

Neutrino frontiers 2024 - focus week

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Neutrinos in very low reheating scenarios

Work done in collaboration with

T. Brinckmann (UniFE), S. Gariazzo (UniTO),  
M. Lattanzi (INFN-FE), S. Pastor (IFIC), O. Pisanti (UniNA)

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# Updated constraints on very low reheating scenarios

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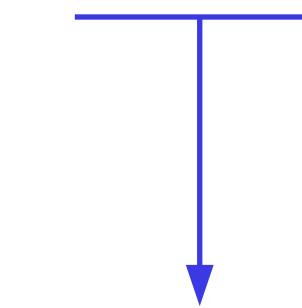
# Models of reheating

- In inflation paradigm, a final reheating phase is needed to reconcile with the standard FLRW radiation dominated Universe

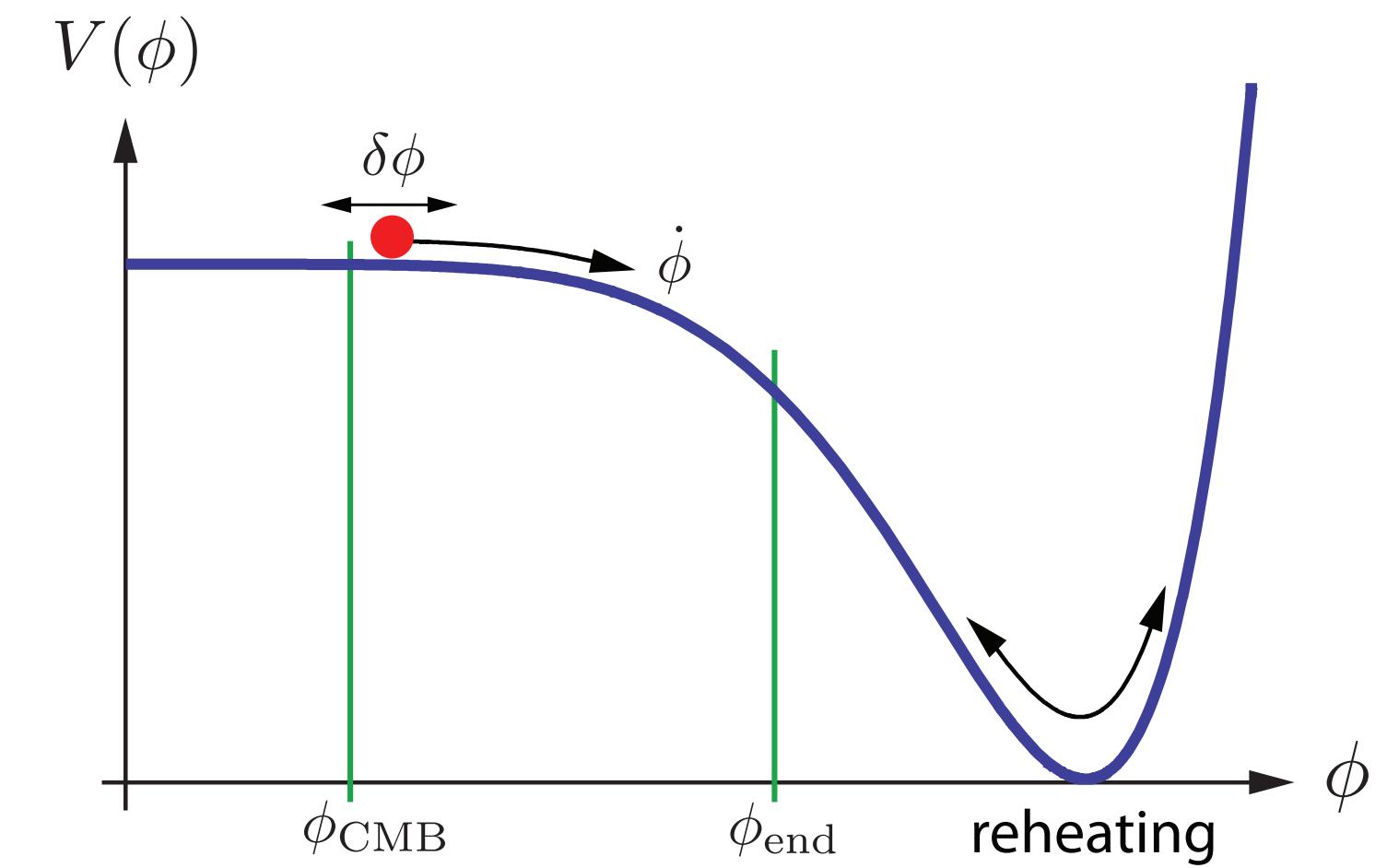
$$\frac{d\rho_\phi}{dt} + (3H + \Gamma_\phi) \rho_\phi = 0$$

- What is the reheating temperature?

$$\Gamma_\phi \equiv 3\cancel{H}(T_{\text{RH}}) \quad \Rightarrow \quad T_{\text{RH}} \simeq 0.7 \left( \frac{\Gamma_\phi}{\text{s}^{-1}} \right)^{1/2} \text{ MeV}$$



$$\cancel{H}(T_{\text{RH}}) = \sqrt{\frac{8\pi}{3m_{\text{pl}}^2} \rho_{\text{rad}}(T_{\text{RH}})} = \sqrt{\frac{8\pi}{90} g_*(T_{\text{RH}})} \frac{T_{\text{RH}}^2}{m_{\text{pl}}}$$



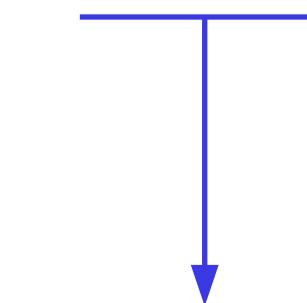
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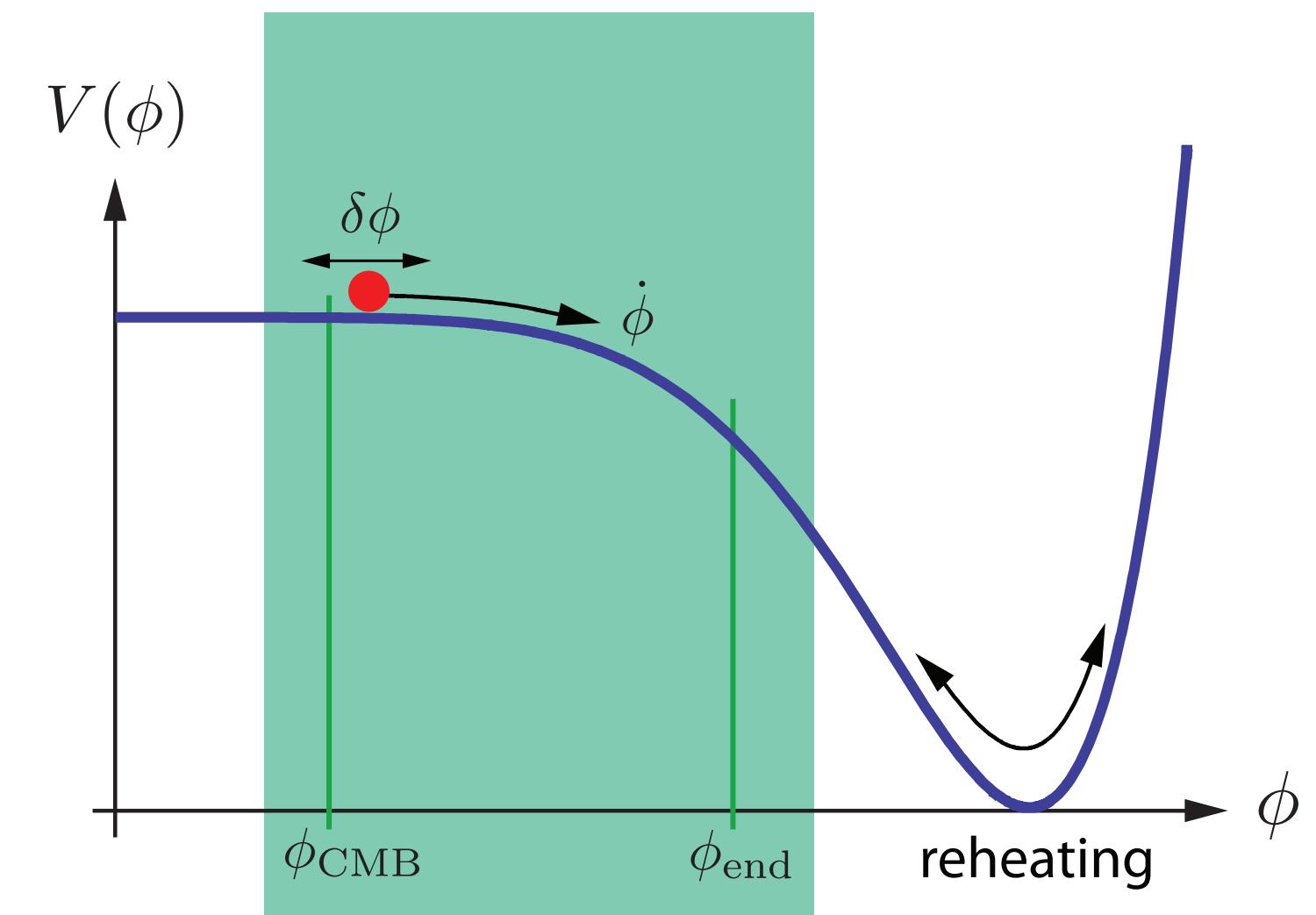
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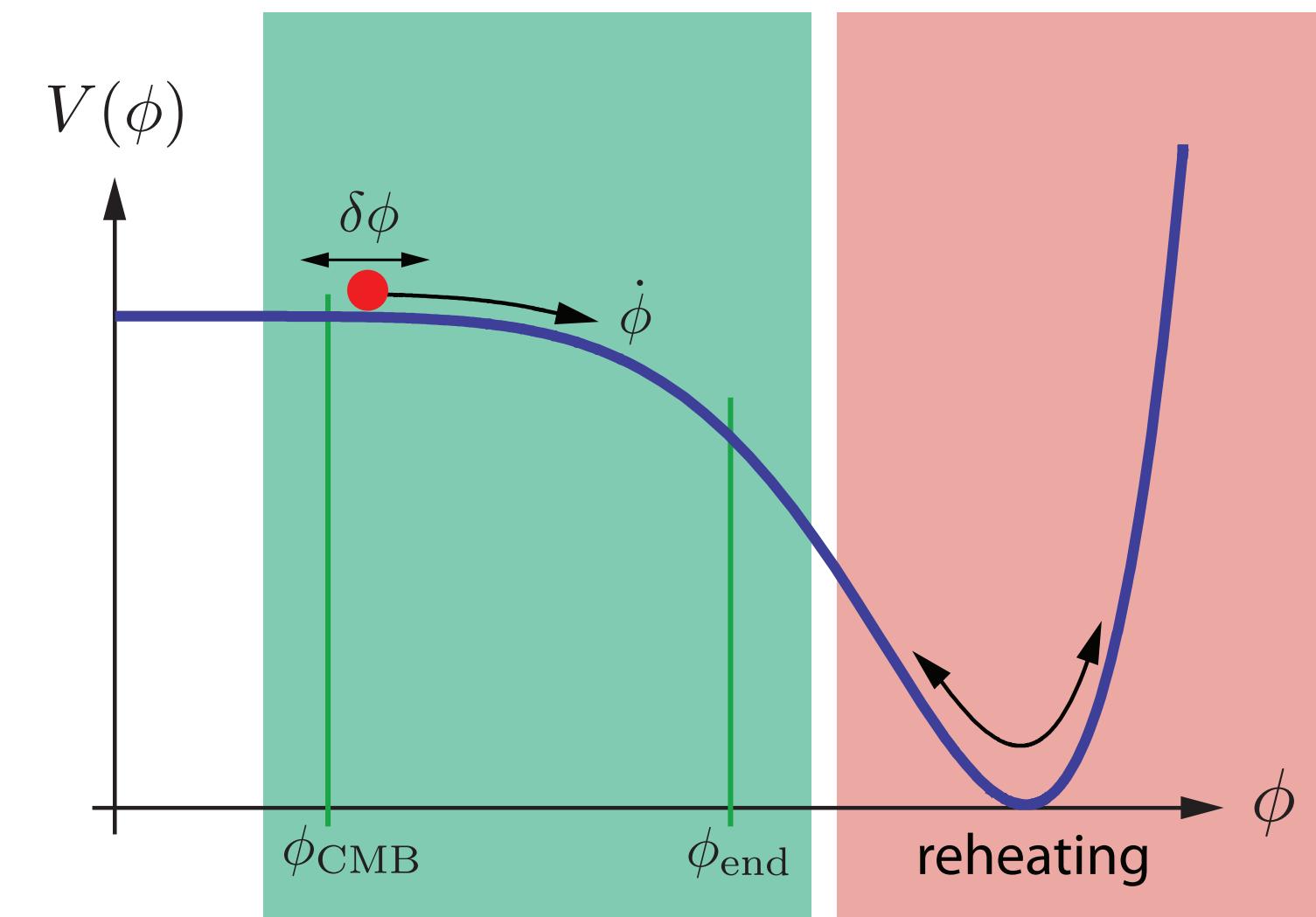
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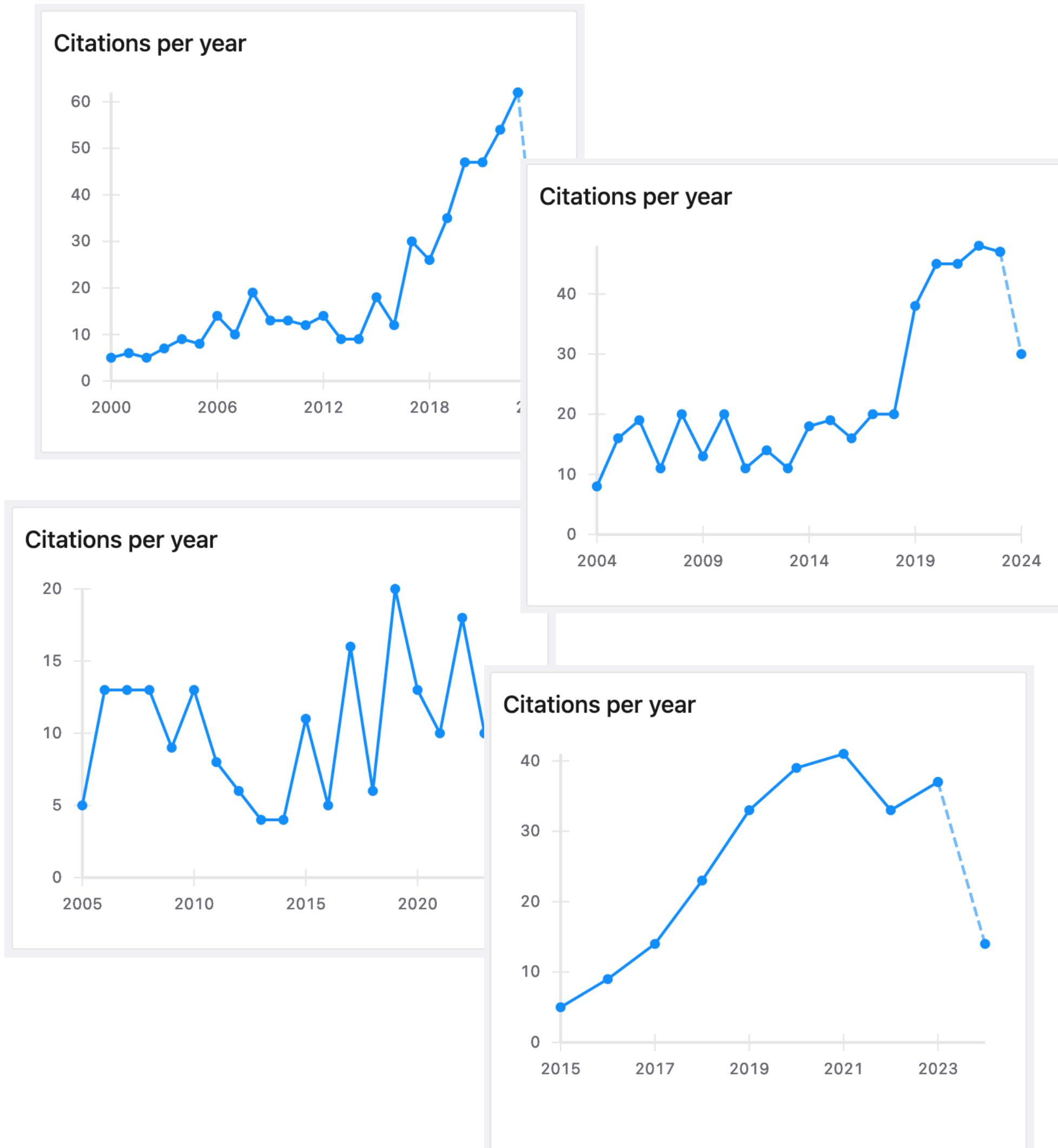
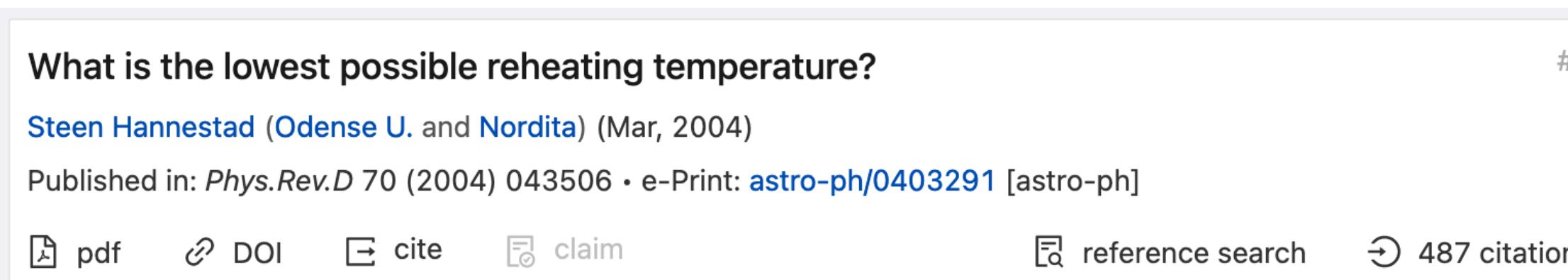
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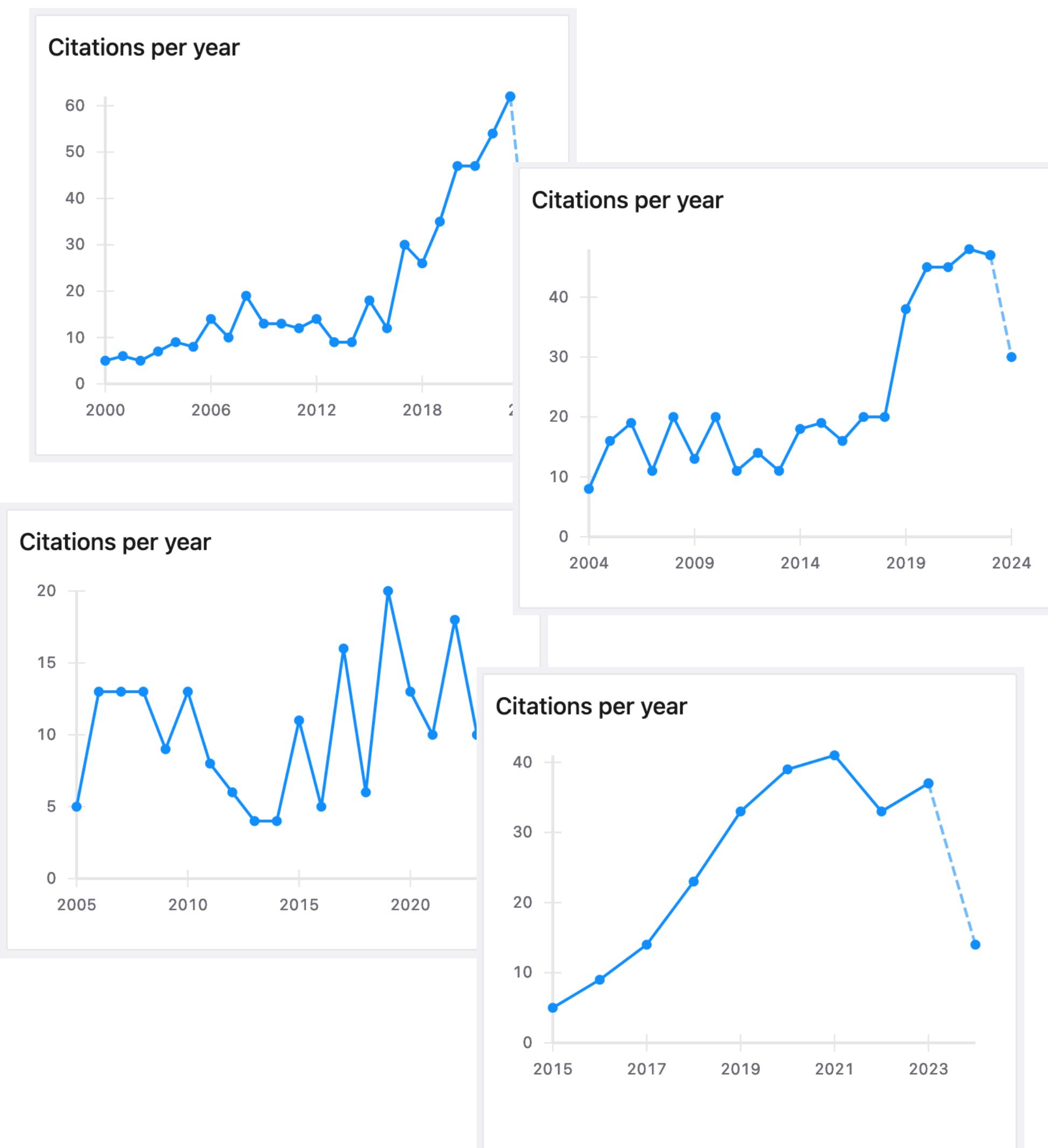
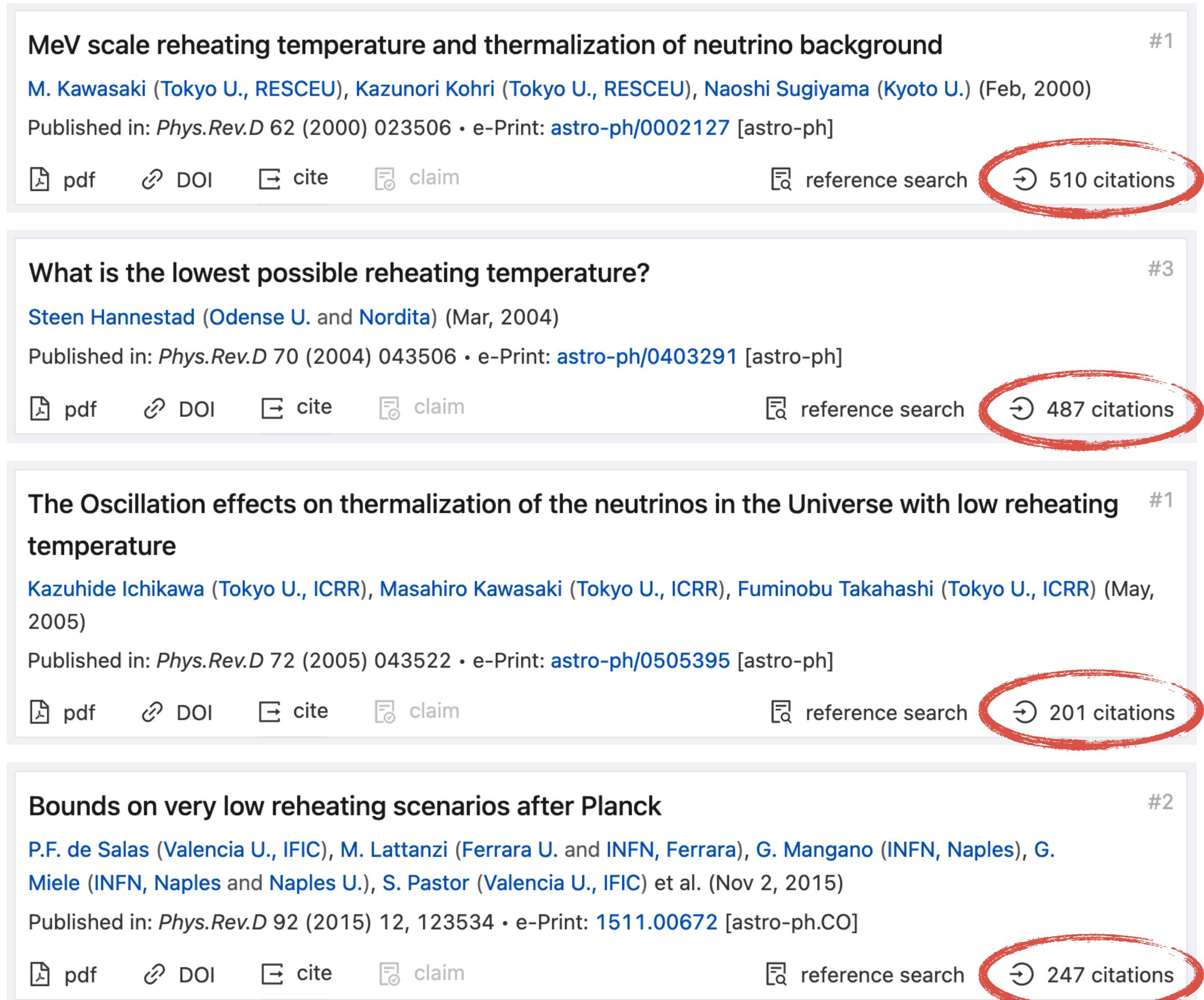


During **reheating** the inflaton decays into Standard Model degrees of freedom

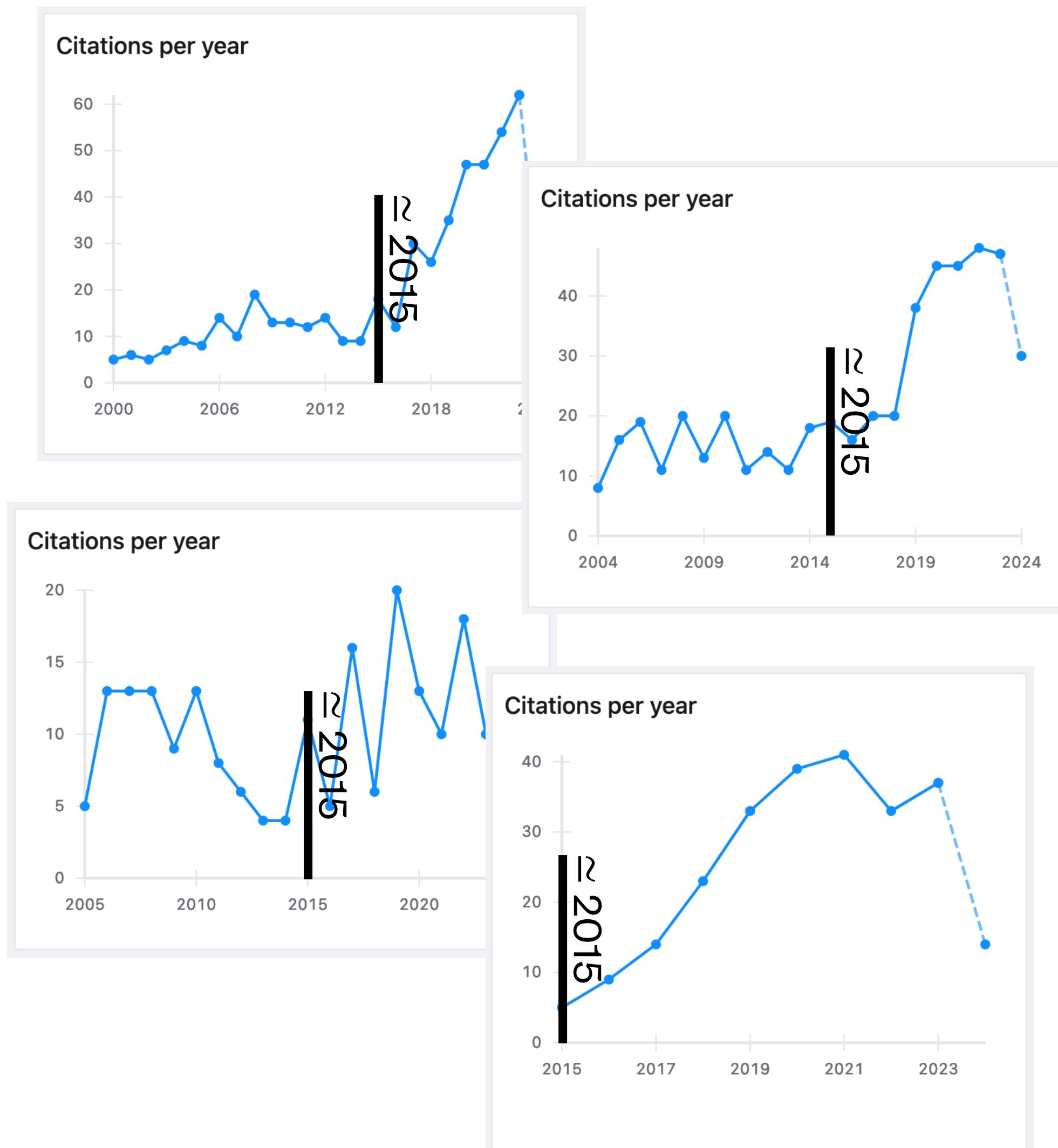
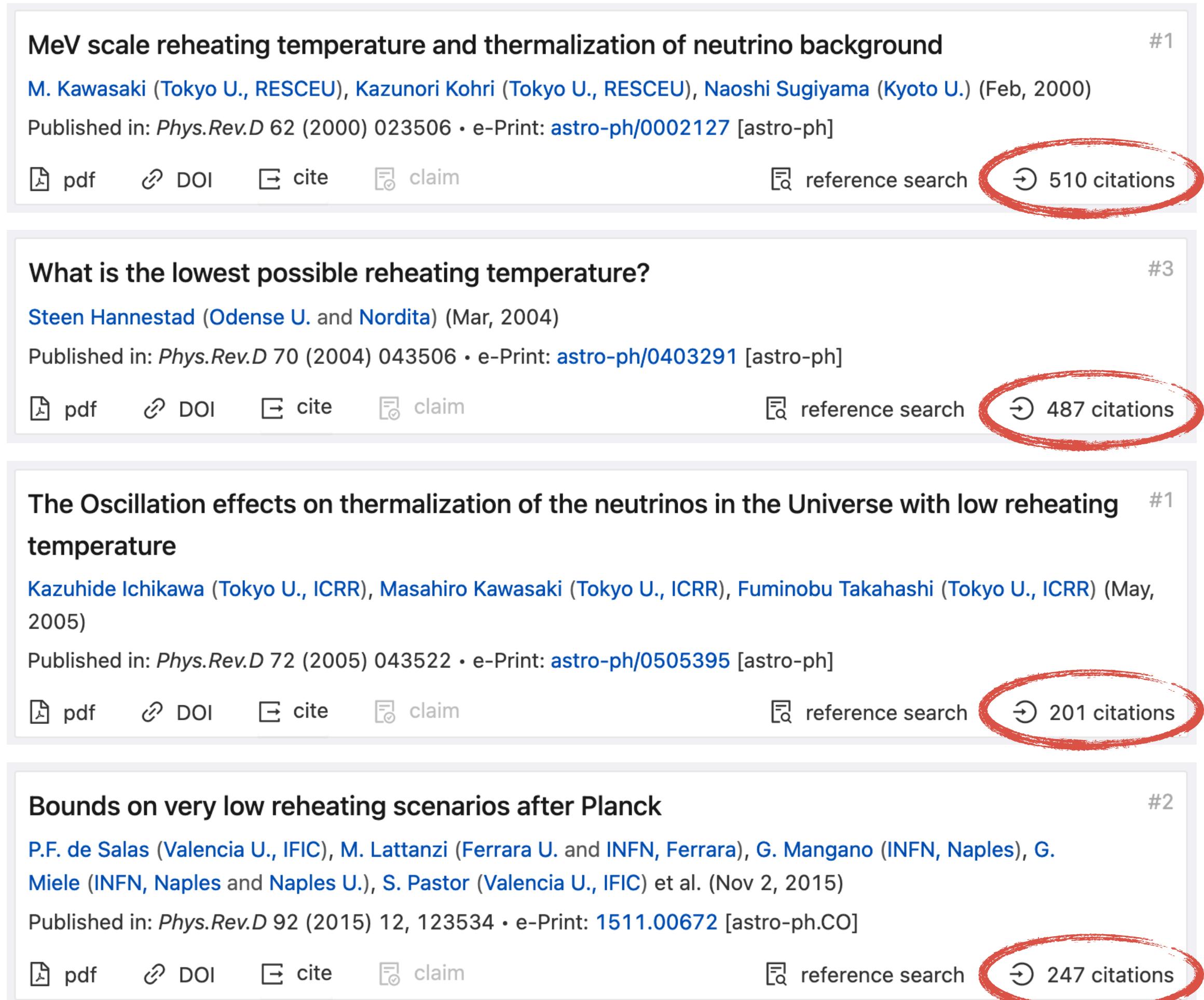
# Interest in low reheating



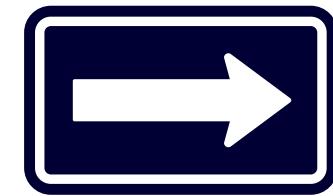
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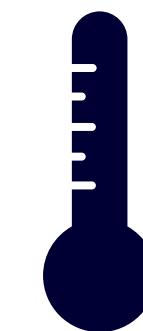


# Assumptions and remarks



Photons, electrons, and other SM particles are populated directly by the **decay of the scalar**

Neutrinos are populated by weak  
**interactions with leptons**



We define a **very low reheating** when it occurs at temperatures  $T_{\text{RH}} \lesssim 20 \text{ MeV}$

**Oscillations** start to be affected at  $T_{\text{RH}} \lesssim 8 \text{ MeV}$



# Neutrino production - I

[See S. Gariazzo's and  
S. Pastor's talks]

- Evolution of three flavour neutrino momentum distributions with oscillations and QED corrections

$$\frac{d\varrho(y, x)}{dx} = \sqrt{\frac{3m_{\text{pl}}^2}{8\pi\rho}} \left\{ -i\frac{x^2}{m_e^3} \left[ \frac{\mathbb{M}_F}{2y} - \frac{2\sqrt{2}G_F y m_e^6}{x^6} \left( \frac{\mathbb{E}_\ell + \mathbb{P}_\ell}{m_W^2} + \frac{4}{3} \frac{\mathbb{E}_\nu}{m_Z^2} \right), \varrho \right] + \frac{m_e^3}{x^4} \mathcal{I}(\varrho) \right\}$$

**NB:** everything expressed  
in terms of comoving variables

$$x \equiv m_e a \quad y \equiv p a \quad z \equiv T_\gamma a$$

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**Density matrix:**

transition probability between  
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$$\varrho(p, t) = \begin{pmatrix} f_{\nu_e} & \varrho_{e\mu} & \varrho_{e\tau} \\ \varrho_{\mu e} & f_{\nu_e} & \varrho_{\mu\tau} \\ \varrho_{\tau e} & \varrho_{\tau\mu} & f_{\nu_e} \end{pmatrix}$$

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**Vacuum oscillations:** quantum effect  
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$$\mathbb{M}_F = U \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} U^\dagger$$

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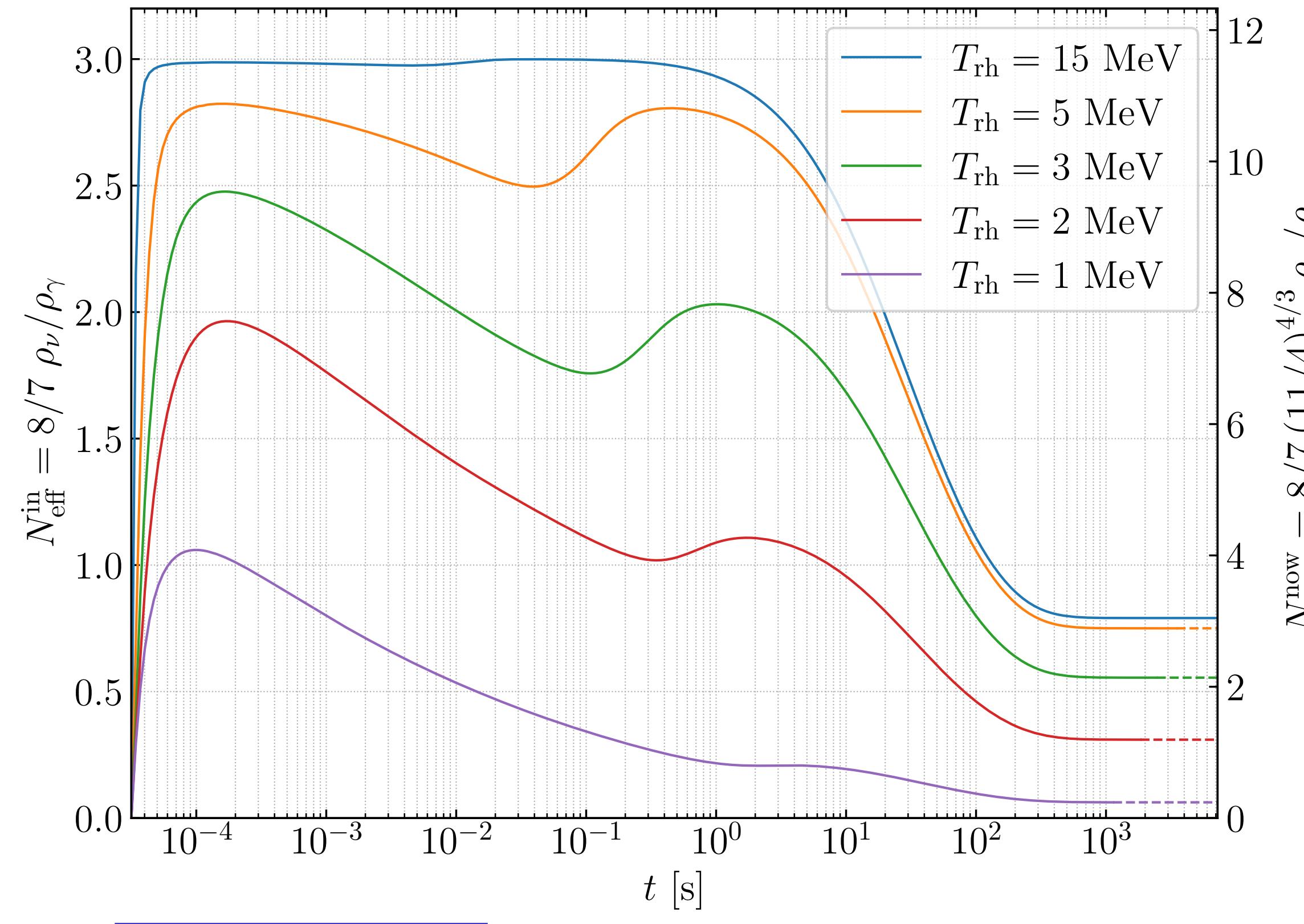
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**Collision integrals:**  
effect of neutrino collisions with exchange of momenta

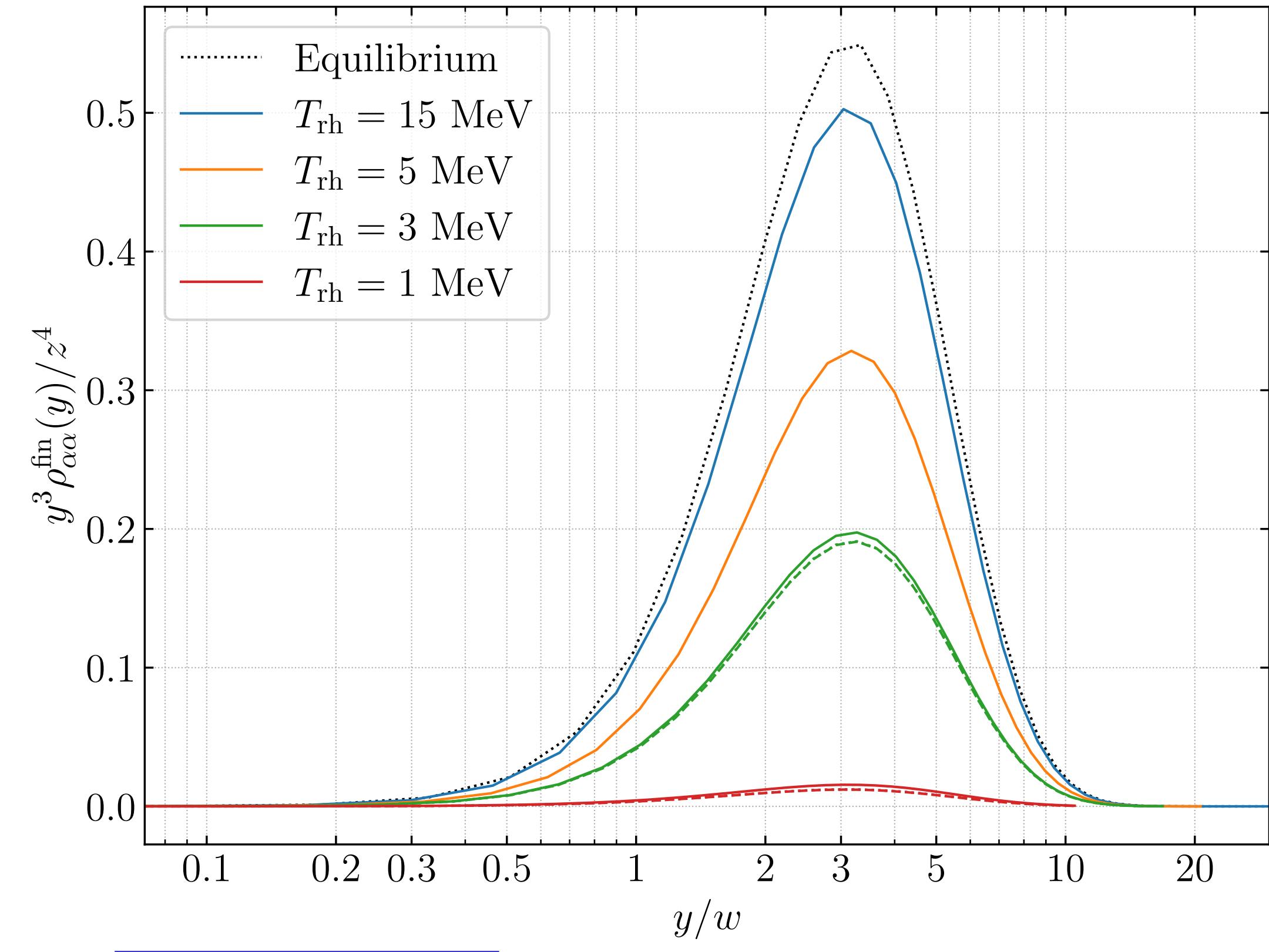
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# Neutrino production - II



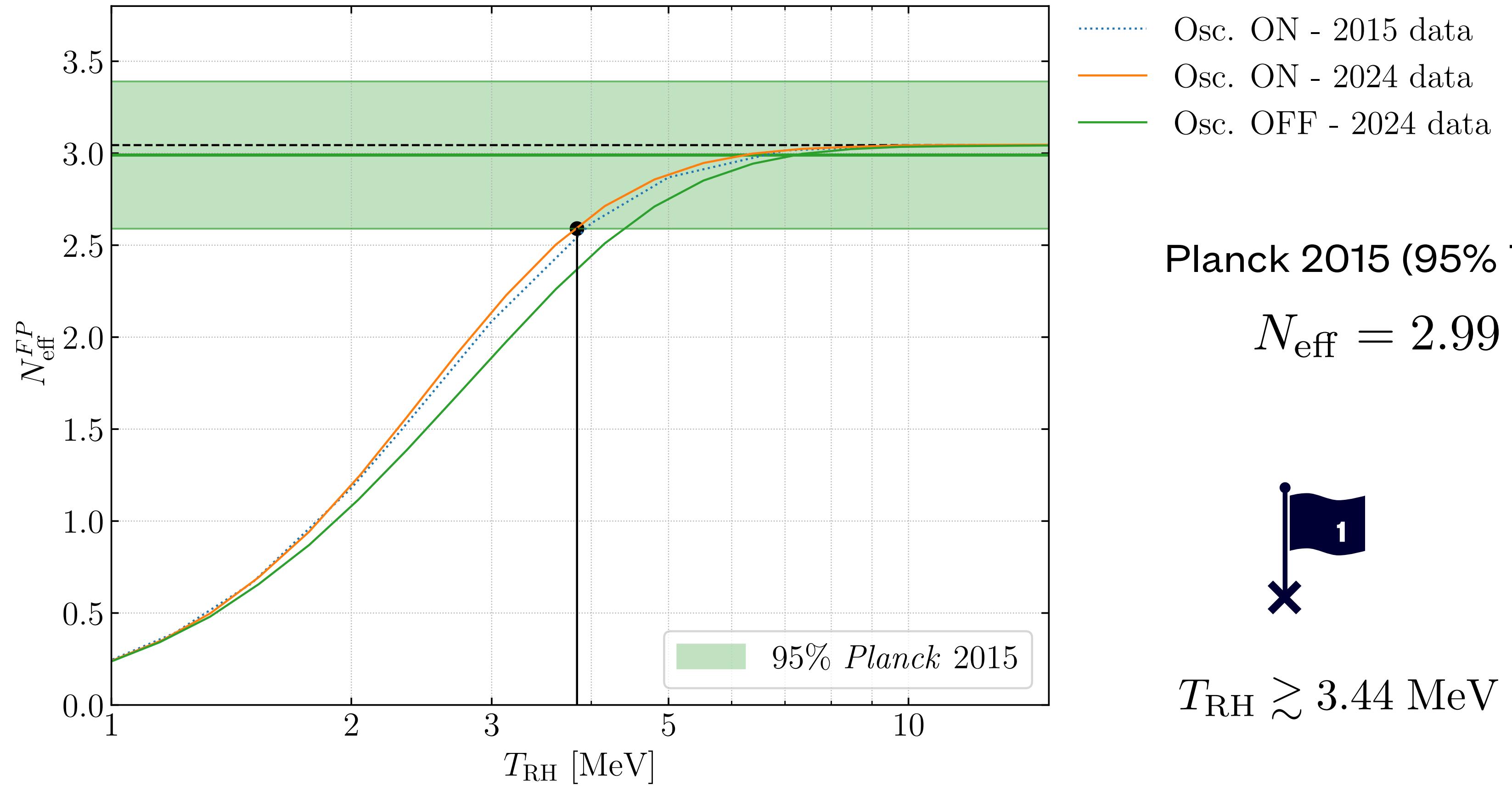
Time evolution of the ratio of energy densities of neutrinos and photons.



Final differential spectra of neutrino energies as a function of the comoving momentum.

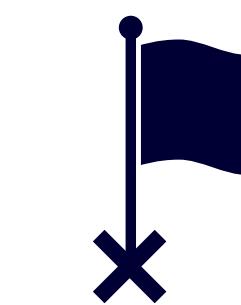
# Neutrino production - III

MODIFIED VERSION OF  
**FORTEPIANO** CODE



Planck 2015 (95% TT,TE,EE+lowP):

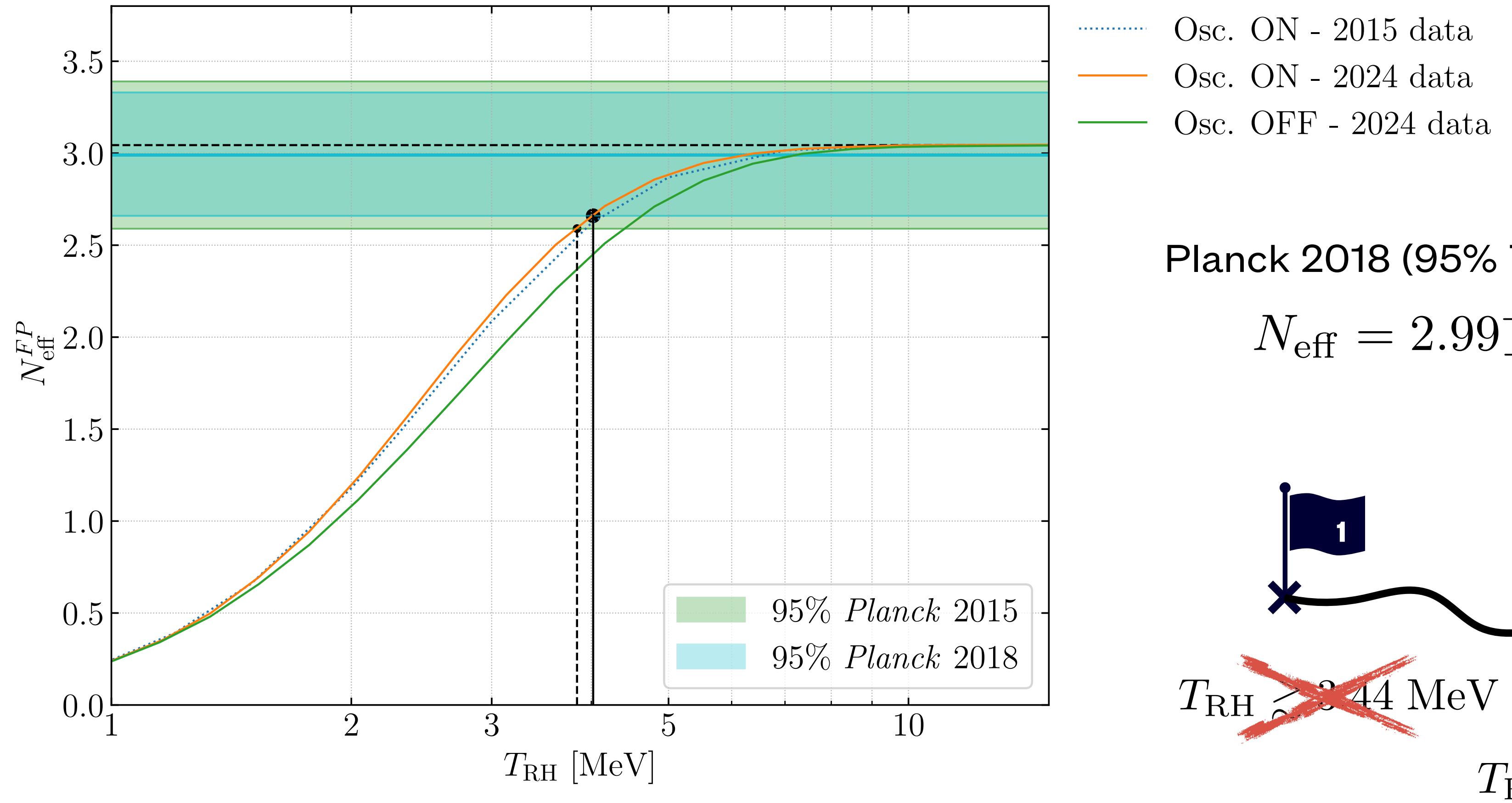
$$N_{\text{eff}} = 2.99 \pm 0.4$$



$$T_{\text{RH}} \gtrsim 3.44 \text{ MeV}$$

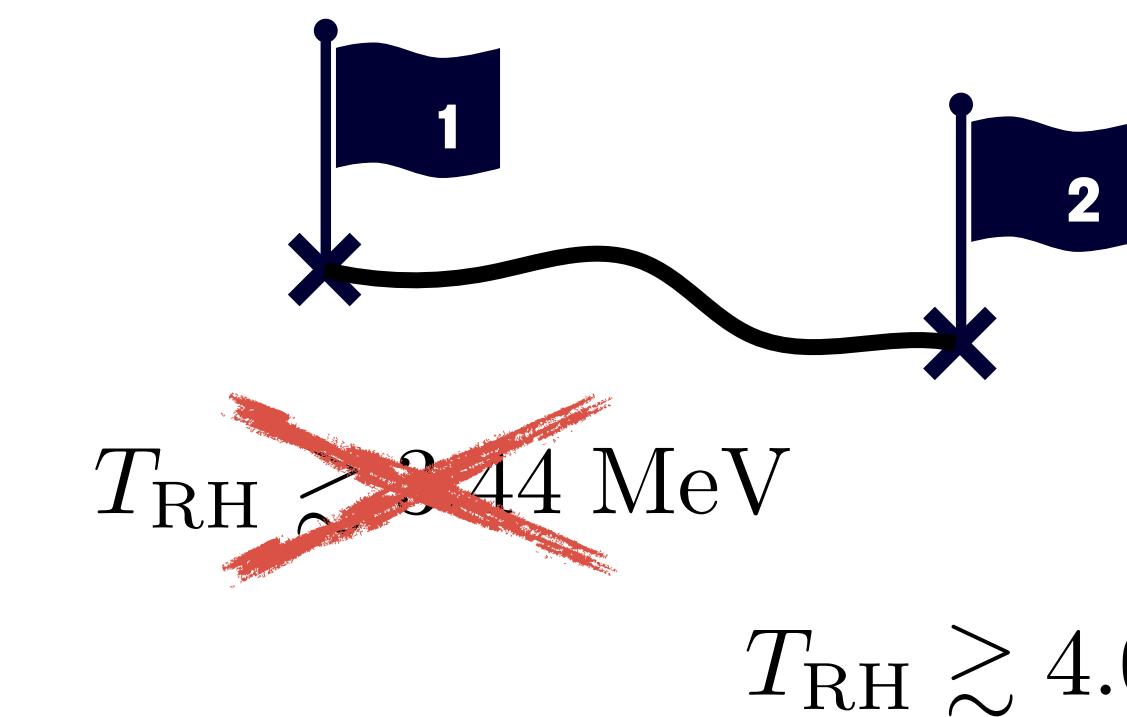
# Neutrino production - III

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Planck 2018 (95% TT,TE,EE+lowE+lensing+BAO):

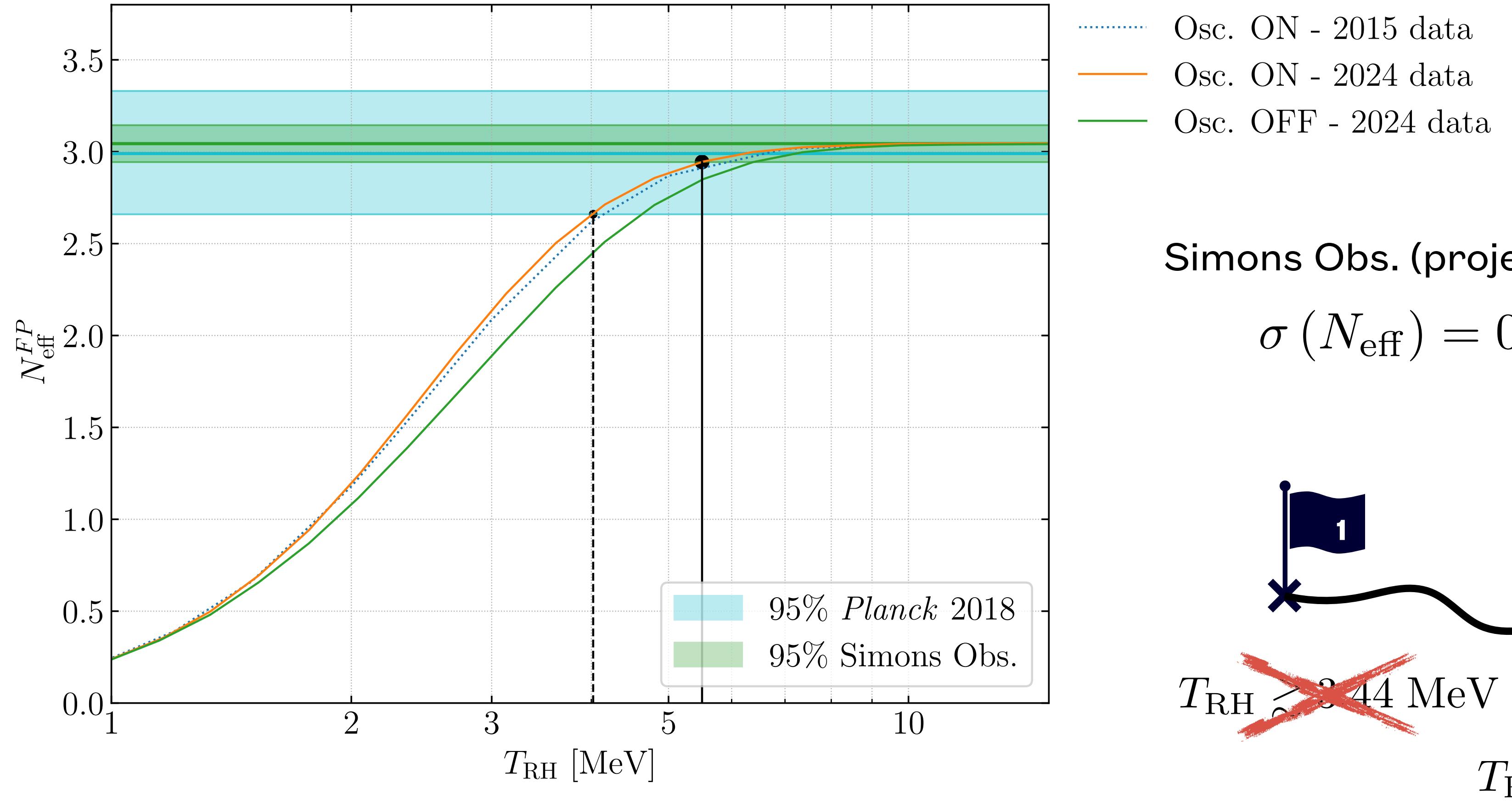
$$N_{\text{eff}} = 2.99^{+0.34}_{-0.33}$$



$$T_{\text{RH}} \gtrsim 4.02 \text{ MeV}$$

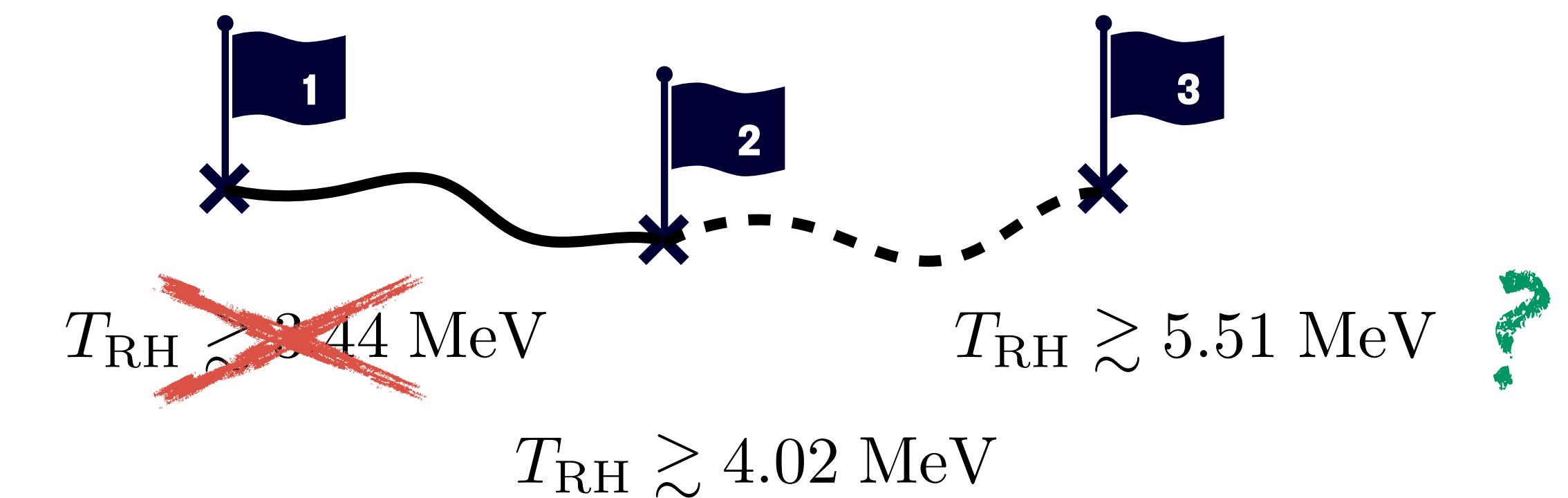
# Neutrino production - III

MODIFIED VERSION OF  
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Simons Obs. (projected sensitivity):

$$\sigma(N_{\text{eff}}) = 0.050$$

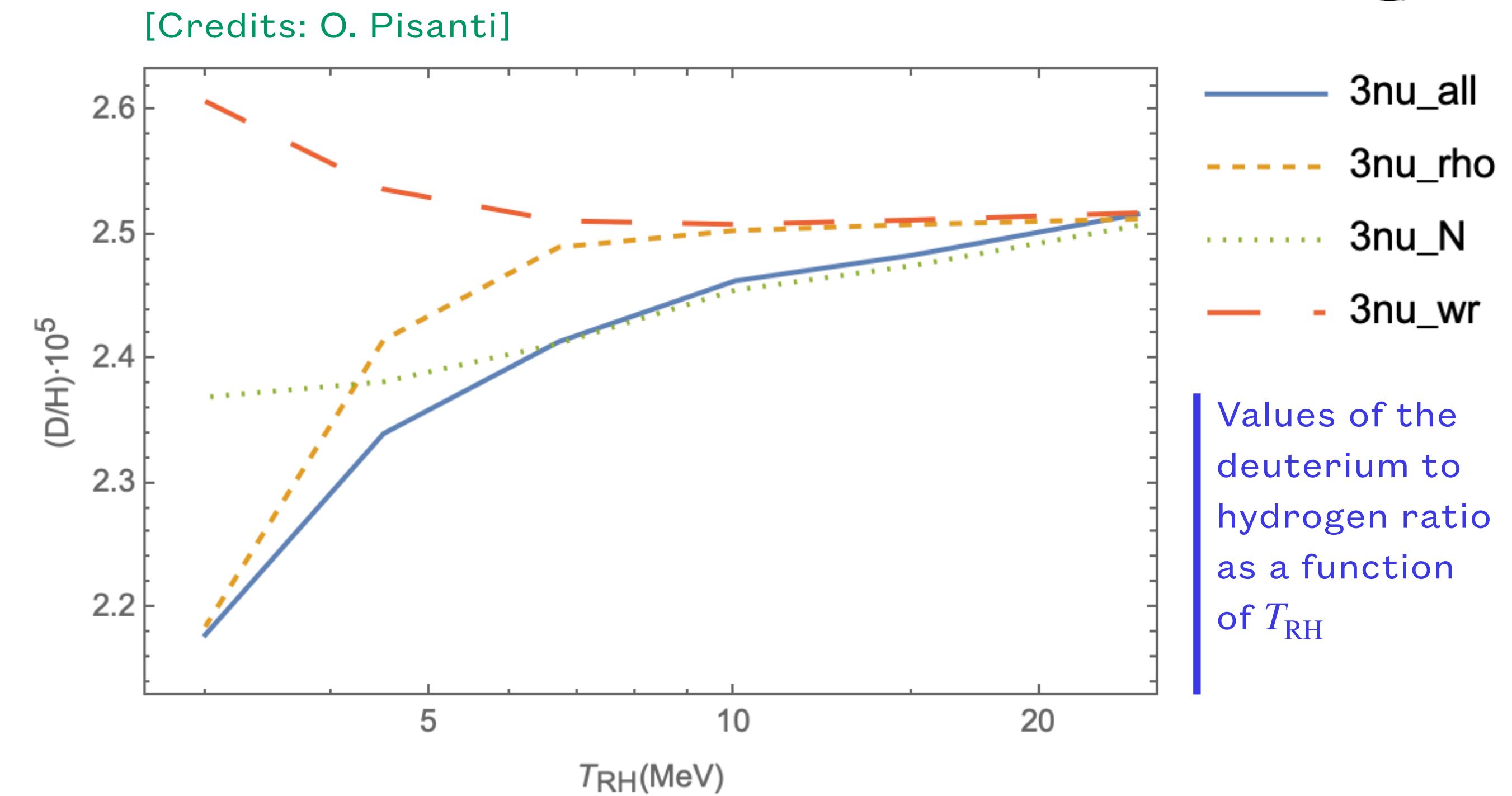


# Probes of low reheating: BBN

MODIFIED VERSION OF  
PARTHENOPE CODE

- The total neutrino energy density contributes to the radiation energy density which leads to the **Hubble expansion rate**;
- Electron neutrinos distribution function enters the charged current weak rates, which govern the **neutron-proton chemical equilibrium**;
- The total neutrino energy density also appears in the **continuity equation**, whose is conventionally handled by defining

$$\mathcal{N} = \frac{1}{z^4} \left( x \frac{d}{dx} \bar{\rho}_\nu \right)$$



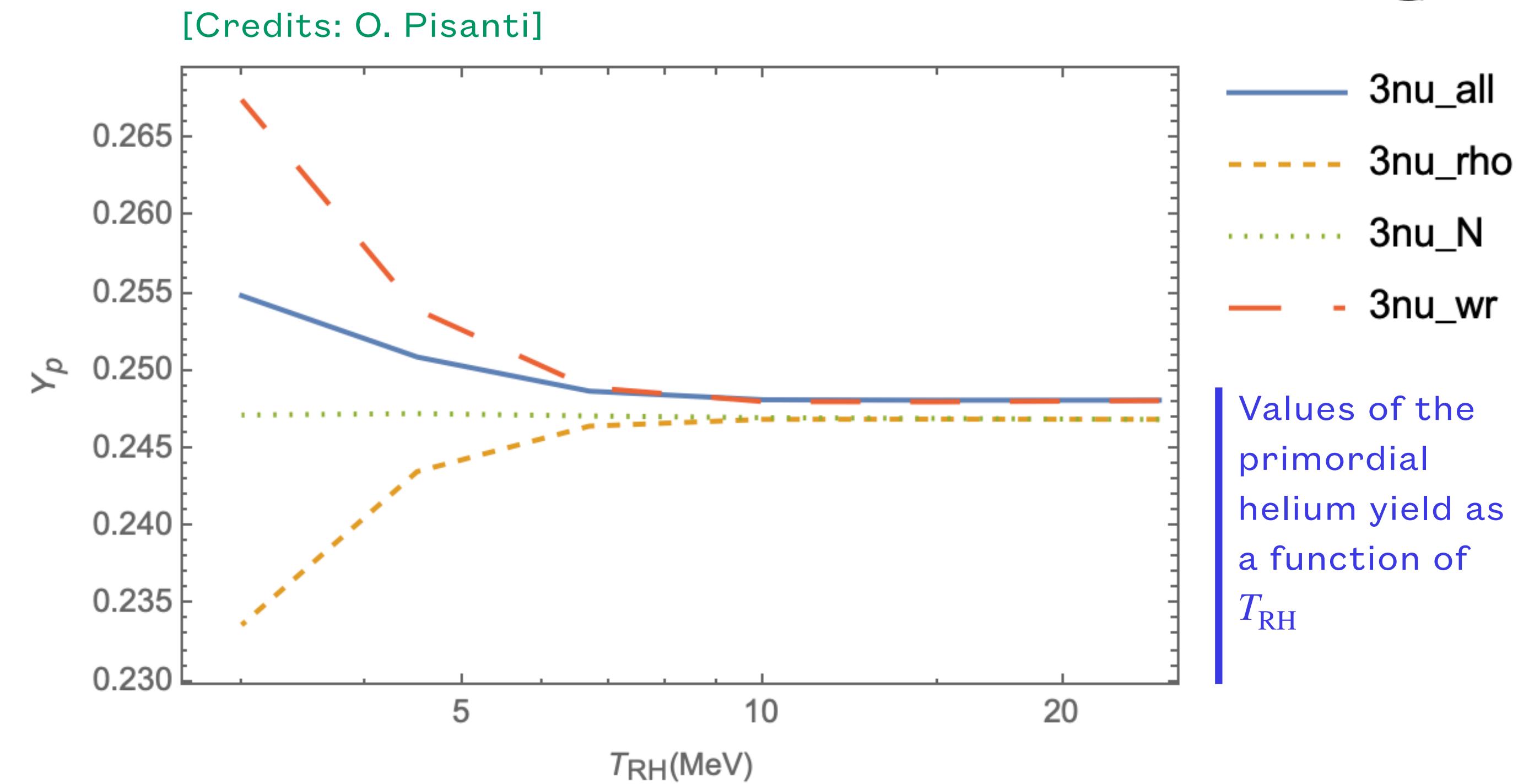
$$(\chi^2_{^4\text{He}} \chi^2_{^2\text{H}}) (T_{RH}) \leq 4 \quad \Rightarrow \quad T_{RH} \geq 4.1 \text{ MeV}$$

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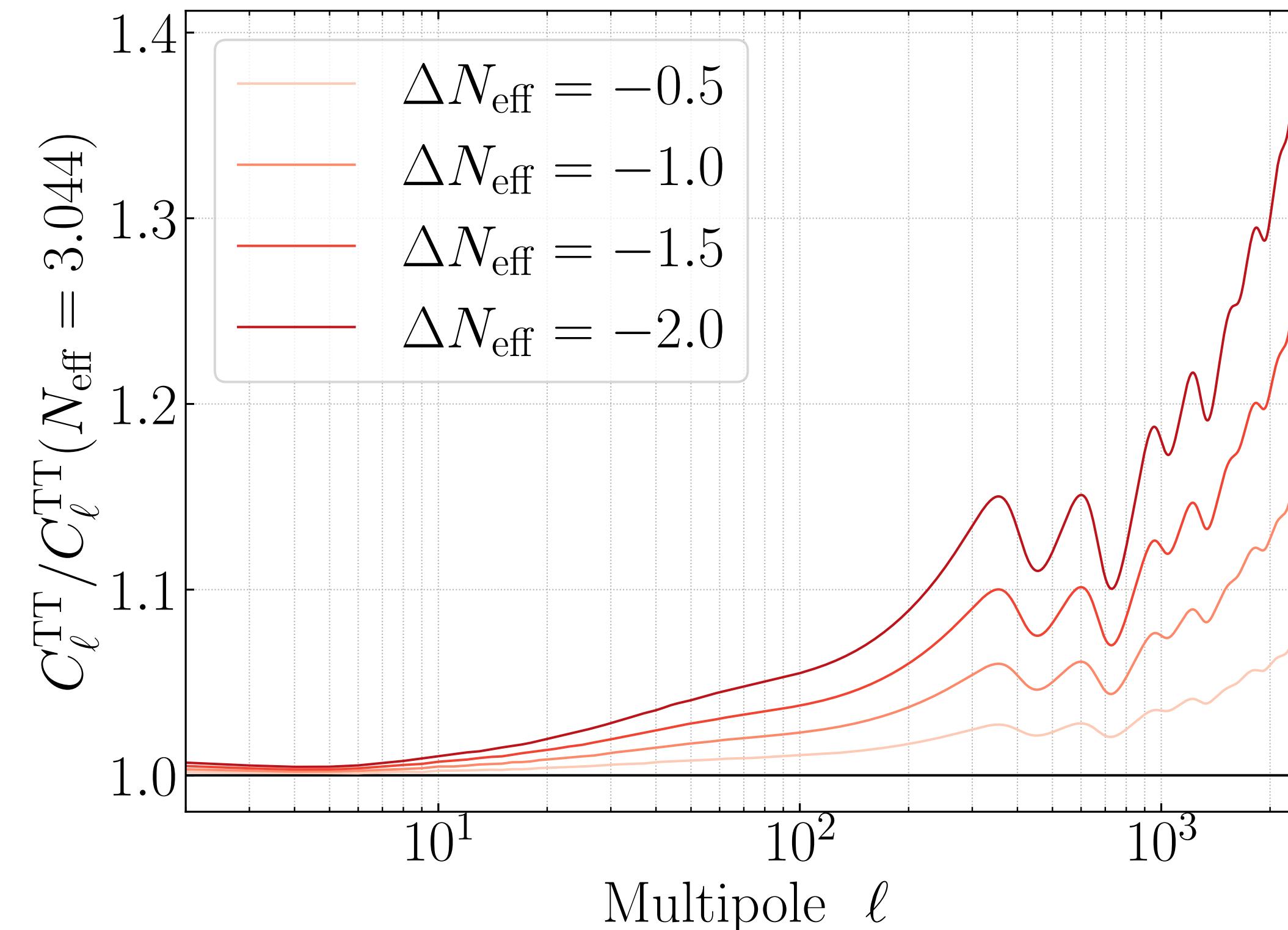
# Probes of low reheating: CMB

MODIFIED VERSION OF  
MONTEPYTHON SAMPLER

- At the redshift of interest for the calculation of CMB anisotropies neutrino PSDs are evolving self-similarly, being only redshifted by the expansion of the Universe;
- Cosmological perturbation equations are sensitive to mass stases PSDs

$$f_{\nu_i}(y) = \sum_{\alpha} |U_{\alpha i}|^2 f_{\nu_{\alpha}}(y)$$

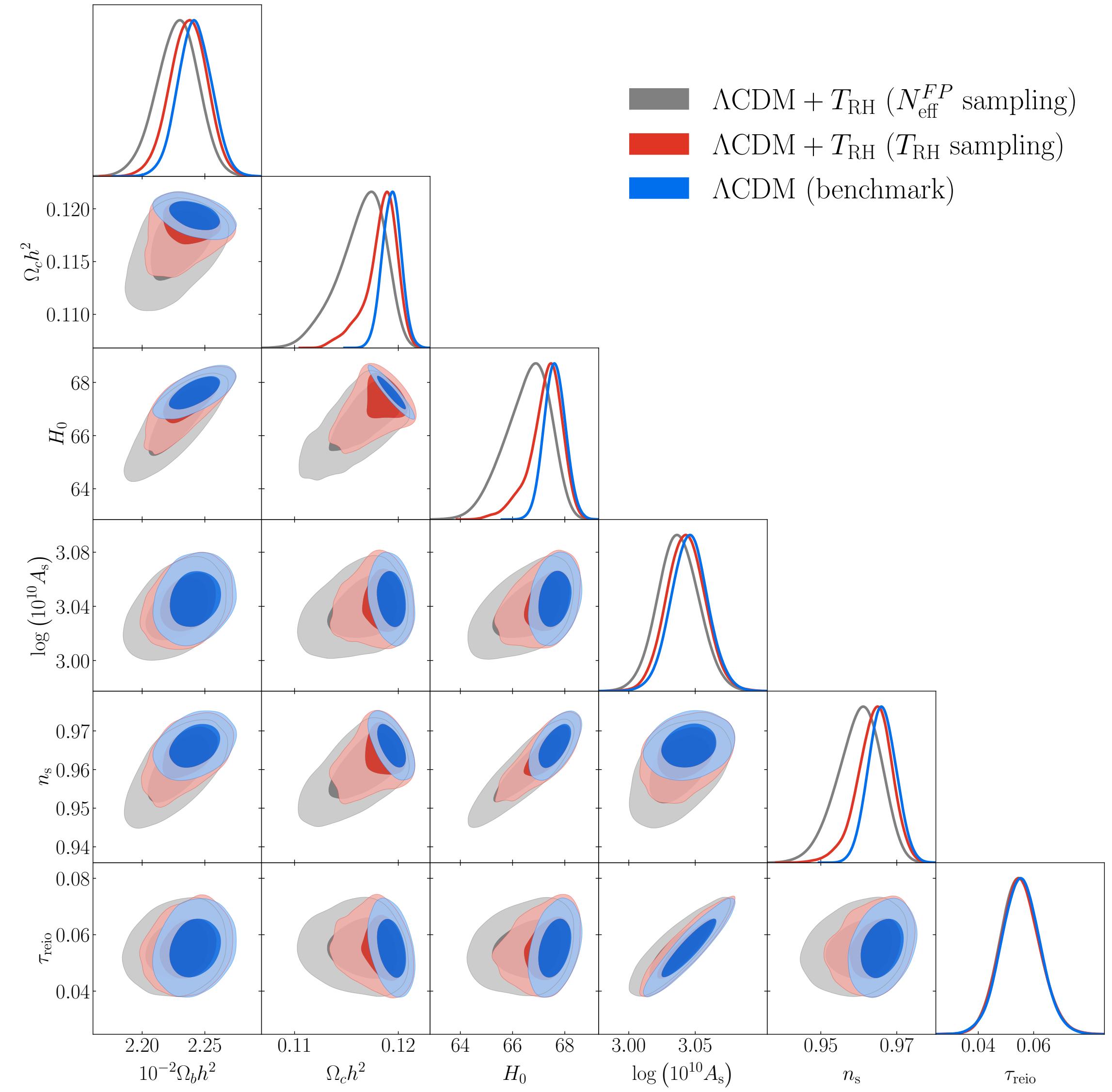
- CMB anisotropies spectrum is sensitive to the primordial helium abundance through its influence on the recombination history.



# How to sample $T_{\text{RH}}$ ?

- **$T_{\text{RH}}$  sampling:** employed in previous works, poor sampling of low reheating temperatures region, direct interpretation of the physical results;
- **$N_{\text{eff}}^{FP}$  sampling:** most direct relationship with the data, uniform sampling of all parameter space, difficult interpretation of the results.

	$\Lambda\text{CDM} + T_{\text{RH}}$ ( $N_{\text{eff}}^{FP}$ sampling)	$\Lambda\text{CDM} + T_{\text{RH}}$ ( $T_{\text{RH}}$ sampling)	$\Lambda\text{CDM}$ ( $T_{\text{RH}} = 25$ MeV)	$\Lambda\text{CDM}$ (Planck 2018)
Parameter	68% limits	68% limits	68% limits	68% limits
$\Omega_b h^2$	$0.02228^{+0.00018}_{-0.00015}$	$0.02237 \pm 0.00015$	$0.02242 \pm 0.00013$	$0.02242 \pm 0.00014$
$\Omega_c h^2$	$0.1164^{+0.0027}_{-0.0017}$	$0.1183^{+0.0018}_{-0.00090}$	$0.11936 \pm 0.00092$	$0.11933 \pm 0.00091$
$\log(10^{10} A_s)$	$3.037 \pm 0.016$	$3.043 \pm 0.015$	$3.046 \pm 0.014$	$3.047 \pm 0.014$
$n_s$	$0.9600^{+0.0064}_{-0.0050}$	$0.9640^{+0.0049}_{-0.0039}$	$0.9662 \pm 0.0037$	$0.9665 \pm 0.0038$
$\tau_{\text{reio}}$	$0.0550^{+0.0067}_{-0.0074}$	$0.0552 \pm 0.0072$	$0.0553 \pm 0.0070$	$0.0561 \pm 0.0071$
$H_0$	$66.6^{+1.0}_{-0.68}$	$67.26^{+0.73}_{-0.42}$	$67.62 \pm 0.41$	$67.66 \pm 0.42$



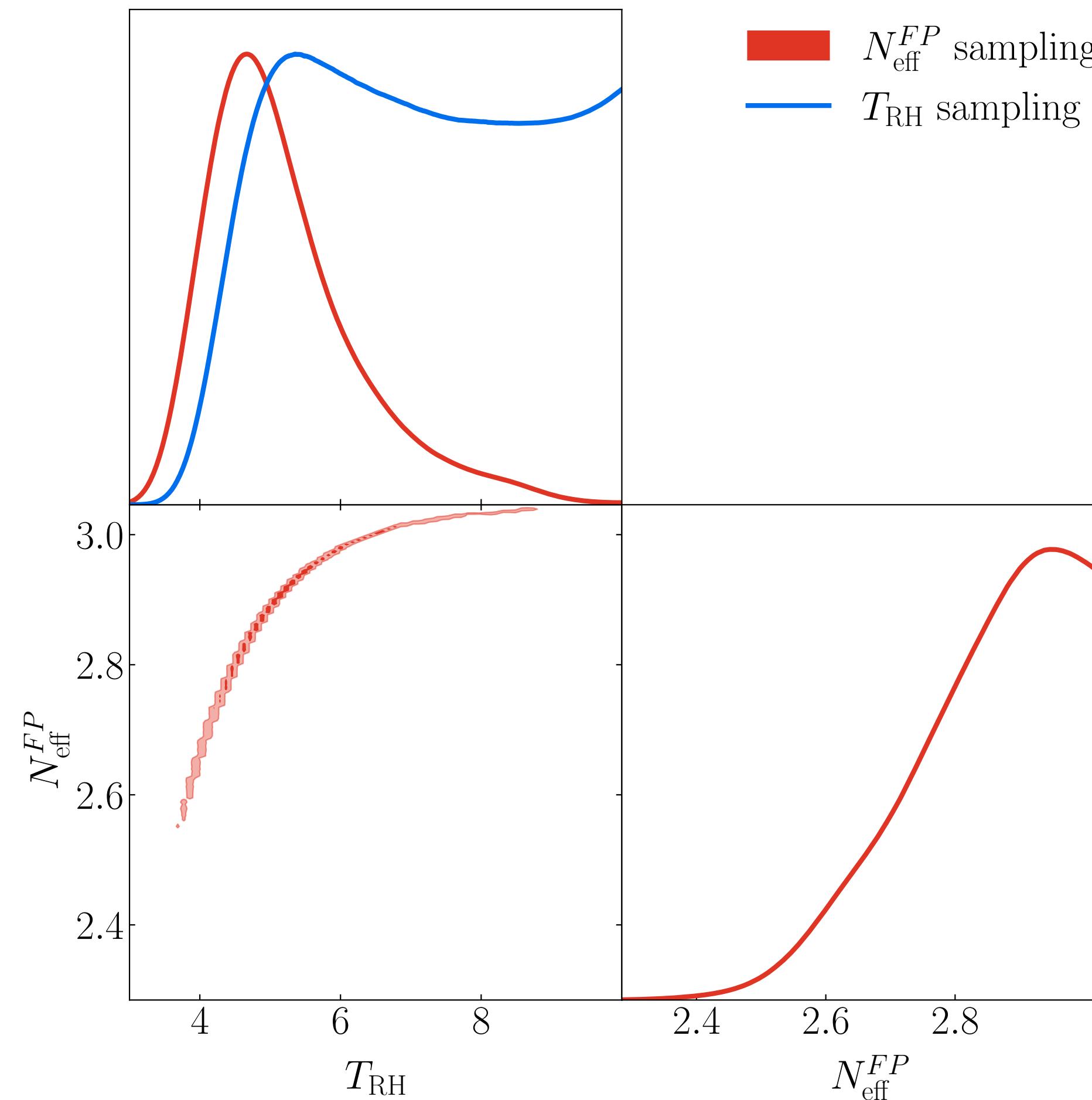
# Bounds on $T_{\text{RH}}$ [MeV]

- $T_{\text{RH}}$  **sampling**: employed in previous works, poor sampling of low reheating temperatures region, direct interpretation of the physical results;
- $N_{\text{eff}}^{FP}$  **sampling**: most direct relationship with the data, uniform sampling of all parameter space, difficult interpretation of the results.
- Summary table:

Parameter	$N_{\text{eff}}^{FP}$ sampling	$T_{\text{RH}}$ sampling
	95% limits	95% limits
$N_{\text{eff}}^{FP}$	> 2.61	–
$T_{\text{RH}}$	$5.2^{+2.5}_{-1.9}$ ( $> 3.86$ )	$> 4.41$

Slightly **relaxed** by new sampling strategy

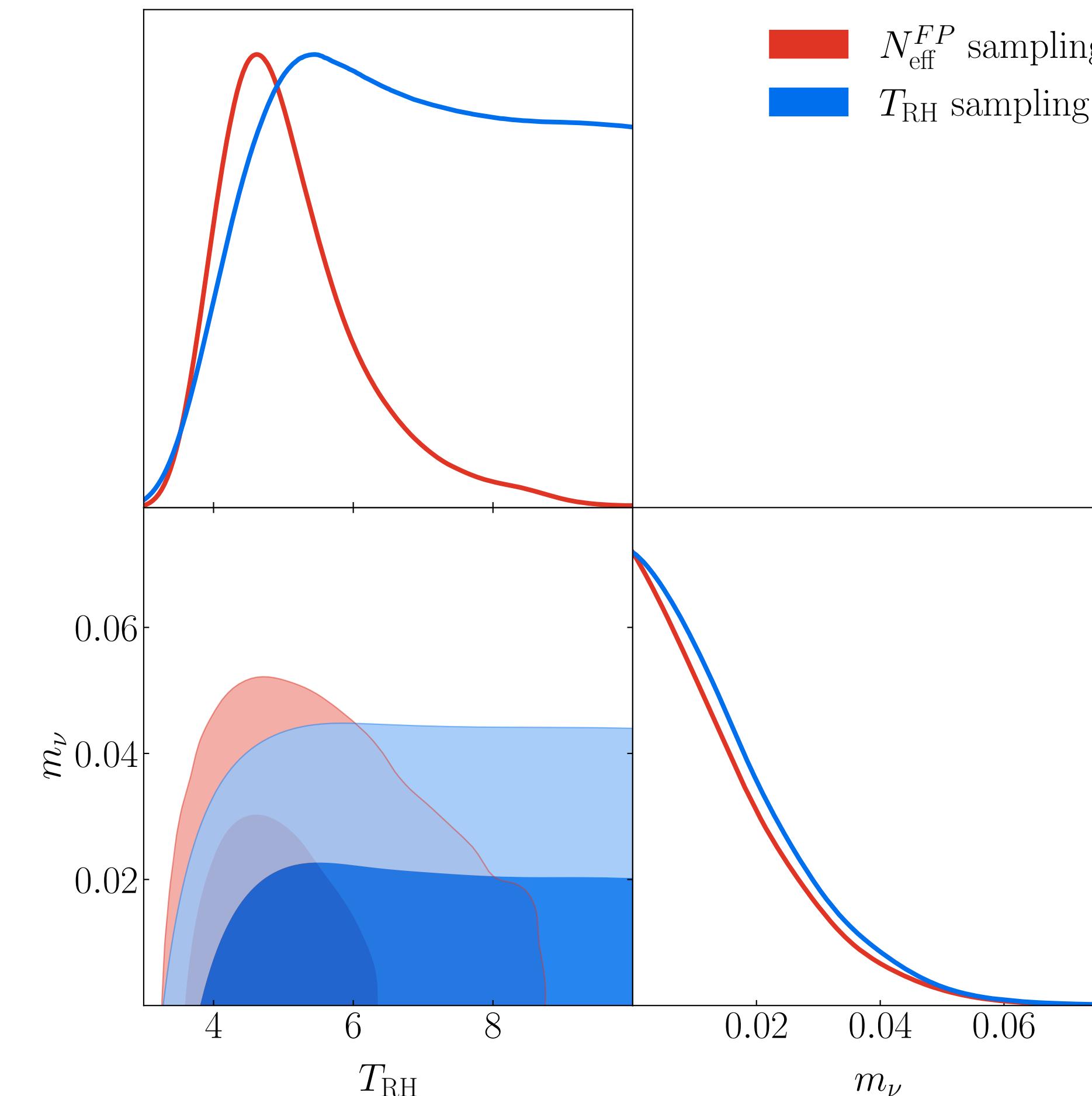
**Compatible** with previous works



# Bounds on $\Sigma m_\nu$ [eV]

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- Summary table:

Parameter	$N_{\text{eff}}^{FP}$ sampling	$T_{\text{RH}}$ sampling
	95% limits	95% limits
$N_{\text{eff}}^{FP}$	> 2.60	–
$T_{\text{RH}}$	$5.2^{+2.5}_{-1.6}$ ( $> 3.83$ )	> 4.09
$m_\nu$	< 0.0389	< 0.0399



# The Kullback-Leibler divergence

- Measure of the “distance” between two distributions

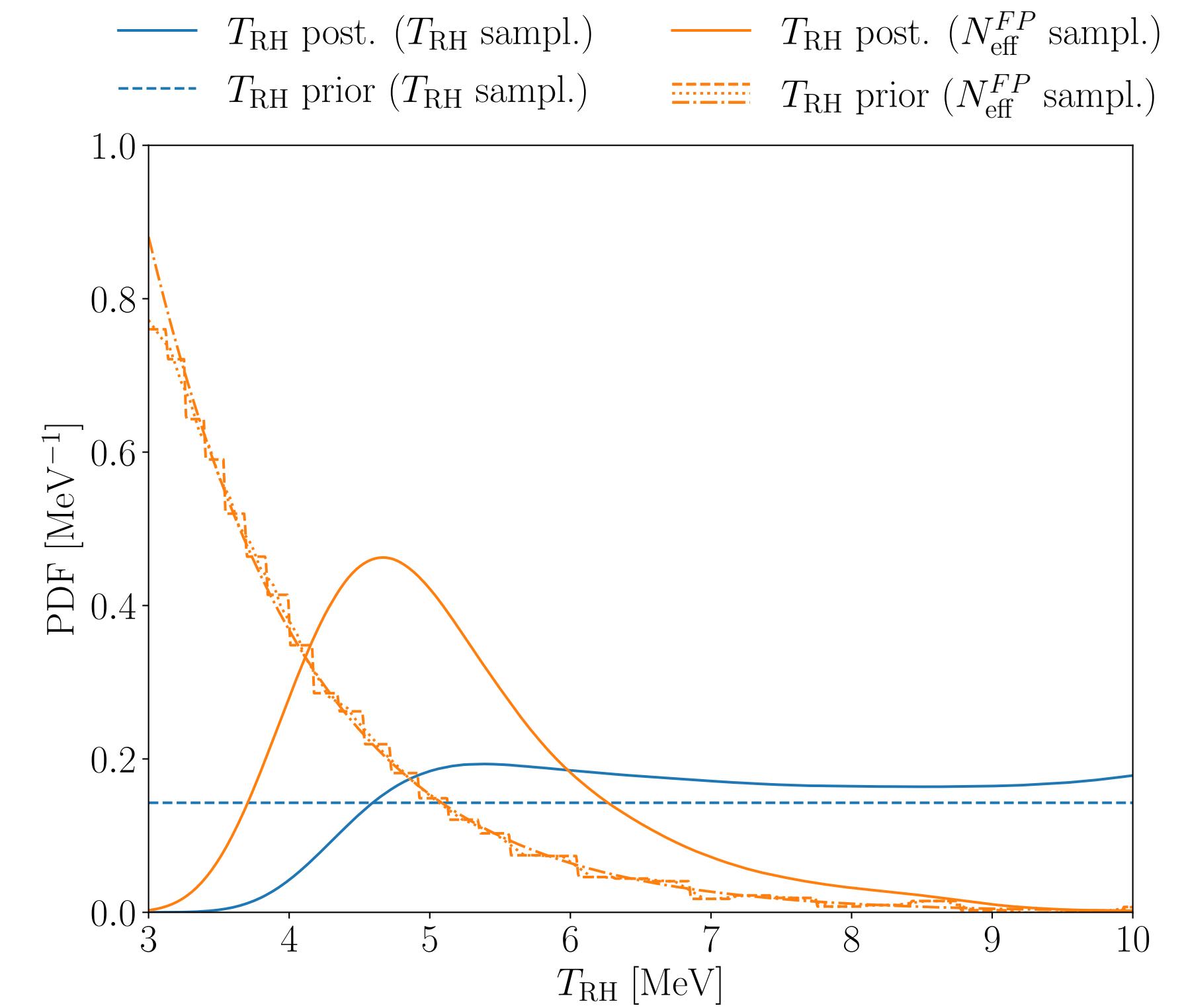
$$\mathcal{D}_{\text{KL}}(P \parallel Q) \equiv \int d\theta p(\theta) \log \left[ \frac{p(\theta)}{q(\theta)} \right]$$

In the context of bayesian analysis it is used to asses the impact of different parameterisations by computing the information gain between the prior and the posterior.

$$\mathcal{D}_{\text{KL}}(\mathcal{P}_{T_{\text{RH}}} \parallel \Pi_{T_{\text{RH}}}) = 0.14$$

$$\mathcal{D}_{\text{KL}}(\mathcal{P}_{N_{\text{eff}}^{\text{FP}}} \parallel \Pi_{N_{\text{eff}}^{\text{FP}}}) = 0.64$$

Slight “preference”  
for  $N_{\text{eff}}^{\text{FP}}$  sampling



Work done in collaboration with  
T. Brinckmann (UniFE), P. F. de Salas (Stockholm U.), M. F. Navarro (Glasgow U.),  
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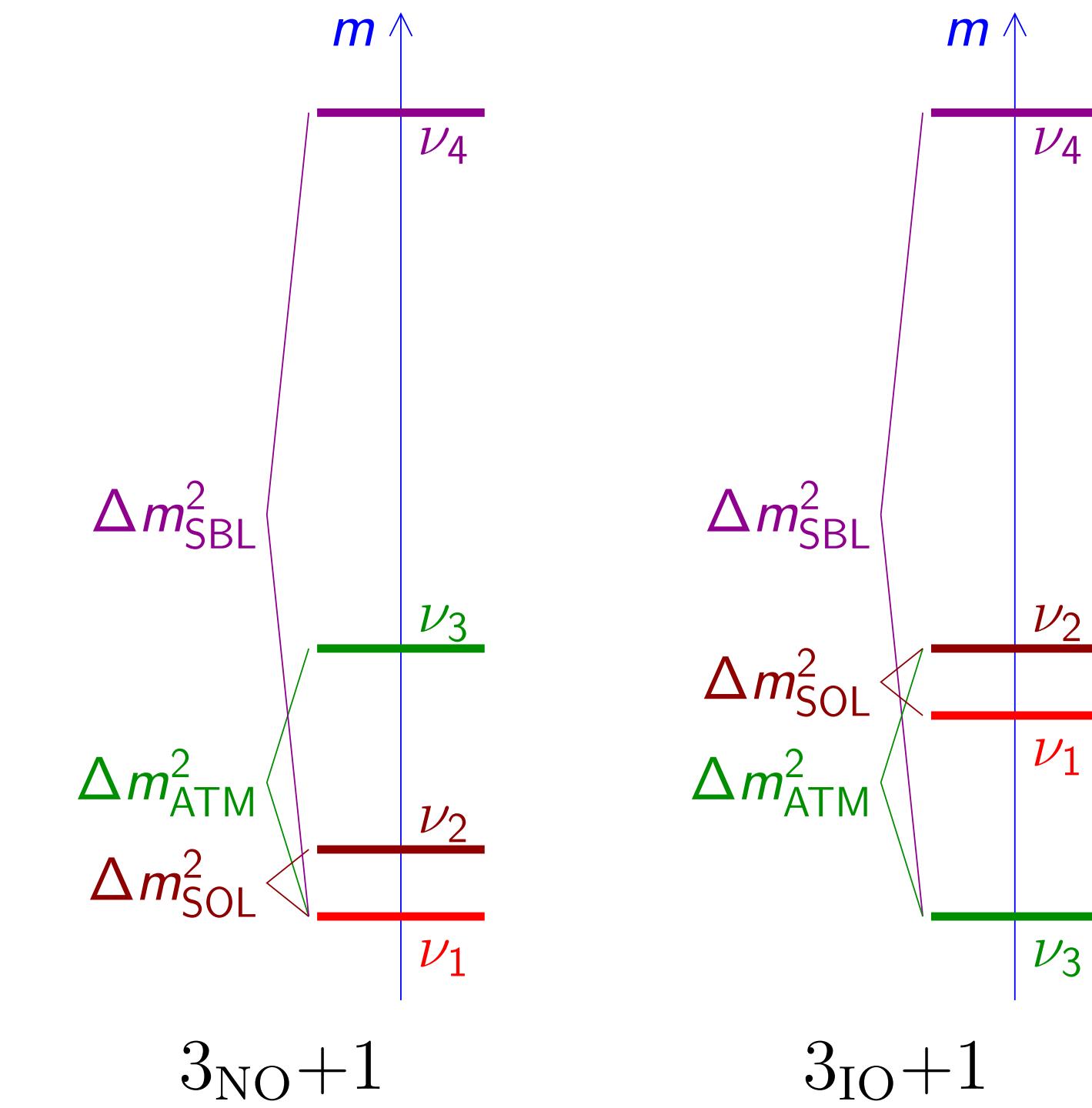
# Bounds on sterile neutrinos oscillations in very low reheating scenarios

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# The (3+1) neutrino framework

- Several anomalies in neutrino oscillation experiments seem to suggest the existence of one **additional sterile state**, mixed with the active neutrinos;
- The parameter space is enlarged by the addition of an **additional mass splitting**,  $\Delta m_{14}^2$ , and **three new mixing angles**  $\theta_{14}$ ,  $\theta_{24}$  and  $\theta_{34}$ ;
- Scenarios fitting the short baseline anomalies point to a fully thermalized sterile state which, however, is completely ruled out by cosmological observations.

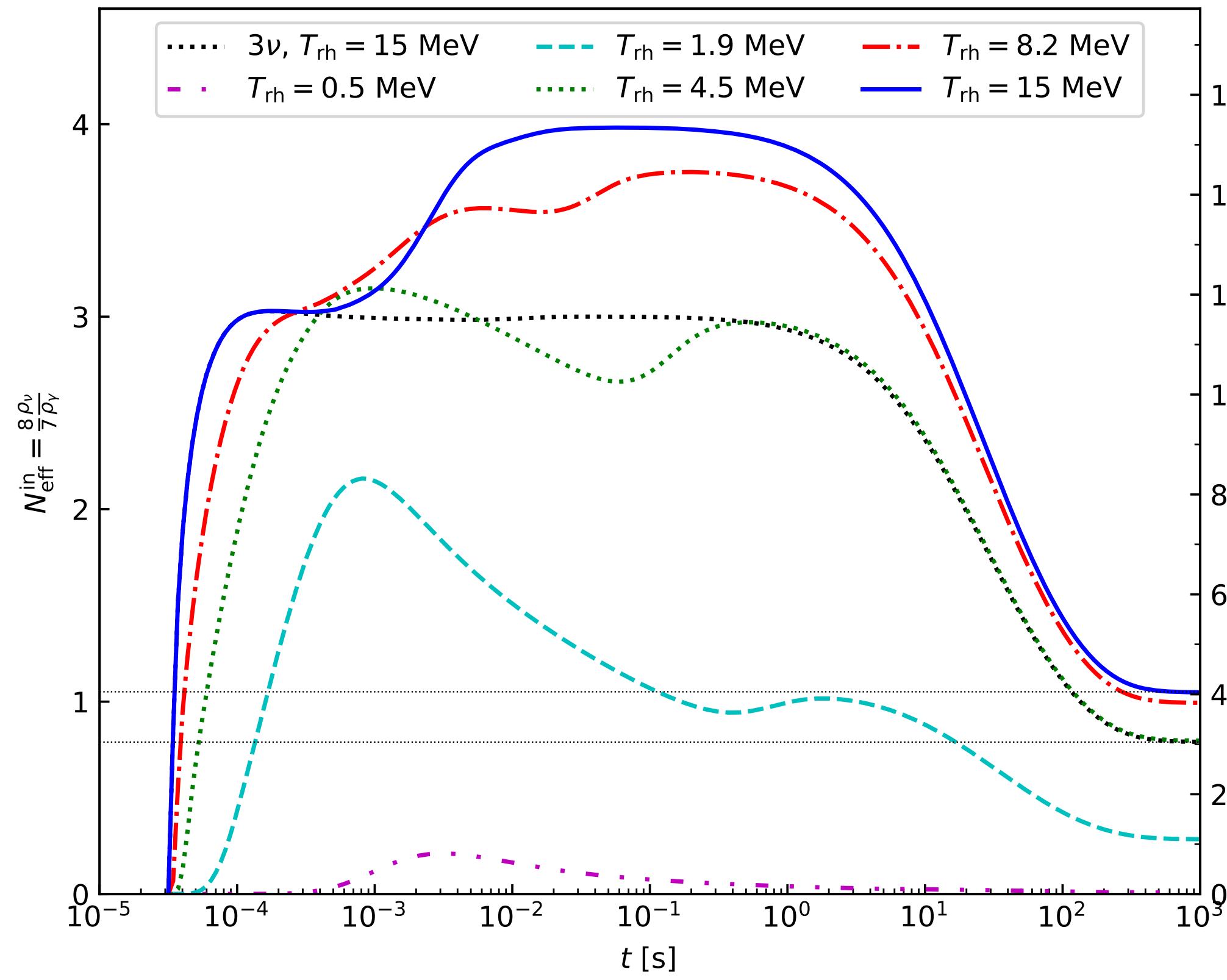
[See S. Pastor's talk]



[Credits: Giunti and Lasserre (2019)]

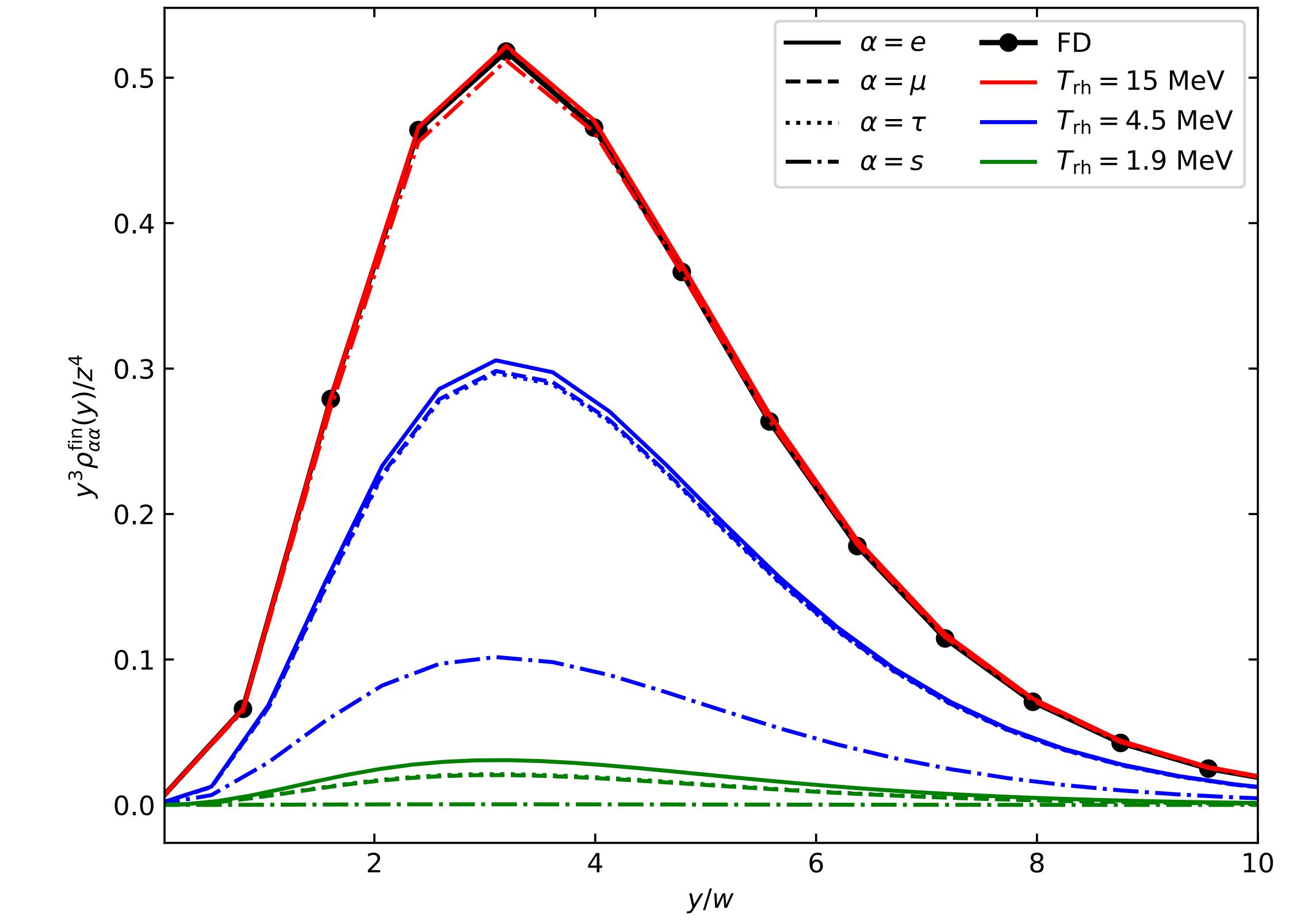
# Neutrino production in (3+1) models

[Credits: S. Gariazzo]



Time evolution of the ratio of energy densities of neutrinos and photons.

[Credits: S. Gariazzo]



Final differential spectra of neutrino energies as a function of the comoving momentum.

# Conclusions

- New improved bounds on  $T_{\text{RH}}$  from new cosmological data with a new sampling strategy;
- Test of the robustness of bounds on the sum of neutrinos masses;
- Low reheating is a quite complicated scenario but it provides an interesting way to reduce  $N_{\text{eff}}$ , leaving room for relativistic particles, such as sterile neutrinos.

*Thank you!*