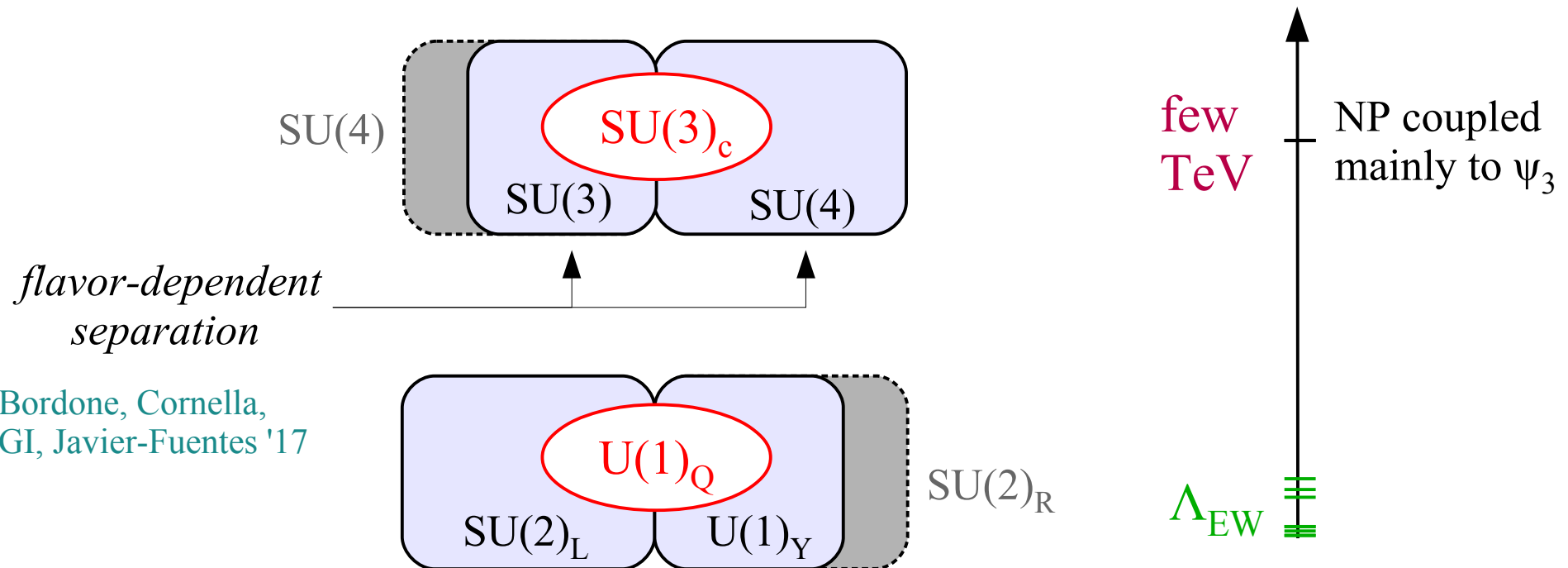
$$SU(4) \times SU(2)_L \times SU(2)_R$$

• *flavor universality*

4321 models:

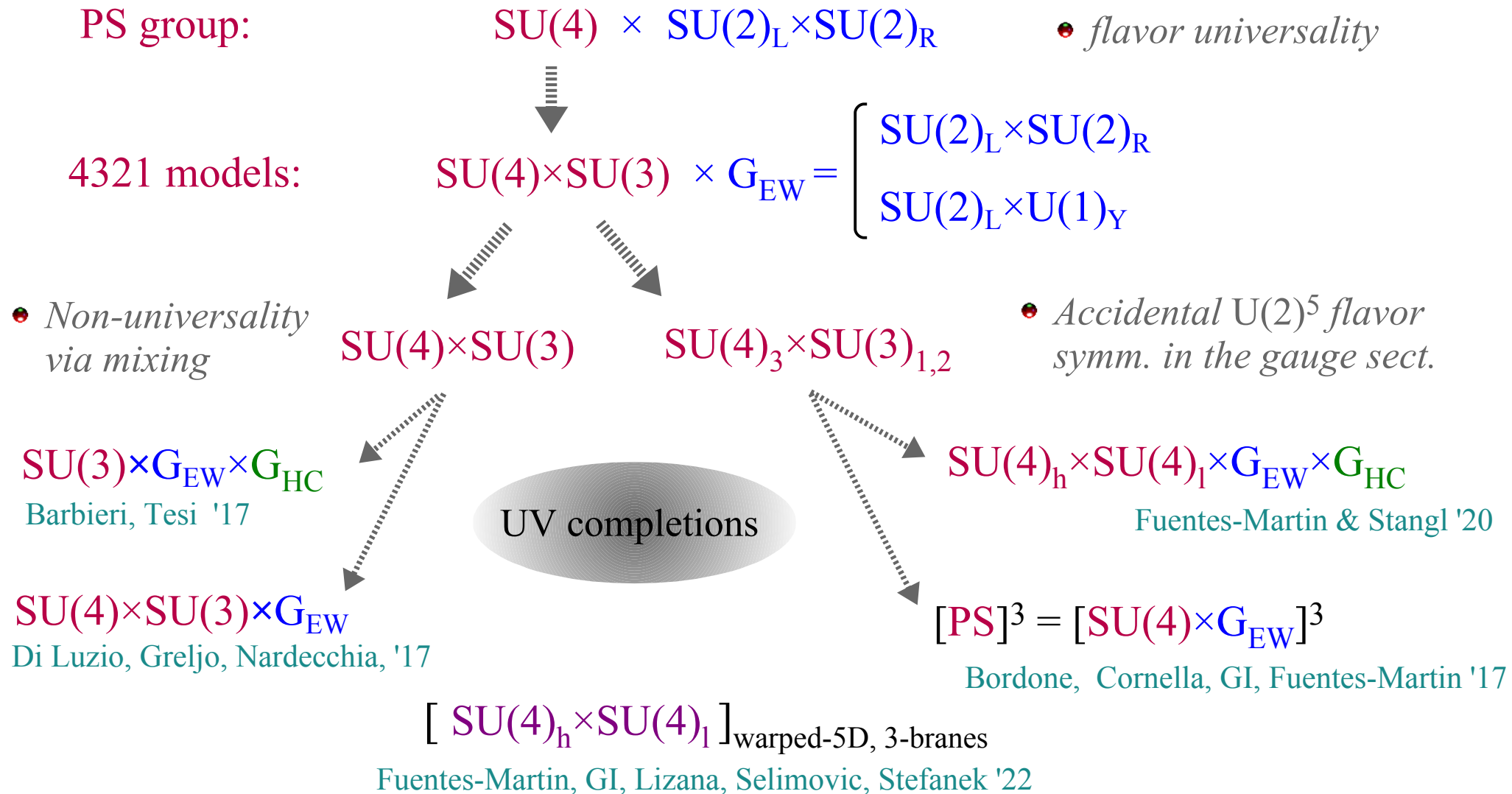
$$SU(4) \times SU(3) \times G_{EW} = \begin{cases} SU(2)_L \times SU(2)_R \\ SU(2)_L \times U(1)_Y \end{cases}$$

Di Luzio, Greljo, Nardecchia, '17



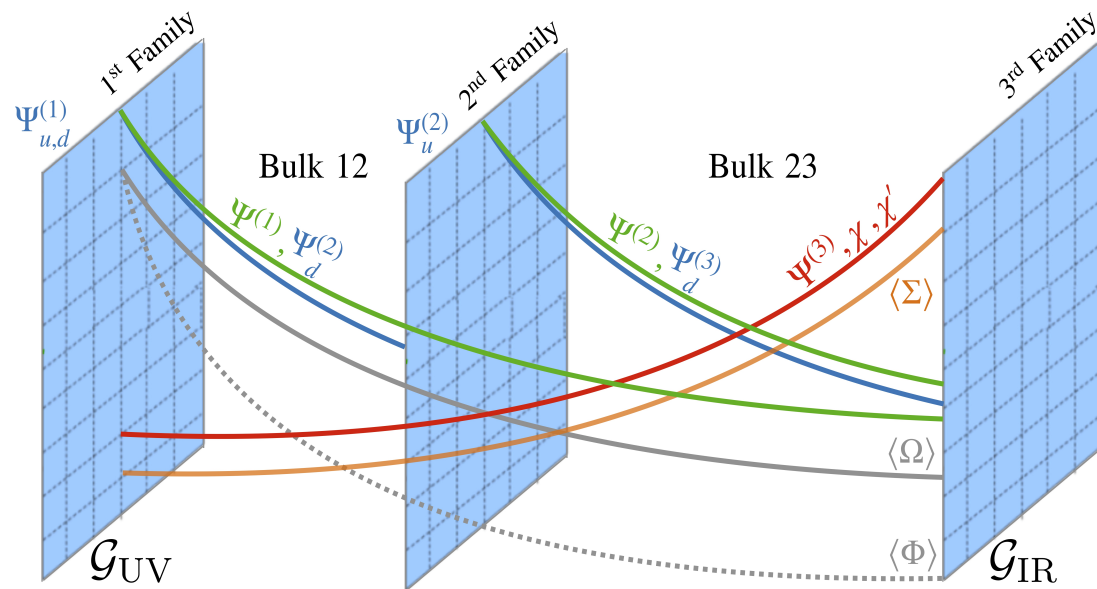
► Speculations on UV completions

Second observation: we can “protect” the light families charging under SU(4) only the 3rd gen. or, more generally, “separating” the universal SU(3) component



► Speculations on UV completions

An ambitious attempt to construct a *full theory of flavor* has been obtained embedding (a variation of the) Pati-Salam gauge group into an extra-dimensional construction:



Flavor \leftrightarrow special position
(*topological defect*) in an extra
(compact) space-like dimension

Dvali & Shifman, '00

Higgs and SU(4)-breaking fields
with oppositely-peaked profiles,
leading to the desired flavor
pattern for masses & anomalies

Bordone, Cornella, GI, Javier-Fuentes '17

★ Anarchic neutrino masses via inverse see-saw mechanism

Fuentes-Martin, GI, Pages, Stefaneke '22

★ “Holographic” (pNGB) Higgs from appropriate choice of bulk/brane gauge symm.

$$[G_{\text{bulk-23}} = \text{SU}(4)_3 \times \text{SU}(3)_{1,2} \times \text{U}(1) \times \text{SO}(5) \quad G_{\text{IR}} = \text{SU}(3)_c \times \text{U}(1)_{\text{B-L}} \times \text{SO}(4)]$$

Fuentes-Martin, Stangl '20

Fuentes-Martin, GI, Lizana, Selimovic, Stefaneke '22

► Speculations on UV completions

In most *PS-extended models* collider and low-energy pheno are controlled by the effective 4321 gauge group that rules TeV-scale dynamics

Despite the apparent complexity, the construction is highly constrained

Renormalizable structure achieved with vector-like fermions

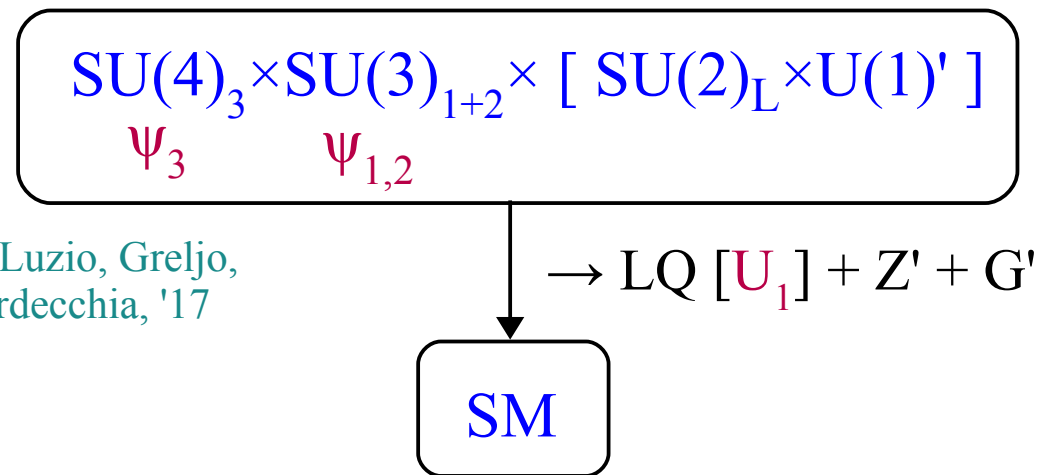
Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$
q_L^i	1	3	2	1/6
u_R^i	1	3	1	2/3
d_R^i	1	3	1	-1/3
ℓ_L^i	1	1	2	-1/2
e_R^i	1	1	1	-1
ψ_L'	4	1	2	0
ψ_u'	4	1	1	1/2
ψ_d'	4	1	1	-1/2
χ_L^i	4	1	2	0
χ_R^i	4	1	2	0
H_1	1	1	2	1/2
H_{15}	15	1	2	1/2
Ω_1	$\bar{4}$	1	1	-1/2
Ω_3	$\bar{4}$	3	1	1/6
Ω_{15}	15	1	1	0



- Positive features the EFT reproduced
- Calculability of $\Delta F=2$ processes
- Precise predictions for high-pT data

consistent with present data

Di Luzio, Greljo, Nardecchia, '17



► Speculations on UV completions

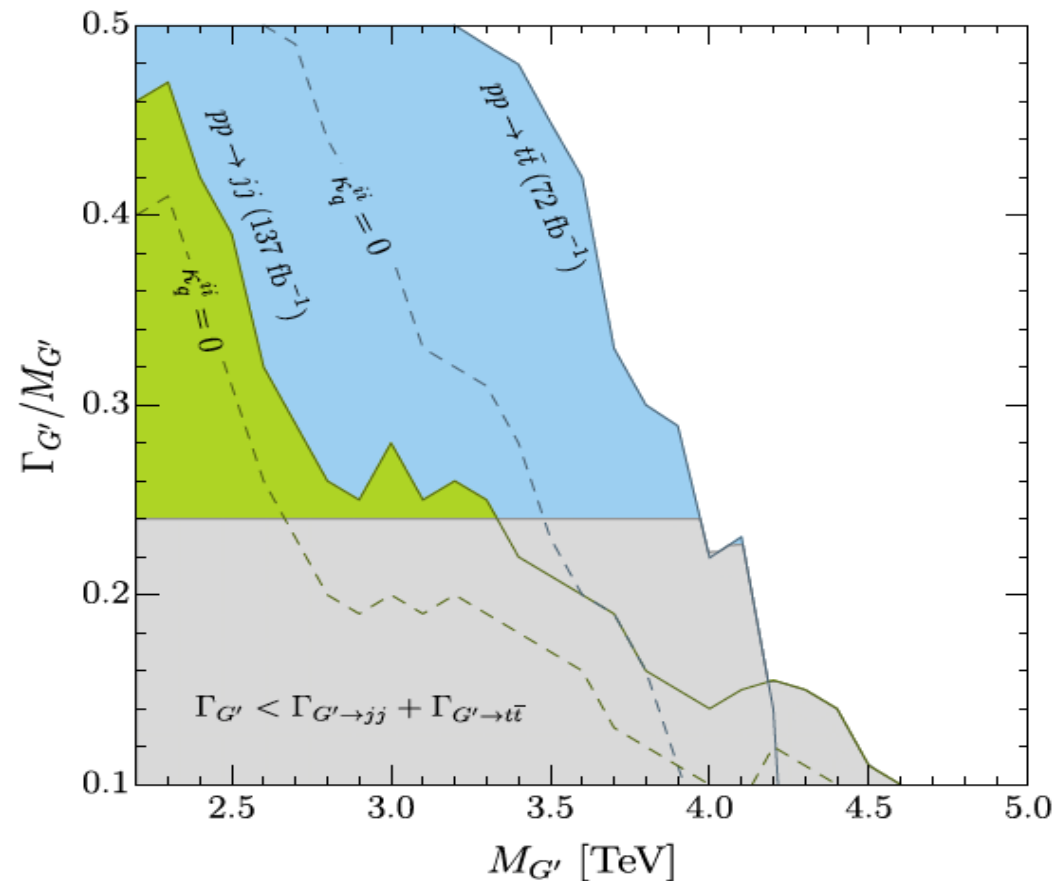
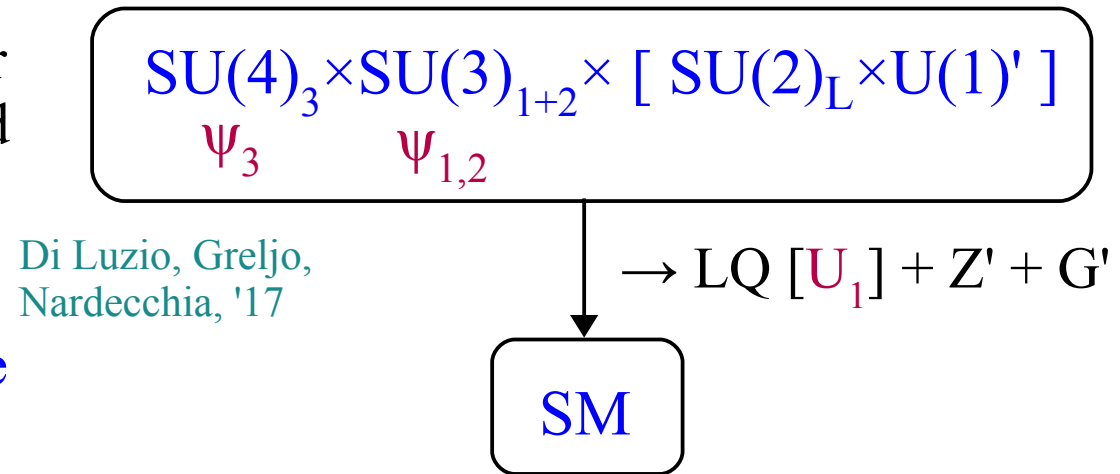
In most *PS-extended models* collider and low-energy pheno are controlled by the effective 4321 gauge group that rules TeV-scale dynamics

Despite the apparent complexity, the construction is highly constrained

New striking collider signature:

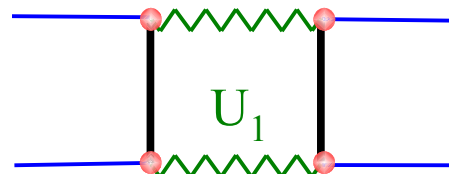
G' (“*coloron*”) = heavy color octet, coupled mainly to 3rd generation quarks

→ strongest constraint on the scale of the model from $pp \rightarrow t \bar{t}$

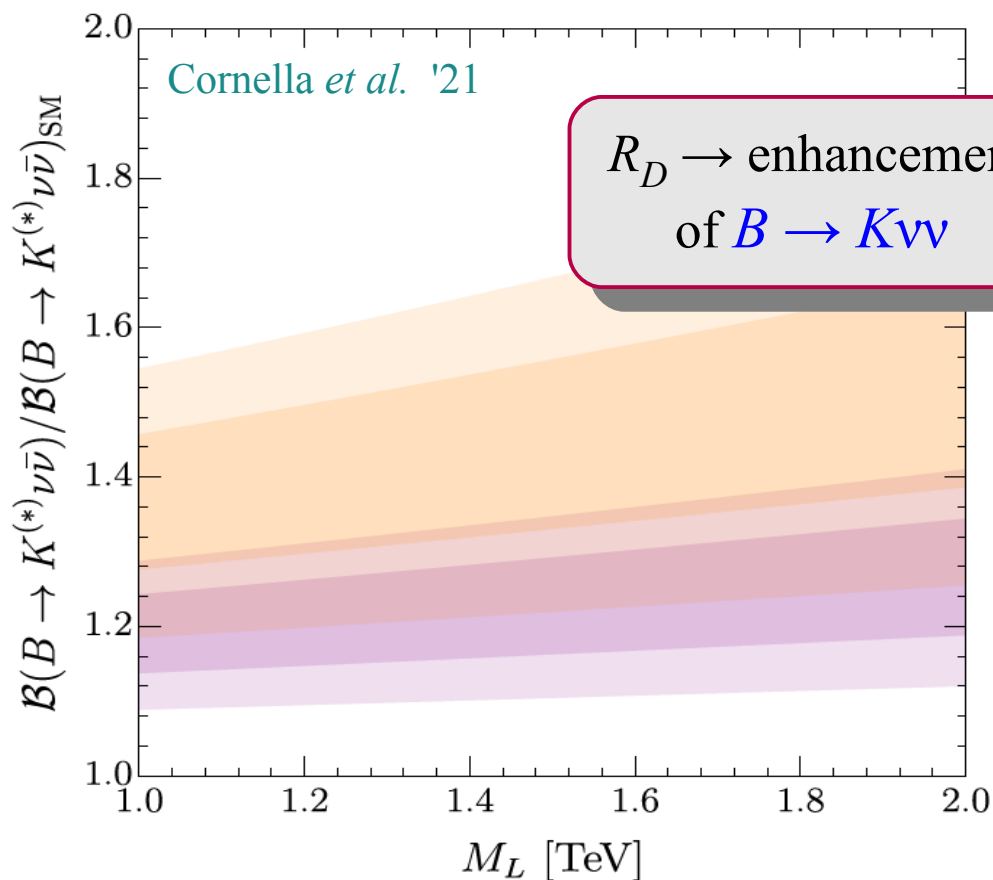


► Speculations on UV completions

UV-sensitive observables in
4321 models

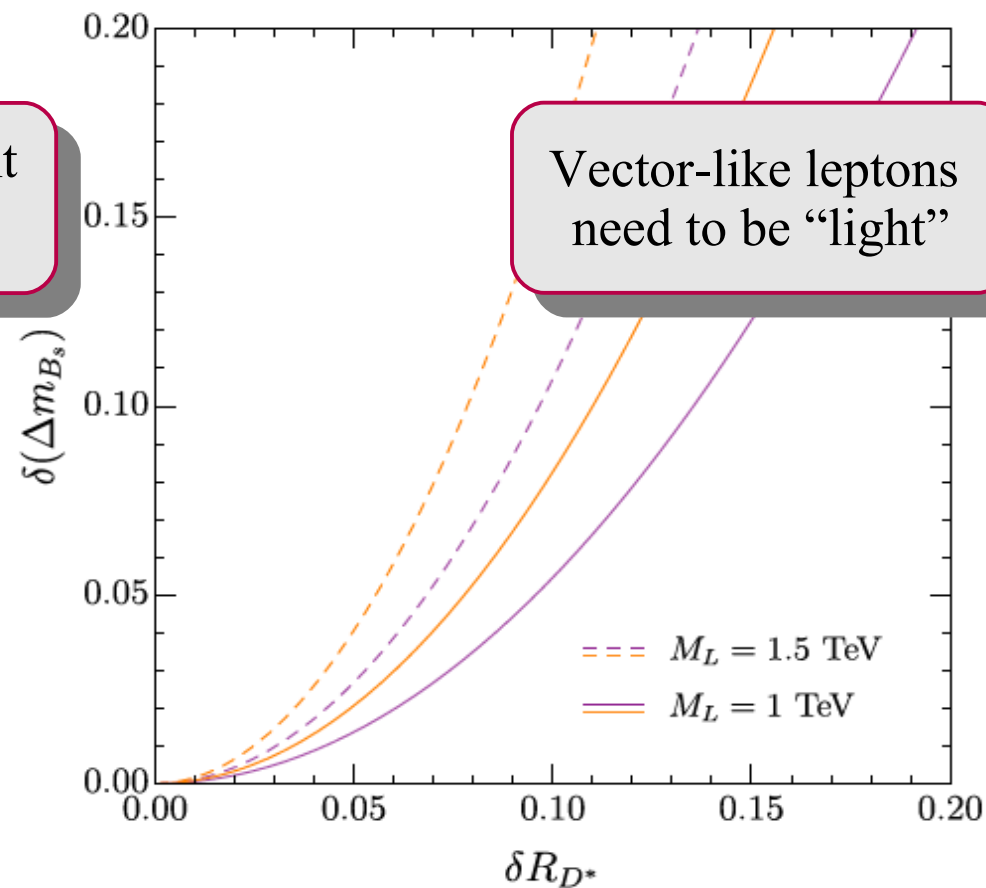


A) $B \rightarrow K \nu \bar{\nu}$



Fuentes-Martin, GI, König, Selimovic, '20

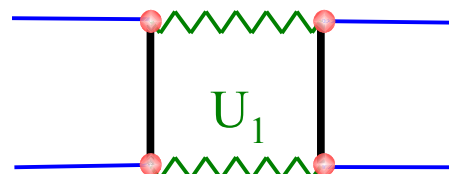
B) B_s mixing [$\Delta F=2$]



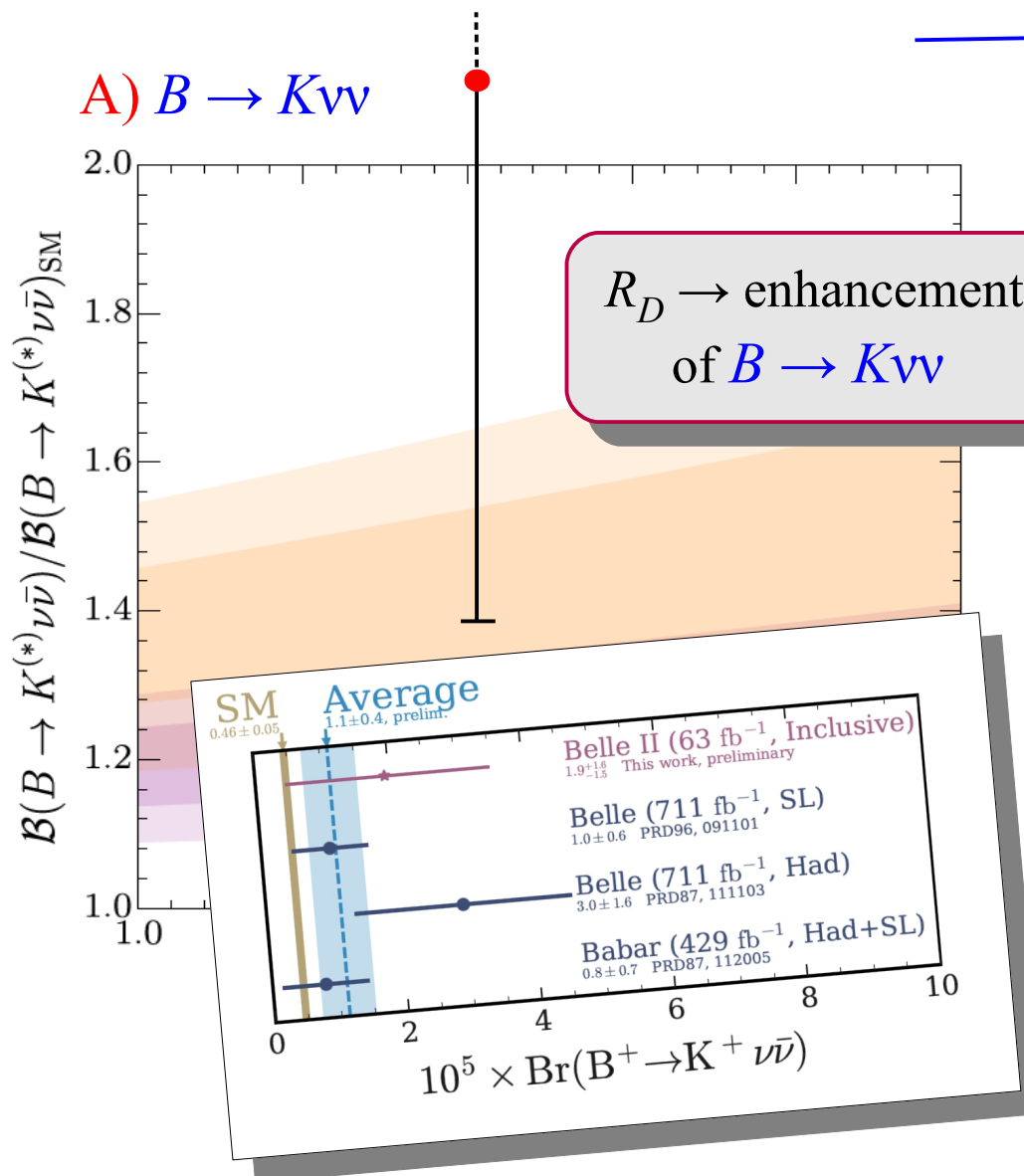
Di Luzio, Fuentes-Martin, Greljo,
Narddecchia, Renner '18

► Speculations on UV completions

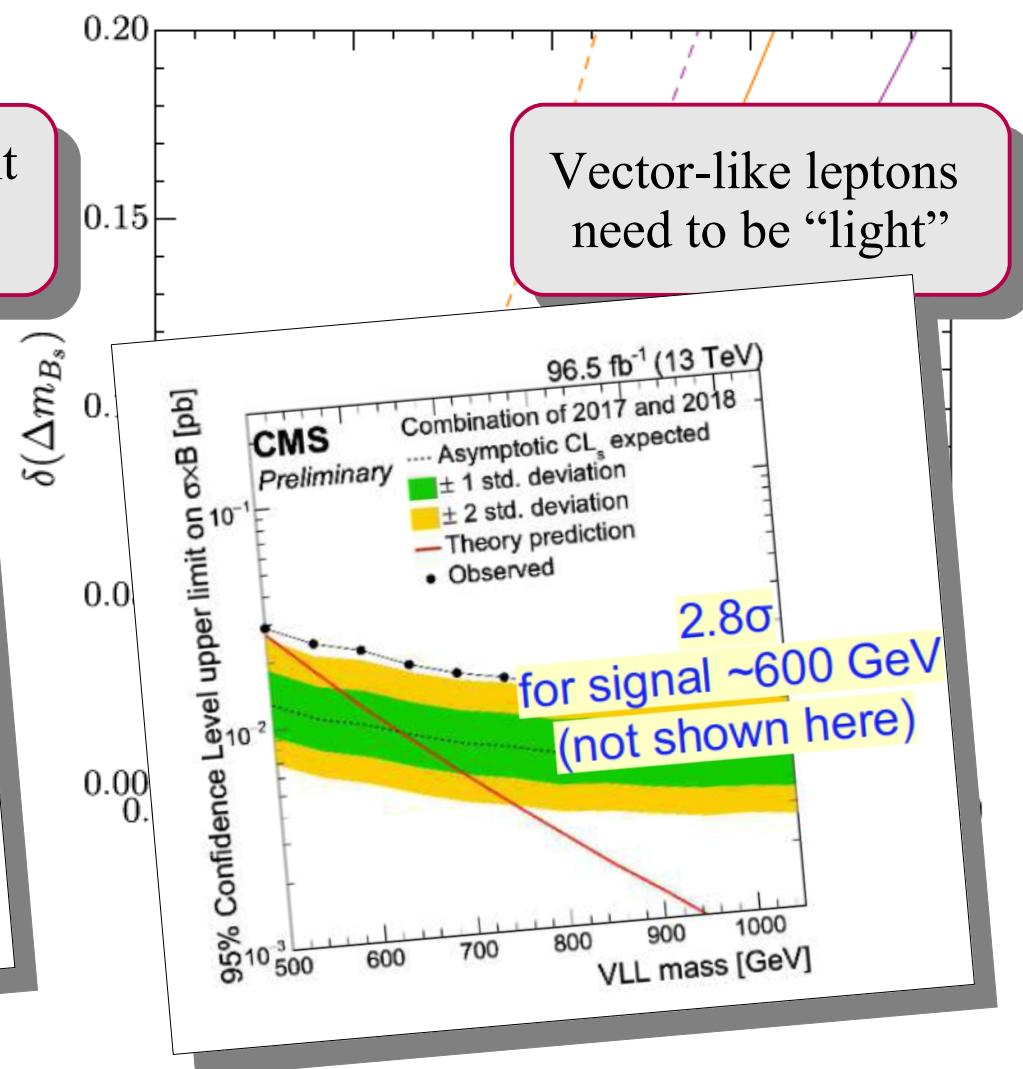
UV-sensitive observables in
4321 models



A) $B \rightarrow K \nu \bar{\nu}$



B) B_s mixing [$\Delta F=2$]



Conclusions

- Flavor is an essential ingredient to understand the structure of the SMEFT. This statement, which we deduce already by the SM Yukawa structure, is reinforced by the recent anomalies in B physics
- The **statistical significance** of the LFU anomalies **is growing**: in the $b \rightarrow s ll$ system, the chance this is a pure statistical fluctuation is marginal.
- If combined, the two sets of anomalies point to non-trivial flavor dynamics around the TeV scale, involving mainly the 3rd family \rightarrow **connection to the origin of flavor** [multi-scale picture at the origin of flavor hierarchies]
- No contradiction with existing low- & high-energy data, but new non-standard effects should emerge soon in both these areas



Very interesting (near-by!) future...
(both on the exp., the pheno,
and the model-building point of view)