

# Simulating NNLO QCD corrections for processes with giant K factors

Sebastian Sapeta

LPTHE, UPMC, CNRS, Paris

in collaboration with Gavin Salam and Mathieu Rubin<sup>1</sup>

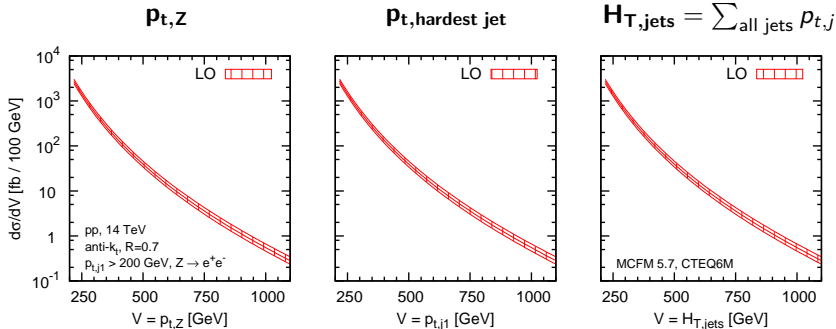
*HP<sup>2</sup>3rd, Florence, 14-17 September 2010*

---

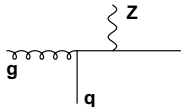
<sup>1</sup>M.Rubin, G.P.Salam and SS, arXiv:1006.2144 [hep-ph]

# The problem of giant K factors

## ► Z+j at the LHC

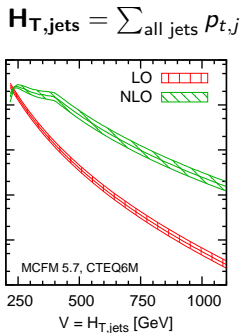
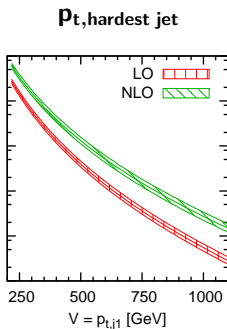
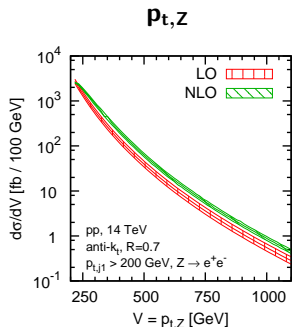


LO:

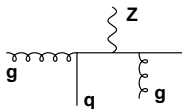


# The problem of giant K factors

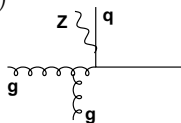
## ► Z+j at the LHC



$$\mathcal{O}(\alpha_{EW}\alpha_s^2)$$



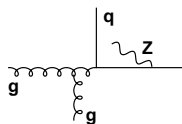
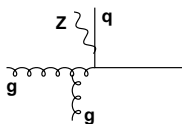
$$\mathcal{O}(\alpha_{EW}\alpha_s^2 \ln^2 p_{t,j1}/M_Z)$$



**NLO:**

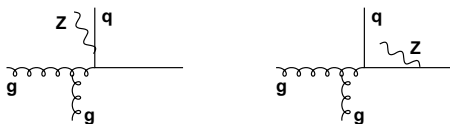
# What do we have and what is missing?

- ▶ The large K factor for the Z+jet comes from the new “dijet type” topologies that appear at NLO



# What do we have and what is missing?

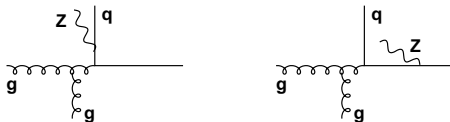
- ▶ The large K factor for the  $Z$ +jet comes from the new “dijet type” topologies that appear at NLO



- ▶ though formally NLO diagrams for  $Z$ +jet, these are in fact leading contributions to  $p_{t,j1}$  and  $H_T$  spectra
- ▶ this raises doubts about the accuracy of these predictions
- ▶ need for subleading contributions for  $Z$ +jet, in this case NNLO

# What do we have and what is missing?

- ▶ The large K factor for the  $Z+\text{jet}$  comes from the new “dijet type” topologies that appear at NLO

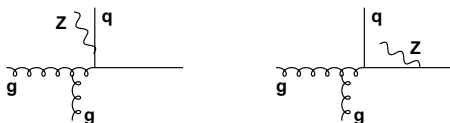


- ▶ though formally NLO diagrams for  $Z+\text{jet}$ , these are in fact leading contributions to  $p_{t,j1}$  and  $H_T$  spectra
- ▶ this raises doubts about the accuracy of these predictions
- ▶ need for subleading contributions for  $Z+\text{jet}$ , in this case NNLO

$$Z+j \text{ at NNLO} = \underbrace{Z+3j \text{ tree} + Z+2j \text{ 1-loop} + Z+j \text{ 2-loop}}_{Z+2j \text{ at NLO}}$$

# What do we have and what is missing?

- ▶ The large K factor for the Z+jet comes from the new “dijet type” topologies that appear at NLO



- ▶ though formally NLO diagrams for Z+jet, these are in fact leading contributions to  $p_{t,j1}$  and  $H_T$  spectra
- ▶ this raises doubts about the accuracy of these predictions
- ▶ need for subleading contributions for Z+jet, in this case NNLO

$$\text{Z+j at NNLO} = \underbrace{\text{Z+3j tree} + \text{Z+2j 1-loop}}_{\text{Z+2j at NLO}} + \text{Z+j 2-loop}$$

## ▶ 2-loop part

- ▶ we need it to cancel IR and collinear divergences from Z+2j at NLO result
- ▶ it will have the topology of Z+j at LO so it will not contribute much to the cross sections with giant K-factor

# The basic idea

How to cancel the infrared and collinear singularities?



# The basic idea

How to cancel the infrared and collinear singularities?

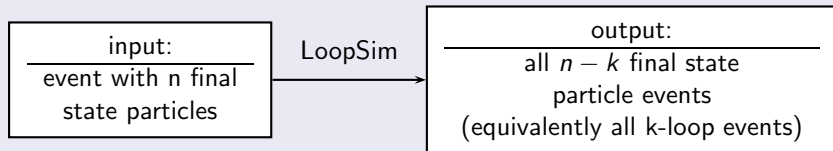
- ▶ use unitarity to simulate the divergent part of 2-loop diagrams

# The basic idea

How to cancel the infrared and collinear singularities?

- ▶ use unitarity to simulate the divergent part of 2-loop diagrams

## LoopSim procedure

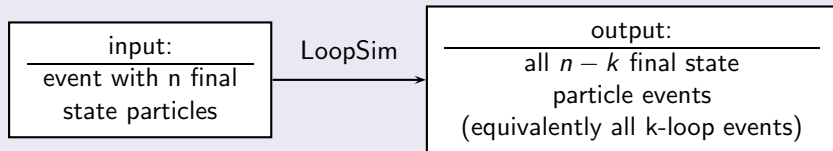


# The basic idea

How to cancel the infrared and collinear singularities?

- ▶ use unitarity to simulate the divergent part of 2-loop diagrams

## LoopSim procedure



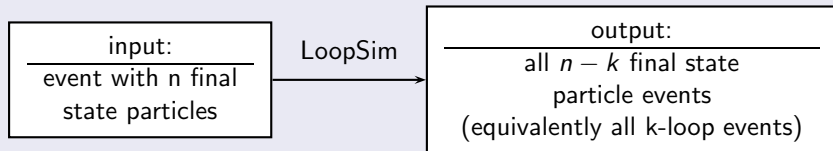
- ▶ notation:
  - $\bar{n}\text{LO}$  – simulated 1-loop
  - $\bar{n}\bar{n}\text{LO}$  – simulated 2-loop and simulated 1-loop
  - $\bar{n}\text{NLO}$  – simulated 2-loop and exact 1-loop

# The basic idea

How to cancel the infrared and collinear singularities?

- ▶ use unitarity to simulate the divergent part of 2-loop diagrams

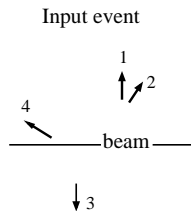
## LoopSim procedure



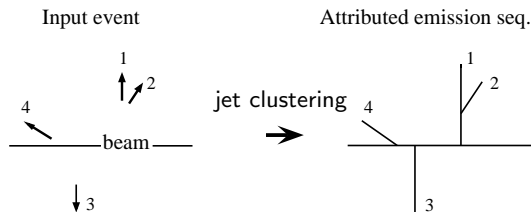
- ▶ notation:
  - $\bar{n}\text{LO}$  – simulated 1-loop
  - $\bar{n}\bar{n}\text{LO}$  – simulated 2-loop and simulated 1-loop
  - $\bar{n}\text{NLO}$  – simulated 2-loop and exact 1-loop
- ▶ this will work very well for the processes with large K factors e.g.

$$\sigma_{\bar{n}\text{NLO}} = \sigma_{\text{NNLO}} \left( 1 + \mathcal{O} \left( \frac{\alpha_s^2}{K_{\text{NNLO}}} \right) \right), \quad K_{\text{NNLO}} \gtrsim K_{\text{NLO}} \gg 1$$

# The LoopSim method: $\bar{n}$ LO, $\bar{n}\bar{n}$ LO etc.

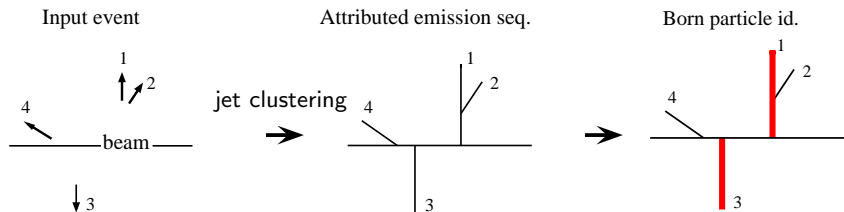


# The LoopSim method: $\bar{n}$ LO, $\bar{n}\bar{n}$ LO etc.



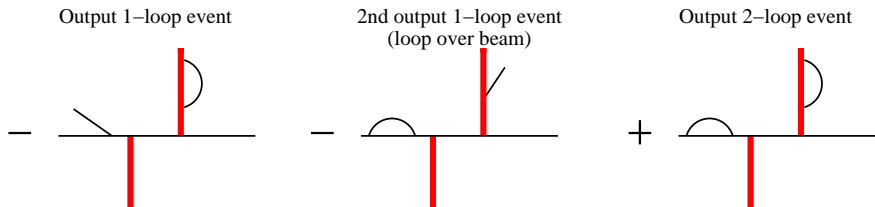
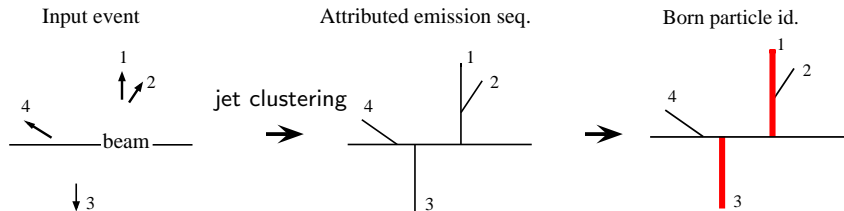
- ▶ jet clustering  $ij \rightarrow k$  is reinterpreted as the splitting  $k \rightarrow ij$

# The LoopSim method: $\bar{n}$ LO, $\bar{n}\bar{n}$ LO etc.



- ▶ jet clustering  $ij \rightarrow k$  is reinterpreted as the splitting  $k \rightarrow ij$

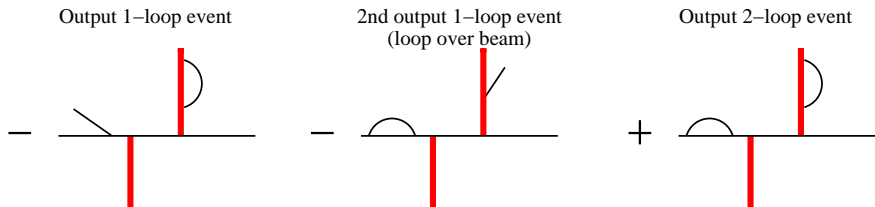
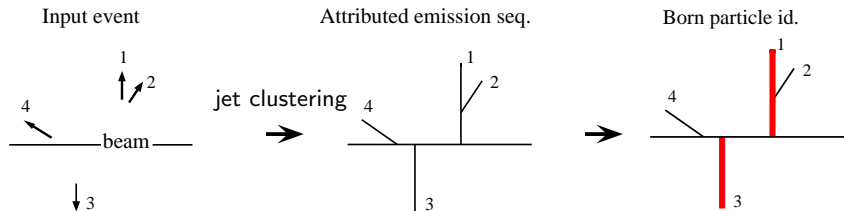
# The LoopSim method: $\bar{n}$ LO, $\bar{n}\bar{n}$ LO etc.



- ▶ jet clustering  $ij \rightarrow k$  is reinterpreted as the splitting  $k \rightarrow ij$
- ▶ weight of an event  $\sim (-1)^{\text{number of loops}}$

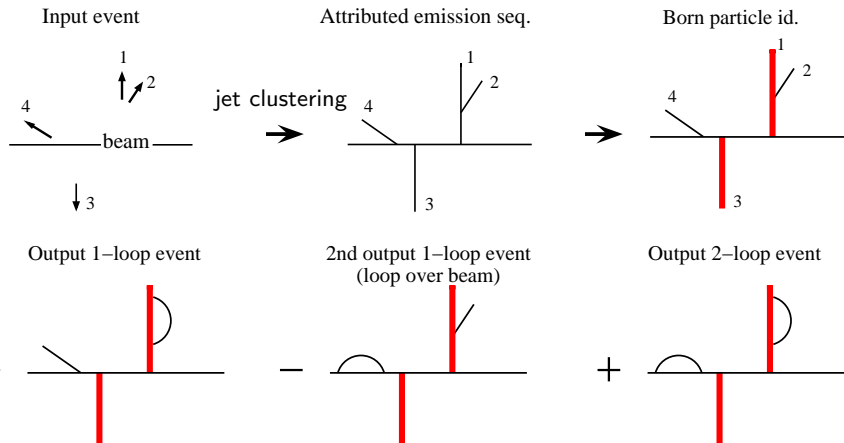


# The LoopSim method: $\bar{n}$ LO, $\bar{n}\bar{n}$ LO etc.



- ▶ jet clustering  $ij \rightarrow k$  is reinterpreted as the splitting  $k \rightarrow ij$
- ▶ weight of an event  $\sim (-1)^{\text{number of loops}}$
- ▶  $\sum$  all weights = 0 (unitarity) [Bloch, Nordsieck and Kinoshita, Lee, Nauenberg]

# The LoopSim method: $\bar{n}$ LO, $\bar{n}\bar{n}$ LO etc.



- ▶ jet clustering  $ij \rightarrow k$  is reinterpreted as the splitting  $k \rightarrow ij$
- ▶ weight of an event  $\sim (-1)^{\text{number of loops}}$
- ▶  $\sum$  all weights = 0 (unitarity) [Bloch, Nordsieck and Kinoshita, Lee, Nauenberg]
- ▶ beware: the loops above are just a shortcut notation!

# Including exact loops

- $E_{n,l}$  – input event with  $n$  final state particles and  $l$  loops
- $U_l^b$  – operator producing event with  $b$  Born particles and  $l$  loops
- $U_{\nabla}^b$  – operator generating all necessary loop diagrams at given order

# Including exact loops

- $E_{n,l}$  – input event with  $n$  final state particles and  $l$  loops
- $U_l^b$  – operator producing event with  $b$  Born particles and  $l$  loops
- $U_{\nabla}^b$  – operator generating all necessary loop diagrams at given order

How to introduce exact loop contributions?

# Including exact loops

- $E_{n,l}$  – input event with  $n$  final state particles and  $l$  loops
- $U_l^b$  – operator producing event with  $b$  Born particles and  $l$  loops
- $U_{\forall}^b$  – operator generating all necessary loop diagrams at given order

## How to introduce exact loop contributions?

$$U_{\forall}^b(E_{n,0})$$

- ▶ generate all diagrams from the tree level event

# Including exact loops

- $E_{n,l}$  – input event with  $n$  final state particles and  $l$  loops
- $U_l^b$  – operator producing event with  $b$  Born particles and  $l$  loops
- $U_{\forall}^b$  – operator generating all necessary loop diagrams at given order

## How to introduce exact loop contributions?

$$U_{\forall}^b(E_{n,0}) + U_{\forall}^b(E_{n-1,1})$$

- ▶ generate all diagrams from the tree level event
- ▶ generate all diagrams from the 1-loop event

# Including exact loops

- $E_{n,l}$  – input event with  $n$  final state particles and  $l$  loops
- $U_l^b$  – operator producing event with  $b$  Born particles and  $l$  loops
- $U_{\forall}^b$  – operator generating all necessary loop diagrams at given order

## How to introduce exact loop contributions?

$$U_{\forall}^b(E_{n,0}) + U_{\forall}^b(E_{n-1,1}) - U_{\forall}^b(U_1^b(E_{n,0}))$$

- ▶ generate all diagrams from the tree level event
- ▶ generate all diagrams from the 1-loop event
- ▶ remove all approximate diagrams from  $U_{\forall}^b(E_{n,0})$  that have exact counterparts provided by  $U_{\forall}^b(E_{n-1,1})$

# Including exact loops

- $E_{n,l}$  – input event with  $n$  final state particles and  $l$  loops
- $U_l^b$  – operator producing event with  $b$  Born particles and  $l$  loops
- $U_{\forall}^b$  – operator generating all necessary loop diagrams at given order

## How to introduce exact loop contributions?

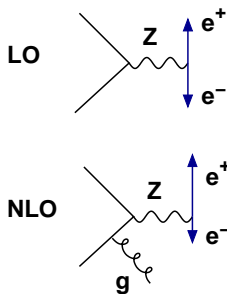
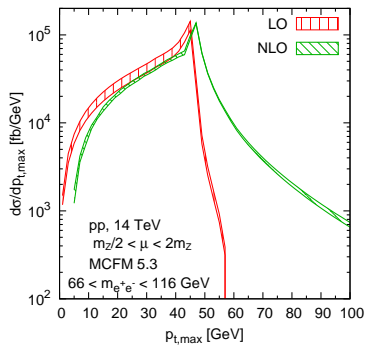
$$U_{\forall}^b(E_{n,0}) + U_{\forall}^b(E_{n-1,1}) - U_{\forall}^b(U_1^b(E_{n,0}))$$

- ▶ generate all diagrams from the tree level event
  - ▶ generate all diagrams from the 1-loop event
  - ▶ remove all approximate diagrams from  $U_{\forall}^b(E_{n,0})$  that have exact counterparts provided by  $U_{\forall}^b(E_{n-1,1})$
- 
- ▶ inclusion of exact loops helps reducing scale uncertainties
  - ▶ straightforward generalization to arbitrary number of exact loops



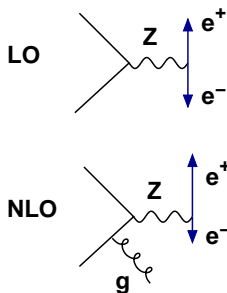
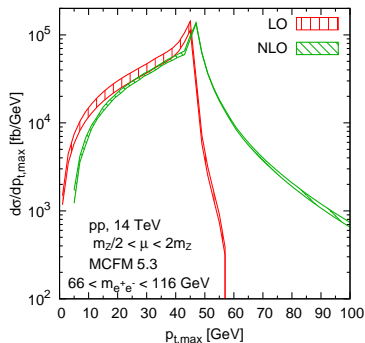
# Validation

# Drell-Yan at NNLO: spectrum of harder lepton



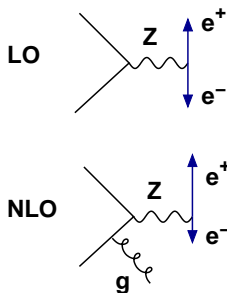
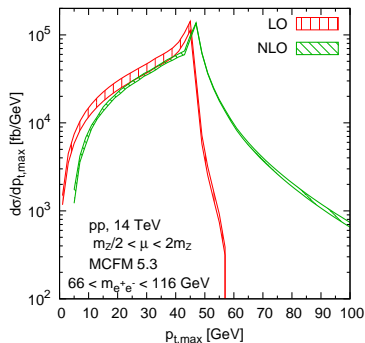
- ▶ giant K factor due to a boost caused by initial state radiation

# Drell-Yan at NNLO: spectrum of harder lepton



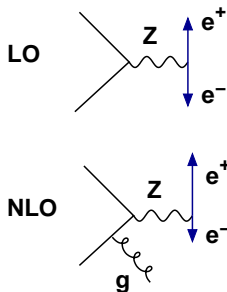
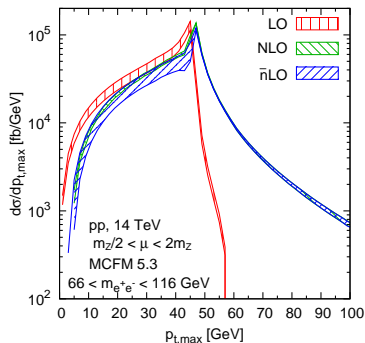
- ▶ giant K factor due to a boost caused by initial state radiation
- ▶ the agreement between NLO and  $\bar{n}$ LO may serve as an indication whether the method works for a given observable,  $Z @ \bar{n}LO = Z @ LO + LoopSim \circ (Z + j @ LO)$

# Drell-Yan at NNLO: spectrum of harder lepton



- ▶ giant K factor due to a boost caused by initial state radiation
- ▶ the agreement between NLO and  $\bar{n}$ LO may serve as an indication whether the method works for a given observable,  $Z @ \bar{n}LO = Z @ LO + LoopSim \circ (Z + j @ LO)$
- ▶ three regions of  $p_{t,max}$ :  $\lesssim \frac{1}{2} M_Z$        $[\frac{1}{2} M_Z, 58 \text{ GeV}]$        $> 58 \text{ GeV}$

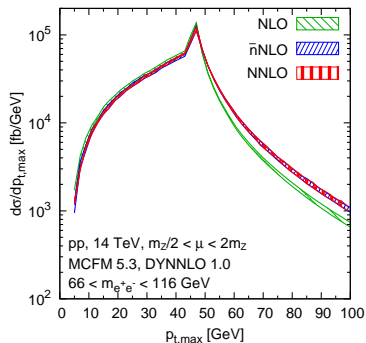
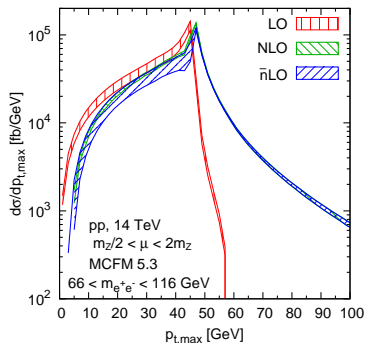
# Drell-Yan at NNLO: spectrum of harder lepton



- ▶ giant K factor due to a boost caused by initial state radiation
- ▶ the agreement between NLO and  $\bar{n}$ LO may serve as an indication whether the method works for a given observable,  $Z @ \bar{n}LO = Z @ LO + LoopSim \circ (Z + j @ LO)$

▶ three regions of $p_{t,\max}$ :	$\lesssim \frac{1}{2} M_Z$	$[\frac{1}{2} M_Z, 58 \text{ GeV}]$	$> 58 \text{ GeV}$
$\bar{n}$ LO vs NLO	very good (not guaranteed)	excellent (expected)	perfect (expected)

# Drell-Yan at NNLO: spectrum of harder lepton



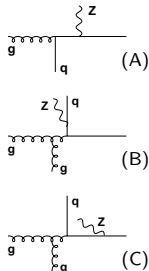
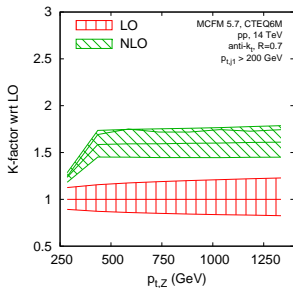
- ▶ giant K factor due to a boost caused by initial state radiation
- ▶ the agreement between NLO and  $\bar{n}$ LO may serve as a indication whether the method works for a given observable,  $Z@n\bar{N}LO = Z@LO + LoopSim \circ (Z + j@LO)$

three regions of $p_{t,\max}$ :	$\lesssim \frac{1}{2}M_Z$	$[\frac{1}{2}M_Z, 58 \text{ GeV}]$	$> 58 \text{ GeV}$
$\bar{n}$ LO vs NLO and $\bar{n}$ NLO vs NNLO	very good (not guaranteed)	excellent (expected)	perfect (expected)

# $\bar{n}$ NLO predictions for LHC

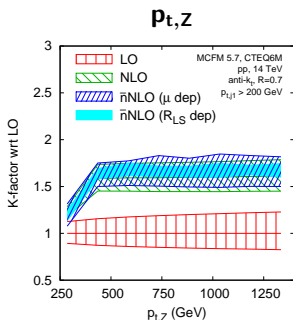
# $Z+\text{jet}$ at $\bar{n}\text{NLO} = Z+j@NLO + \text{LoopSim}_o(Z+2j@NLO_{\text{only}})$

$p_{t,z}$

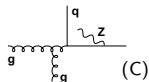
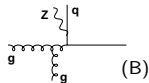
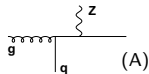




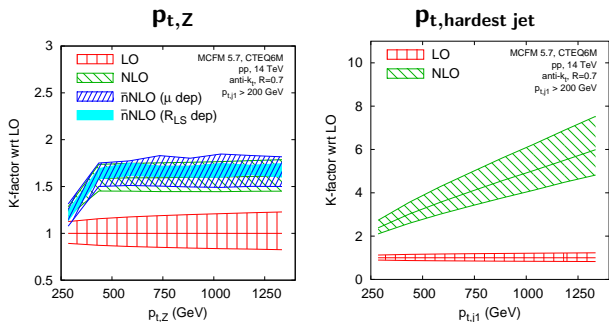
# $Z+\text{jet}$ at $\bar{n}\text{NLO} = Z+j@NLO + \text{LoopSim}_\circ(Z+2j@NLO_{\text{only}})$



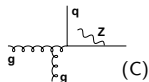
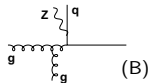
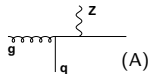
- $p_{t,Z}$ : no correction; topology (A) dominant at high  $p_{t,Z}$  (extra loops w.r.t. NLO do not change much)



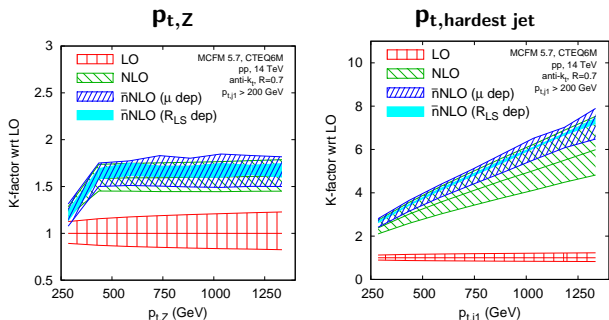
# $Z+\text{jet}$ at $\bar{n}\text{NLO} = Z+j@NLO + \text{LoopSim}_o(Z+2j@NLO_{\text{only}})$



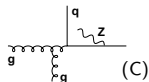
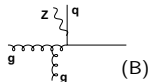
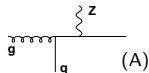
- ▶  $p_{t,Z}$ : no correction; topology (A) dominant at high  $p_{t,Z}$  (extra loops w.r.t. NLO do not change much)



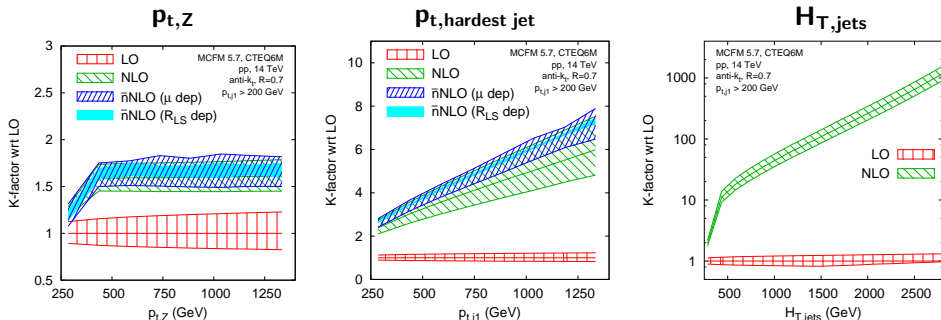
# $Z+\text{jet}$ at $\bar{n}\text{NLO} = Z+j@NLO + \text{LoopSim}_\circ(Z+2j@NLO_{\text{only}})$



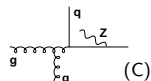
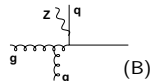
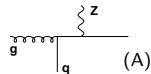
- ▶  $p_{t,Z}$ : no correction; topology (A) dominant at high  $p_{t,Z}$  (extra loops w.r.t. NLO do not change much)
- ▶  $p_{t,j}$ : small correction;  $\bar{n}\text{NLO}$  is like NLO for the dominant (B) and (C) configurations and it behaves like healthy NLO



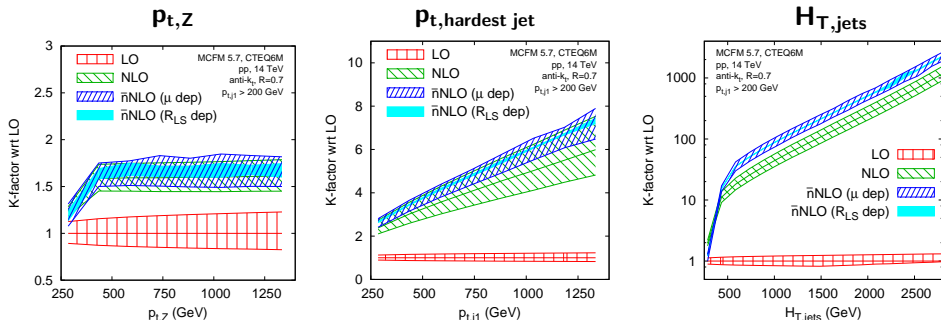
# $Z+\text{jet}$ at $\bar{n}\text{NLO} = Z+j@NLO + \text{LoopSim}_\circ(Z+2j@NLO_{\text{only}})$



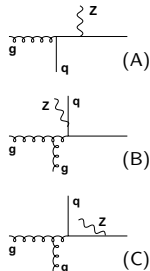
- ▶  $p_{t,Z}$ : no correction; topology (A) dominant at high  $p_{t,Z}$  (extra loops w.r.t. NLO do not change much)
- ▶  $p_{t,j}$ : small correction;  $\bar{n}\text{NLO}$  is like NLO for the dominant (B) and (C) configurations and it behaves like healthy NLO



# $Z + \text{jet}$ at $\bar{n}\text{NLO} = Z + j @ \text{NLO} + \text{LoopSim}_\circ(Z + 2j @ \text{NLO}_{\text{only}})$

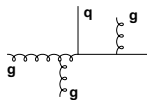
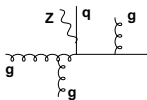


- ▶  $p_{t,Z}$ : no correction; topology (A) dominant at high  $p_{t,Z}$  (extra loops w.r.t. NLO do not change much)
- ▶  $p_{t,j}$ : small correction;  $\bar{n}\text{NLO}$  is like NLO for the dominant (B) and (C) configurations and it behaves like healthy NLO
- ▶  $H_{T,jets}$ : significant correction; K factor  $\sim 2$ ; given that it is more like going from LO to NLO this may happen sometimes, especially for nontrivial observables like  $H_T$ ; can we understand it here?



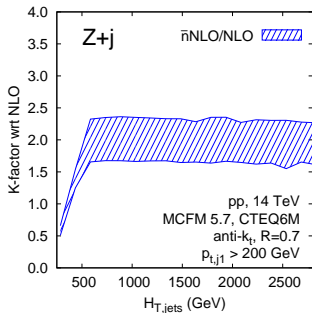
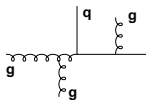
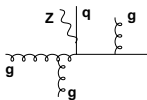
# $H_T$ type observables at $\bar{n}$ NLO for $Z$ +jet and for dijets

- ▶  $Z$ +jet at NNLO like dijets at NLO  
(same topology,  $Z$  only provides the enhancement  $\mathcal{O}(\alpha_{EW} \ln^2 p_{t,j1}/m_Z)$ )



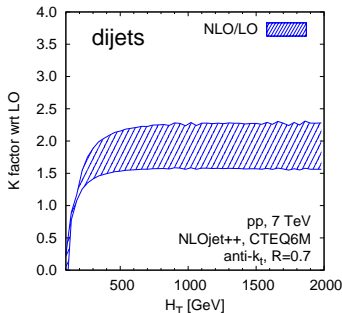
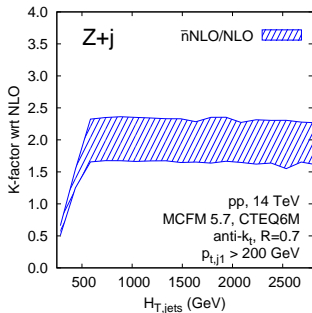
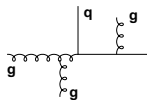
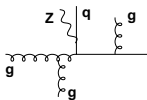
# $H_T$ type observables at $\bar{n}$ NLO for $Z$ +jet and for dijets

- ▶  $Z$ +jet at NNLO like dijets at NLO  
(same topology,  $Z$  only provides the enhancement  $\mathcal{O}(\alpha_{EW} \ln^2 p_{t,j1}/m_Z)$ )



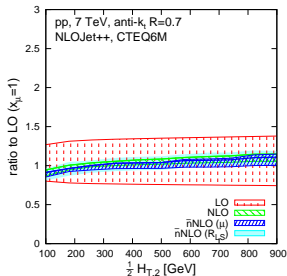
# $H_T$ type observables at $\bar{n}$ NLO for $Z$ +jet and for dijets

- ▶  $Z$ +jet at NNLO like dijets at NLO  
(same topology,  $Z$  only provides the enhancement  $\mathcal{O}(\alpha_{EW} \ln^2 p_{t,j1}/m_Z)$ )

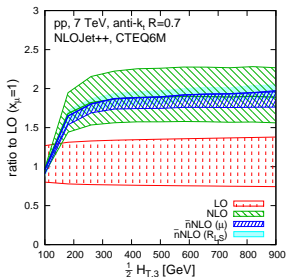
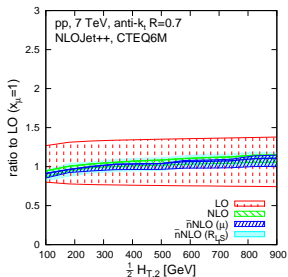


- ▶  $H_T$  for dijets receives large contributions at NLO!
  - ▶ caused by appearance of the third jet from initial state radiation

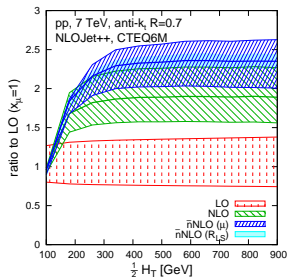
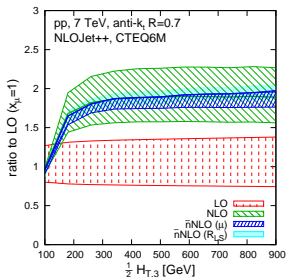
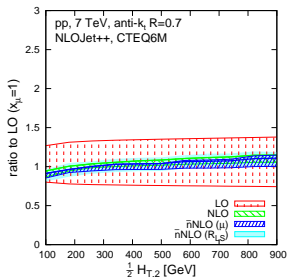




- ▶  $H_{T,2}$ : **central value and scale uncertainties stay the same:** adding NNLO corrections without proper finite part cannot improve the result



- ▶  $H_{T,2}$ : **central value and scale uncertainties stay the same:** adding NNLO corrections without proper finite part cannot improve the result
- ▶  $H_{T,3}$  **converges, significant reduction of scale uncertainty:** the observable comes under control at  $\bar{n}$ NLO



- ▶  $H_{T,2}$ : **central value and scale uncertainties stay the same:** adding NNLO corrections without proper finite part cannot improve the result
- ▶  $H_{T,3}$  **converges, significant reduction of scale uncertainty:** the observable comes under control at  $\bar{n}$ NLO
- ▶  $H_T$  **does not converge:** again caused by the initial state radiation, this time a second emission which shifts the distribution of  $H_T$  to higher values and causes no effect for the  $H_{T,3}$  distribution

# Summary

- ▶ several cases of observables with giant NLO K factor exist
- ▶ those large corrections arise due to appearance of new topologies at NLO
- ▶ we developed a method, called *LoopSim*, which allows one to obtain approximate NNLO corrections for such processes
- ▶ the method is based on unitarity and makes use of combining NLO results for different multiplicities
- ▶ we gave arguments why the method should produce meaningful results and we validated it against NNLO Drell-Yan and also NLO Z+j and NLO dijets
- ▶ we computed approximated NNLO corrections to Z+j and dijets at the LHC finding, depending on observable, either indication of convergence of the perturbative series or further corrections
- ▶ the latter has been understood and attributed to the initial state radiation

## Outlook

- ▶ processes with  $W$ , multibosons, heavy quarks, ...

# BACKUP SLIDES

# The LoopSim method: some more details

For a given input  $E_n$  event with  $n$  final state particles the weights of all diagrams generated by LoopSim sum up to zero (unitarity)

$$\sum_{\text{all diagrams}} w_n = \sum_{\ell=0}^v (-1)^\ell \binom{v}{\ell} = 0, \quad \ell - \text{number of loops, } v - \text{maximal } \ell$$

# The LoopSim method: some more details

For a given input  $E_n$  event with  $n$  final state particles the weights of all diagrams generated by LoopSim sum up to zero (unitarity)

$$\sum_{\text{all diagrams}} w_n = \sum_{\ell=0}^v (-1)^\ell \binom{v}{\ell} = 0, \quad \ell - \text{number of loops, } v - \text{maximal } \ell$$

The principle of the method is simple. There is, however, a number of issues that need to be addressed to fully specify the procedure and make it usable:

# The LoopSim method: some more details

For a given input  $E_n$  event with  $n$  final state particles the weights of all diagrams generated by LoopSim sum up to zero (unitarity)

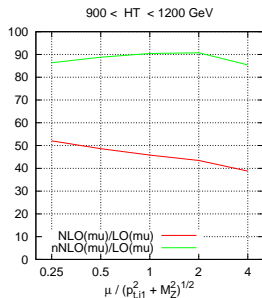
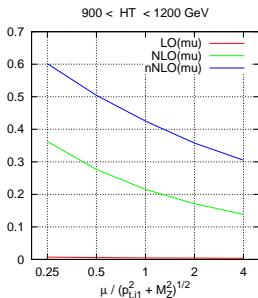
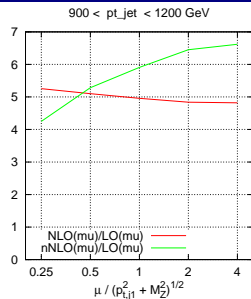
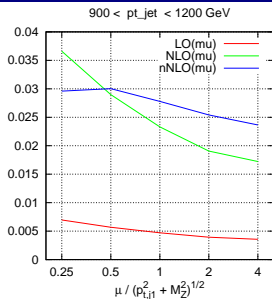
$$\sum_{\text{all diagrams}} w_n = \sum_{\ell=0}^v (-1)^\ell \binom{v}{\ell} = 0, \quad \ell - \text{number of loops, } v - \text{maximal } \ell$$

The principle of the method is simple. There is, however, a number of issues that need to be addressed to fully specify the procedure and make it usable:

- ▶ infrared and collinear safety
- ▶ conservation of four-momentum
- ▶ choice of jet definition (algorithm, value of R)
- ▶ treatment of flavour (e.g. for processes with vector bosons)
  - ▶ Z boson can be emitted only from quarks and never itself emits
- ▶ extension to input events with exact loops



# Scale dependence: $Z + \text{jet}$



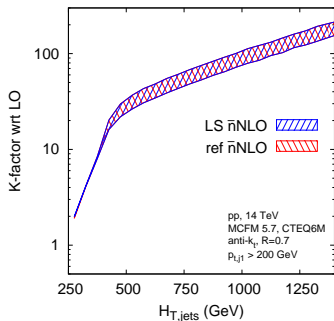
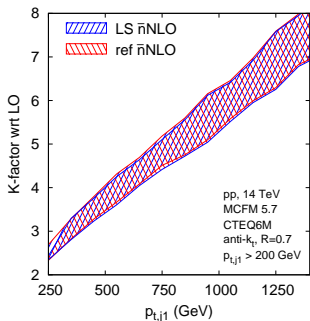
# Reference-observable method

Take a reference observable identical at LO to the observable A

$$\begin{aligned}\sigma_{Z+j@NNLO}^{(A)} &= \sigma_{Z+j@NNLO}^{(\text{ref})} + (\sigma^{(A)} - \sigma^{(\text{ref})})_{Z+j@NNLO} \\ &= \sigma_{Z+j@NNLO}^{(\text{ref})} + (\sigma^{(A)} - \sigma^{(\text{ref})})_{Z+2j@NLO}\end{aligned}$$

If the reference observable converges well

$$\sigma_{Z+j@NNLO}^{(A)} \simeq \sigma_{Z+j@NLO}^{(\text{ref})} + (\sigma^{(A)} - \sigma^{(\text{ref})})_{Z+2j@NLO}$$

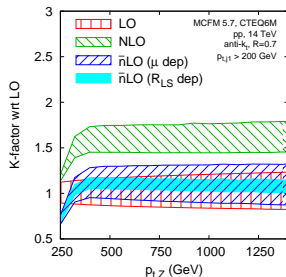


# Z+jet at NLO

- ▶  $Z + j @ \bar{n}LO = Z + j @ LO + \text{LoopSim} \circ (Z + 2j @ LO)$

# Z+jet at NLO

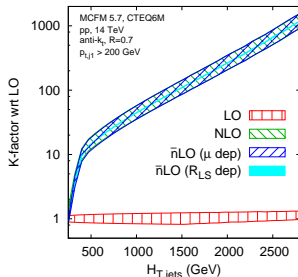
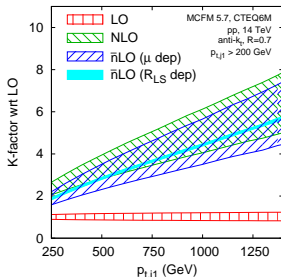
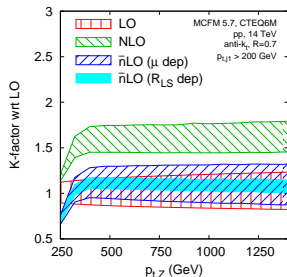
$$\blacktriangleright Z + j @ \bar{n}LO = Z + j @ LO + \text{LoopSim} \circ (Z + 2j @ LO)$$



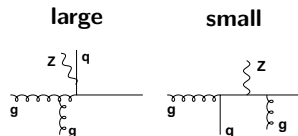
- $\blacktriangleright p_{t,Z}$  (lack of large K-factor):
  - $\blacktriangleright$  finite loop contributions matter
  - $\blacktriangleright$  correctly reproduced dip towards  $p_t = 200$  GeV

# Z+jet at NLO

$$\blacktriangleright Z + j @ \bar{n}LO = Z + j @ LO + \text{LoopSim} \circ (Z + 2j @ LO)$$

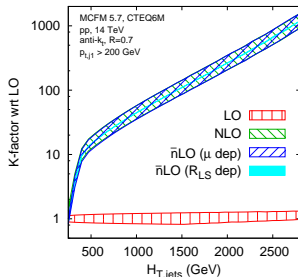
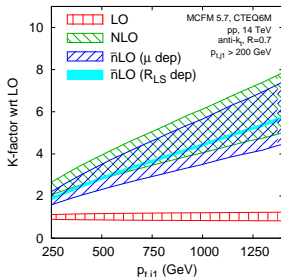
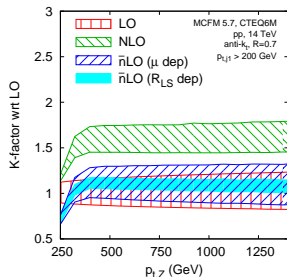


- ▶  $p_{t,Z}$  (lack of large K-factor):
  - ▶ finite loop contributions matter
  - ▶ correctly reproduced dip towards  $p_t = 200$  GeV
- ▶  $p_{t,j}$ ,  $H_{T,jets}$  (giant K-factor):
  - ▶ very good agreement between  $\bar{n}LO$  and NLO

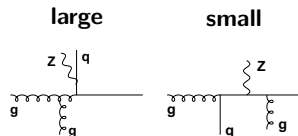


# Z+jet at NLO

$$\blacktriangleright Z + j @ \bar{n}LO = Z + j @ LO + \text{LoopSim} \circ (Z + 2j @ LO)$$

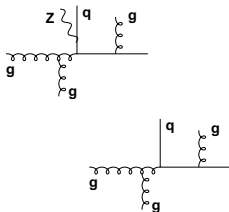


- $p_{t,Z}$  (lack of large K-factor):
  - finite loop contributions matter
  - correctly reproduced dip towards  $p_t = 200$  GeV
- $p_{t,j}$ ,  $H_{T,jets}$  (giant K-factor):
  - very good agreement between  $\bar{n}LO$  and NLO
- small R uncertainties – driven only by subleading diagrams



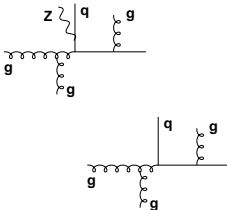
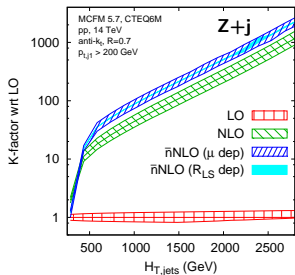
# $H_T$ type observables at $\bar{n}$ NLO for $Z$ +jet and for dijets

- ▶  $Z$ +jet at NNLO like dijets at NLO  
(same topology,  $Z$  only provides the enhancement  $\mathcal{O}(\alpha_s \ln^2 p_{t,j1}/m_Z)$ )



# $H_T$ type observables at $\bar{n}$ NLO for $Z$ +jet and for dijets

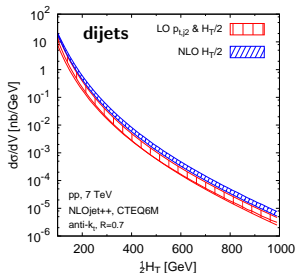
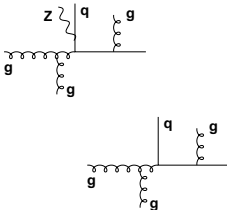
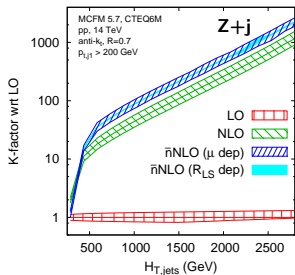
- ▶  $Z$ +jet at NNLO like dijets at NLO  
(same topology,  $Z$  only provides the enhancement  $\mathcal{O}(\alpha_s \ln^2 p_{t,j1}/m_Z)$ )





# $H_T$ type observables at $\bar{n}$ NLO for $Z$ +jet and for dijets

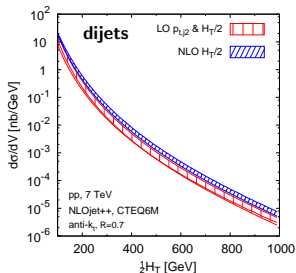
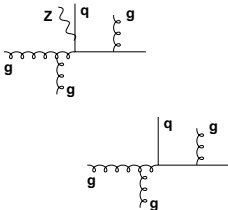
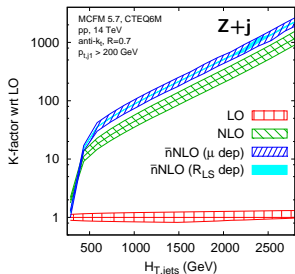
- ▶  $Z$ +jet at NNLO like dijets at NLO  
(same topology,  $Z$  only provides the enhancement  $\mathcal{O}(\alpha_s \ln^2 p_{t,j1}/m_Z)$ )



- ▶  $H_T$  for dijets receives large contributions at NLO!
  - ▶ caused by appearance of the third jet from initial state radiation

# $H_T$ type observables at $\bar{n}$ NLO for $Z$ +jet and for dijets

- ▶  $Z$ +jet at NNLO like dijets at NLO  
(same topology,  $Z$  only provides the enhancement  $\mathcal{O}(\alpha_s \ln^2 p_{t,j1}/m_Z)$ )

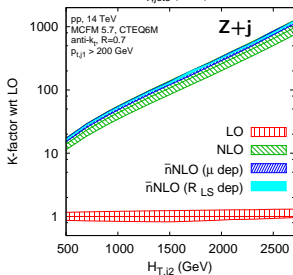
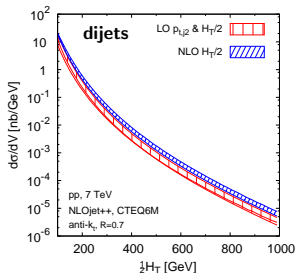
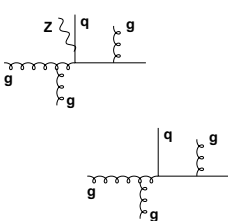
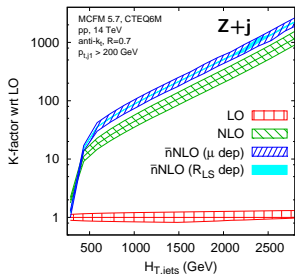


- ▶  $H_T$  for dijets receives large contributions at NLO!
  - ▶ caused by appearance of the third jet from initial state radiation
- ▶ if the same is valid for  $Z + j$  we should see only small correction for  $H_{T,j2} = \sum_{i=1}^2 p_{t,ji}$

# $H_T$ type observables at $\bar{n}$ NLO for $Z$ +jet and for dijets

## ▶ $Z$ +jet at NNLO like dijets at NLO

(same topology,  $Z$  only provides the enhancement  $\mathcal{O}(\alpha_s \ln^2 p_{t,j1}/m_Z)$ )



## ▶ $H_T$ for dijets receives large contributions at NLO!

- ▶ caused by appearance of the third jet from initial state radiation

## ▶ if the same is valid for $Z + j$ we should see only small correction for $H_{T,j2} = \sum_{i=1}^2 p_{t,ji}$

- ▶ and indeed it is small!