

# RCFT ORIENTIFOLDS:

SU(5) GUTs



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GGI, APRIL 6 2009



# What we can compute

- Exact perturbative string spectra
- Gauge couplings in rational points
- RCFT instanton corrections

# What we can't do (yet)

- Compute Yukawa couplings
- Compute couplings to moduli
- Perturbations around rational points
- Moduli stabilization



# ORIENTIFOLD PARTITION FUNCTIONS

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● Closed  $\frac{1}{2} \left[ \sum_{ij} \chi_i(\tau) Z_{ij} \chi_i(\bar{\tau}) + \sum_i K_i \chi_i(2\tau) \right]$

● Open  $\frac{1}{2} \left[ \sum_{i,a,n} N_a N_b A^i_{ab} \chi_i\left(\frac{\tau}{2}\right) + \sum_{i,a} N_a M^i_a \hat{\chi}_i\left(\frac{\tau}{2} + \frac{1}{2}\right) \right]$

$i$  : Primary field label (finite range)

$a$  : Boundary label (finite range)

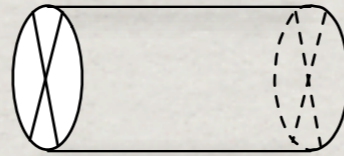
$\chi_i$  : Character

$N_a$  : Chan-Paton (CP) Multiplicity



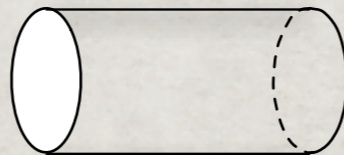
# COEFFICIENTS

● Klein bottle



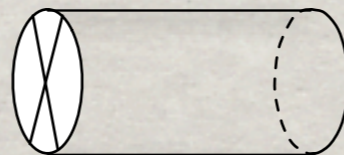
$$K^i = \sum_{m, J, J'} \frac{S_m^i U_{(m, J)} g_{J, J'}^{\Omega, m} U_{(m, J')}}{S_{0m}}$$

● Annulus



$$A_{[a, \psi_a][b, \psi_b]}^i = \sum_{m, J, J'} \frac{S_m^i R_{[a, \psi_a](m, J)} g_{J, J'}^{\Omega, m} R_{[b, \psi_b](m, J')}}{S_{0m}}$$

● Moebius



$$M_{[a, \psi_a]}^i = \sum_{m, J, J'} \frac{P_m^i R_{[a, \psi_a](m, J)} g_{J, J'}^{\Omega, m} U_{(m, J')}}{S_{0m}}$$

$$g_{J, J'}^{\Omega, m} = \frac{S_{m0}}{S_{mK}} \beta_K(J) \delta_{J', J^c}$$



# BOUNDARIES AND CROSSCAPS

## ● Boundary coefficients

$$R_{[a,\psi_a](m,J)} = \sqrt{\frac{|\mathcal{H}|}{|\mathcal{C}_a||\mathcal{S}_a|}} \psi_a^*(J) S_{am}^J$$

## ● Crosscap coefficients

$$U_{(m,J)} = \frac{1}{\sqrt{|\mathcal{H}|}} \sum_{L \in \mathcal{H}} e^{\pi i(h_K - h_{KL})} \beta_K(L) P_{LK,m} \delta_{J,0}$$

*Cardy (1989)*

*Sagnotti, Pradisi, Stanev (~1995)*

*Huiszoon, Fuchs, Schellekens, Schweigert, Walcher (2000)*



# ALGEBRAIC CHOICES

---

- Basic CFT (N=2 tensor (“Gepner Models”<sup>(1)</sup>, free fermions<sup>(2)</sup>...)
- Chiral algebra extension  
May imply space-time symmetry (e.g. Susy: GSO projection).  
**But this is optional!**  
Reduces number of characters.
- Modular Invariant Partition Function (MIPF)  
May imply bulk symmetry (e.g. Susy), not respected by all boundaries.  
Defines the set of boundary states  
(Sagnotti-Pradisi-Stanev completeness condition)
- Orientifold choice

## *Pioneering work:*

<sup>(1)</sup> Angelantonj, Bianchi, Pradisi, Sagnotti, Stanev, *Phys. Lett. B* 387 (1996) 743

Blumenhagen, Wiskirchen, *Phys. Lett. B* 438, 52 (1998), ....

<sup>(2)</sup> Bianchi, Sagnotti (1989-1991)

## *Standard Model Searches:*

<sup>(1)</sup> Dijkstra, Huiszoon, Schellekens, *Nucl.Phys.B*710:3-57,2005

Anastasopoulos, Dijkstra, Kiritsis, Schellekens, *Nucl.Phys.B*759:83-146,2006

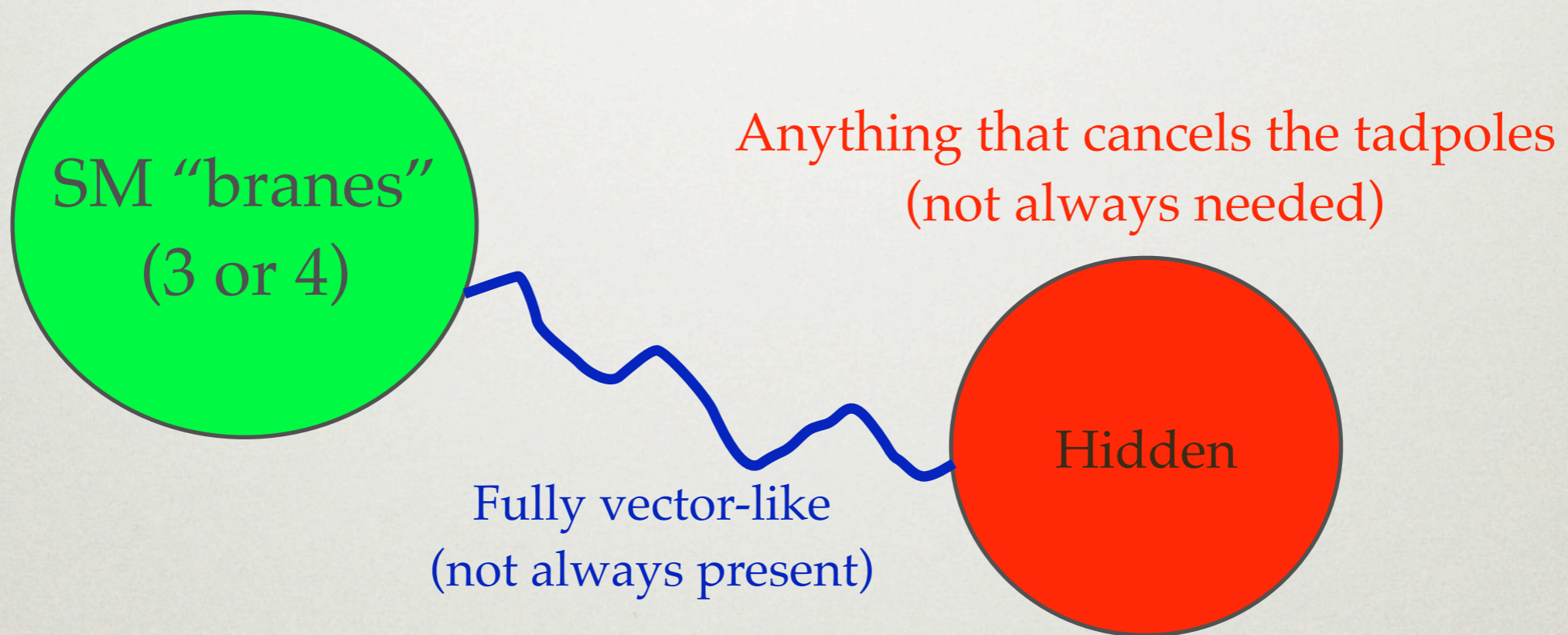
<sup>(2)</sup> Kiritsis, Lennek, Schellekens, *JHEP* 0902:030,2009.



# SM REALIZATION

---

3 families  
+ anything vector-like



Vector-like: mass allowed by  $SU(3) \times SU(2) \times U(1)$

Fully vector-like: mass allowed by all gauge symmetries



# CONSISTENCY CONDITIONS

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- Tadpole cancellation
- Absence of axion mixing for  $Y$
- Global anomalies\*

(Same as for all other orientifold models)

(\*) "Probe Branes" A.~M. Uranga *Nucl. Phys. B*598, 225 (2001)

B. Gato-Rivera and A.N Schellekens *Phys. Lett. B*632, 728 (2006)

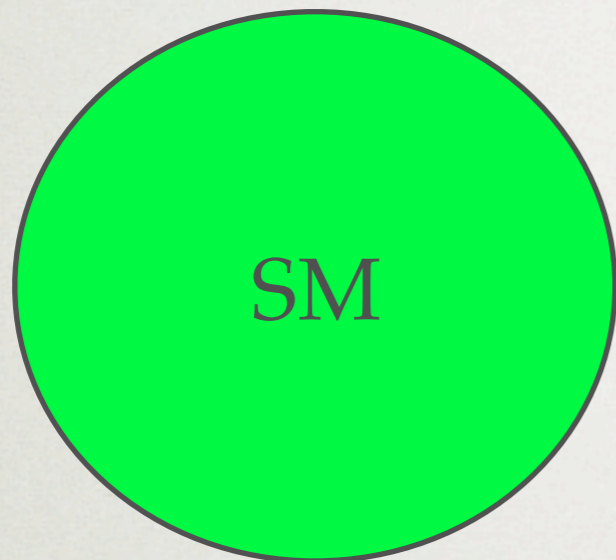


# DHS RESULTS

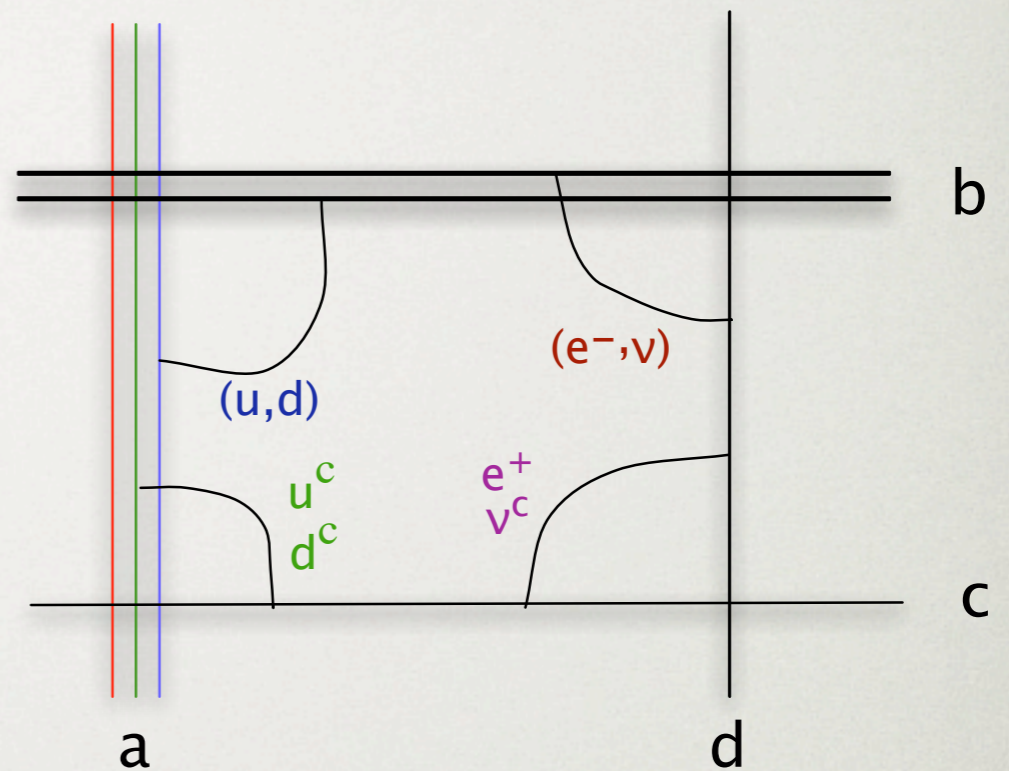
## (2004-2005)

Huiszoon, Dijkstra, Schellekens





=



210000 distinct tadpole-free spectra found

(without chiral exotics, but distinguished by non-chiral exotics)



Best imaginable result:

The exact MSSM spectrum



Gauge group:  $U(3) \times Sp(2) \times U(1) \times U(1)$

Q U D L E	7 x	(V , V , 0 , 0 )	chirality 3
	3 x	(V , 0 , V , 0 )	chirality -3
	3 x	(V , 0 , V* , 0 )	chirality -3
	9 x	(0 , V , 0 , V )	chirality 3
	5 x	(0 , 0 , V , V )	chirality -3
	3 x	(0 , 0 , V , V* )	chirality 3
H	6 x	(V , 0 , 0 , V )	
	10 x	(0 , V , V , 0 )	
	2 x	(Ad , 0 , 0 , 0 )	
	2 x	(A , 0 , 0 , 0 )	
	6 x	(S , 0 , 0 , 0 )	
	14 x	(0 , A , 0 , 0 )	
	10 x	(0 , S , 0 , 0 )	
	9 x	(0 , 0 , Ad , 0 )	
	6 x	(0 , 0 , A , 0 )	
	14 x	(0 , 0 , S , 0 )	
	3 x	(0 , 0 , 0 , Ad)	
	4 x	(0 , 0 , 0 , A )	
6 x	(0 , 0 , 0 , S )		

$$Y = \frac{1}{6}Q_a - \frac{1}{2}Q_c - \frac{1}{2}Q_d$$

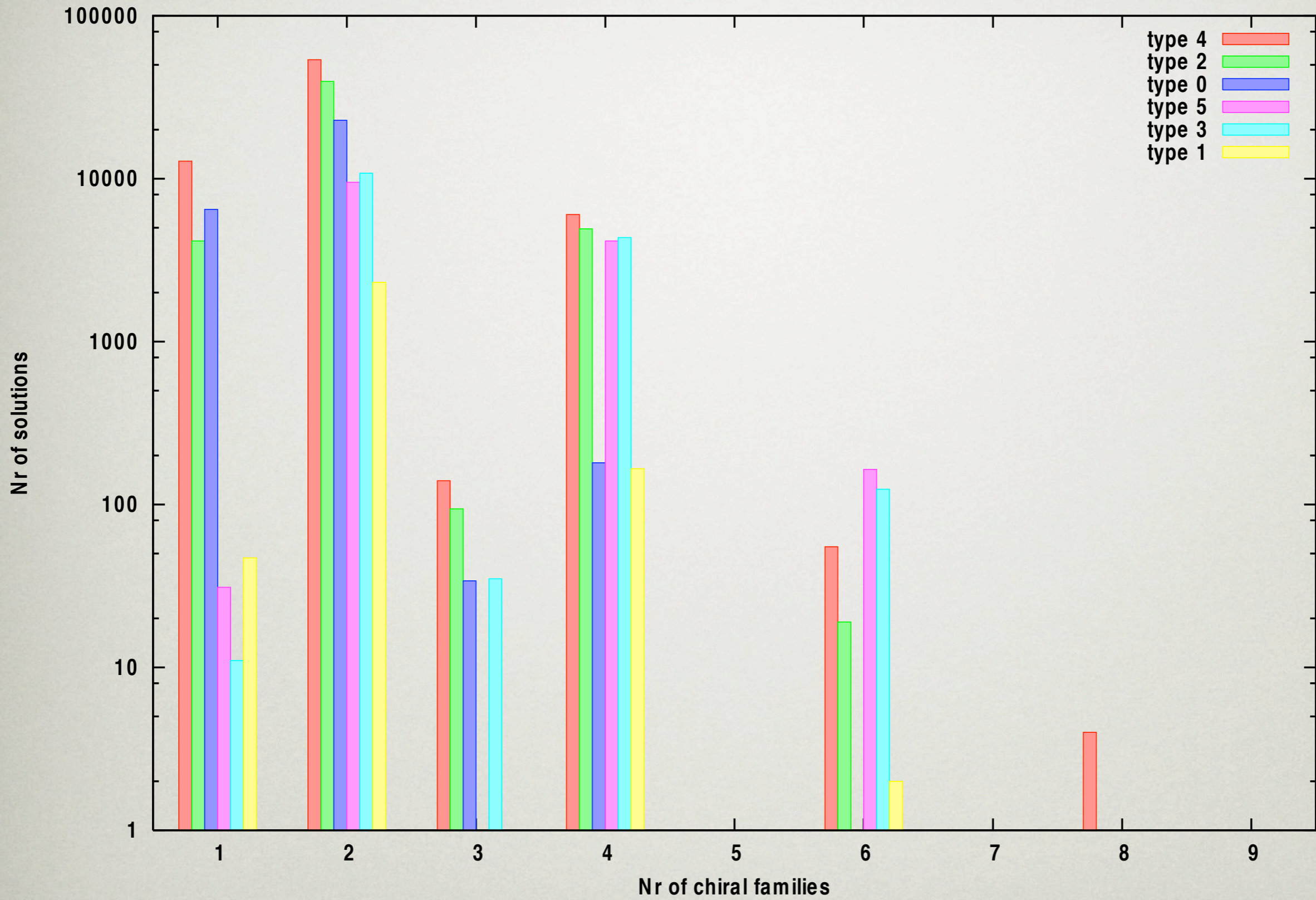
No hidden sector

B-L Massive (axion mixing)

Gauge group:

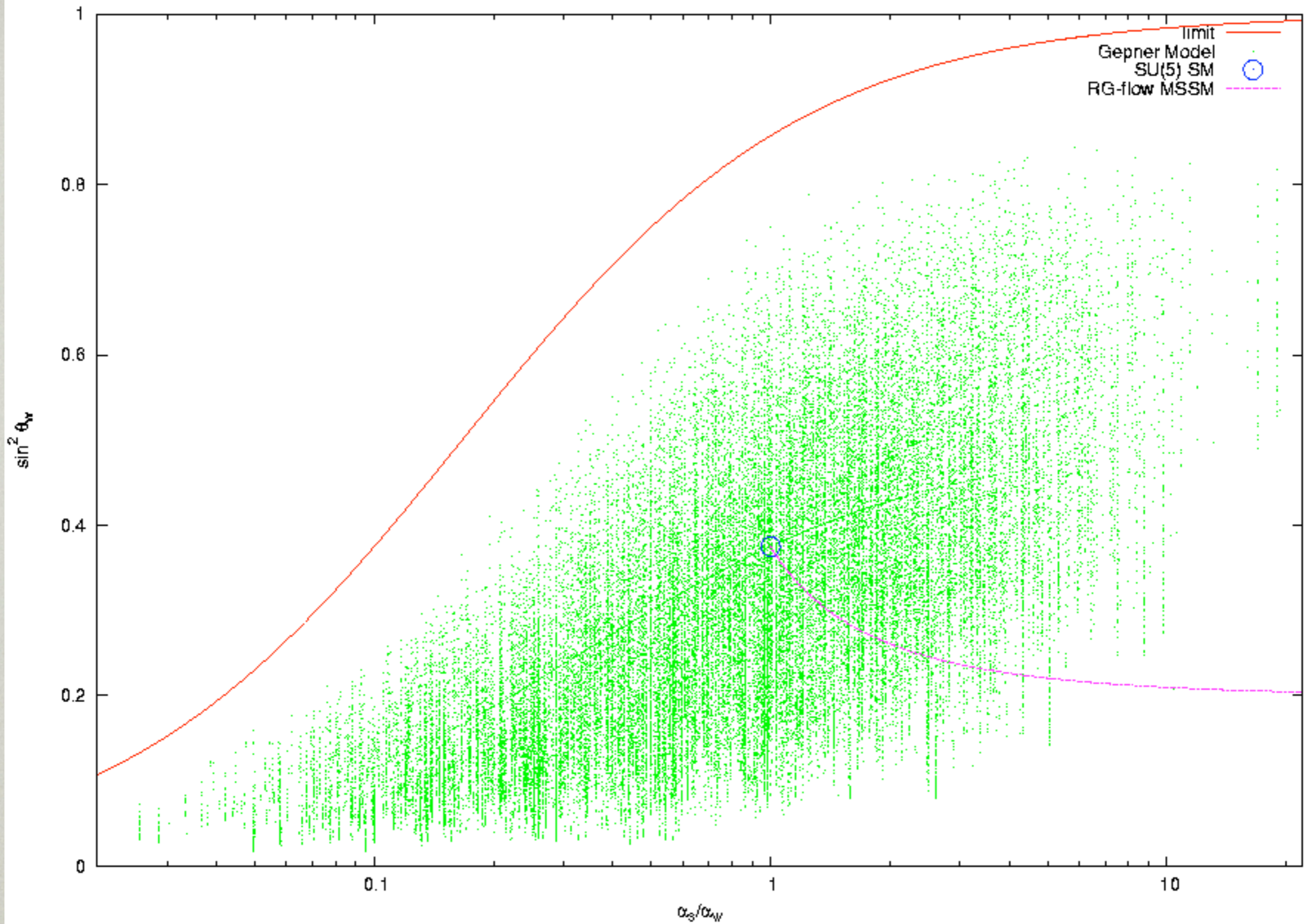
Exactly  $SU(3) \times SU(2) \times U(1)$





*cf. Gmeiner et. al.*





Dijkstra, Huiszoon, Schellekens, **Nucl.Phys.B710:3-57,2005**



# ADKS RESULTS (2005-2006)

Anastasopoulos, Dijkstra, Kiritsis, Schellekens



# SEARCH CRITERIA

Require only:

- $U(3)$  from a single brane
- $U(2)$  from a single brane
- Quarks and leptons,  $Y$  from at most four branes
- $G_{CP} \supset SU(3) \times SU(2) \times U(1)$
- Chiral  $G_{CP}$  fermions reduce to quarks, leptons (plus non-chiral particles)
- Massless  $Y$



# CHAN-PATON GROUP

$$G_{CP} = U(3)_a \times \left\{ \begin{array}{l} U(2)_b \\ Sp(2)_b \end{array} \right\} \times G_c \quad (\times G_d)$$

Embedding of Y:

$$Y = \alpha Q_a + \beta Q_b + \gamma Q_c + \delta Q_d + W_c + W_d$$

Q: Brane charges (for unitary branes)

W: Traceless generators



# CLASSIFICATION

$$Y = \left(x - \frac{1}{3}\right)Q_a + \left(x - \frac{1}{2}\right)Q_b + \underbrace{xQ_c + (x - 1)Q_d}_{\text{Distributed over c and d}}$$

Distributed over  
c and d

Allowed values for  $x$

1/2	Madrid model, Pati-Salam, Flipped SU(5)
0	(broken) SU(5)
1	Antoniadis, Kiritsis, Tomaras model
-1/2, 3/2	
any	Trinification ( $x = 1/3$ ) (orientable)



# RESULTS

- 19345 chirally distinct spectra  
*(19 of Madrid type)*
- 1900 distinct ones with tadpole solutions



# RESULTS

- 19345 chirally distinct spectra  
(19 of Madrid type)
- 1900 distinct ones with tadpole solutions  
( $\approx 1900$  distinct hep-th papers)



# STATISTICS

Value of $x$	Total
0	24483441
$1/2$	138837612
1	30580
$-1/2, 3/2$	0
any	1250080



# A CURIOSITY

Gauge group  $SU(3) \times SU(2) \times U(1) \times [U(2)_{\text{Hidden}}]$

	U3	S2	U1	U1	U2		
3 x	( V	,V	,0	,0	,0 )	chirality 3	Q
3 x	( 0	,0	,V	,V	,0 )	chirality -3	E*
1 x	( V	,0	,0	,V*	,0 )	chirality -1	U*
2 x	( V	,0	,V	,0	,0 )	chirality -2	D*
2 x	( 0	,V	,0	,V	,0 )	chirality 2	L
3 x	( V	,0	,0	,V	,0 )	chirality -1	D*+(D+D*)
3 x	( 0	,V	,V	,0	,0 )	chirality 1	L+H <sub>1</sub> +H <sub>2</sub>
2 x	( V	,0	,V*	,0	,0 )	chirality -2	U*
1 x	( 0	,0	,V	,V*	,0 )	chirality 1	N*
4 x	( A	,0	,0	,0	,0 )		U+U*
2 x	( 0	,0	,0	,S	,0 )		E+E*



# A CURIOSITY

Gauge group  $SU(3) \times SU(2) \times U(1) \times [U(2)_{\text{Hidden}}]$

	U3	S2	U1	U1	U2		
3 x	( V	,V	,0	,0	,0 )	chirality 3	Q
3 x	( 0	,0	,V	,V	,0 )	chirality -3	E*
1 x	( V	,0	,0	,V*	,0 )	chirality -1	U*
2 x	( V	,0	,V	,0	,0 )	chirality -2	D*
2 x	( 0	,V	,0	,V	,0 )	chirality 2	L
3 x	( V	,0	,0	,V	,0 )	chirality -1	D*+(D+D*)
3 x	( 0	,V	,V	,0	,0 )	chirality 1	L+H <sub>1</sub> +H <sub>2</sub>
2 x	( V	,0	,V*	,0	,0 )	chirality -2	U*
1 x	( 0	,0	,V	,V*	,0 )	chirality 1	N*
4 x	( A	,0	,0	,0	,0 )		U+U*
2 x	( 0	,0	,0	,S	,0 )		E+E*

↑  
Truly hidden  
hidden sector



# A CURIOSITY

Gauge group  $SU(3) \times SU(2) \times U(1) \times [U(2)_{\text{Hidden}}]$

	U3	S2	U1	U1	U2		
3 x	( V	,V	,0	,0	,0 )	chirality 3	Q
3 x	( 0	,0	,V	,V	,0 )	chirality -3	E*
1 x	( V	,0	,0	,V*	,0 )	chirality -1	U*
2 x	( V	,0	,V	,0	,0 )	chirality -2	D*
2 x	( 0	,V	,0	,V	,0 )	chirality 2	L
3 x	( V	,0	,0	,V	,0 )	chirality -1	D*+(D+D*)
3 x	( 0	,V	,V	,0	,0 )	chirality 1	L+H <sub>1</sub> +H <sub>2</sub>
2 x	( V	,0	,V*	,0	,0 )	chirality -2	U*
1 x	( 0	,0	,V	,V*	,0 )	chirality 1	N*
4 x	( A	,0	,0	,0	,0 )		U+U*
2 x	( 0	,0	,0	,S	,0 )		E+E*

Free-field realization with (2)<sup>6</sup> Gepner model

(Kiritsis, Schellekens, Tsulaia, arXiv:0809.0083)



# MOST FREQUENT MODELS

nr	Total occ.	MIPFs	Chan-Paton Group	spectrum	x	Solved
1	9801844	648	$U(3) \times Sp(2) \times Sp(6) \times U(1)$	VVVV	1/2	Y!
2	8479808(16227372)	675	$U(3) \times Sp(2) \times Sp(2) \times U(1)$	VVVV	1/2	Y!
3	5775296	821	$U(4) \times Sp(2) \times Sp(6)$	VVV	1/2	Y!
4	4810698	868	$U(4) \times Sp(2) \times Sp(2)$	VVV	1/2	Y!
5	4751603	554	$U(3) \times Sp(2) \times O(6) \times U(1)$	VVVV	1/2	Y!
6	4584392	751	$U(4) \times Sp(2) \times O(6)$	VVV	1/2	Y
7	4509752(9474494)	513	$U(3) \times Sp(2) \times O(2) \times U(1)$	VVVV	1/2	Y!
8	3744864	690	$U(4) \times Sp(2) \times O(2)$	VVV	1/2	Y!
9	3606292	467	$U(3) \times Sp(2) \times Sp(6) \times U(3)$	VVVV	1/2	Y
10	3093933	623	$U(6) \times Sp(2) \times Sp(6)$	VVV	1/2	Y
11	2717632	461	$U(3) \times Sp(2) \times Sp(2) \times U(3)$	VVVV	1/2	Y!
12	2384626	560	$U(6) \times Sp(2) \times O(6)$	VVV	1/2	Y
13	2253928	669	$U(6) \times Sp(2) \times Sp(2)$	VVV	1/2	Y!
14	1803909	519	$U(6) \times Sp(2) \times O(2)$	VVV	1/2	Y!
15	1676493	517	$U(8) \times Sp(2) \times Sp(6)$	VVV	1/2	Y
16	1674416	384	$U(3) \times Sp(2) \times O(6) \times U(3)$	VVVV	1/2	Y
17	1654086	340	$U(3) \times Sp(2) \times U(3) \times U(1)$	VVVV	1/2	Y
18	1654086	340	$U(3) \times Sp(2) \times U(3) \times U(1)$	VVVV	1/2	Y
19	1642669	360	$U(3) \times Sp(2) \times Sp(6) \times U(5)$	VVVV	1/2	Y
20	1486664	346	$U(3) \times Sp(2) \times O(2) \times U(3)$	VVVV	1/2	Y!
21	1323363	476	$U(8) \times Sp(2) \times O(6)$	VVV	1/2	Y
22	1135702	350	$U(3) \times Sp(2) \times Sp(2) \times U(5)$	VVVV	1/2	Y!
23	1050764	532	$U(8) \times Sp(2) \times Sp(2)$	VVV	1/2	Y
24	956980	421	$U(8) \times Sp(2) \times O(2)$	VVV	1/2	Y
25	950003	449	$U(10) \times Sp(2) \times Sp(6)$	VVV	1/2	Y
26	910132	51	$U(3) \times U(2) \times Sp(2) \times O(1)$	AAVV	0	Y
...						



# CURIOSITIES

nr	Total occ.	MIPFs	Chan-Paton Group	Spectrum	x	Solved
617	16845	296	$U(5) \times O(1)$	AV	0	Y
671	14744(*)	29	$U(3) \times U(2) \times U(1) \times U(1)$	VVVV	1/2	
761	12067	26	$U(3) \times U(2) \times U(1)$	AAS	1/2	Y!
762	12067	26	$U(3) \times U(2) \times U(1)$	AAS	0	Y!
1024	7466	7	$U(3) \times U(2) \times U(2) \times U(1)$	VAAV	1	
1125	6432	87	$U(3) \times U(3) \times U(3)$	VVV	*	Y
1201	5764(*)	20	$U(3) \times U(2) \times U(1) \times U(1)$	VVVV	1/2	
1356	5856(*)	10	$U(3) \times U(2) \times U(1) \times U(1)$	VVVV	1/2	Y
1725	2864	14	$U(3) \times U(2) \times U(1) \times U(1)$	VVVV	1/2	Y
1886	2381	115	$U(6) \times Sp(2)$	AV	1/2	Y!
1887	2381	115	$U(6) \times Sp(2)$	AV	0	Y!
1888	2381	115	$U(6) \times Sp(2)$	AV	1/2	Y!
2624	1248	3	$U(3) \times U(2) \times U(2) \times U(3)$	VAAV	1	
2753	1136	74	$U(5) \times U(1)$	AS	0	Y
2880	1049	34	$U(5) \times U(1)$	AS	1/2	Y!
2881	1049	34	$U(5) \times U(1)$	AS	0	Y!
6580	146	18	$U(5) \times U(1)$	AS	0	
14861	12	2	$U(5) \times U(1)$	AS	0	



# GUTS

*(with M. Lennek, E. Kiritsis)*



# GUTs vs. STRINGS

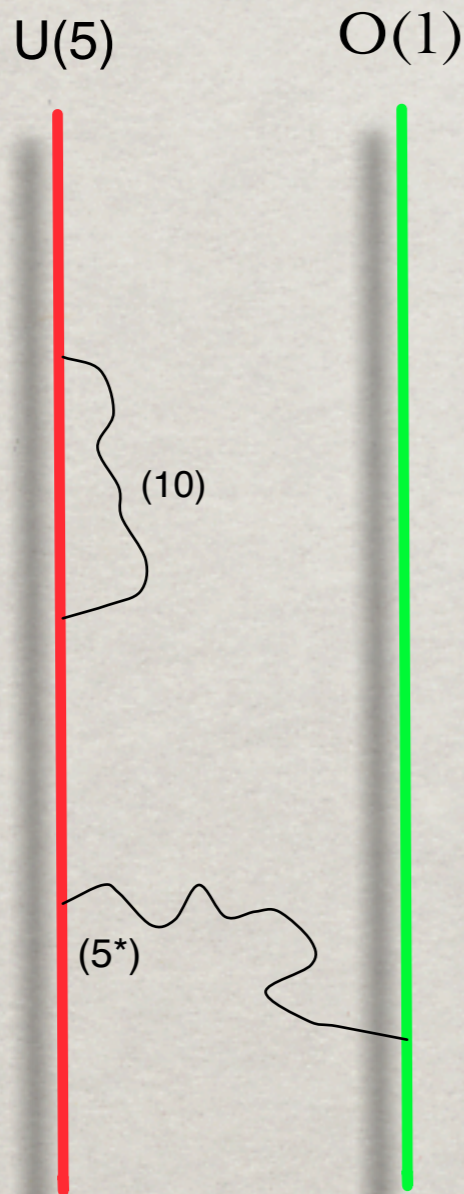
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- Heterotic (affine level 1)
  - + Naturally (16)'s of SO(10) or 27's of E6
  - No adjoints
  - Wrong scale
  - Fractional charges
- Heterotic (higher level)
  - + Adjoint breaking, no fractional charges
  - Statistically challenged
  - Higher representations allowed
- Orientifolds ( $x=1/2$ )
  - + Scale adjustable
  - No coupling unification
  - No SU(5), SO(10)
  - Higher representations allowed
  - Half-integer charges often present
- Orientifolds ( $x=0$ )
  - + Standard SU(5) GUT possible  
(adjoint breaking, no fractional charges)
  - Statistically challenged
  - Higher reps allowed (15)
  - No top Yukawa's perturbatively
- ....



# MODEL NR. 617

*Gauge group is just SU(5)!*



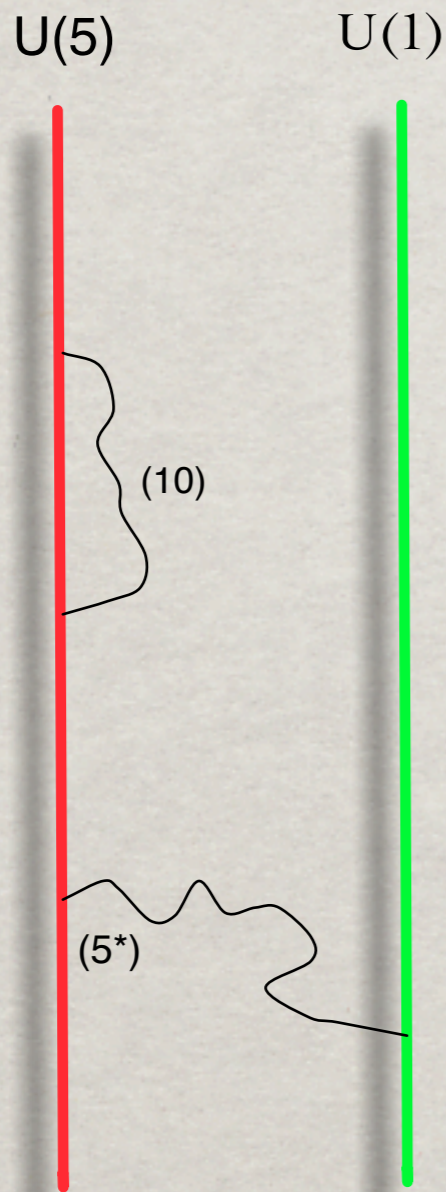
	U5	O1	O1	
3 x	(A ,0	,0	)	chirality 3
11 x	(V ,V	,0	)	chirality -3
8 x	(S ,0	,0	)	
3 x	(Ad ,0	,0	)	
1 x	(0 ,A	,0	)	
3 x	(0 ,V	,V	)	
8 x	(V ,0	,V	)	
2 x	(0 ,S	,0	)	
4 x	(0 ,0	,S	)	
4 x	(0 ,0	,A	)	

Hidden sector



# MODEL NR. 2880

Gauge group is  $SU(5) \times U(1)$



**U5 U1**

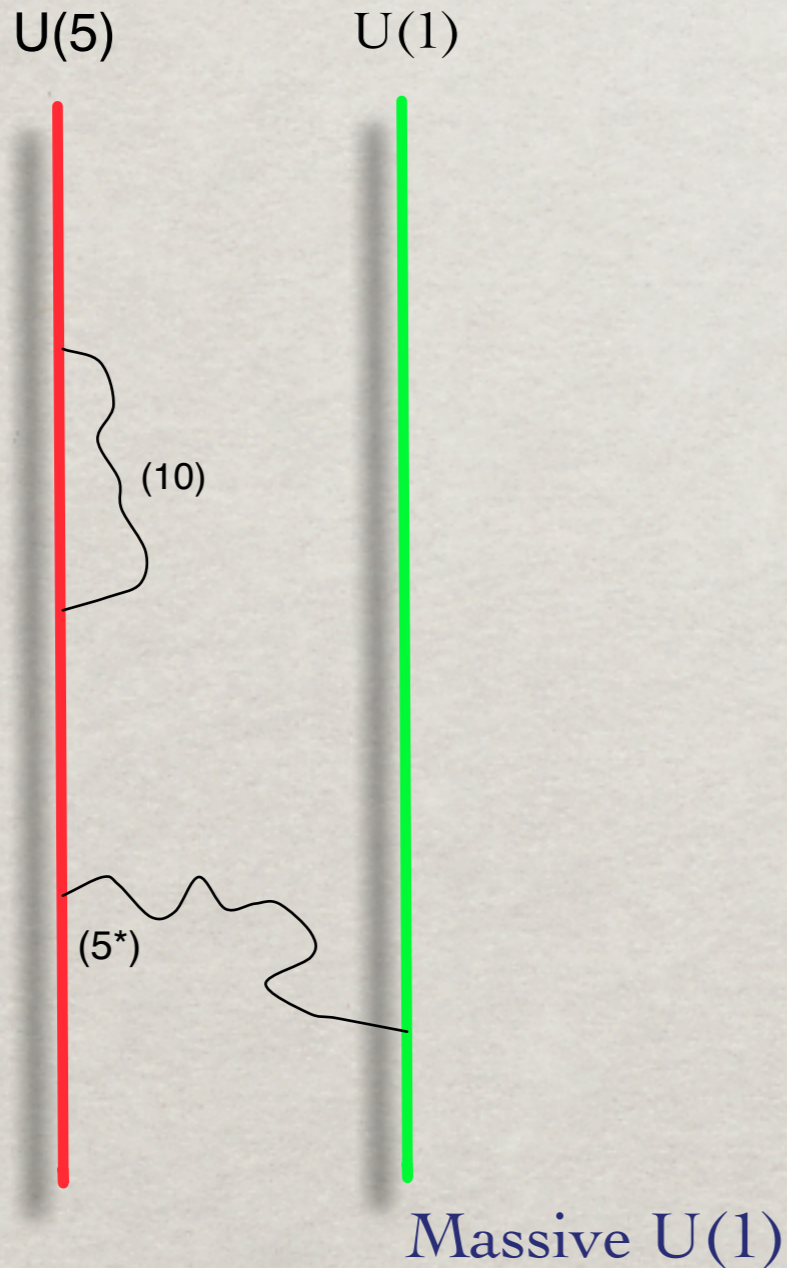
11 x	( 0 ,S )	chirality 3
3 x	( A ,0 )	chirality 3
5 x	( V ,V )	chirality -3
8 x	( S ,0 )	chirality 0
9 x	( Ad,0 )	chirality 0
5 x	( 0 ,Ad)	chirality 0
4 x	( 0 ,A )	chirality 0
12 x	( V ,V*)	chirality 0

Massless U(1)  
Allows flipped SU(5)

No hidden sector!



# MODEL NR. 2753



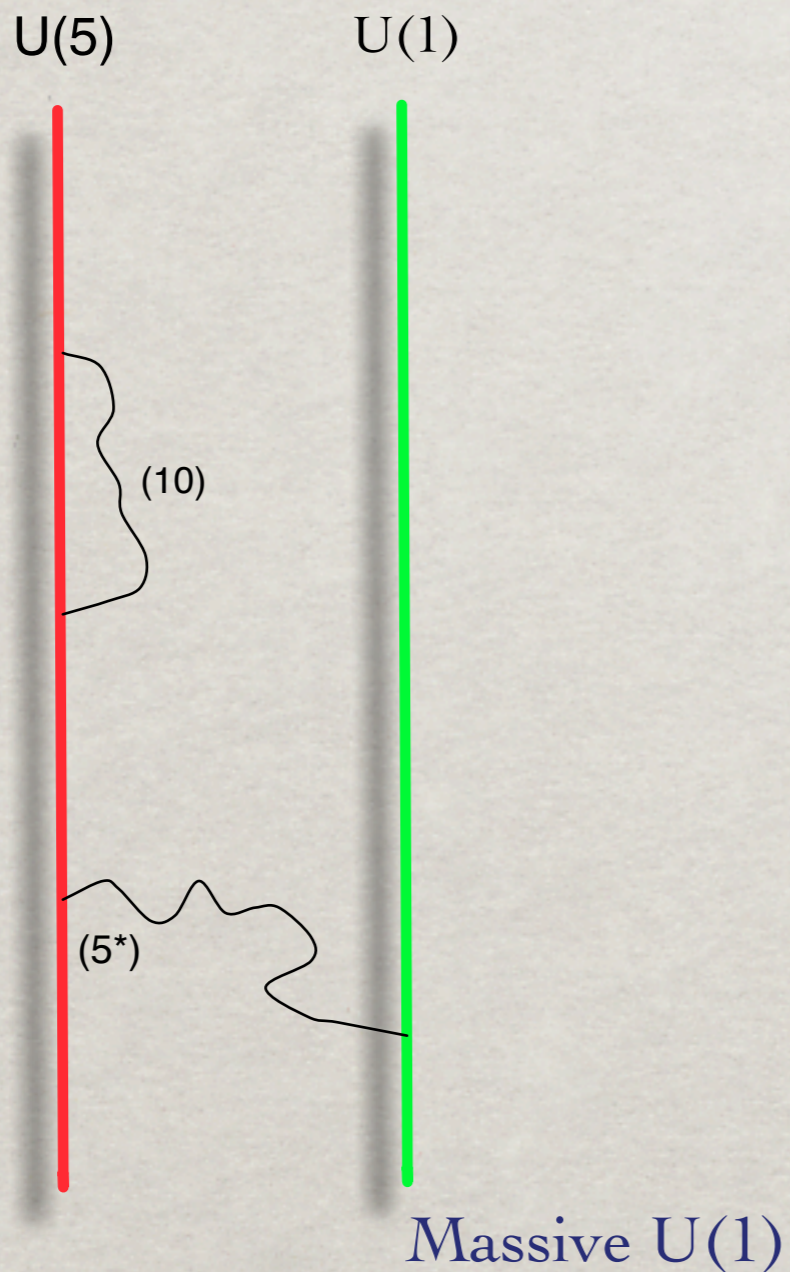
U5 U1 O2 U2 O2 U5 S4 U1 U1

7 x ( 0 , S , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 3
3 x ( A , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 3
3 x ( V , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality -3
2 x ( S , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 0
2 x ( 0 , A , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 0
3 x ( Ad , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 0
2 x ( 0 , Ac , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 0
4 x ( 0 , V , 0 , 0 , V , 0 , 0 , 0 , 0 )	chirality 0
2 x ( V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V* )	chirality 0
4 x ( V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V )	chirality 0
2 x ( V , 0 , 0 , 0 , 0 , V , 0 , 0 , 0 )	chirality 0
2 x ( V , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 )	chirality 0
2 x ( V , 0 , 0 , 0 , 0 , 0 , 0 , V* , 0 )	chirality 0
2 x ( V , V* , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 0
2 x ( 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , V* )	chirality 0
3 x ( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , A )	chirality -1
1 x ( 0 , 0 , 0 , 0 , 0 , 0 , 0 , S , 0 )	chirality 1
1 x ( 0 , 0 , 0 , V , V , 0 , 0 , 0 , 0 )	chirality 1
3 x ( 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , V )	chirality 1
2 x ( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , S )	chirality -2
1 x ( 0 , 0 , V , 0 , 0 , V , 0 , 0 , 0 )	chirality 1
1 x ( 0 , 0 , 0 , V , 0 , V , 0 , 0 , 0 )	chirality -1
1 x ( 0 , 0 , 0 , 0 , 0 , A , 0 , 0 , 0 )	chirality -1
5 x ( 0 , 0 , 0 , 0 , 0 , 0 , 0 , A , 0 )	chirality -1
1 x ( 0 , 0 , 0 , 0 , V , V , 0 , 0 , 0 )	chirality -1
3 x ( 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , V )	chirality 1
2 x ( 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , V* )	chirality 2
2 x ( 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , V )	chirality 2
1 x ( 0 , 0 , V , 0 , 0 , 0 , 0 , V , 0 )	chirality 1
1 x ( 0 , 0 , 0 , V , 0 , 0 , V , 0 , 0 )	chirality 1
1 x ( 0 , 0 , 0 , V , 0 , 0 , 0 , V , 0 )	chirality -1
1 x ( 0 , 0 , 0 , 0 , 0 , V , V , 0 , 0 )	chirality 1
1 x ( 0 , 0 , 0 , 0 , 0 , V , 0 , V , 0 )	chirality -1
3 x ( 0 , 0 , 0 , 0 , V , 0 , 0 , V , 0 )	chirality -3
6 x ( 0 , 0 , 0 , 0 , 0 , 0 , V , V , 0 )	chirality 0
1 x ( 0 , 0 , 0 , 0 , S , 0 , 0 , 0 , 0 )	chirality 0
1 x ( 0 , 0 , 0 , 0 , 0 , 0 , A , 0 , 0 )	chirality 0
2 x ( 0 , 0 , 0 , 0 , 0 , 0 , 0 , Ad , 0 )	chirality 0
2 x ( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , Ac )	chirality 0
1 x ( 0 , 0 , 0 , 0 , 0 , 0 , S , 0 , 0 )	chirality 0

Hidden sector



# MODEL NR. 6580

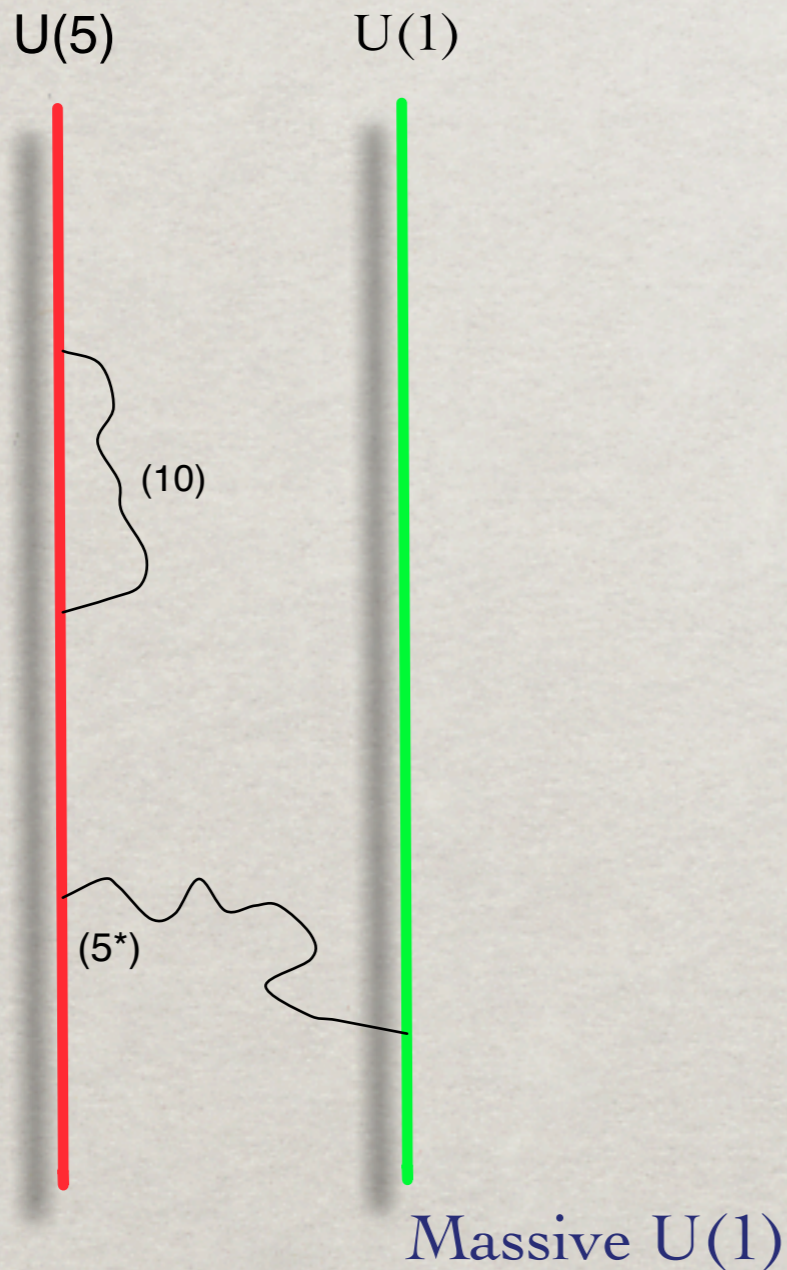


Spectrum  
(without tadpole cancellation)

	U	U	
	5	1	
2 x	(V, V)		chirality -2
1 x	(0, S)		chirality 1
3 x	(A, 0)		chirality 3
1 x	(V, V*)		chirality -1



# MODEL NR. 6580



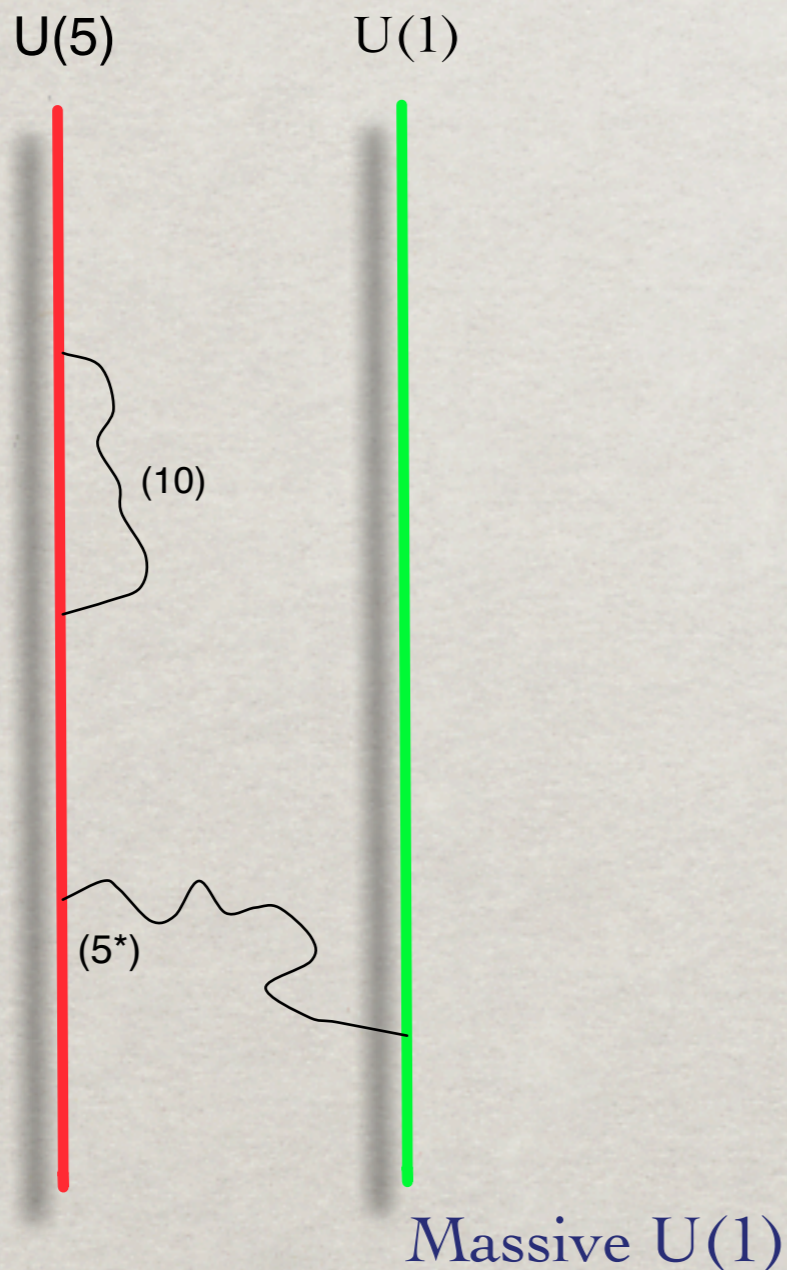
Spectrum  
(without tadpole cancellation)

	U	U	
	5	1	
2 x	(V, V)		chirality -2
1 x	(0, S)		chirality 1
3 x	(A, 0)		chirality 3
1 x	(V, V*)		chirality -1

+ NOTHING!  
(no adjoints, mirrors,  
non-chiral matter)



# MODEL NR. 6580



Spectrum  
(without tadpole cancellation)

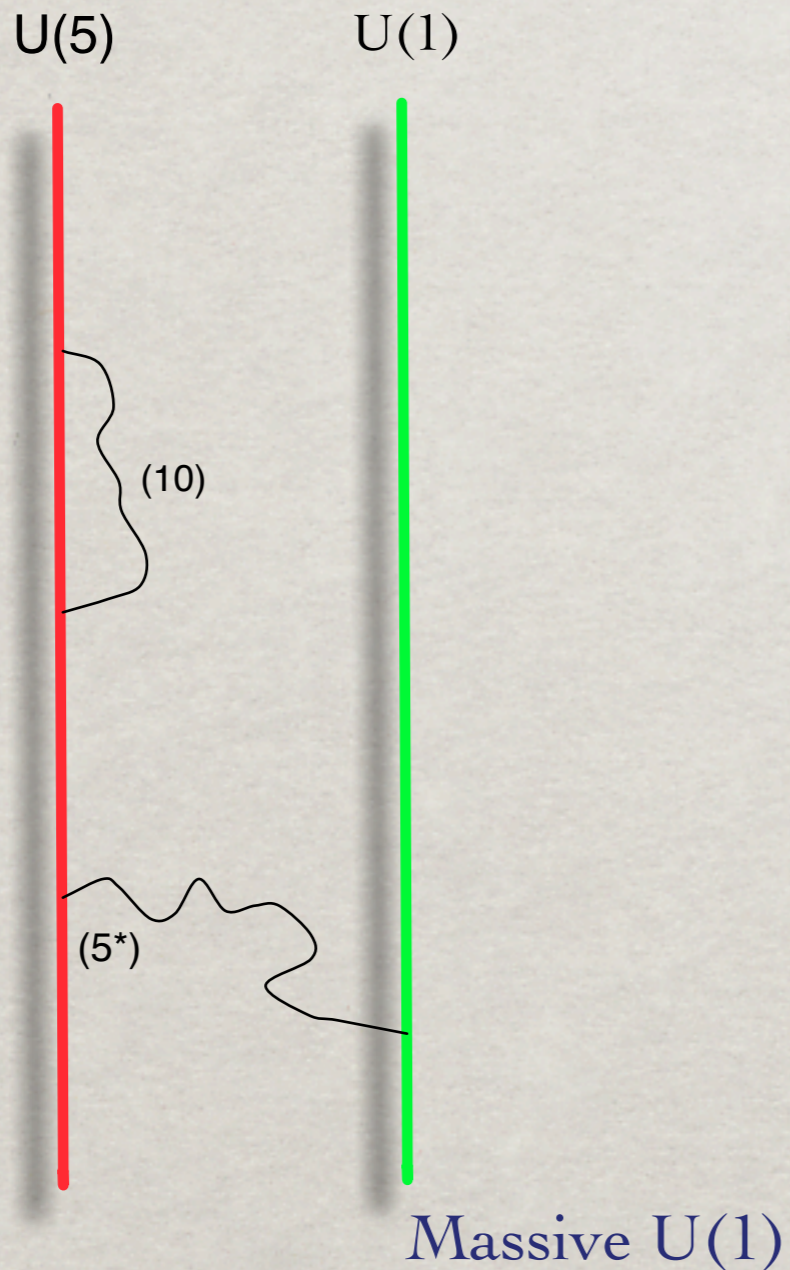
	U	U	
	5	1	
2 x	(V, V)		chirality -2
1 x	(0, S)		chirality 1
3 x	(A, 0)		chirality 3
1 x	(V, V*)		chirality -1

+ NOTHING!  
(no adjoints, mirrors,  
non-chiral matter)

(but also no Higgs)



# MODEL NR. 14861



Spectrum  
(without tadpole cancellation)

	U	U	
	5	1	
3 x	(A, 0)		chirality 3
15 x	(0, S)		chirality 9
6 x	(V, V)		chirality -6
5 x	(V, V*)		chirality 3
1 x	(Ad, 0)		chirality 0
4 x	(0, Ad)		chirality 0

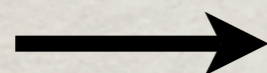


# All tadpole solutions for the $U(5) \times O(1)$ models

## Candidates

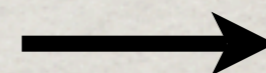
(configurations prior to tadpole cancellation)

16845



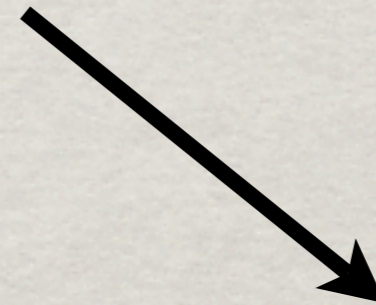
$\left\{ \begin{array}{ll} 15499 & \times \\ 641 & \checkmark \\ 705 & ? \end{array} \right.$

## Allowing chiral OH matter



$\left\{ \begin{array}{ll} 521 & \times \\ 109 & \checkmark \\ 11 & ? \end{array} \right.$

## Allowing only non-chiral OH matter(\*)



$\left\{ \begin{array}{ll} 508 & \times \\ 64 & \checkmark \\ 133 & ? \end{array} \right.$

(\*) as in all previous work with Dijkstra et. al., Anastasopoulos et. al



# YUKAWA COUPLINGS

Top quark Yukawa coupling is forbidden by U(5) brane charge conservation.

$(\mathbf{10})(\bar{\mathbf{5}})(\bar{\mathbf{5}}_H)$  bottom quark masses: charge preserved\*

$(\mathbf{10})(\mathbf{10})(\mathbf{5}_H)$  top quark mass: charges violated

May be generated by stringy/exotic instantons

*(Blumenhagen, Cvetic, Lüst, Richter, Weigand)*

*(More recent work on instantons: See Richter and Ibañez, ref. [18-65])*

(\* forbidden by O(1) charge in the U(5) × O(1) models



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FOR COMPARISON:  
NEUTRINO  
MASSES



# NEUTRINO MASS GENERATION BY INSTANTONS\*

Possible in “Madrid” models with massive B-L  
(391 out of the set of 200.000)

The desired neutrino mass term  $\nu^c \nu^c$   
violates c and d brane charge by two units.  
To compensate this, we must have

$$I_{Mc} = 2 ; I_{Md} = -2 \quad or \quad I_{Md'} = 2 ; I_{Mc'} = -2$$

and all other intersections 0.  
(d' is the boundary conjugate of d)

*(\*) Blumenhagen, Cvetic, Weigand, Nucl.Phys.B771:113-142,2007  
Ibañez, Uranga, JHEP 0703:052,2007*

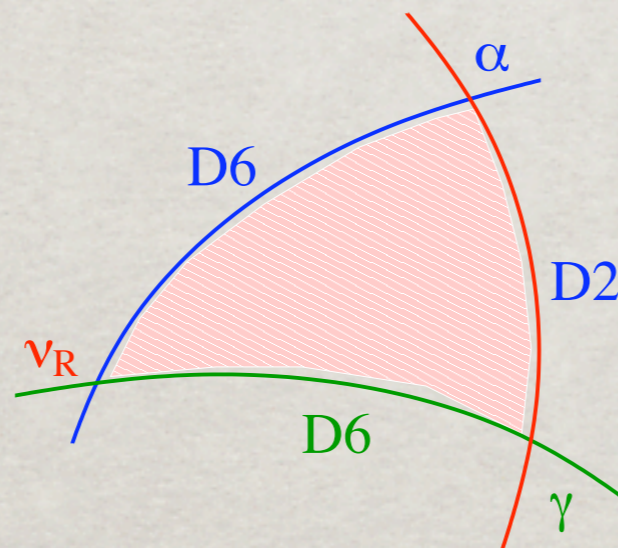
Studied for Gepner orientifolds in

*Ibañez, Schellekens, Uranga, JHEP 0706:011,2007*



# NEUTRINO-ZERO MODE COUPLING

The following world-sheet disk is allowed by all symmetries



$$L_{cubic} \propto d_a^{ij} (\alpha_i \nu^a \gamma_j) , a = 1, 2, 3$$



# ZERO-MODE INTEGRALS

$$\int d^2\alpha d^2\gamma e^{-d_a^{ij} (\alpha_i \nu^a \gamma_j)} = \nu_a \nu_b (\epsilon_{ij} \epsilon_{kl} d_a^{ik} d_b^{jl})$$

Additional zero modes yield additional fermionic integrals and hence nullify the contribution

Therefore  $I_{M_a} = I_{M_b} = I_{M_x} = 0$  ( $x = \text{Hidden sector}$ ), and there should be no vector-like zero modes.

There should also be no instanton-instanton zero-modes except 2 required by susy.



# UNIVERSAL INSTANTON- INSTANTON ZERO-MODES

- $U(k): 4 \text{ Adj}$
- $Sp(2k): 2 A + 2 S$
- $O(k): 2 A + 2 S$

Only  $O(1)$  has the required 2 zero modes



# AN $SP(2)$ INSTANTON MODEL

## U3 S2 U1 U1 O

3 x ( V ,V ,0 ,0 ,0 )	chirality 3
3 x ( V ,0 ,V ,0 ,0 )	chirality -3
3 x ( V ,0 ,V* ,0 ,0 )	chirality -3
3 x ( 0 ,V ,0 ,V ,0 )	chirality 3
5 x ( 0 ,0 ,V ,V ,0 )	chirality -3
3 x ( 0 ,0 ,V ,V* ,0 )	chirality 3
1 x ( 0 ,0 ,V ,0 ,V )	chirality -1
1 x ( 0 ,0 ,0 ,V ,V )	chirality 1
18 x ( 0 ,V ,V ,0 ,0 )	
2 x ( V ,0 ,0 ,V ,0 )	
2 x ( Ad, 0 ,0 ,0 ,0 )	
2 x ( A ,0 ,0 ,0 ,0 )	
6 x ( S ,0 ,0 ,0 ,0 )	
14 x ( 0 ,A ,0 ,0 ,0 )	
6 x ( 0 ,S ,0 ,0 ,0 )	
9 x ( 0 ,0 ,Ad, 0 ,0 )	
6 x ( 0 ,0 ,A ,0 ,0 )	
14 x ( 0 ,0 ,S ,0 ,0 )	
3 x ( 0 ,0 ,0 ,Ad, 0 )	
4 x ( 0 ,0 ,0 ,A ,0 )	
6 x ( 0 ,0 ,0 ,S ,0 )	



# AN $SP(2)$ INSTANTON MODEL

**U3 S2 U1 U1 O**

3 x	( V ,V ,0 ,0 ,0 )	chirality 3
3 x	( V ,0 ,V ,0 ,0 )	chirality -3
3 x	( V ,0 ,V* ,0 ,0 )	chirality -3
3 x	( 0 ,V ,0 ,V ,0 )	chirality 3
5 x	( 0 ,0 ,V ,V ,0 )	chirality -3
3 x	( 0 ,0 ,V ,V* ,0 )	chirality 3
1 x	( 0 ,0 ,V ,0 ,V )	chirality -1
1 x	( 0 ,0 ,0 ,V ,V )	chirality 1
18 x	( 0 ,V ,V ,0 ,0 )	
2 x	( V ,0 ,0 ,V ,0 )	
2 x	( Ad, 0 ,0 ,0 ,0 )	
2 x	( A ,0 ,0 ,0 ,0 )	
6 x	( S ,0 ,0 ,0 ,0 )	
14 x	( 0 ,A ,0 ,0 ,0 )	
6 x	( 0 ,S ,0 ,0 ,0 )	
9 x	( 0 ,0 ,Ad, 0 ,0 )	
6 x	( 0 ,0 ,A ,0 ,0 )	
14 x	( 0 ,0 ,S ,0 ,0 )	
3 x	( 0 ,0 ,0 ,Ad, 0 )	
4 x	( 0 ,0 ,0 ,A ,0 )	
6 x	( 0 ,0 ,0 ,S ,0 )	



# THE O1 INSTANTON

Type:	U	S	U	U	U	O	O	U	O	O	O	U	S	S	O	S	
Dimension	3	2	1	1	1	2	2	3	1	2	3	1	2	2	2	--	
5 x	( V , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality -3															
5 x	( 0 , 0 , V , V* , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 3															
3 x	( V , 0 , V* , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality -3															
3 x	( 0 , 0 , V , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality -3															
3 x	( V , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 3															
3 x	( 0 , V , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 3															
2 x	( 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V )	chirality 2															
12 x	( 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V )	chirality -2															
1 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , V )																
2 x	( 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V )																
1 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , V )																
2 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , V )																
1 x	( 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V )																
3 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , S )																
4 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , V )																
2 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , A )																
2 x	( V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V )																
3 x	( 0 , 0 , 0 , 0 , S , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality -1															
3 x	( 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 )	chirality 1															
1 x	( 0 , 0 , 0 , 0 , A , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality -1															
2 x	( 0 , 0 , 0 , 0 , V , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 2															
1 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 )	chirality -1															
1 x	( 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 )	chirality -1															
1 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , V , 0 , 0 , 0 , 0 )	chirality 1															
1 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , V , 0 , 0 , 0 , 0 )	chirality -1															
1 x	( 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 )	chirality -1															
1 x	( 0 , 0 , 0 , 0 , V , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality -1															
1 x	( 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 )	chirality 1															
1 x	( 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V* , 0 , 0 , 0 , 0 )	chirality -1															
3 x	( 0 , 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 )	chirality 1															
1 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 )	chirality 1															
2 x	( 0 , 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 )																
1 x	( Ad , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )																
2 x	( 0 , S , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )																
1 x	( 0 , 0 , 0 , Ad , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )																
6 x	( 0 , 0 , V , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , V , 0 , 0 )																
1 x	( 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , A )																
1 x	( 0 , 0 , 0 , 0 , Ad , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 , 0 )																

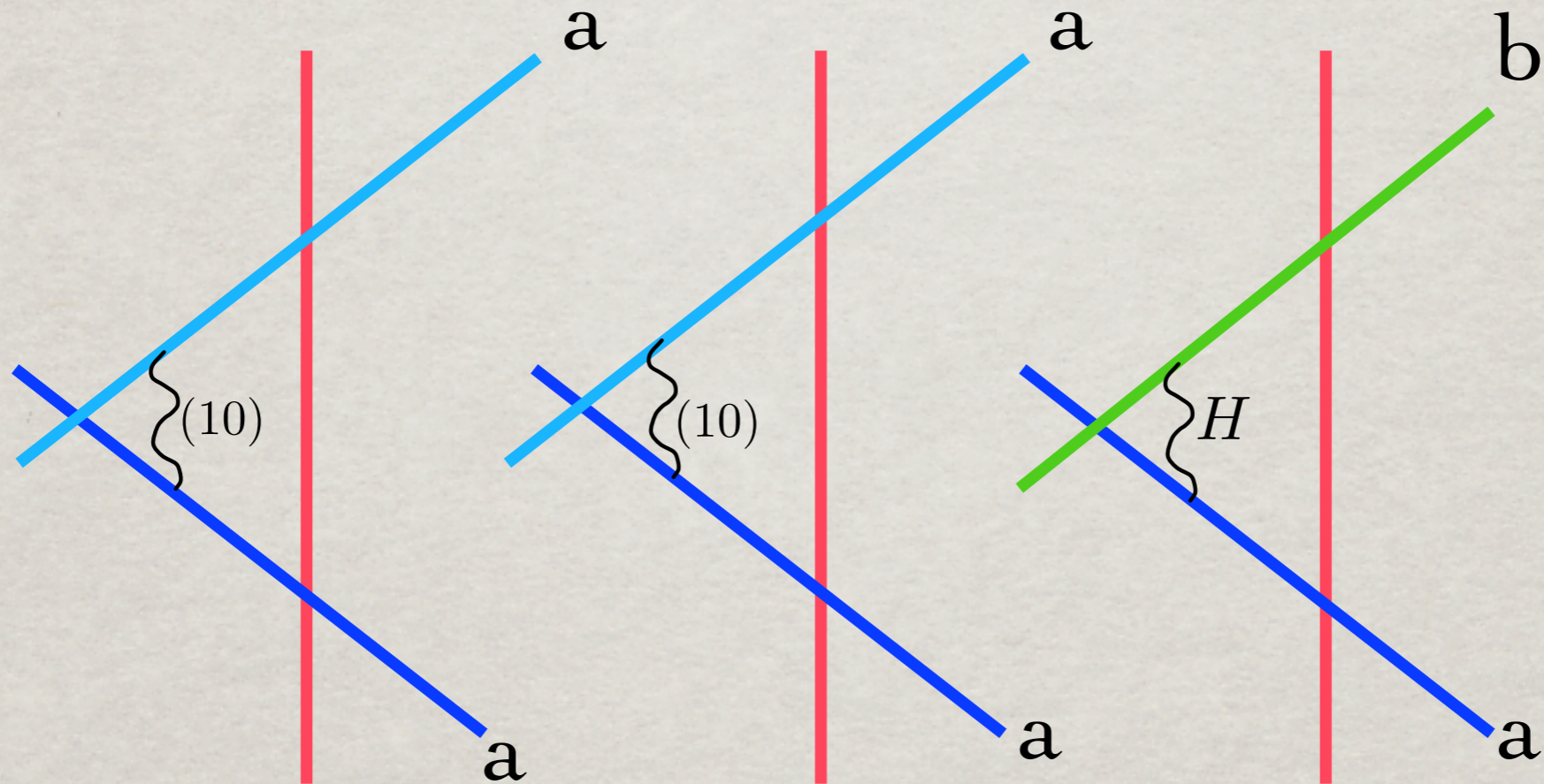




Back to Yukawas...



Find a brane (boundary state) with the right zero mode structure, so that in combination with the following perturbatively allowed disk amplitudes ...



... the instanton associated with that brane can generate the missing couplings.



# INSTANTONS

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Nr.	Models	U1	S2	O1	Zeromodes OK	Solutions
617	16845	$3.5 \times 10^6$	$1.1 \times 10^6$	$6.1 \times 10^5$	12889	0
2753	1136	$4.9 \times 10^5$	$1.5 \times 10^5$	$4.8 \times 10^4$	84	6
2881	1049	$2.1 \times 10^5$	$5.5 \times 10^4$	$4.5 \times 10^4$	30	0
6580	146	$7.0 \times 10^4$	9680	8092	73	0
14861	12	1190	504	0	0	0



	U	U	O	U	O	U	O	O	O	O	O	S	
	5	1	1	1	3	1	2	4	2	2	1	--	
5 x ( 0 ,S ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 3												
5 x ( A ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 3												
3 x ( V ,V ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality -3												
1 x ( 0 ,V ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,V )	chirality 1												
1 x ( V ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,V )	chirality -1												
2 x ( V ,V* ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
1 x ( V ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,0 ,0 )	chirality 1												
1 x ( V ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 )	chirality 1												
2 x ( V ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,0 ,0 ,0 )	chirality -2												
3 x ( 0 ,V ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 )	chirality -1												
1 x ( 0 ,V ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,0 ,0 ,0 )	chirality 1												
2 x ( V ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 )	chirality -2												
2 x ( S ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
4 x ( 0 ,A ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
6 x ( Ad ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
4 x ( 0 ,V ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 )	chirality 0												
2 x ( 0 ,Ad ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
2 x ( 0 ,V ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,0 ,0 )	chirality 0												
4 x ( 0 ,V ,0 ,0 ,0 ,0 ,V ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
2 x ( 0 ,V ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,S ,0 ,0 ,0 ,0 ,0 ,0 )	chirality -1												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,A ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 1												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,V ,V ,0 ,0 ,0 ,0 ,0 )	chirality 1												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,V ,0 ,0 ,0 ,0 )	chirality 1												
1 x ( 0 ,0 ,0 ,V ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,0 )	chirality -1												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,V ,0 ,0 ,0 )	chirality 1												
1 x ( 0 ,0 ,0 ,V ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 )	chirality 1												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,0 ,V ,0 ,0 )	chirality 1												
2 x ( 0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,0 ,0 ,V ,0 )	chirality -2												
2 x ( 0 ,0 ,0 ,0 ,V ,V ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,V ,0 ,V ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
2 x ( 0 ,0 ,0 ,V ,0 ,V* ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,A ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,0 ,Ad ,0 ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,S ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,V ,V ,0 ,0 ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,0 ,S ,0 ,0 ,0 ,0 ,0 )	chirality 0												
2 x ( 0 ,0 ,V ,0 ,0 ,0 ,V ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
2 x ( 0 ,0 ,0 ,0 ,V ,0 ,V ,0 ,0 ,0 ,0 ,0 ,0 )	chirality 0												
2 x ( 0 ,0 ,0 ,0 ,V ,0 ,0 ,V ,0 ,0 ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,V ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,S ,0 ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,0 ,V ,V ,0 ,0 ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,V ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,A ,0 ,0 ,0 )	chirality 0												
2 x ( 0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,V ,V ,0 )	chirality 0												
2 x ( 0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,A ,0 )	chirality 0												
2 x ( 0 ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,0 ,V ,0 ,0 )	chirality 0												
1 x ( 0 ,0 ,0 ,0 ,0 ,0 ,0 ,0 ,V ,0 ,V ,0 ,0 )	chirality 0												



		U	U	O	U	O	U	O	O	O	O	S				
		5	1	1	1	3	1	2	4	2	2	1	--			
5	x	(	0	,	S	,	0	,	0	,	0	,	0	)	chirality	3
5	x	(	A	,	0	,	0	,	0	,	0	,	0	)	chirality	3
3	x	(	V	,	V	,	0	,	0	,	0	,	0	)	chirality	-3
1	x	(	0	,	V	,	0	,	0	,	0	,	0	)	chirality	1
1	x	(	V	,	0	,	0	,	0	,	0	,	0	)	chirality	-1
2	x	(	V	,	V*	,	0	,	0	,	0	,	0	)	chirality	0
1	x	(	V	,	0	,	0	,	0	,	0	,	V	)	chirality	1
1	x	(	V	,	0	,	0	,	0	,	0	,	V	)	chirality	1
2	x	(	V	,	0	,	0	,	0	,	V	,	0	)	chirality	-2
3	x	(	0	,	V	,	0	,	0	,	0	,	V	)	chirality	-1
1	x	(	0	,	V	,	0	,	0	,	V	,	0	)	chirality	1
2	x	(	V	,	0	,	0	,	0	,	0	,	V	)	chirality	-2
2	x	(	S	,	0	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	A	,	0	,	0	,	0	,	0	)	chirality	0
6	x	(	Ad	,	0	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	V	,	0	,	0	,	0	,	V	)	chirality	0
2	x	(	0	,	Ad	,	0	,	0	,	0	,	0	)	chirality	0
2	x	(	0	,	V	,	0	,	0	,	0	,	V	)	chirality	0
4	x	(	0	,	V	,	0	,	0	,	V	,	0	)	chirality	0
2	x	(	0	,	V	,	0	,	0	,	0	,	V	)	chirality	0
1	x	(	0	,	0	,	0	,	0	,	S	,	0	)	chirality	-1
1	x	(	0	,	0	,	0	,	0	,	A	,	0	)	chirality	1
1	x	(	0	,	0	,	0	,	0	,	V	,	V	)	chirality	1
1	x	(	0	,	0	,	0	,	0	,	V	,	V	)	chirality	1
1	x	(	0	,	0	,	0	,	V	,	0	,	V	)	chirality	-1
1	x	(	0	,	0	,	0	,	0	,	V	,	V	)	chirality	1



		U	U	O	U	O	U	O	O	O	O	S				
		5	1	1	1	3	1	2	4	2	2	1	--			
5	x	(	0	,	S	,	0	,	0	,	0	,	0	)	chirality	3
5	x	(	A	,	0	,	0	,	0	,	0	,	0	)	chirality	3
3	x	(	V	,	V	,	0	,	0	,	0	,	0	)	chirality	-3
1	x	(	0	,	V	,	0	,	0	,	0	,	0	)	chirality	1
1	x	(	V	,	0	,	0	,	0	,	0	,	0	)	chirality	-1
2	x	(	V	,	V*	,	0	,	0	,	0	,	0	)	chirality	0
1	x	(	V	,	0	,	0	,	0	,	0	,	0	)	chirality	1
1	x	(	V	,	0	,	0	,	0	,	0	,	0	)	chirality	1
2	x	(	V	,	0	,	0	,	0	,	0	,	0	)	chirality	-2
3	x	(	0	,	V	,	0	,	0	,	0	,	0	)	chirality	-1
1	x	(	0	,	V	,	0	,	0	,	0	,	0	)	chirality	1
2	x	(	V	,	0	,	0	,	0	,	0	,	0	)	chirality	-2
2	x	(	S	,	0	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	A	,	0	,	0	,	0	,	0	)	chirality	0
6	x	(	Ad	,	0	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	V	,	0	,	0	,	0	,	0	)	chirality	0
2	x	(	0	,	Ad	,	0	,	0	,	0	,	0	)	chirality	0
2	x	(	0	,	V	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	V	,	0	,	0	,	0	,	0	)	chirality	0
2	x	(	0	,	V	,	0	,	0	,	0	,	0	)	chirality	0
1	x	(	0	,	0	,	0	,	0	,	0	,	0	)	chirality	-1
1	x	(	0	,	0	,	0	,	0	,	0	,	0	)	chirality	1
1	x	(	0	,	0	,	0	,	0	,	0	,	0	)	chirality	1
1	x	(	0	,	0	,	0	,	0	,	0	,	0	)	chirality	1



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5	x	(	0	,	S	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	3		
5	x	(	A	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	3		
3	x	(	V	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	-3		
1	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	)	chirality	1
1	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	)	chirality	-1
2	x	(	V	,	V*	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
1	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	)	chirality	1
1	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	)	chirality	1
2	x	(	V	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	,	0	)	chirality	-2
3	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	)	chirality	-1
1	x	(	0	,	V	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	,	0	)	chirality	1
2	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	)	chirality	-2
2	x	(	S	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	A	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
6	x	(	Ad	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	)	chirality	0
2	x	(	0	,	Ad	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
2	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	V	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
2	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	)	chirality	0
1	x	(	0	,	0	,	0	,	0	,	0	,	0	,	S	,	0	,	0	,	0	,	0	,	0	)	chirality	-1
1	x	(	0	,	0	,	0	,	0	,	0	,	0	,	A	,	0	,	0	,	0	,	0	,	0	)	chirality	1
1	x	(	0	,	0	,	0	,	0	,	0	,	V	,	V	,	0	,	0	,	0	,	0	,	0	)	chirality	1
1	x	(	0	,	0	,	0	,	0	,	0	,	V	,	0	,	V	,	0	,	0	,	0	,	0	)	chirality	1

Quarks,  
Leptons



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5	x	(	0	,	S	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	3
5	x	(	A	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	3
3	x	(	V	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	-3

Quarks,  
Leptons

1	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	)	chirality	1
1	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	)	chirality	-1

2	x	(	V	,	V*	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
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Higgs

1	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	)	chirality	1		
1	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	)	chirality	1		
2	x	(	V	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	,	0	)	chirality	-2		
3	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	)	chirality	-1		
1	x	(	0	,	V	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	,	0	)	chirality	1		
2	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	)	chirality	-2
2	x	(	S	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0		
4	x	(	0	,	A	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0		
6	x	(	Ad	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0		
4	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	)	chirality	0
2	x	(	0	,	Ad	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0		
2	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	)	chirality	0		
4	x	(	0	,	V	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0		
2	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	)	chirality	0		
1	x	(	0	,	0	,	0	,	0	,	0	,	0	,	S	,	0	,	0	,	0	,	0	,	0	)	chirality	-1		
1	x	(	0	,	0	,	0	,	0	,	0	,	0	,	A	,	0	,	0	,	0	,	0	,	0	)	chirality	1		
1	x	(	0	,	0	,	0	,	0	,	0	,	0	,	V	,	V	,	0	,	0	,	0	,	0	)	chirality	1		
1	x	(	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	V	,	0	,	0	,	0	)	chirality	1		



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5	x	(	0	,	S	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	3		
5	x	(	A	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	3		
3	x	(	V	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	-3		
1	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	)	chirality	1
1	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	)	chirality	-1
2	x	(	V	,	V*	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
1	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	)	chirality	1
1	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	)	chirality	1
2	x	(	V	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	,	0	)	chirality	-2
3	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	)	chirality	-1
1	x	(	0	,	V	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	,	0	)	chirality	1
2	x	(	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	)	chirality	-2
2	x	(	S	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	A	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
6	x	(	Ad	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	V	)	chirality	0
2	x	(	0	,	Ad	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
2	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	)	chirality	0
4	x	(	0	,	V	,	0	,	0	,	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	)	chirality	0
2	x	(	0	,	V	,	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	0	,	0	)	chirality	0
1	x	(	0	,	0	,	0	,	0	,	0	,	0	,	S	,	0	,	0	,	0	,	0	,	0	)	chirality	-1
1	x	(	0	,	0	,	0	,	0	,	0	,	0	,	A	,	0	,	0	,	0	,	0	,	0	)	chirality	1
1	x	(	0	,	0	,	0	,	0	,	0	,	0	,	V	,	V	,	0	,	0	,	0	,	0	)	chirality	1
1	x	(	0	,	0	,	0	,	0	,	0	,	0	,	V	,	0	,	V	,	0	,	0	,	0	)	chirality	1

Quarks,  
Leptons

Instanton

Higgs



# THE BOTTOM OF THE BARREL

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- 2004: 200.000 SM spectra, 18 chiral types.  
*(with Dijkstra, Huiszoon)*
- 2006: 19000 chiral types.  
*(with Anastasopoulos, Dijkstra, Kiritsis)*
- Neutrino masses: No perfect solution found.  
*(with Ibañez, Uranga)*
- Free Fermion Orientifolds: No solution.  
*(with Kiritsis, Lennek)*
- Tachyon-free non-susy strings: No SM.  
*(with Gato-Rivera)*
- Yukawa couplings from instantons: solution, but  
with chiral exotics. *(with Kiritsis, Lennek)*



# CONCLUSIONS

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- RCFT orientifolds have proved to be a powerful probe of the orientifold landscape.
- In general “richer” than free field theory based methods.
- We are reaching the end of statistics with RCFT.
- A lesson: don't focus too much on 3 families?