

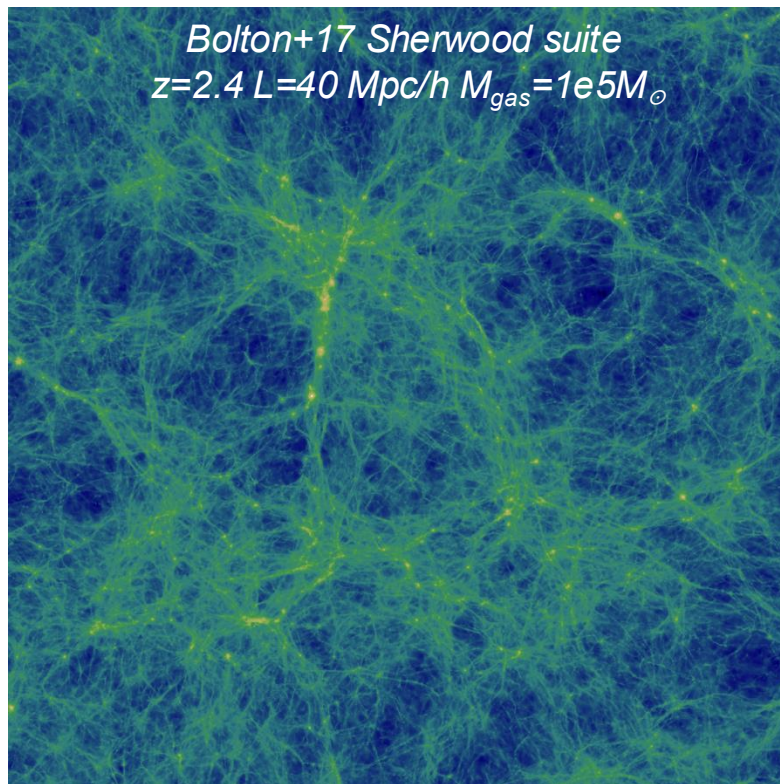
Cosmology with the Ly α forest

Matteo Viel - SISSA (Trieste, Italy)

GGI - 30/9/2025



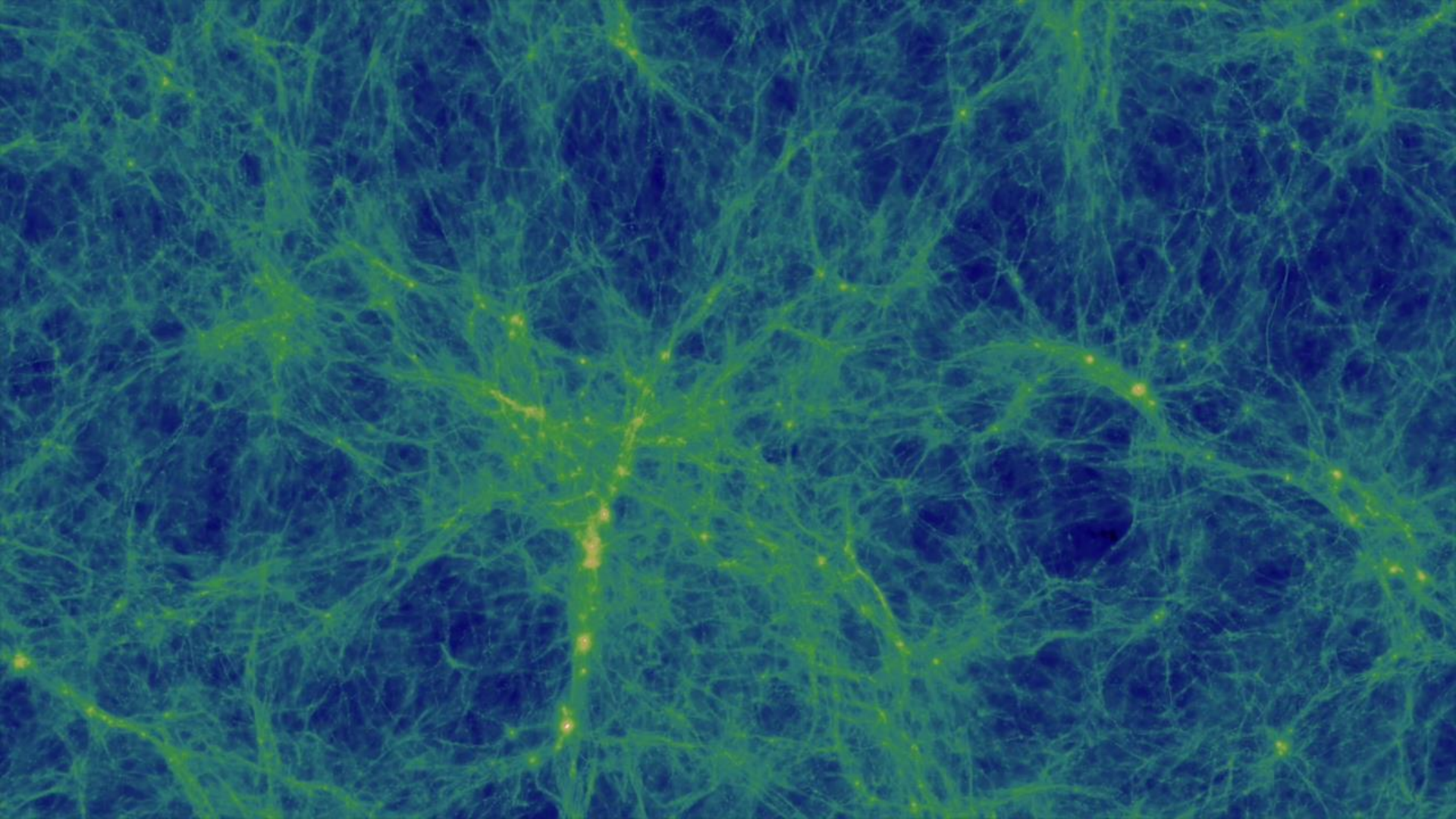
Intro: the simple physics of the cosmic web



Intergalactic Cosmic Web

- ✓ Filamentary gaseous cosmic web as predicted in Λ CDM hydro sims
- ✓ Key physics relatively simple: **gas cooling** and **heating** by a (uniform) **UV background** in an **expanding Universe**
- ✓ Physical properties can be derived by assuming two physical fluids (DM and gas) evolving, with the latter having its pressure (Jeans scale)

Bi & Davidsen 1997, Schaye 2001, Gnedin & Hui 98



Physics of the gas: filtering scale

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DM

$$\frac{d^2\delta_X}{dt^2} + 2H\frac{d\delta_X}{dt} = 4\pi G\bar{\rho}(f_X\delta_X + f_b\delta_b), \quad k_J = \frac{a}{c_S} \sqrt{4\pi G\bar{\rho}}.$$

GAS

$$\frac{d^2\delta_b}{dt^2} + 2H\frac{d\delta_b}{dt} = 4\pi G\bar{\rho}(f_X\delta_X + f_b\delta_b) - \frac{c_S^2}{a^2}k^2\delta_b$$

Thermal history

Equation of motion of
gas element

$$\frac{d\mathbf{v}}{dt} + H\mathbf{v} = -\nabla\phi - \frac{1}{\rho}\nabla P, \quad \psi = \phi + \mathcal{H}$$

$$\frac{d\mathbf{v}}{dt} + H\mathbf{v} = -\nabla\psi, \quad \mathcal{H}(\rho) = \frac{P(\rho)}{\rho} + \int_1^\rho \frac{P(\rho')}{\rho'} \frac{d\rho'}{\rho'}$$

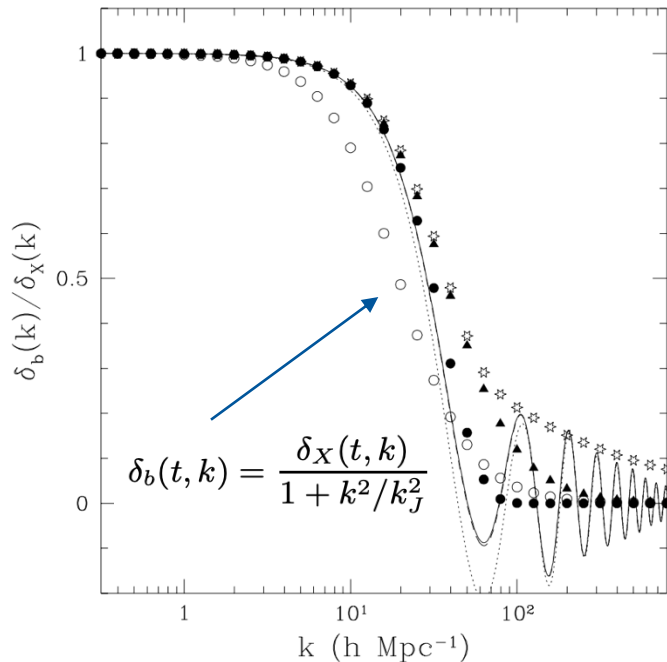
Specific enthalpy

Filtering scale

$$\frac{1}{k_F^2(t)} = \frac{1}{D_+(t)} \int_0^t dt' a^2(t') \frac{\ddot{D}_+(t') + 2H(t')\dot{D}_+(t')}{k_J^2(t')} \int_{t'}^t \frac{dt''}{a^2(t'')}.$$

Filtering scale k_F rather than k_J is used

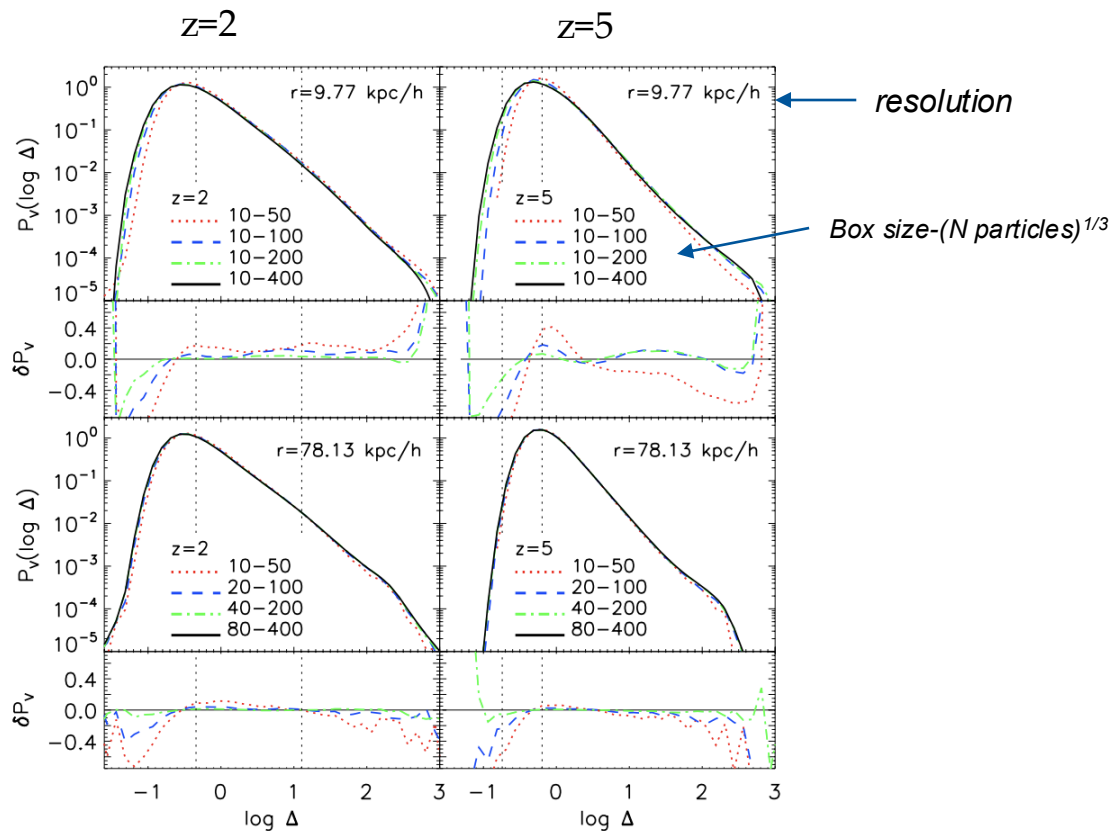
And k_F depends on the **whole thermal history** (unlike k_J)



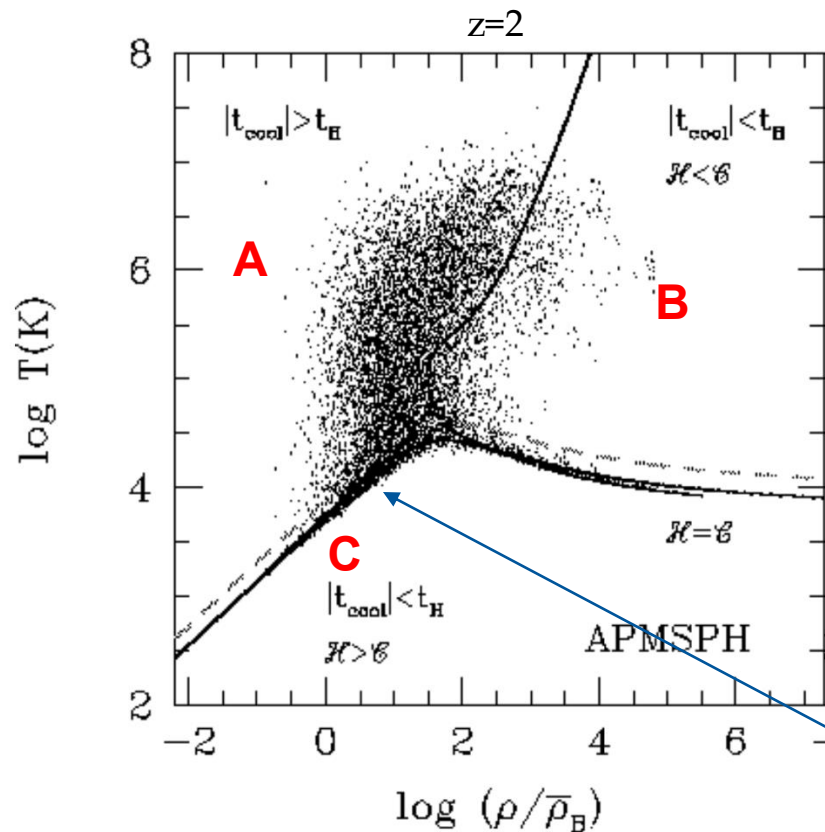
*Gnedin & Hui 1998, Gnedin 2000,
He & Gnedin 2020*

Physics of the gas: the gas PDF

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- ✓ Volume-weighted gas pdf is a skewed Gaussian – **Lognormal** fit works reasonably well
- ✓ 8th order polynomial fit provided in Becker&Bolton 2009, but earlier models are also in agreement (Bi, Miralda-Escudé et al. 97)
- ✓ Unfortunately, this is not observable....



Theuns+98

$$t_{\text{cool}} = \frac{u}{|\dot{u}|} = \frac{3k_B T}{2\mu} \frac{m_H}{\rho(1-Y)^2(\mathcal{C} - \mathcal{H})}$$

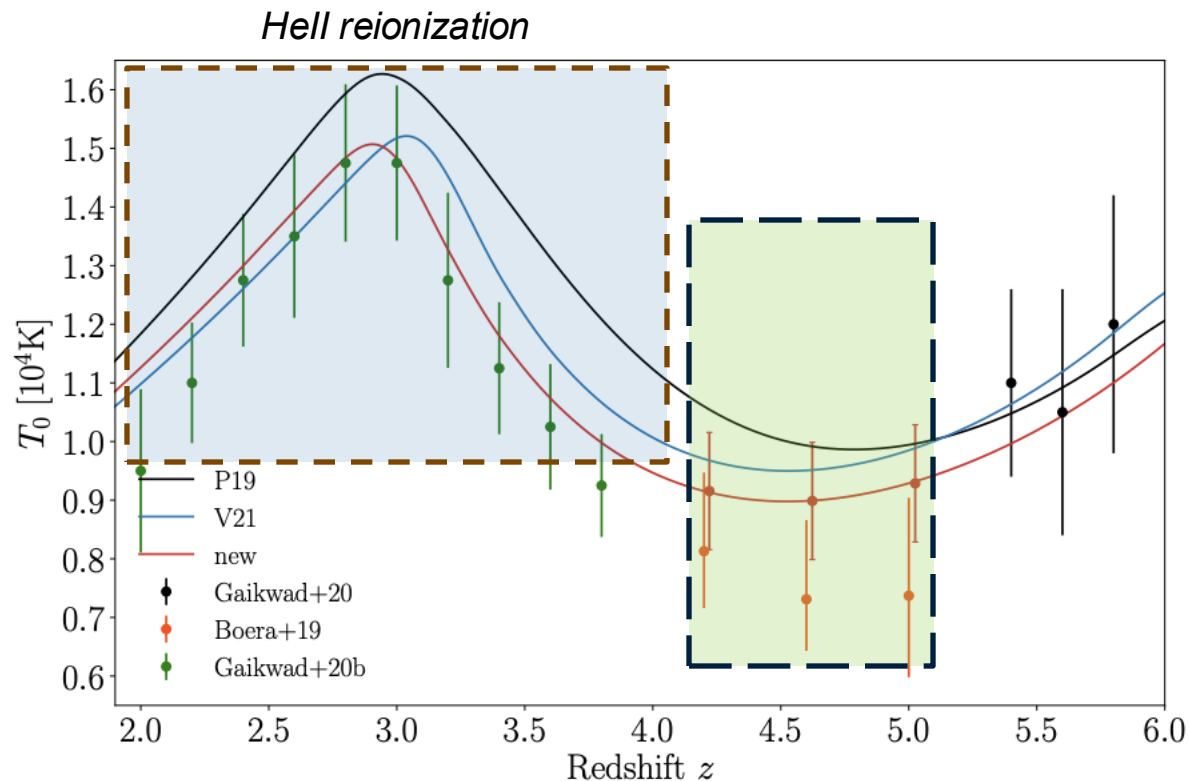
t_{cool} : cooling time with \mathcal{C} and \mathcal{H} are normalized cooling and heating rates

- ✓ 3 regions in the T - ρ plane:
 - A)** cooling time much longer than Hubble time: \mathcal{C} and \mathcal{H} are not effective
 - B)** Bremsstrahlung and line cooling are effective $\rightarrow t_{\text{cool}} < t_H$
 - C)** Region with efficient photoheating (HI and HeII)

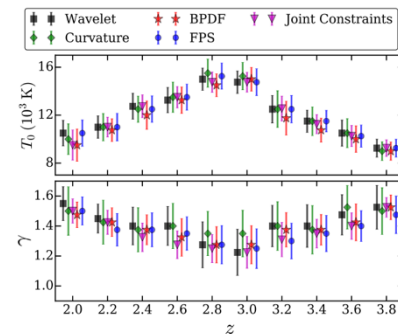
- ✓ $T = T_0(1+\delta)^{\gamma-1}$ for the low-density region
- ✓ Most of the gas in a cool/cold phase

The IGM thermal state

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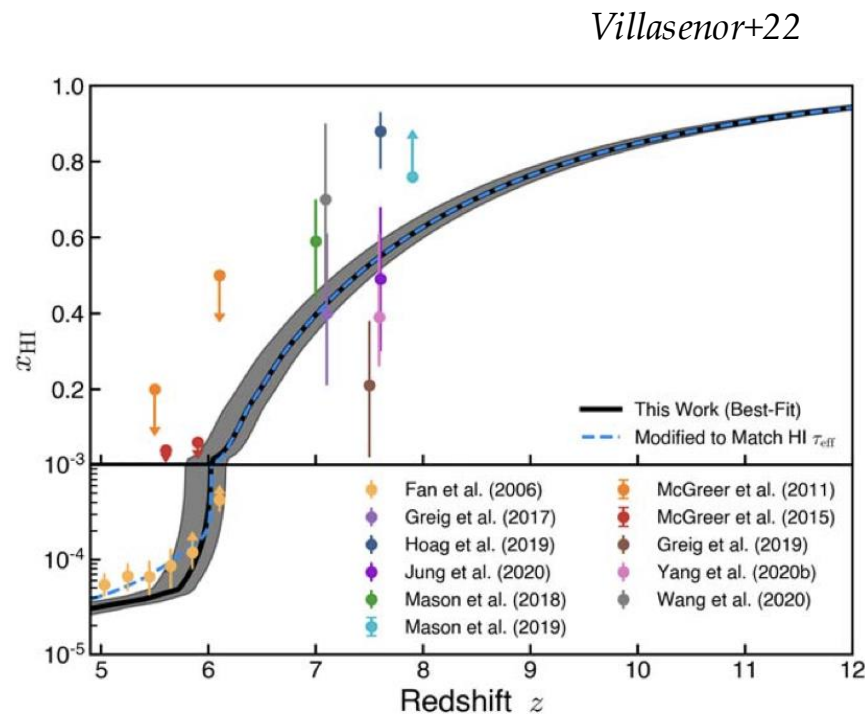
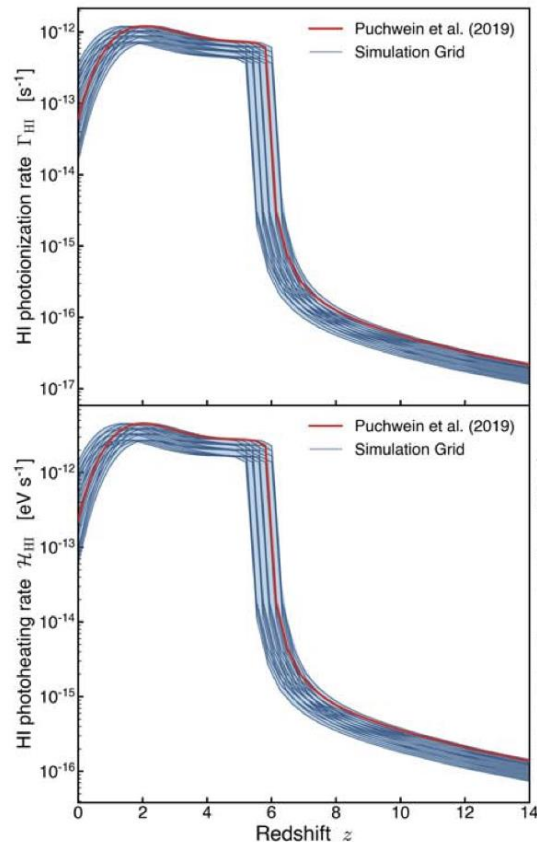
Walter+19



- Constraints obtained with a variety of data and methods
- Sensitive to lines rather than the lines' clustering
- HeII bump quite well detected

Ionization history

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Most of this “global” uncertainty is captured by requiring the sims to reproduce a given mean flux value (which is very well measured by data)

“New” astrophysics in the cosmic web

Patchy reionization

Simulating the high-redshift cosmic web

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<https://www.nottingham.ac.uk/astronomy/sherwood/>

Bolton+17

Puchwein, Bolton+23



J. Bolton

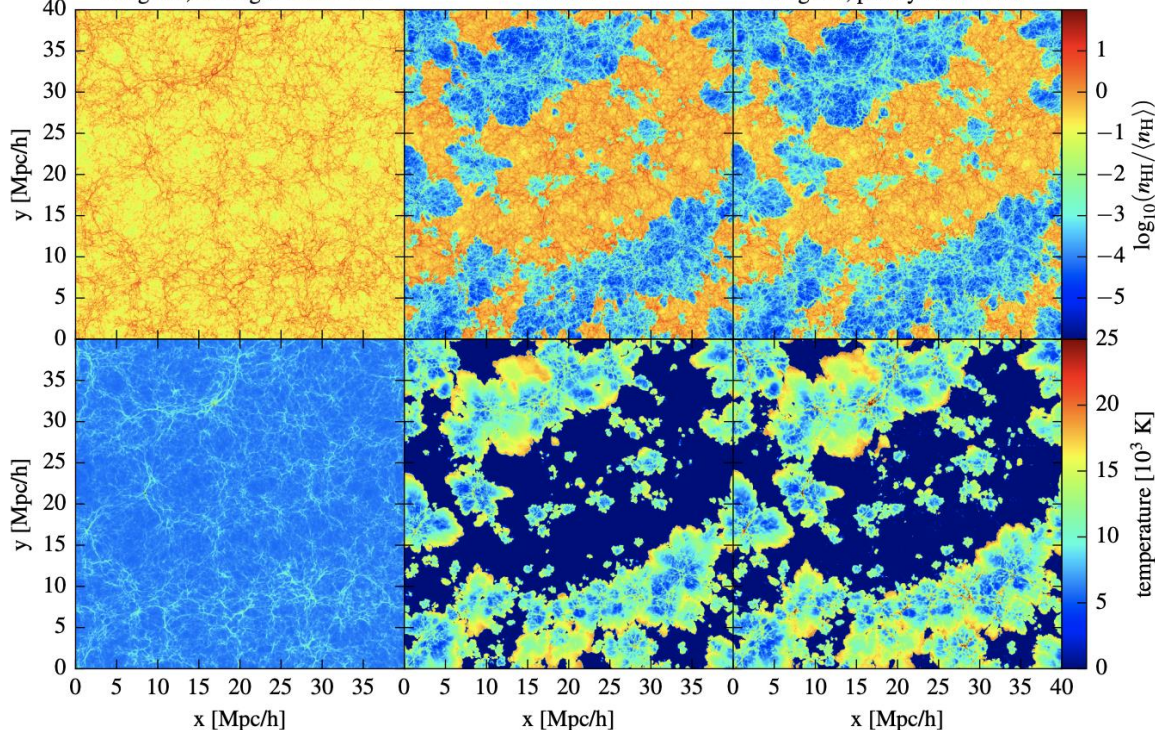
E. Puchwein

$z=7$ (with reionization finishing at $z=5.3$)

Gadget-3, homogeneous UVB

ATON

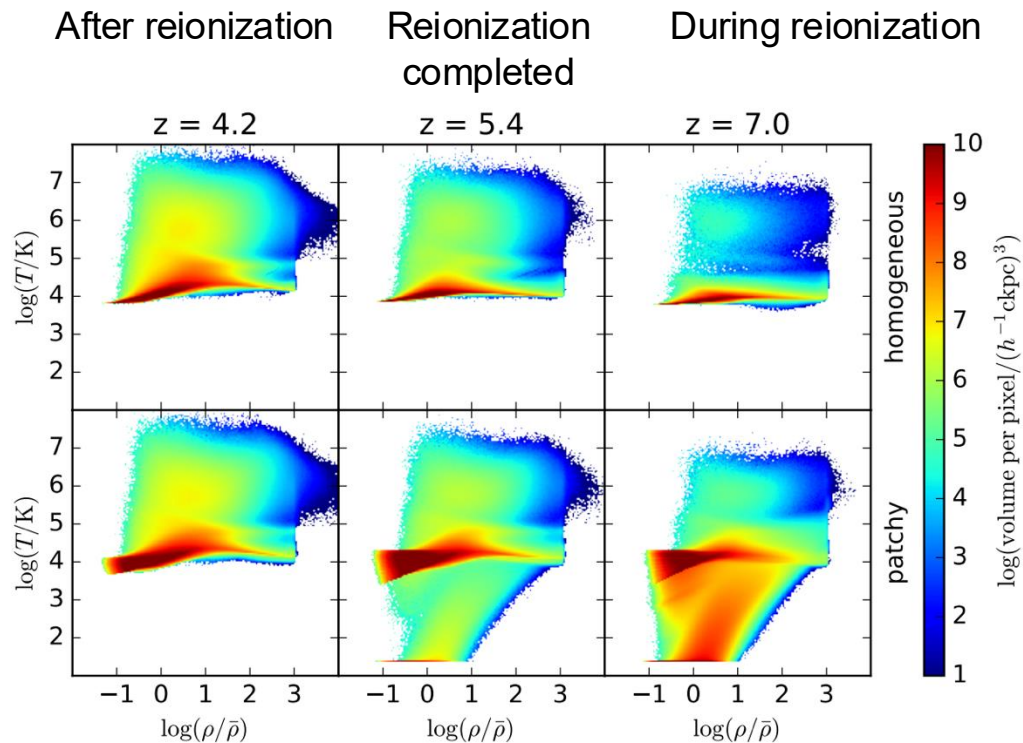
Gadget-3, patchy reionization



- ✓ **Sherwood-Relics suite** (>200 simulations: boxes 5-160 cMpc/h; $M_{\text{gas}}=3.7\text{e}3\text{-}6.4\text{e}6 M_{\odot}$) – about 75 Million CPU hrs
- ✓ G3 code + ATON to perform radiative transfer for patchy reionization
- ✓ Focus (and model calibration) on the high- z ($z>4$) forest

Physics of the gas: the gas thermal state at high- z

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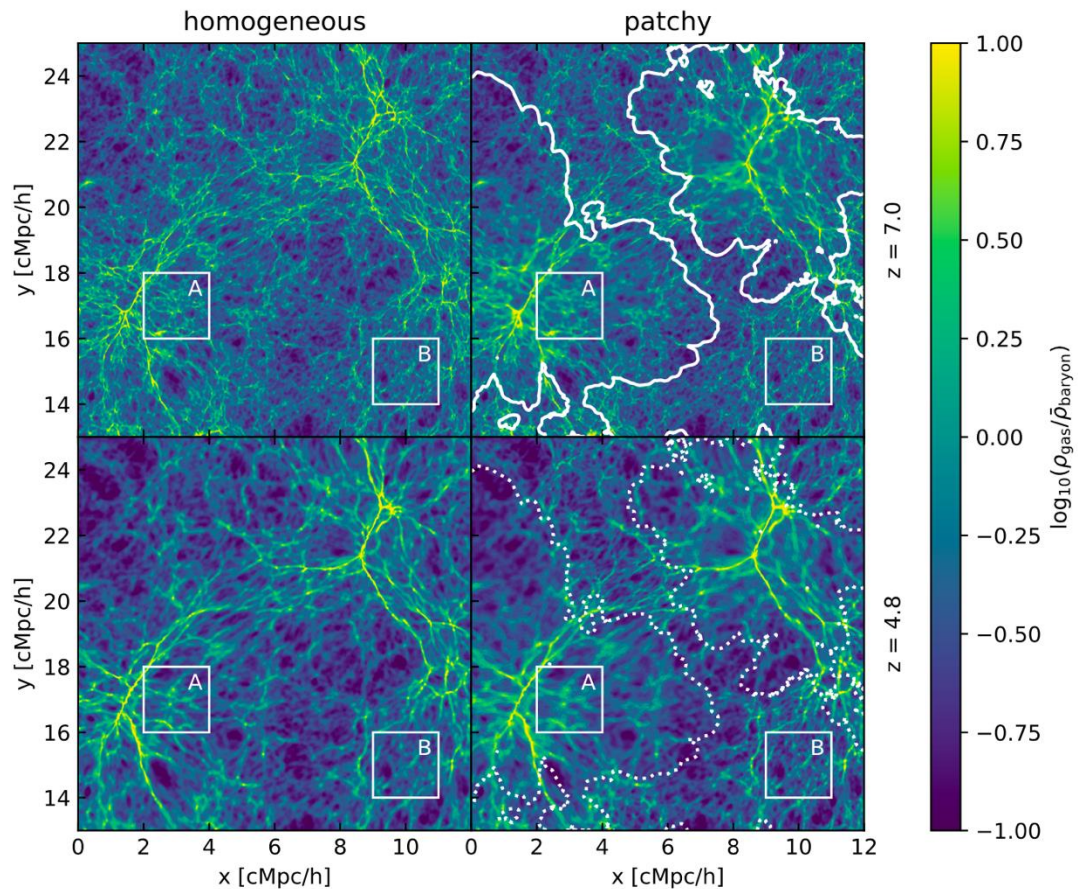
- ✓ T - ρ relation somewhat flatter at high- z – moving closer to reionization
- ✓ ... and prone to the effects of a patchy reionization

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During reionization

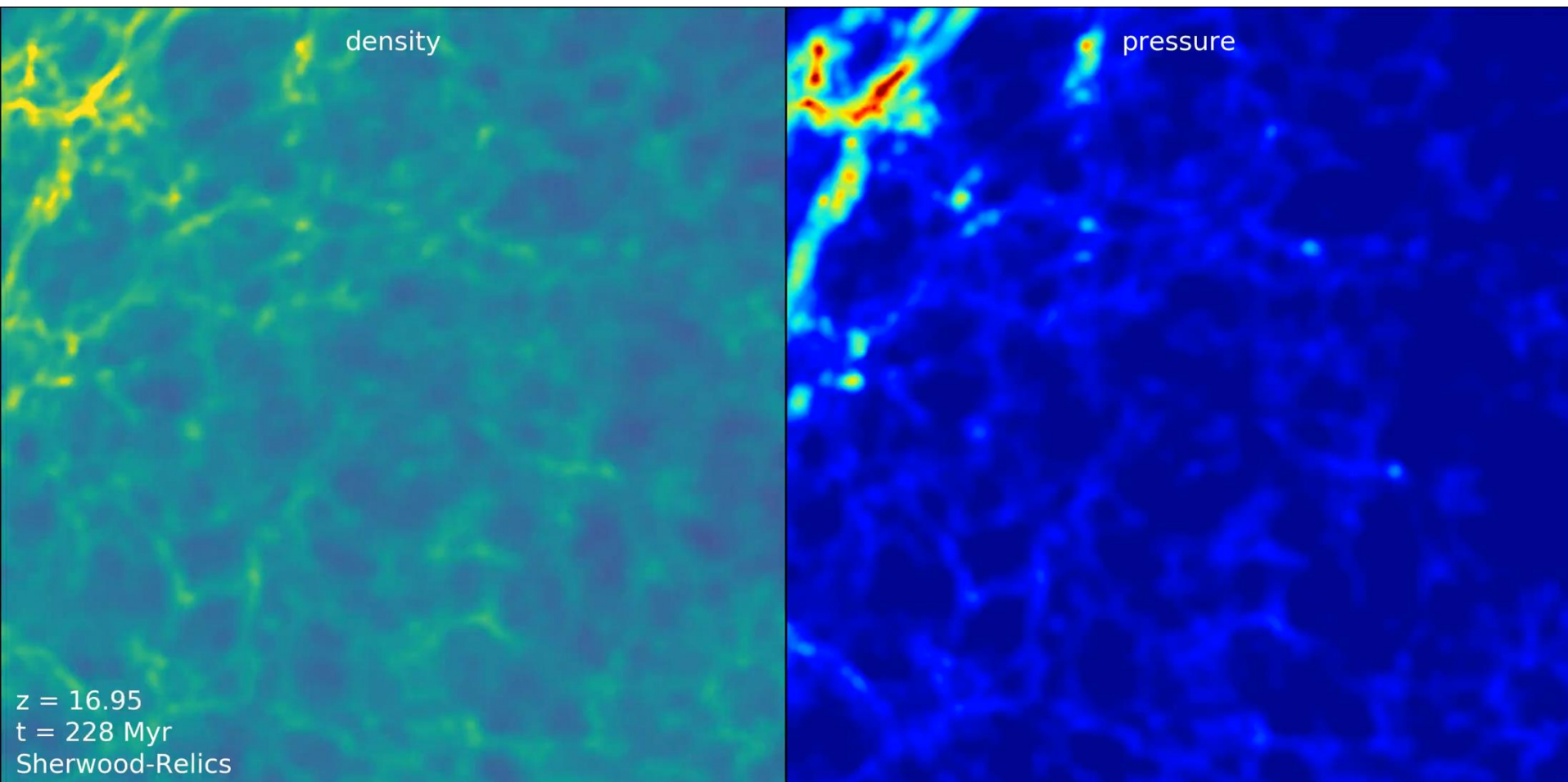
Note:
Reionization ends
at $z=5.3$

After reionization is complete



Patchy reionization - II

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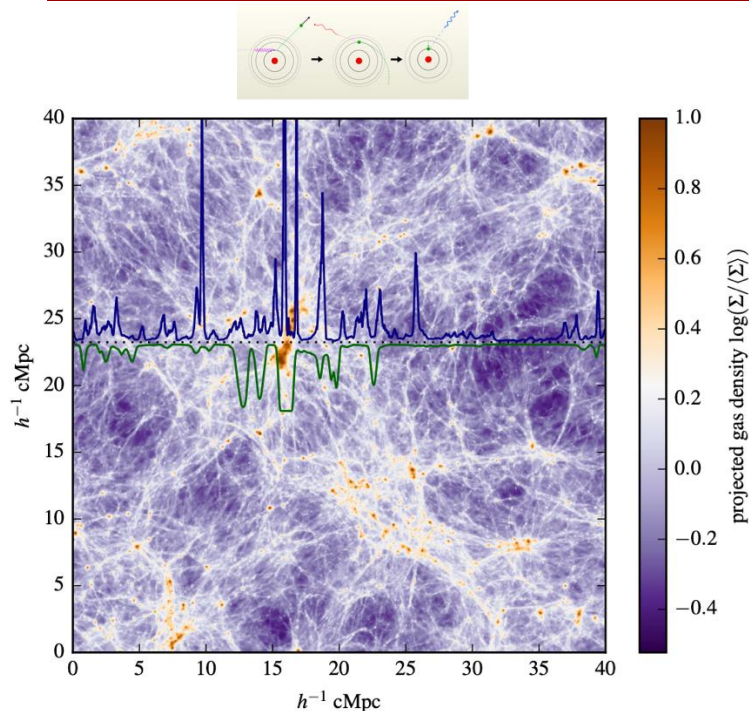
- ✓ There is a physical model of the low-density cosmic web based on gravitational instability, hydrostatic equilibrium (Jeans scale) + UV background, at $z=2-5$.
- ✓ Cosmic filaments do trace underlying gravitational (DM) potential above the filtering scale
- ✓ Thermal and ionization history are reasonably constrained and support: **patchy reionization**, HeII “heating” bump
- ✓ Feedback effects are small, impact more the low z regime, no evidence for turbulence
- ✓ Any astrophysical or fundamental physical process able either to:
 - dump heat in the low density IGM
 - or modify the matter power spectrumcould have an impact
- ✓ How can we observe this?

Lyman- α forest as a manifestation of the cosmic web

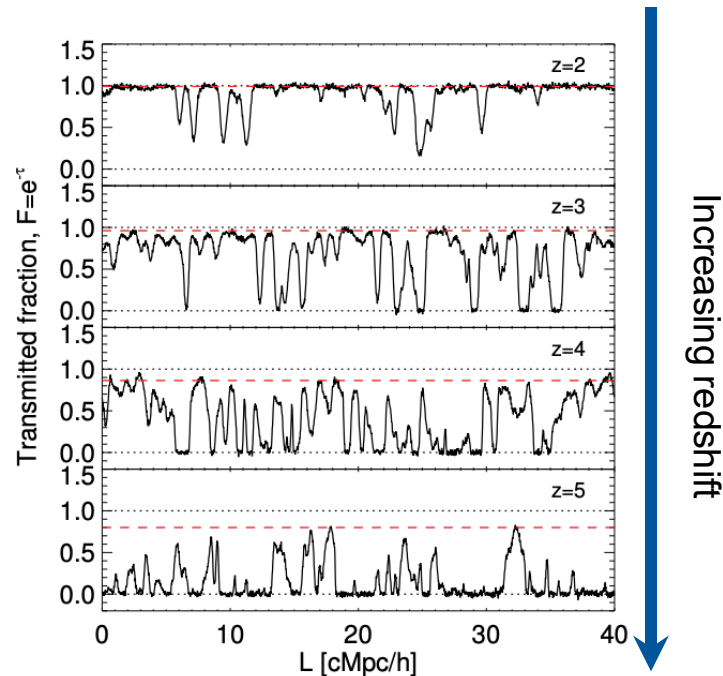
Modelling
Cosmology

The Lyman- α forest

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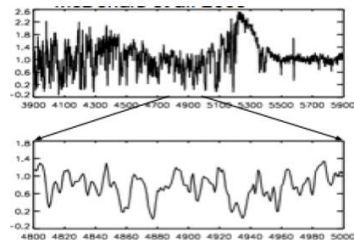


Most of the flux statistics are in agreement with Λ CDM – 216,000 flux models fed into MCMC analysis



Increasing $z \rightarrow$ increasing HI \rightarrow more Absorption – at high z even underdense gas can produce absorption

DESI BOSS/SDSS-III



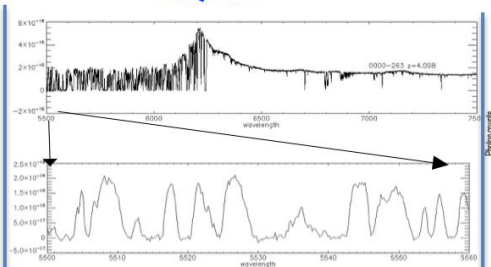
Low resolution BOSS and SDSS-III spectra
S/N~2-3 - 160,000 spectra

Used to detect BAOs at $z=2.3$ and correlations in the transverse direction

Used to place stringent constraints on neutrino masses <0.12 eV

*Busca+13, Slosar+14, Font-Ribera+14
Palanque-Delabrouille+15
Seljak+06, Baur+16, Yeche+17 etc.*

XQ-100



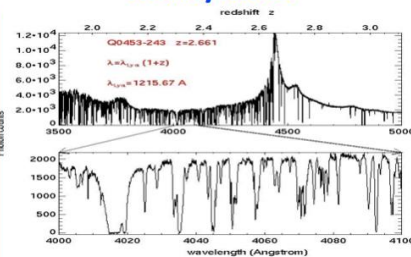
Medium resolution X-Shooter VLT spectra
S/N ~ 30

100 spectra at $z>3.5$

Used to place stringent constraints on Warm Dark Matter in combination with high res. spectra

*Irsic, MV+ 17a,17b
Lopez+16, Irsic+16*

HIRES/MIKE



High resolution VLT or Keck spectra S/N ~100 - ~hundreds of spectra

Used for WDM, astrophysics of the IGM and galaxy formation, variation of fundamental constants

*MV+05,08,13, Becker+11
Yeche+17, Garzilli+18,
Bosman+18*

Modelling the 3D flux power

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3D flux power

Linear power

$$P_F(k, \mu) = b_\delta^2 (1 + \beta \mu^2)^2 P_L(k) D(k, \mu)$$

$$\beta = \frac{b_{F\eta} f(\Omega)}{b_{F\delta}}$$

See Seljak 12 for analytical understanding of Lya bias

Linear
tracer

$$\delta_F = b_{F\delta} \delta + b_{F\eta} \eta$$

$$b_{F\delta} = \frac{\partial \delta_F}{\partial \delta} ; \quad b_{F\eta} = \frac{\partial \delta_F}{\partial \eta} \quad \eta = -\frac{1}{aH} \frac{\partial v_p}{\partial x_p}$$

Density bias

Velocity grad. bias

Pec. Vel. Grad.

Non linearities

See Desjacques+18 for bias expansion

McDonald 2003

$$D(k, \mu) \equiv \exp \left\{ \left[\frac{k}{k_{\text{NL}}} \right]^{\alpha_{\text{NL}}} - \left[\frac{k}{k_P} \right]^{\alpha_P} - \left[\frac{k_{\parallel}}{k_V(k)} \right]^{\alpha_V} \right\}$$

Non-linear power Pressure smoothing RSD and thermal broadening

Arinyo-i-prats+ 2015

$$D_1(k, \mu) = \exp \left\{ [q_1 \Delta^2(k) + q_2 \Delta^4(k)] \left[1 - \left(\frac{k}{k_v} \right)^{a_v} \mu^{b_v} \right] - \left(\frac{k}{k_p} \right)^2 \right\}$$

Fewer params, better behaved at small k

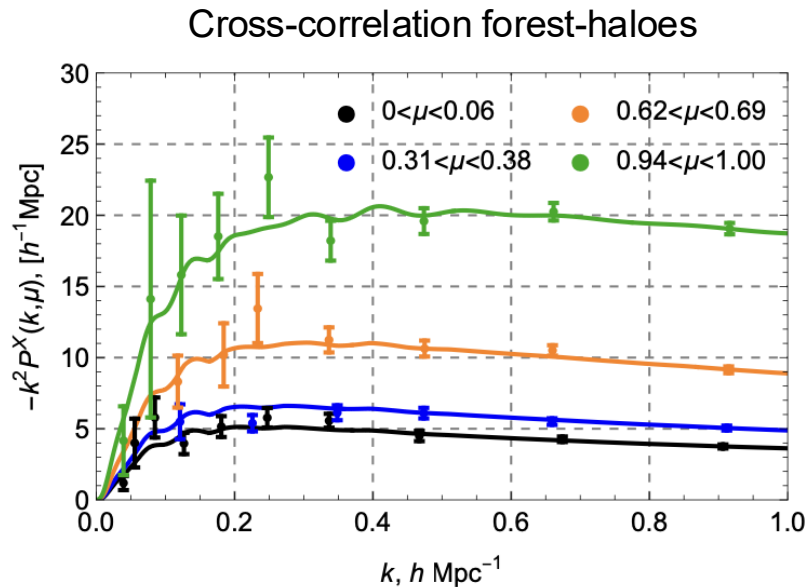
$$k_{\text{NL}} \sim 5 \text{ h/Mpc} \quad k_P \sim 10 \text{ h/Mpc} \quad k_v \sim 5-10 \text{ h/Mpc} \quad q_1 \sim 0.5-1.5$$

$$\delta_F(\mathbf{x}) = b_1 \delta_m(\mathbf{x}) + b_\eta \eta(\mathbf{x}) + \sum_i b_{\mathcal{O}_i} \mathcal{O}_i(\mathbf{x}) + \delta_{\text{ctr}}(\mathbf{x}) + \epsilon(\mathbf{x})$$

- ✓ EFT for the forest (Ivanov 23) 3D flux power with 15 params: 8 free parameters + analytical marginalization on other 7 param
Good fit up to $k_{\text{max}}=3 \text{ h/Mpc}$ ($z=2.8$)
- ✓ Extended also to cross-correlation (Chudaykin & Ivanov 25) – good fit to $k_{\text{max}} = 1 \text{ h/Mpc}$
- ✓ Extended to **1D flux power**, tested on sims and applied to data to constrain PBH
Ivanov & Trifinopoulos 25

$$P_F(k_{\parallel}, z) = \frac{1}{2\pi} \int_{k_{\parallel}}^{\infty} dk k P_F^{3D}(k, k_{\parallel}, z)$$

- ✓ And also to 3D flux power estimate from cross power in transverse direction *Abdul-Karim+25*



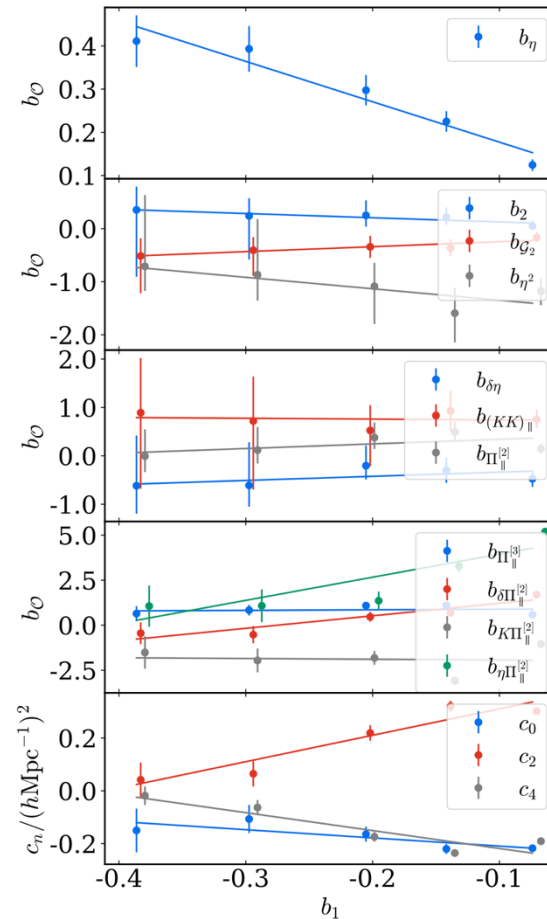
Chudaykin & Ivanov 25

Modelling the 3D flux power

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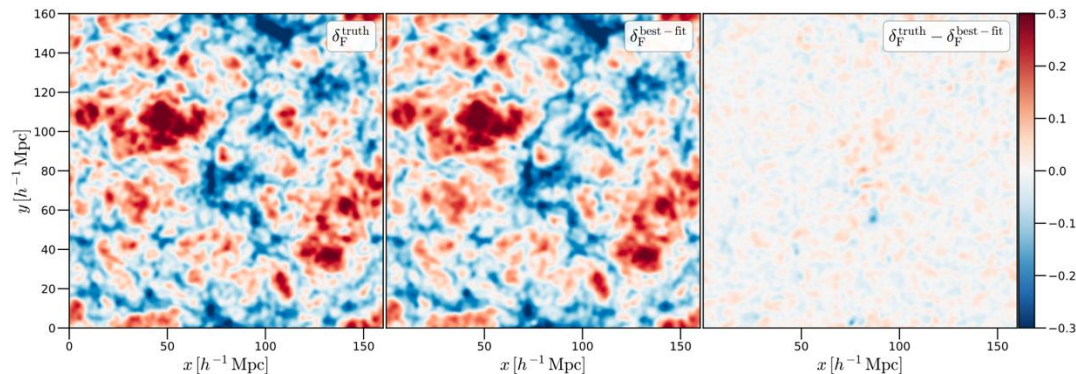
- ✓ Nyx code (Adaptive Mesh Refinement and grid based). DeBelsunce+24 – $k_{\text{max}}=2h/\text{Mpc}$
- ✓ Degeneracies between the many parameters are crucial

EFT Parameter (Sampled)	Prior	EFT Parameter (Marginalized)	Prior
b_1	$\mathcal{U}(-2, 2)$	$\frac{c_{0,2,4,6}}{[h^{-1}\text{Mpc}]^2}$	$\mathcal{N}(0, 1^2)$
b_η	$\mathcal{U}(-2, 2)$	P_{shot}	$\mathcal{N}(0, 5^2)$
b_2	$\mathcal{N}(0, 2^2)$	$\frac{a_{0,2}}{[h^{-1}\text{Mpc}]^2}$	$\mathcal{N}(0, 5^2)$
$b_{\mathcal{G}_2}$	$\mathcal{N}(0, 2^2)$	$b_{(K\Pi^{[2]})\parallel}$	$\mathcal{N}(0, 2^2)$
$b_{(KK)\parallel}$	$\mathcal{N}(0, 2^2)$	$b_{\delta\Pi^{[2]}\parallel}$	$\mathcal{N}(0, 2^2)$
$b_{\Pi^{[2]}\parallel}$	$\mathcal{N}(0, 2^2)$	$b_{\eta\Pi^{[2]}\parallel}$	$\mathcal{N}(0, 2^2)$
$b_{\delta\eta}$	$\mathcal{N}(0, 2^2)$	$b_{\Pi^{[3]}\parallel}$	$\mathcal{N}(0, 2^2)$
b_{η^2}	$\mathcal{N}(0, 2^2)$		

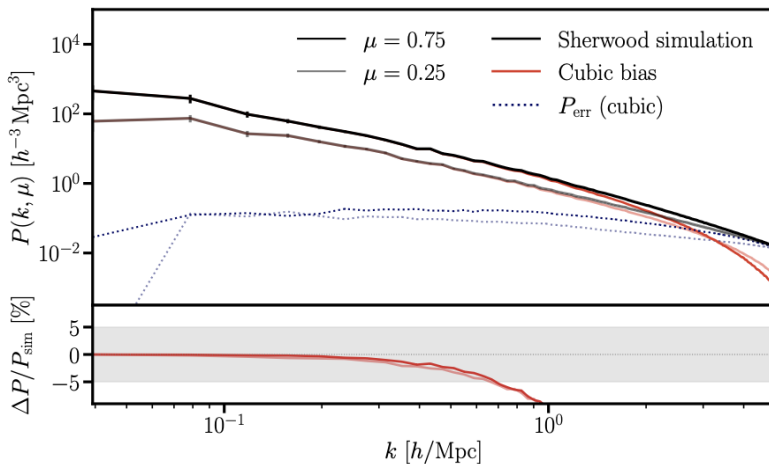


Modelling the 3D flux power at the field level

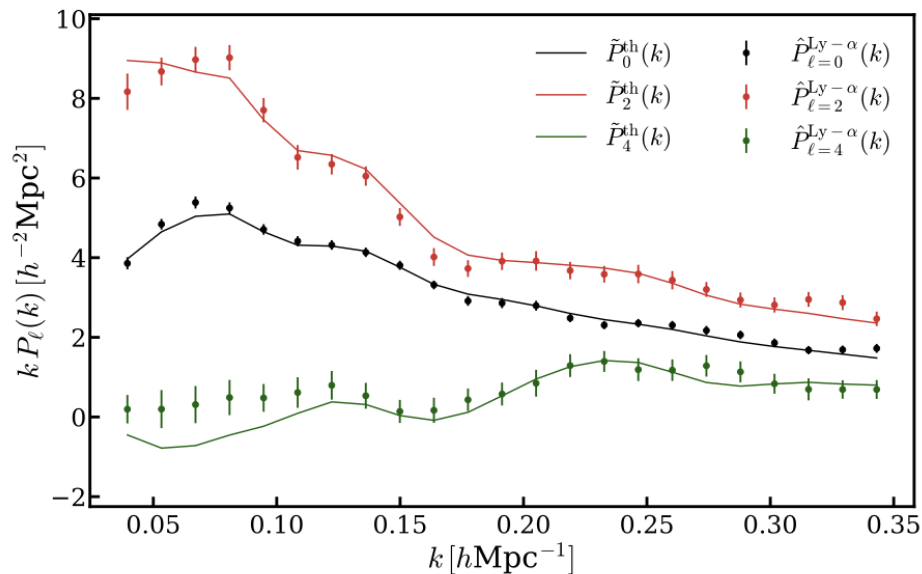
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$$\begin{aligned} \delta_F^{\text{model}}(\mathbf{k}) = & \beta_1^F(k, \mu) \tilde{\delta}_1(\mathbf{k}) \\ & + \beta_\eta^F(k, \mu) \left(\delta_Z(\mathbf{k}) - \frac{3}{7} f \mu^2 \tilde{\mathcal{G}}_2 \right)^\perp \\ & + \beta_2^F(k, \mu) (\tilde{\delta}_1^2)^\perp(\mathbf{k}) + \beta_{\tilde{\mathcal{G}}_2}^F(k, \mu) \tilde{\mathcal{G}}_2^\perp(\mathbf{k}) \\ & + \beta_{\delta_\eta}^F(k, \mu) [\tilde{\delta}_\eta]^\perp(\mathbf{k}) \\ & + \beta_{\eta^2}^F(k, \mu) \tilde{\eta}^{2,\perp}(\mathbf{k}) + \beta_{KK_\parallel}^F(k, \mu) (K\tilde{K})_\parallel^\perp(\mathbf{k}) \end{aligned}$$



- ✓ De Belsunce et al. 2025: Field level, EFT inspired reconstruction of the flux field (and cross with haloes)
- ✓ Tested on flux power but also on flux pdf (very difficult to fit)



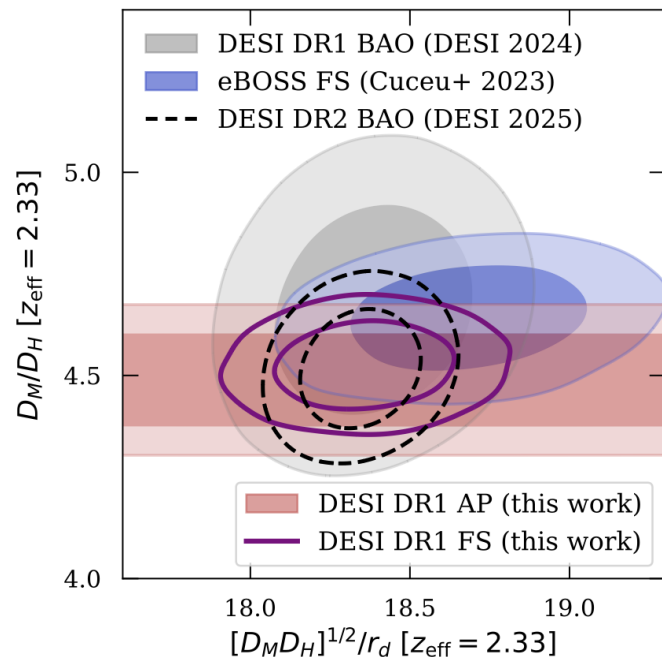
- ✓ De Belsunce+24: 205,000 QSOs with $\langle z \rangle = 2.33$ - Pair-count estimator in real space (good for window)
- ✓ Tested against Gaussian mocks and CoLoRe.
- ✓ Kaiser formula + non-linear correction is a good fit for 0.02-0.35 h/Mpc

3D correlation function from DESI

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$$P_F(\mathbf{k}) = b_F'^2 (1 + \beta_F' \mu_k^2)^2 G(\mathbf{k}) F_{NL}(\mathbf{k}) P_{\text{fid}}(k)$$

$$P_{F \times Q}(\mathbf{k}) = b_F' (1 + \beta_F' \mu_k^2) (b_Q + f \mu_k^2) G(\mathbf{k}) X_{NL}(\mathbf{k}) P_{\text{fid}}(k)$$

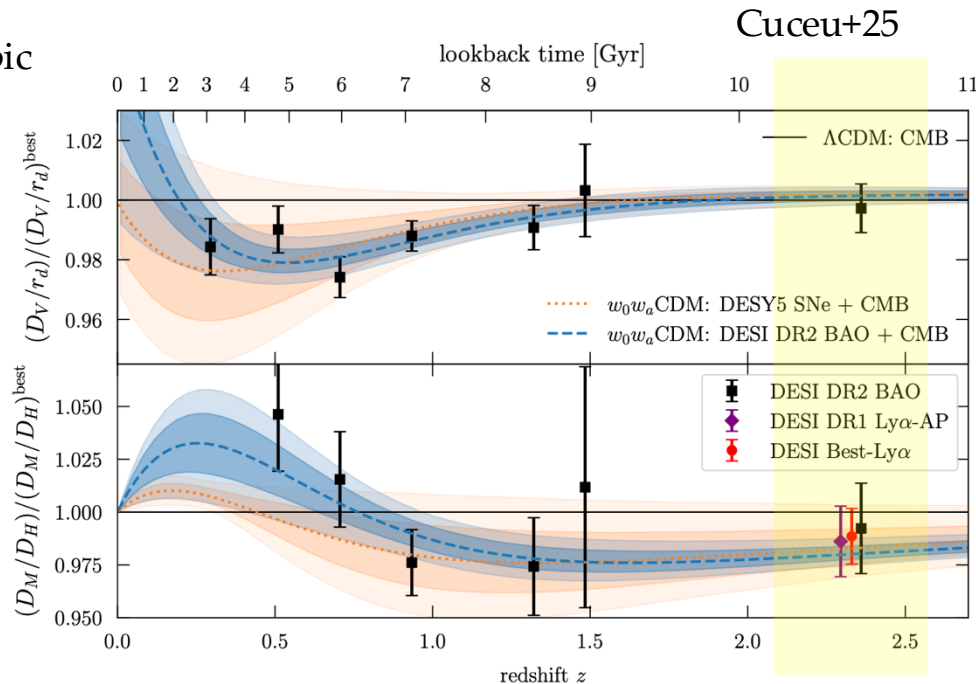


- ✓ Full-shape analysis of DESI DR1 (Cuceu+25) measurement of Alcock-Paczynski (AP) and RSD - about 750,000 QSOs at $z > 1.7$
- ✓ β parameter marginalized over. Fit for b_F , b_Q and f
- ✓ Tightest AP constraints at $z > 1$, 2.4 times improvement over BAO only
- ✓ First measurement of $f\sigma_8$ from cross

3D corr. function from DESI: dynamical dark energy

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Isotropic
BAO



- ✓ Consistent with both CMB and galaxy BAOs
- ✓ Ly α is good at measuring D_H
- ✓ 2.7σ tension with SHOES
- ✓ Slightly reduced tension in w_0 - w_a plane w.r.t. LCDM when Ly α is combined ($3.3\sigma \rightarrow 3.1\sigma$)
- ✓ 1.7% on the AP at $z=2.33$ (could go down to 0.3% at DESI yr5)

$$\sum m_\nu < 0.0638 \text{ eV (95\%, Ly}\alpha\text{-AP+BAO+CMB)}$$

Particle physics in the cosmic web

Neutrino interactions
Warm Dark Matter
Cold+Warm Dark Matter

Promises of the post-reionization Universe

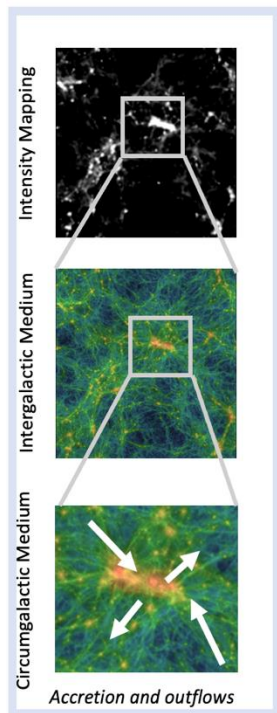
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Long lever arm in terms of scales/redshifts will in turn allow to break degeneracies between astro and cosmo parameters with:

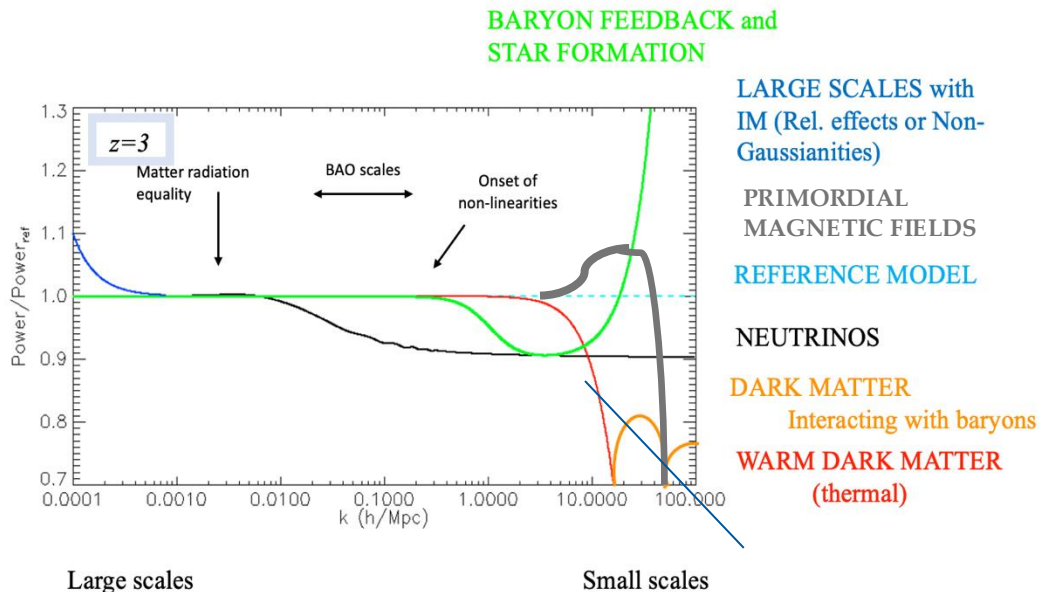
- **Power spectrum**
- **cross-correlations** of different tracers
- **new estimators** (e.g. 1-point function, bispectrum, Machine Learning)

It is an “active phase” of structure formation processes (feedback, star formation, black holes, cosmic bayron cycle etc.)

Environments



Physical Scales

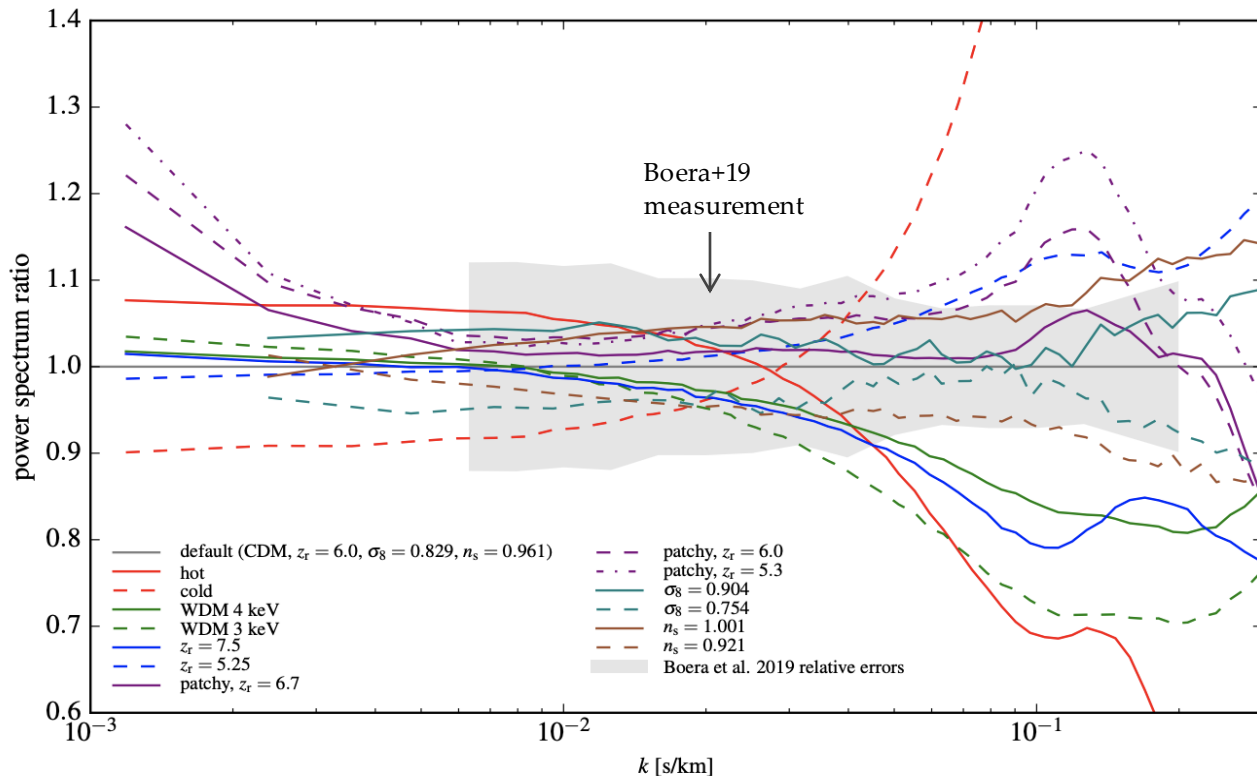


HI measures density perturbations in a matter dominated regime!

Impact on 1D flux power

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Simulated 1D flux power @ $z=4.6$

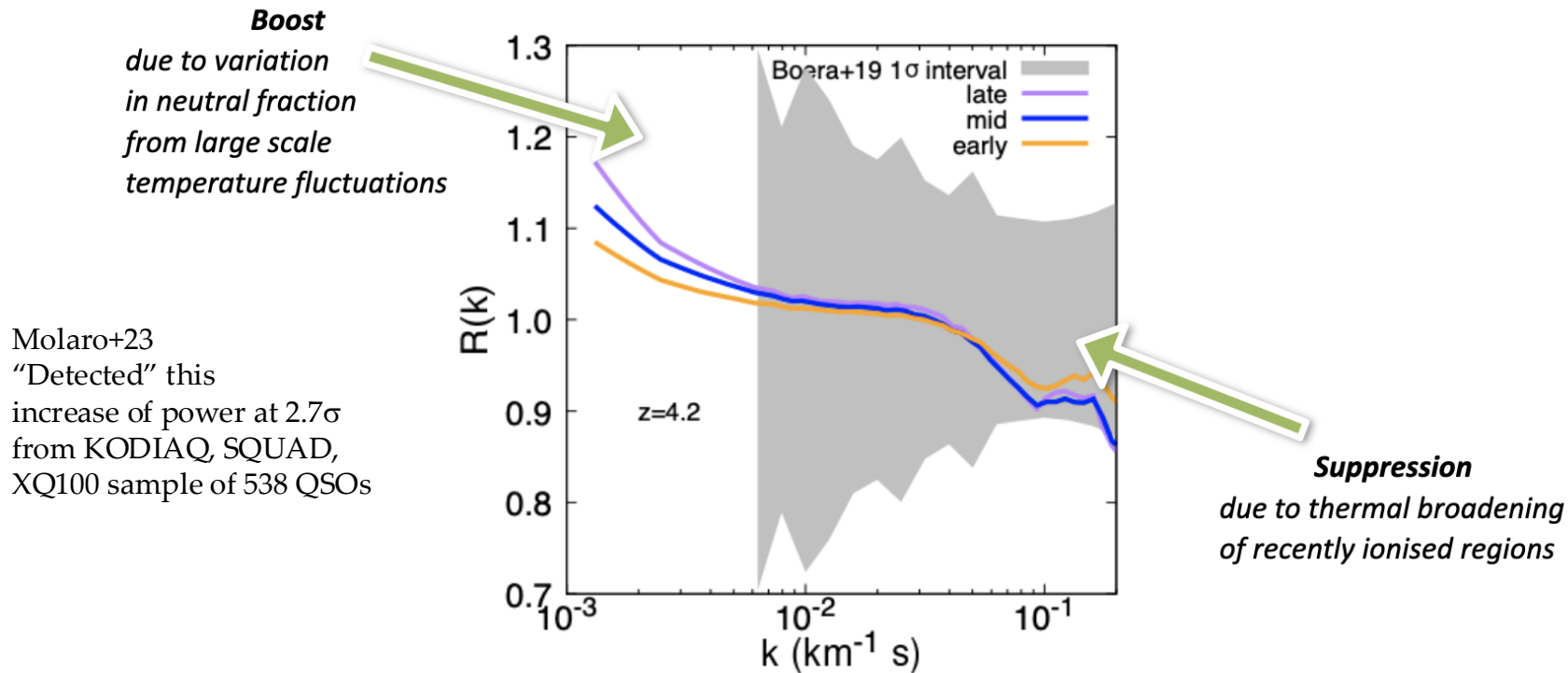


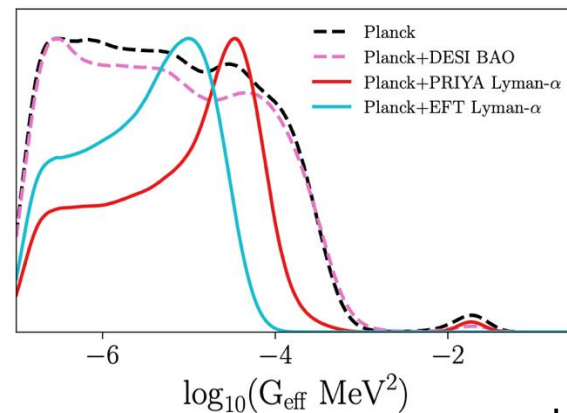
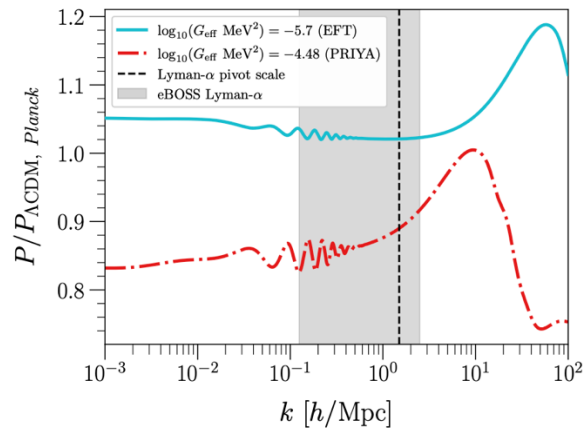
More power

Less power

Patchy Reionization – Impact on 1D flux power

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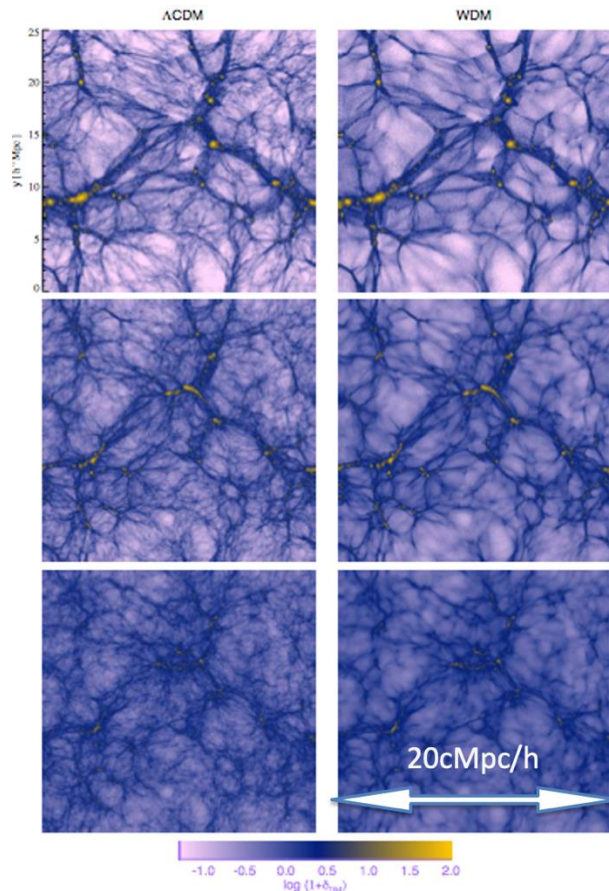


He+25

- ✓ He+24: strong preference for neutrino self interactions (delayed onset of free streaming) from BOSS full shape analysis of forest (and other data) pointed to $G_{\text{eff}}=0.01$ at 5s, with a compressed likelihood (based on LCDM)
- ✓ New likelihood either EFT based or based on a new suite of simulations (Bird et al.) and applied to eBOSS data: result goes away

A warm cosmic web?

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$z=0$

$$k_{\text{FS}} \sim 15.6 \frac{h}{\text{Mpc}} \left(\frac{m_{\text{WDM}}}{1 \text{ keV}} \right)^{4/3} \left(\frac{0.12}{\Omega_{\text{DM}} h^2} \right)^{1/3}$$

$z=2$

Free streaming scale
of thermal warm dark
matter

$z=5$

Viel et al 2005

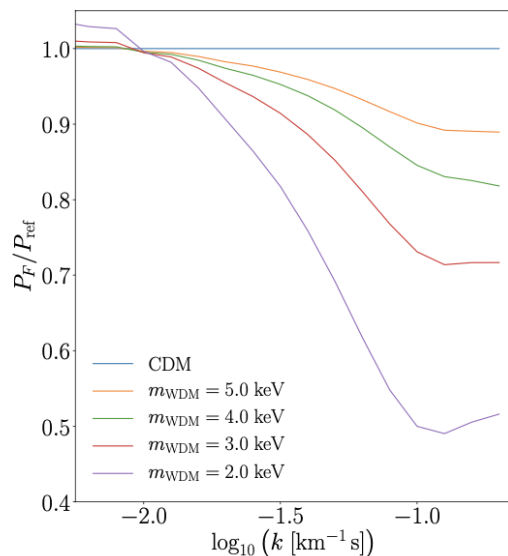
Vid Irsic



Unveiling Dark Matter free-streaming at the smallest scales with high redshift Lyman-alpha forest

Vid Irsiĉ^{1,2}, Matteo Viel^{3,4,5,6,7}, Martin G. Haehnelt^{1,8}, James S. Bolton⁹, Margherita Molaro⁹, Ewald Puchwein¹⁰, Elisa Boera^{5,6}, George D. Becker¹¹, Prakash Gaikwad¹², Laura C. Keating¹³, Girish Kulkarni¹⁴
¹*Kavli Institute for Cosmology, University of Cambridge*

WDM free streaming



The smoothing scales

Matteo Viel

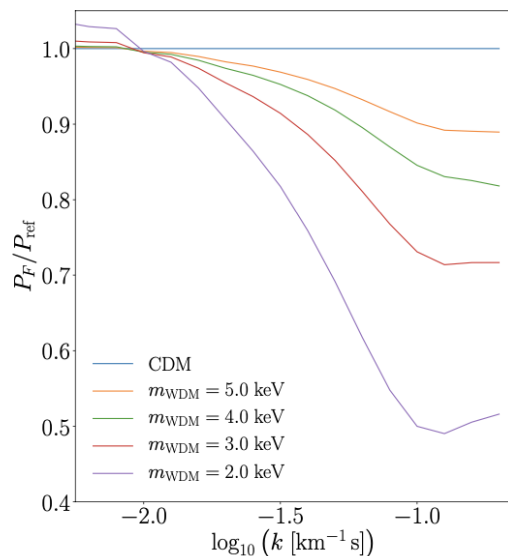
Vid Irsic



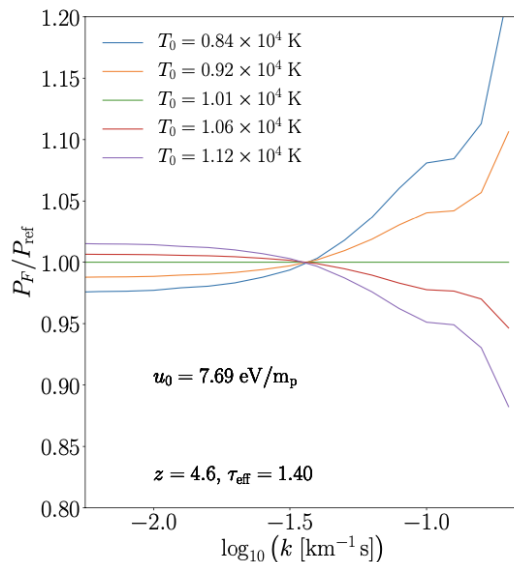
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WDM free streaming



Thermal broadening



The smoothing scales

Matteo Viel

Vid Irsic

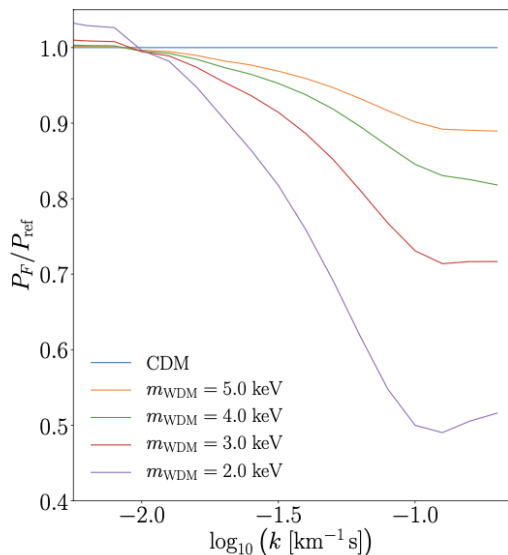


Unveiling Dark Matter free-streaming at the smallest scales with high redshift Lyman-alpha forest

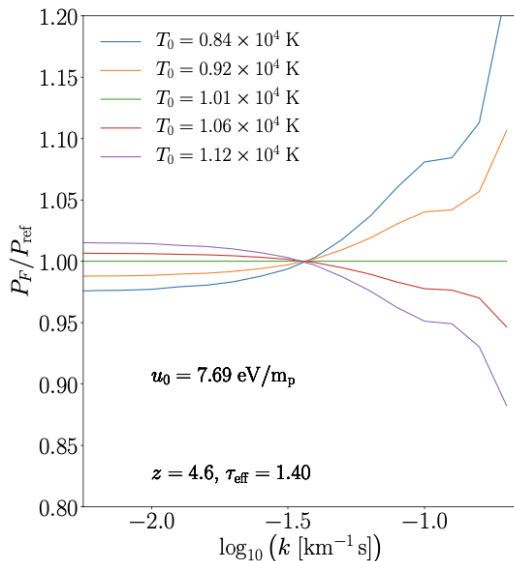
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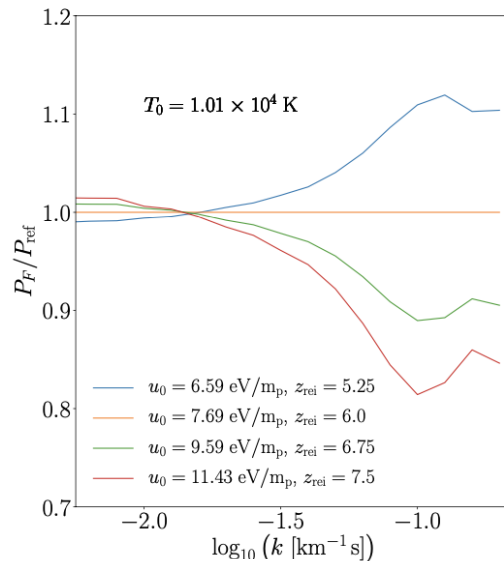
WDM free streaming



Thermal broadening



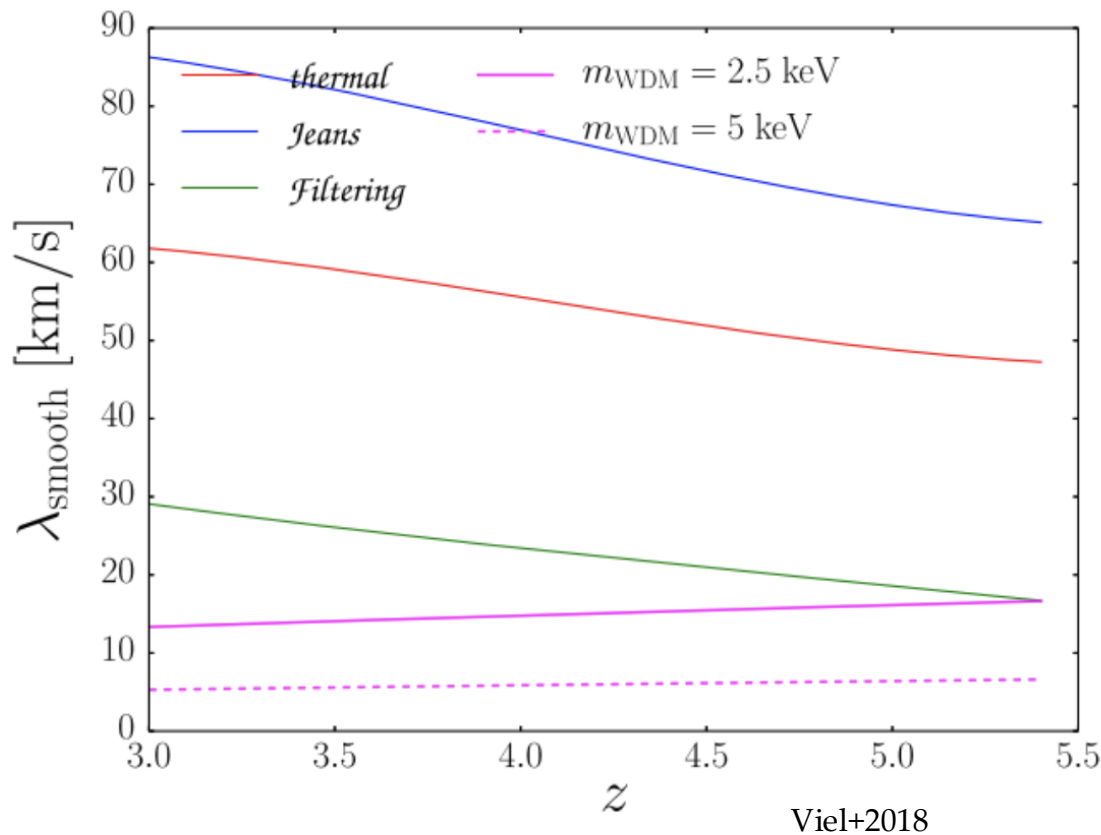
Gas pressure



$$u_0(t) = \int_0^t dt \frac{\mathcal{H}}{\bar{\rho}_m} \frac{3k_B}{2\mu} \quad H \text{ is heating rate}$$

The smoothing scales - II

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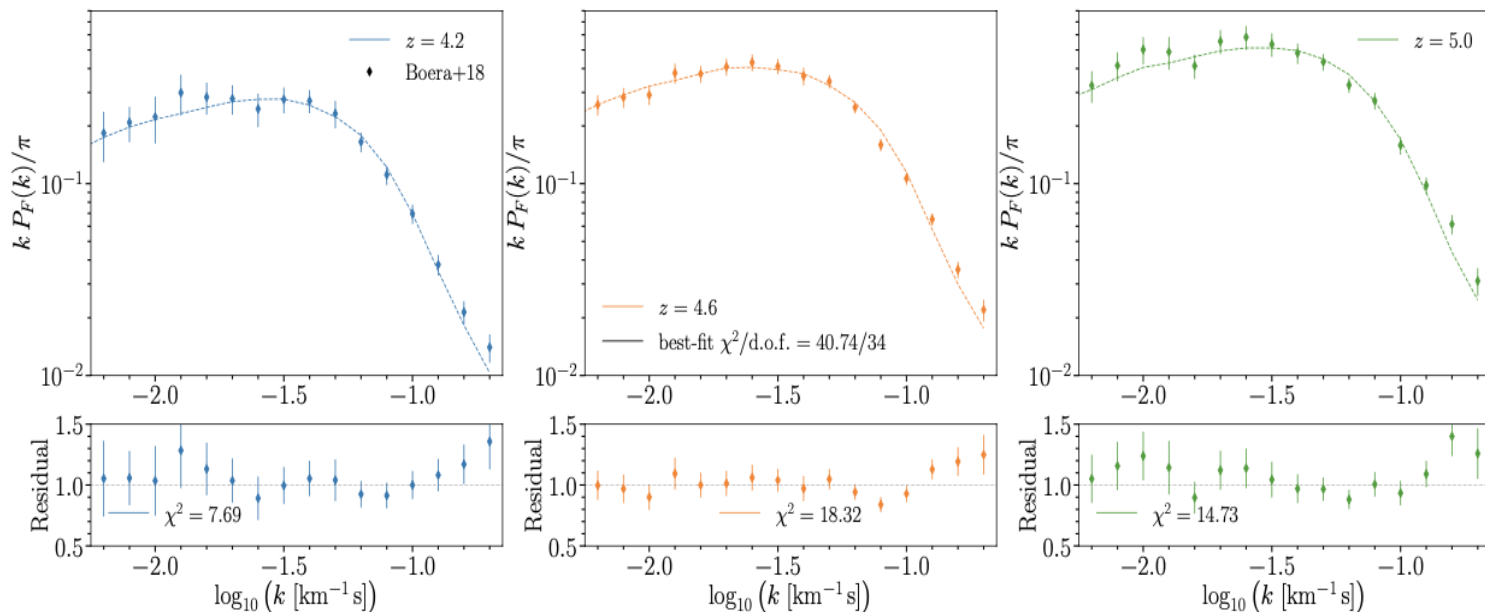


Different physical scales (on top of instrumental resolution) affect the power spectrum cutoff:

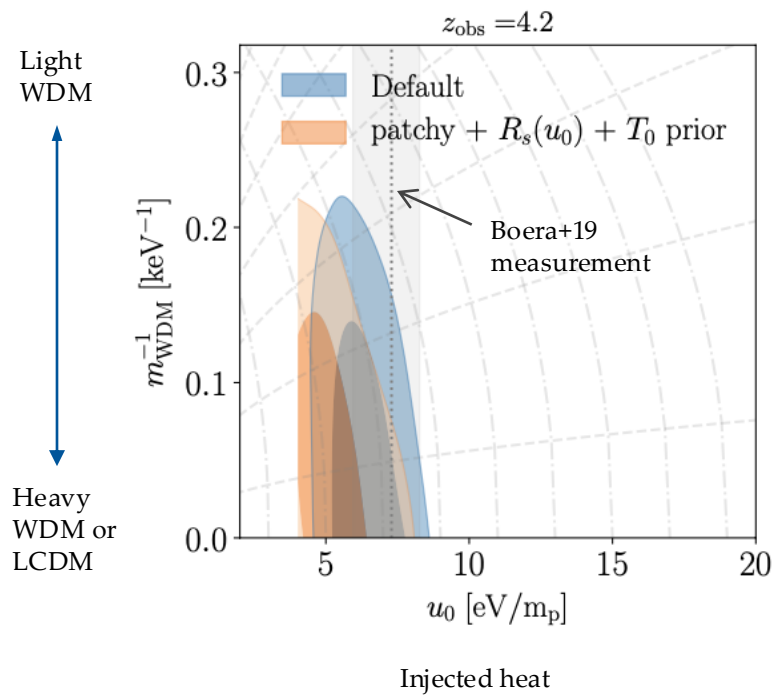
- thermal: instantaneous temperature at that redshift;
- filtering scale: depends on all the past thermal history – related to Jeans scale;
- WDM cutoffs are basically redshift independent

The data at $z=4-5$

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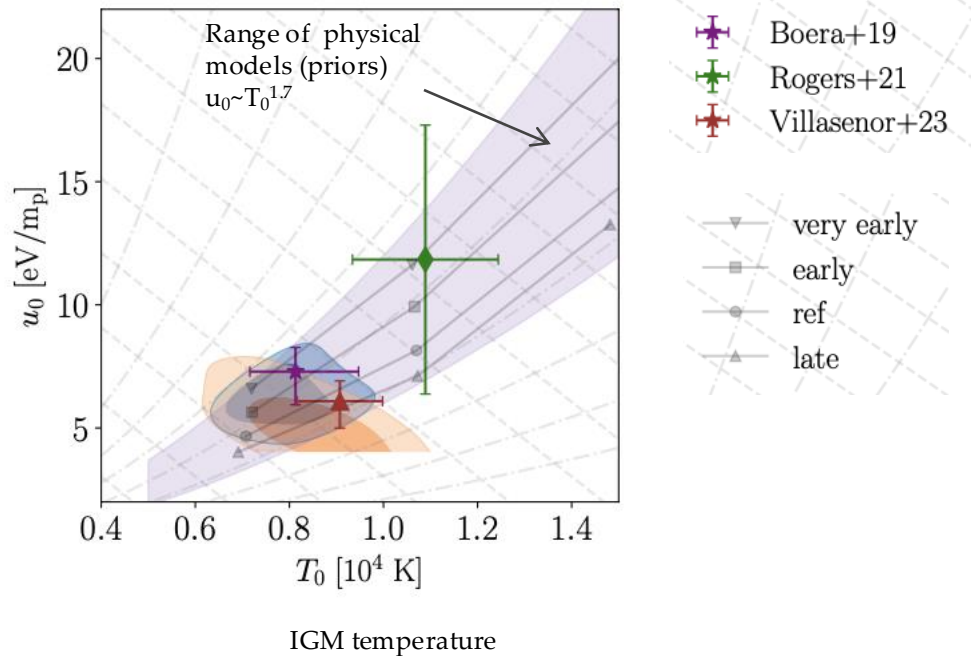
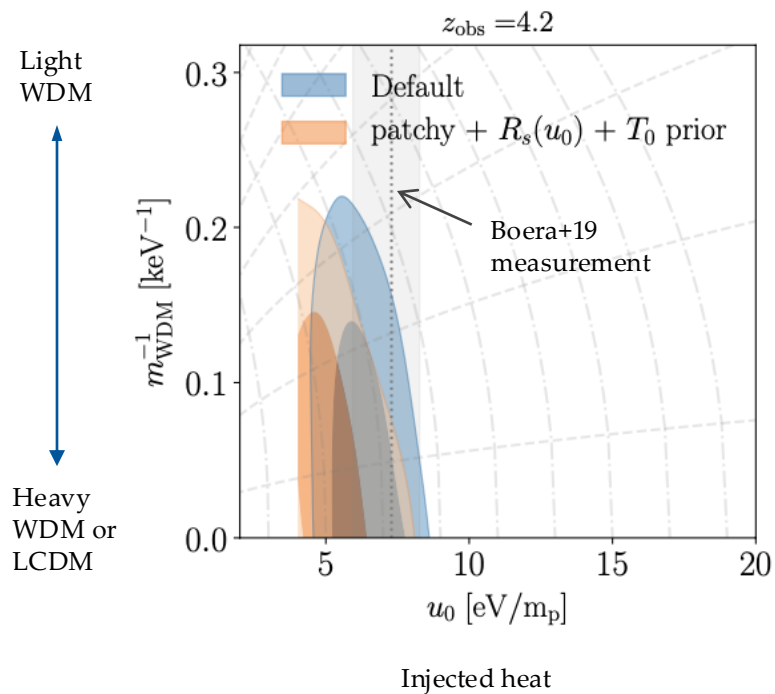


Boera+19, Irsic+23

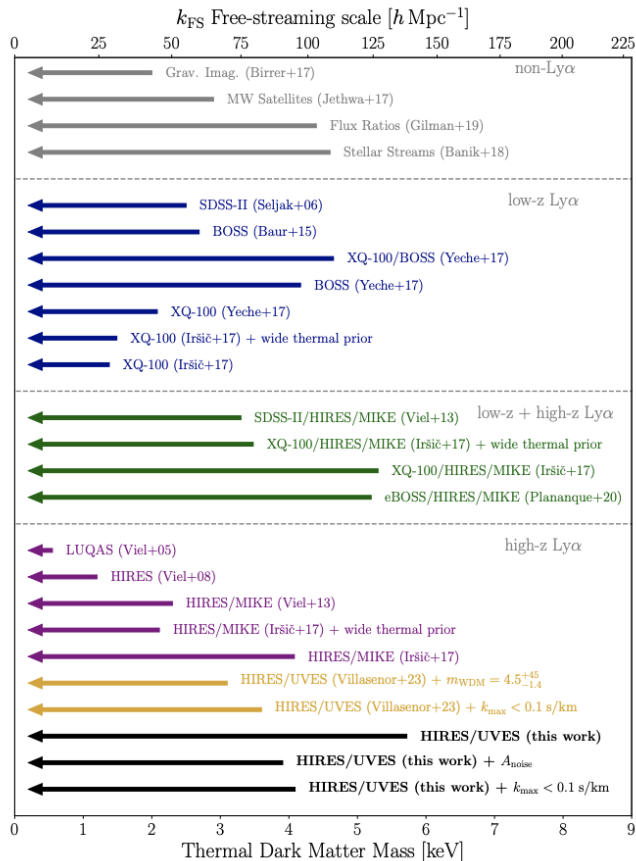


Thermal WDM - II

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Irsic, MV +23



Tests made:

Cut small scales

Marginalize over data noise

Assume/Remove T_0 priors

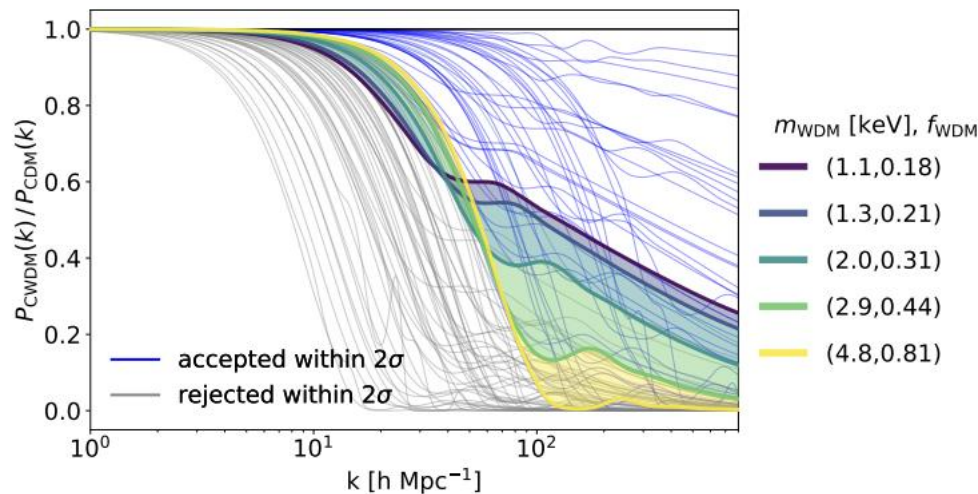
Correct for a model dependent resolution

Patchy reionization models

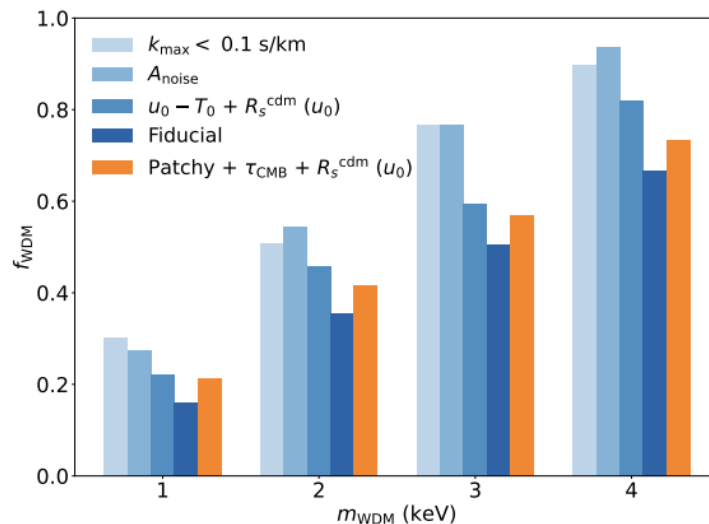
Name	m_{WDM} [keV] (2σ)	$\tau_{\text{eff}}(z=4.6)$	$T_0(z=4.6)$ [10^4 K]	$\gamma(z=4.6)$	$u_0(z=4.6)$ [eV/ m_p]	$A_{\text{noise}}(z=4.6)$	χ^2/dof
Default	> 5.72	$1.502^{+0.061}_{-0.061}$	$0.743^{+0.041}_{-0.075}$	$1.35^{+0.24}_{-0.19}$	$6.19^{+0.68}_{-0.68}$	-	40.7/34
$k_{\text{max}} < 0.1 \text{ km}^{-1} \text{ s}$	> 4.10	$1.501^{+0.060}_{-0.074}$	$0.840^{+0.095}_{-0.340}$	$1.28^{+0.09}_{-0.28}$	$8.91^{+1.57}_{-5.26}$	-	10.2/20
A_{noise}	> 3.91	$1.458^{+0.053}_{-0.074}$	$0.966^{+0.156}_{-0.466}$	$1.23^{+0.06}_{-0.23}$	$5.93^{+0.38}_{-2.28}$	$1.12^{+0.49}_{-0.29}$	18.4/31
T_0 prior	> 5.85	$1.494^{+0.062}_{-0.077}$	$0.770^{+0.110}_{-0.120}$	$1.31^{+0.10}_{-0.31}$	$6.50^{+1.00}_{-1.60}$	-	47.6/34
$R_s(u_0)$ mass resolution	> 4.44	$1.531^{+0.073}_{-0.064}$	$0.617^{+0.007}_{-0.118}$	$1.38^{+0.28}_{-0.13}$	$7.90^{+1.70}_{-2.30}$	-	30.7/34
patchy reion.	> 5.10	$1.486^{+0.058}_{-0.068}$	$0.686^{+0.046}_{-0.080}$	$1.33^{+0.17}_{-0.26}$	$5.32^{+0.58}_{-0.52}$	-	41.0/34
$R_s(u_0) + T_0$ prior	> 4.24	$1.473^{+0.056}_{-0.076}$	$0.83^{+0.11}_{-0.11}$	$1.28^{+0.09}_{-0.28}$	$5.53^{+0.73}_{-1.2}$	-	39.4/34
patchy + $R_s(u_0) + T_0$ prior	> 5.90	$1.450^{+0.051}_{-0.070}$	$0.828^{+0.098}_{-0.098}$	$1.26^{+0.08}_{-0.26}$	$4.87^{+0.52}_{-0.71}$	-	40.8/34

Mixed (Cold + Warm) dark matter models

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- ✓ 5 CDM models allowed by the data and their suppression in terms of matter power



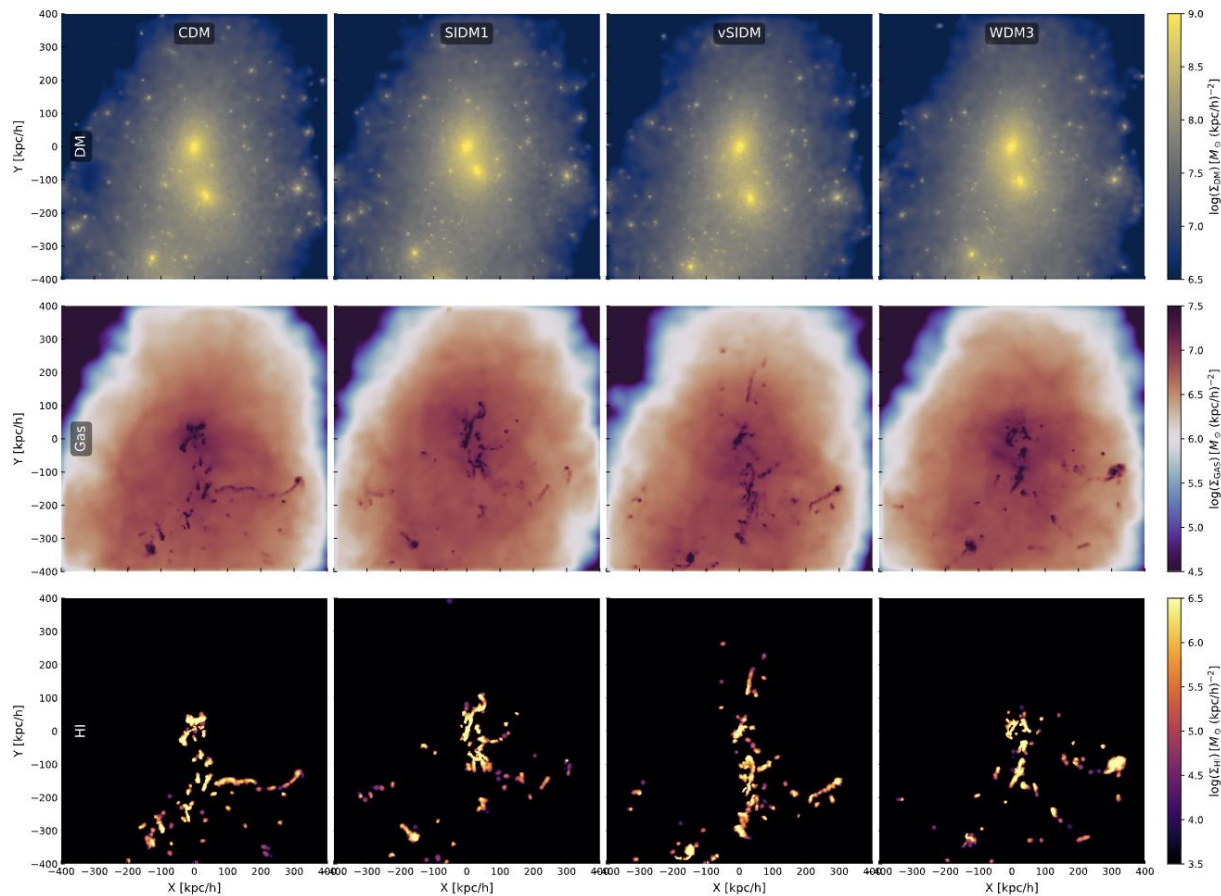
- ✓ Constraints

$$f_{\text{WDM}} = 0.14 (1\text{keV}/m_{\text{WDM}})^{-1.1}.$$

DM + galaxy formation halo environments

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$4.3 \times 10^{13} M_{\odot}$ halo
At $z=0$
50 Mpc/h box
 $M_{\text{gas}} = 6.8 \times 10^5 M_{\odot}$



How is HI distributed in non-cold DM haloes at $z=0$?

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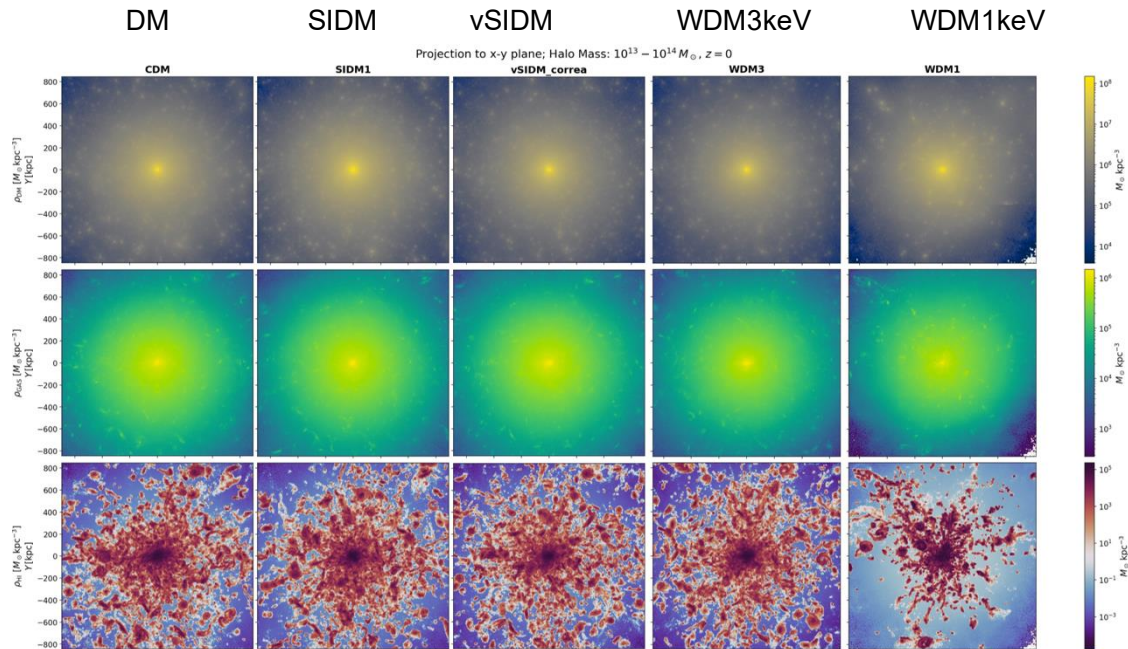
**Redshift $z=0$
stacking of 100
haloes $10^{13}-10^{14} M_{\odot}$**

DM

GAS

HI

Temperature



How is HI distributed in non-cold DM haloes at $z=3$?

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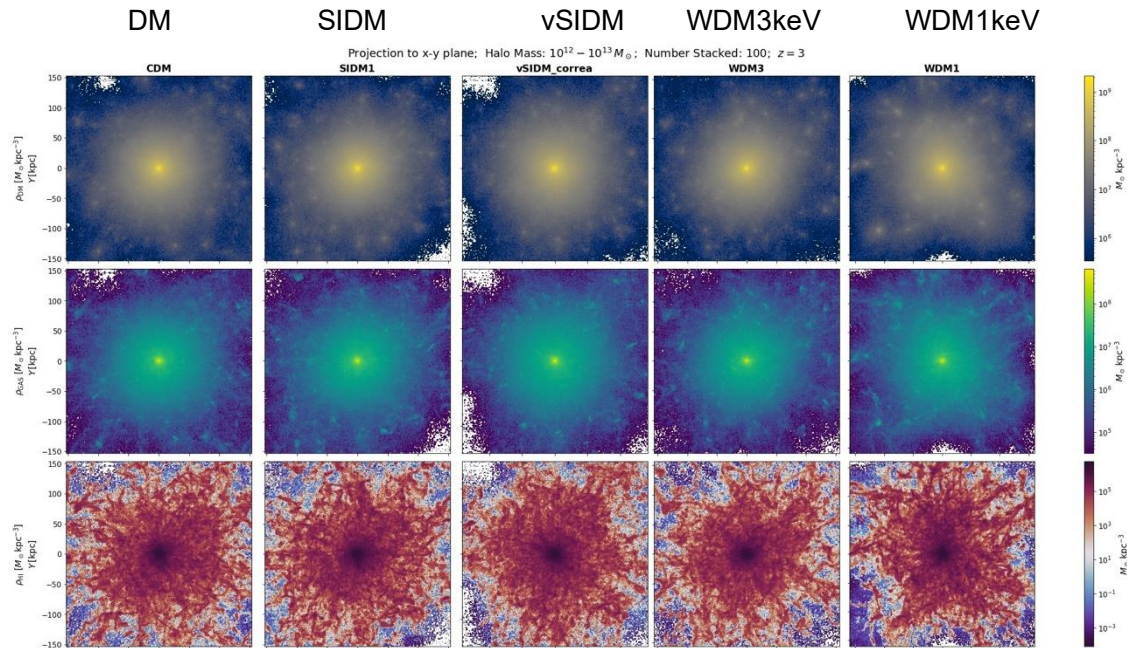
**Redshift $z=3$
stacking of 100
haloes $10^{12}-10^{13} M_{\odot}$**

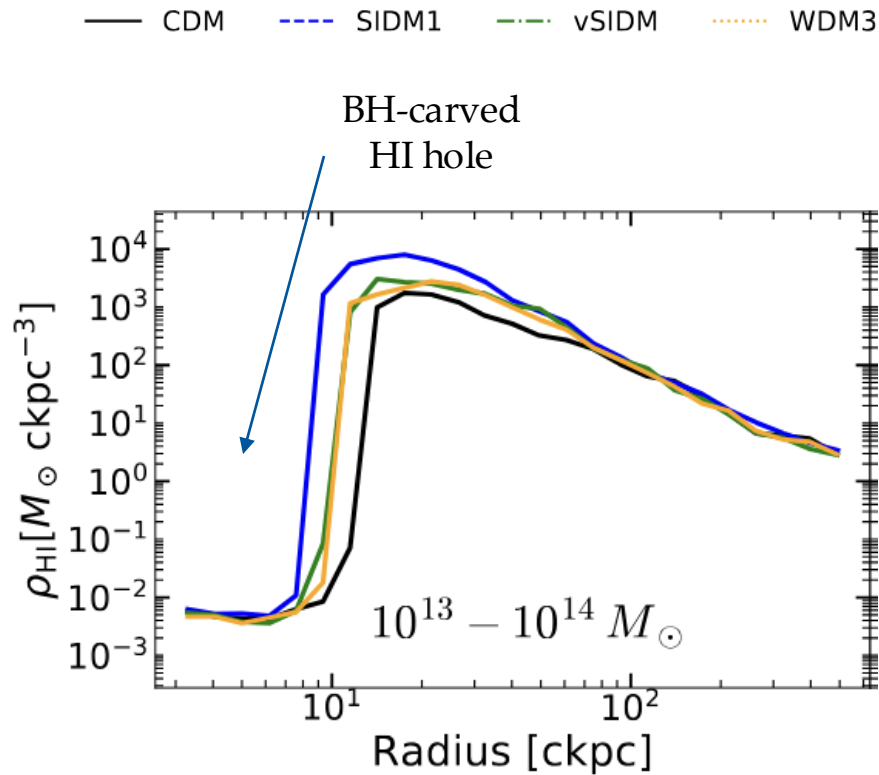
DM

GAS

HI

Temperature





- ✓ The low-density cosmic web as seen in the high redshift Lyman- α forest allows to constrain DM properties through 1D flux power
- ✓ WDM mass is constrained ($<3\text{-}5$ keV)
- ✓ WDM fraction is also constrained ($f < 0.2$ – depending on mass)
- ✓ Cosmic web is relatively cold consistent with CDM
- ✓ No sign of neutrino interactions
- ✓ Small scale HI distribution inside haloes could be impacted by DM nature

What about increase in power?

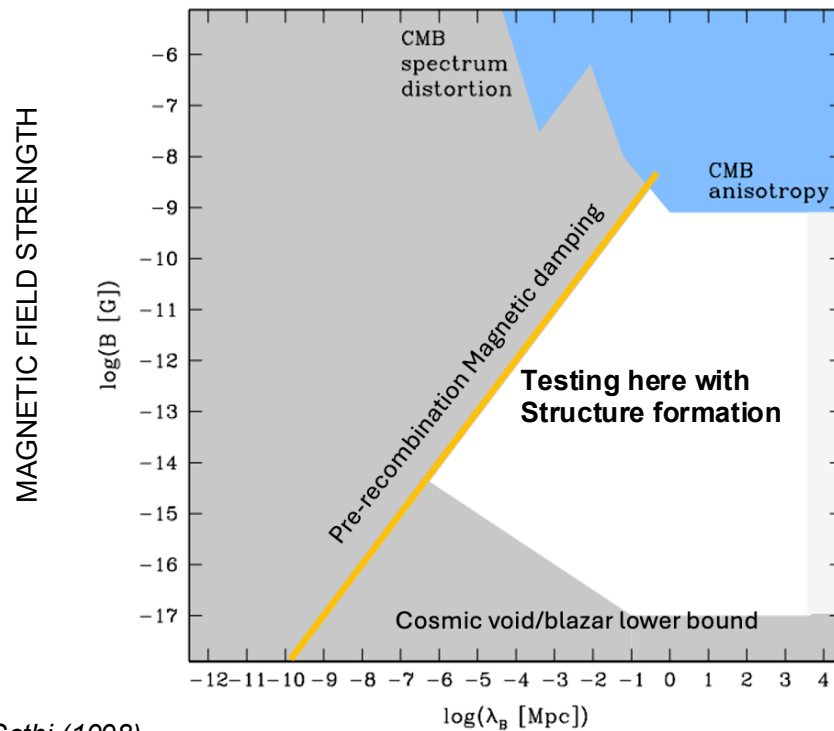
- ✓ Why do we care: observed in the Universe from planet scales up to cosmological scales even in cosmic voids (!)
- ✓ What can they tell us: they could be of astro or primordial origin (produced during inflation or phase transitions in the early Universe)
- ✓ When considered: strong implications for structure formation

Primordial Magnetic Fields (PMFs)

Matteo Viel

Durrer and Neronov 2013

- ✓ Why do we care: observed in the Universe from planet scales up to cosmological scales even in cosmic voids (!)
- ✓ What can they tell us: they could be of astro or primordial origin (produced during inflation or phase transitions in the early Universe)
- ✓ When considered: strong implications for structure formation



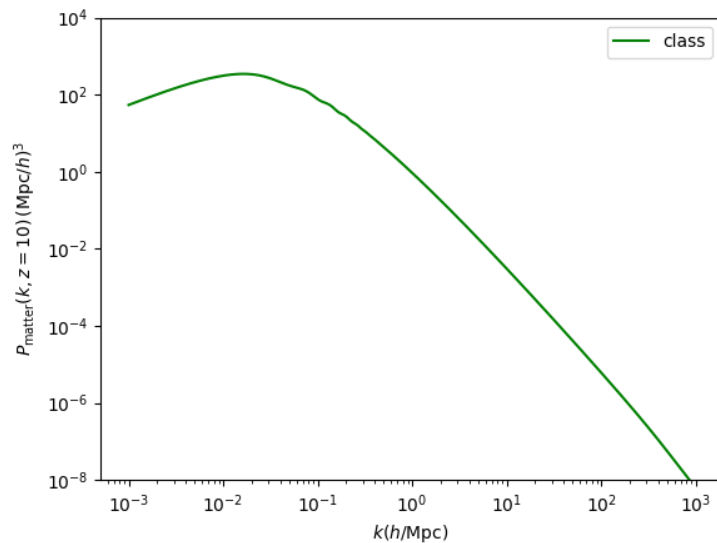
Wasserman (1978); Kim+ (1996); Subramanian & Barrow (1997); Gopal&Sethi (1998)

Kanhashvili+15, Sanati+20, Katz+21, Mtchelidze+22, Paoletti+22, Vazza+24, Dolag+15, Jedamzik+20

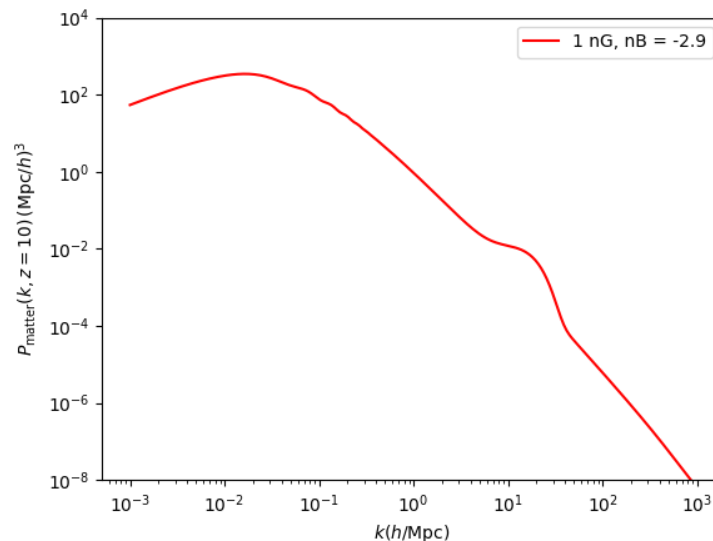
$$\langle B_i(k) B_j^*(k') \rangle = (2\pi)^3 \delta^3(k - k') \left(\delta_{ij} - \frac{k_i k_j}{k^2} \right) \frac{P_B(k)}{2}$$

$$P_B(k) \propto B_{1\text{Mpc}}^2 k^{n_B}$$

$P_{\Lambda\text{CDM}}$



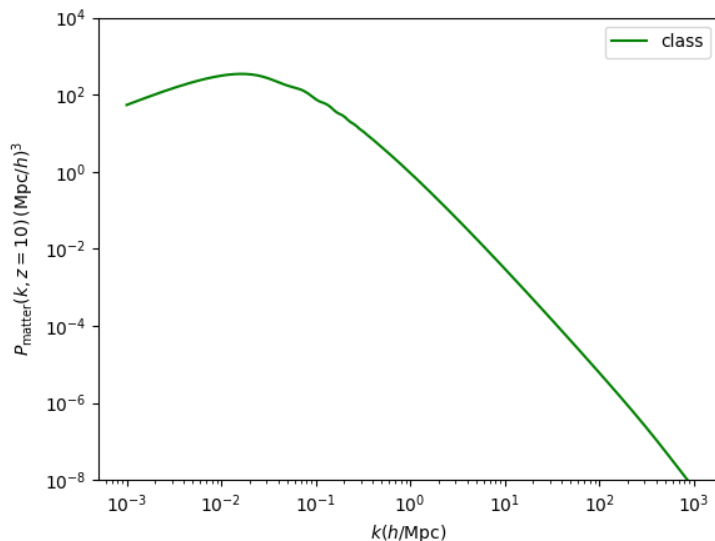
$P_{\Lambda\text{CDM}} + P_{\text{PMF}}$



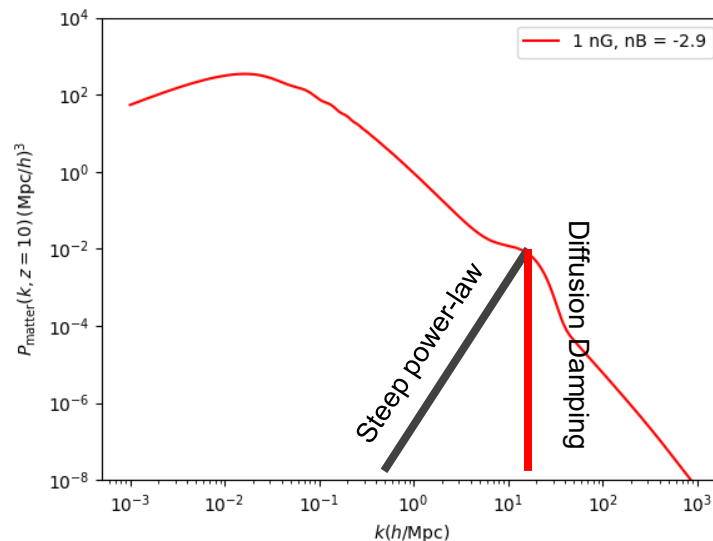
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$P_{\Lambda\text{CDM}}$



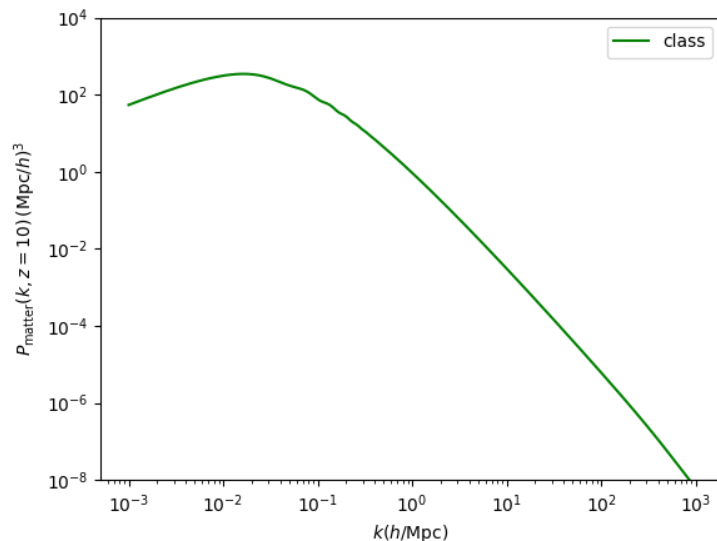
$P_{\Lambda\text{CDM}} + P_{\text{PMF}}$



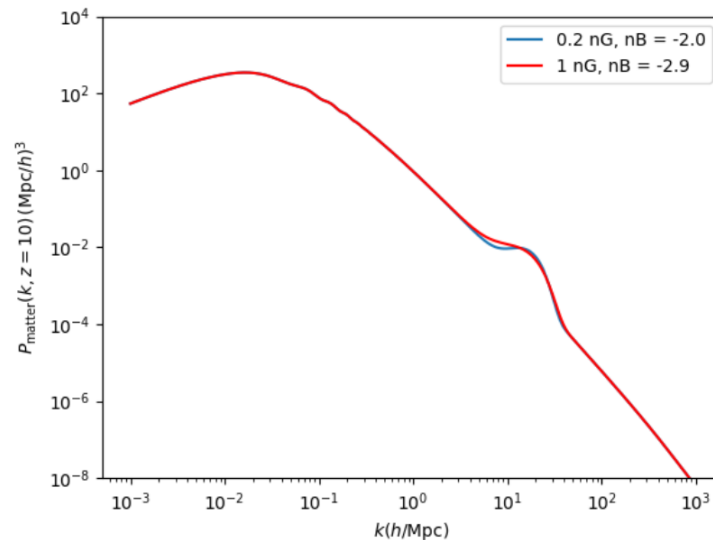
$$\langle B_i(k) B_j^*(k') \rangle = (2\pi)^3 \delta^3(k - k') \left(\delta_{ij} - \frac{k_i k_j}{k^2} \right) \frac{P_B(k)}{2}$$

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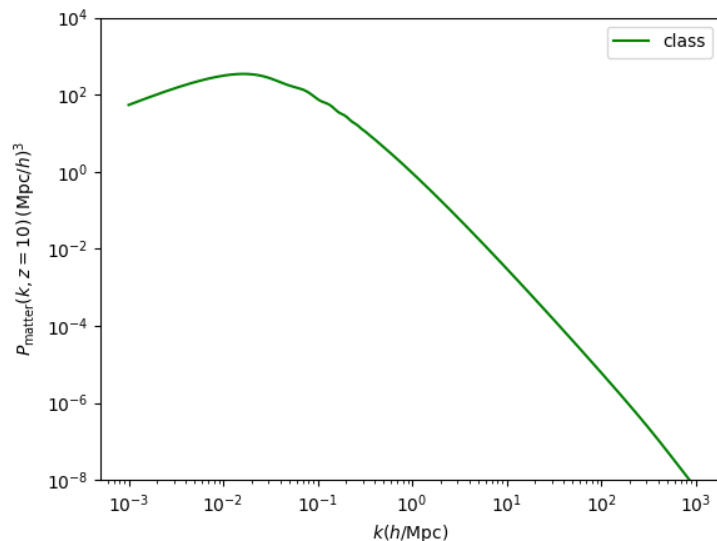
$P_{\Lambda\text{CDM}} + P_{\text{PMF}}$



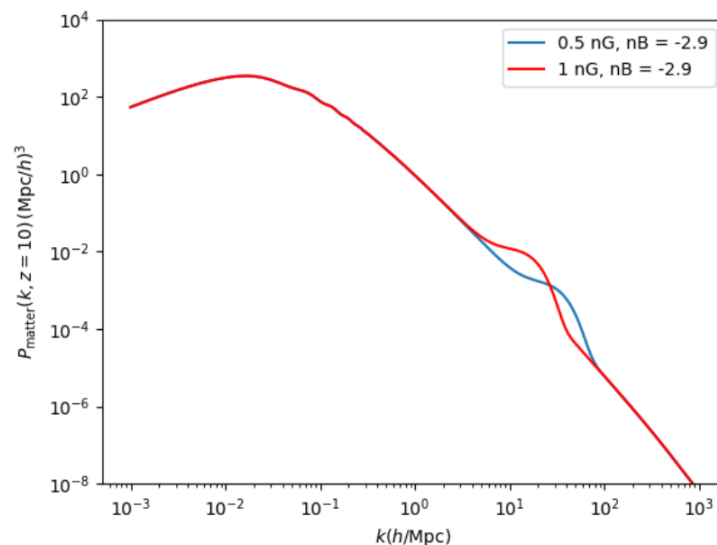
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$$P_B(k) \propto B_{1\text{Mpc}}^2 k^{n_B}$$

$P_{\Lambda\text{CDM}}$



$P_{\Lambda\text{CDM}} + P_{\text{PMF}}$



$$\frac{\partial (\vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \times \vec{B})}{a}$$

$$\frac{\partial \vec{v}_b}{\partial t} + H \vec{v}_b + \frac{(\vec{v}_b \cdot \nabla) \vec{v}_b}{a} = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a^5 \rho_b} - \frac{c_b^2 \nabla \delta_b}{a} - \frac{\nabla \phi}{a}$$

$$\frac{\partial \delta_b}{\partial t} = -\frac{\nabla \cdot \vec{v}_b}{a} - \frac{\nabla \cdot (\delta_b \vec{v}_b)}{a}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \left[\frac{\partial \ln(a^2 H)}{\partial \ln a} + 1 \right] \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

$$\frac{\partial \vec{B}}{\partial t} = \frac{\nabla \times (\vec{v} \times \vec{B})}{a}$$

$$\frac{\partial \vec{v}_b}{\partial t} + H \vec{v}_b + \frac{(\vec{v}_b \cdot \nabla) \vec{v}_b}{a} = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a^5 \rho_b} - \frac{c_b^2 \nabla \delta_b}{a} - \frac{\nabla \phi}{a}$$

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At large scales

$$\delta \ll 1$$

$$v_b \ll aH$$

Velocity field is generated

$$\partial_t v_b \propto (\nabla \times B) \times B$$

Ideal MHD in the postrecombination Universe

Matteo Viel

$$\frac{\partial (\vec{B})}{\partial t} = 0$$

Comoving Magnetic field is conserved

$$\frac{\partial^2 \delta_b}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_b}{a \partial a} = - \frac{\nabla \cdot (\nabla \times \vec{B}) \times \vec{B}}{(4\pi a^3 \rho_b) a^5 H^2} + \frac{\nabla^2 \phi}{(a^2 H)^2}$$

Baryon perturbations driven by magnetic field and gravity

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

Gravity has the usual form

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

Ideal MHD in the postrecombination Universe

Matteo Viel

$$\frac{\partial (\vec{B})}{\partial t} = 0$$

$$\frac{\partial^2 \delta_b}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_b}{a \partial a} = - \frac{\nabla \cdot (\nabla \times \vec{B}) \times \vec{B}}{(4\pi a^3 \rho_b) a^5 H^2} + \frac{\nabla^2 \phi}{(a^2 H)^2}$$

$S_0/a^3 H^2$

$$S_0 = \frac{\nabla \cdot [(\nabla \times \vec{B}) \times \vec{B}]}{4\pi a^3 \rho_b}$$

Key ingredient is the S_0 source term

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

Ideal MHD in the postrecombination Universe

Matteo Viel

$$a^2 \frac{\partial^2 \delta_b}{\partial a^2} + a \frac{3}{2} \frac{\partial \delta_b}{\partial a} - \frac{3}{2} \frac{\Omega_b}{\Omega_m(1 + a_{\text{eq}}/a)} \delta_b = -\frac{S_0}{a^3 H^2} + \frac{3}{2} \frac{\Omega_{\text{DM}}}{\Omega_m(1 + a_{\text{eq}}/a)} \delta_{\text{DM}}$$

DM

Coupled differential equations

$$a^2 \frac{\partial^2 \delta_{\text{DM}}}{\partial a^2} + a \frac{3}{2} \frac{\partial \delta_{\text{DM}}}{\partial a} - \frac{3}{2} \frac{\Omega_{\text{DM}}}{\Omega_m(1 + a_{\text{eq}}/a)} \delta_{\text{DM}} = \frac{3}{2} \frac{\Omega_b}{\Omega_m(1 + a_{\text{eq}}/a)} \delta_b.$$

baryons

$$\delta_b^{\text{PMF}} = -\xi_b(a) \frac{S_0}{a^3 H^2}$$

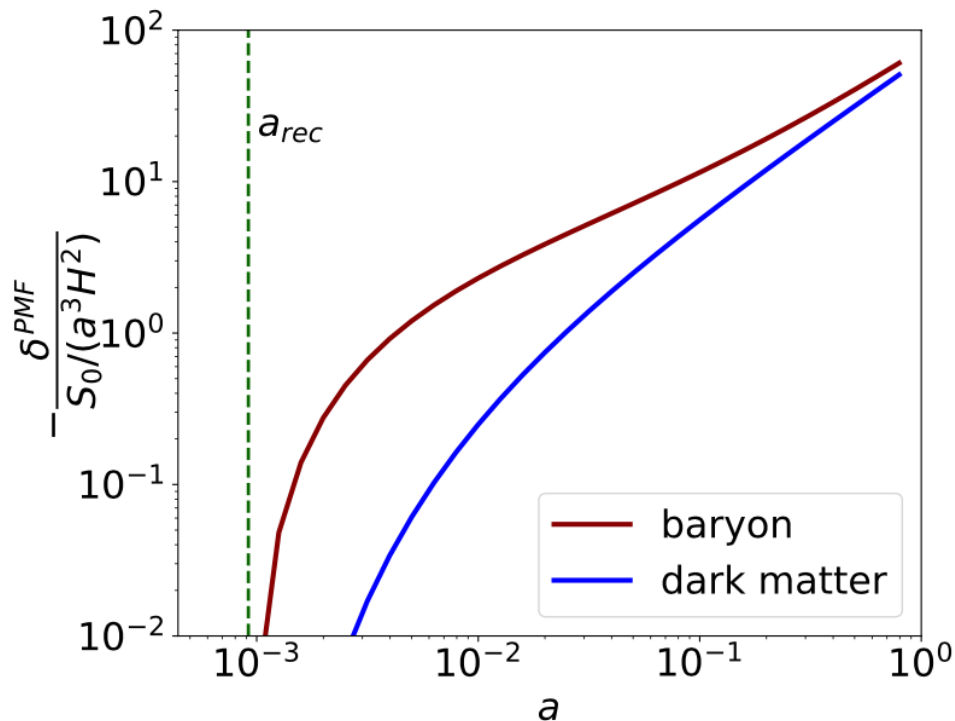
$$\delta_{\text{DM}}^{\text{PMF}} = -\xi_{\text{DM}}(a) \frac{S_0}{a^3 H^2}.$$

$$P_b^{\text{PMF}} \propto P_{S_0}$$

Power spectrum of Lorentz force
For $n_B \sim -3$ (scale invariant) this returns
 $P_{\text{matter}} \sim k$

Ideal MHD in the postrecombination Universe

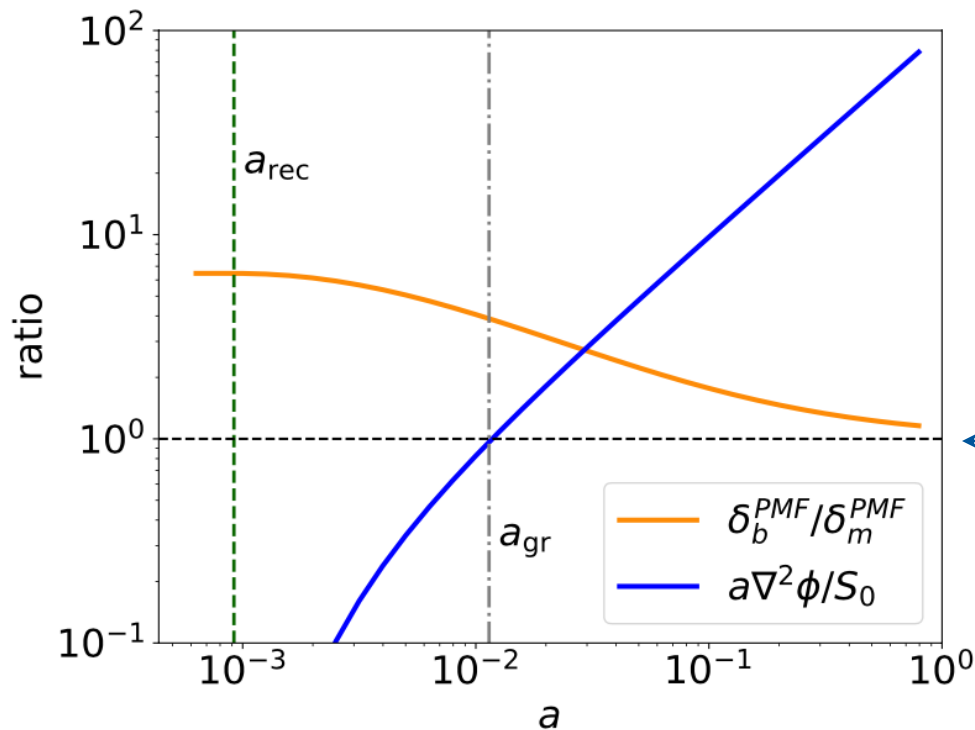
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- ✓ Time evolution of perturbations (scale dependence is hidden in S_0)
- ✓ Baryons are primarily enhanced
- ✓ DM is lagging behind and eventually catches up at $z \sim 0$

Ideal MHD in the postrecombination Universe

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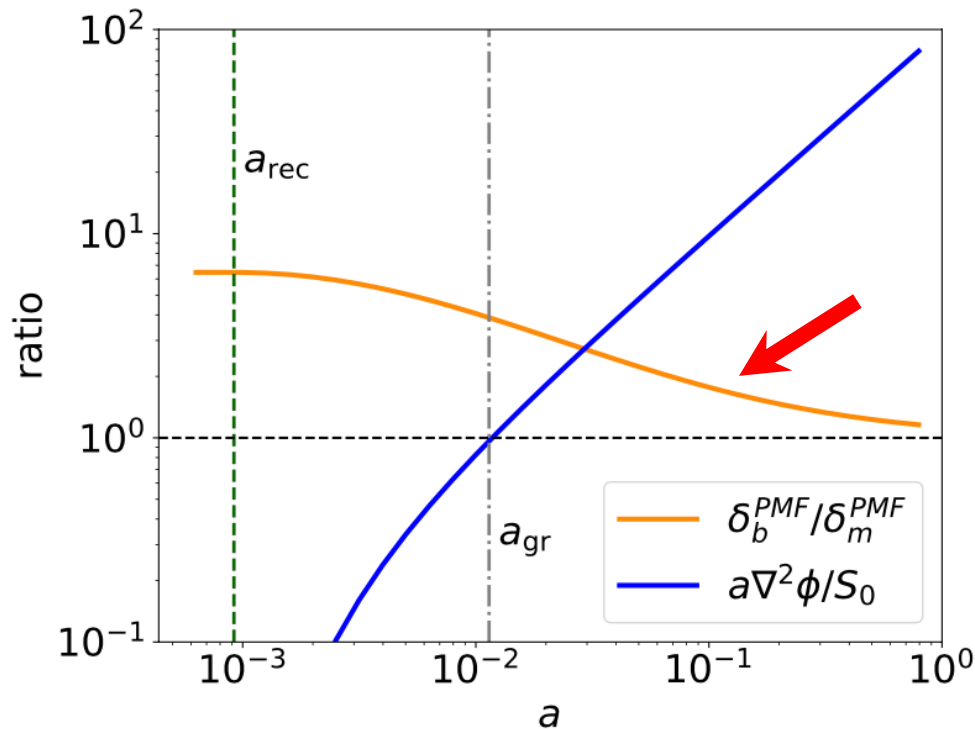


- ✓ Ratio of perturbations is equivalent to baryon fraction and starts very high and only now reaches the cosmic mean 0.17 value

← Cosmic mean

Ideal MHD in the postrecombination Universe

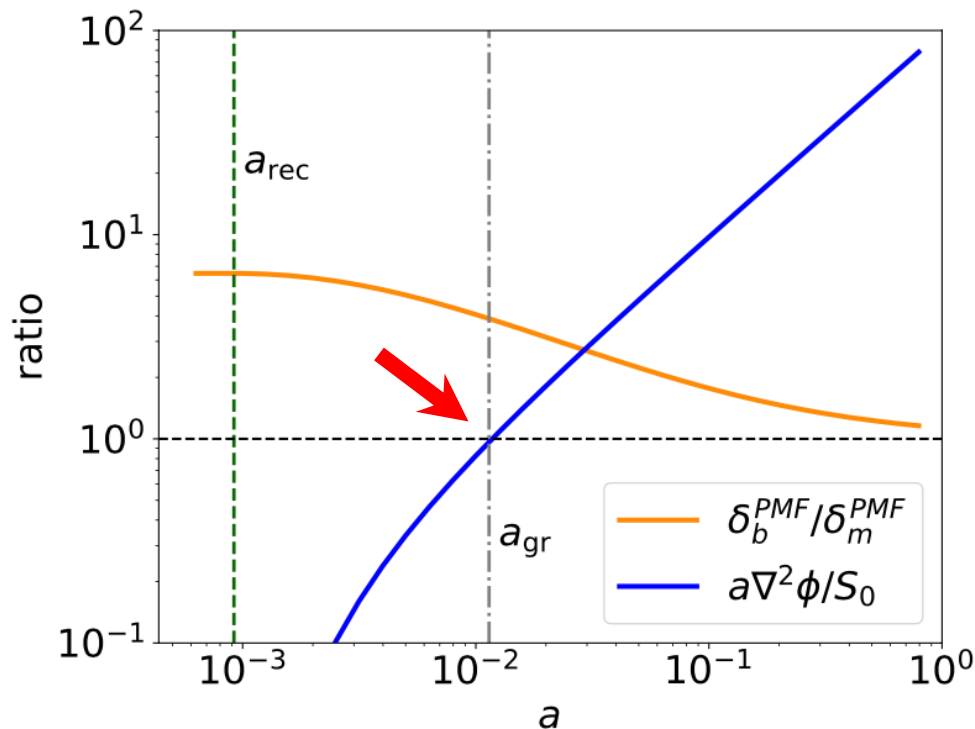
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- ✓ Ratio of perturbations is equivalent to baryon fraction starts very high and only now reaches the cosmic mean 0.17 value
- ✓ At $z=10$ baryon fraction is 2 times the cosmic mean

Ideal MHD in the postrecombination Universe

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- ✓ Ratio of perturbations is equivalent to baryon fraction starts very high and only now reaches the cosmic mean 0.17 value
- ✓ At $z=10$ baryon fraction is 2 times the cosmic mean
- ✓ At $z=100$ gravity overcomes Lorentz force (this is independent of B and at all scales)

$$v_b \sim \frac{1}{aH\lambda_D} \frac{\vec{B}_{\text{phys}}^2}{4\pi\rho_b}.$$

Baryon flow velocity from Euler Equation (Lorentz force)

$$v_b/\lambda_D \sim aH$$

Breaking of linearity

$$v_A^2 \equiv \frac{\langle \vec{B}_{\text{phys}}^2 \rangle}{4\pi\rho_b}$$

Alfven velocity def.

$$\lambda_D \sim \frac{v_A}{aH}$$

- ✓ Linear perturbation theory does not work at small scales
- ✓ Density perturbations backreact on the magnetic field
- ✓ MHD Turbulence suppresses perturbations

$$\lambda_D \sim 0.1 \text{Mpc} \left(\frac{B}{\text{nG}} \right) \quad k_D \sim 3(nG/B_0) \text{Mpc}^{-1}$$

The baryon PMF induced power spectrum

Matteo Viel

$$P_B(k) = A k^{n_B} e^{-k^2 \lambda_D^2}$$

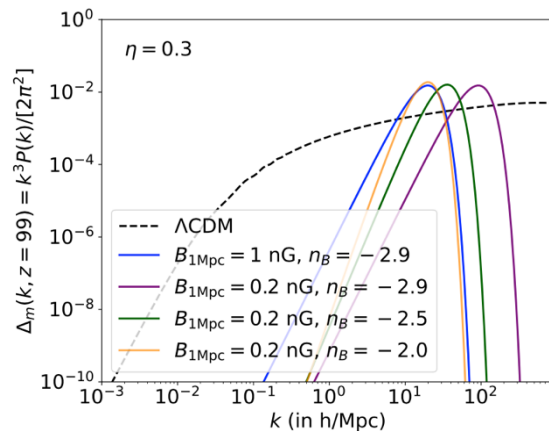
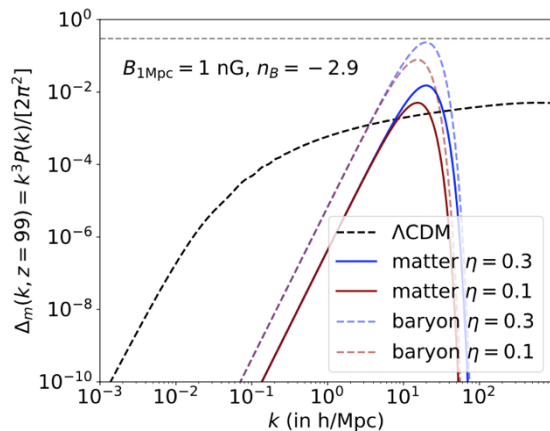
$$B_{1\text{Mpc}}^2 \equiv \int \frac{d^3 k}{(2\pi)^3} P_B(k) e^{-k^2 \lambda_{\text{Mpc}}^2} = \frac{A \lambda_{\text{Mpc}}^{-(3+n_B)}}{4\pi^2} \Gamma([n_B + 3]/2)$$

$$P_b^{\text{PMF}}(k) = \xi_b^2(a) \frac{k^4}{8(4\pi a^3 \rho_b [a^3 H^2])^2} \int \frac{d^3 q}{(2\pi)^3} \frac{P_B(q) P_B(k-q)}{(k-q)^2} \left[k^2 + 2q^2 + 4 \frac{(q \cdot k)^4}{k^4 q^2} - 4 \frac{(q \cdot k)^2}{k^2} - 4 \frac{(q \cdot k)^3}{k^2 q^2} + \frac{(q \cdot k)^2}{q^2} \right]$$

$$\Delta_b^{\text{PMF}}(k) \equiv \frac{k^3 P_b^{\text{PMF}}(k)}{2\pi^2} = 10^{-4} \xi_b^2(a) \left(\frac{k}{\text{Mpc}^{-1}} \right)^{2n_B+10} \left(\frac{B_{1\text{Mpc}}}{\text{nG}} \right)^4 G_{n_B} e^{-2k^2 \lambda_D^2}, \quad (2.)$$

where G_{n_B} is a dimensionless number determined by

$$G_{n_B} = \int_0^\infty dx \int_{-1}^1 \frac{dy}{2} x^{n_B+2} (1+x^2-2xy)^{n_B/2-1} \frac{[1+2x^2+4y^4x^2-4y^2x^2-4y^3x+y^2]}{\Gamma^2([n_B+3]/2)}$$

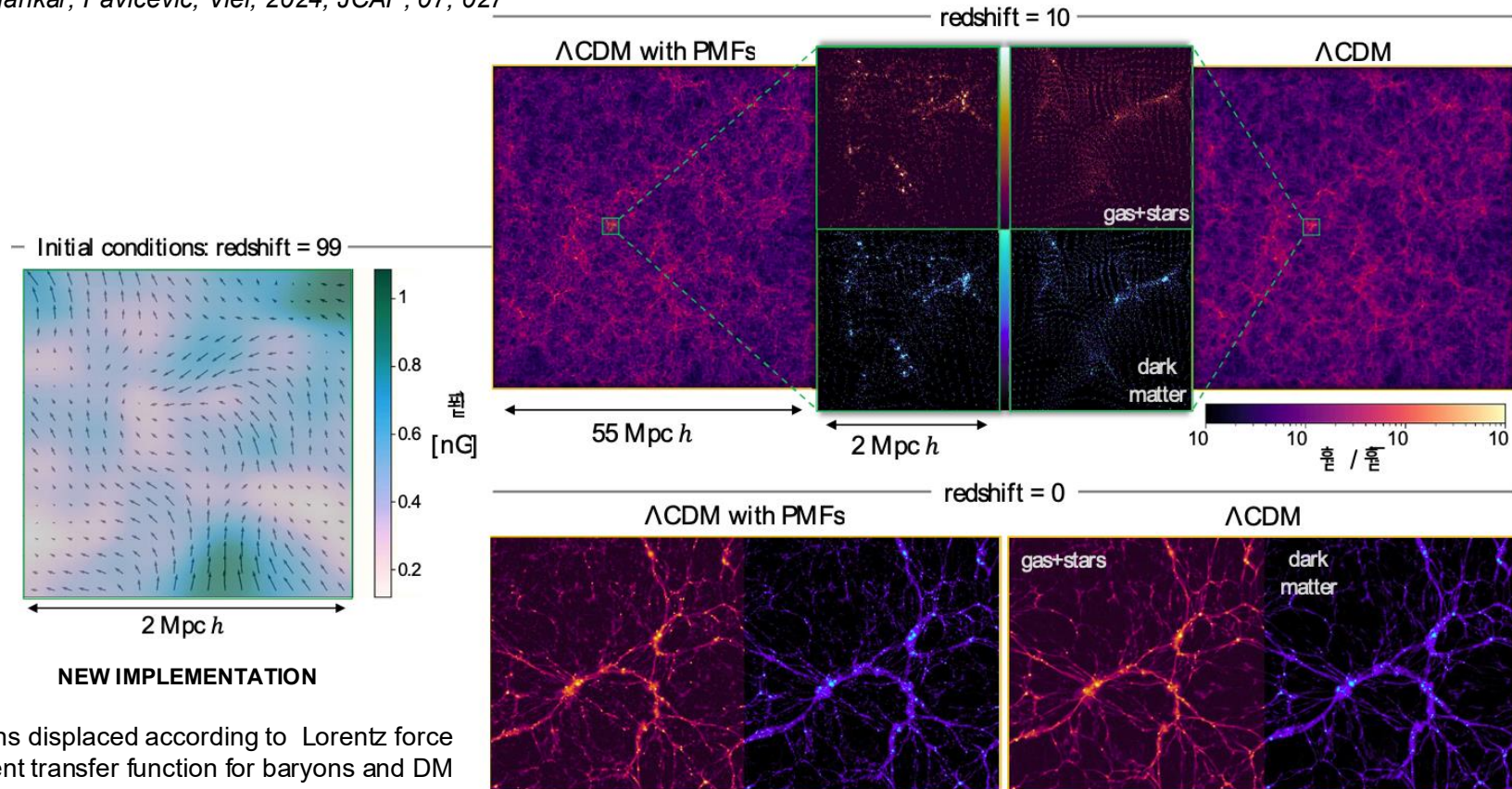


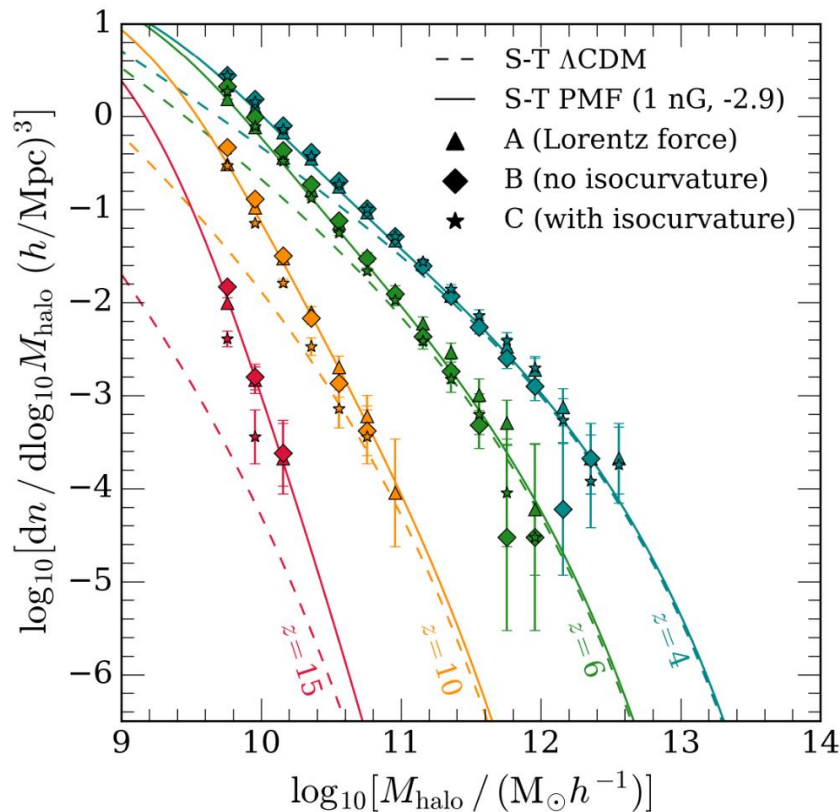
Ralegankar, Pavicevic, Viel 2024
Adi, Cruz, Kamionkowski 2024

Hydro sims

Matteo Viel

Ralegankar, Pavicevic, Viel, 2024, JCAP, 07, 027

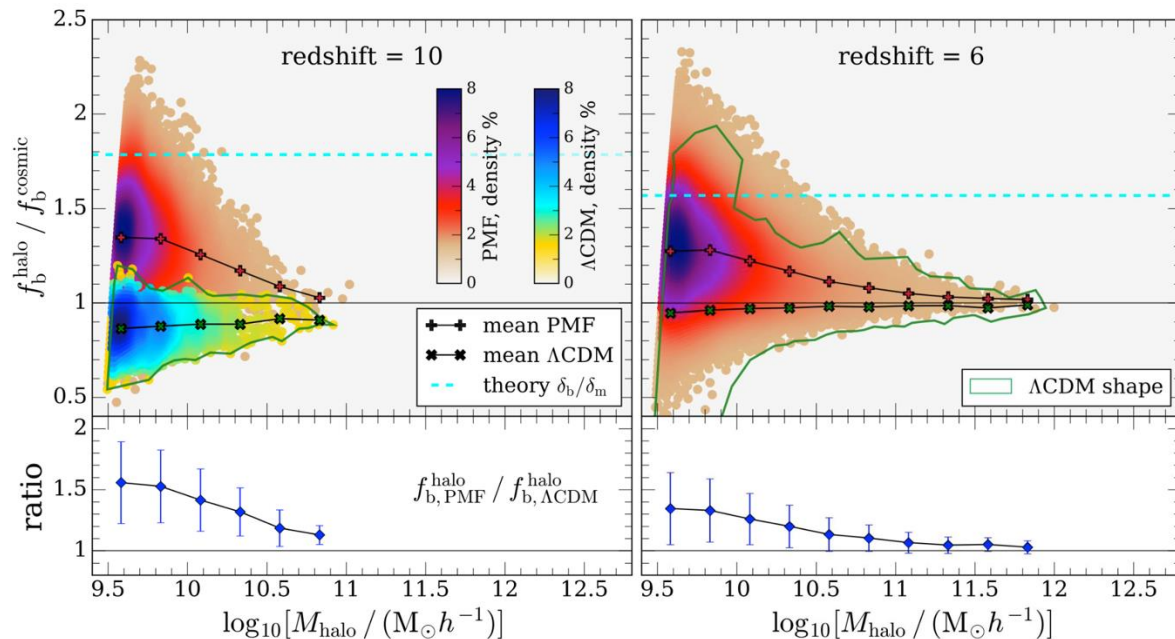




- ✓ Extra PMFs power produces more haloes, at “low” mass
- ✓ With lower B values (< 1 nG) the enhancement will move to lower masses
- ✓ Below 0.05 nG effect is probably too small at any scale

Halo Baryon Fractions at high redshift

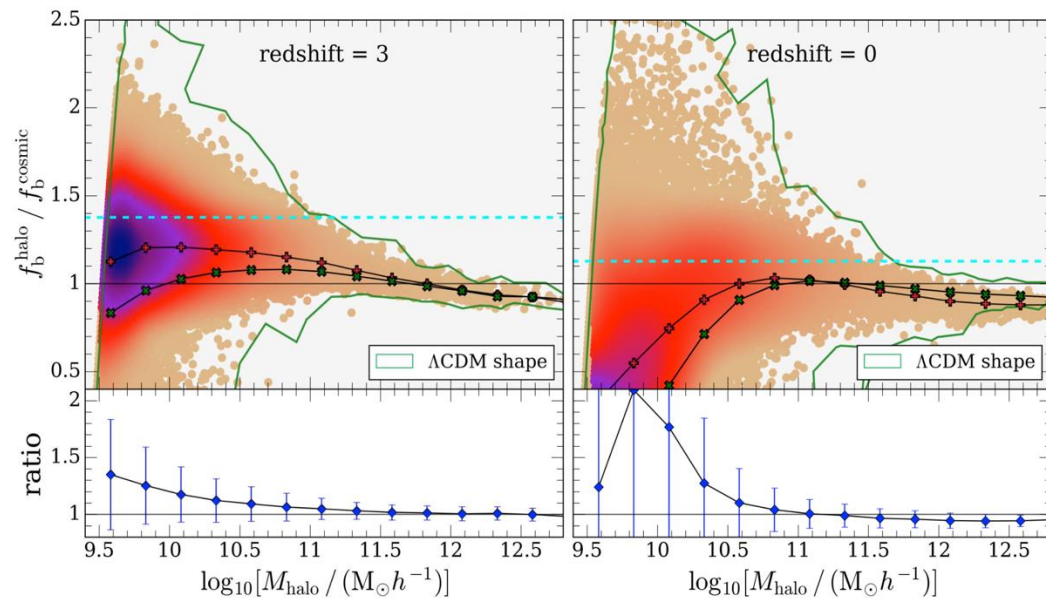
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- ✓ Larger baryon fraction in haloes also shown in hydro sims
- ✓ At large masses (scales) cosmic values is recovered
- ✓ More scatter in PMF models

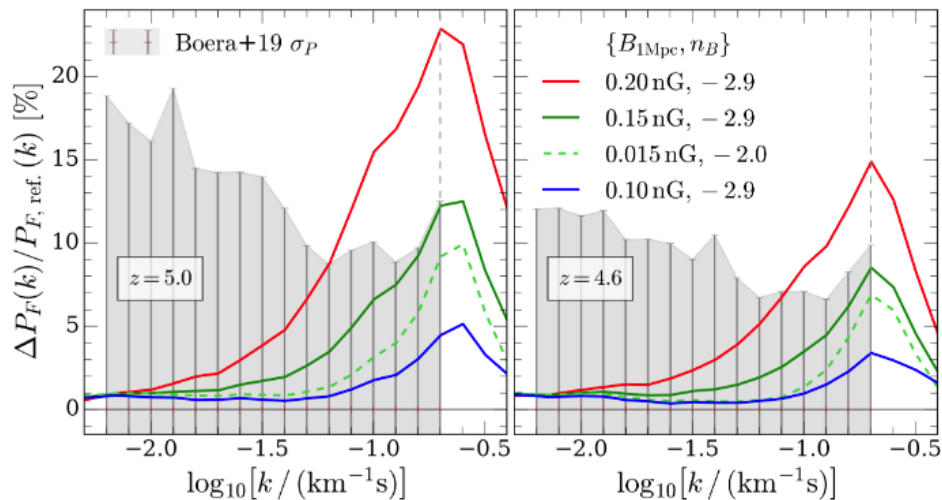
Halo Baryon fraction at lower redshift

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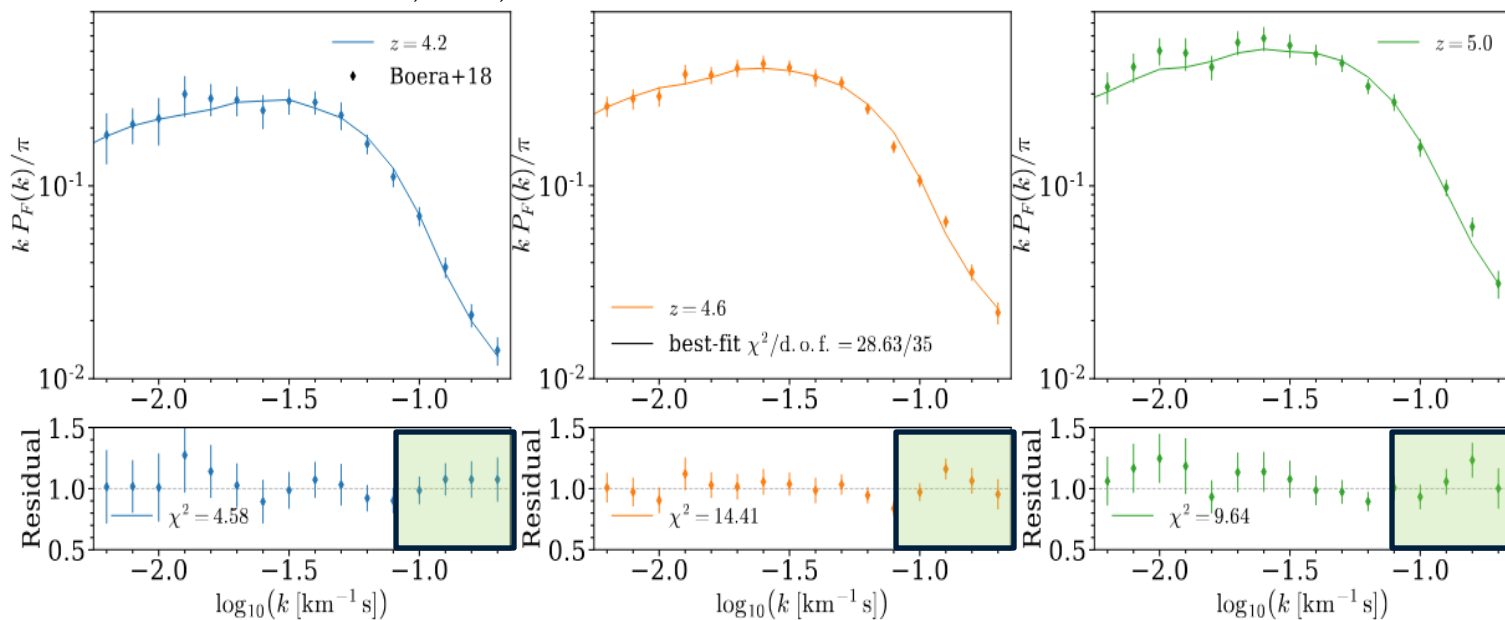
- ✓ At low ($z < 3$) redshift the effect vanishes

Pavicevic, Irsic, MV et al. 2025



✓ Strong scale/z dependent increase of power

Pavicevic, Irsic, MV et al. 2025

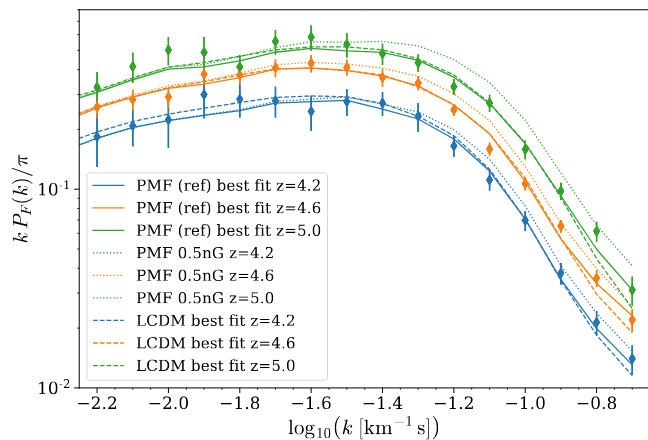


$$\chi^2_{\Lambda\text{CDM}} = 40.8 \text{ for } 36 \text{ d.o.f.}$$

$$\chi^2_{\text{PMF}} = 28.63 \text{ for } 35 \text{ d.o.f.}$$

Constraints on peak position

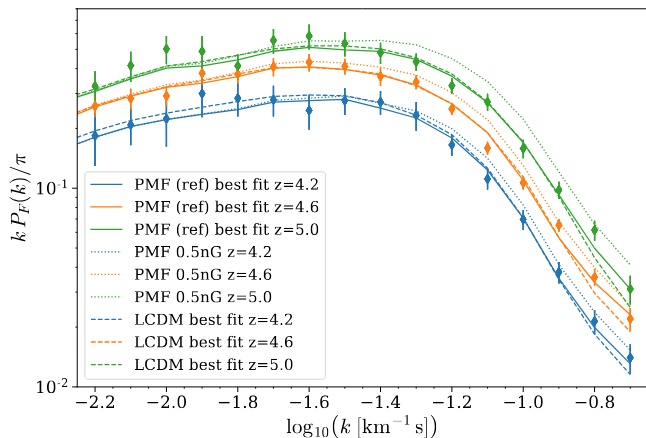
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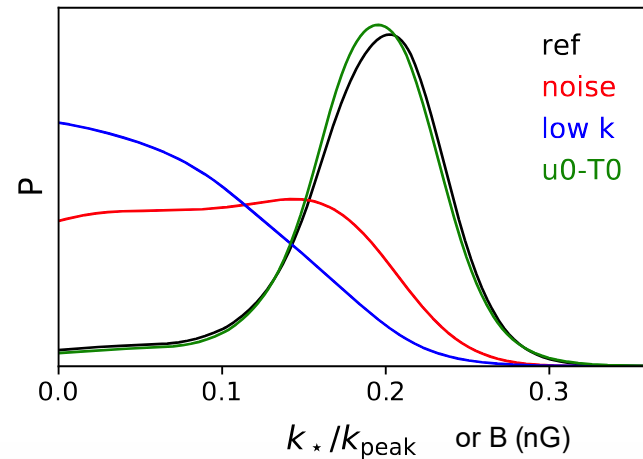
Constraints on peak position

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$$k_{\text{peak}} = \lambda_D^{-1} \sqrt{\frac{n_B + 5}{2}} \text{ Mpc}^{-1} \quad k_{\star} = 10 \text{ Mpc}^{-1}$$



Pavicevic, Irsic, MV et al. 2025



Detection $\rightarrow B = 0.2 \pm 0.05 \text{ nG}$ (1s)

Upper limit $\rightarrow B = 0.3 \text{ nG}$ (3s)

IGM as a calorimeter

- ✓ Dark Photon Dark Matter: simple extension of the SM of particle physics

$$\mathcal{L}_{\gamma A'} = -\frac{1}{4}F_{\mu\nu}^2 - \frac{1}{4}(F'_{\mu\nu})^2 - \frac{\epsilon}{2}F^{\mu\nu}F'_{\mu\nu} + \frac{1}{2}m_{A'}^2 A_{\mu}' A_{\mu}'$$

- ✓ Dark photon converts into standard photon when a resonance condition is met

$$E_{A' \rightarrow \gamma} \sim 2.5 \text{ eV} \left(\frac{\epsilon_{-14}}{0.5} \right)^2 \left(\frac{3}{1+z_{\text{res}}} \right)^{3/2} \left(\frac{m_{-13}}{0.8} \right)$$

The IGM as a thermometer

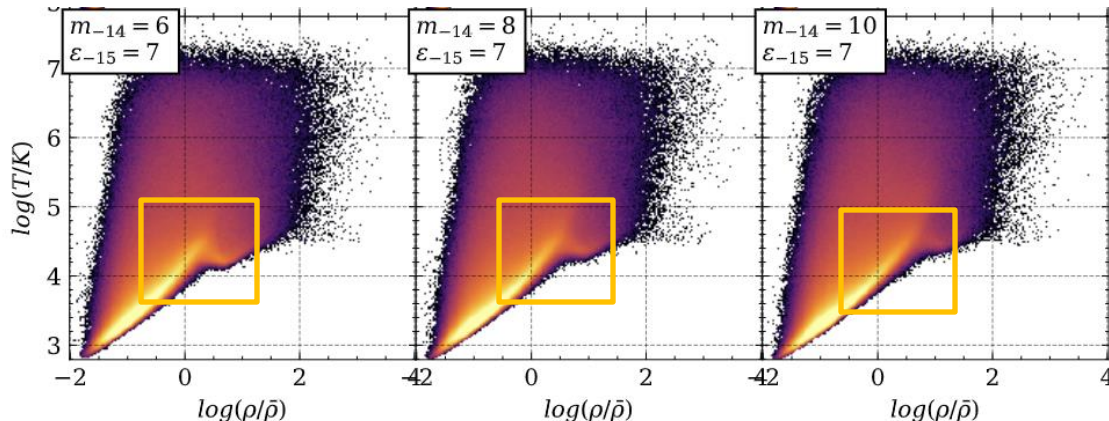
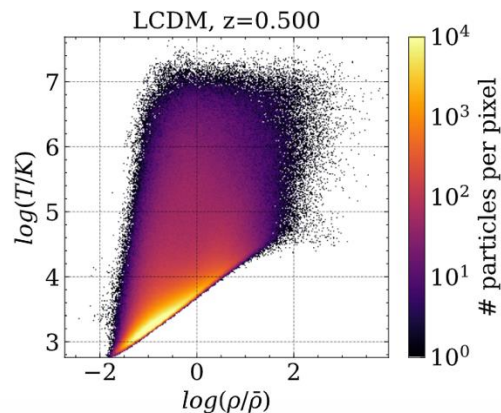
Matteo Viel

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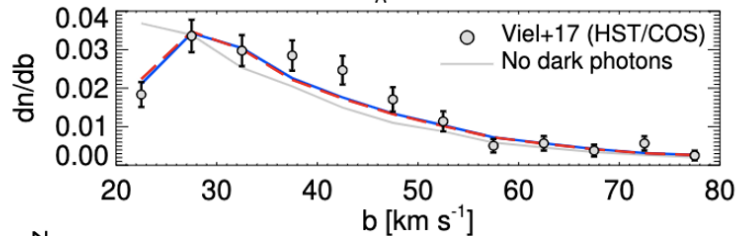
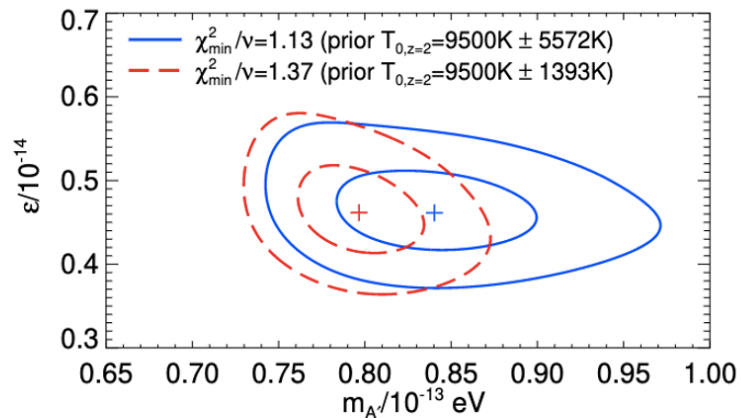
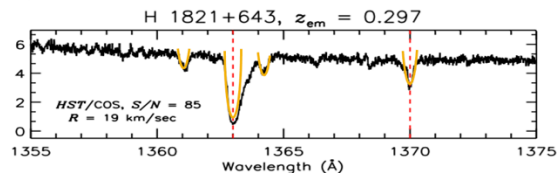
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The IGM as a thermometer - II

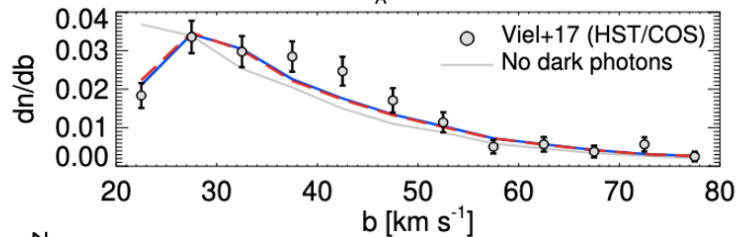
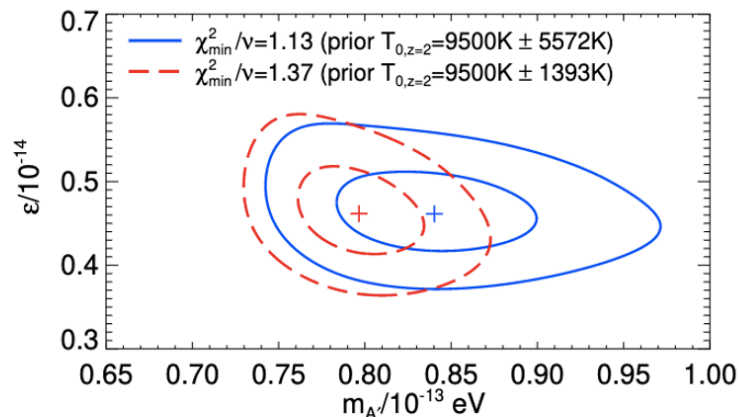
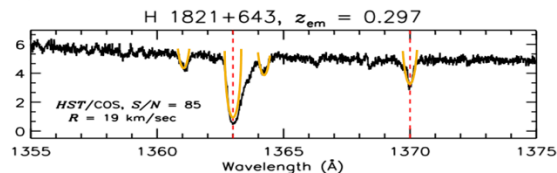
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- ✓ Effect is small but can be used to place constraints on extra-heating
- ✓ At $z=0.1$ COS/HST lines are broader than expected (feedback, turbulence?)

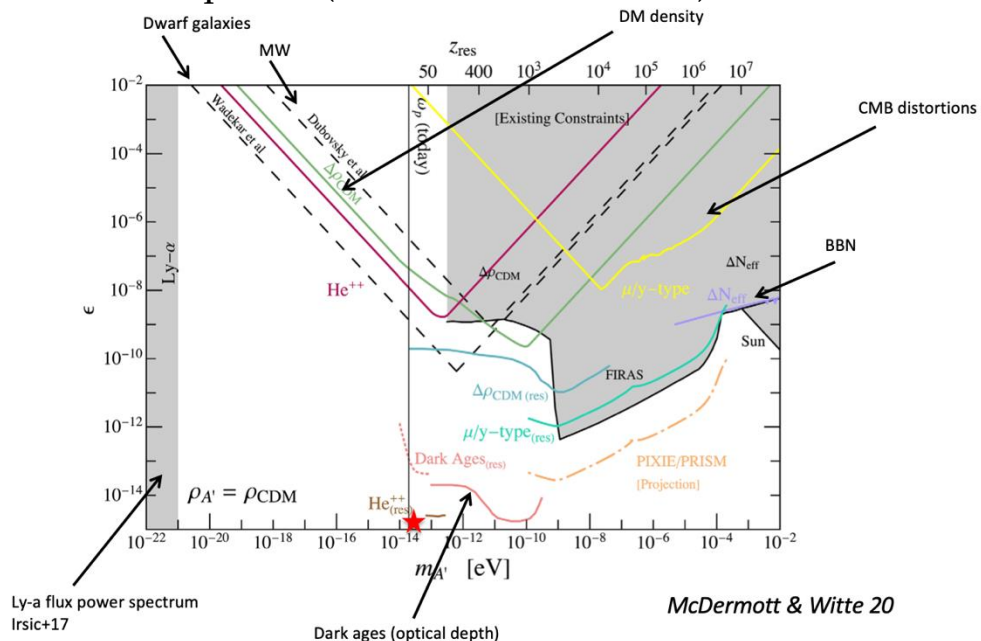
The IGM as a thermometer - II

Matteo Viel



➤ Effect is small but can be used to place constraints on extra-heating

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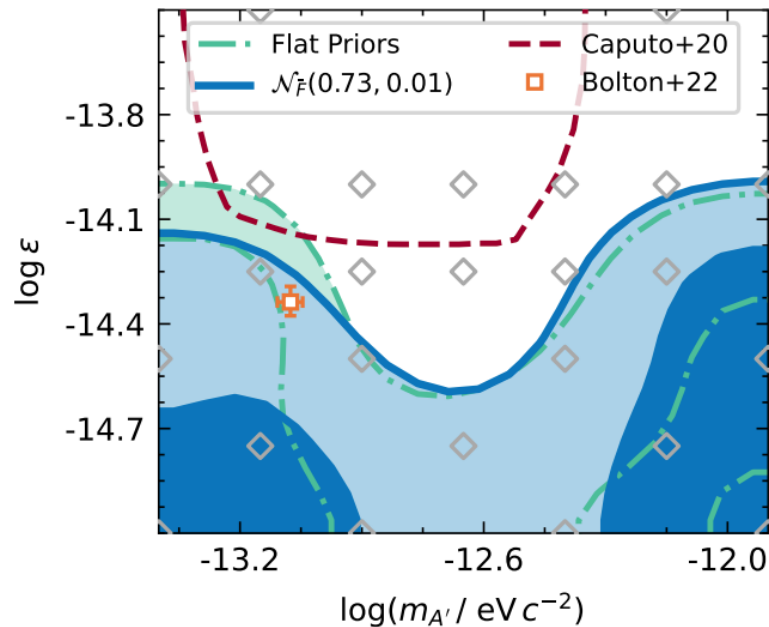
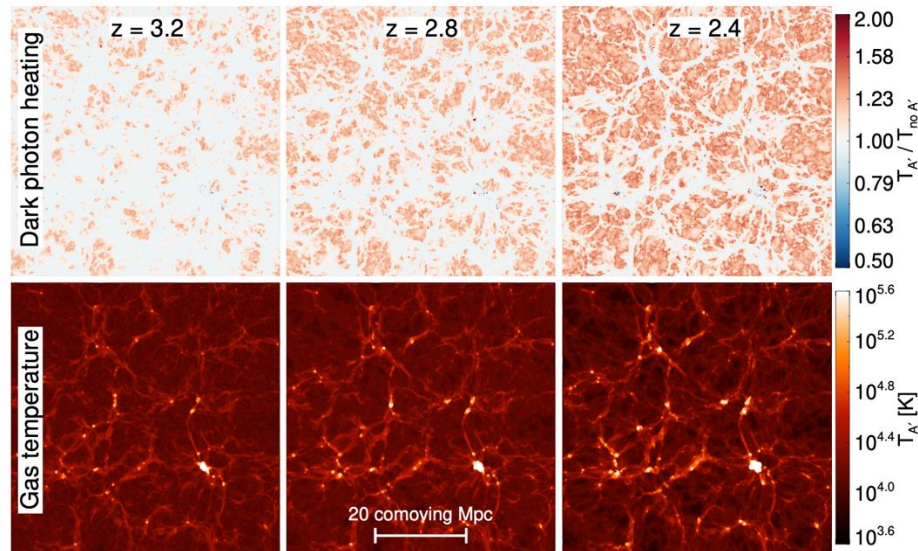


McDermott & Witte 20

The IGM as a thermometer - II

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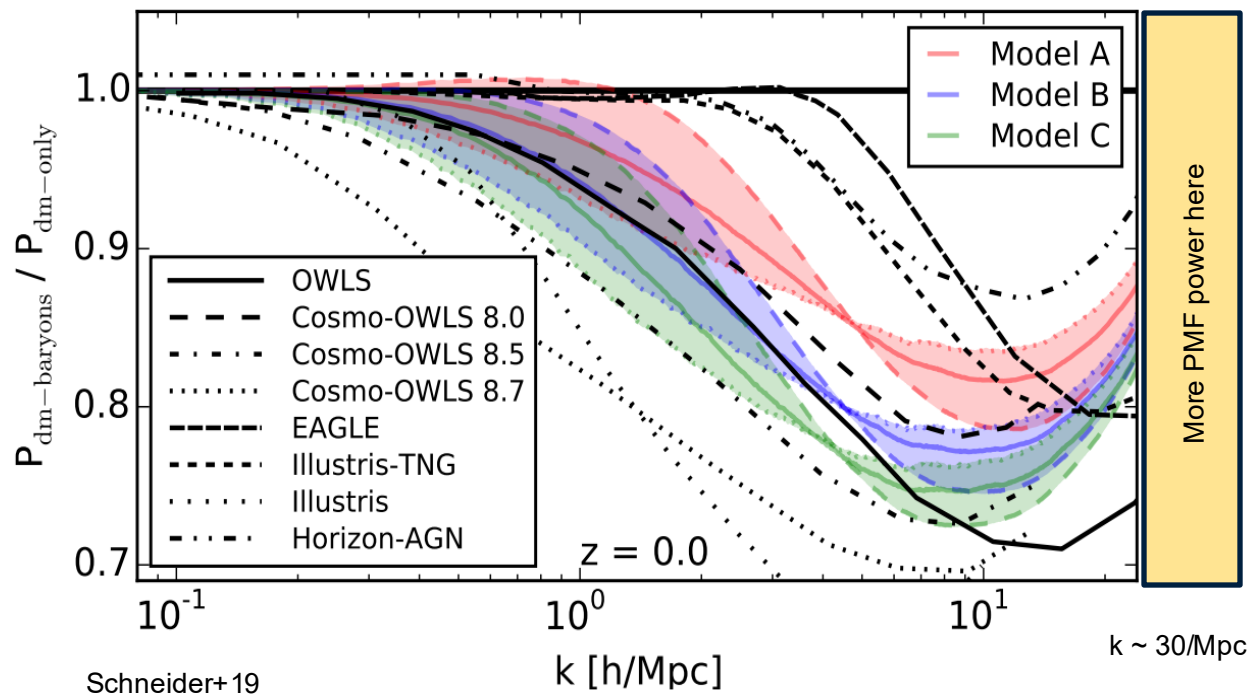
Distinctive heating mechanism happening far away from complex astrophysics



- ✓ PMFs can enhance baryon fraction apart from enhancing matter power spectrum
- ✓ Can affect **star formation/important for JWST**
- ✓ Observing **high baryon fraction** at high redshift will be smoking gun signal for PMFs
- ✓ **Ly α forest ideal probe** of PMFs, since it samples low density environments far from galaxies
- ✓ Constraints from Ly α forest point to a **detection at 0.2 nG** or more conservatively a tight 3σ **upper limit of 0.3 nG**

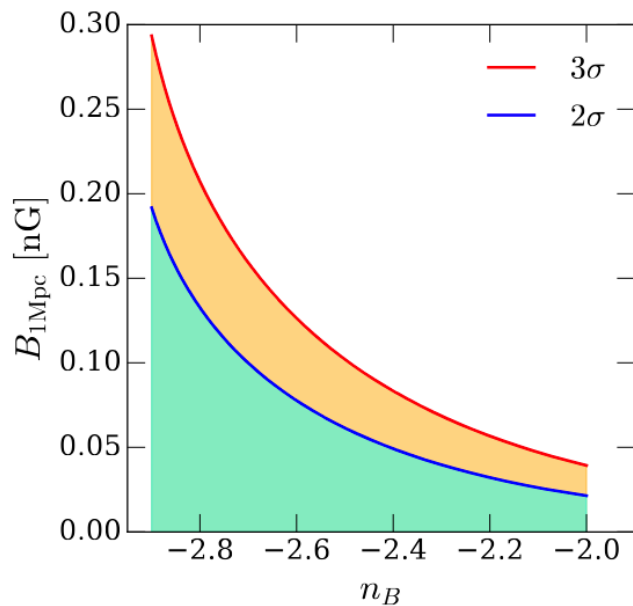
PMFs: interplay with baryonic corrections

Matteo Viel

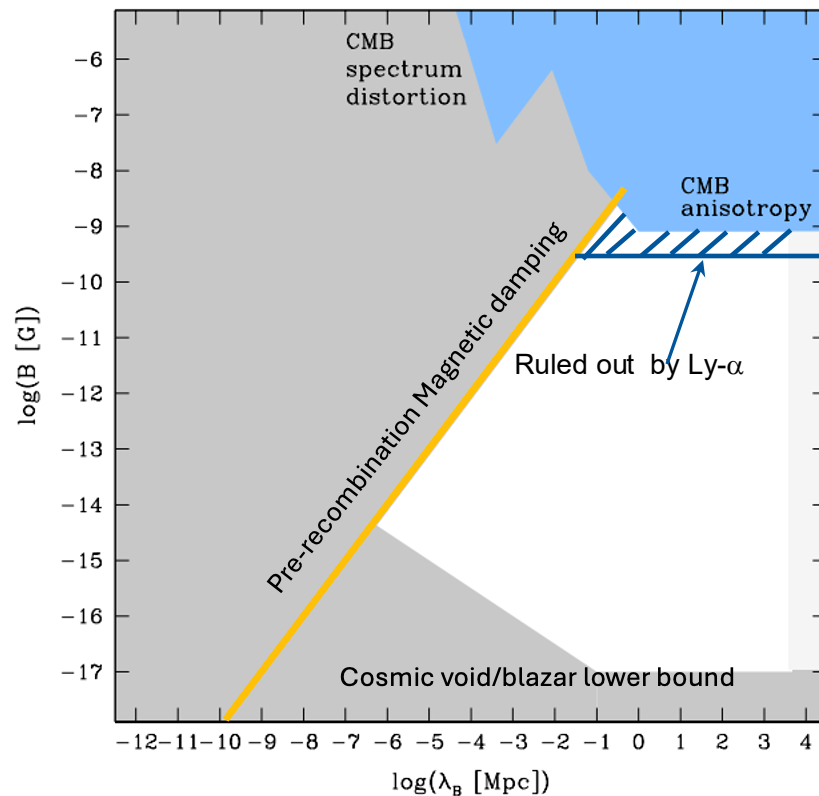


Constraints on peak position

Matteo Viel

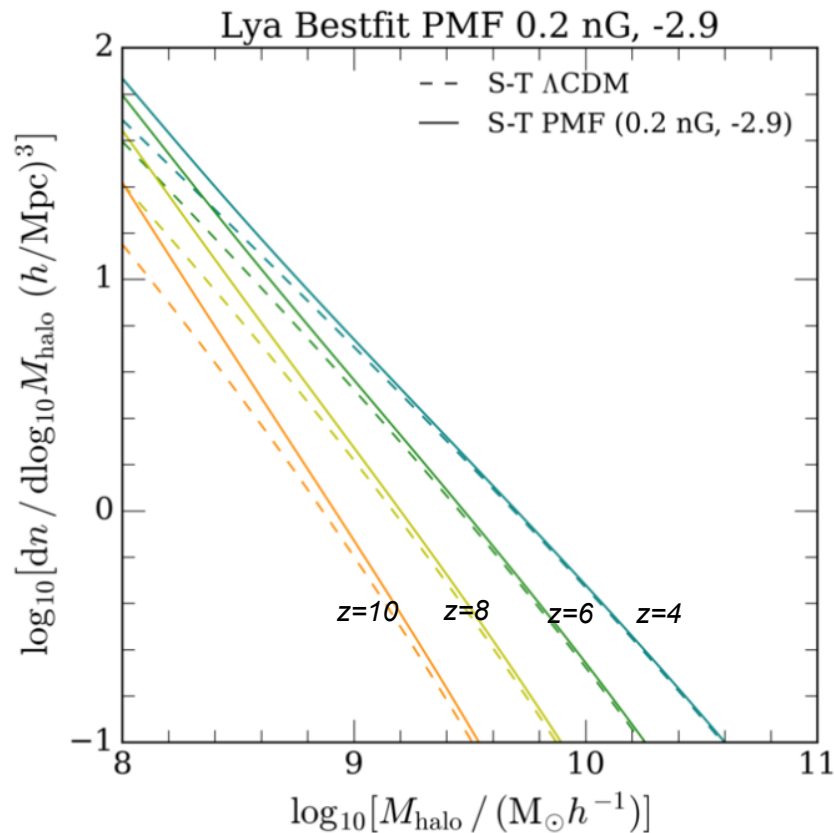


Extending to other n_B values

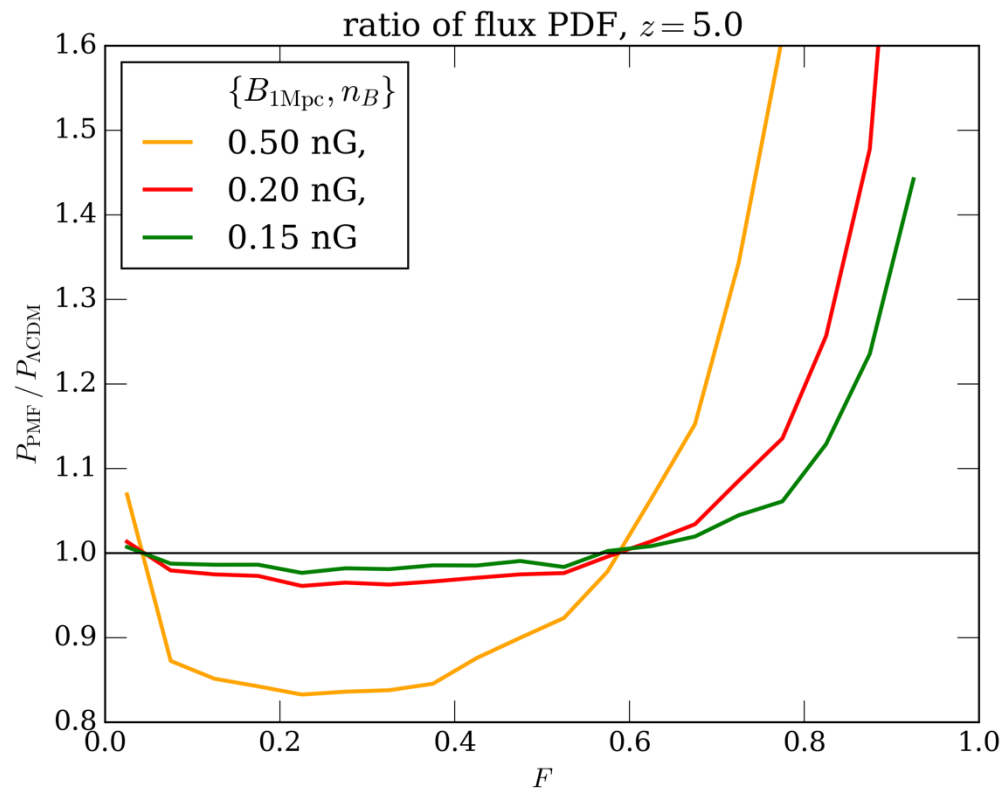


Implications for the detection

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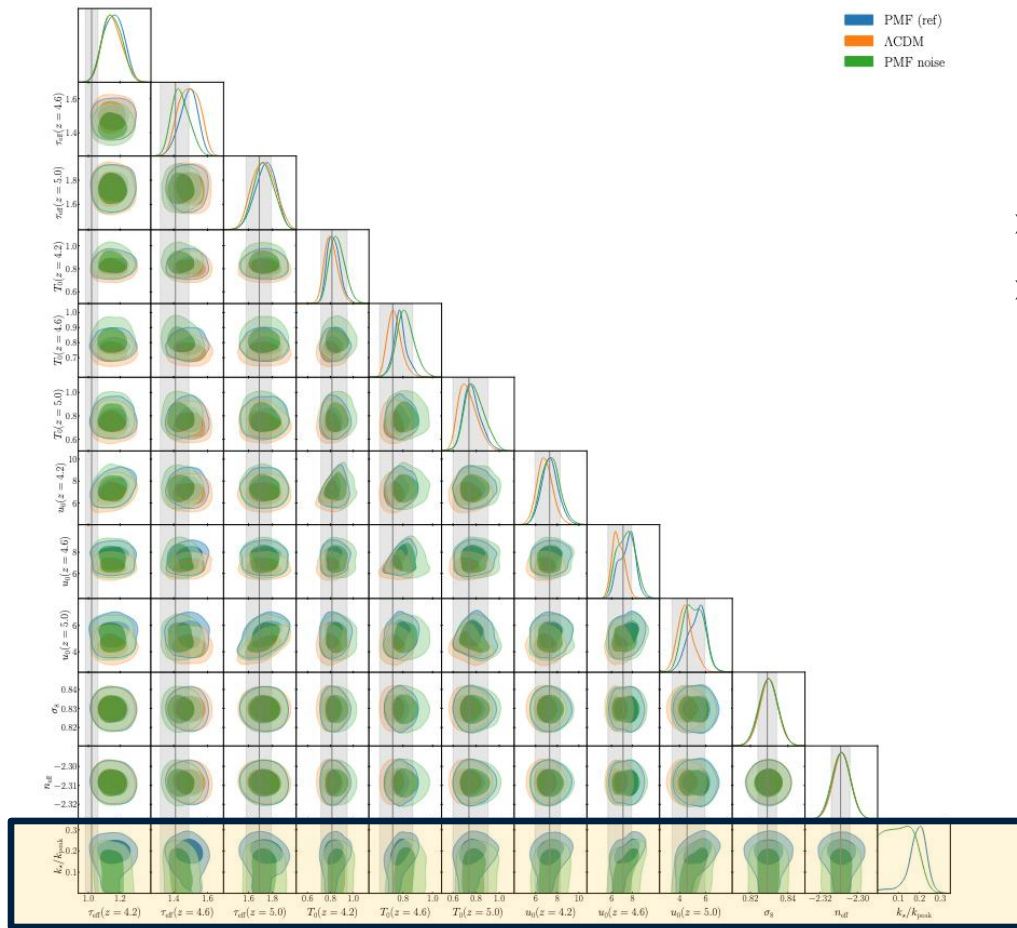


- MF is boosted at $M_{\text{halo}} < 10^9 M_{\odot}/h$
- ~2 more $10^8 M_{\odot}/h$ haloes at $z=10$ expected compared to Λ CDM



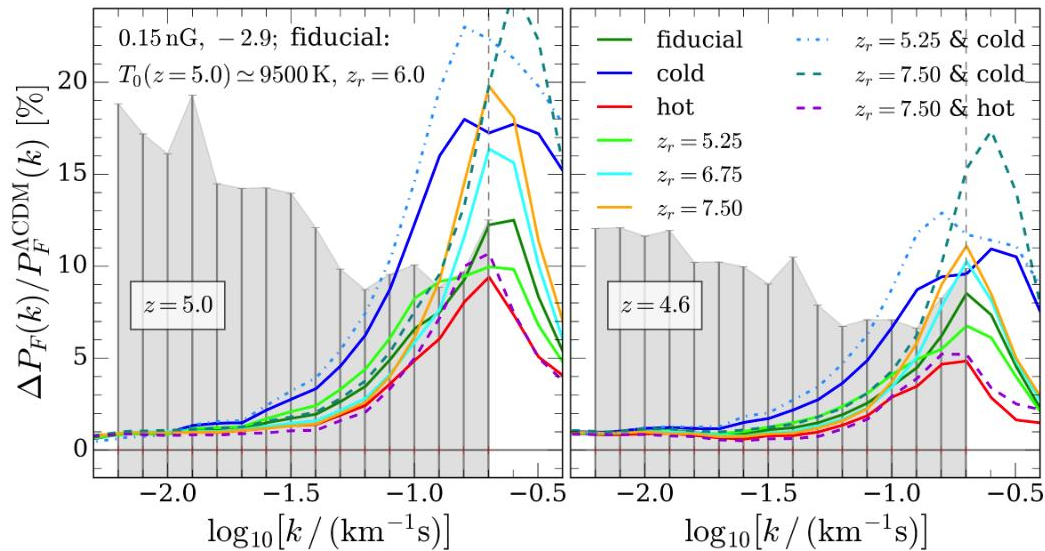
Extra slides: triangle plot

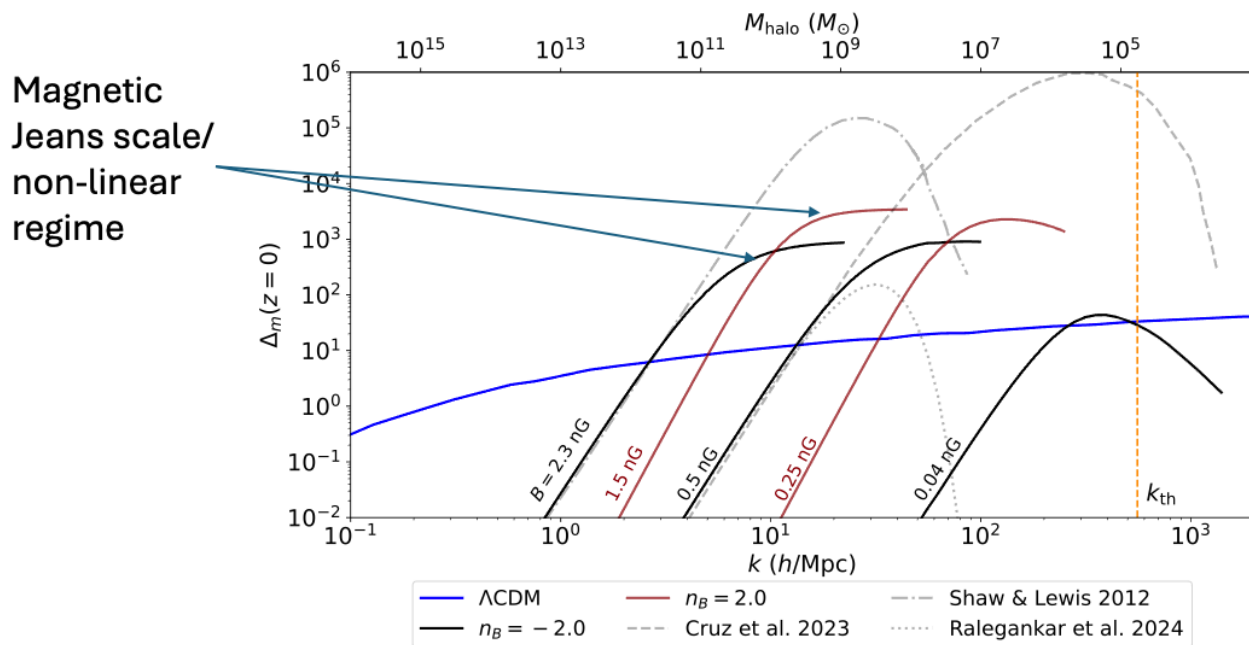
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- Not strong degeneracies present
- Weak degeneracies with injected heat and noise modelling

Extra slides: PMFs vs thermal parameters

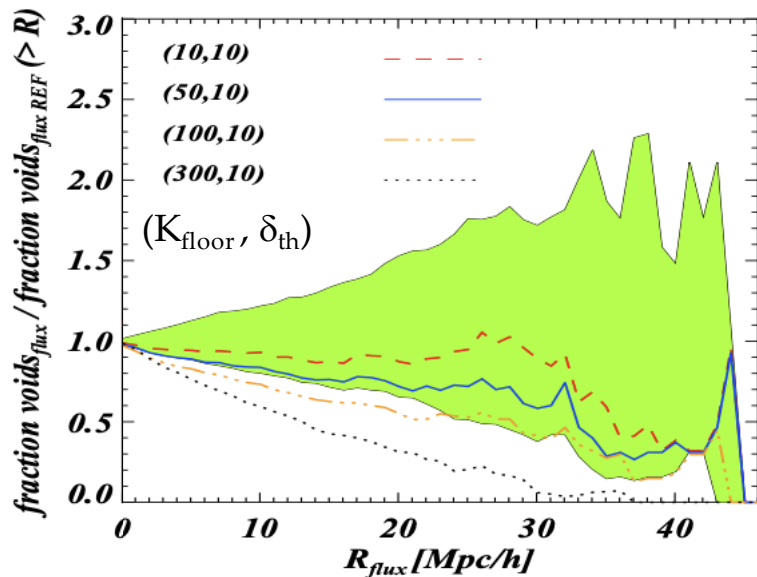




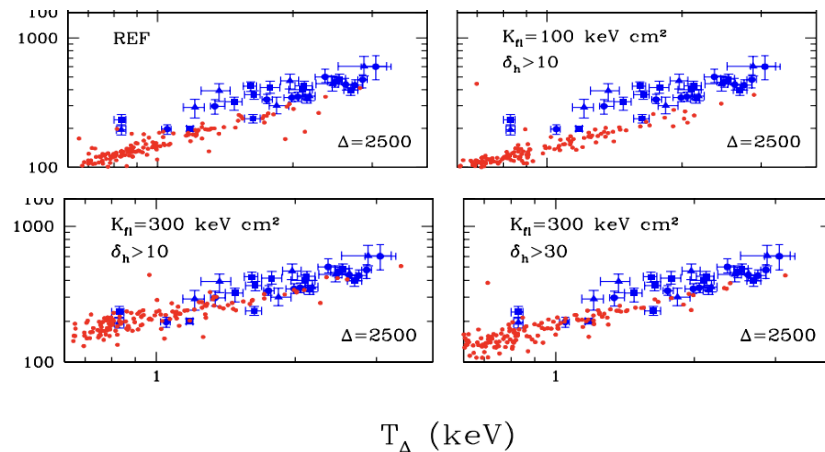
Connection to low z: entropy-temperature relation of groups

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Forest Voids' statistics at $z=2$



CHANDRA entropy-temperature profiles

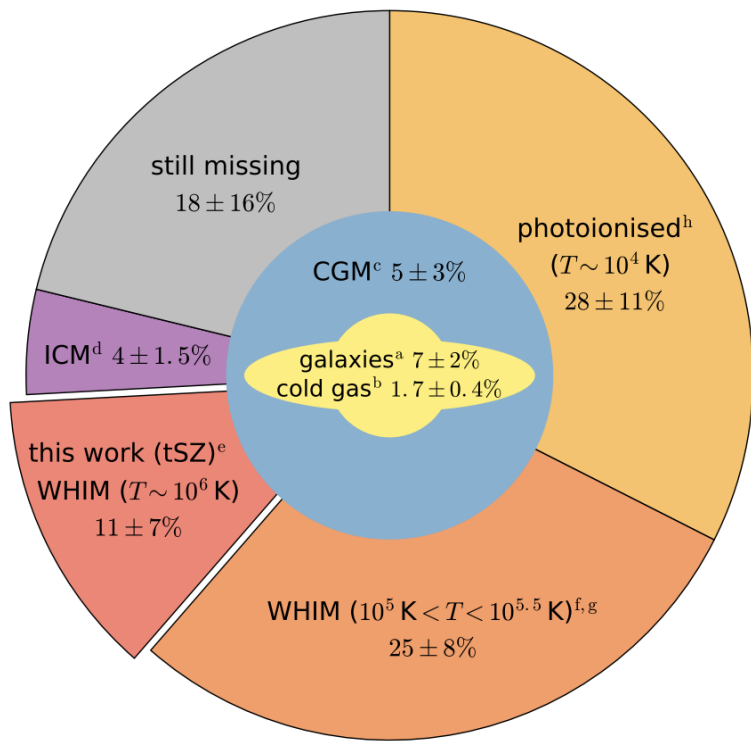


Pre-heating: gas at $z=4$ with $\delta > \delta_{\text{th}}$ and $K < K_{\text{floor}}$

Must occur at $\delta > 10-30$ and/or at $z < 1$

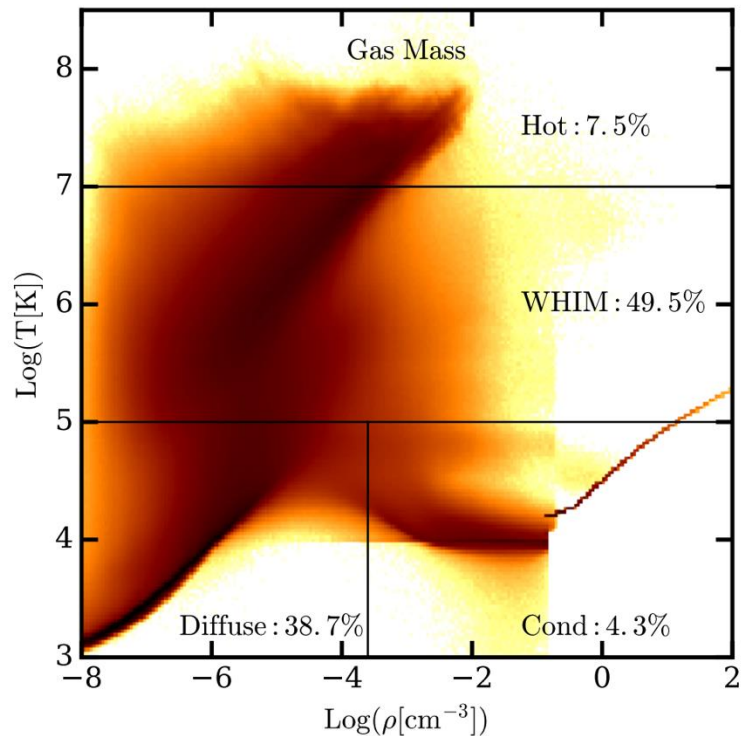
Connection to low z: census of the baryons at z=0

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De Graaf et al. 2019

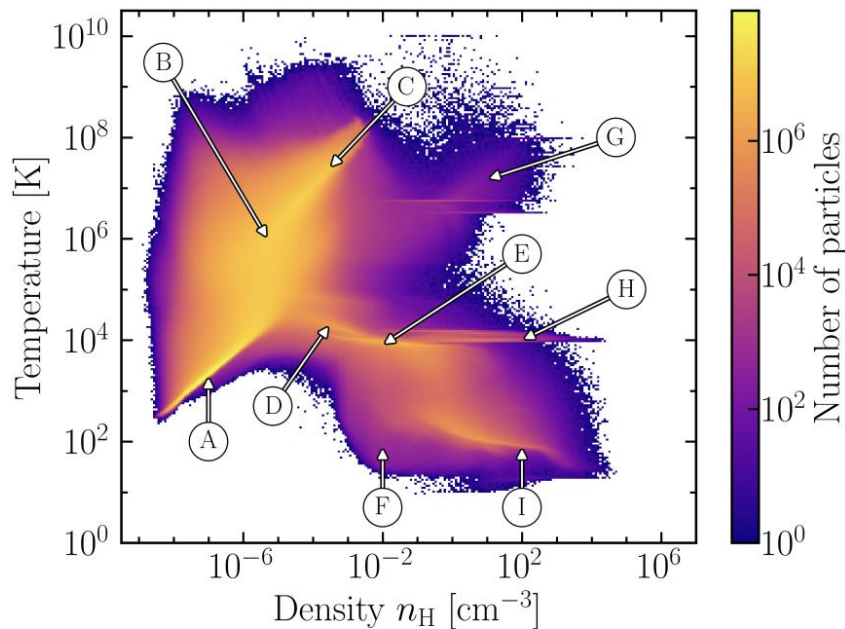
Parimbelli, Branchini, MV, Villaescusa-Navarro, ZuHone 2023



Torrey+19 [IllustrisTNG]

Connection to low- z : The physics of the T - ρ relation ($z=0$)

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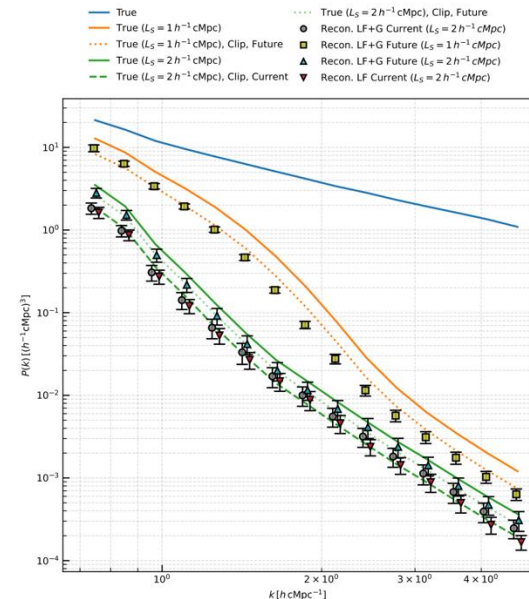
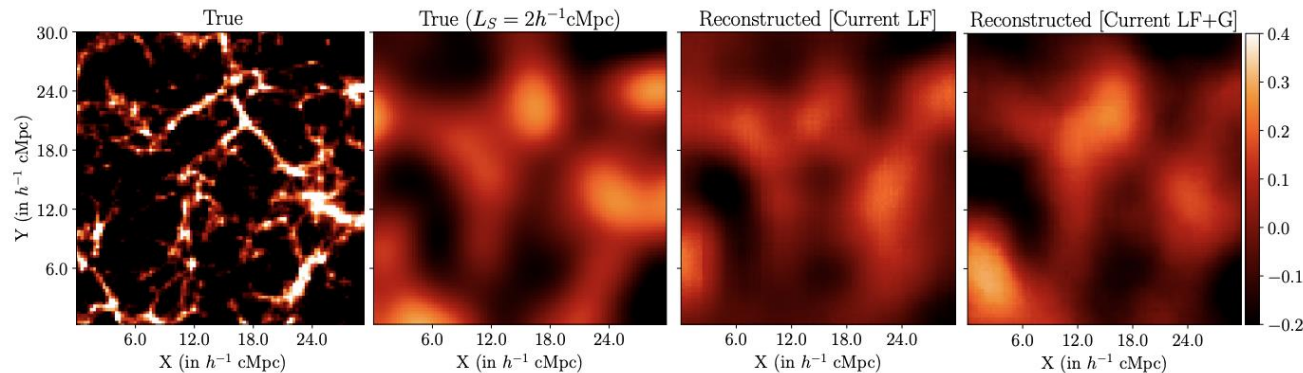
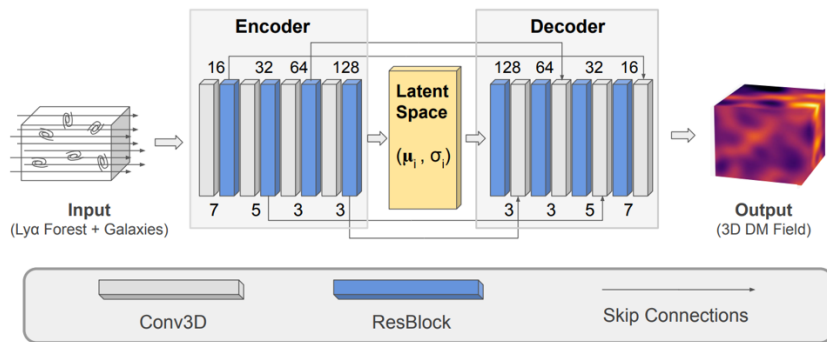
Impressive dynamical range

- ✓ A: diffuse IGM
- ✓ B: WHIM and CGM
- ✓ C: ICM
- ✓ D: cool CGM
- ✓ E: thermal equilibrium of low Z gas
- ✓ F: cold ISM
- ✓ G: hot ISM (from feedback)
- ✓ H: HII ionized regions
- ✓ I: very cold ISM

Schaye+25 COLIBRE simulations

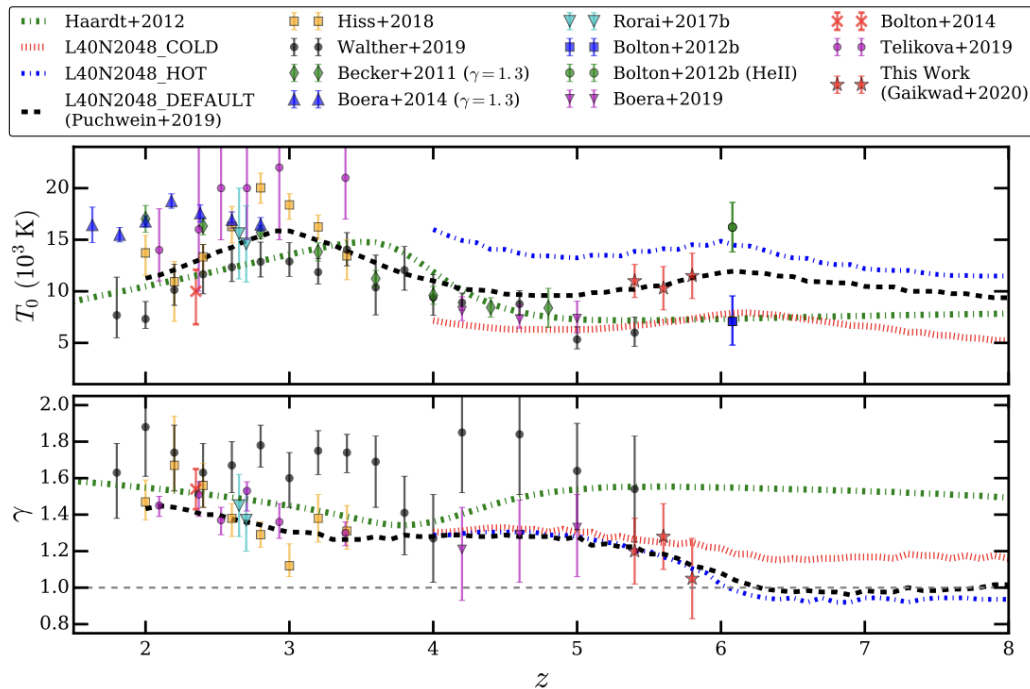
Reconstructing the 3D DM cosmic web with ML

Matteo Viel



Physics of the gas: the gas thermal state

Matteo Viel

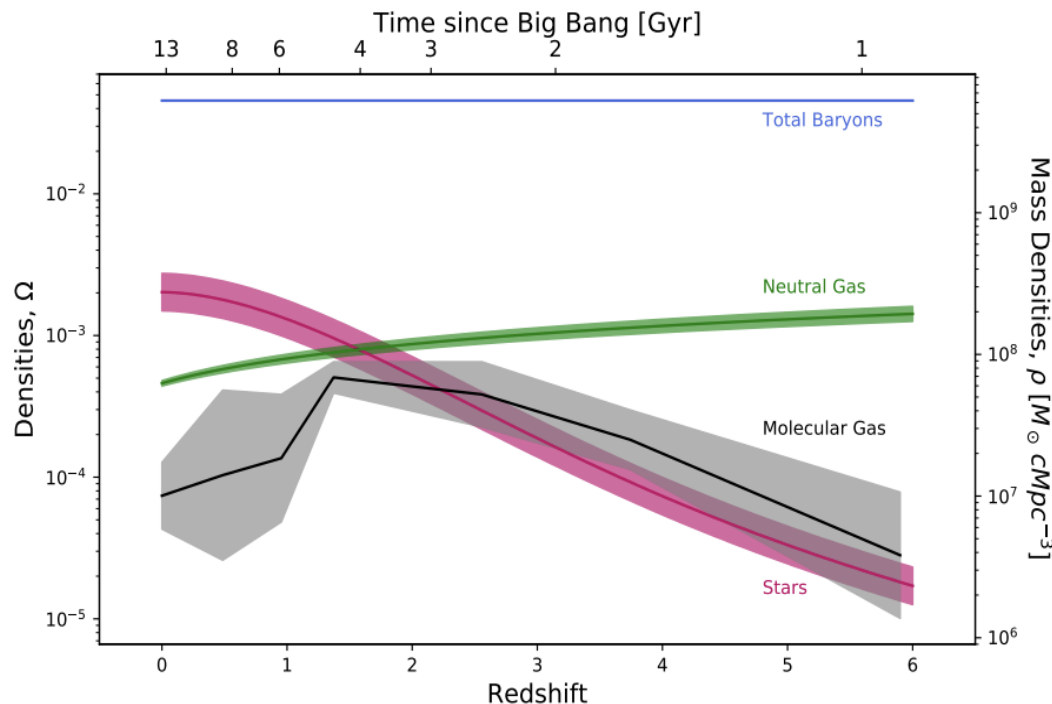


Gaikwad+20

- ✓ Temperature density relation can indeed be measured by using a variety of methods like wavelets, pdf of the gas, power spectrum, bispectrum, Voigt profile fitting.
- ✓ HeII bump quite “prominent”

Evolution of the condensed phases

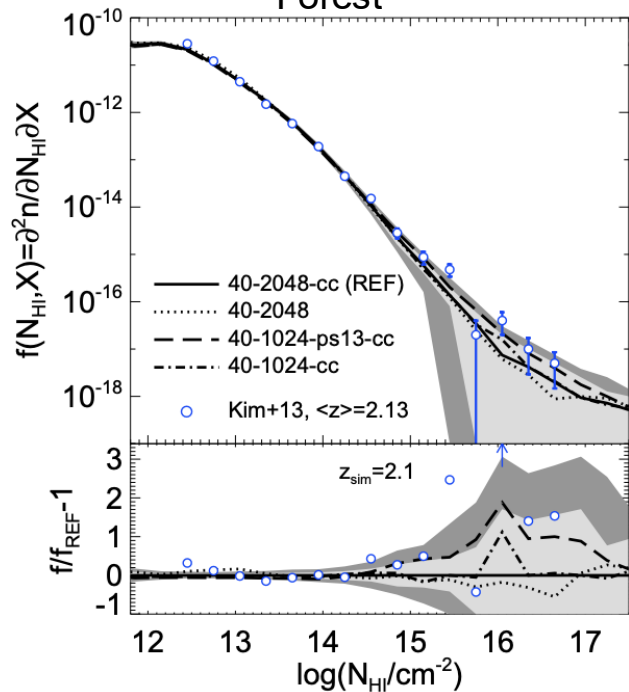
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- ✓ Molecular gas traces star formation rate
- ✓ Neutral gas always dominating the budget at $z > 2$ and always above the molecular
- ✓ Total budget is subdominant compared to total baryons

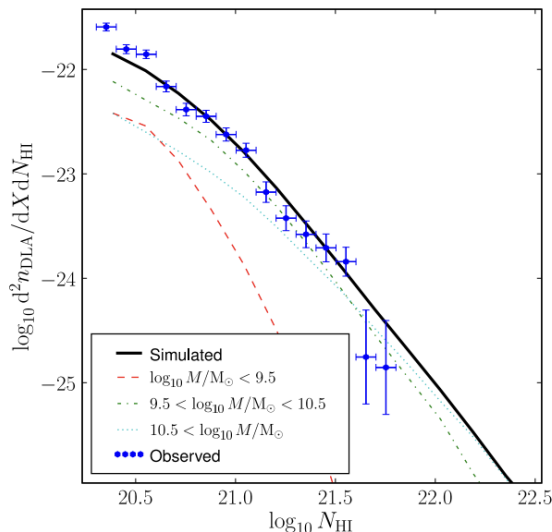
Peroux & Howk 2021

Forest



Bolton+17

Damped systems

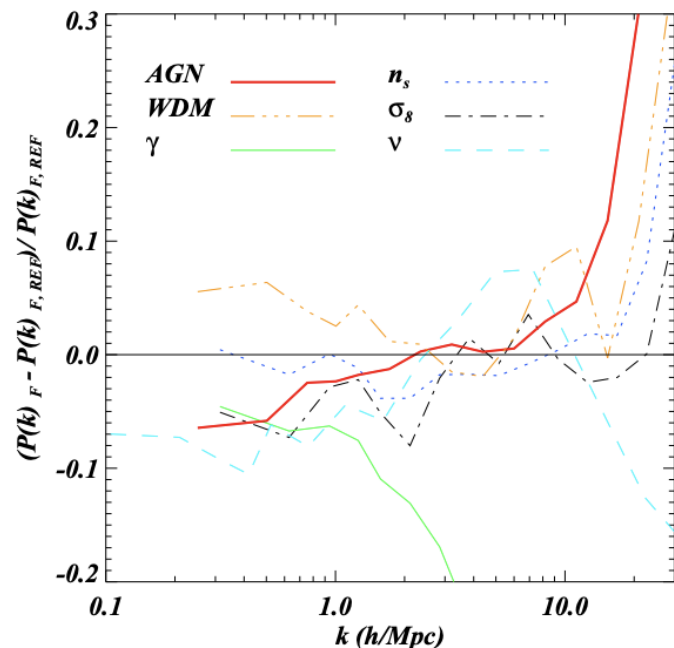


Pontzen+09

- ✓ Fitting with Voigt profile allows to extract the HI column density
- ✓ Good agreement over about 10 orders of magnitude, spanning very underdense gas up to Damped systems (galaxies)
- ✓ Smaller scales are more complex and rich in physics (feedback, AGN, star formation, molecules, dust, metals)

Feedback and Lyman- α forest

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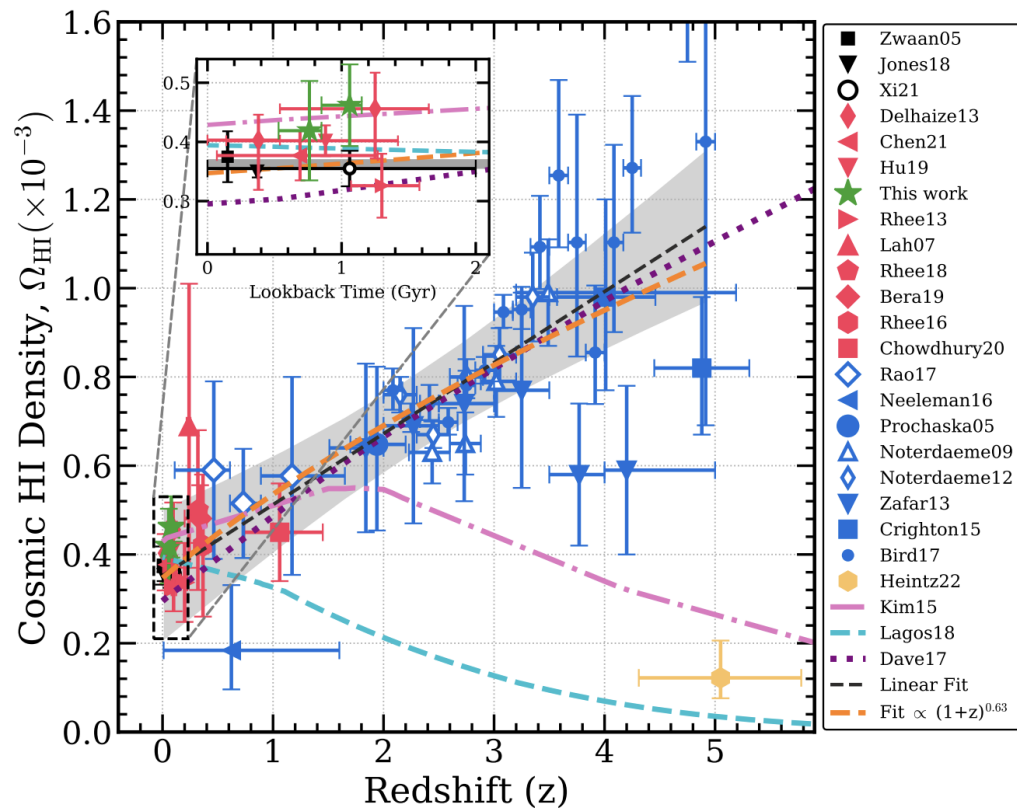


- ✓ Impact of AGN feedback at low z ($z \sim 2$) is of the same order of the cosmo params
- ✓ These effects can only partially be captured by changes in the Temp. density relation of photo-ionized gas
- ✓ Especially for AGN, changes in the density distribution and in the fraction of hot, collisionally ionised gas ($T > 10^5 K$)

Viel, Schaye & Booth 2012
Chabanier+2025

HI evolution with redshift

Matteo Viel



Peroux & Nelson 2024

- ✓ Evolution of HI mass density is relatively mild compared to other physical quantities like SFR
- ✓ This quantity is dominated by DLAs and is important when 21cm intensity mapping models are built