

# Frontiers in Nuclear and Hadronic Physics 2025

## The Galileo Galilei Institute For Theoretical Physics

Centro Nazionale di Studi Avanzati dell'Istituto Nazionale di Fisica Nucleare

Arcetri, Firenze



## Hadron Spectroscopy

Feb 24, 2025 - Feb 28, 2025

J. Nieves



- Lowest lying odd parity resonances in the charm sector:  
 $SU(6)_{\text{lsf}} \times \text{HQSS model}$ 
  - ✓  $\Lambda_c(2595)$  and  $\Lambda_c(2625)$
  - ✓  $\Omega_c$  (LHCb) and  $\Xi_c$  excited states
  - ✓ Extension to the bottom sector
- Lowest lying  $\left(\frac{1}{2}\right)^-$  and  $\left(\frac{3}{2}\right)^-$   $\Lambda_Q$  resonances: from the strange to the bottom sectors
  - ✓ Interplay between chiral meson-baryon and CQM degrees of freedom and the role played by the renormalization scheme
  - ✓ Molecular content, HQSS and thresholds:  $\Lambda_b(5912)/\Lambda_c(5920)$ ,  $\Lambda_c(2595)/\Lambda_c(2625)$  and  $\Lambda(1405)/\Lambda(1520)$
  - ✓ Higher resonances:  $\Lambda_b(6070)$  and  $\Lambda_c(2765)$ ; molecules versus CQM 2S states

Lowest lying odd parity resonances in the  
charm sector:  $SU(6)_{\text{lsf}} \times \text{HQSS}$  model

$$\Lambda_c(2625)^+$$

$$I(J^P) = 0(3/2^-)$$

The spin-parity has not been measured but is expected to be  $3/2^-$ : this is presumably the charm counterpart of the strange  $\Lambda(1520)$ .

$\Lambda_c(2625)^+$  MASS

$2628.11 \pm 0.19$  MeV (S = 1.1)

$\Lambda_c(2625)^+ - \Lambda_c^+$  MASS DIFFERENCE

$341.65 \pm 0.13$  MeV (S = 1.1)

$\Lambda_c(2625)^+$  WIDTH

$< 0.97$  MeV CL=90.0%

### $\Lambda_c(2625)^+$ Decay Modes

$\Lambda_c^+ \pi \pi$  and its submode  $\Sigma(2455)\pi$  are the only strong decays allowed to an excited  $\Lambda_c^+$  having this mass.

	Mode	Fraction ( $\Gamma_i / \Gamma$ )	Scale Factor/ Conf. Level
$\Gamma_1$	$\Lambda_c^+ \pi^+ \pi^-$	$\approx 67\%$	
$\Gamma_2$	$\Sigma_c(2455)^{++} \pi^-$	$< 5$	CL=90%
$\Gamma_3$	$\Sigma_c(2455)^0 \pi^+$	$< 5$	CL=90%
$\Gamma_4$	$\Lambda_c^+ \pi^+ \pi^-$ 3-body	large	
$\Gamma_5$	$\Lambda_c^+ \pi^0$	[1] not seen	
$\Gamma_6$	$\Lambda_c^+ \gamma$	not seen	

## charm sector

$$\Lambda_c(2595)^+$$

$$I(J^P) = 0(1/2^-)$$

The  $\Lambda_c^+ \pi^+ \pi^-$  mode is largely, and perhaps entirely,  $\Sigma_c \pi$ , which is just at threshold; since the  $\Sigma_c$  has  $J^P = 1/2^+$ , the  $J^P$  here is almost certainly  $1/2^-$ . This result is in accord with the theoretical expectation that this is the charm counterpart of the strange  $\Lambda(1405)$ .

$\Lambda_c(2595)^+$  MASS

$2592.25 \pm 0.28$  MeV

$\Lambda_c(2595)^+ - \Lambda_c^+$  MASS DIFFERENCE

$305.79 \pm 0.24$  MeV

$\Lambda_c(2595)^+$  WIDTH

$2.6 \pm 0.6$  MeV

### $\Lambda_c(2595)^+$ Decay Modes

$\Lambda_c^+ \pi \pi$  and its submode  $\Sigma_c(2455)\pi$  – the latter just barely – are the only strong decays allowed to an excited  $\Lambda_c^+$  having this mass; and the submode seems to dominate.

	Mode	Fraction ( $\Gamma_i / \Gamma$ )	Scale Factor/ Conf. Level	$P(\text{MeV}/c)$
$\Gamma_1$	$\Lambda_c^+ \pi^+ \pi^-$	[1]		117
$\Gamma_2$	$\Sigma_c(2455)^{++} \pi^-$	$24 \pm 7\%$		3
$\Gamma_3$	$\Sigma_c(2455)^0 \pi^+$	$24 \pm 7\%$		3
$\Gamma_4$	$\Lambda_c^+ \pi^+ \pi^-$ 3-body	$18 \pm 10\%$		117
$\Gamma_5$	$\Lambda_c^+ \pi^0$	[2] not seen		258
$\Gamma_6$	$\Lambda_c^+ \gamma$	not seen		288

# $\Lambda_b(5920)^0$

Quantum numbers are based on quark model expectations.

$$I(J^P) = 0(3/2^-)$$

$\Lambda_b(5920)^0$  MASS

$5920.09 \pm 0.17$  MeV

$\Lambda_b(5920)^0$  WIDTH

$< 0.19$  MeV CL=90.0%

## $\Lambda_b(5920)^0$ Decay Modes

	Mode	Fraction ( $\Gamma_i / \Gamma$ )	Scale Factor/ Conf. Level	P(MeV/c)	
$\Gamma_1$	$\Lambda_b^0 \pi^+ \pi^-$	seen		108	▼

bottom sector

# $\Lambda_b(5912)^0$

Quantum numbers are based on quark model expectations.

$$I(J^P) = 0(1/2^-)$$

$\Lambda_b(5912)^0$  MASS

$5912.19 \pm 0.17$  MeV

$\Lambda_b(5912)^0$  WIDTH

$< 0.25$  MeV CL=90.0%

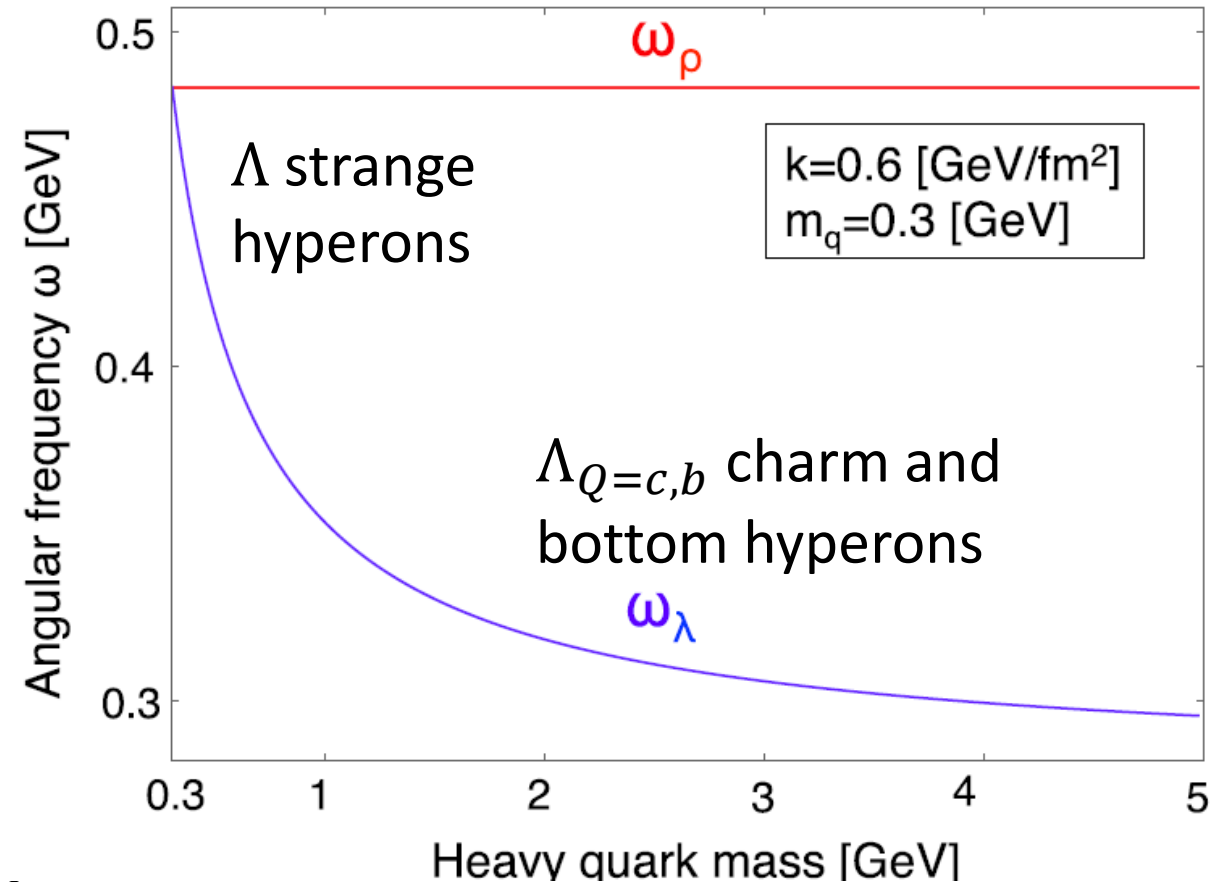
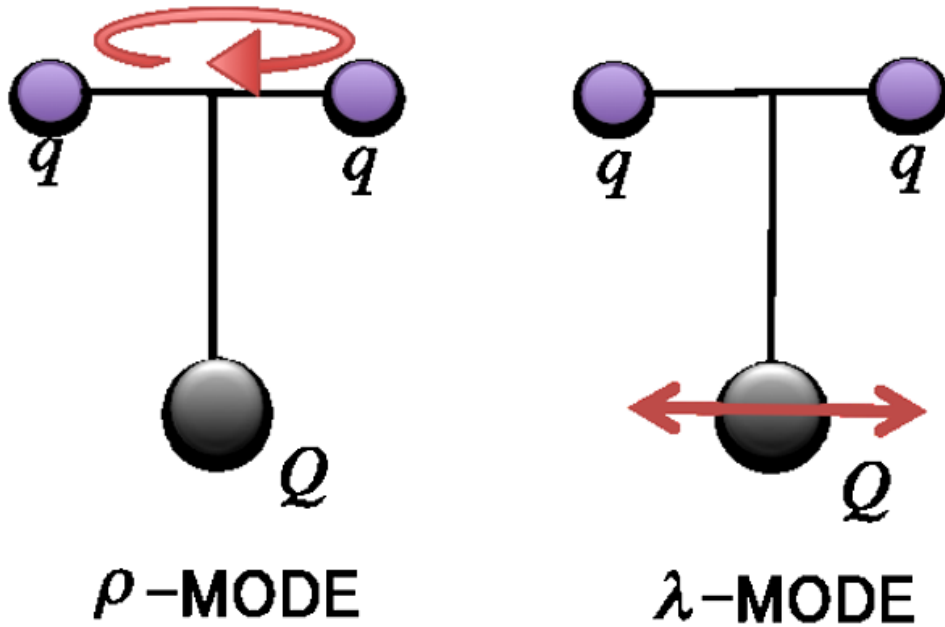
## $\Lambda_b(5912)^0$ Decay Modes

	Mode	Fraction ( $\Gamma_i / \Gamma$ )	Scale Factor/ Conf. Level	P(MeV/c)	
$\Gamma_1$	$\Lambda_b^0 \pi^+ \pi^-$	seen		86	▼

# Spectrum of heavy baryons in the quark model

## Constituent Quark Model (CQM)

T. Yoshida,<sup>1,\*</sup> E. Hiyama,<sup>2,1,3</sup> A. Hosaka,<sup>4,3</sup> M. Oka,<sup>1,3</sup> and K. Sadato<sup>4,†</sup>



$\rho$ - and  $\lambda$ -mode excitations of a **single-heavy baryon**  
 $\lambda$  mode: excitations between the  $Q$  and the  $ldof$   
 $\rho$  mode.: excitations in the inner structure of the  $ldof$

# Heavy quark spin-flavor symmetry

The light degrees of freedom in the hadron orbit around the heavy quark, which acts as a source of color moving with the hadrons's velocity. On average, this is also the velocity of the “brown muck”.

light degrees of freedom

light degrees of freedom

light degrees of freedom

$\vec{J} = \vec{S}_Q + \vec{J}_{ldof}$

$\vec{J}_{ldof}^2$  is conserved!  
HQSS

**$SU(2N_h)$  symmetry in the  $m_Q \rightarrow \infty$  limit**

Heavy quark flavor symmetry HQFS

$Q = b, c$

$Q$

$\mathcal{L}_{\text{eff}} = \bar{h}_v i v \cdot D h_v + \frac{1}{2m_Q} \bar{h}_v (iD_\perp)^2 h_v + \frac{g_s}{4m_Q} \bar{h}_v \sigma_{\alpha\beta} G^{\alpha\beta} h_v + \mathcal{O}(1/m_Q^2)$

$D_{\alpha\beta}^\mu \equiv \delta_{\alpha\beta} \partial^\mu - ig_s T_{\alpha\beta}^a G_a^\mu$

Juan Nieves, IFIC (CSIC & UV)



**HQSS** predicts that all types of spin interactions vanish for infinitely massive quarks: **the dynamics is unchanged under arbitrary transformations in the spin of the heavy quark  $Q$ .** The spin-dependent interactions are proportional to the chromomagnetic moment of the heavy quark, hence are of the order of  $1/m_Q$ .

*The total angular momentum  $\vec{j}_{ldof}$  of the brown muck, which is the subsystem of the hadron apart from the heavy quark, is conserved and hadrons with  $J = j_{ldof} \pm \boxed{1/2}$  form a degenerate doublet. For instance,  $m_{\bar{B}^*}(J^P = 1^-) - m_{\bar{B}}(J^P = 0^-) = 45.22 \pm 0.21 \text{ MeV} \sim \Lambda_{QCD}, m_d, m_u$  doublet for  $j_{ldof}^P = 1/2^-$*   $S_Q$

**HQFS** predicts that, besides the mass of the heavy quark, **the single-heavy hadron mass is independent of the flavor of the heavy quark  $Q$ .** The flavor-dependent interactions are proportional to  $1/m_Q$ ,  $M_H/m_Q \sim (1 + \frac{O(\Lambda_{QCD})}{M_Q})$

$$[m_{\bar{B}^*}(J^P = 1^-) - m_{\bar{B}}(J^P = 0^-)] \sim [m_{D^*}(J^P = 1^-) - m_D(J^P = 0^-)] \sim \Lambda_{QCD}, m_d, m_u$$

**HQSFS  $SU(2N_h)$  approximate symmetry seen in the hadron spectrum**



# Chiral perturbation theory for hadrons containing a heavy quark

consistent with the  
1/m<sub>Q</sub> expansion: HMChPT

Mark B. Wise

*California Institute of Technology, Pasadena, California 91125*

(Received 10 January 1992)

An effective Lagrangian that describes the low-momentum interactions of mesons containing a heavy quark with the pseudo Goldstone bosons  $\pi$ ,  $K$ , and  $\eta$  is constructed. It is invariant under both heavy-quark spin symmetry and chiral  $SU(3)_L \times SU(3)_R$  symmetry. Implications for semileptonic  $B$  and  $D$  decays are discussed.

PACS number(s): 14.40.Jz, 11.30.Rd, 13.20.Fc, 13.20.Jf

$$\mathcal{L} = -i \text{Tr} \bar{H}_a v_\mu \partial^\mu H_a + \frac{1}{2} i \text{Tr} \bar{H}_a H_b v^\mu (\xi^\dagger \partial_\mu \xi + \xi \partial_\mu \xi^\dagger)_{ba} \\ + \frac{1}{2} i g \text{Tr} \bar{H}_a H_b \gamma_\nu \gamma_5 (\xi^\dagger \partial^\nu \xi - \xi \partial^\nu \xi^\dagger)_{ba} + \dots, \quad (12)$$

Goldstone bosons

hadron velocity

For instance, for heavy  
mesons: super-field  
including the  
 $j_{ldof}^P = 1/2^-$  doublet

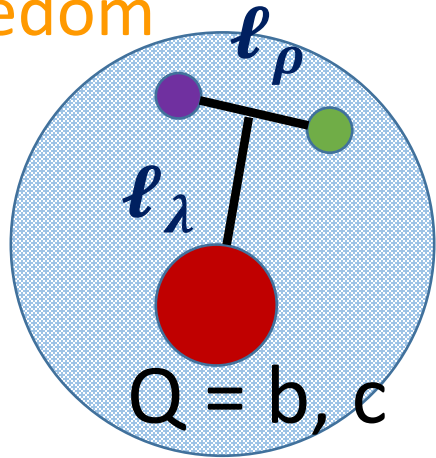
$$H_a = \frac{1 + \not{v}}{2} (P_{a\mu}^* \gamma^\mu - P_a \gamma_5)$$

$1^-$  $0^-$

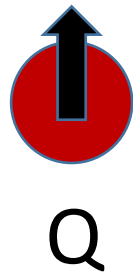
# HQSFS: ground states

The light degrees of freedom in the hadron orbit around the heavy quark, which acts as a source of color moving with the hadrons's velocity. On average, this is also the velocity of the "brown muck".

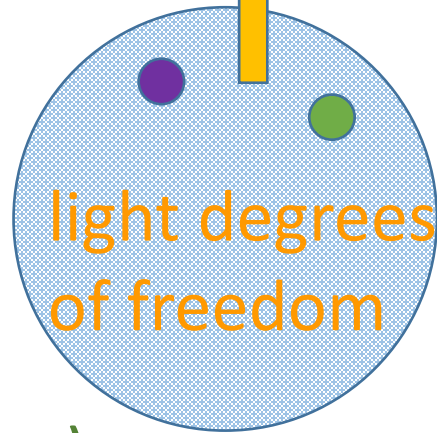
light degrees  
of freedom



$$\vec{J} = \vec{S}_Q + \vec{J}_{ldof}$$



+



light degrees  
of freedom

$\vec{J}_{ldof}^2$  is conserved!  
HQSS

$SU(2N_h)$  symmetry  
in the  $m_Q \rightarrow \infty$  limit

$\ell_\lambda = \ell_\rho = 0, S=0, I=0$  (sym)

$$\underbrace{1/2^+}_{S_Q^P} \otimes \underbrace{1^+}_{j_{ldof}^P} = \underbrace{1/2^+}_{\Sigma_c(2455)}, \underbrace{3/2^+}_{\Sigma_c^*(2520)}$$

HQSS doublet

$$\underbrace{1/2^+}_{S_Q^P} \otimes \underbrace{0^+}_{j_{ldof}^P} = \underbrace{1/2^+}_{\Lambda_c(2286)}$$

# HQSFS: odd parity excited states

CQM: T. Yoshida, E. Hiyaama, A. Hosaka, M. Oka, and K. Sadato, PRD92 (2015) 114029

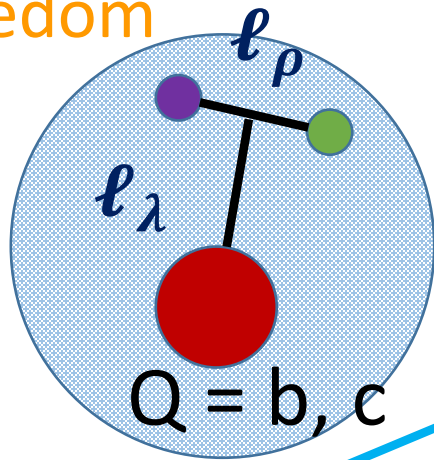
The light degrees of freedom in the hadron orbit around the heavy quark, which acts as a source of color moving with the hadrons's velocity. On average, this is also the velocity of the "brown muck".

light degrees  
of freedom

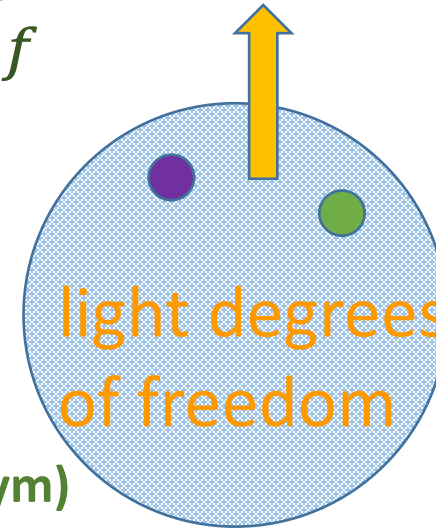
$$\vec{J} = \vec{S}_Q + \vec{J}_{ldof}$$

$\vec{J}_{ldof}^2$  is conserved!  
HQSS

$SU(2N_h)$  symmetry  
in the  $m_Q \rightarrow \infty$  limit



$Q$



light degrees  
of freedom

$\ell_\lambda = 0, \ell_\rho = 1, S=1, I=0$  (sym)

$\ell_\lambda = 1, \ell_\rho = 0, S=0, I=0$  (sym)

$$\underbrace{1/2^+}_{S_Q^P} \otimes \underbrace{1^-}_{j_{ldof}^P} = \underbrace{1/2^-}_{\Lambda_c(2595)}, \underbrace{3/2^-}_{\Lambda_c(2625)} \quad \text{CQM states} \quad \underbrace{1/2^+}_{S_Q^P} \otimes \underbrace{0^-, 1^-, 2^-}_{j_{ldof}^P} = \underbrace{1/2^-, \dots}_{\Lambda_c^*}$$

$\lambda$  - mode excitations

$\rho$  - mode excitations

# HQSFS: odd parity excited states

## chiral molecules

$$\underbrace{\Sigma_c^{(*)} \pi}_{l\text{dof}: 1^+ \otimes 0^- = 1^-} \Rightarrow J^P = 1/2^-, 3/2^-$$

**NLO SU(3) ChPT**: J.-X. Lu, Y. Zhou, H.-X. Chen, J.-J. Xie, and L.-S. Geng, PRD92 (2015) 014036

obtains the  $\Lambda_c(2625)$  [ $J^P = \frac{3}{2}^-$ ] using a moderately large UV cutoff  $\sim 2.1$  GeV

- ✓ CQM degrees of freedom
- ✓ Analogy  $\Lambda(1520)$ ,  $\Lambda(1405)$

$$\Sigma^{(*)} \leftrightarrow \Sigma_c^{(*)}, \bar{K}^{(*)} \leftrightarrow D^{(*)}$$

L. Tolos, J. Schaner-Bielich, and A. Mishra, PRC70 (2004) 025203 ; J. Hofmann and M. Lutz, NPA763 (2005) 90; 766 (2006) 7 ; T. Mizutani and A. Ramos, PRC74 (2006) 065201

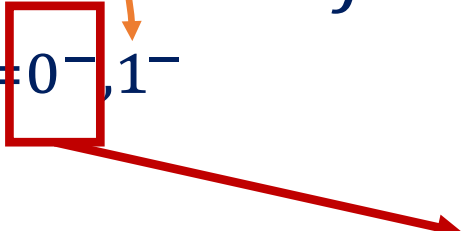
existence of some relevant degrees of freedom (CQM states and/or  $ND^{(*)}$ ) that are not properly accounted for ?

F.-K. Guo, U.-G. Meissner, and B.-S. Zou, Commun. Theor. Phys. 65 (2016) 593  
M. Albaladejo, JN, E. Oset, Z.-F. Sun, and X. Liu, PLB757 (2016) 515

# HQSFS: odd parity excited states hadron molecules

$$\underbrace{\Sigma_c^{(*)} \pi}_{l\text{dof}: 1^+ \otimes 0^- = 1^-} \Rightarrow J^P = 1/2^-, 3/2^-$$

$$\underbrace{ND^{(*)}}_{l\text{dof}: 1/2^+ \otimes 1/2^- = 0^-, 1^-} \Rightarrow J^P = 1/2^-, 3/2^-$$

$\bar{\ell}$  

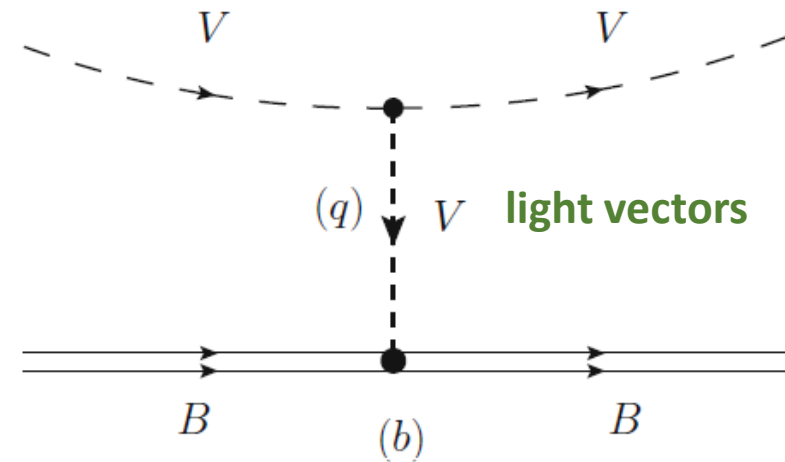
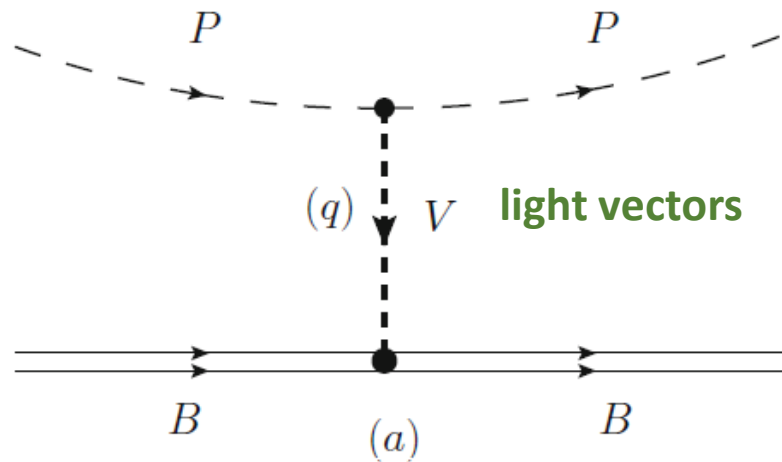
**new configuration !**

key issue:  $ND^{(*)} \rightarrow ND^{(*)}, \Sigma_c^{(*)} \pi$  coupled-channels interaction consistent with HQSS and its breaking pattern. In addition renormalization of BSE amplitudes & short distance (UV) physics

$\Sigma_c$  and  $\Sigma_c^*$  or  $D$  and  $D^*$  are related by a charm quark spin rotation, which commutes with  $H_{QCD}$ , up to  $\Lambda_{QCD}/m_c$  corrections.

LO HQSS does not fix  $ND^{(*)} \rightarrow ND^{(*)}, \Sigma_c^{(*)} \pi$  coupled-channels interaction;  
 There exist several models in the literature consistent with LO HQSS constraints. Moreover, renormalization parameters can be fine tuned to reproduce the position of the  $\Lambda_c(2595)$  and  $\Lambda_c(2625)$  resonances....

*Extended local hidden gauge (ELHG) model* W. Liang, T. Uchino, C. Xiao, E. Oset, EPJ A**51** (2015) 16



+

# A different approach: $SU(6)_{\text{lsf}} \times SU(2)_{\text{HQSS}}$ extension of the Weinberg-Tomozawa $N\pi$ interaction

✓  $\pi$  –octet,  $\rho$  –nonet,

$D_{(s)}^{(*)}, \bar{D}_{(s)}^{(*)}$

✓  $N$  –octet,  $\Delta$  –decuplet,

$\Lambda_c, \Sigma_c^{(*)}, \Xi_c^{(*,')}, \Omega_c^{(*)}$

light spin-flavor (mesons  
and baryons)

- ✓ consistent with HQSS and chiral symmetry
- ✓ dependence of renormalization scheme

- $C = 1$ , C. Garcia-Recio, V.K. Magas, T. Mizutani, JN, A. Ramos, L.L. Salcedo, L. Tolos, PRD79 (2009), 054004; O. Romanets, L. Tolos, C. Garcia-Recio, JN, L.L. Salcedo and R.G.E. Timmermans, PRD85 (2012) 114032.
- $C = -1$ , D. Gamermann, C. Garcia-Recio, JN, L.L. Salcedo and L. Tolos, PRD81 (2010) 094016.
- beauty  $\Lambda_b(5912)$  and  $\Lambda_b(5920)$ , C. Garcia-Recio, JN, O. Romanets, L.L. Salcedo and L. Tolos, PRD 87 (2013) 034032.
- LHCb  $\Omega_c^*$  states, JN, R. Pavao and L. Tolos, EPJC78 (2018) 114.
- $\Xi_c^*$  and  $\Xi_b^*$  states, JN, R. Pavao and L. Tolos, EPJC80 (2020) 22.



## CHARMED BARYONS ( $C = +1$ )

$$\Lambda_c^+ = udc, \Sigma_c^{++} = uuc, \Sigma_c^+ = udc, \Sigma_c^0 = ddc, \\ \Xi_c^+ = usc, \Xi_c^0 = dsc, \Omega_c^0 = ssc$$

See related review:  
[Charmed Baryons](#)

$\Lambda_c^+$	$1/2^+$	****
$\Lambda_c(2595)^+$	$1/2^-$	***
$\Lambda_c(2625)^+$	$3/2^-$	***
$\Lambda_c(2765)^+$ or $\Sigma_c(2765)$		*
$\Lambda_c(2860)^+$	$3/2^+$	***
$\Lambda_c(2880)^+$	$5/2^+$	***
$\Lambda_c(2940)^+$	$3/2^-$	***
$\Sigma_c(2455)$	$1/2^+$	****
$\Sigma_c(2520)$	$3/2^+$	***
$\Sigma_c(2800)$		***
$\Xi_c^+$	$1/2^+$	***
$\Xi_c^0$	$1/2^+$	****
$\Xi_c^{*+}$	$1/2^+$	***
$\Xi_c^{*0}$	$1/2^+$	***
$\Xi_c(2645)$	$3/2^+$	***
$\Xi_c(2790)$	$1/2^-$	***
$\Xi_c(2815)$	$3/2^-$	***
$\Xi_c(2930)$		**
$\Xi_c(2970)$		***
was $\Xi_c(2980)$		
$\Xi_c(3055)$		***
$\Xi_c(3080)$		***
$\Xi_c(3123)$		*
$\Omega_c^0$	$1/2^+$	***
$\Omega_c(2770)^0$	$3/2^+$	***
$\Omega_c(3000)^0$		***
$\Omega_c(3050)^0$		***
$\Omega_c(3065)^0$		***
$\Omega_c(3090)^0$		***
$\Omega_c(3120)^0$		***

Belle

LHCb

## BOTTOM BARYONS ( $B = -1$ )

$$\Lambda_b^0 = udb, \Xi_b^0 = usb, \Xi_b^- = dsb, \Omega_b^- = ssb$$

$\Lambda_b^0$	$1/2^+$	***
$\Lambda_b(5912)^0$	$1/2^-$	***
$\Lambda_b(5920)^0$	$3/2^-$	***
$\Sigma_b$	$1/2^+$	***
$\Sigma_b^*$	$3/2^+$	***
$\Sigma_b(6097)^+$		***
$\Sigma_b(6097)^-$		***
$\Xi_b^0, \Xi_b^-$	$1/2^+$	***
$\Xi_b'(5935)^-$	$1/2^+$	***
$\Xi_b(5945)^0$	$3/2^+$	***
$\Xi_b(5955)^-$	$3/2^+$	***
$\Xi_b(6227)$		***
$\Omega_b^-$	$1/2^+$	***

$b$ -baryon ADMIXTURE ( $\Lambda_b, \Xi_b, \Sigma_b, \Omega_b$ )

LHCb

\*\*\* Existence ranges from very likely to certain, but further confirmation is desirable and/or quantum numbers, branching fractions, etc. are not well determined.

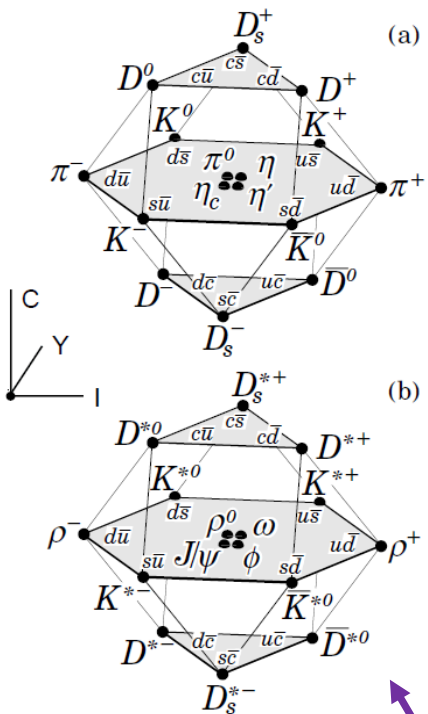
Odd parity open heavy-flavor baryons

\*\*\*\* Existence is certain, and properties are at least fairly explored.

\*\*\* Existence ranges from very likely to certain, but further confirmation is desirable and/or quantum numbers, branching fractions, etc. are not well determined.

\*\* Evidence of existence is only fair.

\* Evidence of existence is poor.



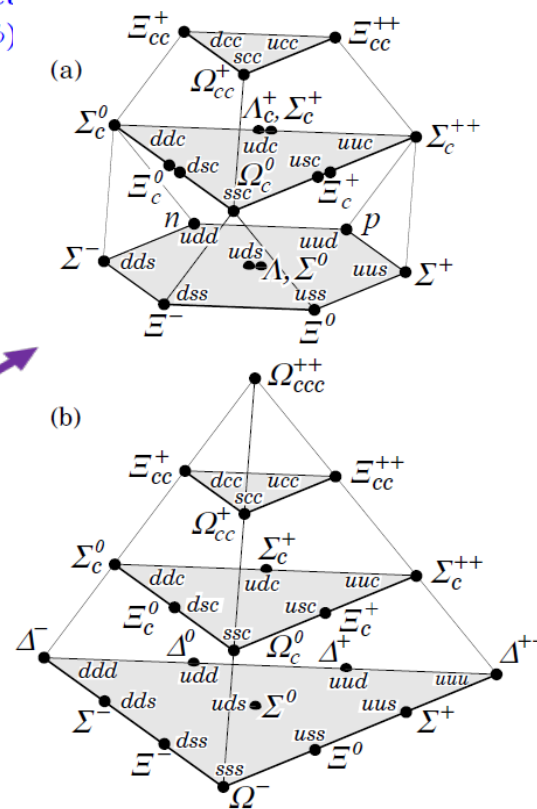
MESONS

With four flavors and the inclusion of spin, there are **64 quark–antiquark ( $q\bar{q}$ ) states**,

$$8 \otimes 8^* = 63 \oplus 1 = \underbrace{(15_1 \oplus 15_3 \oplus 1_3)}_{63} \oplus 1_1.$$

Assuming that the lowest bound state is a  $s$ -state and since the relative parity of a fermion–antifermion pair is odd, the **SU(4) 15-plet of pseudoscalar ( $D_s, D, K, \pi, \eta, \eta_c, \bar{K}, \bar{D}, \bar{D}_s$ ) and the 16-plet of vector ( $D_s^*, D^*, K^*, \rho, \omega, J/\Psi, \bar{K}^*, \bar{D}^*, \bar{D}_s^*, \phi$ ) mesons are placed in the 63 representation.**

BARYONS



With four flavors and the inclusion of spin, there are **512 three quark states**,

$$8 \otimes 8 \otimes 8 = 120 \oplus 56 \oplus 168 \oplus 168 = \underbrace{(20_2 \oplus 20'_4)}_{120} \oplus \underbrace{(4_4 \oplus 20_2)}_{56} \oplus 2 \times \underbrace{(20'_2 \oplus 20_4 \oplus 20_2 \oplus 4_2)}_{168}.$$

with  $\begin{smallmatrix} \square & \square \\ \square & \square \end{smallmatrix}$  and  $\begin{smallmatrix} \square & \square & \square \\ \square & \square & \square \end{smallmatrix}$ , the **20** and **20'** SU(4) representations, respectively. Lowest-lying baryons are placed in the **120 of SU(8)**, since it can accommodate in the light sector an octet of spin-1/2 baryons and a decuplet of spin-3/2 baryons, which are precisely the SU(3)-spin combinations of the low-lying baryon states ( $N, \Sigma, \Lambda, \Xi$  and  $\Delta, \Sigma^*, \Xi^*, \Omega$ ). The remaining states in the  $20_2$  and  $20'_4$  are completed with the charmed baryons:  $\Xi_{cc}, \Omega_{cc}, \Lambda_c, \Sigma_c, \Xi_c, \Xi'_c, \Omega_c$  and  $\Omega_{ccc}, \Xi_{cc}^*, \Omega_{cc}^*, \Sigma_c^*, \Xi_c^*$ , respectively.

$$63 \otimes 120 = 120 \oplus 168 \oplus 2520 \oplus 4752$$

**SU(8) symmetry**  $\rightarrow$  4 **WEIME's**. Equivalently,

$$63 \otimes 63 = 1 \oplus 63_s \oplus 63_a \oplus 720 \oplus 945 \oplus 945^* \oplus 1232$$

$$120 \otimes 120^* = 1 \oplus 63 \oplus 1232 \oplus 13104$$

lead<sup>a</sup> to a total of 4 different  $t$ -channel **SU(8) couplings**

$$\begin{aligned} & \left( (M^\dagger \otimes M)_1 \otimes (B^\dagger \otimes B)_1 \right)_1, & \left( (M^\dagger \otimes M)_{63_a} \otimes (B^\dagger \otimes B)_{63} \right)_1, \\ & \left( (M^\dagger \otimes M)_{63_s} \otimes (B^\dagger \otimes B)_{63} \right)_1, & \left( (M^\dagger \otimes M)_{1232} \otimes (B^\dagger \otimes B)_{1232} \right)_1 \end{aligned}$$

<sup>a</sup>The singlet representation **1** only appears in the reduction of the product of one representation by its complex-conjugate. **1**, **63** and **1232** are self-complex conjugate representations.

TABLE II:  $I = 0, J = 1/2, S = 0, C = 1$ . Meson-Baryon states with more than one  $c$  quark have not been included.

	$ND$	$\Lambda D_s$	$\Lambda_c \eta$	$\Lambda_c \eta'$	$\Sigma_c \pi$	$\Xi'_c K$	$\Xi_c K$	$ND^*$	$\Lambda D_s^*$	$\Lambda_c \omega$	$\Lambda_c \phi$	$\Sigma_c \rho$	$\Xi'_c K^*$	$\Xi_c K^*$	$\Sigma_c^* \rho$	$\Xi_c^* K^*$
$ND$	-3	$-\sqrt{3}$	$\sqrt{\frac{1}{2}}$	1	$\sqrt{\frac{3}{2}}$	0	0	$-\sqrt{27}$	-3	$\sqrt{\frac{2}{3}}$	0	$-\sqrt{\frac{1}{2}}$	0	0	2	0
$\Lambda D_s$	$-\sqrt{3}$	-1	$-\sqrt{\frac{2}{3}}$	$\sqrt{\frac{1}{3}}$	0	$\sqrt{\frac{3}{2}}$	$\sqrt{\frac{1}{2}}$	-3	$-\sqrt{3}$	0	$-\sqrt{3}$	0	$-\sqrt{\frac{1}{2}}$	$\sqrt{\frac{3}{2}}$	0	2
$\Lambda_c \eta$	$\sqrt{\frac{1}{2}}$	$-\sqrt{\frac{2}{3}}$	0	0	0	0	$-\sqrt{3}$	$\sqrt{\frac{3}{2}}$	$-\sqrt{2}$	0	0	0	$-\sqrt{3}$	0	0	$-\sqrt{6}$
$\Lambda_c \eta'$	1	$\sqrt{\frac{1}{3}}$	0	0	0	0	0	$\sqrt{3}$	1	0	0	0	0	0	0	0
$\Sigma_c \pi$	$\sqrt{\frac{3}{2}}$	0	0	0	-4	$-\sqrt{3}$	0	$-\sqrt{\frac{1}{2}}$	0	0	0	$-\sqrt{\frac{4}{3}}$	-2	$-\sqrt{3}$	$\sqrt{\frac{32}{3}}$	$\sqrt{2}$
$\Xi'_c K$	0	$\sqrt{\frac{3}{2}}$	0	0	$-\sqrt{3}$	-2	0	0	$-\sqrt{\frac{1}{2}}$	-1	$-\sqrt{2}$	-2	$-\sqrt{\frac{16}{3}}$	0	$\sqrt{2}$	$\sqrt{\frac{8}{3}}$
$\Xi_c K$	0	$\sqrt{\frac{1}{2}}$	$-\sqrt{3}$	0	0	0	-2	0	$\sqrt{\frac{3}{2}}$	0	0	$-\sqrt{3}$	0	0	$-\sqrt{6}$	0
$ND^*$	$-\sqrt{27}$	-3	$\sqrt{\frac{3}{2}}$	$\sqrt{3}$	$-\sqrt{\frac{1}{2}}$	0	0	-9	$-\sqrt{27}$	$-\sqrt{\frac{3}{2}}$	0	$\sqrt{\frac{25}{6}}$	0	0	$\sqrt{\frac{4}{3}}$	0
$\Lambda D_s^*$	-3	$-\sqrt{3}$	$-\sqrt{2}$	1	0	$-\sqrt{\frac{1}{2}}$	$\sqrt{\frac{3}{2}}$	$-\sqrt{27}$	-3	0	1	0	$\sqrt{\frac{25}{6}}$	$-\sqrt{\frac{1}{2}}$	0	$\sqrt{\frac{4}{3}}$
$\Lambda_c \omega$	$\sqrt{\frac{3}{2}}$	0	0	0	0	-1	0	$-\sqrt{\frac{3}{2}}$	0	0	0	-4	$-\sqrt{\frac{4}{3}}$	-1	$\sqrt{8}$	$\sqrt{\frac{64}{3}}$
$\Lambda_c \phi$	0	$-\sqrt{3}$	0	0	0	$-\sqrt{2}$	0	0	1	0	0	0	$\sqrt{\frac{8}{3}}$	$-\sqrt{2}$	0	$-\sqrt{\frac{4}{3}}$
$\Sigma_c \rho$	$-\sqrt{\frac{1}{2}}$	0	0	0	$-\sqrt{\frac{64}{3}}$	-2	$-\sqrt{3}$	$\sqrt{\frac{25}{6}}$	0	-4	0	$-\frac{20}{3}$	$-\sqrt{\frac{49}{3}}$	-2	$-\sqrt{\frac{8}{3}}$	$-\sqrt{\frac{32}{3}}$
$\Xi'_c K^*$	0	$-\sqrt{\frac{1}{2}}$	$-\sqrt{3}$	0	-2	$-\sqrt{\frac{16}{3}}$	0	0	$\sqrt{\frac{25}{6}}$	$-\sqrt{\frac{4}{3}}$	$\sqrt{\frac{8}{3}}$	$-\sqrt{\frac{49}{3}}$	-2	$-\sqrt{\frac{16}{3}}$	$-\sqrt{\frac{3}{3}}$	0
$\Xi_c K^*$	0	$\sqrt{\frac{3}{2}}$	0	0	$-\sqrt{3}$	0	0	0	$-\sqrt{\frac{1}{2}}$	-1	$-\sqrt{2}$	-2	$-\sqrt{\frac{16}{3}}$	-2	$\sqrt{2}$	$\sqrt{\frac{4}{3}}$
$\Sigma_c^* \rho$	2	0	0	0	$\sqrt{\frac{32}{3}}$	$\sqrt{2}$	$-\sqrt{6}$	$\sqrt{\frac{4}{3}}$	0	$\sqrt{8}$	0	$-\sqrt{\frac{8}{3}}$	$-\sqrt{\frac{4}{3}}$	$\sqrt{2}$	$-\frac{22}{3}$	$-\sqrt{\frac{52}{3}}$
$\Xi_c^* K^*$	0	2	$-\sqrt{6}$	0	$\sqrt{2}$	$\sqrt{\frac{8}{3}}$	0	0	$\sqrt{\frac{4}{3}}$	$\sqrt{\frac{2}{3}}$	$-\sqrt{\frac{4}{3}}$	$-\sqrt{\frac{2}{3}}$	0	$\sqrt{\frac{8}{3}}$	$-\sqrt{\frac{64}{3}}$	-2

and  $D$  a matrix in the coupled channel space. f.i.,  $I = 0, J = 1/2, S = 0, C = 1$ :  $ND, \Lambda D_s, \Lambda_c \eta, \Lambda_c \eta', \Sigma_c \pi, \Xi'_c K, \Xi_c K, ND^*, \Lambda D_s^*, \Lambda_c \omega, \Lambda_c \phi, \Sigma_c \rho, \Xi'_c K^*, \Xi_c K^*, \Sigma_c^* \rho, \Xi_c^* K^*$ .

# SU(6)<sub>lsf</sub> $\times$ HQSS Extension of the WT Lagrangian

$DN - D^*N$  might play an important role  $\Leftarrow$  necessary to accommodate spin symmetry in the charm sector.

+ symmetry breaking: masses and decay constants

To guaranty that the SU(8) amplitudes will reduce to those deduced from the SU(3) WT Lagrangian (**63**  $\Rightarrow$  **adjoint representation**)

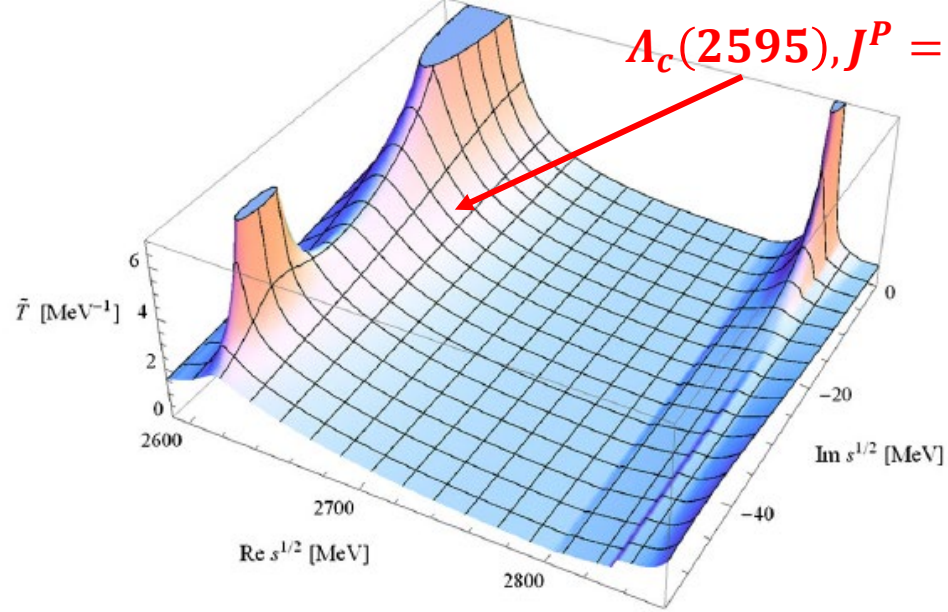
$$\mathcal{L}_{\text{WT}}^{\text{SU}(8)} = \left( (M^\dagger \otimes M)_{63_a} \otimes (B^\dagger \otimes B)_{63} \right)_1$$

$$\mathcal{L}_{\text{WT}}^{\text{SU}(6)} = \left( (M^\dagger \otimes M)_{35_a} \otimes (B^\dagger \otimes B)_{35} \right)_1$$

which is the natural and unique SU(8) extension of the usual SU(3) WT Lagrangian. The reduction of this lagrangian to the SU(6) sector reproduces  $\mathcal{L}_{\text{WT}}^{\text{SU}(6)}$ . Tree level amplitudes in a  $JISC$  sector,

$$V_{ab}^{JISC}(\sqrt{s}) = D_{ab}^{JISC} \frac{\sqrt{s} - M}{4f^2}$$

$M$  the common mass of the baryons of the SU(8) 120.



$\Lambda_c(2595), J^P = \frac{1}{2}^-$

Dynamics of  $\Lambda_c(2595)$ :

PHYSICAL REVIEW D **85**, 114032 (2012)

- Two pole structure: Narrow (wide)  $\Rightarrow$  small (large) coupling to the open channel  $\Sigma_c \pi$ . Similar to  $\Lambda(1405)$ .
- Narrow  $\Lambda_c(2595)$ : Reminiscent of a  $D^* N$  bound state  
Hofmann+Lutz, NPA763 (2005) 90  $\Rightarrow$   $DN$  bound state,

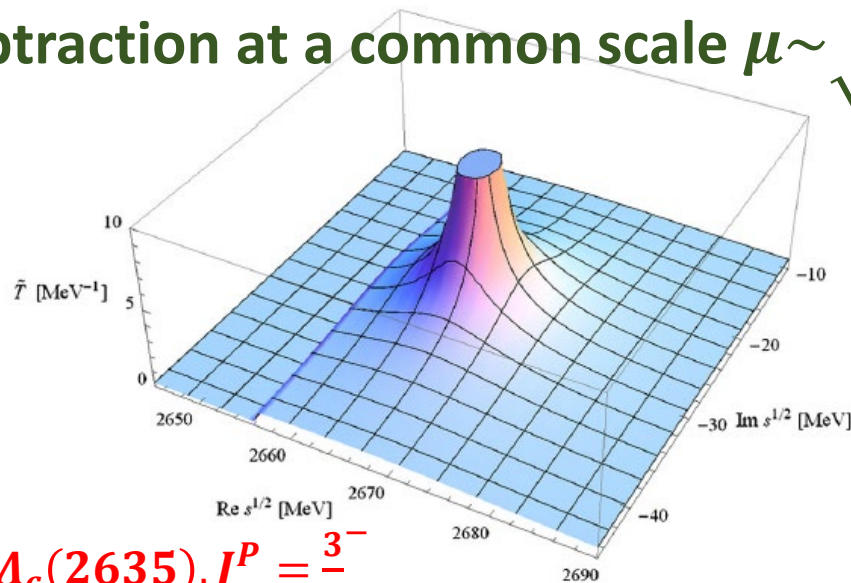
$$V = -3 \frac{\sqrt{s} - M_N}{4 \boxed{f_\pi^2}}$$

HQSS  $\Rightarrow$   $DN$ ,  $D^* N$  coupled channels,

$$V = D \frac{\sqrt{s} - M_N}{4 \boxed{f_D^2}}, \quad D = \begin{pmatrix} -3 & -\sqrt{27} \\ -\sqrt{27} & -9 \end{pmatrix} \begin{matrix} DN \\ D^* N \end{matrix}$$

J. Hofmann and M. Lutz, NPA763 (2005) 90

subtraction at a common scale  $\mu \sim \sqrt{m_\pi^2 + M_{\Sigma_c}^2}$



$\Lambda_c(2635), J^P = \frac{3}{2}^-$

Eigenvalues and eigenvectors,

light degrees of freedom  
coupled to spin-parity  $0^-$

HQSS

$$\lambda_1 = -12 \Rightarrow |1\rangle = \frac{1}{2}|DN\rangle + \frac{\sqrt{3}}{2}|D^*N\rangle, \quad \overbrace{-12/f_D^2}^{\text{HQSS}} \sim \underbrace{-3/f_\pi^2}_{\text{SU}(4)}$$

$$\lambda_1 = 0 \Rightarrow |2\rangle = \frac{1}{2}|D^*N\rangle - \frac{\sqrt{3}}{2}|DN\rangle, \quad (\text{sterile})$$



$$T^J(s) = \frac{1}{1 - V^J(s)G^J(s)} V^J(s),$$

dependence of  
renormalization scheme

$$G_i(s) = i2M_i \int \frac{d^4q}{(2\pi)^4} \frac{1}{q^2 - m_i^2 + i\epsilon} \frac{1}{(P - q)^2 - M_i^2 + i\epsilon}$$

$$= \underbrace{\overline{G}_i(s)}_{\text{finite}} + \underbrace{G_i(s_{i+})}_{\text{UV divergent}}, \quad s_{i+} = (M_i + m_i)^2$$

different UV cutoffs for each  
meson-baryon channel

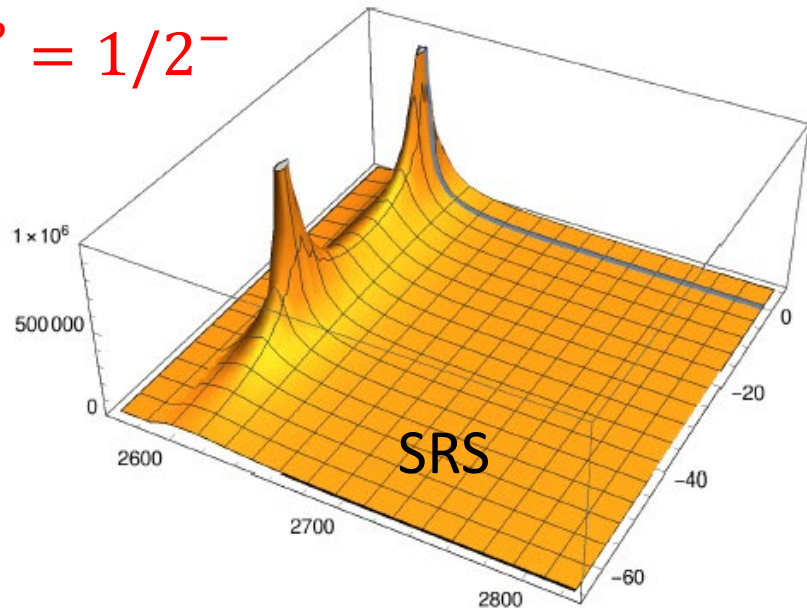
**subtraction at a common scale  $\mu \sim \sqrt{m_\pi^2 + M_{\Sigma_c}^2}$ :**  
J. Hofmann and M. Lutz, NPA763 (2005) 90

$$G_i^\mu(s_{i+}) = -\overline{G}_i(\mu^2)$$

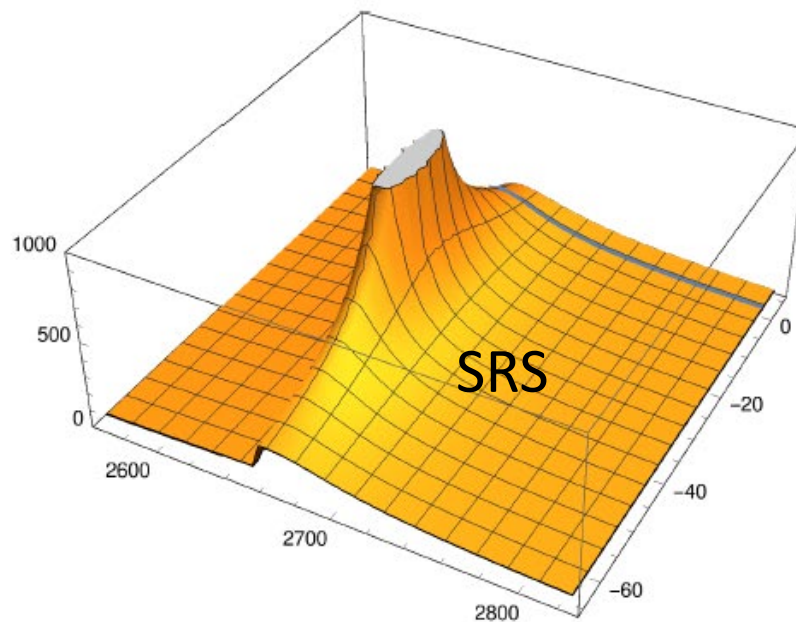
**common UV cutoff  $\Lambda = 650 \text{ MeV}$**

$$G_i^\Lambda(s_{i+}) = \frac{1}{4\pi^2} \frac{M_i}{m_i + M_i} \left( m_i \ln \boxed{\Lambda} + \sqrt{\Lambda^2 + m_i^2} + M_i \ln \boxed{\Lambda} + \sqrt{\Lambda^2 + M_i^2} \right)$$

$$J^P = 1/2^-$$



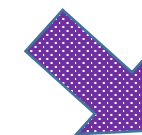
$$J^P = 3/2^-$$



subtraction at a common  
scale (no fit!)

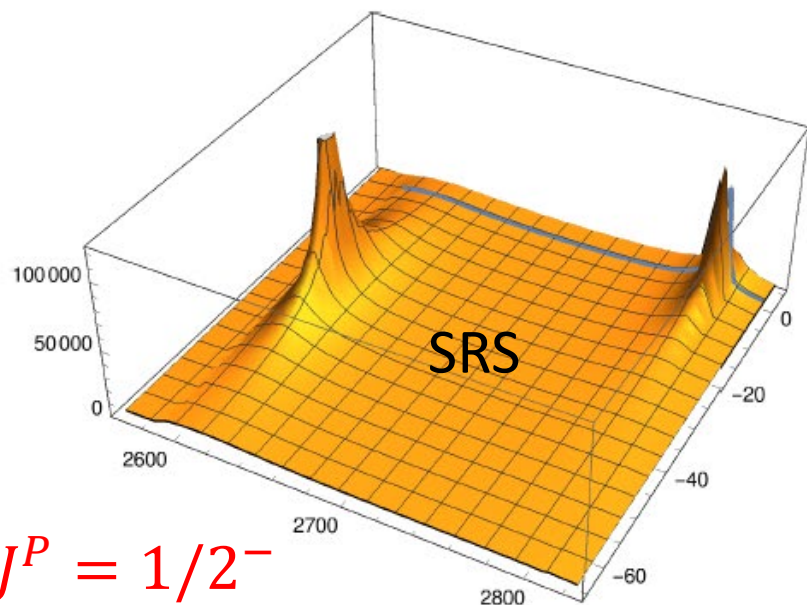
- ✓ main features of  $3/2^-$  pole do not depend much on the RS:  $M = 2660 - 2680$  MeV and  $\Gamma = 55 - 65$  MeV: difficult to assign it to the narrow  $\Lambda_c(2625)$ .

- ✓ spectrum in the  $1/2^-$  sector depends strongly on the adopted RS

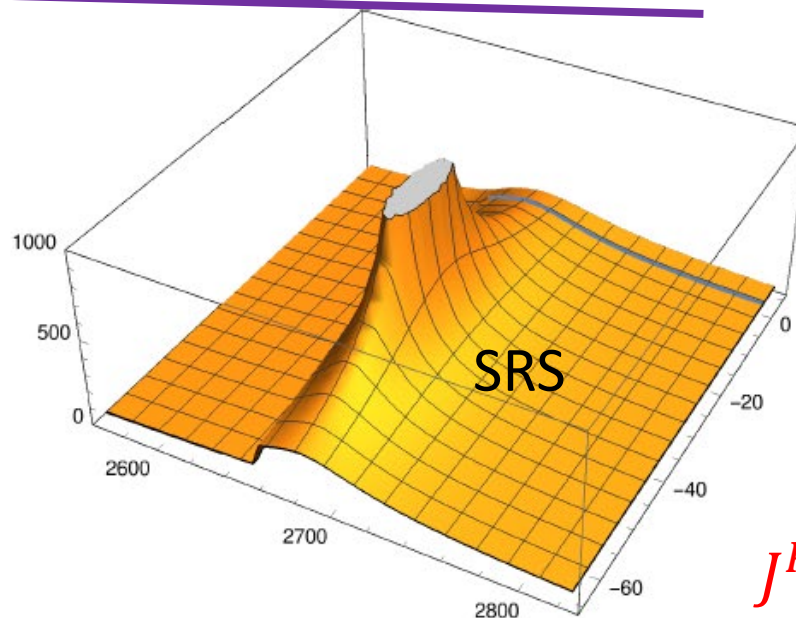


common UV cutoff 650 MeV  
(no fit!)

$$J^P = 1/2^-$$

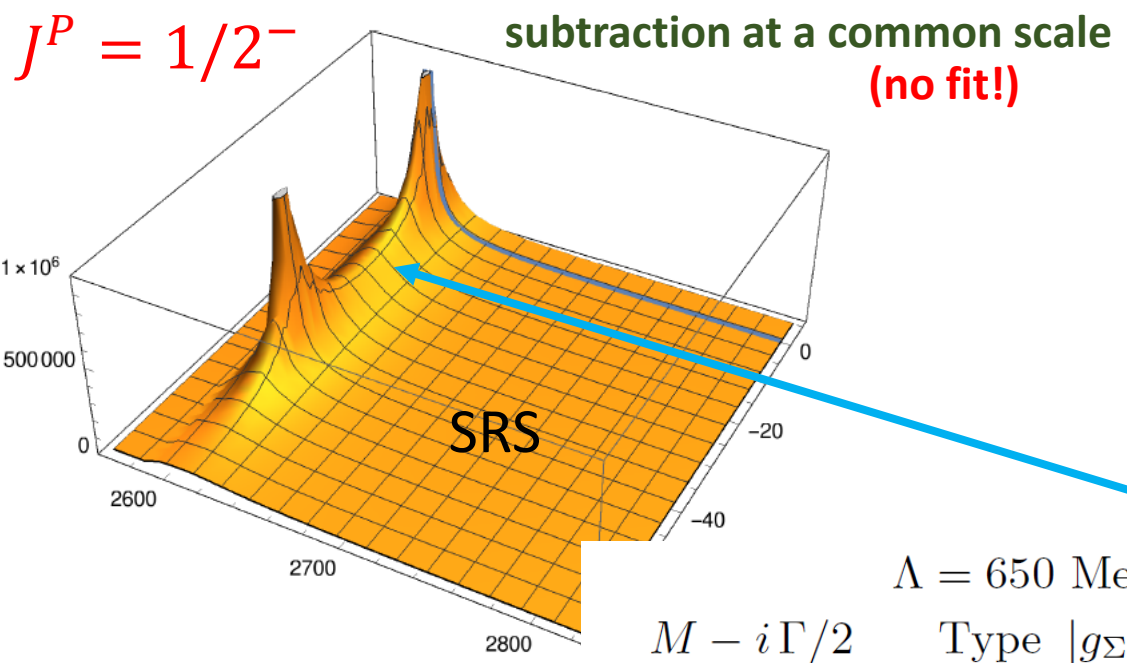


$$J^P = 3/2^-$$



$$C = 1, ND^{(*)}, \Sigma_c^{(*)} \pi \text{ coupled-channels}$$

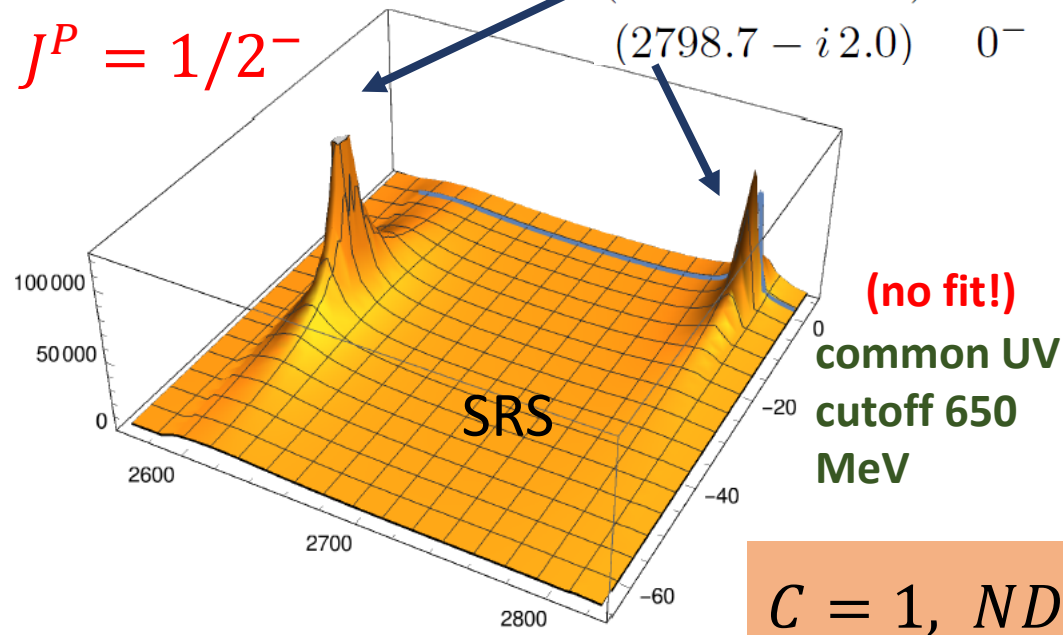
Absolute value of the determinant of the  $T$ -matrix



Two pole pattern, but

- ✓ **narrow resonance** has a small coupling to  $\Sigma_c \pi$ , since it has **dominant  $0^-$  configuration** for the light degrees of freedom. Moreover **its position depends strongly on the RS**, since it might appear close to the  $ND$  or  $\Sigma_c \pi$  thresholds ( $\sim 200$  MeV of difference!). In the latter case (subtraction at a common scale), it could be identified with the  $\Lambda_c(2595)$ . In both RS's the narrow resonance has large  $ND$  and  $ND^*$  components.

$\Lambda = 650$ MeV						$SC_\mu (\alpha = 0.95)$				
$M - i \Gamma/2$	Type	$ g_{\Sigma_c \pi} $	$ g_{ND} $	$ g_{ND^*} $		$M - i \Gamma/2$	Type	$ g_{\Sigma_c \pi} $	$ g_{ND} $	$ g_{ND^*} $
$(2609.9 - i 28.8)$	$1^-$	2.0	2.3	0.7		$(2608.9 - i 38.6)$	$1^-$	2.3	2.0	1.9
$(2798.7 - i 2.0)$	$0^-$	0.3	1.8	4.1		$(2610.2 - i 1.2)$	$0^-$	0.5	3.9	6.2



- ✓ **broad resonance** has a large coupling to  $\Sigma_c \pi$ , and hence has a **dominant  $1^-$  configuration** for the light degrees of freedom. It is located around 2610 MeV and with a width of 60-80 MeV. In the subtraction at a common scale RS, this state will be completely shadowed by the narrow  $\Lambda_c(2595)$  state. When a common UV cutoff is used, it is difficult to assign this pole to the  $\Lambda_c(2595)$ .

$C = 1, ND^{(*)}, \Sigma_c^{(*)} \pi$  coupled-channels



# ...and CQM predictions:

$$\underbrace{1/2^+}_{s_Q^P} \otimes \underbrace{1^-}_{j_{ldof}^P} = \underbrace{1/2^-}_{\Lambda_c(2595)}, \underbrace{3/2^-}_{\Lambda_c(2625)}$$

PHYSICAL REVIEW D **92**, 114029 (2015)

## Spectrum of heavy baryons in the quark model

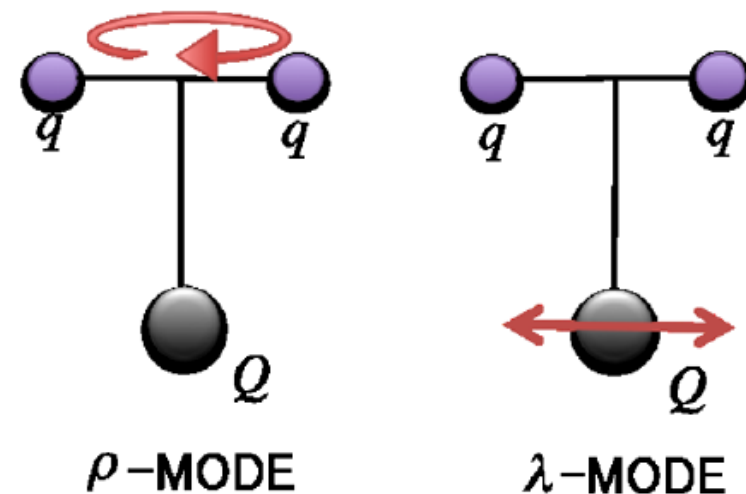
T. Yoshida,<sup>1,\*</sup> E. Hiyama,<sup>2,1,3</sup> A. Hosaka,<sup>4,3</sup> M. Oka,<sup>1,3</sup> and K. Sadato<sup>4,†</sup>

$\Lambda_c$		
$J^P$	Theory (MeV)	Experiment (MeV)
$\frac{1}{2}^+$	2285	2285
	2857	
	3123	
	2920	
$\frac{3}{2}^+$	3175	
	3191	
	2922	
	3202	
$\frac{5}{2}^+$	3230	2881
$\frac{1}{2}^-$	2628	2595
	2890	
	2933	

$\Lambda_c$		
$J^P$	Theory (MeV)	Experiment (MeV)
$\frac{3}{2}^-$	2630	2628
	2917	
	2956	
	2960	
	3444	
	3491	

**bare CQM state should be explicitly taken into account in the dynamics, in particular for the  $\Lambda_c(2625)$  resonance: for these energies it produces a rapidly changing energy dependent interaction**

$\lambda$  – mode excitations



$\ell_\lambda = 1, \ell_\rho = 0, S=0, L=0$  (sym)

Lowest lying  $\left(\frac{1}{2}\right)^-$  and  $\left(\frac{3}{2}\right)^-$   $\Lambda_Q$  resonances:  
from the strange to the bottom sectors

## CHARMED BARYONS ( $C = +1$ )



$$\Lambda_c^+ = udc, \Sigma_c^{++} = uuc, \Sigma_c^+ = udc, \Sigma_c^0 = ddc,$$

$$\Xi_c^+ = usc, \Xi_c^0 = dsc, \Omega_c^0 = ssc$$

$$\Lambda_c^+ \quad 1/2^+ \quad ****$$

$$\Lambda_c(2595)^+ \quad 1/2^- \quad ***$$

$$\Lambda_c(2625)^+ \quad 3/2^- \quad ***$$

$$\Lambda_c(2765)^+ \text{ or } \Sigma_c(2765) \quad *$$

$$\Lambda_c(2860)^+ \quad 3/2^+ \quad ***$$

$$\Lambda_c(2880)^+ \quad 5/2^+ \quad ***$$

$$\Lambda_c(2940)^+ \quad 3/2^- \quad ***$$

$$\Sigma_c(2455) \quad 1/2^+ \quad ****$$

$$\Sigma_c(2520) \quad 3/2^+ \quad ***$$

## BOTTOM BARYONS ( $B = -1$ )

$$\Lambda_b^0 = udb, \Xi_b^0 = usb, \Xi_b^- = dsb, \Omega_b^- = ssb$$

$$\Lambda_b^0 \quad 1/2^+ \quad ***$$

$$\Lambda_b(5912)^0 \quad 1/2^- \quad ***$$

$$\Lambda_b(5920)^0 \quad 3/2^- \quad ***$$

$$\Lambda_b(6070)^0 \quad 1/2^+ \quad ***$$

$$\Lambda_b(6146)^0 \quad 3/2^+ \quad ***$$

$$\Lambda_b(6152)^0 \quad 5/2^+ \quad ***$$

$$\Sigma_b \quad 1/2^+ \quad ***$$

$$\Sigma_b^* \quad 3/2^+ \quad ***$$

Lowest-lying open  
heavy-flavor baryons

# HQSFS: odd parity excited states

CQM: T. Yoshida, E. Hiyama, A. Hosaka, M. Oka, and K. Sadato, PRD92 (2015) 114029

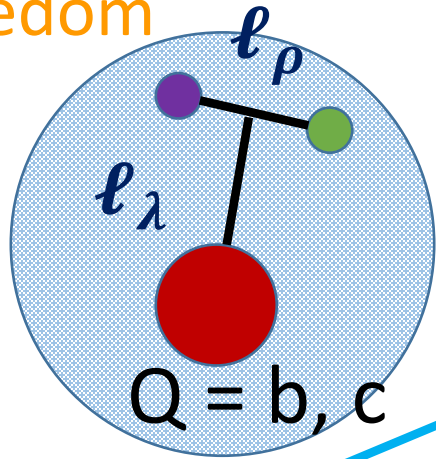
The light degrees of freedom in the hadron orbit around the heavy quark, which acts as a source of color moving with the hadrons's velocity. On average, this is also the velocity of the "brown muck".

light degrees  
of freedom

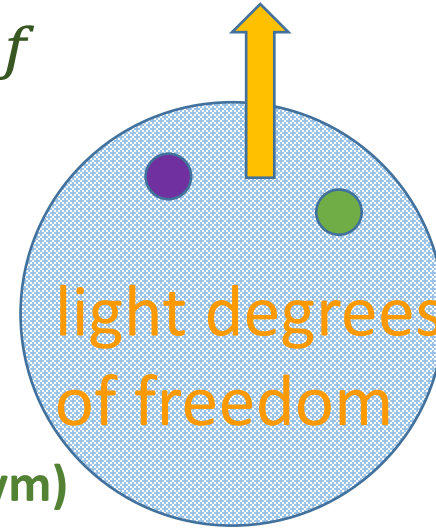
$$\vec{J} = \vec{S}_Q + \vec{J}_{l\text{dof}}$$

$\vec{J}_{l\text{dof}}^2$  is conserved!  
HQSS

$SU(2N_h)$  symmetry  
in the  $m_Q \rightarrow \infty$  limit



$Q$



light degrees  
of freedom

$$\ell_\lambda = 0, \ell_\rho = 1, S=1, I=0 \text{ (sym)}$$

$$\ell_\lambda = 1, \ell_\rho = 0, S=0, I=0 \text{ (sym)}$$

$$\underbrace{1/2^+}_{S_Q^P} \otimes \underbrace{1^-}_{j_{l\text{dof}}^P} = \underbrace{1/2^-}_{\Lambda_c(2595)}, \underbrace{3/2^-}_{\Lambda_c(2625)} \quad \text{CQM states} \quad \underbrace{1/2^+}_{S_Q^P} \otimes \underbrace{0^-, 1^-, 2^-}_{j_{l\text{dof}}^P} = \underbrace{1/2^-, \dots}_{\Lambda_c^*}$$

$\lambda$  - mode excitations

$\rho$  - mode excitations

# HQSFS: odd parity excited states

## chiral molecules

$$\underbrace{\sum_c^{(*)} \pi}_{l\text{dof}: 1^+ \otimes 0^- = 1^-} \Rightarrow J^P = 1/2^-, 3/2^-$$

**NLO SU(3) ChPT**: J.-X. Lu, Y. Zhou, H.-X. Chen, J.-J. Xie, and L.-S. Geng, PRD92 (2015) 014036

obtains the  $\Lambda_c(2625)$  [ $J^P = \frac{3}{2}^-$ ] using a moderately large UV cutoff  $\sim 2.1$  GeV

- ✓ CQM degrees of freedom
- ✓ Analogy  $\Lambda(1520)$ ,  $\Lambda(1405)$

$$\Sigma^{(*)} \leftrightarrow \Sigma_c^{(*)}, \bar{K}^{(*)} \leftrightarrow D^{(*)}$$

L. Tolos, J. Schaner-Bielich, and A. Mishra, PRC70 (2004) 025203 ; J. Hofmann and M. Lutz, NPA763 (2005) 90; 766 (2006) 7 ; T. Mizutani and A. Ramos, PRC74 (2006) 065201

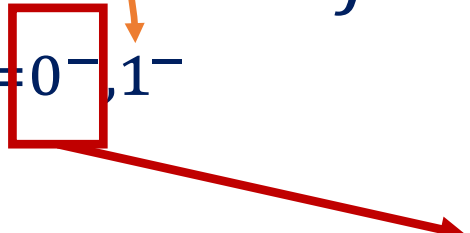
existence of some relevant degrees of freedom (CQM states and/or  $ND^{(*)}$ ) that are not properly accounted for ?

F.-K. Guo, U.-G. Meissner, and B.-S. Zou, Commun. Theor. Phys. 65 (2016) 593  
M. Albaladejo, JN, E. Oset, Z.-F. Sun, and X. Liu, PLB757 (2016) 515

# HQSFS: odd parity excited states hadron molecules

$$\underbrace{\Sigma_c^{(*)} \pi}_{l\text{dof}: 1^+ \otimes 0^- = 1^-} \Rightarrow J^P = 1/2^-, 3/2^-$$

$$\underbrace{ND^{(*)}}_{l\text{dof}: 1/2^+ \otimes 1/2^- = 0^-, 1^-} \Rightarrow J^P = 1/2^-, 3/2^-$$

$\bar{\ell}$  

but....

**new configuration !**

key issue:  $ND^{(*)} \rightarrow ND^{(*)}, \Sigma_c^{(*)} \pi$  coupled-channels interaction consistent with HQSS and its breaking pattern. In addition renormalization of BSE amplitudes & short distance (UV) physics

$\Sigma_c$  and  $\Sigma_c^*$  or  $D$  and  $D^*$  are related by a charm quark spin rotation, which commutes with  $H_{QCD}$ , up to  $\Lambda_{QCD}/m_c$  corrections.





$$T^J(s) = \frac{1}{1 - V^J(s)G^J(s)} V^J(s),$$

$$V_\chi^{J=1/2} \sim V_\chi^{J=3/2} \sim -4 \frac{\sqrt{s} - M}{2f^2}$$

$$V^J = V_\chi^J + V_{ex}^J$$

$$G_i(s) = i2M_i \int \frac{d^4q}{(2\pi)^4} \frac{1}{q^2 - m_i^2 + i\epsilon} \frac{1}{(P - q)^2 - M_i^2 + i\epsilon}$$

$$= \underbrace{\overline{G}_i(s)}_{\text{finite}} + \underbrace{G_i(s_{i+})}_{\text{UV divergent}}, \quad s_{i+} = (M_i + m_i)^2$$

different UV cutoffs for each meson-baryon channel

subtraction at a common scale  $\mu \sim \sqrt{m_\pi^2 + M_{\Sigma_c}^2}$ :  
J. Hofmann and M. Lutz, NPA763 (2005) 90

$$G_i^\mu(s_{i+}) = -\overline{G}_i(\mu^2)$$

common UV cutoff  
 $\Lambda \sim 0.5 - 1 \text{ GeV}$

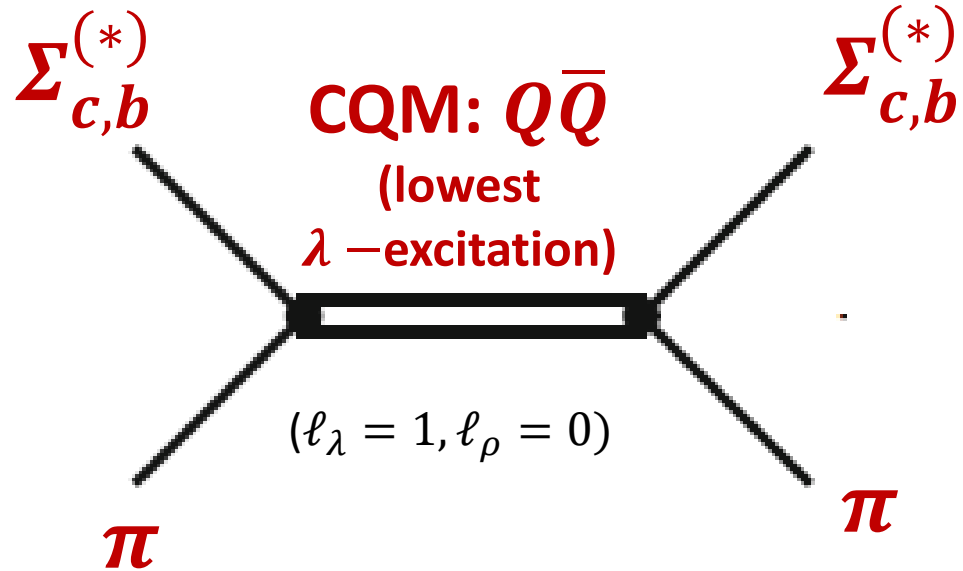
$$G_i^\Lambda(s_{i+}) = \frac{1}{4\pi^2} \frac{M_i}{m_i + M_i} \left( m_i \ln \frac{m_i}{\Lambda + \sqrt{\Lambda^2 + m_i^2}} + M_i \ln \frac{M_i}{\Lambda + \sqrt{\Lambda^2 + M_i^2}} \right)$$

renormalization scheme  
consistent with HQS

J.-X. Lu et al., PRD92 (2015) 014036



CQM: T. Yoshida, E. Hiyama, A. Hosaka, M. Oka, and K. Sadato,  
PRD92 (2015) 114029



$$V_{ex}^{J=1/2} \sim V_{ex}^{J=3/2} = 2M_{\text{CQM}} \frac{d_Q^2}{s - M_{\text{CQM}}^2}$$

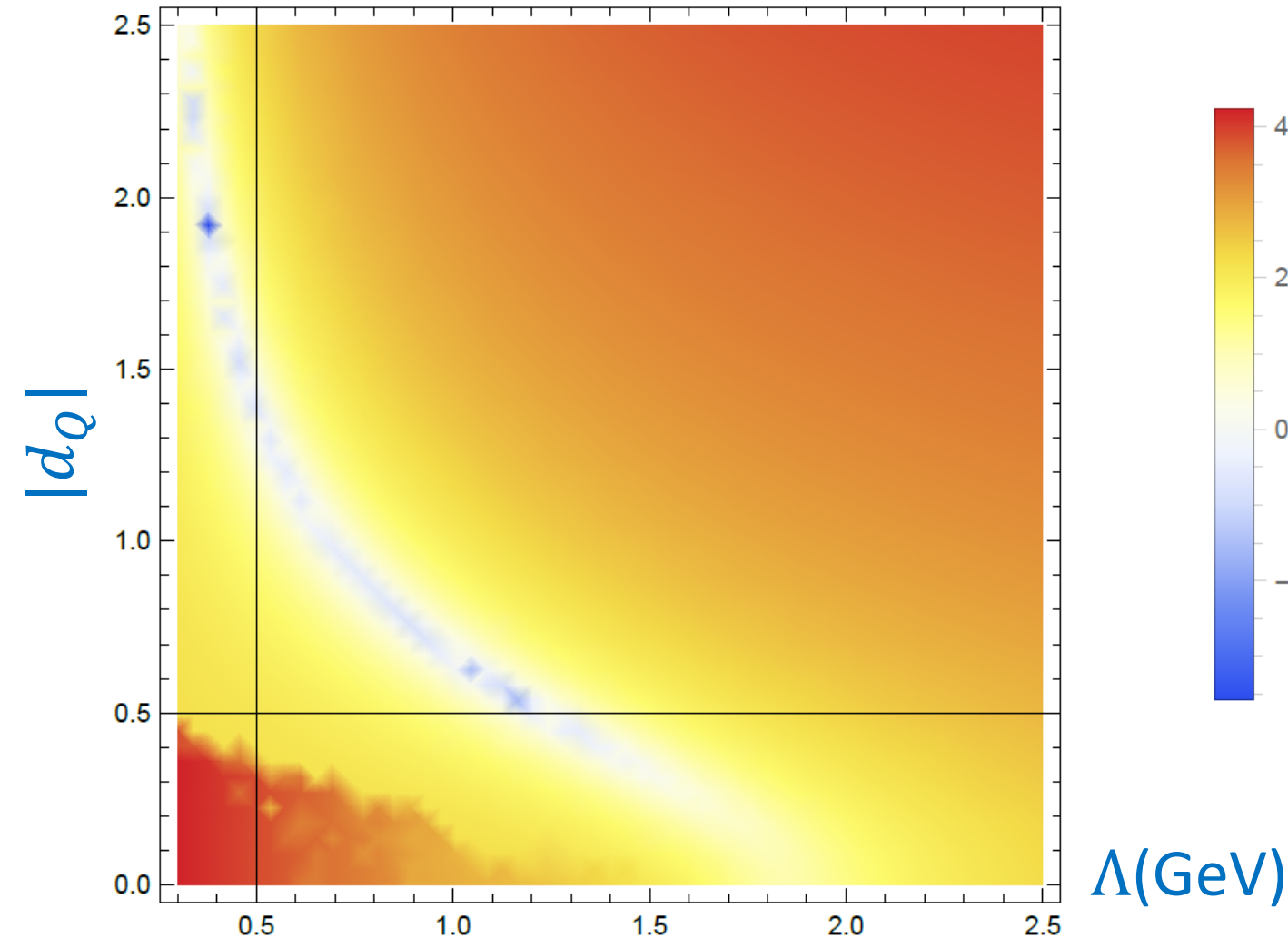
LEC  $d_Q^2$  (up to  $\Lambda_{\text{QCD}}/m_Q$  corrections):

- HQSS: independent of heavy quark spin ( $J=1/2$  or  $J=3/2$ )
- HQFS: independent of heavy quark flavor (bottom or charm)

$$\underbrace{1/2^+}_{S_Q^P} \otimes \underbrace{1^-}_{j_{ldof}^P} = \underbrace{1/2^-}_{\Lambda_b(5912), \Lambda_c(2595)}, \underbrace{3/2^-}_{\Lambda_b(5920), \Lambda_c(2625)}$$

$$\chi^2(|d_Q|, \Lambda) = \left[ \frac{M_{\Lambda_b(5912)} - M_{R\text{-BSE}}^{J^P=1/2^-}(|d_Q|, \Lambda)}{\sigma(\Sigma_b)} \right]^2 + \left[ \frac{M_{\Lambda_b(5920)} - M_{R\text{-BSE}}^{J^P=3/2^-}(|d_Q|, \Lambda)}{\sigma(\Sigma_b^*)} \right]^2$$

$\text{Log}[\chi^2(|d_Q|, \Lambda)]$



we determine  $|d_Q|$  for different UV cutoffs  $\Lambda$  from the pole position of the  $\Lambda_b(5912) [J^P = (1/2)^-]$  and  $\Lambda_b(5920) [J^P = (3/2)^-]$

$\Lambda_b(5912)$							$\Lambda_b(5920)$				
			$\Sigma_b \pi \quad J^P = \frac{1}{2}^-$				$\Sigma_b^* \pi \quad J^P = \frac{3}{2}^-$				
$\Lambda$ [GeV]	$\chi^2$	$ d_Q $	$M$ [MeV]	$ g_{\Sigma_b \pi} $	$P_{\Sigma_b \pi}$	$\Gamma_{\Lambda_b \pi \pi}^R$ [keV]	$M$ [MeV]	$ g_{\Sigma_b^* \pi} $	$P_{\Sigma_b^* \pi}$	$\Gamma_{\Lambda_b \pi \pi}^R$ [keV]	
0.4	0.02	$1.79 \pm 0.11$	$5912.4 \pm 2.0$	$1.67 \pm 0.06$	$0.35 \pm 0.02$	$18 \pm 5$	$5919.8 \pm 1.6$	$1.66 \pm 0.07$	$0.31 \pm 0.03$	$37 \pm 5$	
0.65	0.32	$1.06 \pm 0.06$	$5913.1 \pm 2.0$	$1.34 \pm 0.04$	$0.23 \pm 0.01$	$13 \pm 4$	$5919.1 \pm 1.7$	$1.26 \pm 0.05$	$0.18 \pm 0.01$	$19 \pm 3$	
0.9	0.16	$0.75 \pm 0.04$	$5912.9 \pm 1.7$	$1.23 \pm 0.03$	$0.19 \pm 0.01$	$10 \pm 3$	$5919.5 \pm 1.6$	$1.11 \pm 0.04$	$0.14 \pm 0.01$	$16 \pm 3$	
1.15	0.00	$0.55 \pm 0.04$	$5912.1 \pm 2.0$	$1.21 \pm 0.02$	$0.18 \pm 0.01$	$9 \pm 3$	$5920.2 \pm 1.9$	$1.04 \pm 0.03$	$0.12 \pm 0.01$	$15 \pm 3$	
$1.85 \pm 0.04$	12	0	$5905.5 \pm 1.7$	$1.27 \pm 0.02$	$0.19 \pm 0.01$	$2.5 \pm 1.2$	$5924.9 \pm 1.7$	$1.27 \pm 0.02$	$0.19 \pm 0.01$	$39 \pm 8$	

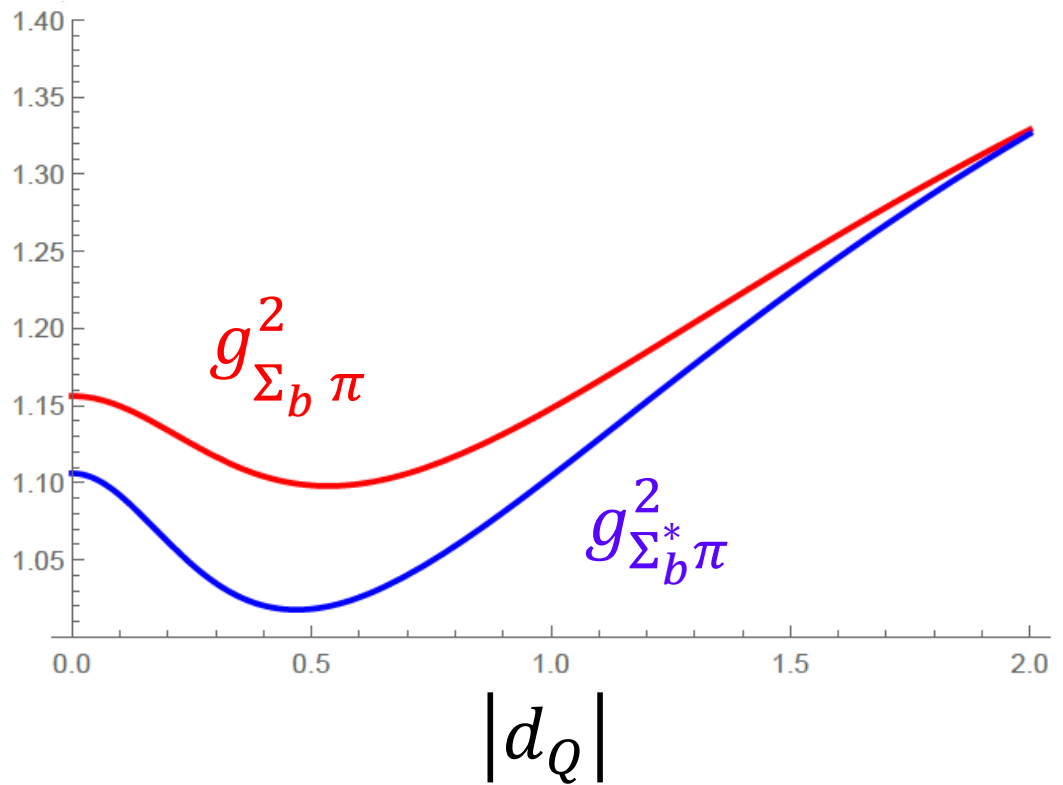
D. Gamermann, J.N., E. Oset, and E. Ruiz Arriola, PRD81 (2010) 014029

molecular probability

$$P_{\Sigma_Q^{(*)} \pi} = -g_{\Sigma_Q^{(*)} \pi}^2 \overbrace{\left. \frac{\partial \bar{G}_{\Sigma_Q^{(*)} \pi}(\sqrt{s})}{\partial \sqrt{s}} \right|_{\sqrt{s}=\sqrt{s_R}}}^{\sim -0.1}$$

~ 0.15 – 0.35  
 $\Lambda_b(5912)$  and  $\Lambda_b(5920)$  are:

- largely CQM states
- HQSS partners



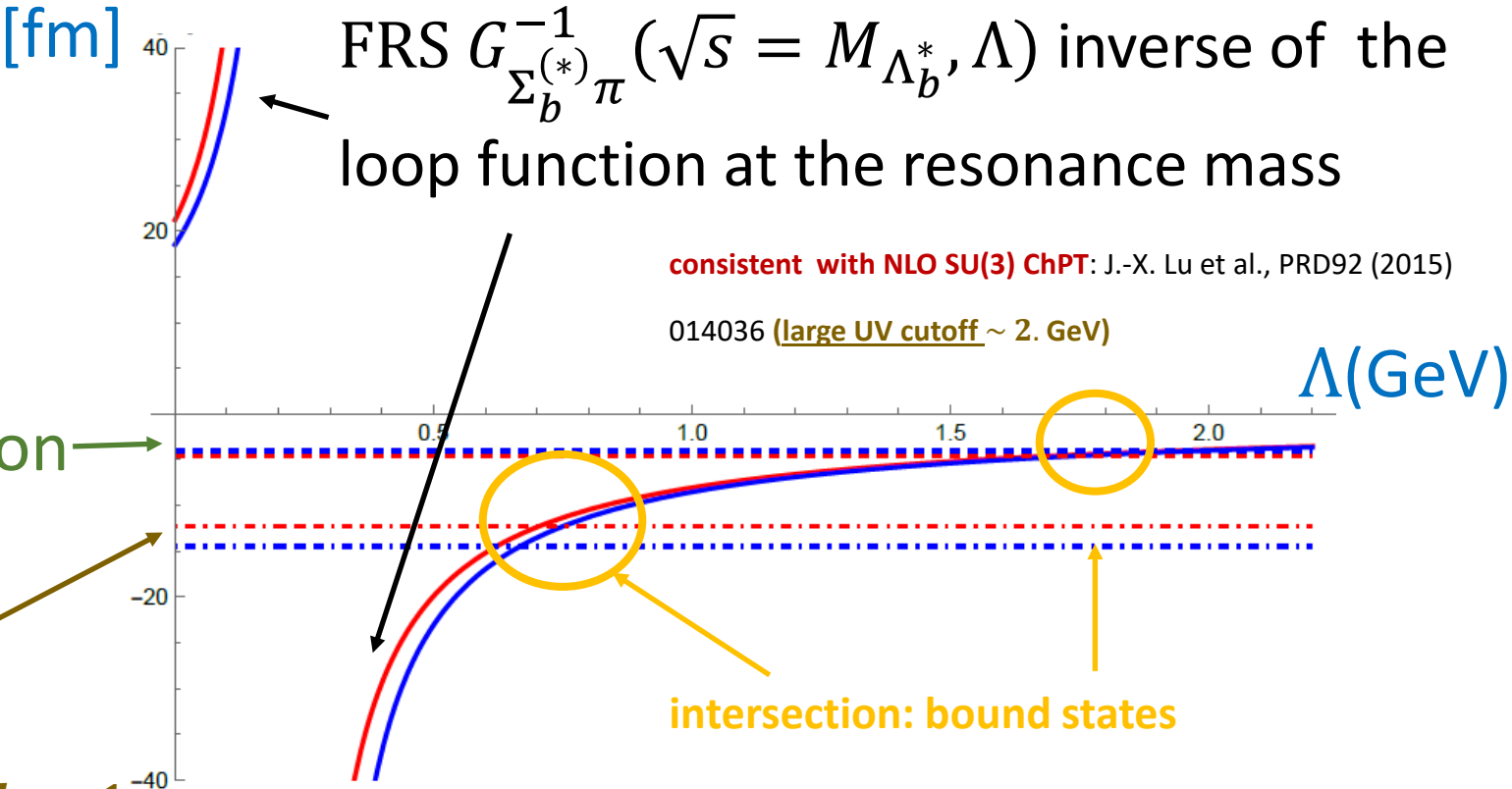
$\Lambda_b(5912)$							$\Lambda_b(5920)$				
$\Lambda$ [GeV]			$\Sigma_b \pi \ J^P = \frac{1}{2}^-$						$\Sigma_b^* \pi \ J^P = \frac{3}{2}^-$		
	$\chi^2$	$ d_Q $	$M$ [MeV]	$ g_{\Sigma_b \pi} $	$P_{\Sigma_b \pi}$	$\Gamma_{\Lambda_b \pi \pi}^R$ [keV]	$M$ [MeV]	$ g_{\Sigma_b^* \pi} $	$P_{\Sigma_b^* \pi}$	$\Gamma_{\Lambda_b \pi \pi}^R$ [keV]	
0.4	0.02	$1.79 \pm 0.11$	$5912.4 \pm 2.0$	$1.67 \pm 0.06$	$0.35 \pm 0.02$	$18 \pm 5$	$5919.8 \pm 1.6$	$1.66 \pm 0.07$	$0.31 \pm 0.03$	$37 \pm 5$	
0.65	0.32	$1.06 \pm 0.06$	$5913.1 \pm 2.0$	$1.34 \pm 0.04$	$0.23 \pm 0.01$	$13 \pm 4$	$5919.1 \pm 1.7$	$1.26 \pm 0.05$	$0.18 \pm 0.01$	$19 \pm 3$	
0.9	0.16	$0.75 \pm 0.04$	$5912.9 \pm 1.7$	$1.23 \pm 0.03$	$0.19 \pm 0.01$	$10 \pm 3$	$5919.5 \pm 1.6$	$1.11 \pm 0.04$	$0.14 \pm 0.01$	$16 \pm 3$	
1.15	0.00	$0.55 \pm 0.04$	$5912.1 \pm 2.0$	$1.21 \pm 0.02$	$0.18 \pm 0.01$	$9 \pm 3$	$5920.2 \pm 1.9$	$1.04 \pm 0.03$	$0.12 \pm 0.01$	$15 \pm 3$	
$1.85 \pm 0.04$	12	0	$5905.5 \pm 1.7$	$1.27 \pm 0.02$	$0.19 \pm 0.01$	$2.5 \pm 1.2$	$5924.9 \pm 1.7$	$1.27 \pm 0.02$	$0.19 \pm 0.01$	$39 \pm 8$	

neglecting the interaction driven by the CQM bare state

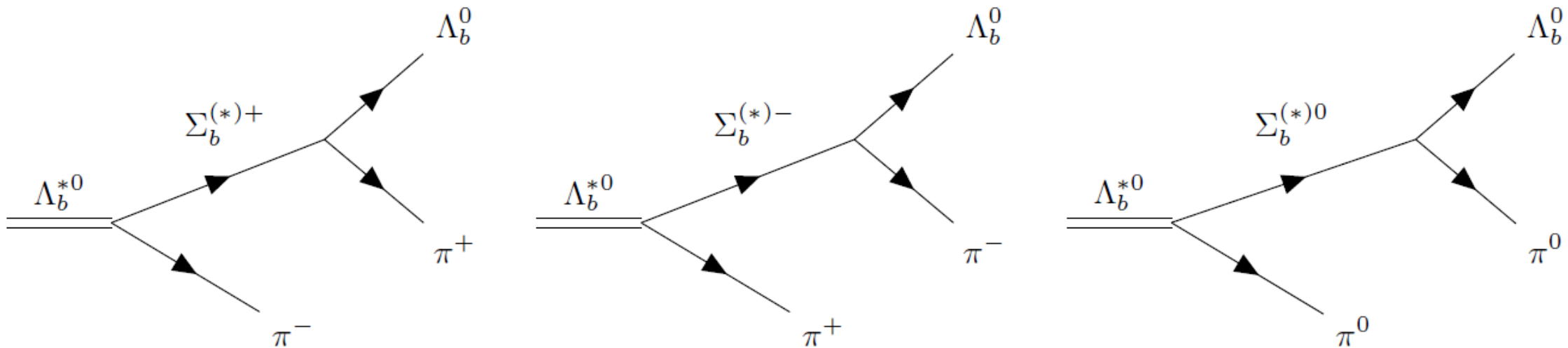
$V_\chi^J (\sqrt{s} = M_{\Lambda_b^*})$  chiral interaction

$V_\chi^J (\sqrt{s} = M_{\Lambda_b^*}) + \frac{2M_{\text{CQM}}}{M_{\Lambda_b^*}^2 - M_{\text{CQM}}^2}$

CQM exchange potential for  $d_Q = 1$

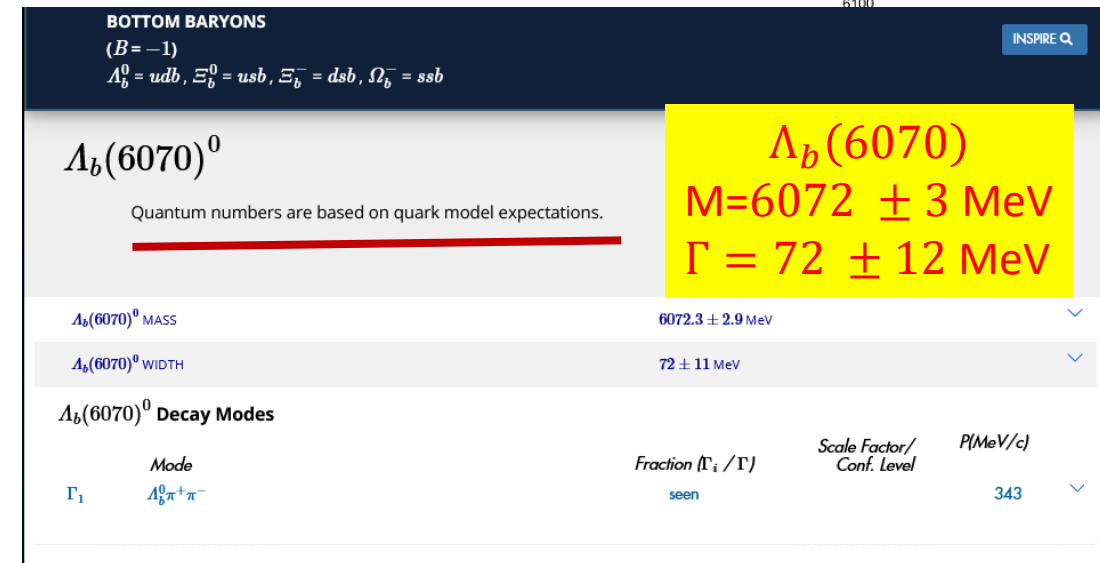
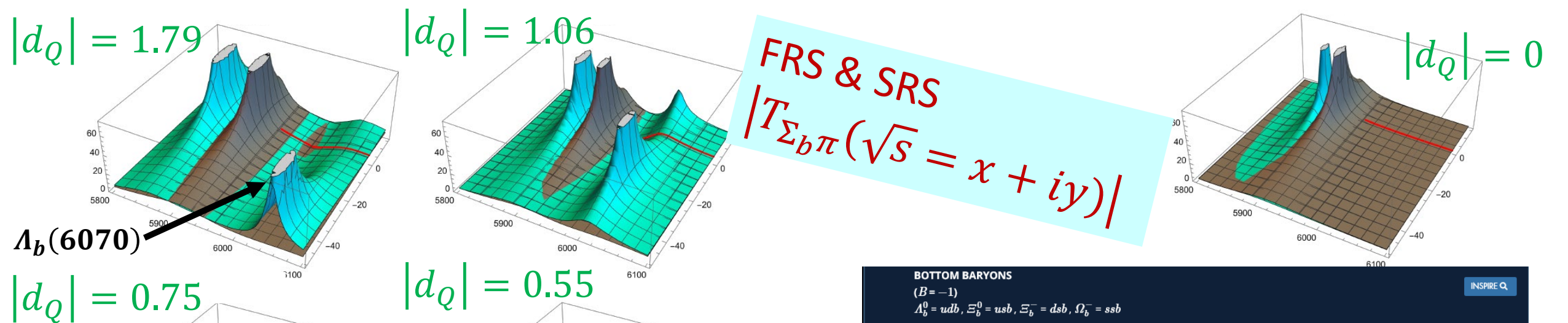


$\Lambda_b(5912)$						$\Lambda_b(5920)$				
	$\Sigma_b \pi \ J^P = \frac{1}{2}^-$					$\Sigma_b^* \pi \ J^P = \frac{3}{2}^-$				
$\Lambda$ [GeV]	$\chi^2$	$ d_Q $	$M$ [MeV]	$ g_{\Sigma_b \pi} $	$P_{\Sigma_b \pi}$	$\Gamma_{\Lambda_b \pi \pi}^R$ [keV]	$M$ [MeV]	$ g_{\Sigma_b^* \pi} $	$P_{\Sigma_b^* \pi}$	$\Gamma_{\Lambda_b \pi \pi}^R$ [keV]
0.4	0.02	$1.79 \pm 0.11$	$5912.4 \pm 2.0$	$1.67 \pm 0.06$	$0.35 \pm 0.02$	$18 \pm 5$	$5919.8 \pm 1.6$	$1.66 \pm 0.07$	$0.31 \pm 0.03$	$37 \pm 5$
0.65	0.32	$1.06 \pm 0.06$	$5913.1 \pm 2.0$	$1.34 \pm 0.04$	$0.23 \pm 0.01$	$13 \pm 4$	$5919.1 \pm 1.7$	$1.26 \pm 0.05$	$0.18 \pm 0.01$	$19 \pm 3$
0.9	0.16	$0.75 \pm 0.04$	$5912.9 \pm 1.7$	$1.23 \pm 0.03$	$0.19 \pm 0.01$	$10 \pm 3$	$5919.5 \pm 1.6$	$1.11 \pm 0.04$	$0.14 \pm 0.01$	$16 \pm 3$
1.15	0.00	$0.55 \pm 0.04$	$5912.1 \pm 2.0$	$1.21 \pm 0.02$	$0.18 \pm 0.01$	$9 \pm 3$	$5920.2 \pm 1.9$	$1.04 \pm 0.03$	$0.12 \pm 0.01$	$15 \pm 3$
$1.85 \pm 0.04$	12	0	$5905.5 \pm 1.7$	$1.27 \pm 0.02$	$0.19 \pm 0.01$	$2.5 \pm 1.2$	$5924.9 \pm 1.7$	$1.27 \pm 0.02$	$0.19 \pm 0.01$	$39 \pm 8$



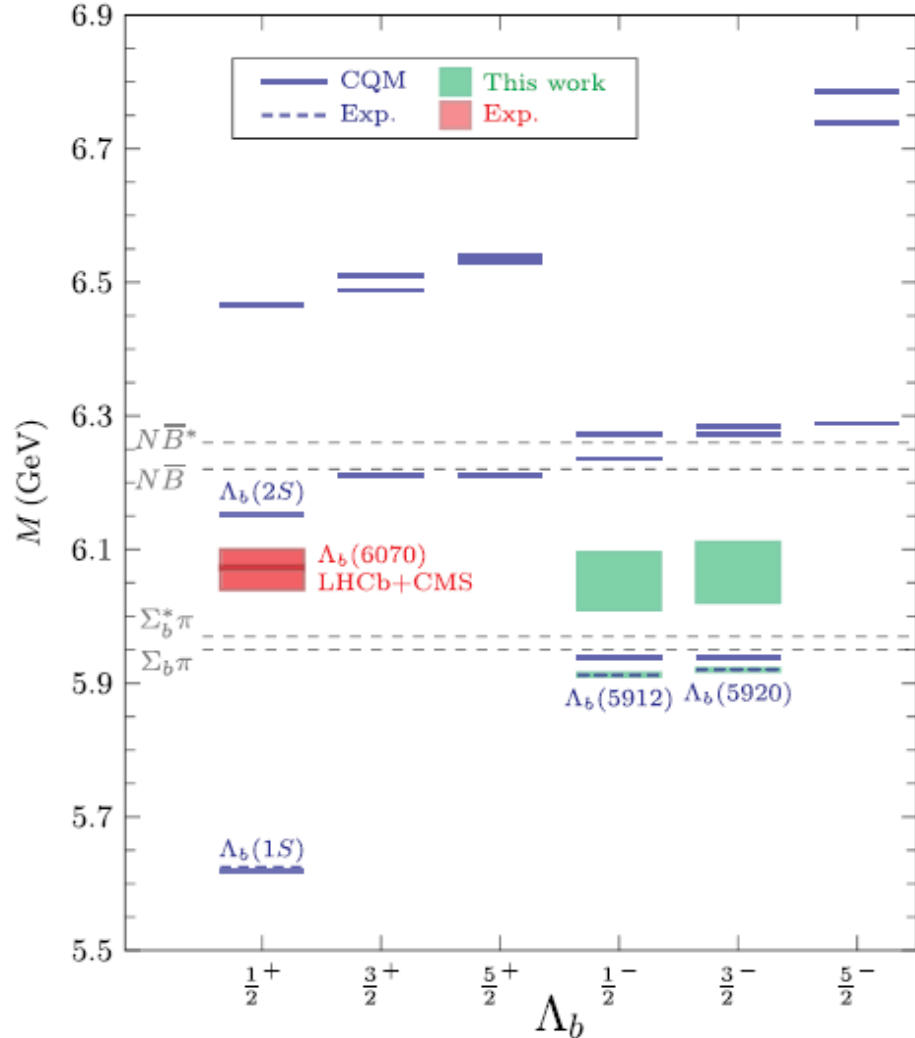
small 3-body decay widths (tens of keV)





poles in the SRS

$\Sigma_b \pi [J^P = 1/2^-]$						$\Sigma_b^* \pi [J^P = 3/2^-]$			
$\Lambda$ [GeV]	$ d_Q $	$M$ [MeV]	$\Gamma$ [MeV]	$ g_{\Sigma_b \pi} $	$\phi_{\Sigma_b \pi}$	$M$ [MeV]	$\Gamma$ [MeV]	$ g_{\Sigma_b^* \pi} $	$\phi_{\Sigma_b^* \pi}$
0.4	$1.79 \pm 0.11$	$6053 \pm 6$	$85.2 \pm 0.4$	$1.60 \pm 0.03$	$-0.70 \pm 0.01$	$6066 \pm 6$	$90.0 \pm 0.5$	$1.65 \pm 0.03$	$-0.67 \pm 0.01$
0.65	$1.06 \pm 0.06$	$6008 \pm 3$	$49.6 \pm 0.5$	$1.46 \pm 0.02$	$-0.53 \pm 0.01$	$6021 \pm 3$	$52.9 \pm 0.4$	$1.54 \pm 0.02$	$-0.50 \pm 0.01$
0.9	$0.75 \pm 0.04$	$5983 \pm 3$	$24.5 \pm 0.7$	$1.23 \pm 0.01$	$-0.41 \pm 0.01$	$5995 \pm 2$	$25.9 \pm 0.8$	$1.35 \pm 0.01$	$-0.38 \pm 0.01$
1.15	$0.55 \pm 0.04$	$5966 \pm 3$	$9.5 \pm 1.1$	$0.97 \pm 0.01$	$-0.30 \pm 0.01$	$5976 \pm 3$	$7 \pm 2$	$1.15^{+0.06}_{-0.02}$	$-0.30^{+0.01}_{-0.05}$



- LHCb reported a broad excess of events in the  $\Lambda_b \pi^+ \pi^-$  spectrum in region of 6040 - 6100 MeV.
- The spin and parity quantum-numbers of the  $\Lambda_b(6070)$  were not established by LHCb.
- In the RPP, it is assumed to be the radial excitation  $\Lambda_b(2S)$ , which would have  $J^P = (1/2)^+$
- We naturally find for UV cutoffs around 500 MeV two resonances ( $J^P = (1/2)^-$  and  $J^P = (3/2)^-$ ) which should be observed in the  $\Lambda_b \pi^+ \pi^-$  in the region of 6050 MeV

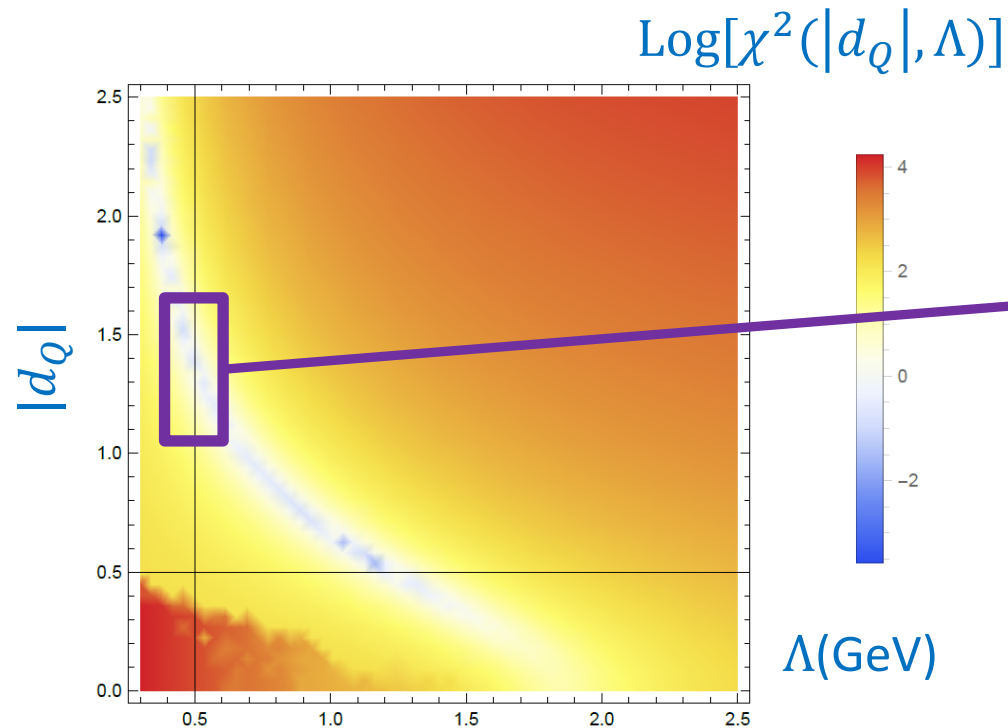
the vertical range shows masses  $\pm$  widths of our predicted resonances. The horizontal range does not have any meaning since the resonances have  $(1/2)^-$  and  $(3/2)^-$  spin-parities

CQM( $\lambda, \rho$ ): T. Yoshida, E. Hiyama, A. Hosaka, M. Oka, and K. Sadato, PRD92 (2015) 114029

$\Lambda$ [GeV]	$ d_Q $	$\Sigma_b \pi [J^P = 1/2^-]$				$\Sigma_b^* \pi [J^P = 3/2^-]$			
		$M$ [MeV]	$\Gamma$ [MeV]	$ g_{\Sigma_b \pi} $	$\phi_{\Sigma_b \pi}$	$M$ [MeV]	$\Gamma$ [MeV]	$ g_{\Sigma_b^* \pi} $	$\phi_{\Sigma_b^* \pi}$
0.4	$1.79 \pm 0.11$	$6053 \pm 6$	$85.2 \pm 0.4$	$1.60 \pm 0.03$	$-0.70 \pm 0.01$	$6066 \pm 6$	$90.0 \pm 0.5$	$1.65 \pm 0.03$	$-0.67 \pm 0.01$
0.65	$1.06 \pm 0.06$	$6008 \pm 3$	$49.6 \pm 0.5$	$1.46 \pm 0.02$	$-0.53 \pm 0.01$	$6021 \pm 3$	$52.9 \pm 0.4$	$1.54 \pm 0.02$	$-0.50 \pm 0.01$
0.9	$0.75 \pm 0.04$	$5983 \pm 3$	$24.5 \pm 0.7$	$1.23 \pm 0.01$	$-0.41 \pm 0.01$	$5995 \pm 2$	$25.3 \pm 0.3$	$1.33 \pm 0.01$	$-0.33 \pm 0.01$
1.15	$0.55 \pm 0.04$	$5966 \pm 3$	$9.5 \pm 1.1$	$0.97 \pm 0.01$	$-0.30 \pm 0.01$	$5976 \pm 3$	$7 \pm 2$	$1.15^{+0.06}_{-0.02}$	$-0.30^{+0.01}_{-0.05}$

- LHCb reported a broad excess of events in the  $\Lambda_b \pi^+ \pi^-$  spectrum in region of 6040 - 6100 MeV.
- The spin and parity quantum-numbers of the  $\Lambda_b(6070)$  were not established by LHCb.
- In the RPP, it is assumed to be the radial excitation  $\Lambda_b(2S)$ , which would have  $J^P = (1/2)^+$
- We naturally find for UV cutoffs around 500 MeV two resonances ( $J^P = (1/2)^-$  and  $J^P = (3/2)^-$ ) which should be observed in the  $\Lambda_b \pi^+ \pi^-$  in the region of 6050 MeV

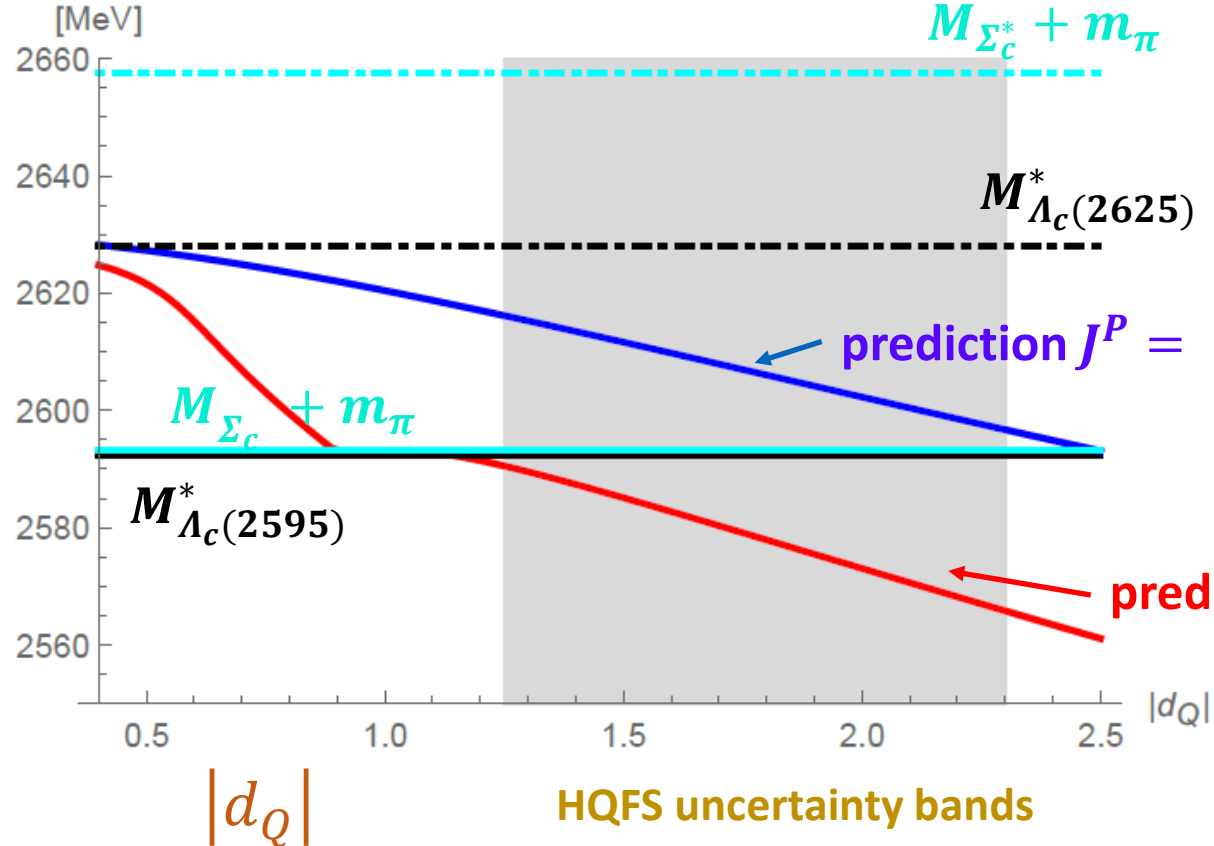
- Hence, we can fix the UV cutoffs and the strength  $d_Q$  of the coupling of the  $\Sigma_c^{(*)} \pi$  pair to the CQM lowest-lying  $\lambda$  -mode excitation, which are now fully determined by the pole position of the  $\Lambda_b(5912)$  and  $\Lambda_b(5920)$  resonances
- Now using Heavy Quark Flavor Symmetry we can make predictions in the charm sector



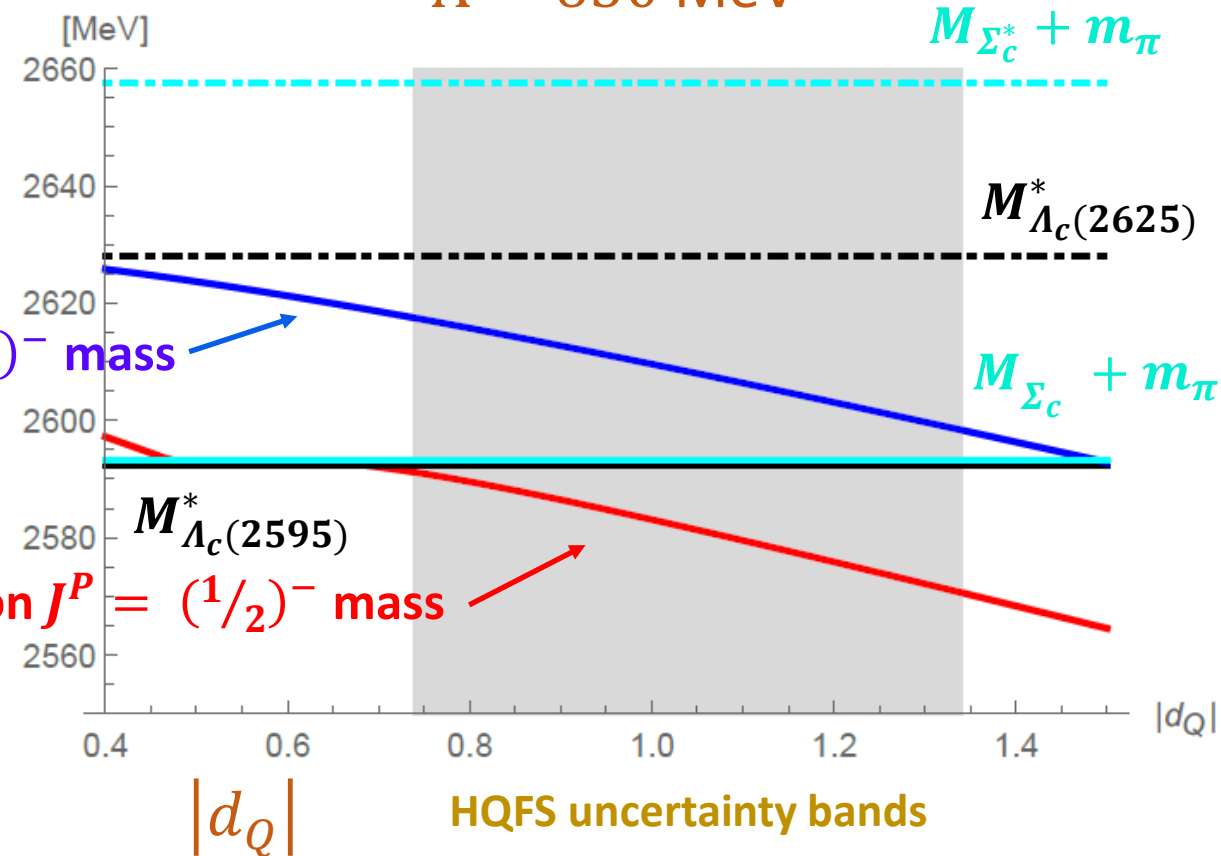
**favored natural size UV cutoffs**  
 $\Lambda \sim 650 - 400 \text{ MeV}$   
 and  $|d_Q(\Lambda)| \sim 1-1.8$

# charm sector

$\Lambda = 400 \text{ MeV}$

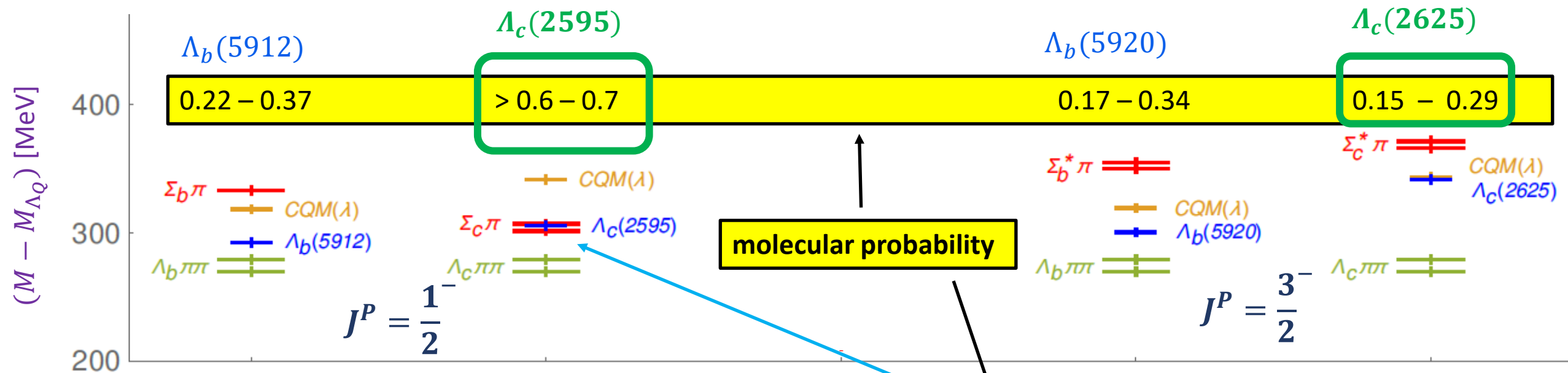


$\Lambda = 650 \text{ MeV}$



For each UV cutoff, the **grey band** shows the range of values for  $|d_Q|$  obtained in the bottom sector, enhanced by HQFS breaking corrections

Reasonable simultaneous description of the  $\Lambda_c(2595)$  and  $\Lambda_c(2625)$  resonances considering chiral  $\Sigma_c^{(*)}\pi$  pairs and their coupling to lowest-lying  $\lambda$ -mode CQM states fixed in the bottom sector from  $\Lambda_b(5912)$ ,  $\Lambda_b(5920)$  and  $\Lambda_b(6070)$



- ✓ The  $\Lambda_c(2595)$  and the  $\Lambda_c(2625)$  might not be HQSS partners ( $\Lambda_c^*$  – puzzle)
- ✓ The  $J^P = 3/2^-$  resonance should be viewed mostly as a quark-model state naturally predicted to lie very close to its nominal mass
- ✓ The  $\Lambda_c(2595)$  is predicted to have a predominant chiral  $\Sigma_c \pi$  molecular structure, which threshold is located much more closer than the mass of the bare three-quark state

$$\left. \frac{\partial \bar{G}_{\Sigma_c \pi}}{\partial \sqrt{s}} \right|_{\sqrt{s}=M_{\Lambda_c(2595)}} \sim -(0.7^{+2.4}_{-0.2})$$

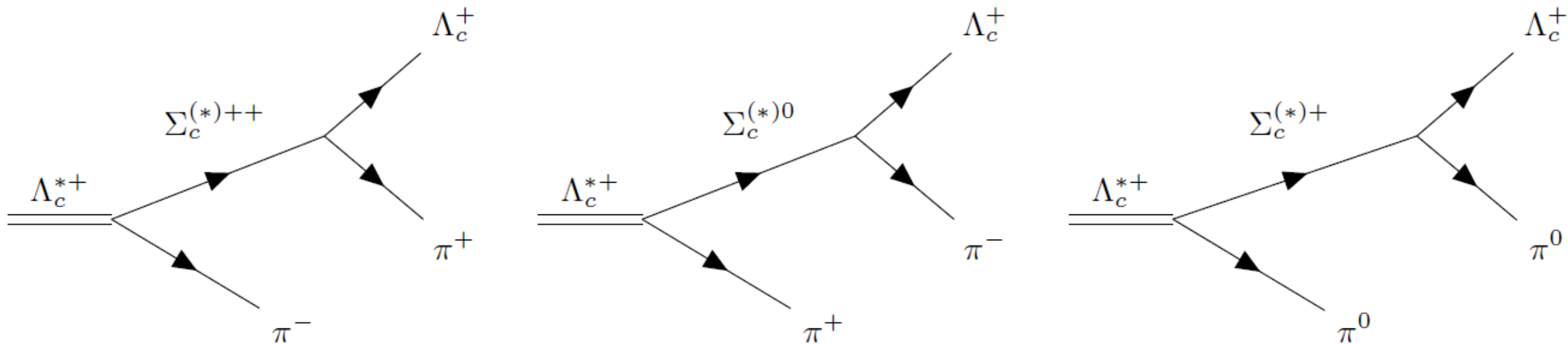
diverges at threshold!

$$P_{\Sigma_Q^{(*)}\pi} = -g_{\Sigma_Q^{(*)}\pi}^2 \frac{\partial \bar{G}_{\Sigma_Q^{(*)}\pi}(\sqrt{s})}{\partial \sqrt{s}} \bigg|_{\sqrt{s}=\sqrt{s_R}}$$

$$g_{\Lambda_c(2595)\Sigma_c \pi}^2 = 1.37 \pm 0.35$$



# Three body $\Lambda_c \pi \pi$ decay width and the $g_{\Lambda_c^* \Sigma_c^{(*)} \pi}$ coupling



$$\Gamma^{R\dagger}[\Lambda_c(2595) \rightarrow \Lambda_c \pi \pi] = (1.9 \pm 0.2) \times g_{\Lambda_c(2595) \Sigma_c \pi}^2 \text{ [MeV]},$$

$$\Gamma^{R\dagger}[\Lambda_c(2625) \rightarrow \Lambda_c \pi \pi] = (0.27 \pm 0.01) \times g_{\Lambda_c(2625) \Sigma_c^* \pi}^2 \text{ [MeV]}$$

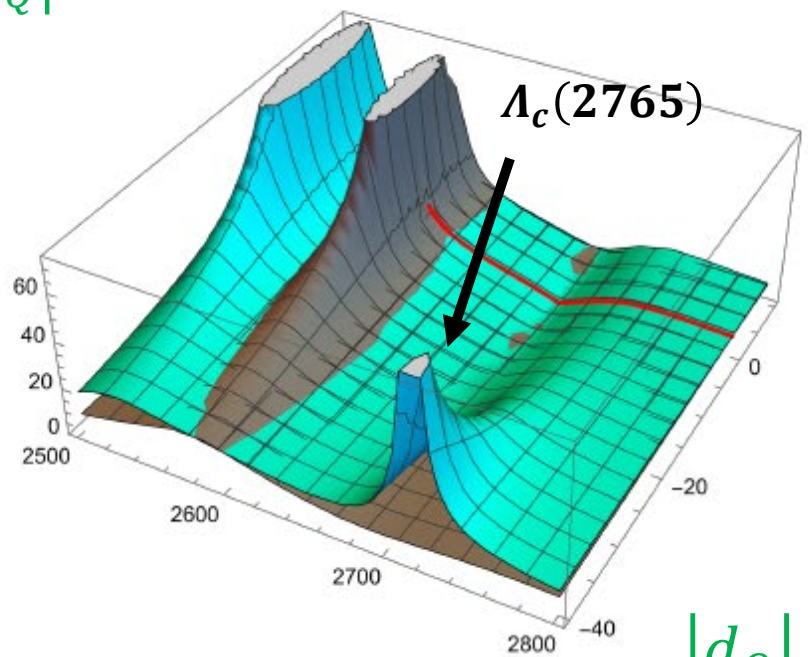
$$\Gamma[\Lambda_c(2595)] = 2.6 \pm 0.6 \text{ MeV}$$



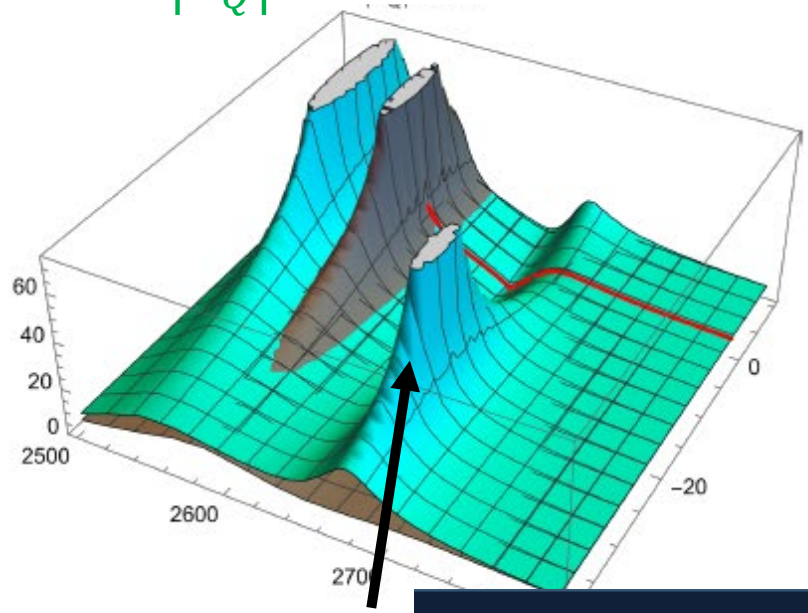
$$g_{\Lambda_c(2595) \Sigma_c \pi}^2 = 1.37 \pm 0.35$$

In the charm sector, these resonant contributions to the  $\Lambda_c \pi \pi$  three-body decay channel are much larger than in the bottom sector because **the intermediate  $\Sigma_c$  and  $\Sigma_c^*$  states are closer to be on the mass shell**, especially for the  $\Lambda_c(2595)$

$|d_Q| = 1.79 \text{ \& } \Lambda = 0.4 \text{ GeV}$



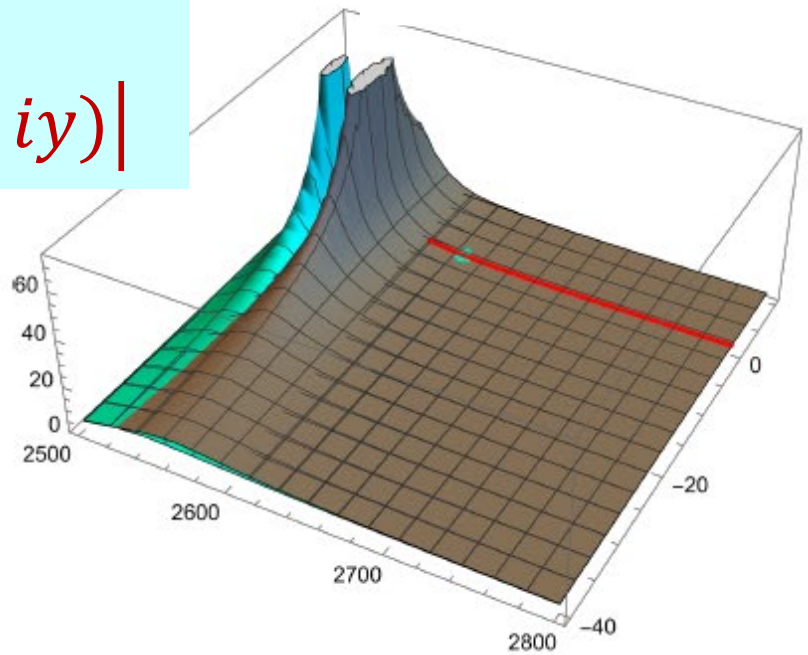
$|d_Q| = 1.06 \text{ \& } \Lambda = 0.65 \text{ GeV}$



$I(J^P) = ?(??)$

$\Lambda_c(2765)$  or  $\Sigma_c(2765)$   
or  
 $M=2766 \pm 3 \text{ MeV}$   
 $\Gamma \simeq 50 \text{ MeV}$

$|d_Q| = 0$   $\Lambda_c(2765)$



FRS & SRS

$|T_{\Sigma_c \pi}(\sqrt{s} = x + iy)|$

if  $d_Q = 0$ , the second resonance is not generated

**CHARMED BARYONS**  
( $C = +1$ )  
 $\Lambda_c^+ = udc$ ,  $\Sigma_c^{++} = uuc$ ,  $\Sigma_c^+ = udc$ ,  $\Sigma_c^0 = ddc$ ,  
 $\Xi_c^+ = usc$ ,  $\Xi_c^0 = dsc$ ,  $\Omega_c^0 = ssc$

**$\Lambda_c(2765)^+$  or  $\Sigma_c(2765)$**   $I(J^P) = ?(??)$

A broad, statistically significant peak ( $997^{+141}_{-129}$  events) seen in  $\Lambda_c^+ \pi^+ \pi^-$ . However, nothing at all is known about its quantum numbers, including whether it is a  $\Lambda_c^+$  or a  $\Sigma_c$ , or whether the width might be due to overlapping states.

$\Lambda_c(2765)^+$ MASS	$2766.6 \pm 2.4 \text{ MeV}$
$\Lambda_c(2765)^+ - \Lambda_c^+$ MASS DIFFERENCE	$480.1 \pm 2.4 \text{ MeV}$
$\Lambda_c(2765)^+$ WIDTH	$50 \text{ MeV}$

**$\Lambda_c(2765)^+$  or  $\Sigma_c(2765)$  Decay Modes**

Mode	Fraction ( $\Gamma_i / \Gamma$ )	Scale Factor/ Conf. Level	$P(\text{MeV}/c)$
$\Gamma_1$ $\Lambda_c^+ \pi^+ \pi^-$	seen		356

# poles in the SRS

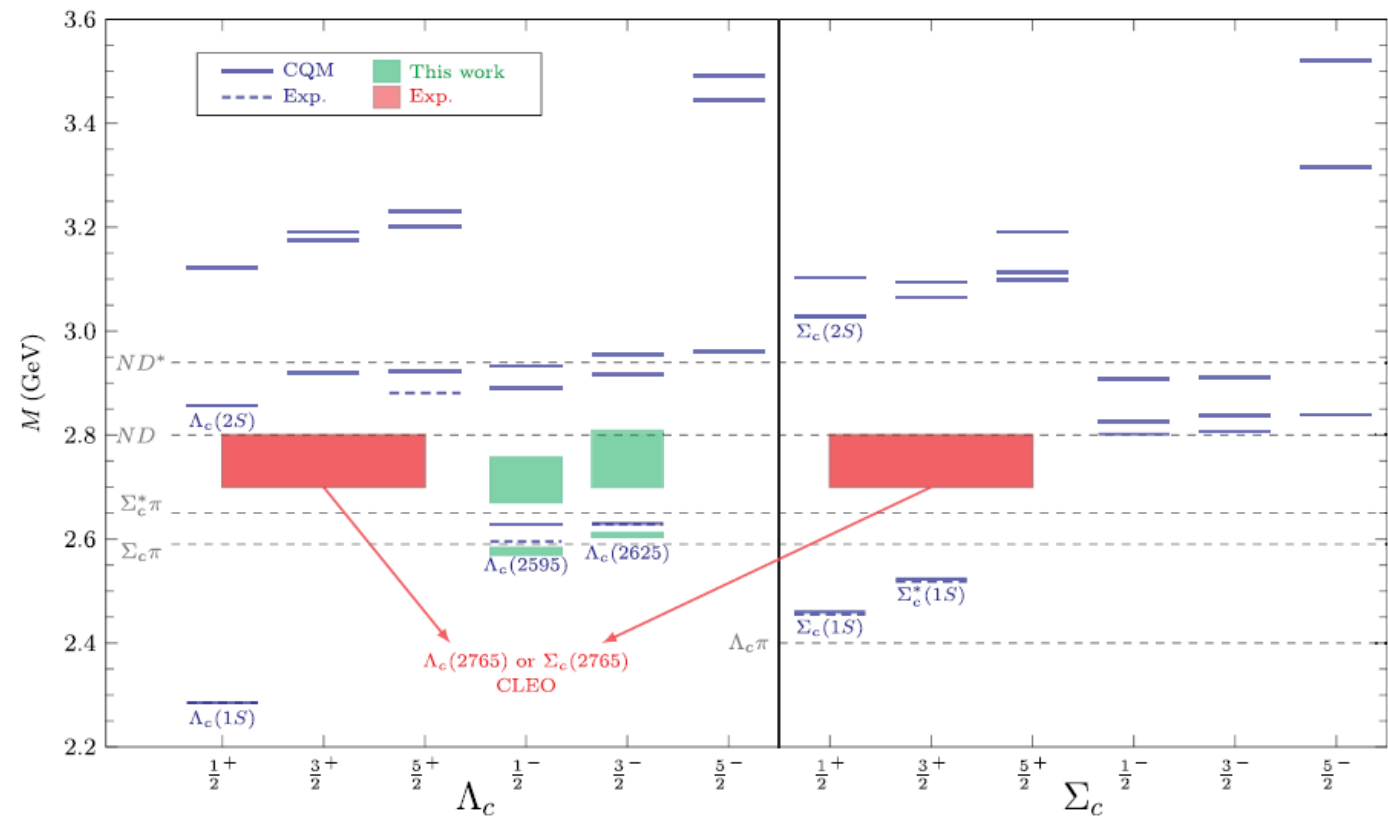
$\Lambda$ [GeV]	$ d_Q $	$\Sigma_c \pi [J^P = 1/2^-]$					$\Sigma_c^* \pi [J^P = 3/2^-]$			
		$M$ [MeV]	$\Gamma$ [MeV]	$ g_{\Sigma_c \pi} $	$\phi_{\Sigma_c \pi}$		$M$ [MeV]	$\Gamma$ [MeV]	$ g_{\Sigma_c^* \pi} $	$\phi_{\Sigma_c^* \pi}$
0.4	$1.79 \pm 0.11$	$2714 \pm 6$	$85.7 \pm 0.6$	$1.60 \pm 0.02$	$-0.92 \pm 0.01$		$2754 \pm 6$	$107.7 \pm 0.3$	$1.80 \pm 0.03$	$-0.77 \pm 0.01$
0.65	$1.06 \pm 0.06$	$2674 \pm 4$	$45.2 \pm 1.1$	$1.33 \pm 0.01$	$-0.75 \pm 0.01$		$2711 \pm 3$	$62.5 \pm 0.5$	$1.66 \pm 0.02$	$-0.57 \pm 0.01$

- The CLEO collaboration investigated the spectrum of charmed baryons which decay into  $\Lambda_c \pi^+ \pi^-$  spectrum and found a evidence of a broad state ( $\Gamma \approx 50$  MeV) which would have an invariant mass roughly 480 MeV above that of the  $\Lambda_c$  ground state baryon
- This is collected in the RPP as the  $\Lambda_c(2765)$  or  $\Sigma_c(2765)$  and it is explicitly stated that **nothing at all is known about its quantum numbers**, including whether it is a  $\Lambda_c$ , or a  $\Sigma_c$ , or whether **the width might be due to overlapping states**
- For UV cutoffs in the range 400-650 MeV, we obtain broad resonances around 2675-2755 MeV in both the  $J^P = (1/2)^-$  and  $J^P = (3/2)^-$  sectors, which will provide a natural explanation for the excess of events in the  $\Lambda_c \pi^+ \pi^-$  spectrum reported by CLEO.
- **These resonances will be heavy quark flavor siblings of those related to the  $\Lambda_b(6070)$  in the bottom sector.**



# poles in the SRS

$\Sigma_c \pi \ [J^P = 1/2^-]$						$\Sigma_c^* \pi \ [J^P = 3/2^-]$			
$\Lambda \ [\text{GeV}]$	$ d_Q $	$M \ [\text{MeV}]$	$\Gamma \ [\text{MeV}]$	$ g_{\Sigma_c \pi} $	$\phi_{\Sigma_c \pi}$	$M \ [\text{MeV}]$	$\Gamma \ [\text{MeV}]$	$ g_{\Sigma_c^* \pi} $	$\phi_{\Sigma_c^* \pi}$
0.4	$1.79 \pm 0.11$	$2714 \pm 6$	$85.7 \pm 0.6$	$1.60 \pm 0.02$	$-0.92 \pm 0.01$	$2754 \pm 6$	$107.7 \pm 0.3$	$1.80 \pm 0.03$	$-0.77 \pm 0.01$
0.65	$1.06 \pm 0.06$	$2674 \pm 4$	$45.2 \pm 1.1$	$1.33 \pm 0.01$	$-0.75 \pm 0.01$	$2711 \pm 3$	$62.5 \pm 0.5$	$1.66 \pm 0.02$	$-0.57 \pm 0.01$

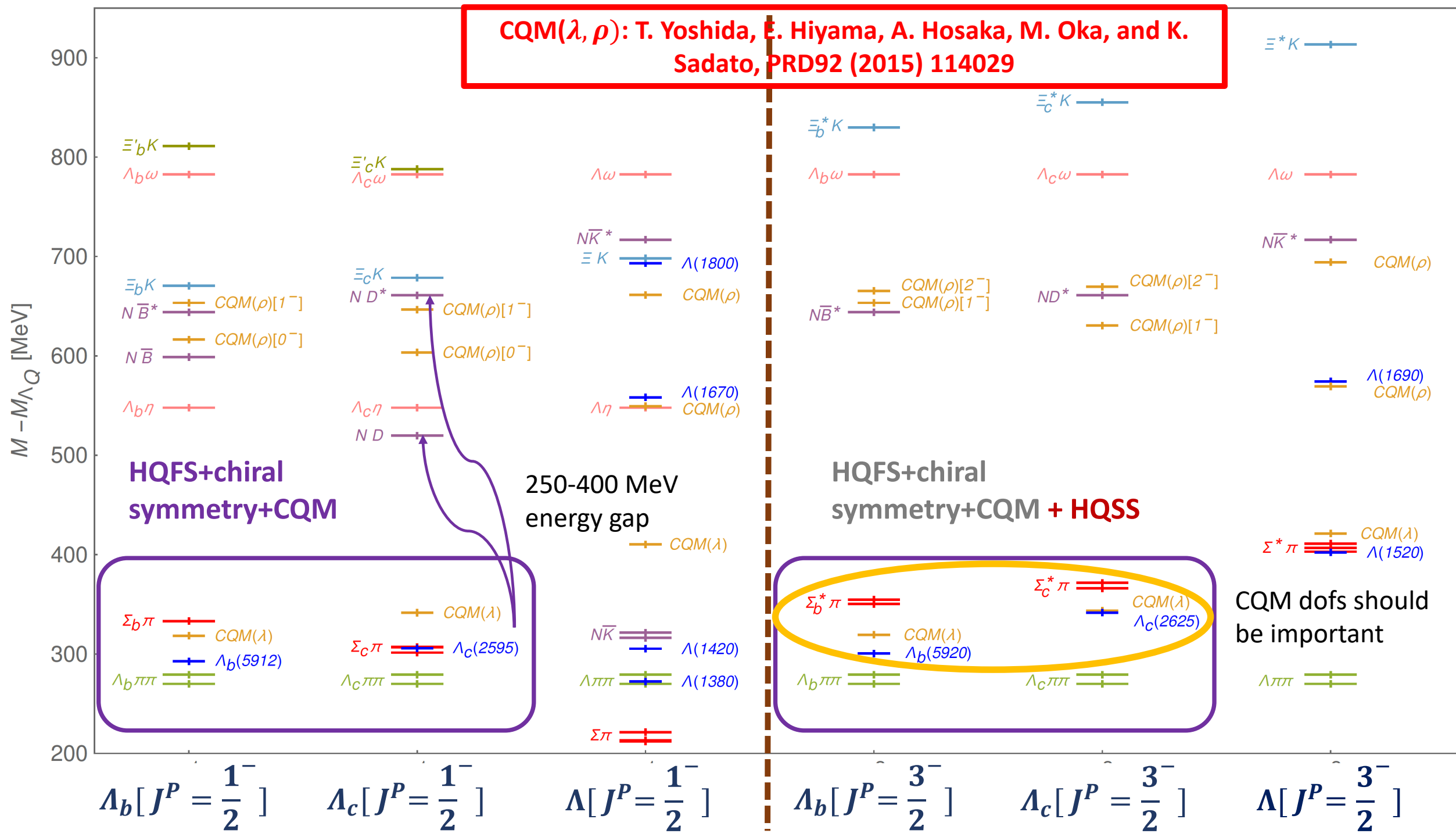


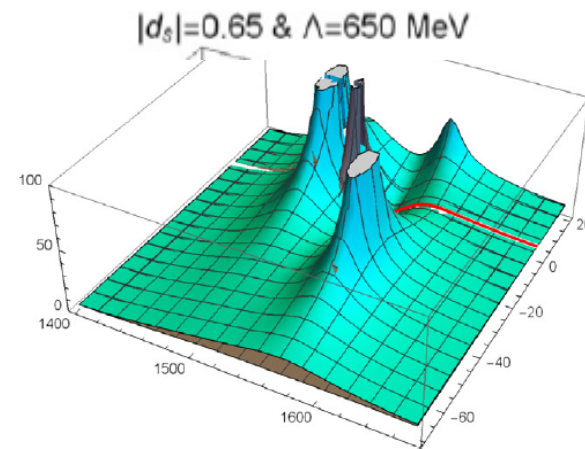
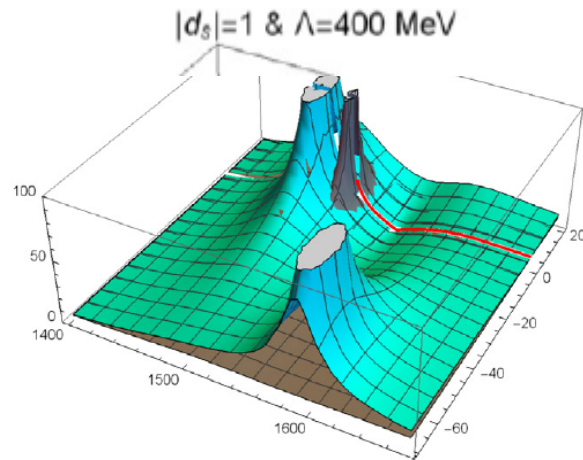
the vertical range shows masses  $\pm$  widths of our predicted resonances. The horizontal range does not have any meaning since the resonances have  $(1/2)^-$  and  $(3/2)^-$  spin-parities

CQM( $\lambda, \rho$ ): T. Yoshida, E. Hiyama, A. Hosaka, M. Oka, and K. Sadato, PRD92 (2015) 114029

$\Lambda_c(2765)$  or  $\Sigma_c(2765)$   
or  
 $M=2766 \pm 3 \text{ MeV}$   
 $\Gamma \simeq 50 \text{ MeV}$   
CLEO

**CQM( $\lambda, \rho$ ): T. Yoshida, E. Hiyama, A. Hosaka, M. Oka, and K. Sadato, PRD92 (2015) 114029**



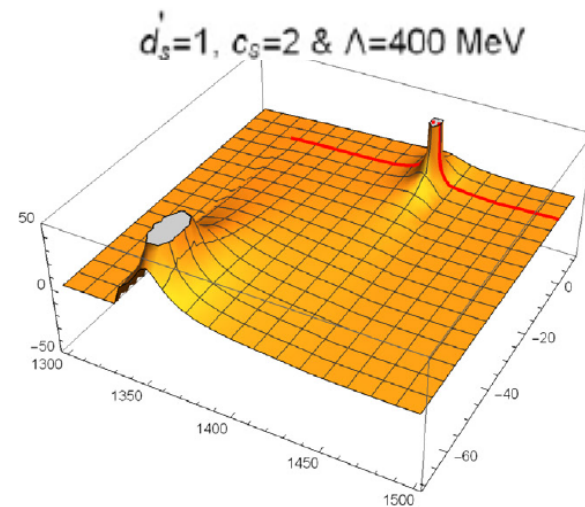
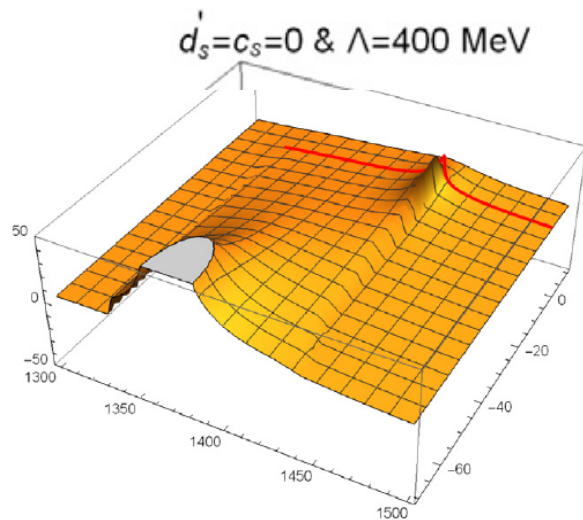


## strange sector

$$J^P = 3/2^- \quad \Lambda(1520) + 1R$$

$$\pi\Sigma^* \rightarrow \pi\Sigma^*$$

**Fig. 3.8.** Absolute value of the  $T_{\Sigma^*\pi}$ -matrix (fermi units), both in the FRS (gray) and SRS (greenish hues) and for  $(|d_Q| = 1.0, \Lambda = 400 \text{ MeV})$  (left) and  $(|d_Q| = 0.65, \Lambda = 650 \text{ MeV})$  (right), as a function of complex  $\sqrt{s} = x + iy$  in MeV. The FRS pole is placed at 1518 MeV in both cases, while the above threshold SRS ones are located at  $(M, \Gamma) = (1590, 115) \text{ MeV}$  and  $(M, \Gamma) = (1571, 60) \text{ MeV}$ , resp.



$$J^P = 1/2^-$$

$$\text{double pole } \Lambda(1405)$$

$$\bar{K}N \rightarrow \pi\Sigma$$

**Fig. 3.9.** Absolute value of the  $[J^P = 1/2^-] T_{N\bar{K} \rightarrow \Sigma\pi}$  matrix element (in fermi units) for both the FRS [ $\text{Im}\sqrt{s} > 0$ ] and the SRS [ $\text{Im}\sqrt{s} < 0$ ] as a function of the complex  $\sqrt{s} = x + iy$  in MeV. The UV cutoff is  $\Lambda = 400 \text{ MeV}$ , and CQM degrees of freedom are disconnected in the left plot, while they are coupled to the baryon-meson pairs in the right panel using  $d'_s = 1$  and  $c_s = 2$ . We also display the scattering line (red solid curve) in both cases. As noted in Table 3.5, in the left panel, the higher  $\Lambda(1405)$  pole is related to a virtual state which produces peaks in the FRS and SRS. In the right panel, the higher  $\Lambda(1405)$  shows up as a narrow resonance (pole in the SRS) close, but below, the  $N\bar{K}$  threshold.

# Backup Slides