

Stefano Gariazzo

UniTO and INFN via P. Giuria 1, 10125 Torino (IT)

stefano.gariazzo@unito.it

Relic neutrinos: decoupling and direct detection perspectives

Neutrino Frontiers: Focus week. GGI, Firenze, 01-05/07/2024





The Standard Model of Particle Physics



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The Standard Model of Particle Physics



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Neutrino spectrum



neutrinos at all energies provide valuable information!

Three Neutrino Oscillations

$$u_{lpha} = \sum_{k=1}^{3} U_{lpha k} \nu_k \quad (lpha = e, \mu, \tau)$$

 $U_{\alpha k}$ described by 3 mixing angles $\theta_{12}, \theta_{13}, \theta_{23}$ and one CP phase δ

Current knowledge of the 3 active ν mixing: [JHEP 02 (2021) update]



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Based on:

- Planck 2018
- JCAP 04 (2021) 073



History of the universe



History of the universe



before BBN: neutrinos coupled to plasma ($\nu_{\alpha}\bar{\nu}_{\alpha} \leftrightarrow e^+e^-$, $\nu e \leftrightarrow \nu e$)



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[Bennett, SG+, JCAP 2021] ν oscillations in the early universe [Sigl, Raffelt, 1993] comoving coordinates: a = 1/T $x \equiv m_e a$ $y \equiv p a$ $z \equiv T_{\gamma} a$ $w \equiv T_{\nu} a$ $\begin{array}{ccc} \text{density matrix:} & \varrho(x,y) = \begin{pmatrix} \varrho_{ee} \equiv f_{\nu_e} & \varrho_{e\mu} & \varrho_{e\tau} \\ \varrho_{\mu e} & \varrho_{\mu\mu} \equiv f_{\nu_{\mu}} & \varrho_{\mu\tau} \\ \varrho_{\tau e} & \varrho_{\tau\mu} & \varrho_{\tau\tau} \equiv f_{\nu_{\tau}} \end{pmatrix}$ off-diagonals to take into account coherency in the neutrino system ϱ evolution from $x H \frac{\mathrm{d}\varrho(y,x)}{\mathrm{d}x} = -ia[\mathcal{H}_{\mathrm{eff}},\varrho] + b\mathcal{I}$ *H* Hubble factor \rightarrow expansion (depends on universe content) effective Hamiltonian $\mathcal{H}_{eff} = \frac{\mathbb{M}_{F}}{2y} - \frac{2\sqrt{2}G_{F}ym_{e}^{6}}{x^{6}} \left(\frac{\mathbb{E}_{\ell} + \mathbb{P}_{\ell}}{m_{\mu\nu}^{2}} + \frac{4}{3} \frac{\mathbb{E}_{\nu}}{m_{\tau}^{2}}\right)$ vacuum oscillations -→ matter effects

 ${\mathcal I}$ collision integrals

take into account $\nu-e$ scattering and pair annihilation, $\nu-\nu$ interactions

2D integrals over momentum, take most of the computation time

solve together with z evolution, from $x \frac{d\rho(x)}{dx} = \rho - 3P$

 $\rho,\,P$ total energy density and pressure, also take into account FTQED corrections

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Relic neutrinos: decoupling and direct detection perspectives"

Distortion of the momentum distribution ($f_{\rm FD}$: Fermi-Dirac at equilibrium)



Distortion of the momentum distribution (f_{FD} : Fermi-Dirac at equilibrium)





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"Relic neutrinos: decoupling and direct detection perspectives"

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$$N_{\text{eff}}^{\text{any time}} = \frac{8}{7} \left(\frac{T_{\gamma}}{T_{\nu}}\right)^4 \frac{\rho_{\nu}}{\rho_{\gamma}} = \frac{8}{7} \left(\frac{T_{\gamma}}{T_{\nu}}\right)^4 \frac{1}{\rho_{\gamma}} \sum_i g_i \int \frac{d^3 p}{(2\pi)^3} E(p) f_{\nu,i}(p)$$



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[Bennett, SG+, JCAP 2021]

Effect of neutrino oscillations



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[Bennett, SG+, JCAP 2021]

Effect of neutrino oscillations



lic neutrinos: decoupling and direct detection perspective

Full 3ν mixing results:



Full 3ν mixing results:



Full 3ν mixing results:



Full 3ν mixing results:



Full 3ν mixing results:



Full 3ν mixing results:



$N_{\rm eff}$ and CMB



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D Direct detection of relic neutrinos

Based on:

- JCAP 01 (2023) 003
- JCAP 08 (2014) 038
- JCAP 07 (2019) 047



The oldest picture of the Universe

The Cosmic Microwave Background, generated at $t \simeq 4 \times 10^5$ years COBE (1992) WMAP (2003) Planck (2013)



The oldest picture of the Universe

The Cosmic Neutrino Background, generated at $t \simeq 1$ s

 $\ldots \rightarrow 2024 \rightarrow \ldots$



$T_{\nu}~\sim~10^{-4}$ eV, $E_{\nu}~\sim~5~\times~10^{-4}$ eV today! We need thresholdless detection process... How do we get them?

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Stodolsky effect?

How to directly detect non-relativistic neutrinos?



Stodolsky effect?

How to directly detect non-relativistic neutrinos?



expected
$$a_{
u} \simeq \mathcal{O}(10^{-26}) \text{ cm/s}^2 \longrightarrow a_{\mathrm{exp}} \simeq \mathcal{O}(10^{-12}) \text{ cm/s}^2$$

 $\frac{\text{CE}\nu\text{NS?}}{\text{First of all: what's Coherent Elastic }\nu\text{-Nucleous Scattering?}}$

elastic scattering where ν interacts with nucleous "as a whole"



Predicted for $|\vec{q}|R \lesssim 1$ by [Freedman, PRD 1974]

small recoil energies! \lesssim 10 keV. . . difficult to measure

 $\frac{d\sigma}{dT}(E_{\nu},T) \sim \frac{G_F^2 M}{4\pi} N^2$ [Drukier, Stodolsky, PRD 1984] enhancement N² because ν interacts coherently with all nucleons

may give huge cross section enhancement



[Shergold, JCAP 2021]

First of all: what's Coherent Elastic *v*-Nucleous Scattering?

elastic scattering where ν interacts with nucleous "as a whole"

Can we detect relic neutrinos with CE ν NS?

relic neutrinos have de Broglie length $\lambda \sim 2\pi/p_{\nu}$

enhancement in interactions due to coherence with nuclei in volume λ^3





[Shergold, JCAP 2021]

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At interferometers?

How to directly detect non-relativistic neutrinos?



At interferometers?





Neutrino capture

[Long+, JCAP 08 (2014) 038]

How to directly detect non-relativistic neutrinos?

Remember that $\langle E_{
u}
angle \ \simeq \ {\cal O}(10^{-4}) \ {
m eV}$ today

a process without energy threshold is necessary

[Weinberg, 1962]: neutrino capture in eta–decaying nuclei $u+n
ightarrow p+e^-$

Main background: β decay $n \rightarrow p + e^- + \bar{\nu}!$



What material?

[Cocco+, JCAP 06 (2007) 015]

best element has highest $\sigma_{
m NCB}(\textit{v}_{
u}/\textit{c})\cdot\textit{t}_{1/2}$

to minimize contamination from β decay background

Isotope	Decay	$Q_{\beta} \; (\text{keV})$	Half-life (s)	$\sigma_{\rm NCB}(v_{\nu}/c) \ (10^{-41} \ {\rm cm}^2)$
$^{3}\mathrm{H}$	β^{-}	18.591	3.8878×10^8	7.84×10^{-4}
⁶³ Ni	β^{-}	66.945	3.1588×10^9	1.38×10^{-6}
$^{93}\mathrm{Zr}$	β^{-}	60.63	4.952×10^{13}	2.39×10^{-10}
$^{106}\mathrm{Ru}$	β^{-}	39.4	3.2278×10^7	5.88×10^{-4}
$^{107}\mathrm{Pd}$	β^{-}	33	2.0512×10^{14}	2.58×10^{-10}
$^{187}\mathrm{Re}$	β^{-}	2.64	1.3727×10^{18}	4.32×10^{-11}
$^{11}\mathrm{C}$	β^+	960.2	1.226×10^3	4.66×10^{-3}
$^{13}\mathrm{N}$	β^+	1198.5	$5.99 imes 10^2$	$5.3 imes 10^{-3}$
$^{15}\mathrm{O}$	β^+	1732	1.224×10^2	9.75×10^{-3}
$^{18}\mathrm{F}$	β^+	633.5	6.809×10^3	2.63×10^{-3}
22 Na	β^+	545.6	$9.07 imes 10^7$	3.04×10^{-7}
$^{45}\mathrm{Ti}$	β^+	1040.4	1.307×10^4	3.87×10^{-4}

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³H better because the cross section (\rightarrow event rate) is higher

β and Neutrino Capture spectra

[PTOLEMY, JCAP 07 (2019) 047]

$$\left(\frac{d\widetilde{\Gamma}_{\text{CNB}}}{dE_e}(E_e) = \frac{1}{\sqrt{2\pi}\sigma} \sum_{i=1}^{N_{\nu}} \overline{\sigma} N_T |U_{ei}|^2 n_0 f_c(m_i) \times e^{-\frac{[E_e - (E_{\text{end}} + m_i + m_{\text{lightest}})]^2}{2\sigma^2}}\right)$$

$$\frac{d\Gamma_{\beta}}{dE_{e}} = \frac{\bar{\sigma}}{\pi^{2}} N_{T} \sum_{i=1}^{N_{\nu}} |U_{ei}|^{2} H(E_{e}, m_{i})$$

$$\left[\frac{d\widetilde{\Gamma}_{\beta}}{dE_{e}}(E_{e}) = \frac{1}{\sqrt{2\pi}\sigma} \int_{-\infty}^{+\infty} dx \, \frac{d\Gamma_{\beta}}{dE_{e}}(x) \, \exp\left[-\frac{(E_{e}-x)^{2}}{2\sigma^{2}}\right]\right]$$

β and Neutrino Capture spectra

[PTOLEMY, JCAP 07 (2019) 047]



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$$\begin{split} \hline & \Gamma_{\text{CNB}} = \sum_{i=1}^{3} |U_{ei}|^2 [n_i(\nu_{h_R}) + n_i(\nu_{h_L})] \, N_T \, \bar{\sigma} \\ & N_T \text{ number of }^{3}\text{H nuclei in a sample of mass } M_T \quad \bar{\sigma} \simeq 3.834 \times 10^{-45} \text{ cm}^2 \quad n_i \text{ number density of neutrino } i \\ & \text{(without clustering)} \end{split}$$





[PTOLEMY Lol, arxiv:1808.01892]



[Courtesy A. Esposito]

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[PTOLEMY Lol, arxiv:1808.01892]



[Courtesy V. Tozzini]

[Courtesy A. Esposito]

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[PTOLEMY Lol, arxiv:1808.01892]



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[PTOLEMY Lol, arxiv:1808.01892]



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[PTOLEMY Lol, arxiv:1808.01892]



[Courtesy A. Esposito]

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Detection of the relic neutrinos

[PTOLEMY, JCAP 07 (2019) 047]

using the definition:

$$N_{ ext{th}}^{i}(m{ heta}) = A_{eta}N_{eta}^{i}(\hat{E}_{end} + \Delta E_{end}, m_{i}, U) + m{A}_{ ext{CNB}}N_{ ext{CNB}}^{i}(\hat{E}_{end} + \Delta E_{end}, m_{i}, U) + N_{b}$$

if $m{A}_{
m CNB} > 0$ at $N\sigma$, direct detection of CNB accomplished at $N\sigma$



Quantum uncertainty and PTOLEMY [PTOLEMY, PRD 106 (2022)]

Tritium atoms will be attached to graphene sheets

Quantum uncertainty on electron energy due to condensed matter state



Binding potential depends on distance graphene-tritium and graphene sheet configuration

> Concave sites behave differently than convex ones

Hydrogen coverage (amount of *H* atoms in the graphene sheet) is also important Quantum uncertainty and PTOLEMY [PTOLEMY, PRD 106 (2022)]

Tritium atoms will be attached to graphene sheets

Quantum uncertainty on electron energy due to condensed matter state



Nanotube configurations have flat potential parallel to nanotube axis

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Quantum uncertainty and PTOLEMY [PTOLEMY, PRD 106 (2022)]

Tritium atoms will be attached to graphene sheets

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Graphene configuration can make observation range from completely impossible or suppressed but possible

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What do we learn from relic neutrinos?



What do we learn from relic neutrinos?



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