

Mixed Dark Matter and Galaxy Clustering: The Importance of Relative Perturbations

Şafak Çelik

with Fabian Schmidt

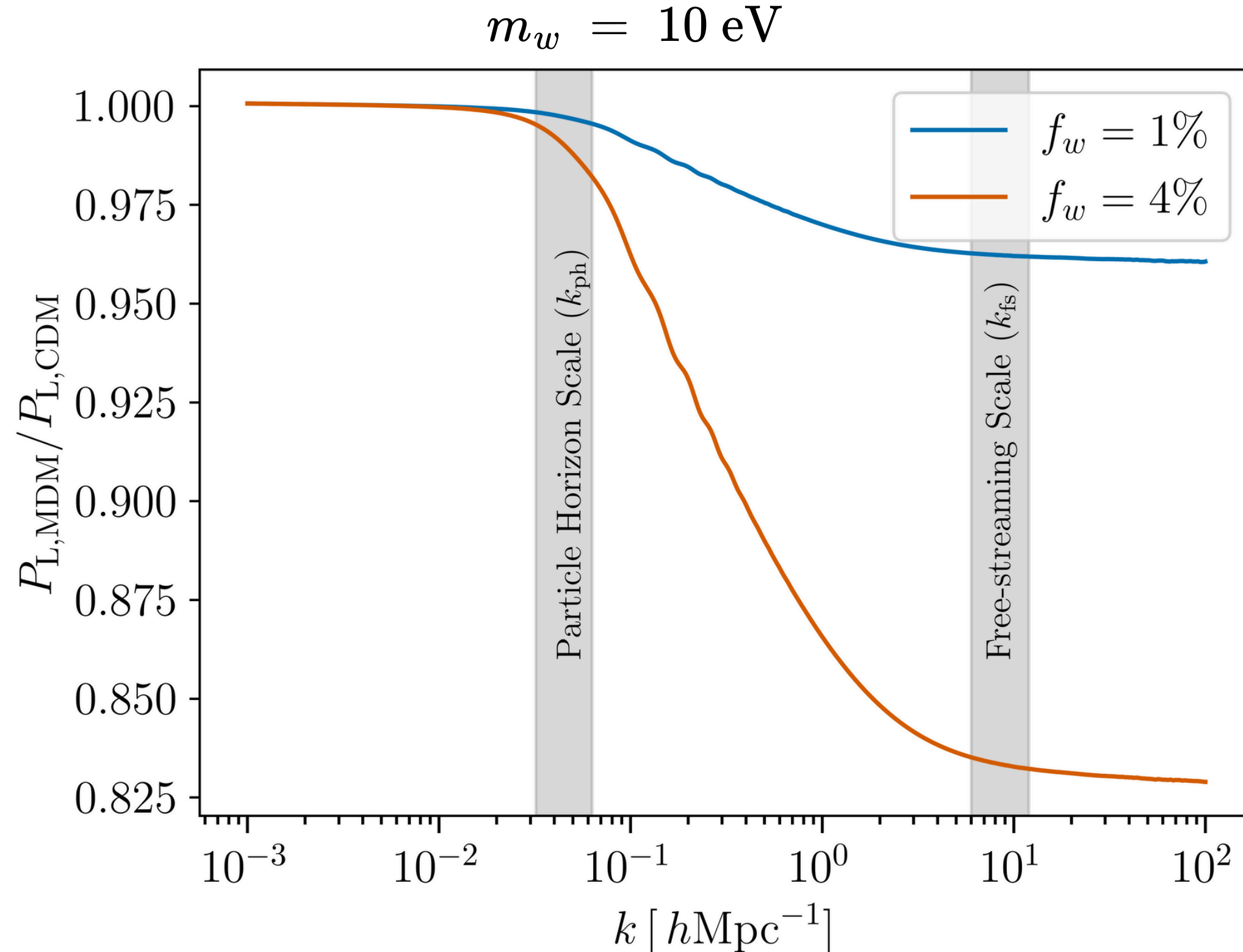
30.09.2025

New Physics from Galaxy Clustering, @GGI

Based on: [2508.21481](#)



Warm Dark Matter and Structure Formation

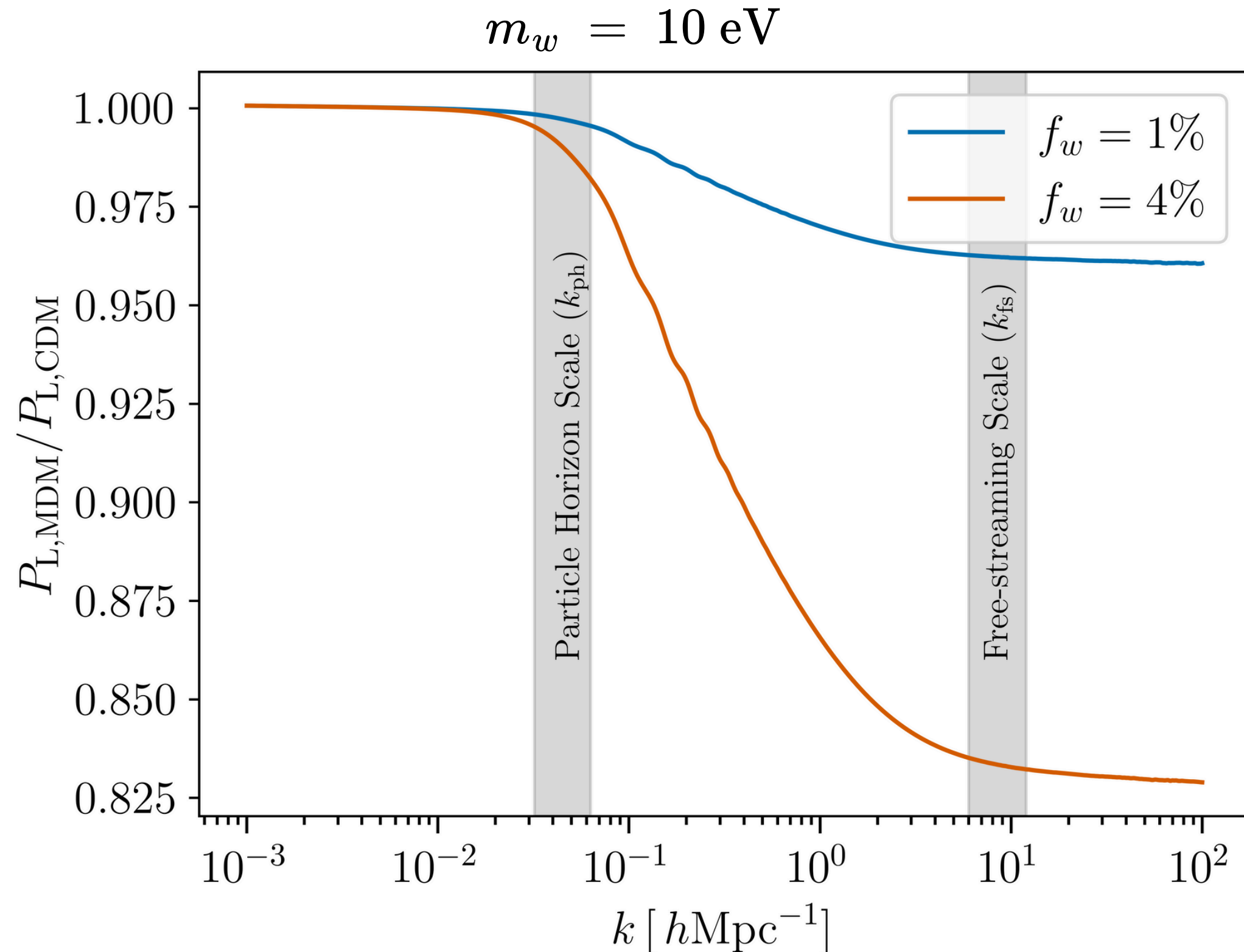


$$f_w \equiv \frac{\Omega_w}{\Omega_c + \Omega_w} = \frac{\Omega_w}{\Omega_{DM}}$$

Boyarsky+ 2009
Xu+ 2022
Parimbelli+ 2022

- CDM paradigm has well known problems especially on small scales.
- MDM with sterile neutrinos produced by DW mechanism
- Two scales (k_{ph} , k_{fs}) and two parameters (m_w , f_w)

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- CDM paradigm has well known problems especially on small scales.
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- Two scales (k_{ph} , k_{fs}) and two parameters (m_w , f_w)
- The question: **How accurate the single fluid treatment is?**

Equations for the Two Fluid Picture

Shoji+ 2010
Verdiani+ 2025

$$\delta'_c + \theta_c = 0$$

$$\theta'_c + \mathcal{H}\theta_c + \frac{3}{2}\Omega_m(a)\mathcal{H}^2\delta_m = 0$$

$$\delta'_w + \theta_w = 0$$

$$\theta'_w + \mathcal{H}\theta_w + \frac{3}{2}\Omega_m(a)\mathcal{H}^2\delta_m - c_s^2(a)k^2\delta_w = 0$$

$$\begin{array}{l} \delta_m := f_w\delta_w + f_c\delta_c \\ \delta_r := \delta_c - \delta_w \end{array} \rightarrow$$

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Solutions:

$$\delta_m^{(1)}(\mathbf{k}, a) = a\delta_m^{(0)}(\mathbf{k}) - \frac{R_p(\mathbf{k})f_w}{3H_0} + \mathcal{O}\left(\frac{k}{k_{\text{fs}}}\right)^4$$

$$\theta_m^{(1)}(\mathbf{k}, a) = -a^{\frac{1}{2}}H_0\delta_m^{(0)}(\mathbf{k}) + \mathcal{O}\left(\frac{k}{k_{\text{fs}}}\right)^4$$

with $R_p(\mathbf{k}) = -\frac{2c_{si}^2 k^2}{H_0}\delta_m^{(0)}(\mathbf{k})$

$$\delta_r^{(1)}(\mathbf{k}, a) = R_0(\mathbf{k}) - \ln(a)\frac{R_p(\mathbf{k})}{H_0} + \frac{R_-(\mathbf{k})}{\sqrt{a}H_0}$$

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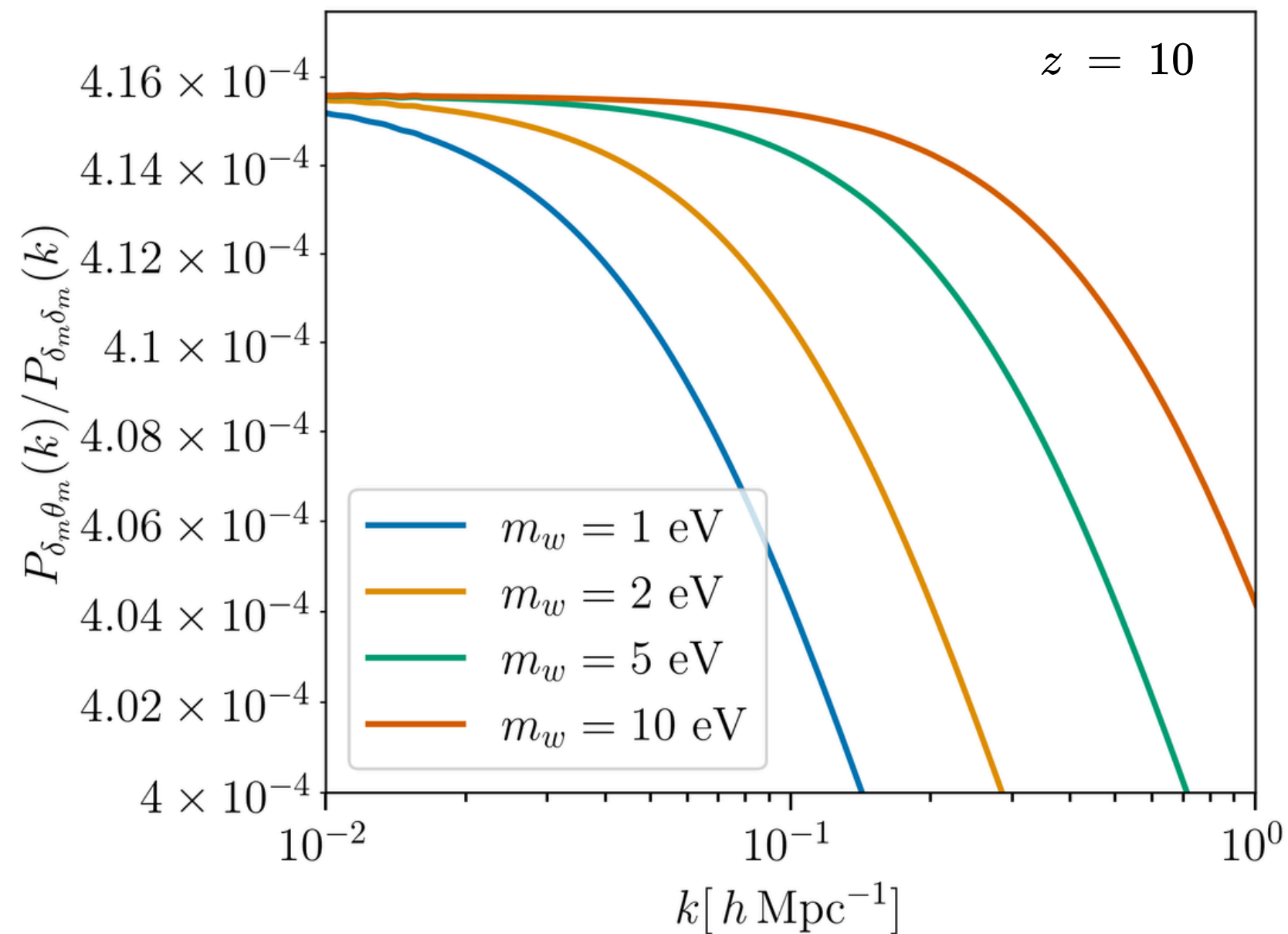
WHAT ABOUT SCALE DEPENDENT GROWTH (&BIAS)

???

Numerical Results from CLASS

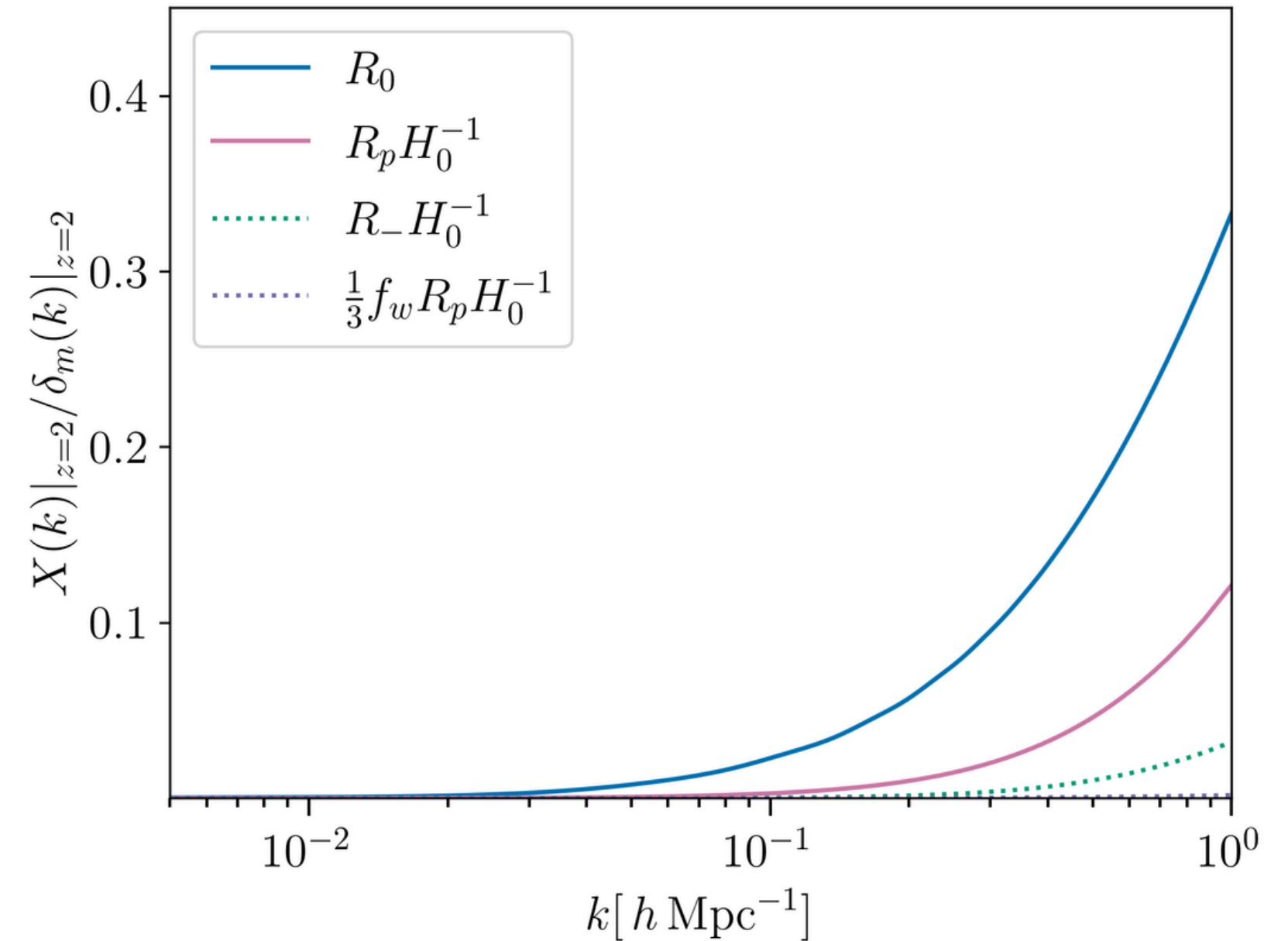
Lesgourgues+ 2015

Scale Dependence



Hierarchy in Between the Modes

$$m_w = 10 \text{ eV}, f_w = 5 \%$$

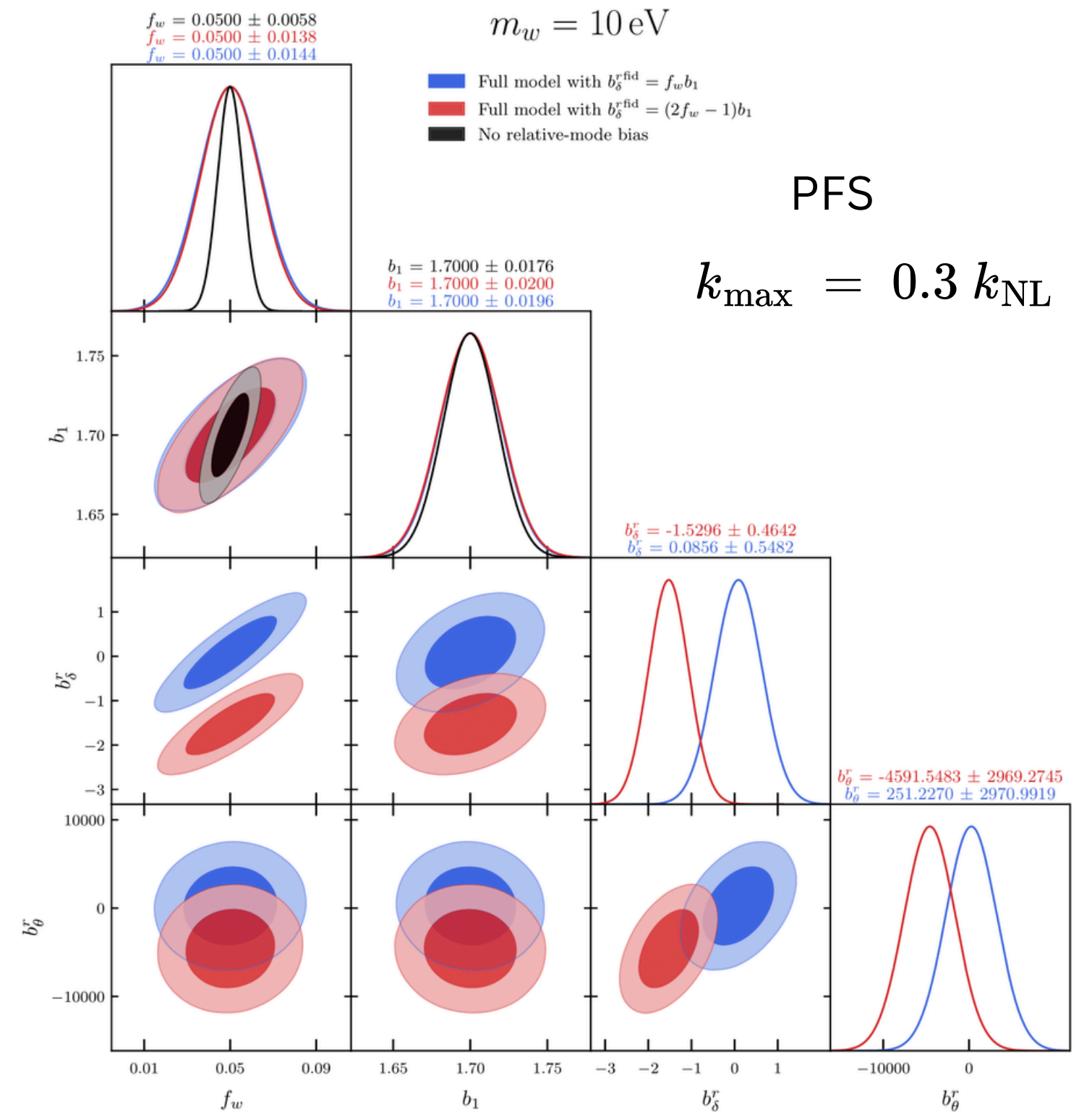
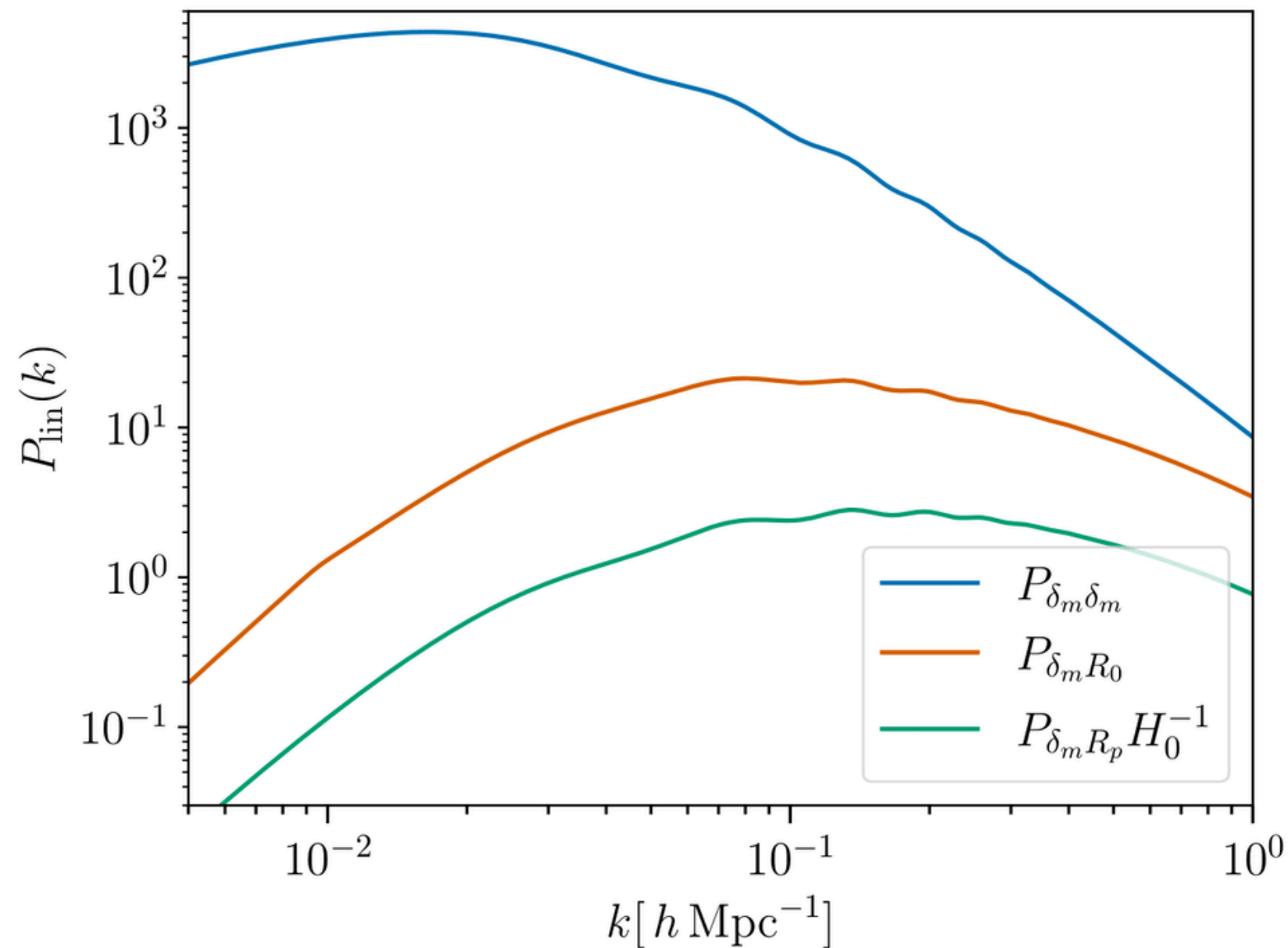


Galaxy bias Expansion

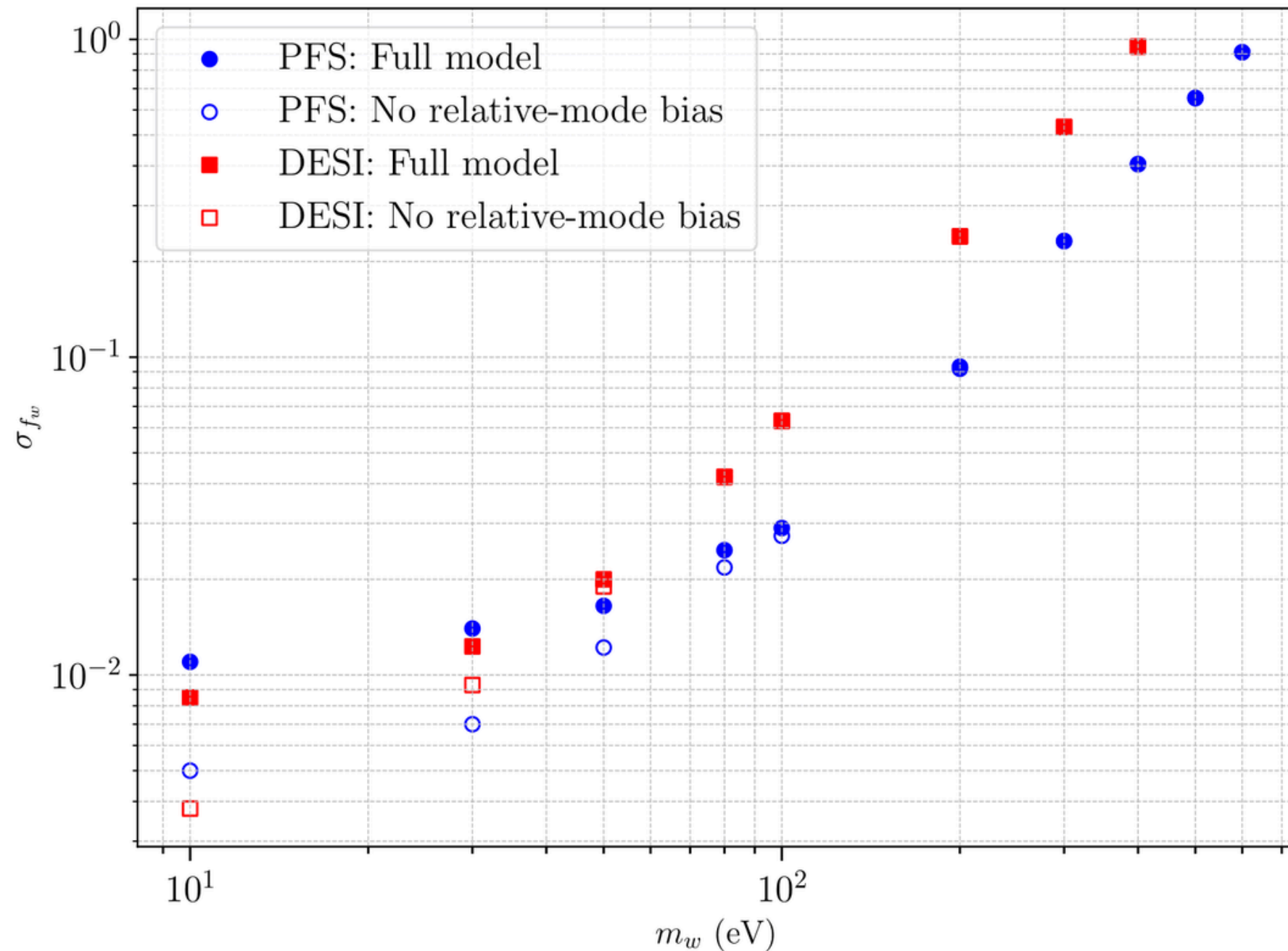
Schmidt 2016
Verdiani+ 2025

$$\delta_g(\mathbf{k}, \eta) = \sum_{\mathcal{O}} b_{\mathcal{O}}(\eta) \mathcal{O}(\mathbf{k}, \eta) \xrightarrow{\text{Two fluid system}} \delta_g^{(1)}(\mathbf{x}, \eta) = b_1(\eta) \delta_m^{(1)}(\mathbf{x}, \eta) + b_{\delta}^r(\eta) R_0(\mathbf{x}, \eta) + b_{\theta}^r(\eta) R_p(\mathbf{x}, \eta) + \epsilon(\mathbf{x}, \eta)$$

$m_w = 10\text{eV}, f_w = 5\%$



Fisher Results for PFS&DESI



Some Remarks:

- The relative perturbations are significant especially for low mass warm components.
- DESI best constrains low mass; PFS pushes sensitivity to higher mass.
- Fisher bias for the lightest particle up to 5.7σ for PFS and 3.6σ DESI.

Future Prospects:

- Going beyond linear order, and look at the ranking of the additional modes.
- Extending the literature in Lyman-alpha forest and galaxy shape analysis.
- Measuring the relative mode biases with the help of simulations.