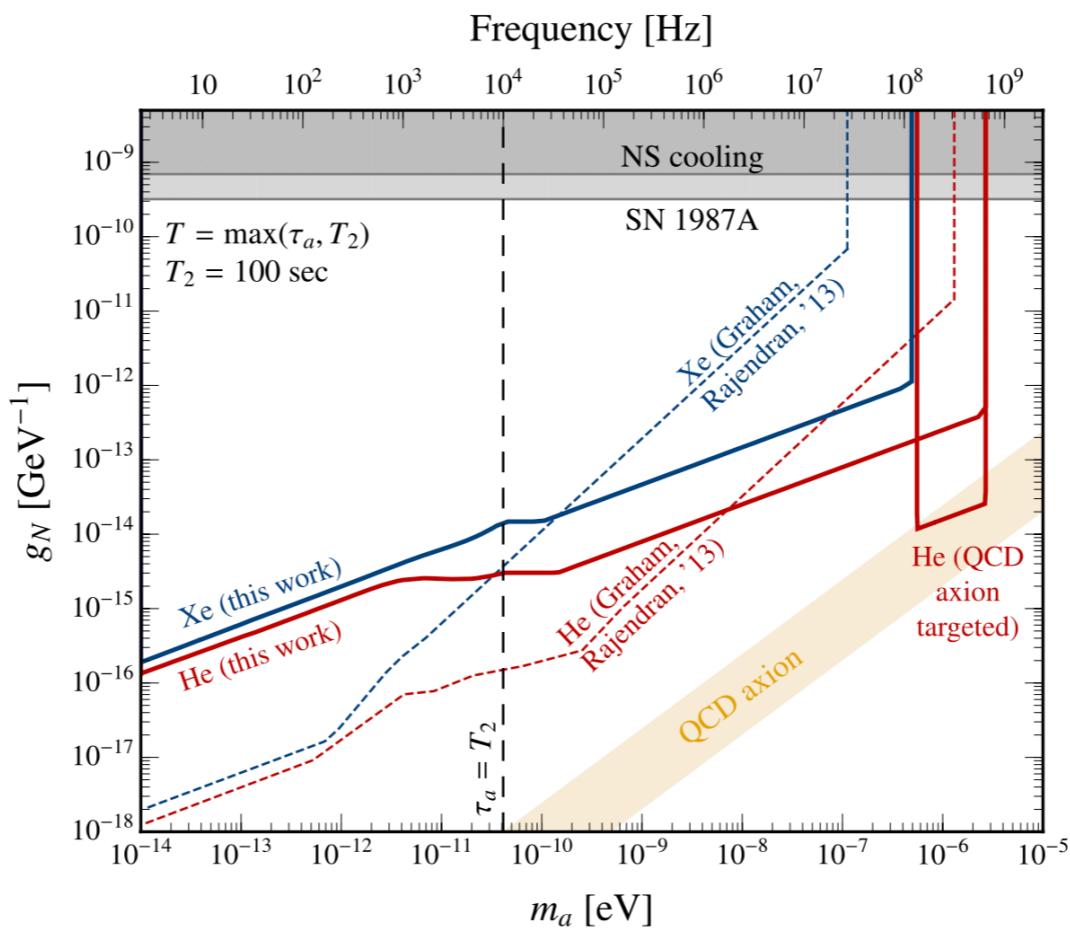


[PRL 2022] w/ Kevin Langhoff, Nadav Outmezguine

# The Irreducible Axion





[PRL 2023] w/ Jeff Dror, Stefania Gori, Jacob Leedom

# Bonus: the SH0 and axion haloscopes

---



# Motivation

---

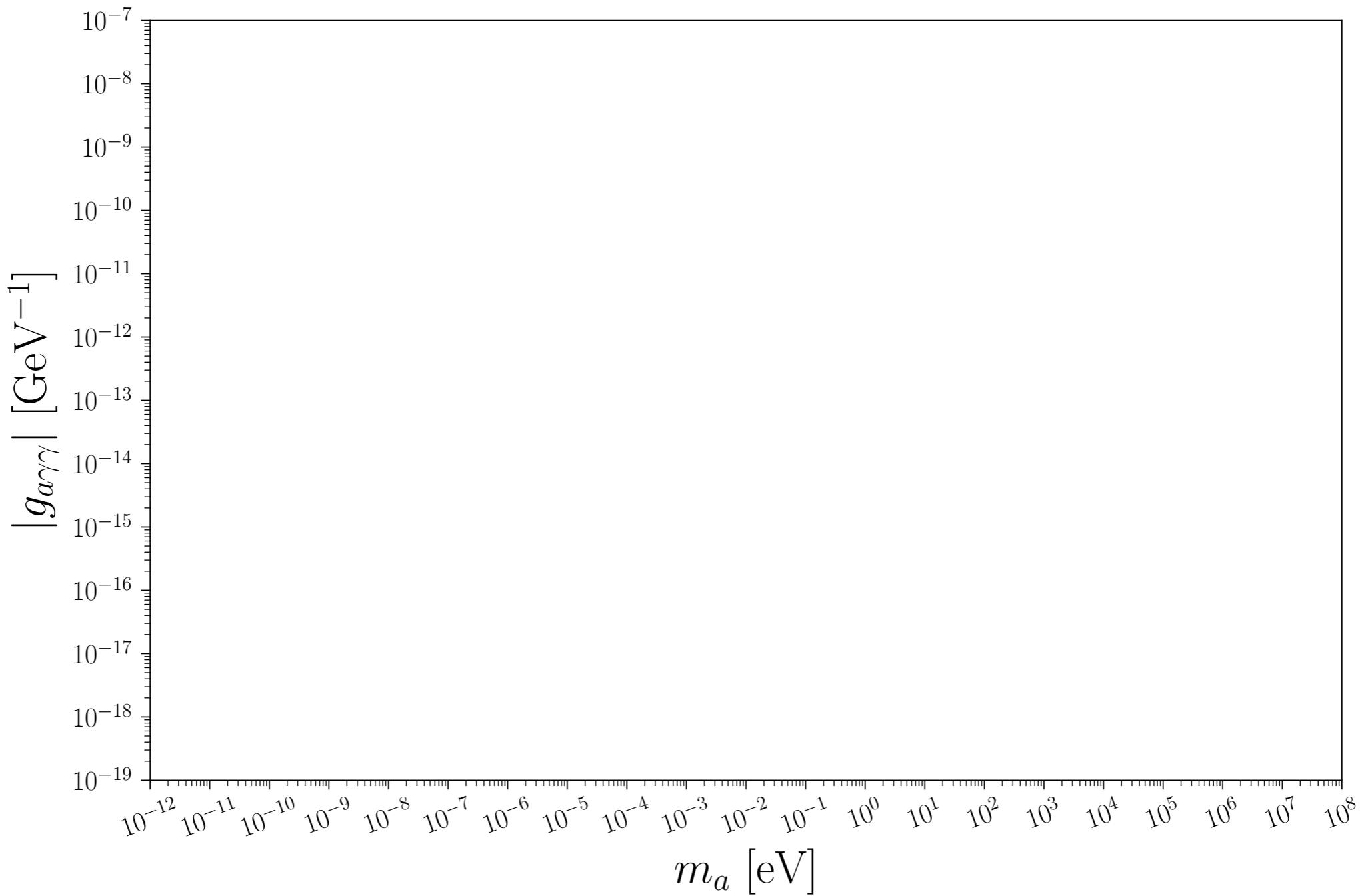
$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$



# Motivation

---

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

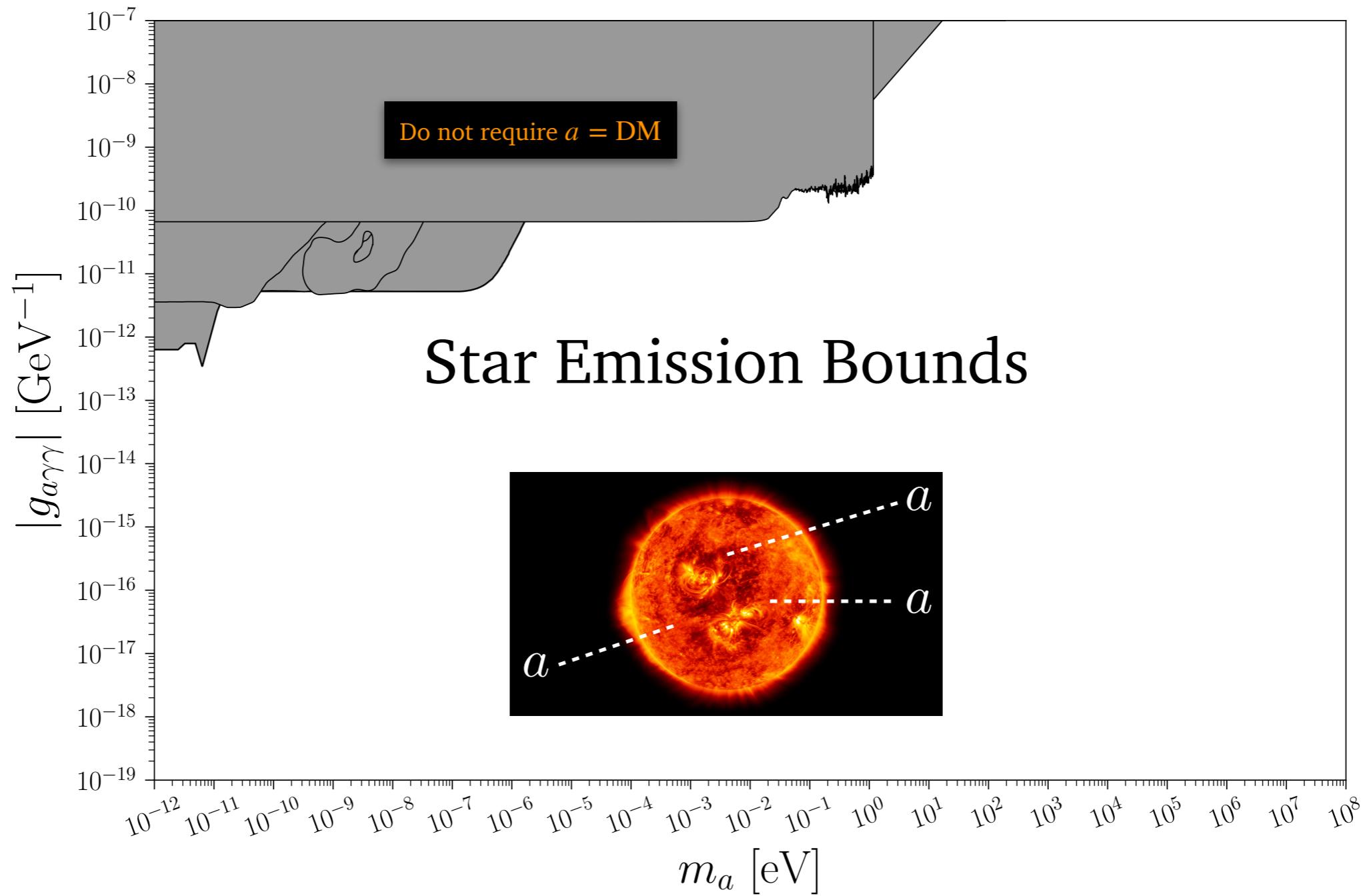


Partial summary  
[O'Hare github]



# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

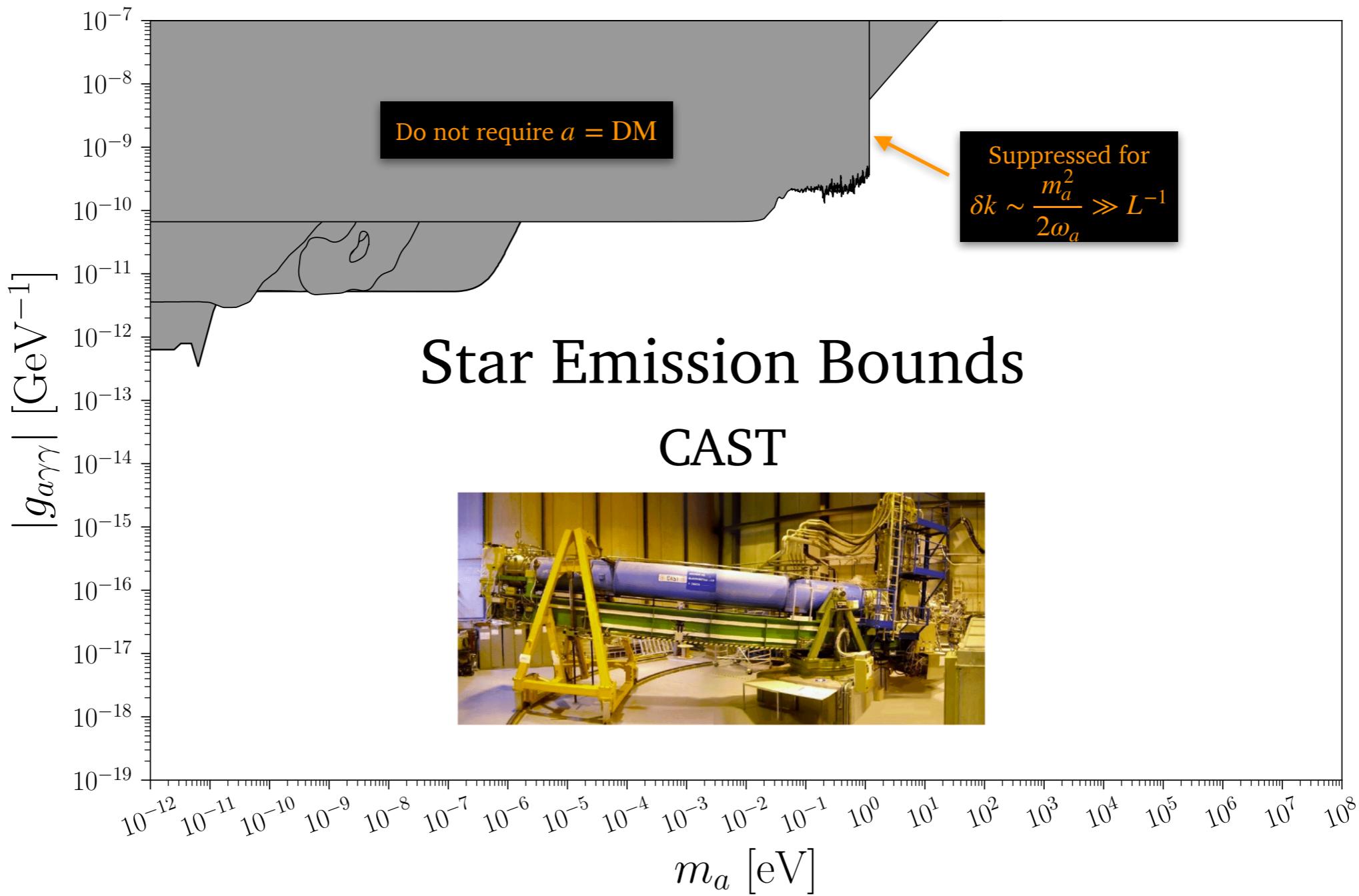


Partial summary  
[O'Hare github]



# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

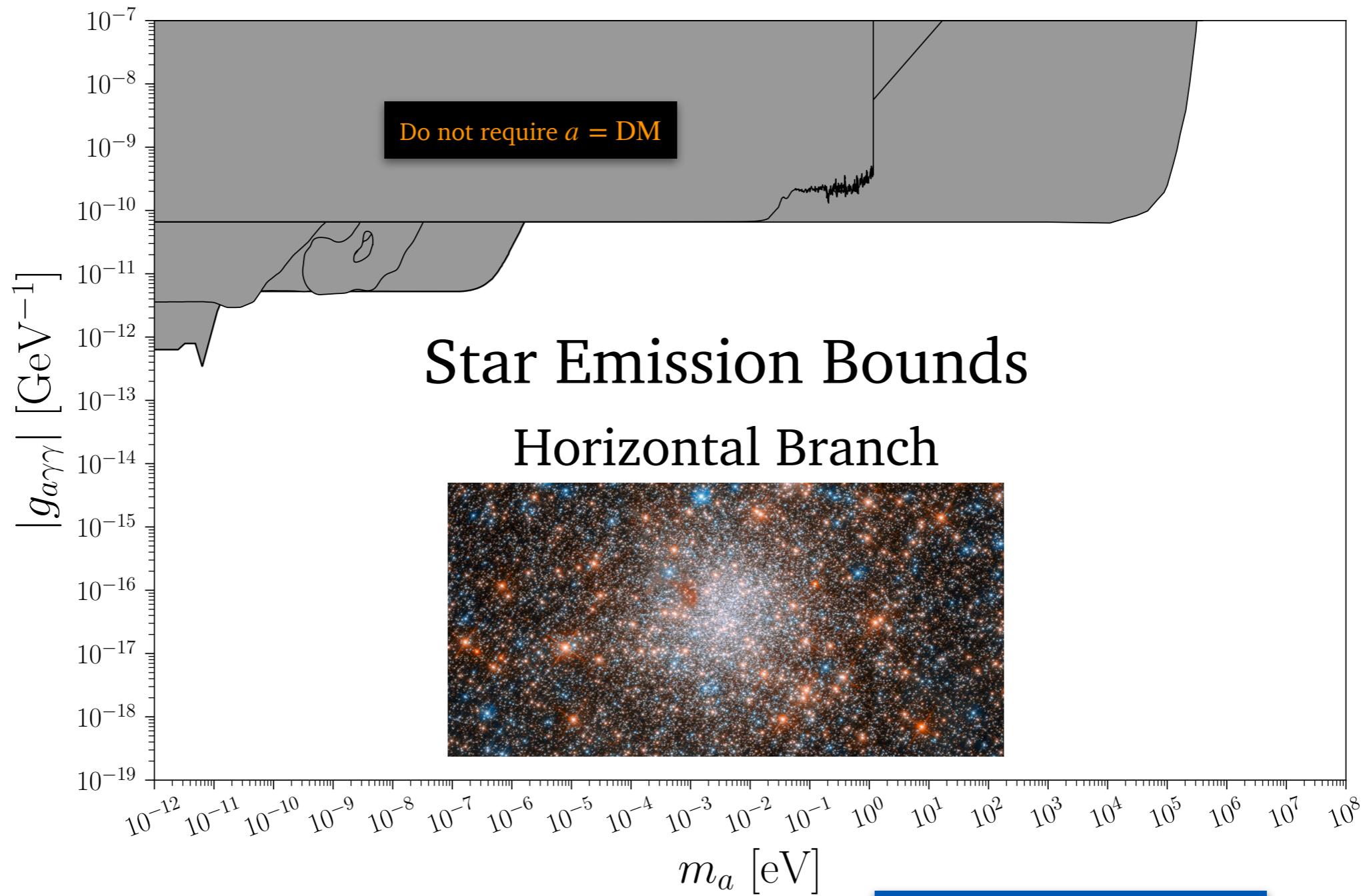


Partial summary  
[O'Hare github]



# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$



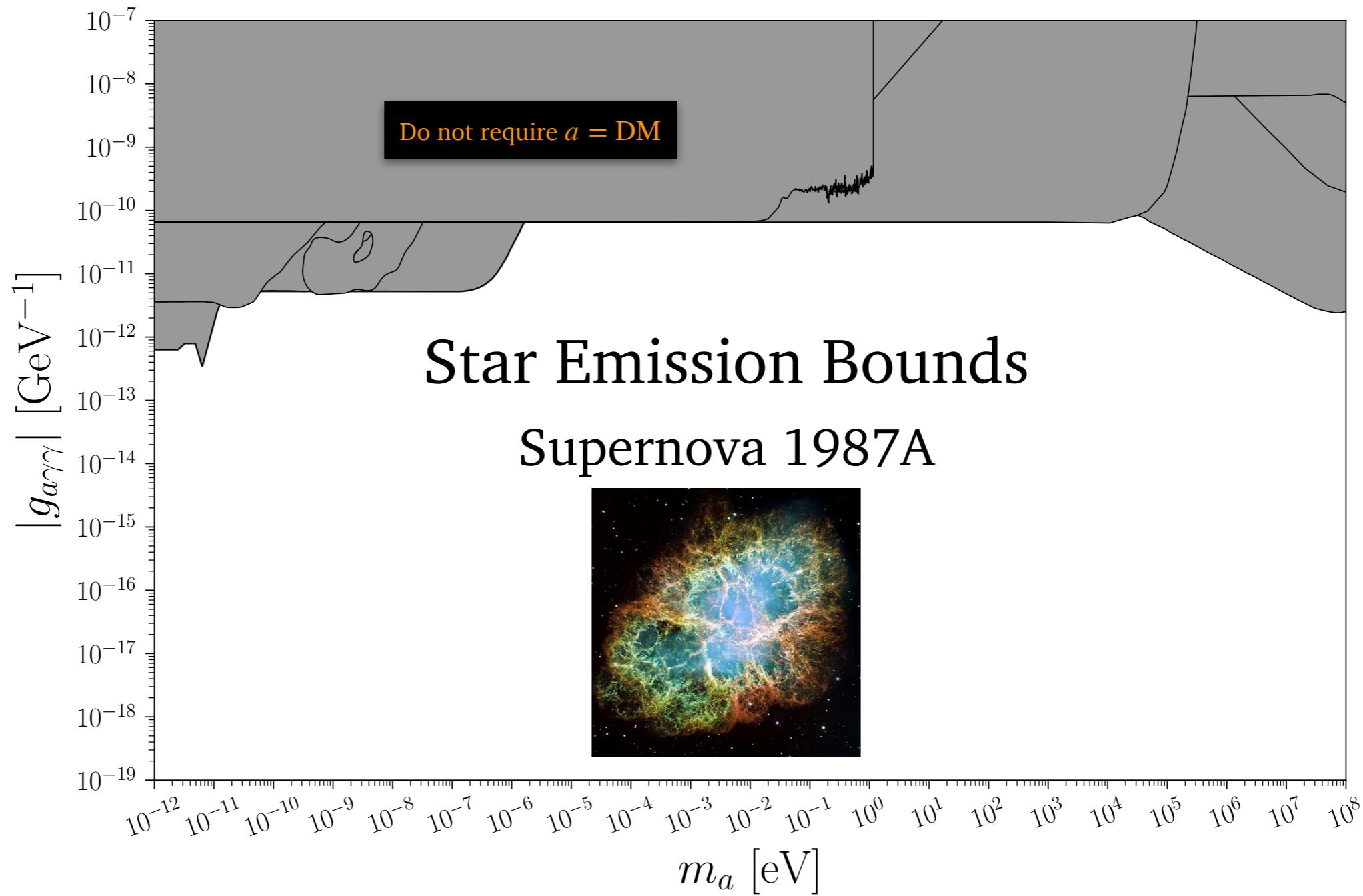
[Ayala+ 2014], [Carenza+ 2020],  
cf. [Dolan+ 2207.03102]

Partial summary  
[O'Hare github]



# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

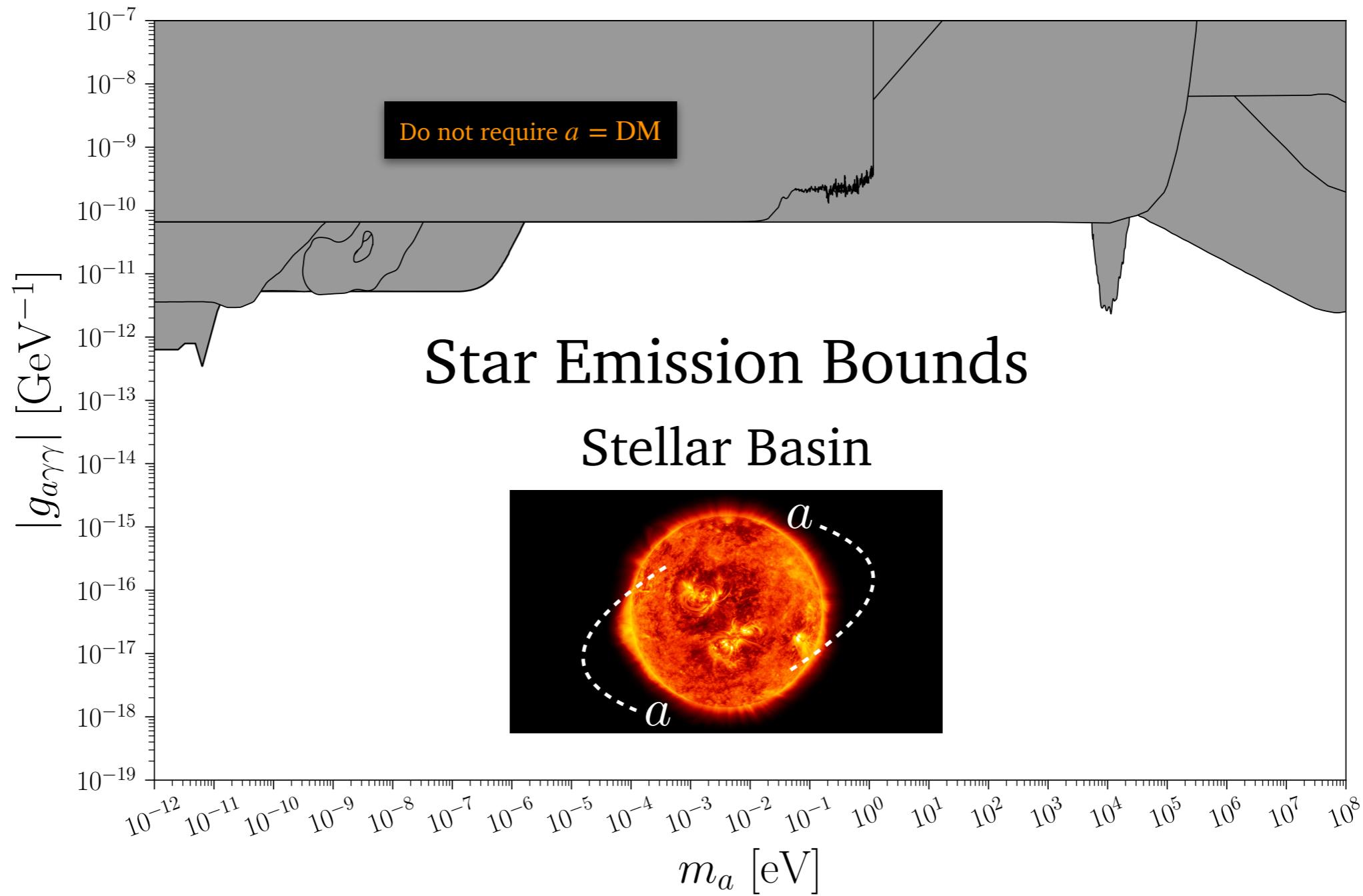


Partial summary  
[O'Hare github]



# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

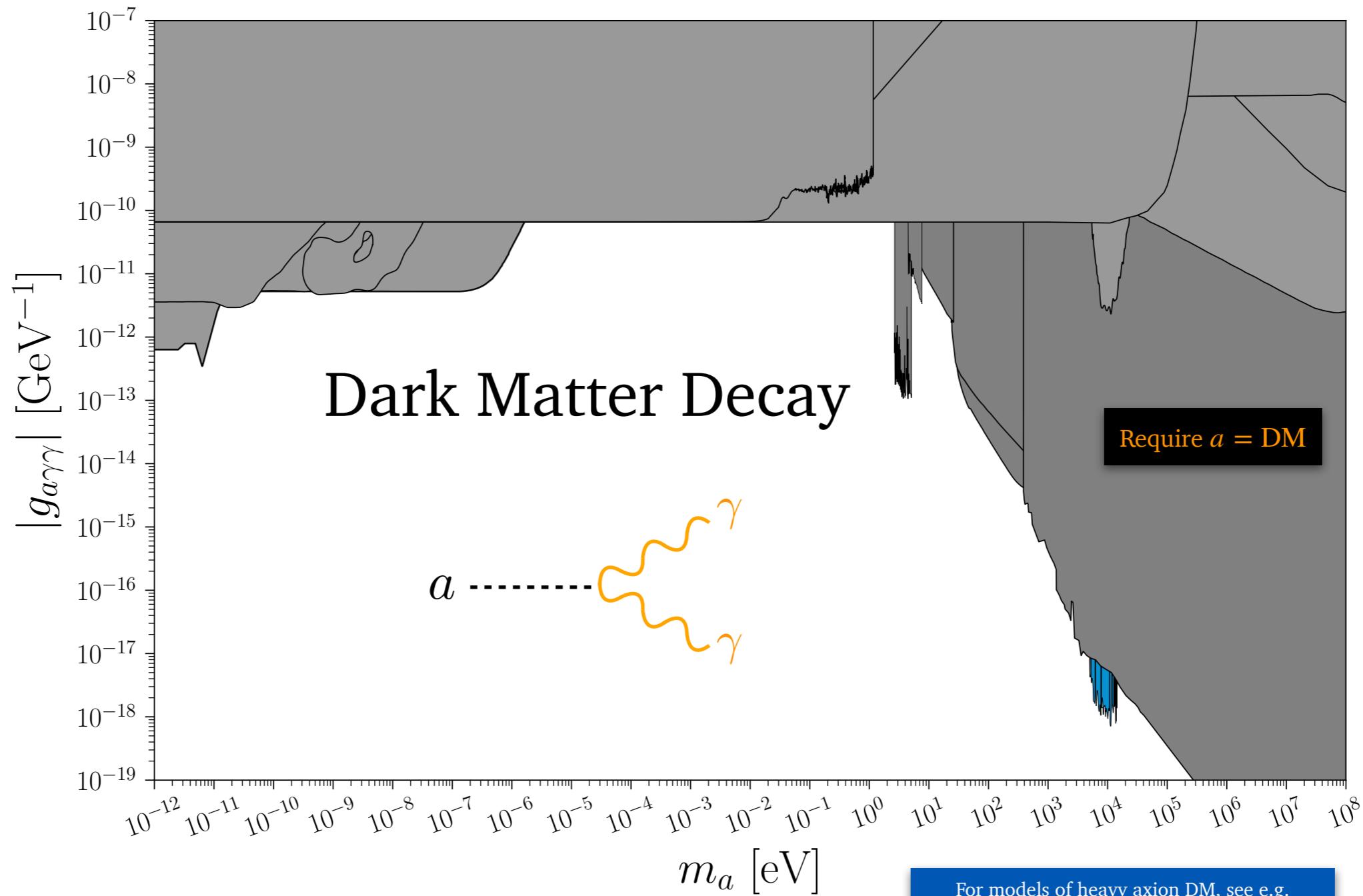


Partial summary  
[O'Hare github]



# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$



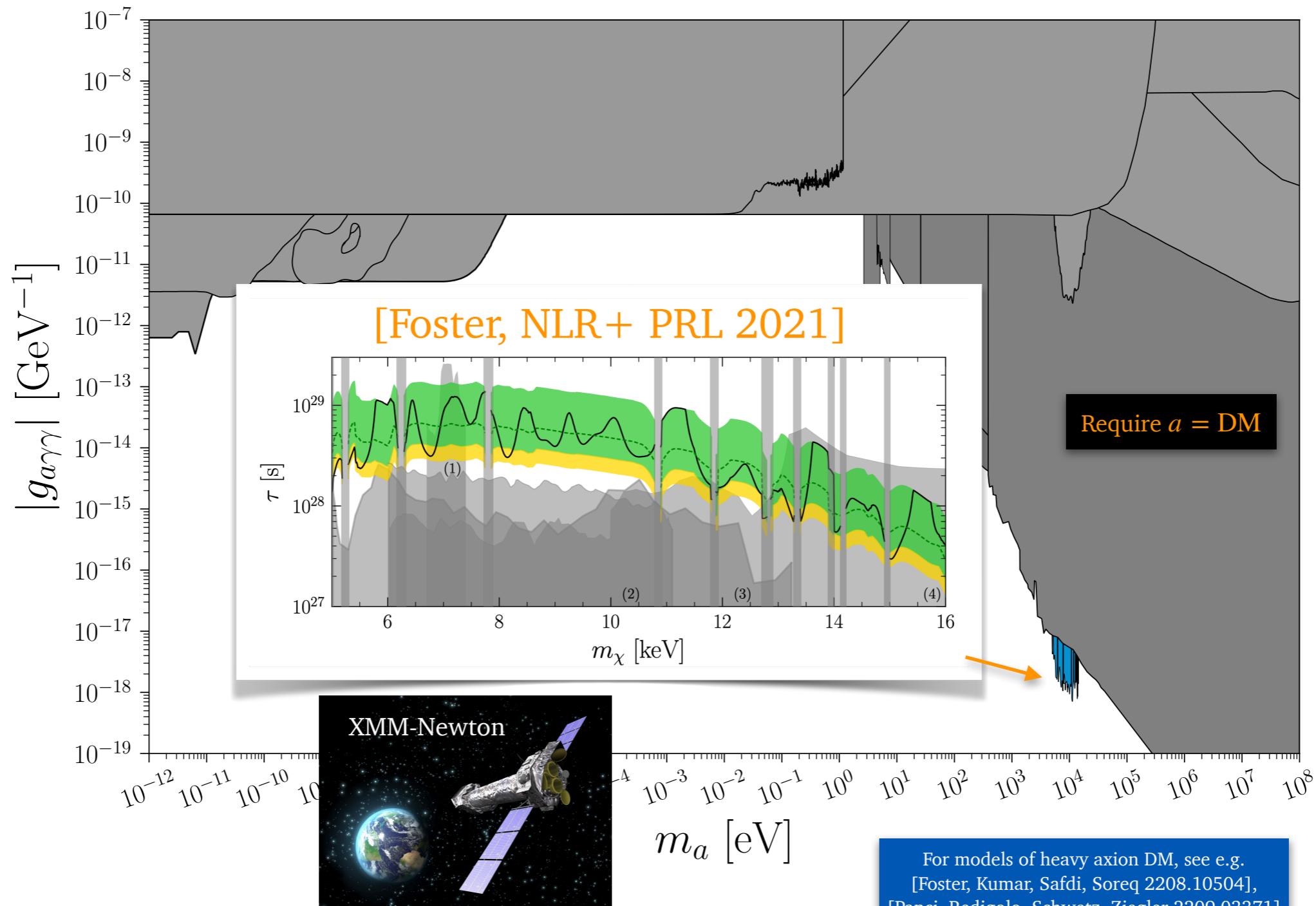
For models of heavy axion DM, see e.g.  
[Foster, Kumar, Safdi, Soreq 2208.10504],  
[Panci, Redigolo, Schwetz, Ziegler 2209.03371]

Partial summary  
[O'Hare github]



# Motivation

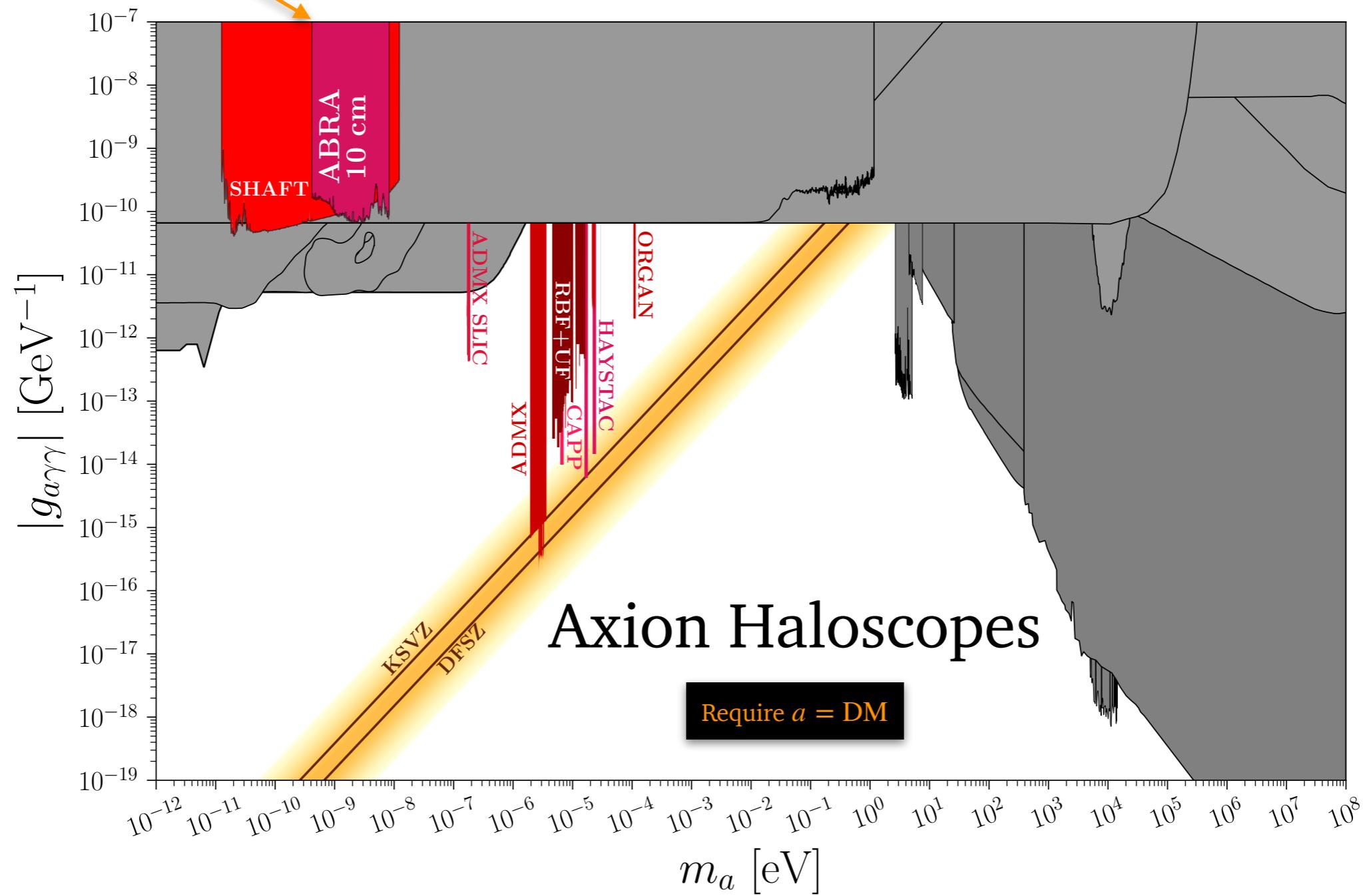
$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$



# Motivation

[Salemi, NLR+ PRL 2021]  
[Gramolin+ Nature Physics 2021]

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

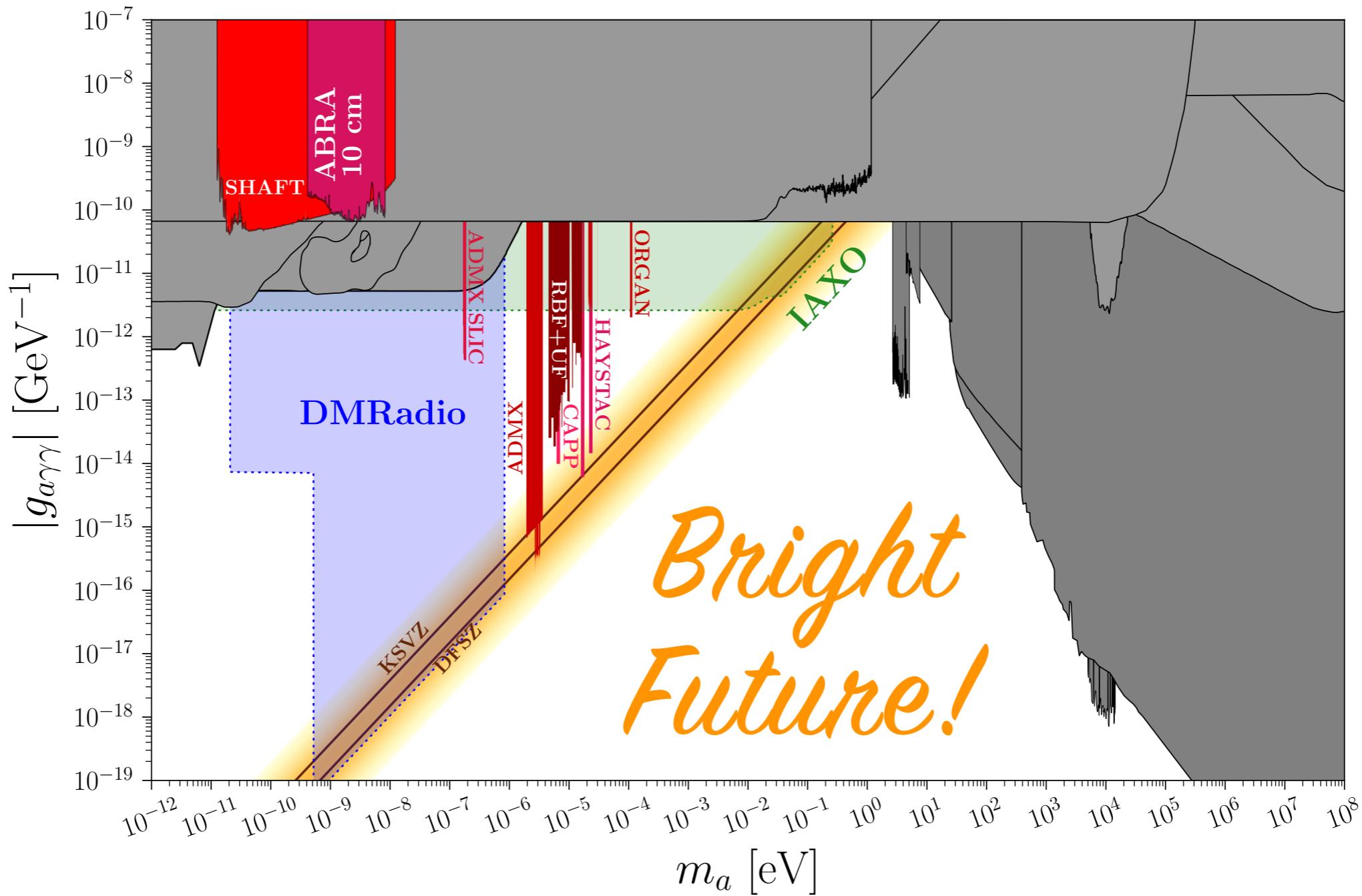


Partial summary  
[O'Hare github]



# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

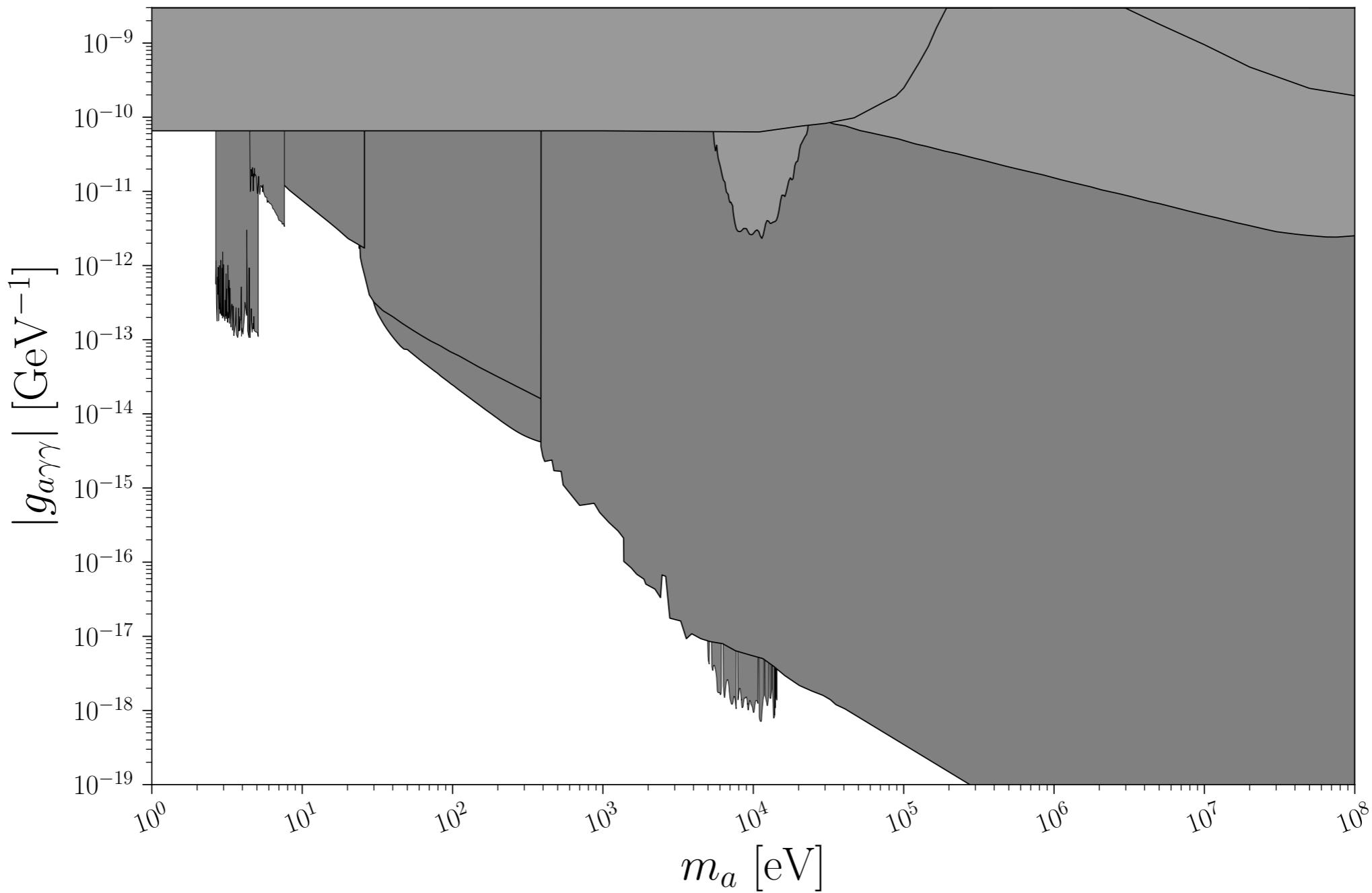


Partial summary  
[O'Hare github]



# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

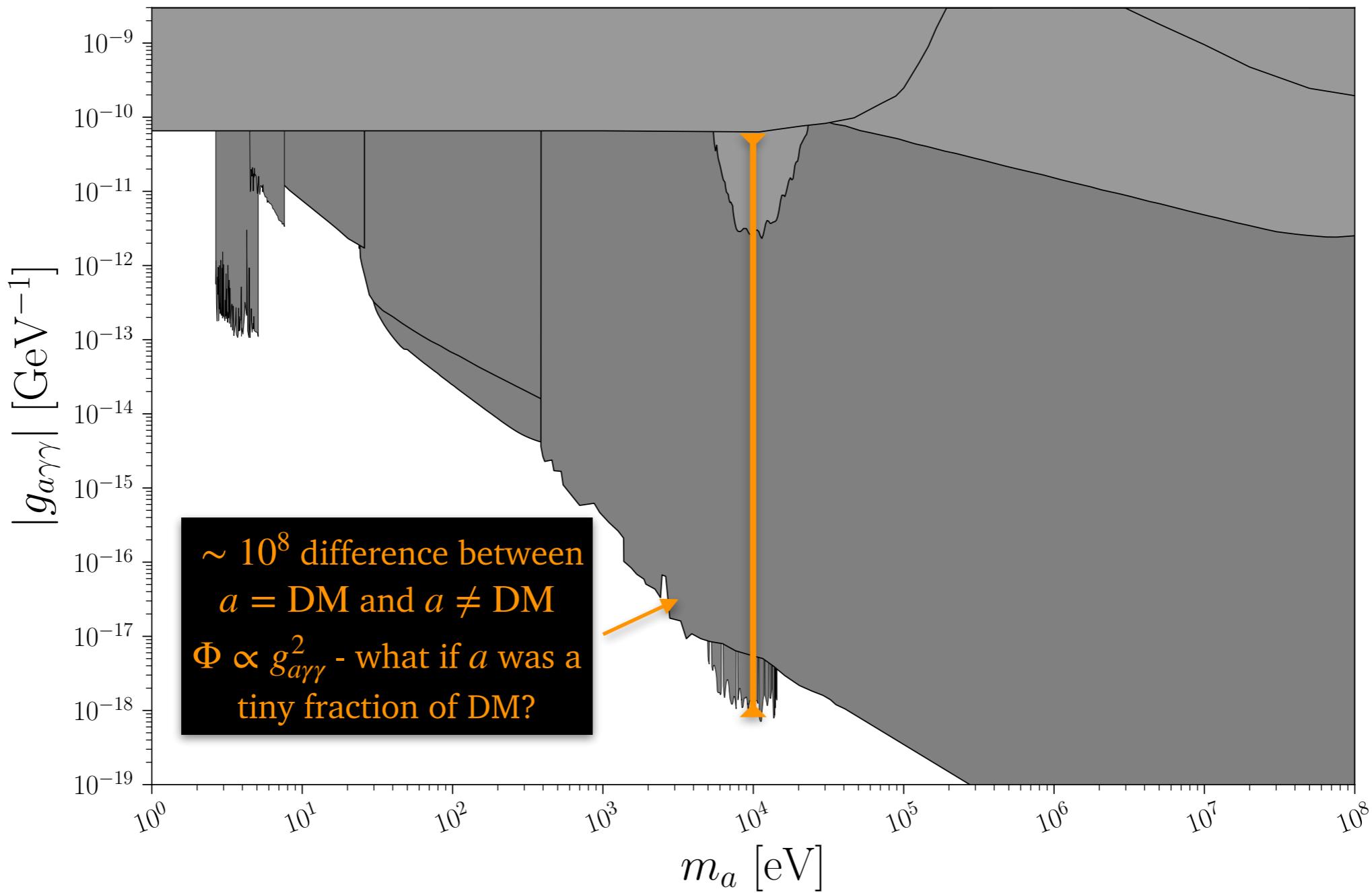


Partial summary  
[O'Hare github]



# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

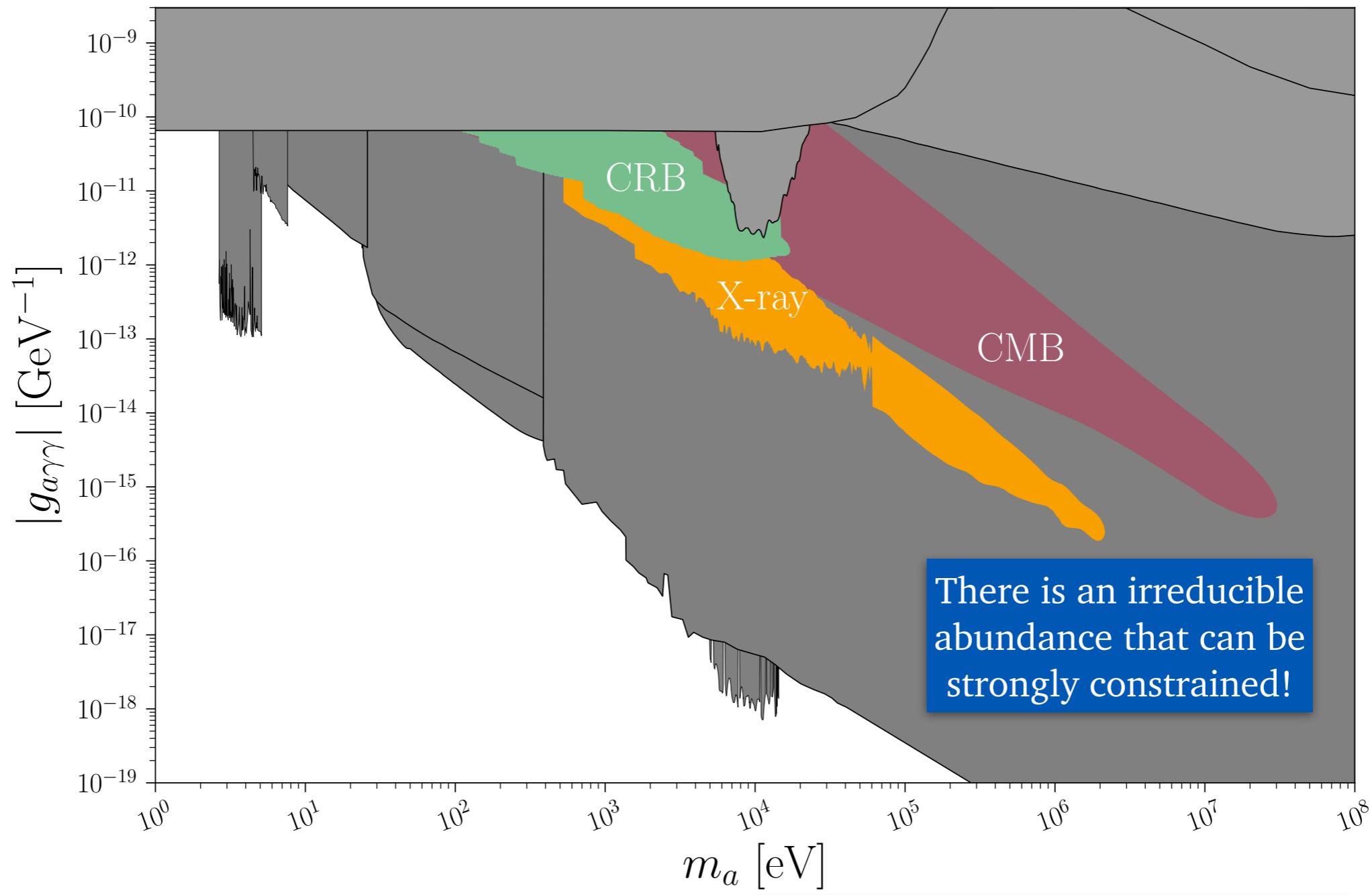


Partial summary  
[O'Hare github]



# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$



Partial summary  
[O'Hare github]



# Outline

---

1. Sensitivity Estimate

2. Abundance

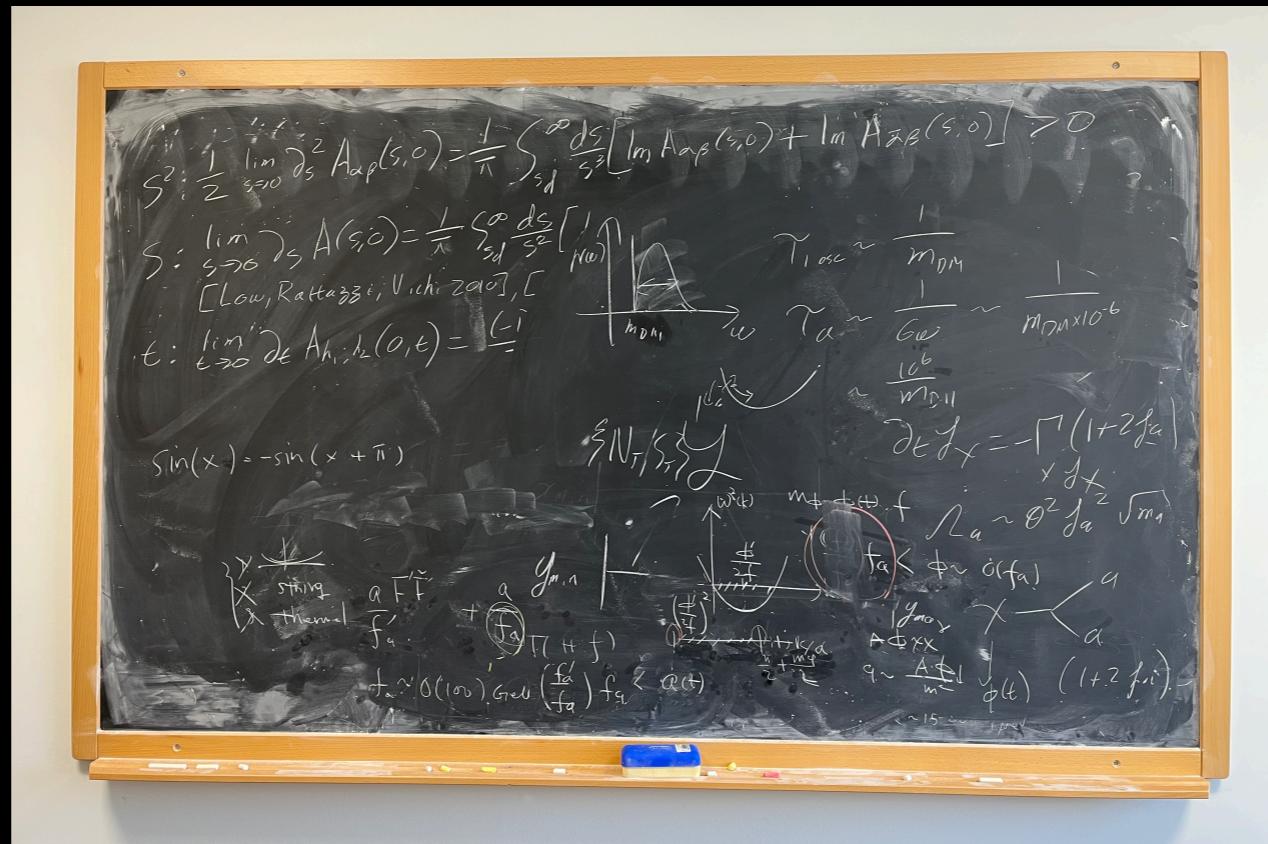
3. Constraints

4. Extensions

(Bonus: a few words on Haloscope Sensitivity)



# Sensitivity Estimate



# Sensitivity Estimate

Take  $m_a = 10$  keV

Early Universe: photon conversion ( $\gamma e \rightarrow ae$ )  
freezes-in axions

$$\mathcal{F}_a \simeq 10^{-4} \left( \frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{HB}}} \right)^2 \left( \frac{T_{\text{RH}}}{5 \text{ MeV}} \right) \quad (1)$$

$= \rho_a / \rho_{\text{DM}}$

UV dominated



# Sensitivity Estimate

---

X-ray constraints at  $\sim 10$  keV require

$$\tau_{\text{DM}} \gtrsim 10^{29} \text{ s} \Rightarrow g_{a\gamma\gamma}^{\text{DM}} \lesssim 7 \times 10^{-19} \text{ GeV}^{-1} \simeq 10^{-8} g_{a\gamma\gamma}^{\text{HB}}$$



# Sensitivity Estimate

X-ray constraints at  $\sim 10$  keV require

$$\tau_{\text{DM}} \gtrsim 10^{29} \text{ s} \Rightarrow g_{a\gamma\gamma}^{\text{DM}} \lesssim 7 \times 10^{-19} \text{ GeV}^{-1} \simeq 10^{-8} g_{a\gamma\gamma}^{\text{HB}}$$

Must satisfy  $\rho_a/\tau_a \lesssim \rho_{\text{DM}}/\tau_{\text{DM}}$  and  $\tau^{-1} \propto g_{a\gamma\gamma}^2$ , so

$$\mathcal{F}_a \lesssim \frac{\tau_a}{\tau_{\text{DM}}} = \left( \frac{g_{a\gamma\gamma}^{\text{DM}}}{g_{a\gamma\gamma}} \right)^2 \quad (2)$$



# Sensitivity Estimate

$$\mathcal{F}_a \simeq 10^{-4} \left( \frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{HB}}} \right)^2 \left( \frac{T_{\text{RH}}}{5 \text{ MeV}} \right) \quad (1)$$

$$\mathcal{F}_a \lesssim \frac{\tau_a}{\tau_{\text{DM}}} = \left( \frac{g_{a\gamma\gamma}^{\text{DM}}}{g_{a\gamma\gamma}} \right)^2 \quad (2)$$

Combine (1) and (2)

$$10^{-4} \left( \frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{HB}}} \right)^2 \lesssim \left( \frac{g_{a\gamma\gamma}^{\text{DM}}}{g_{a\gamma\gamma}} \right)^2$$



# Sensitivity Estimate

$$\mathcal{F}_a \simeq 10^{-4} \left( \frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{HB}}} \right)^2 \left( \frac{T_{\text{RH}}}{5 \text{ MeV}} \right) \quad (1)$$

$$\mathcal{F}_a \lesssim \frac{\tau_a}{\tau_{\text{DM}}} = \left( \frac{g_{a\gamma\gamma}^{\text{DM}}}{g_{a\gamma\gamma}} \right)^2 \quad (2)$$

Combine (1) and (2)

$$10^{-4} \left( \frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{HB}}} \right)^2 \lesssim \left( \frac{g_{a\gamma\gamma}^{\text{DM}}}{g_{a\gamma\gamma}} \right)^2$$
$$\Rightarrow \frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{HB}}} \lesssim \left[ 10^4 \left( \frac{g_{a\gamma\gamma}^{\text{DM}}}{g_{a\gamma\gamma}^{\text{HB}}} \right)^2 \right]^{1/4} \simeq (10^{-12})^{1/4} \simeq 10^{-3}$$



# Sensitivity Estimate

$$\mathcal{F}_a \simeq 10^{-4} \left( \frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{HB}}} \right)^2 \left( \frac{T_{\text{RH}}}{5 \text{ MeV}} \right) \quad (1)$$

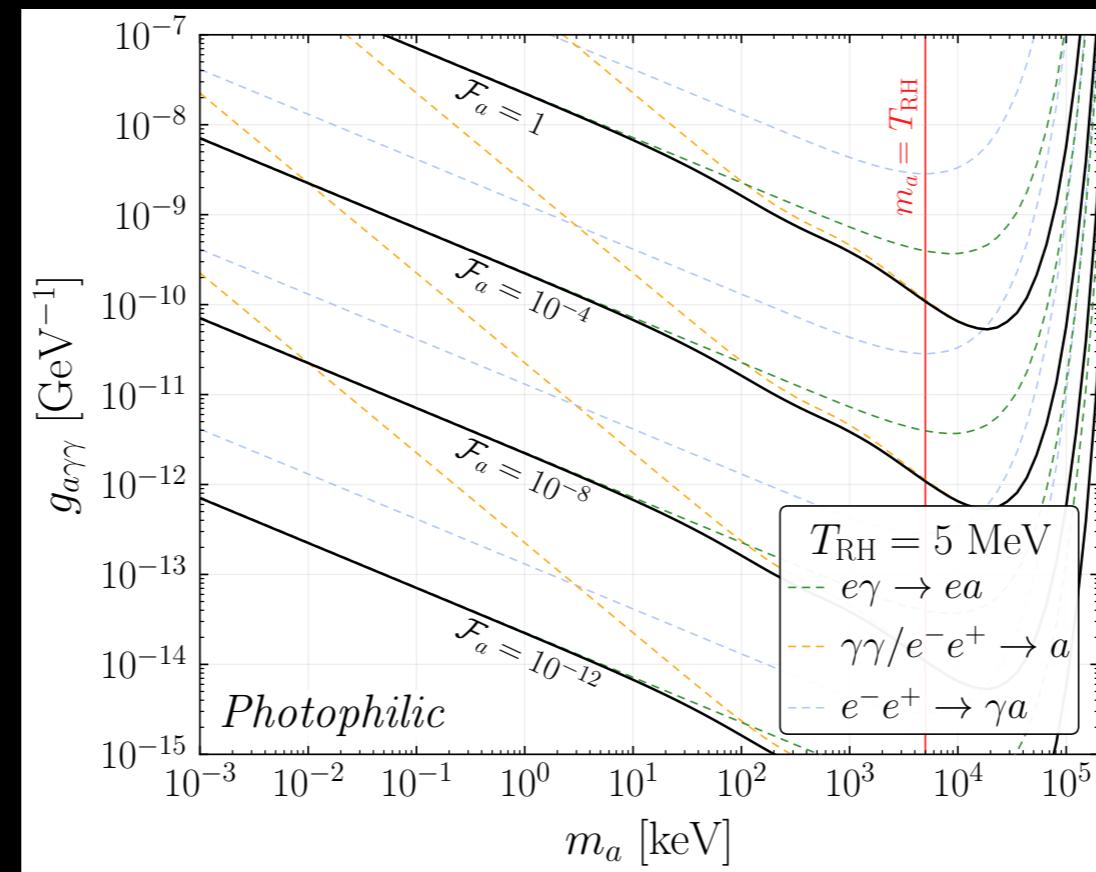
$$\mathcal{F}_a \lesssim \frac{\tau_a}{\tau_{\text{DM}}} = \left( \frac{g_{a\gamma\gamma}^{\text{DM}}}{g_{a\gamma\gamma}} \right)^2 \quad (2)$$

Combine (1) and (2)

$$\begin{aligned} 10^{-4} \left( \frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{HB}}} \right)^2 &\lesssim \left( \frac{g_{a\gamma\gamma}^{\text{DM}}}{g_{a\gamma\gamma}} \right)^2 \\ \Rightarrow \frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{HB}}} &\lesssim \left[ 10^4 \left( \frac{g_{a\gamma\gamma}^{\text{DM}}}{g_{a\gamma\gamma}^{\text{HB}}} \right)^2 \right]^{1/4} \simeq (10^{-12})^{1/4} \simeq 10^{-3} \\ \Rightarrow g_{a\gamma\gamma} &\lesssim 7 \times 10^{-14} \text{ GeV}^{-1} \ll g_{a\gamma\gamma}^{\text{HB}} \end{aligned}$$

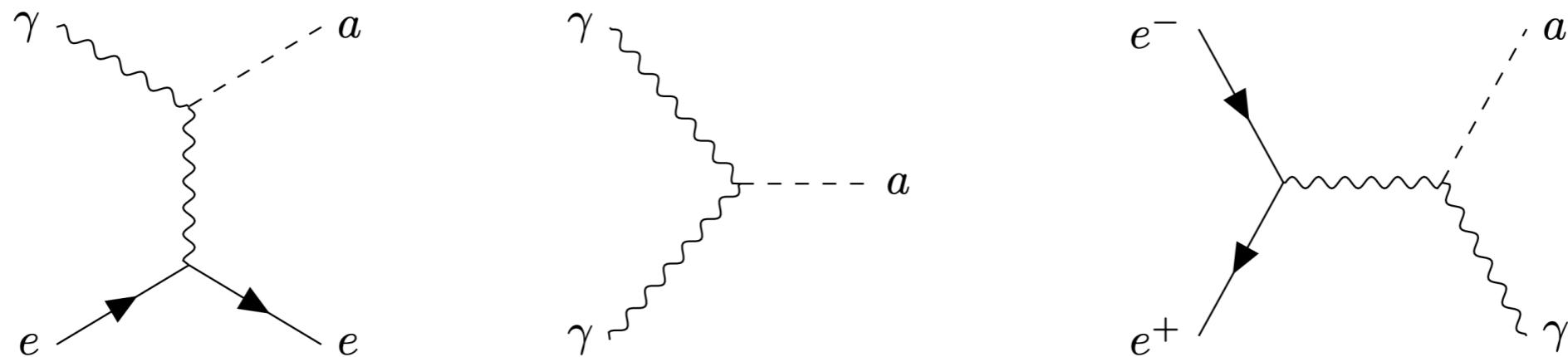


# Abundance



# Abundance

Axions produced by at least three interactions



Two are UV dominated - depend critically on  $T_{\text{RH}}$ ,  
but there is a minimal value consistent with BBN

$$T_{\text{RH}} \gtrsim 5 \text{ MeV}$$

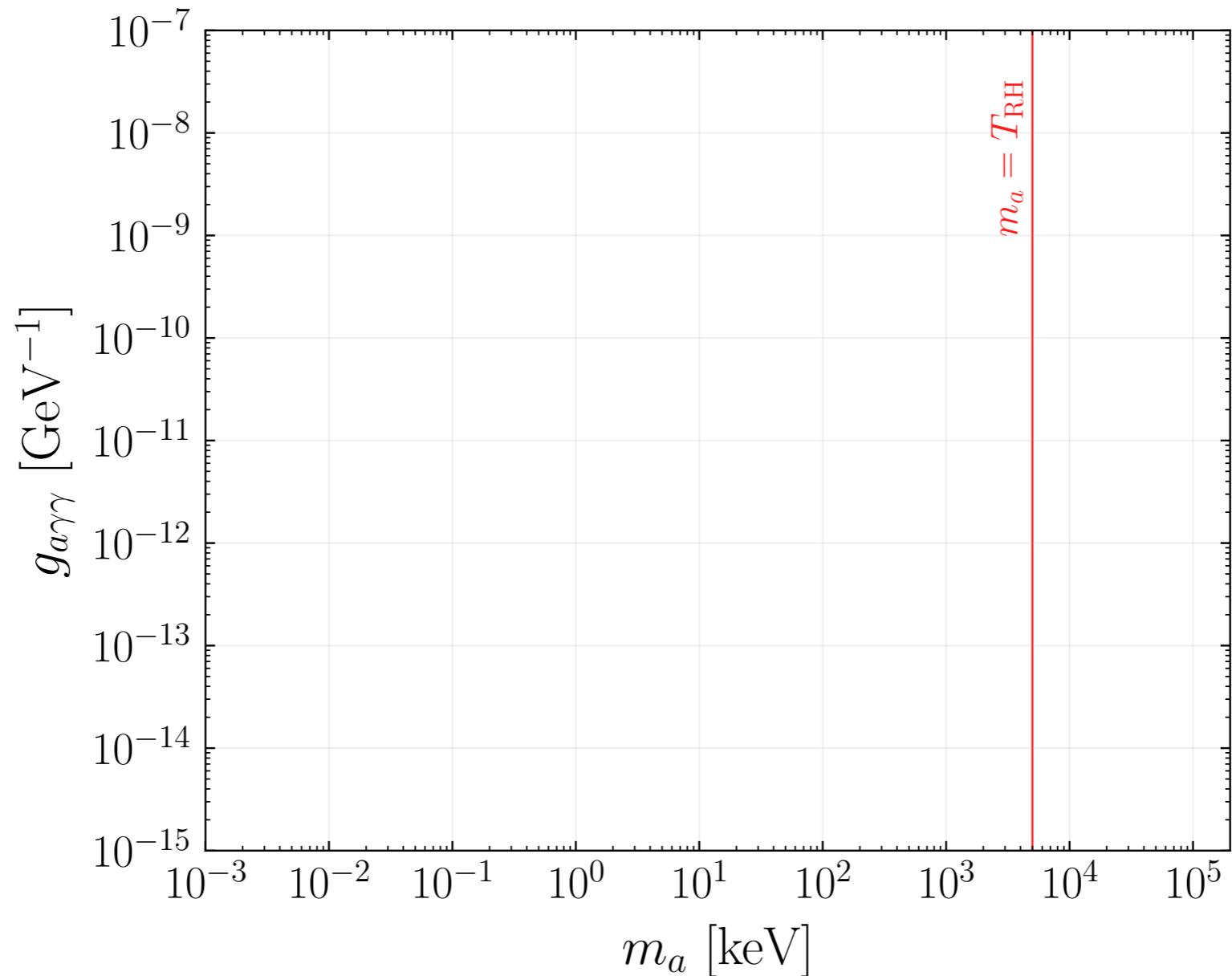
[Hannestad 2004], [Kawasaki+ 1999, 2000], [Ichikawa+ 2005, 2007],  
[Salas+ 2015], [Hasegawa+ 2019]

Cf. [Balázs+ 2205.13549]



# Abundance

Compute the freeze-in abundance\*  $\mathcal{F}_a = \rho_a / \rho_{\text{DM}}$

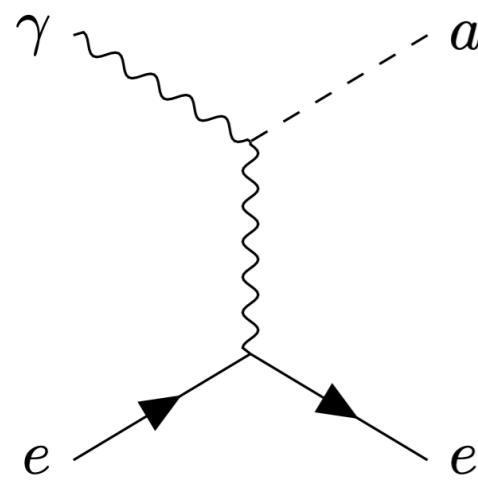


\*For  $T_{\text{RH}}^{\min}$  thermalizes  
for  $g_{a\gamma\gamma} \gtrsim 10^{-7} \text{ GeV}^{-1}$

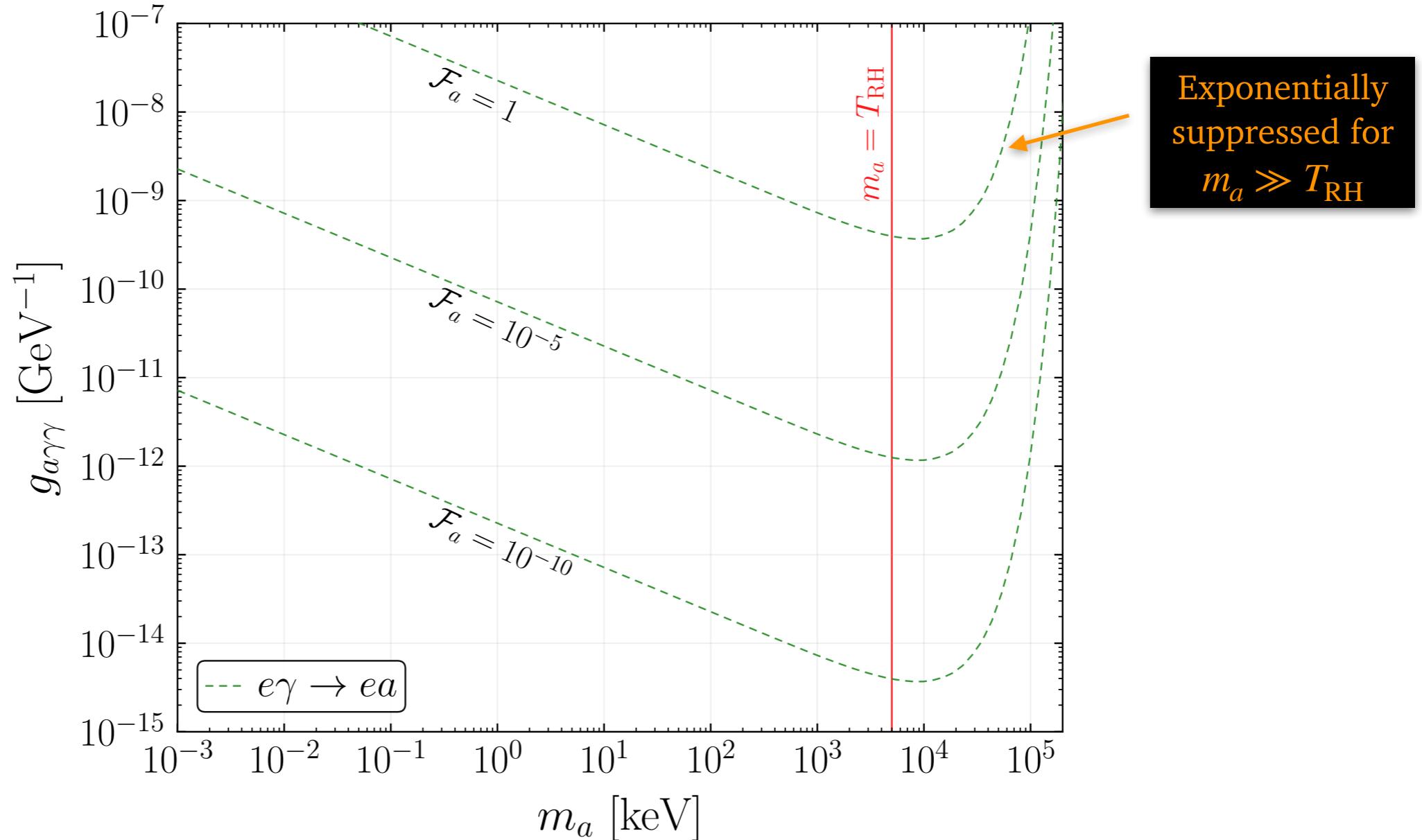


# Abundance

Compute the freeze-in abundance\*  $\mathcal{F}_a = \rho_a / \rho_{\text{DM}}$



Photon Conversion

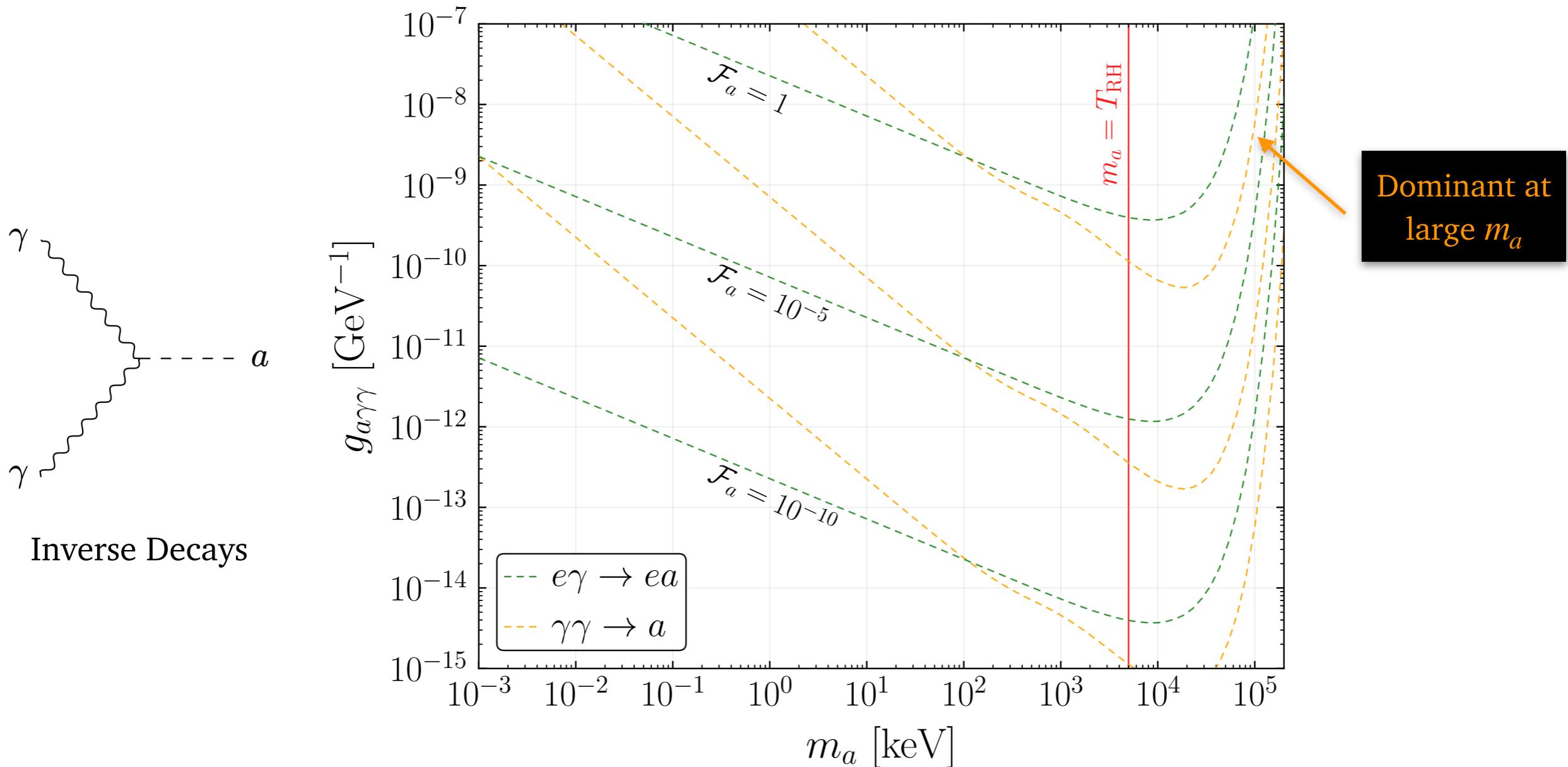


\*For  $T_{\text{RH}}^{\min}$  thermalizes  
for  $g_{a\gamma\gamma} \gtrsim 10^{-7} \text{ GeV}^{-1}$



# Abundance

Compute the freeze-in abundance\*  $\mathcal{F}_a = \rho_a / \rho_{\text{DM}}$



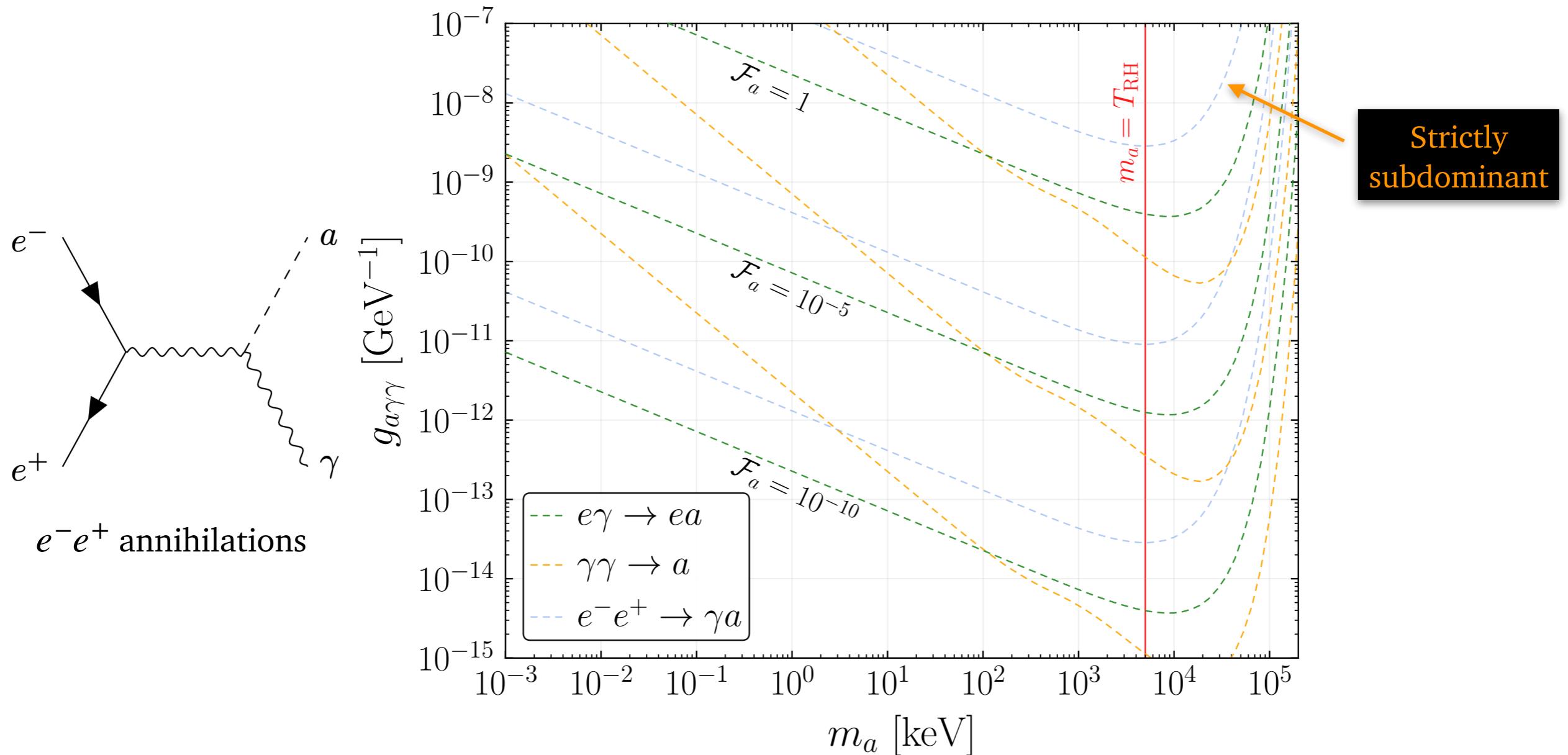
\*For  $T_{\text{RH}}^{\min}$  thermalizes  
for  $g_{a\gamma\gamma} \gtrsim 10^{-7} \text{ GeV}^{-1}$

[Langhoff, Outmezguine, NLR PRL 2022]



# Abundance

Compute the freeze-in abundance\*  $\mathcal{F}_a = \rho_a / \rho_{\text{DM}}$

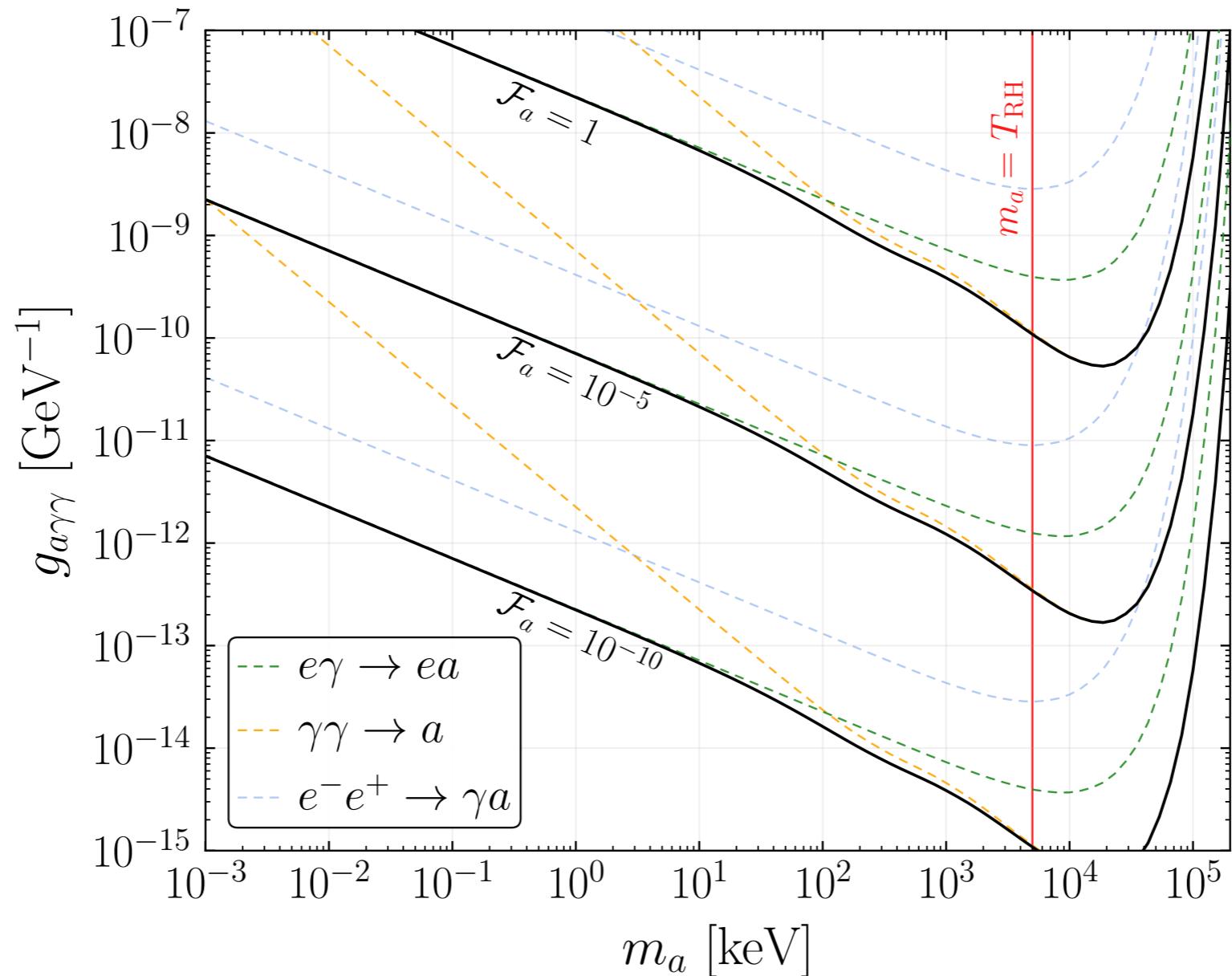


\*For  $T_{\text{RH}}^{\min}$  thermalizes  
for  $g_{a\gamma\gamma} \gtrsim 10^{-7} \text{ GeV}^{-1}$



# Abundance

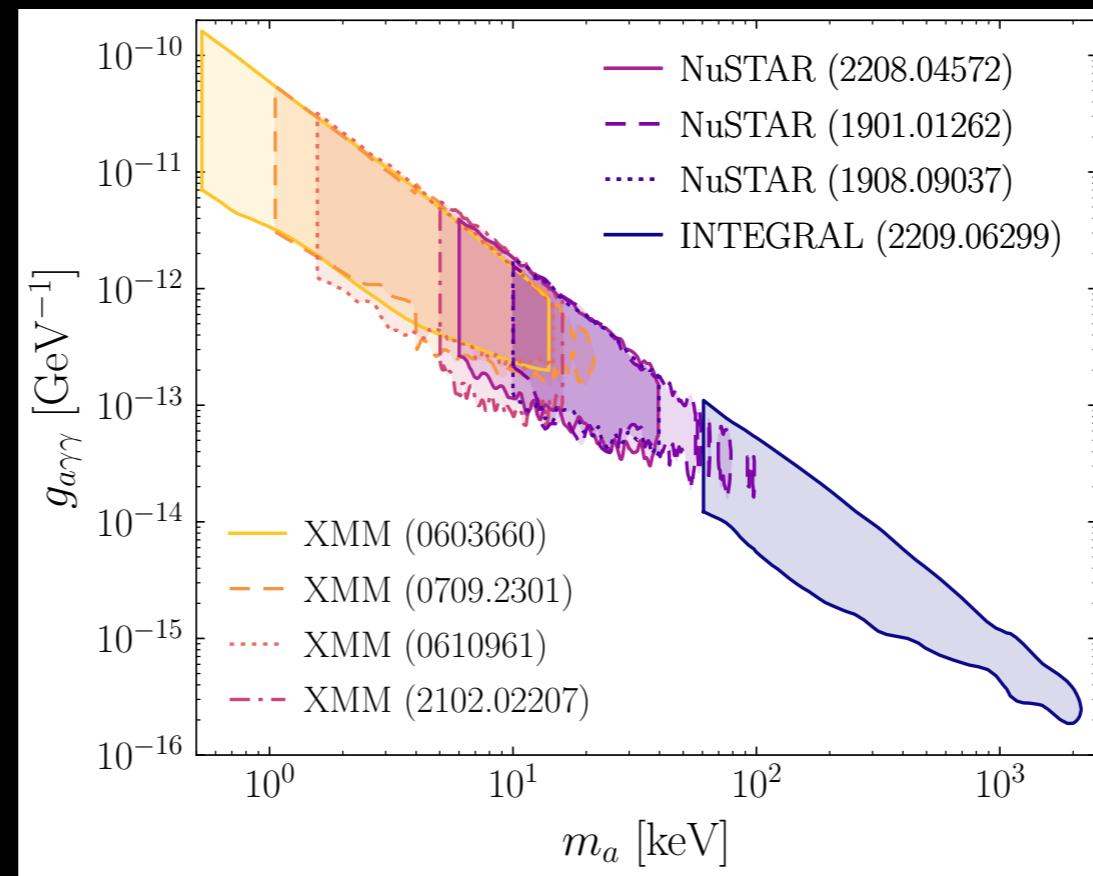
Compute the freeze-in abundance\*  $\mathcal{F}_a = \rho_a / \rho_{\text{DM}}$



\*For  $T_{\text{RH}}^{\min}$  thermalizes  
for  $g_{a\gamma\gamma} \gtrsim 10^{-7} \text{ GeV}^{-1}$

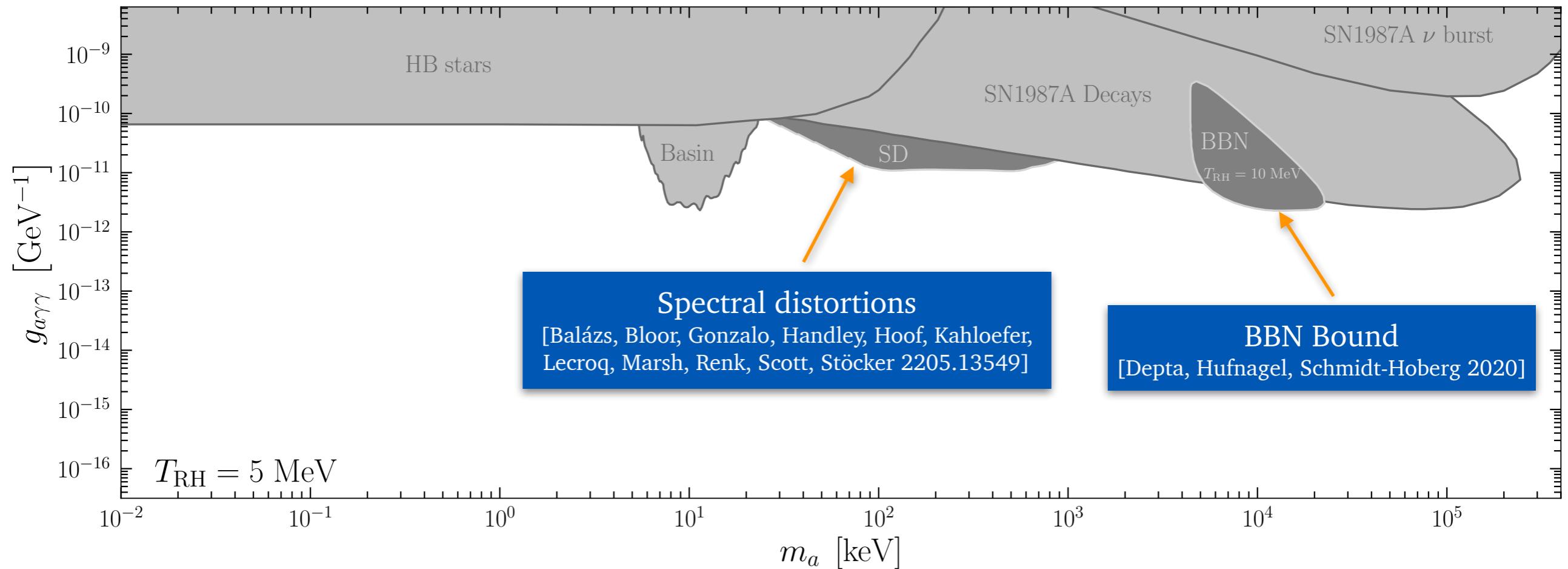


# Constraints



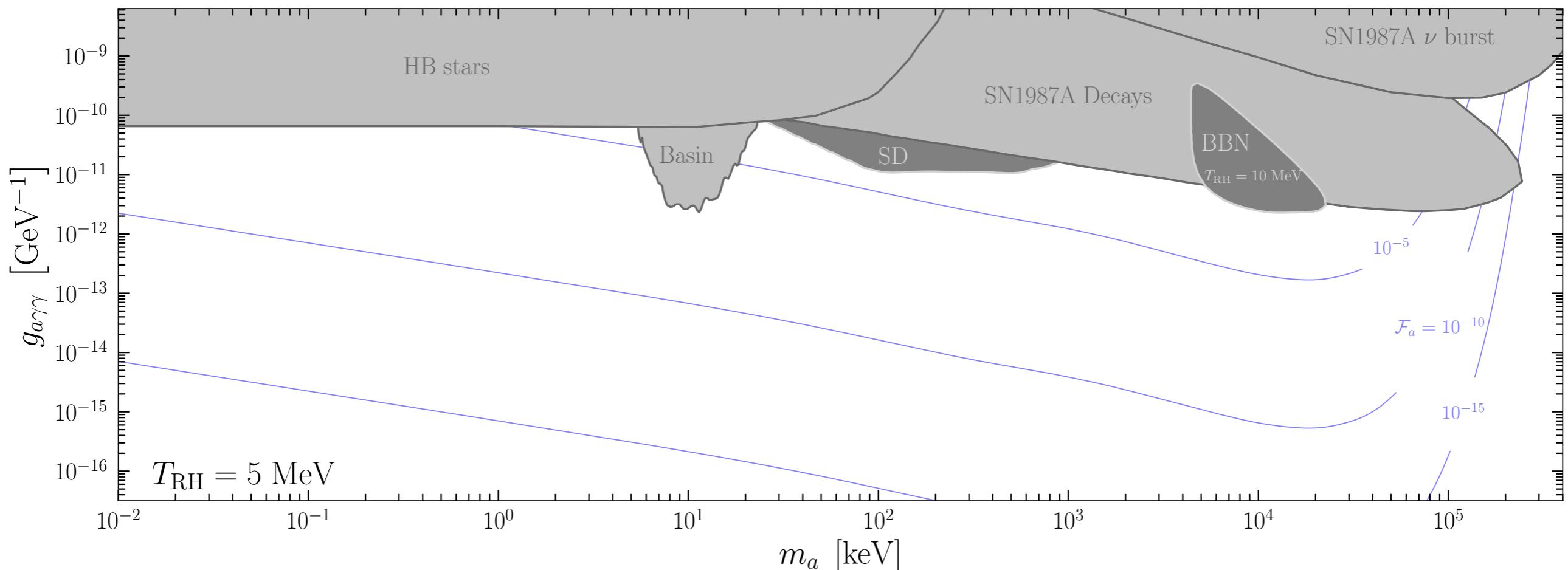
# Constraints

Start with  $a \neq \text{DM}$  constraints



# Constraints

Irreducible abundance is small, but testable

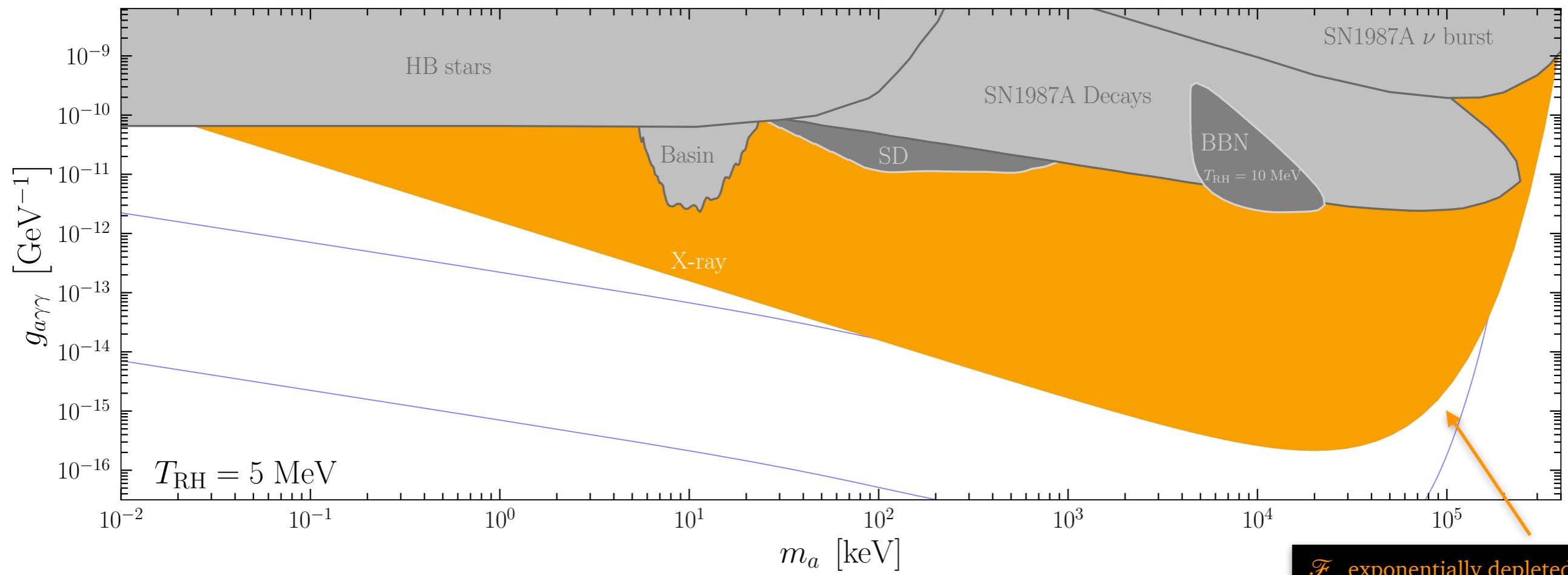


# Constraints

Starting point: X-ray Constraints

$$\Phi_a = \Phi_{\text{DM}} \Rightarrow \mathcal{F}_a \simeq \tau_{a \rightarrow \gamma\gamma} / \tau_{\text{DM}}$$

Assume mass independent  
 $\tau_{\text{DM}} = 10^{28} \text{ s}$



For this simple example,  
ignore inverse decays

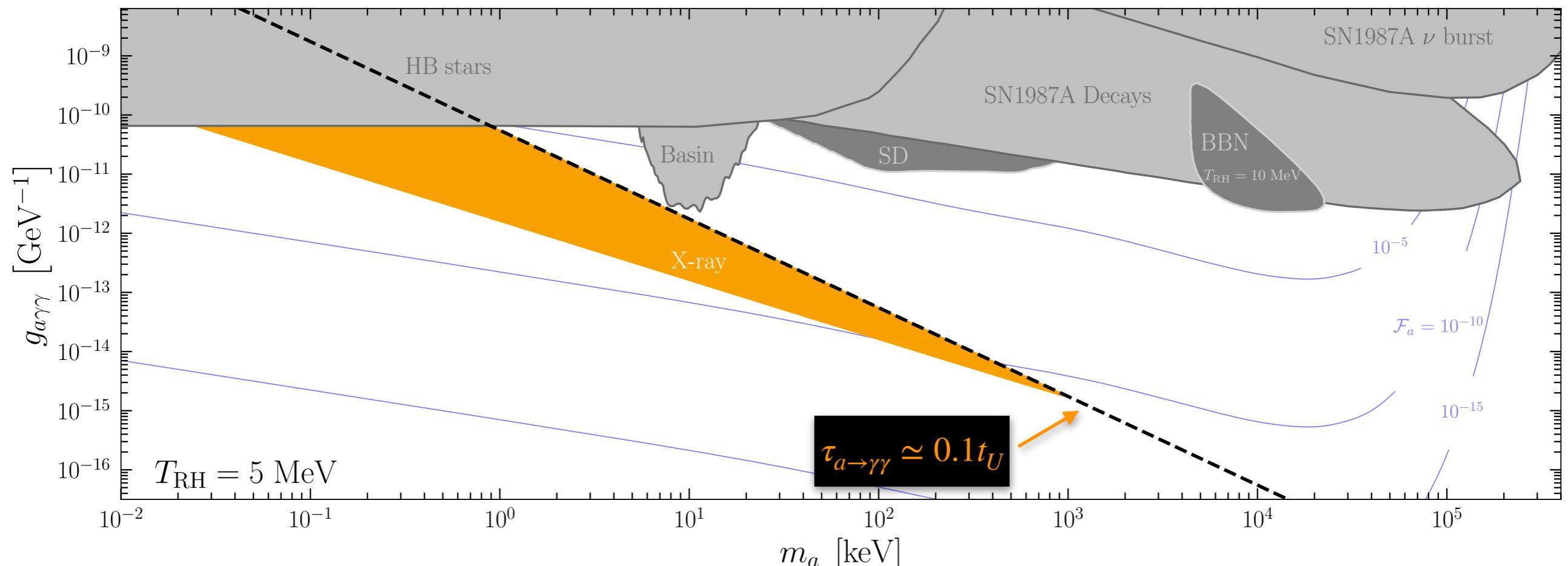


# Constraints

## Starting point: X-ray Constraints

$$\Phi \propto \tau_{a \rightarrow \gamma\gamma}^{-1} \exp[-t_U/\tau_a]$$

Neglected previously - cuts constraints at large couplings

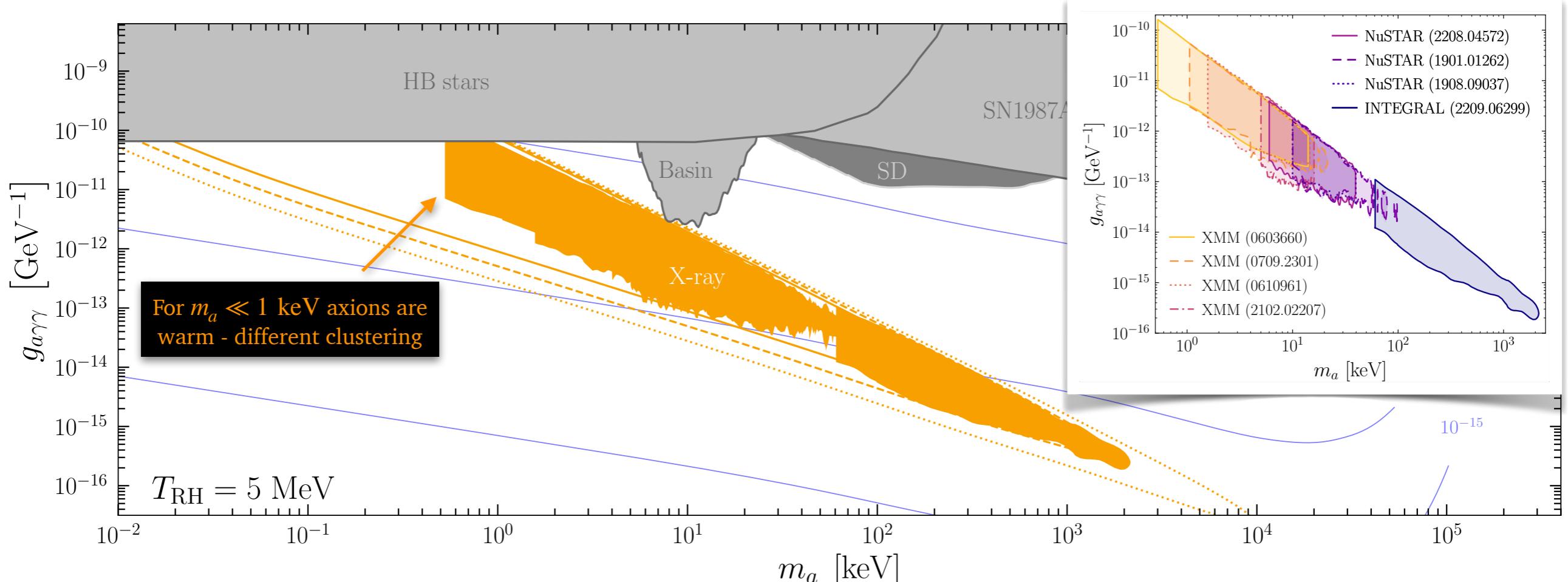


# Constraints

## Starting point: X-ray Constraints

$$\Phi \propto \tau_{a \rightarrow \gamma\gamma}^{-1} \exp[-t_U/\tau_a]$$

Neglected previously - cuts constraints at large couplings



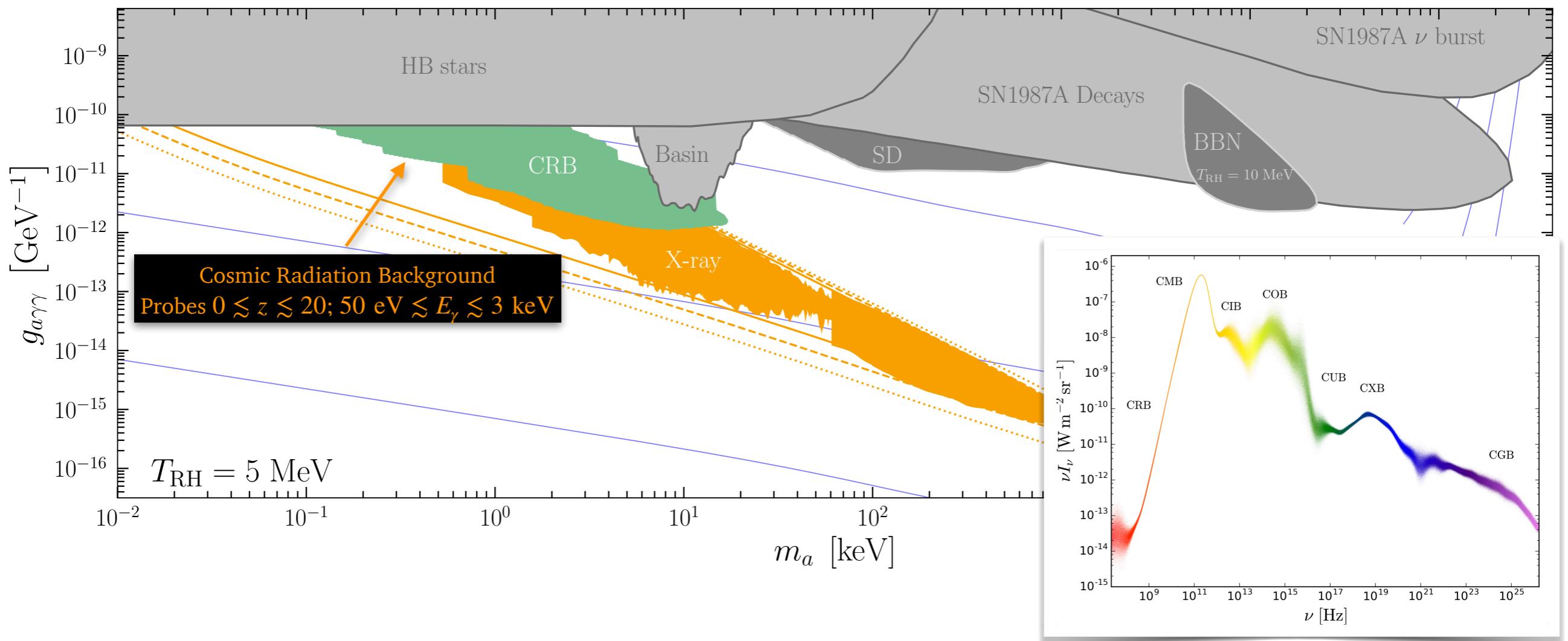
Solid/dashed/dotted curves: mass independent limits of  $10^{29}/10^{30}/10^{31}$  s



# Constraints

Need earlier probes, even if weaker for DM

Consider decays throughout the Universe

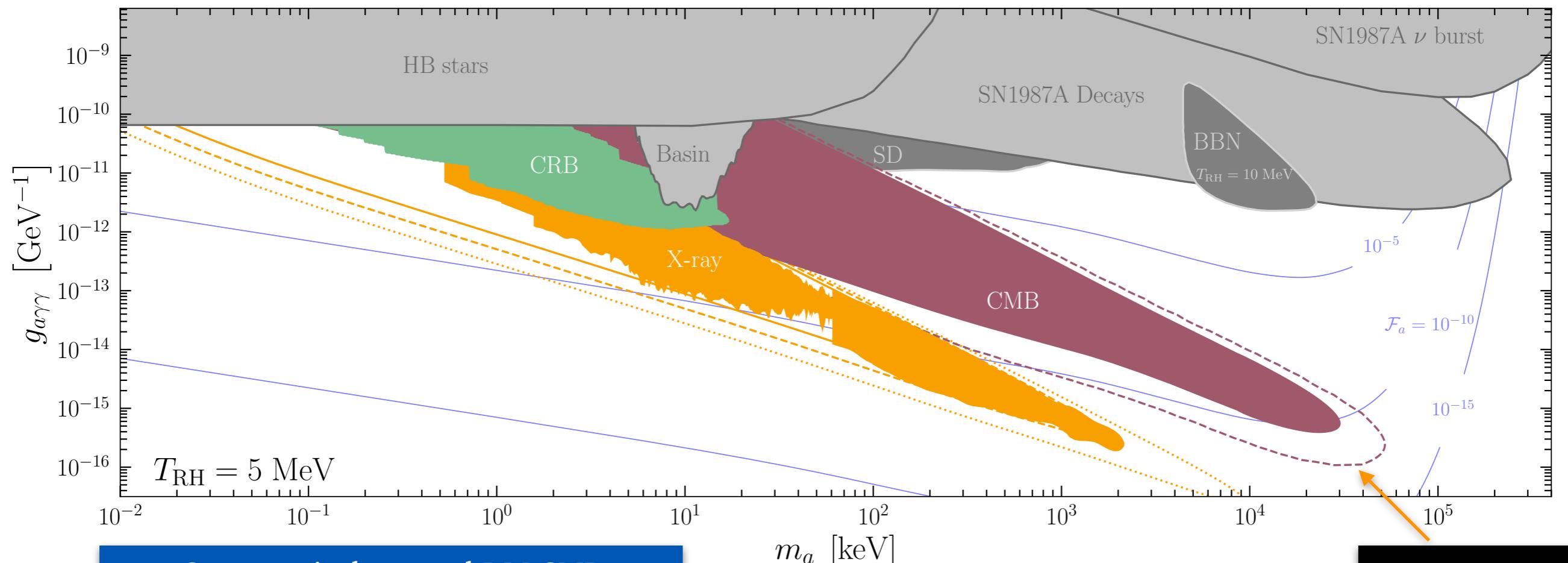


[“The Spectrum of the Universe”  
Hill, Masui, Scott 2018]



# Constraints

CMB allows for probes of earlier epochs still



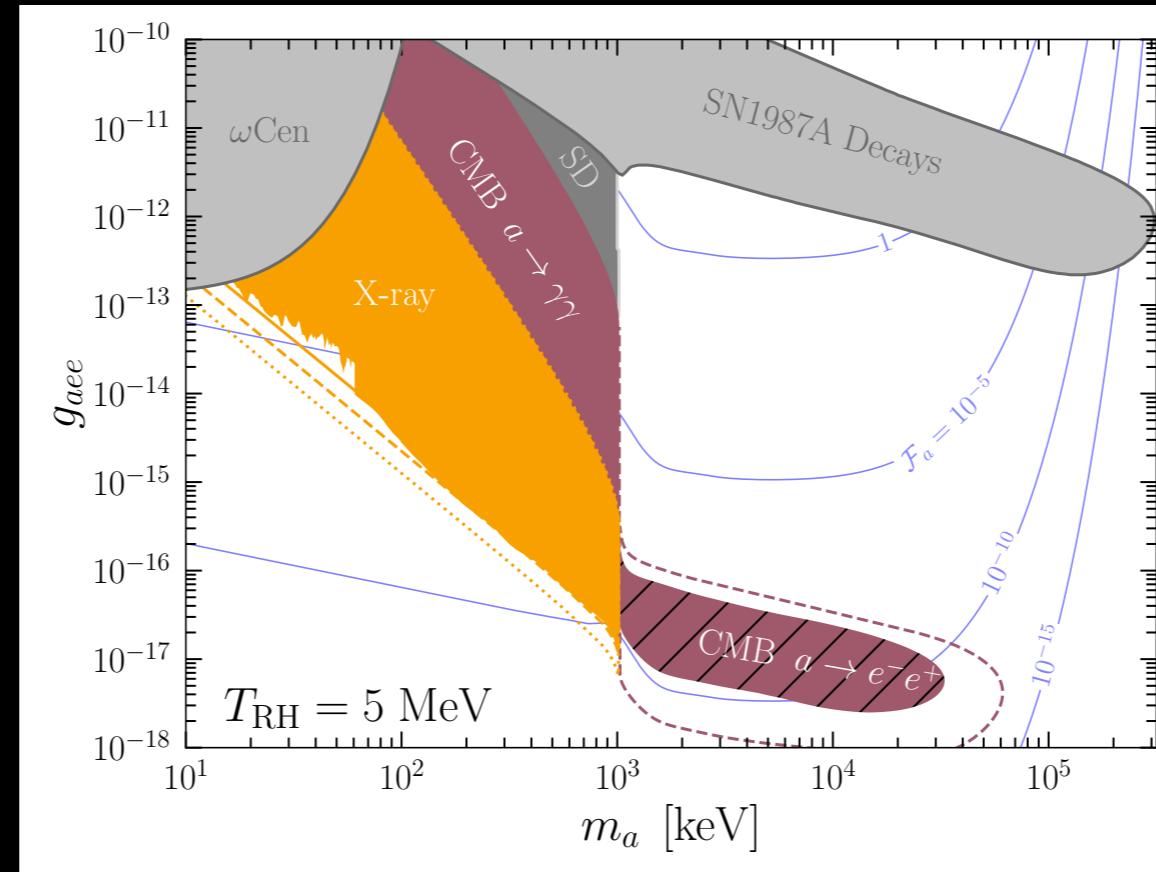
Conservatively extend DM CMB  
constraints to  $\mathcal{F}_a \ll 1$

[Slatyer, Wu 2017], [Poulin, Lesgourgues, Serpico 2017],  
[Cang, Gao, Ma 2020], [Bolliet, Chluba, Battye 2021]

See [Balázs+ 2205.13549]  
for a full CMB analysis



# Extensions



# Extensions

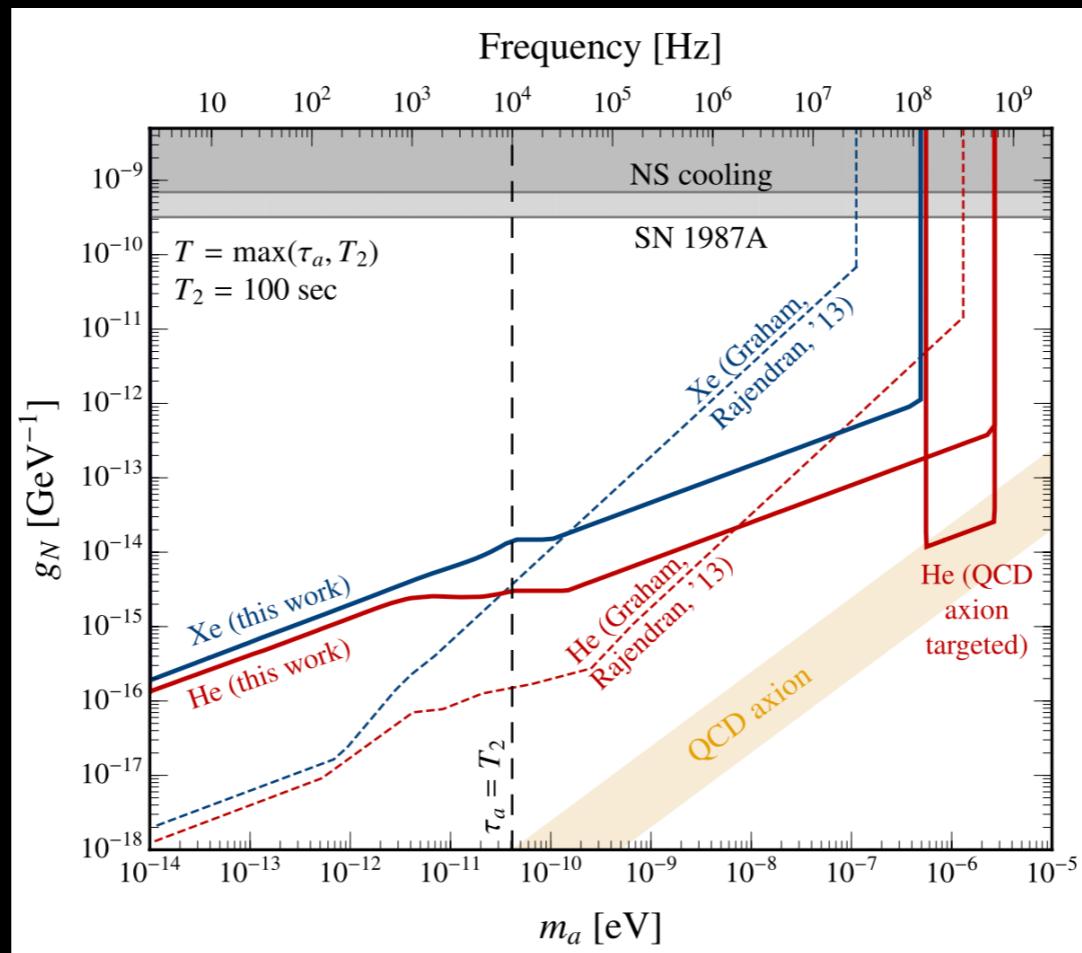
---

Logic readily extends to the electron coupling and can also add a contribution from misalignment

Irreducible abundance can also be considered for the sterile neutrino, dark photon, gravitino, ...



# Bonus: haloscope sensitivity



# Haloscope Sensitivity

---

A result commonly used for haloscope sensitivity

$$g \propto \begin{cases} T^{-1/2} & T \ll \tau_a \\ T^{-1/4} & T \gg \tau_a \end{cases}$$

[Budker, Graham, Ledbetter,  
Rajendran, Sushkov 2013]



# Haloscope Sensitivity

A result commonly used for haloscope sensitivity

$$g \propto \begin{cases} T^{-1/2} & T \ll \tau_a \\ T^{-1/4} & T \gg \tau_a \end{cases}$$

Dicke radiometer  
equation predicts:  $T^{-1/4}$

[Budker, Graham, Ledbetter,  
Rajendran, Sushkov 2013]

Axion coherence time  
 $\tau_a \sim 2\pi/m_a v^2$   
 $\sim 1 \text{ s} (1 \text{ neV}/m_a)$



# Haloscope Sensitivity

That scaling does not hold in general

$$g \propto \begin{cases} T^{-3/2} & T \ll \tau_a, \tau_r \\ T^{-1} & \tau_a \ll T \ll \tau_r \\ T^{-1/2} & \tau_r \ll T \ll \tau_a \\ T^{-1/4} & T \gg \tau_a, \tau_r \end{cases}$$

Instrument coherence time, e.g.  $T_2$  for NMR or  $2\pi Q/\bar{\omega}$  for a cavity

Straightforward to derive: axion is a weak driving force for resonant systems, problem maps to the SHO, and can be solved analytically



# Haloscope Sensitivity

Example: axion NMR

$$\frac{d\mathbf{M}}{dt} = \mathbf{M} \times \gamma \mathbf{B} - \frac{M_x \hat{\mathbf{x}} + M_y \hat{\mathbf{y}}}{T_2} - \frac{(M_z - M_0) \hat{\mathbf{z}}}{T_1}$$

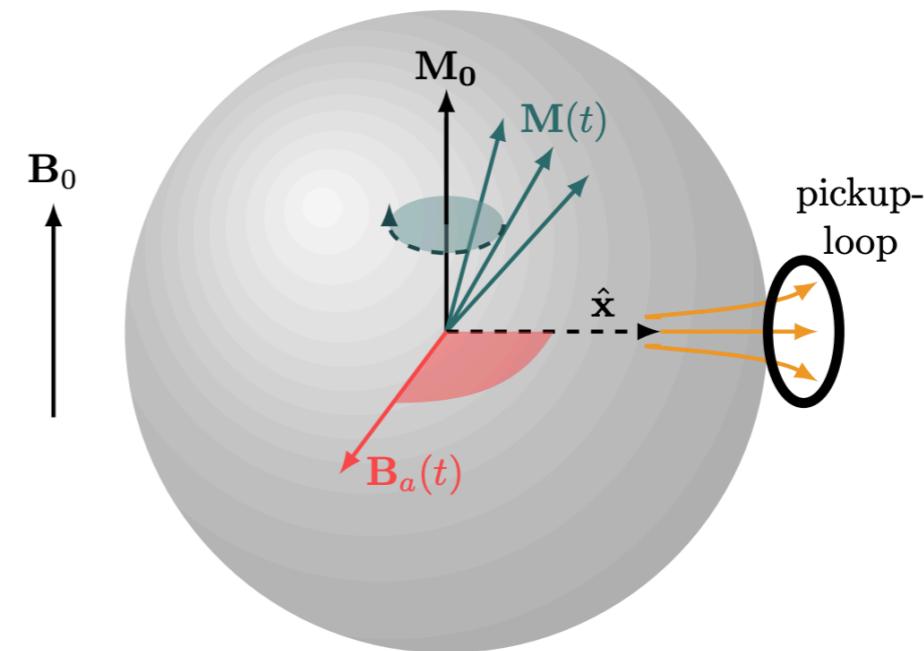


# Haloscope Sensitivity

Example: axion NMR

$$\frac{d\mathbf{M}}{dt} = \mathbf{M} \times \gamma \mathbf{B} - \frac{M_x \hat{\mathbf{x}} + M_y \hat{\mathbf{y}}}{T_2} - \frac{(M_z - M_0) \hat{\mathbf{z}}}{T_1}$$

Axion-nucleon coupling generates a magnetic field  
 $\mathbf{B} = (-2g_N/\gamma) \nabla a$



# Haloscope Sensitivity

Example: axion NMR

$$\frac{d\mathbf{M}}{dt} = \mathbf{M} \times \gamma \mathbf{B} - \frac{M_x \hat{\mathbf{x}} + M_y \hat{\mathbf{y}}}{T_2} - \frac{(M_z - M_0) \hat{\mathbf{z}}}{T_1}$$

Treat axion as a small perturbation

$$\ddot{M}_x + 2T_2^{-1}\dot{M}_x + \omega_0^2 = \gamma M_0 [\omega_0 B_x - \dot{B}_y]$$



# Haloscope Sensitivity

Example: axion NMR

$$\frac{d\mathbf{M}}{dt} = \mathbf{M} \times \gamma \mathbf{B} - \frac{M_x \hat{\mathbf{x}} + M_y \hat{\mathbf{y}}}{T_2} - \frac{(M_z - M_0) \hat{\mathbf{z}}}{T_1}$$

Treat axion as a small perturbation

$$\ddot{M}_x + 2T_2^{-1}\dot{M}_x + \omega_0^2 = \gamma M_0 [\omega_0 B_x - \dot{B}_y]$$

$T_2$  = coherence of  
the response

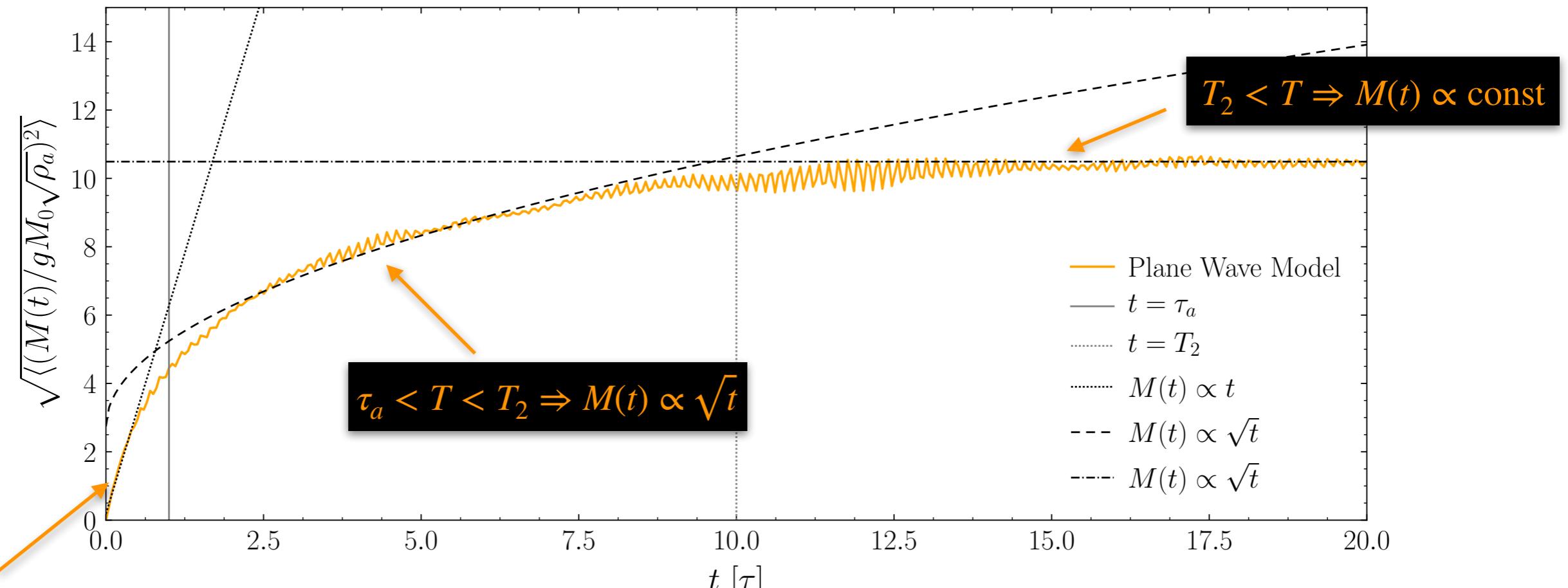
The simple harmonic oscillator - holds  
for general resonant axion halo scopes

$\tau_a$  = coherence of  
the driving force



# Haloscope Sensitivity

Solve for the growth of  $M_x$  analytically



# Haloscope Sensitivity

Sensitivity scaling:  $\sigma = P_{\text{sig}}/P_{\text{bkg}}$  ( $P_{\text{sig}} \propto g^2$ )

$$g \propto \begin{cases} T^{-3/2} & T \ll \tau_a, \tau_r \\ T^{-1} & \tau_a \ll T \ll \tau_r \\ T^{-1/2} & \tau_r \ll T \ll \tau_a \\ T^{-1/4} & T \gg \tau_a, \tau_r \end{cases}$$



# Haloscope Sensitivity

Sensitivity scaling:  $\sigma = P_{\text{sig}}/P_{\text{bkg}}$  ( $P_{\text{sig}} \propto g^2$ )

$$g \propto \begin{cases} T^{-3/2} & T \ll \tau_a, \tau_r \\ T^{-1} & \tau_a \ll T \ll \tau_r \\ T^{-1/2} & \tau_r \ll T \ll \tau_a \\ T^{-1/4} & T \gg \tau_a, \tau_r \end{cases}$$

$P_{\text{sig}} \propto M^2 \propto T^2$  and  $P_{\text{bkg}} \propto 1/T$

White noise: larger  $T$  integrate over a smaller range



# Haloscope Sensitivity

Sensitivity scaling:  $\sigma = P_{\text{sig}}/P_{\text{bkg}}$  ( $P_{\text{sig}} \propto g^2$ )

$$g \propto \begin{cases} T^{-3/2} & T \ll \tau_a, \tau_r \\ T^{-1} & \tau_a \ll T \ll \tau_r \\ T^{-1/2} & \tau_r \ll T \ll \tau_a \\ T^{-1/4} & T \gg \tau_a, \tau_r \end{cases}$$

$P_{\text{sig}} \propto M^2 \propto T$  and  $P_{\text{bkg}} \propto 1/T$



# Haloscope Sensitivity

Sensitivity scaling:  $\sigma = P_{\text{sig}}/P_{\text{bkg}}$  ( $P_{\text{sig}} \propto g^2$ )

$$g \propto \begin{cases} T^{-3/2} & T \ll \tau_a, \tau_r \\ T^{-1} & \tau_a \ll T \ll \tau_r \\ T^{-1/2} & \tau_r \ll T \ll \tau_a \\ T^{-1/4} & T \gg \tau_a, \tau_r \end{cases}$$

$P_{\text{sig}} \propto M^2 \propto \text{const}$  and  $P_{\text{bkg}} \propto 1/T$



# Haloscope Sensitivity

Sensitivity scaling:  $\sigma = P_{\text{sig}}/P_{\text{bkg}}$  ( $P_{\text{sig}} \propto g^2$ )

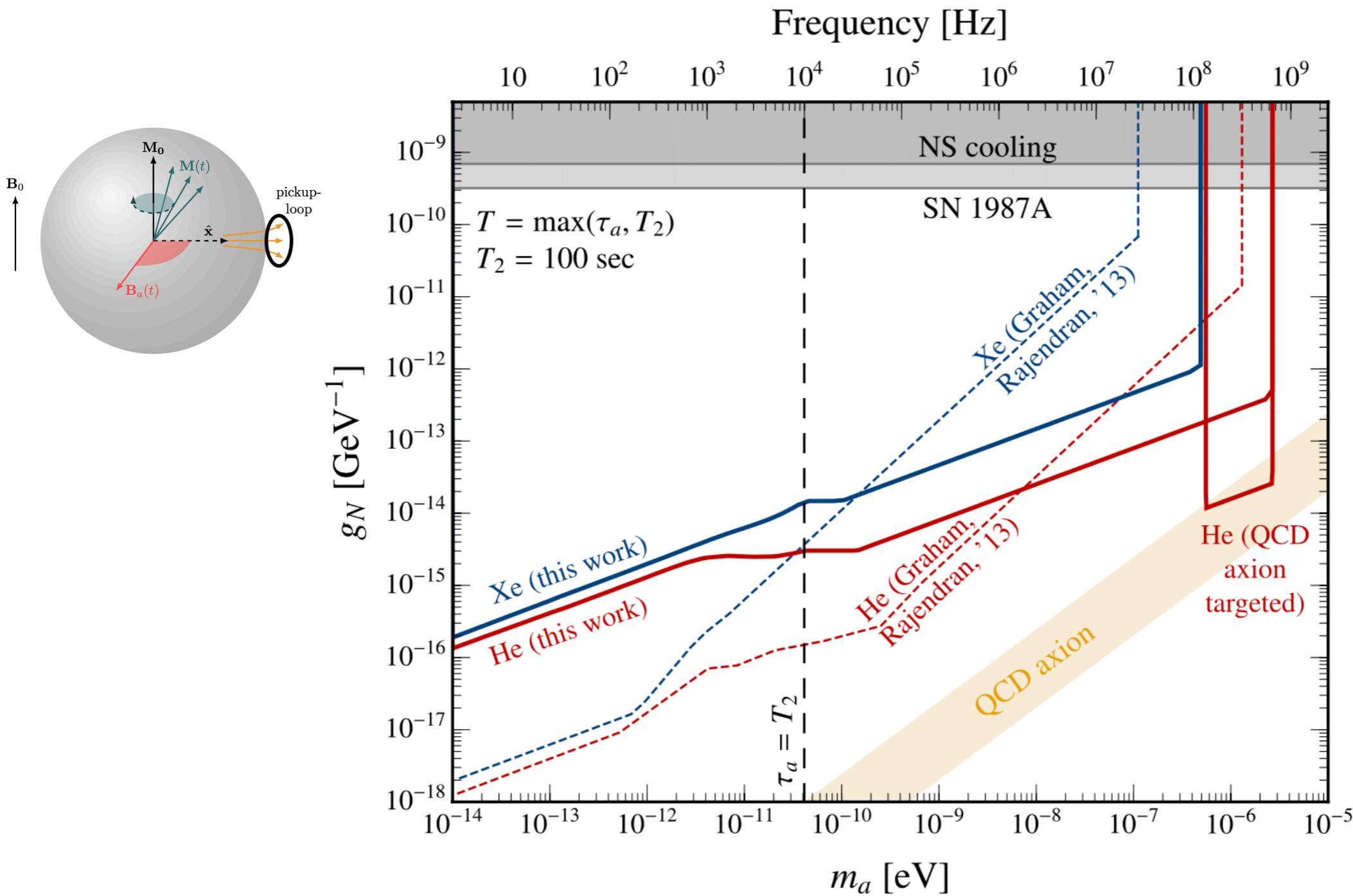
$$g \propto \begin{cases} T^{-3/2} & T \ll \tau_a, \tau_r \\ T^{-1} & \tau_a \ll T \ll \tau_r \\ T^{-1/2} & \tau_r \ll T \ll \tau_a \\ T^{-1/4} & T \gg \tau_a, \tau_r \end{cases}$$

Resolve signal in  $N \propto T$  bins,  $P_{\text{sig}}$  enhanced by  $\sqrt{N}$



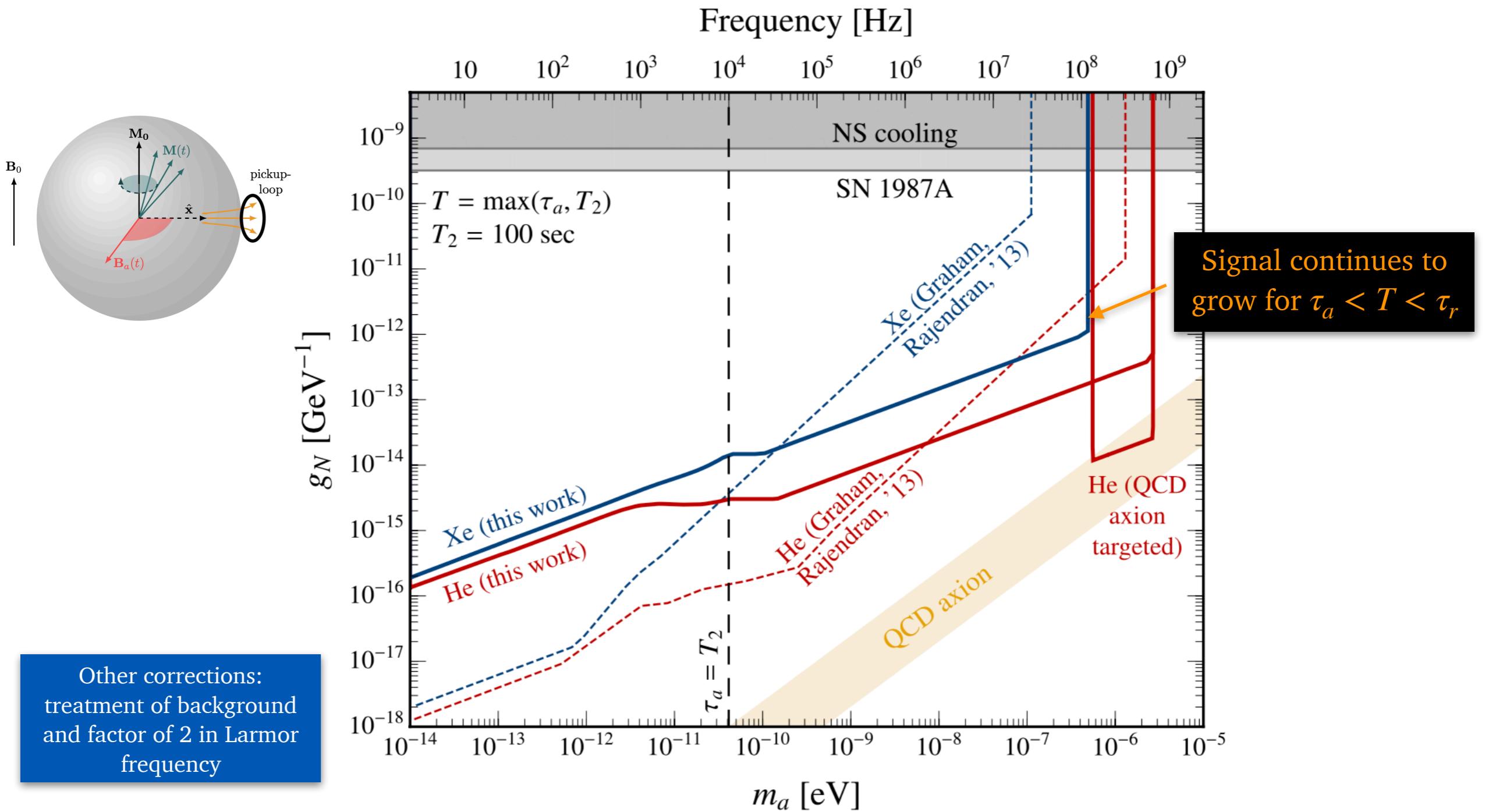
# Haloscope Sensitivity

## Implications for CASPER-Wind



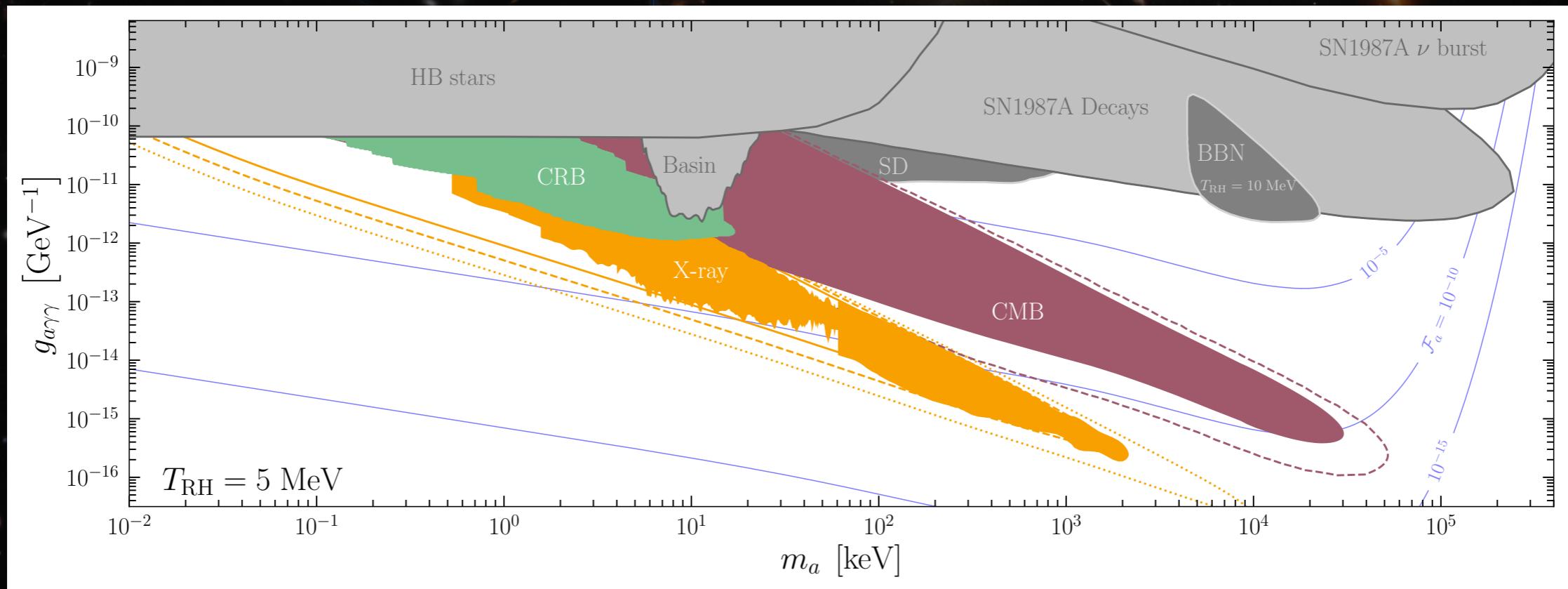
# Haloscope Sensitivity

## Implications for CASPER-Wind



# Conclusion

DM searches can strongly constrain non-DM axions



[Langhoff, Outmezguine, NLR PRL 2022]

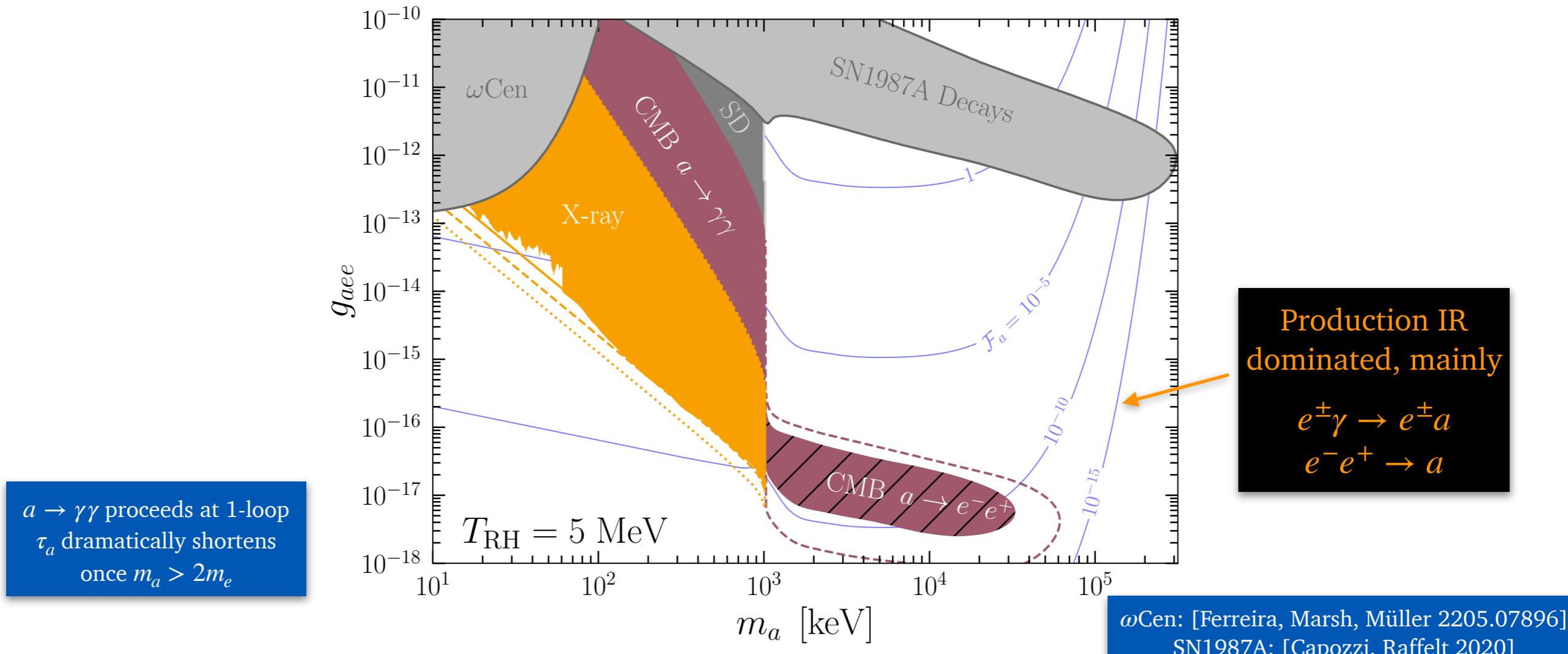


# Backup Slides

# Extensions

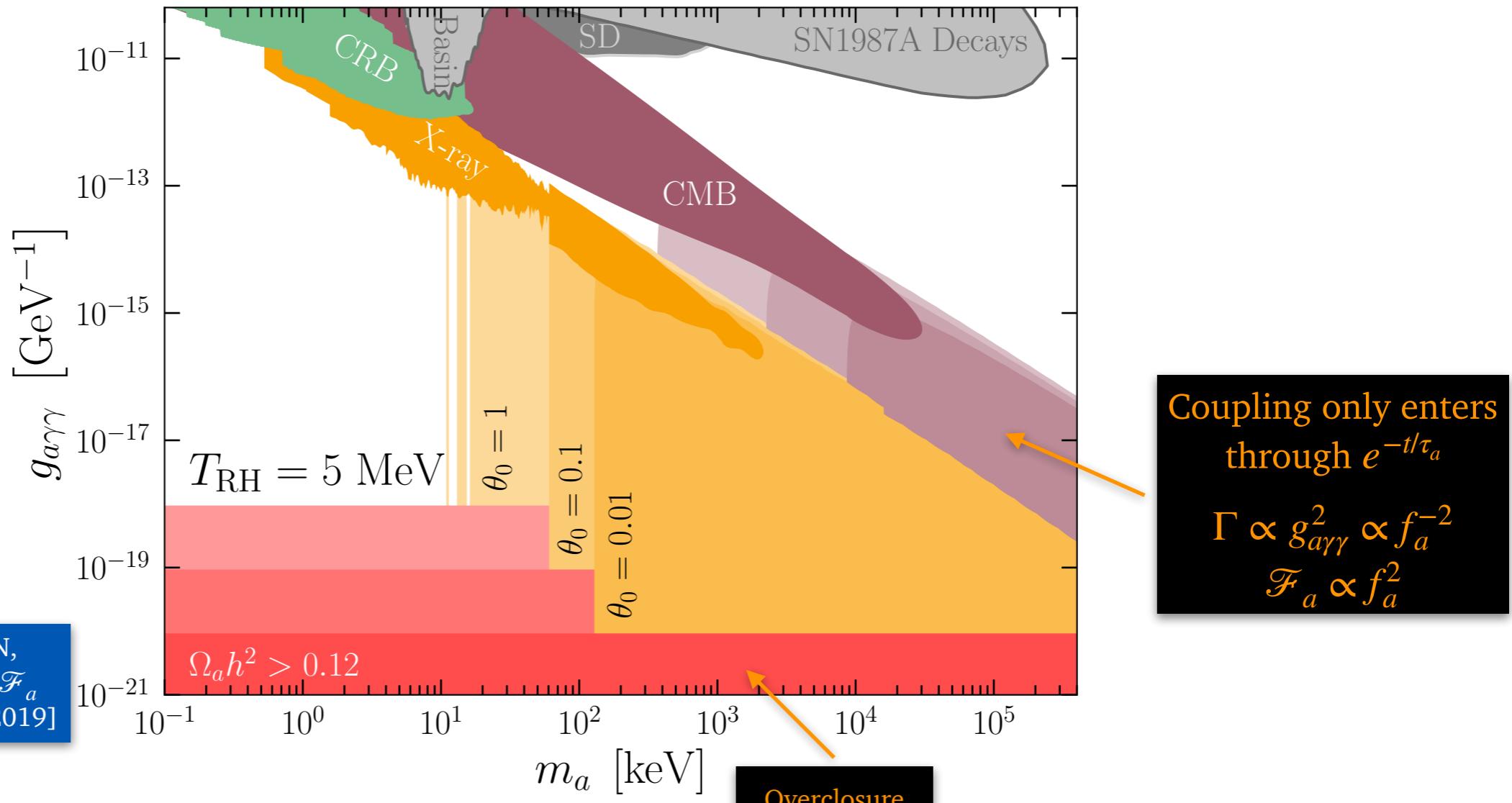
Argument immediately extends to other couplings, e.g.

$$\frac{g_{aee}}{2m_e} (\partial_\mu a) \bar{e} \gamma^\mu \gamma_5 e$$



# Extensions

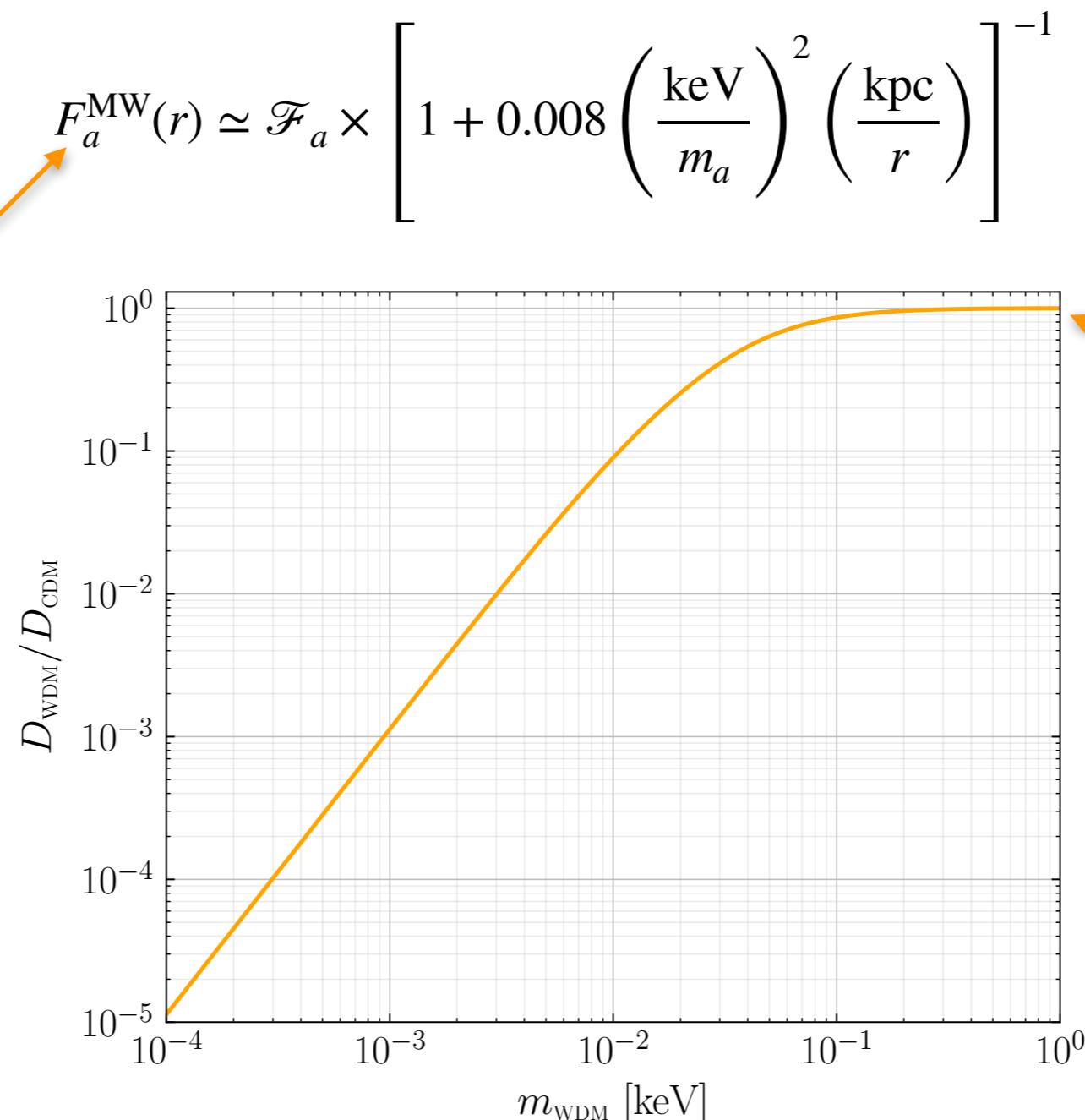
Misalignment contribution not irreducible, but can include conservatively\*



# Clustering at low mass

Impact on X-ray constraints due to warm DM not clustering

N-body Milky Way study  
[Anderhalden, Diemand, Bertone,  
Maccio, Schneider 2012]

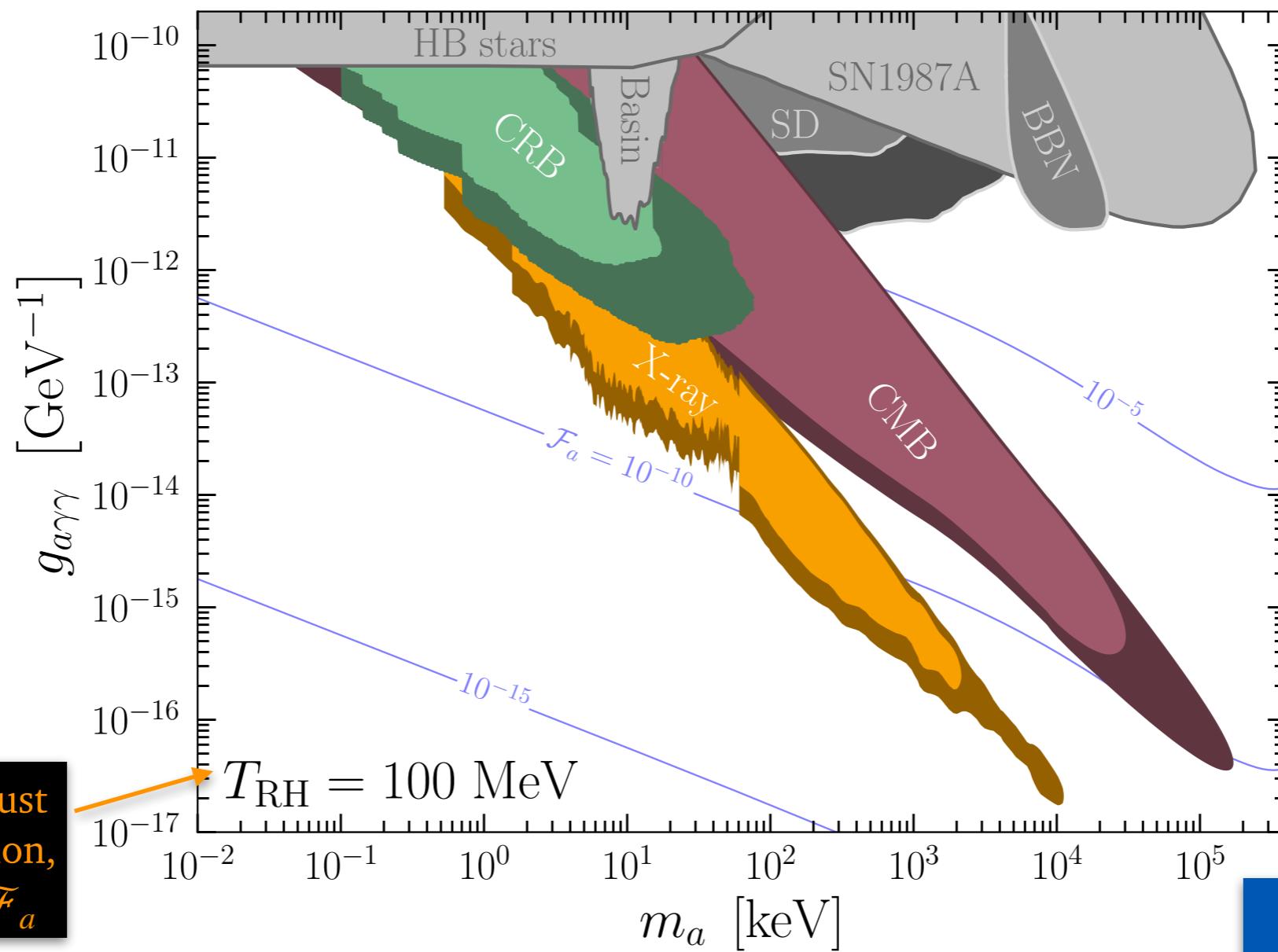


Safe for  $m_a \gtrsim 1$  keV



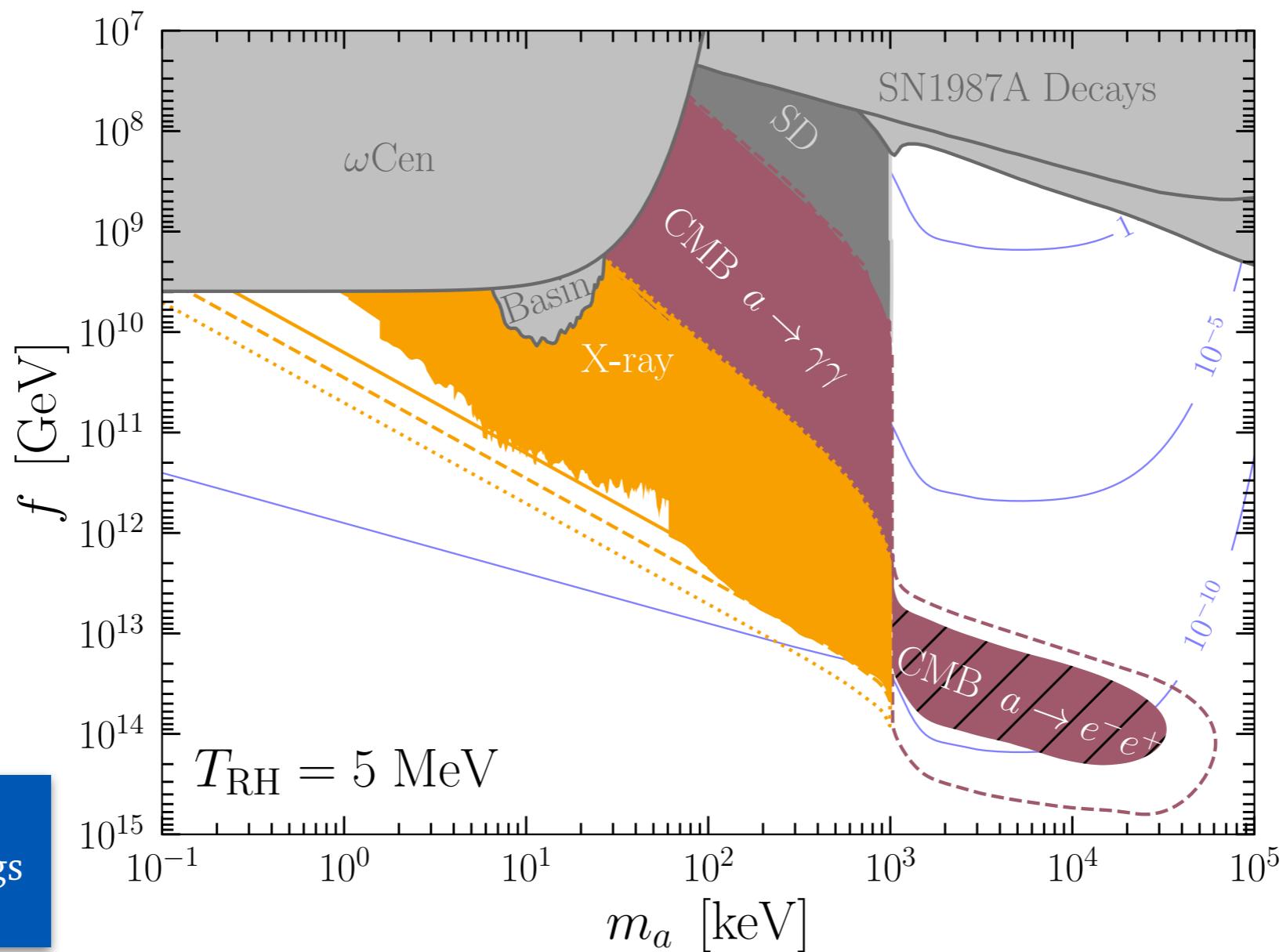
# $T_{\text{RH}}$ dependence

Production UV dominated:  $\mathcal{F}_a \propto T_{\text{RH}} \Rightarrow g_{a\gamma\gamma} \propto T_{\text{RH}}^{1/4}$



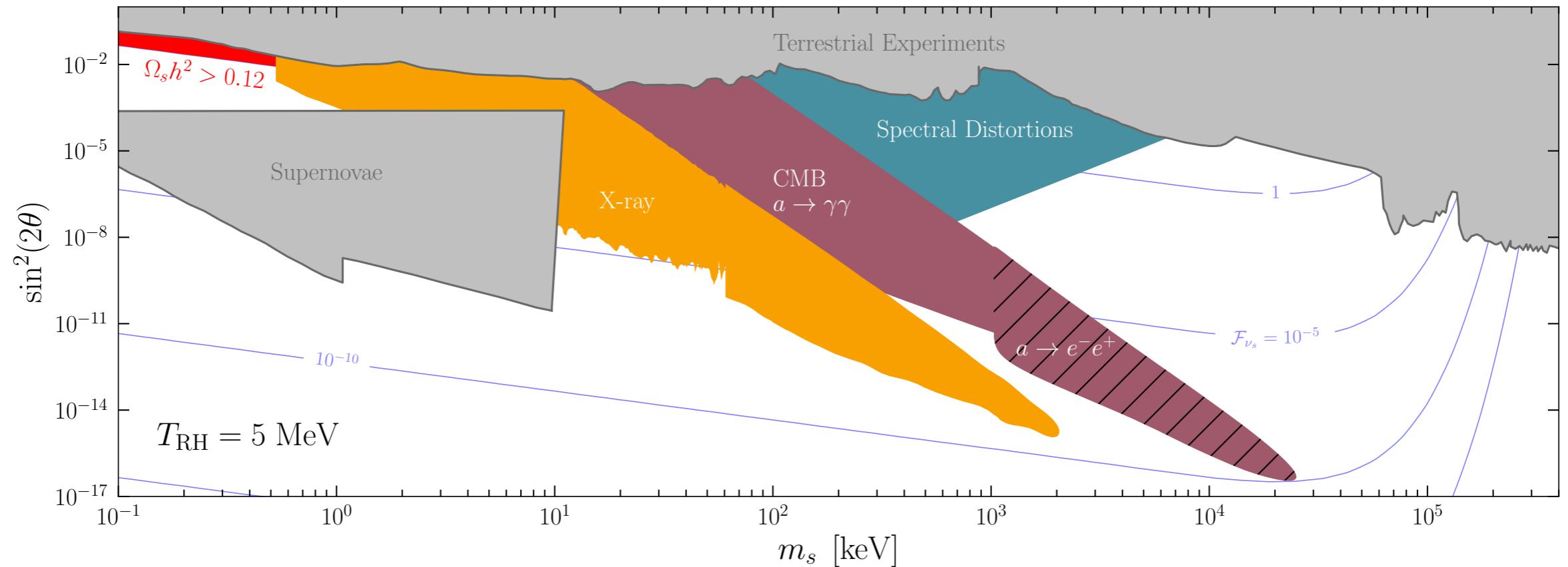
# Universal Couplings

$$g_{a\gamma\gamma} = \alpha/2\pi f_a \text{ and } g_{aee} = m_e/f_a$$



# Sterile Neutrinos

Idea readily extend to other states (graviton, dark photon...)

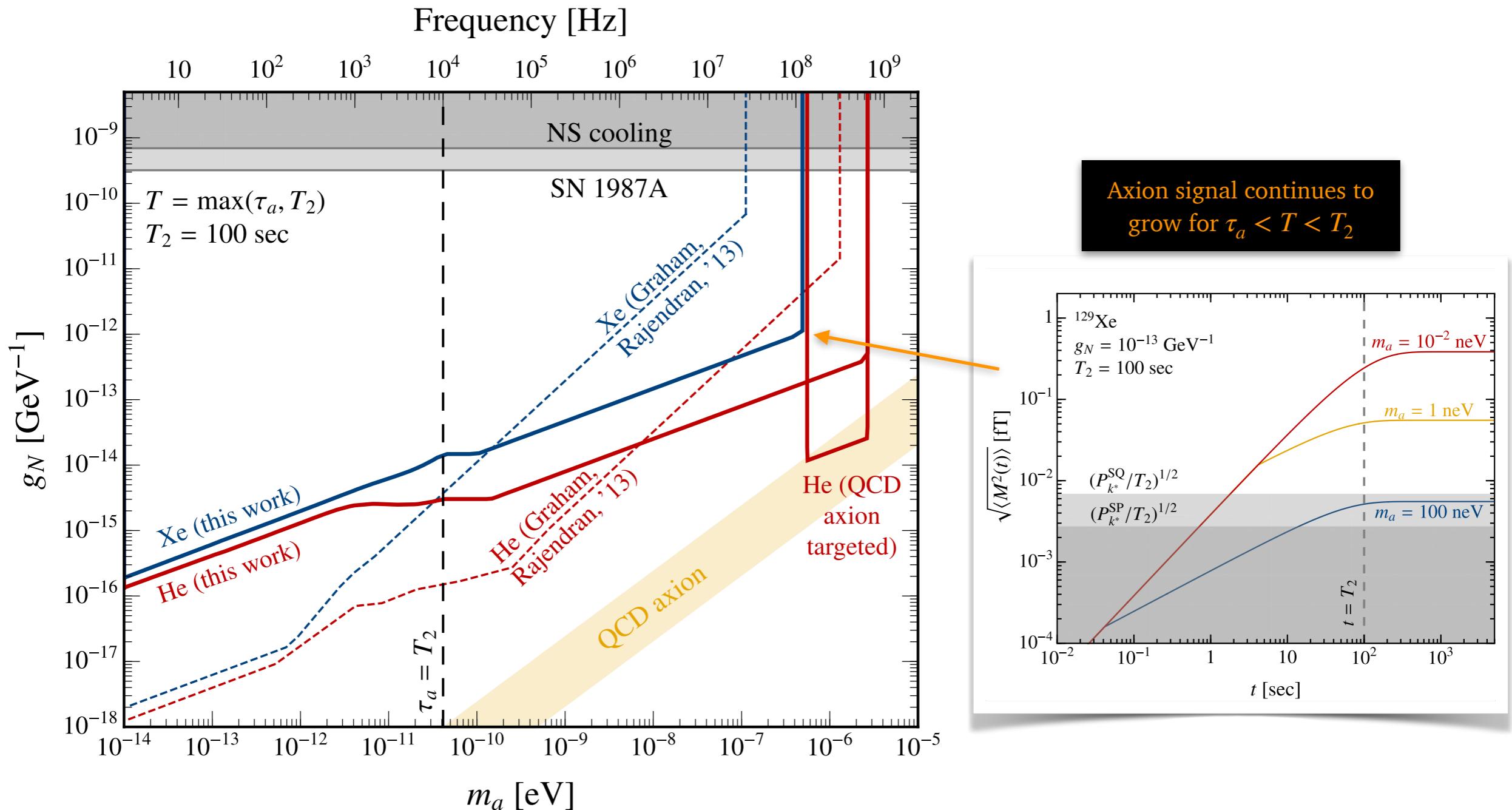


Cf. [Gelmini, Osoba, Palomares-Ruiz, Pascoli 2008],  
[Gelmini, Lu, Takhistov 2019]



# Axion NMR

$$\mathcal{L} \supset g_N (\partial_\mu a) \bar{N} \gamma^\mu \gamma_5 N$$



# Axion NMR

## Impact for CASPER-Electric

