

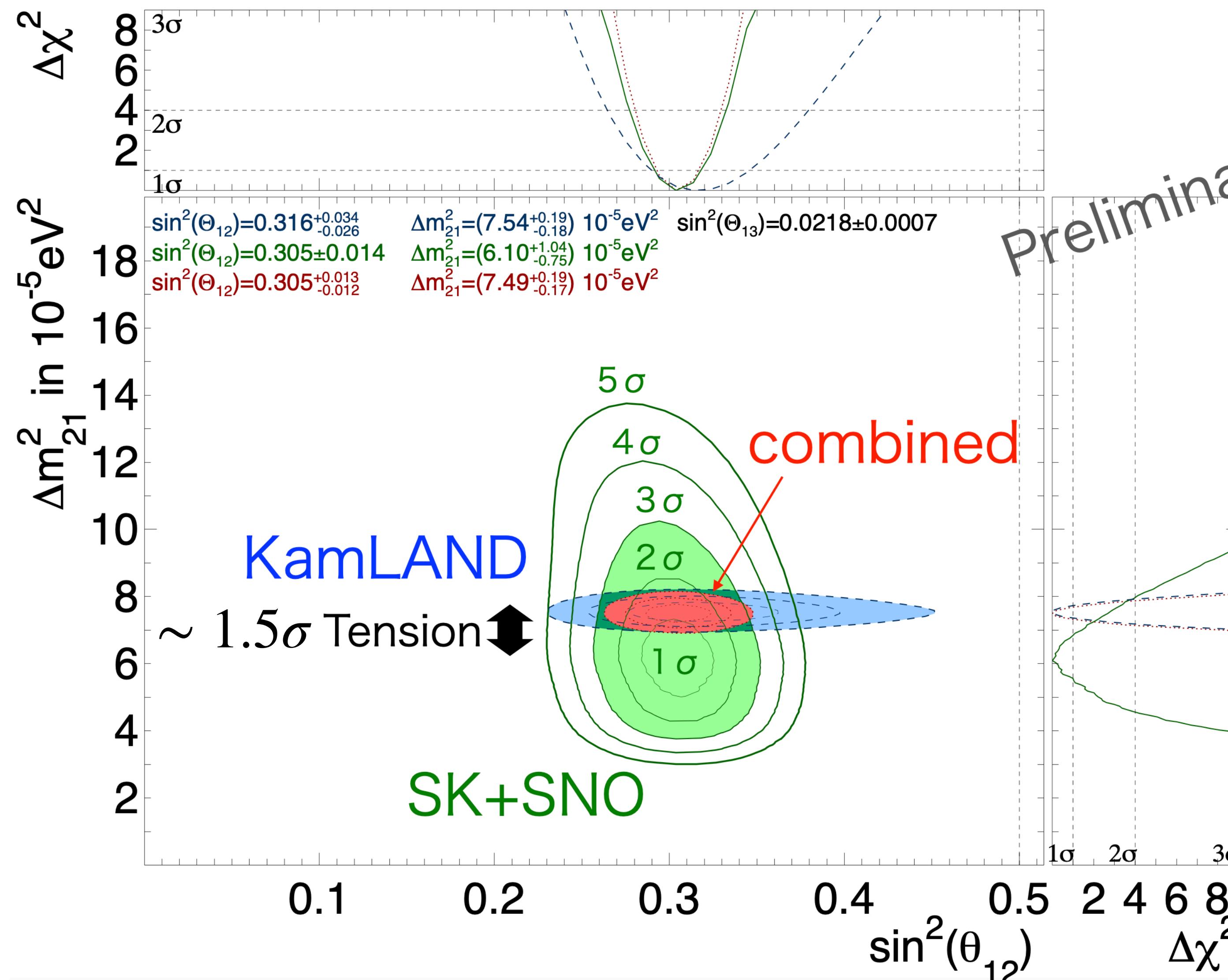
Shedding light on the Δm_{21}^2 tension with supernova neutrinos

Rasmi E. Hajjar Muñoz

based on PLB 854 (2024) 138719 and *Phys. Rev. D* 108 (2023) 083011
with Olga Mena and Sergio Palomares-Ruiz

Main goal of this work: tension?

Plot extracted from Neutrino22 contribution of Yusuke Koshio, SK collaboration

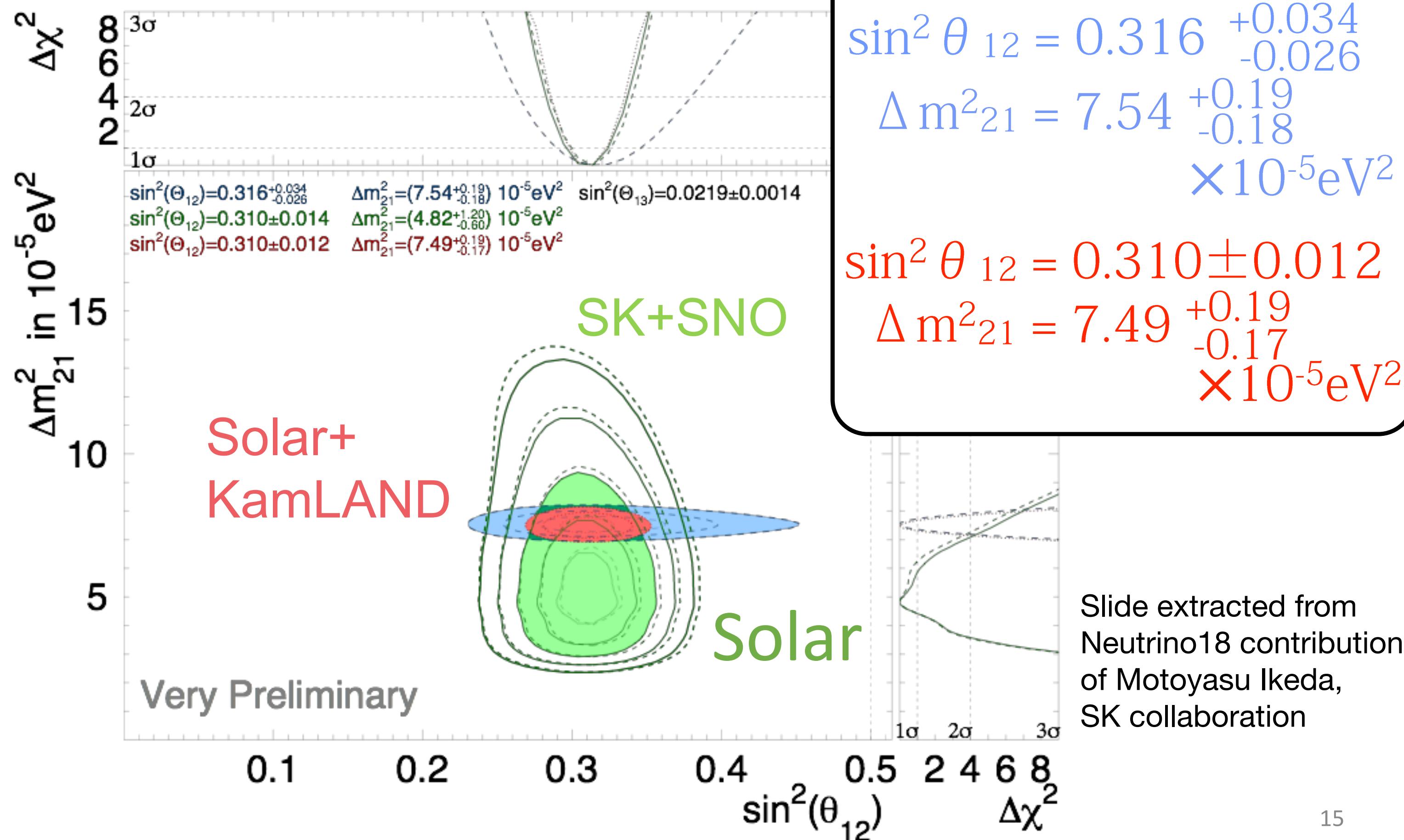


Preliminary

- There is a $\sim 1.5\sigma$ tension between **KamLAND** and **SK+SNO** measurements.
- **KamLAND**: reactor neutrinos.
- **SK+SNO**: solar neutrinos sensitive to Sun and Earth matter effects.
- **OUR MAIN GOAL**: solve tension using SN neutrinos sensitive to Earth matter effects.

Main goal of this work: tension!

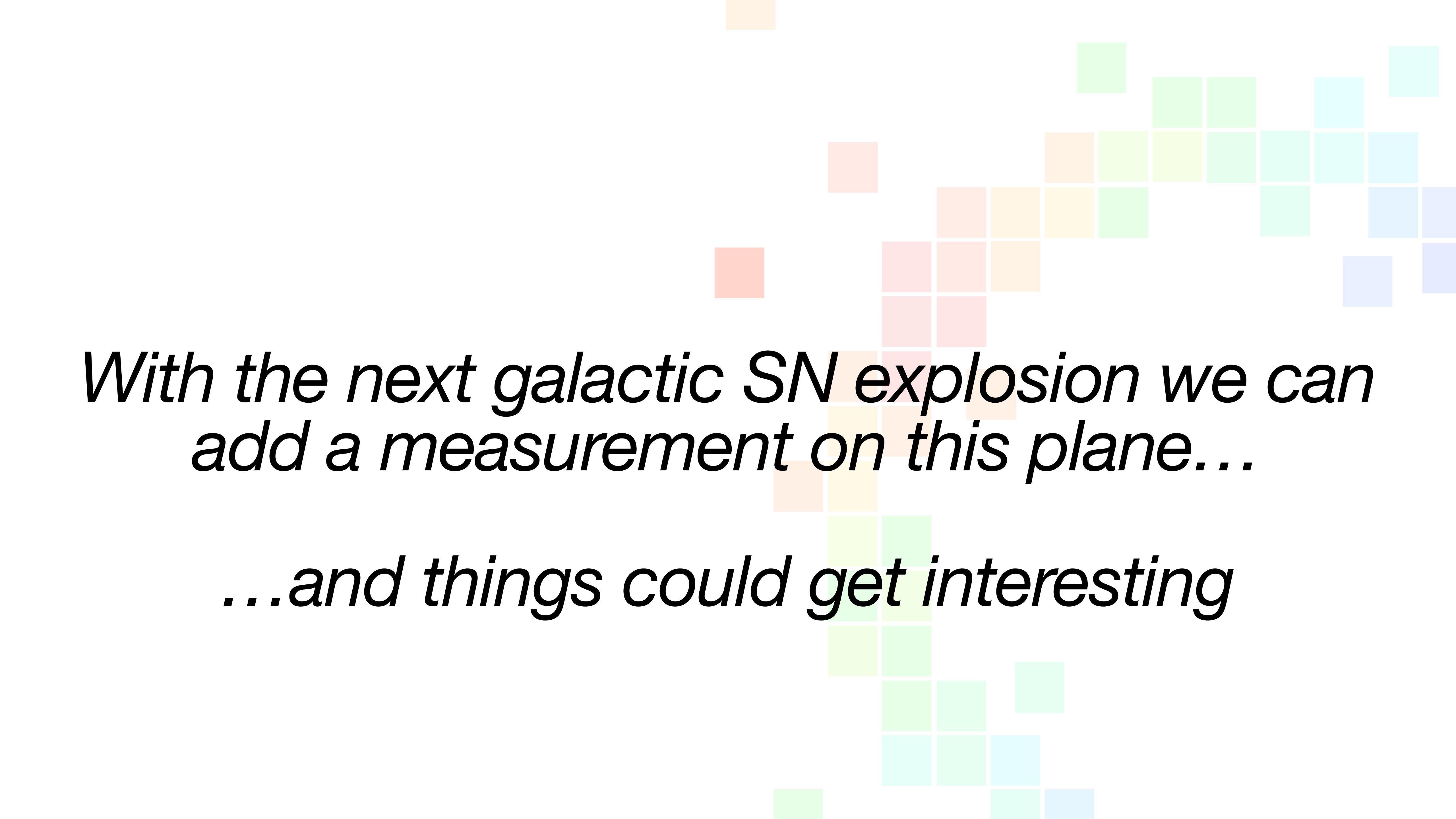
Solar v Angle θ_{12} & Mass



- Now the tension relaxed...
- But in the past this tension was higher!
- $\sim 2.3\sigma$ tension between **KamLAND** and **SK+SNO** measurements without the last data inclusion.



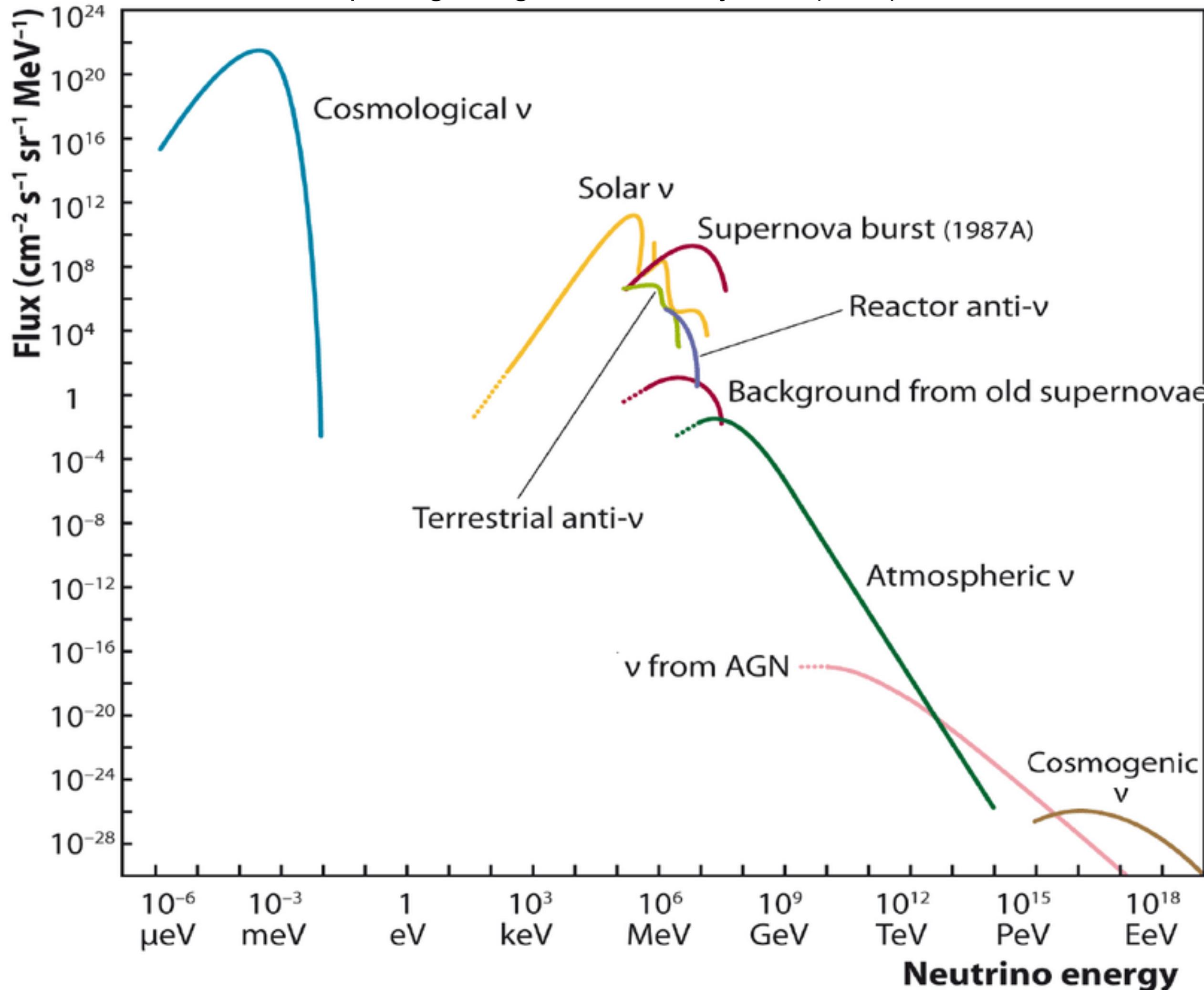
*With the next galactic SN explosion we can
add a measurement on this plane...*



*With the next galactic SN explosion we can
add a measurement on this plane...
...and things could get interesting*

Supernova neutrinos

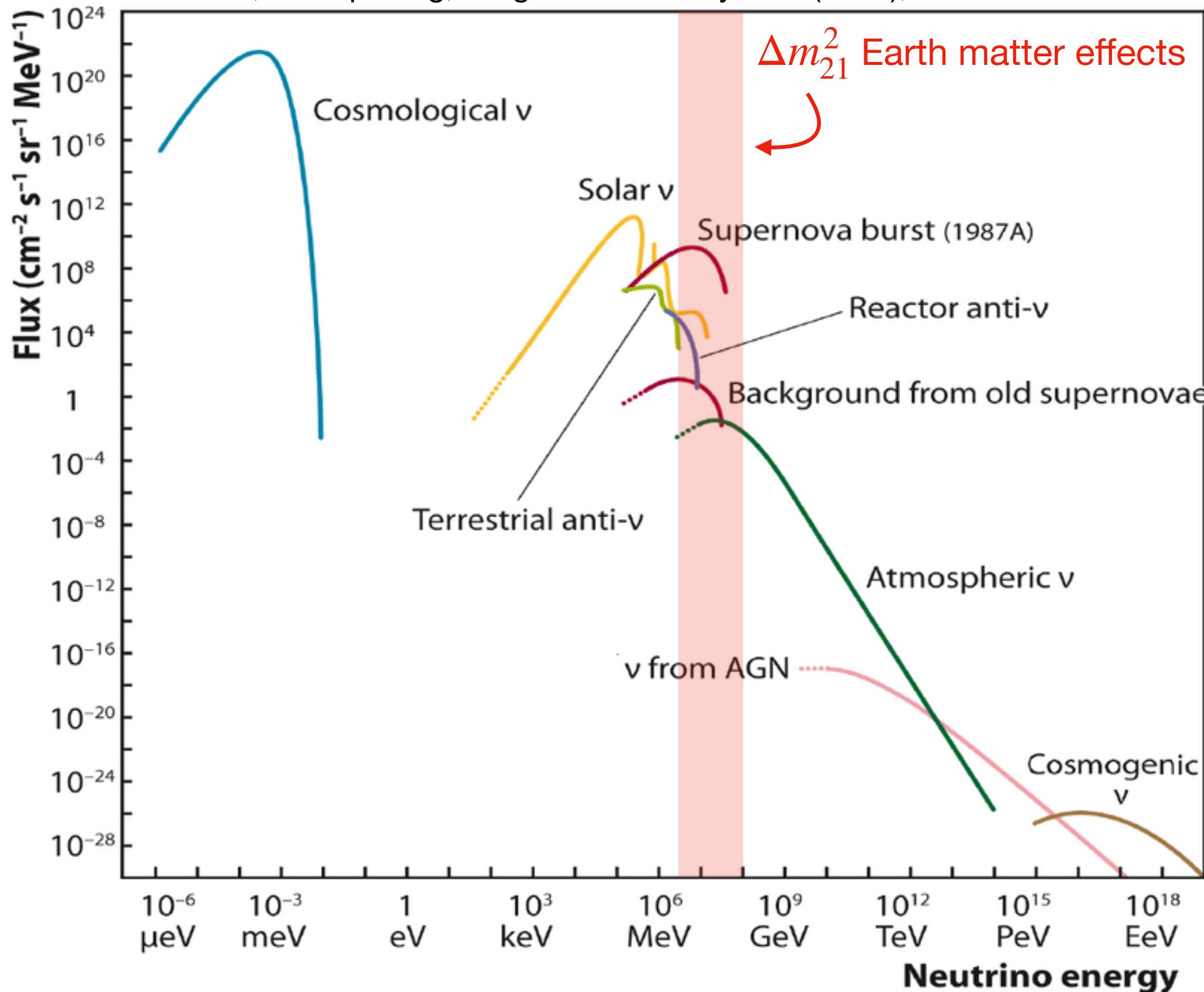
U.F. Katz, Ch. Spiering, Prog.Part.Nucl.Phys. 67 (2012), 651-704



- Core-collapse SN is the violent explosion during death of massive stars.
- 99% energy of star ($\sim 10^{53}$ erg) is released in the form of neutrinos.
- Excellent source due to high flux and low background when applied temporal cut.

Supernova neutrinos

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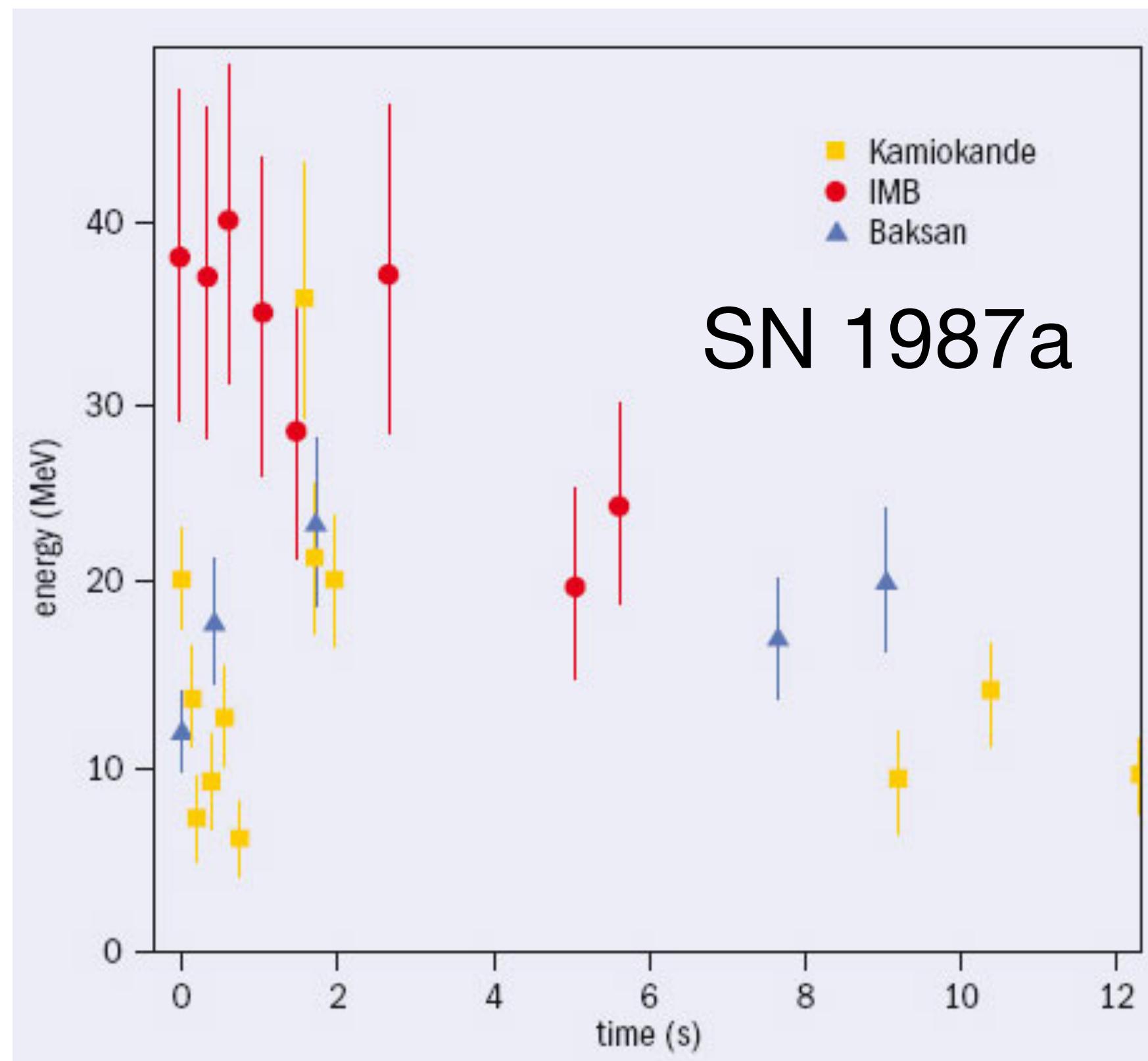


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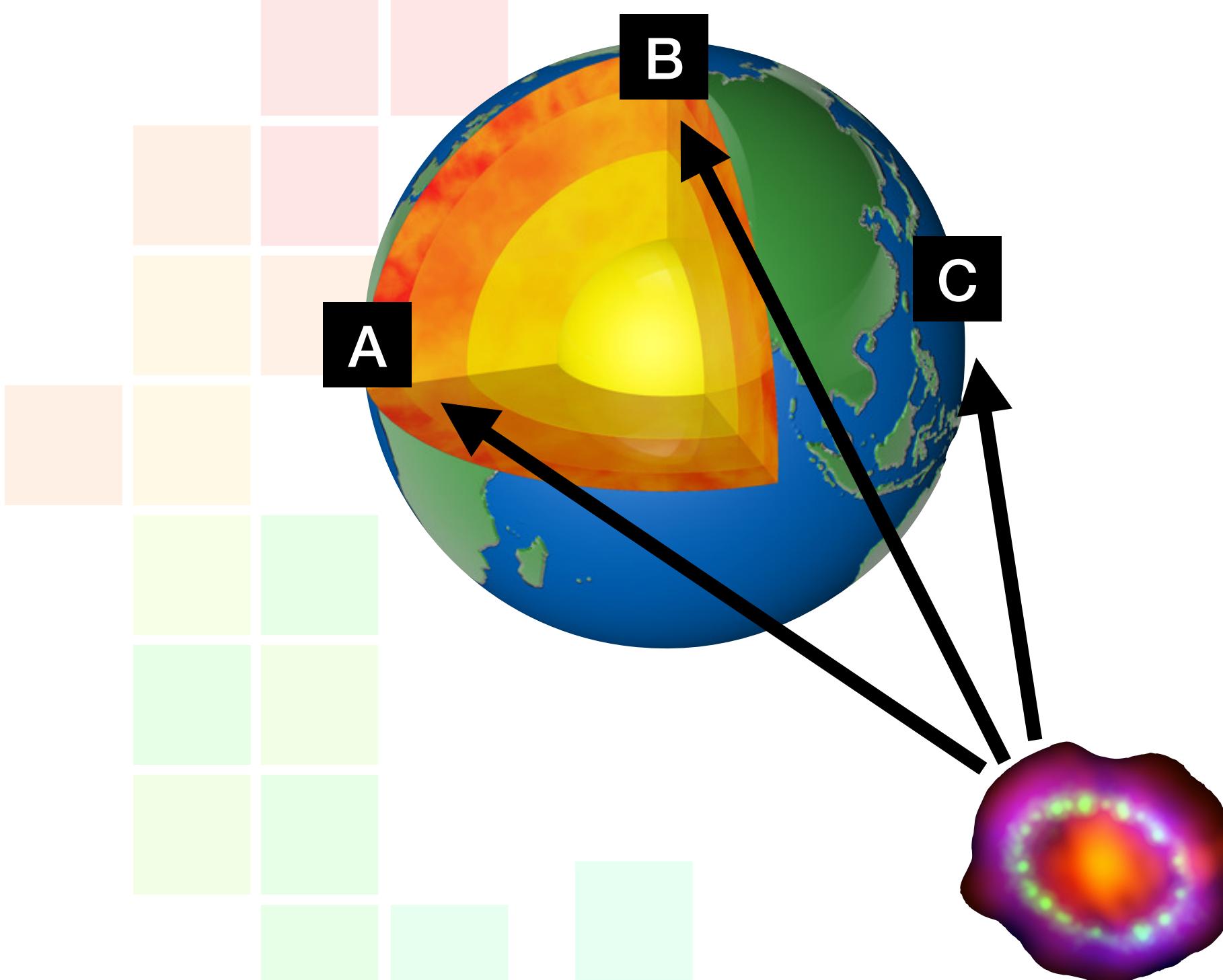
Supernova neutrinos

Main drawbacks

Uncertainty on fluxes



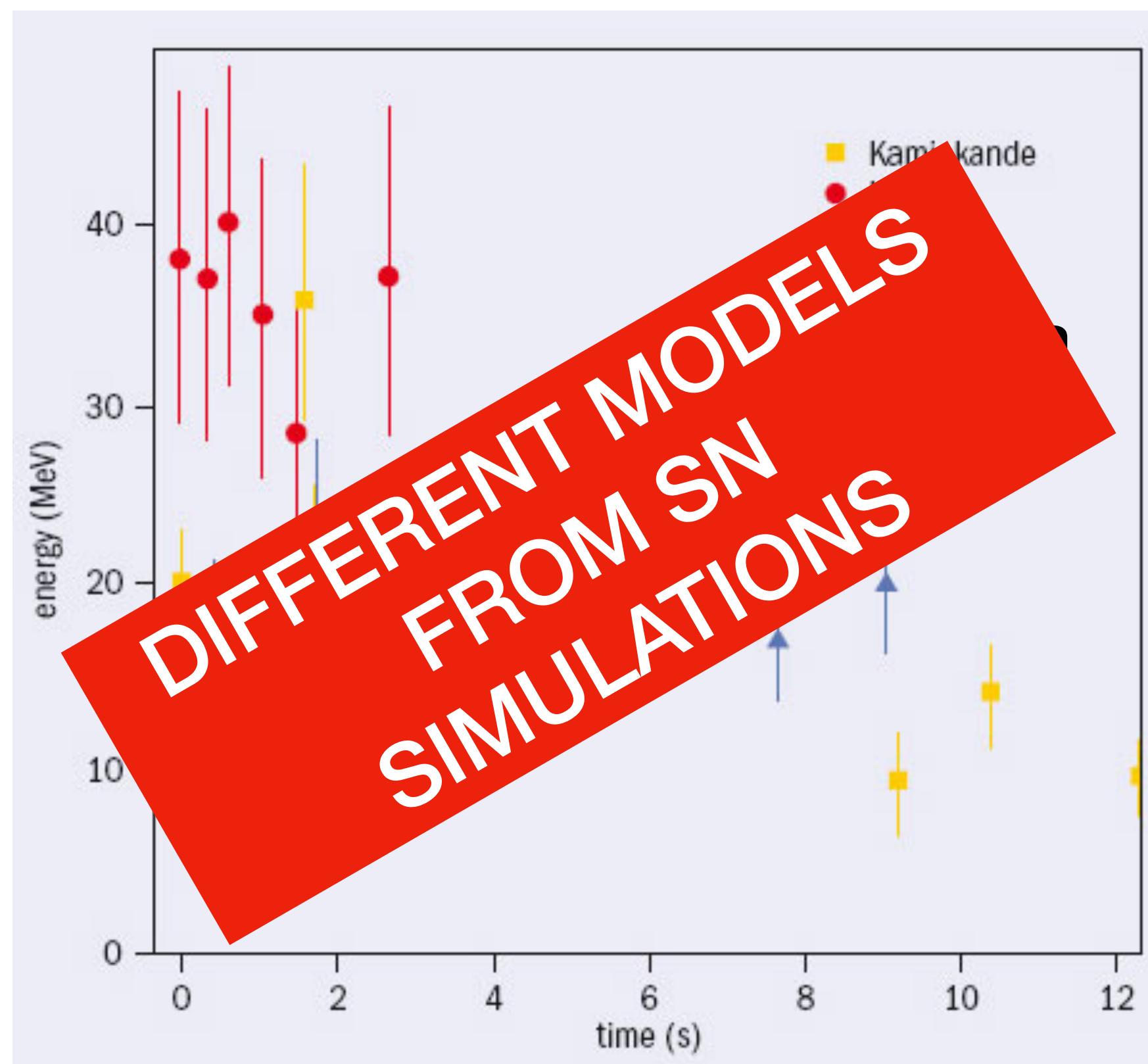
One direction per detector



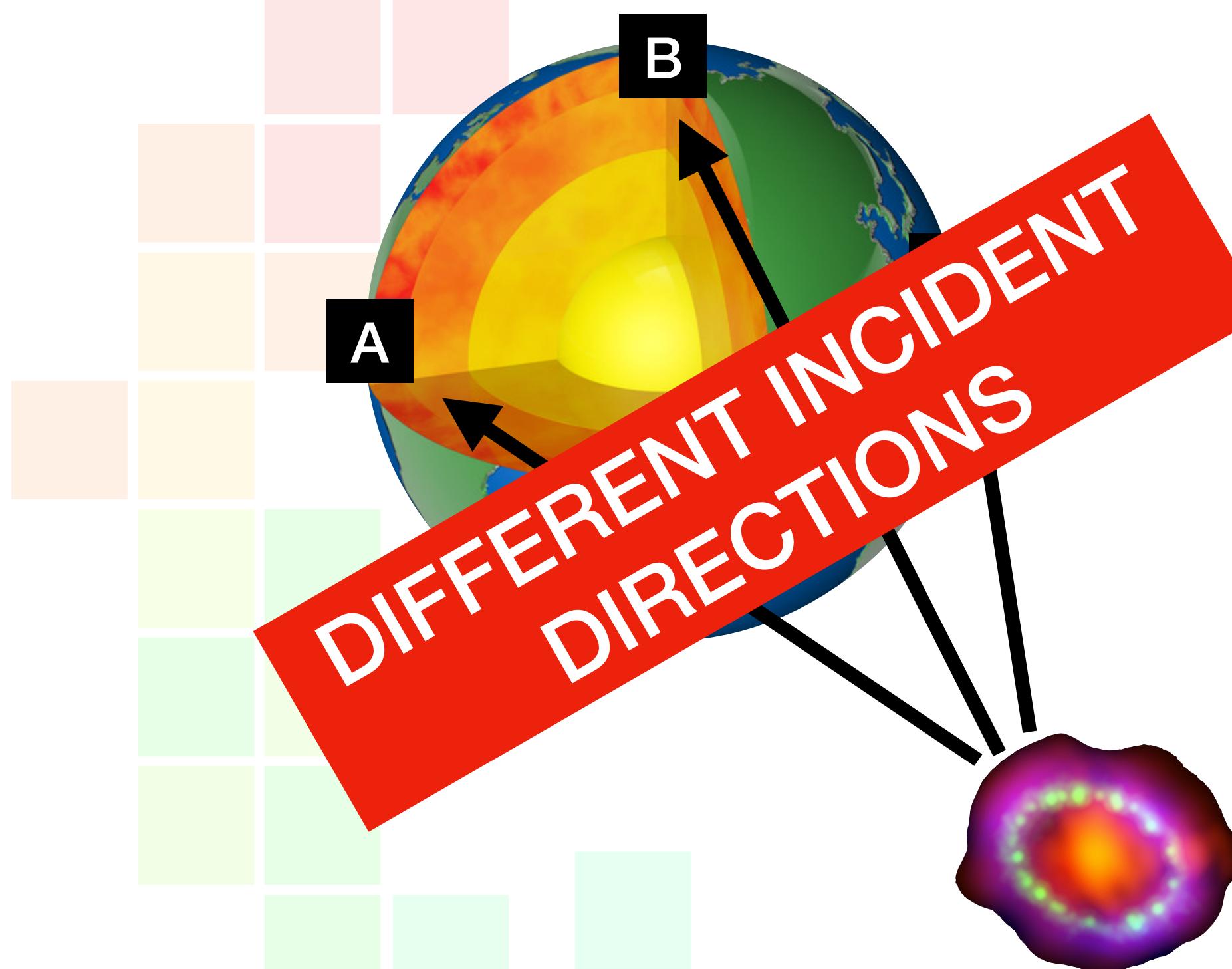
Supernova neutrinos

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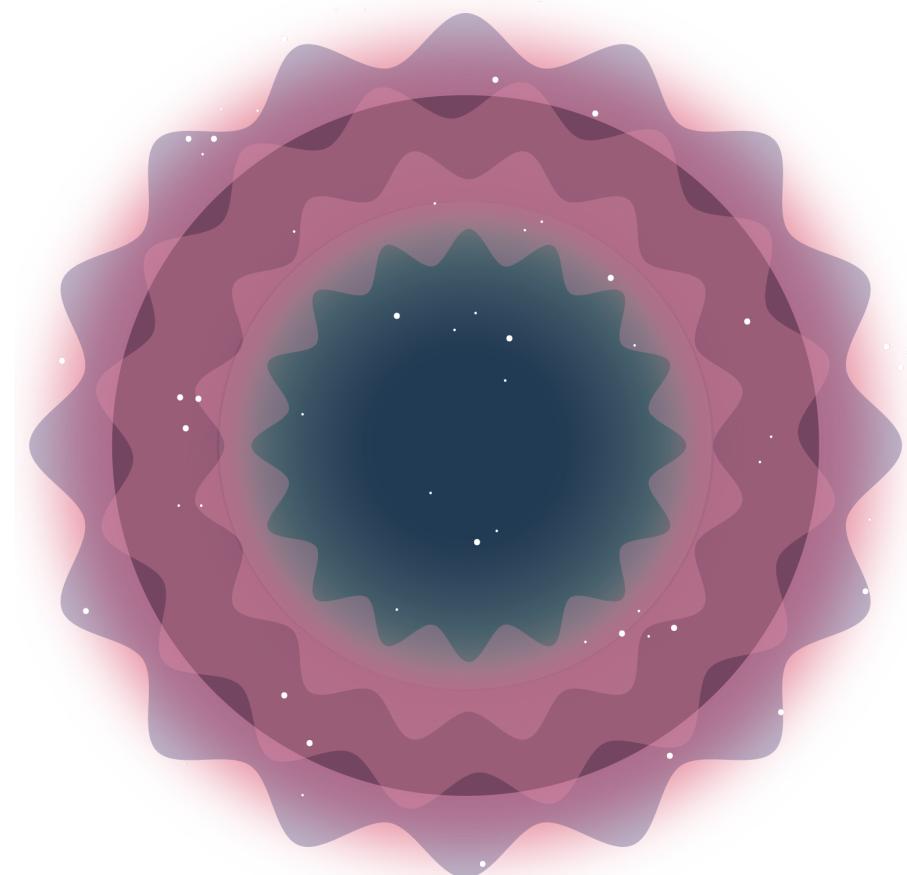
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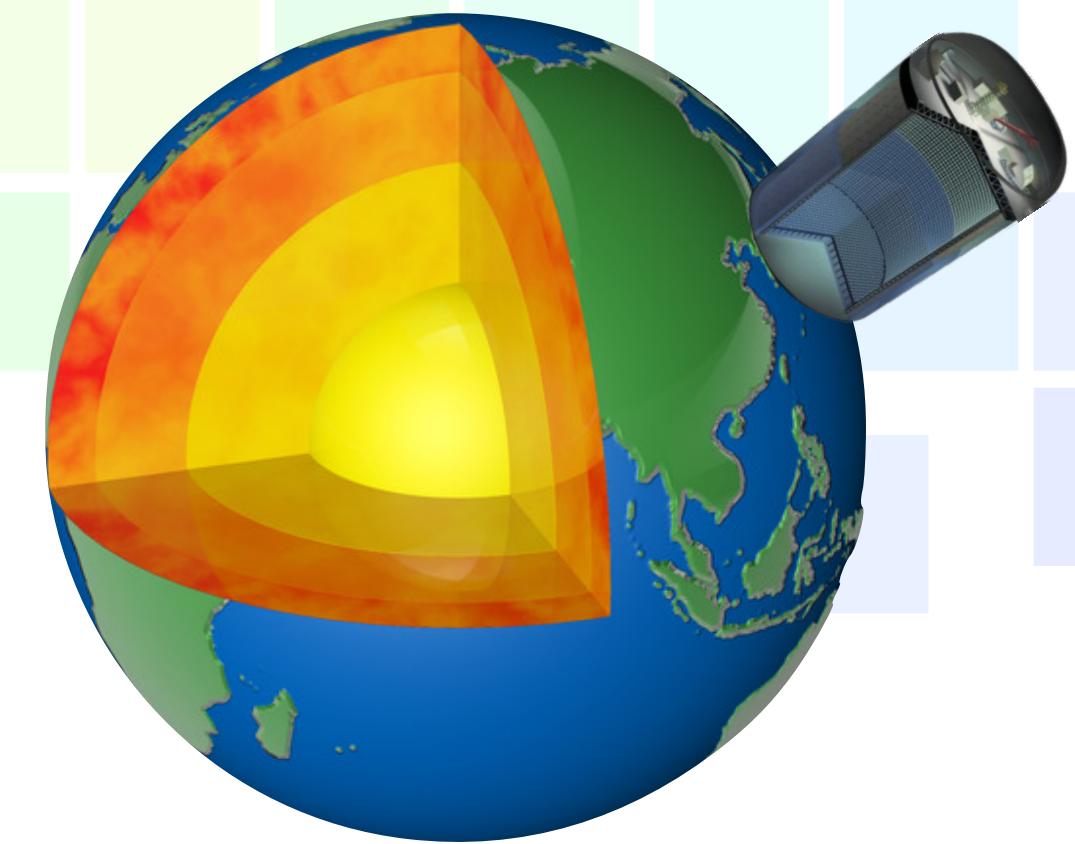
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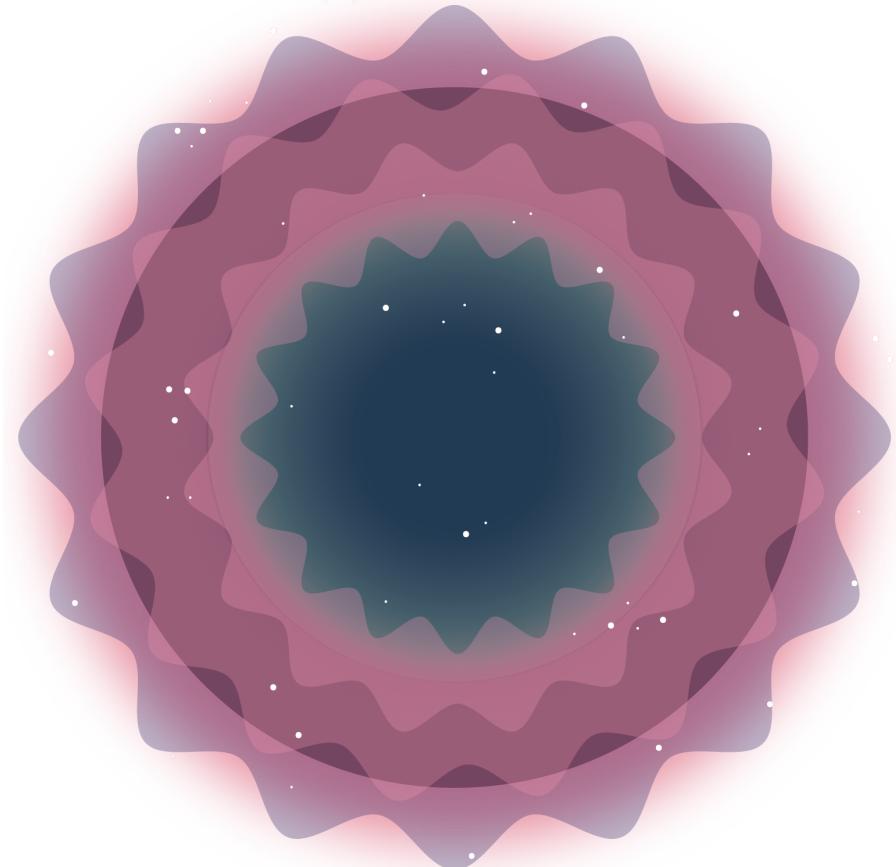
Supernova neutrino journey



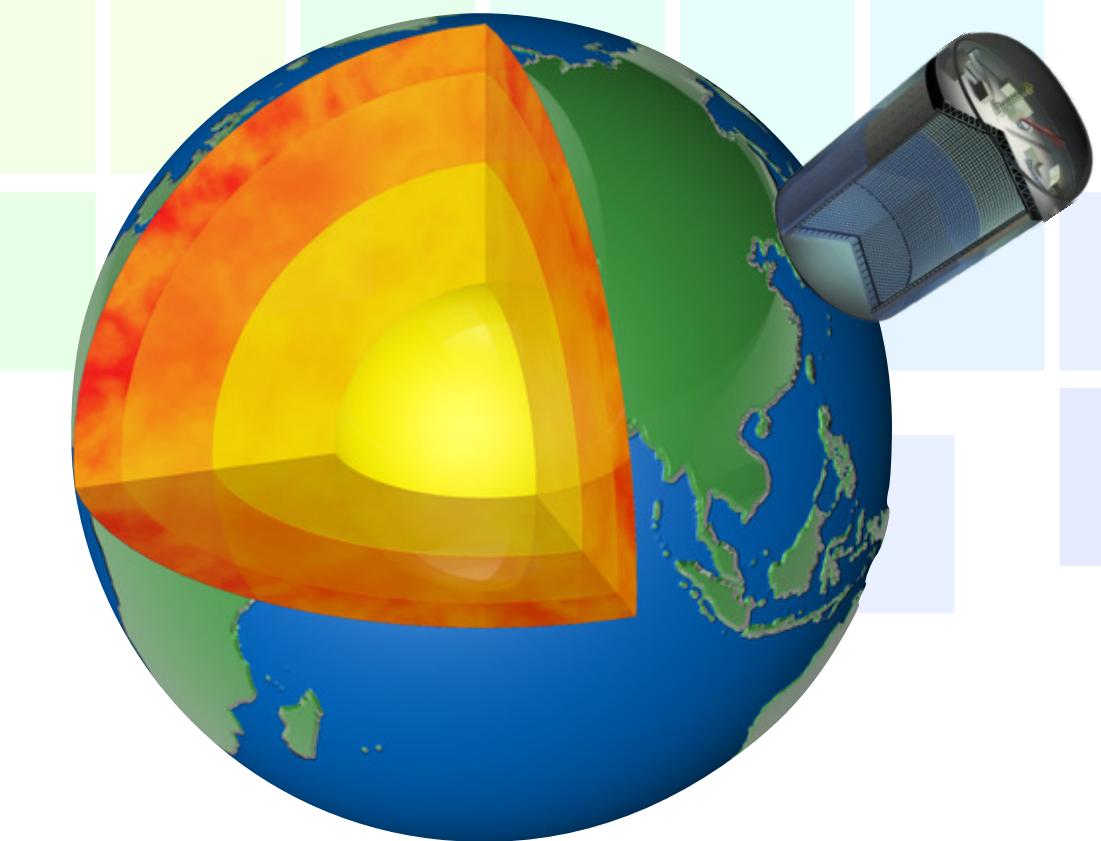
$$F_{\nu_e}^D = p F_{\nu_e}^0 + (1 - p) F_{\nu_x}^0$$



Supernova neutrino journey



$$F_{\nu_e}^D = p F_{\nu_e}^0 + (1 - p) F_{\nu_\chi}^0$$



- In order to obtain p we need to know neutrino evolution;

$$M^2 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix}$$

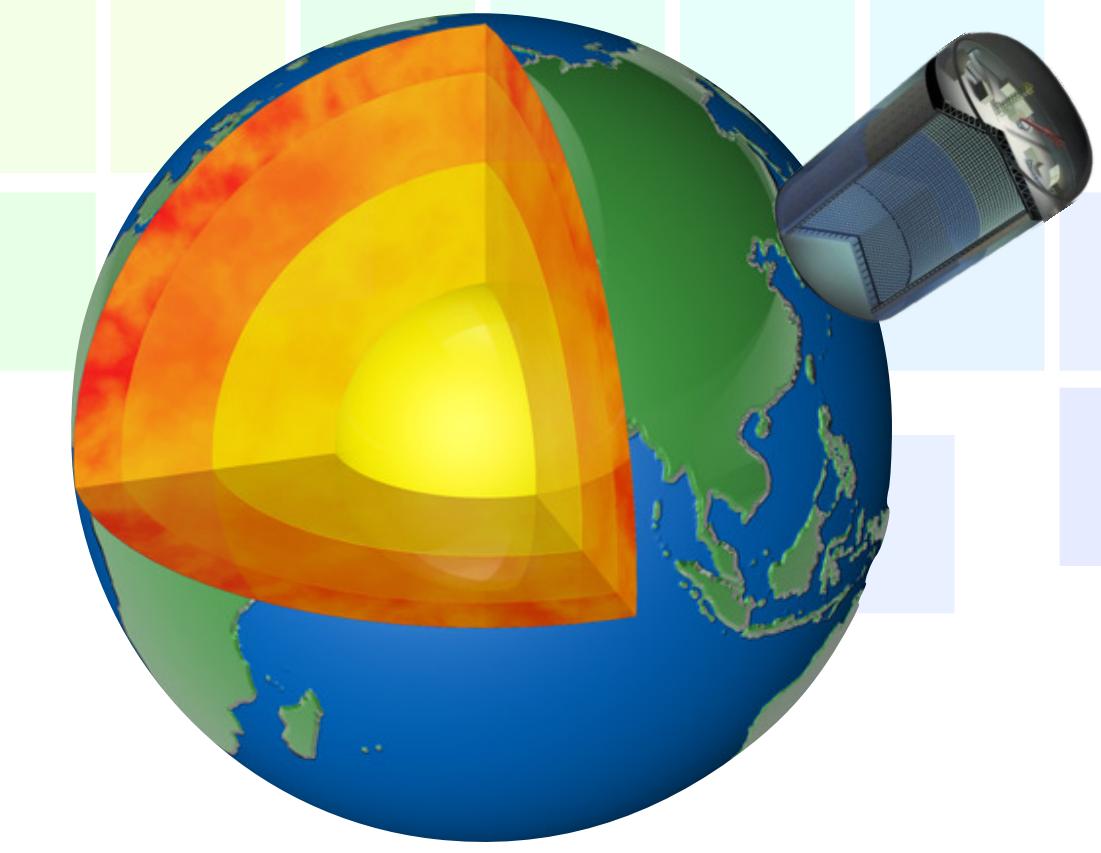
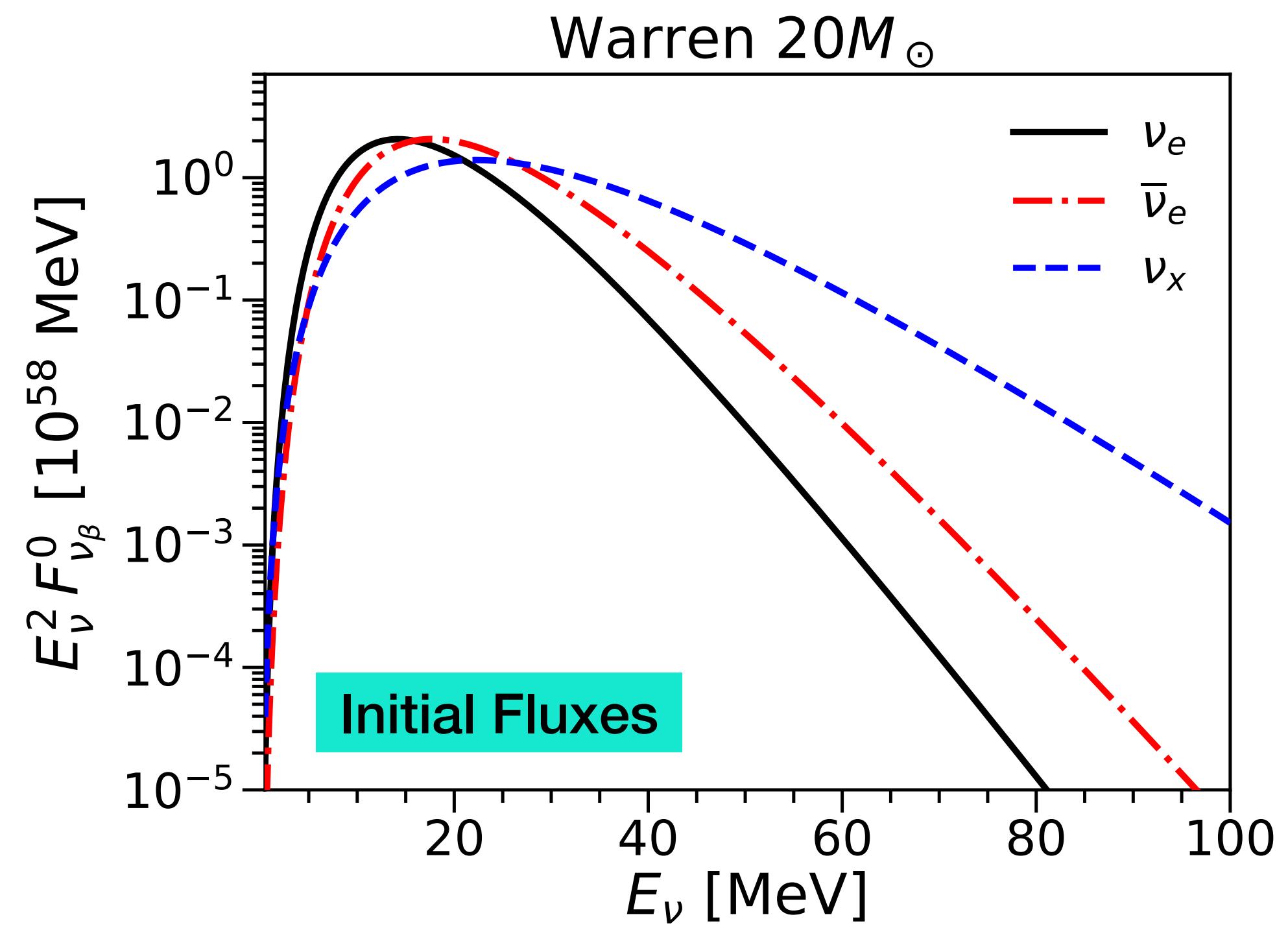
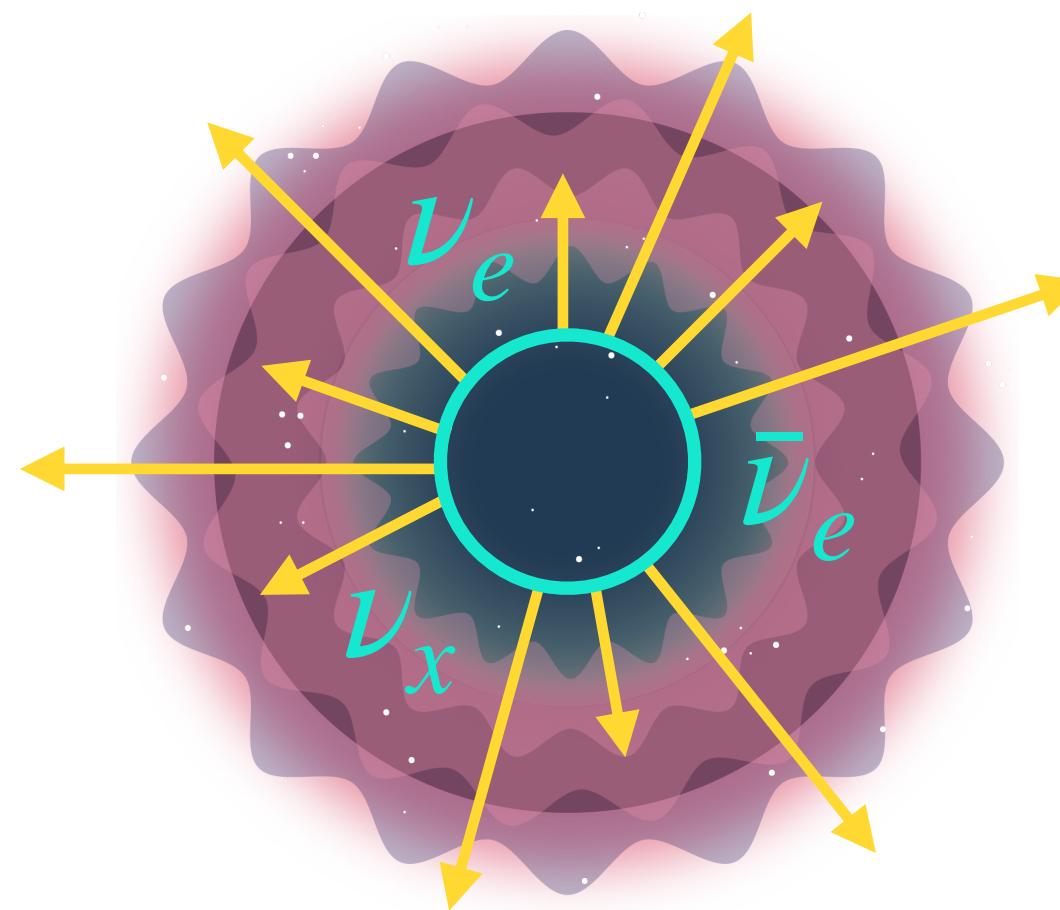
$$V = \begin{pmatrix} V(n_e) & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\mathcal{H}_{\text{flavor}} = \frac{1}{2E} \overline{U} M^2 U^\dagger + \overline{V}$$

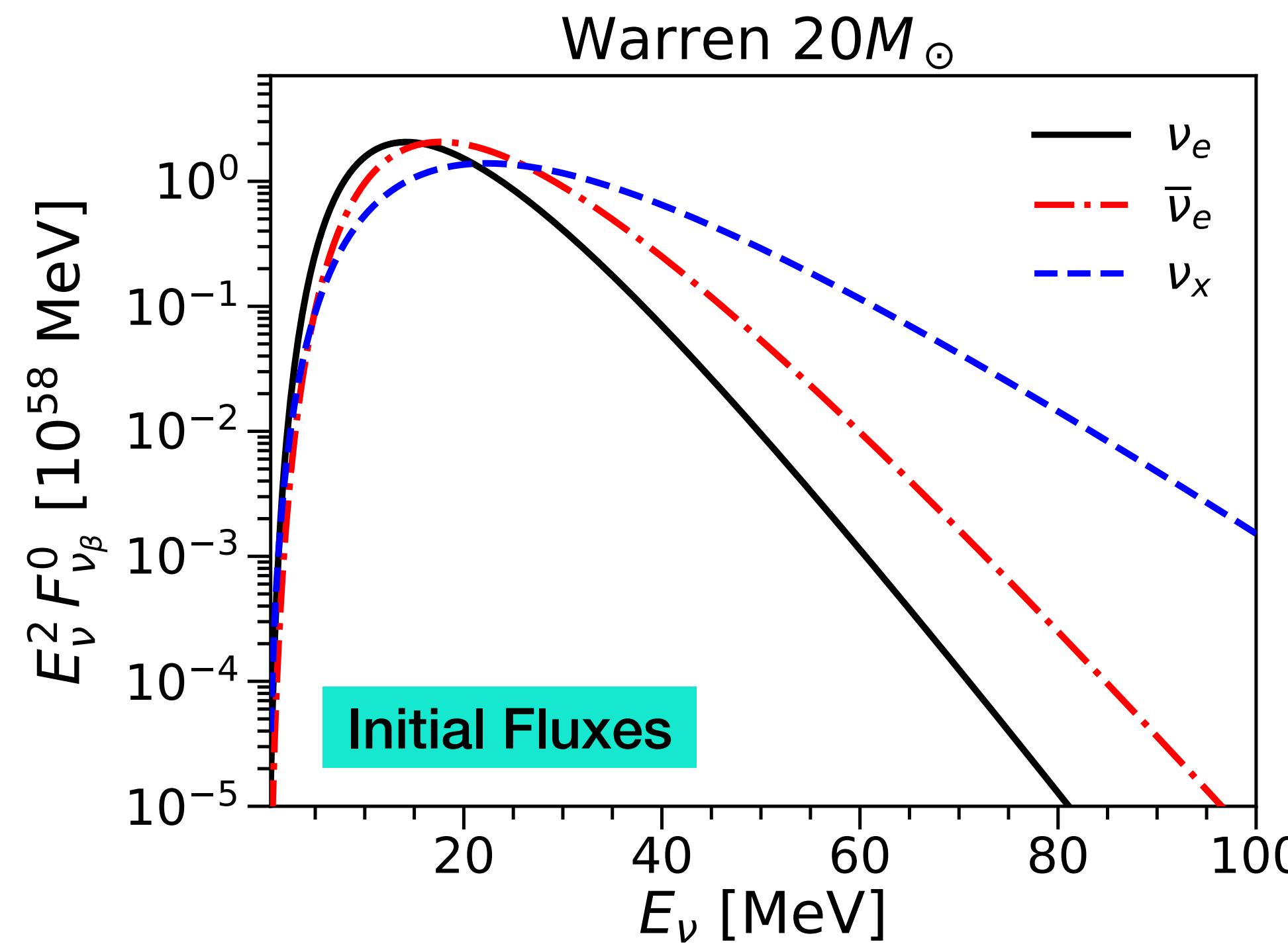
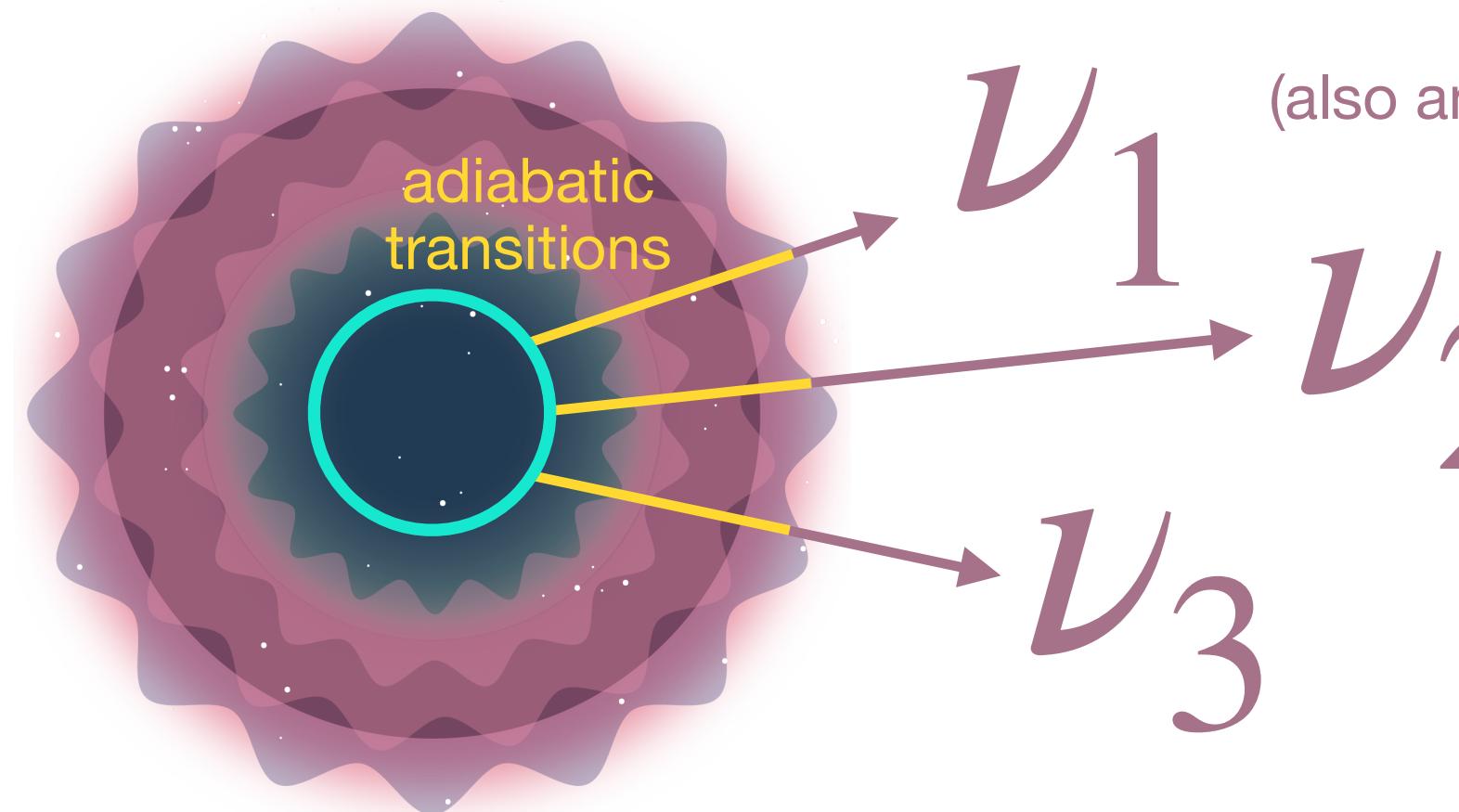
$$U = U_{23} \Gamma_\delta U_{13} U_{12}$$

PMNS matrix

Supernova neutrino journey



Supernova neutrino journey



SN adiabatic transitions in NO

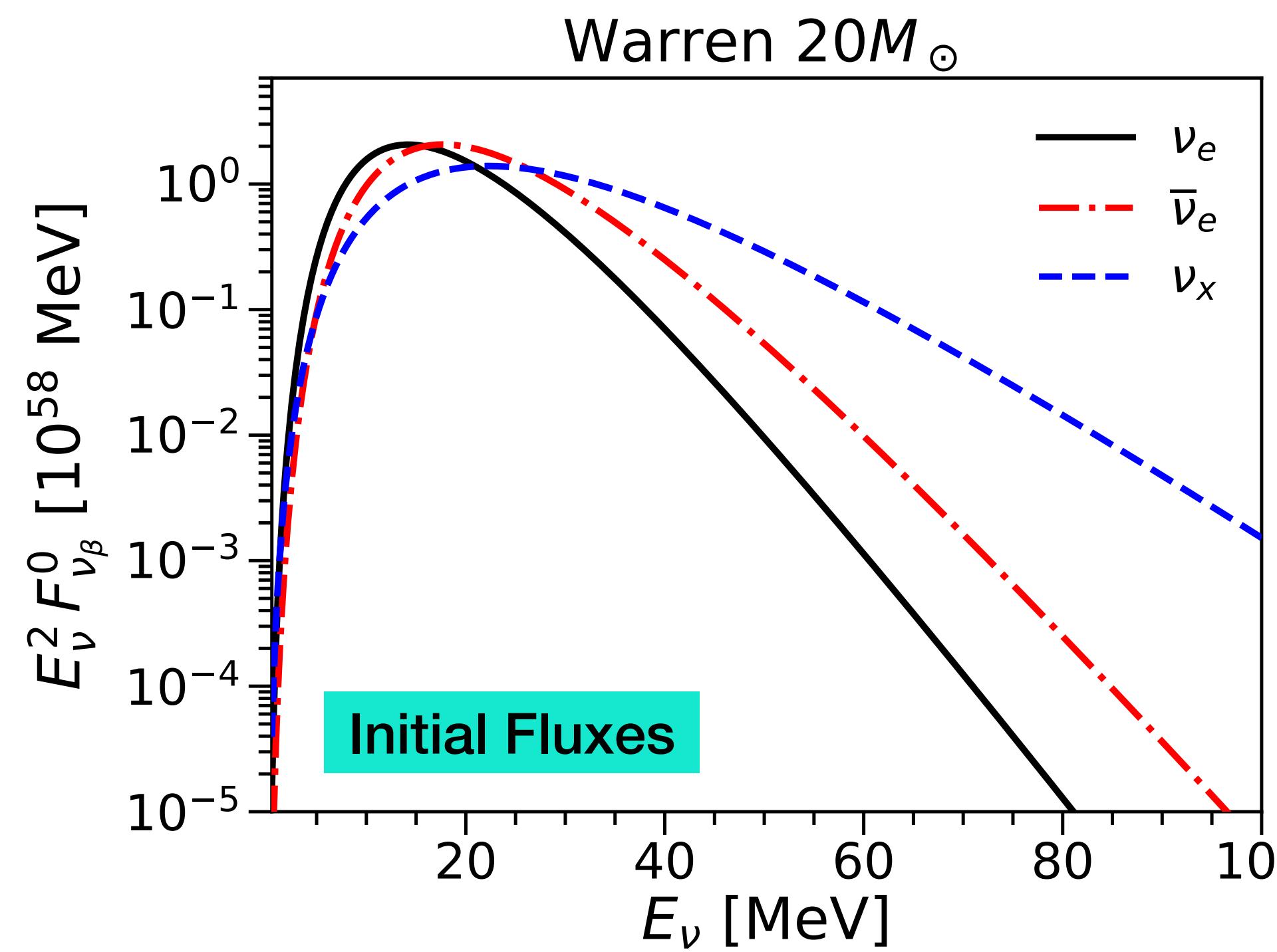
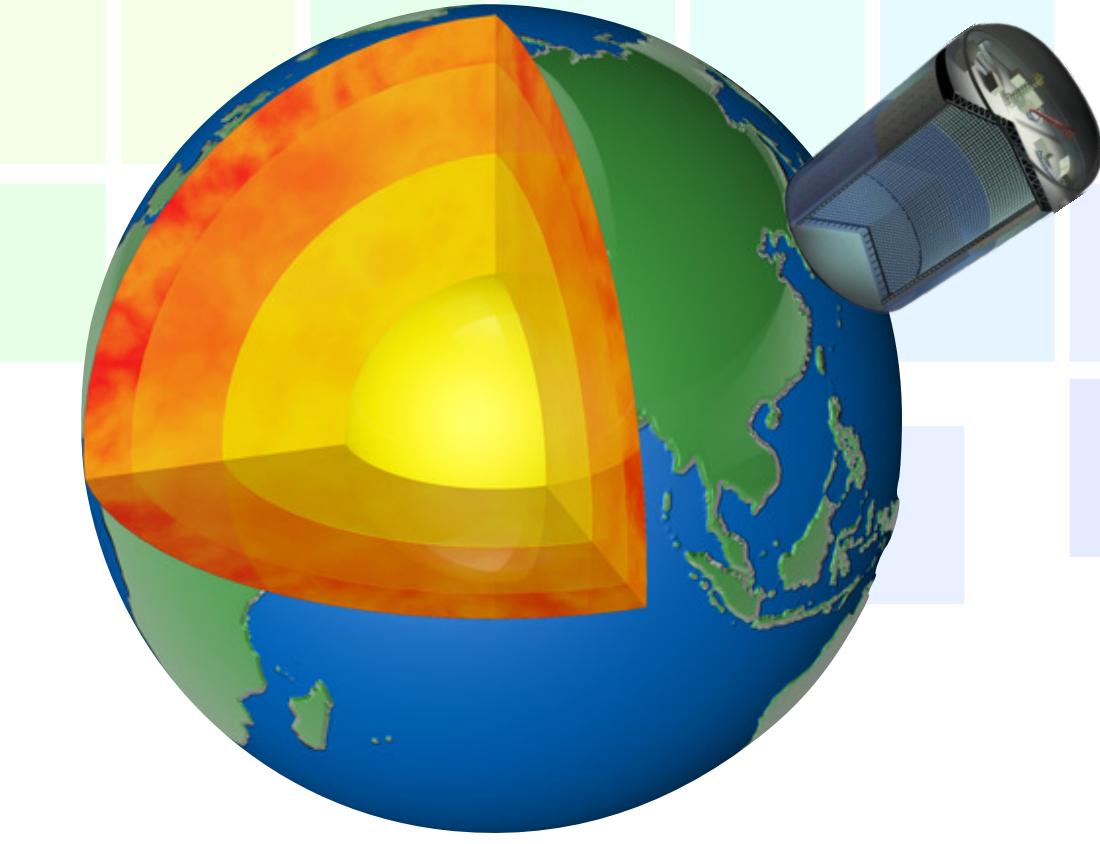
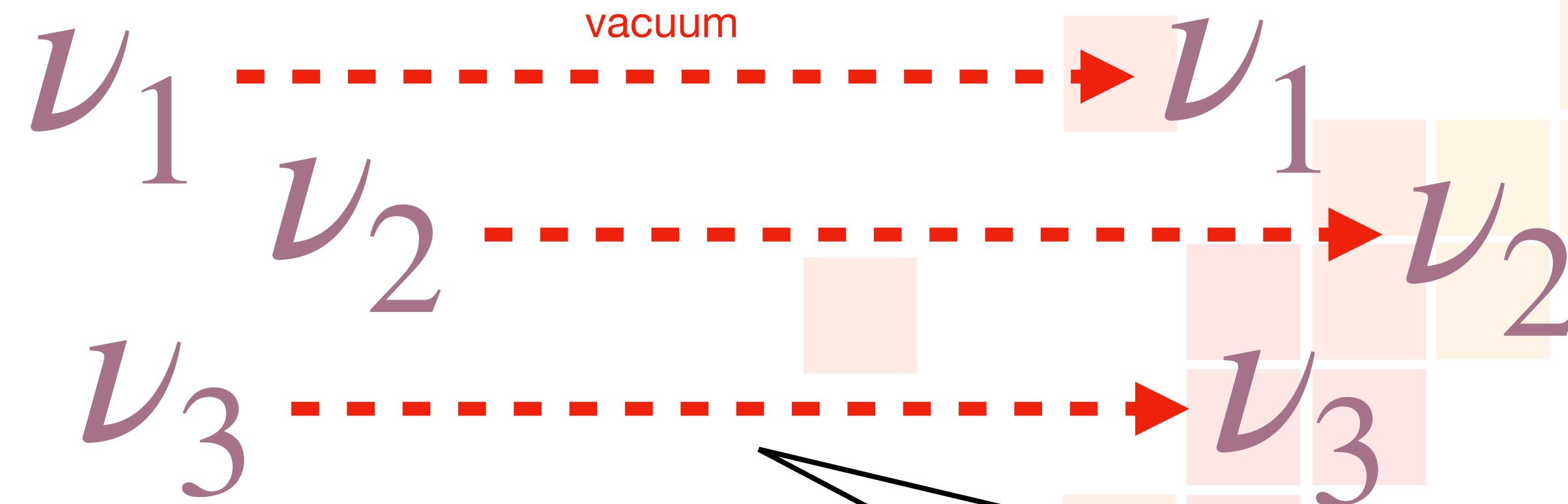
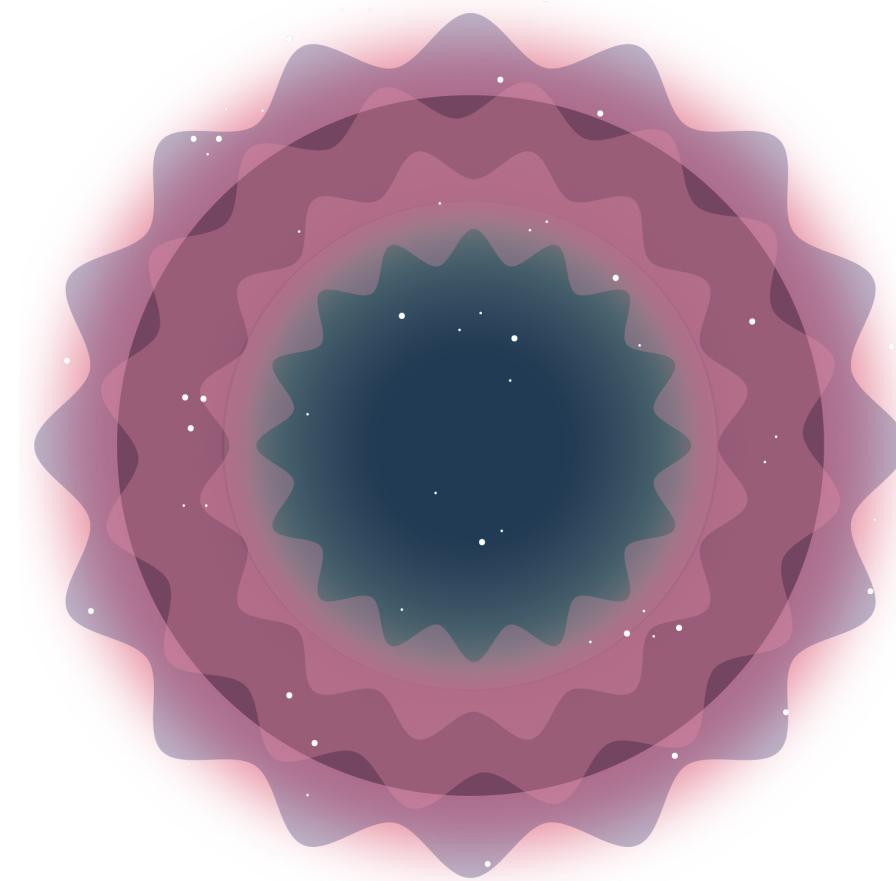
$$\begin{aligned}\nu_e &\rightarrow \nu_3 \\ \bar{\nu}_e &\rightarrow \bar{\nu}_1\end{aligned}$$

SN adiabatic transitions in IO

$$\begin{aligned}\nu_e &\rightarrow \nu_2 \\ \bar{\nu}_e &\rightarrow \bar{\nu}_3\end{aligned}$$



Supernova neutrino journey



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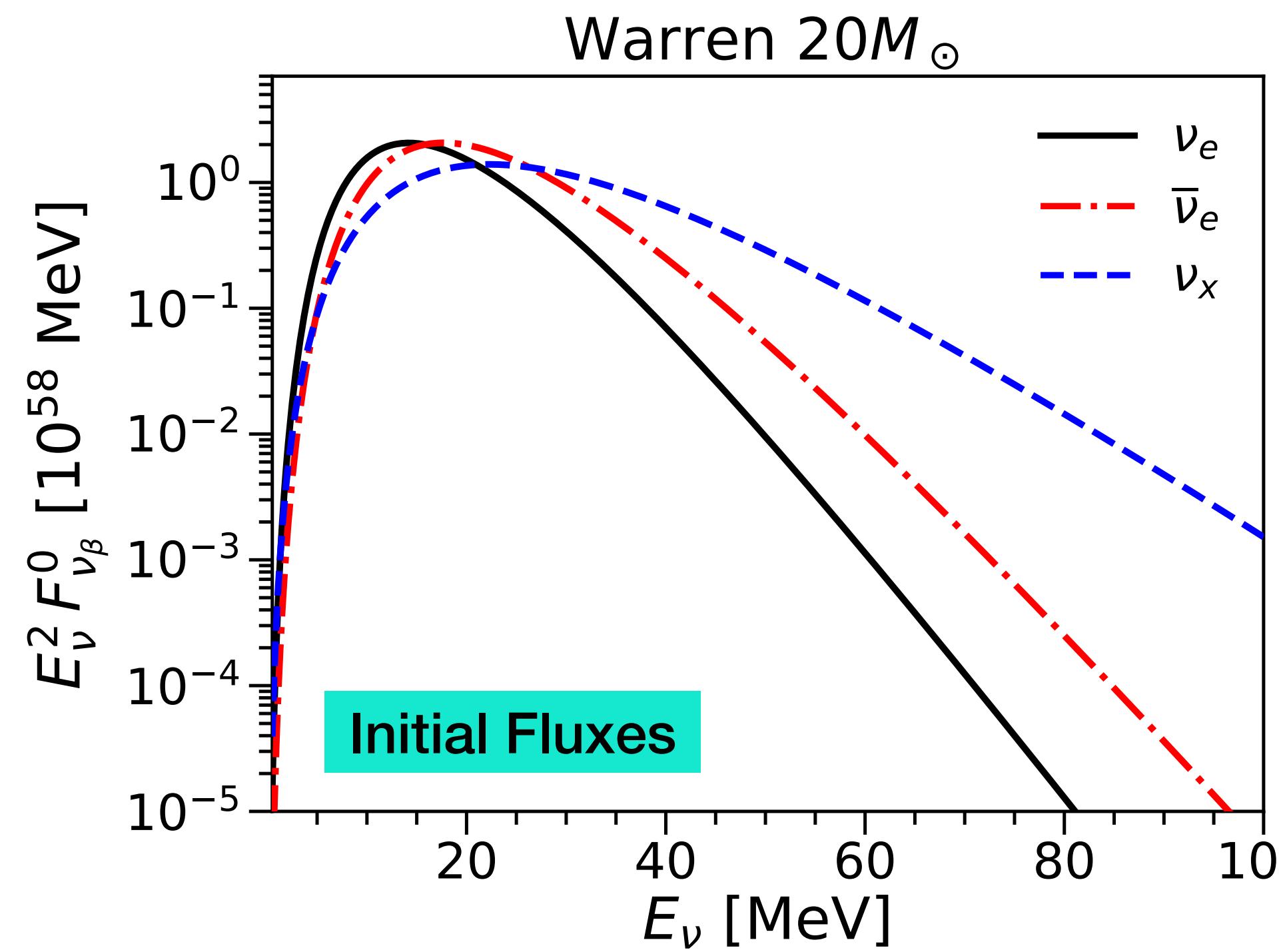
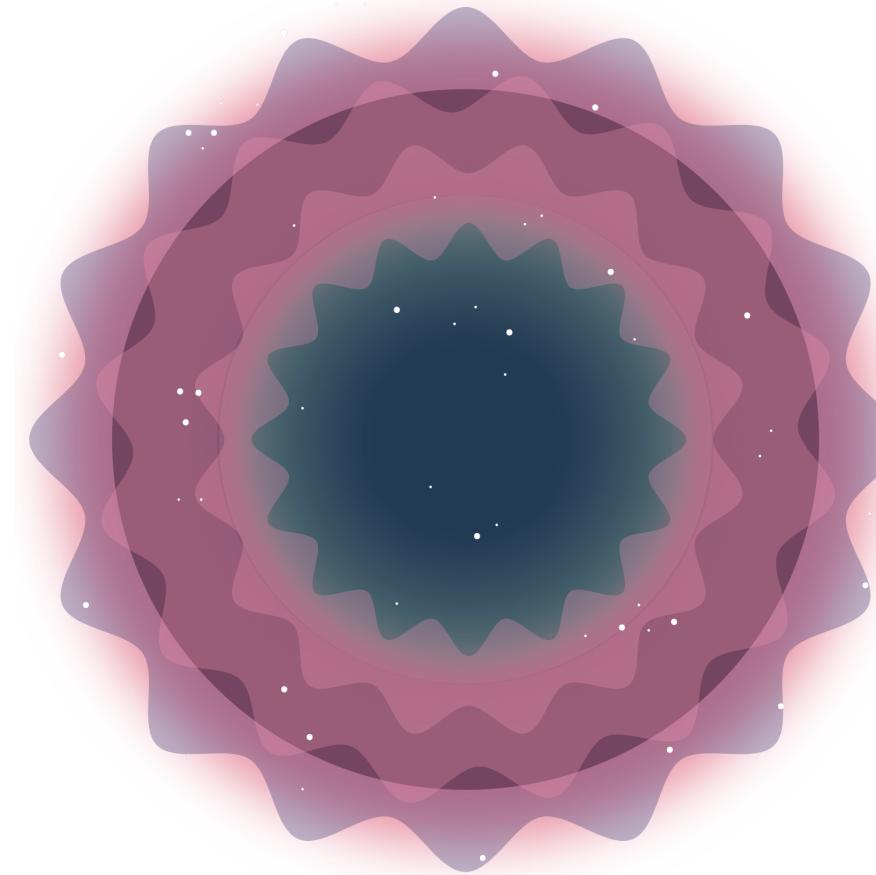
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Vacuum transport

$$\mathcal{H}_{\text{mass}} = \frac{1}{2E} \mathbb{M}^2$$

$$\mathbb{M}^2 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix}$$

Supernova neutrino journey

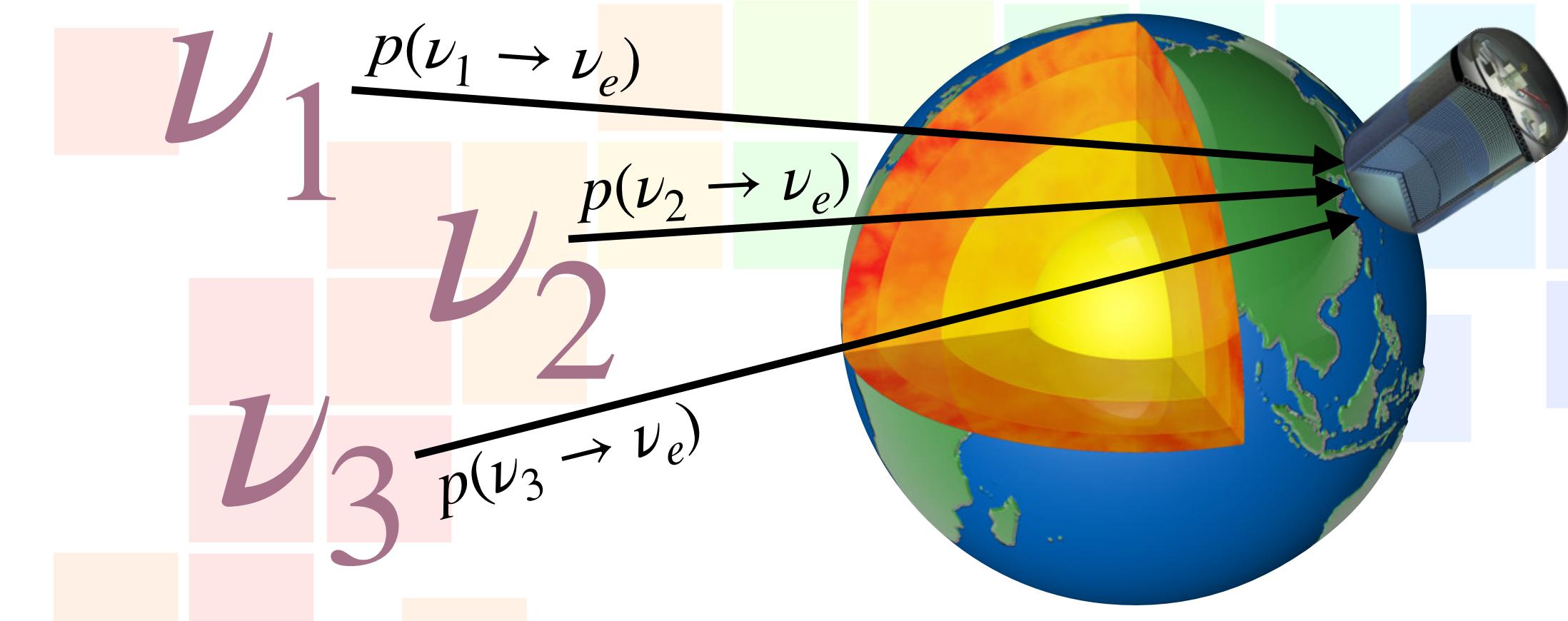


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Earth matter effects
(constant ρ)

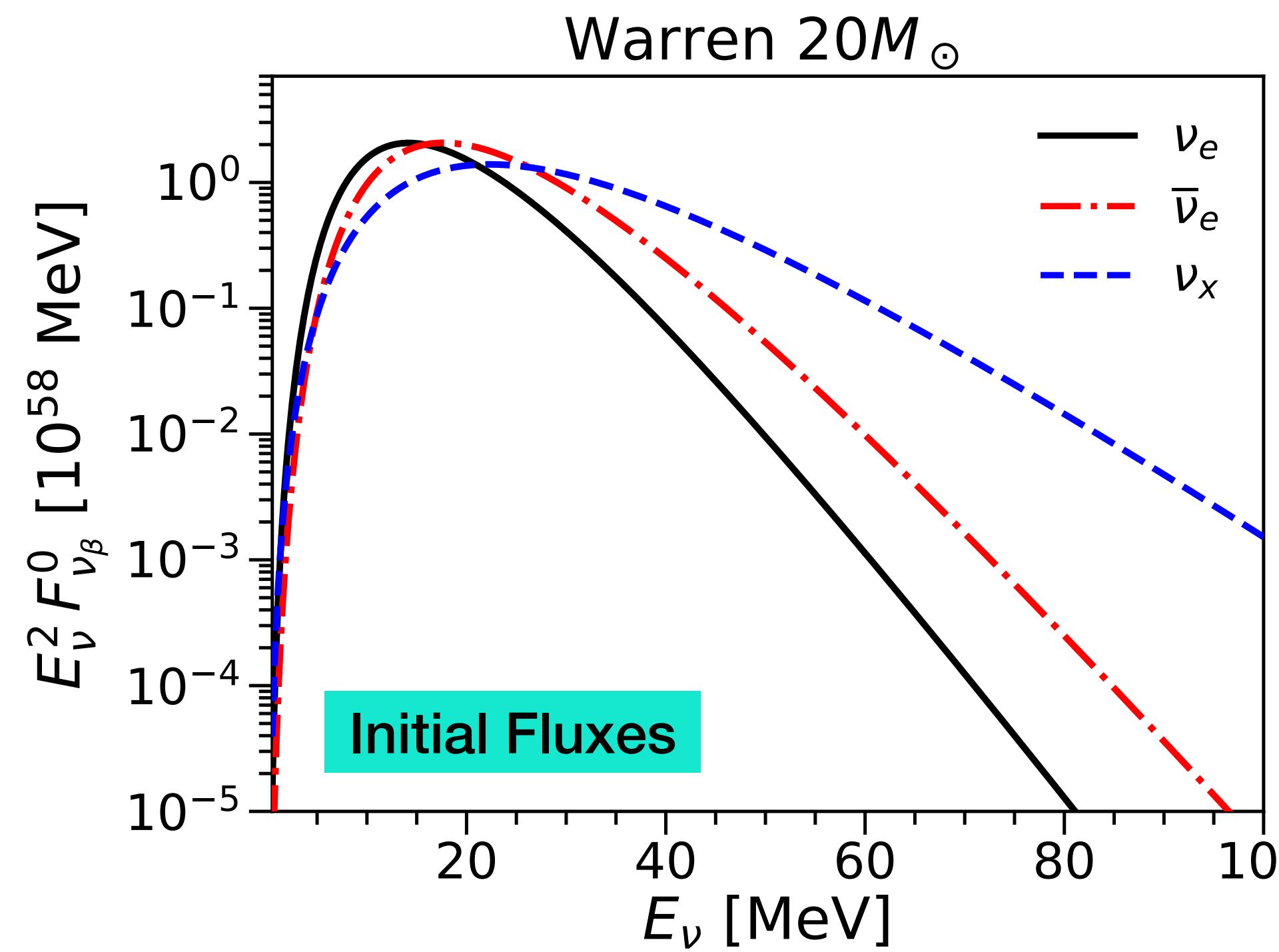
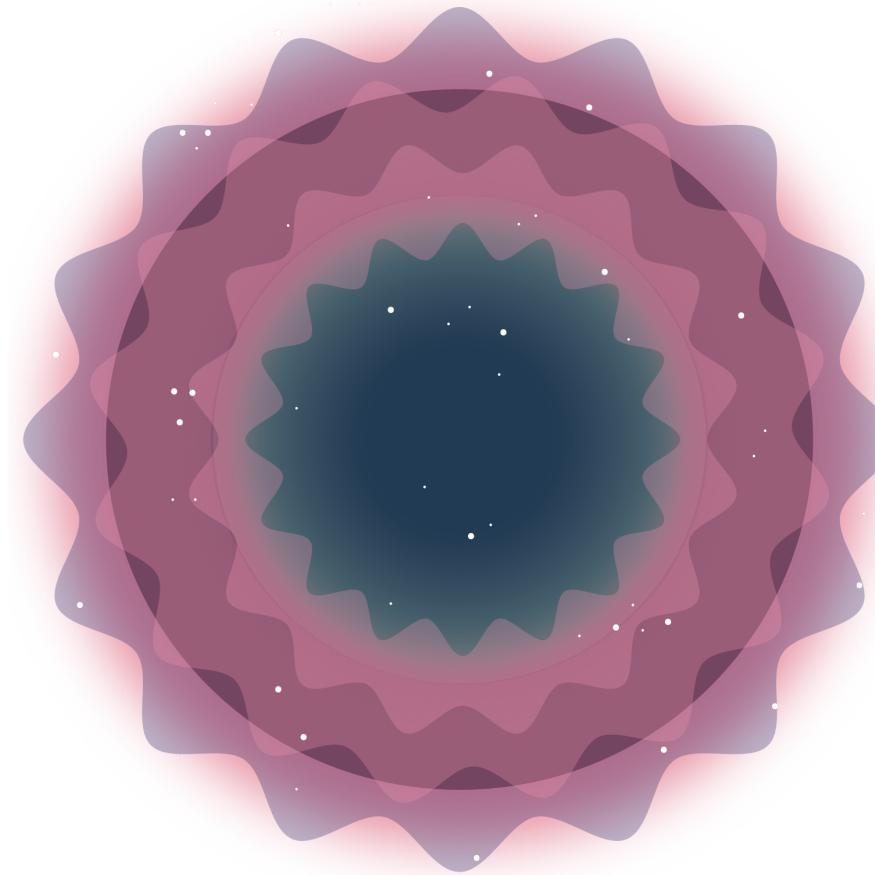
$$p_{\oplus}^{\text{NO}} \equiv P_{\oplus}(\nu_3 \rightarrow \nu_e) \simeq \sin^2 \theta_{13}$$

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Supernova neutrino journey

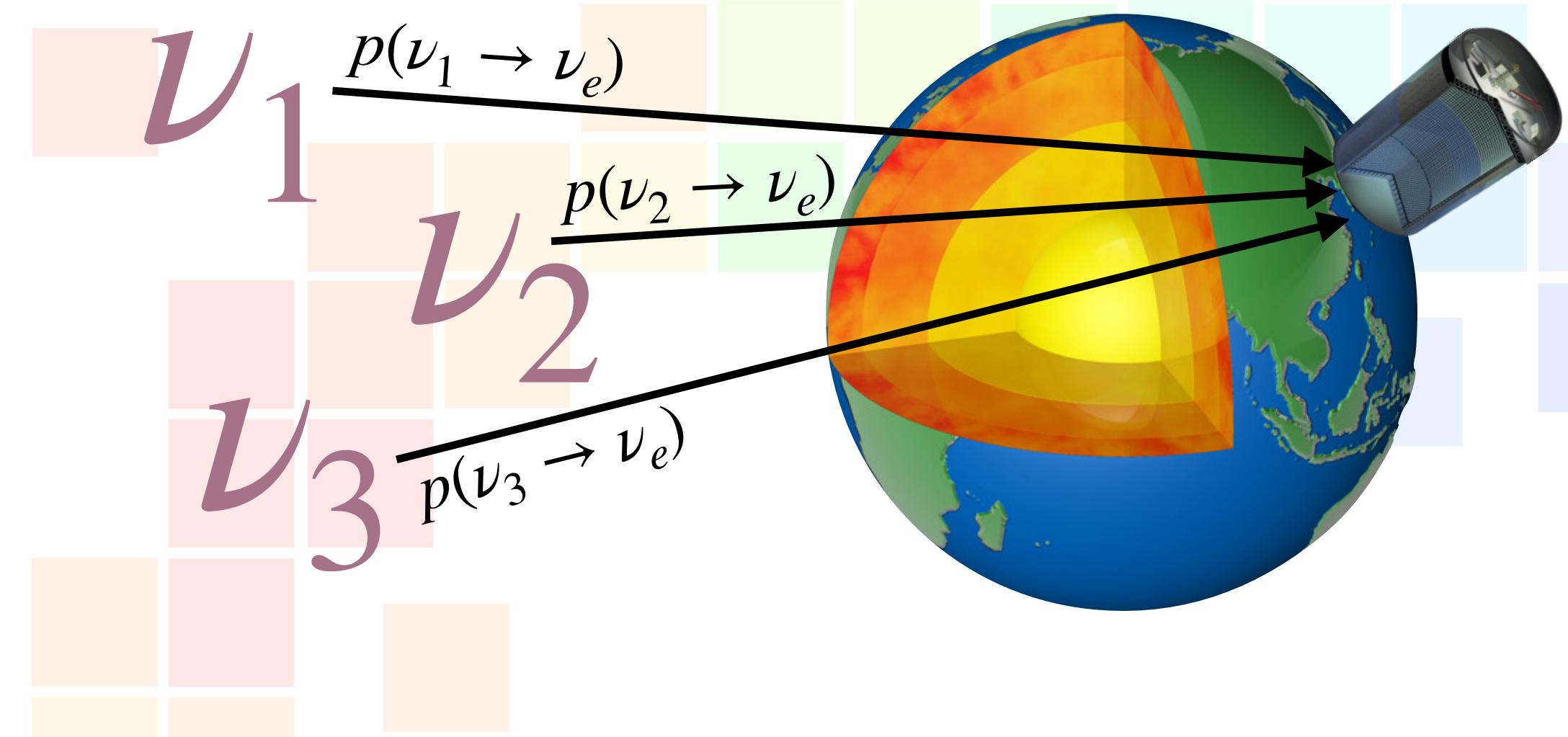


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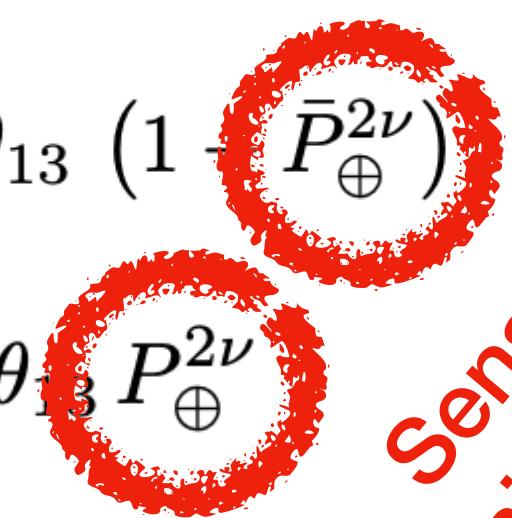
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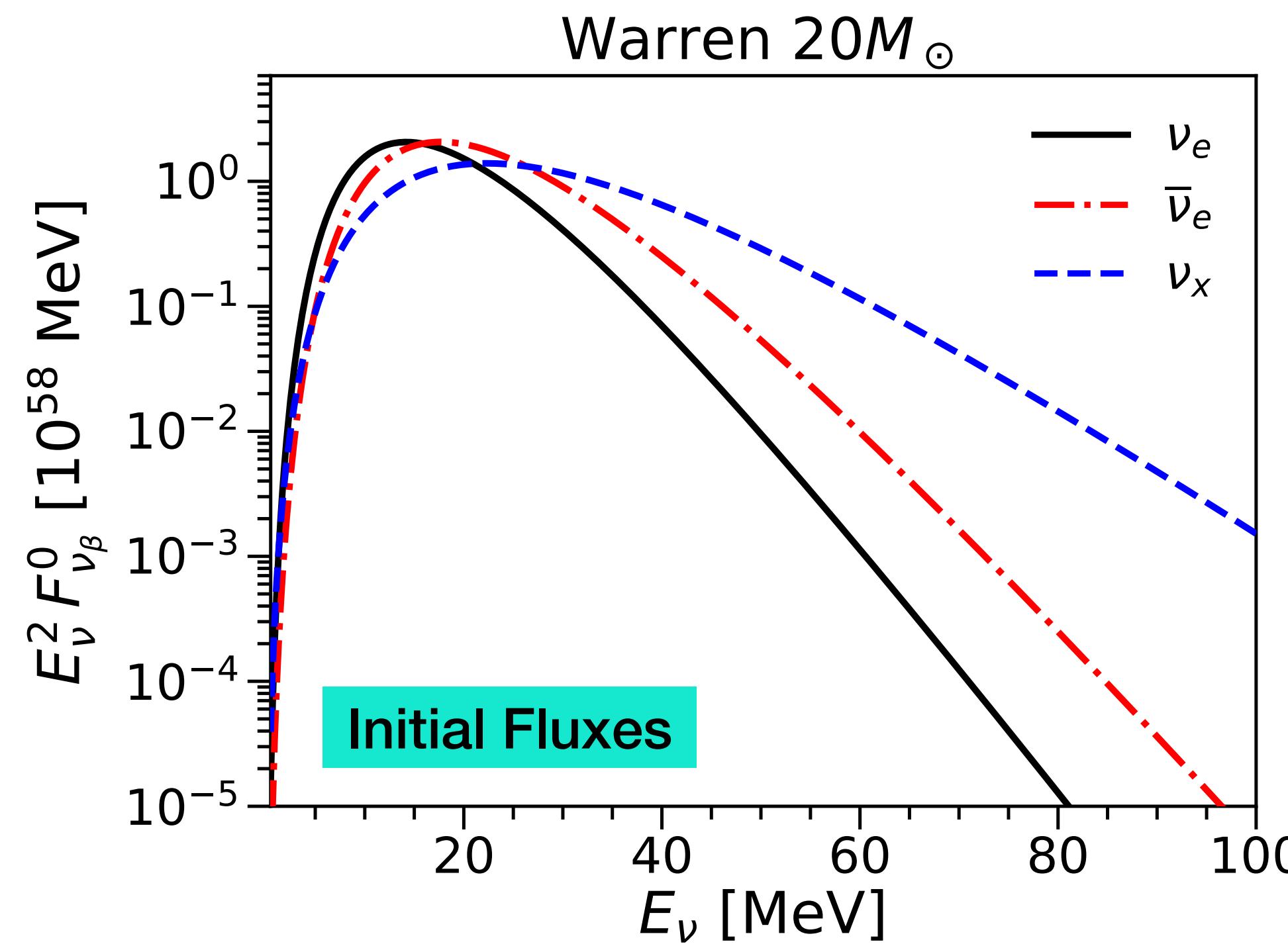
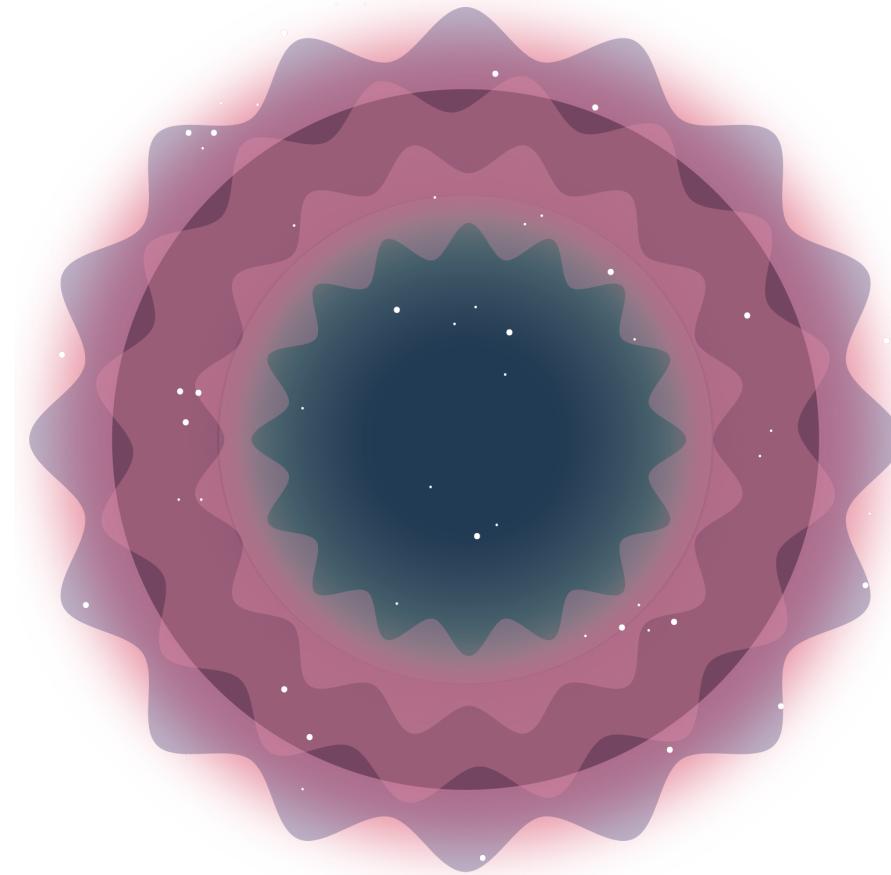
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Sensitive to solar mixing parameters!

Supernova neutrino journey

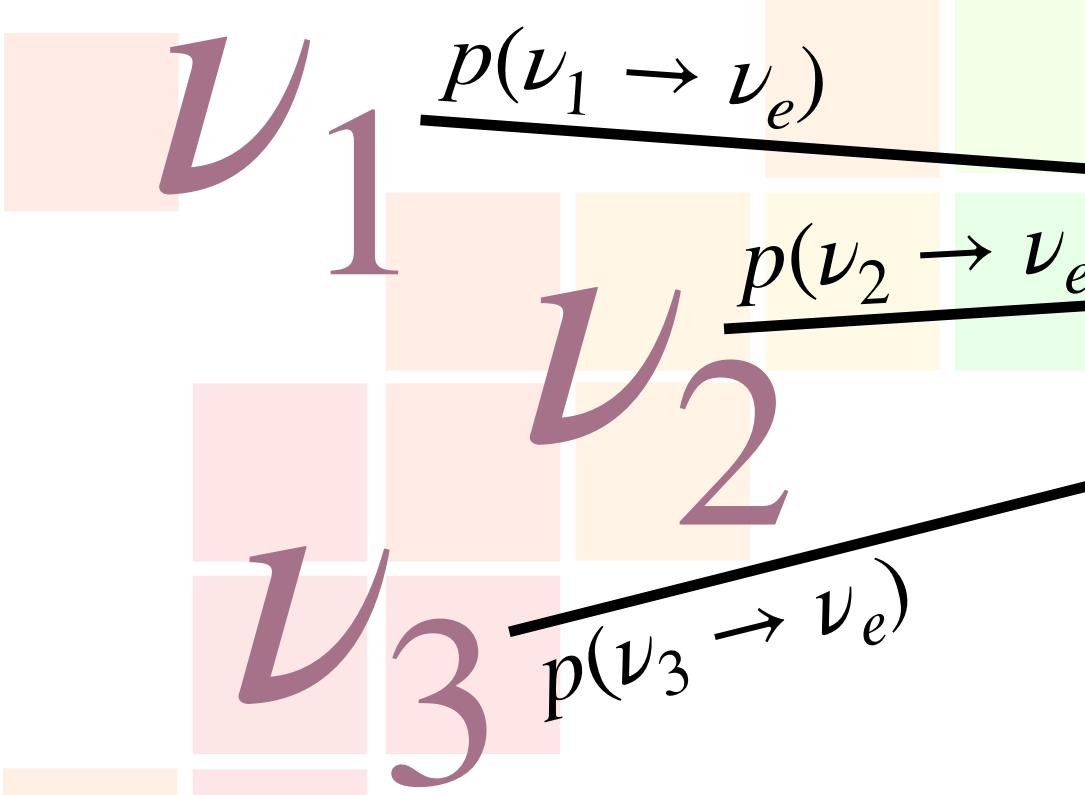


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HK detection
$\bar{\nu}_e + p \rightarrow e^+ + n$
$\nu_e + {}^{16}\text{O} \rightarrow e^- + X$
$\bar{\nu}_e + {}^{16}\text{O} \rightarrow e^+ + X$
$N_t^p = 2.94 \cdot 10^{34}$
0.9 IBD
0.1 IBD +
$\nu_e \text{O - CC} +$
$\bar{\nu}_e \text{O - CC}$

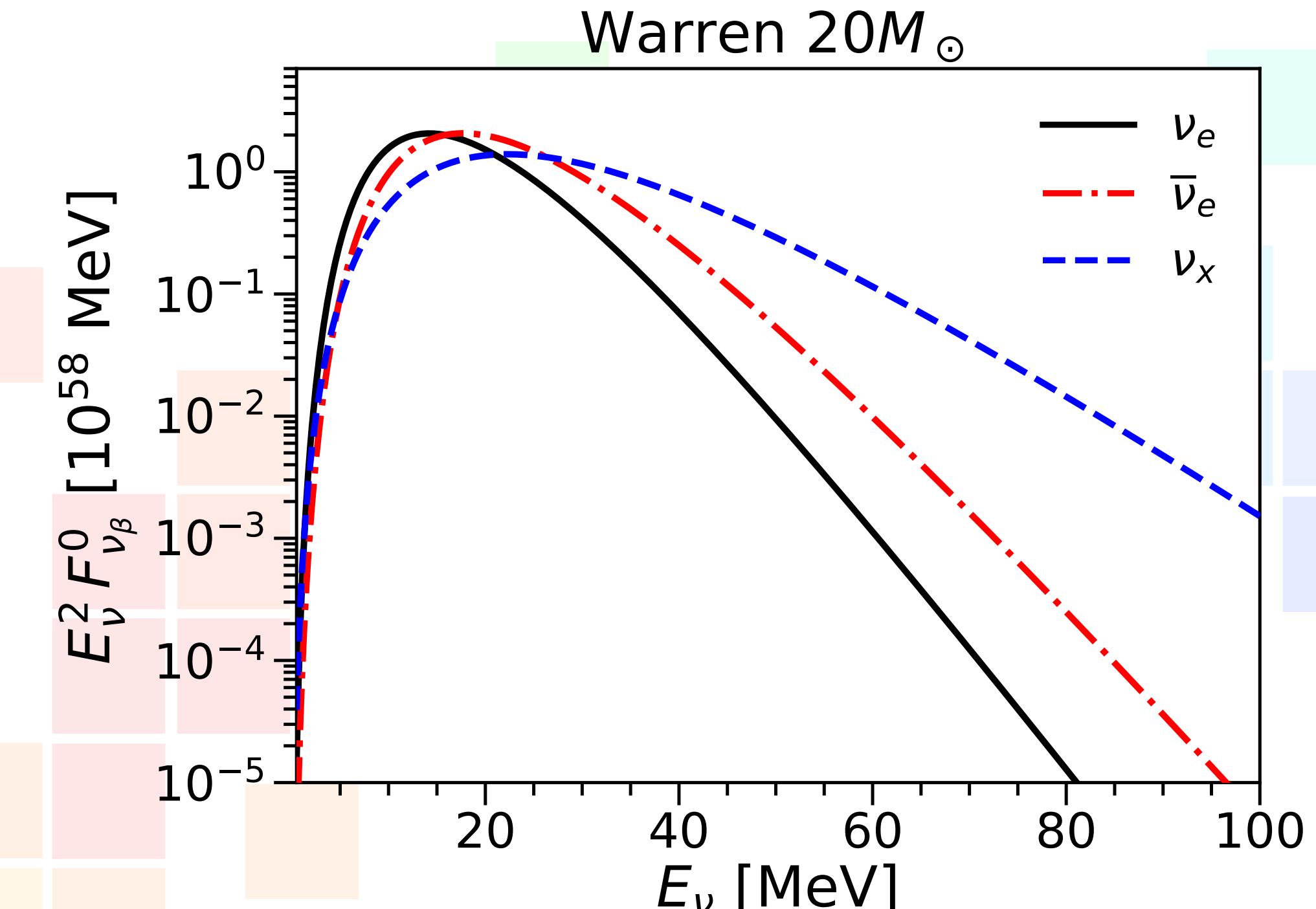
Solar mixing parameters

- Fluxes at the detector:

$$F_{\nu_e}^D = p(\epsilon) F_{\nu_e}^0 + (1 - p(\epsilon)) F_{\nu_x}^0$$

$$\epsilon \equiv \frac{2 E_\nu V}{\Delta m_{21}^2} \simeq 0.12 \left(\frac{E_\nu}{20 \text{ MeV}} \right) \left(\frac{Y_e \rho}{3 \text{ g/cm}^3} \right) \left(\frac{7.5 \times 10^{-5} \text{ eV}^2}{\Delta m_{21}^2} \right)$$

- Earth matter effects contain information on the solar mixing parameters: Δm_{21}^2 and θ_{12} .



Solar mixing parameters

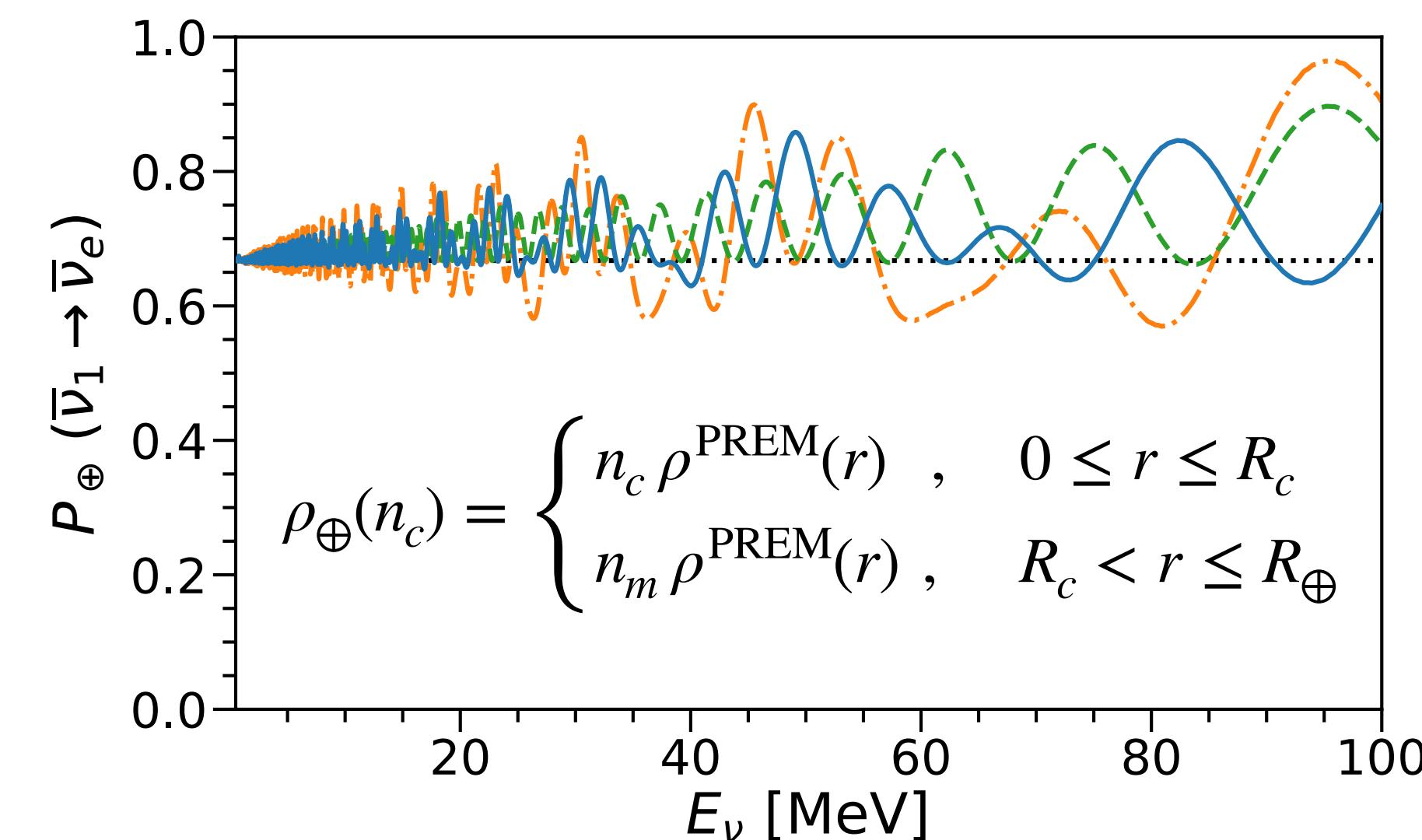
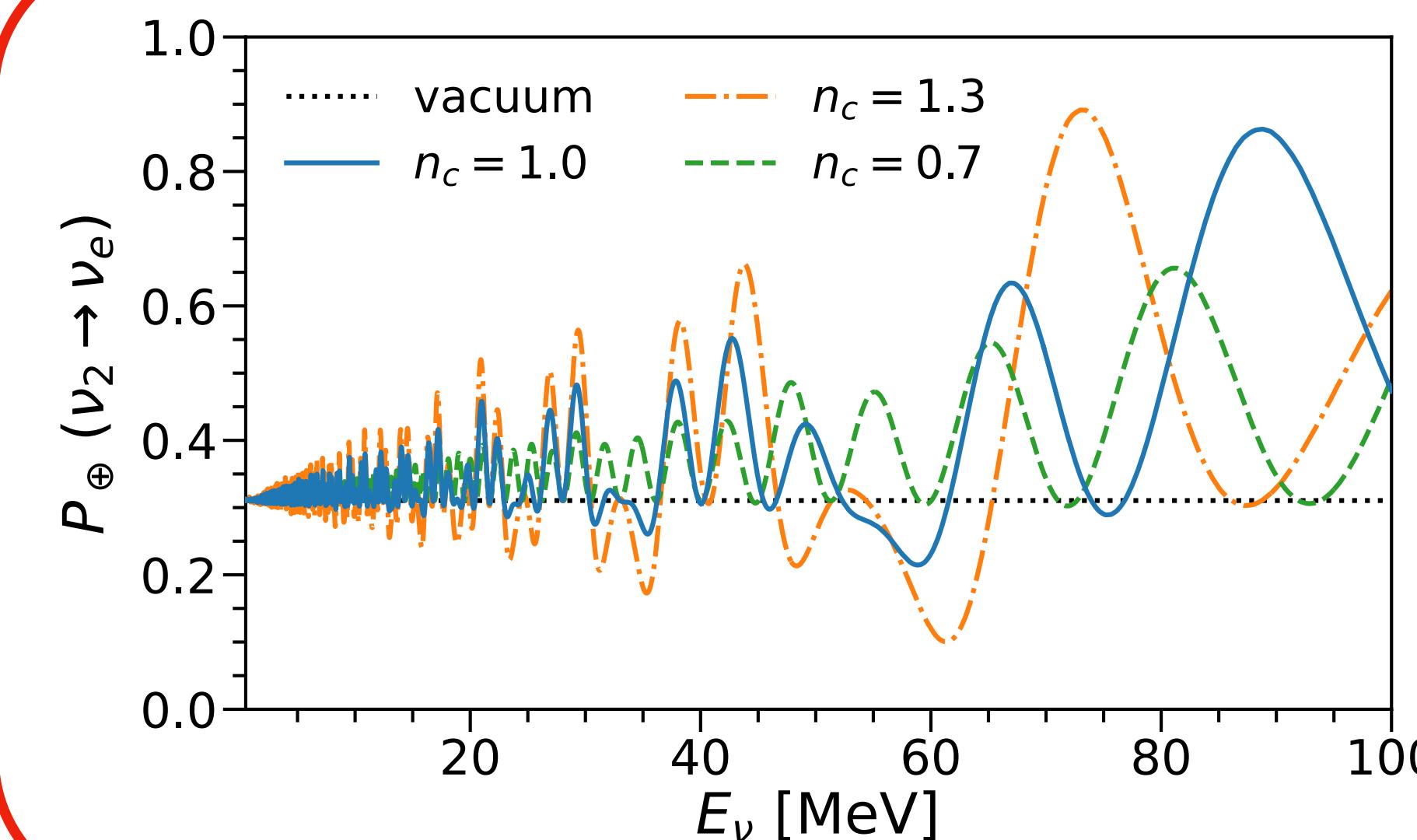
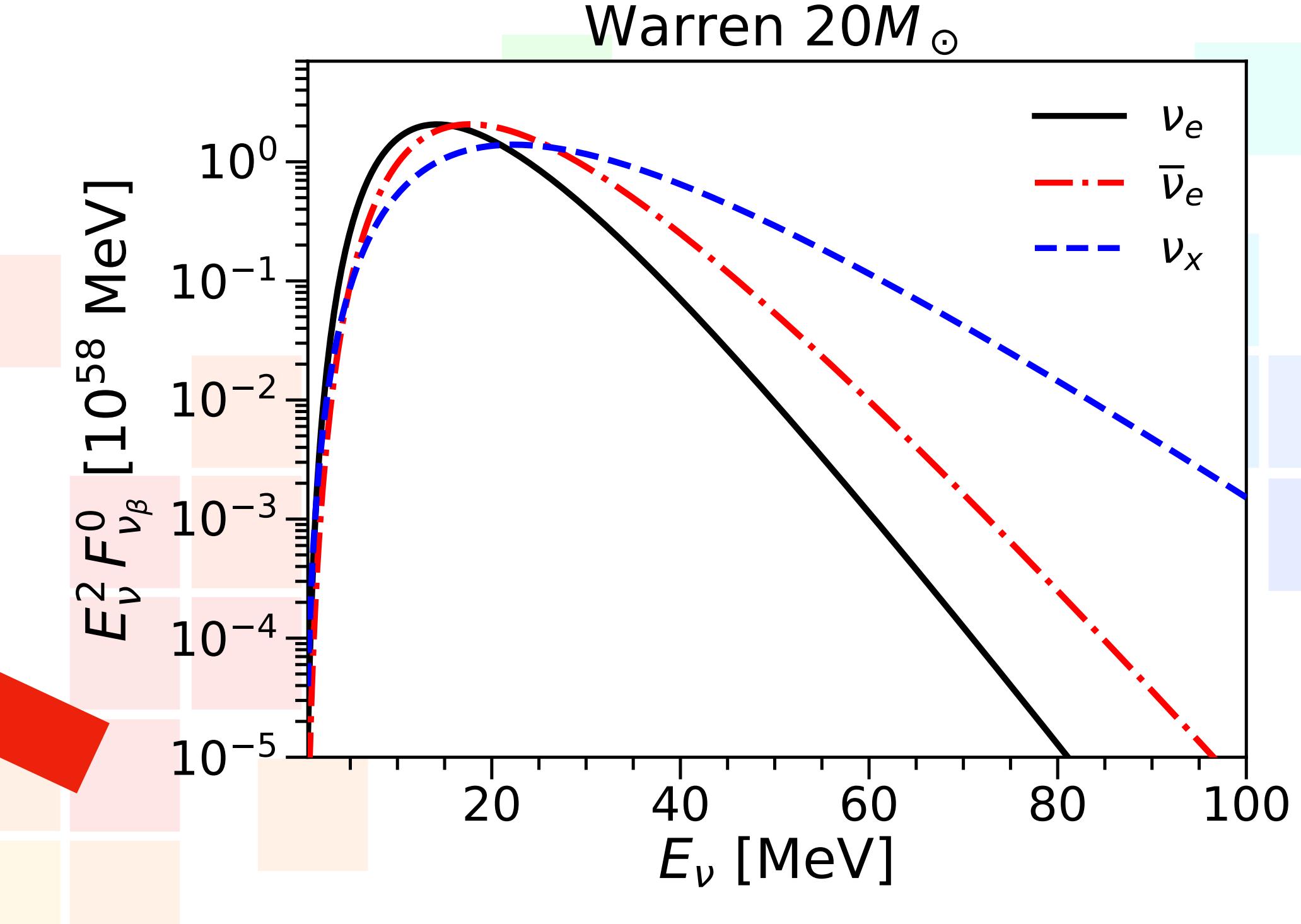
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Fix solar mass splitting

- Earth matter effects contain information on Δm_{21}^2 and θ_{12} .



Solar mixing parameters

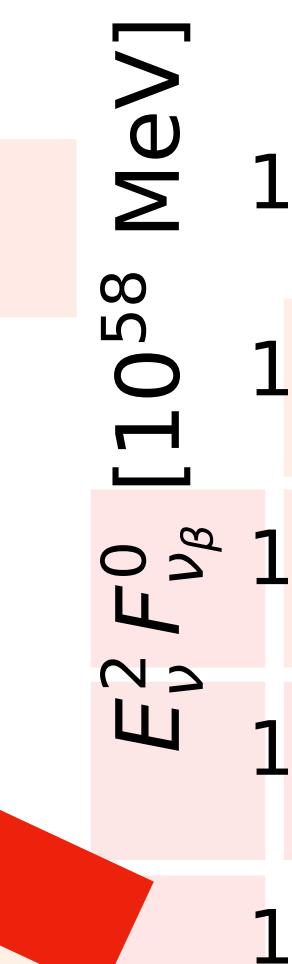
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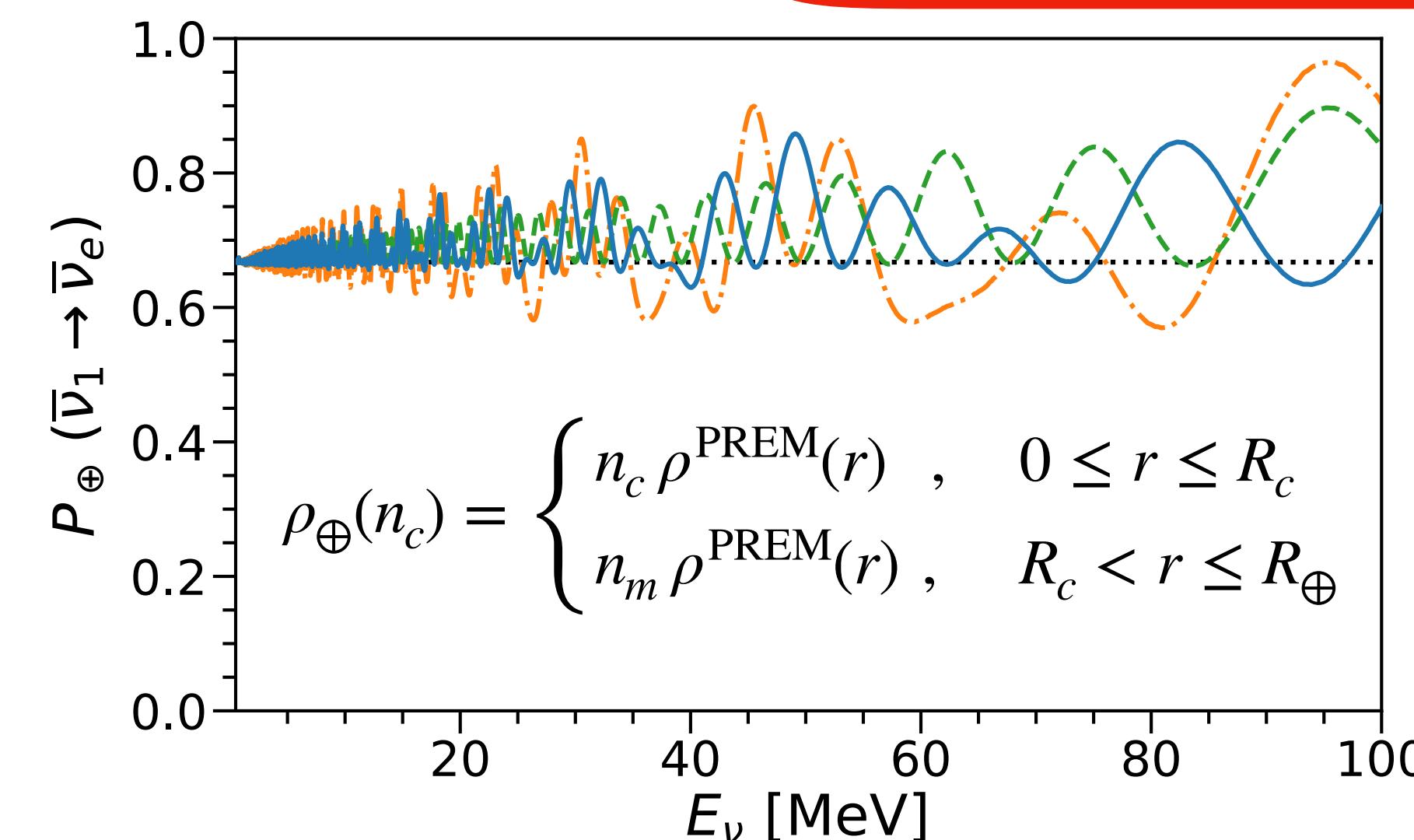
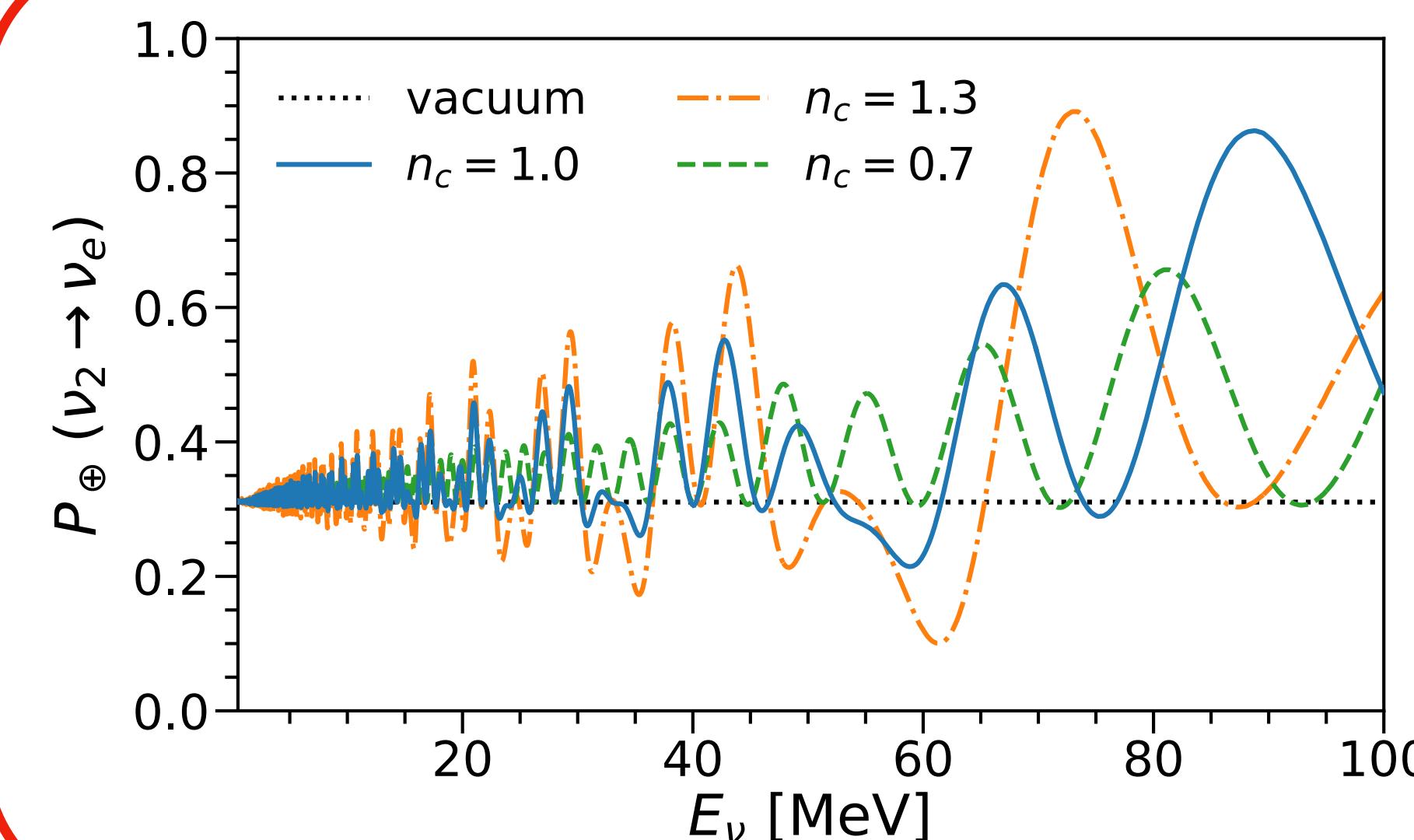
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Earth tomography with SN neutrinos
at future neutrino detectors

RH, O. Mena and
S. Palomares-Ruiz

Phys.Rev.D 108 (2023) 083011



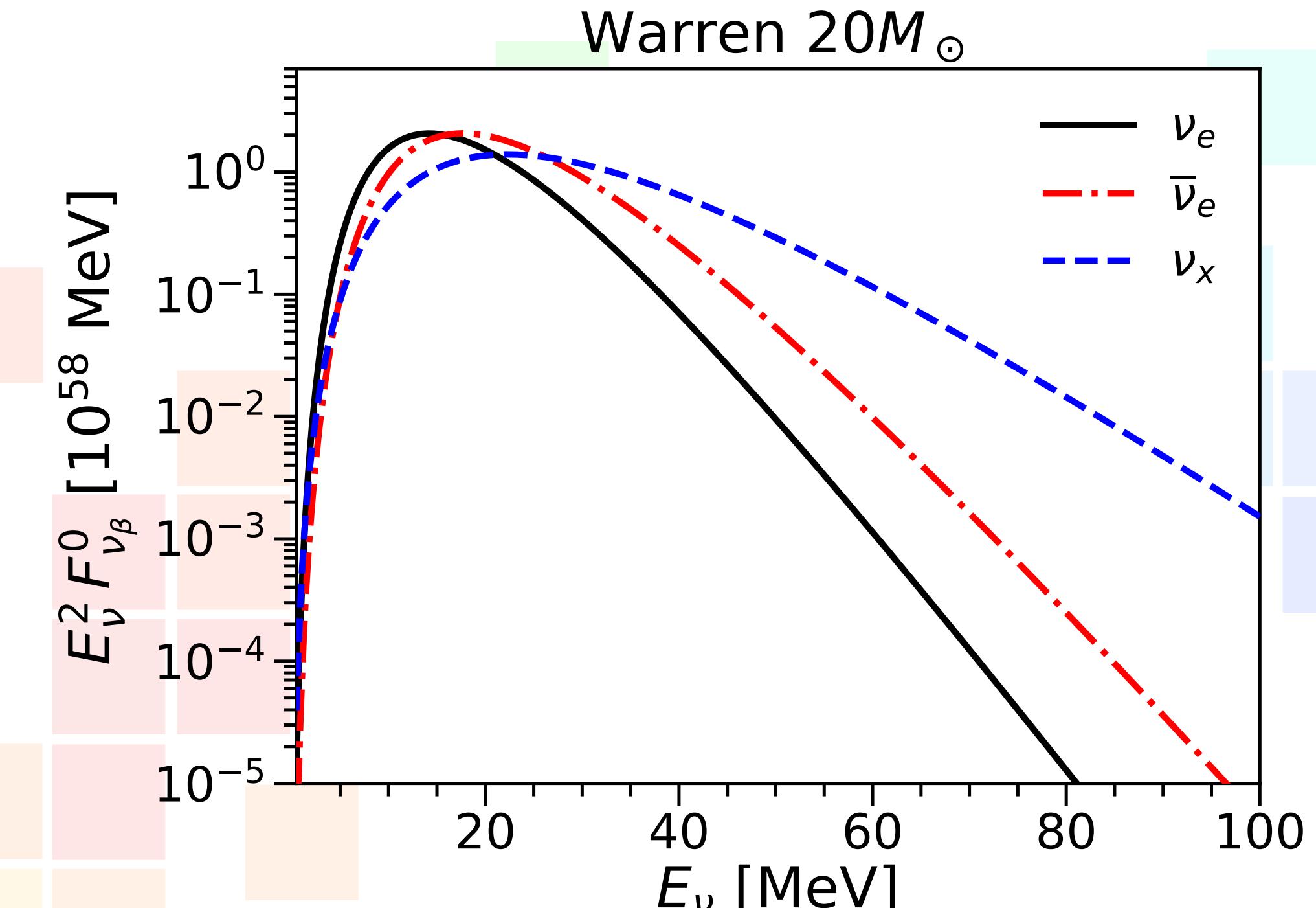
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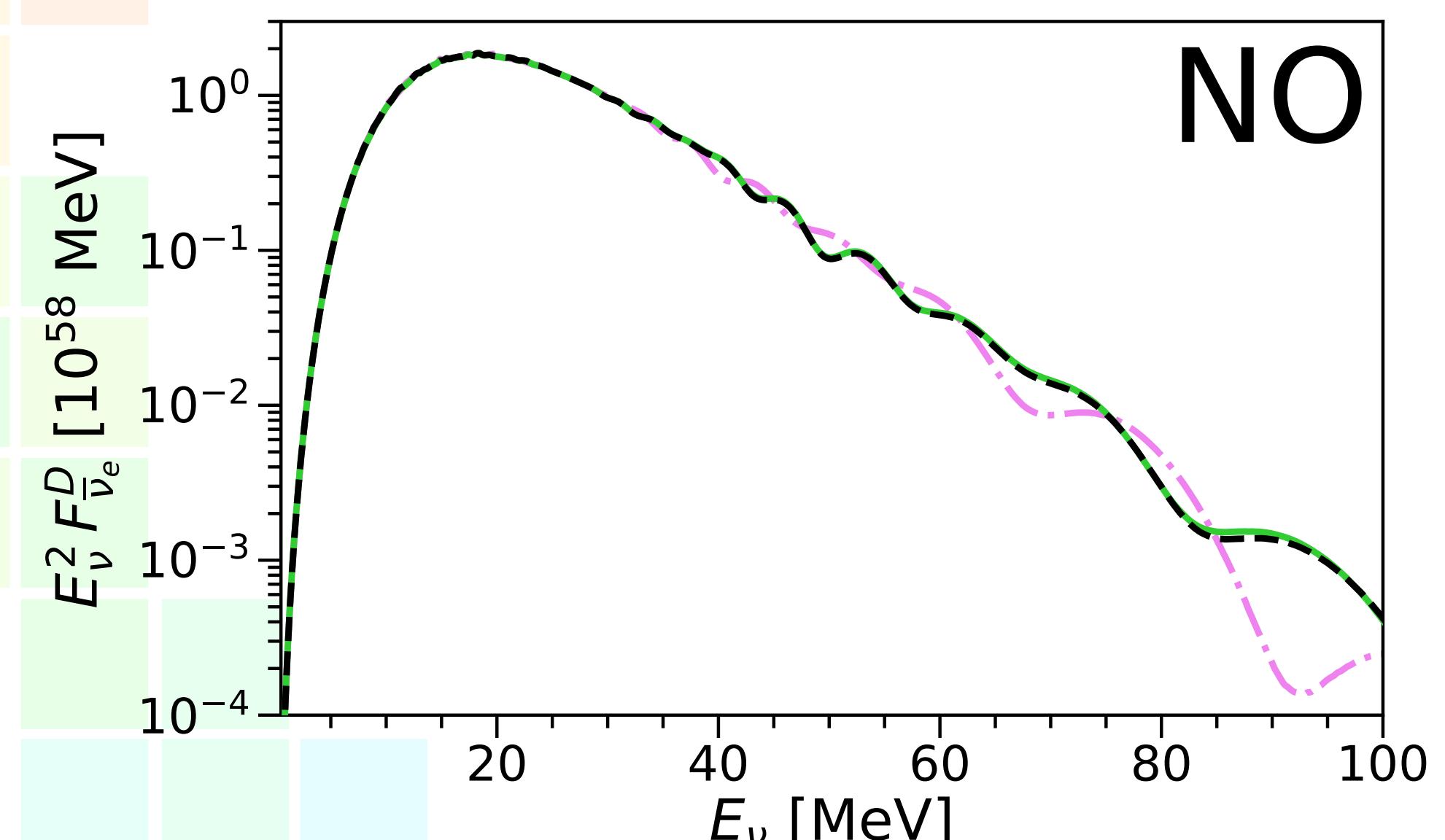
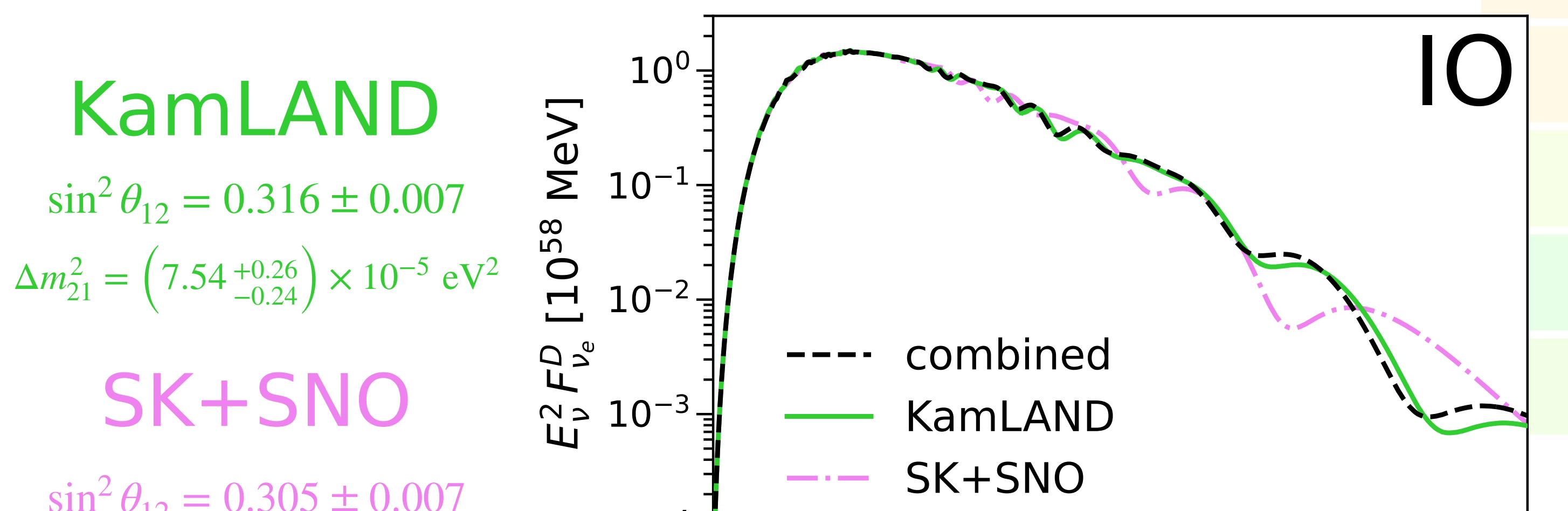
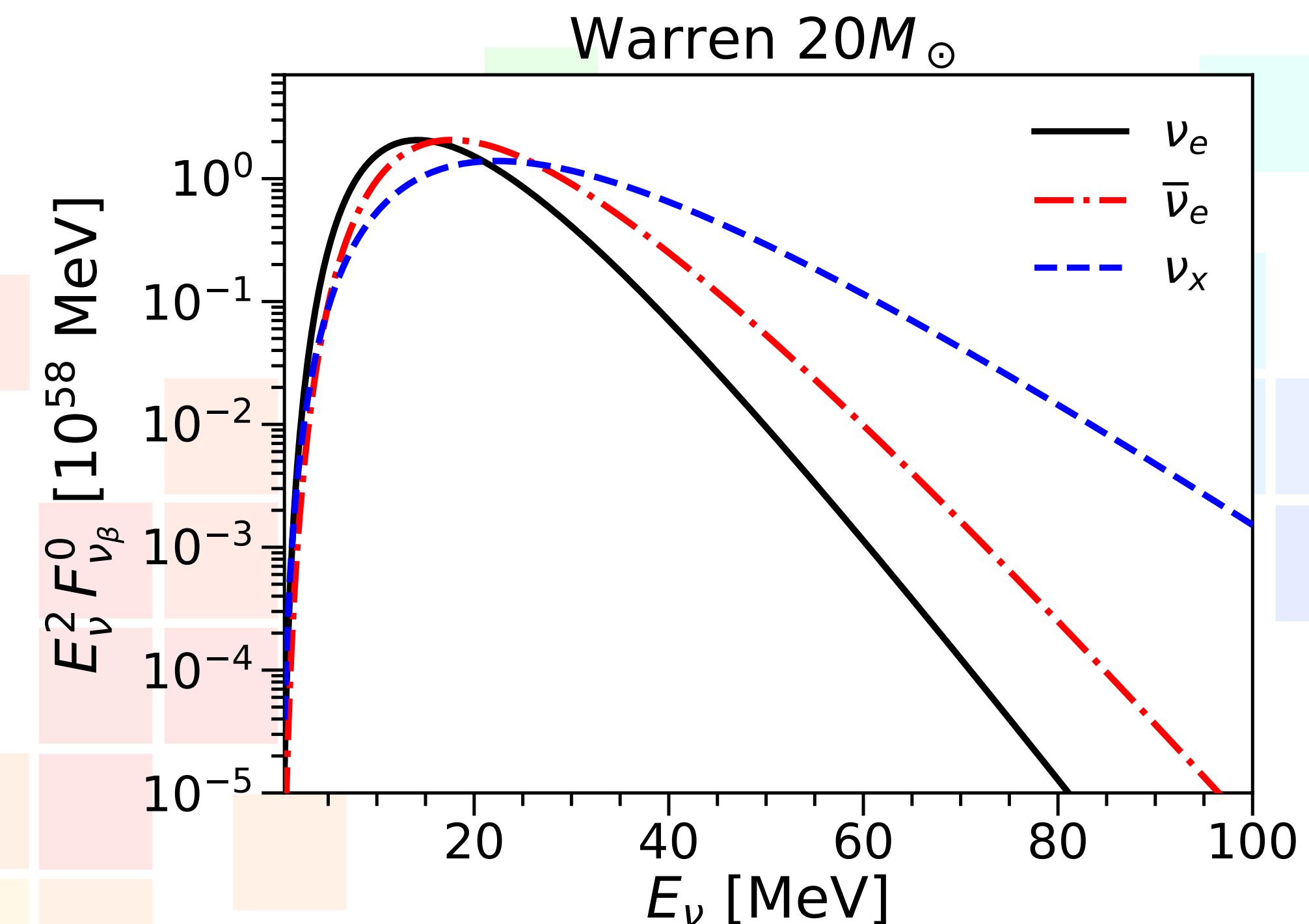
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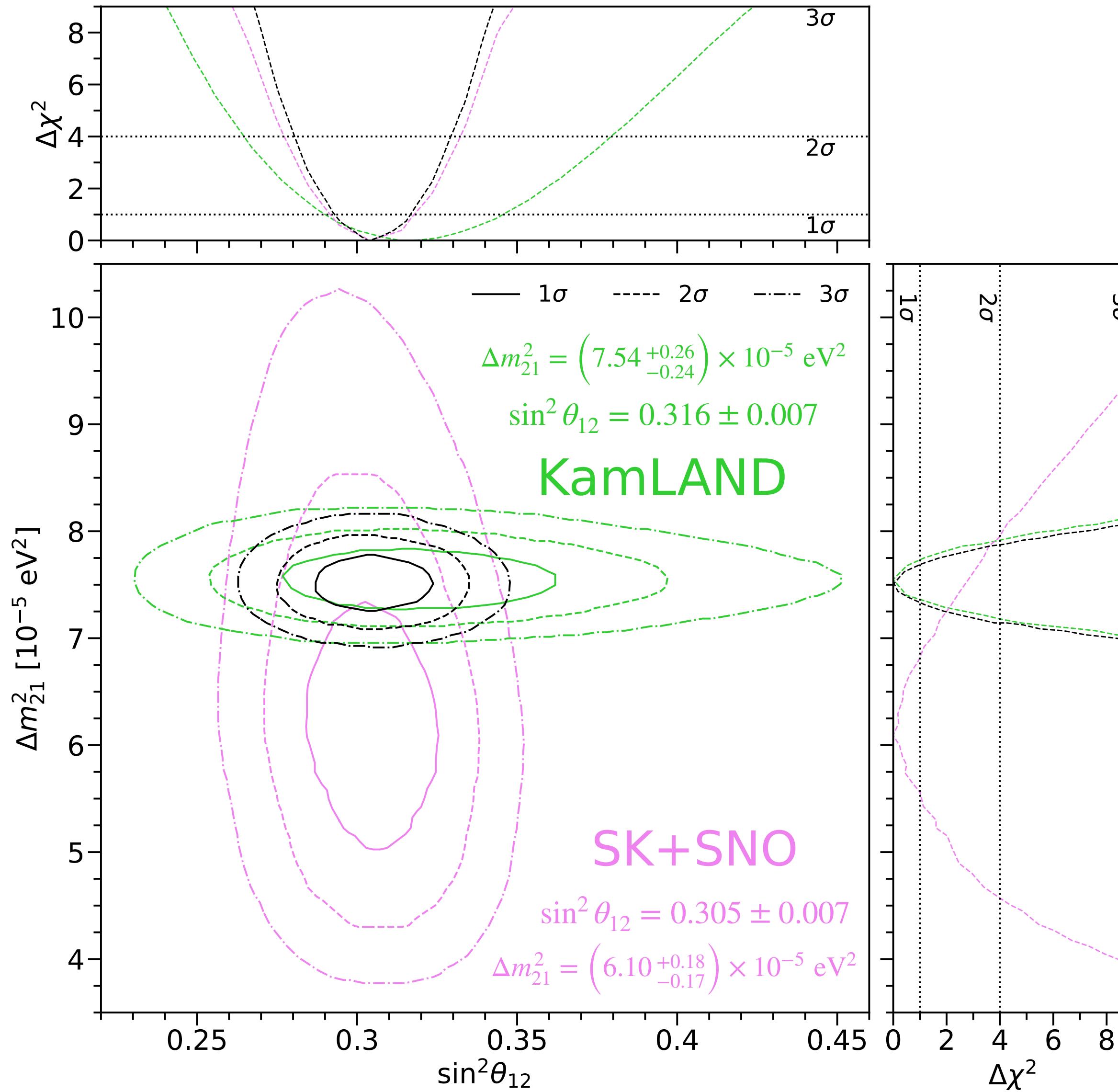
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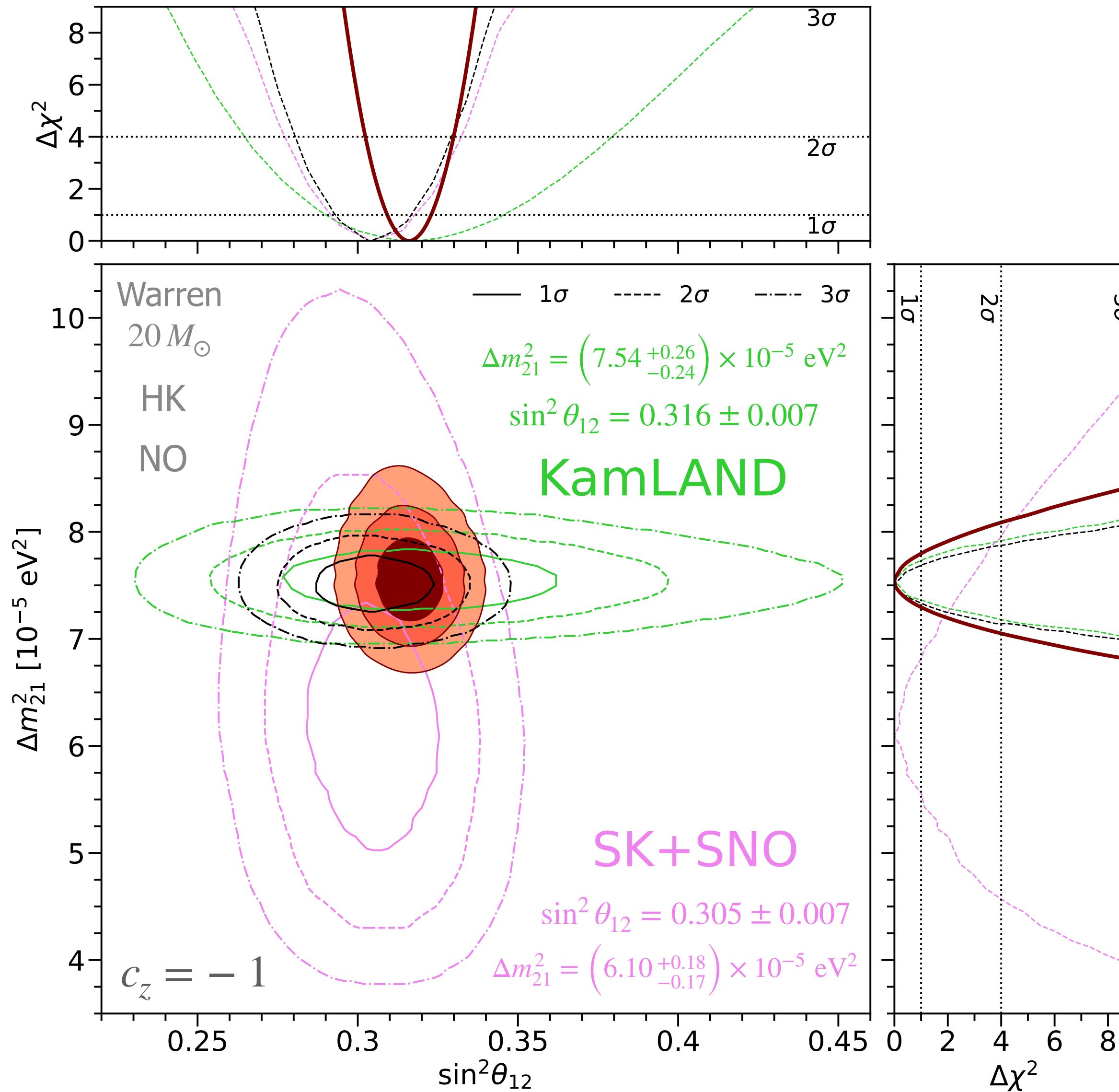


Results



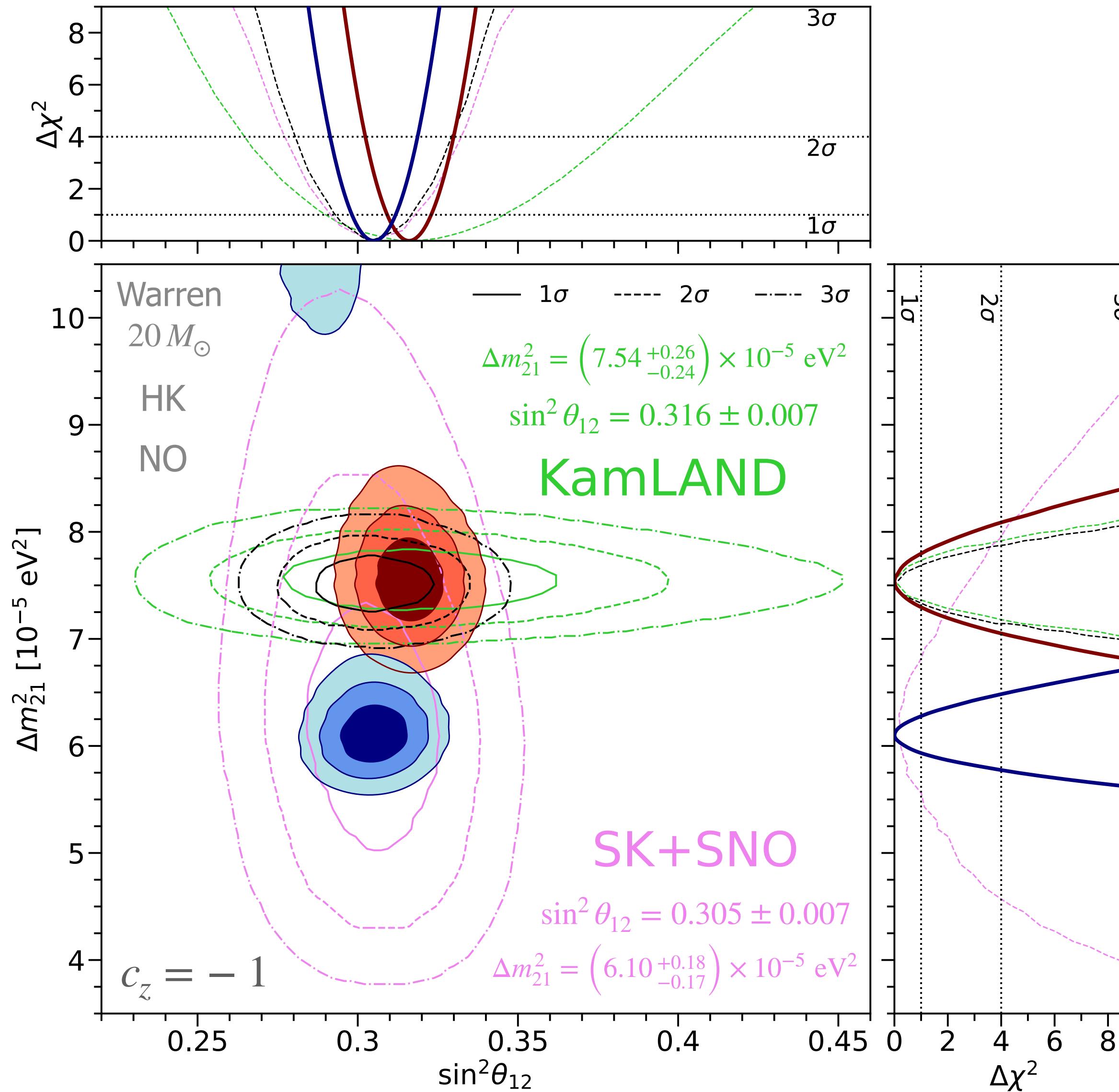
- Forecasts for a SN burst at 10 kpc.
- Current KamLAND allowed regions
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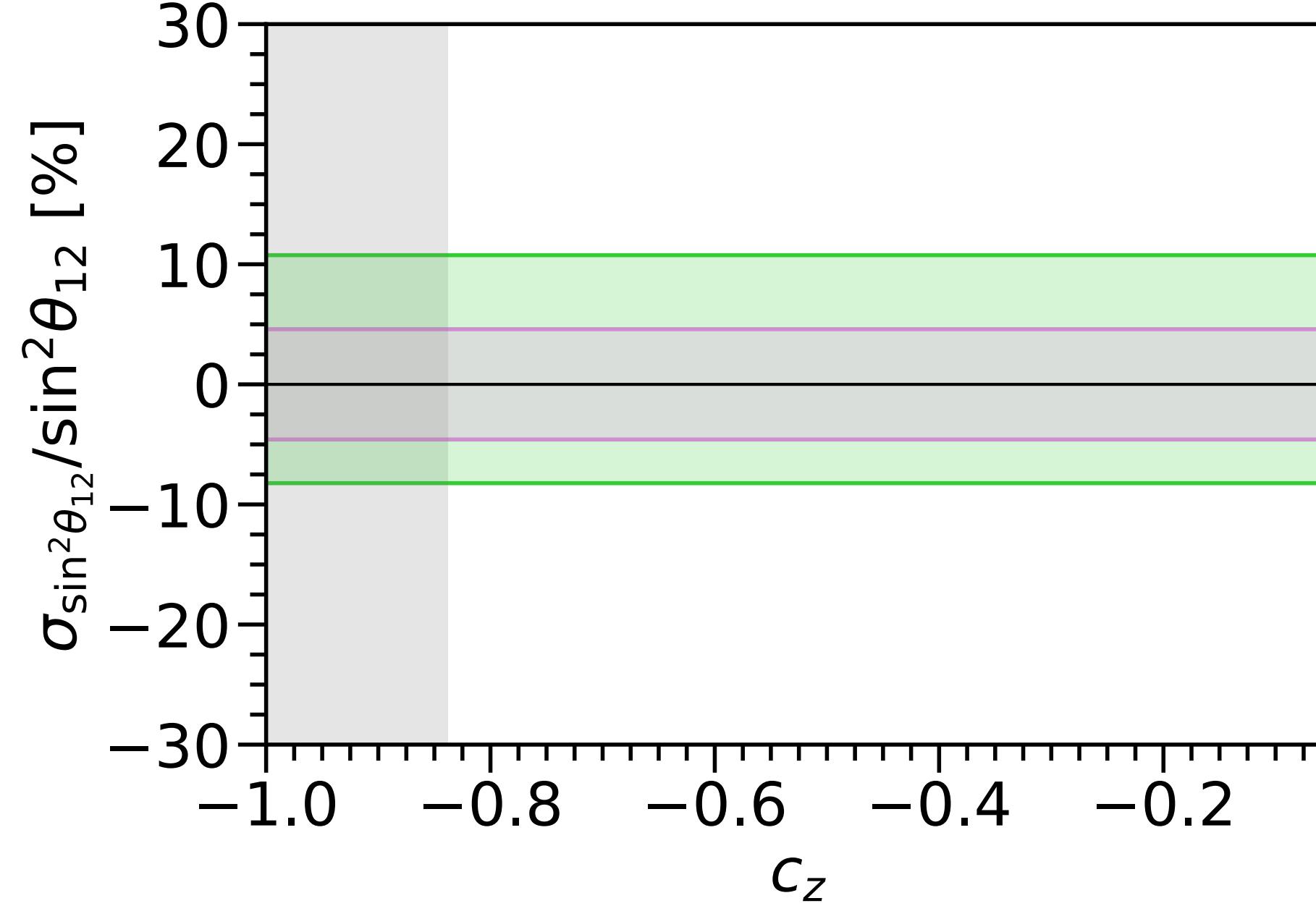
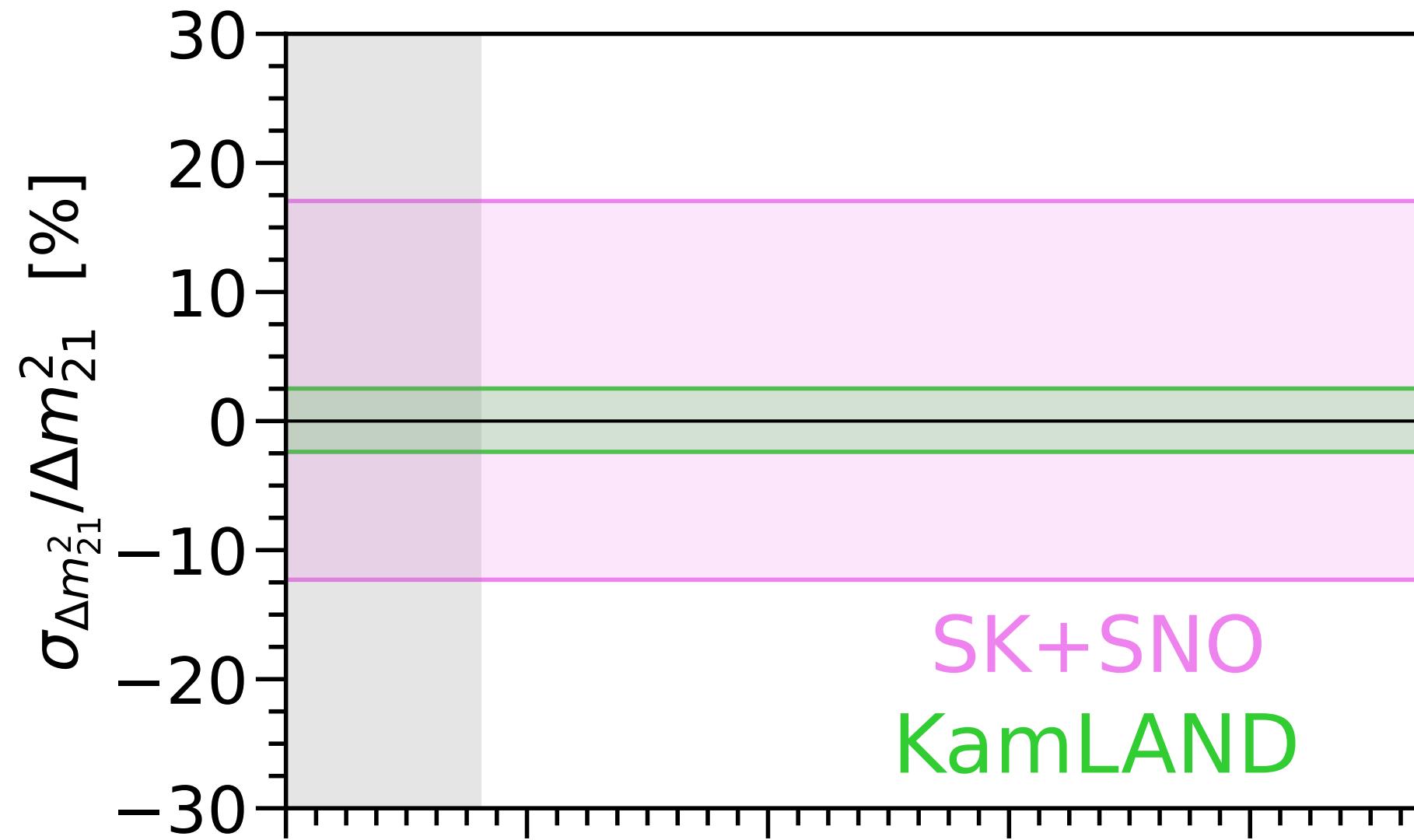
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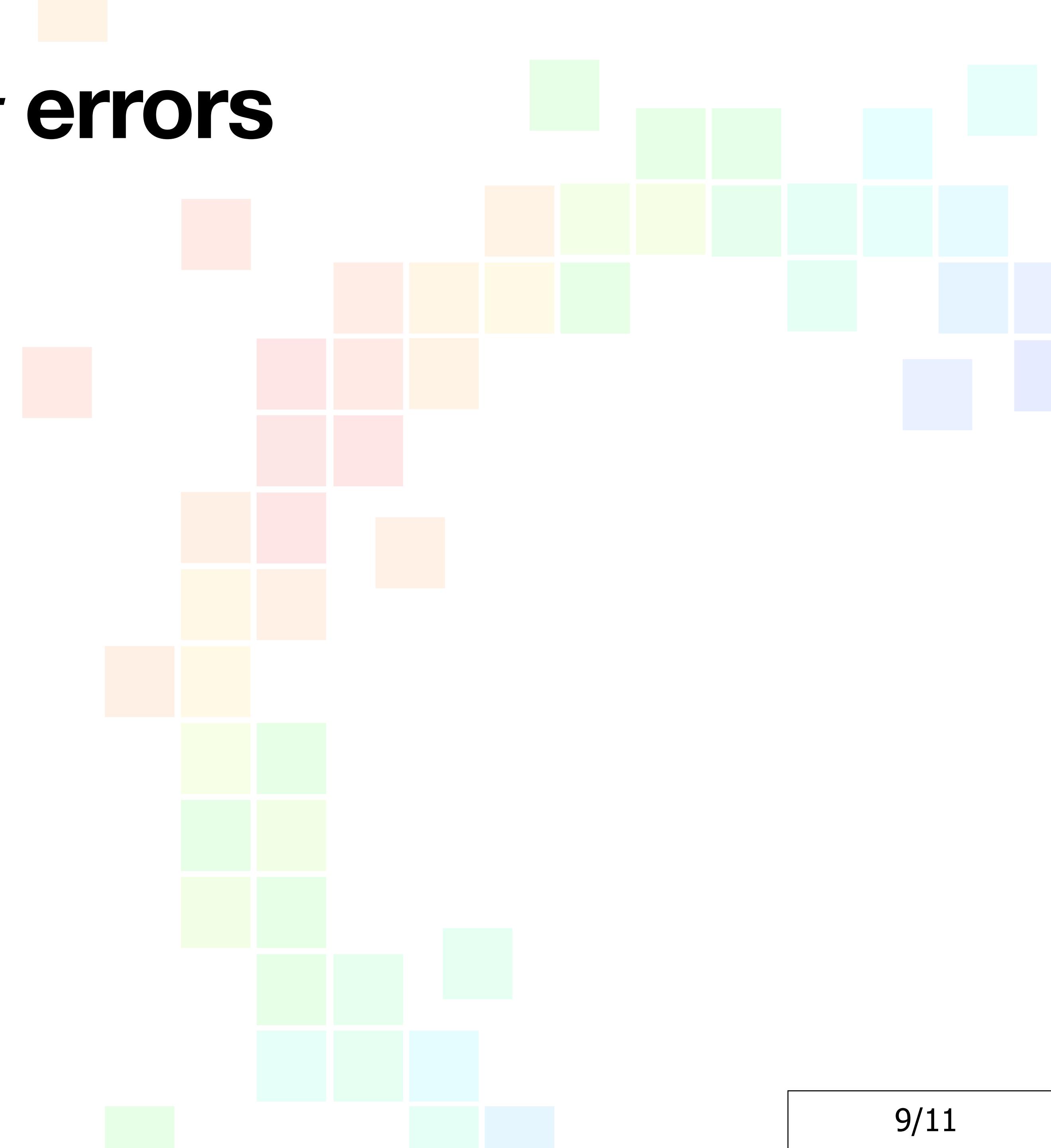
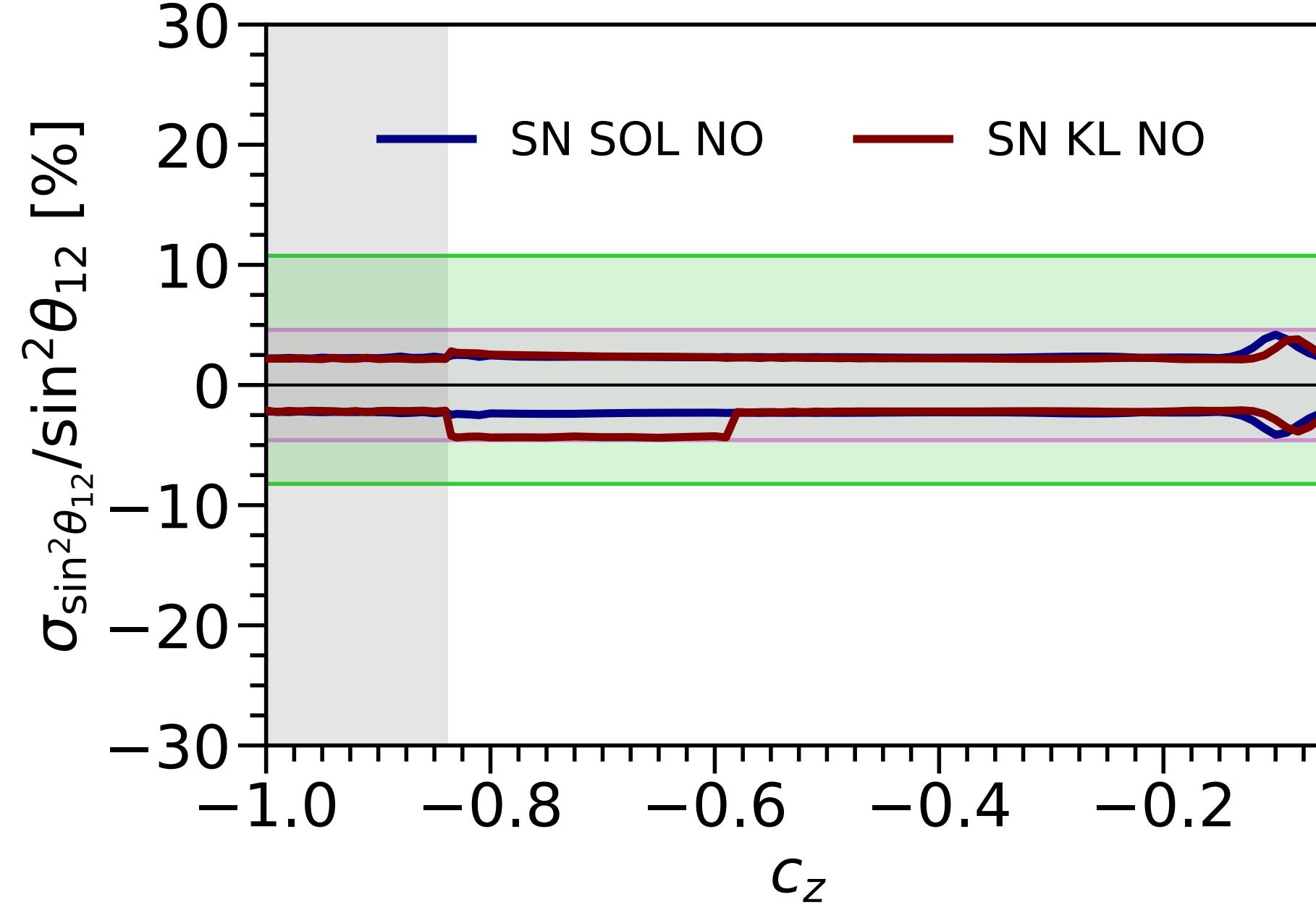
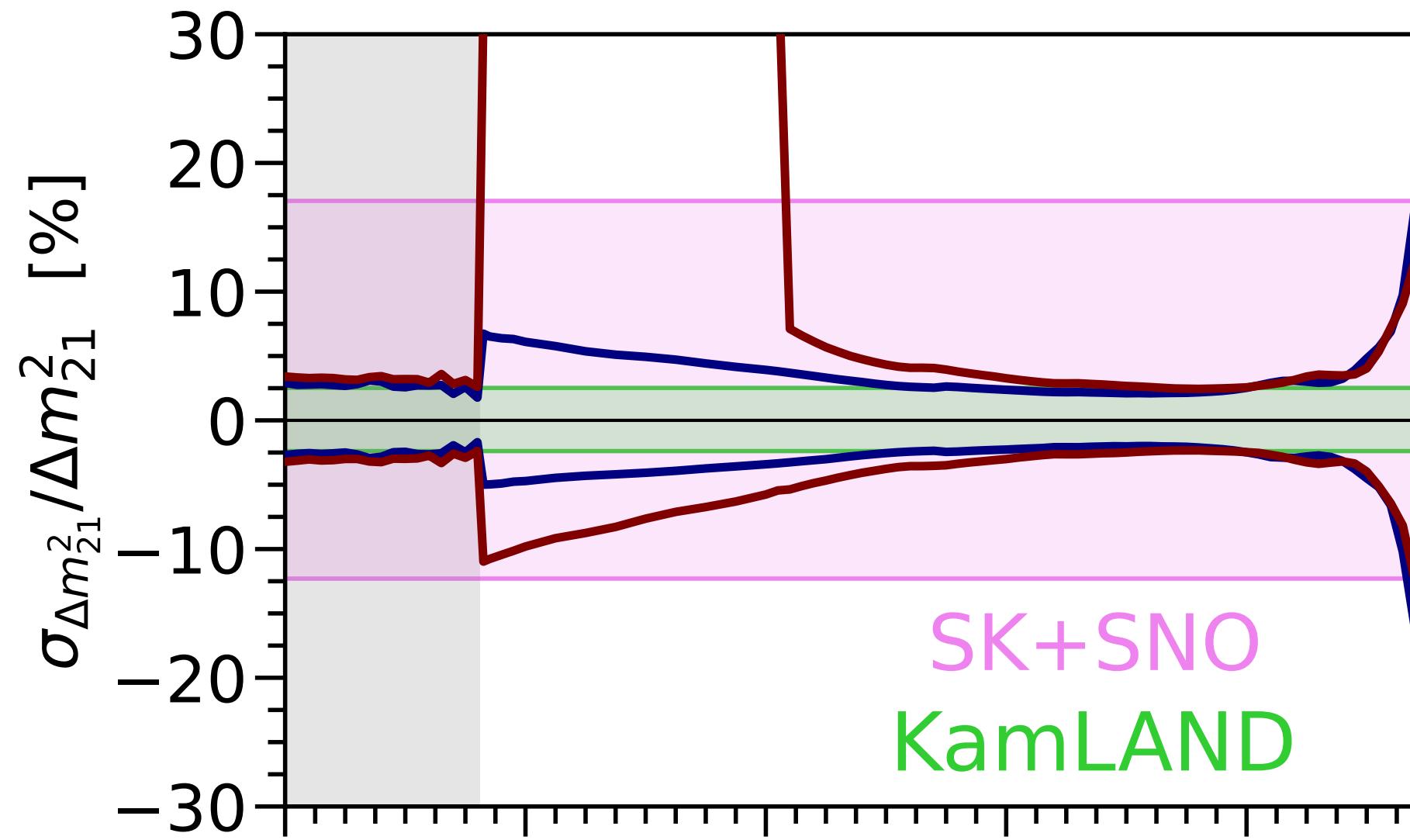


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- Forecast assuming as “true=nature” value SK+SNO best fit
 - Increase tension between reactor and matter effects.

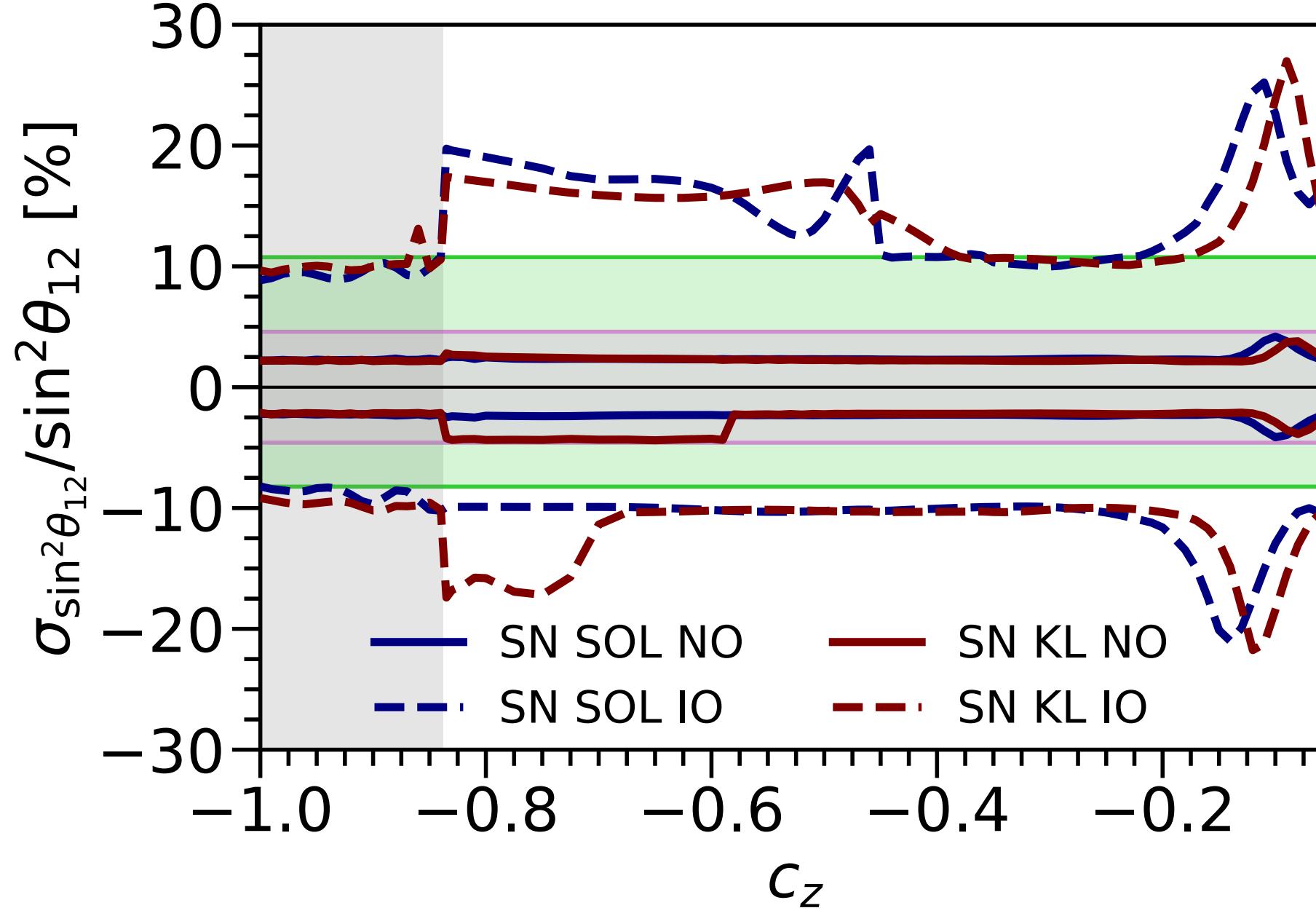
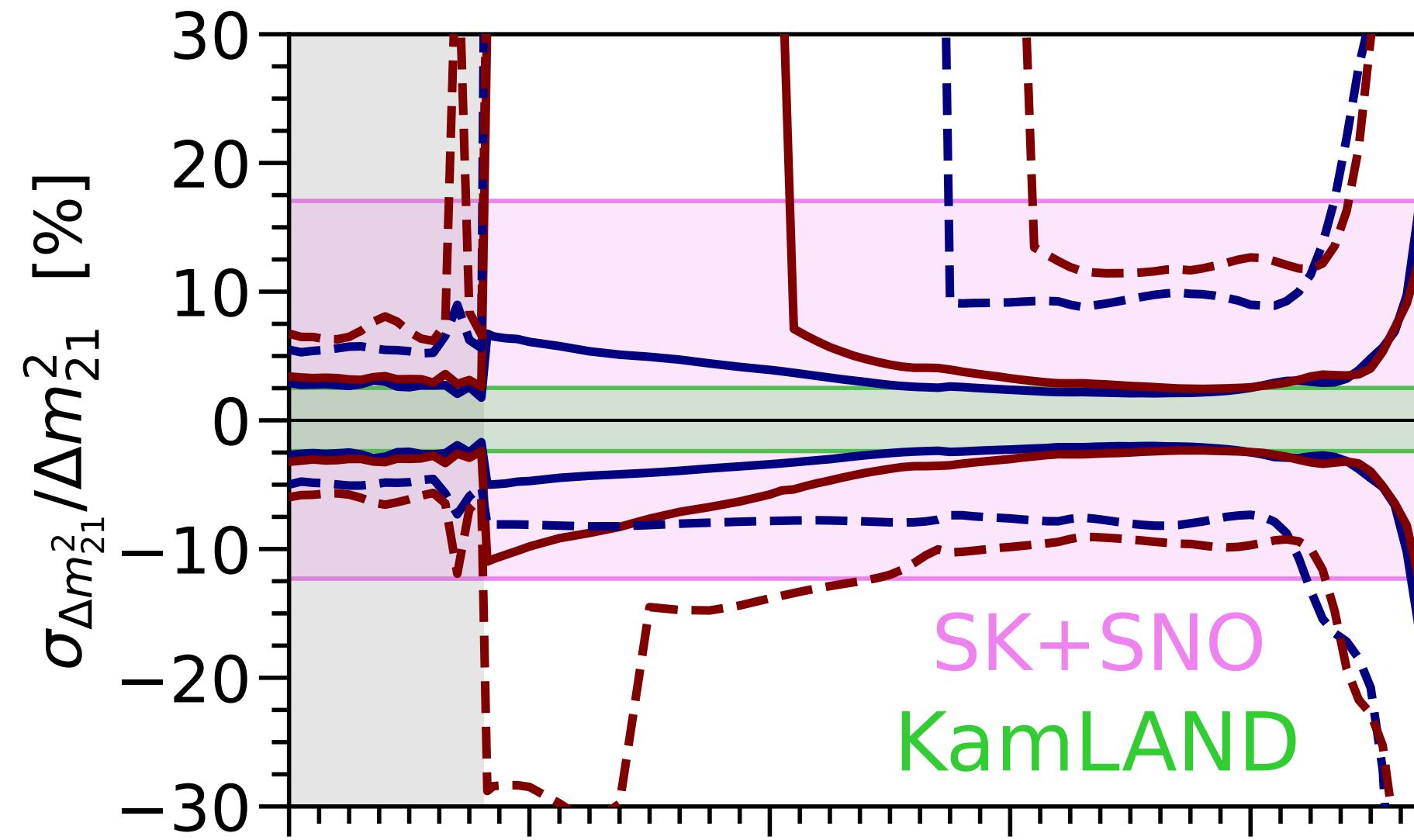
Results: Projected 1σ errors



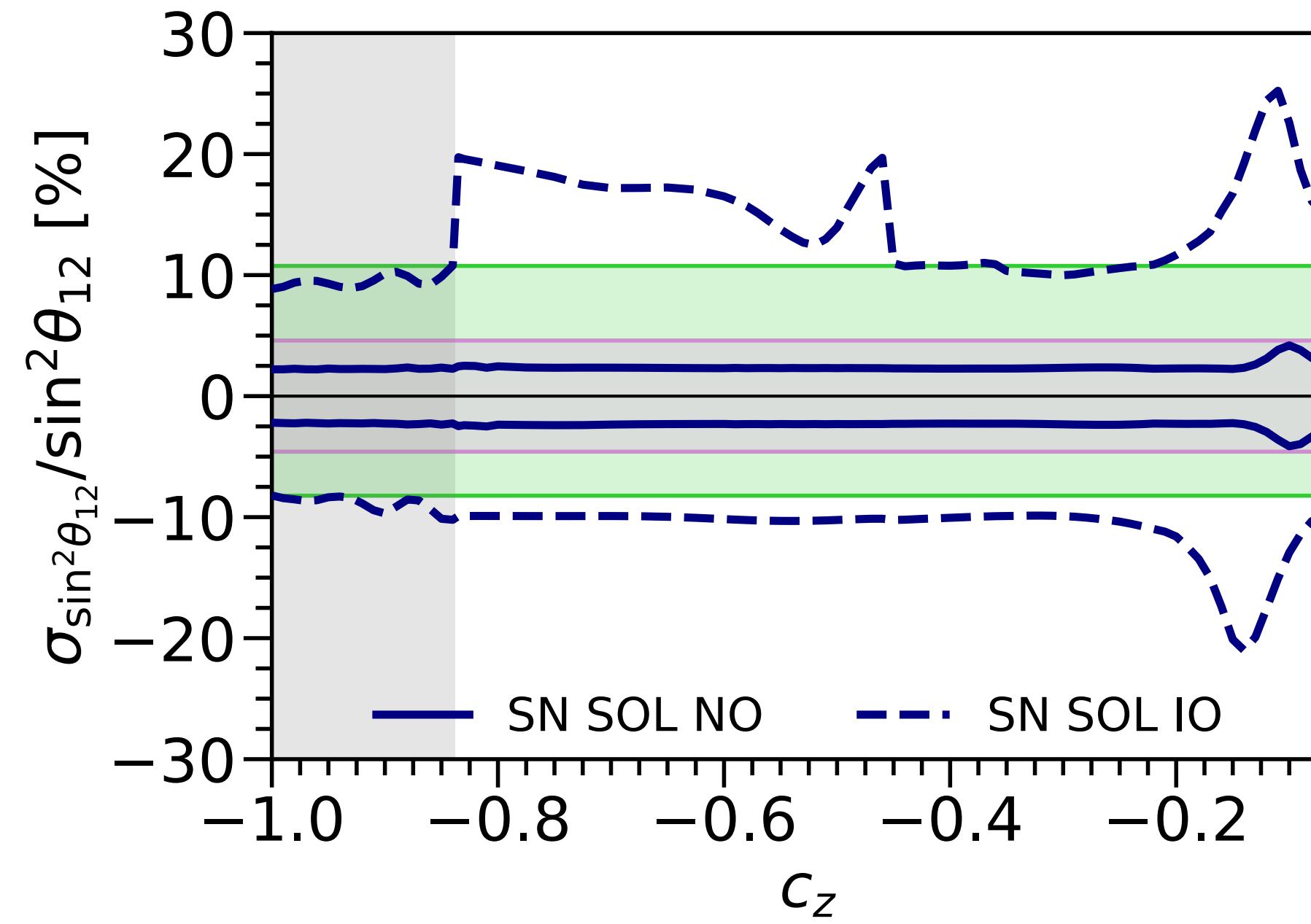
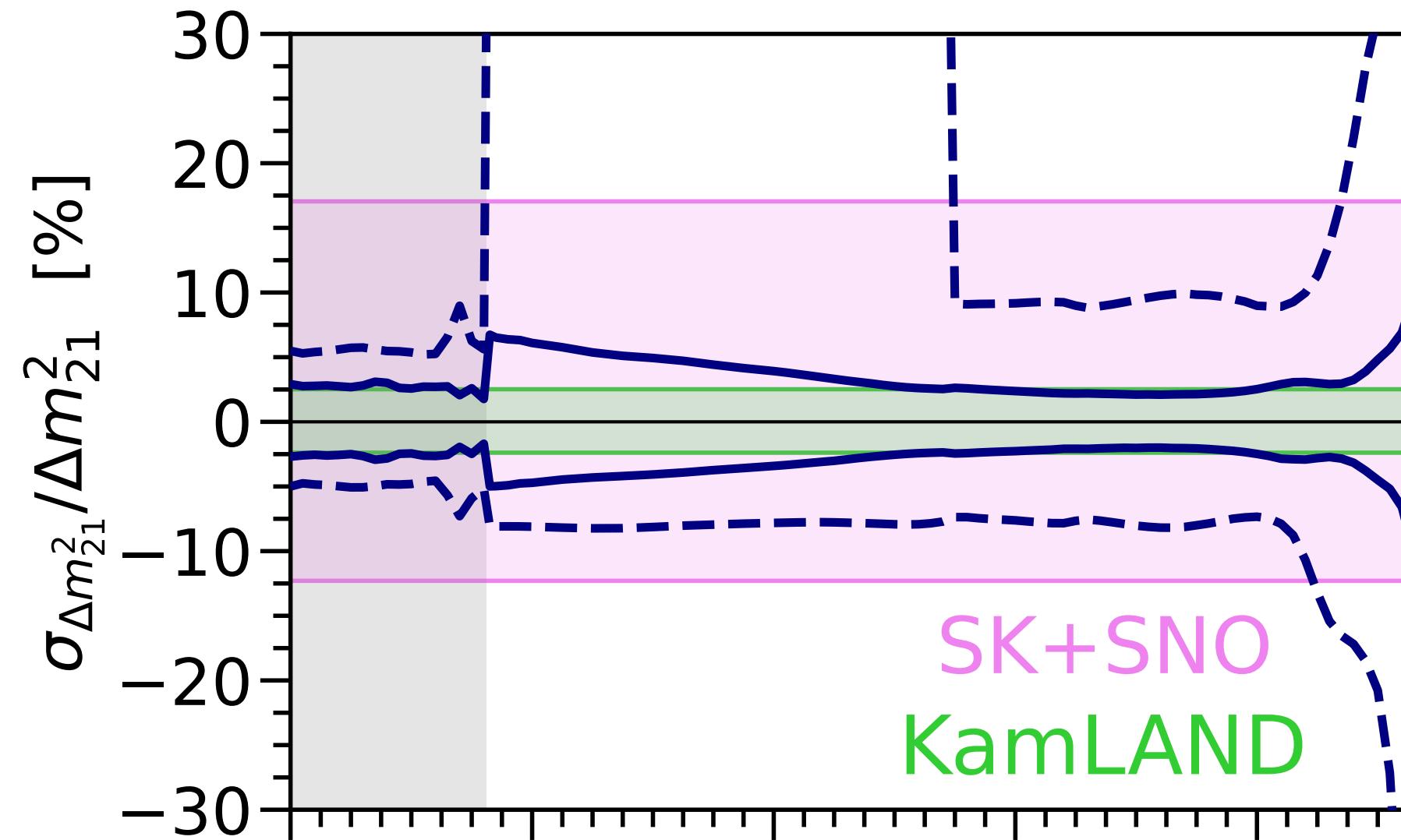
Results: Projected 1σ errors



Results: Projected 1σ errors



Results: Projected 1σ errors and tension



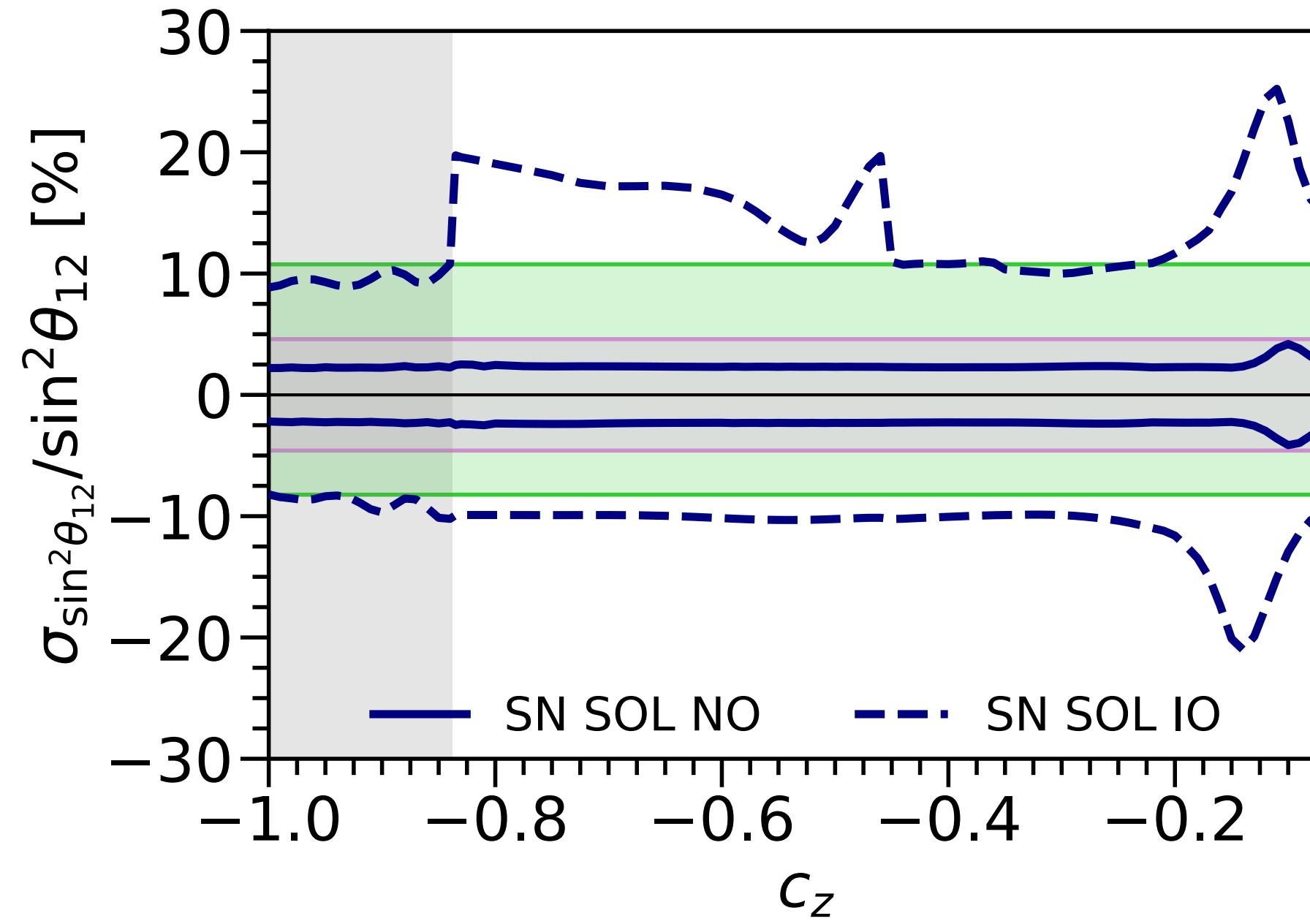
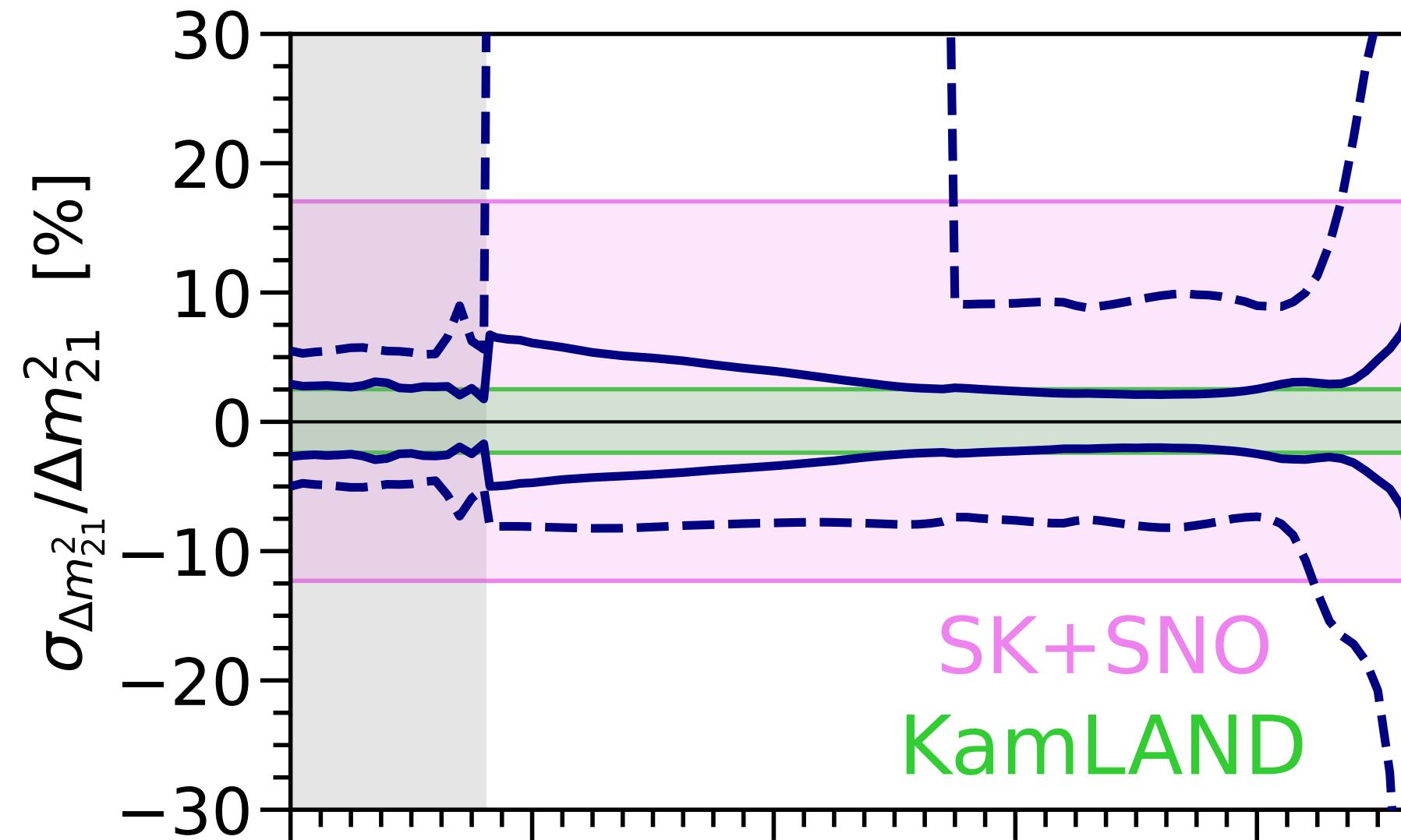
$$\mu_{21} = \frac{\Delta m_{21}^2|_{\text{KL}} - \Delta m_{21}^2|_{\text{solar}}}{\sqrt{\sigma_{\text{KL}}^2 + \sigma_{\text{SN}}^2(c_z)}}$$



With SN SOL
we can define
tension with
reactor
measurement

Matter vs
Vacuum
oscillations
measurements

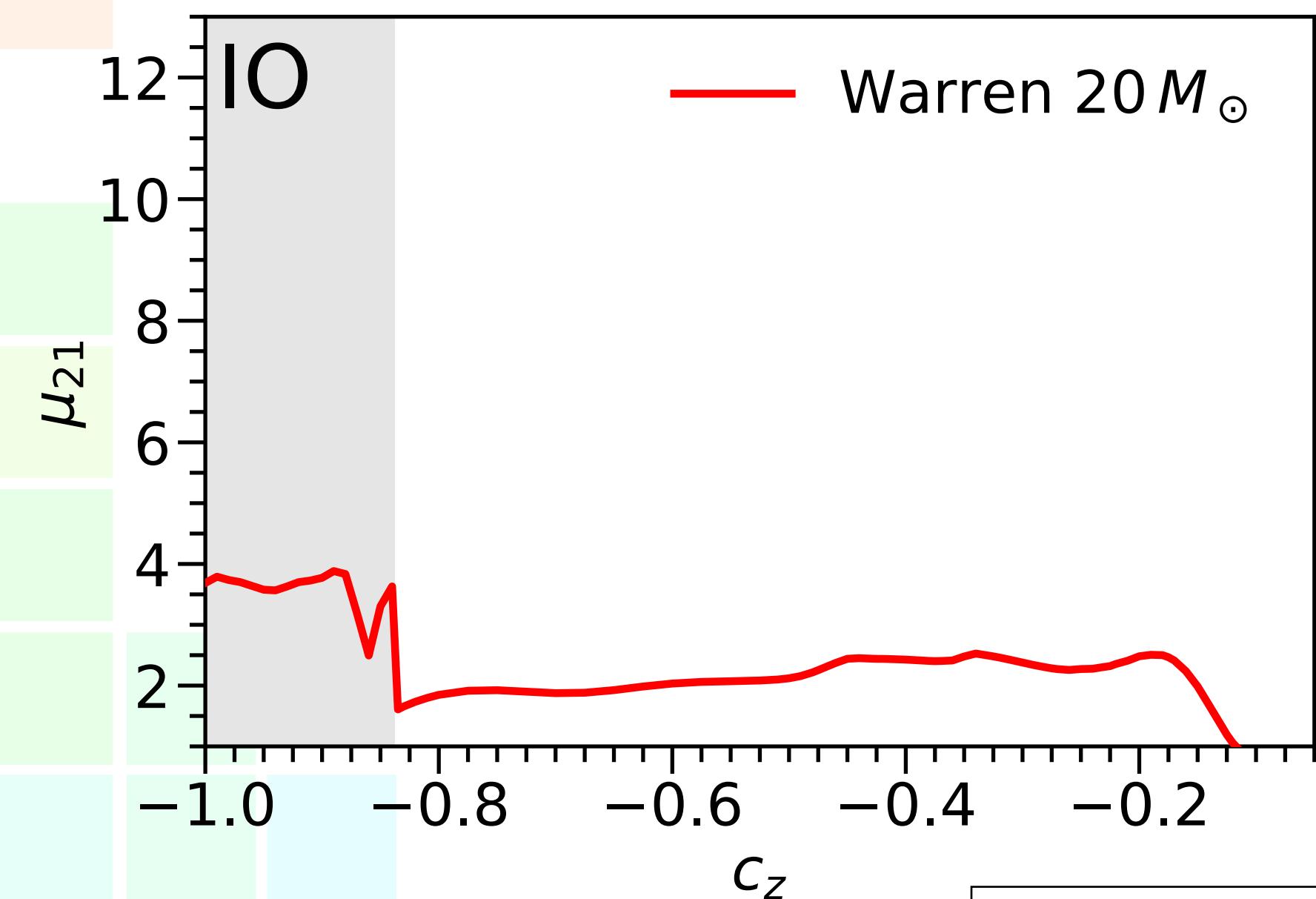
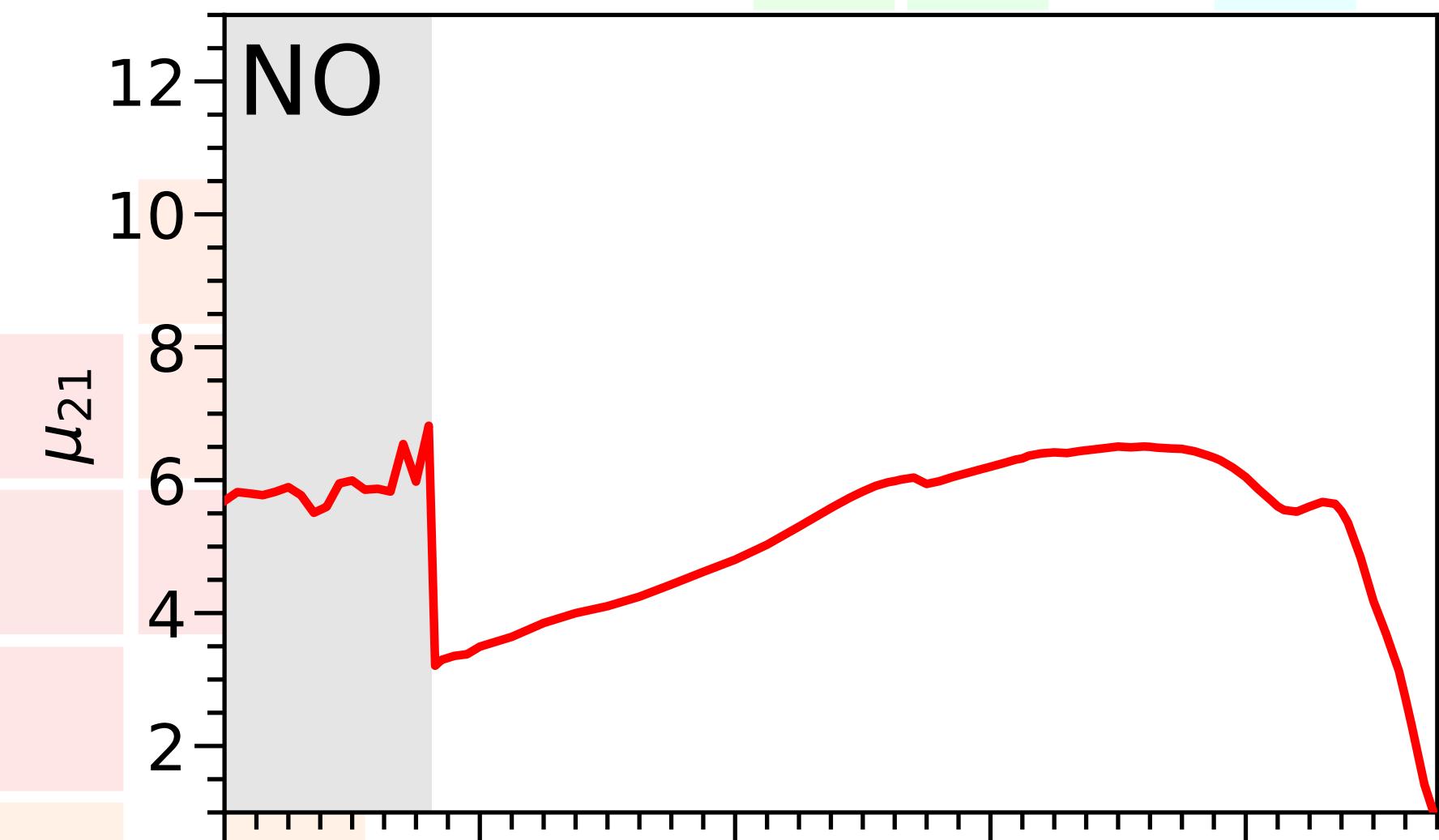
Results: Projected 1σ errors and tension



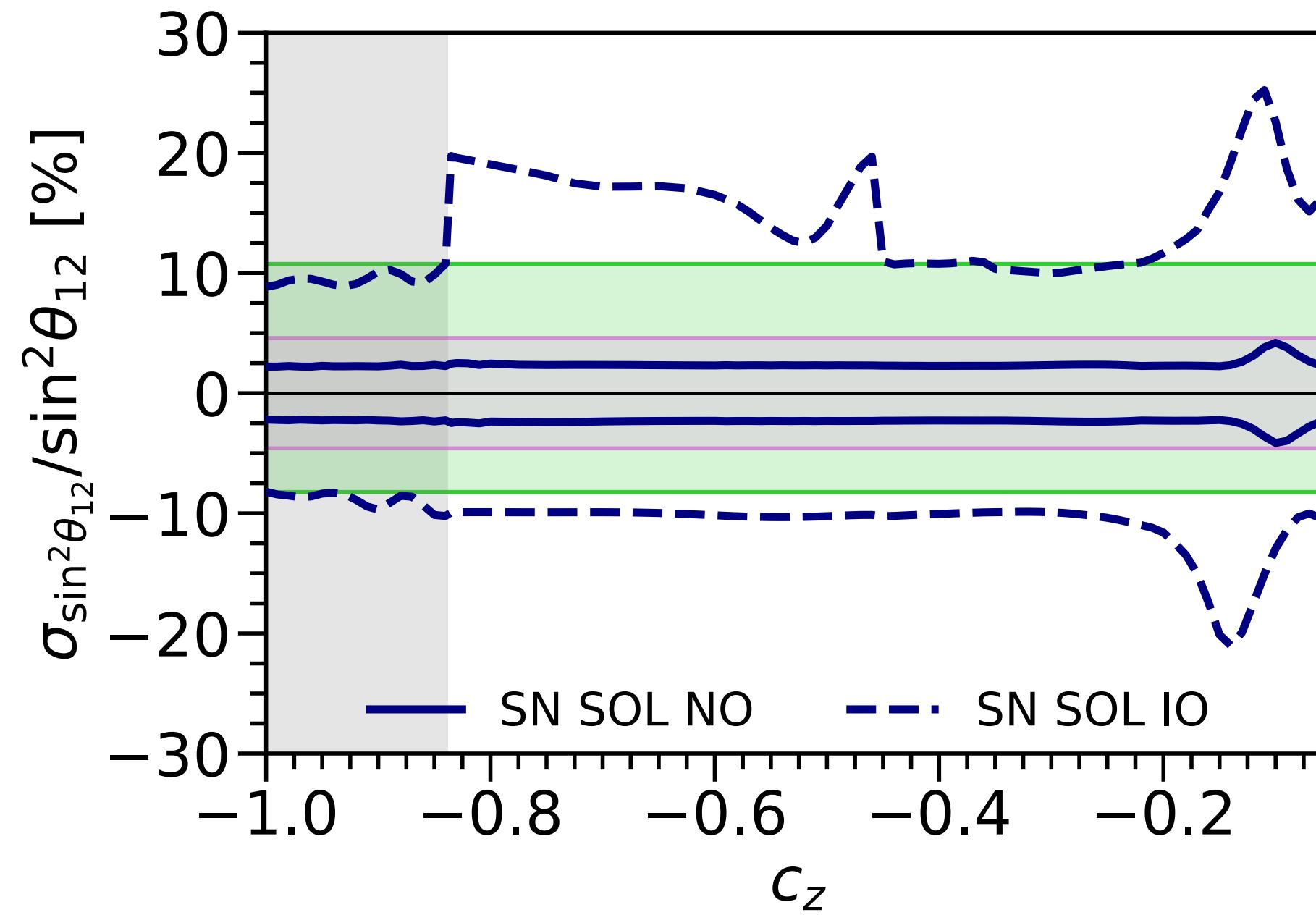
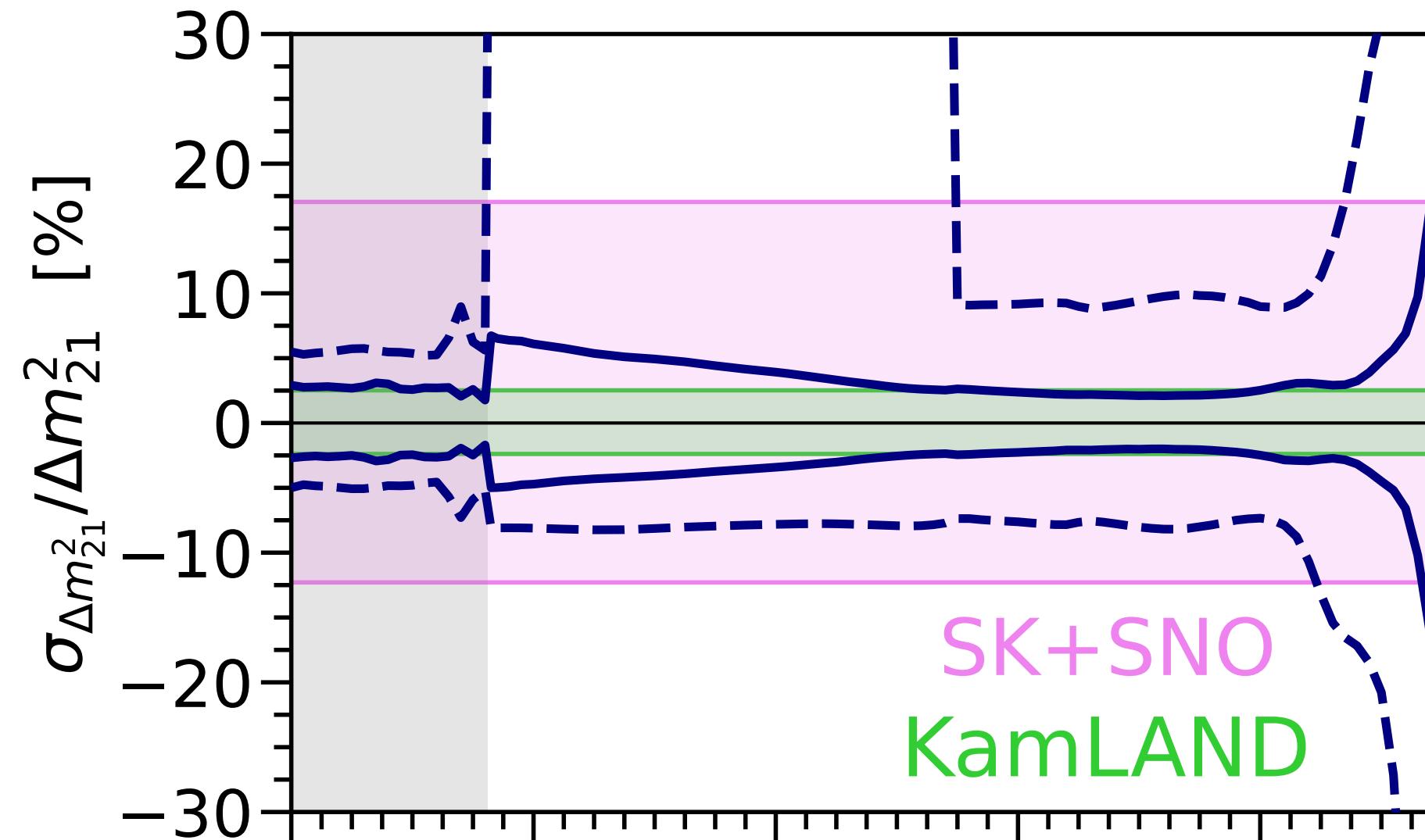
$$\mu_{21} = \frac{\Delta m_{21}^2|_{\text{KL}} - \Delta m_{21}^2|_{\text{solar}}}{\sqrt{\sigma_{\text{KL}}^2 + \sigma_{\text{SN}}^2(c_z)}}$$

Tension
exacerbates for NO.

Tension increases
with matter effects.



Results: Projected 1σ errors and tension

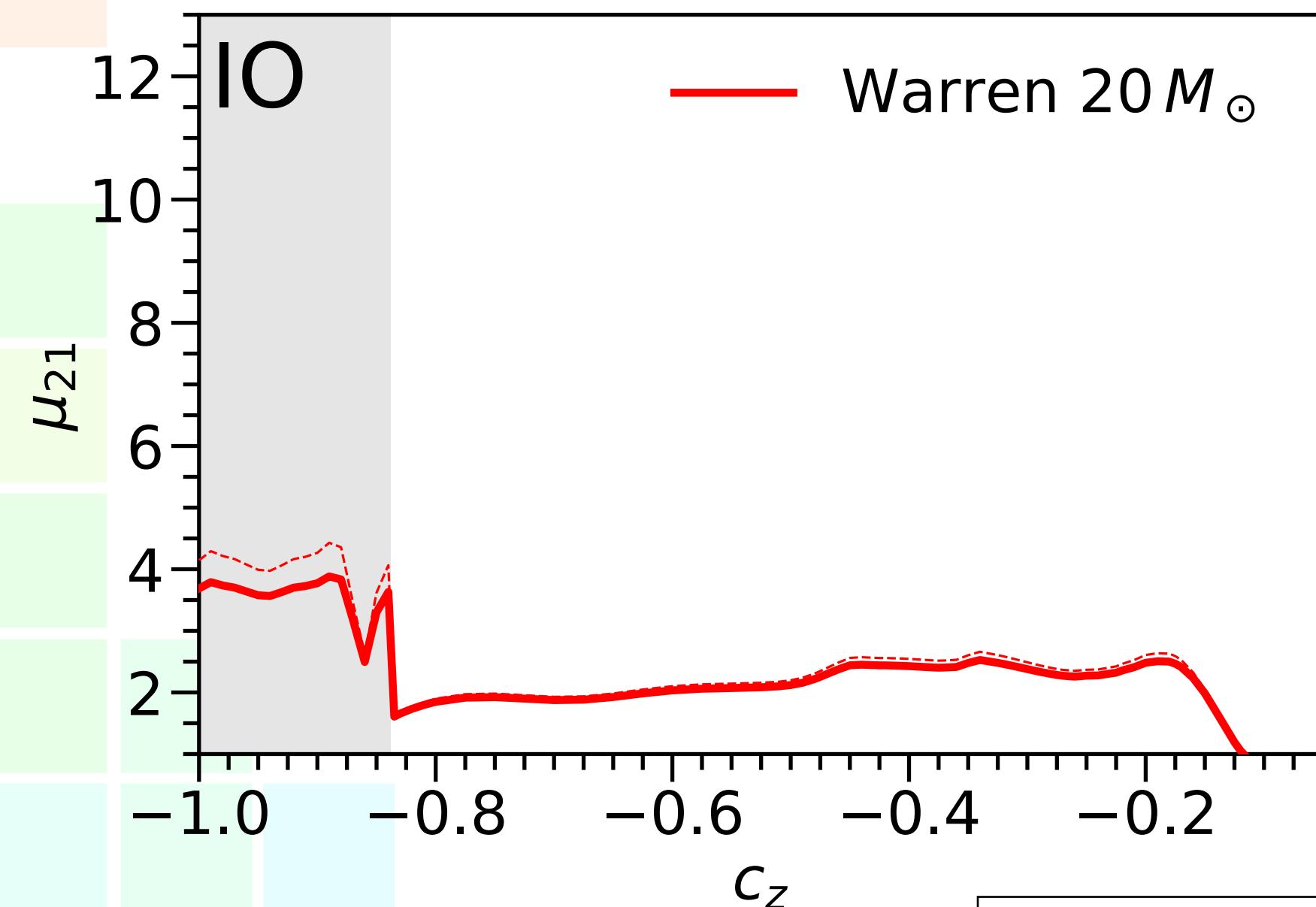
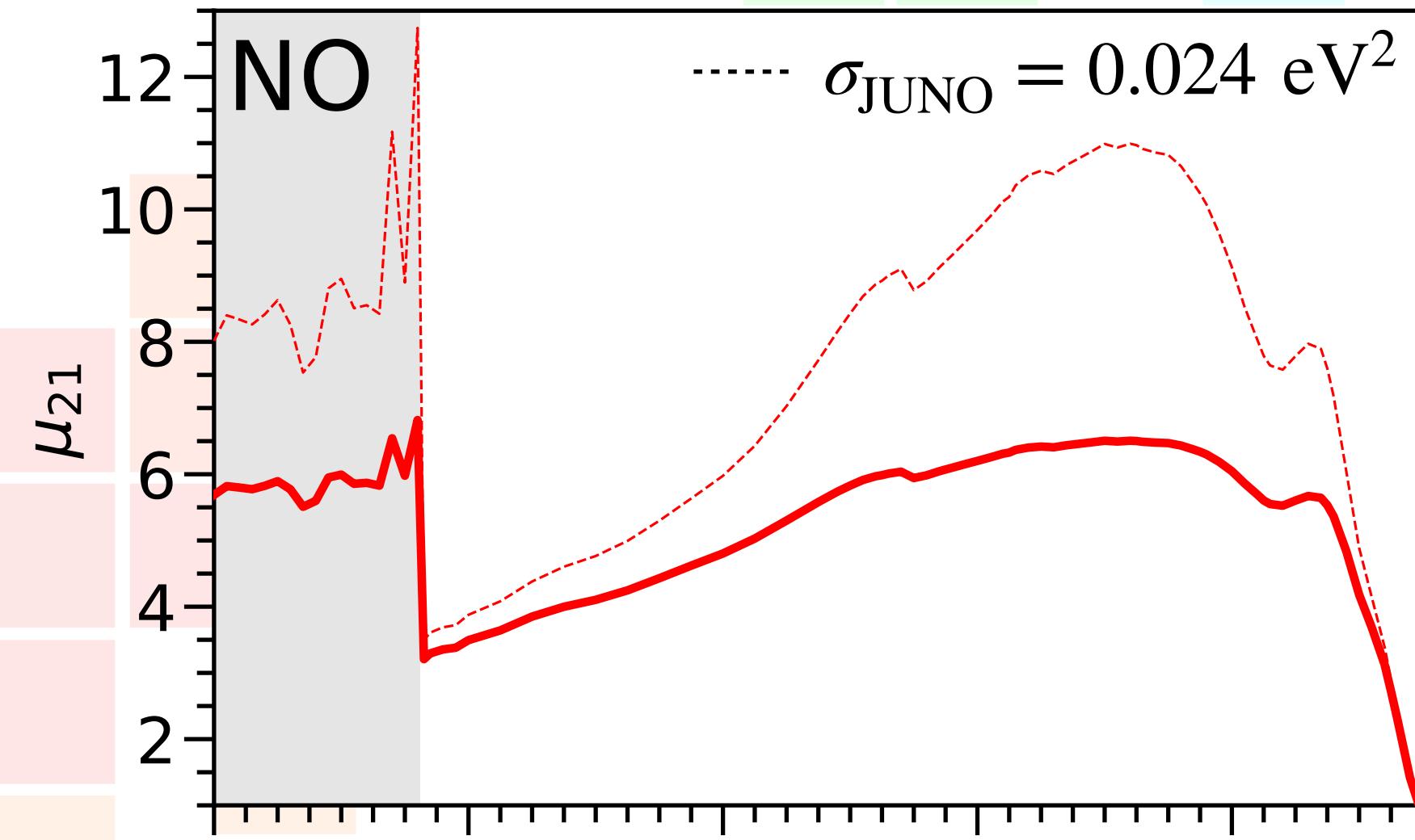


$$\mu_{21} = \frac{\Delta m_{21}^2|_{KL} - \Delta m_{21}^2|_{\text{solar}}}{\sqrt{\sigma_{KL}^2 + \sigma_{\text{SN}}^2(c_z)}}$$

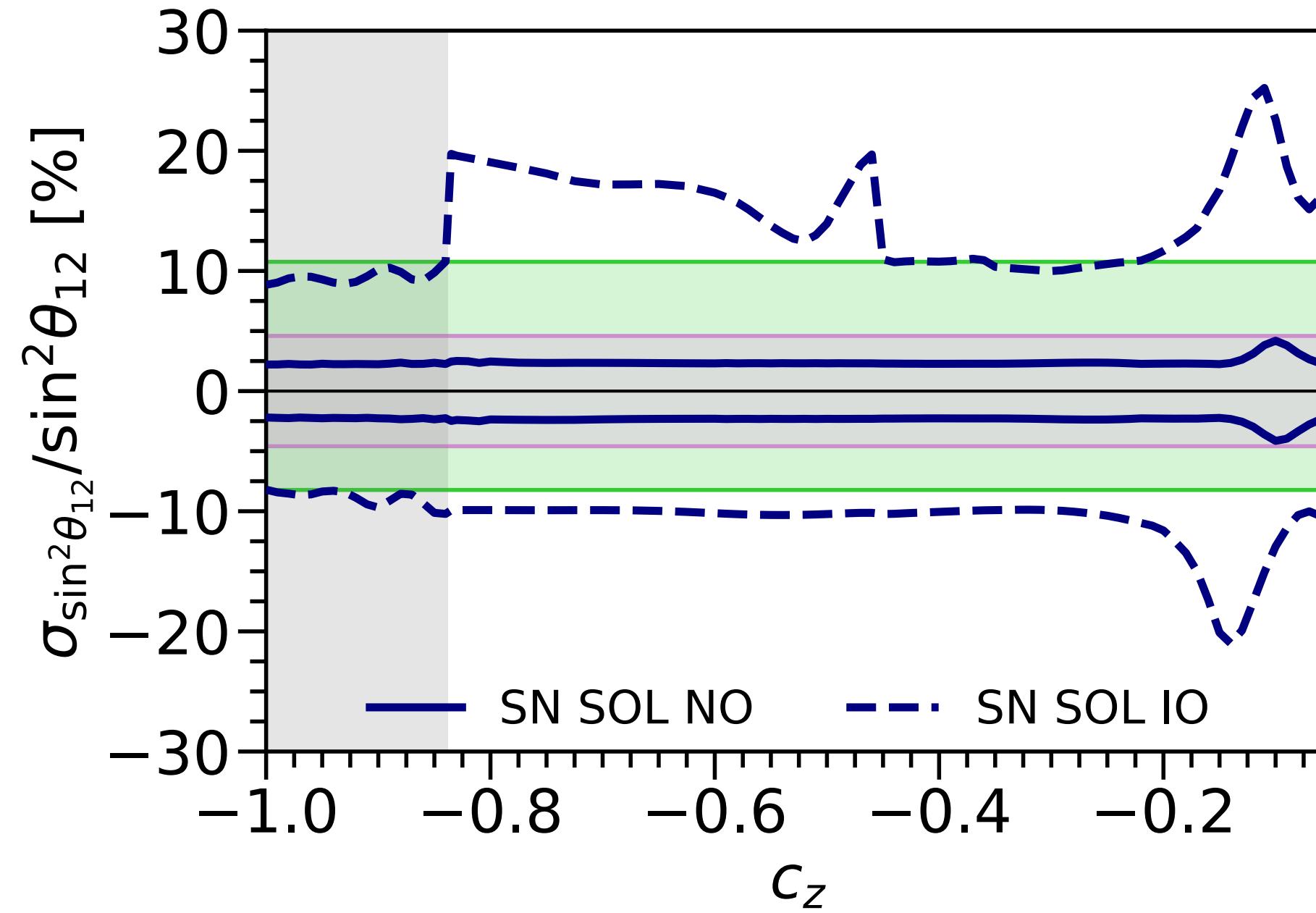
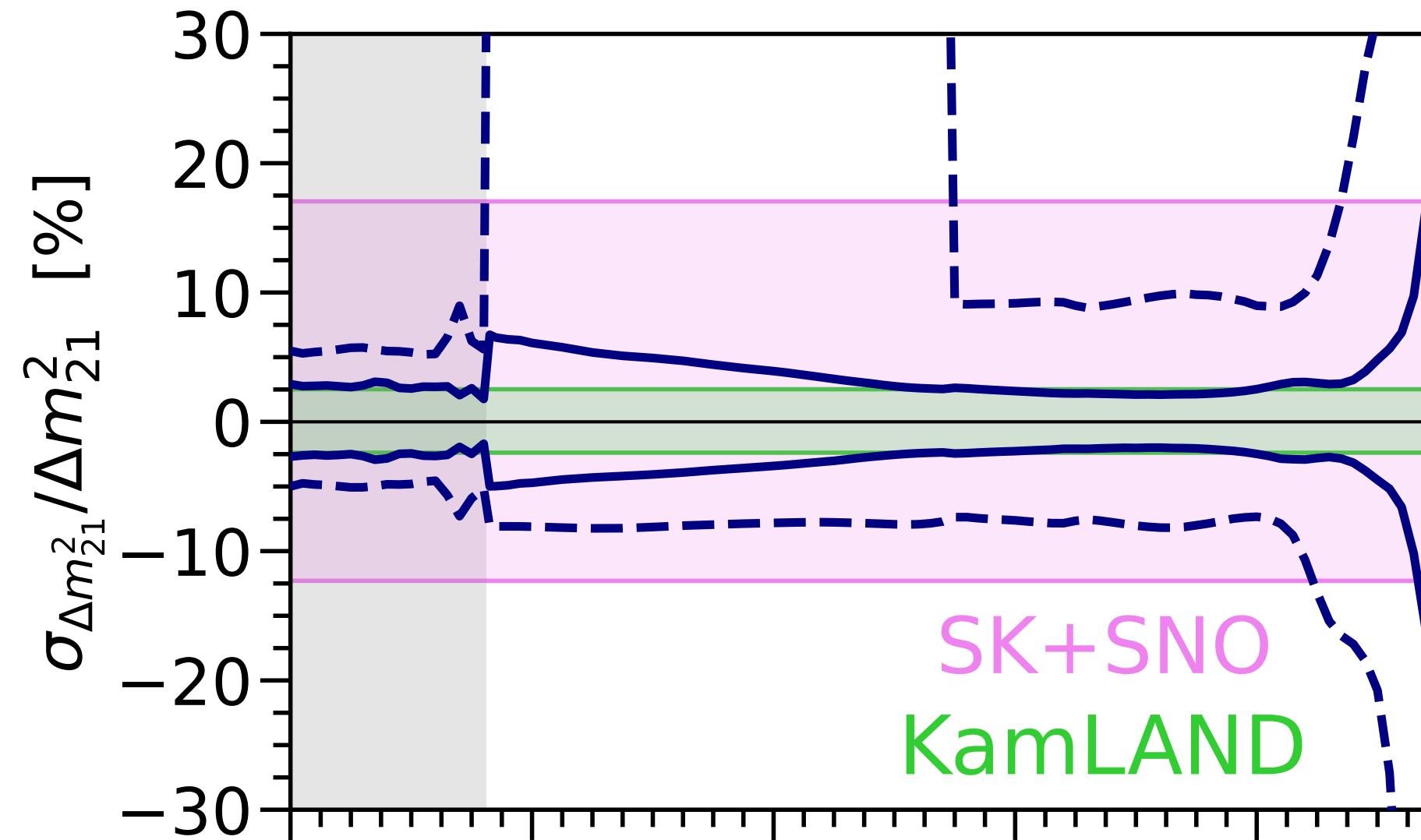
Tension
exacerbates for NO.

Tension increases
with matter effects.

Tension could be
 $> 10\sigma$ in future
detectors



Results: Tension for different models



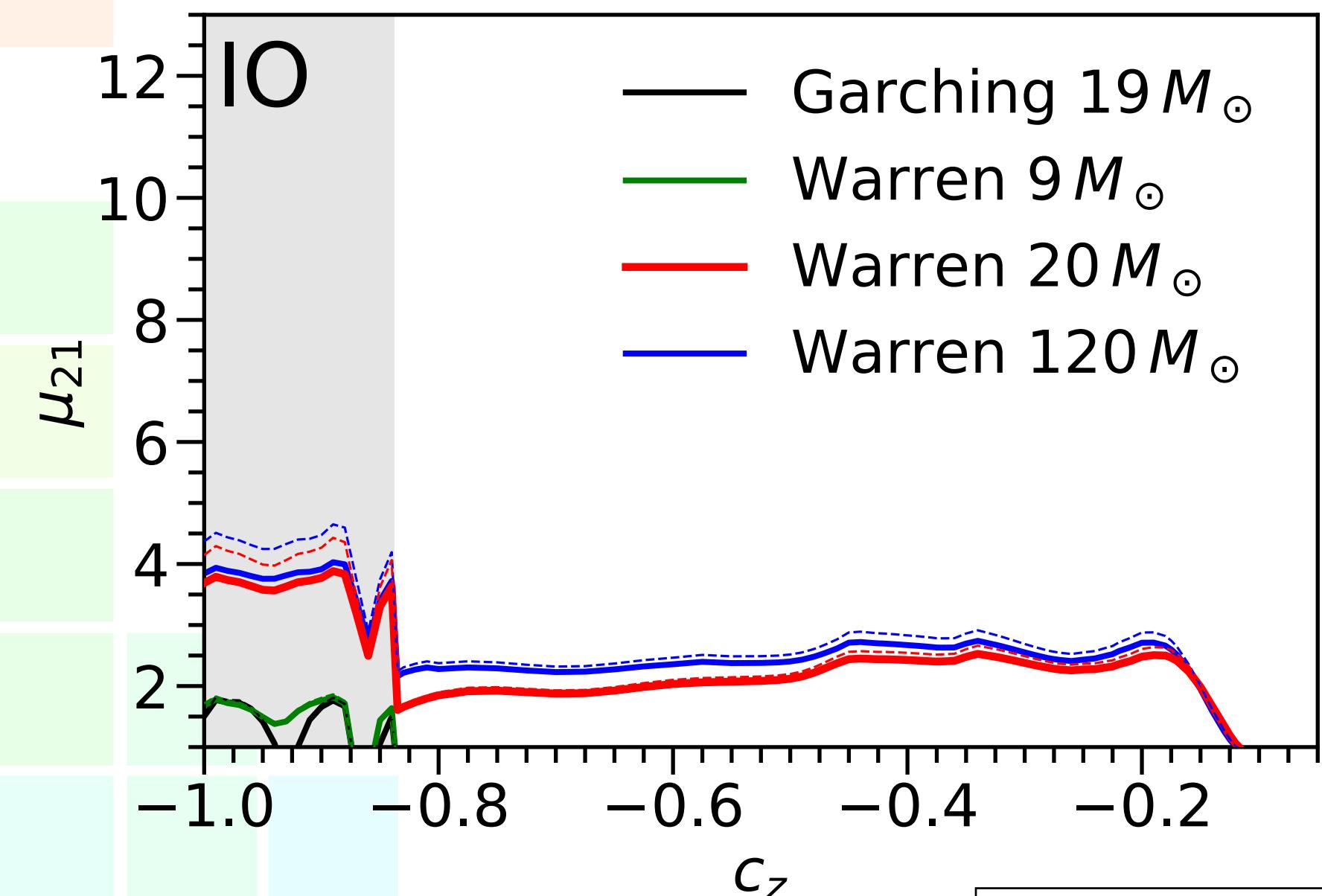
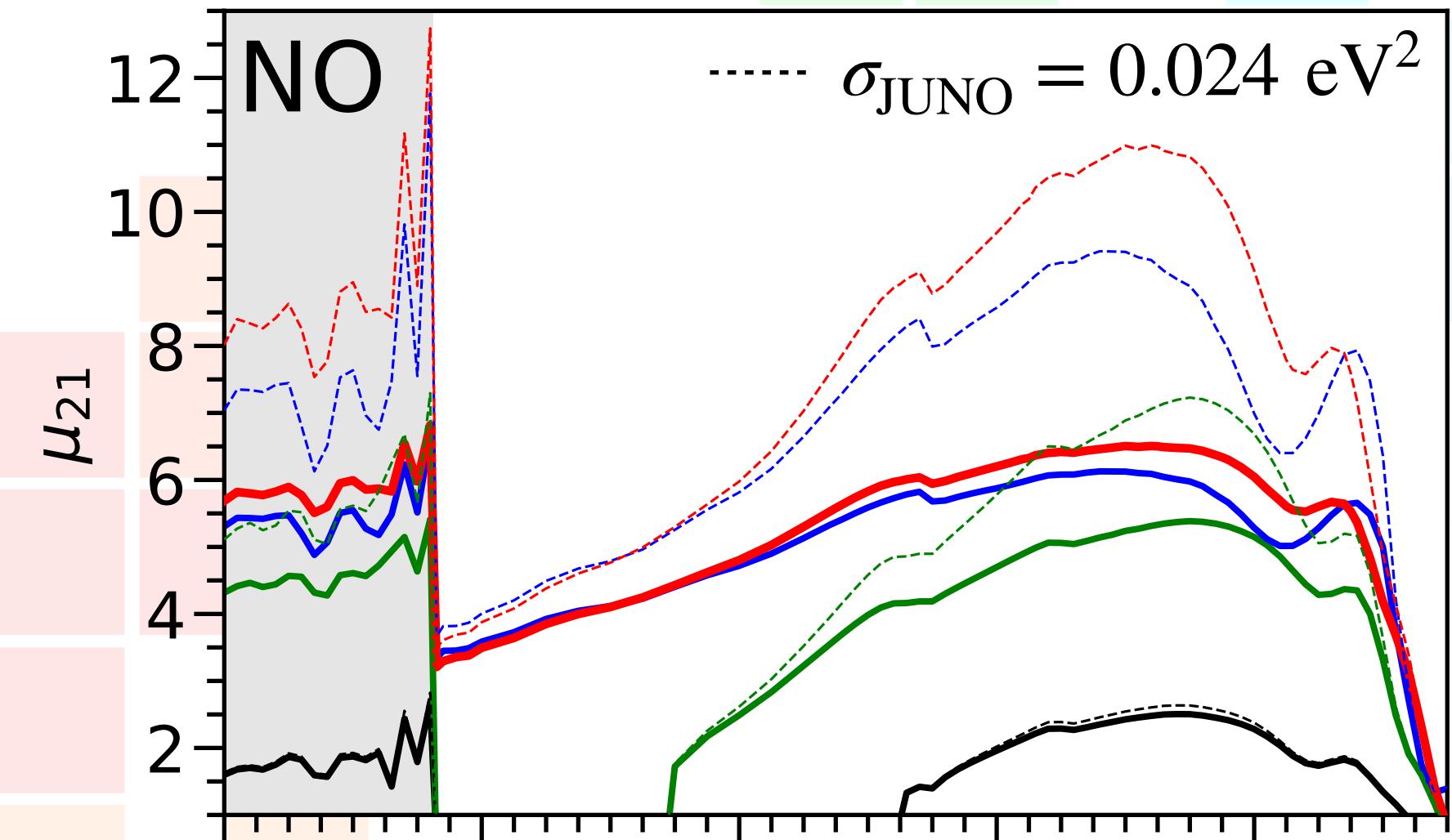
$$\mu_{21} = \frac{\Delta m_{21}^2|_{KL} - \Delta m_{21}^2|_{\text{solar}}}{\sqrt{\sigma_{KL}^2 + \sigma_{\text{SN}}^2(c_z)}}$$

Tension
exacerbates for NO.

Tension increases
with matter effects.

Tension could be
 $> 10\sigma$ in future
detectors

Results very model
dependent!



Take home message

A future galactic SN explosion could provide:

- A competitive measurement of the solar mixing parameters (Δm_{21}^2 and $\sin^2 \theta_{12}$).
- A solution to the longstanding tension between solar neutrino and reactor antineutrino data.

Take home message

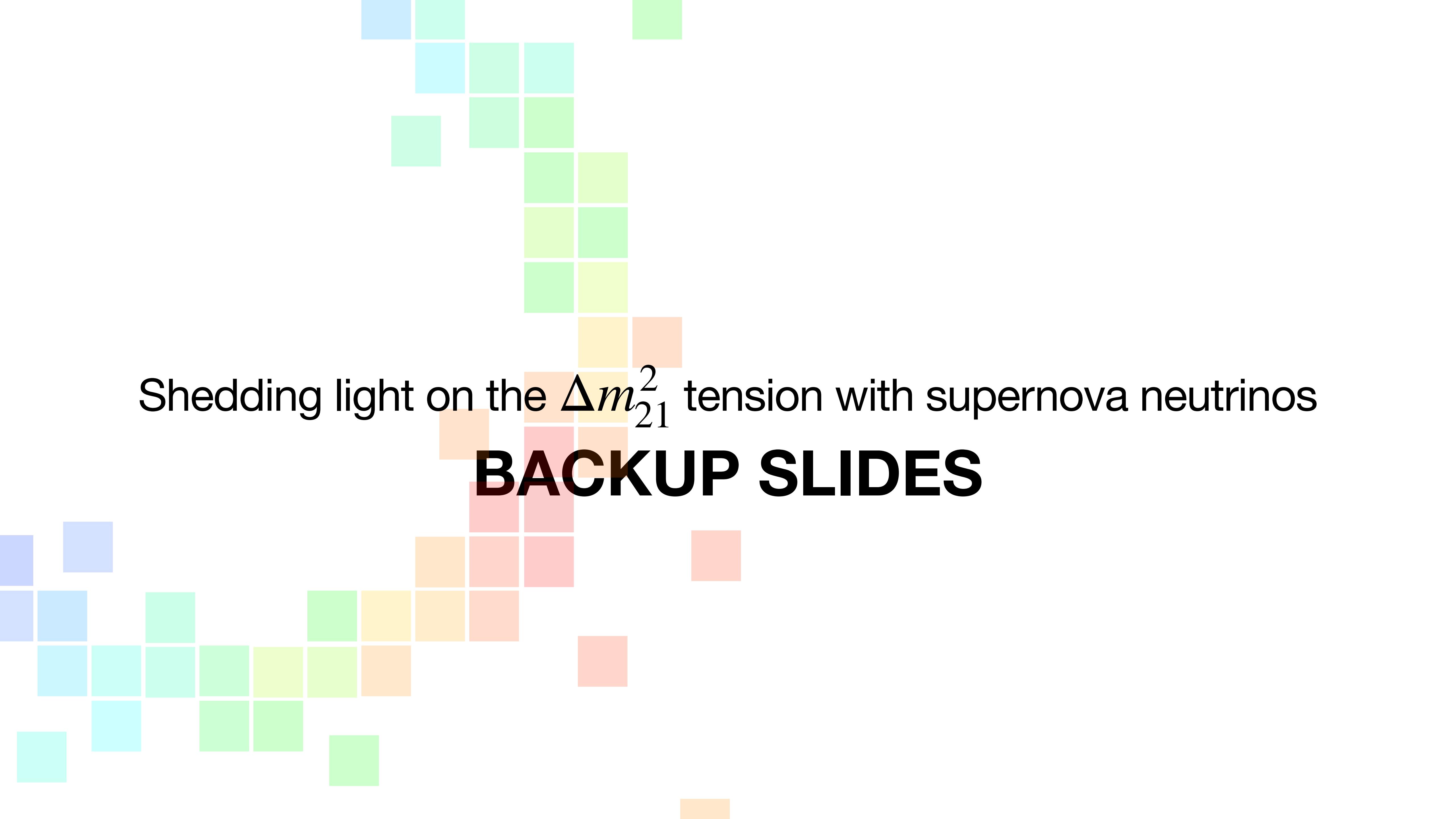
A future galactic SN explosion could provide:

- A competitive measurement of the solar mixing parameters (Δm_{21}^2 and $\sin^2 \theta_{12}$).
→ If no equipartition there will be a measurement.
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Take home message

A future galactic SN explosion could provide:

- A competitive measurement of the solar mixing parameters (Δm_{21}^2 and $\sin^2 \theta_{12}$).
→ If no equipartition there will be a measurement.
- A solution to the longstanding tension between solar neutrino and reactor antineutrino data.
→ Or if you like new physics the tension could increase!

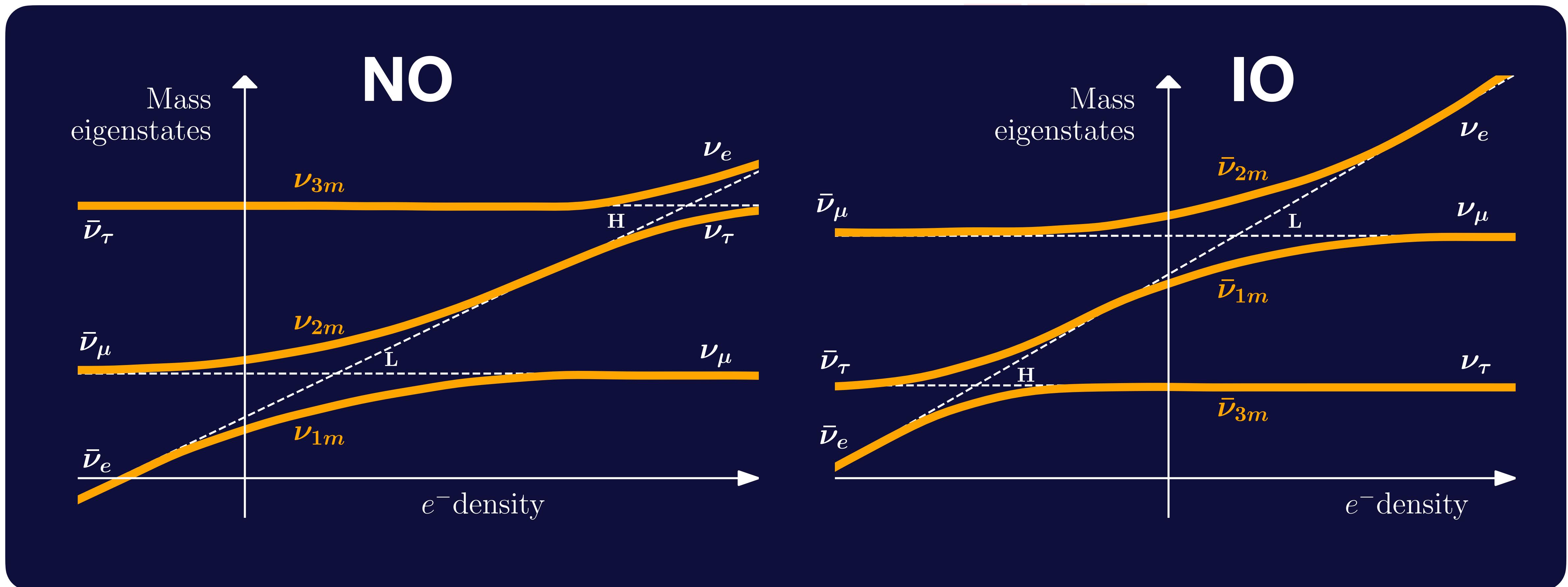


Shedding light on the Δm_{21}^2 tension with supernova neutrinos

BACKUP SLIDES

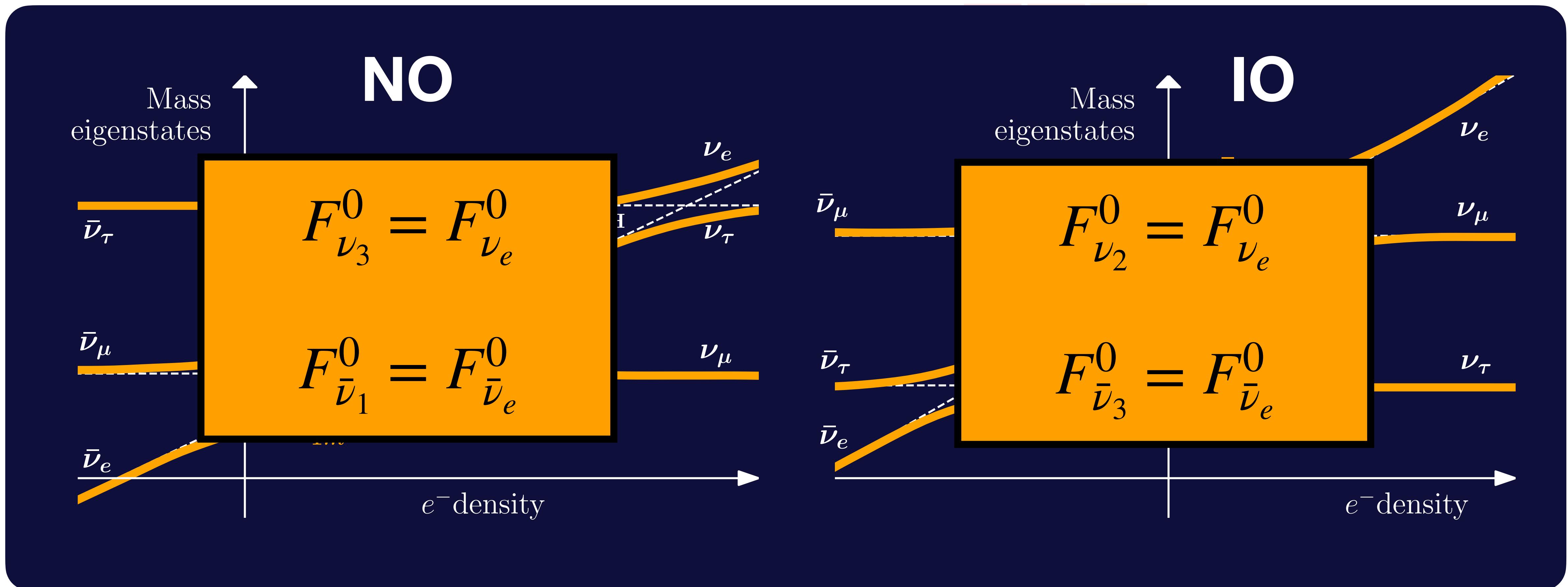
Supernova neutrinos: adiabatic transitions

- Adiabatic transitions make neutrinos go out from the SN as mass eigenstates.



Supernova neutrinos: adiabatic transitions

- Adiabatic transitions make neutrinos go out from the SN as mass eigenstates.



Neutrino oscillations in matter

- Coherent effect in neutrino propagation

$$\frac{d\phi_\nu(E_\nu, x)}{dx} = -i \left(\frac{1}{2E} U M^2 U^\dagger + V \right) \phi_\nu(E_\nu, x)$$

Vacuum Matter

- For 2 families and constant density

$$P_{2\nu}(\nu_\alpha \rightarrow \nu_\beta) = \sin^2(2\theta^m) \sin^2\left(\frac{\Delta^m L}{4E}\right)$$

Effect of mixing parameters

Supernova neutrino fluxes

- Fluxes at detectors are a combination of fluxes at production:

$$F_{\nu_e}^D = p F_{\nu_e}^0 + (1 - p) F_{\nu_x}^0$$

$$F_{\bar{\nu}_e}^D = \bar{p} F_{\bar{\nu}_e}^0 + (1 - \bar{p}) F_{\bar{\nu}_x}^0$$

$$F_{\nu_x}^D = \frac{1 - p}{2} F_{\nu_e}^0 + \frac{1 + p}{2} F_{\nu_x}^0$$

$$F_{\bar{\nu}_x}^D = \frac{1 - \bar{p}}{2} F_{\bar{\nu}_e}^0 + \frac{1 + \bar{p}}{2} F_{\bar{\nu}_x}^0$$

Vacuum probabilities

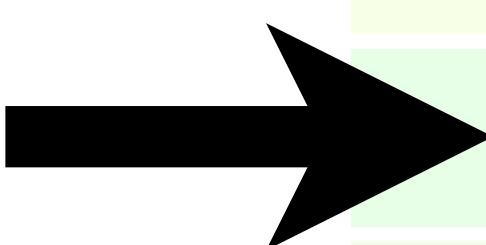
$$p_{\text{vac}}^{\text{NO}} \equiv P_{\text{vac}}(\nu_3 \rightarrow \nu_e) = |U_{e3}|^2 = \sin^2 \theta_{13}$$

$$\bar{p}_{\text{vac}}^{\text{NO}} \equiv P_{\text{vac}}(\bar{\nu}_1 \rightarrow \bar{\nu}_e) = |U_{e1}|^2 = \cos^2 \theta_{12} \cos^2 \theta_{13}$$

$$p_{\text{vac}}^{\text{IO}} \equiv P_{\text{vac}}(\nu_2 \rightarrow \nu_e) = |U_{e2}|^2 = \sin^2 \theta_{12} \cos^2 \theta_{13}$$

$$\bar{p}_{\text{vac}}^{\text{IO}} \equiv P_{\text{vac}}(\bar{\nu}_3 \rightarrow \bar{\nu}_e) = |U_{e3}|^2 = \sin^2 \theta_{13}$$

$V \neq 0$



Constant density probabilities

$$p_{\oplus}^{\text{NO}} \equiv P_{\oplus}(\nu_3 \rightarrow \nu_e) \simeq \sin^2 \theta_{13}$$

$$\bar{p}_{\oplus}^{\text{NO}} \equiv P_{\oplus}(\bar{\nu}_1 \rightarrow \bar{\nu}_e) \simeq \cos^2 \theta_{13} (1 - P_{\oplus}^{2\nu})$$

$$p_{\oplus}^{\text{IO}} \equiv P_{\oplus}(\nu_2 \rightarrow \nu_e) \simeq \cos^2 \theta_{13} P_{\oplus}^{2\nu}$$

$$\bar{p}_{\oplus}^{\text{IO}} \equiv P_{\oplus}(\bar{\nu}_3 \rightarrow \bar{\nu}_e) \simeq \sin^2 \theta_{13}$$

Detector configurations

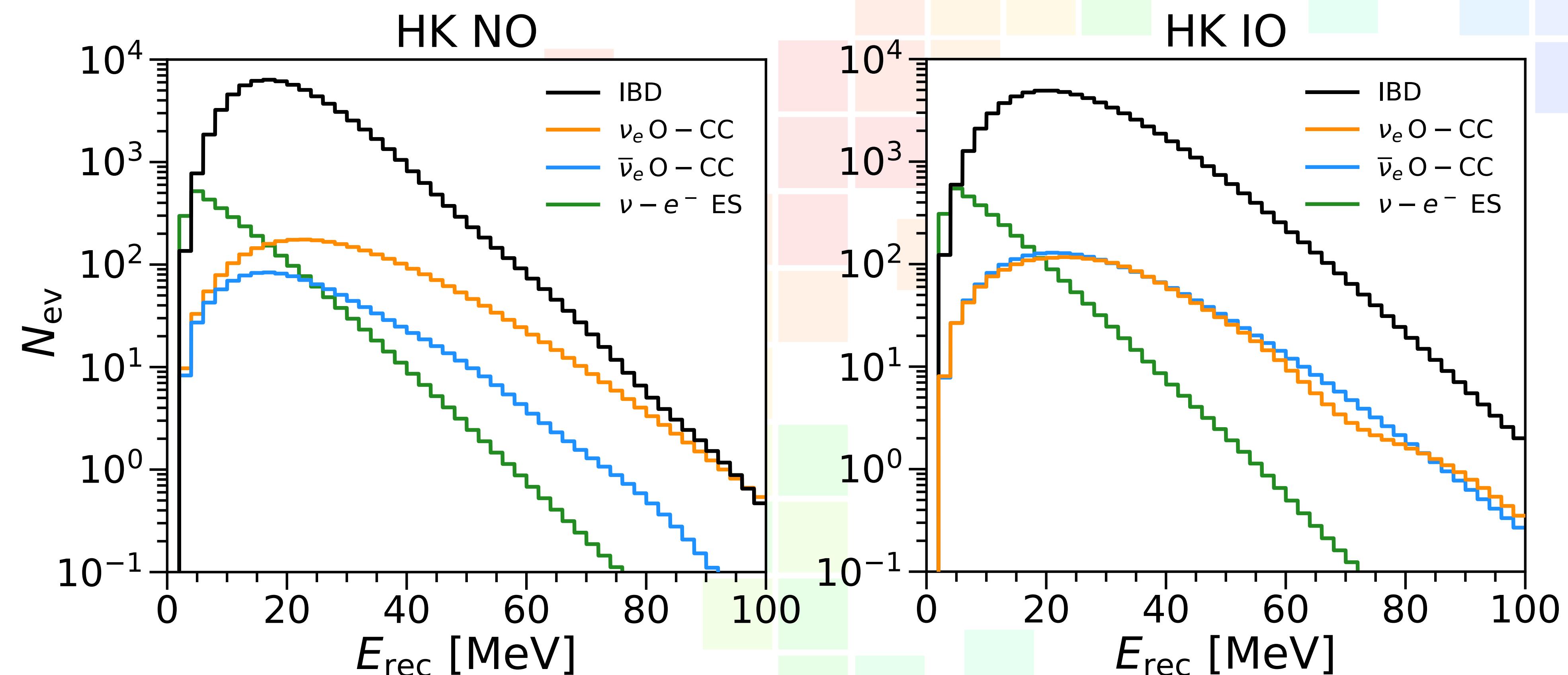
DUNE (LIQUID ARGON)	HK (WATER CHERENKOV)	JUNO (LIQUID SCINTILLATOR)
$\nu_e \text{Ar} - \text{CC} : \quad \nu_e + {}^{40} \text{Ar} \rightarrow e^- + X ,$ $\bar{\nu}_e \text{Ar} - \text{CC} : \quad \bar{\nu}_e + {}^{40} \text{Ar} \rightarrow e^+ + X ,$ $\nu - e^- \text{ES} : \quad \nu + e^- \rightarrow \nu + e^- .$	IBD : $\bar{\nu}_e + p \rightarrow e^+ + n ,$ $\nu_e \text{O} - \text{CC} : \quad \nu_e + {}^{16} \text{O} \rightarrow e^- + X ,$ $\bar{\nu}_e \text{O} - \text{CC} : \quad \bar{\nu}_e + {}^{16} \text{O} \rightarrow e^+ + X ,$ $\nu - e^- \text{ES} : \quad \nu + e^- \rightarrow \nu + e^- .$	IBD : $\bar{\nu}_e + p \rightarrow e^+ + n ,$ $\nu_e \text{C} - \text{CC} : \quad \nu_e + {}^{12} \text{C} \rightarrow e^- + X ,$ $\bar{\nu}_e \text{C} - \text{CC} : \quad \bar{\nu}_e + {}^{12} \text{C} \rightarrow e^+ + X ,$ $\nu - e^- \text{ES} : \quad \nu + e^- \rightarrow \nu + e^- .$
$N_t^{Ar} = 6.03 \cdot 10^{32}$ 20% ENERGY RESOLUTION	$N_t^p = 2.94 \cdot 10^{34}$ MEDIUM ENERGY RESOLUTION	$N_t^p = 1.47 \cdot 10^{33}$ GOOD ENERGY RESOLUTION
$\nu_e \text{Ar} - \text{CC} + \bar{\nu}_e \text{Ar} - \text{CC}$ $\nu - e^- \text{ES}$	0.9 IBD 0.1 IBD + $\nu_e \text{O} - \text{CC} +$ $+ \bar{\nu}_e \text{O} - \text{CC} + \nu - e^- \text{ES}$	0.95 IBD 0.05 IBD + $\nu_e \text{O} - \text{CC} +$ $+ \bar{\nu}_e \text{O} - \text{CC} + \nu - e^- \text{ES}$

Supernova neutrino event rates at HK

- Warren20,
 $c_z = -1$,
 $d_{\text{SN}} = 10 \text{ kpc}$

NO
effect in
antineutrinos

IO
effect in
neutrinos



Results: effect of detector resolution

Effect of resolution of the detector in the final result:

$$\sigma_{\text{detector}} = f \sigma_{\text{HK}}$$

