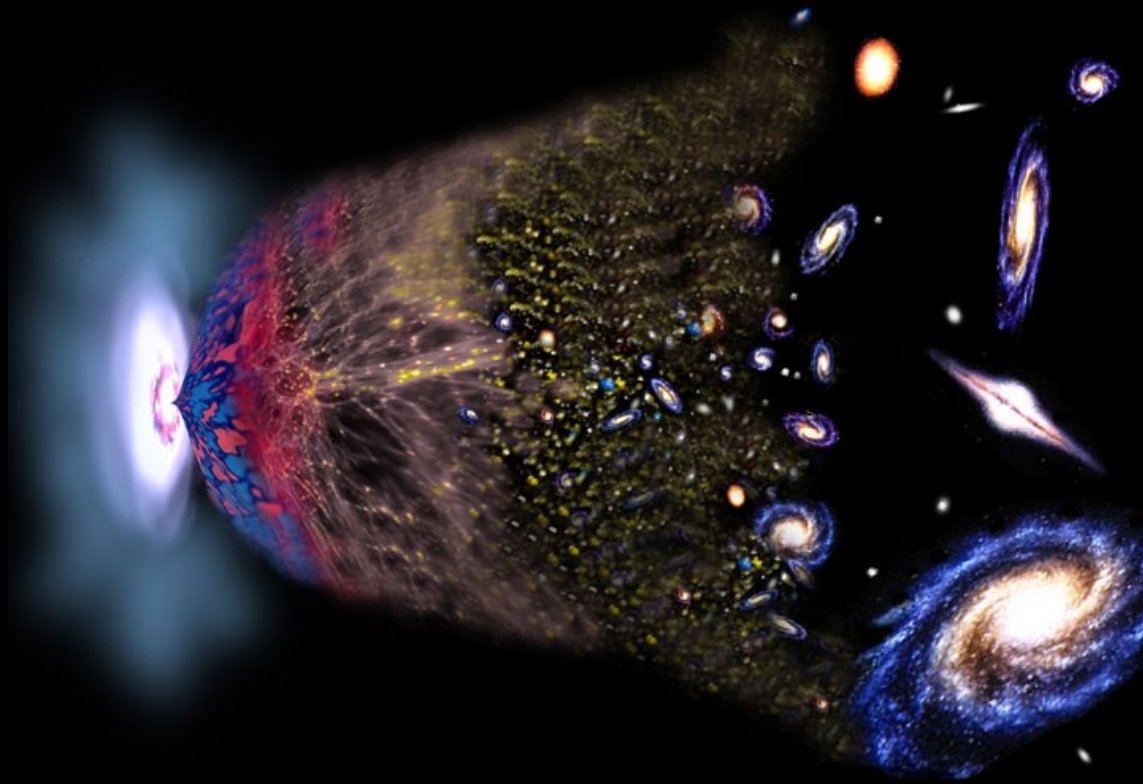


# Challenges of the accelerating Universe: Measuring the expansion rate



Raul Jimenez

[www.ice.csic.es/personal/jimenez](http://www.ice.csic.es/personal/jimenez)

# The basics

Action describing the dynamics of the universe is:

$$S = \int dt d^3x \sqrt{-g} \left\{ -\frac{m_p^2}{16\pi} \left( R + f(R, R^{\mu\nu} R_{\mu\nu}) \right) + \frac{g^{\mu\nu}}{2} \partial_\mu q \partial_\nu q - V(q) + S_{matter} \right\}$$

Consider quintessence a perfect fluid:

$$\rho_Q = \frac{1}{2} \dot{q}^2 + V(q)$$
$$p_Q = \frac{1}{2} \dot{q}^2 - V(q)$$

Which has conservation law:

$$\dot{\rho}_q + 3H(\rho_q + p_q) = 0$$

For full treatment see Simon, Verde, RJ (2005)

All left now is use Einstein eq:

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi}{3m_p^2}(\rho_m + \rho_q)$$

And Klein-Gordon equation:


$$\ddot{q} + 3H\dot{q} + V' = 0$$

What I want to know is shape of potential V

$$\varepsilon_1 = -\frac{\dot{H}}{H^2}; \quad \varepsilon_2 = \frac{\dot{\varepsilon}_1}{H\varepsilon_1}$$

$$V(z) = (3 - \varepsilon_1) \frac{H^2}{m_p} - \frac{1}{2} \sum_i (1 - w_i) \rho_i - \frac{1}{2} (\rho_f - p_f)$$

But what I really need is V(q)


$$V(q) = \varepsilon_1 \frac{H^2}{m_p} - \frac{1}{2} (\rho_T + p_T)$$

**We can “measure” dark energy because of its effects on the expansion history of the universe and the growth of structure**

$$\frac{\dot{a}(t)}{a(t)} = H(z) = -\frac{1}{(1+z)} \frac{dz}{dt}$$

$$H^2 = H_0^2 [\rho(z) / \rho(0)]$$

$$\dot{\rho}_Q = -3H(z)(1+w(z))\rho_Q$$

SN: measure  $d_L$

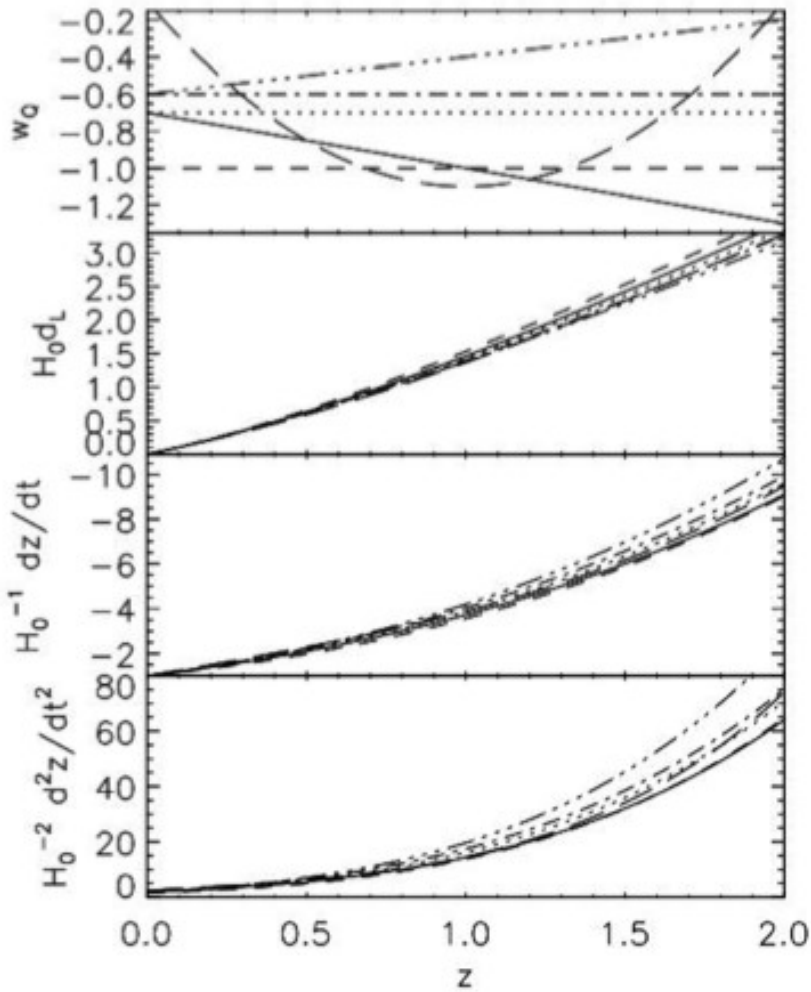
$$d_L = (1+z) \int_z^0 (1+z') \frac{dt}{dz'} dz'$$

CMB:  $\theta_A$  and ISW  $\rightarrow a(t)$

LSS or LENSING:  $g(z)$  or  $r(z) \rightarrow a(t)$

AGES:  $H(z) \rightarrow a(t)$

$$H_0^{-1} \frac{dz}{dt} = -(1+z)^{5/2} \left\{ \Omega_m(0) + \Omega_Q(0) \exp\left[3 \int_0^z \frac{dz'}{(1+z')} w_Q\right] \right\}^{1/2}$$



30% variation in  $w(z)$   
corresponds to:

- 5% variation in  $d_L$
- 10% variation in  $dz/dt$
- 30% variation in  $d^2z/dt^2$

## Challenge n2: is it dynamical?

Theoretical physicists: which parameterization?

To give you a flavor, assume it is a slowly rolling potential and think about inflation

$$\epsilon_1 = -\frac{\dot{H}}{H^2} = 1 - \frac{\ddot{a}}{a} H^{-2} = \frac{dH}{dz} \frac{(1+z)}{H}$$

Similar to horizon flow parameters  
(from Simon, Verde, RJ PRD 2005)

$$V(z) = (3 - \epsilon_1) \frac{H^2}{\kappa} - \frac{1}{2} \rho_m$$

$H(z)$

$\dot{H}(z)$

$$K(z) = \epsilon_1 \frac{H^2}{\kappa} - \frac{1}{2} \rho_m$$

Just integrate to get  $\phi(z)$

But if you have a parameterization (or a model)

$$3H^2(z) - \frac{1}{2} (1+z) \frac{dH^2(z)}{dz} = \kappa \left( V(\alpha_i, z) + \frac{1}{2} \rho_m(z) \right) \equiv g(\alpha_i, z)$$

Can be integrated analytically!

## Unfortunately....

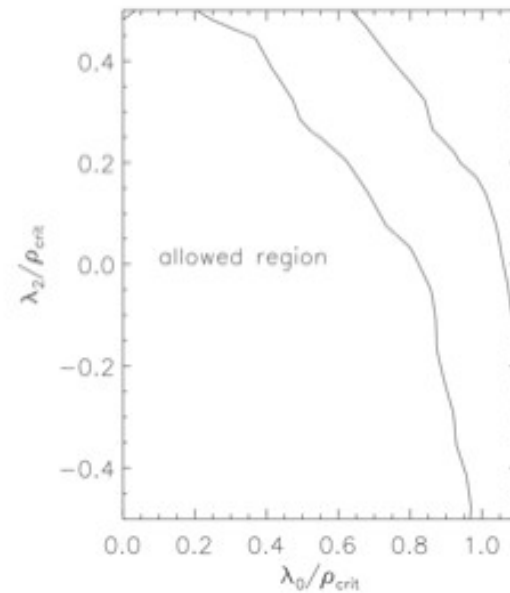
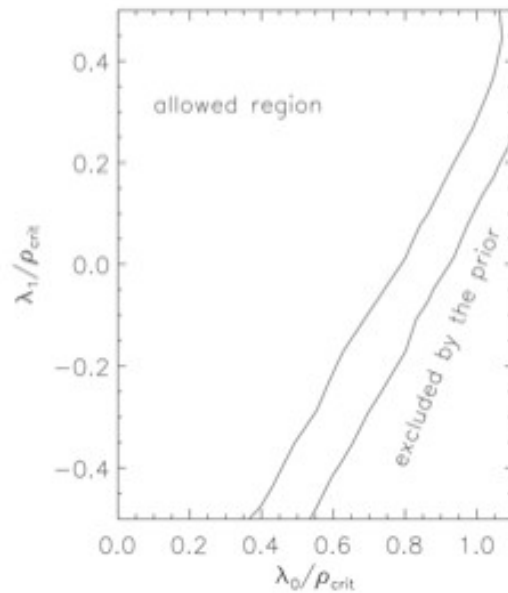
Data are not yet good enough for a fully non-parametric reconstruction

**Chebyshev** to the rescue...

$$V(z) = \sum_{n=0}^M \lambda_n T_n[x(z)], \quad x(z) = \frac{2z}{z_{\max}} - 1$$

No data, priors only

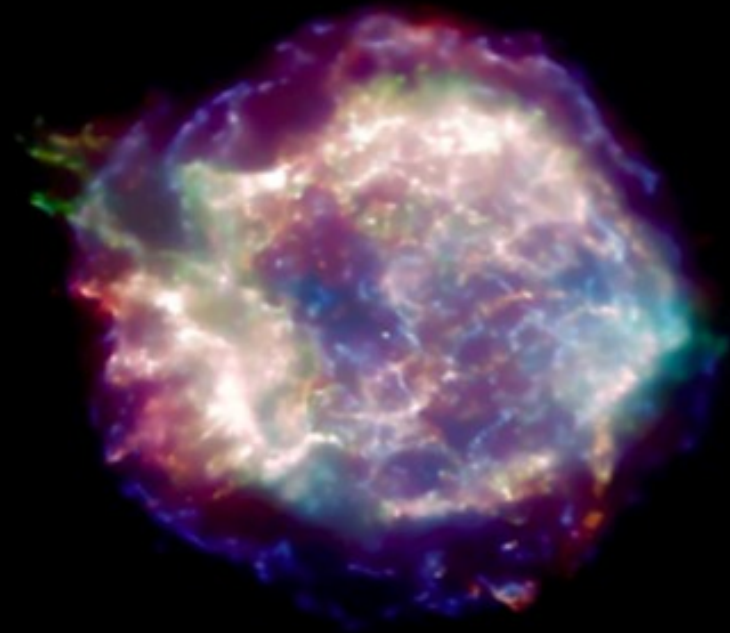
$K > 0$      $\rho_T > 0$  that is  $H^2 > 0$      $V_0 + K_0 = \Omega_{Q,0}\rho_c$     Flatness



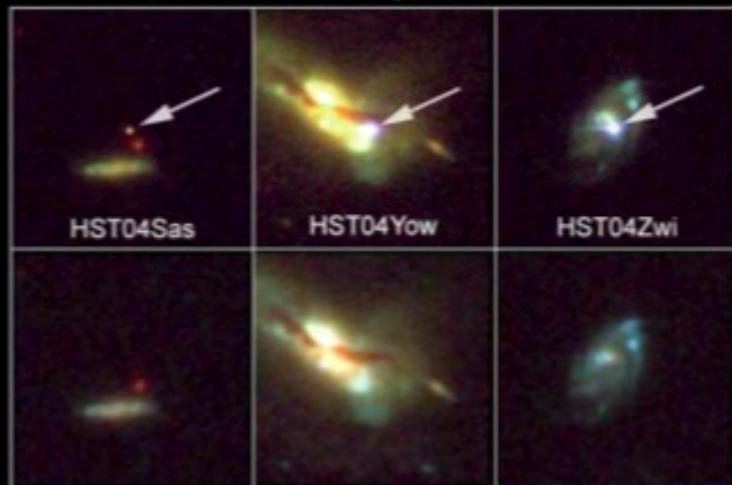
$\Omega_{m,0} = 0.27 \pm 0.07$     From large-scale structure !



# Standard Candle

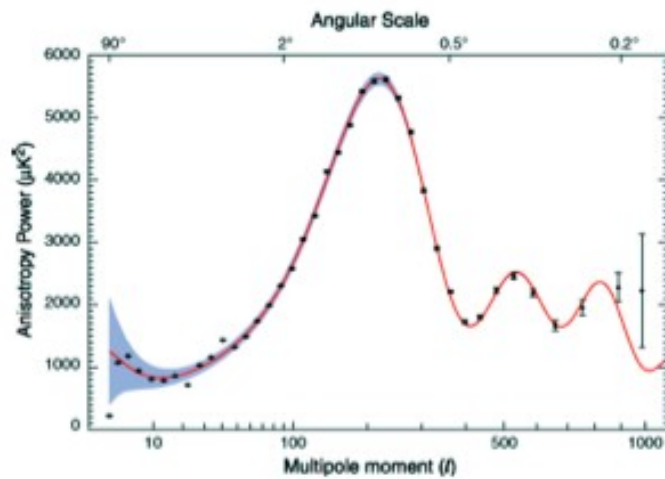
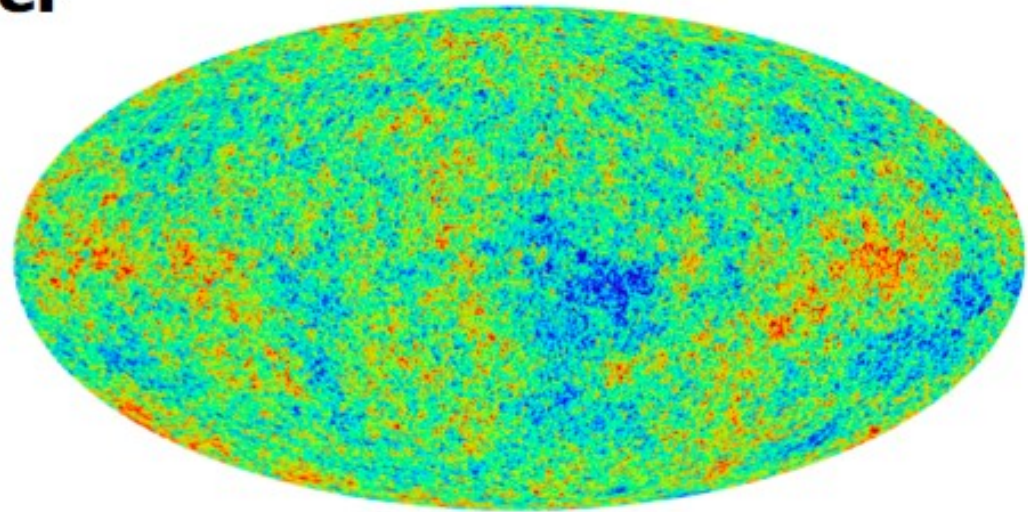


Host Galaxies of Distant Supernovae



NASA, ESA, and A. Riess (STScI)

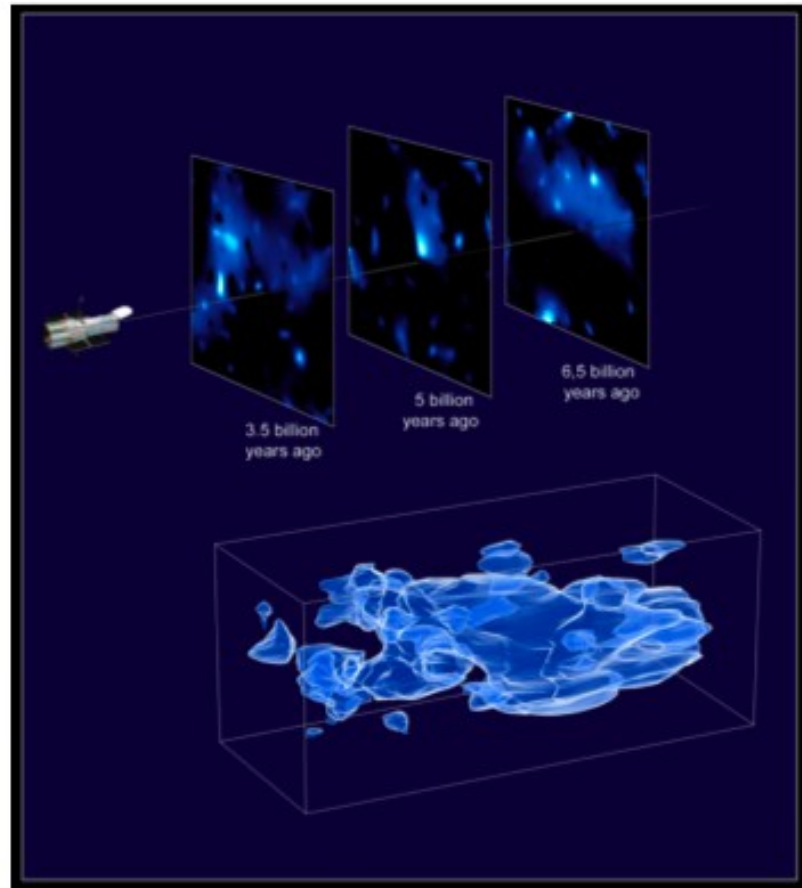
# Standard Ruler



baryon acoustic oscillations  
(radio galaxies)

# Structure Formation

weak lensing  
galaxy clusters



Rotate Image Right

# Standard Clock



early-type galaxies



# Kinetic SZ/Ostriker-Vishniac (OV)

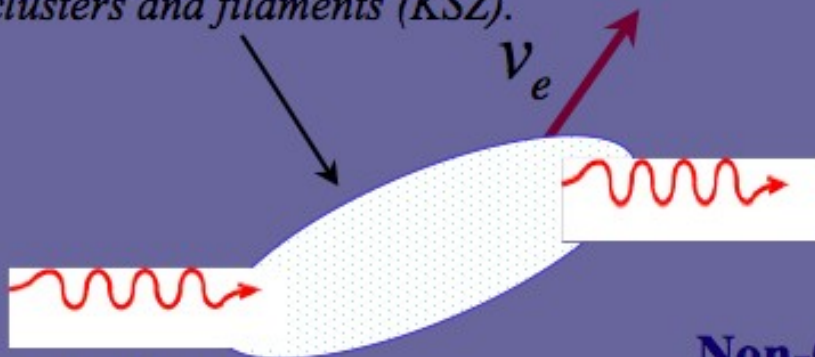
$$\delta T_{kSZ} \propto n_e \mathbf{v}_e \cdot \mathbf{n}$$

**Amplitude** of OV signal determines epoch of reionization.

**Bulk Velocity** of hot electrons.

Bulk velocity of **HOT** electrons from ionization by the first stars (OV) or in clusters and filaments (KSZ).

**OV power spectrum** measures the density and velocity fluctuations at reionization.



CMB photon

**KSZ** measures cluster bulk velocity field at low z.

**Non-Gaussian** but with CMB frequency spectrum. Spatially distinguishable. Requires a high fidelity map.

# Using the KSZ signal

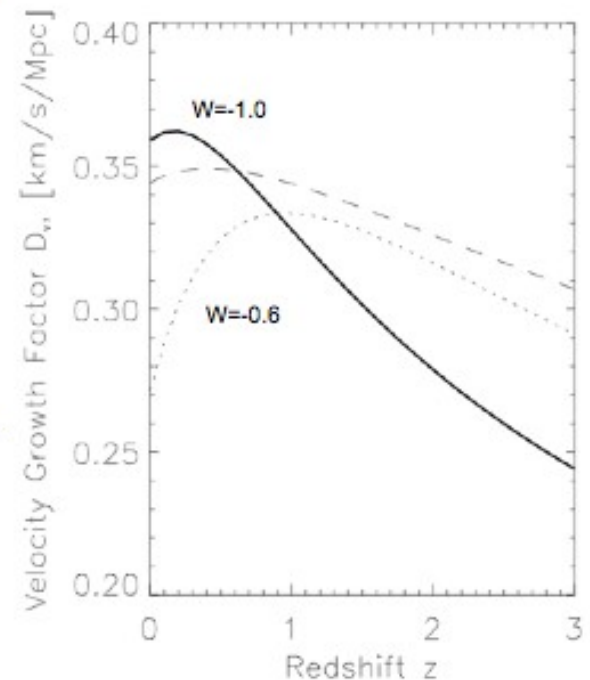
(Hernandez-Monteagudo, Verde, RJ, Spergel 2005)

The peculiar velocity field is sensitive to the onset of the late acceleration of the Universe.

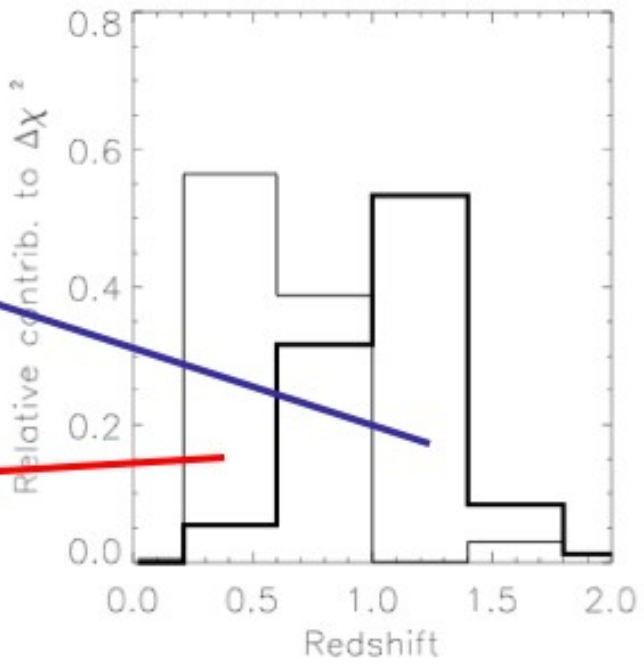
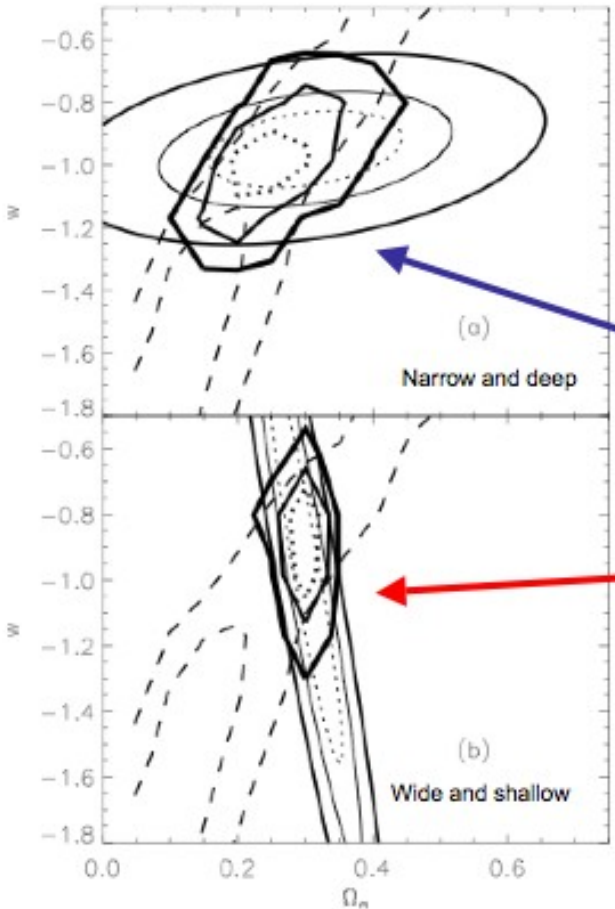
Recall that KSZ  $\delta T_{kSZ} \propto n_e \mathbf{v}_e \cdot \mathbf{n}$

The power spectrum of the velocities is

$$P_{vv}(k) = \left( H(z) \left| \frac{dD_\delta}{dz} \right| \right)^2 \frac{P_m(k)}{k^2} = \mathcal{D}_v^2 \frac{P_m(k)}{k^2},$$



# KSZ sensitivity to $w$

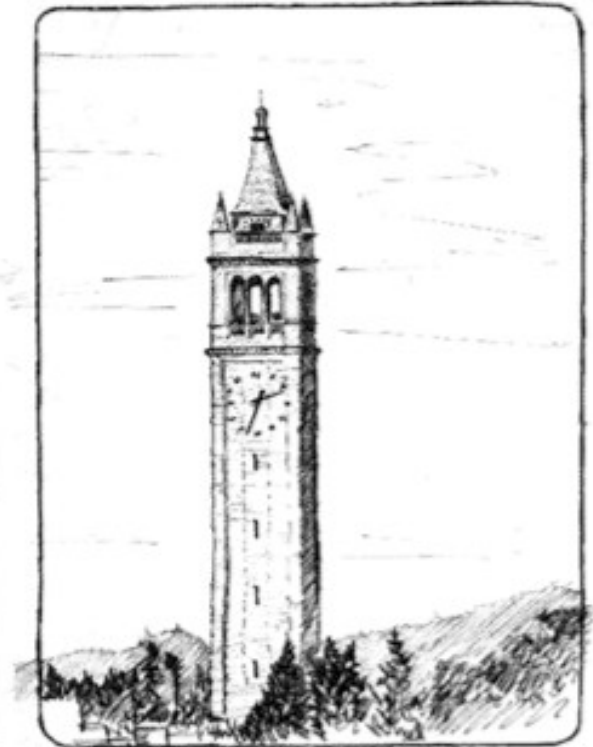


(from Hernandez-Monteagudo et al.2005)

# Cosmic Clocks:

## Constraining the Equation of State of Dark Energy

with Dan Stern (JPL/Caltech)  
Marc Kamionkowski (Caltech)  
Licia Verde (Barcelona)





## Experimental concerns

How well can gE's be approximated as passively evolving, old systems?

- mergers; early-type galaxies still assembling at  $z < 1$ ?
- on-going star formation (“frosting”)

How can we best model the stellar ages?

- systematics between stellar synthesis models

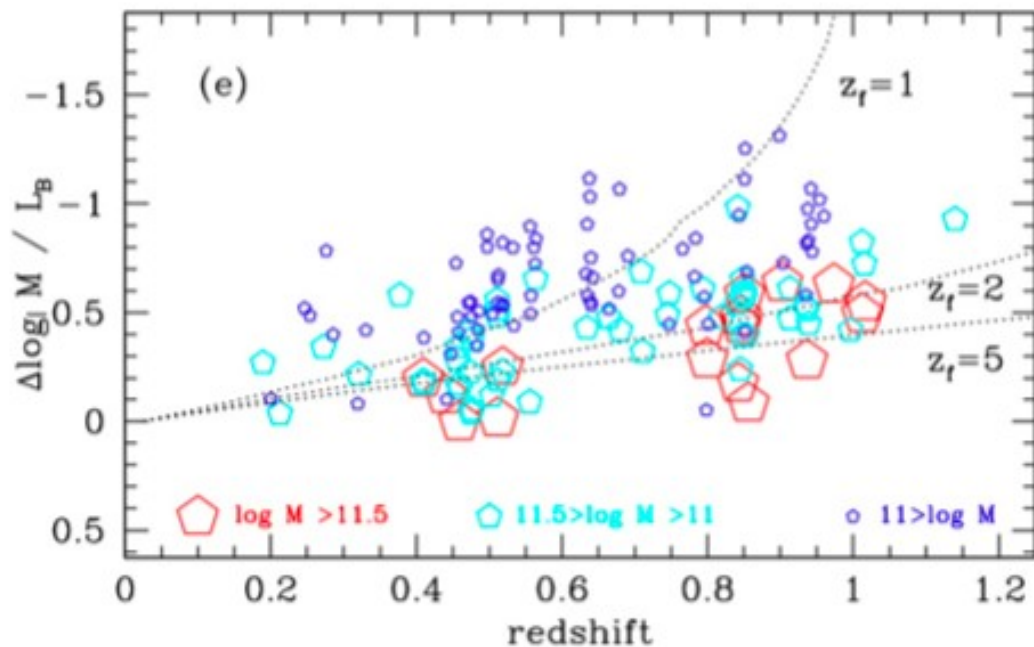
How can we best measure the stellar ages?

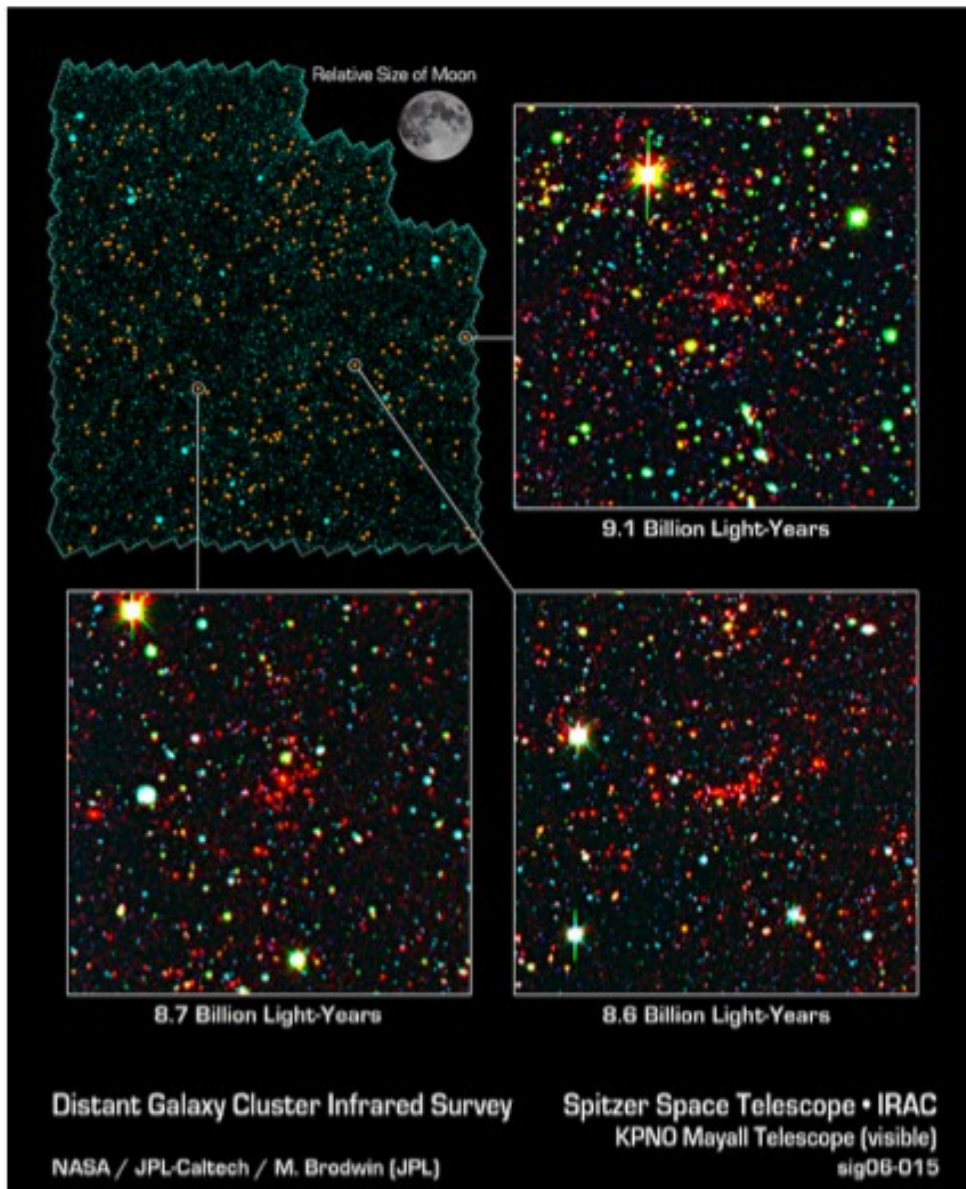
- ability to measure accurate stellar ages
- efficiency at obtaining spectra



# gE's as passively evolving, old systems

the most massive early-type galaxies are the oldest





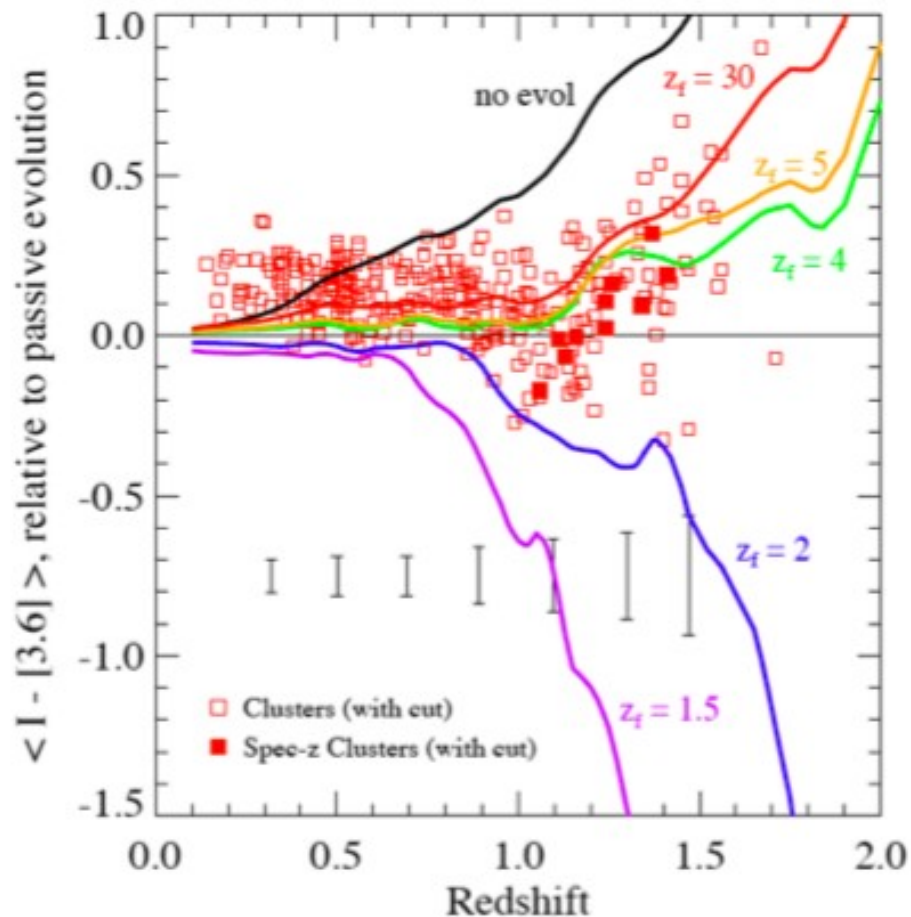
## IRAC Shallow Cluster Survey (Boötes field)

**14 confirmed**  
galaxy clusters at  $z > 1$

- Stanford et al. 2005, ApJL, 634, L129
- Elston et al. 2006, ApJ, 639, 816
- Brodwin et al. 2006, ApJ, 651,
- Brodwin et al. 2007, ApJL, 671, L93
- Eisenhardt et al., ApJ, submitted
- Galametz et al., in preparation

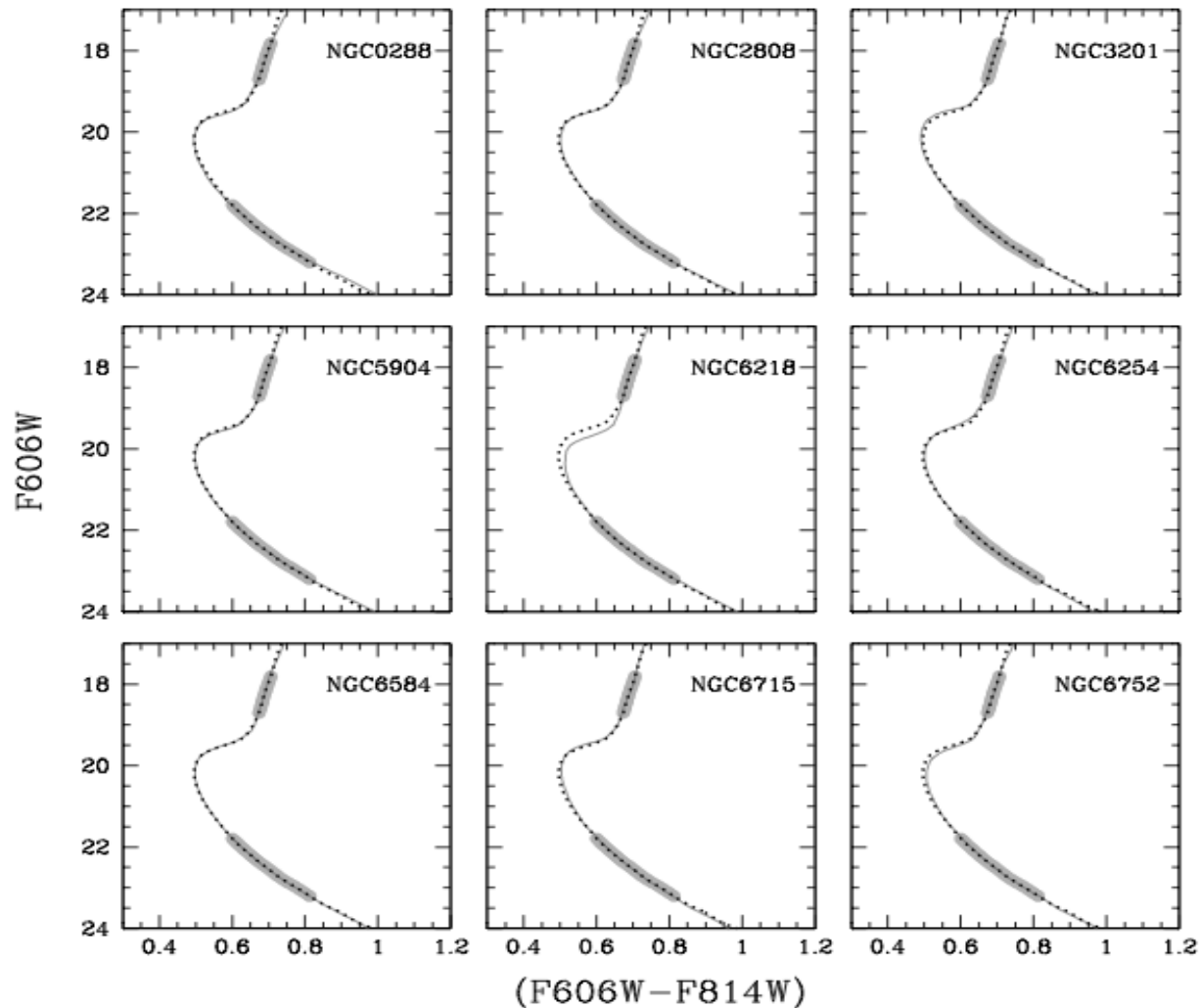
# gE's as passively evolving, old systems

colors indicate a high formation redshift (for cluster gE's)



# A Lesson from the past: Globular Cluster **RELATIVE AGES**

“This method provides relative ages to a formal precision of 2–7%. We demonstrate that the calculated relative ages are independent of the choice of theoretical model.” (0812.4541)







First attempt in 2004 ... failed at the proposal stage

2005 thru mid-2007 ... lots of bad weather

UT 2007 Aug 15-16

- Hurricane Flossie
- two earthquakes (5.4 & 4.0)
- fire
- tsunami warning

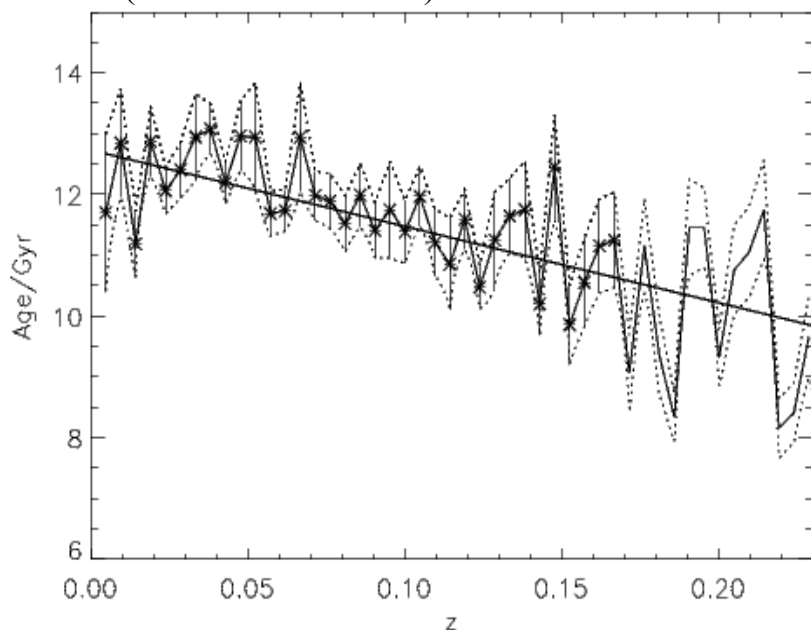


# Reconstruct $w(z)$ : **RELATIVE GALAXY AGES**

At  $z=0$   $dz/dt$  gives  $H_0$  and we have SDSS galaxies:

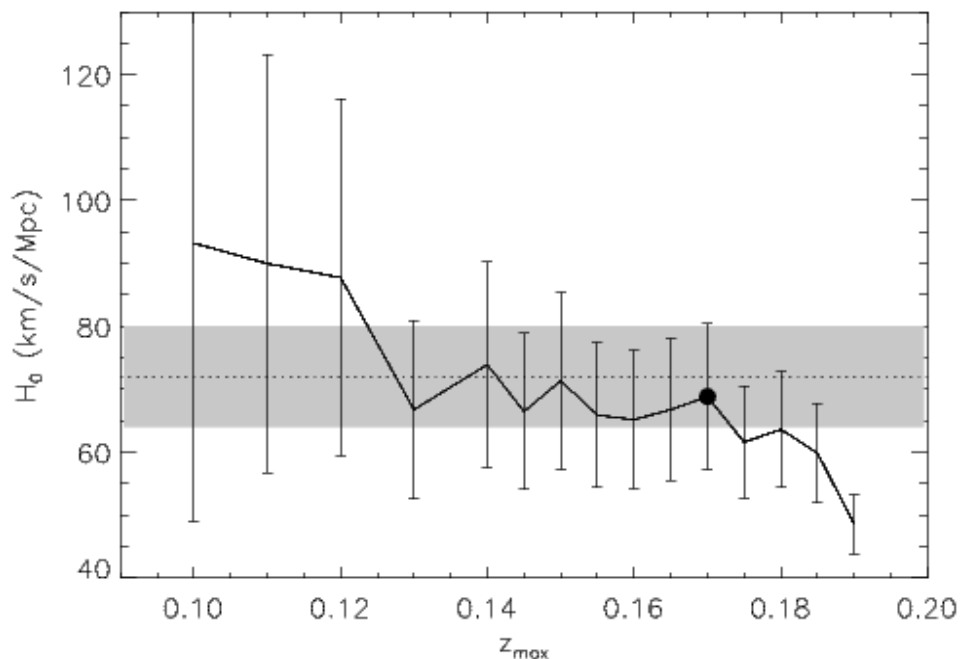
$$H(z) = -\frac{1}{(1+z)} \frac{dz}{dt}$$

(Jimenez et al. 2003)



**The edge for  $z < 0.2$**

(Jimenez et al. 2003)



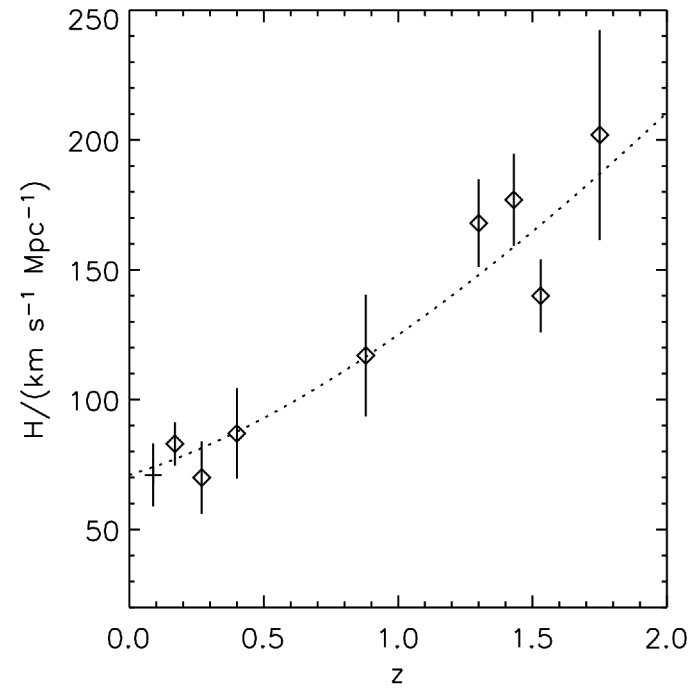
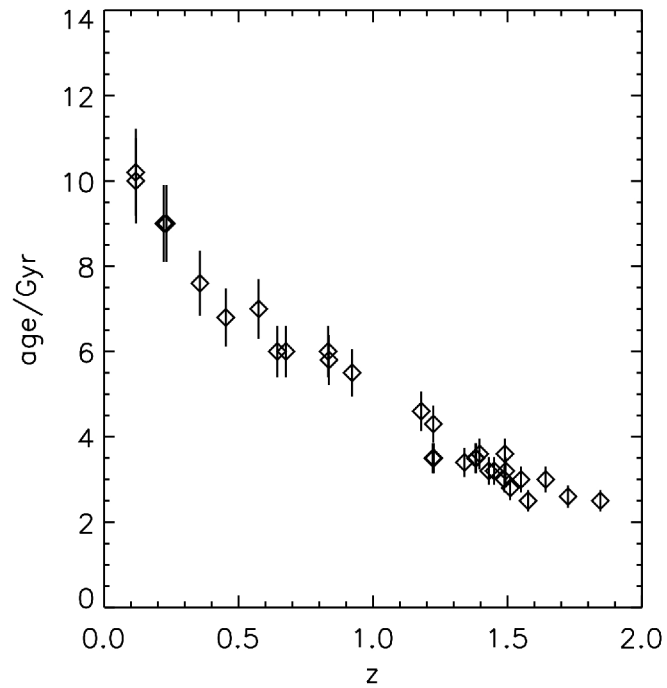
Similar trend found by Bernardi et al. (astro-ph/0509360) using alpha-enhanced models

**The value of  $H_0$**



# GDDS

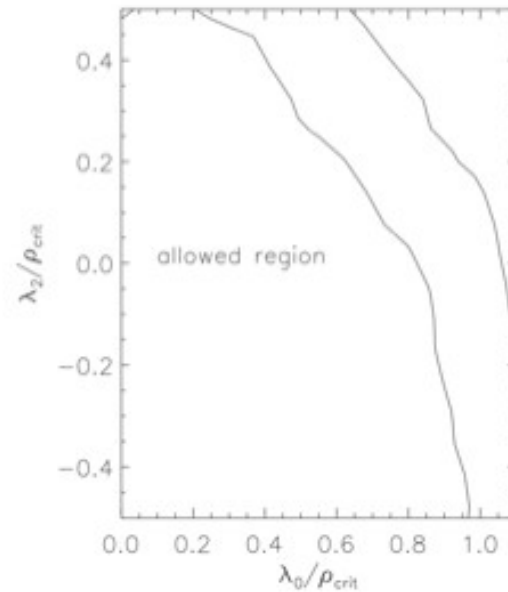
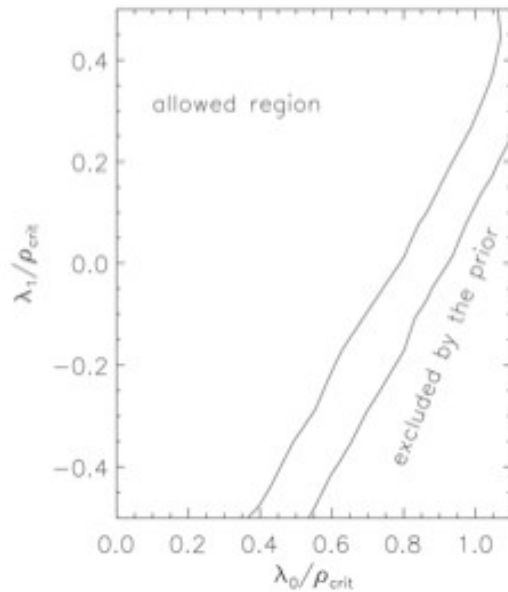
+high z radiogalaxies + Treu et al. 2000 sample



From Simon, Verde, RJ (2005)

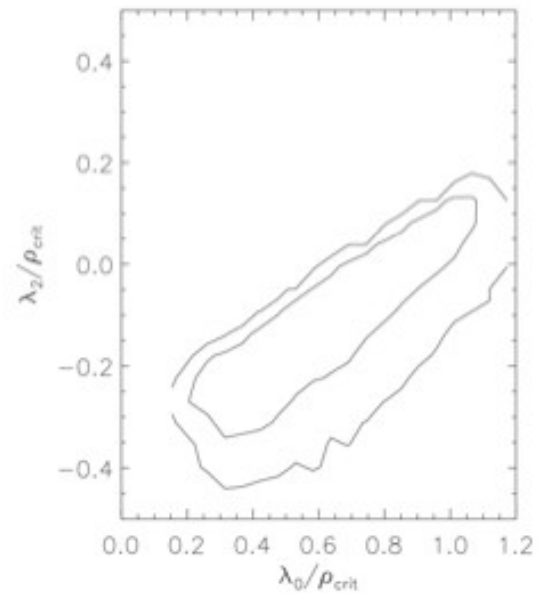
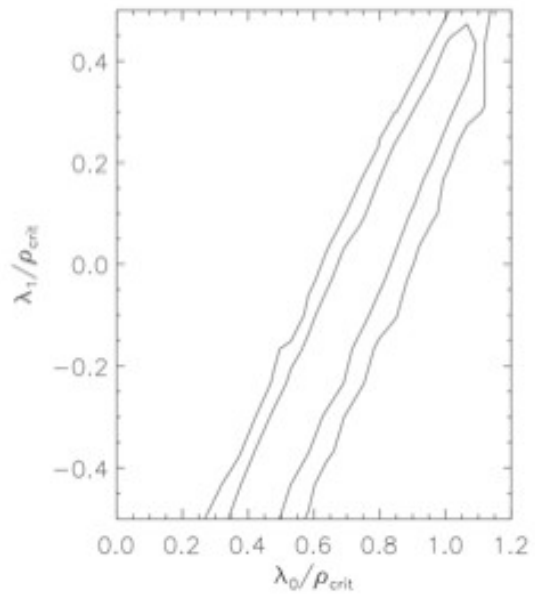
No data, priors only

$K > 0$      $\rho_T > 0$  that is  $H^2 > 0$      $V_0 + K_0 = \Omega_{Q,0}\rho_c$     Flatness

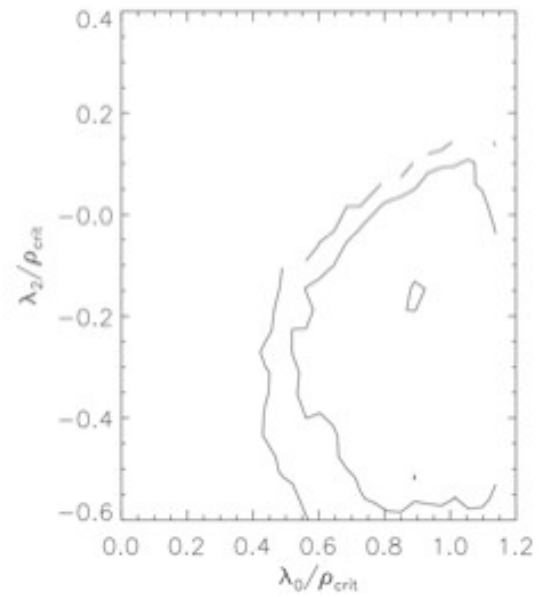
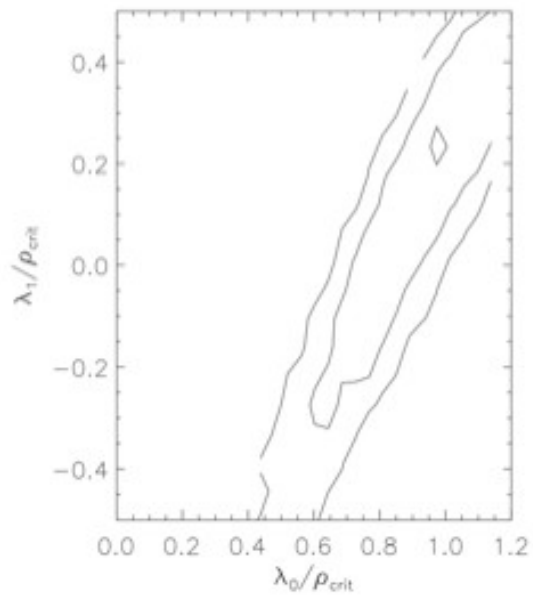


$\Omega_{m,0} = 0.27 \pm 0.07$     From large-scale structure !

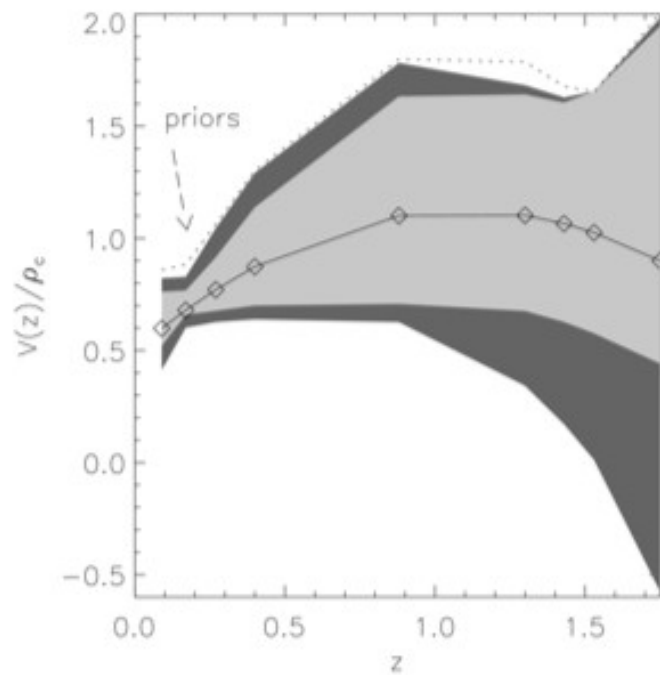
**As a benchmark let's consider the Supernovae**



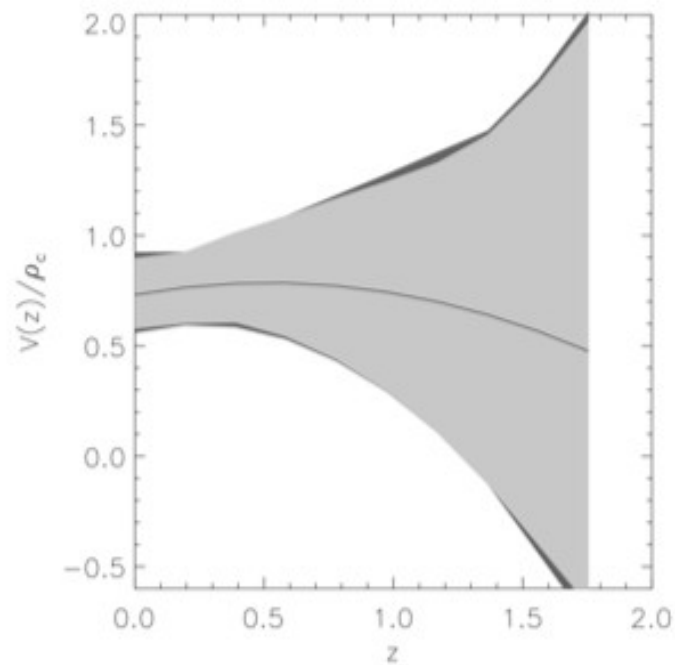
## Using galaxy ages



From Simon, Verde, RJ (2005)

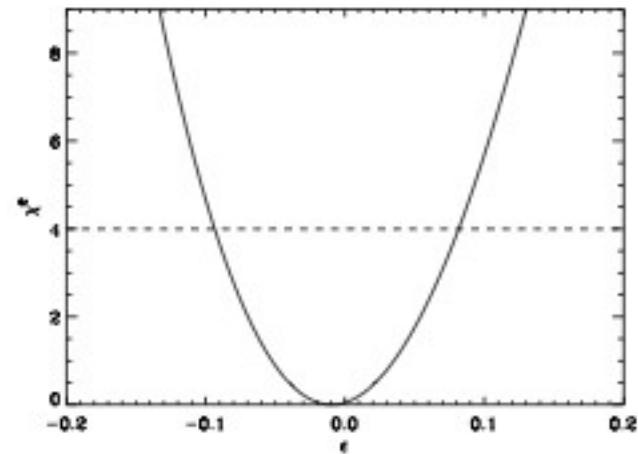
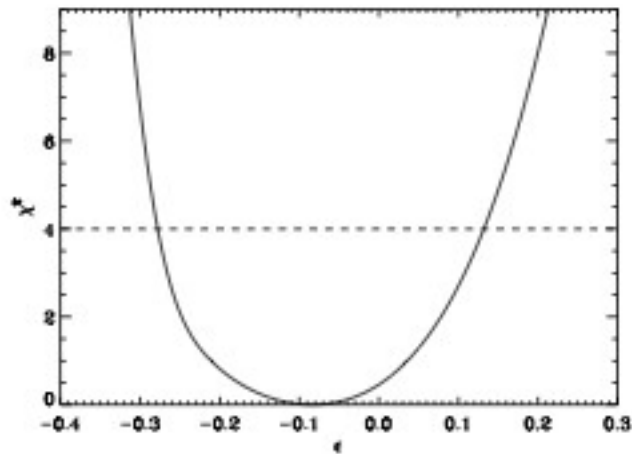


Galaxies

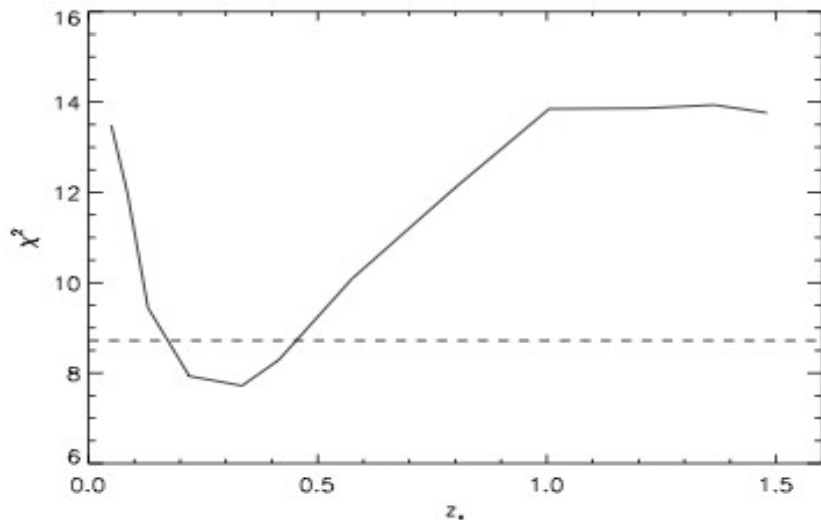


SN1A, Riess et al '04

# Multiple uses of $H(z)$

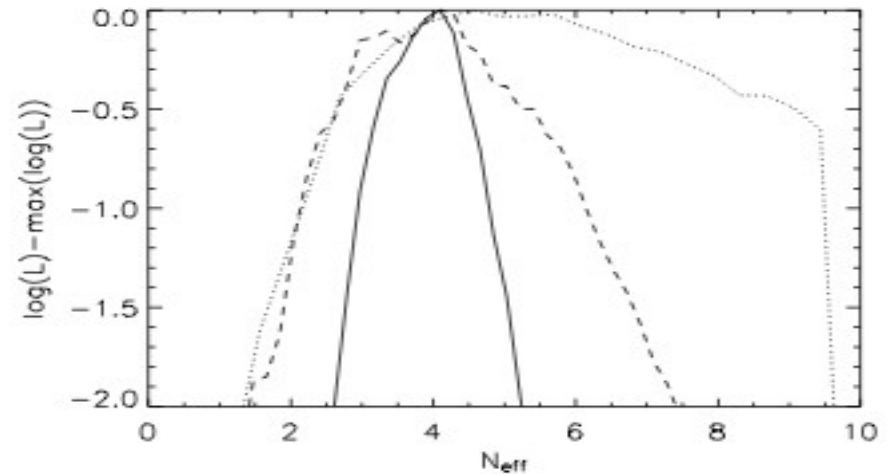
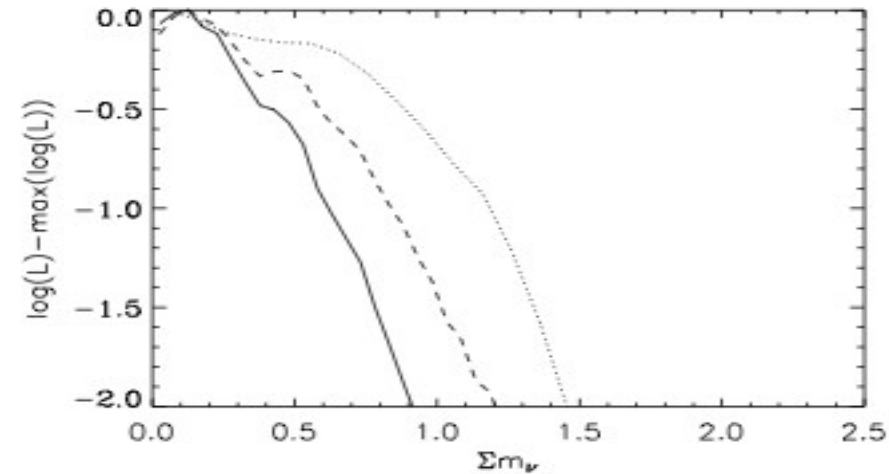


A factor 5 improvement on universe transparency (Avgoustidis, Verde, RJ  
arXiv:0902.2006)

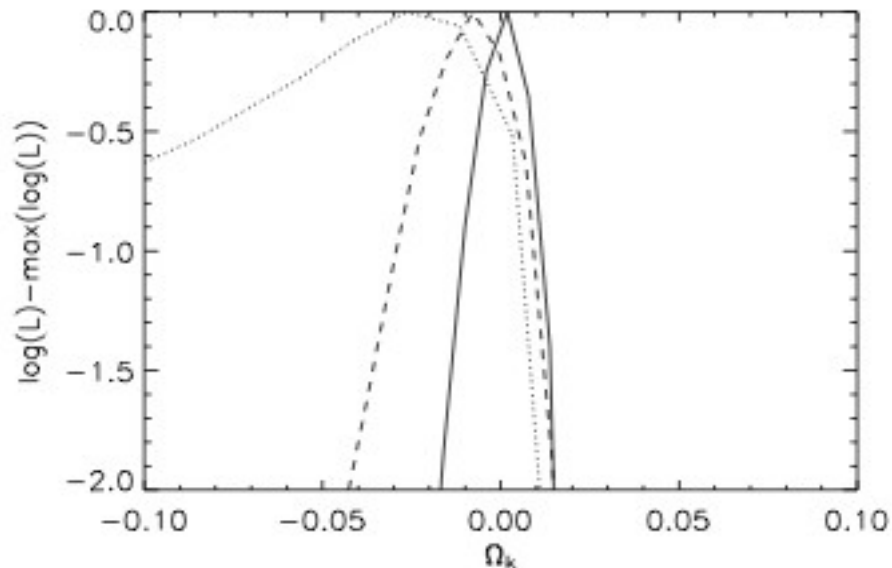


Detection of  
aceleration/deceleration  
(Avgoustidis, Verde, RJ  
arXiv:0902.2006)

# Multiple uses of $H(z)$



Constraints on the mass and number of relativistic particles (de Bernardis et al. JCAP0803:020,2008 Figueroa, Verde, RJ JCAP0810:038,2008) and on the curvature

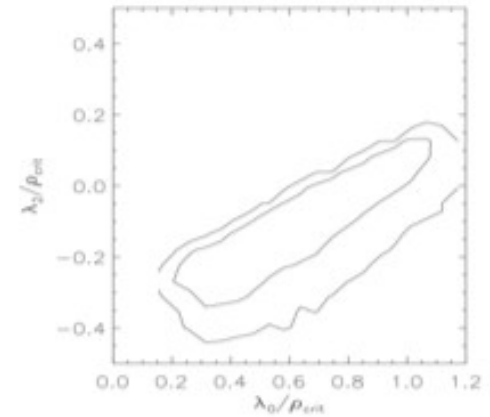
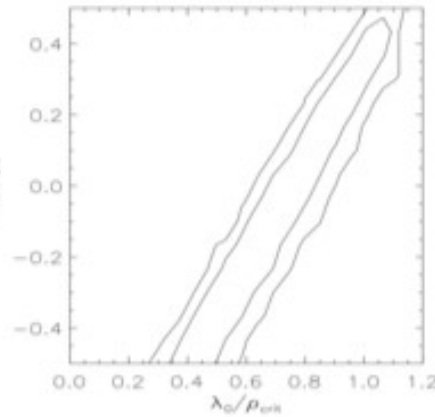


Simon, Verde, RJ '05

## Current constraints (SN)

$$3H^2(z) - \frac{1}{2}(1+z) \frac{dH^2(z)}{dz} = \kappa \left( V(\alpha_i, z) + \frac{1}{2} \rho_m(z) \right) \equiv g(\alpha_i, z)$$

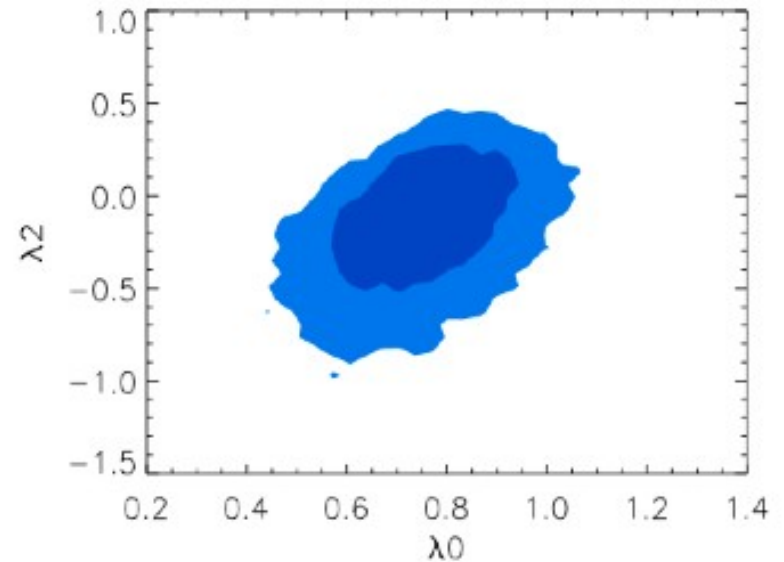
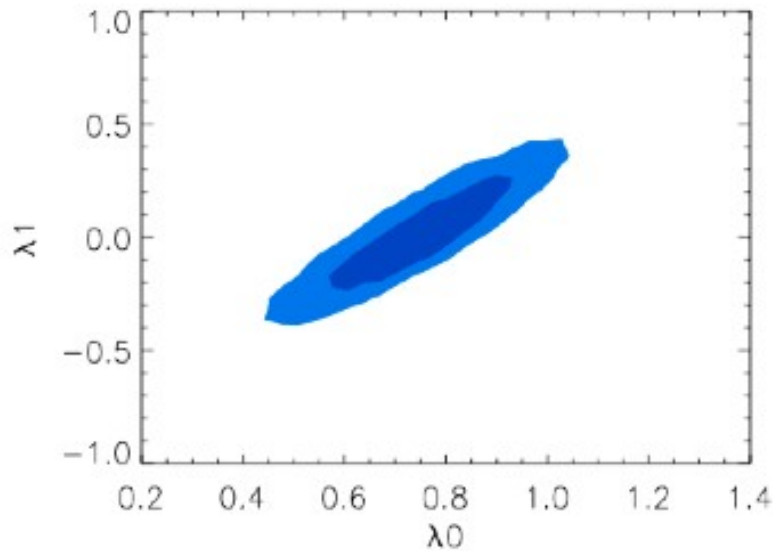
Use Chebyshev expansion of V



Fernandez-Martinez, Verde '08

# BOSS

(no flatness prior!)

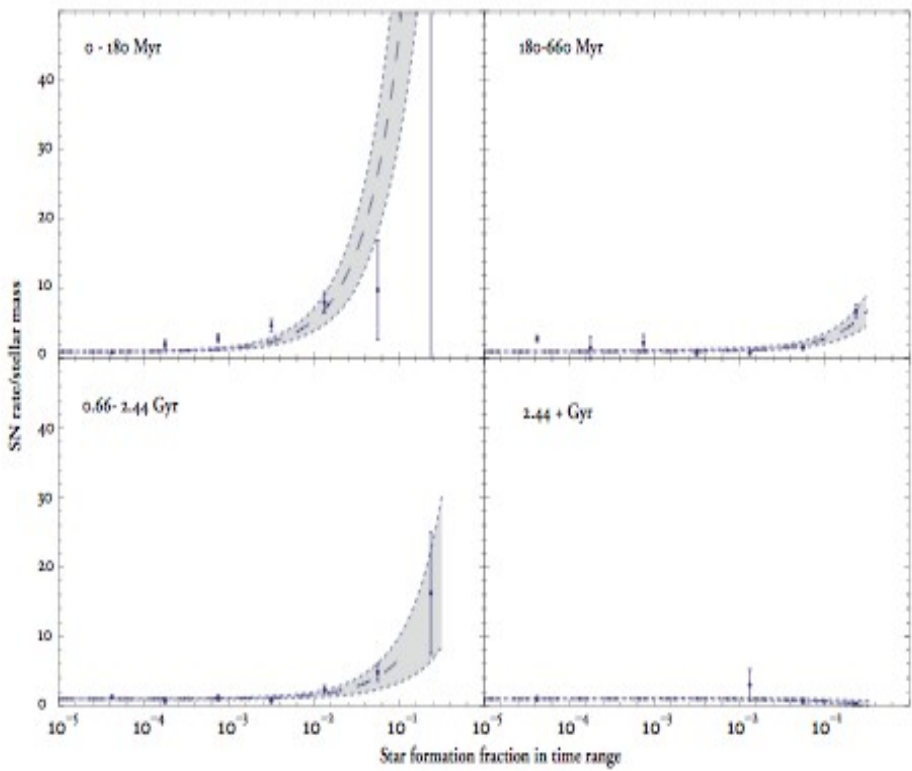




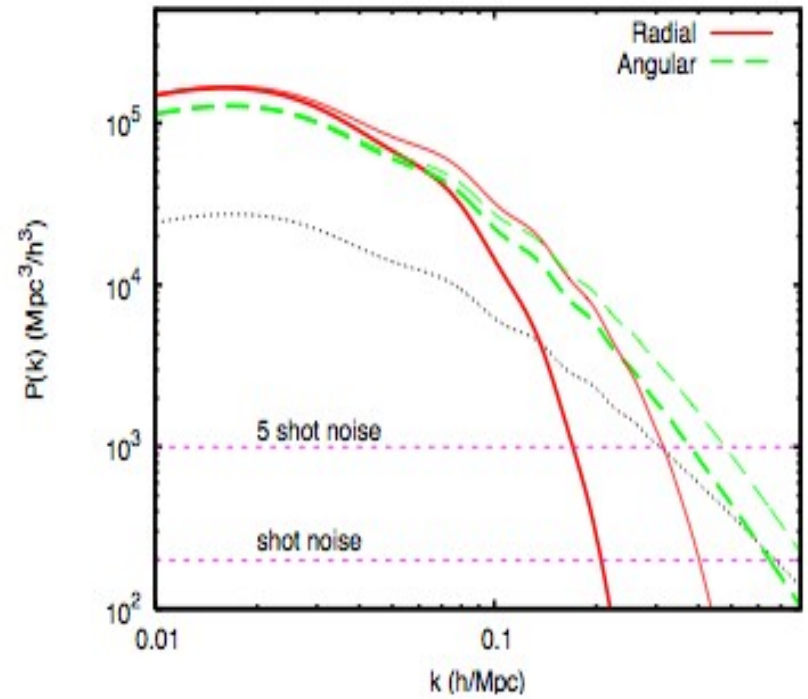
# The importance of having high S/N spectra

Spectra of SN Ia hosts may help to tighten the H diagram

If you want to do radial BAOs you do need spectra



Aubourg et al. (2008)



Roig et al. (2009)