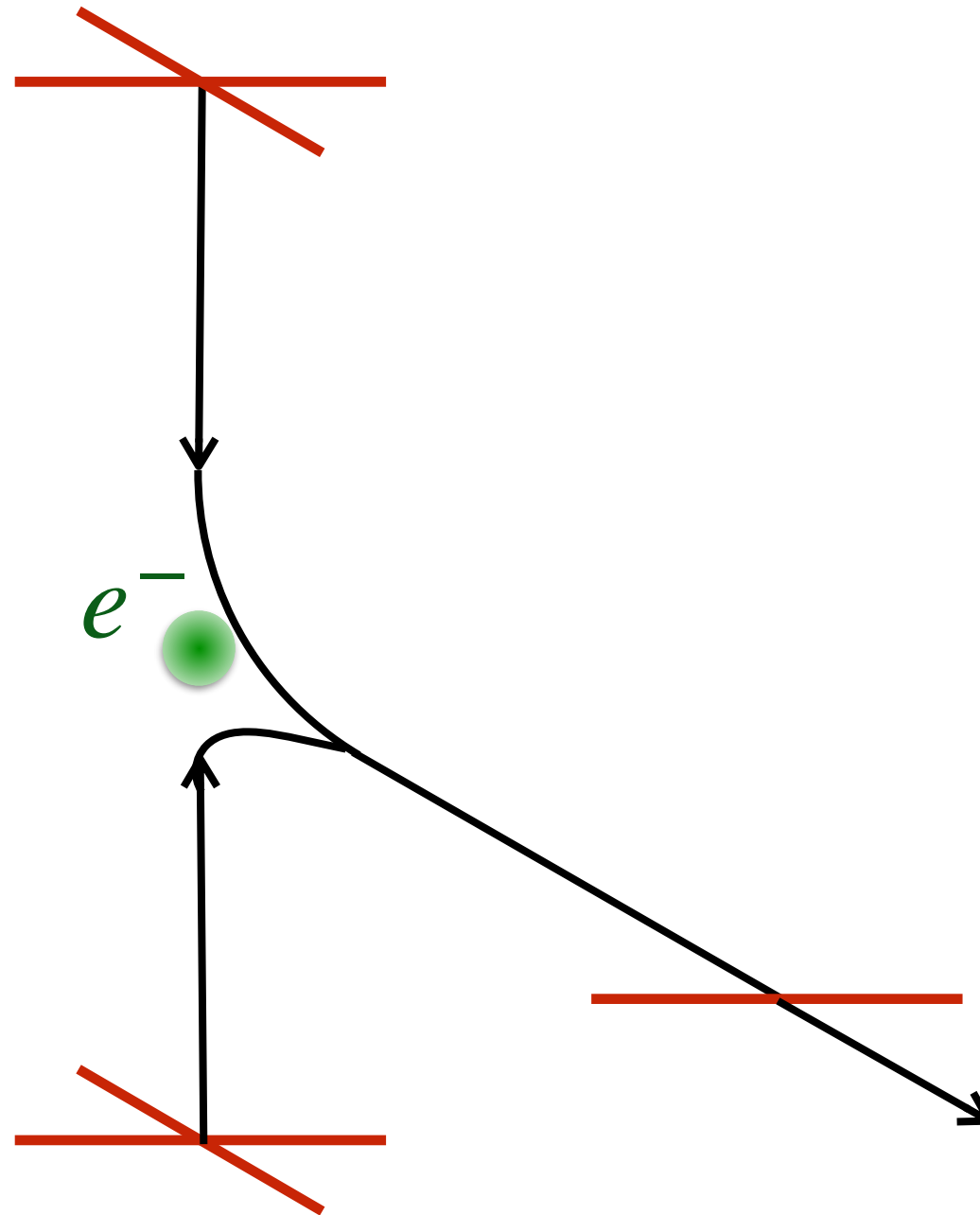


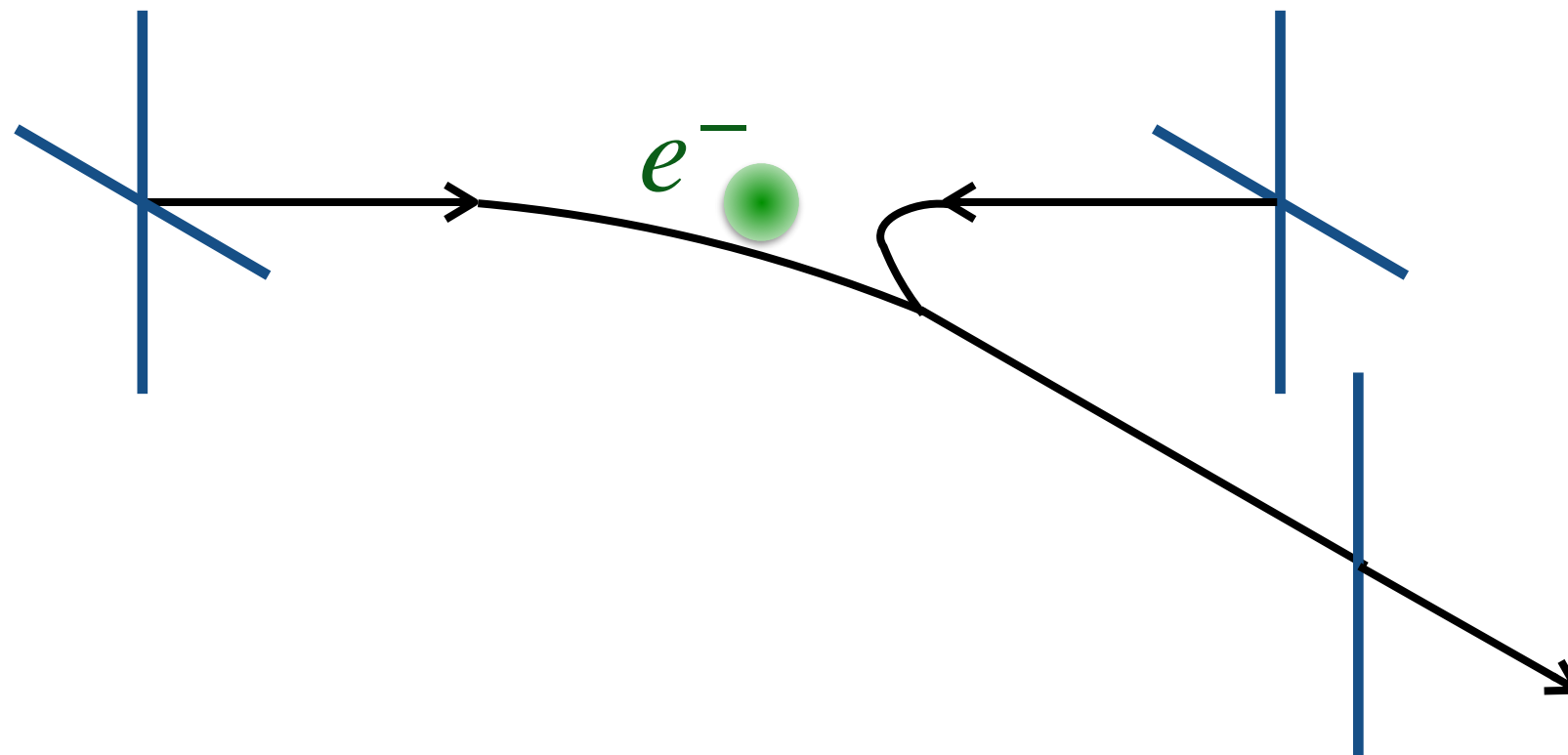
# CMB polarisation

# CMB polarisation

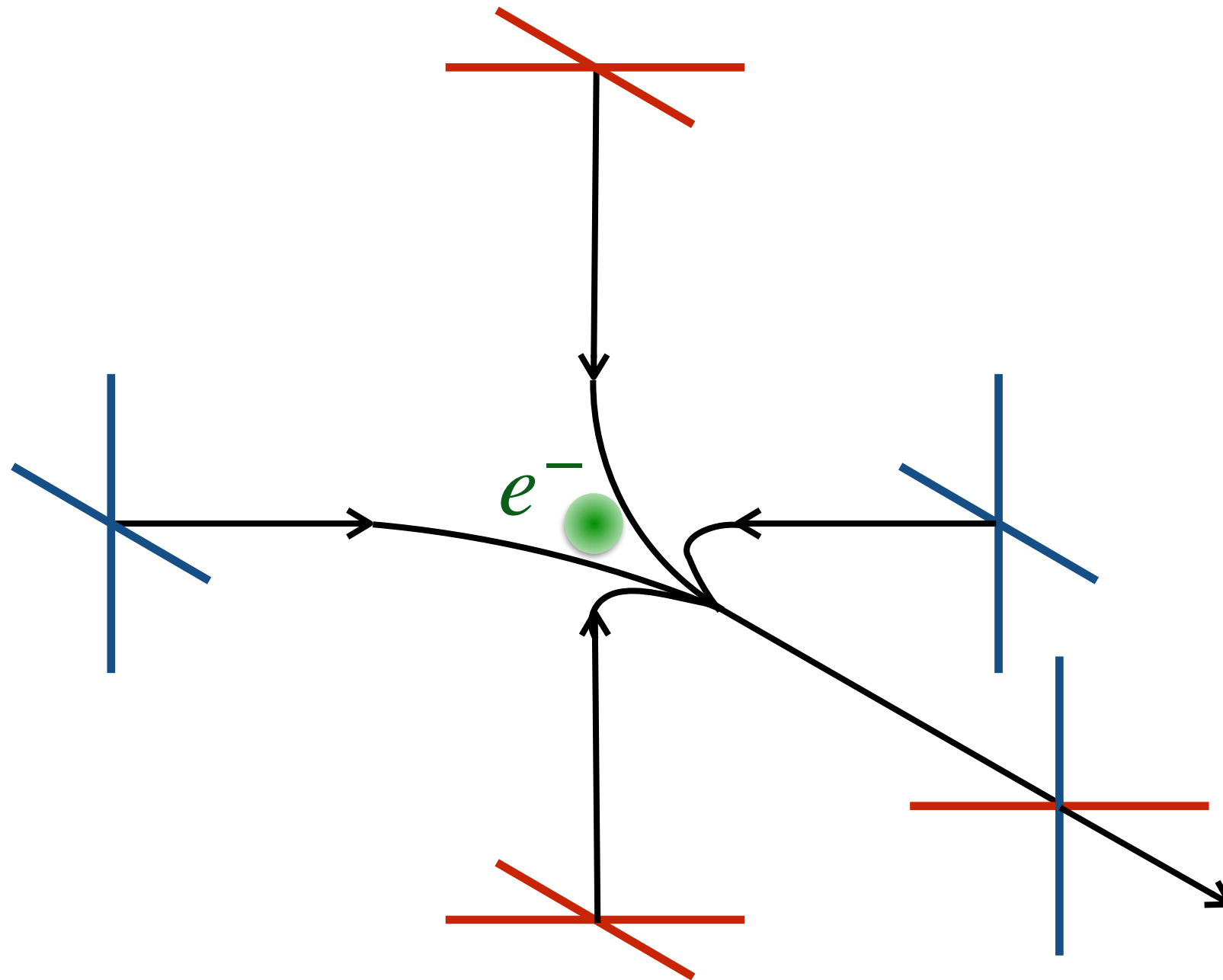




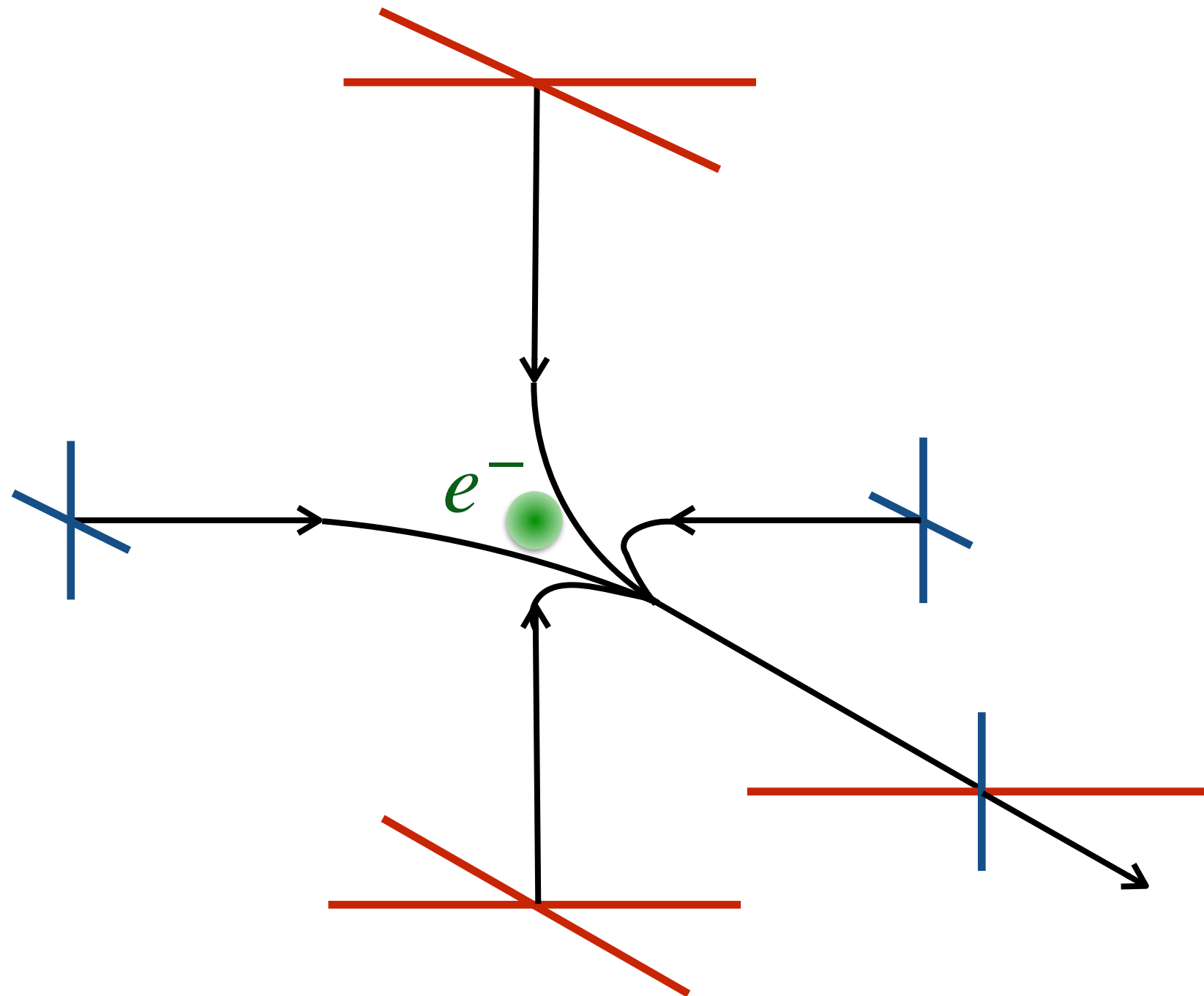
# CMB polarisation



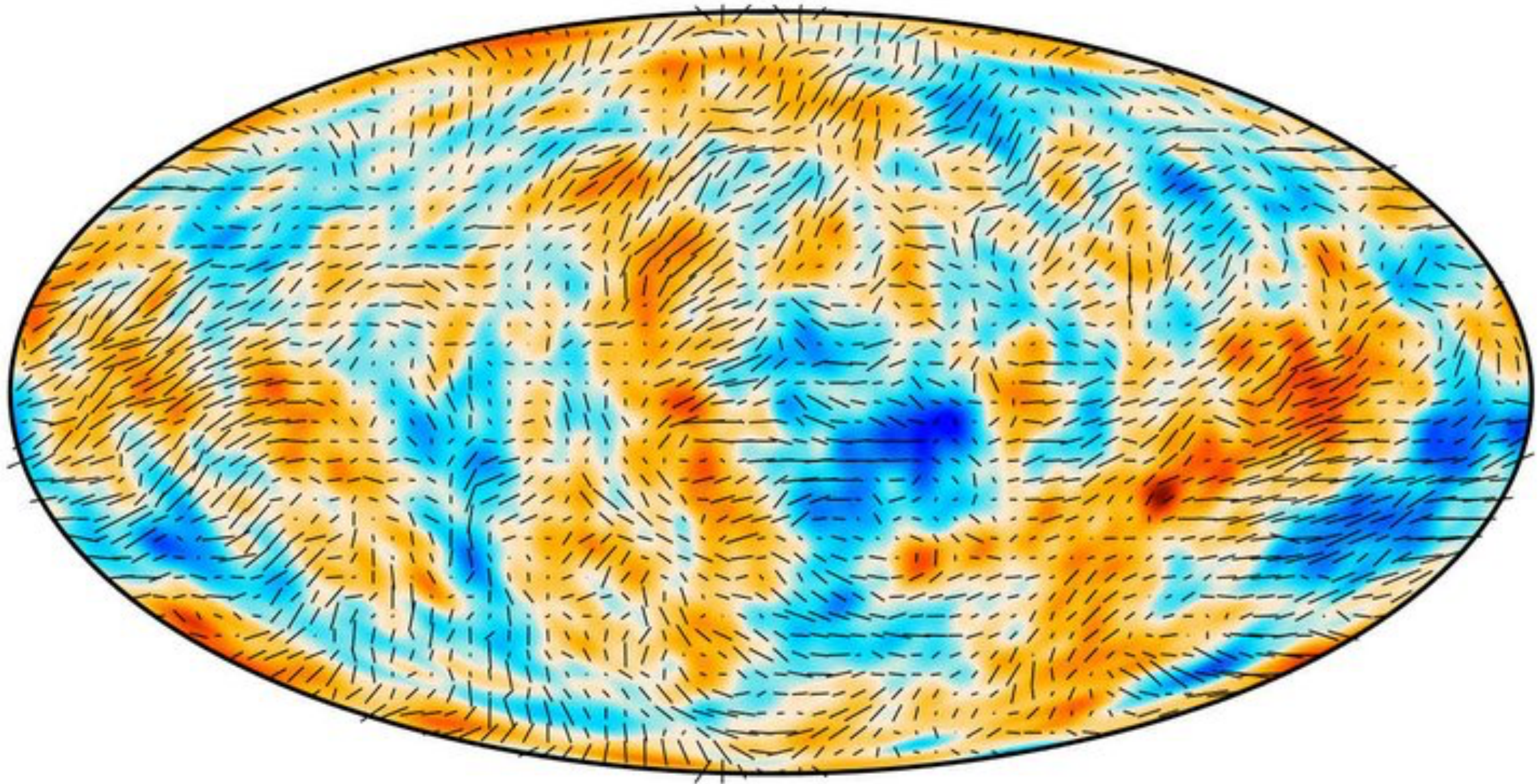
# CMB polarisation



# CMB polarisation

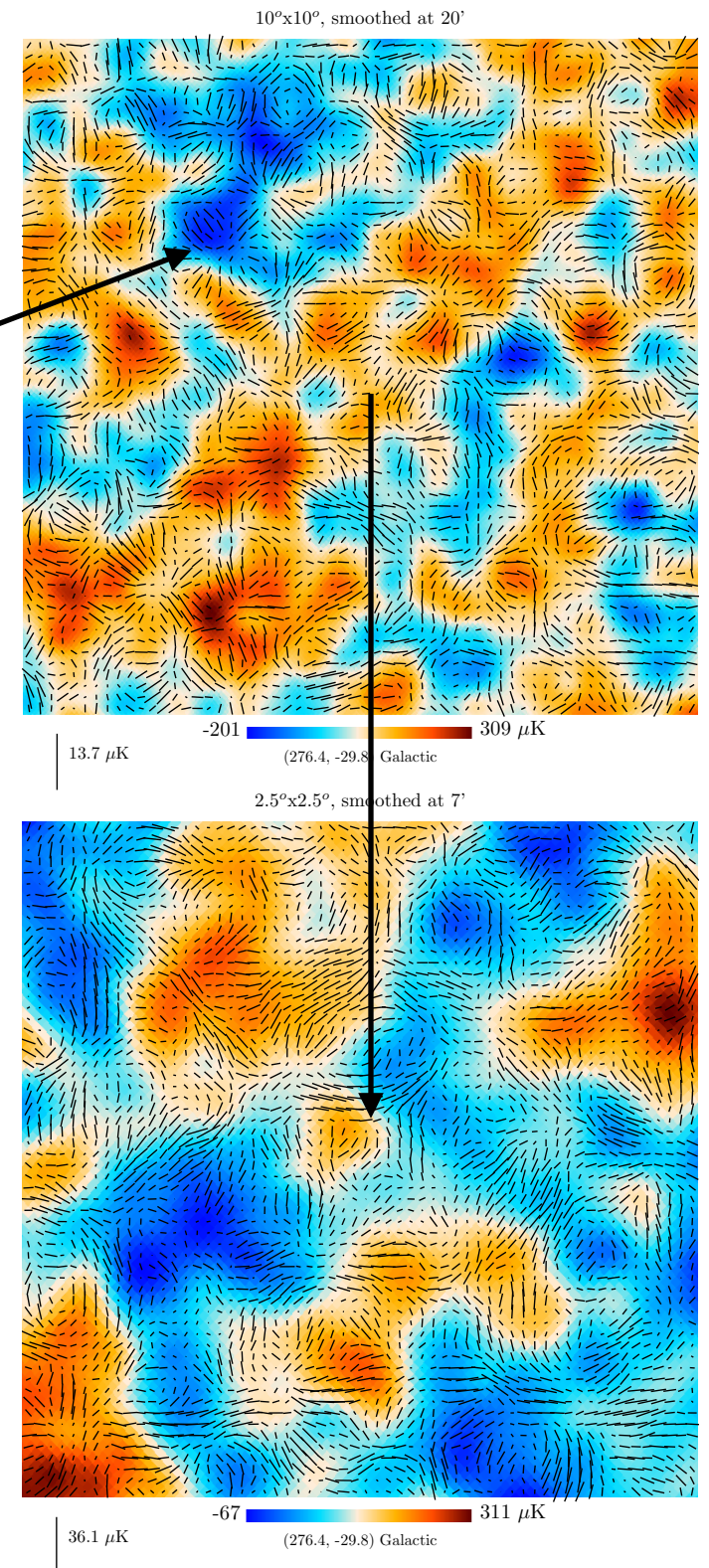
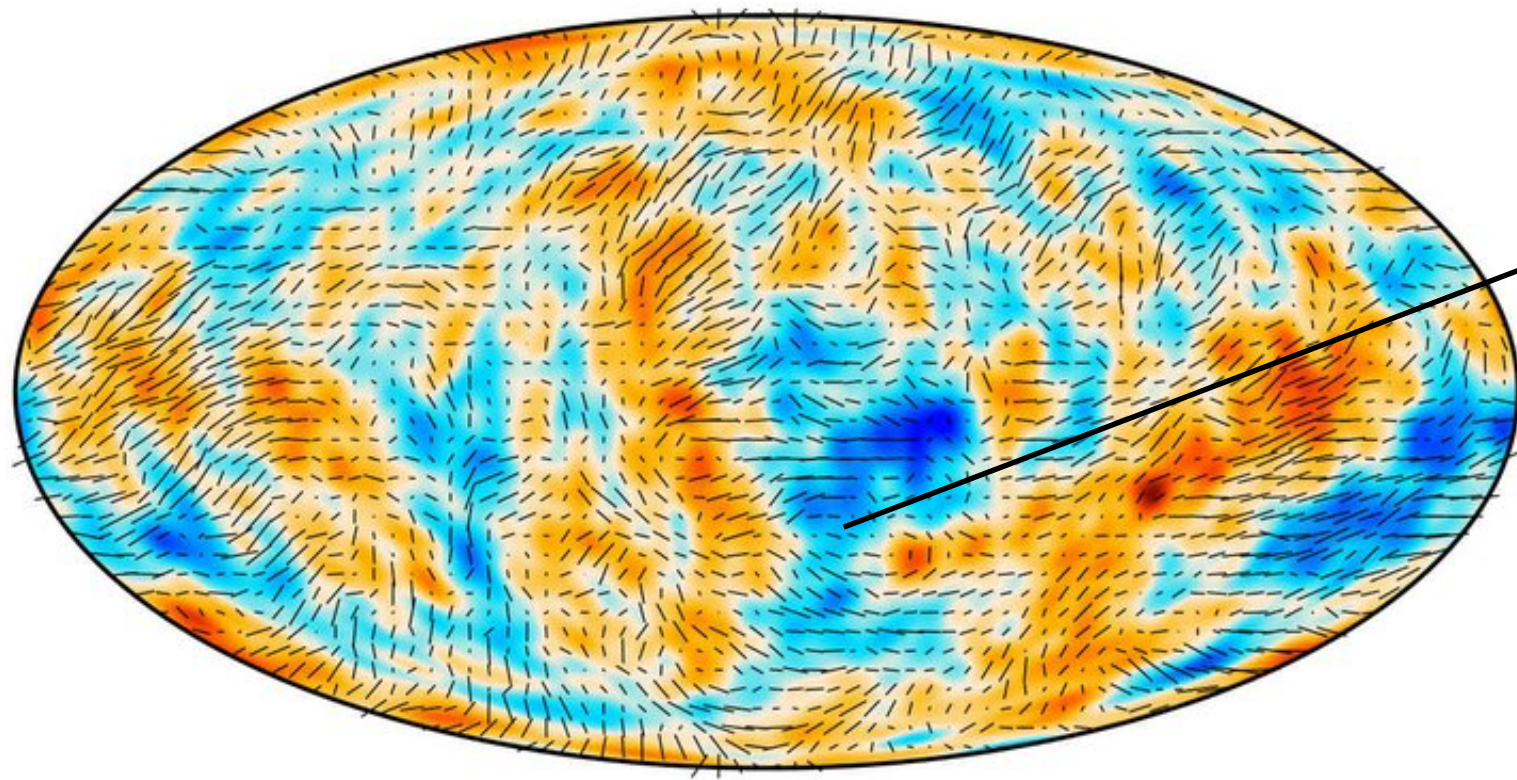


# CMB polarisation



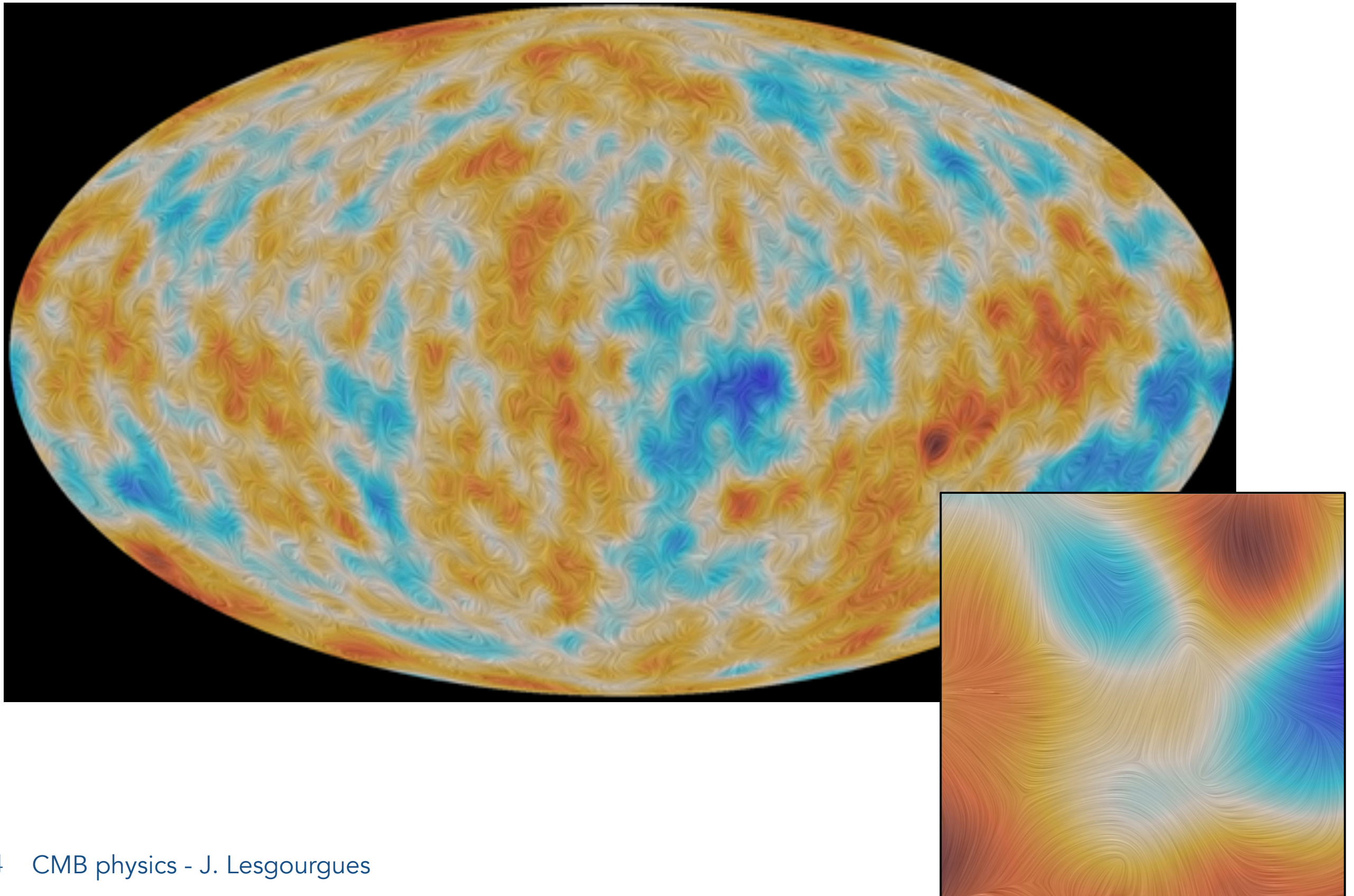


# CMB polarisation



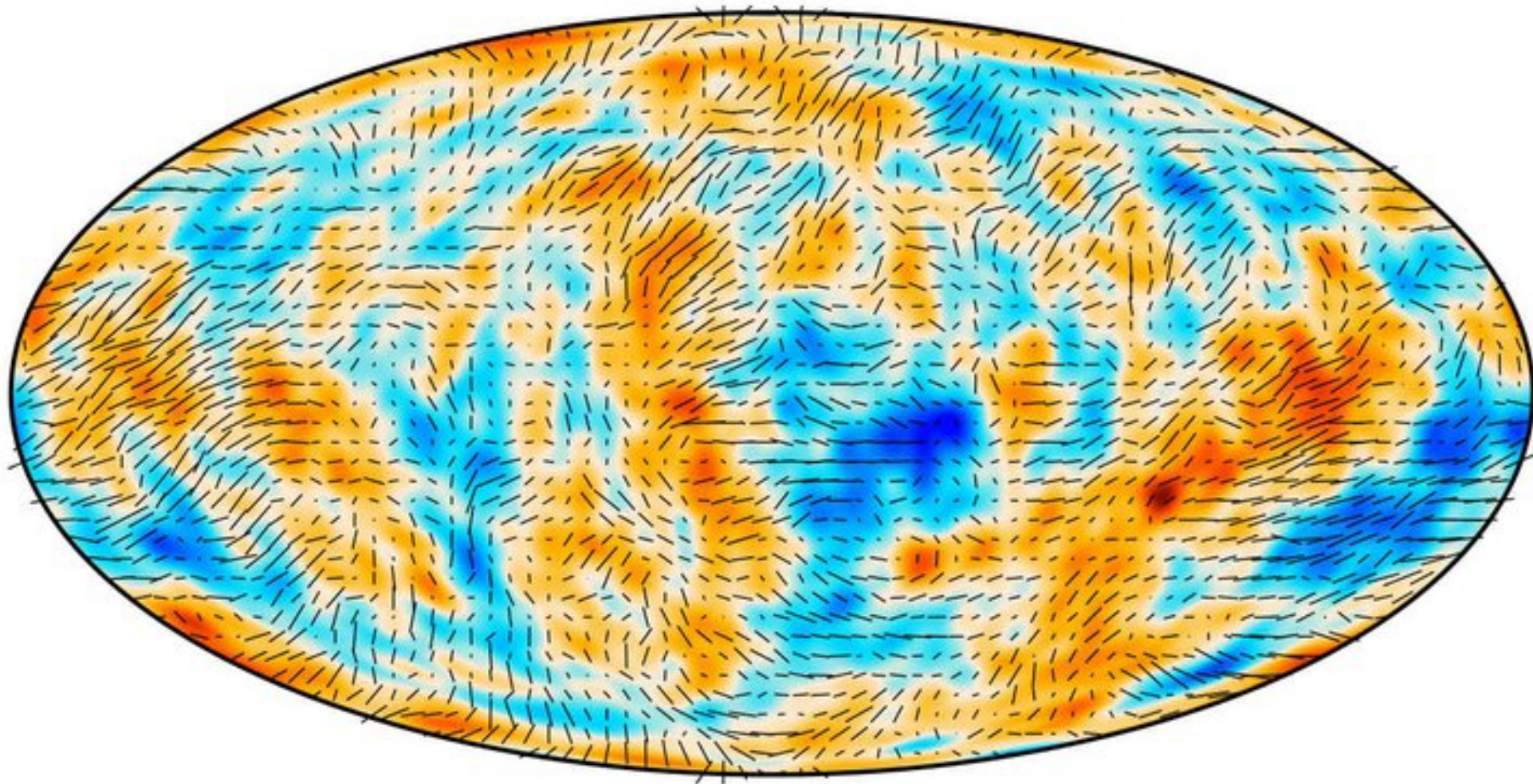


# CMB polarisation



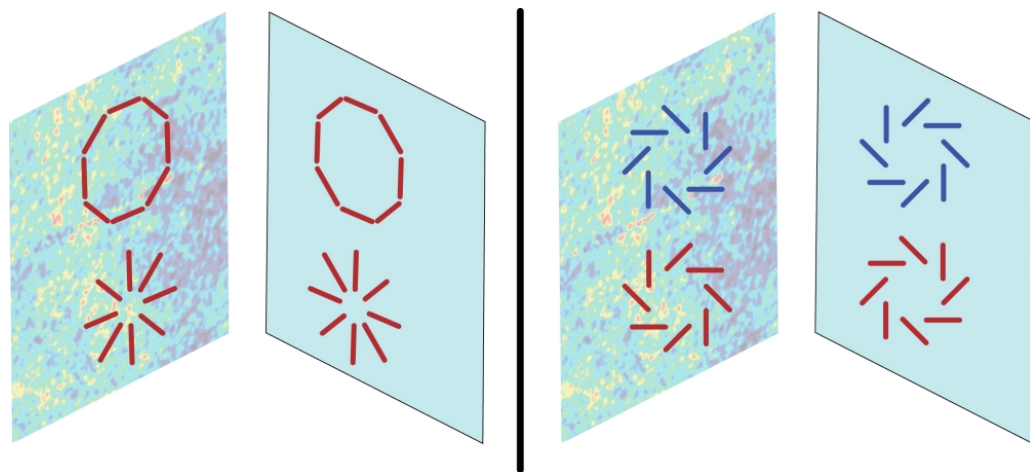


# CMB polarisation

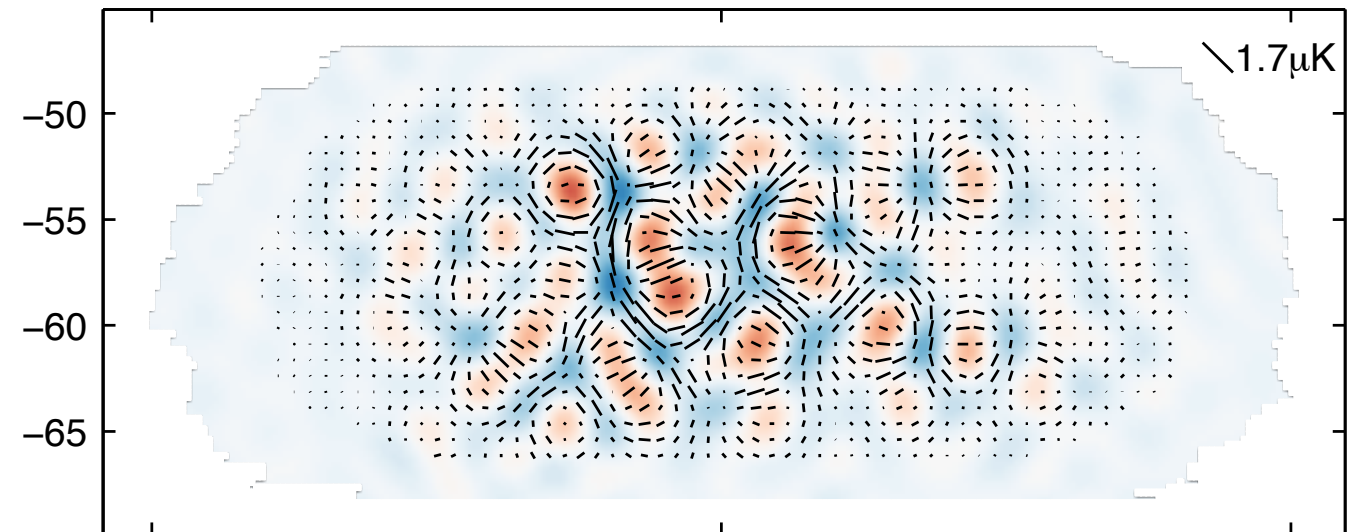


1 spin-two map  $\Leftrightarrow$  2 scalar maps (E = gradient field, B = rotation field), but:  
scalar modes  $\rightarrow$  gradients  $\rightarrow$  B-mode vanish

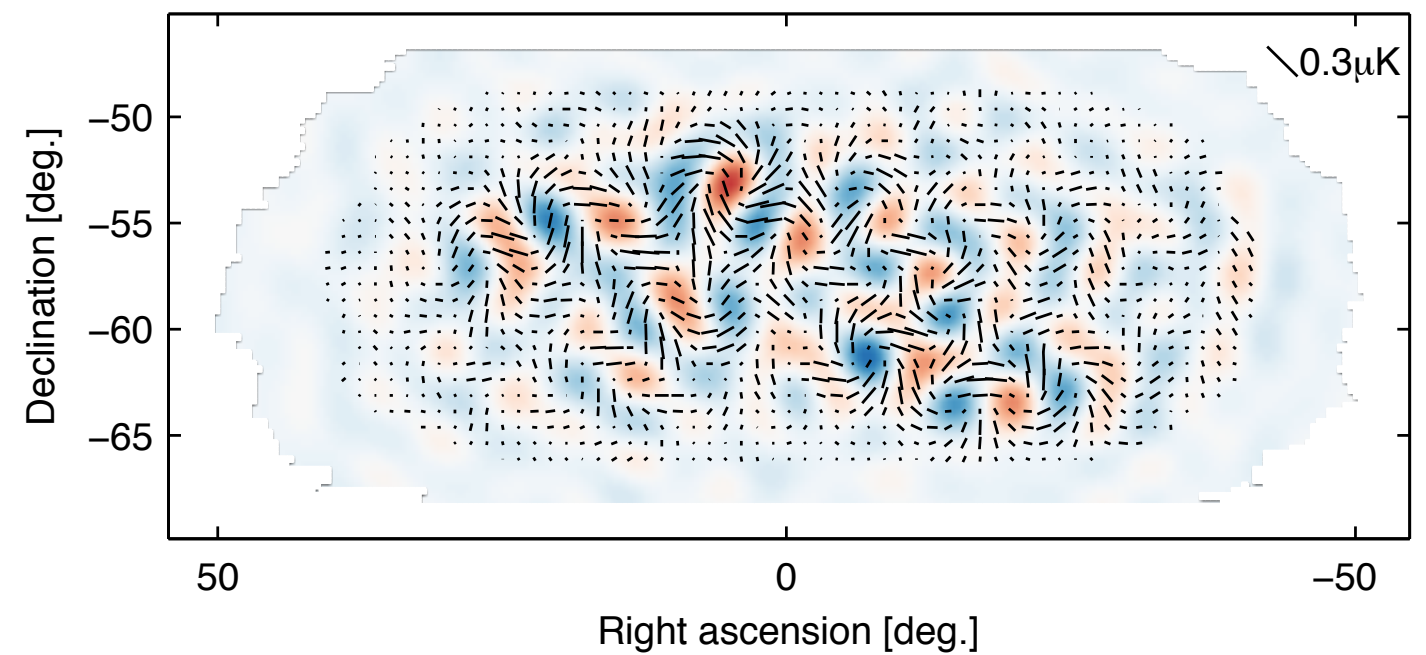
# CMB polarisation



BICEP2: E signal



BICEP2: B signal





# CMB polarisation

Temperature spectrum:  $C_{\ell}^{TT} = \langle a_{lm}^T a_{lm}^{T*} \rangle = \frac{2}{\pi} \int dk k^2 [\Theta_{\ell}(\eta_0, k)]^2 P_{\mathcal{R}}(k)$

with transfer function  $\Theta_l(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta \{ g (\Theta_0 + \psi) j_l(k(\eta_0 - \eta))$   
 $+ g k^{-1} \theta_b j'_l(k(\eta_0 - \eta))$   
 $+ e^{-\tau} (\phi' + \psi') j_l(k(\eta_0 - \eta)) \}$

For polarisation:

Kosowsky 1996; Seljak & Zaldarriaga astro-ph/9609170; Hu & White astro-ph/9702170

# CMB polarisation

Temperature spectrum:  $C_{\ell}^{TT} = \langle a_{lm}^T a_{lm}^{T*} \rangle = \frac{2}{\pi} \int dk k^2 [\Theta_{\ell}(\eta_0, k)]^2 P_{\mathcal{R}}(k)$

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For polarisation:

Kosowsky 1996; Seljak & Zaldarriaga astro-ph/9609170; Hu & White astro-ph/9702170

E-mode polarisation spectrum:  $C_{\ell}^{EE} = \langle a_{lm}^E a_{lm}^{E*} \rangle = \frac{2}{\pi} \int dk k^2 [\Delta_{\ell}^E(\eta_0, k)]^2 P_{\mathcal{R}}(k)$

with transfer function  $\Delta_l^E(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta g \{ \Theta_2 + \dots \} (\dots) j_l(k(\eta_0 - \eta))$

# CMB polarisation

Temperature spectrum:  $C_{\ell}^{TT} = \langle a_{lm}^T a_{lm}^{T*} \rangle = \frac{2}{\pi} \int dk k^2 [\Theta_{\ell}(\eta_0, k)]^2 P_{\mathcal{R}}(k)$

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 $+ g k^{-1} \theta_b j_l'(k(\eta_0 - \eta))$   
 $+ e^{-\tau} (\phi' + \psi') j_l(k(\eta_0 - \eta)) \} + \dots$

For polarisation:

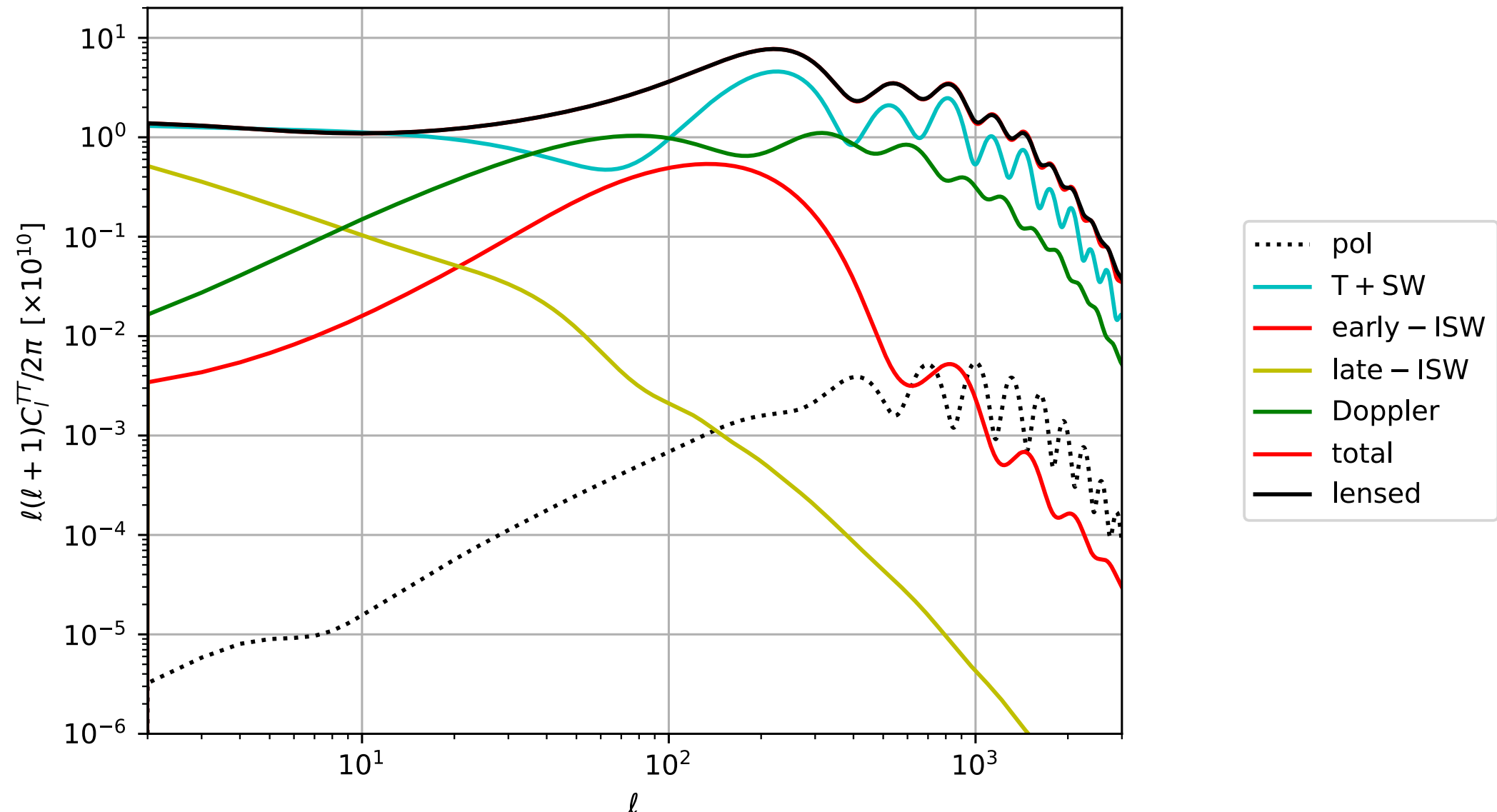
Kosowsky 1996; Seljak & Zaldarriaga astro-ph/9609170; Hu & White astro-ph/9702170

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with transfer function  $\Delta_l^E(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta g \{ \Theta_2 + \dots \} (\dots) j_l(k(\eta_0 - \eta))$

# CMB polarisation

Corrections to temperature spectrum taking into account polarisation anisotropies



`notebooks/cltt_terms.ipynb + loglog + 'temperature_contributions': 'pol'`

# CMB polarisation

Temperature spectrum:  $C_{\ell}^{TT} = \langle a_{lm}^T a_{lm}^{T*} \rangle = \frac{2}{\pi} \int dk k^2 [\Theta_{\ell}(\eta_0, k)]^2 P_{\mathcal{R}}(k)$

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 $+ e^{-\tau} (\phi' + \psi') j_l(k(\eta_0 - \eta)) \} + \dots$

For polarisation:

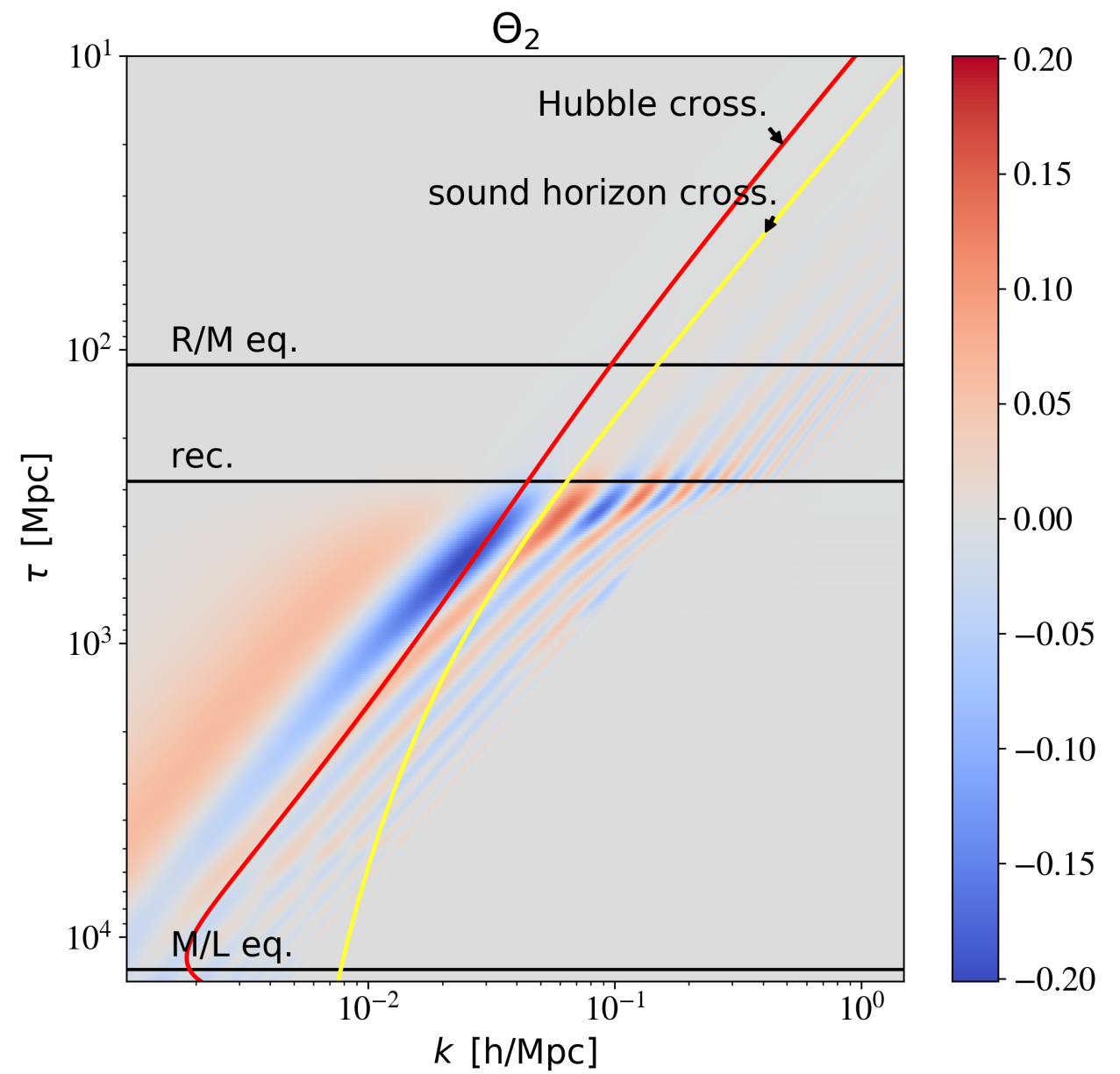
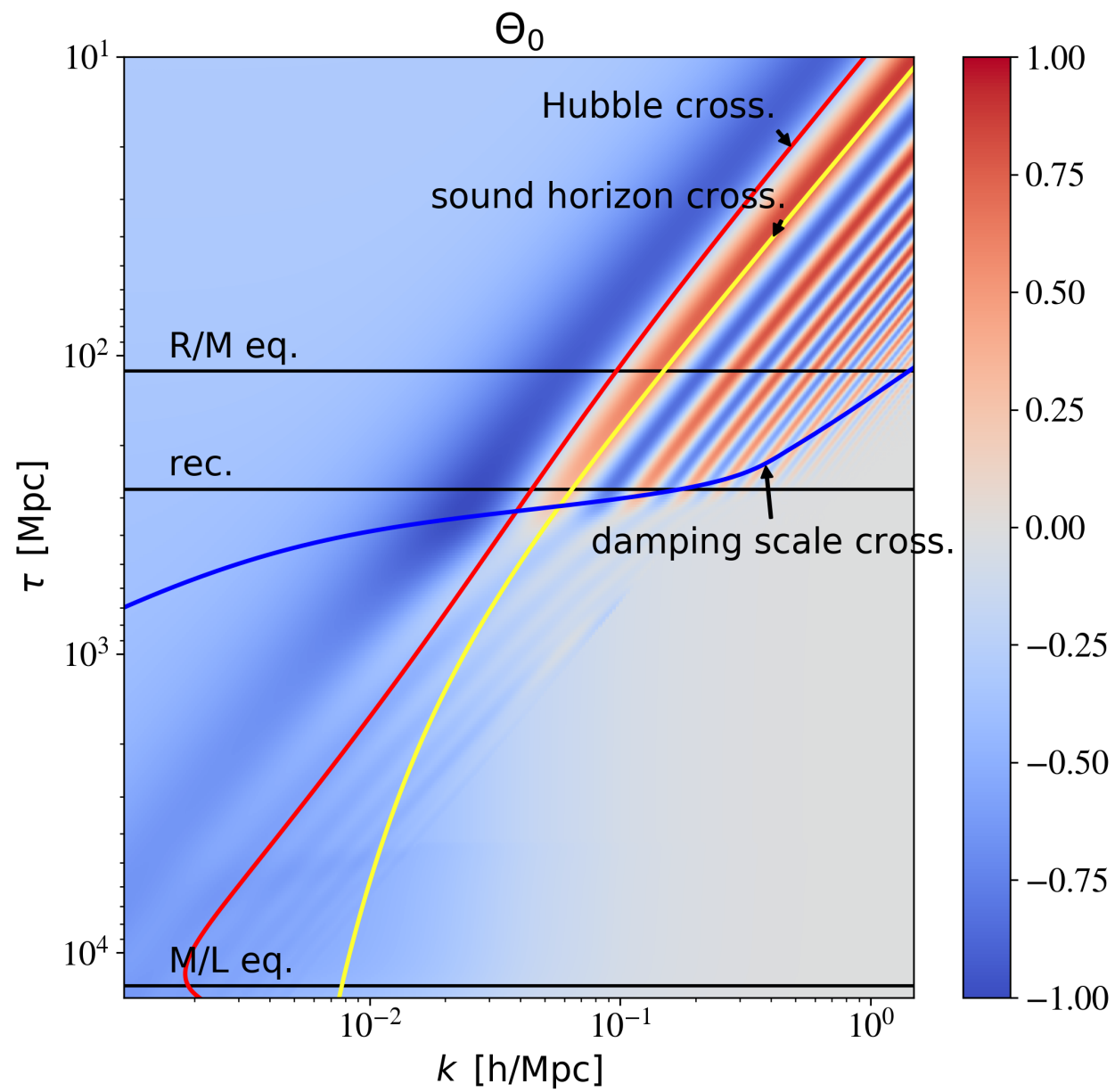
Kosowsky 1996; Seljak & Zaldarriaga astro-ph/9609170; Hu & White astro-ph/9702170

E-mode polarisation spectrum:  $C_{\ell}^{EE} = \langle a_{lm}^E a_{lm}^{E*} \rangle = \frac{2}{\pi} \int dk k^2 [\Delta_{\ell}^E(\eta_0, k)]^2 P_{\mathcal{R}}(k)$

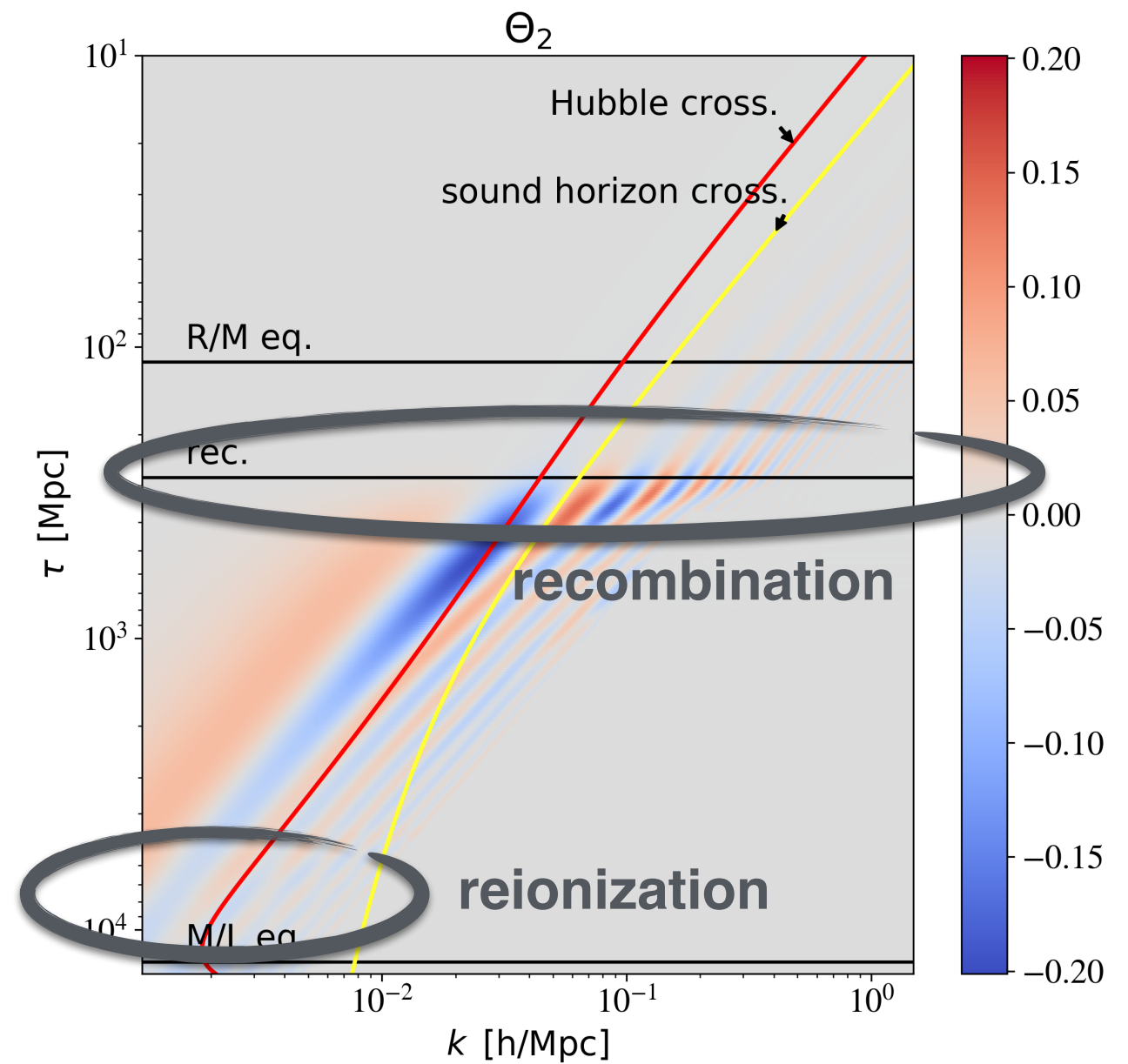
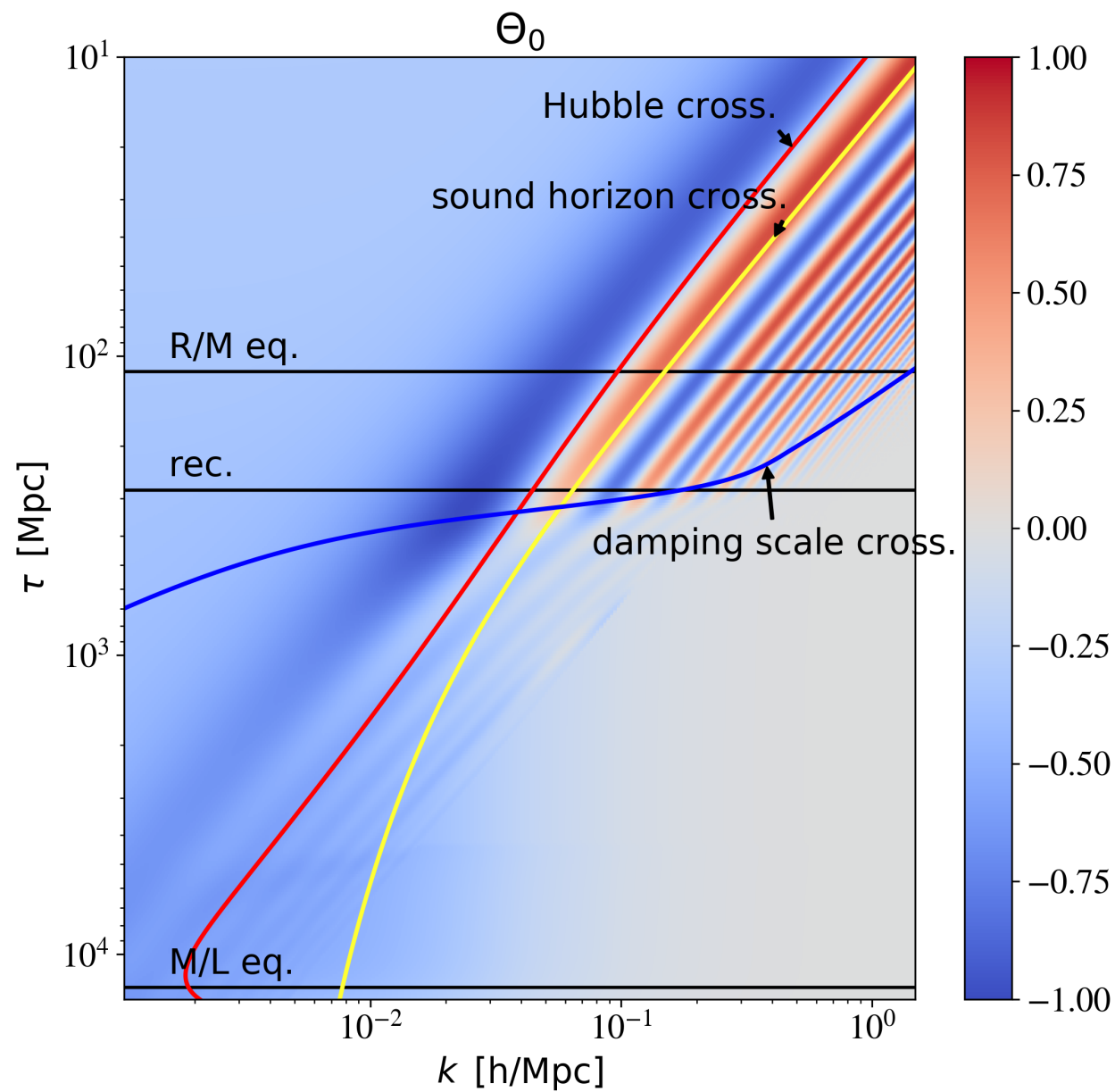
with transfer function  $\Delta_l^E(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta g \{ \Theta_2 + \dots \} (\dots) j_l(k(\eta_0 - \eta))$

... no Doppler ... no Sachs-Wolfe ... no ISW ...

# CMB polarisation



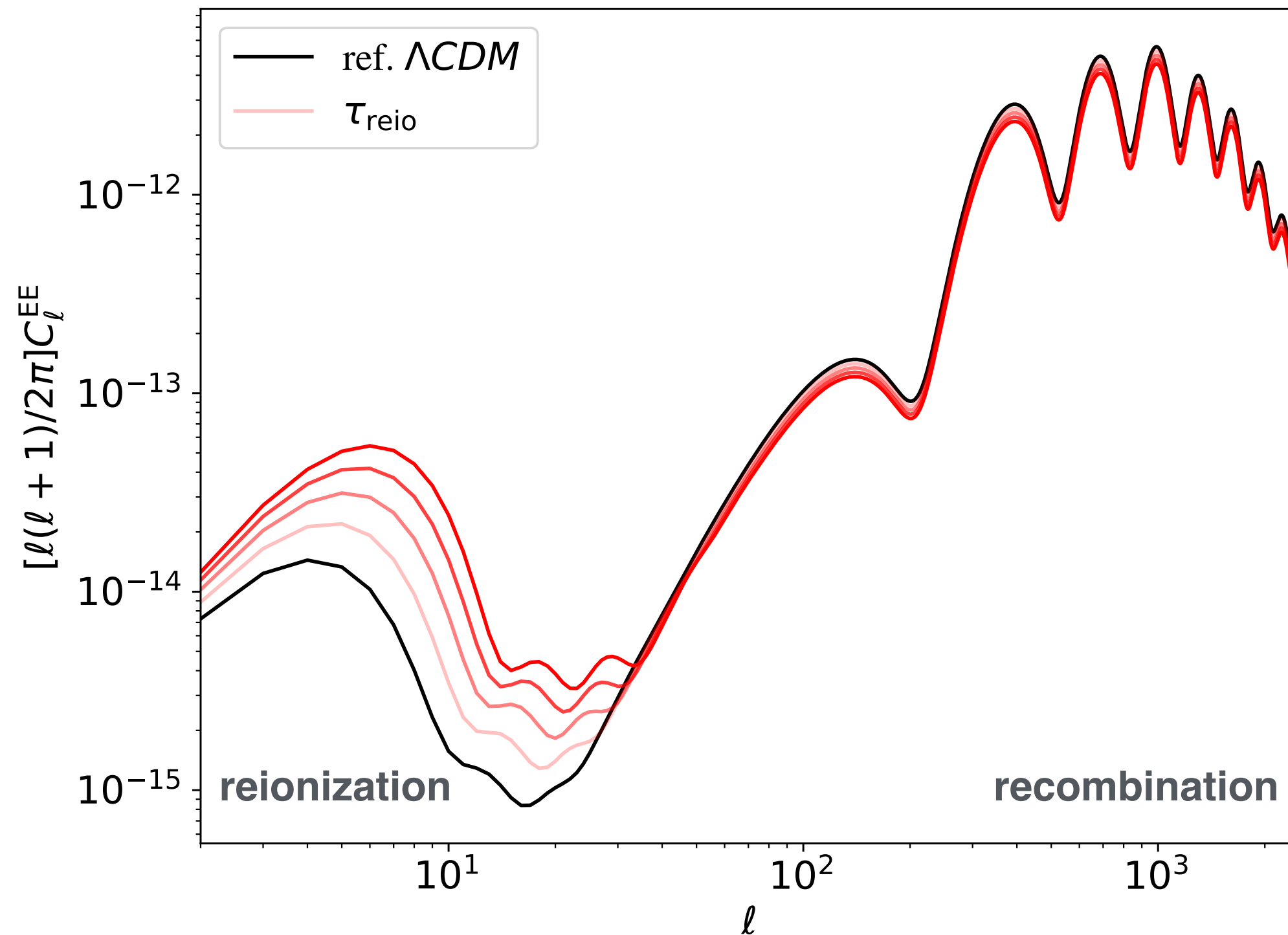
# CMB polarisation



$$\Delta_l(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta \, g \{ \Theta_2 + \dots \} (\dots) j_l(k(\eta_0 - \eta))$$



# CMB polarisation





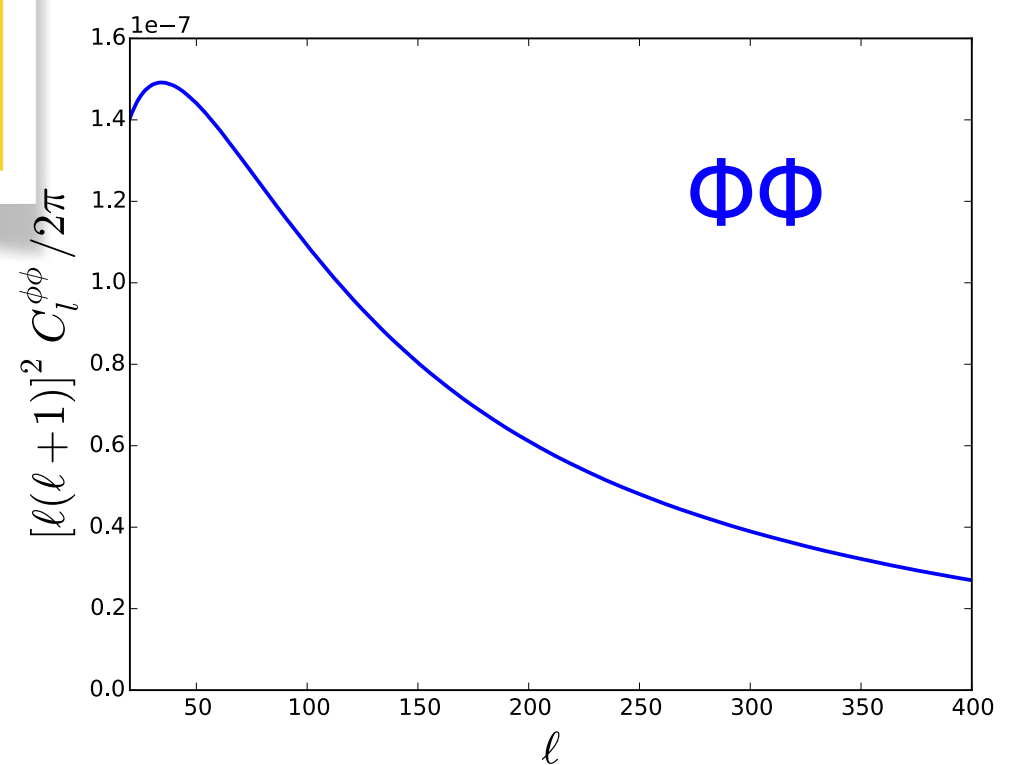
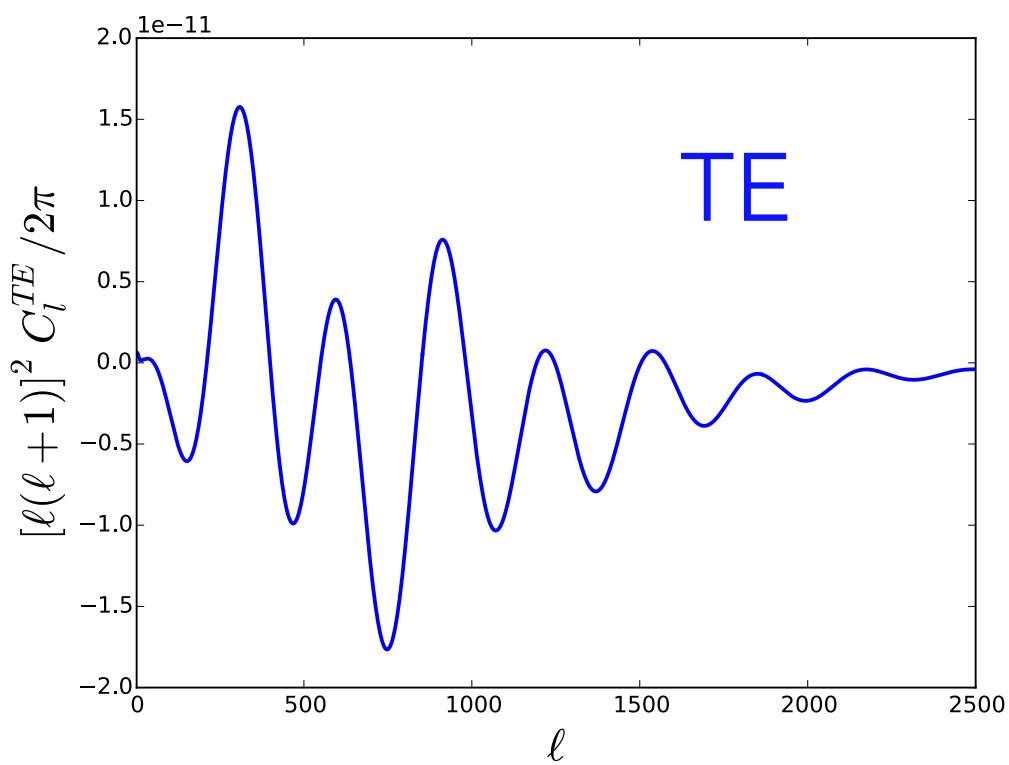
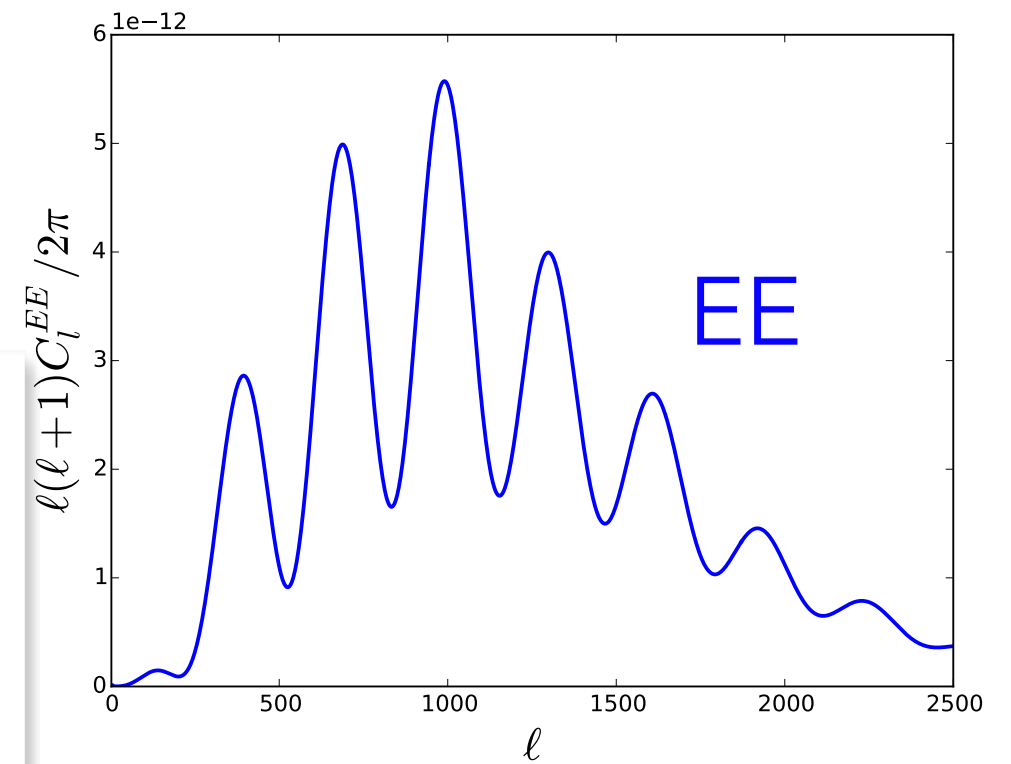
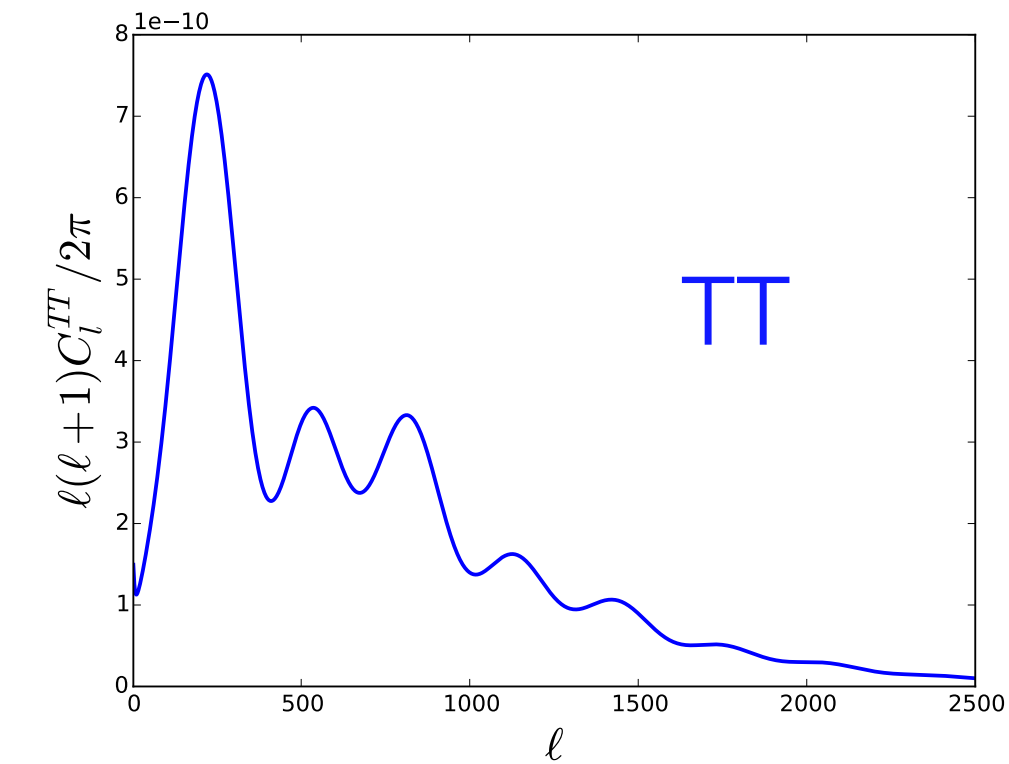
# CMB polarisation

Cross spectrum:  $C_{\ell}^{TE} = \left\langle \frac{a_{lm}^T a_{lm}^{E*} + a_{lm}^E a_{lm}^{T*}}{2} \right\rangle = \frac{2}{\pi} \int dk k^2 \Theta_{\ell}(\eta_0, k) \Delta_{\ell}^E(\eta_0, k) P_{\mathcal{R}}(k)$

with transfer function  $\Theta_l(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta \{ g (\Theta_0 + \psi) j_l(k(\eta_0 - \eta))$   
 $+ g k^{-1} \theta_b j'_l(k(\eta_0 - \eta))$   
 $+ e^{-\tau} (\phi' + \psi') j_l(k(\eta_0 - \eta)) \} + \dots$

and  $\Delta_l^E(\eta_0, k) = \int_{\eta_{\text{ini}}}^{\eta_0} d\eta g \{ \Theta_2 + \dots \} (\dots) j_l(k(\eta_0 - \eta))$

# CMB polarisation



Bardeen scalars



CMB information  
stored in 4 spectra

$$C_l^{XY}$$

# Tensor modes

# Tensor modes

$$g_{\mu\nu} = a^2(\eta_{\mu\nu} + h_{\mu\nu})$$

Bardeen scalars (spin-0)

$$h_{\mu\nu} = \begin{pmatrix} -2\psi & 0 & 0 & 0 \\ 0 & -2\phi & 0 & 0 \\ 0 & 0 & -2\phi & 0 \\ 0 & 0 & 0 & -2\phi \end{pmatrix}$$

(Newtonian gauge)

Bardeen tensors (spin-2)

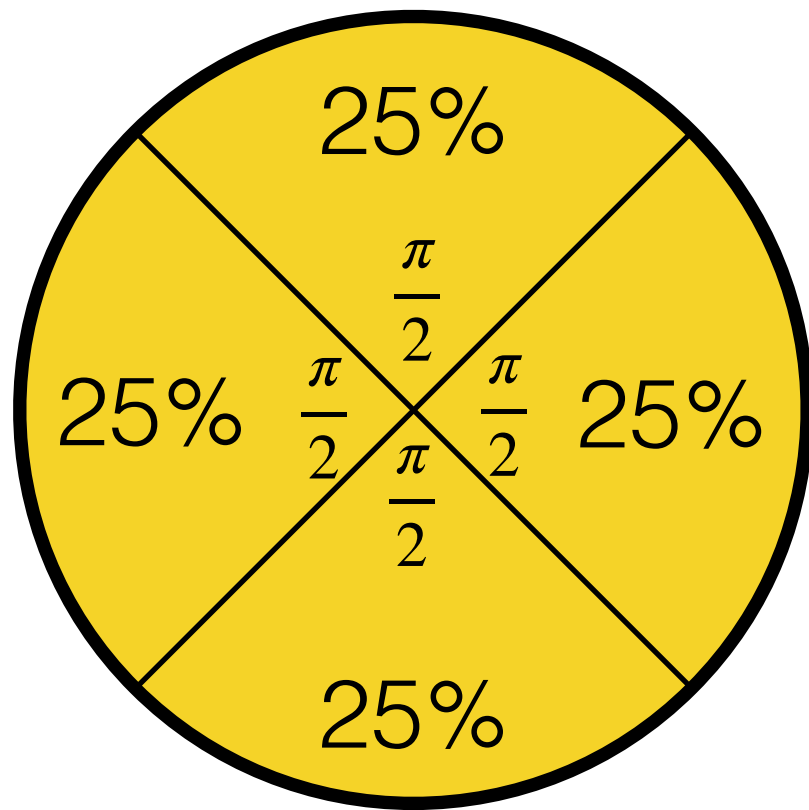
$$h_{\mu\nu} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & h_1 & h_2 & 0 \\ 0 & h_2 & -h_1 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

(for GWs along  $x^3$ )

Boltzmann with scalars:  $\Theta' + \hat{n} \cdot \vec{\nabla} \Theta = \hat{n} \cdot \vec{\nabla} \psi - \phi' + [\text{Thomson}]$   
 grav. Dop.    dilation

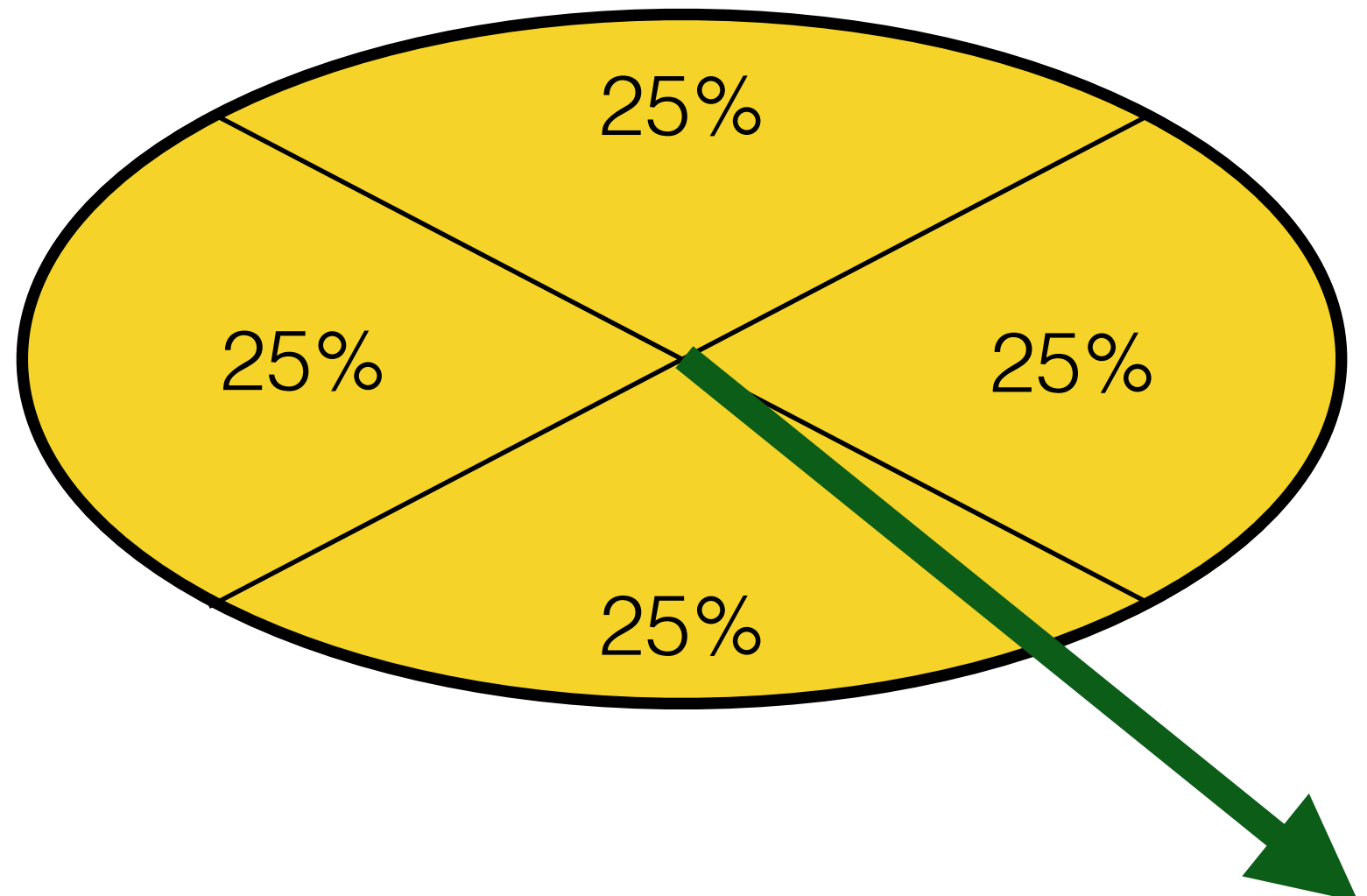
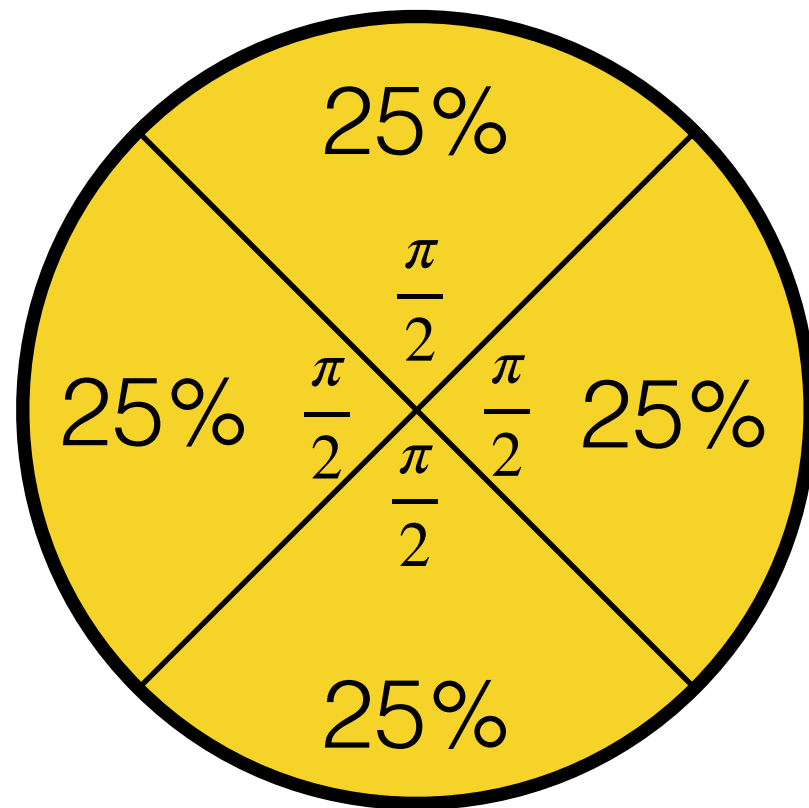
Boltzmann with tensors:  $\Theta' + \hat{n} \cdot \vec{\nabla} \Theta = -\frac{1}{2} h'_{ij} \hat{n}^i \hat{n}^j + [\text{Thomson}]$

# Tensor modes



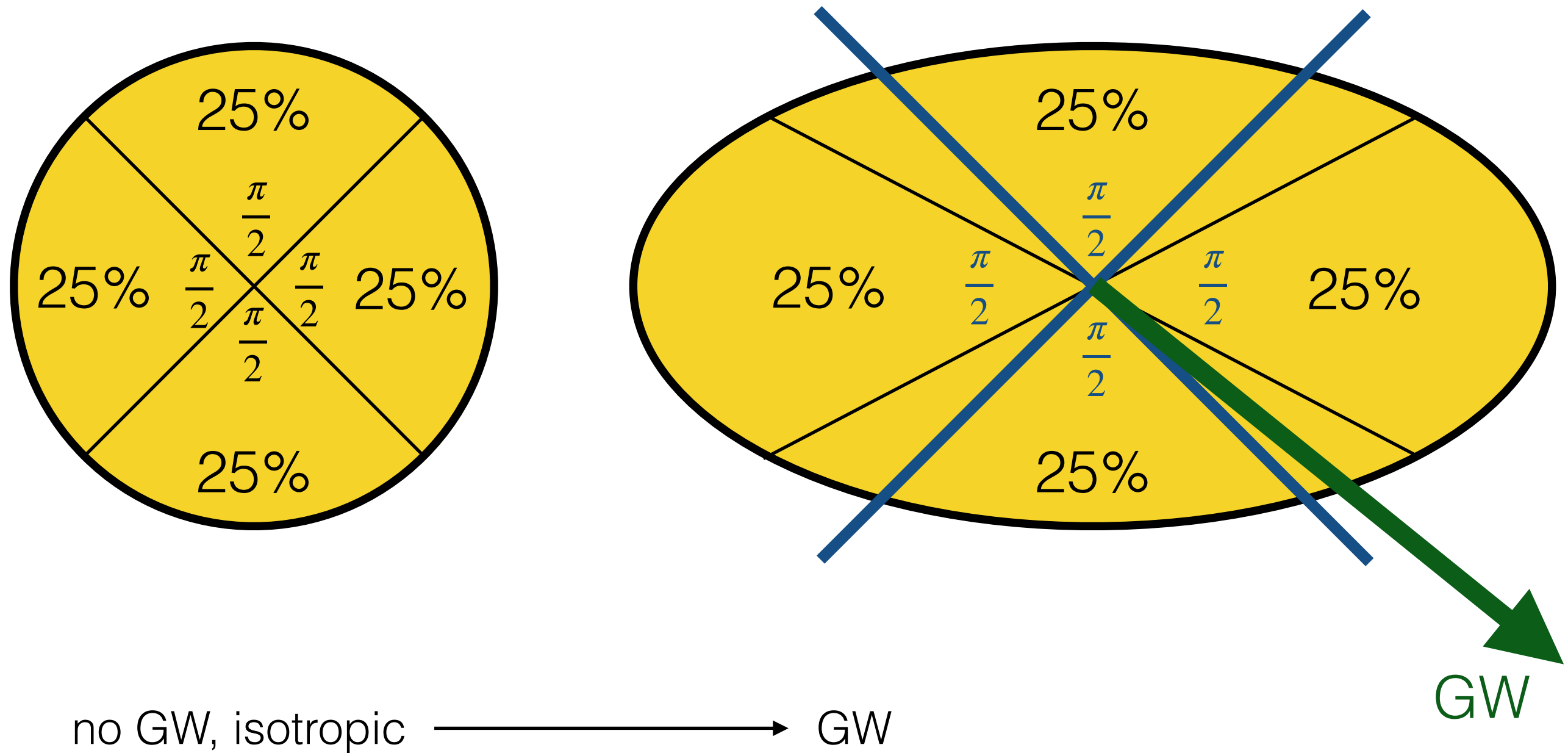
no GW, isotropic

# Tensor modes

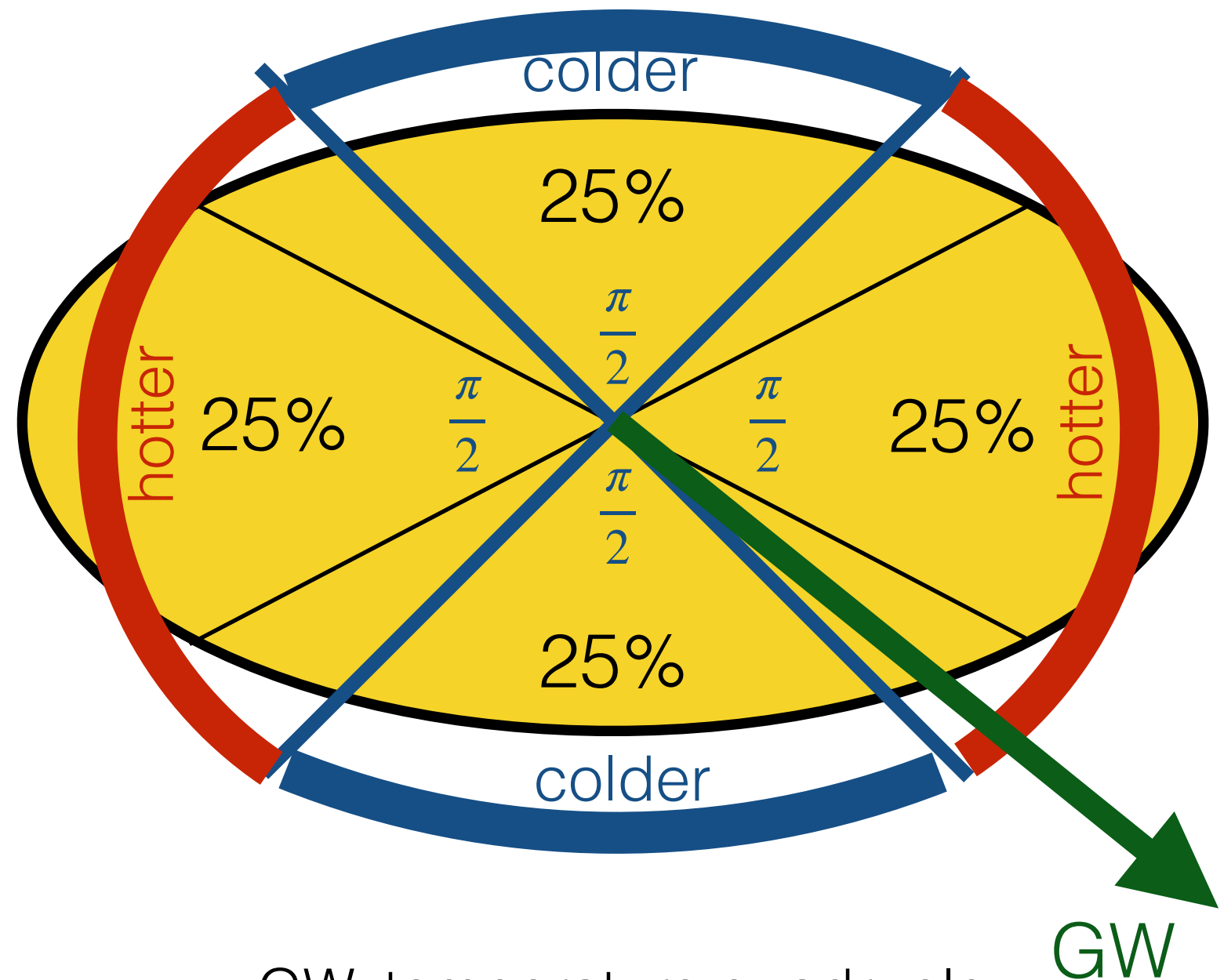
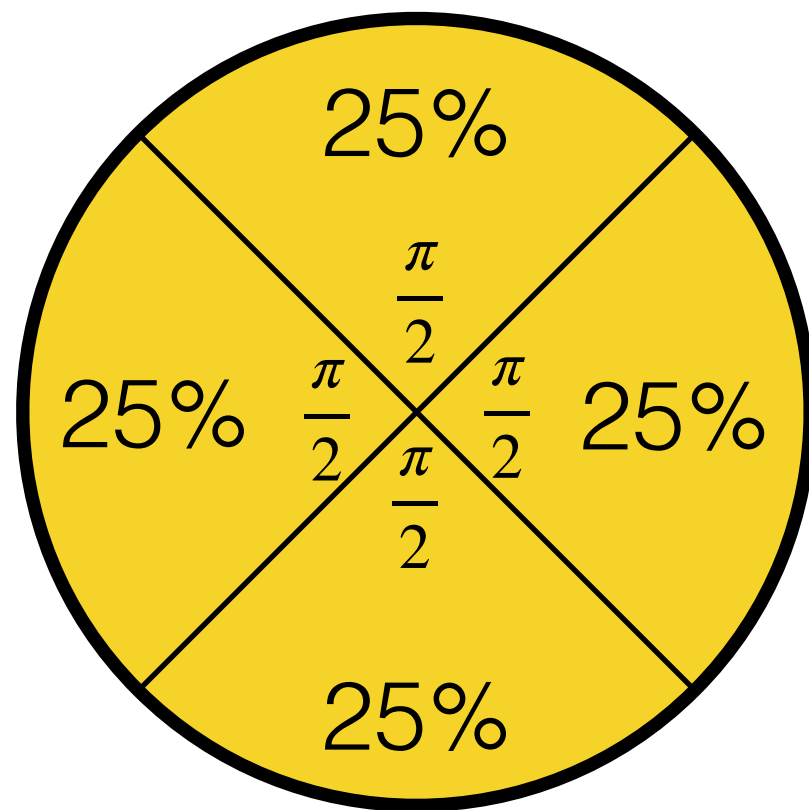


no GW, isotropic → GW

# Tensor modes



# Tensor modes



no GW, isotropic → GW, temperature quadrupole



# Tensor modes

Scalar Boltzmann:  $\Theta' + \hat{n} \cdot \vec{\nabla} \Theta = \hat{n} \cdot \vec{\nabla} \psi - \phi' + [\text{Thomson}]$

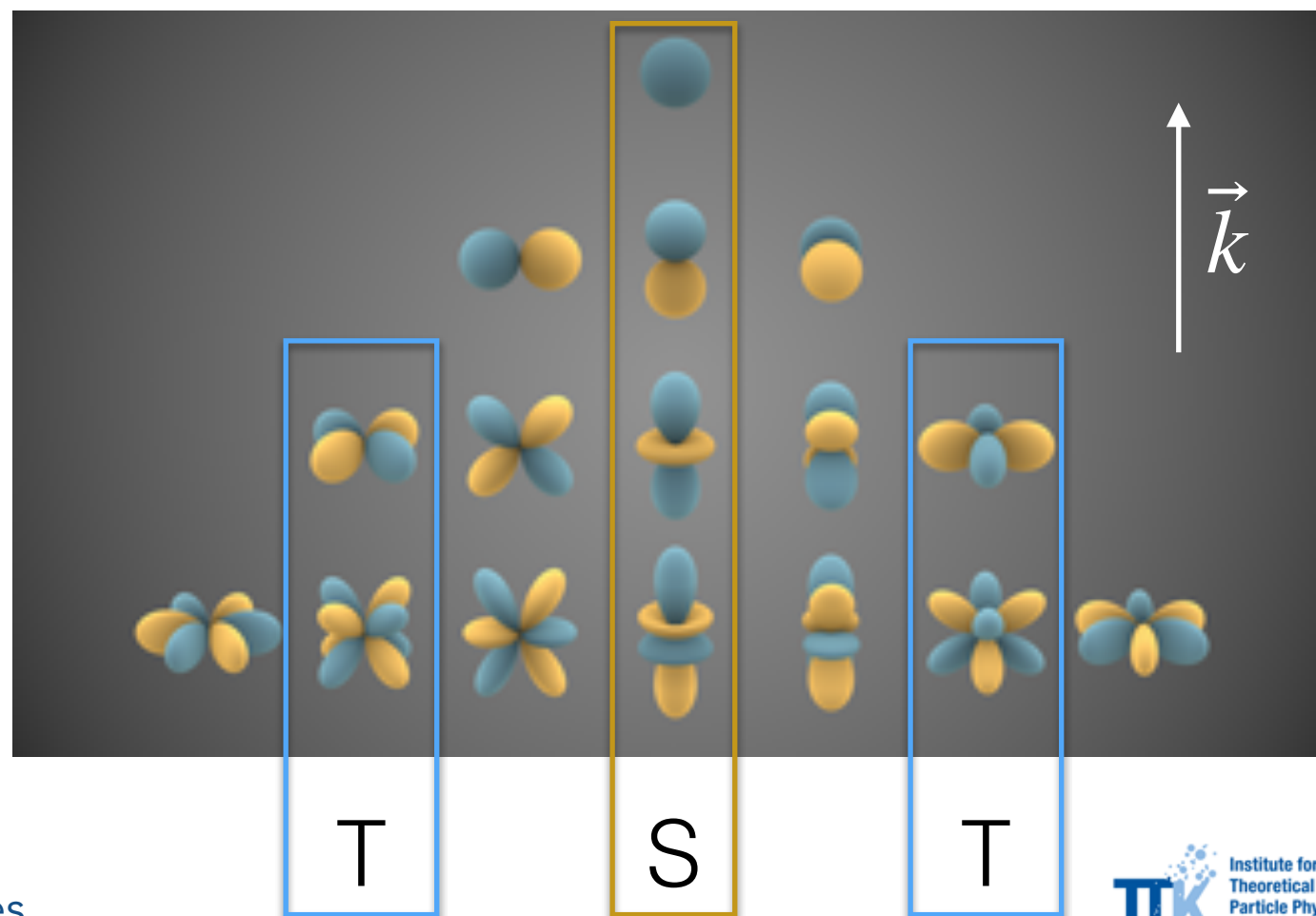
Tensor Boltzmann:  $\Theta' + \hat{n} \cdot \vec{\nabla} \Theta = -\frac{1}{2} h'_{ij} \hat{n}^i \hat{n}^j + [\text{Thomson}]$

# Tensor modes

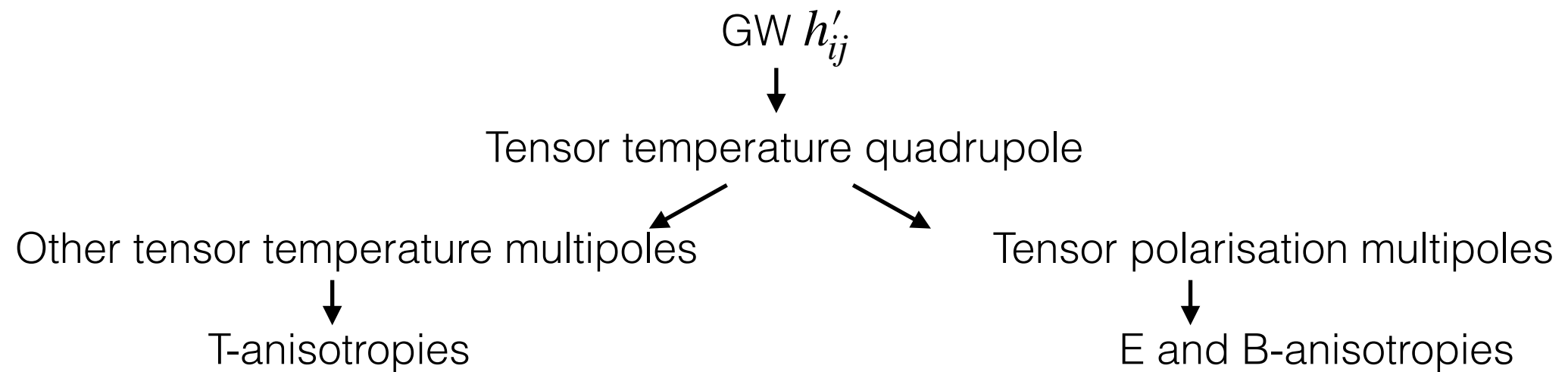
Scalar Boltzmann:  $\Theta' + \hat{n} \cdot \vec{\nabla} \Theta = \hat{n} \cdot \vec{\nabla} \psi - \phi' + [\text{Thomson}]$

Tensor Boltzmann:  $\Theta' + \hat{n} \cdot \vec{\nabla} \Theta = -\frac{1}{2} h'_{ij} \hat{n}^i \hat{n}^j + [\text{Thomson}]$

General expansion:  $\Theta(\eta, \vec{x}, \hat{n}) \longrightarrow \Theta(\eta, \vec{k}, \hat{n}) = \sum_{lm} \Theta_{lm}(\eta, \vec{k}) Y_{lm}(\hat{n})$

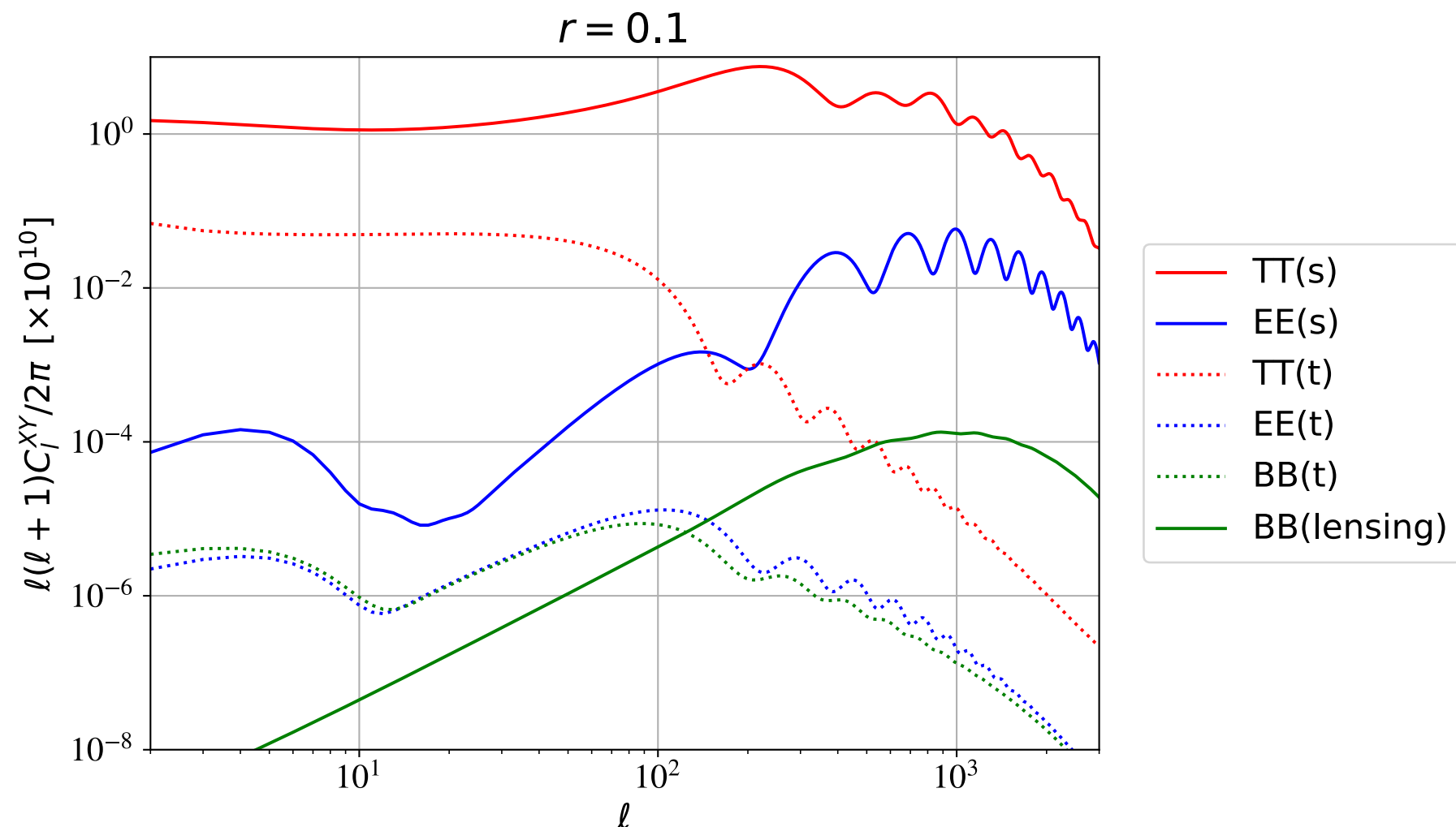


# Tensor modes

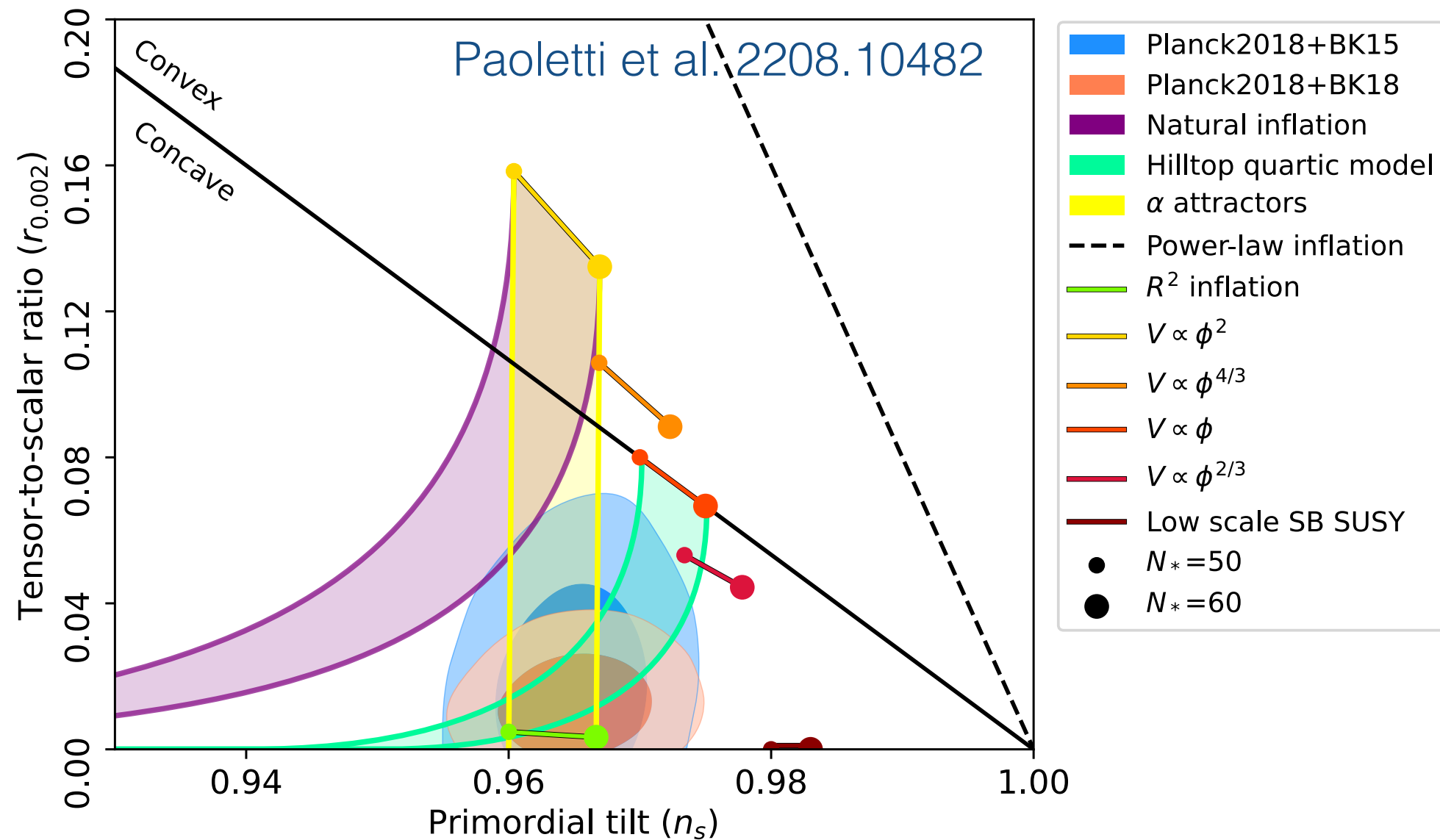


Scalar and tensor sector statistically independent, solved independently,

$$\begin{aligned}
 C_l^{TT} &= C_l^{TT(s)} + C_l^{TT(t)} \\
 C_l^{EE} &= C_l^{EE(s)} + C_l^{EE(t)} \\
 C_l^{TE} &= C_l^{TE(s)} + C_l^{TE(t)} \\
 C_l^{BB} &= 0 + C_l^{BB(t)}
 \end{aligned}$$



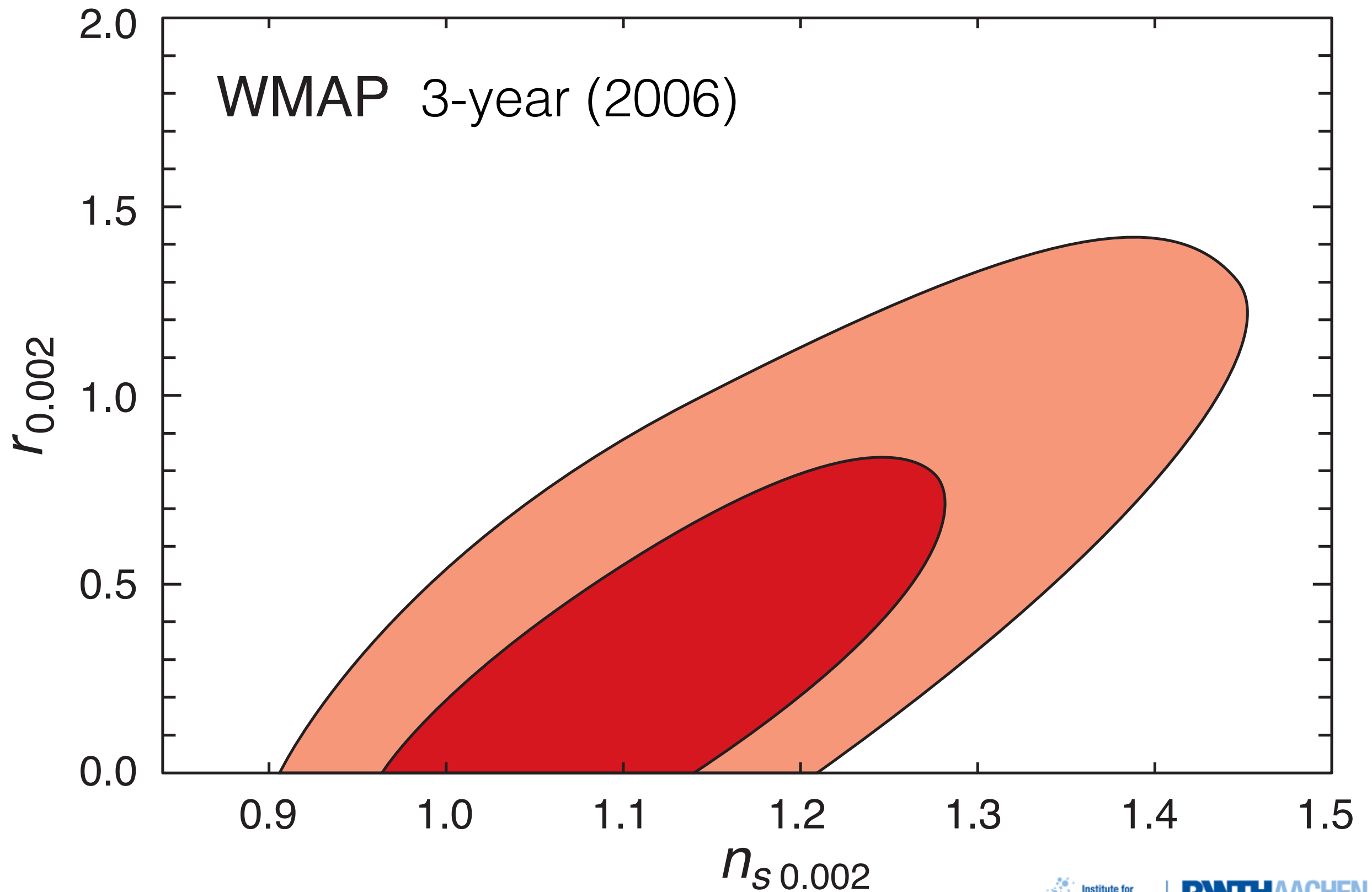
# Observational constraints on $\Lambda$ CDM + r



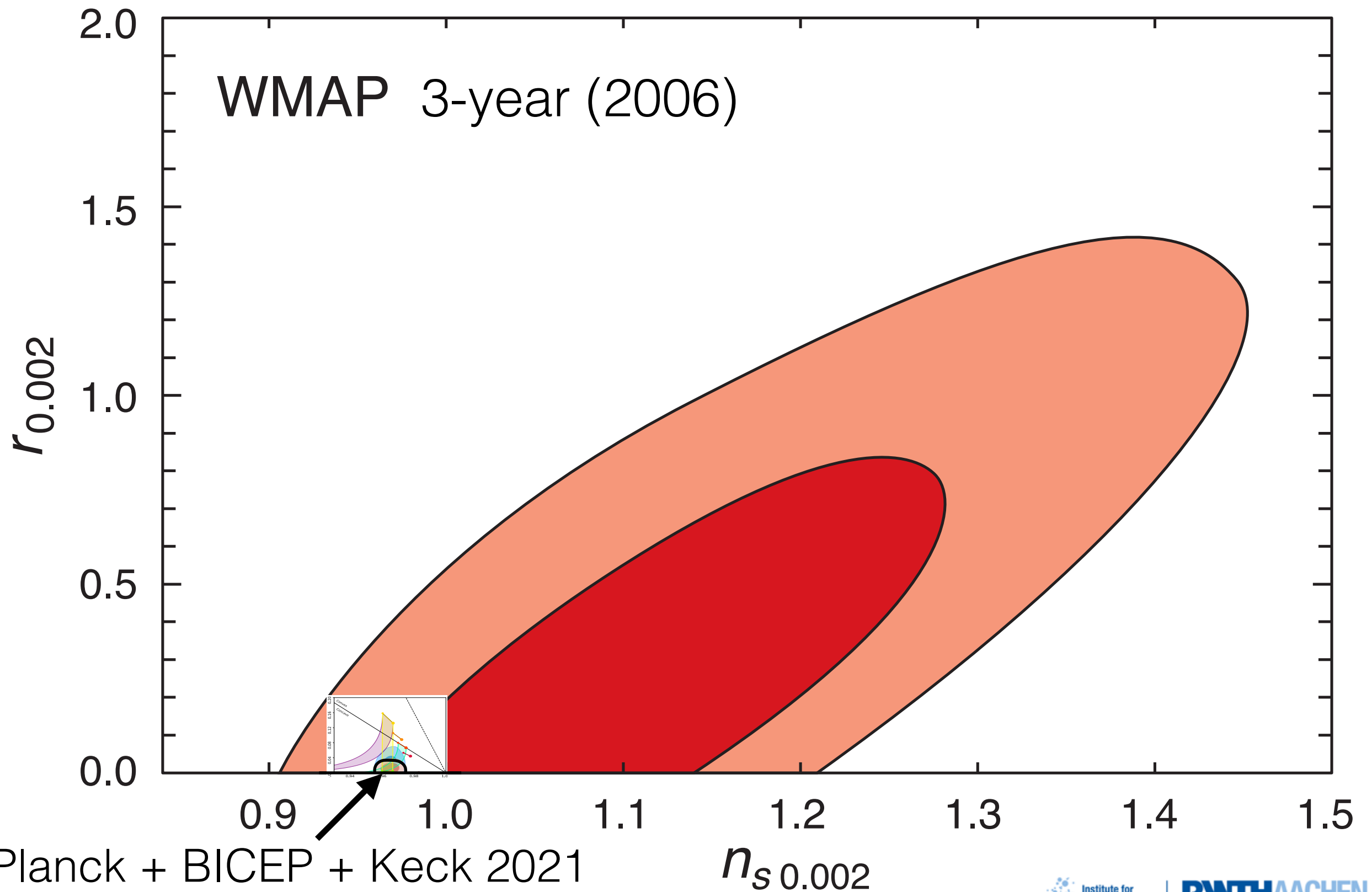
Energy scale of inflation  $V_*$

$$V_* = \frac{3\pi^2 A_s}{2} r M_{\text{Pl}}^4 < (1.4 \times 10^{16} \text{ GeV})^4 \quad (95\% \text{ CL})$$

# Observational constraints on $\Lambda$ CDM + r

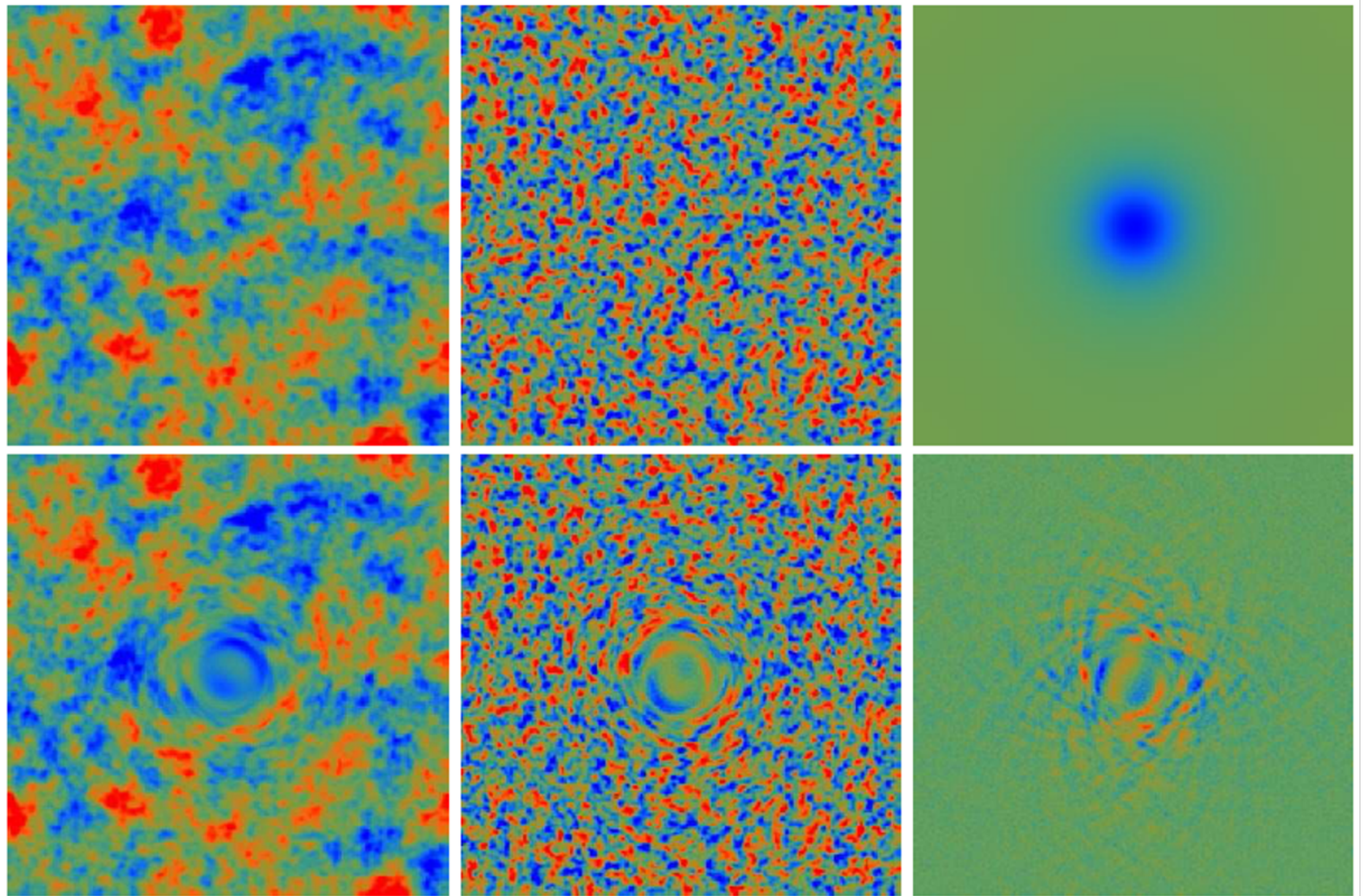


# Observational constraints on $\Lambda$ CDM + r



# CMB lensing





from W. Hu



# Basic math

## Deflection field

$$\frac{\delta T^{\text{obs}}}{T}(\hat{n}) = \frac{\delta T^{\text{raw}}}{T} \left( \hat{n} + \overset{\substack{\text{typically } \sim \text{ arc minutes} \\ \downarrow}}{\vec{d}(\hat{n})}} \right) = \frac{\delta T^{\text{raw}}}{T} \left( \hat{n} + \vec{\nabla} \Phi(\hat{n}) \right)$$

## CMB lensing potential

$$\Phi(\hat{n}) = \int_{\eta_0}^{\eta_{\text{dec}}} d\eta \, W(\eta) \, \phi(\eta, \vec{r}(\eta)) = \sum_{lm} \Phi_{lm} Y_{lm}(\hat{n})$$

## CMB lensing spectrum

$$C_{\ell}^{\Phi\Phi} = \langle |\Phi_{lm}|^2 \rangle \quad \text{easy to predict with EBS (linear pert.)}$$

# Many important goals

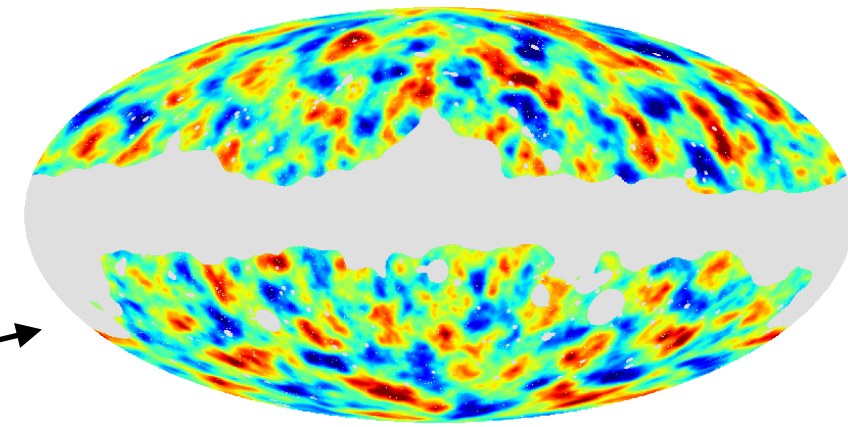
1. How are observable  $C_\ell^{TT}$ ,  $C_\ell^{EE}$ ,  $C_\ell^{TE}$ ,  $C_\ell^{BB}$  affected?  
(needed for fitting theory)

2. Infer map  $\Phi(\hat{n})$  from data

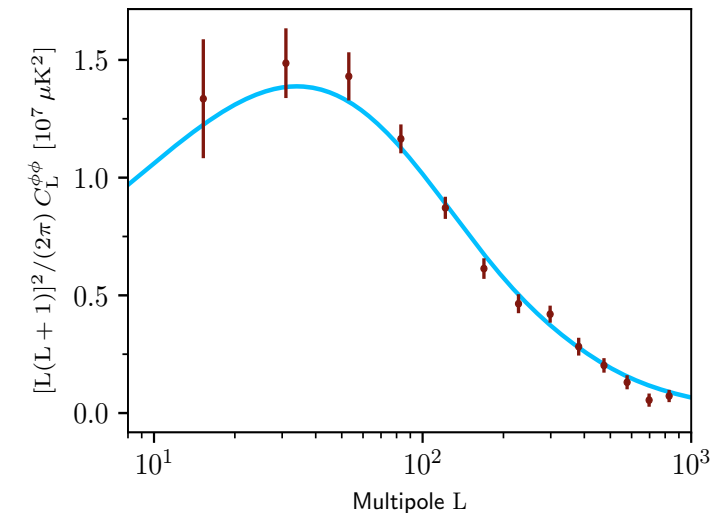
3. Infer the  $C_\ell^{\Phi\Phi}$  from data and fit theory  
(more information than in 1)

4. Delens temperature and polarisation maps

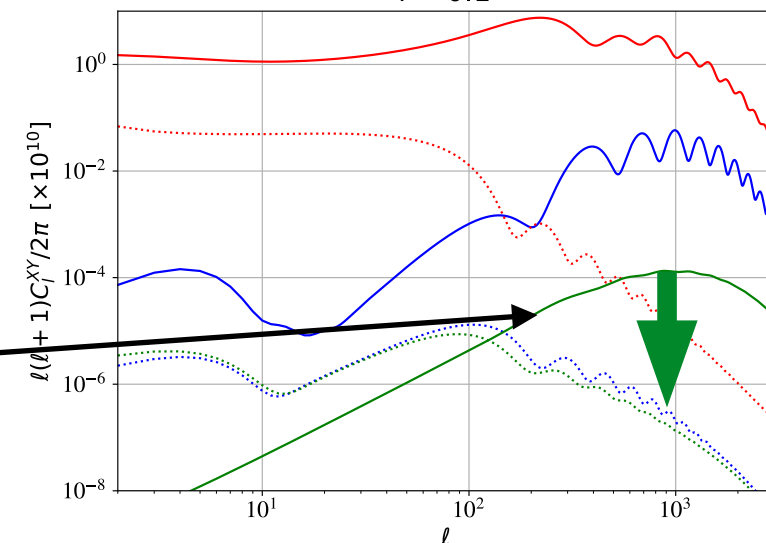
5. Delens spectra  $C_\ell^{TT}$ ,  $C_\ell^{EE}$ ,  $C_\ell^{TE}$ ,  $C_\ell^{BB}$



-4e-05 4e-05 rad.



$r = 0.1$



# Basic method

Taylor

$$X^{\text{obs}}(\hat{n}) = X^{\text{raw}} \left( \hat{n} + \vec{\nabla} \Phi(\hat{n}) \right) = X^{\text{raw}} + D_i \Phi D^i X^{\text{raw}} + \frac{1}{2} D_i \Phi D_j \Phi D^i D^j X^{\text{raw}} + \dots$$

Harmonic

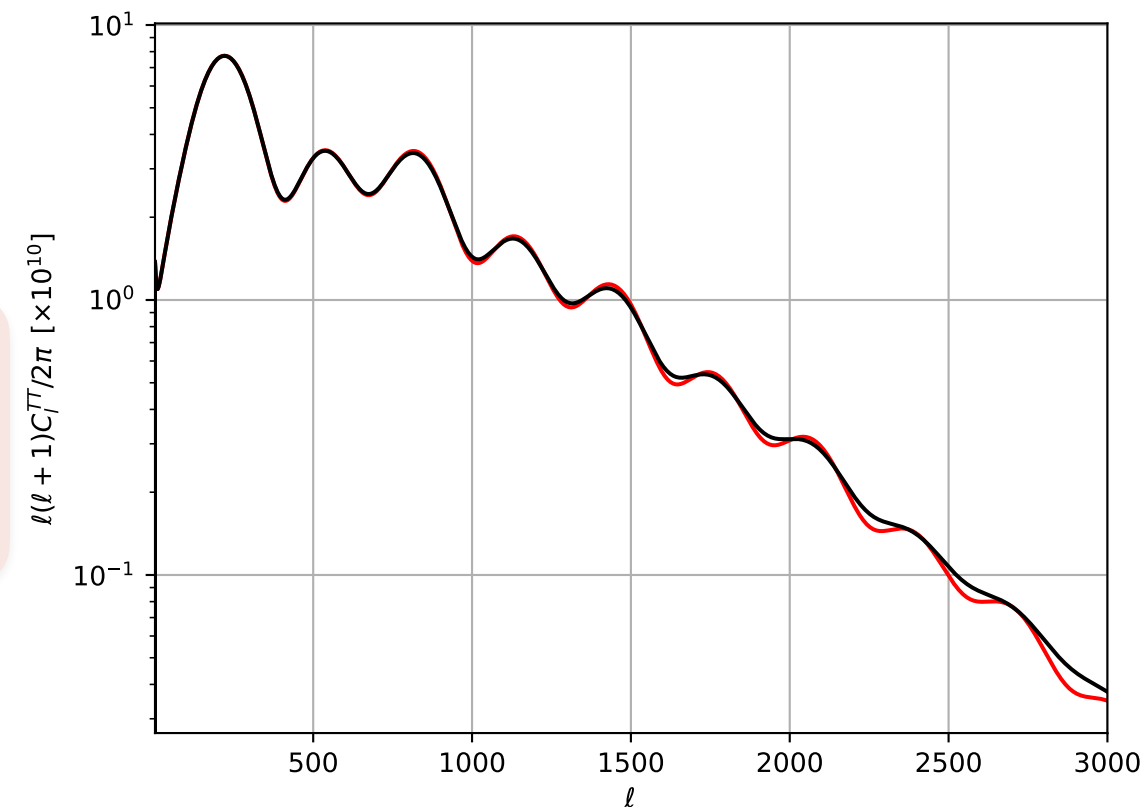
$$X_{lm}^{\text{obs}} = X_{lm}^{\text{raw}} + I_{lm}^{l_1 m_1 l_2 m_2} \Phi_{l_1 m_1} X_{l_2 m_2}^{\text{raw}} + J_{lm}^{l_1 m_1 l_2 m_2 l_3 m_3} \Phi_{l_1 m_1} \Phi_{l_2 m_2} X_{l_3 m_3}^{\text{raw}} + \dots$$

1. How are observable  $C_{\ell}^{TT}, C_{\ell}^{EE}, C_{\ell}^{TE}, C_{\ell}^{BB}$  affected?

Compute  $\langle |X_{lm}^{\text{obs}}|^2 \rangle$  with  $X_{lm}^{\text{raw}}$  and  $\Phi_{lm}$  seen as gaussian independent variables:

$$C_{\ell}^{XY, \text{obs}} = C_{\ell}^{XY, \text{raw}} \text{ smoothed by kernel that depends on } C_{\ell}^{\Phi\Phi}.$$

Both  $I$  and  $J$  matter!



# Basic method

Taylor

$$X^{\text{obs}}(\hat{n}) = X^{\text{raw}} \left( \hat{n} + \vec{\nabla} \Phi(\hat{n}) \right) = X^{\text{raw}} + D_i \Phi D^i X^{\text{raw}} + \frac{1}{2} D_i \Phi D_j \Phi D^i D^j X^{\text{raw}} + \dots$$

Harmonic

$$X_{lm}^{\text{obs}} = X_{lm}^{\text{raw}} + I_{lm}^{l_1 m_1 l_2 m_2} \Phi_{l_1 m_1} X_{l_2 m_2}^{\text{raw}} + J_{lm}^{l_1 m_1 l_2 m_2 l_3 m_3} \Phi_{l_1 m_1} \Phi_{l_2 m_2} X_{l_3 m_3}^{\text{raw}} + \dots$$

2. Infer map  $\Phi(\hat{n})$  from data

Neglect  $J$ -term. Previous relation cannot be just inverted... exploit non-Gaussianity of  $X_{lm}^{\text{obs}}$  !

$$X_{lm}^{\text{obs}} Y_{l'm'}^{\text{obs}} = X_{lm}^{\text{raw}} Y_{l'm'}^{\text{raw}} + K_{lml'm'}^{l_1 m_1 l_2 m_2 l_3 m_3} \Phi_{l_1 m_1} X_{l_2 m_2}^{\text{raw}} Y_{l_3 m_3}^{\text{raw}}$$

Imagine “average over realisations” for  $l \neq l', m \neq m'$ :

$$\langle X_{lm}^{\text{obs}} Y_{l'm'}^{\text{obs}} \rangle_{\text{CMB}} = K_{lml'm'}^{l_1 m_1 l_2 m_2 l_3 m_3} \delta_{l_2 l_3} \delta_{m_2 m_3} C_{l_2}^{XY, \text{raw}} \Phi_{l_1 m_1}$$

Linear combinations of many  $X_{lm}^{\text{obs}} Y_{l'm'}^{\text{obs}}$  reveals one  $\Phi_{l_1 m_1}$  up to some “cosmic variance”:

quadratic estimator of [Hu & Okamoto astro-ph/0301031](#)

# CMB spectral distortions

# Blackbody radiation in early Universe

Elastic and inelastic scattering,  $\Gamma > H$



Momentum exchange



Thermal/kinetic equilibrium  
Bose-Einstein / Fermi-Dirac

$$f(p) = \frac{1}{e^{(E-\mu)/T} - 1}$$



for massless particles

$$f(p) = \frac{1}{e^{p/T} - 1}$$

Inelastic scattering,  $\Gamma > H$



Chemical equilibrium

$$\sum \mu_i|_{\text{left}} = \sum \mu_i|_{\text{right}}$$



For particle without conserved numbers:

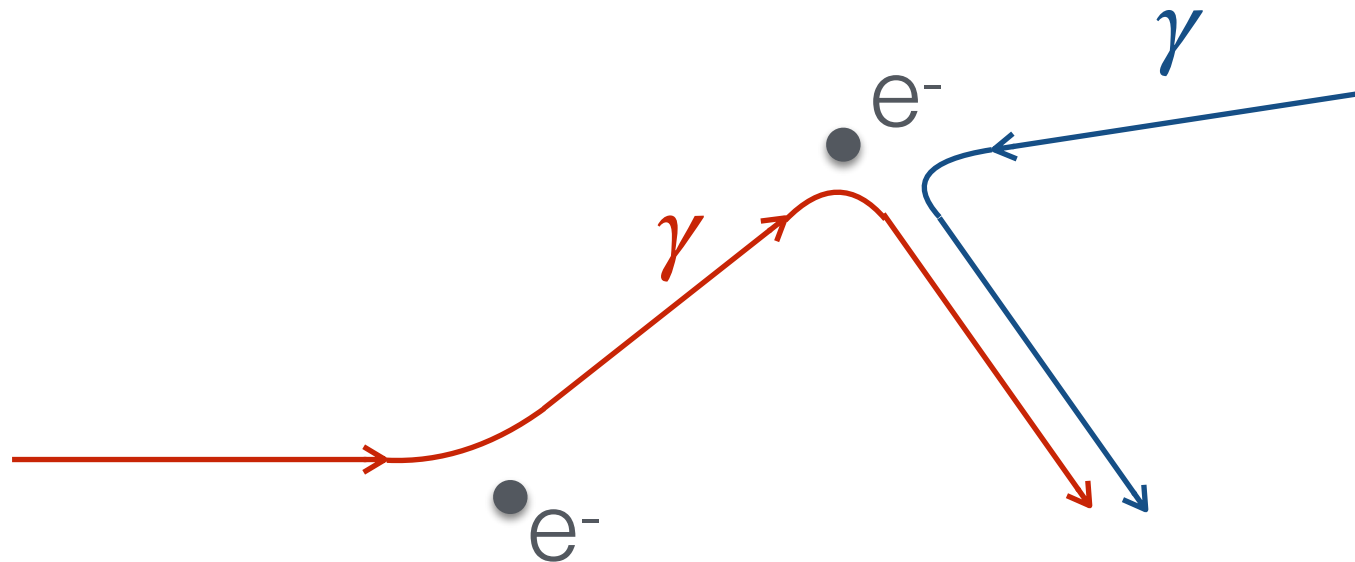
Number-changing reactions



$$\mu = 0$$

Photons:  $f(p) = \frac{1}{e^{p/T} - 1}$  = blackbody/Planck spectrum

# Blackbody radiation in early Universe



Redshifting along geodesics: 
$$\frac{d \ln(a p)}{d\eta} = \phi' - \hat{n} \cdot \vec{\nabla} \psi$$

Gravity preserves blackbody, but what about late interactions?

# Blackbody radiation in early Universe

- Compton scattering (CS):

$$\gamma + e^- \longrightarrow \gamma + e^- \text{ (number conserving)}$$

$$\frac{\partial f}{\partial t} = \dot{\tau} \frac{T_e}{m_e} \frac{1}{x^2} \frac{\partial}{\partial x} \left( x^4 \left[ \frac{\partial f}{\partial x} + \frac{T_z}{T_e} f(1+f) \right] \right)$$

Kompaneets equation

(solution: BE with arbitrary  $\mu$ )

- double Compton scattering (DC):

$$\gamma + e^- \longrightarrow \gamma + \gamma + e^- \text{ (non-number conserving)}$$

- Bremsstrahlung (BR):

$$e^- \longrightarrow e^- + \gamma \text{ (non-number conserving)}$$



# Blackbody radiation in early Universe

- $z > 3 \times 10^6$ : CS, DC, BR efficient: BE with  $\mu = 0$  = blackbody  
energy injection-> no distortion

- $z > 4 \times 10^4$ : only CS: BE with arbitrary  $\mu$ , Kompaneets can only impose

$$f(p; T, \mu = 0) \rightarrow f(p; T', \mu) \simeq f_{BE}(p; T, 0) \left\{ 1 + \mu \left[ 0.4561 - \frac{T}{p} \right] \right\}$$

energy injection->  $\mu$ -distortion

- $z > 10^3$ : CS not efficient: Kompaneets at next-to-leading order in  $H/\Gamma$  can only impose

$$f(p; T, \mu = 0) \rightarrow f_{BE}(p; T, 0) \left\{ 1 + y \left[ \frac{p}{T} \frac{e^{p/T} + 1}{e^{p/T} - 1} - 4 \right] \right\}$$

energy injection->  $y$ -distortion

- $z \sim 10^3$ : additional residuals

- Even later: CMB photons decoupled anyway

- Reionization: CS again, possible  $y$ -distortions (Sunyaev-Zel'dovich 1970)

# Source of distortions in standard cosmology

- Adiabatic cooling of electrons and photons:

Lucca, Schöneberg, Hooper,  
JL, Chluba 1910.04619

- UR particles in equilibrium with themselves:  $T \propto a^{-1}$
- NR particles in equilibrium with themselves:  $T \propto a^{-2}$
- Efficient CS:  $T_e = T_b = T_\gamma \propto a^{-1}$
- Inefficient CS:  $T_e = T_b < T_\gamma$

→ energy extracted from photon,  $\mu = -3 \times 10^{-9}$ ,  $y = -5 \times 10^{-10}$

- Dissipation of acoustic waves:

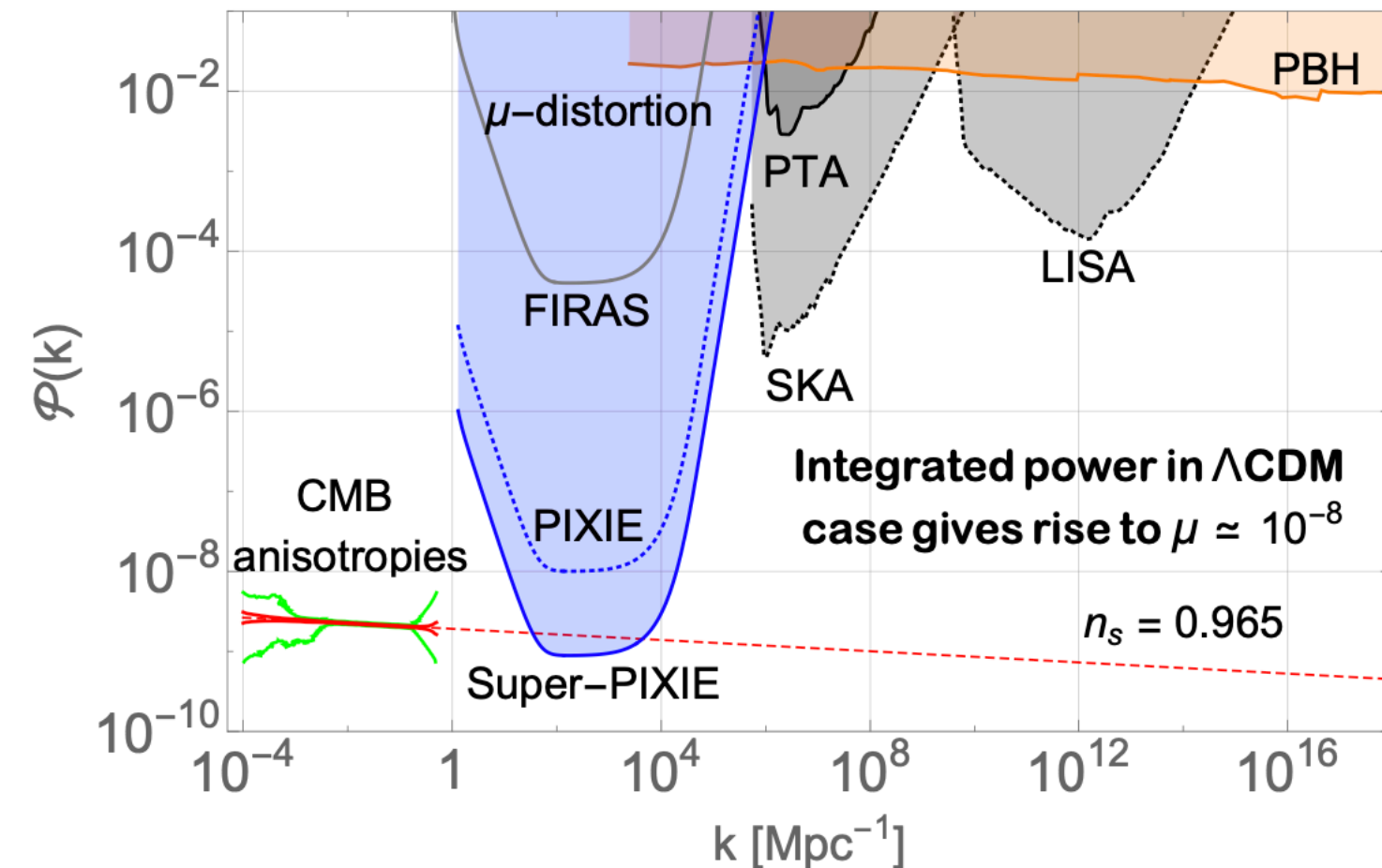
- Diffusion damping → superposition of BB with different temperature,  
→ reprocessed as  $\mu = 2 \times 10^{-8}$ ,  $y = 4 \times 10^{-9}$
- Transfer of energy from small-scale anisotropies to spectral distortions
- Accurately computed by CLASS
- Probe of  $P_{\mathcal{R}}(k)$  on very small scales

- Emission/absorption lines during H and He recombination: y-distorsions + small residuals

- Sunyaev-Zel'dovich effect from hot electrons during reionization →  $y \sim 10^{-6}$

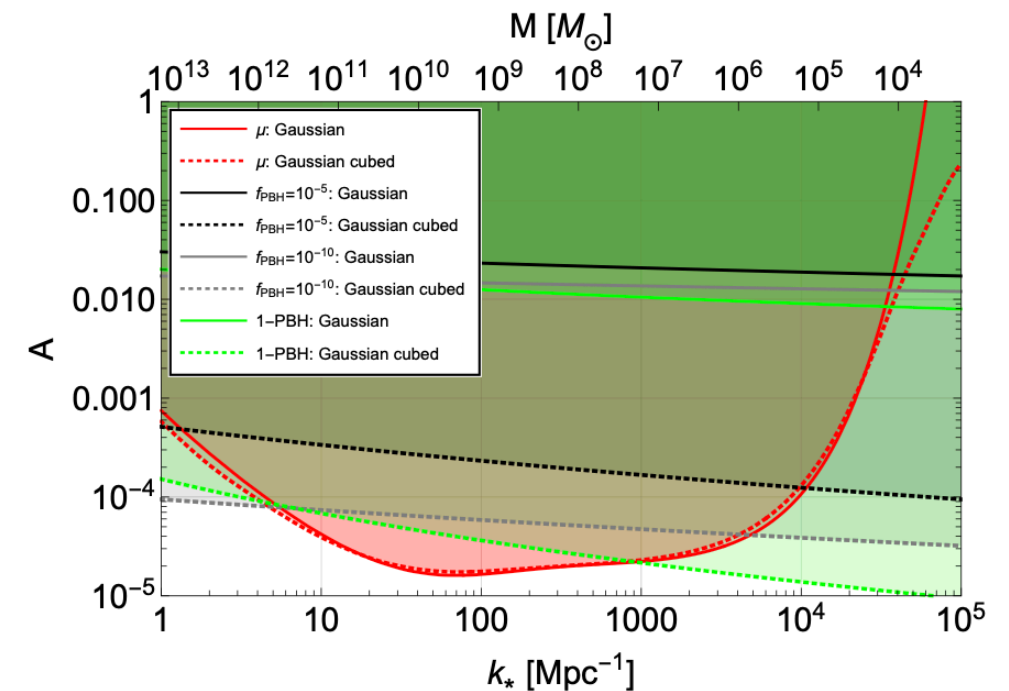
# Source of distortions in non-minimal cosmology

- Extra power in small-scale  $P_{\mathcal{R}}(k)$



J. Chluba et al., BAAS 51, 184 (2019), 1903.04218

Exclusion plots on peaks producing PBH



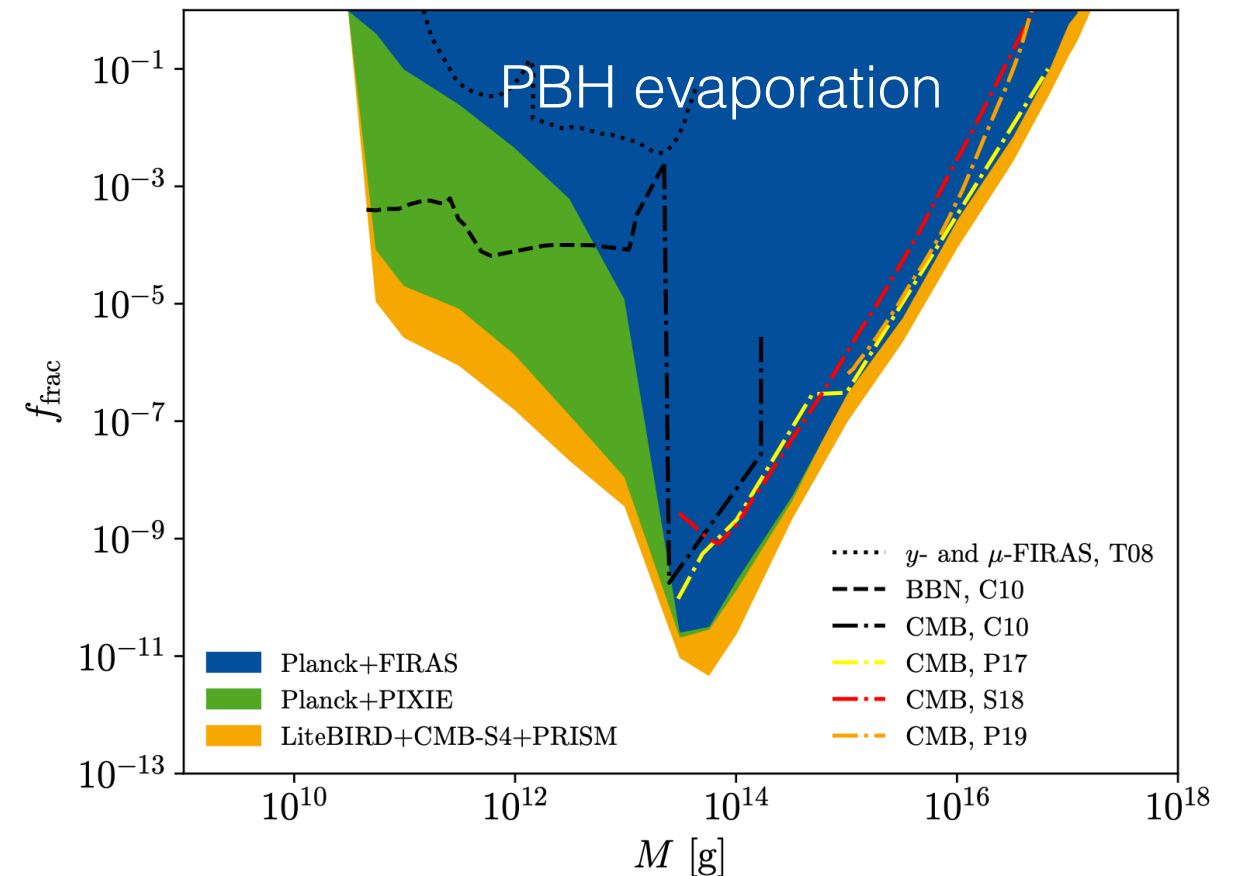
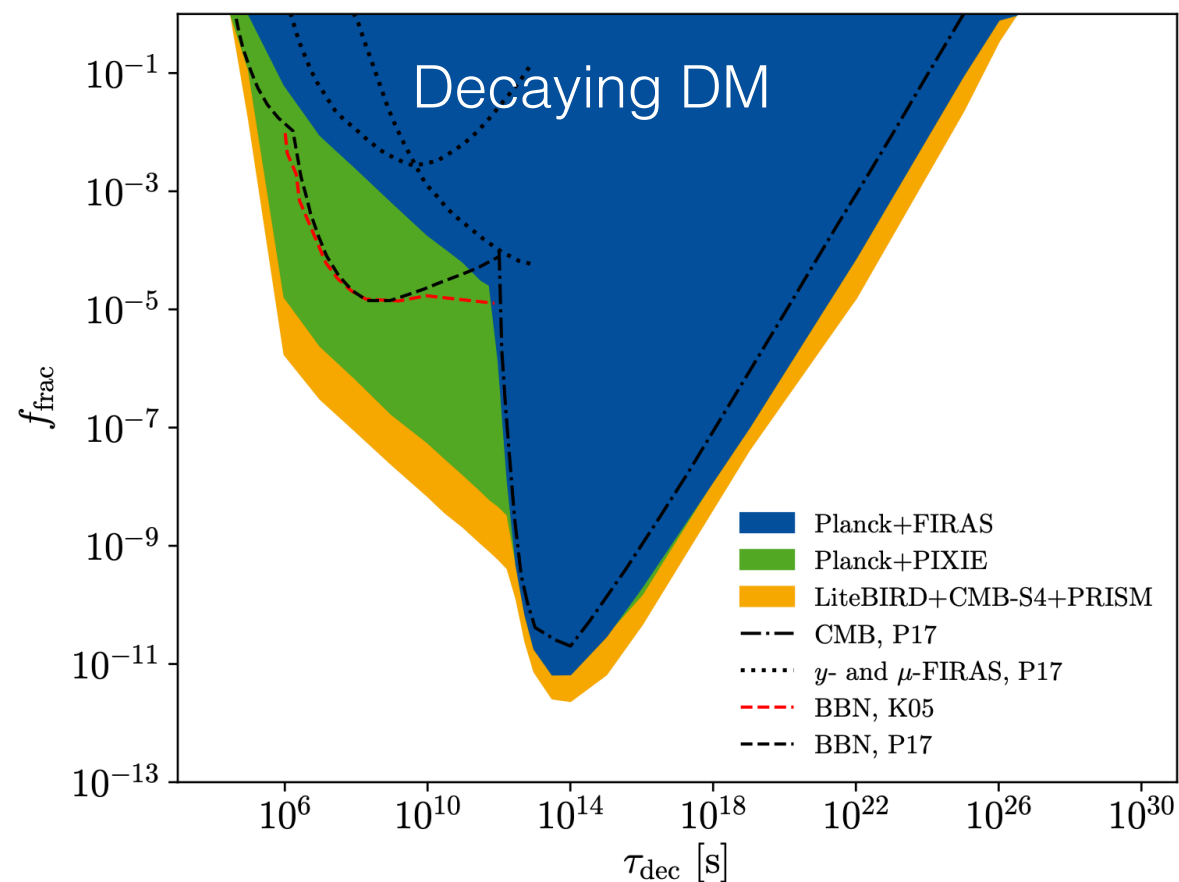
Pritchard, Byrnes, JL, Sharma 2505.08442

# Source of distortions in non-minimal cosmology

- DM annihilation or decay: products end up heating electrons
- PBH accretion or evaporation
- Other exotic energy injection mechanisms in dark sector

Lucca, Schöneberg, Hooper,  
JL, Chluba 1910.04619

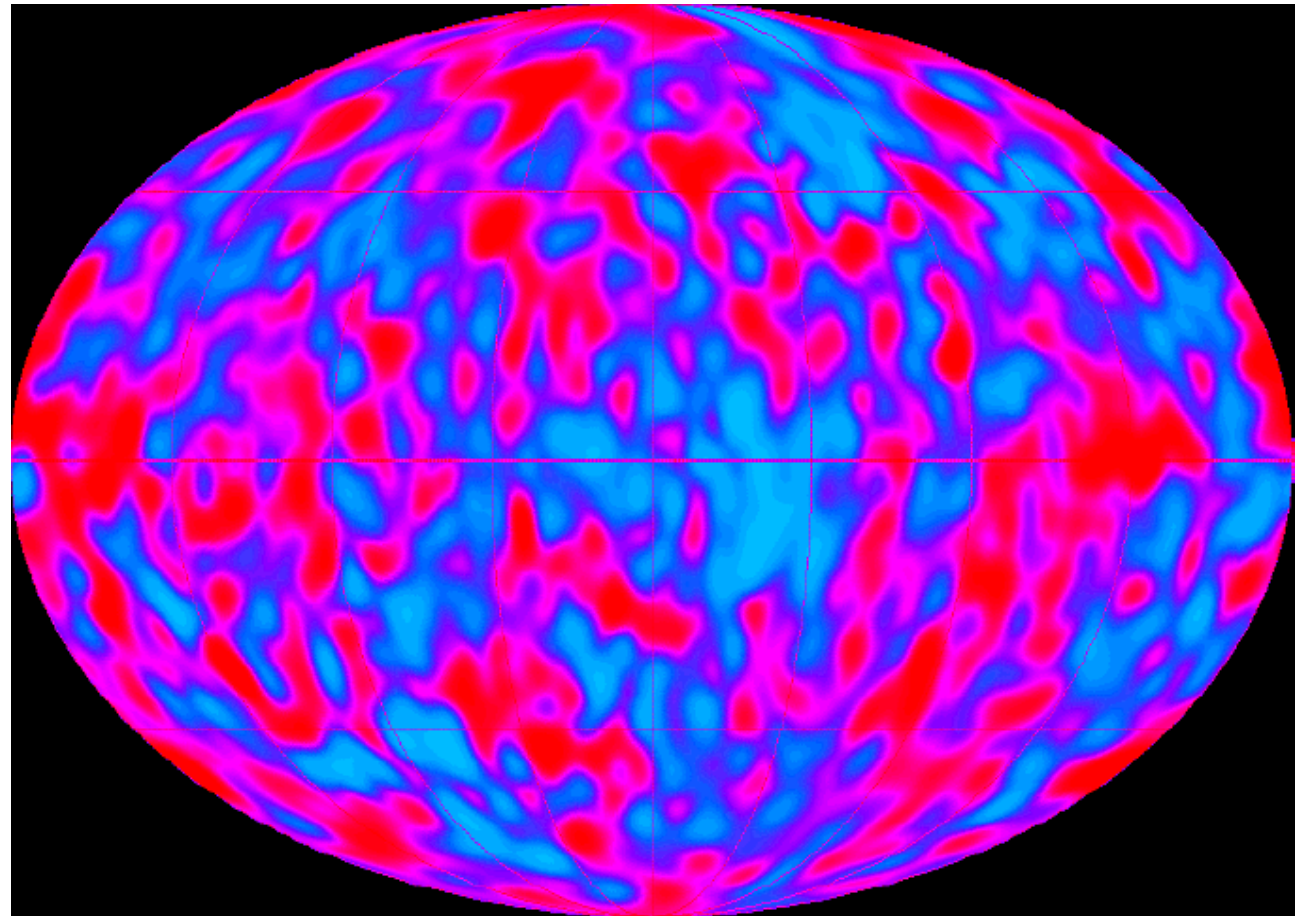
- also produces change in recombination, and thus CMB anisotropies...  
→ anisotropy/distortion synergy → distortion module in CLASS, ExoCLASS branch



# Observations

# From COBE to Planck

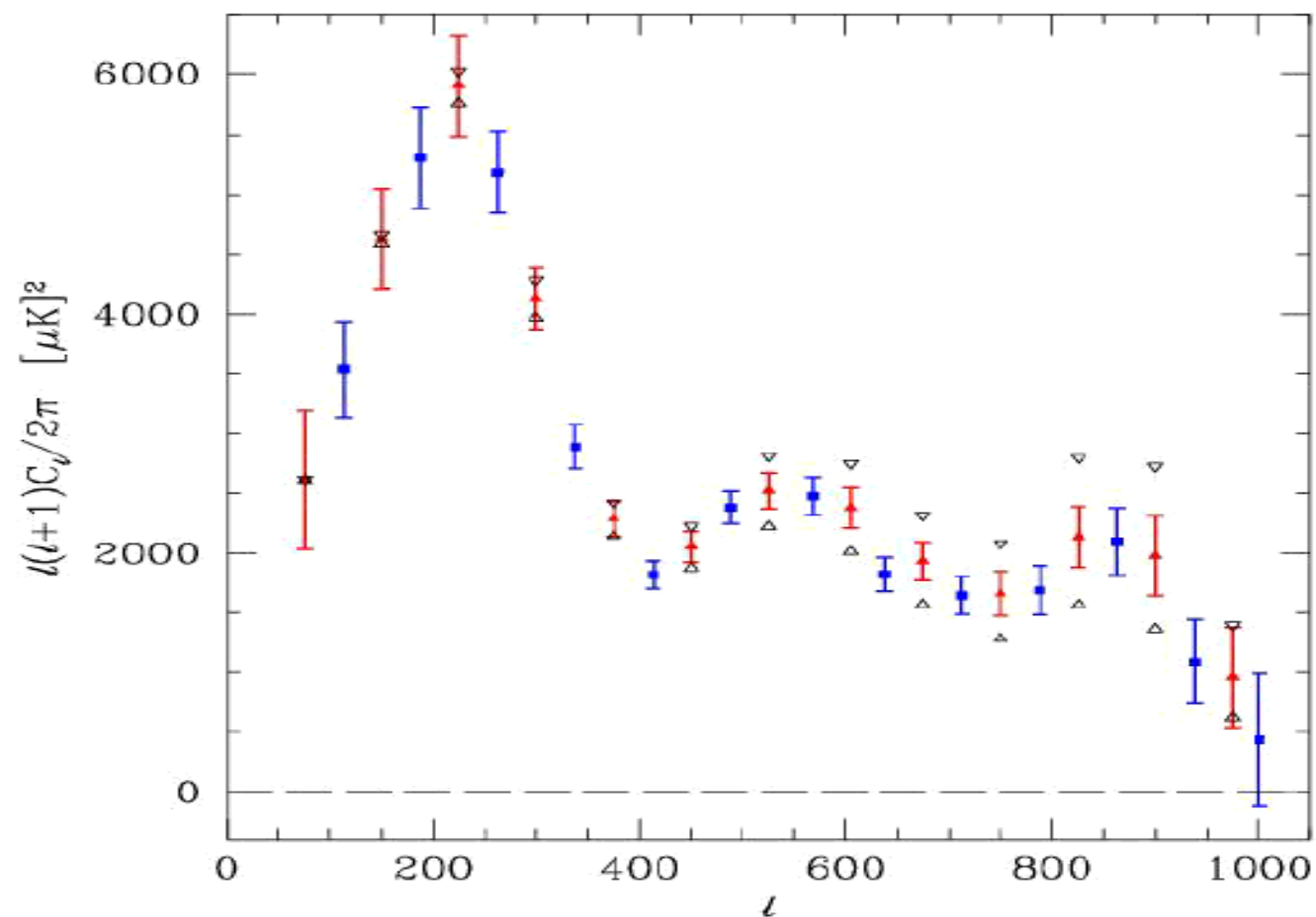
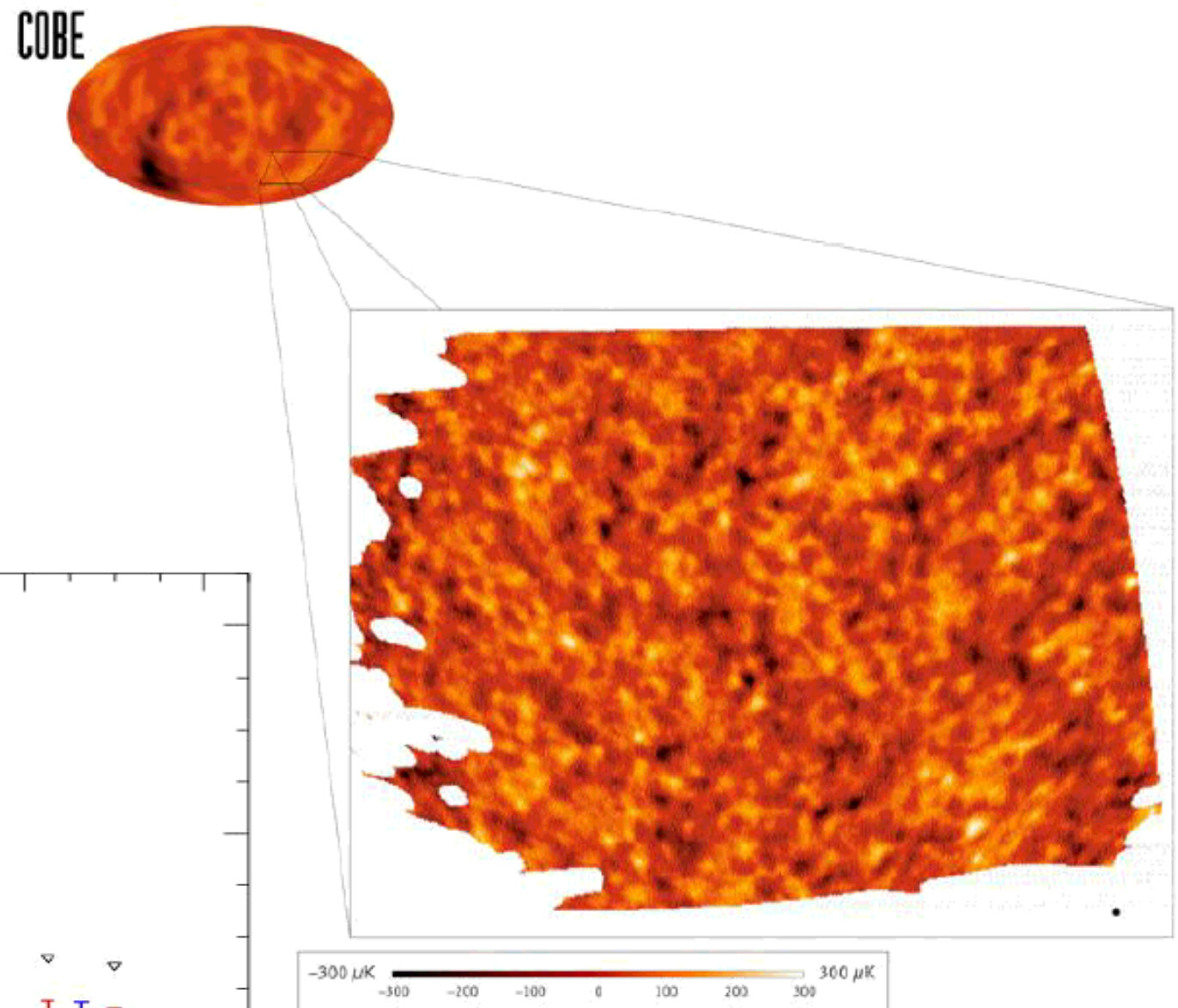
- CMB anisotropies:
  - 1992-94 : COBE confirms roughly flat spectrum for  $l < 20$
  - 2000 : Boomerang
  - 2003 -2011 : WMAP
  - 2013-2015 : Planck





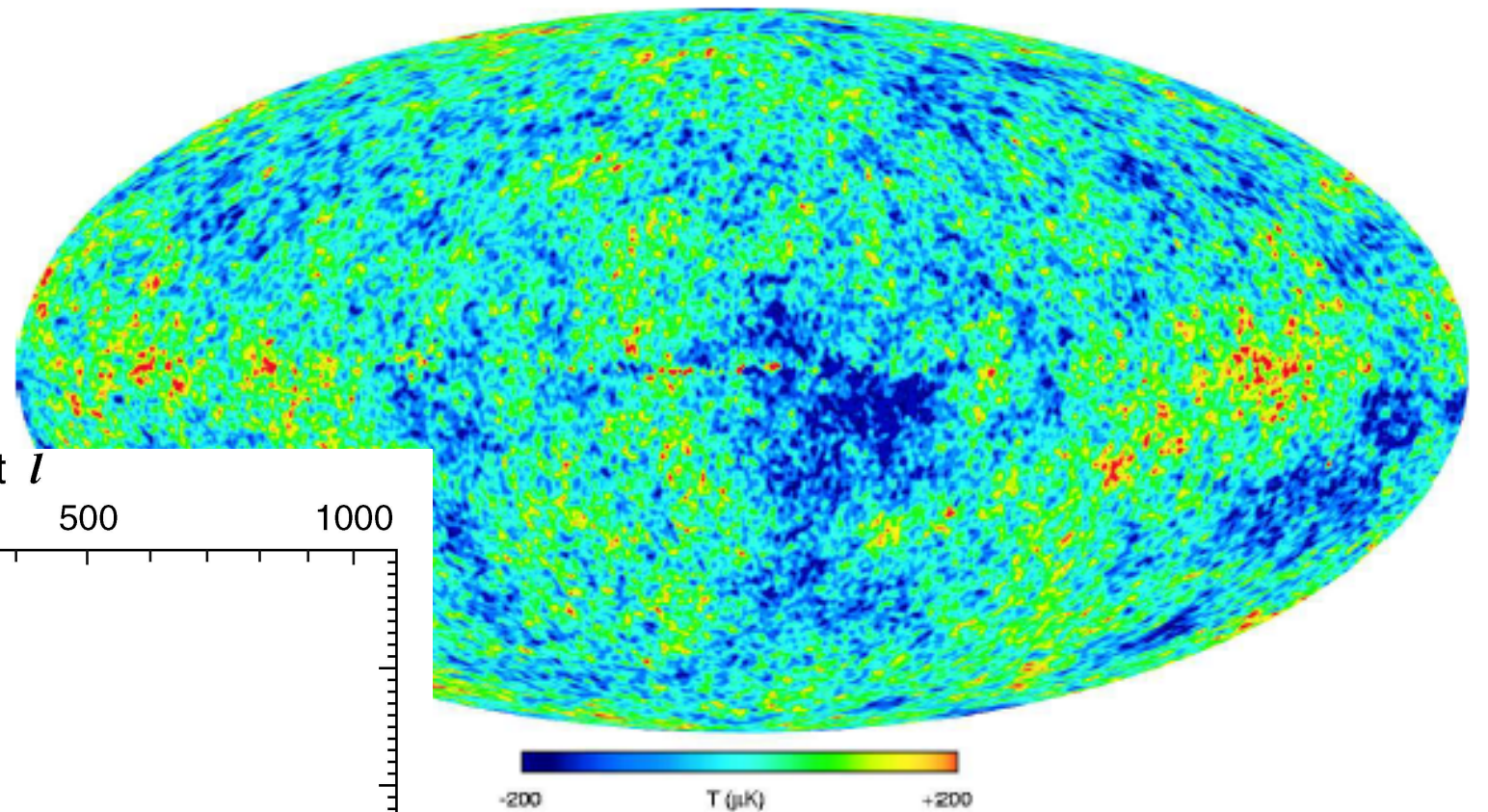
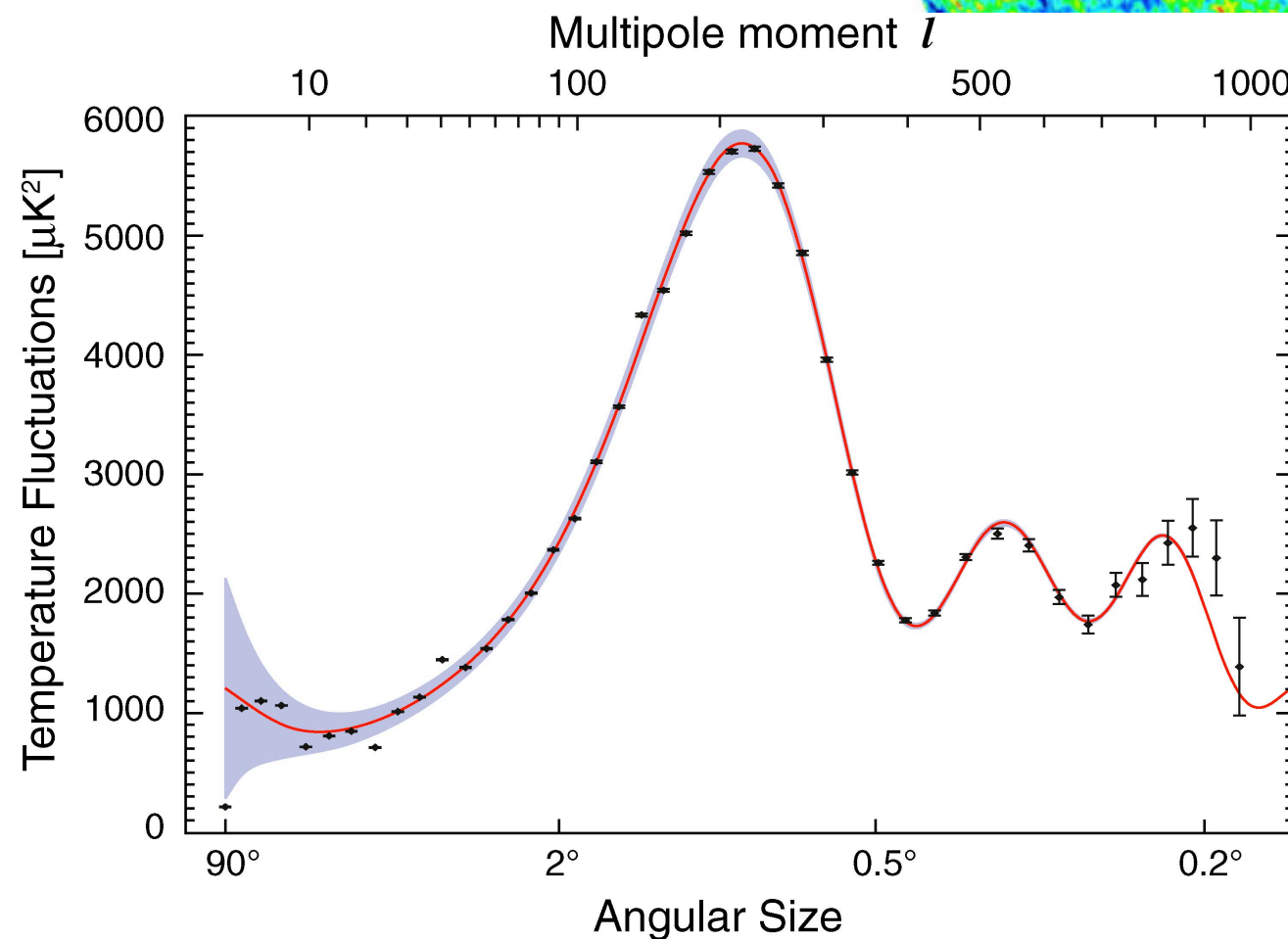
# CMB lensing

- CMB anisotropies:
  - 1992-94 : COBE
  - 2000 : Boomerang
  - 2003 -2011 : WMAP
  - 2013-2015 : Planck



# CMB lensing

- CMB anisotropies:
  - 1992-94 : COBE
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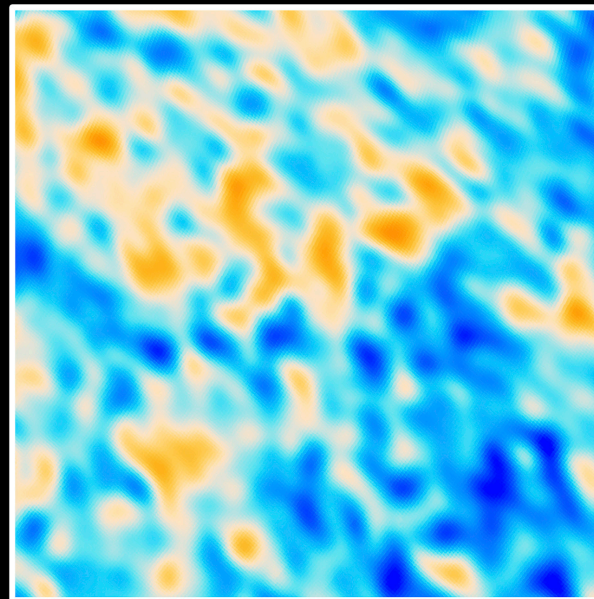
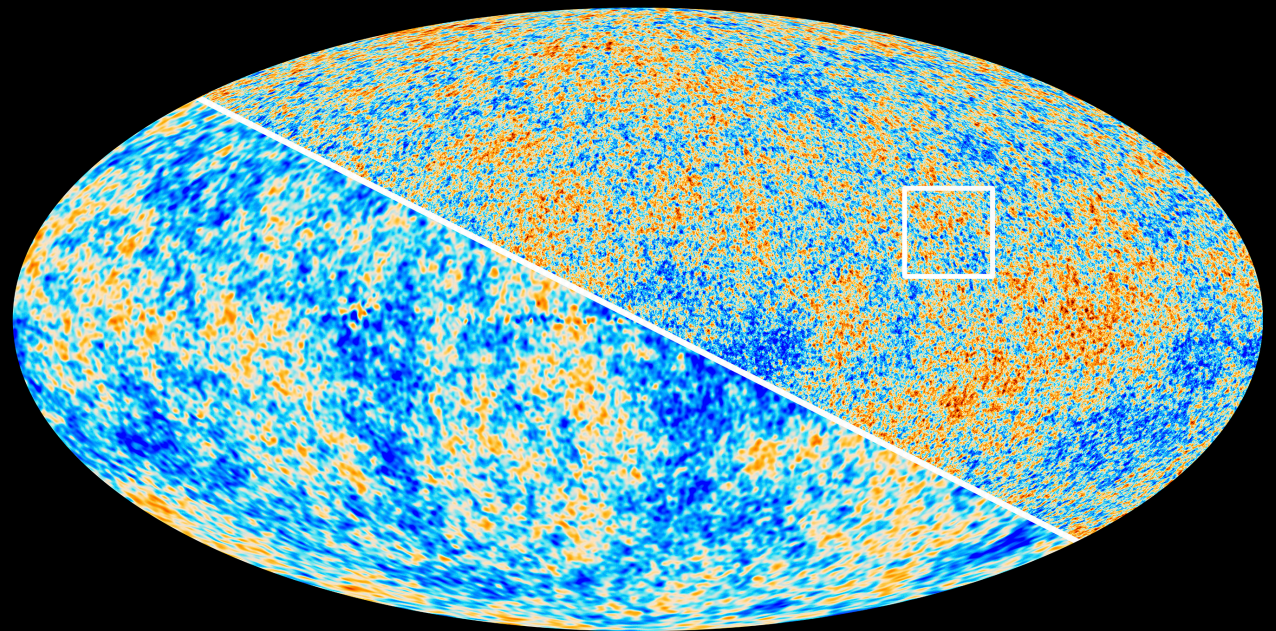




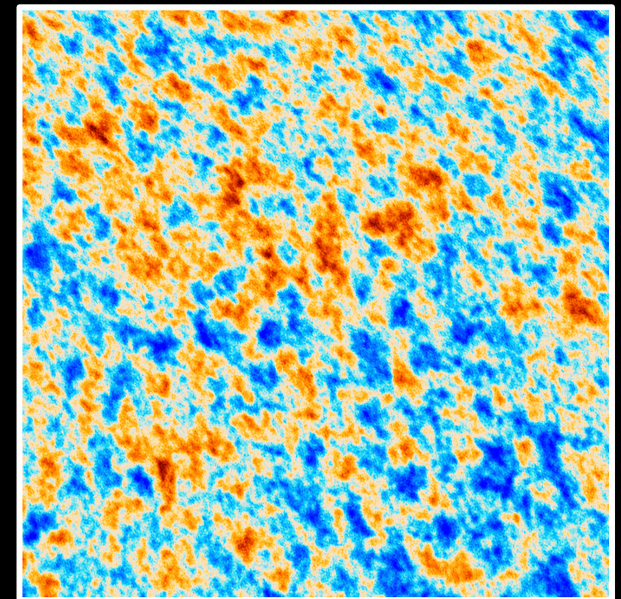
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- CMB anisotropies:
  - 1992-94 : COBE
  - 2000 : Boomerang
  - 2003 -2011 : WMAP
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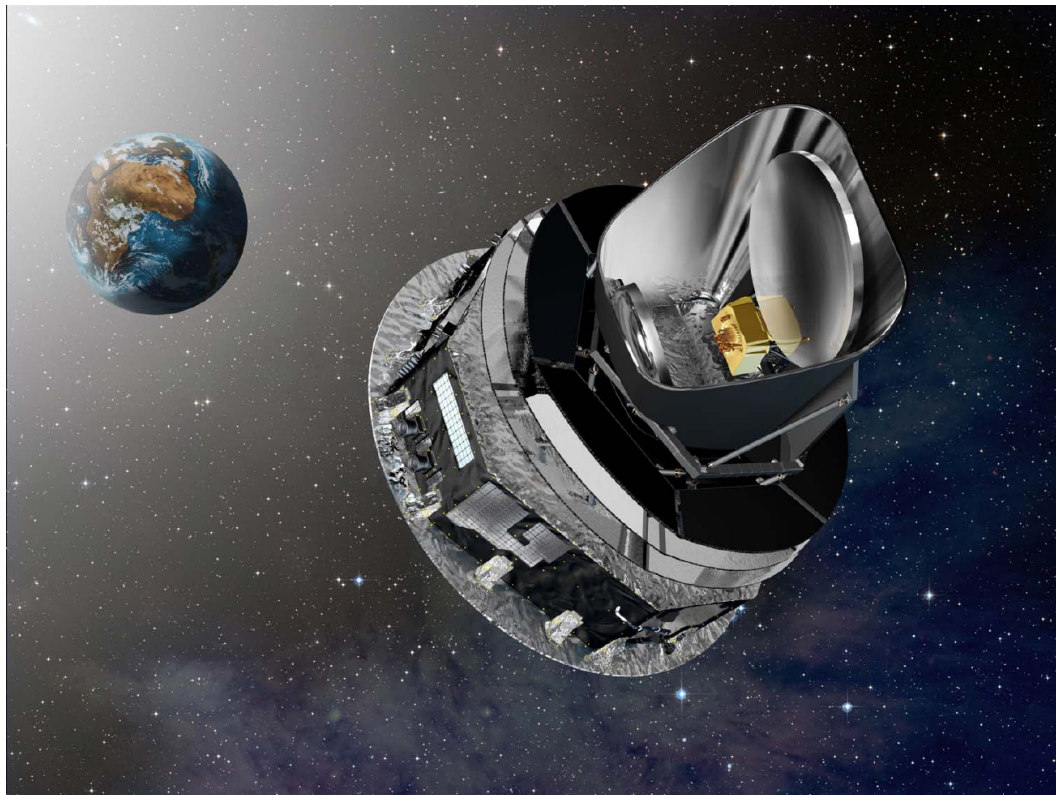
*The Cosmic Microwave Background as seen by Planck and WMAP*



**WMAP**

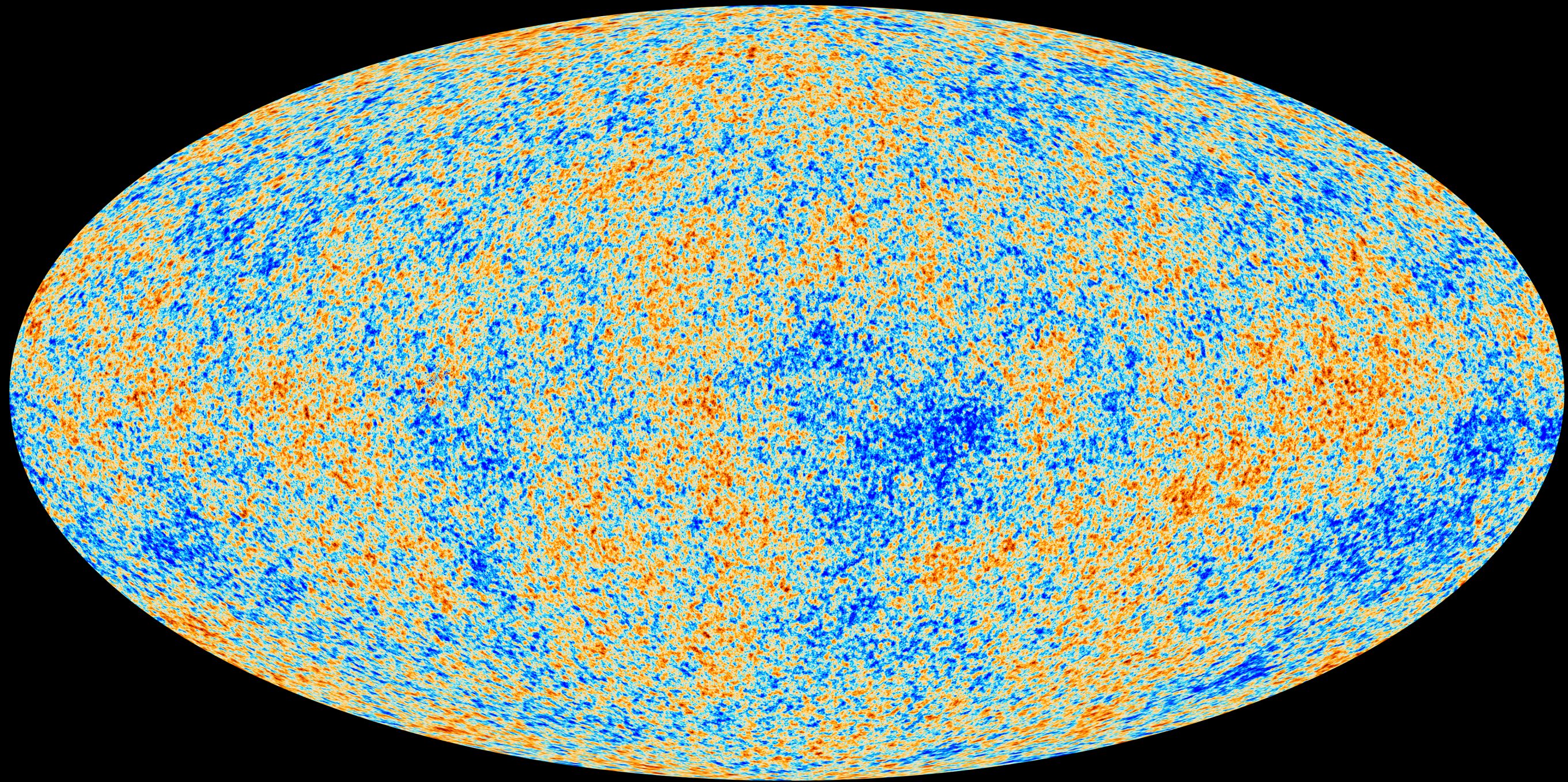


**Planck**



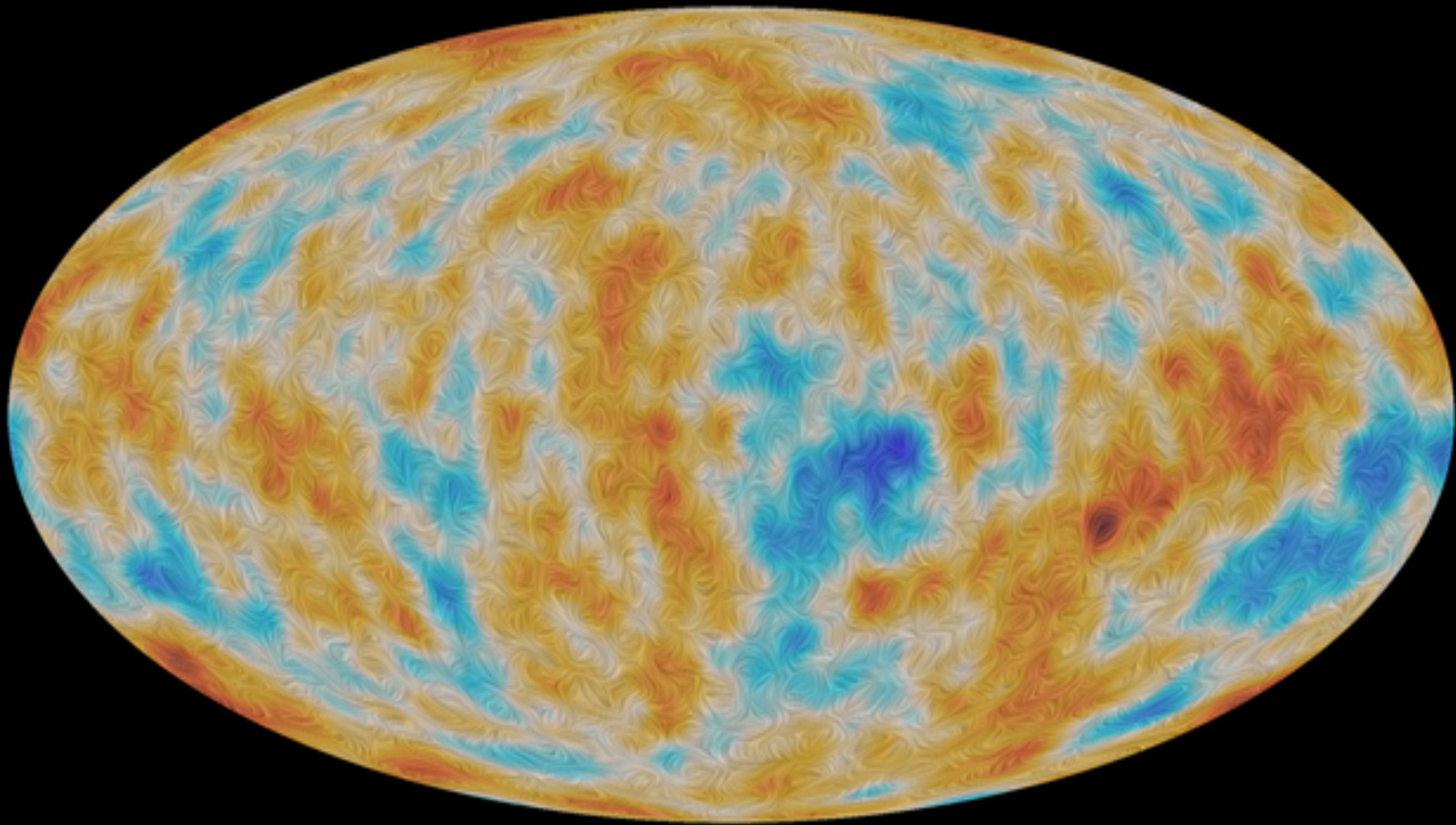


# Three main observables



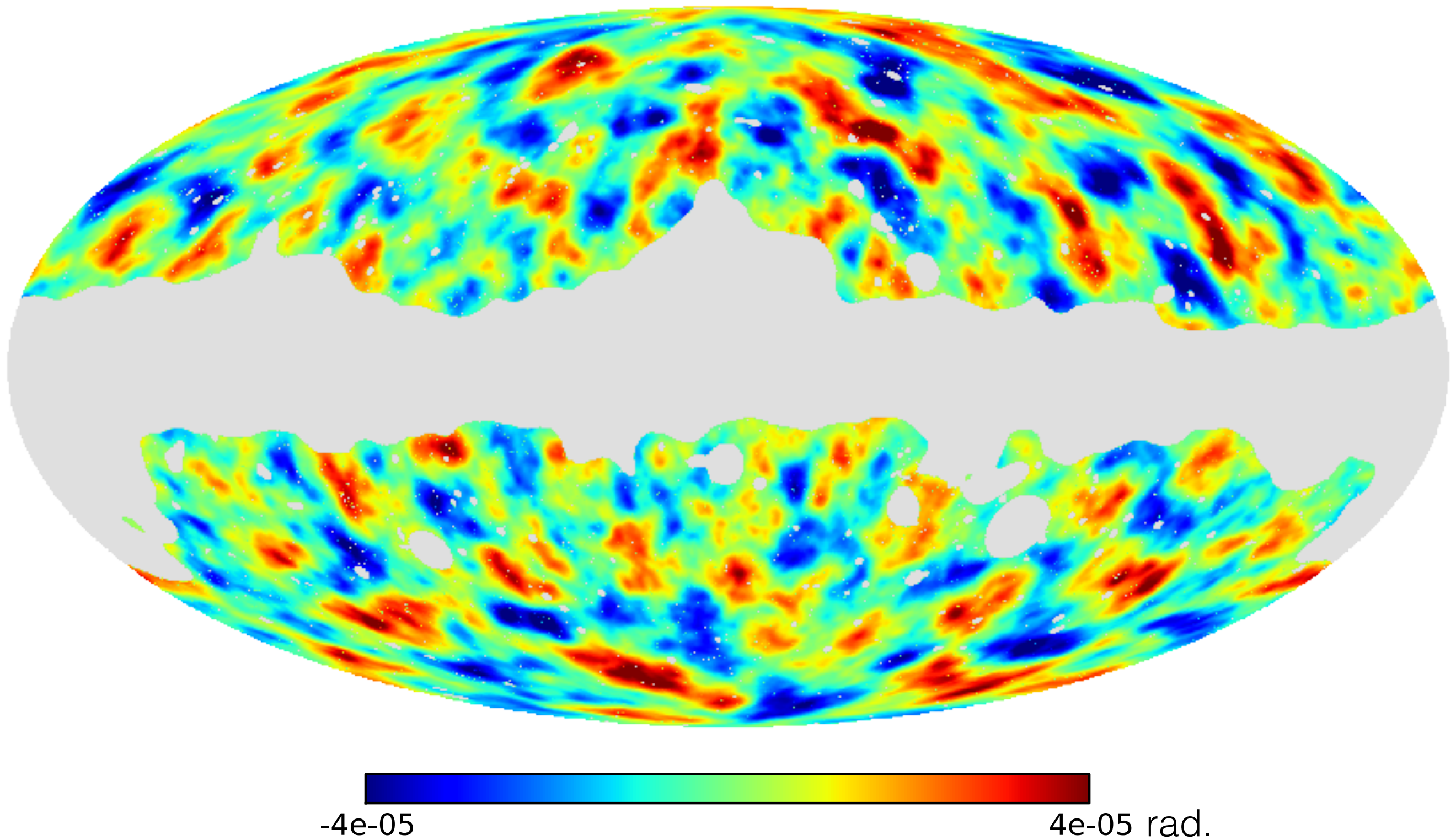


# Three main observables

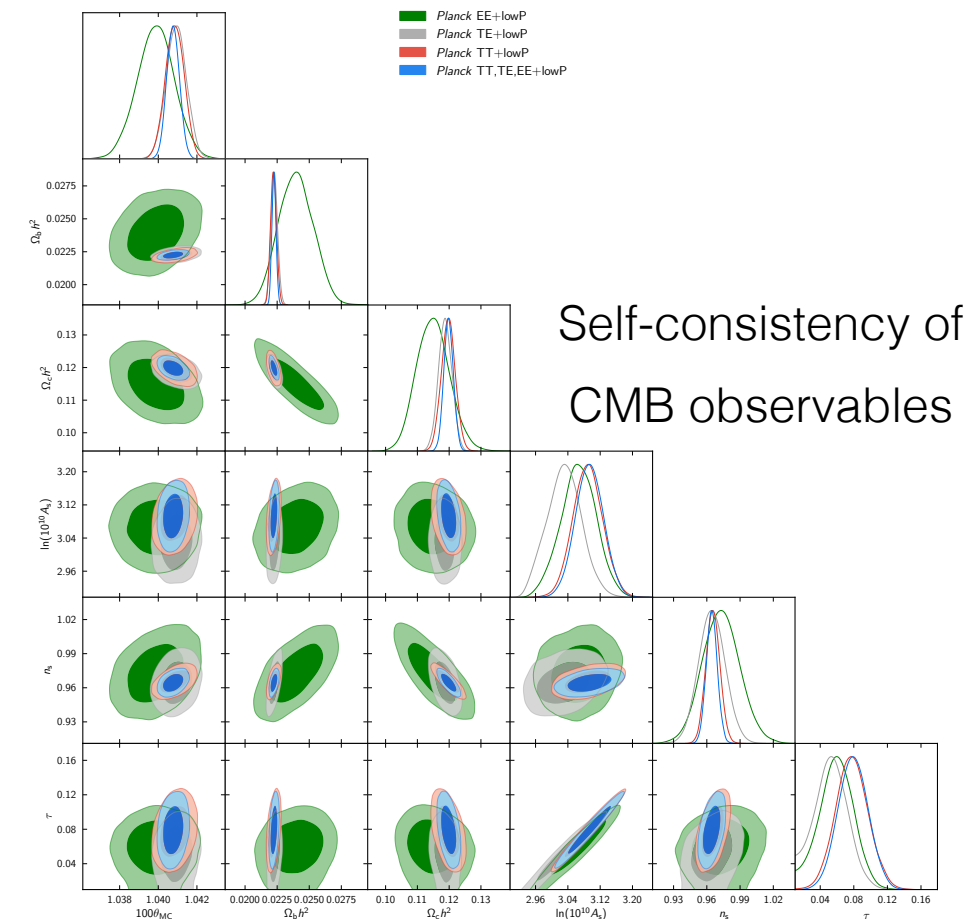
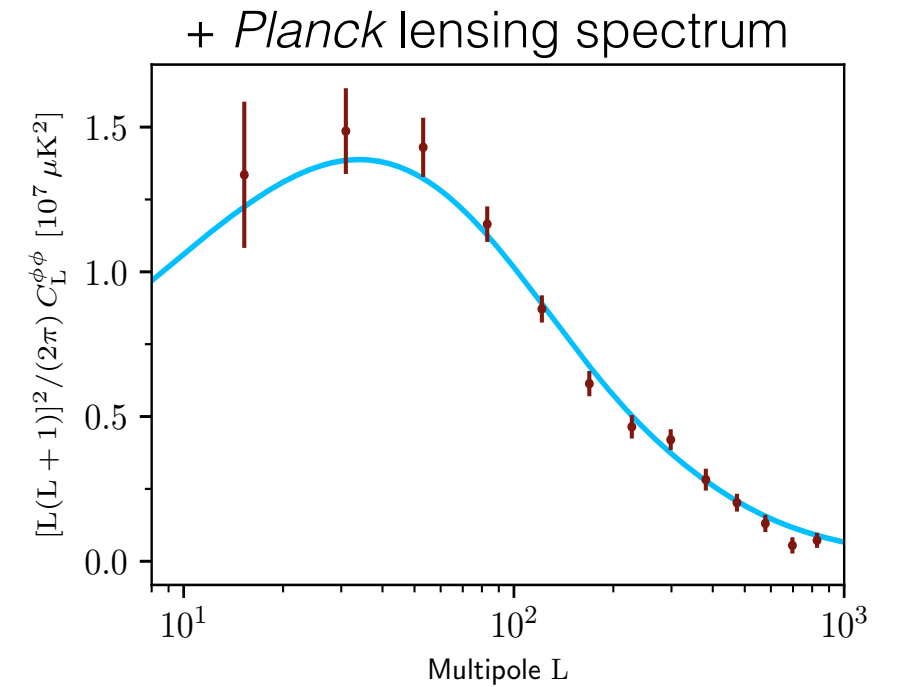
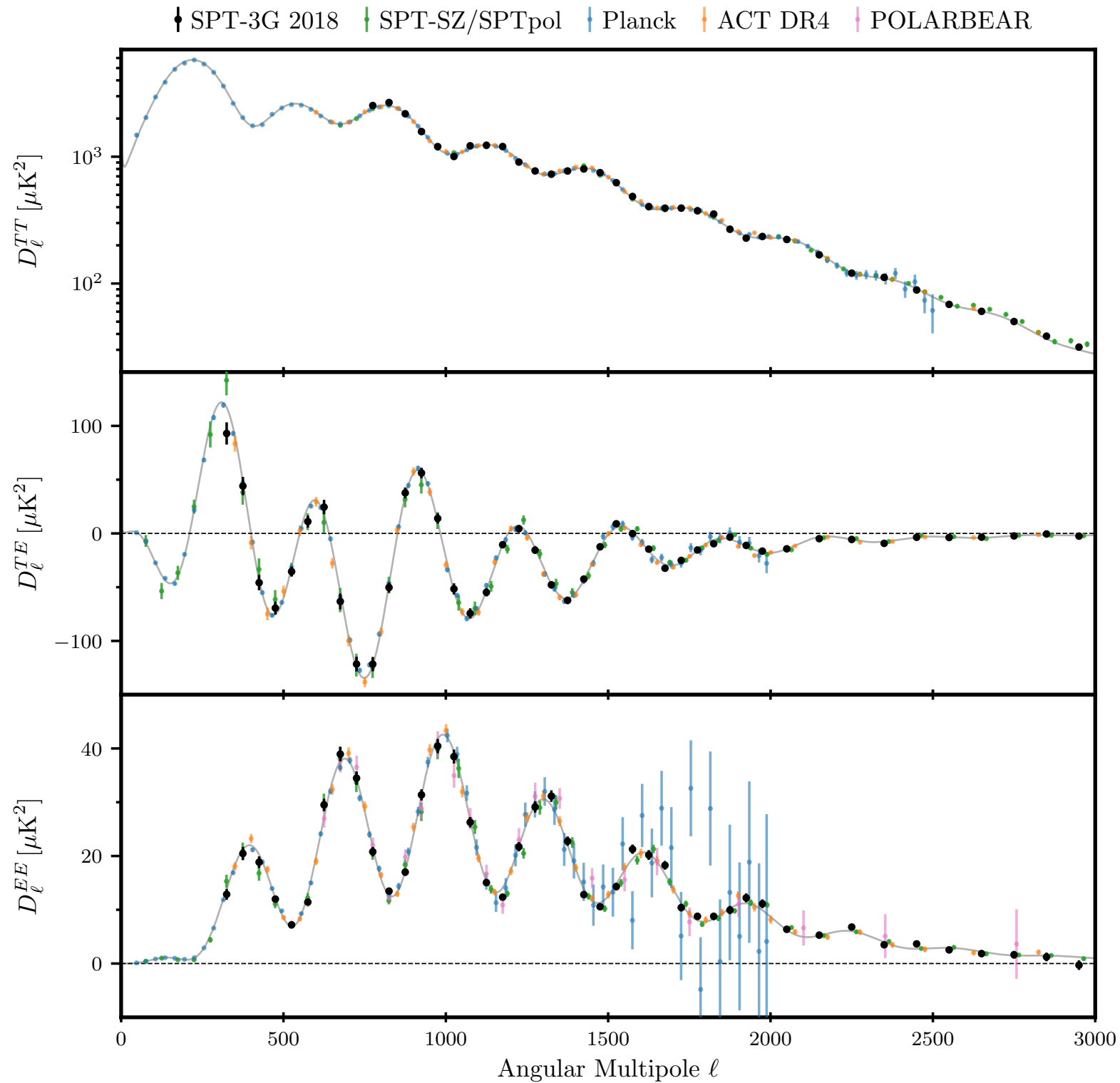




# Three main observables



# Most recent results



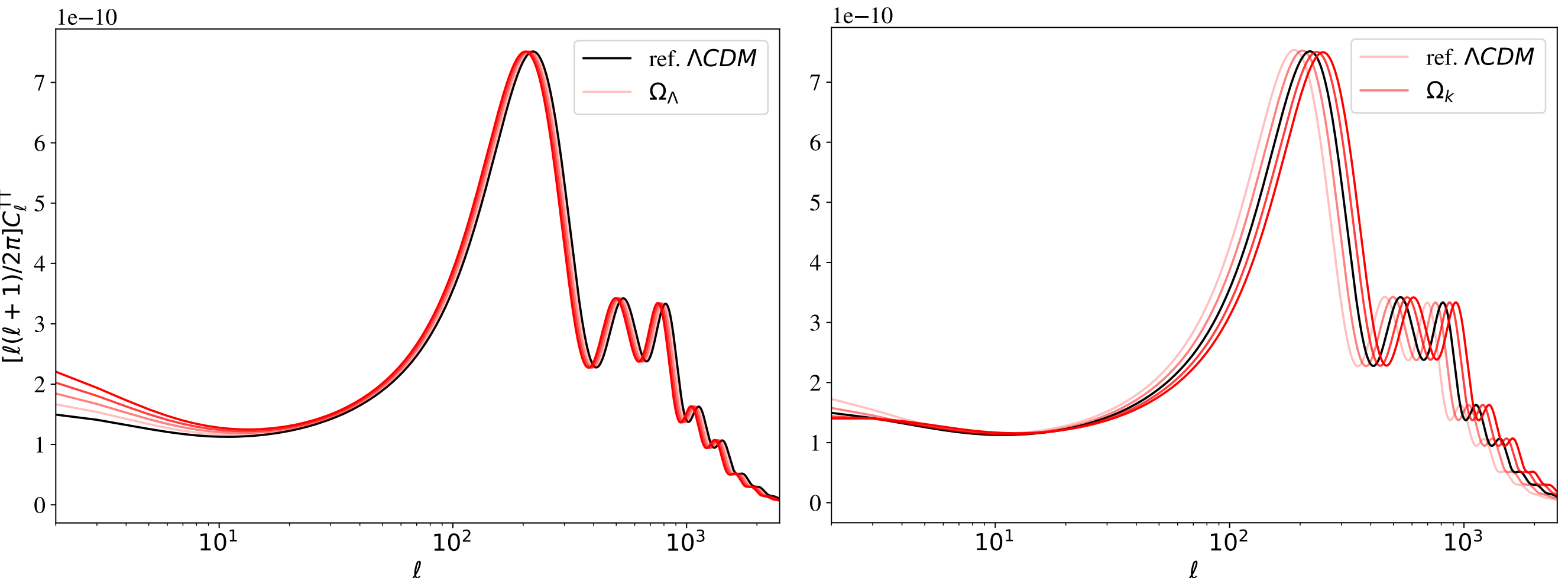
# Most recent $\Lambda$ CDM results from Planck 2018 + SPT-3G

Flat,  $M_\nu$  fixed to 0.06eV, 68%CL

$\tau_{\text{reio}}$ (Planck only)	$0.0540 \pm 0.0074$	← consistent with quasars (Gunn-Peterson, ...)
SPT-3G 2018 + <i>Planck</i>		
$\Omega_b h^2$	$0.02233 \pm 0.00013$	← consistent with BBN
$\Omega_c h^2$	$0.1201 \pm 0.0012$	← $100\sigma$ detection
$100\theta_{\text{MC}}$	$1.04075 \pm 0.00028$	
$10^9 A_s e^{-2\tau}$	$1.884 \pm 0.010$	
$n_s$	$0.9649 \pm 0.0041$	← consistent with inflation
$H_0$ [km s <sup>-1</sup> Mpc <sup>-1</sup> ]	$67.24 \pm 0.54$	← consistent with BAO+BBN but not with distance ladder
$\sigma_8$	$0.8099 \pm 0.0067$	
$S_8 \equiv \sigma_8 \sqrt{\Omega_m/0.3}$	$0.832 \pm 0.014$	← small tension with weak lensing?
$\Omega_\Lambda$	$0.6835 \pm 0.0075$	← consistent with remote SNIa
Age/Gyr	$13.807 \pm 0.021$	← consistent with age data

# Results beyond $\Lambda$ CDM

- spatial curvature  $\Omega_k$

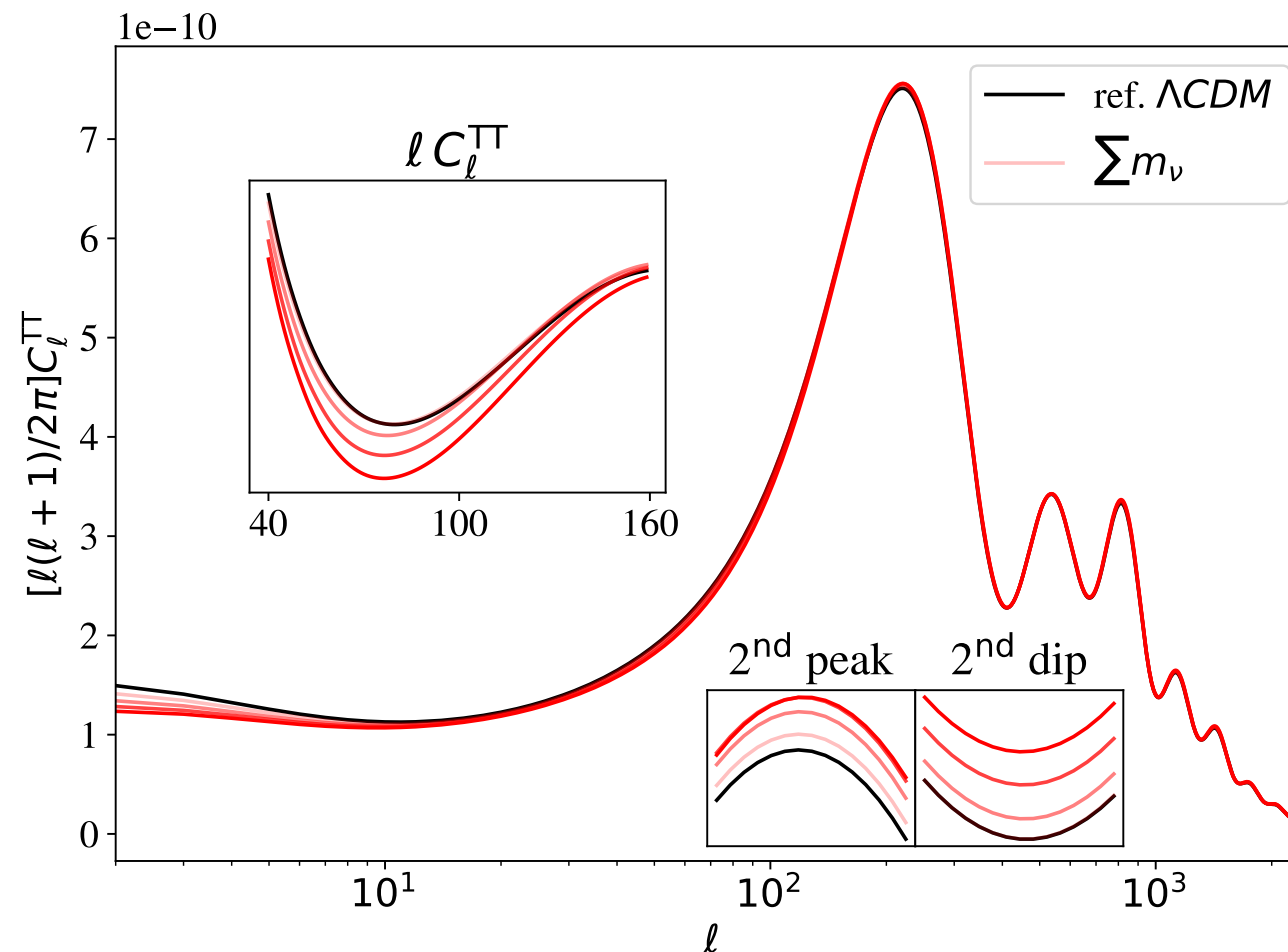


In  $\Lambda$ CDM +  $\Omega_k$ , same 8 effects only, but tight to 7 parameters: CMB also measures  $\Omega_k$

Parameter	<i>Planck</i> alone	<i>Planck</i> + BAO	
$\Omega_K$ . . . . .	$-0.0096 \pm 0.0061$	$0.0007 \pm 0.0019$	95% CL

# Results beyond $\Lambda$ CDM

- Total neutrino mass  $M_\nu$



In  $\Lambda$ CDM +  $M_\nu$  , new effects (early ISW, extra lensing)

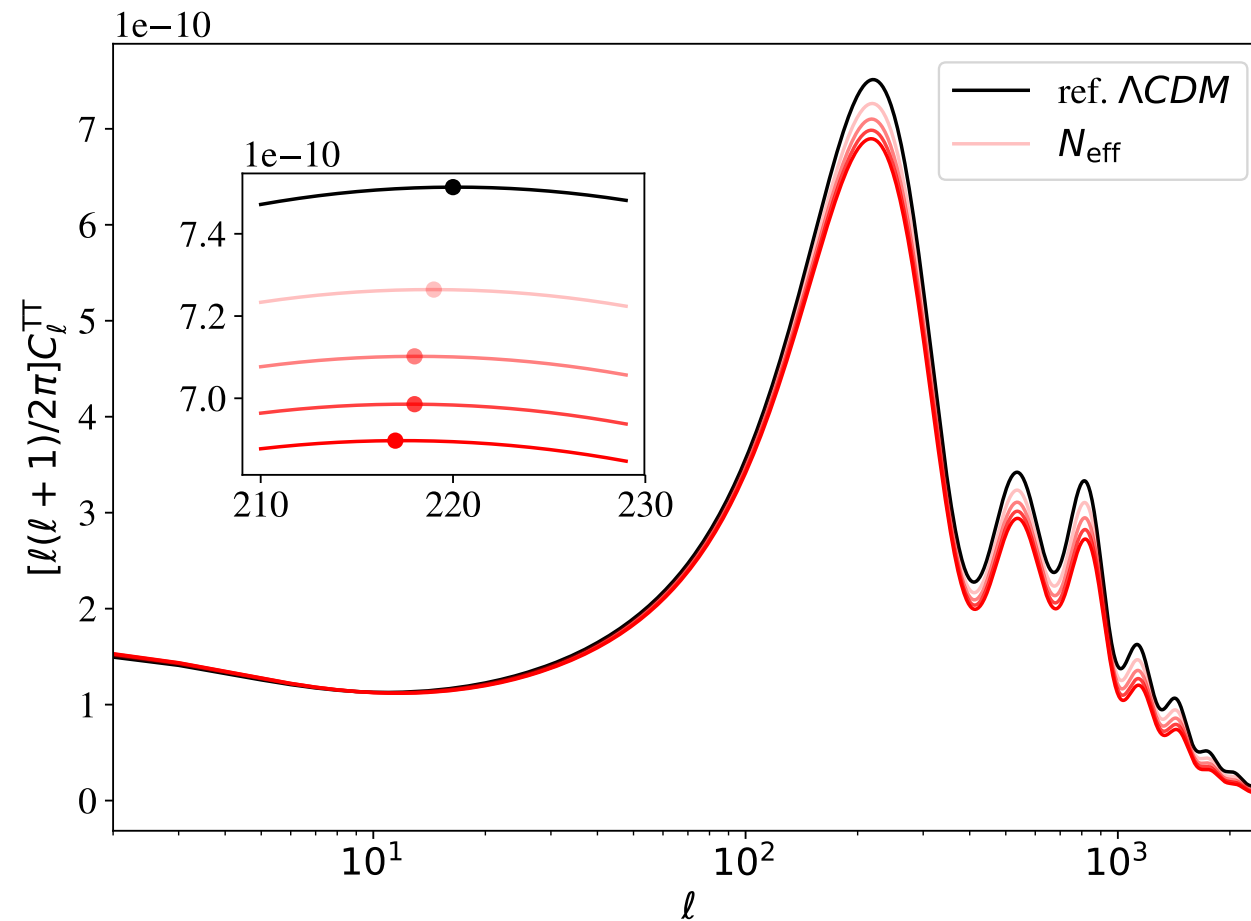
Parameter	<i>Planck</i> alone	<i>Planck</i> + BAO
$\Sigma m_\nu$ [eV] . . . . .	< 0.241	< 0.120

95% CL



# Results beyond $\Lambda$ CDM

- Density of relativistic relics in units of neutrino density,  $N_{\text{eff}}$



In  $\Lambda$ CDM +  $N_{\text{eff}}$ , new effects (peak shift, damping scale relative to sound scale)

Parameter	<i>Planck</i> alone	<i>Planck</i> + BAO	
$N_{\text{eff}}$ . . . . .	$2.89^{+0.36}_{-0.38}$	$2.99^{+0.34}_{-0.33}$	95% CL

# Observational constraints on $\Lambda$ CDM + r

$\Lambda$ CDM + r

$\Lambda$ CDM + r + running

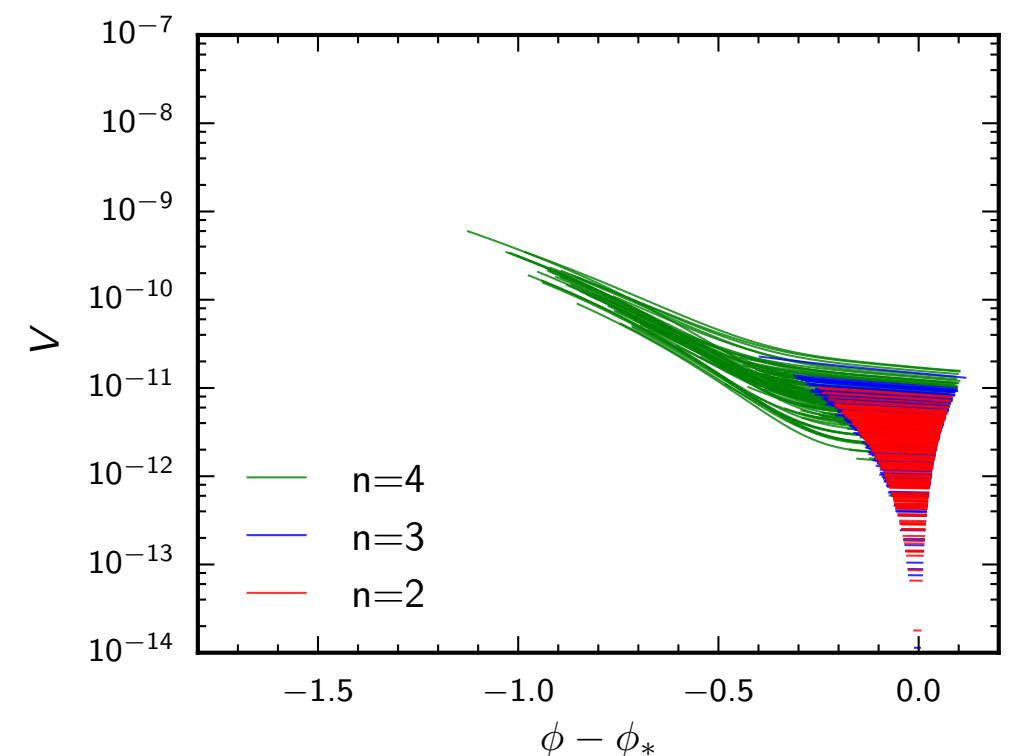
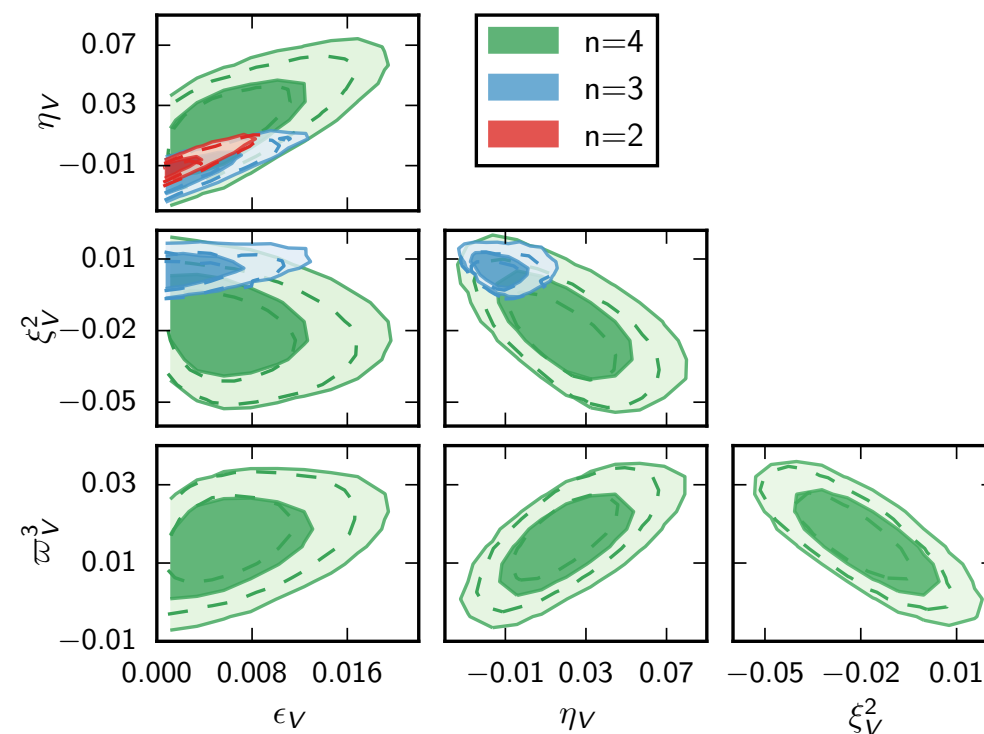
$\Lambda$ CDM + r + running + running of the running

$\Lambda$ CDM + r + primordial spectra with parametrised features

$\Lambda$ CDM + r + binned primordial spectra

$\Lambda$ CDM + r + parametrised inflation potential

$\Lambda$ CDM + r + isocurvature modes  
etc.



Planck 2015 XX constraints on inflation 1502.02114 (see also 1807.06211)

# Future observations

# Targets and future observations

- Current status with **Planck, ACT, SPTpol**...
  - temperature error bar below C.V. till  $l \sim 1800$
  - polarisation error bar below C.V. till  $l \sim 700$
- Future objectives:
  - Low- $l$  polarisation:
    - primordial B-mode,  $r$ , inflation,  $\tau_{\text{reio}}$ , reionisation
    - **LiteBIRD** (JAXA) ( $\sigma(r_{0.01}) \sim 0.003$ )
  - High- $l$  polarisation:
    - polarisation peak scale and damping tail,  $N_{\text{eff}}$ , exotic models (EDE, shifted recombination, etc.)
    - lensing,  $M_\nu$ , exotic models (non-standard neutrino/DM, modified gravity, EDE, shifted recombination, etc.)
    - **Simons Observatory, CMB-S4** ( $\sigma(N_{\text{eff}}) \sim 0.04$ )

**THE END**



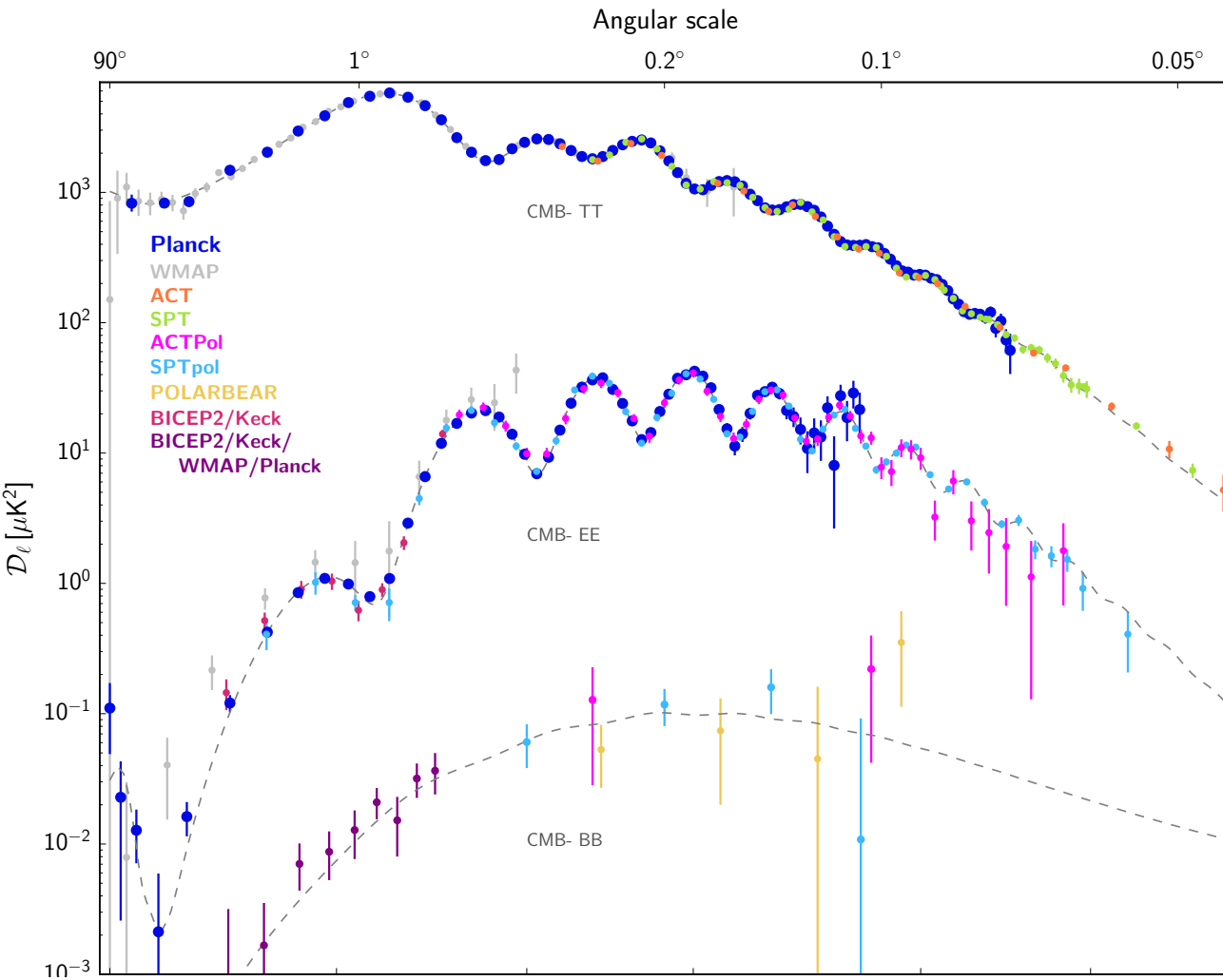
## Books:

- *The Young Universe: Primordial Cosmology*,  
edited by R. Taillet (John Wiley & Sons, 2022) ISBN : 1789450322  
→ Chapter 2: Cosmological Microwave Background, by JL
- *Neutrino cosmology*,  
JL, G. Mangano, G. Miele, S. Pastor (Cambridge University Press 2013)  
→ Chapter 5: Cosmological Microwave Background, by JL

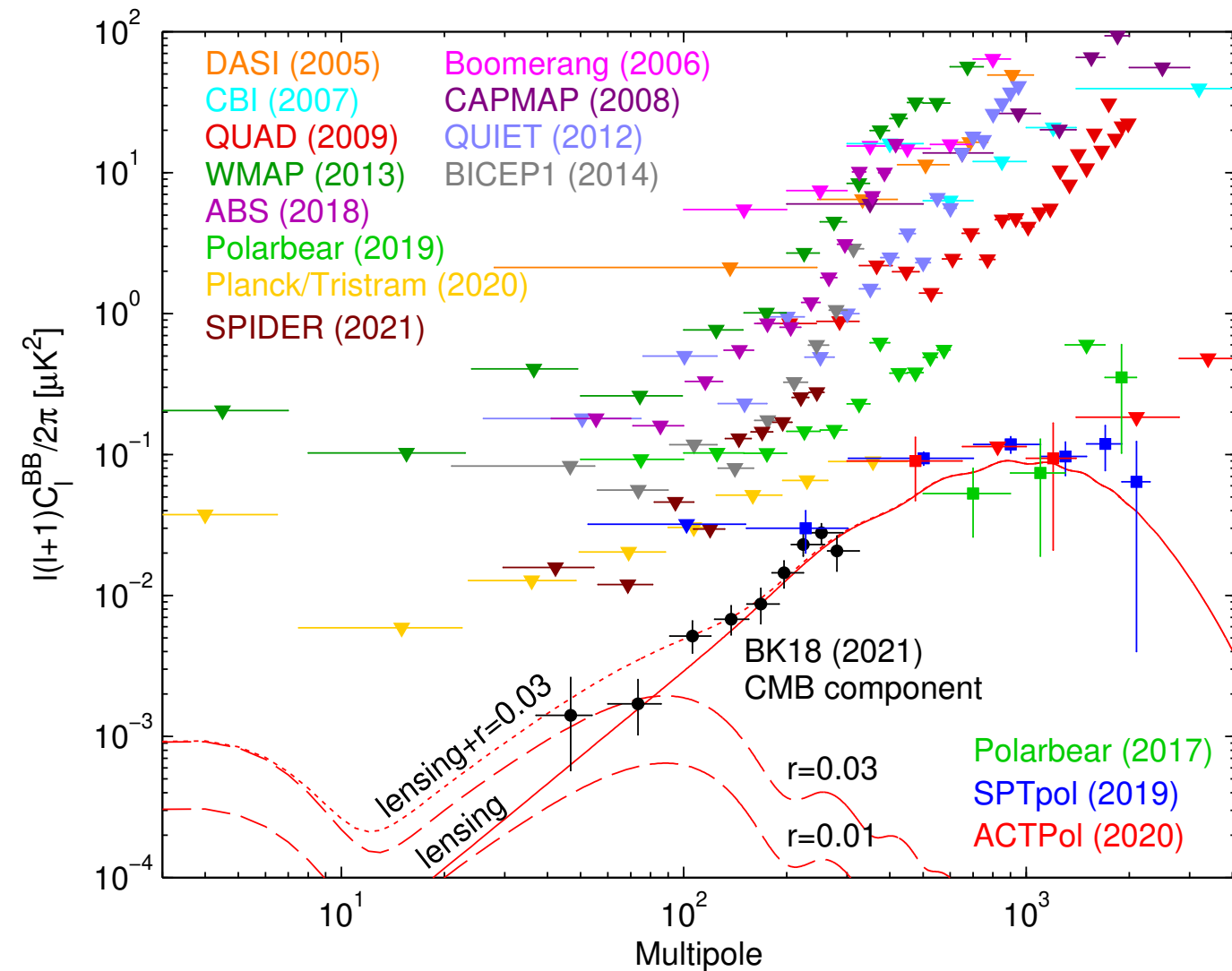
## Notes from Master course on advanced Cosmology:

- *The Ingredients of the Universe*,  
JL, course at RWTH Aachen University  
1. Recalls on homogeneous cosmology  
2. Thermal history of the Universe  
3. Linearised gravity  
4. Inflation  
5. CMB anisotropies  
6. Large Scale Structure
- > [link on Indico page of this school](#)

# Scalar versus tensor spectra



data summary on TT, EE, BB



small-l BB measurements

(Bicep/Keck 2110.00483)

Tensor-to-scalar ratio  $r$ :  $r_{0.005} < 0.030$  } (95% CL, *Planck* TT,TE,EE  
 $r_{0.02} < 0.098$  } +lowE+lensing+BK18).

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