

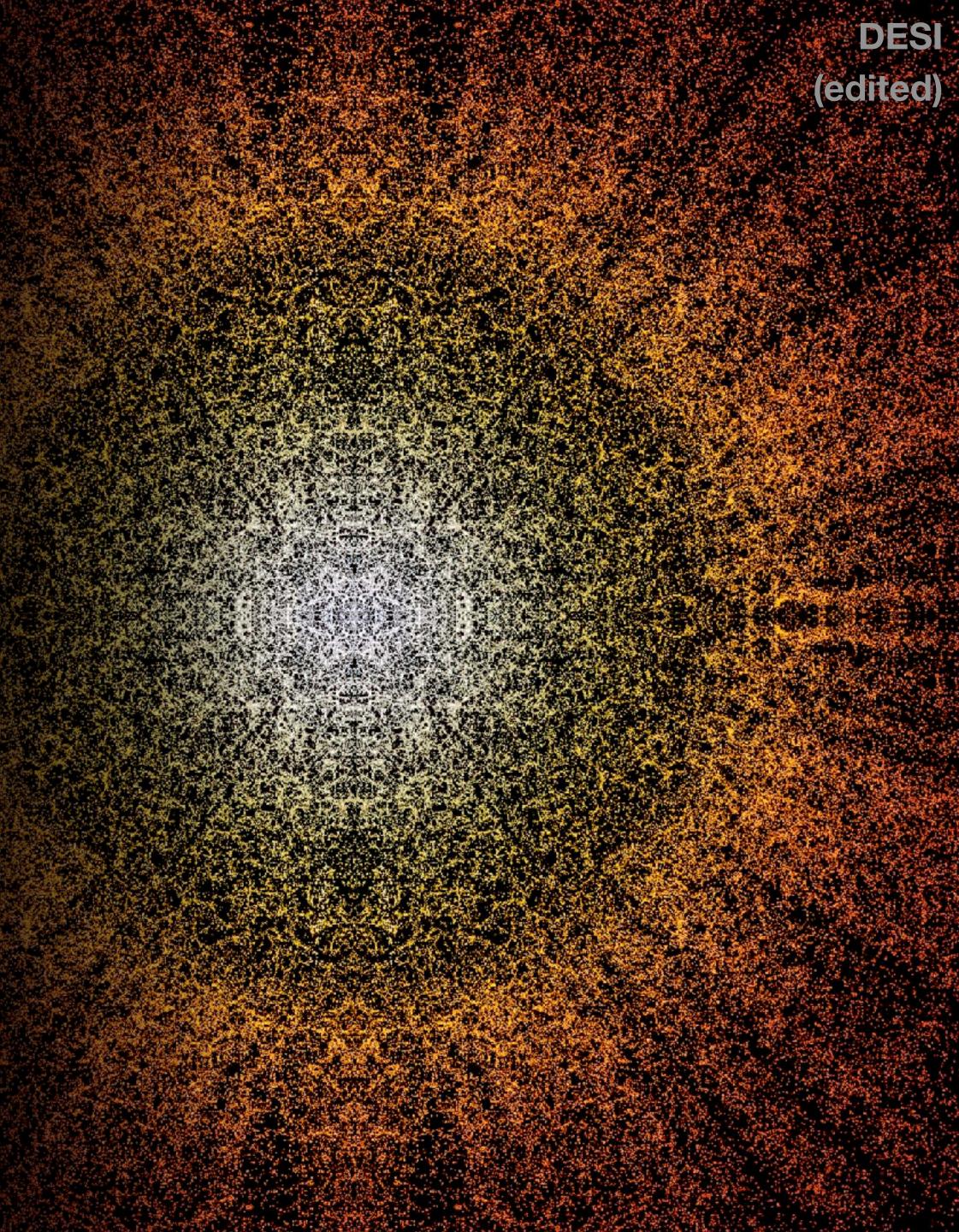
# INFLATION

What have we learnt?

What can we learn?

Why should we care?

Oliver H. E. Philcox



### What do we want to know about inflation?

#### Simplest (phenomenological) model

- A single field,  $\phi$  evolving along an almost flat potential
- Curvature is sourced by **quantum fluctuations** in  $\delta\phi$

$$\mathcal{L} \sim \frac{1}{2} (\partial \phi)^2 - V(\phi)$$

#### **HOWEVER:**

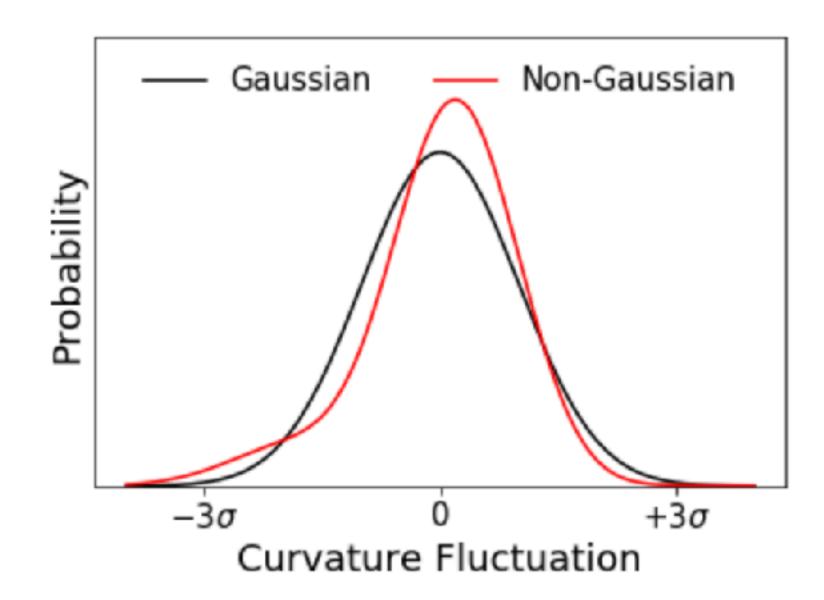
• What sets the potential? \_\_\_\_\_\_ 
$$V(\phi)=???$$

• Were there other fields during inflation? — 
$$\phi o \phi, \chi, \psi_u, \cdots$$

### How do we learn about inflation?

Vanilla inflation leads to Gaussian fluctuations in the primordial curvature perturbations,  $\zeta$ 

New physics in the early Universe gives non-Gaussian curvature fluctuations



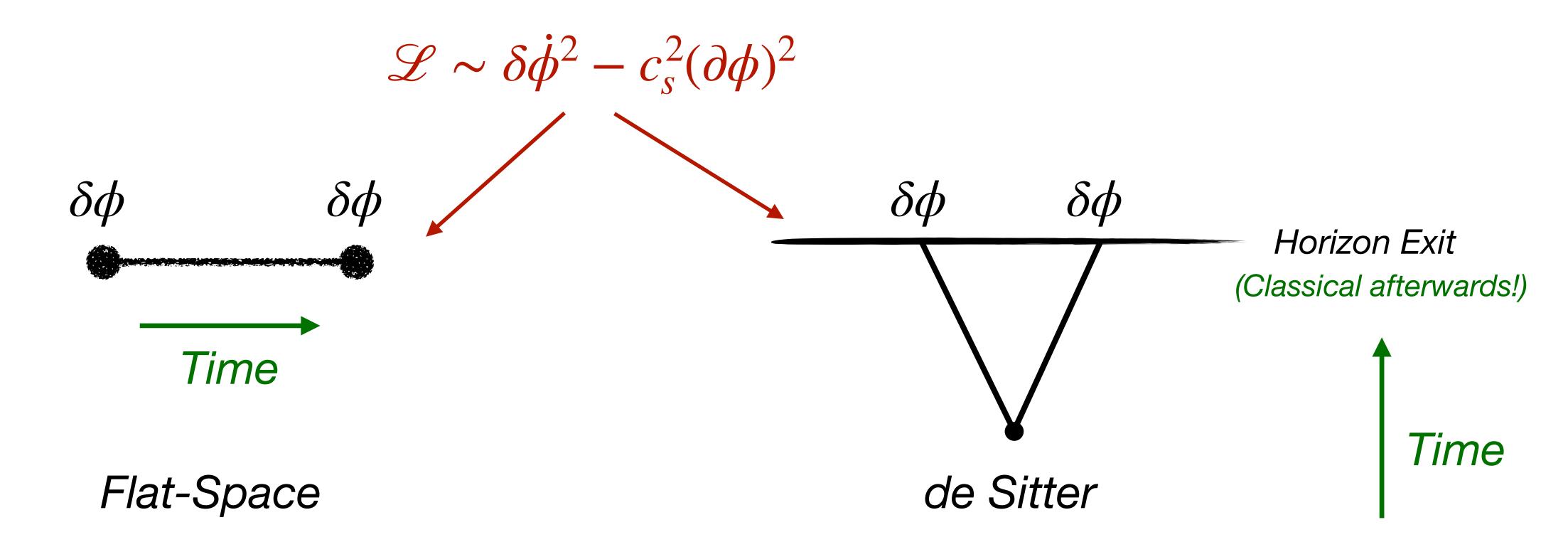
START: Quantum Fluctuations in  $\phi$ Gaussian Non-Gaussian

By searching for non-Gaussianity, we can constrain inflationary physics!

END: Classical Fluctuations in  $\zeta$ 

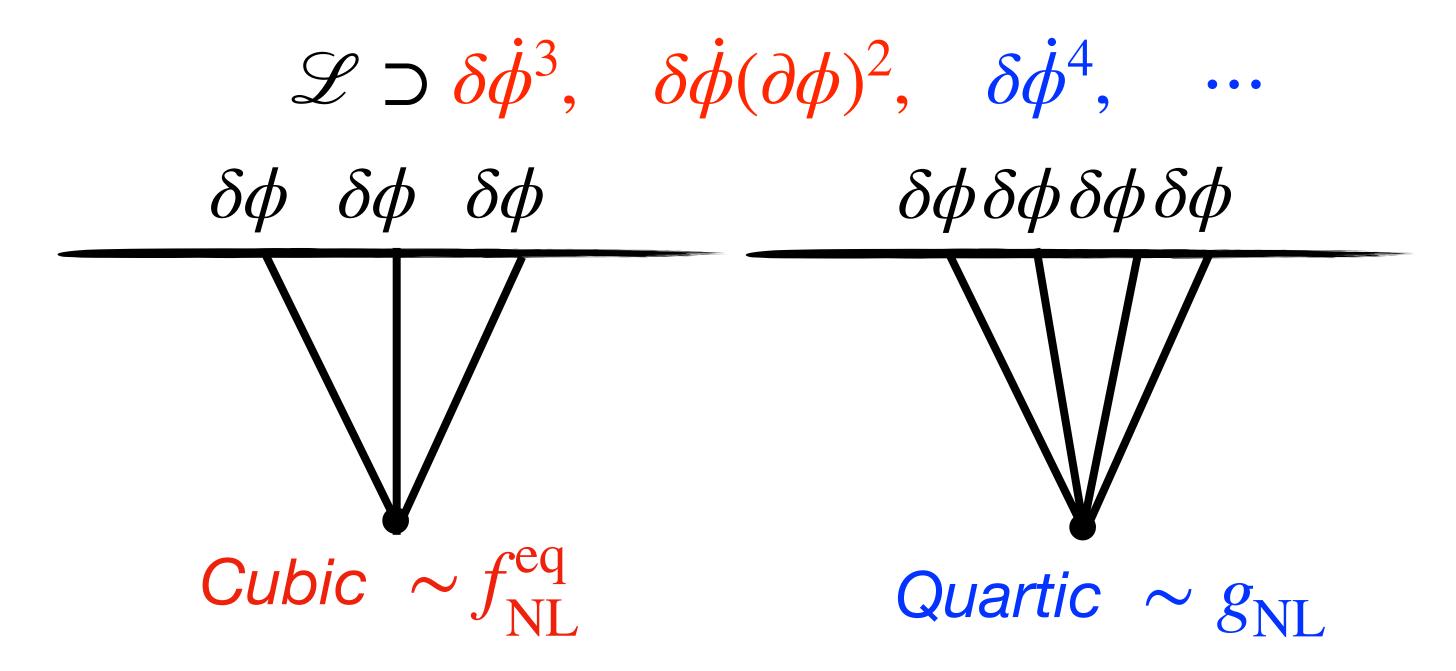
### Two-Point Functions

- Let's assume we have just a **single field**  $\phi$  in inflation (the "inflaton")
- The simplest inflationary action is quadratic in perturbations:



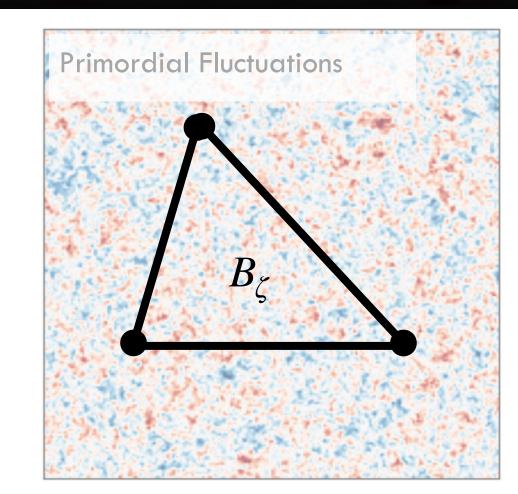
### Self-Interactions

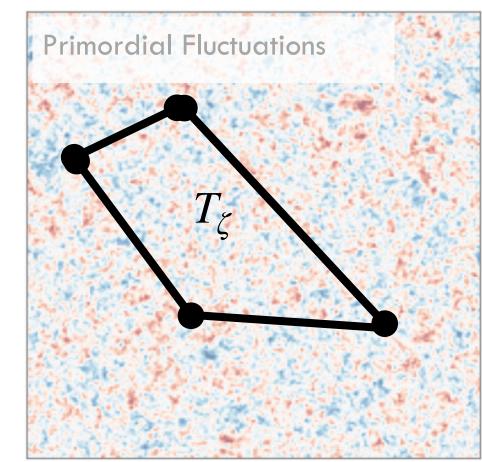
• Many models of inflation feature self-interactions:



- This leads to three- and four-point functions at the end of inflation
- The shape encodes the vertex, the amplitude encodes the microphysics

e.g. 
$$\langle \zeta(\mathbf{k}_1)\zeta(\mathbf{k}_2)\zeta(\mathbf{k}_3)\rangle \sim f_{\mathrm{NL}}^{\mathrm{eq}} \times \mathrm{shape}$$

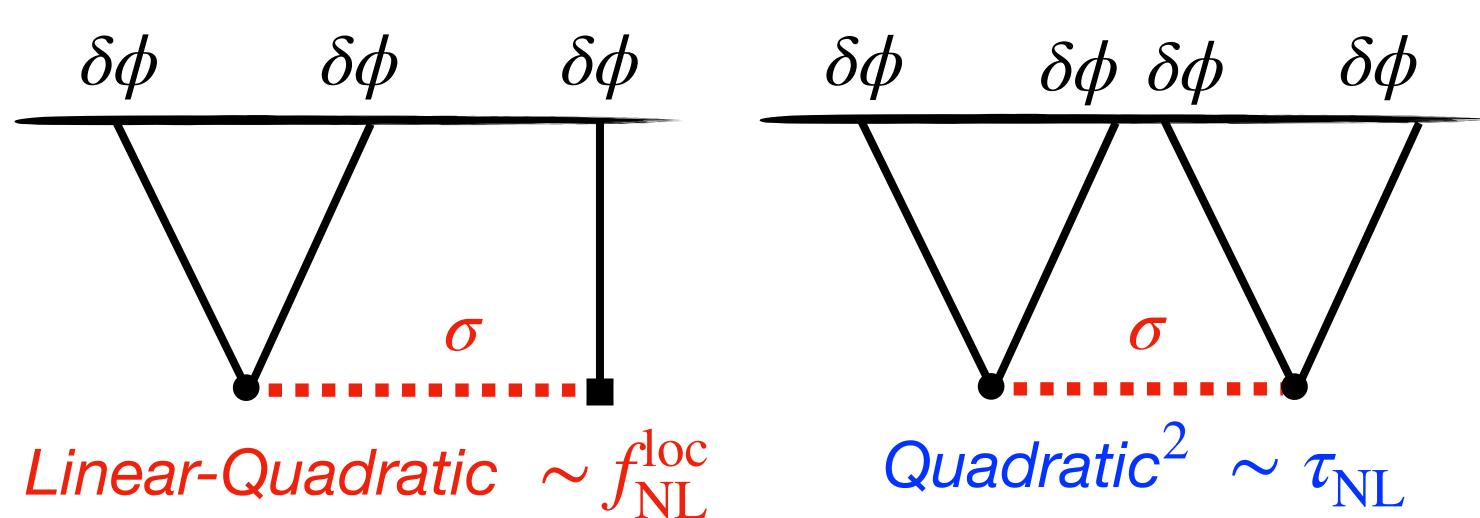




### Self-Interactions

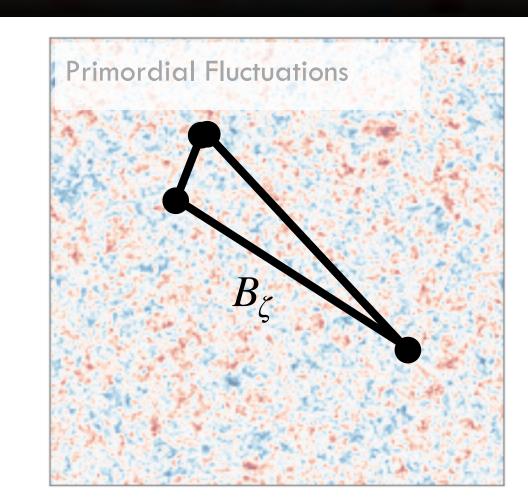
• Other models feature **new particles**,  $\sigma$ :

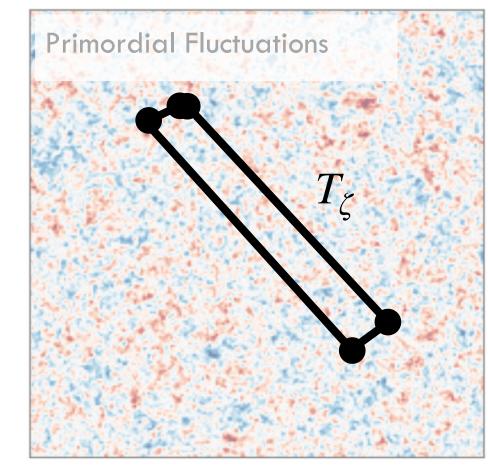
$$\mathcal{L} \supset \delta \dot{\phi} \sigma, \quad \delta \dot{\phi}^2 \sigma, \quad \cdots$$



- This leads to three- and four-point functions at the end of inflation
- The **shape** encodes the vertex, the **amplitude** encodes the microphysics

e.g. 
$$\langle \zeta(\mathbf{k}_1)\zeta(\mathbf{k}_2)\zeta(\mathbf{k}_3)\rangle \sim f_{\rm NL}^{\rm loc} \times {\rm shape}$$





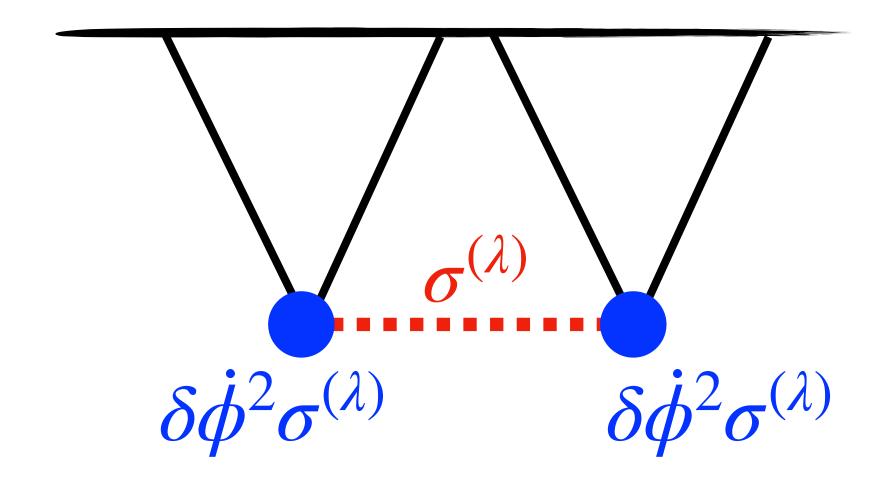
## The Cosmological Collider

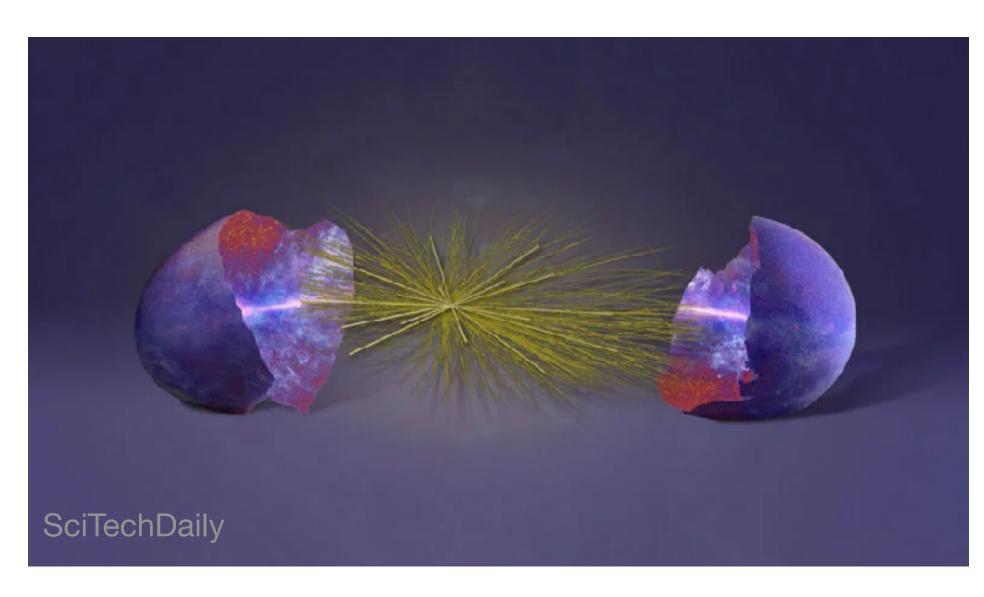
- The four-point function tracks the **exchange** of a particle  $\sigma_{\mu_1\cdots\mu_s}$  of mass  $m_\sigma\sim H$  and spin  $s=0,1,2,\cdots$
- This depends on the power spectrum of  $\sigma$ , including all its helicity states,  $\sigma^{(\lambda)}$

$$\langle \zeta(\mathbf{k}_1)\zeta(\mathbf{k}_2)\zeta(\mathbf{k}_3)\zeta(\mathbf{k}_4)\rangle \sim \sum_{\lambda} P_{\zeta}(k_1)P_{\zeta}(k_3)P_{\sigma^{(\lambda)}}(K) \times \text{coupling}$$

- In the collapsed limit (low exchange momentum), the inflationary signatures are set by symmetry
- They depend only on mass and spin (and the speed) not on the microphysical model!

By studying the trispectrum we can probe new particles present during inflation!





## The Cosmological Collider

 The three-point function also probes particleexchange
 See Sam's talk!

$$B_{\zeta}(k_1, k_2, k_3) \sim P_{\zeta}(k_1) P_{\sigma^{(0)}}(k_3) \times \text{coupling}$$

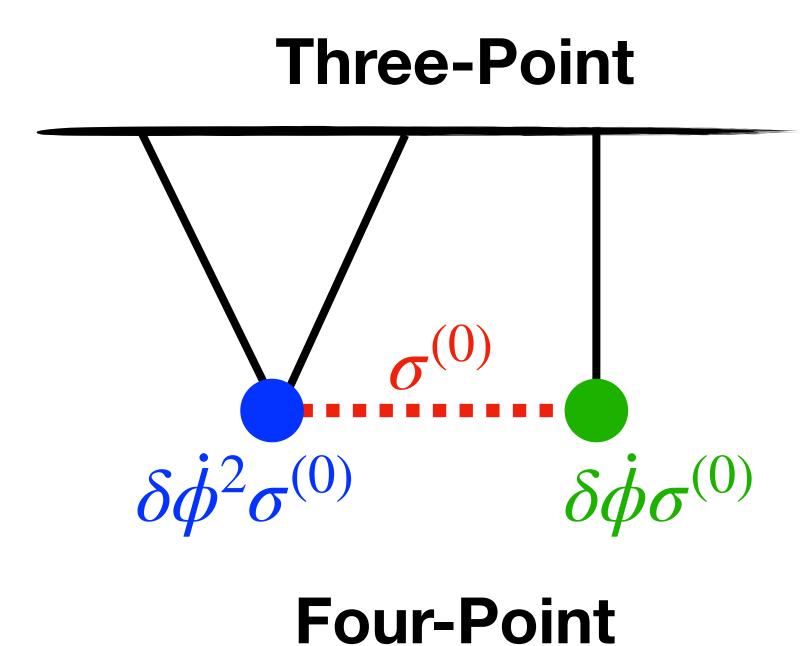
- However,
  - It requires a quadratic coupling

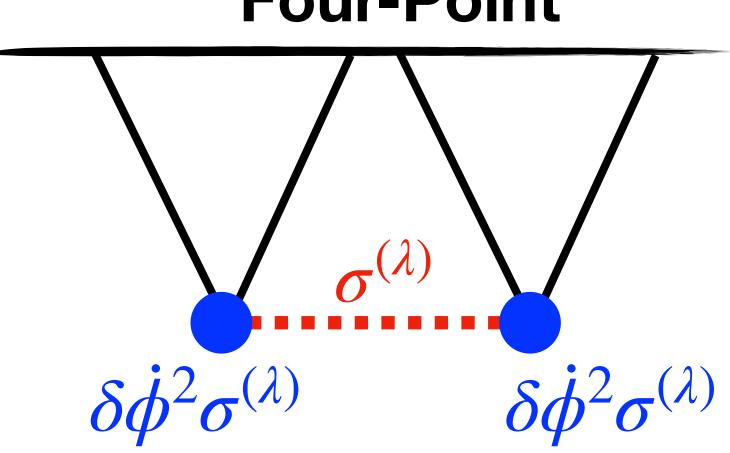
(which could be slow-roll suppressed)

• It only probes the longitudinal mode,  $\sigma^{(0)}$ 

(which could be subdominant)

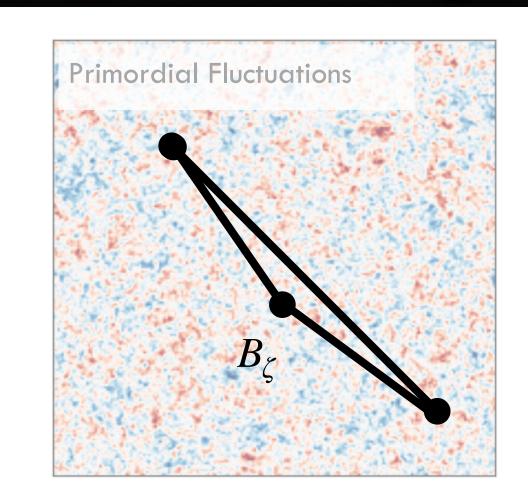
 We need the four-point function to fully probe collider physics!

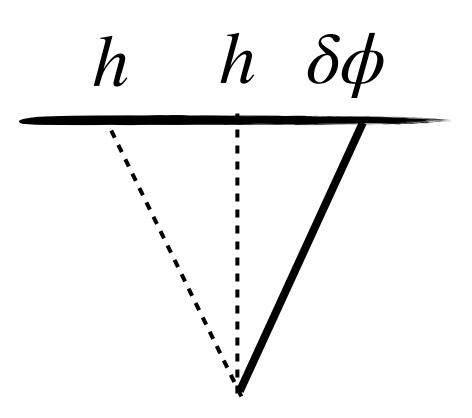




## Other Inflationary Effects

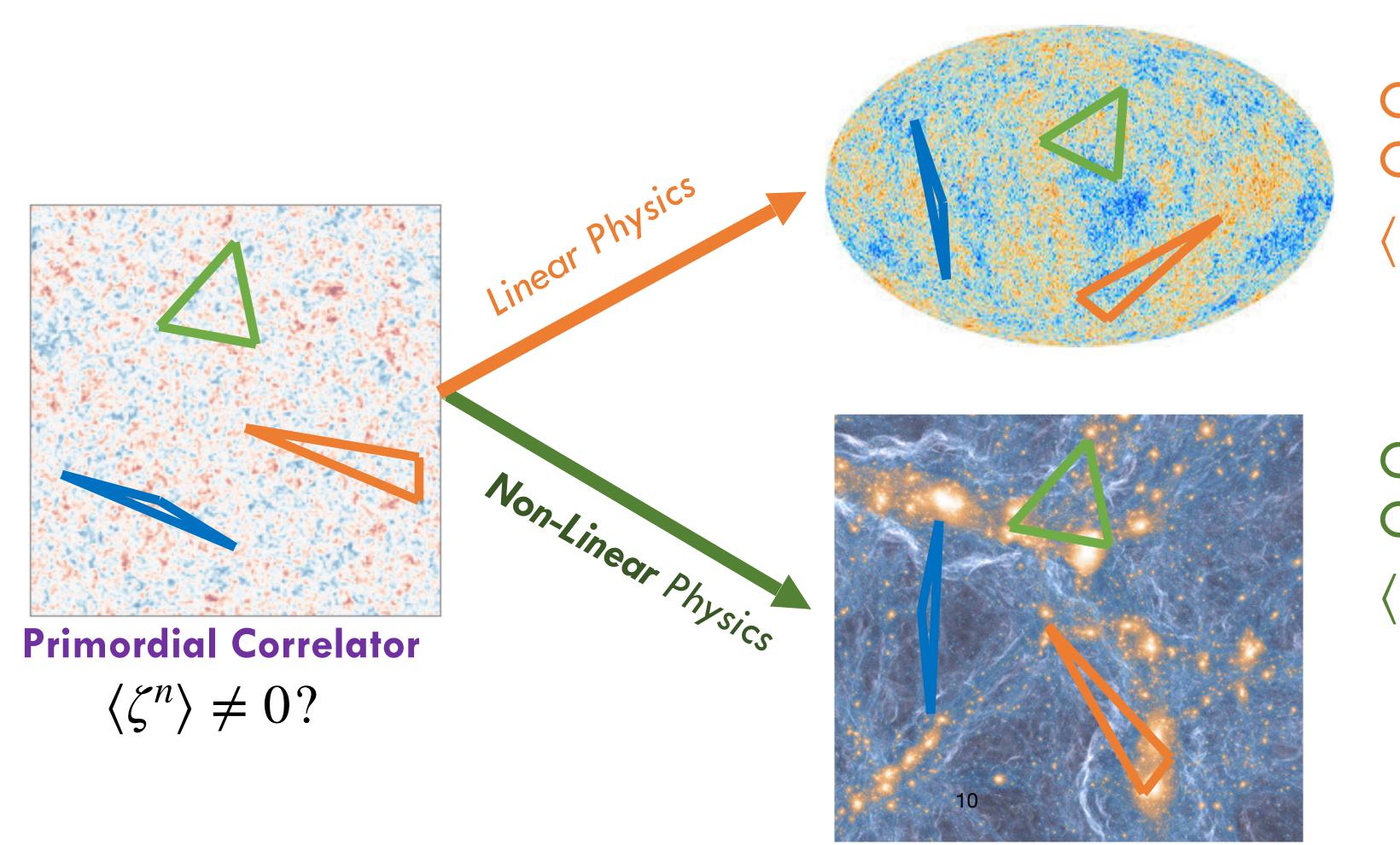
- Folded non-Gaussianity?
  - Dissipative effects in inflation
  - Modified initial conditions
- Oscillatory effects and non-perturbativity?
  - Resonances, axions
  - Very massive particles
- Tensor non-Gaussianity?
  - Modified gravity, gauge fields, massive gravity, magnetic fields...





 $\langle h\zeta\zeta\rangle, \langle hh\zeta\rangle, \langle hhh\rangle \neq 0$ ?

### How to Measure Primordial Non-Gaussianity



Cosmic Microwave Background Correlator

 $\langle \delta T^n \rangle \neq 0$ ?

Galaxy Distribution
Correlator

$$\langle \delta \rho_{\text{galaxy}}^n \rangle \neq 0$$
?

## CMB Constraints (Easyish)

• Planck placed strong constraints on scalar three-point functions

Planck 2018 Local . . . . . . . . 
$$-0.9 \pm 5.1$$
 Equilateral . . . . .  $-26 \pm 47$  Orthogonal . . . . .  $-38 \pm 24$ 

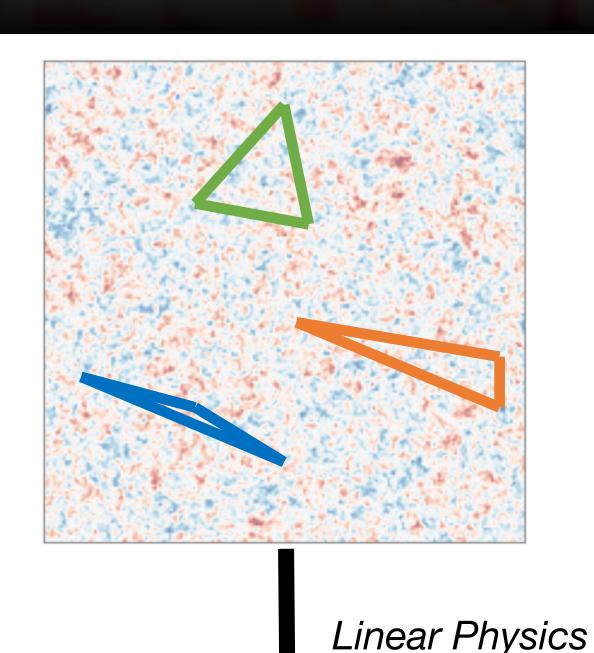
- These span many phenomenological templates
- Recent work by Wuhyun Sohn++ group probed cosmological collider bispectra

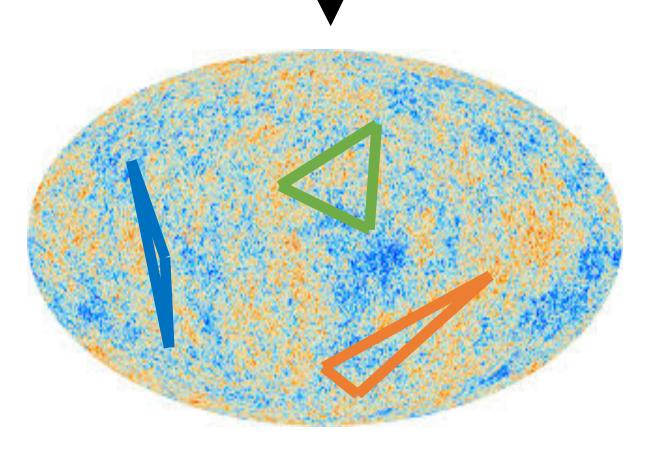
Conclusion: Scalar primordial non-Gaussianity is small!

$$10^{-5} |f_{\rm NL}| \ll 1$$

However, we are still far from the (vaguely defined) theory limits

$$\sigma(f_{\rm NL}) \sim 1$$





## CMB Constraints (Hardish)

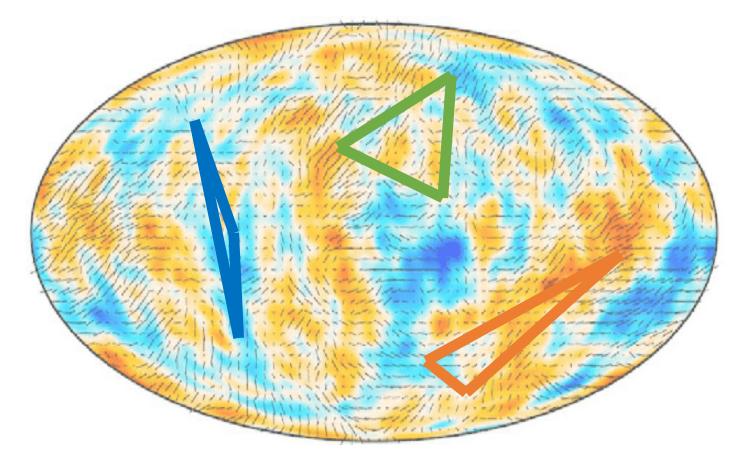
• Planck can also constrain tensor three-point functions

e.g., 
$$\langle TTB \rangle \sim \langle \zeta \zeta (h_{+} - h_{\times}) \rangle$$

- Recent work has constrained several gravitational wave templates:
  - Weyl gravity, squeezed bispectra, massive gravity, gauge fields, ...
- This uses binned bispectrum estimators (not very optimal)
- The signals are mostly on large scales due to tensor transferfunctions
- This is limited by lensing and B-mode noise, not cosmic variance

Conclusion: Tensor primordial non-Gaussianity is small!

$$10^{-5} |f_{\rm NL}^{\rm tens}| \ll 1$$



Model		Planck		
		Т	T+E	T+E+B
Tensor-Tensor-Tensor				
Squeezed	$(\times 10^{-1})$	$51 \pm 32$	$-4 \pm 13$	$7\pm 9$
Equilateral	$(\times 10^{-2})$	$-5 \pm 13$	$-3 \pm 5$	$-0\pm3$
$W^3 \left( n_{ m NL} = +1  ight)$	$(\times 10^{-3})$	$-63 \pm 34$	$-7\pm7$	$8\pm4$
$W^3 \left( n_{ m NL} = 0  ight)$	$(\times 10^{-2})$	$-8 \pm 14$	$-4 \pm 6$	$4\pm4$
$W^3 \left( n_{ m NL} = -1  ight)$	$(\times 10^{0})$	$-3 \pm 41$	$-7\pm27$	$\mathbf{-6} \pm 15$
$\widetilde{W}W^2$ $(n_{ m NL}=+1)$	$(\times 10^{-3})$	$61 \pm 98$	$-18\pm15$	$-8\pm6$
$\widetilde{W}W^2  (n_{ m NL}=0)$	$(\times 10^{-2})$	$42 \pm 63$	$-9 \pm 11$	$-3\pm 5$
$\widetilde{W}W^2$ $(n_{ m NL}=-1)$	$(\times 10^{0})$	$136 \pm 222$	$-24 \pm 55$	$5 \pm 20$
$\widetilde{F}F$	$(\times 10^{-2})$	$-16 \pm 27$	$-10\pm10$	$3\pm 6$
$Tensor ext{-} Tensor ext{-} Scalar$				
$\widetilde{W}W$	$(\times 10^{-2})$	$29 \pm 460$	$31 \pm 67$	$5 \pm 11$
Tensor-Scalar-Scalar				
Squeezed	$(\times 10^{0})$	$-17 \pm 31$	$9 \pm 15$	13 ± 10

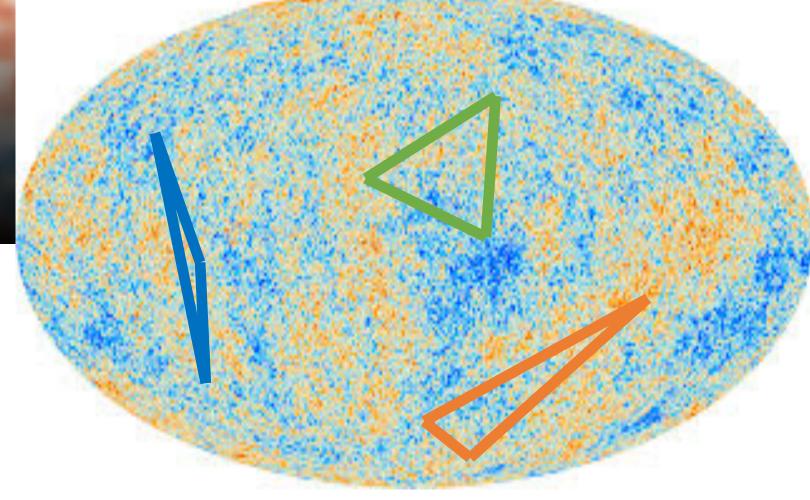
## CMB Constraints (Nightmarish)

 Very few previous works have considered four-point functions!

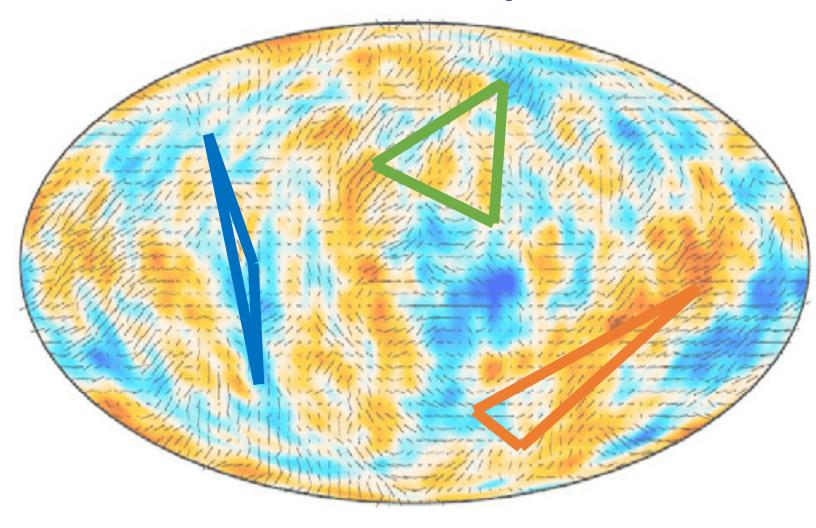
- Until recently, we only had constraints on
  - Local effects  $(g_{\rm NL}^{\rm loc}, au_{\rm NL}^{\rm loc})$
  - Self-interactions (from the EFT of inflation:  $g_{
    m NL}^{
    m equil}$  imes 3)

There's much more to learn from the CMB!

Let's search for primordial physics in the CMB four-point function!



Planck CMB Temperature



**Planck CMB Polarization** 

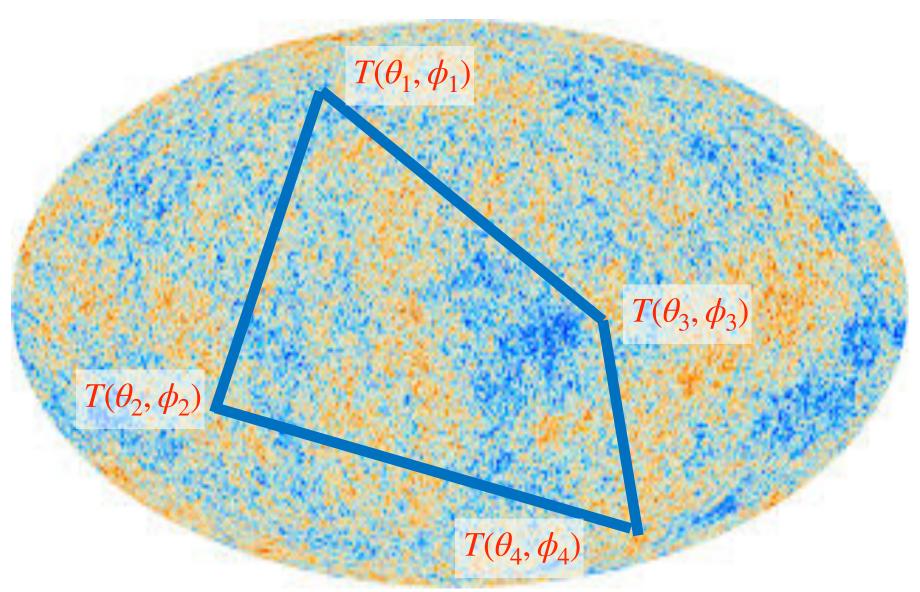
### How to Measure a Four-Point Function

 CMB experiments measure the temperature and polarization across the whole sky

$$T(\theta,\phi), \quad E(\theta,\phi) \quad \leftrightarrow \quad a_{\ell m}^T, \quad a_{\ell m}^E$$

 Since the physics is linear we just need to correlate the CMB at four angles

$$\langle T(\theta_1, \phi_1) T(\theta_2, \phi_2) T(\theta_3, \phi_3) T(\theta_4, \phi_4) \rangle \leftrightarrow \langle a_{\ell_1 m_1}^T a_{\ell_2 m_2}^T a_{\ell_3 m_3}^T a_{\ell_4 m_4}^T \rangle$$



- BUT:
  - The trispectrum is 8-dimensional!?
  - There's  $10^{28}$  combinations of points?!

## Optimal Trispectrum Analyses

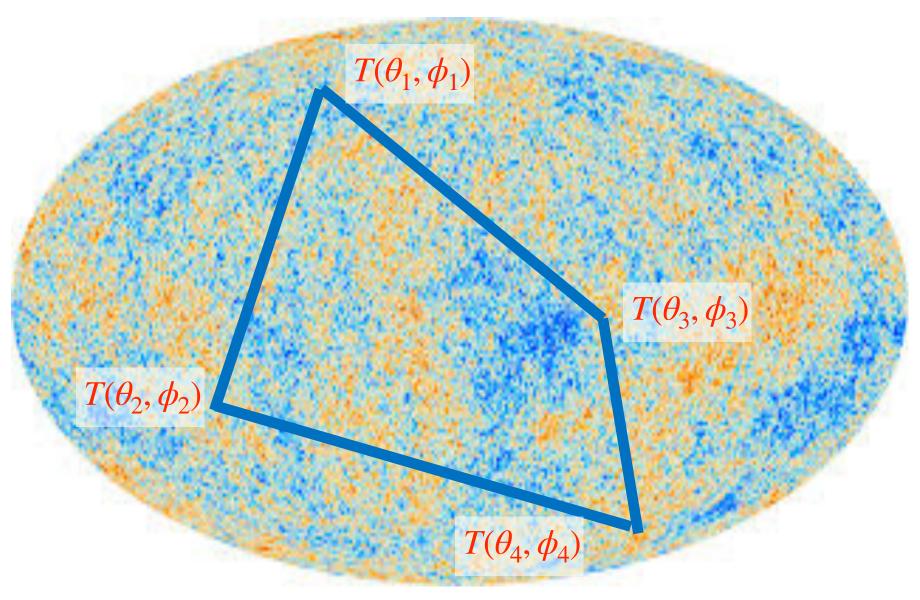
• To compress the data, we'll use techniques from signal processing

$$\widehat{A} \sim \sum_{\ell_1 m_1 \ell_2 m_2 \ell_3 m_3 \ell_4 m_4} \langle a_{\ell_1 m_1} a_{\ell_2 m_2} a_{\ell_3 m_3} a_{\ell_4 m_4} \rangle_{\text{theory}}^{\dagger} \times (a_{\ell_1 m_1} a_{\ell_2 m_2} a_{\ell_3 m_3} a_{\ell_4 m_4})$$

#### Model

#### Data

- We compress all  $10^{28}$  elements into a **single** number!
- This encodes the **amplitude** of a specific model, e.g.,  $au_{\rm NL}$ , which traces the **microphysics** of inflation
- To **compute** the  $\ell$ , m sum we use a variety of tricks, including low-dimensional integrals, harmonic transforms, and Monte Carlo summation
- If the trispectrum can be (integral-)factorized, this reduces the complexity from  $\mathcal{O}(\ell_{\max}^8)$  to  $\mathcal{O}(\ell_{\max}^2 \log \ell_{\max})$



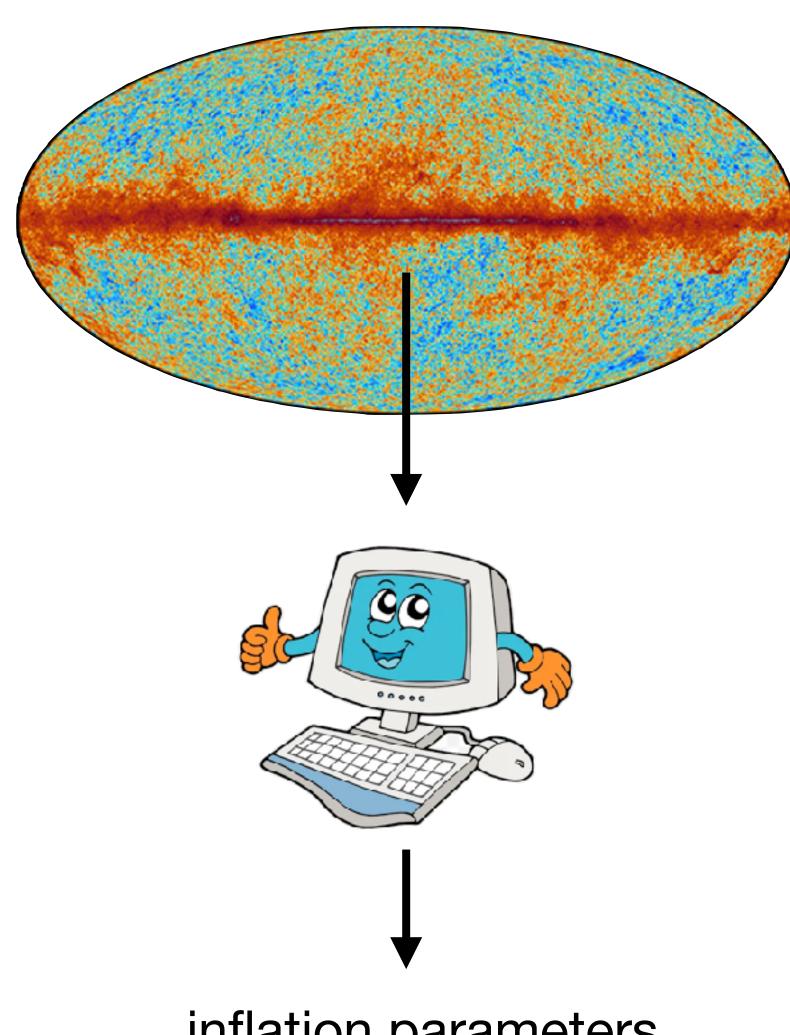
### Optimal Trispectrum Analyses



The result: **fast** estimation of four-point amplitudes!

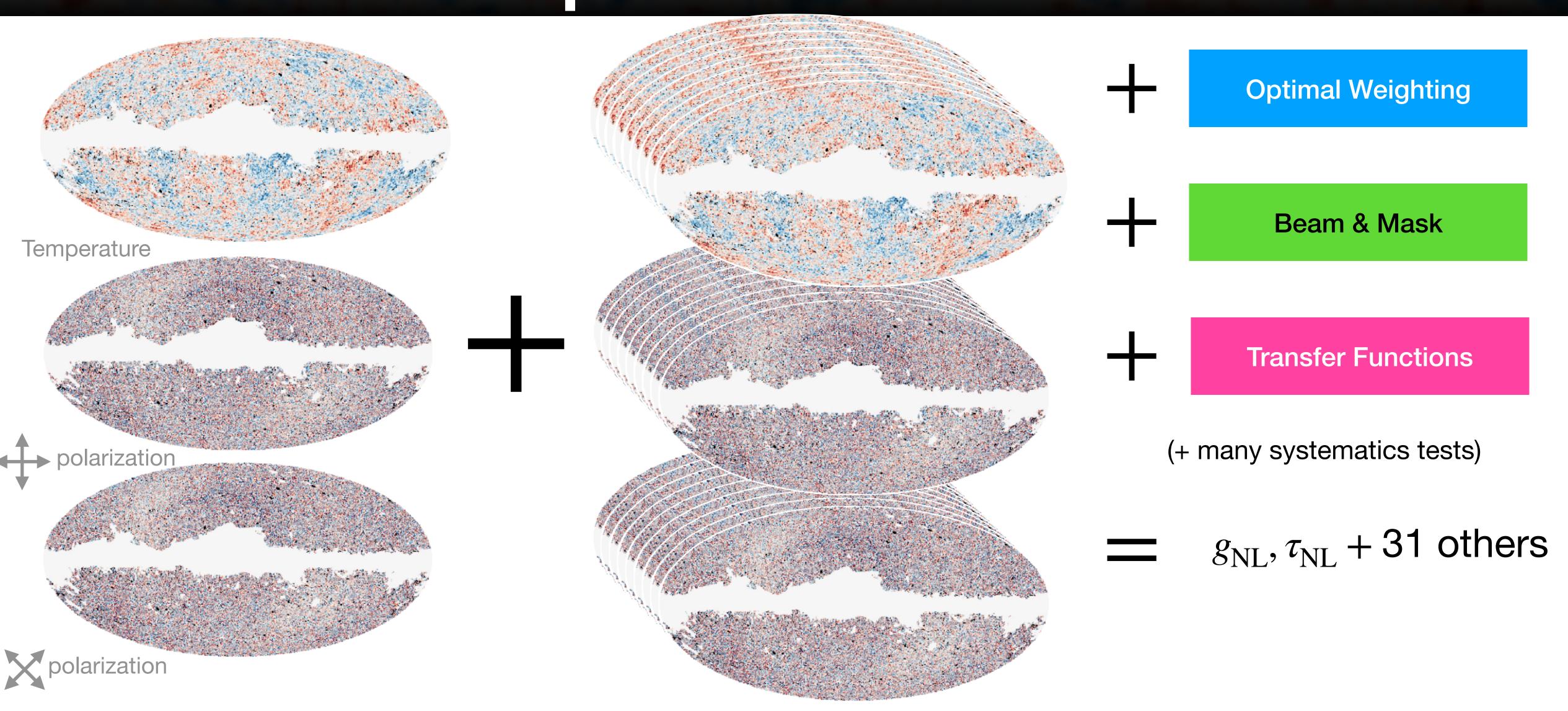
#### The estimators are

- Unbiased (by the mask, geometry, beams, lensing, ...)
- Efficient (limited by spherical harmonic transforms)
- Minimum-Variance (they saturate the Cramer-Rao bound)
- Open-Source (entirely written in Python/Cython)
- General (17 classes of model included so far)



inflation parameters

## The Planck Trispectrum



Planck PR4/NPIPE data

**100 FFP10 simulations** 





#### What did we try to detect?

- 1. Cubic local shape  $(g_{NL}^{loc})$
- 2. Quadratic<sup>2</sup> local shape  $(\tau_{NL}^{loc})$
- 3. Constant shape  $(g_{NL}^{con})$
- 4. Effective Field Theory of Inflation shapes ( $\times 3$ )
- 5. Direction-Dependent shapes
- 6. Cosmological Collider Shapes
- 7. Weak Gravitational Lensing
- 8. Unresolved **Point-Sources**
- 9. ISW-lensing Trispectra





#### What did we try to detect?

1. Cubic local shape  $(g_{NI}^{loc})$ 

2. Quadratic<sup>2</sup> local shape  $(\tau_{NI}^{loc})$ 

3. Constant shape  $(g_{NL}^{con})$ 

4. Effective Field Theory of Inflation shapes ( $\times 3$ )

**Direction-dependent** shapes

Cosmological Collider shapes

7. Weak Gravitational Lensing

Unresolved **Point-Sources** 

ISW-lensing Trispectra

#### Did we detect it?

No

No

No

No  $(\times 3)$ 

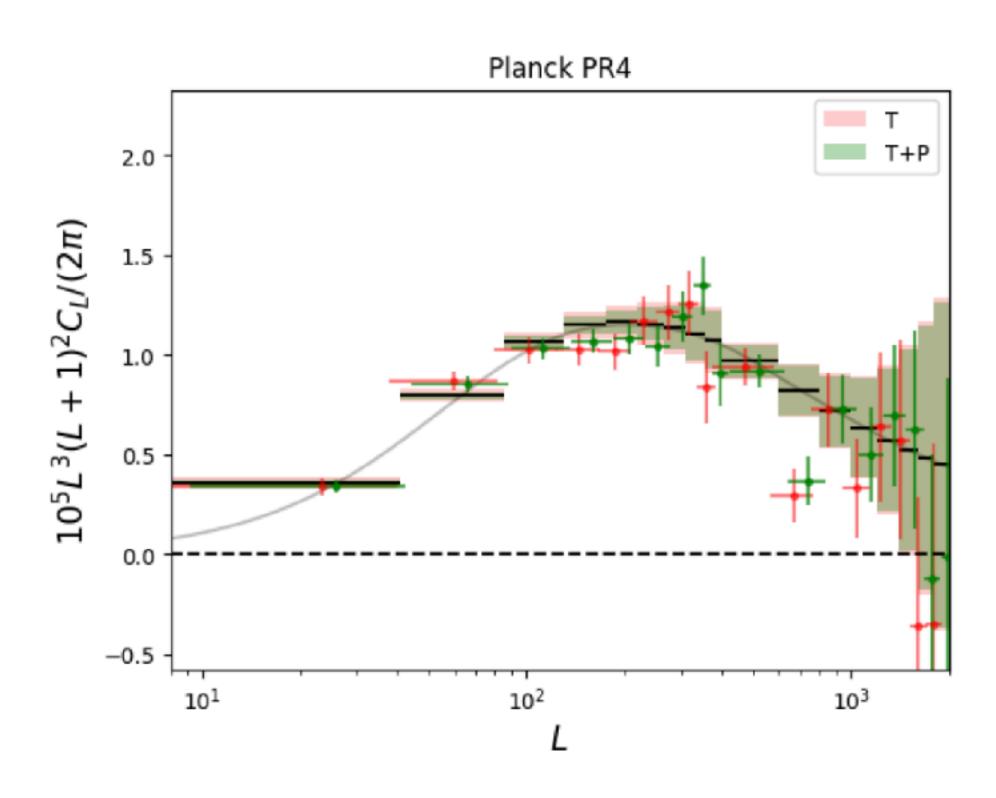
No  $(\times 8)$ 

No  $(\times 17)$ 

Yes!!!

No

No



**OMG!** Lensing! (already detected many times)

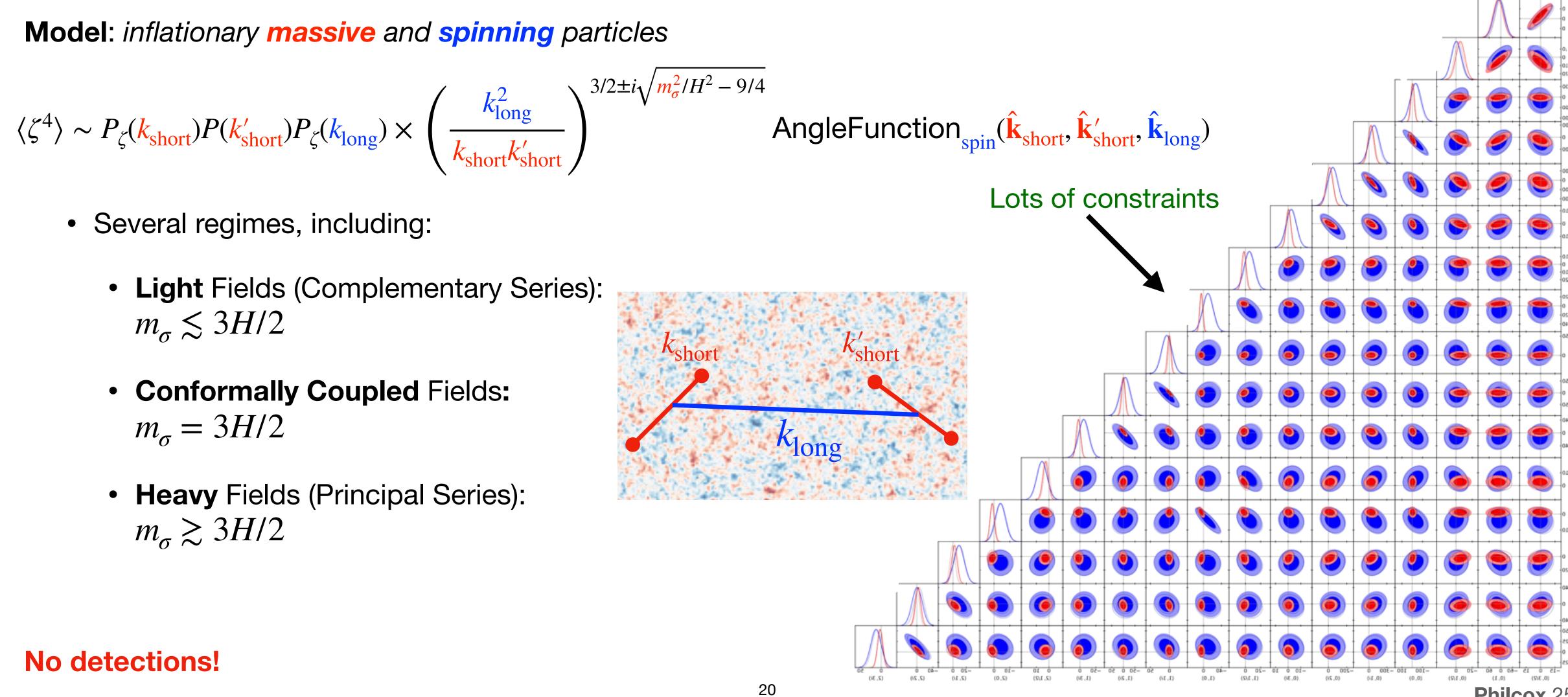
## An Example: Cosmological Colliders

Model: inflationary massive and spinning particles

$$\langle \zeta^4 \rangle \sim P_{\zeta}(k_{\text{short}})P(k'_{\text{short}})P_{\zeta}(k_{\text{long}}) \times \left(\frac{k_{\text{long}}^2}{k_{\text{short}}k'_{\text{short}}}\right)^3$$

Several regimes, including:

- Light Fields (Complementary Series):  $m_{\sigma} \lesssim 3H/2$
- Conformally Coupled Fields:  $m_{\sigma} = 3H/2$
- Heavy Fields (Principal Series):  $m_{\sigma} \gtrsim 3H/2$



No detections!

## What's Next For the Trispectrum?

There are many ways to extend.

1. More Data

$$\sigma(\tau_{\rm NL}) \sim \ell_{\rm max}^{-2}$$



- ACT, SPT, Simons Observatory, LiteBird, CMB-HD, CMB-S4 will provide data down to much smaller scales!
- Polarization will be particularly useful and could benefit from delensing

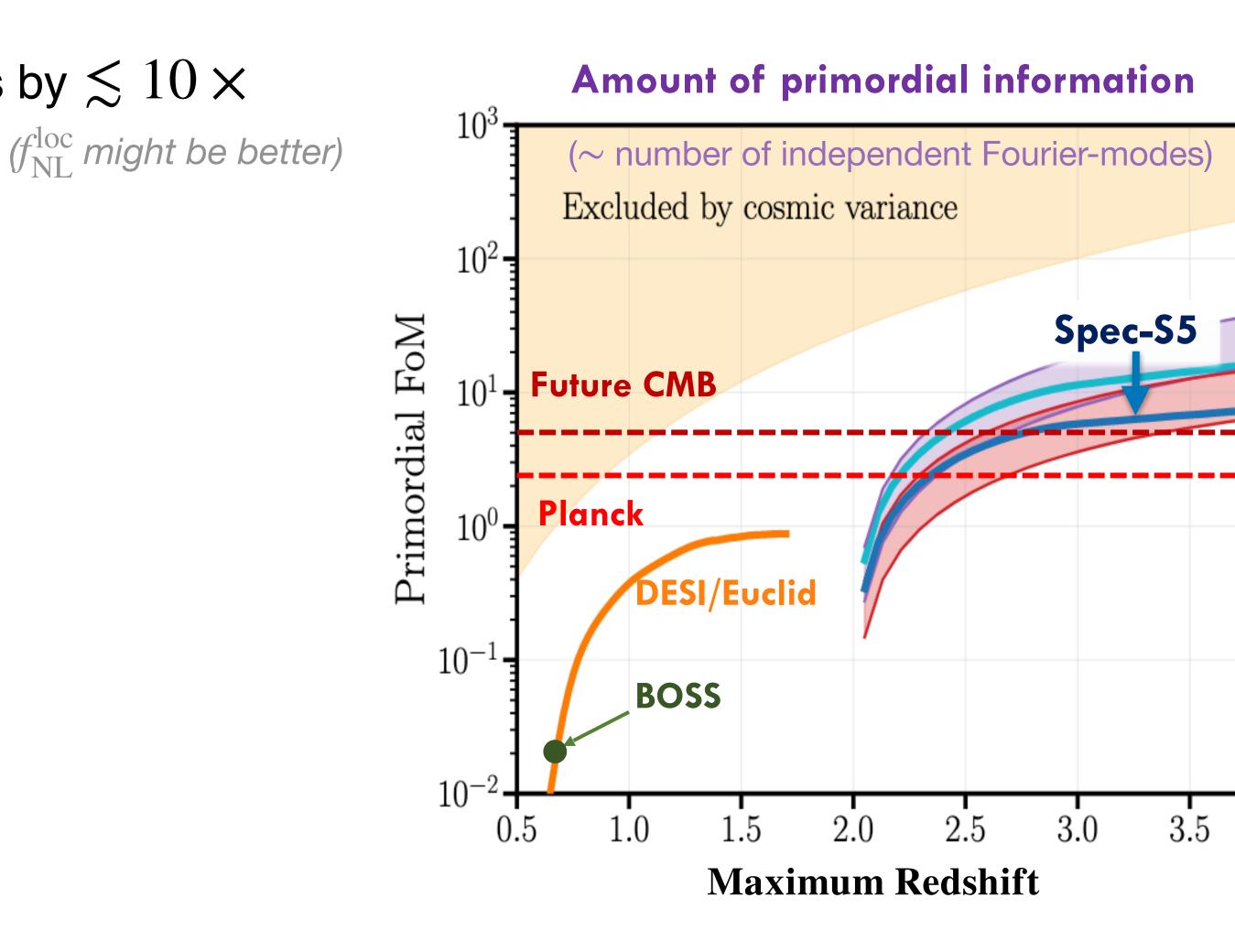
#### 2. More Models

- Lighter particles? Heavier particles?
- Tensor non-Gaussianity?
- Collider physics beyond the collapsed limit?
- Thermal baths? Higher-spin particles? Modified sound speeds? Fermions?
- Scale-dependence? Isocurvature? Primordial magnetic fields?

### The Future of Non-Gaussianity

- Future CMB experiments will improve bounds by  $\lesssim 10 \, \times$ 
  - This is a two-dimensional field
  - We're running out of modes to look at!
  - Small-scales are hard

- What about galaxy surveys?
  - The data precision is rapidly increasing
  - This is a **three-dimensional** field
    - We aren't limited by projection effects
  - There are new observables e.g., galaxy **shapes**

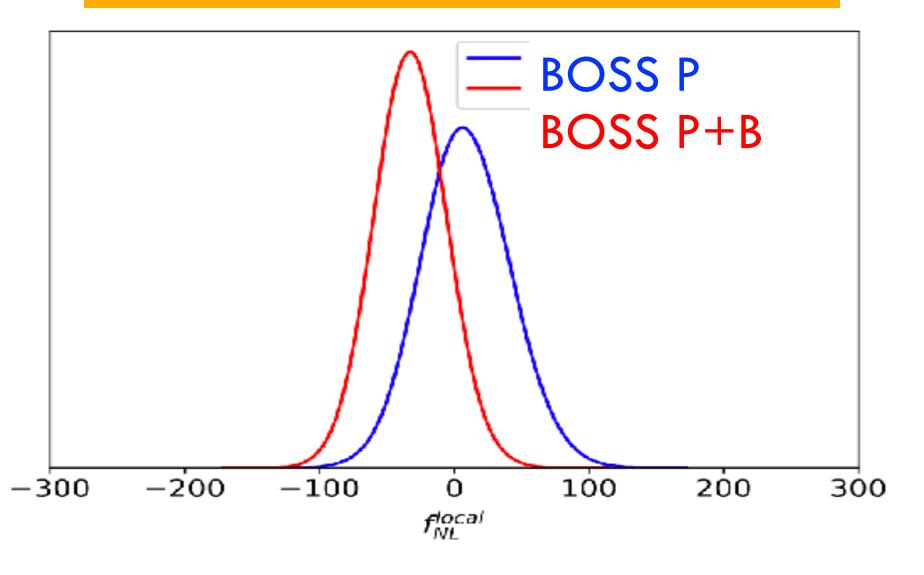


## Inflation from Galaxy Surveys

- The BOSS galaxy survey has been used to constrain primordial three-point functions using the
  - One-loop power spectrum:  $P_{\mathcal{C}}(k) \supset f_{\mathrm{NL}} P_{12}$
  - Tree-level bispectrum:  $B_0(k_1,k_2,k_3)\supset f_{\rm NL}B_{111}$
  - Skew-spectra:  $P[\delta, \delta \star \delta] \supset f_{\rm NL} B_{111}$
- We have constrained:
  - Local three-point functions  $f_{
    m NL}^{
    m loc}$  from additional light fields

#### LOCAL

See Dennis' talk for Euclid prospects! See Marina's talk for eBOSS quasars!



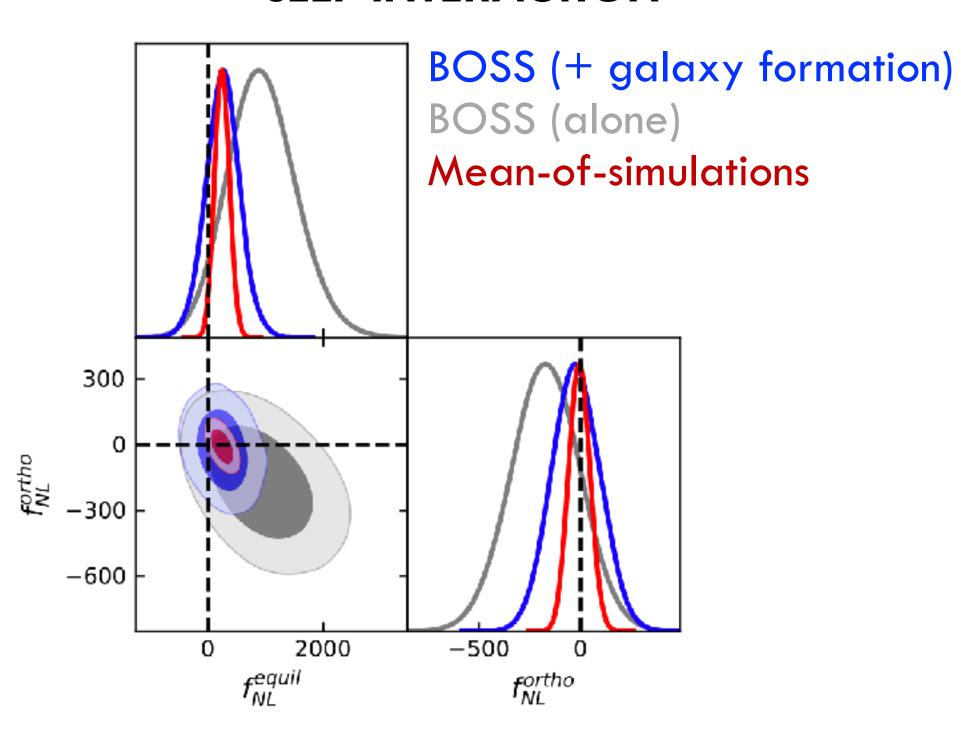
$$f_{\rm NL}^{\rm loc} = -33 \pm 28 \quad (9 \pm 34 \, \text{w/o} \, B_g)$$
 (Now better with DESI Quasars:  $\pm 9$ )

(CMB:  $\pm 5$ , Target:  $\pm 1$ )

## Inflation from Galaxy Surveys

- The BOSS galaxy survey has been used to constrain primordial three-point functions using the
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- We have constrained:
  - Local three-point functions  $f_{
    m NL}^{
    m loc}$  from additional light fields
  - Equilateral three-point functions  $f_{
    m NL}^{
    m eq,orth}$  from cubic interactions in single-field inflation

#### SELF-INTERACTION



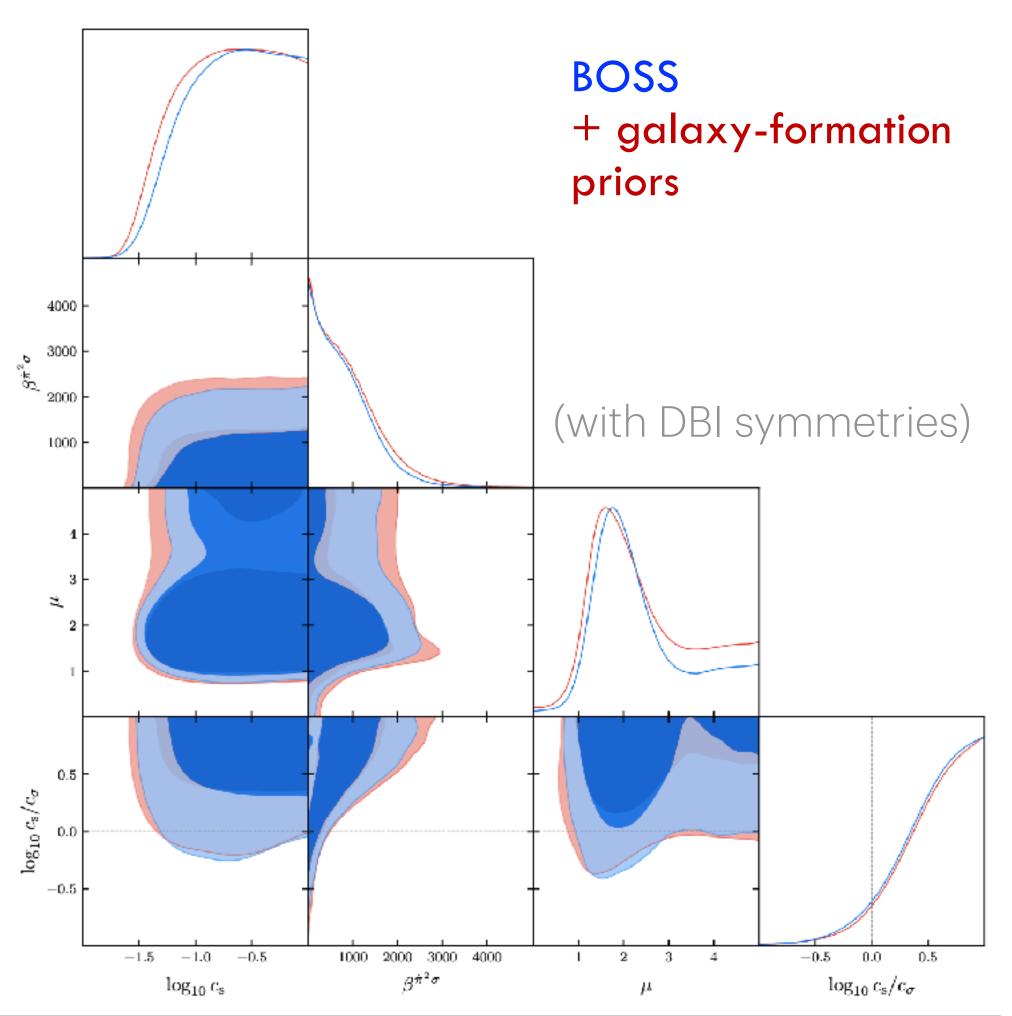
$$f_{\rm NL}^{\rm eq} = 260 \pm 300, f_{\rm NL}^{\rm orth} = -23 \pm 120$$

(CMB:  $\pm 50$ ,  $\pm 25$ , Target:  $\pm 1$ )

## Inflation from Galaxy Surveys

- The BOSS galaxy survey has been used to constrain primordial three-point functions using the
  - One-loop power spectrum:  $P_{\mathcal{C}}(k) \supset f_{\mathrm{NL}} P_{12}$
  - Tree-level bispectrum:  $B_0(k_1,k_2,k_3)\supset f_{\rm NL}B_{111}$
  - Skew-spectra:  $P[\delta, \delta \star \delta] \supset f_{\rm NL}B_{111}$
- We have constrained:
  - Local three-point functions  $f_{
    m NL}^{
    m loc}$  from additional light fields
  - **Equilateral** three-point functions  $f_{\rm NL}^{\rm eq,orth}$  from cubic interactions in single-field inflation
  - Collider three-point functions from the exchange of massive scalar fields

#### **MASSIVE PARTICLE**



- Current LSS constraints are  $\sim 5 20 \times$  worse than the CMB, because:
  - Volume BOSS contains fewer modes than Planck

• Scale-cuts — we can't model beyond  $k_{
m NL}$ 

• Galaxy formation — few assumptions on non-linear physics

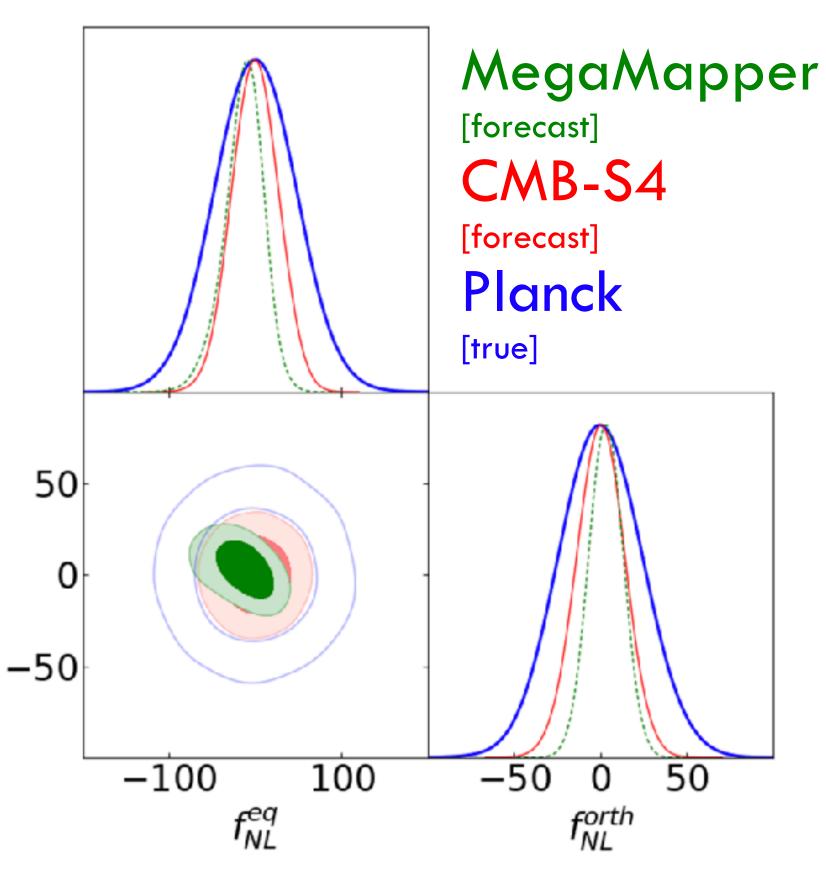
• Statistics — information propagates to other observables

- Current LSS constraints are  $\sim 5 20 \times$  worse than the CMB, because:
  - Volume BOSS contains fewer modes than Planck
    - DESI, Euclid, Spec-S5 will improve this
  - Scale-cuts we can't model beyond  $k_{
    m NL}$ 
    - Use **simulations** or *non-linear responses*

See Sam's talk / Will's talk

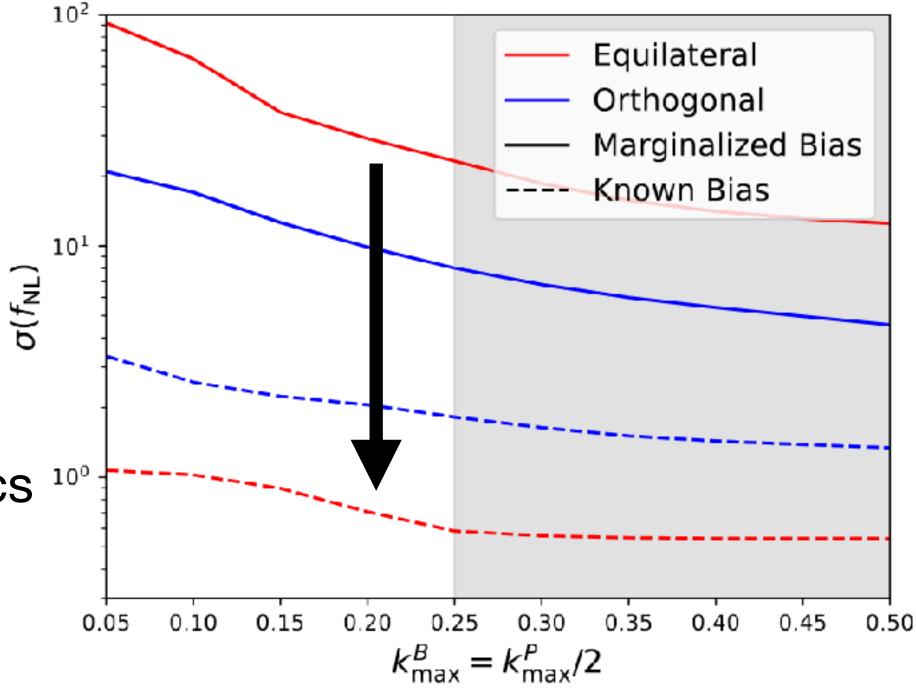
- Galaxy formation few assumptions on non-linear physics \( \bar{\gamma} \)
  - (Careful) priors on bias parameter relations
- Statistics information propagates to other observables
  - Use new statistics

#### Self-Interactions



- Current LSS constraints are  $\sim 5-20 \times$  worse than the CMB, because:
  - Volume BOSS contains fewer modes than Planck
    - DESI, Euclid, Spec-S5 will improve this
  - Scale-cuts we can't model beyond  $k_{
    m NL}$ 
    - Use **simulations** or *non-linear responses*
  - Galaxy formation few assumptions on non-linear physics
    - (Careful) priors on bias parameter relations
  - Statistics information propagates to other observables
    - Use new statistics





(Optimistic  $k_{\rm max}$  — see Jamie's talk)

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  - Scale-cuts we can't model beyond  $k_{
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    - Use **simulations** or *non-linear responses*
  - Galaxy formation few assumptions on non-linear physics
    - (Careful) **priors** on bias parameter relations
  - Statistics information propagates to other observables
    - Use new statistics

#### Other observables

Trispectra / kurtospectra
 kSZ correlators

CMB lensing correlators

Weak lensing statistics

Galaxy shapes

Galaxy spins

Halo mass functions

(and many others)

### The Next Generation of LSS

- DESI has already observed millions of galaxies across a wide range of redshifts
- So far, this has been used primarily through:
  - BAO parameters:  $\alpha_{\parallel,\perp} \sim r_d/D_{\!A}(z), H(z)r_d$
  - Power spectra (galaxies & Ly- $\alpha$ )
- to measure  $\Lambda CDM$  + extensions:
  - $H_0, \Omega_m, \sigma_8, \sum m_{\nu}$
  - $\Omega_k, w_0, w_a$
  - $f_{\rm NL}^{\rm loc}$



Each blob is a 3D galaxy position!

The year one data is now **public** — what else could we measure?

### The Next Generation of LSS

- The first (roughly independent) re-analyses of DESI data are being performed!
  - These include power spectra & bispectra from all galaxy chunks
- This is hard:
  - The public data only contains galaxy positions and weights
  - There's no simulations to use or covariances
- There's lots of systematics to account for, including:
  - Fiber collisions
  - **Bispectrum** window functions
  - Angular systematics

TARGETID	Z	NTILE	RA	DEC	
int64	float64	int64	float64	float64	
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39627546836338876	0.8668980715716706	1	158.44667596279407	-9.962760066342906	
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39627546848923381	0.569430729151765	1	159.17802210549974	-9.97892860399317	
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39627546853115682	0.9274570688680336	1	159.30835543527493	-10.106935803496164	

#### Reanalyzing DESI DR1:

1. ACDM Constraints from the Power Spectrum & Bispectrum

Anton Chudaykin,<sup>1,\*</sup> Mikhail M. Ivanov,<sup>2,3,†</sup> and Oliver H.E. Philcox<sup>4,5,6,7,‡</sup>

arXiv:2507.13433



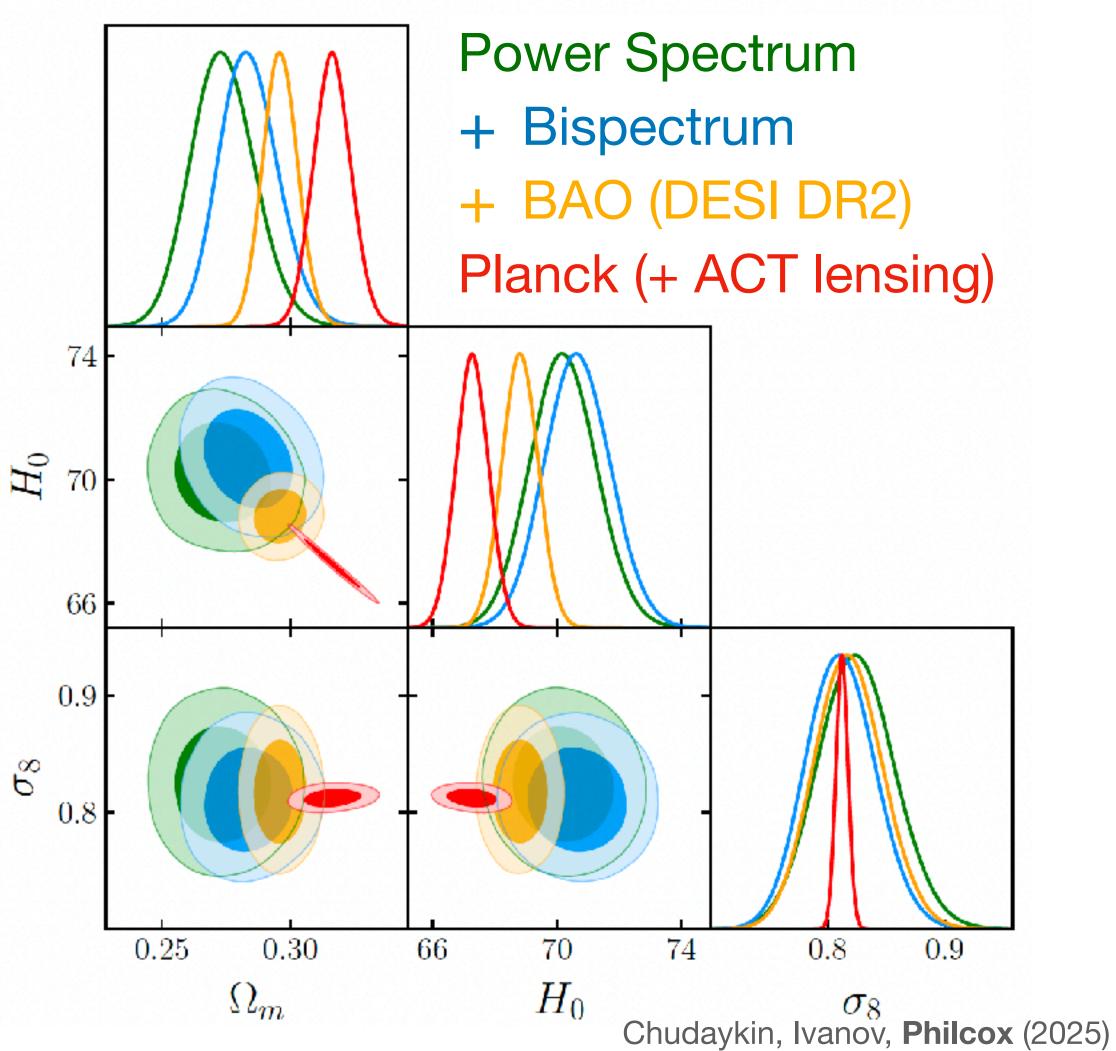




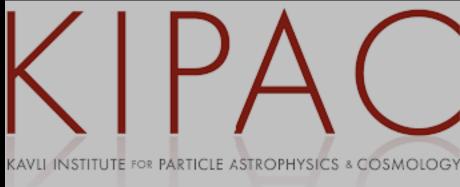
### The Next Generation of LSS

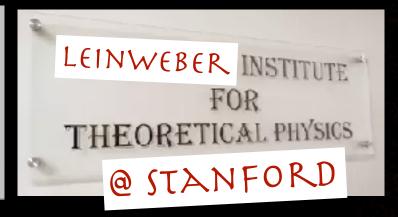
- The first (roughly independent) re-analyses of DESI data are being performed!
  - These include power spectra & bispectra from all galaxy chunks
- So far, we only have published  $\Lambda \text{CDM}$  constraints
  - $\Lambda$ CDM extensions coming soon!
- There's a **lot** more to explore, including:
  - Bispectrum templates:  $f_{\rm NL}^{\rm loc}$ ,  $f_{\rm NL}^{\rm eq}$ ,  $f_{\rm NL}^{\rm orth}$
  - Cosmological colliders (including mass and spin)
  - Trispectrum templates:  $g_{\mathrm{NL}}^{\mathrm{loc}}, au_{\mathrm{NL}}^{\mathrm{loc}}, g_{\mathrm{NL}}^{\mathrm{eq}}, \cdots$

#### **DESI DR1 Constraints**







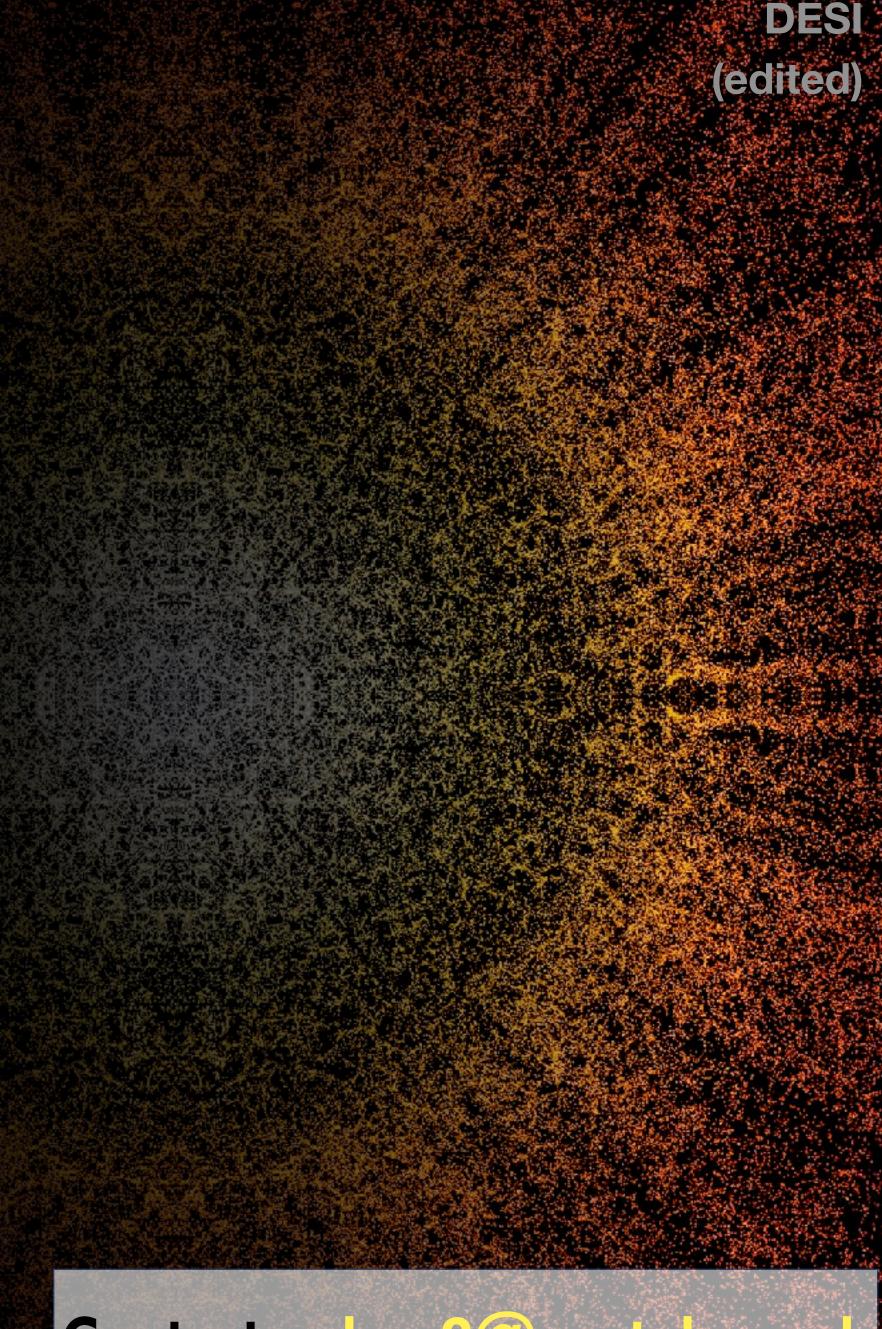


## Summary

There are many sources of inflationary non-Gaussianity

 The CMB is a powerful probe for measuring PNG (though the results are depressing)

 Galaxies will become a leading probe of PNG (eventually)



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