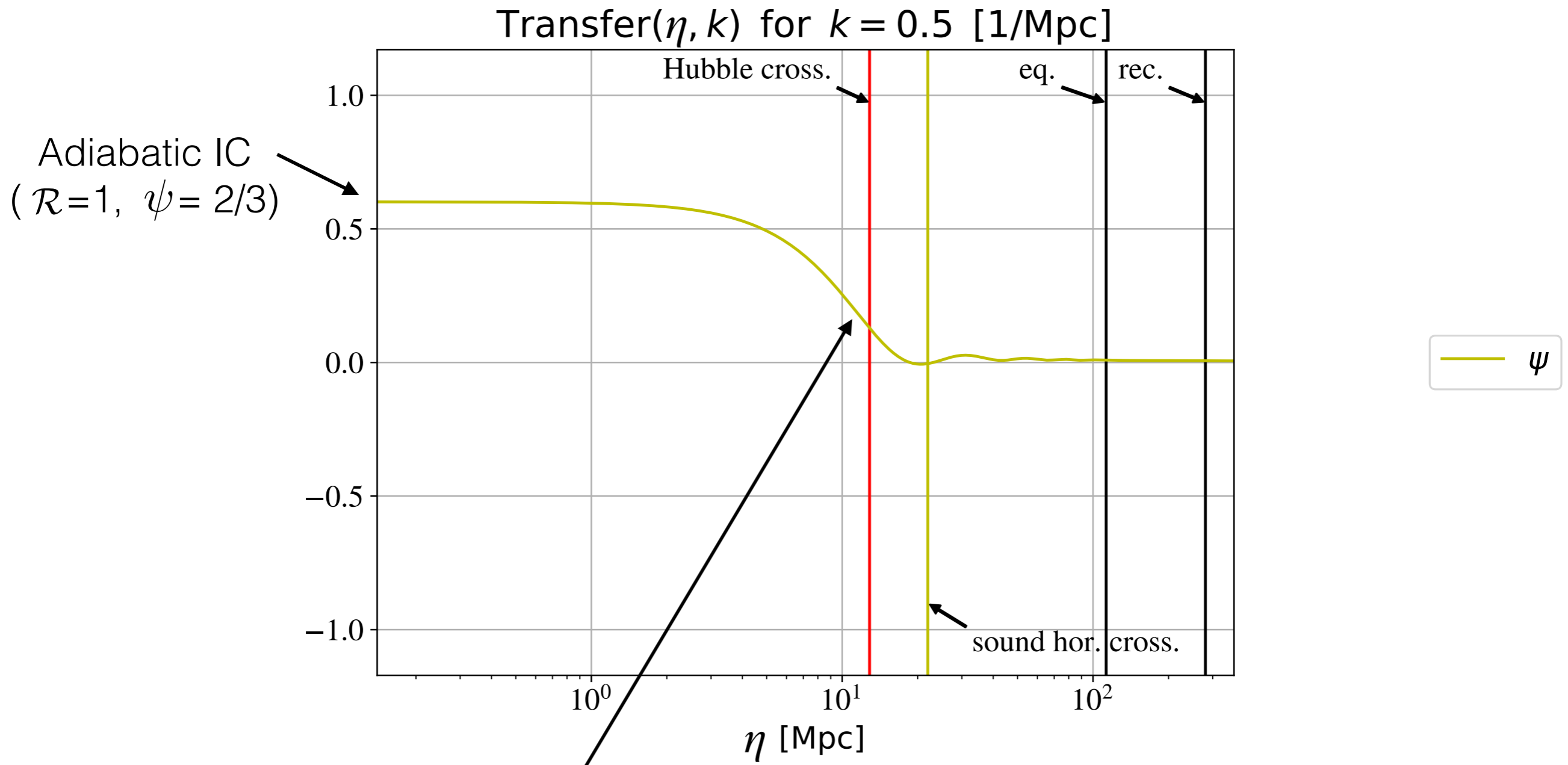


Evolution for one mode with given k

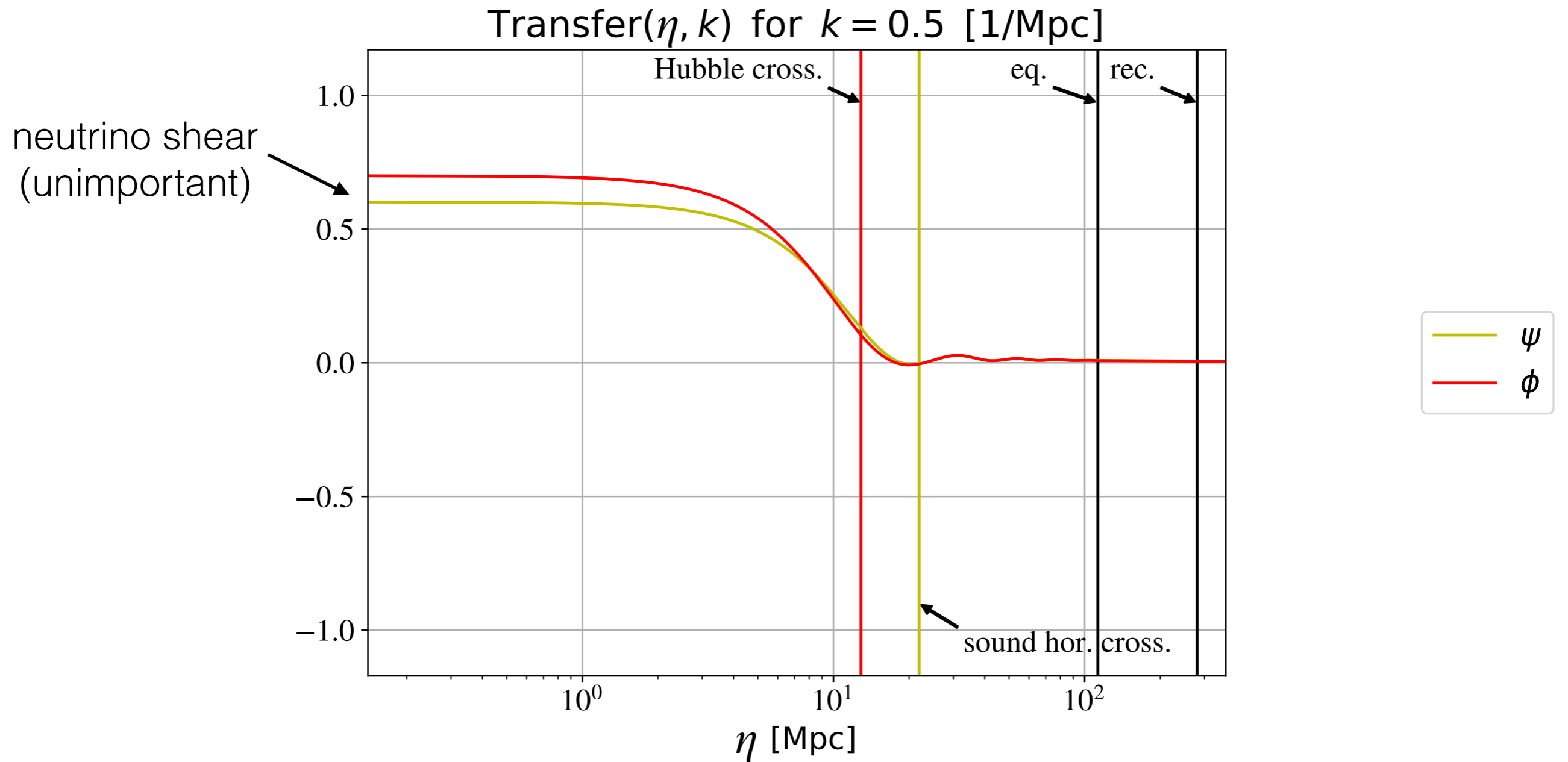


Metric damped near Hubble crossing during RD

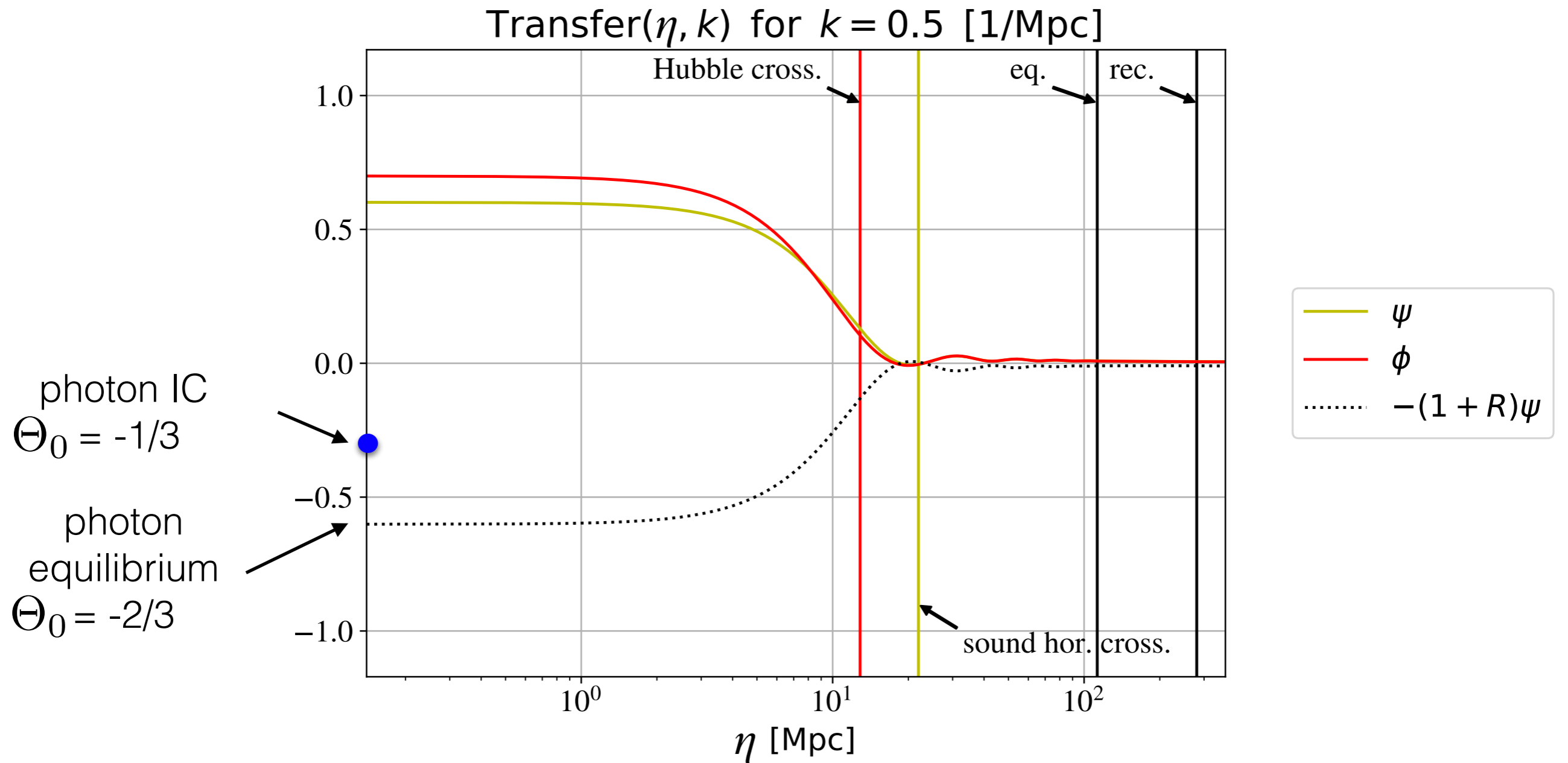
—> photon pressure, Poisson: $-k^2 \phi = 4\pi G a^2 \delta \rho_r \propto a^2 \rho_r \delta_r \sim a^{2-4+0} \sim a^{-2}$

—> very different from MD: $-k^2 \phi = 4\pi G a^2 \delta \rho_m \propto a^2 \rho_m \delta_m \sim a^{2-3+1} \sim \text{constant}$

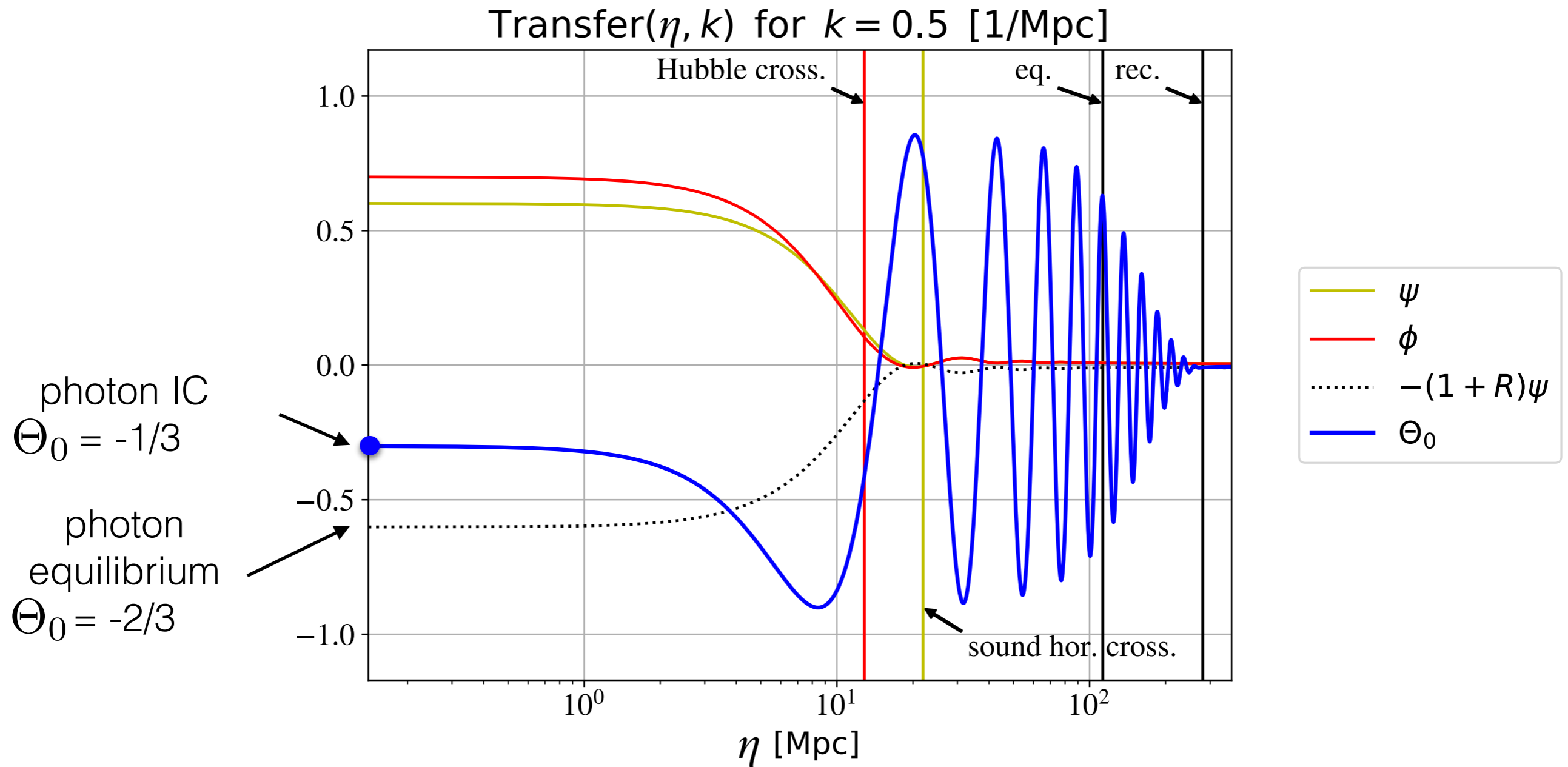
Evolution for one mode



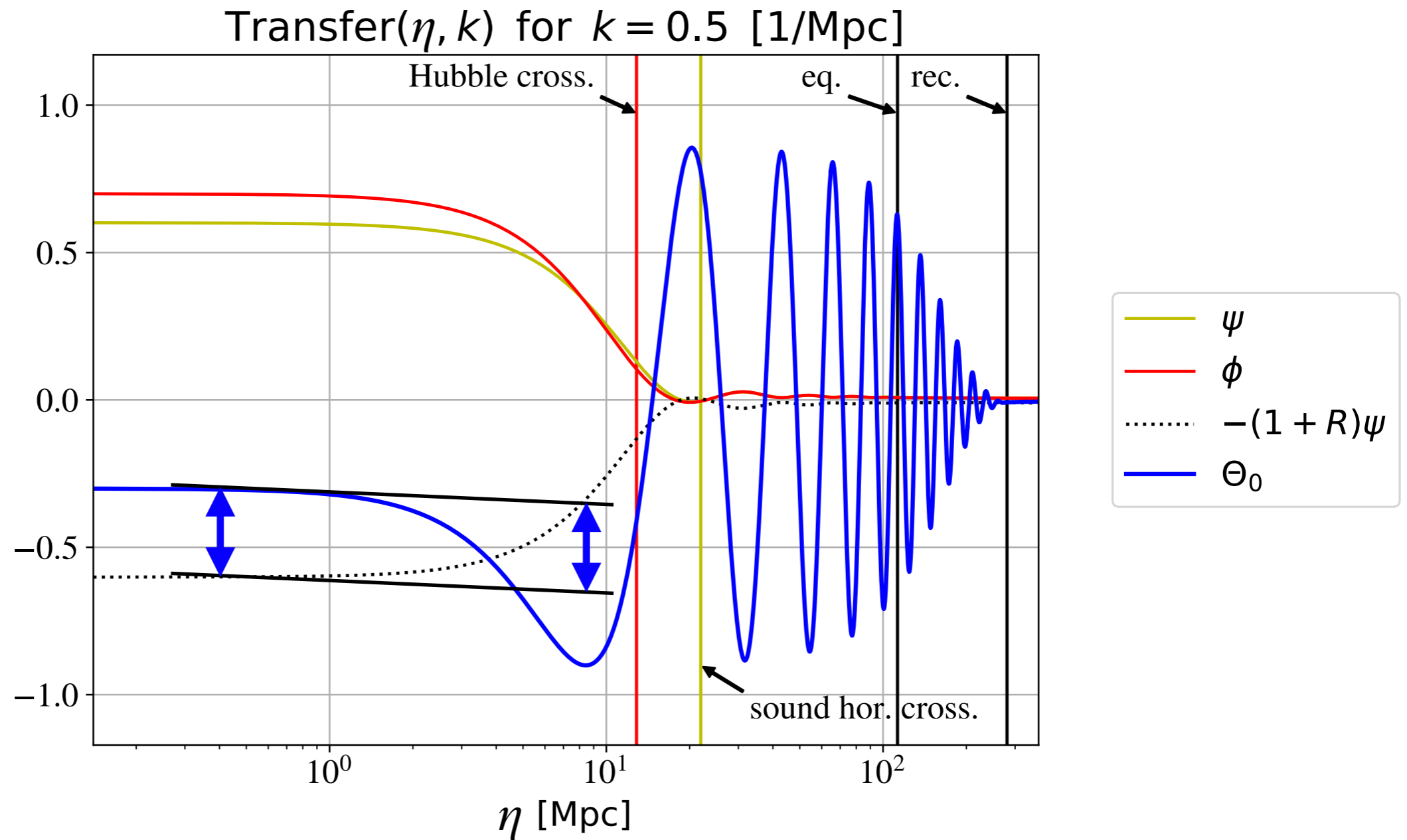
Evolution for one mode



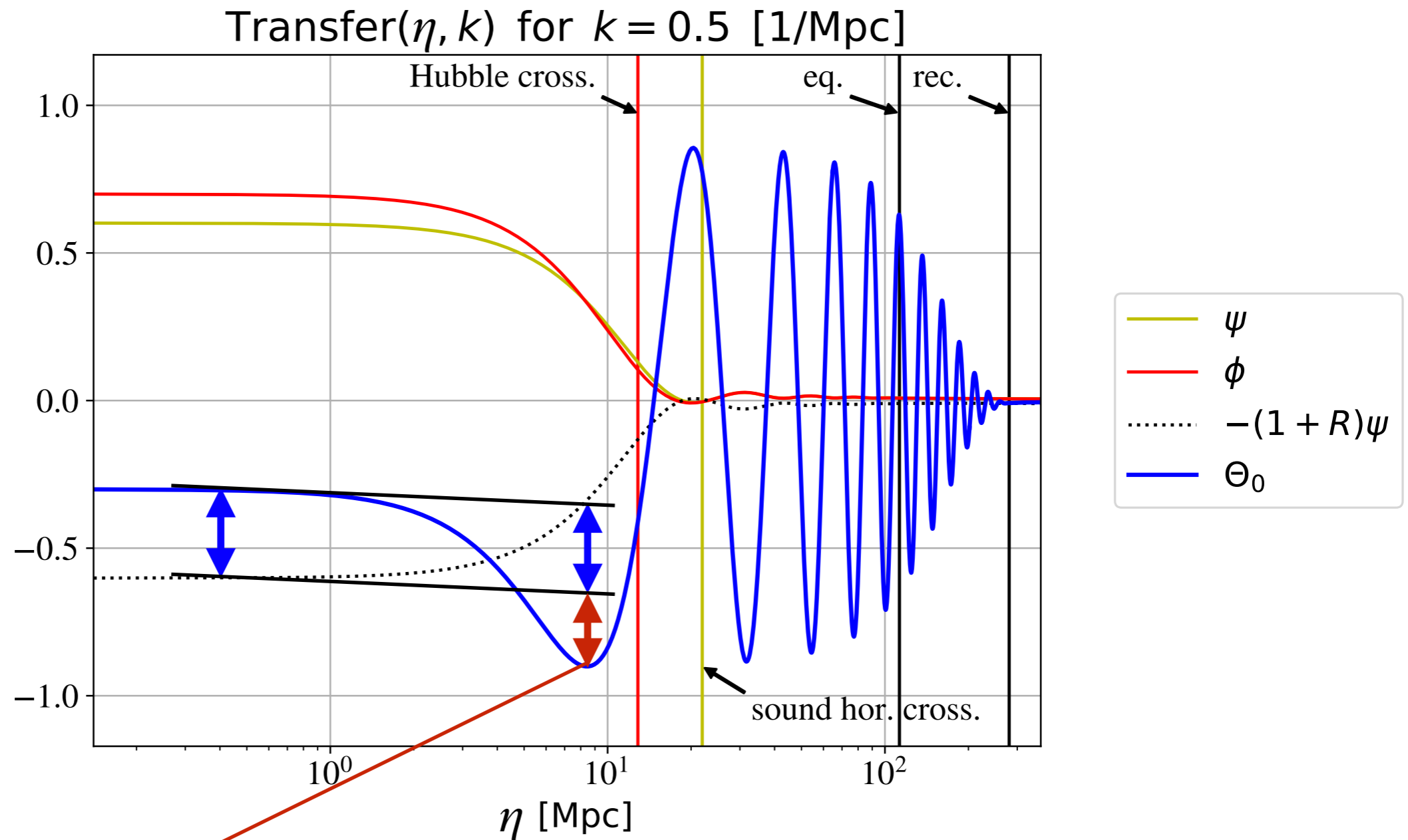
Evolution for one mode



Evolution for one mode



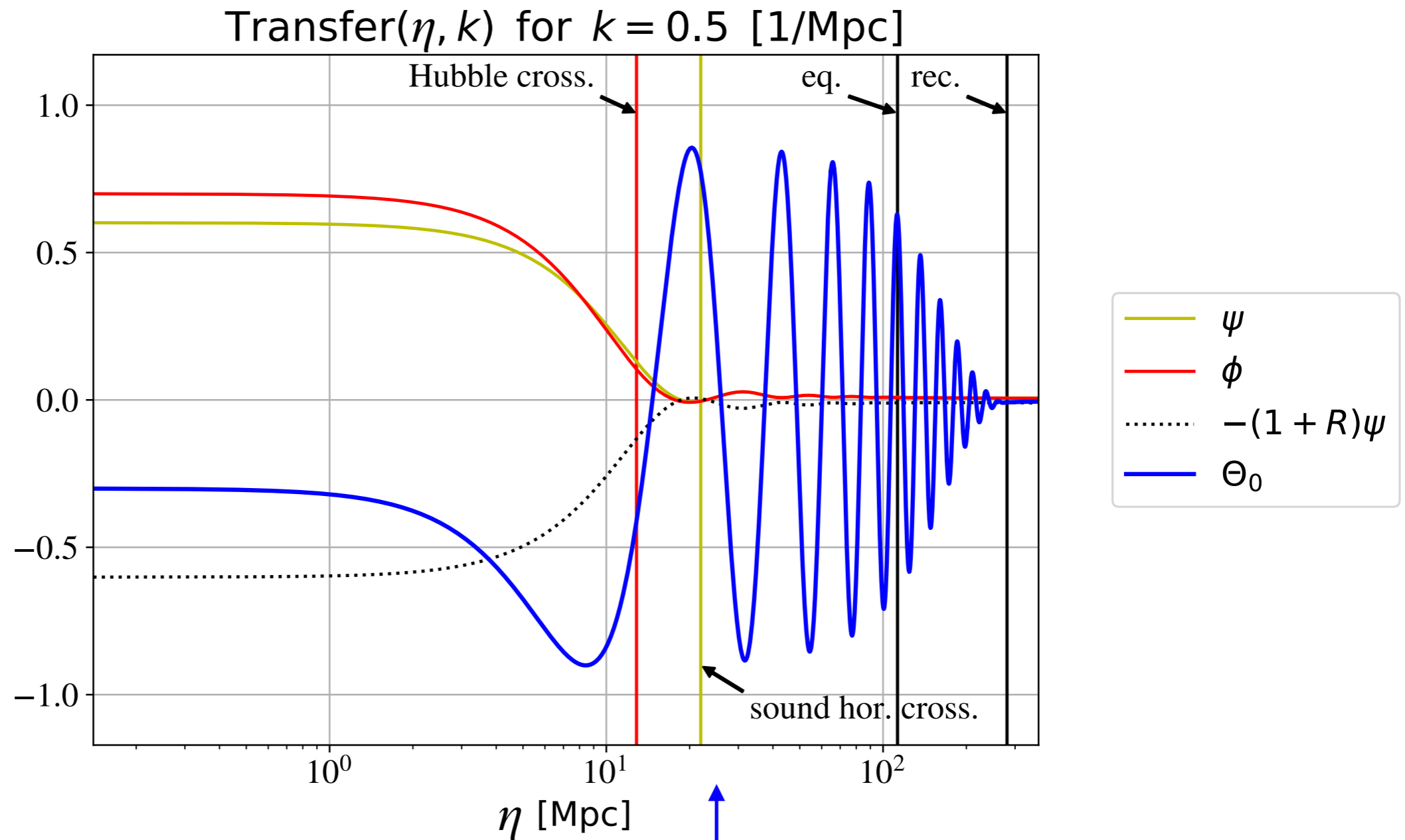
Evolution for one mode



Gravity boost effect from $\frac{R'}{1+R}\phi' + \phi''$

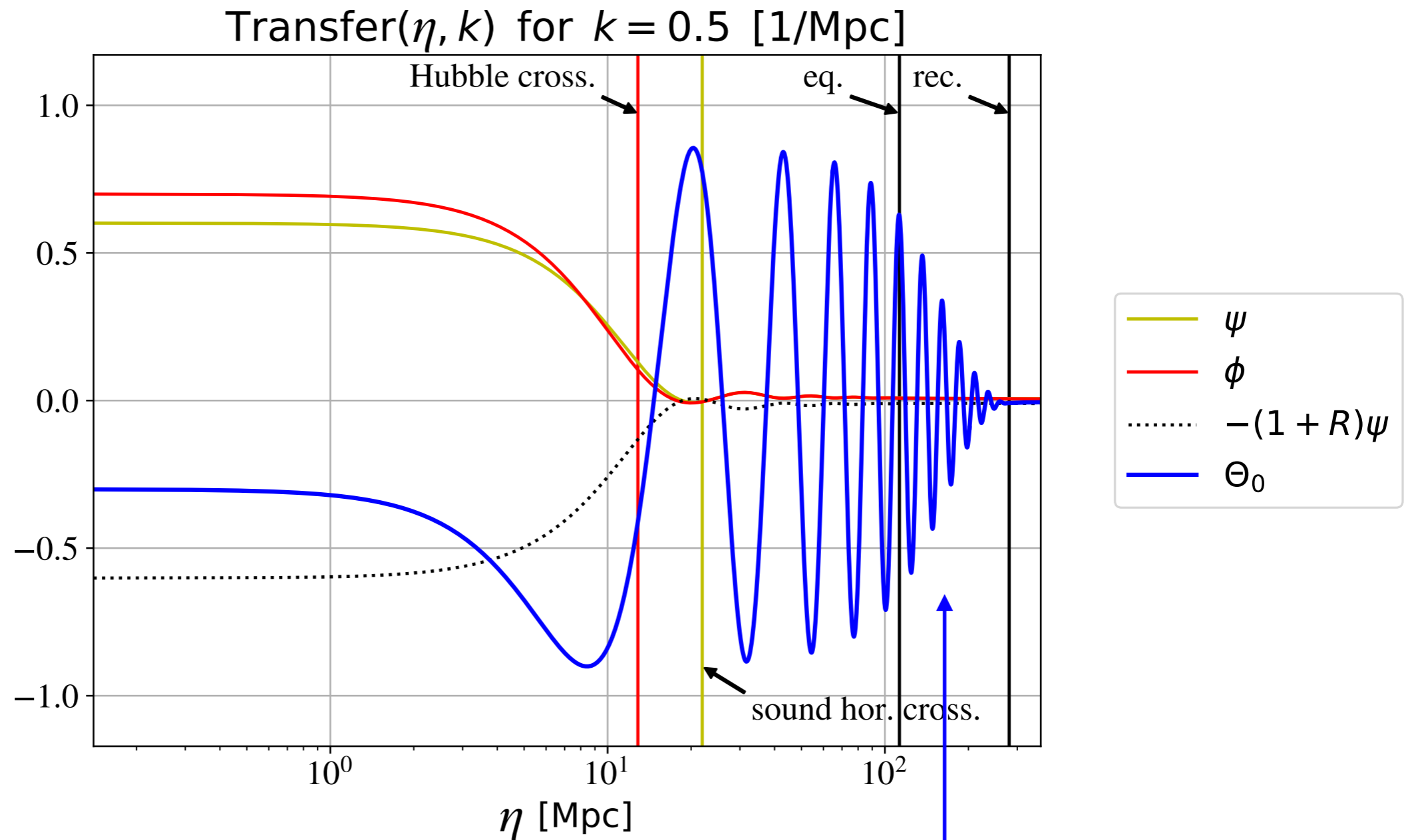
Will be important for effect of neutrinos, DR...

Evolution for one mode



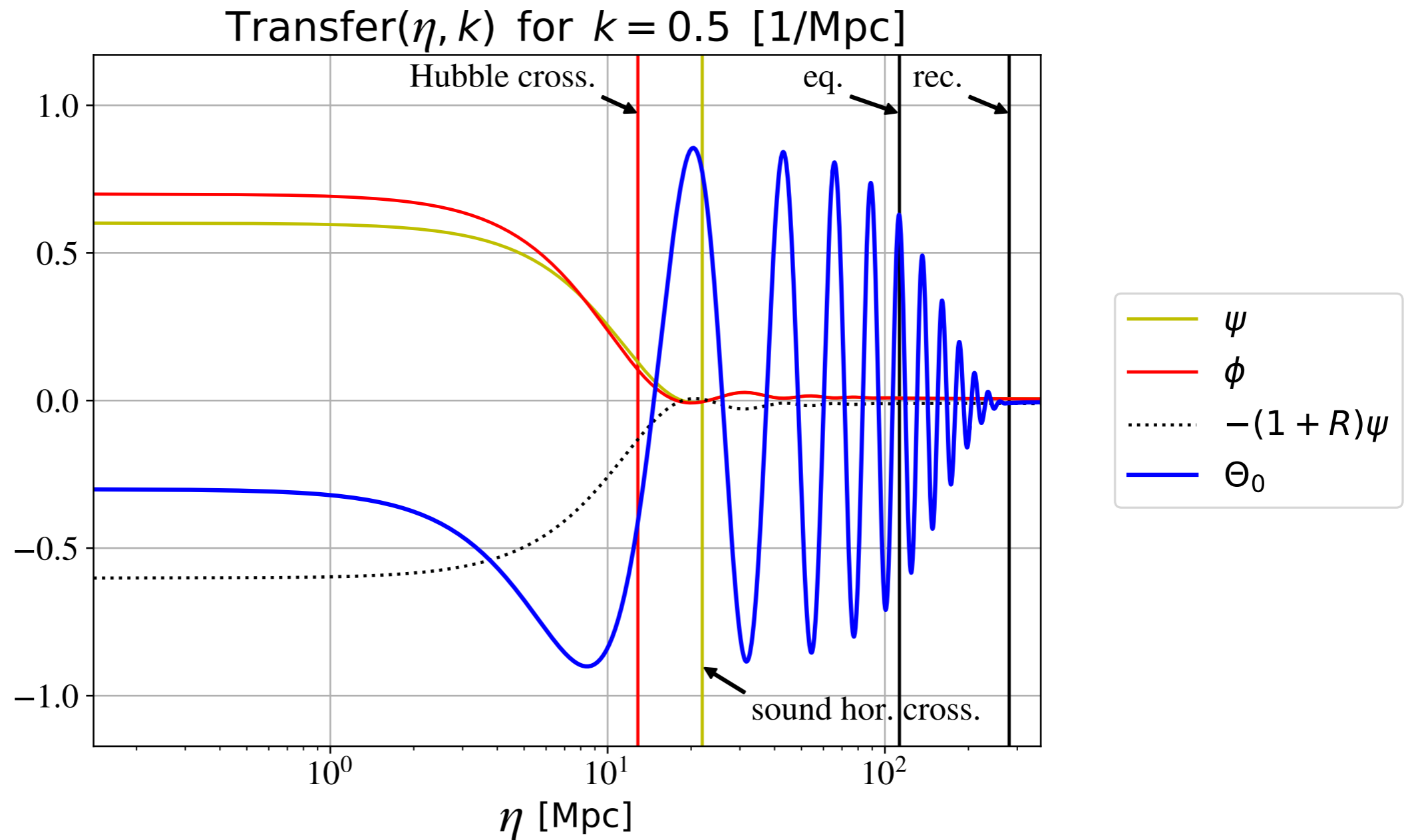
symmetric and stationary oscillation
(deep sub-Hubble, deep DR)

Evolution for one mode



exponentially damped oscillations
(approaching recombination)

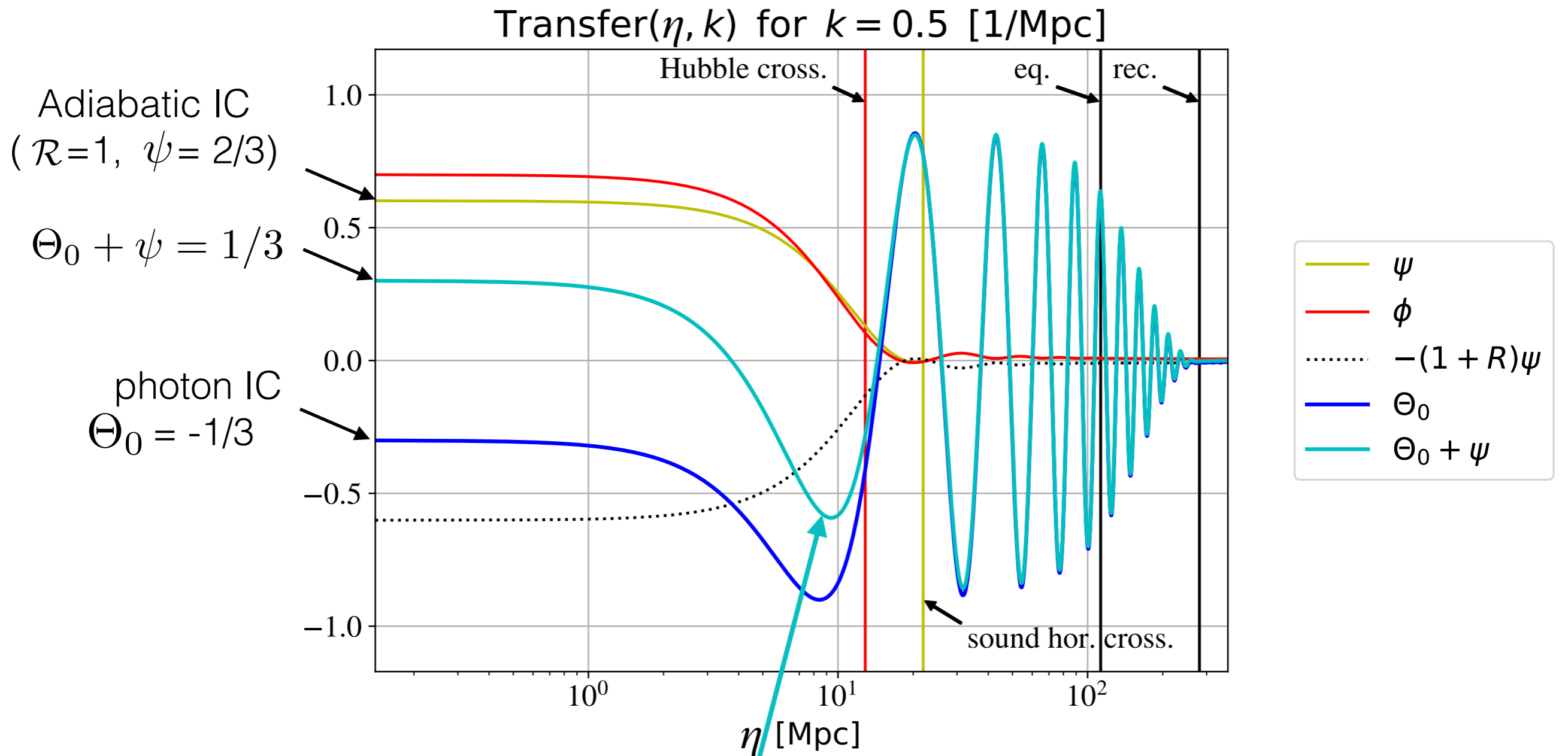
Evolution for one mode



Final goal:
(MZ's line-of-sight
integral)

$$\Theta_l(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta \left(\underbrace{g(\Theta_0 + \psi)}_{\text{SW}} + \underbrace{(g k^{-2} \theta_b)'}_{\text{Doppler}} + \underbrace{e^{-\tau}(\phi' + \psi')}_{\text{ISW}} \right) j_l(k(\eta_0 - \eta))$$

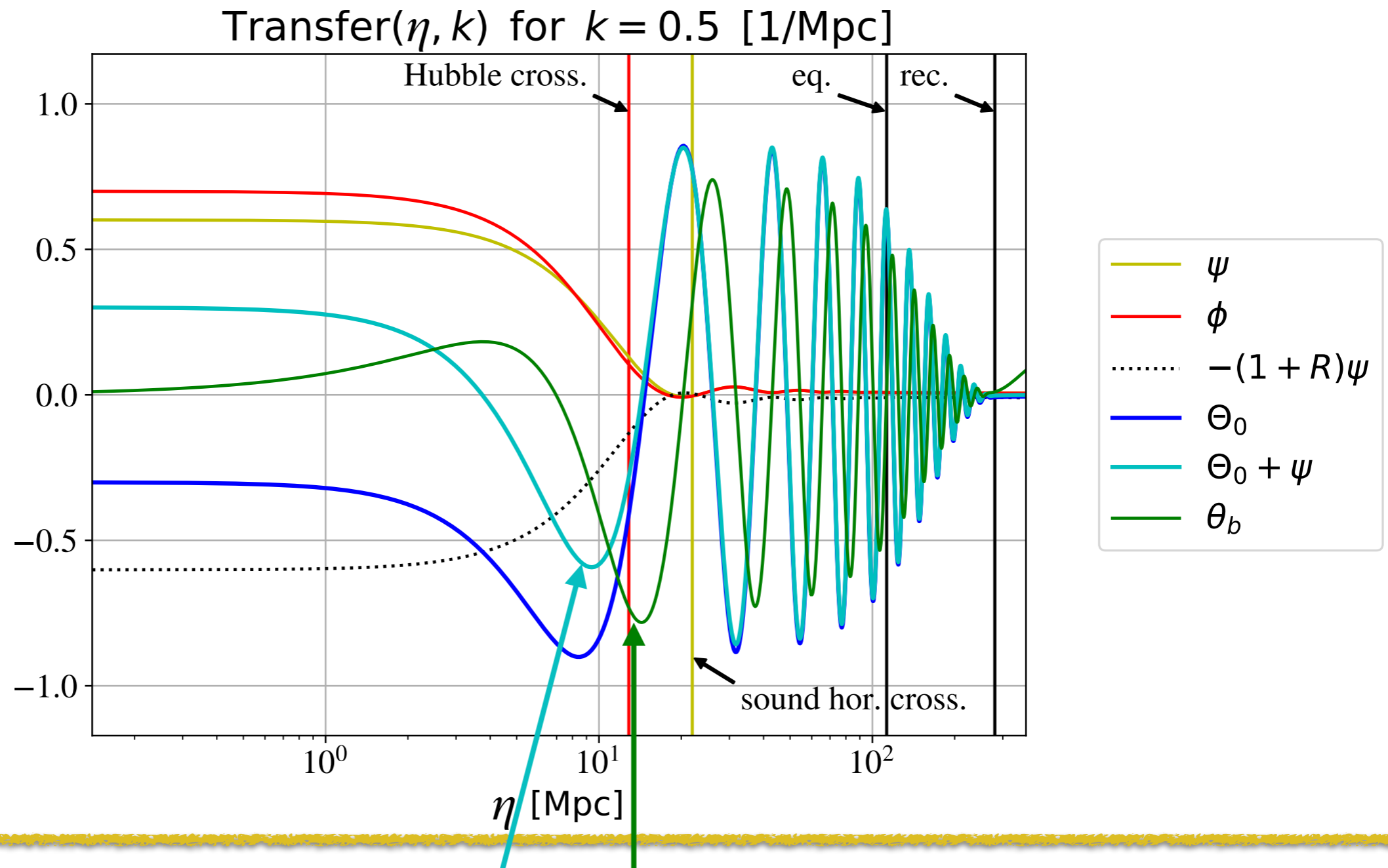
Evolution for one mode



Final goal:
(MZ's line-of-sight
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$$\Theta_l(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta \left(\underbrace{g(\Theta_0 + \psi)}_{\text{SW}} + \underbrace{(g k^{-2} \theta_b)'}_{\text{Doppler}} + \underbrace{e^{-\tau}(\phi' + \psi')}_{\text{ISW}} \right) j_l(k(\eta_0 - \eta))$$

Evolution for one mode

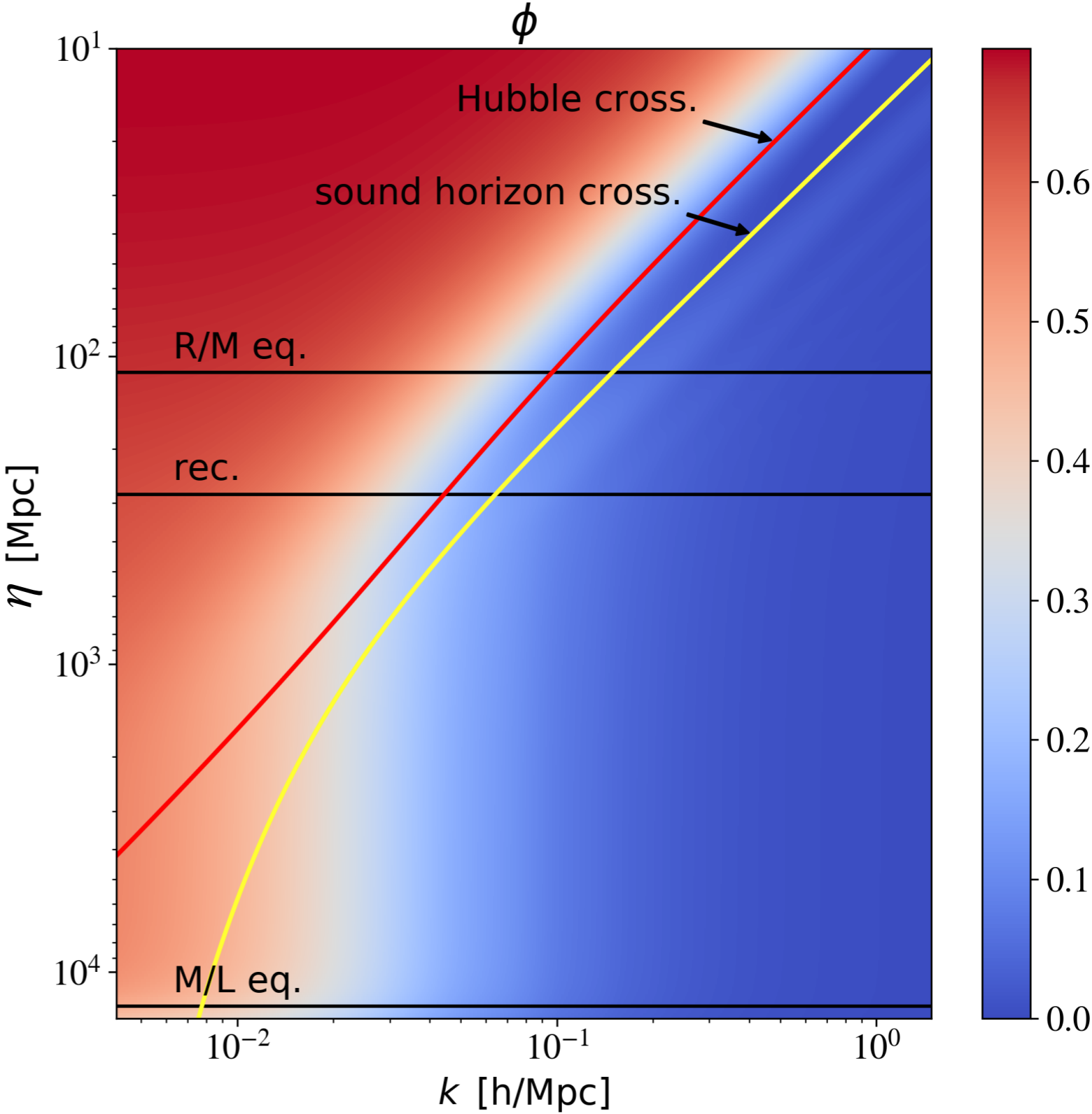


Final goal:
(MZ's line-of-sight
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$$\Theta_l(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta \left(\underbrace{g(\Theta_0 + \psi)}_{\text{SW}} + \underbrace{(g k^{-2} \theta_b)'}_{\text{Doppler}} + \underbrace{e^{-\tau}(\phi' + \psi')}_{\text{ISW}} \right) j_l(k(\eta_0 - \eta))$$

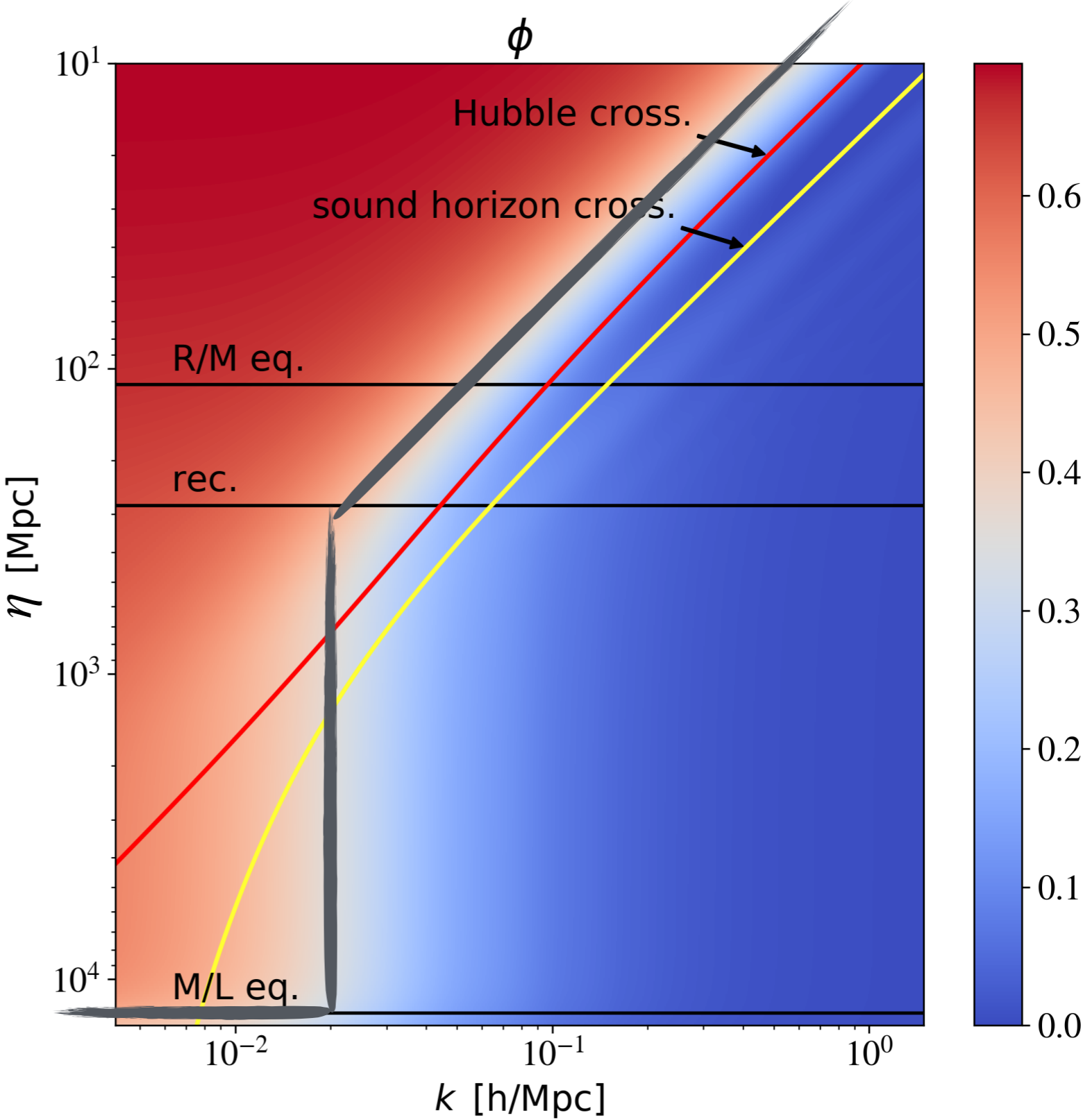
Evolution for all wavenumbers

Metric $\phi(\eta, k)$:



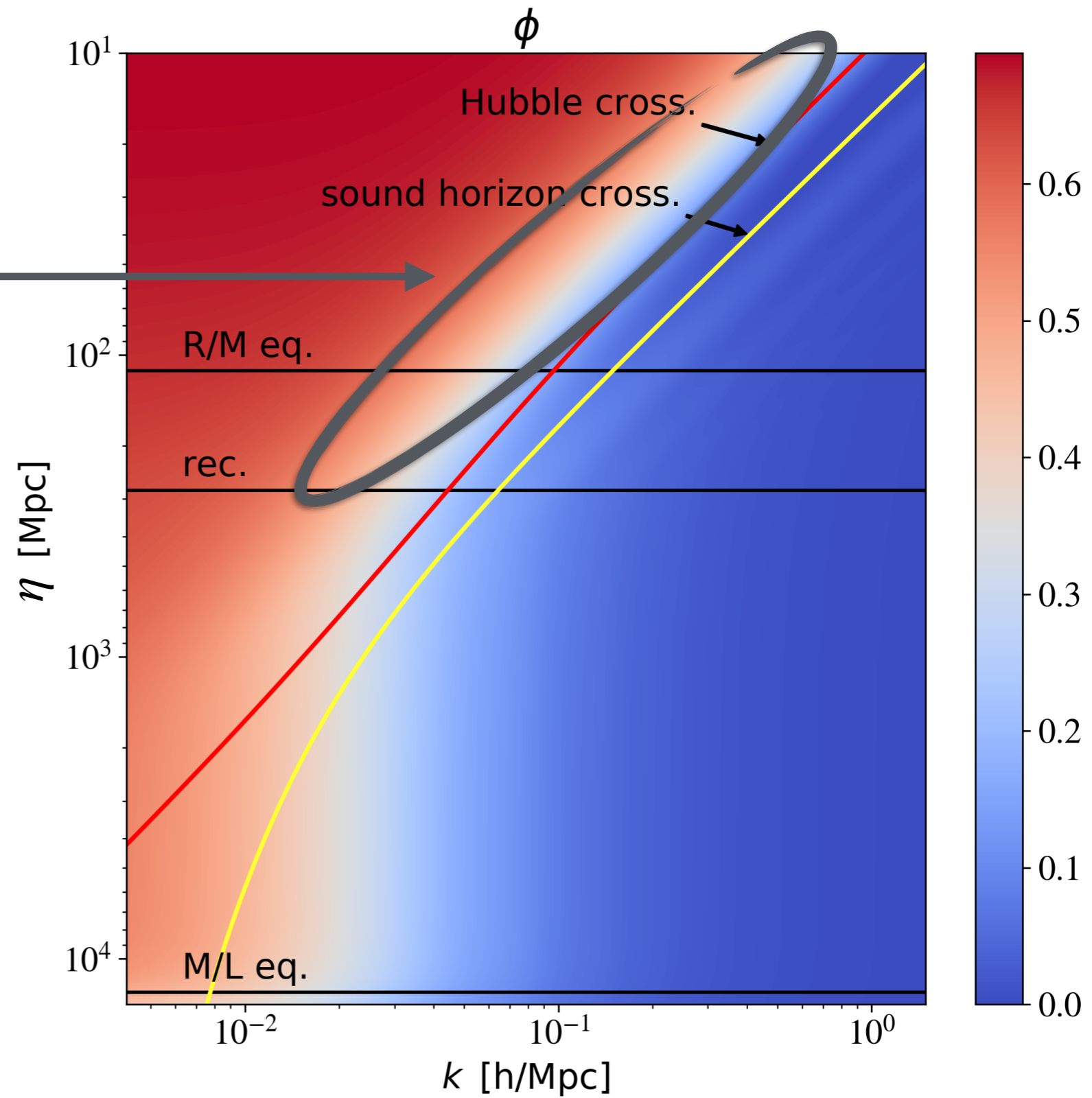
Evolution for all wavenumbers

Metric $\phi(\eta, k)$:

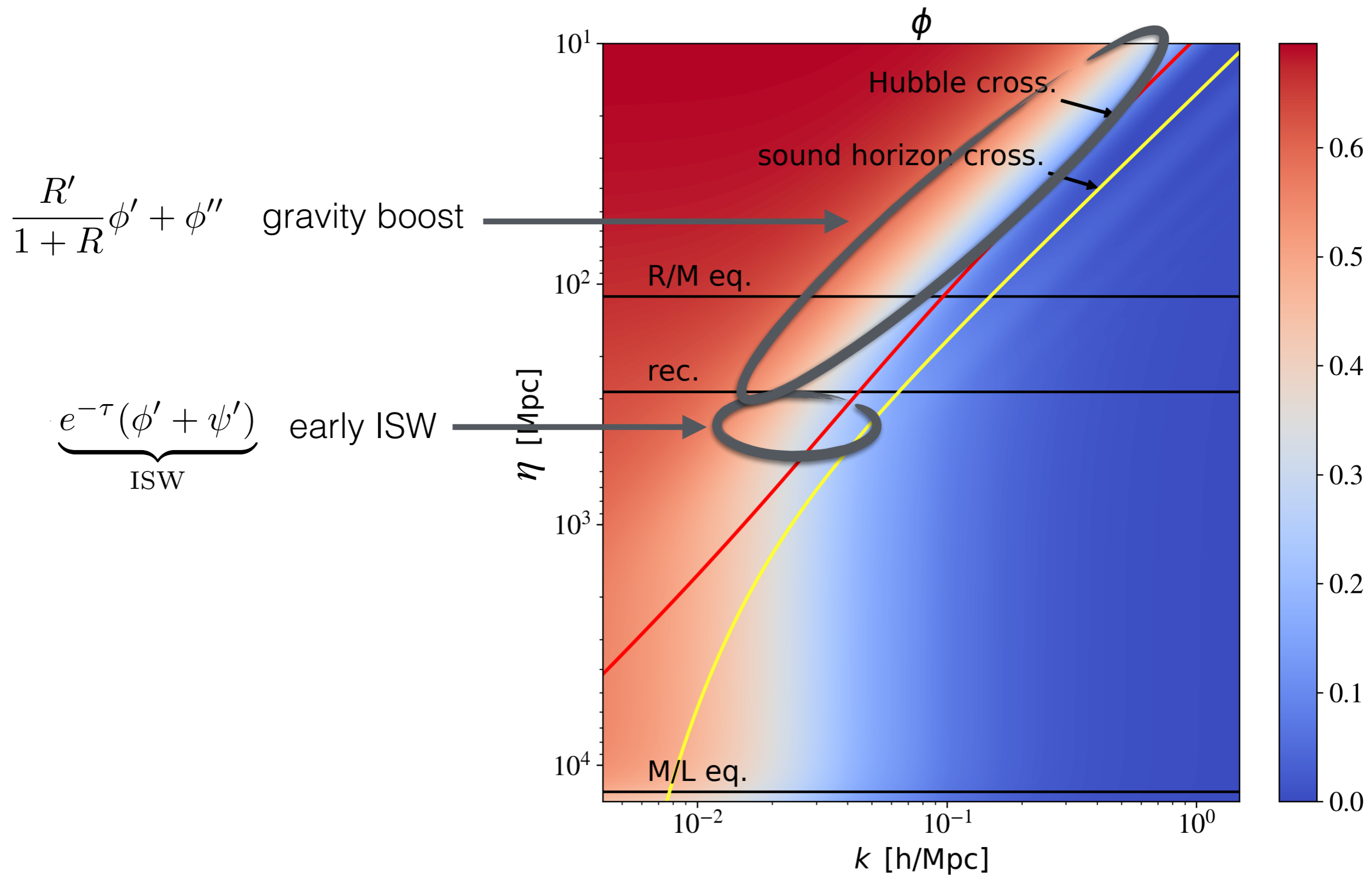


Evolution for all wavenumbers

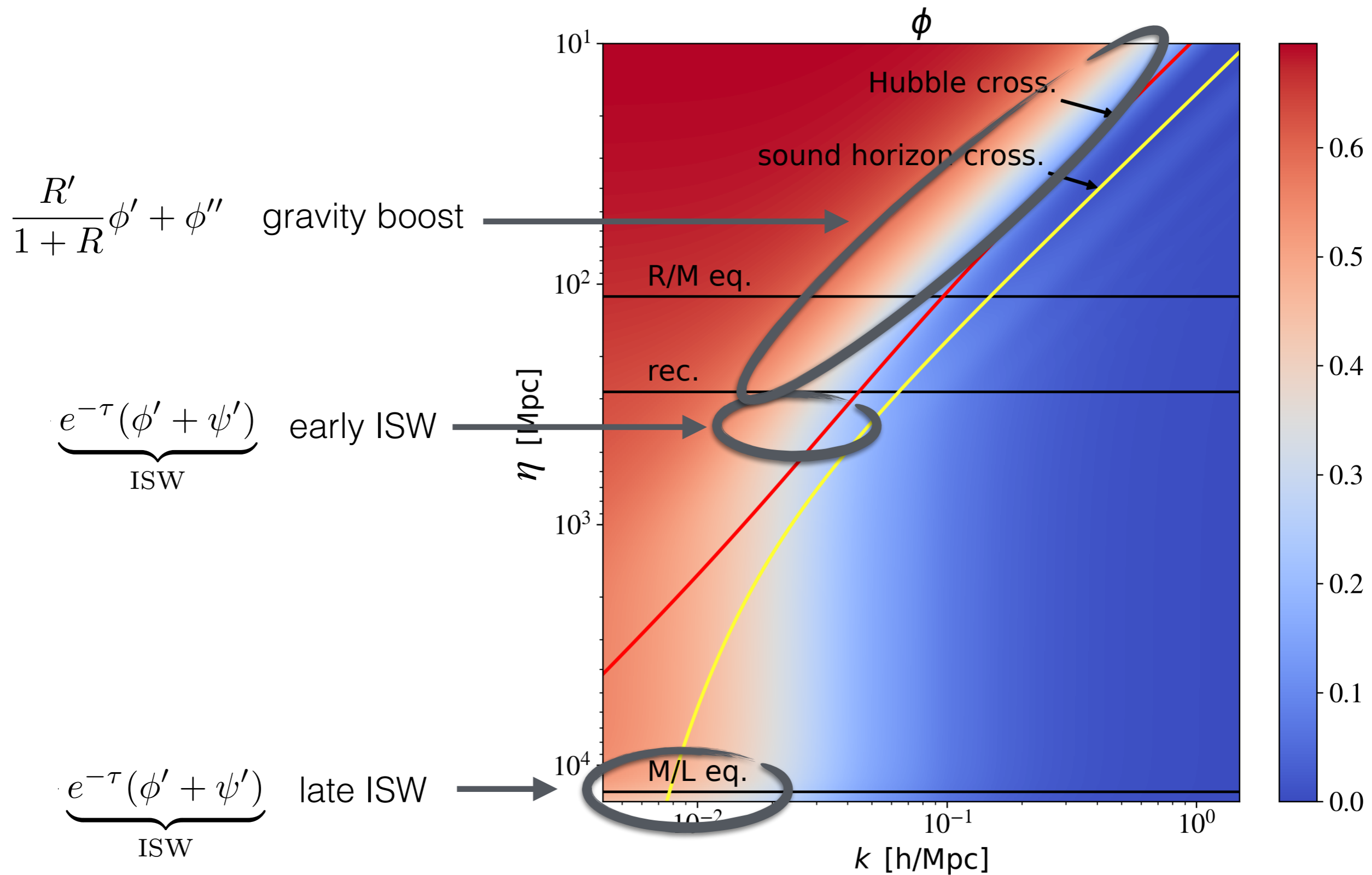
$$\frac{R'}{1+R}\phi' + \phi'' \Rightarrow \text{gravity boost}$$



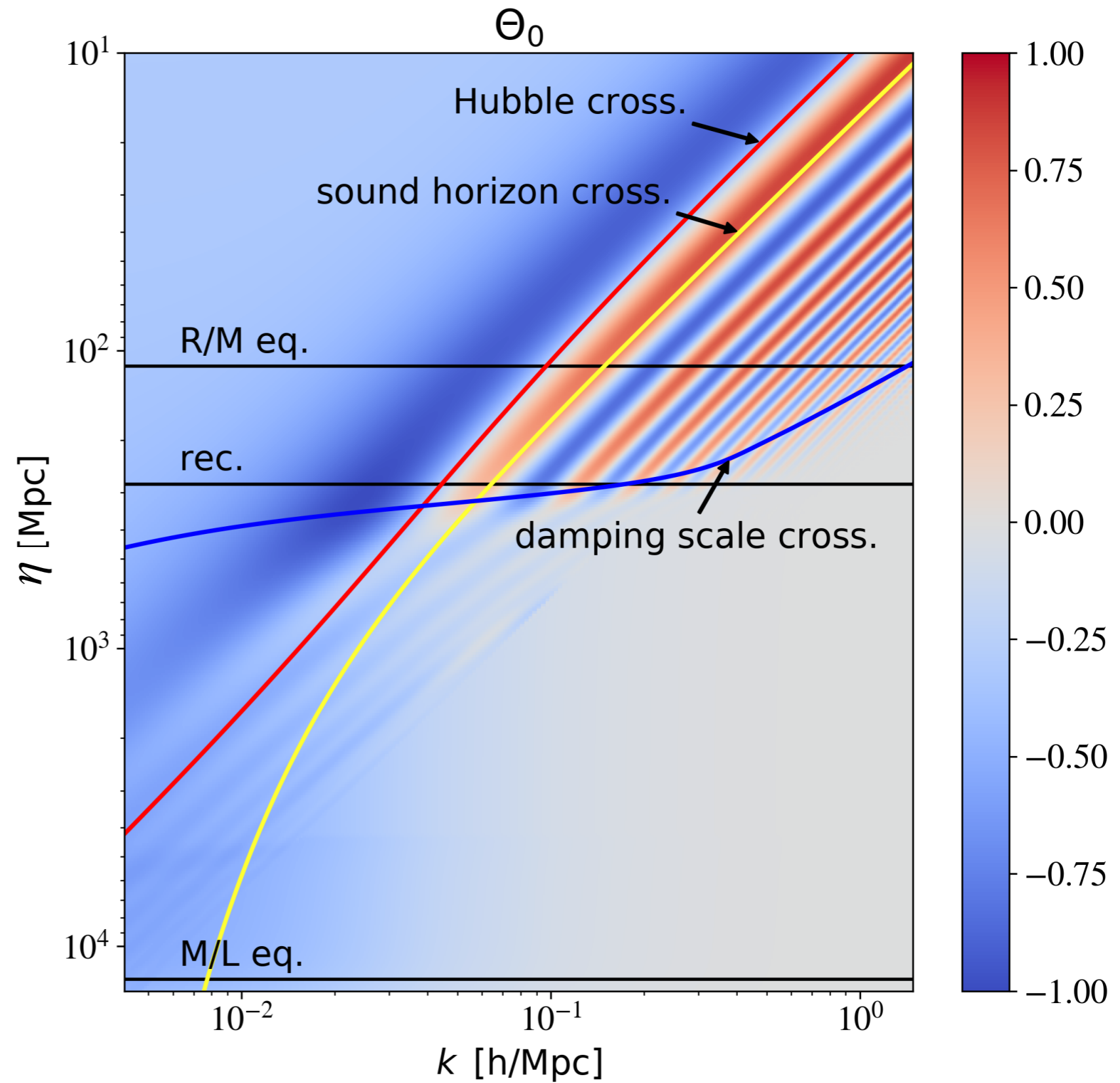
Evolution for all wavenumbers



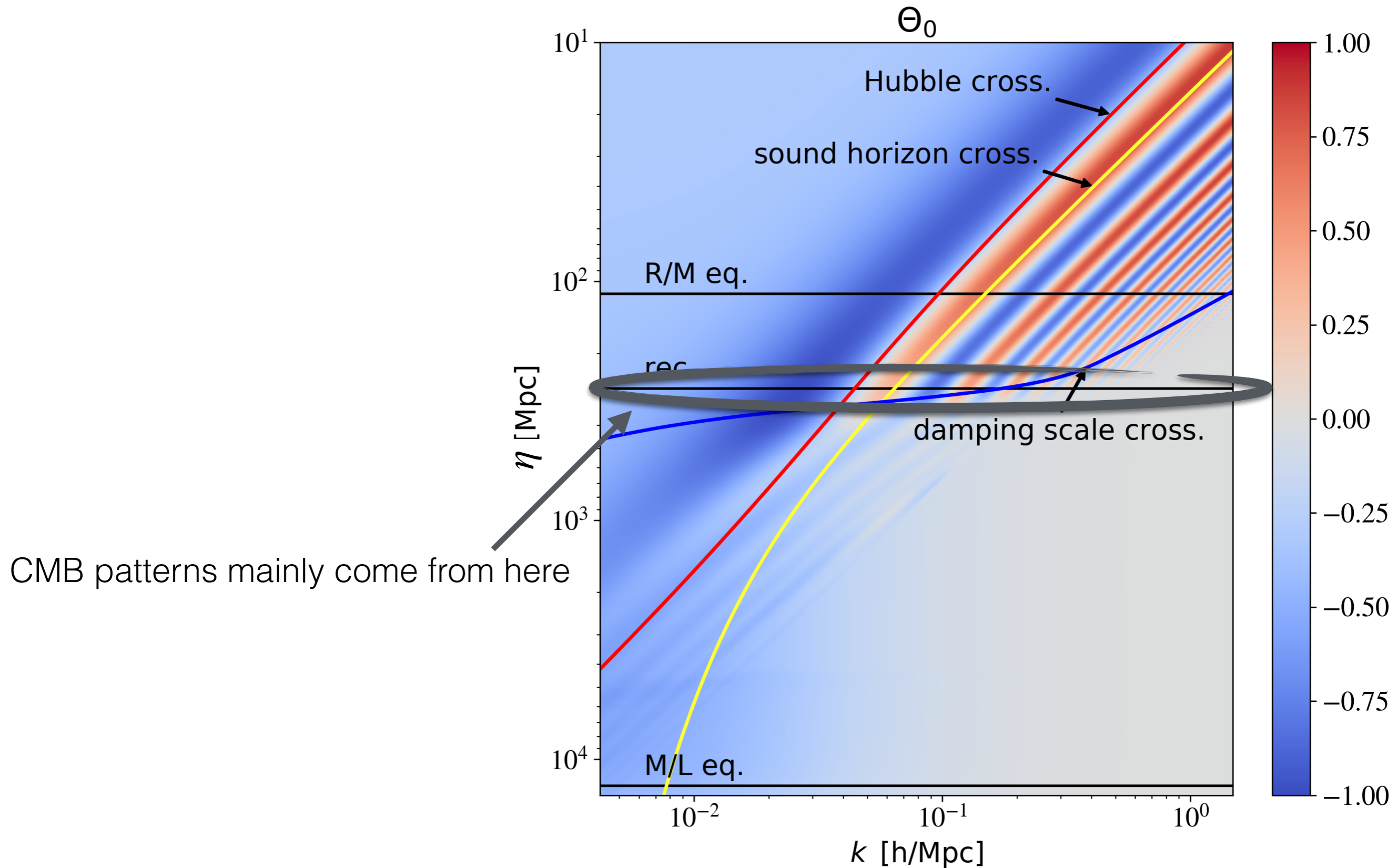
Evolution for all wavenumbers



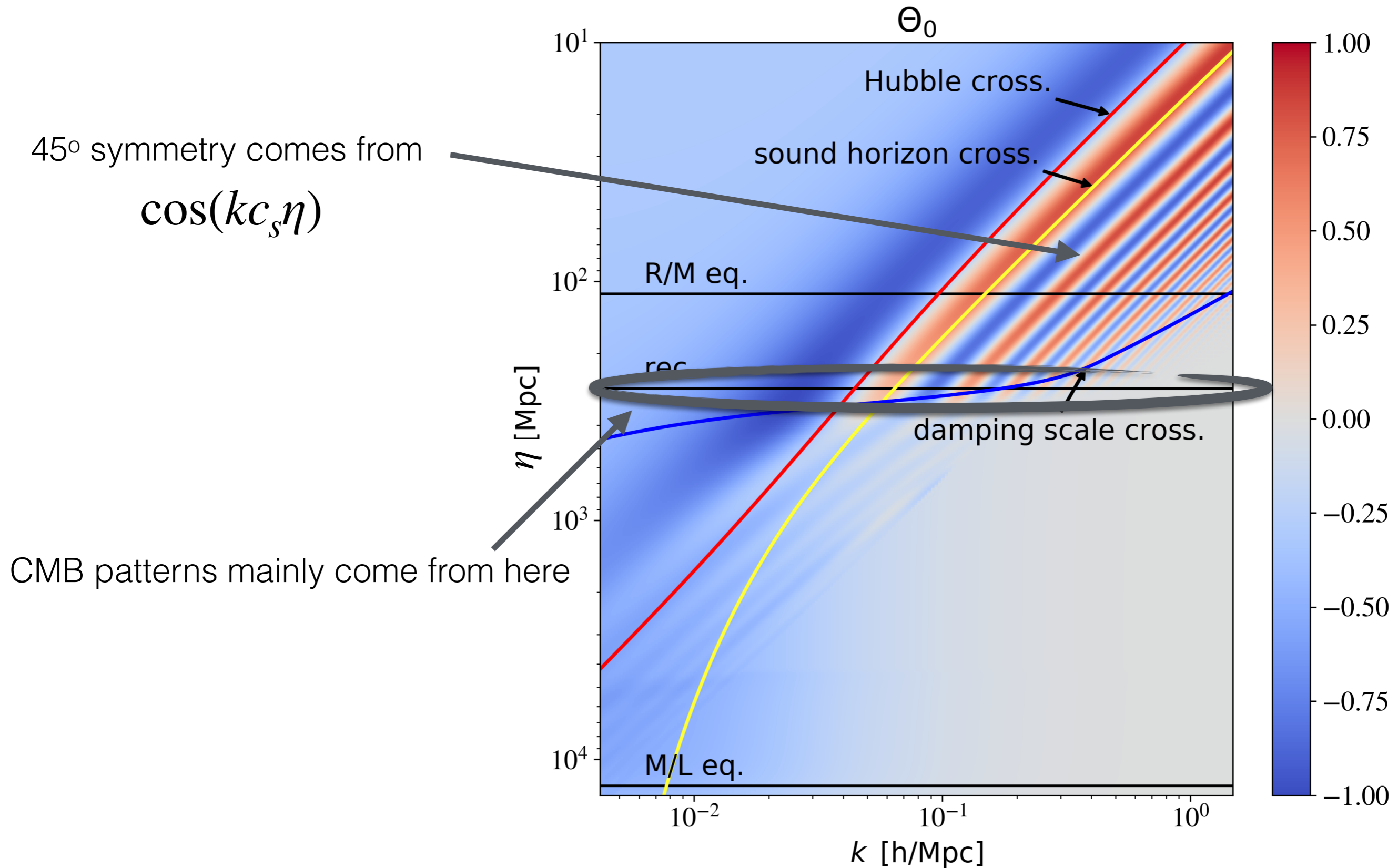
Evolution for all wavenumbers



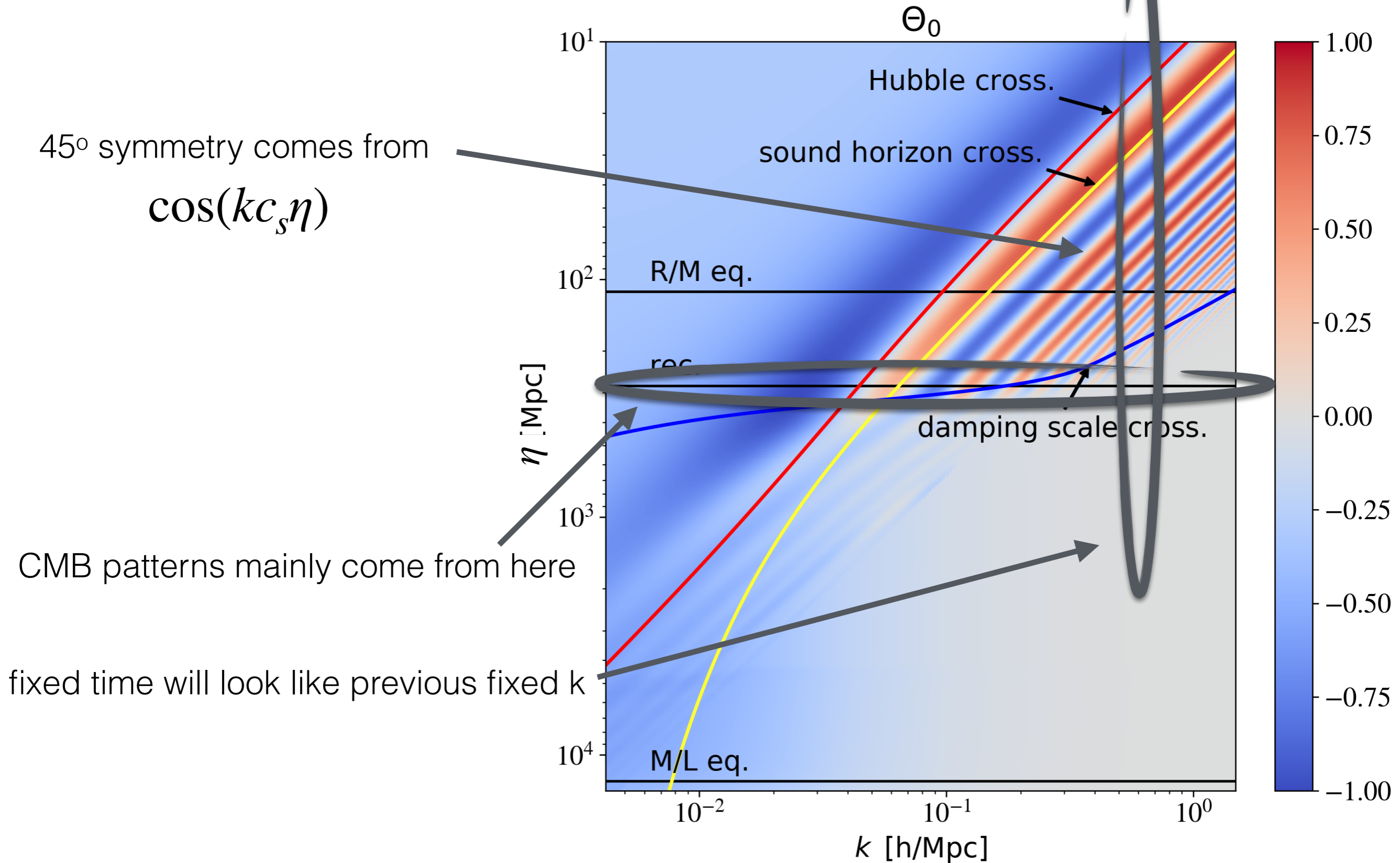
Evolution for all wavenumbers



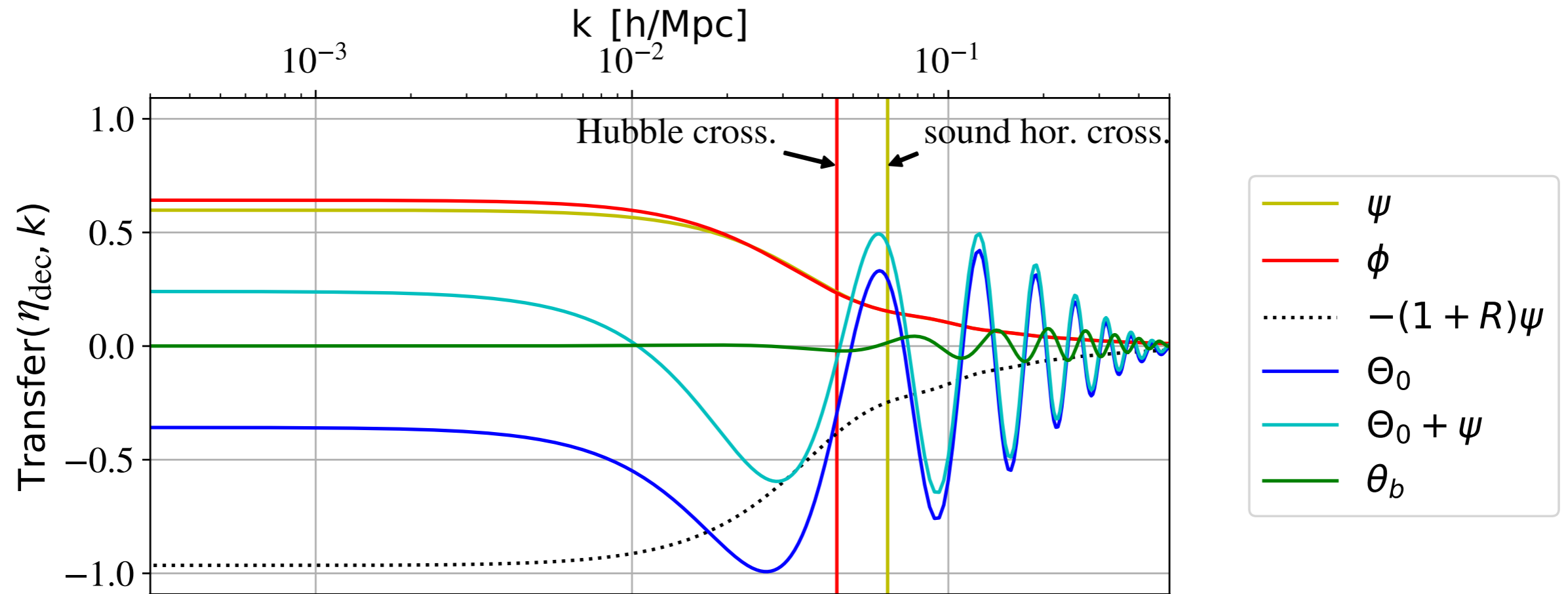
Evolution for all wavenumbers

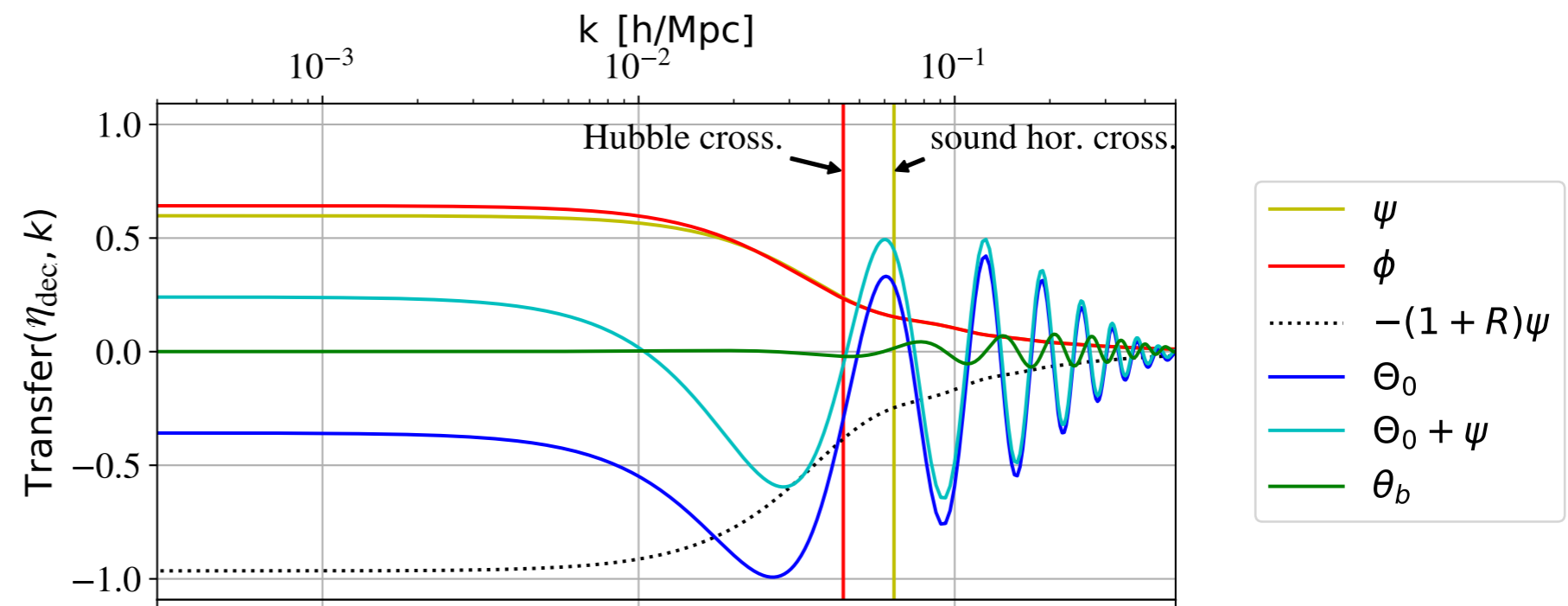


Evolution for all wavenumbers



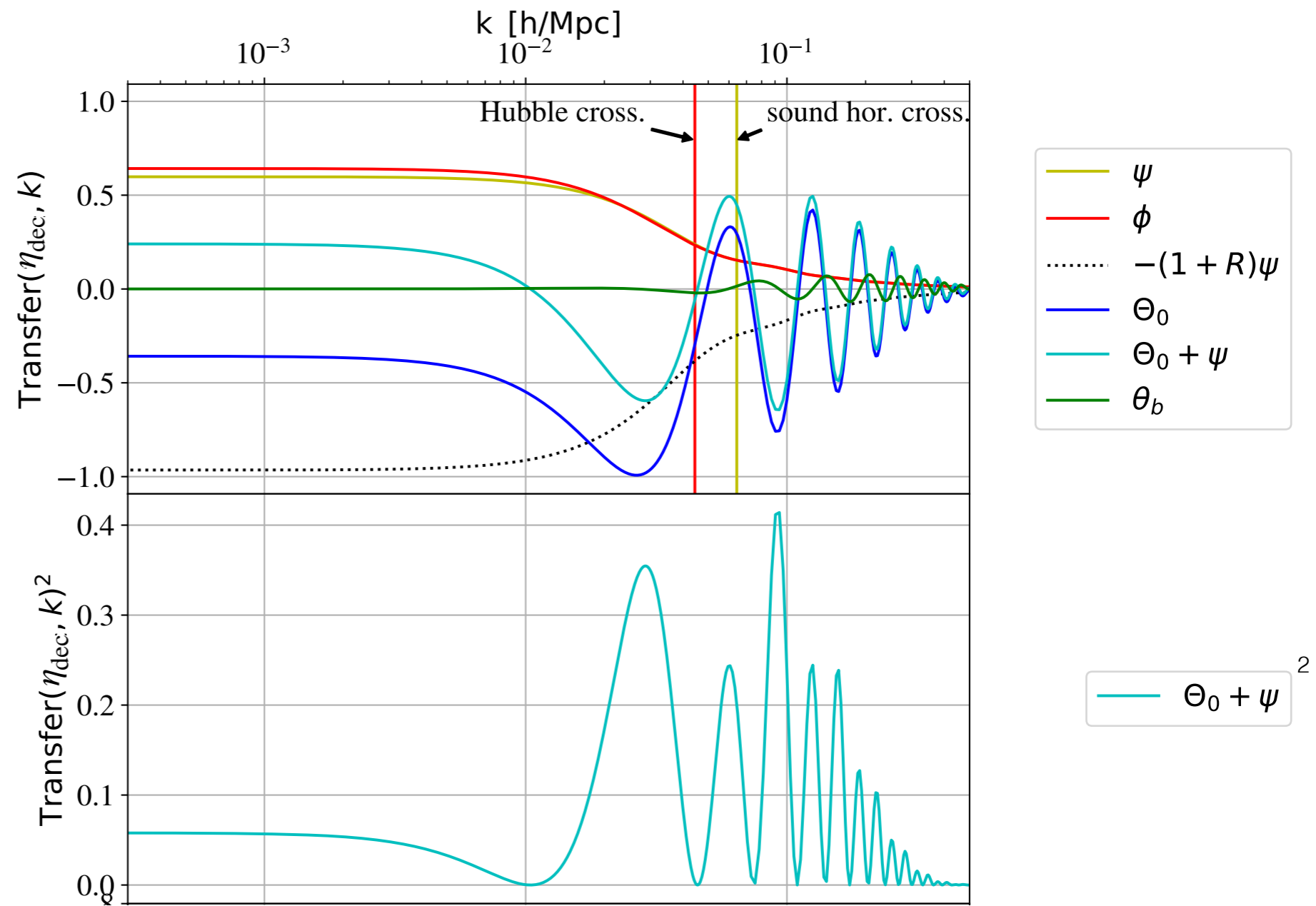
Transfer functions at recombination/decoupling





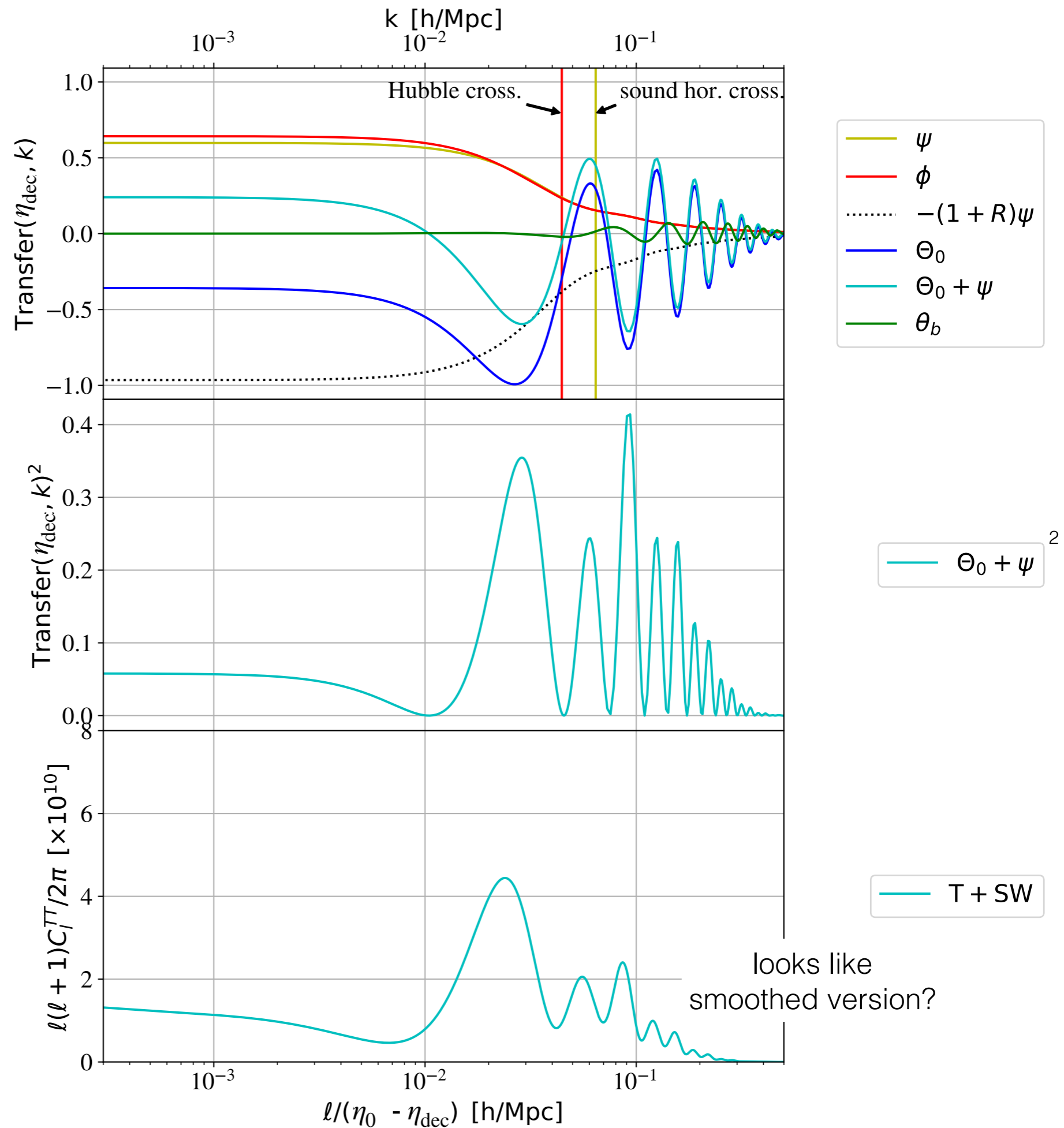
from transfer
to C_ℓ :

from transfer
to C_ℓ :



from transfer
to C_ℓ :

$\Theta_0(\eta_{\text{dec}}, k) + \psi(\eta_{\text{dec}}, k)$
independent of k would
give $l(l+1)C_l = \text{constant}$



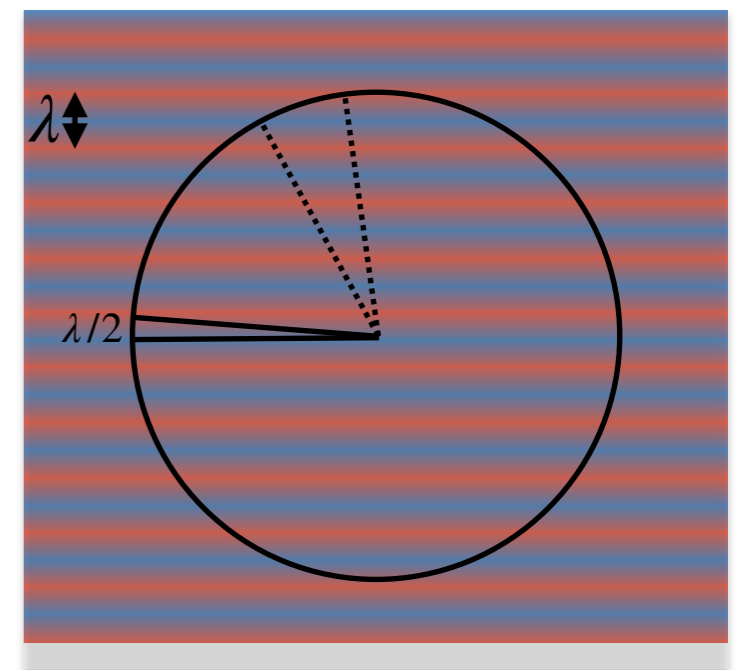
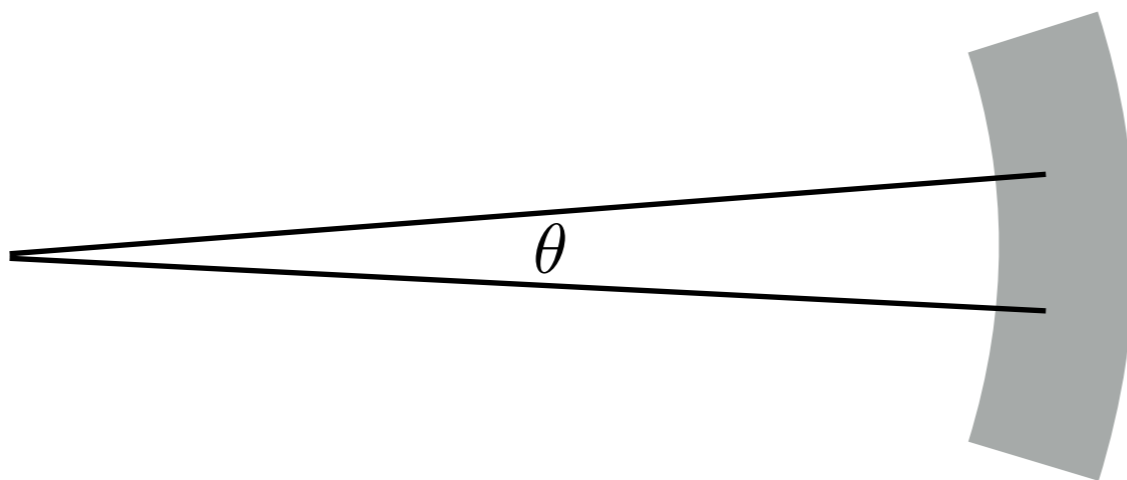
Projection effects

- two reasons for smoothing when going from k-space to l-space:

$$\Theta_l(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta \left(g(\Theta_0 + \psi) + \dots \right) j_l(k(\eta_0 - \eta))$$

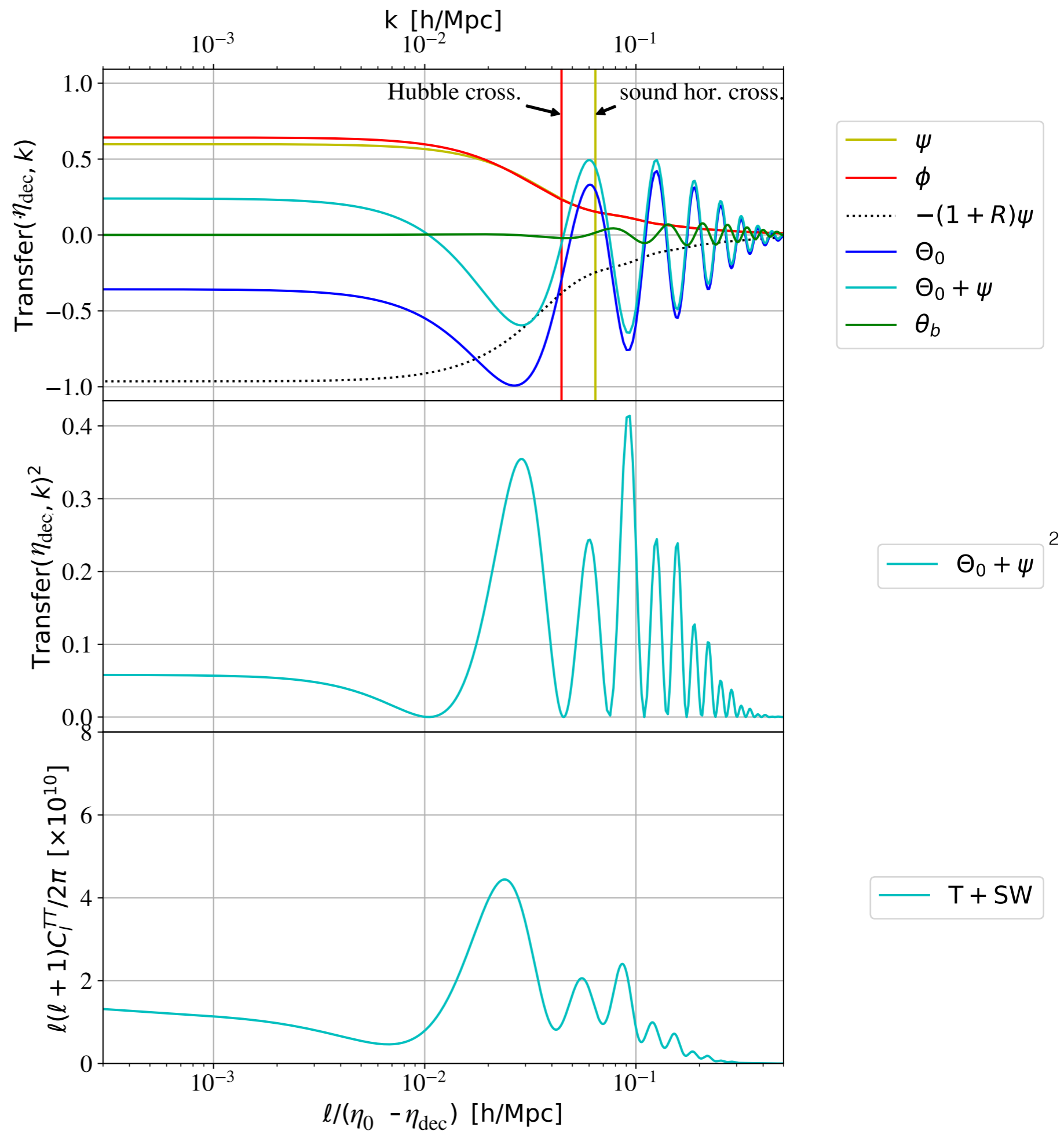
$$C_l \equiv \langle |a_{lm}|^2 \rangle = \frac{1}{2\pi^2} \int \frac{dk}{k} \Theta_l^2(\eta_0, k) \mathcal{P}_{\mathcal{R}}(k)$$

—> contribution of wide range of *times* and *wavenumber* to single C_l

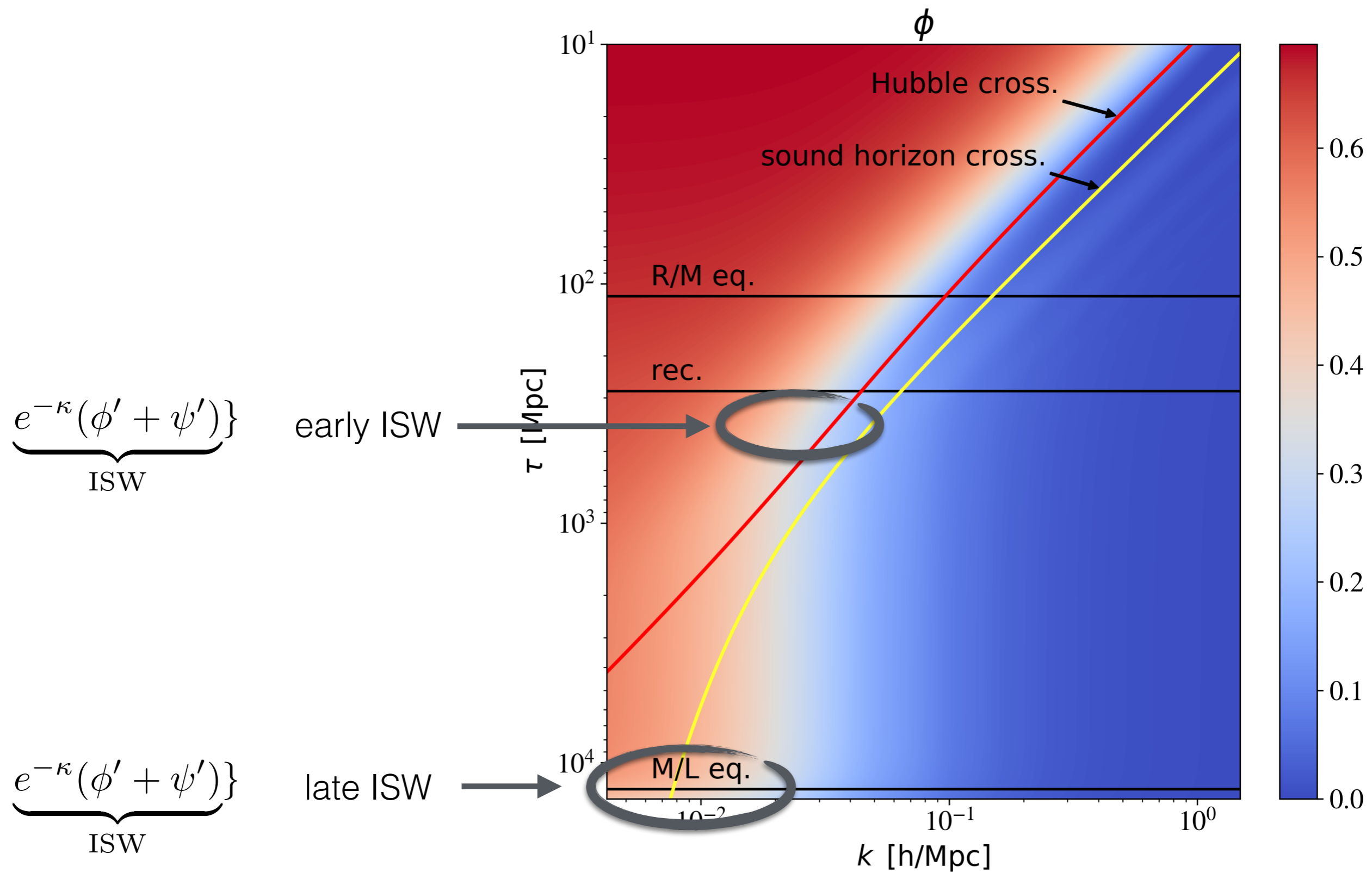


from transfer
to C_ℓ :

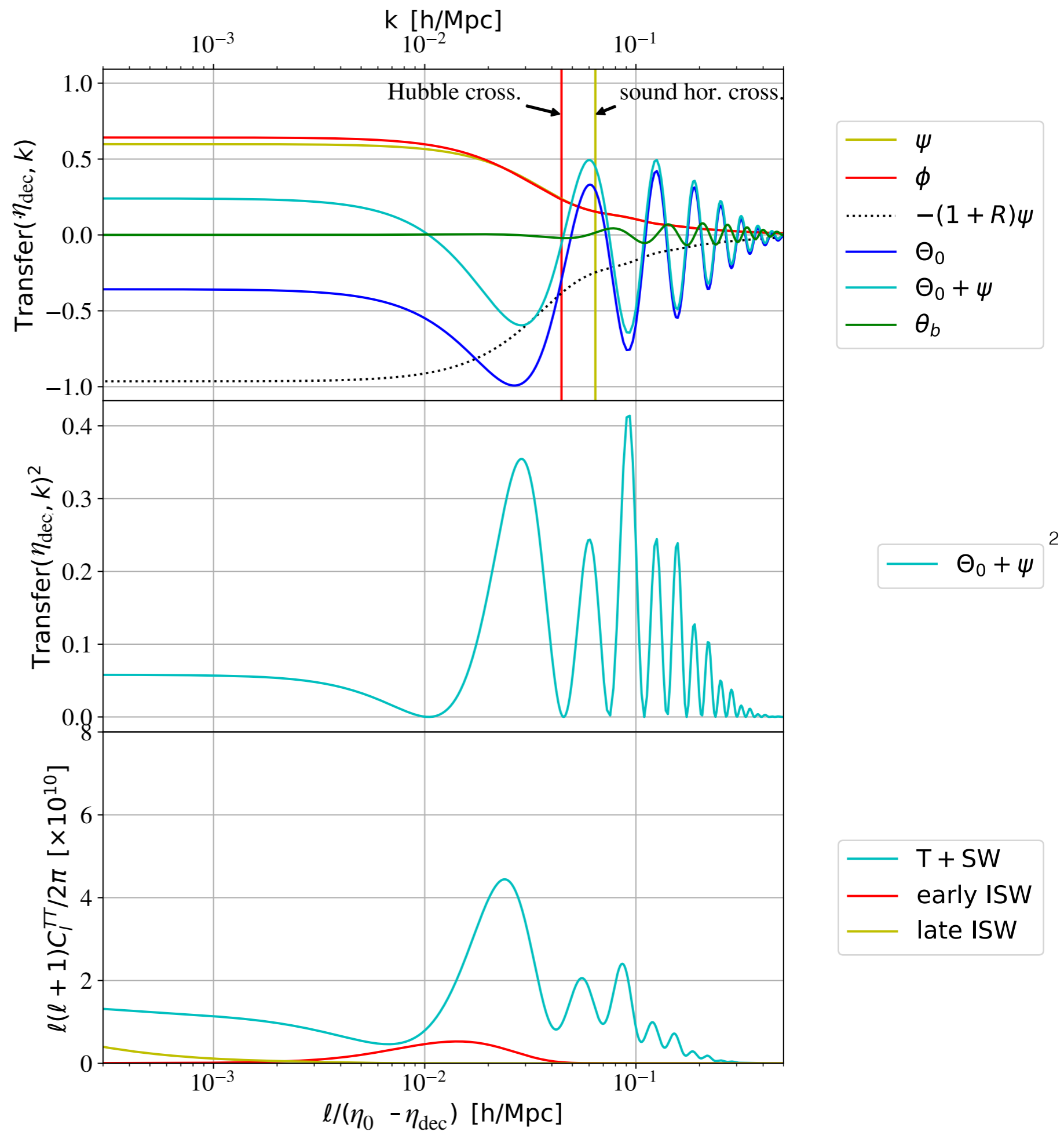
$\Theta_0(\eta_{\text{dec}}, k) + \psi(\eta_{\text{dec}}, k)$
independent of k would
give $l(l+1)C_l = \text{constant}$



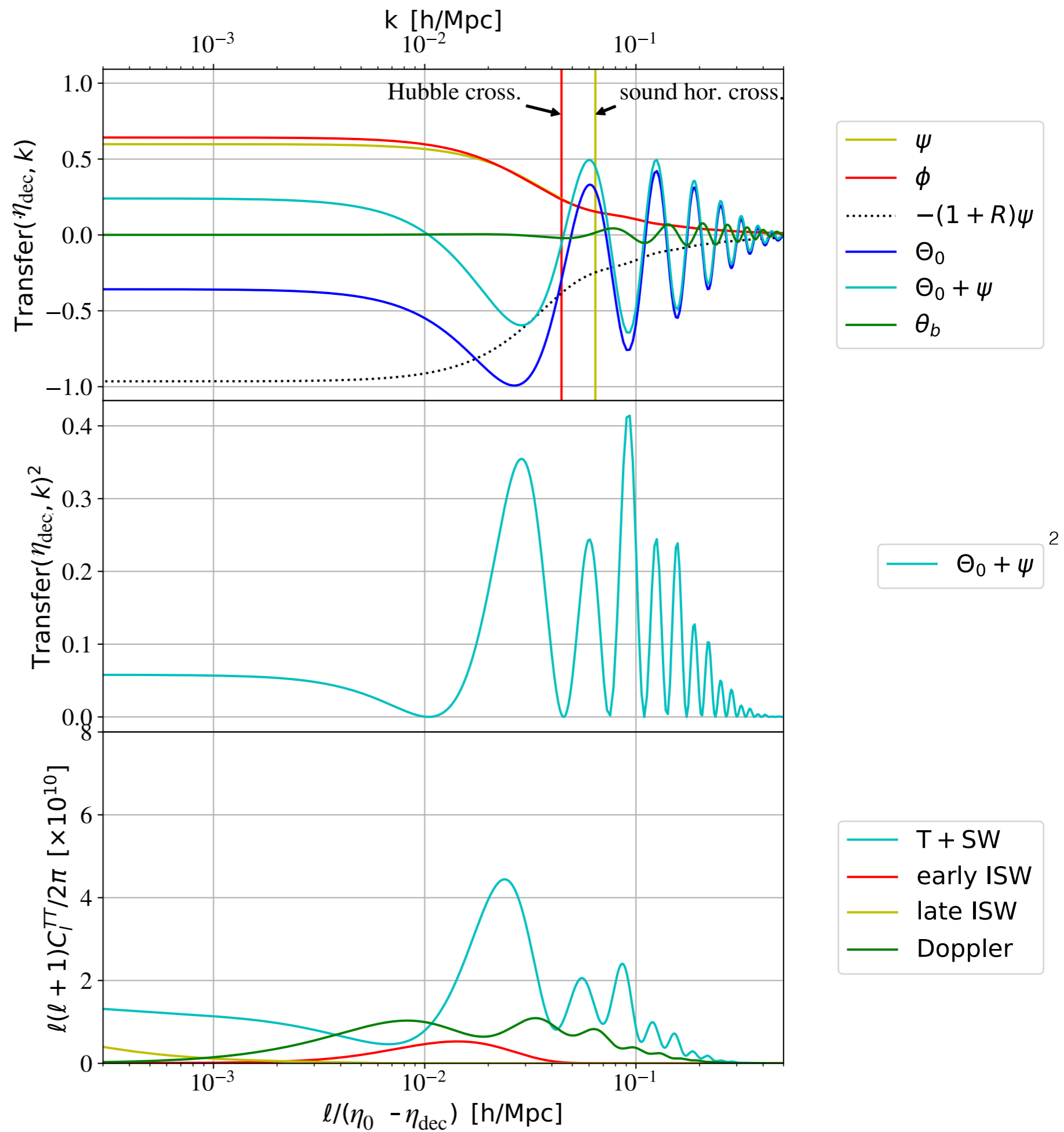
ISW contribution



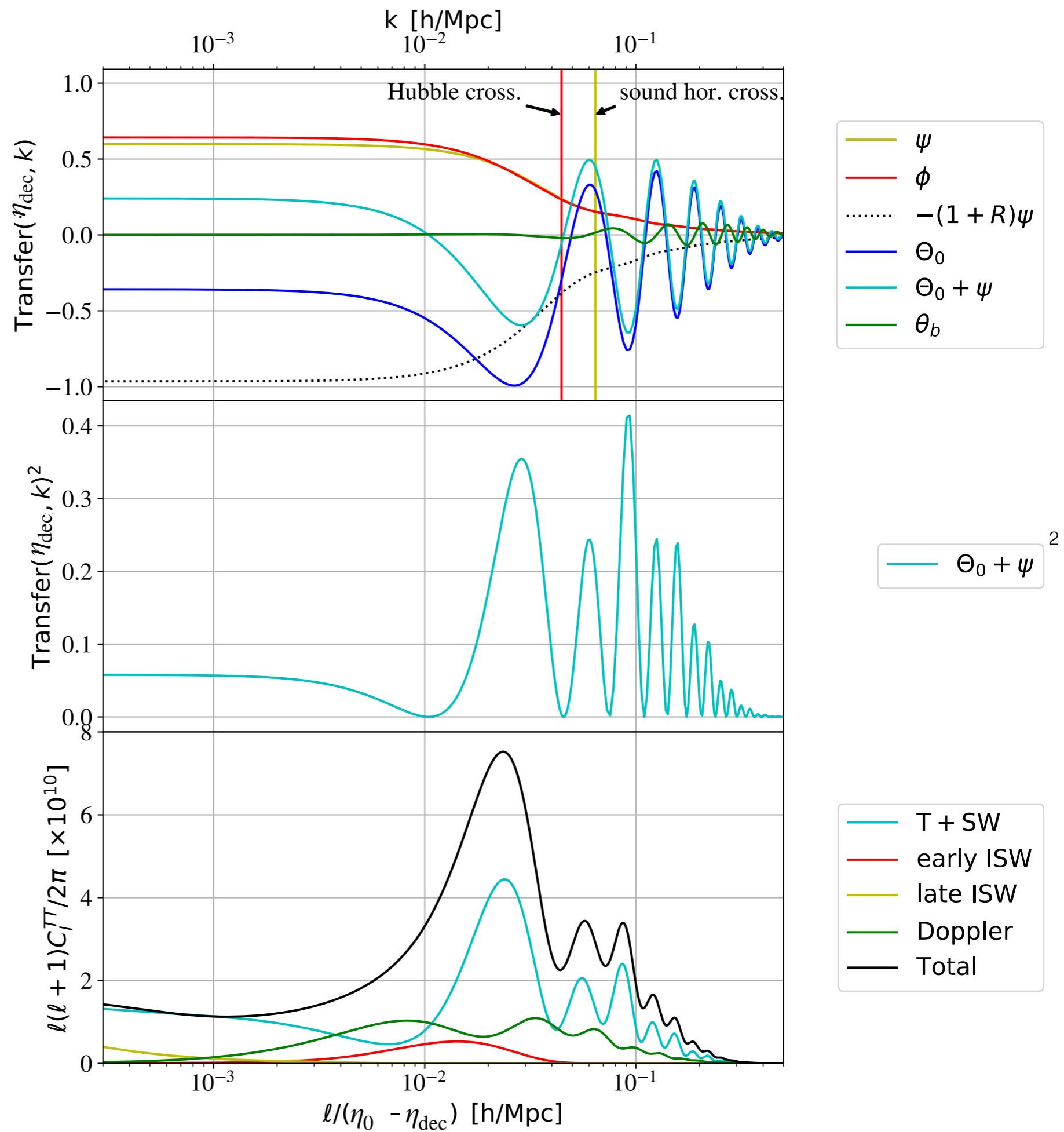
from transfer
to C_ℓ :



from transfer
to C_ℓ :



from transfer
to C_ℓ :

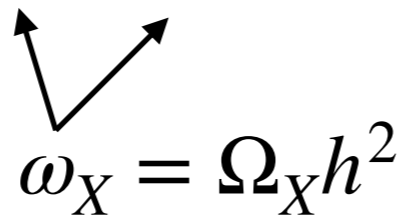


Λ CDM parameter effects on temperature spectrum

Why can we measure 6 Λ CDM parameters independently with CMB?

- Flat FLRW ($\Omega_k = 0$),
- Cosmological constant ($w = -1$),
- Plain decoupled / stable / cold dark matter,
- Neutrino mass neglected or fixed to minimal value,
- $N_{\text{eff}} = 3.044$,
- Power-law primordial spectrum...

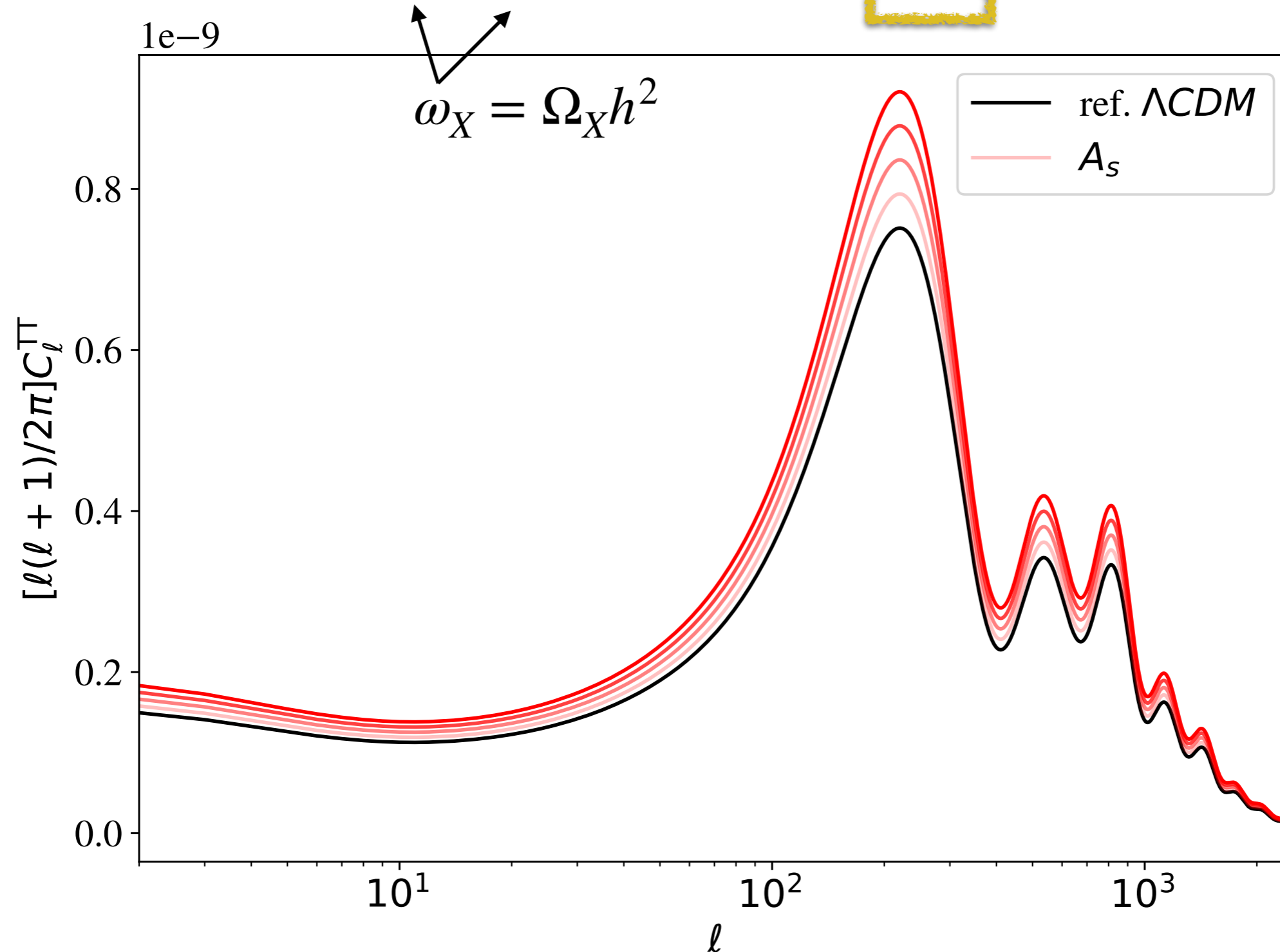
Possible basis: $\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$


$$\omega_X = \Omega_X h^2$$



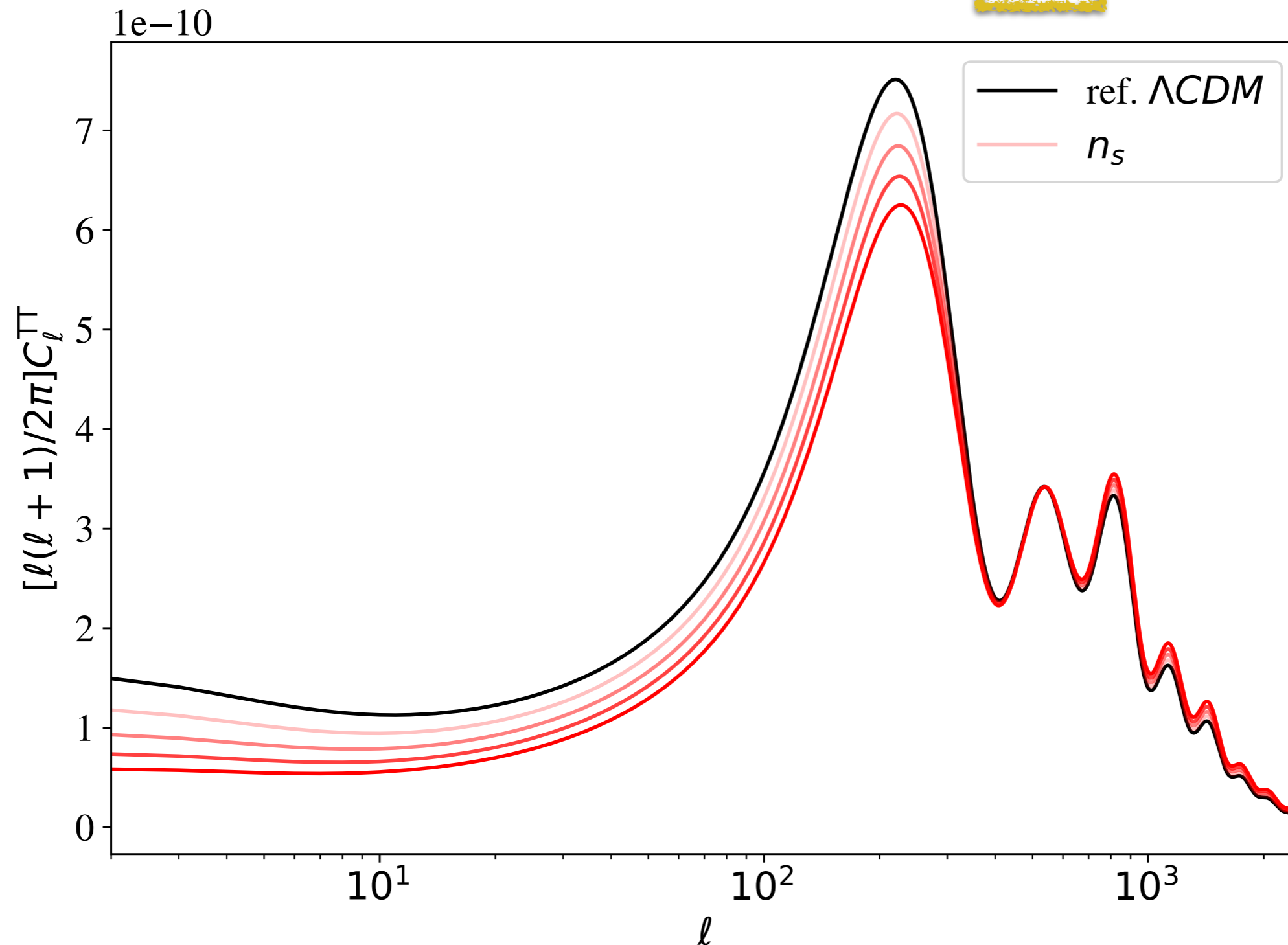
parameter of CMB, not of LSS

$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$



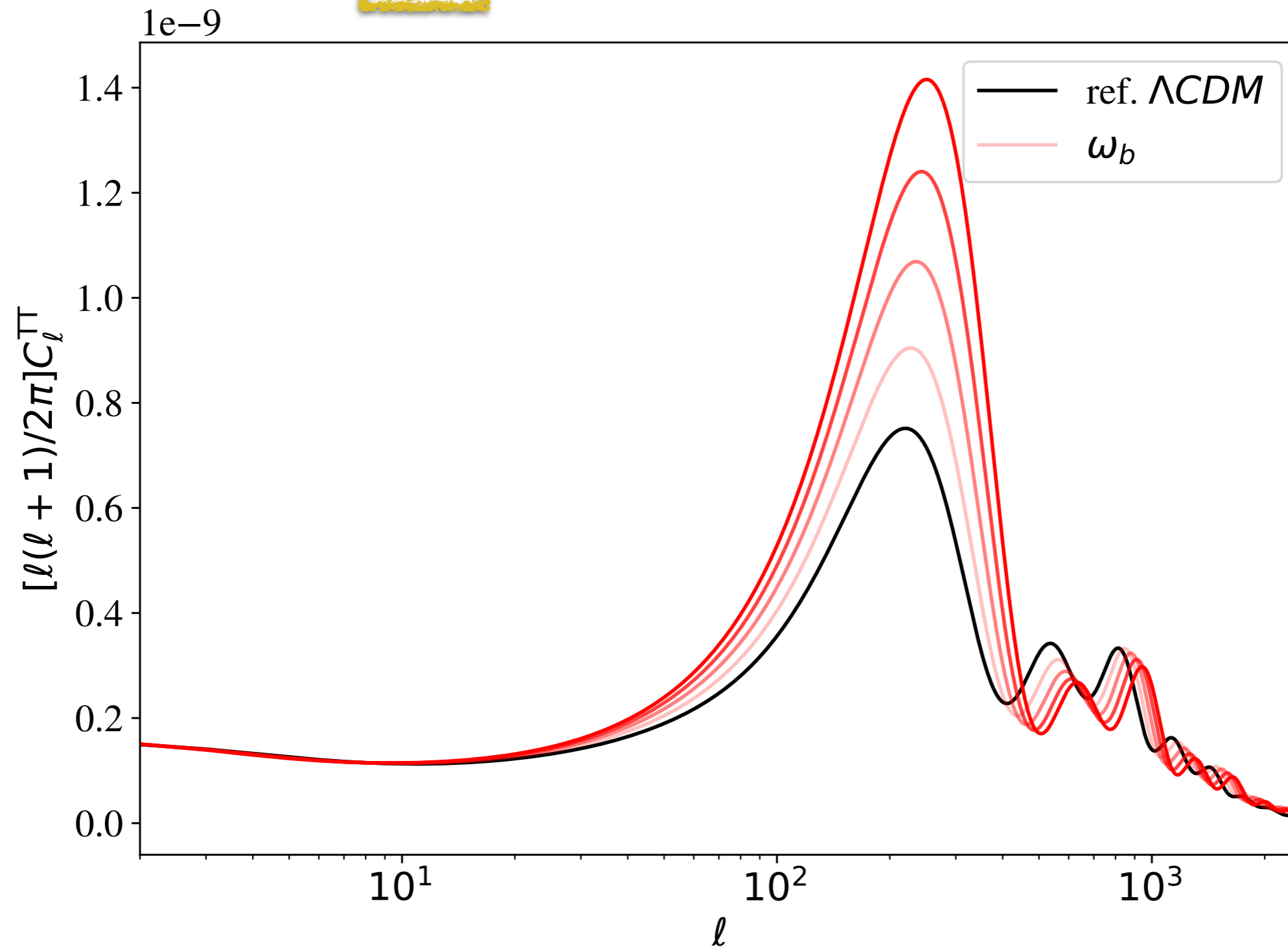
$$C_l^{XY} = 4\pi \int dk \, k^2 \Delta_l^X(k) \Delta_l^Y(k) \mathcal{P}_{\mathcal{R}}(k) \quad \mathcal{P}_{\mathcal{R}}(k) = A_s(k_*) \left(\frac{k}{k_*} \right)^{n_s-1}$$

$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$

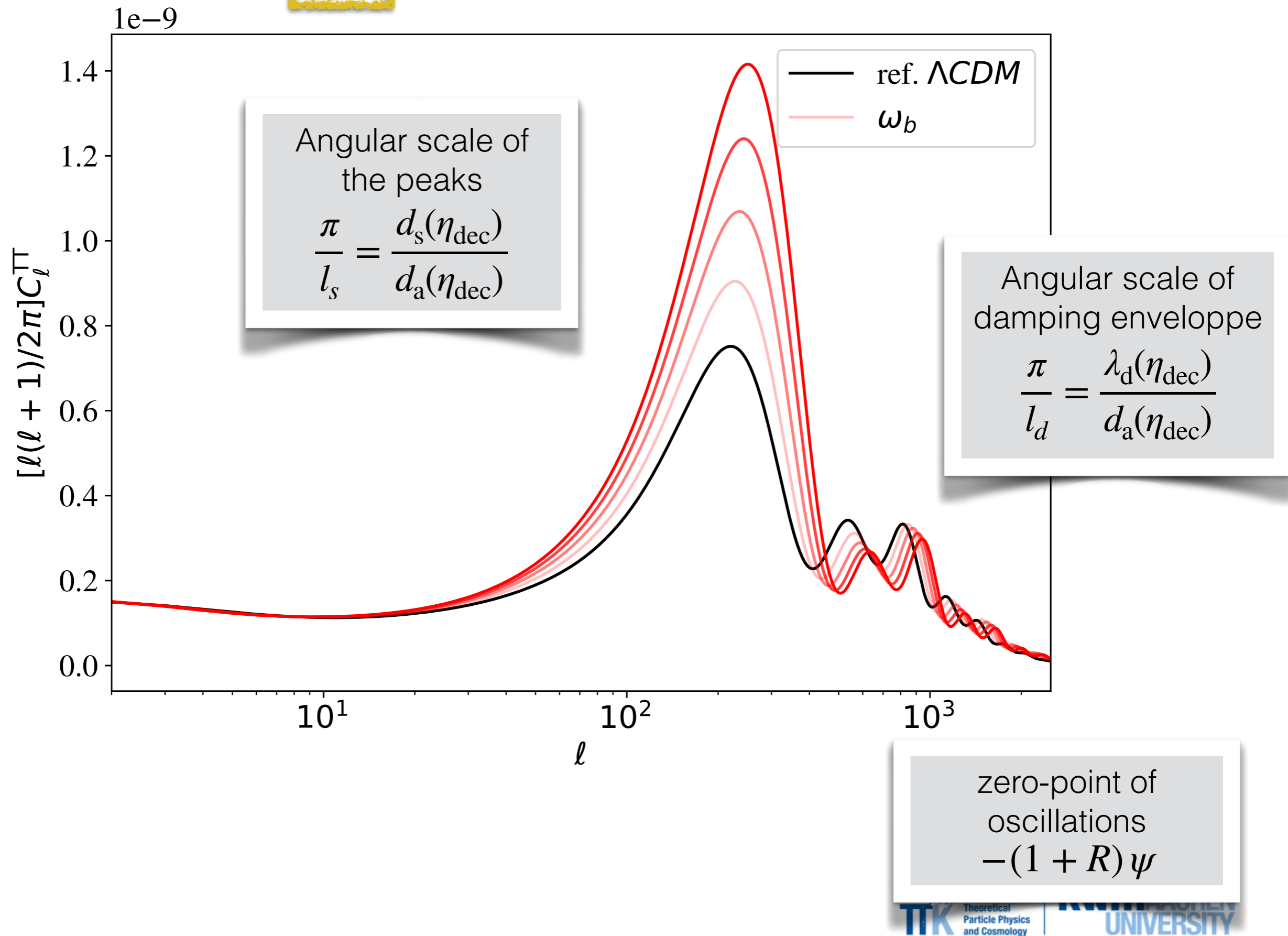


$$C_l^{XY} = 4\pi \int dk \, k^2 \Delta_l^X(k) \Delta_l^Y(k) \mathcal{P}_{\mathcal{R}}(k) \quad \mathcal{P}_{\mathcal{R}}(k) = A_s(k_*) \left(\frac{k}{k_*} \right)^{n_s-1}$$

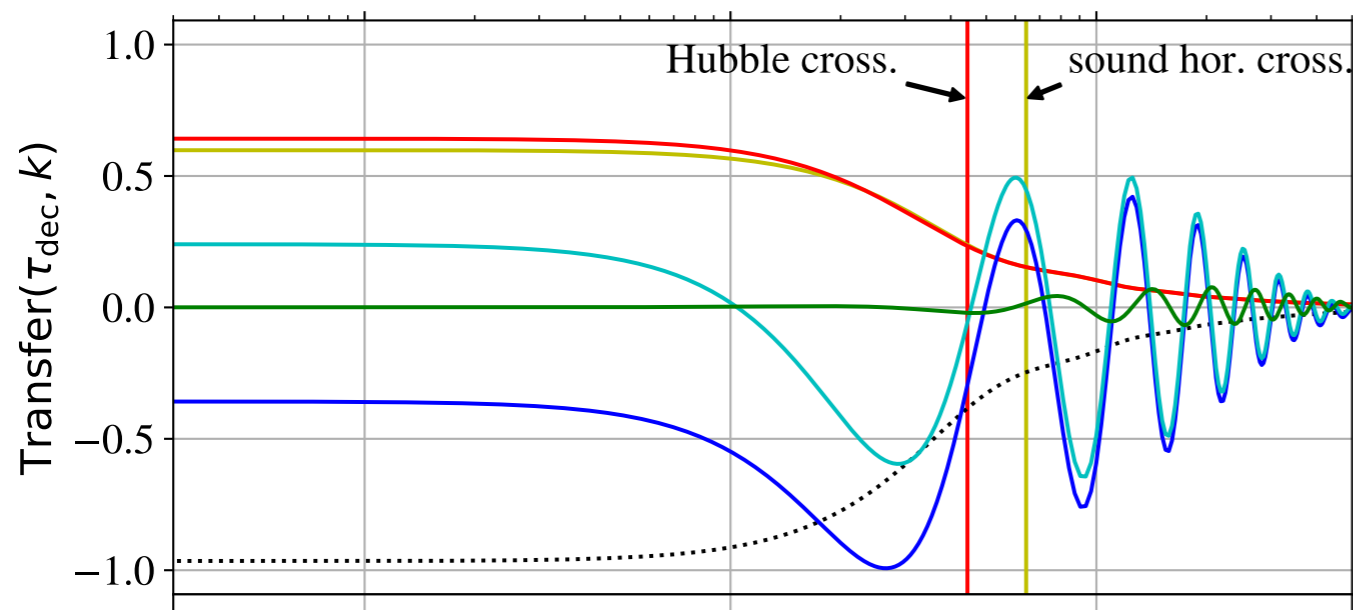
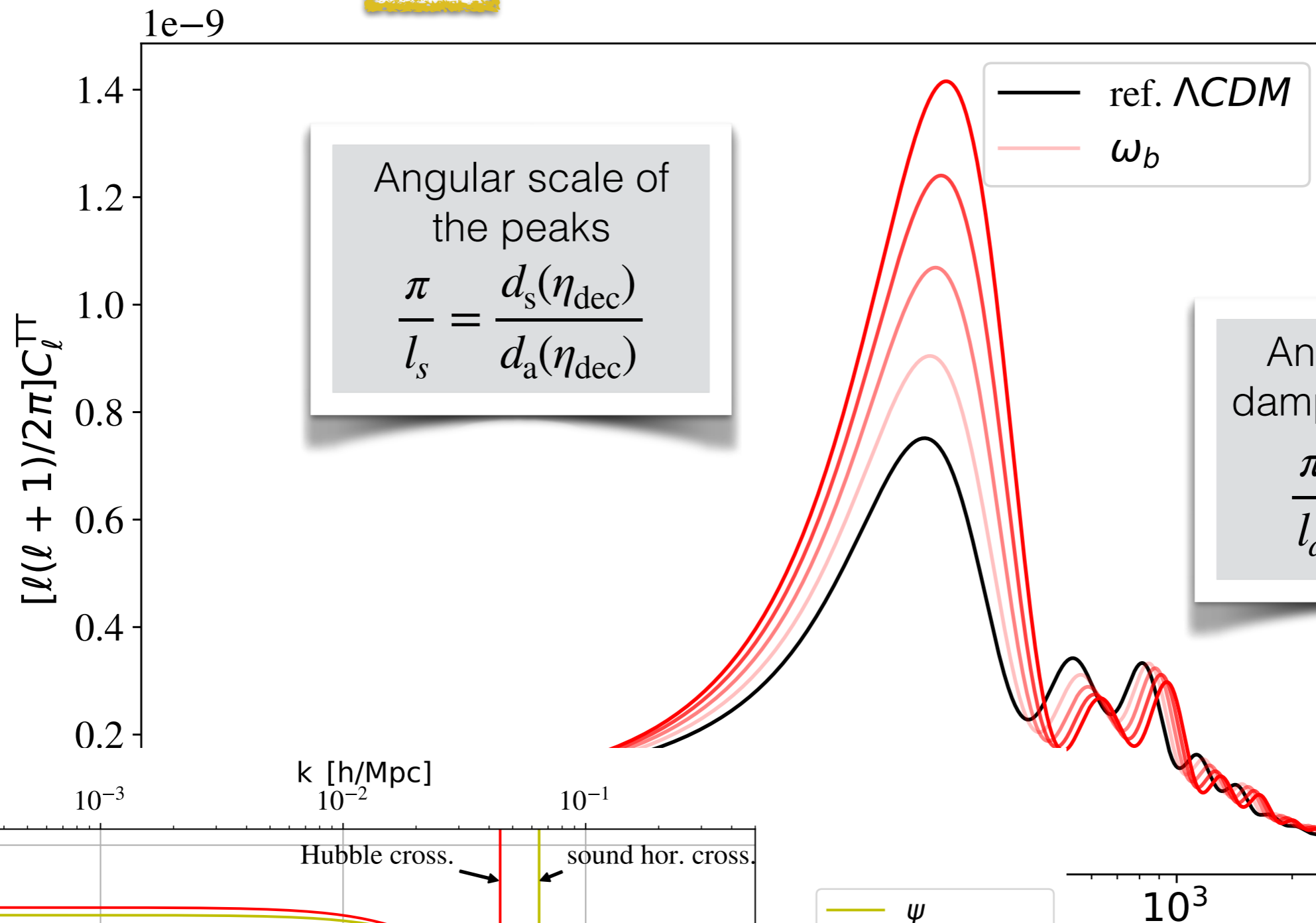
$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$



$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$



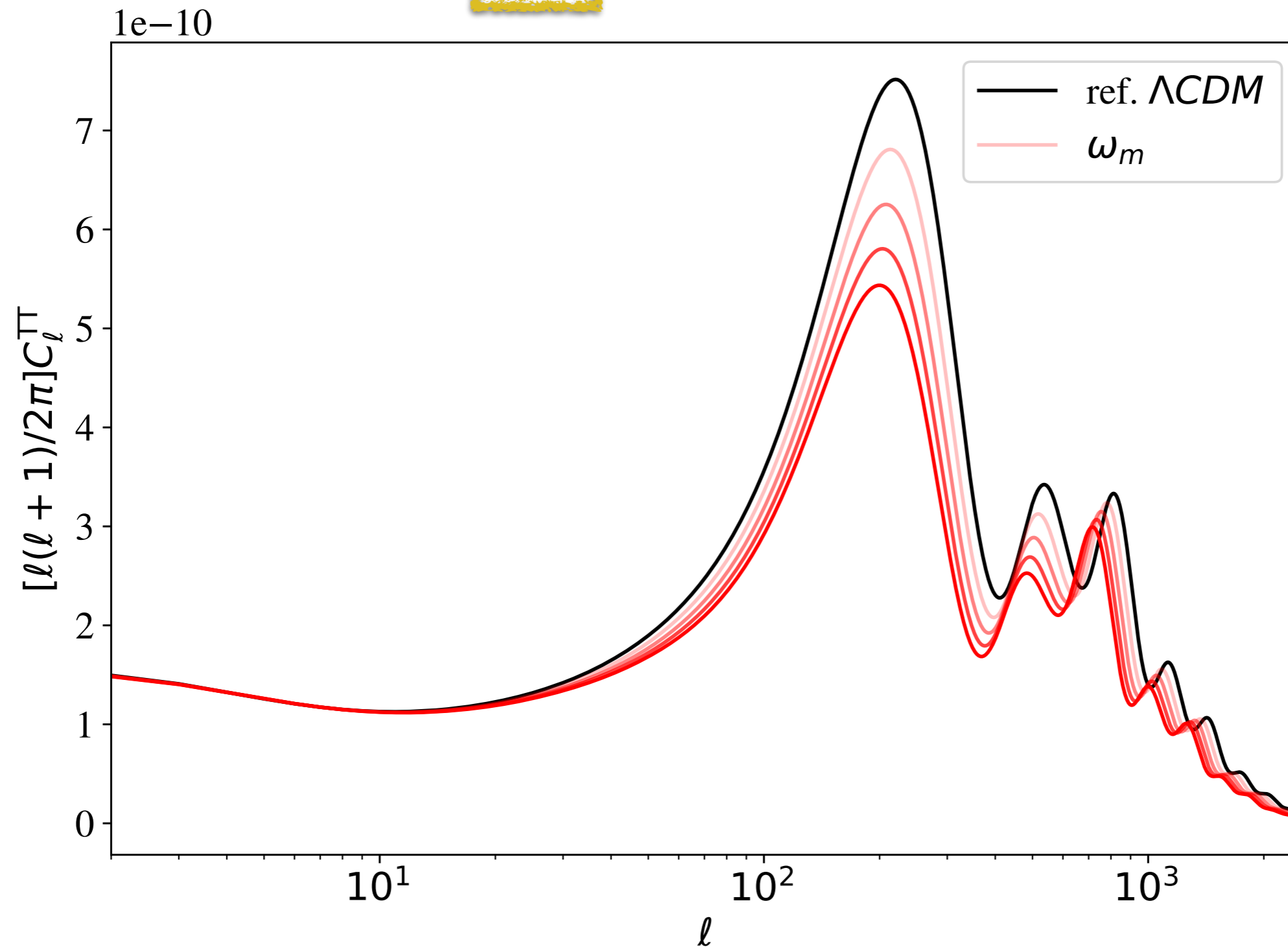
$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$



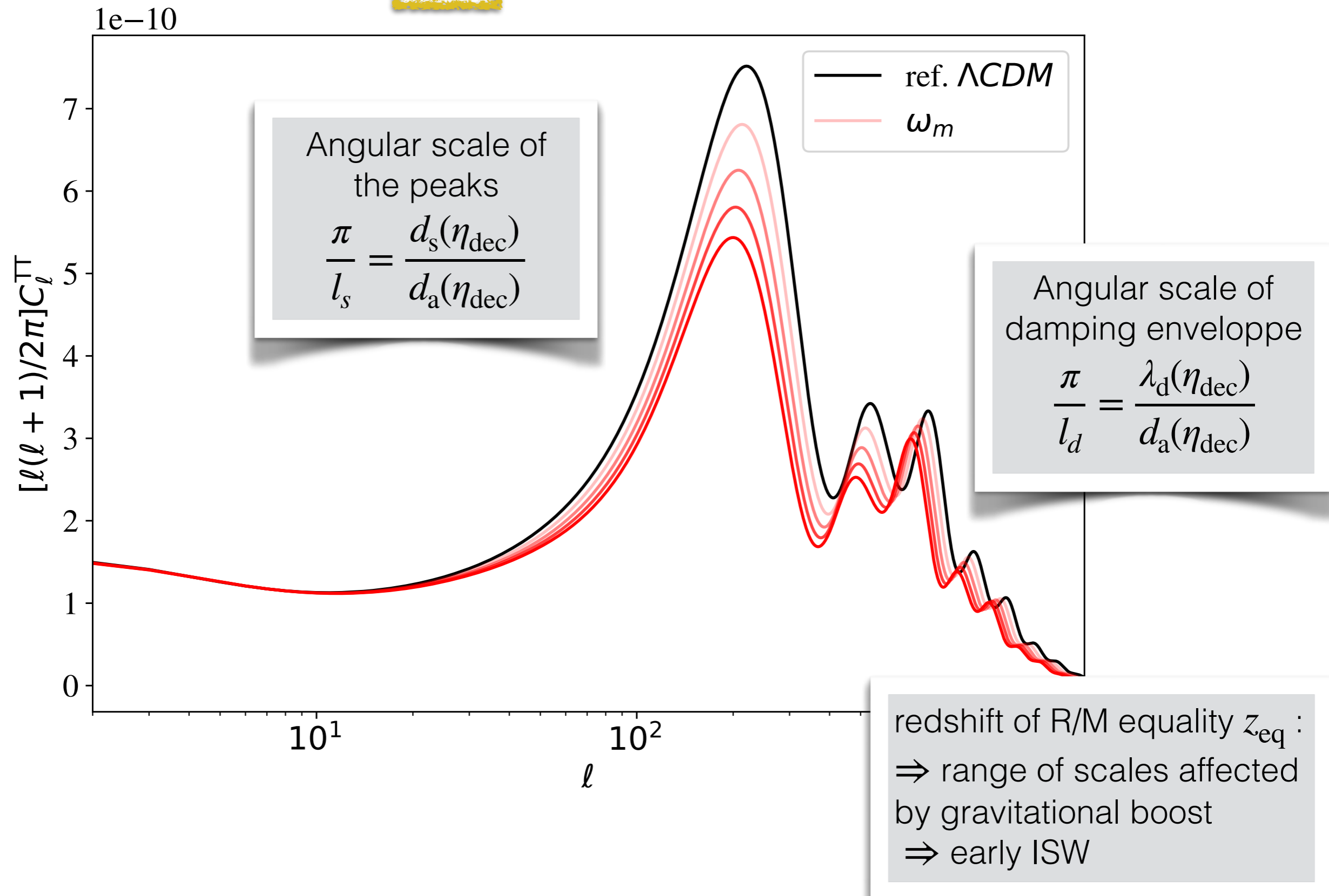
- ψ
- ϕ
- $\cdots \cdots -(1+R)\psi$
- Θ_0
- $\Theta_0 + \psi$
- θ_b

zero-point of oscillations
 $-(1+R)\psi$

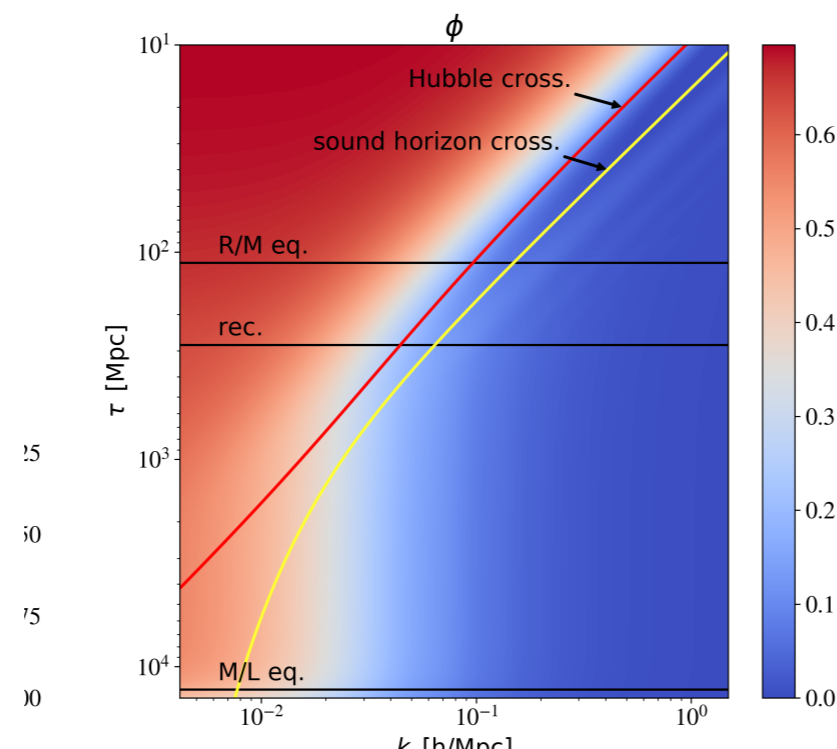
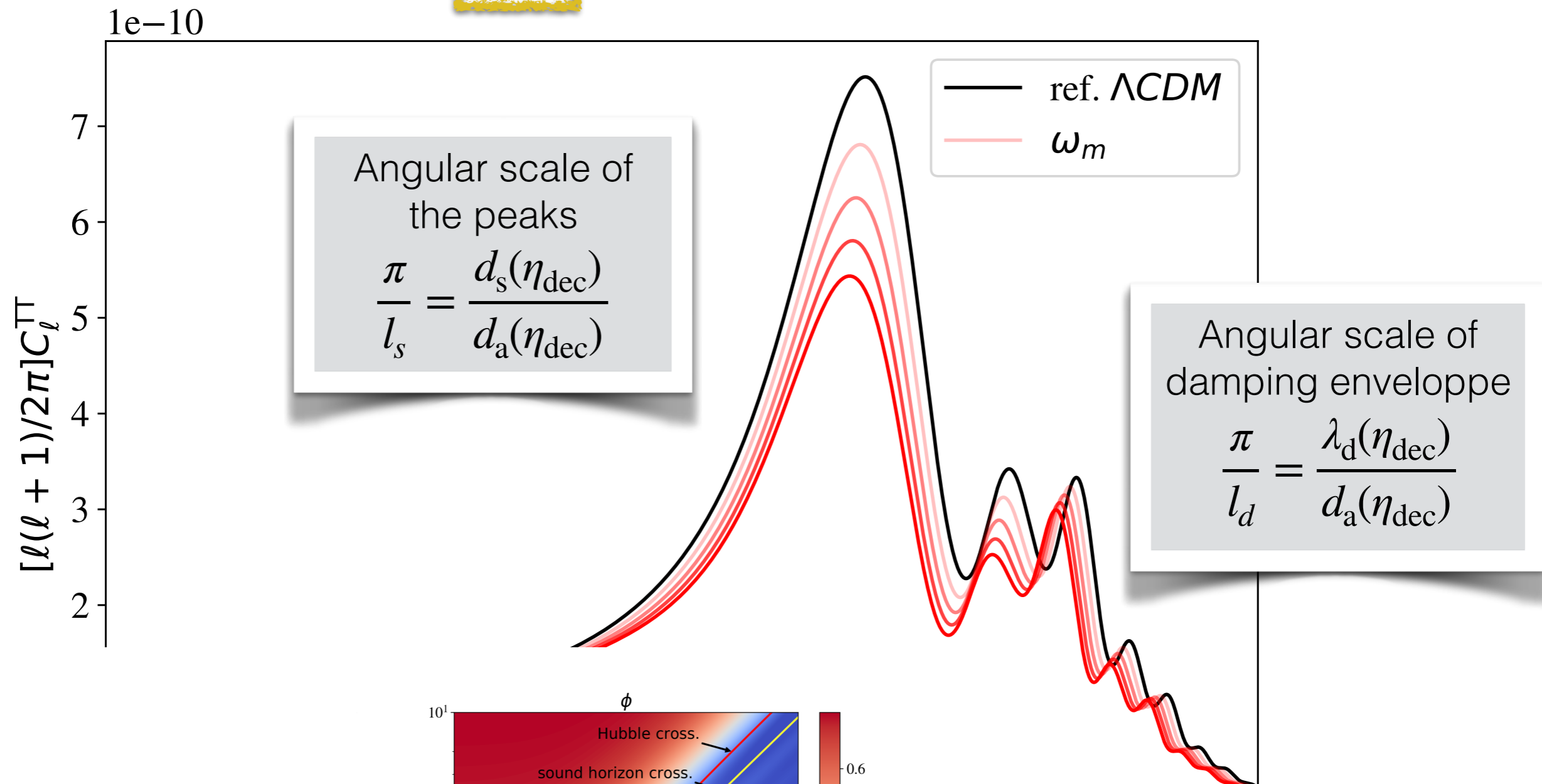
$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$



$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$

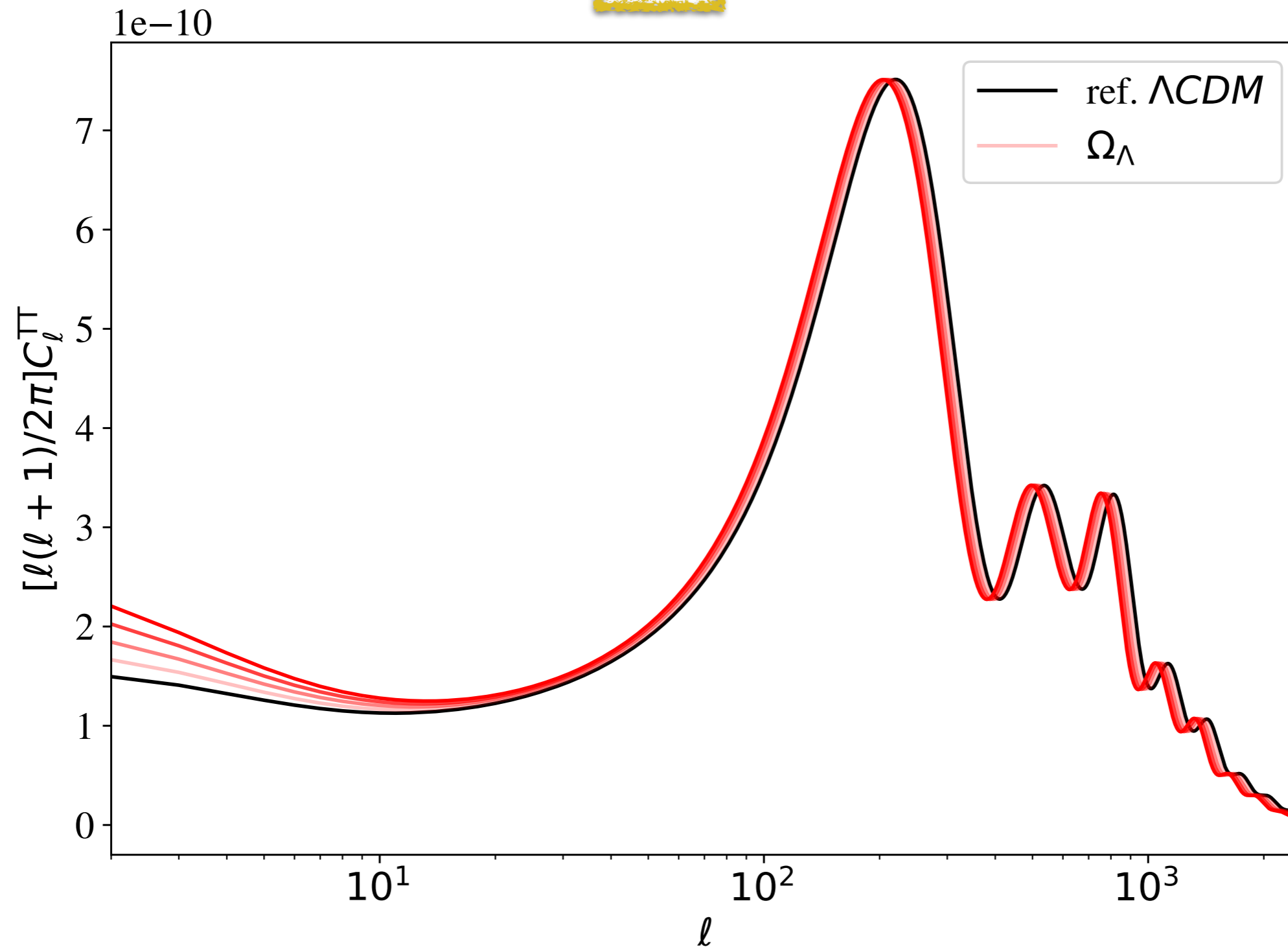


$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$

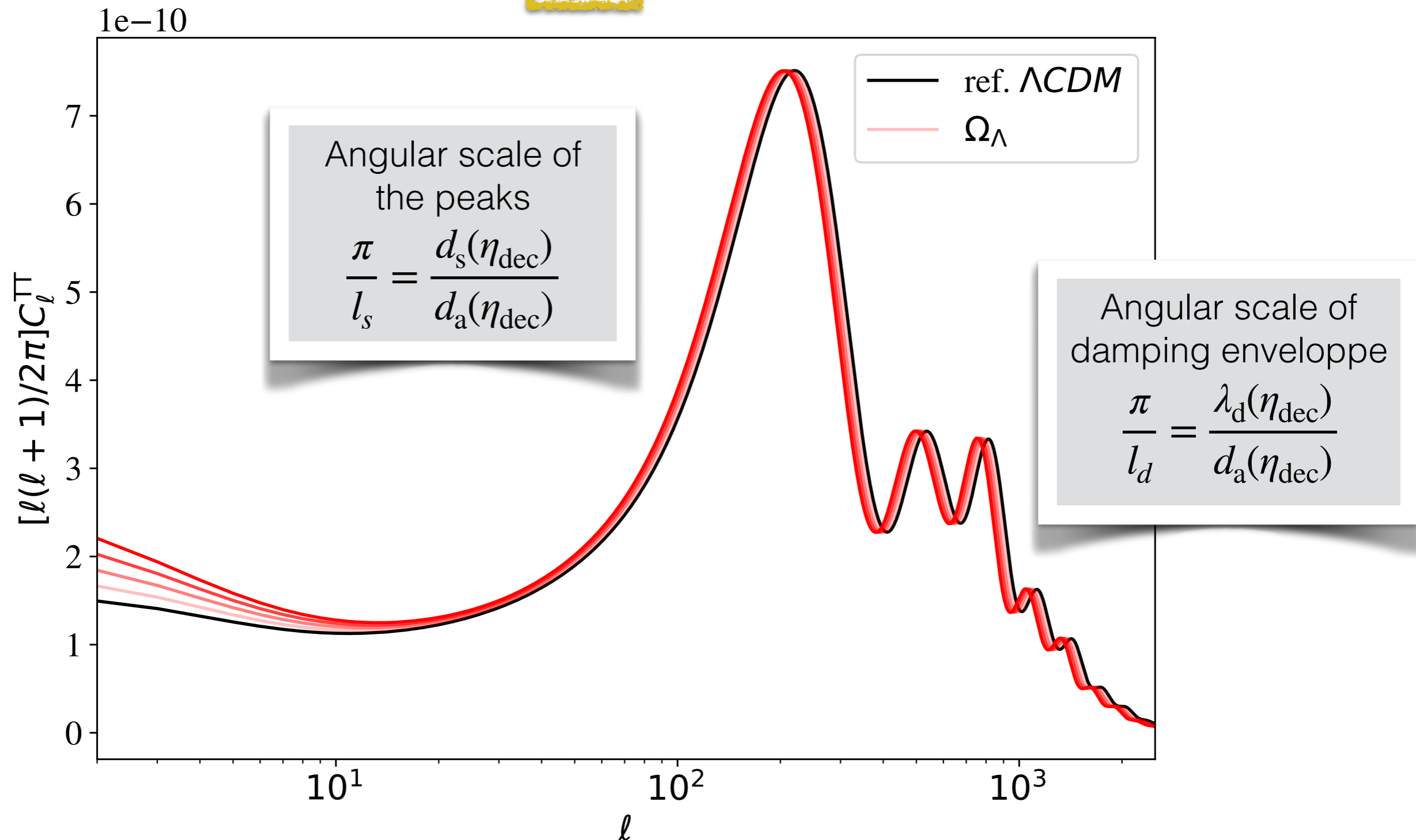


redshift of R/M equality z_{eq} :
 \Rightarrow range of scales affected
 by gravitational boost
 \Rightarrow early ISW

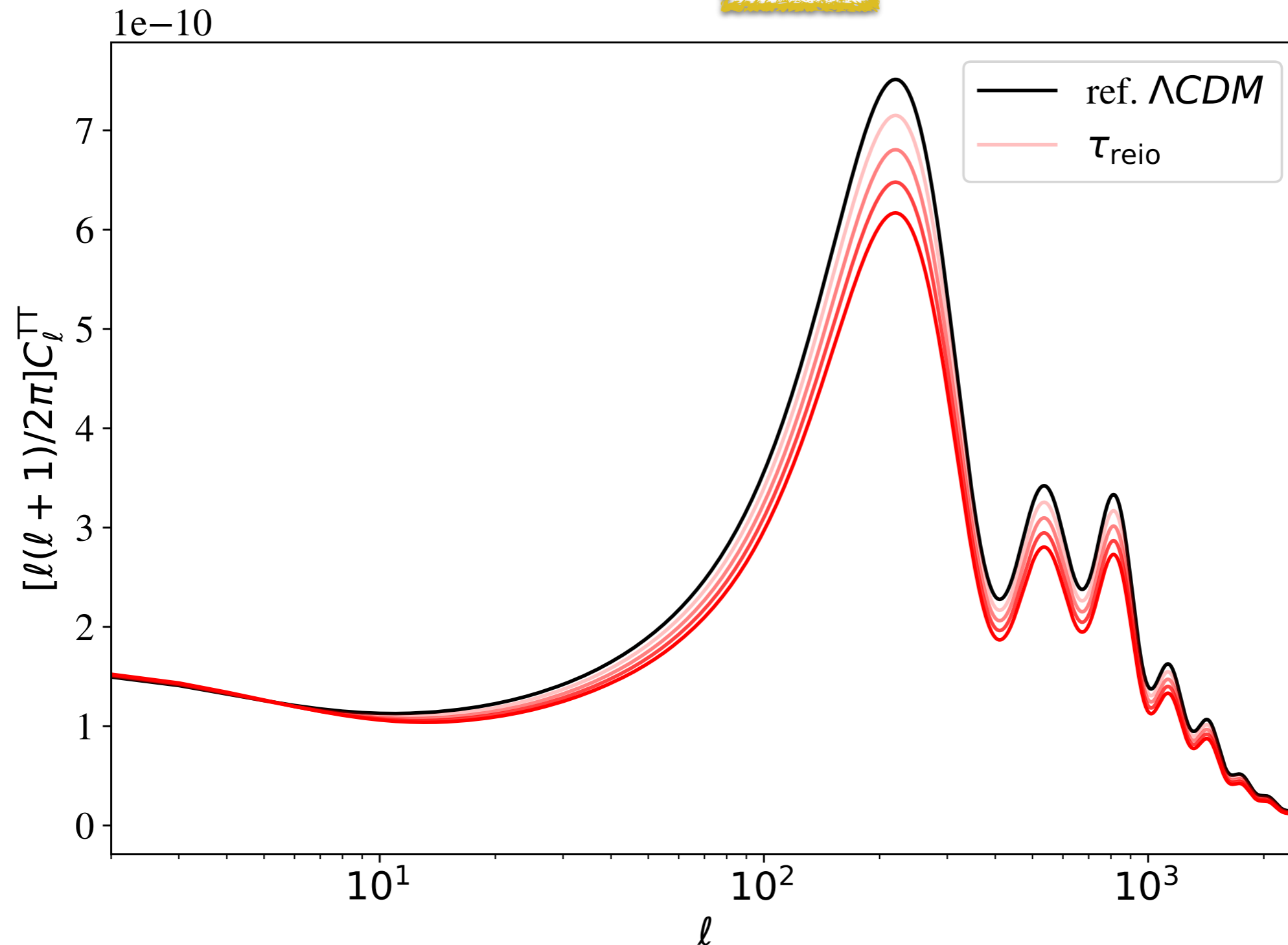
$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$



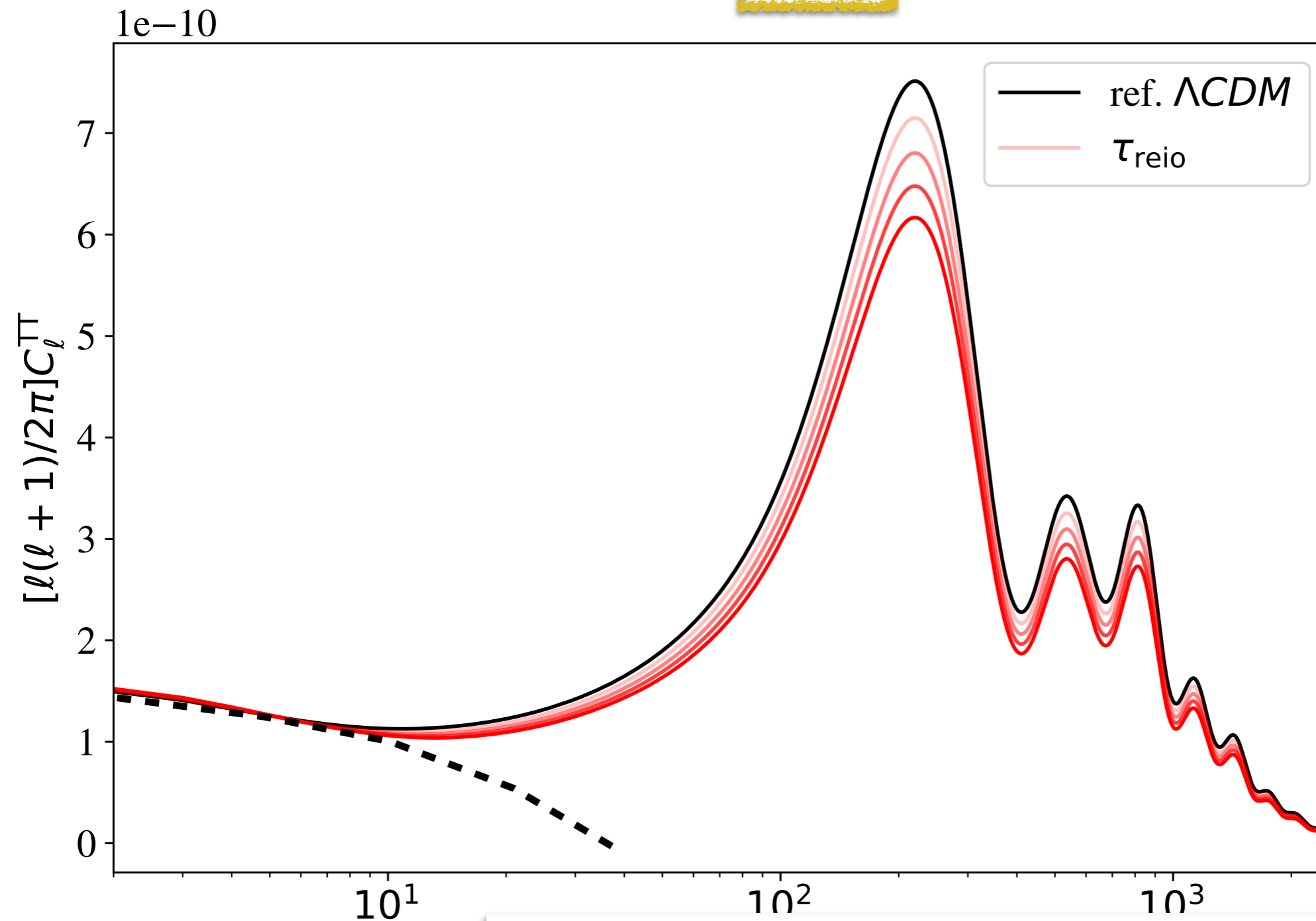
$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$



$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$



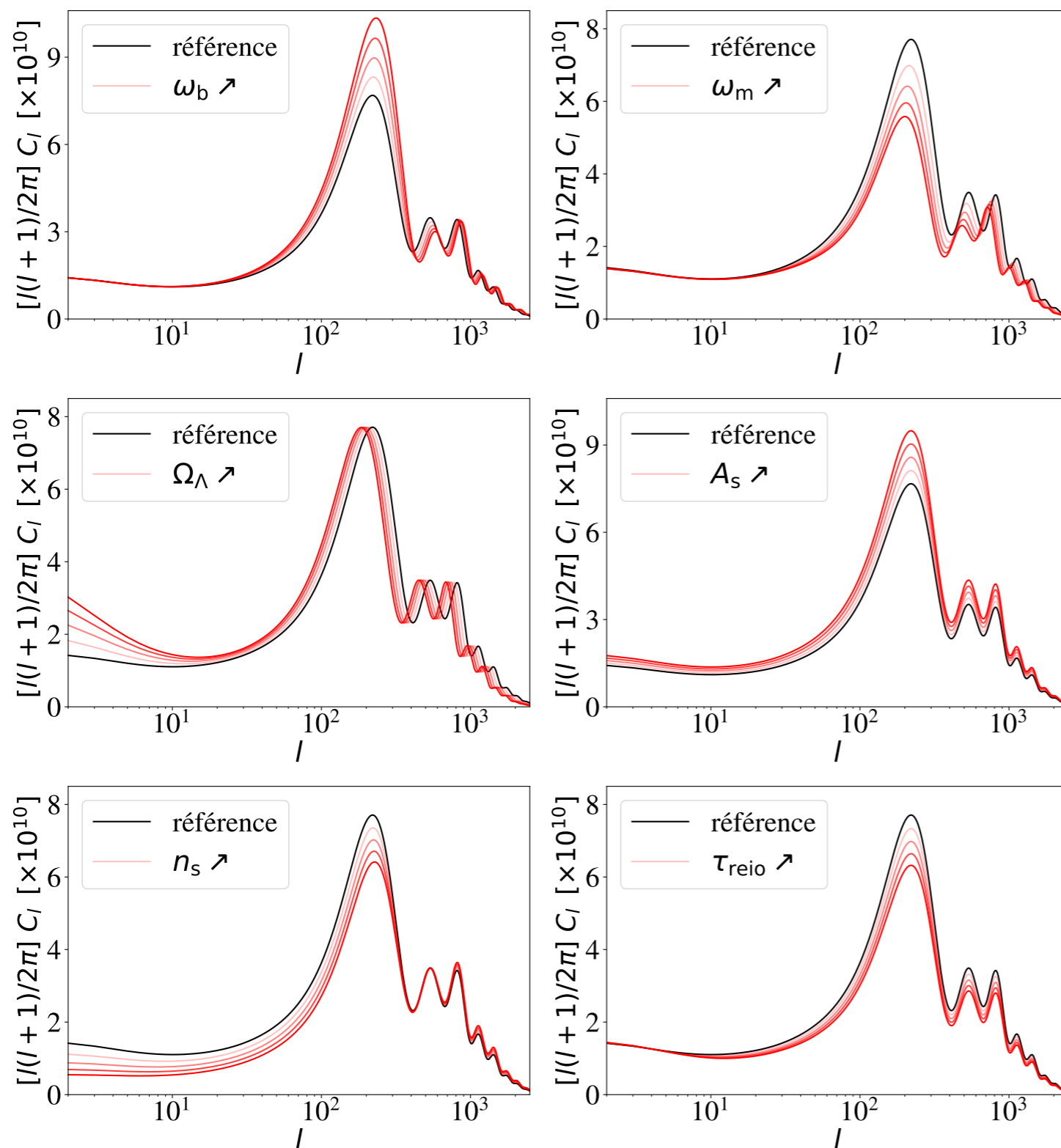
$$\{\omega_b, \omega_m, \Omega_\Lambda, \tau_{\text{reio}}, A_s, n_s\}$$



Visibility function
 $g(\eta) \simeq \delta(\eta - \eta_{\text{dec}})$

↓

$$g(\eta) \simeq e^{-\tau_{\text{reio}}} \delta(\eta - \eta_{\text{dec}}) + (1 - e^{-\tau_{\text{reio}}}) \delta(\eta - \eta_{\text{reio}})$$



8 physical governing C_l 's shape

- C1: angular scale of the peaks, θ_s
- C2: gravity/pressure at rec., R_{rec}
- C3: interval between z_{eq} and z_{dec}
- C4: angular scale of damping, θ_d
- C5: global amplitude
- C6: global tilt
- C7: plateau tilting by late ISW
- C8: reionisation steplike suppression

but all tight to 6 parameters in Λ CDM

Extended cosmologies? ... more parameters ... but also more effects ...