



# SM Higgs boson search at CMS

# Five slides on statistics

(many more in backup)

# What is $\mu$ ?

SM Higgs boson cross section:  $\sigma_{SM}$

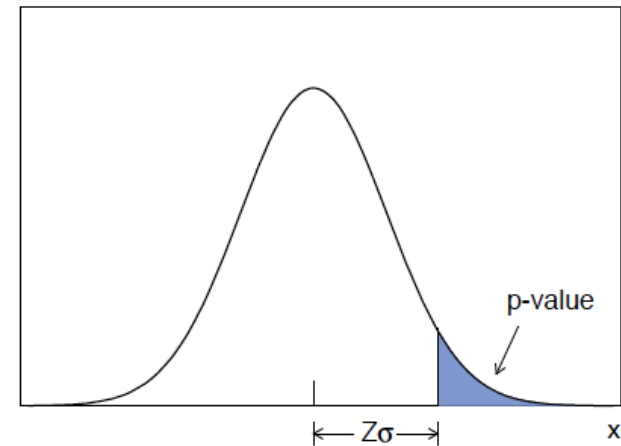
Hypothetical Higgs boson cross section:  $\sigma = \mu \sigma_{SM}$

# Excesses

- ***p-value***: chance of bkgd fluctuating as high as or higher than what has been observed in data

$$p = P( n \geq n_{\text{obs}} \mid b )$$

- ***significance Z*** is related to *p-value* via the tail probability of the normal distribution



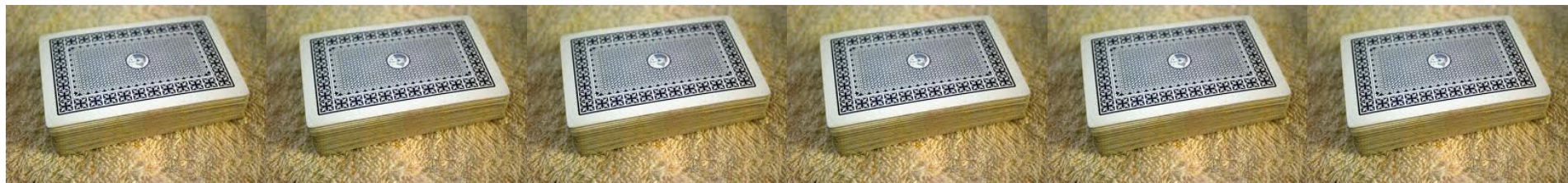
- *p-value* does not tell us whether the excess is consistent with the SM Higgs boson CS. Hence, we also quote the **best-fit value of the signal strength modifier  $\hat{\mu}$**

# Look-elsewhere effect (LEE)



What is the chance that the top card in **a deck** is Queen of Hearts?

*Local  $p$ -value*



What is the chance that the top card in **at least one of N decks** is Queen of Hearts?

*Global  $p$ -value*

The fact that the two answers are not the same is known under a fancy name **Look-Elsewhere Effect**. The ratio of the two probabilities = **trials factor**.

# Limits

- **CL<sub>s</sub> method:** “know your odds”

There are other methods available. ATLAS and CMS agreed on CL<sub>s</sub>, or, more accurately, on one particular flavor of it.

$$CL_s = \frac{P( n \leq n_{\text{obs}} \mid b + s_{\text{SM}} )}{P( n \leq n_{\text{obs}} \mid b )}$$

- **Confidence Level:**

$CL_s < \alpha \implies$  “SM signal is excluded with  $1-\alpha$  Confidence Level”.

95% C.L. ( $\alpha < 0.05$ ) is a popular convention for an exclusion...

- **Signal strength modifier  $\mu$  excluded at 95% C.L.:**

common factor by which all the SM Higgs boson event yields are to be rescaled ( $\sigma = \mu \times \sigma_{\text{SM}}$ ) in order to exclude the modified signal at 95% C.L.

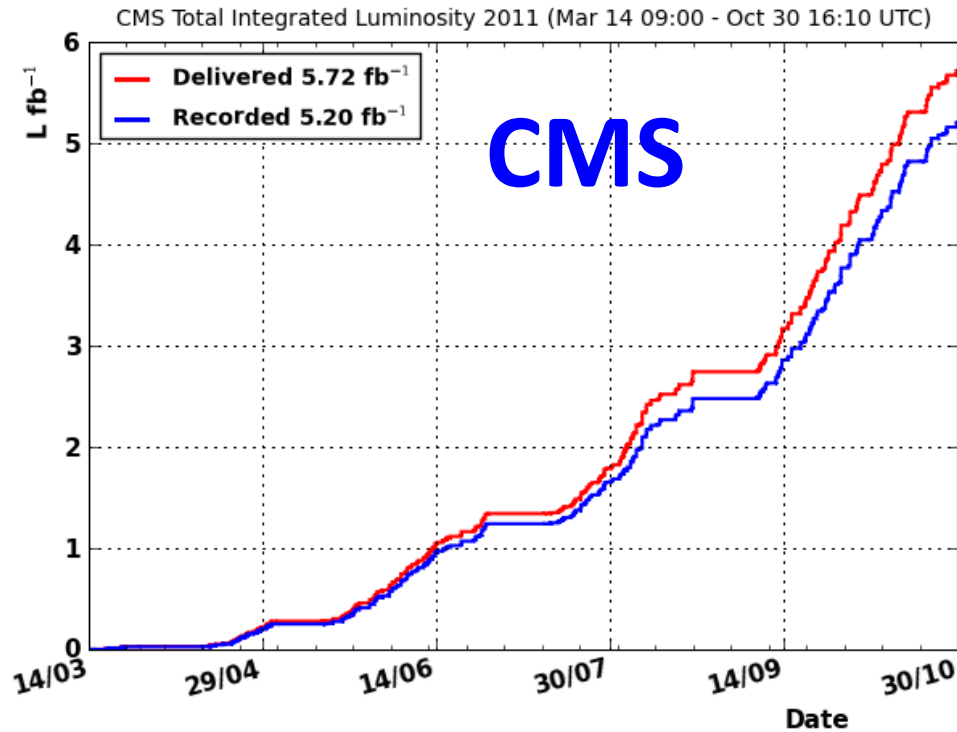
# Real multi-channel combination

- **Many channels:**
  - **Choices on Observation** → **TestStatistic conversion**
- **Systematic uncertainties:**
  - **Choices on modeling uncertainties**
  - **Choices on handling uncertainties in combination**
  - **Choices on correlations of uncertainties**

# CMS Performance



# LHC performance in 2011



>5 fb<sup>-1</sup> delivered.  
LHC target for this year  
was 1 fb<sup>-1</sup> per exp.

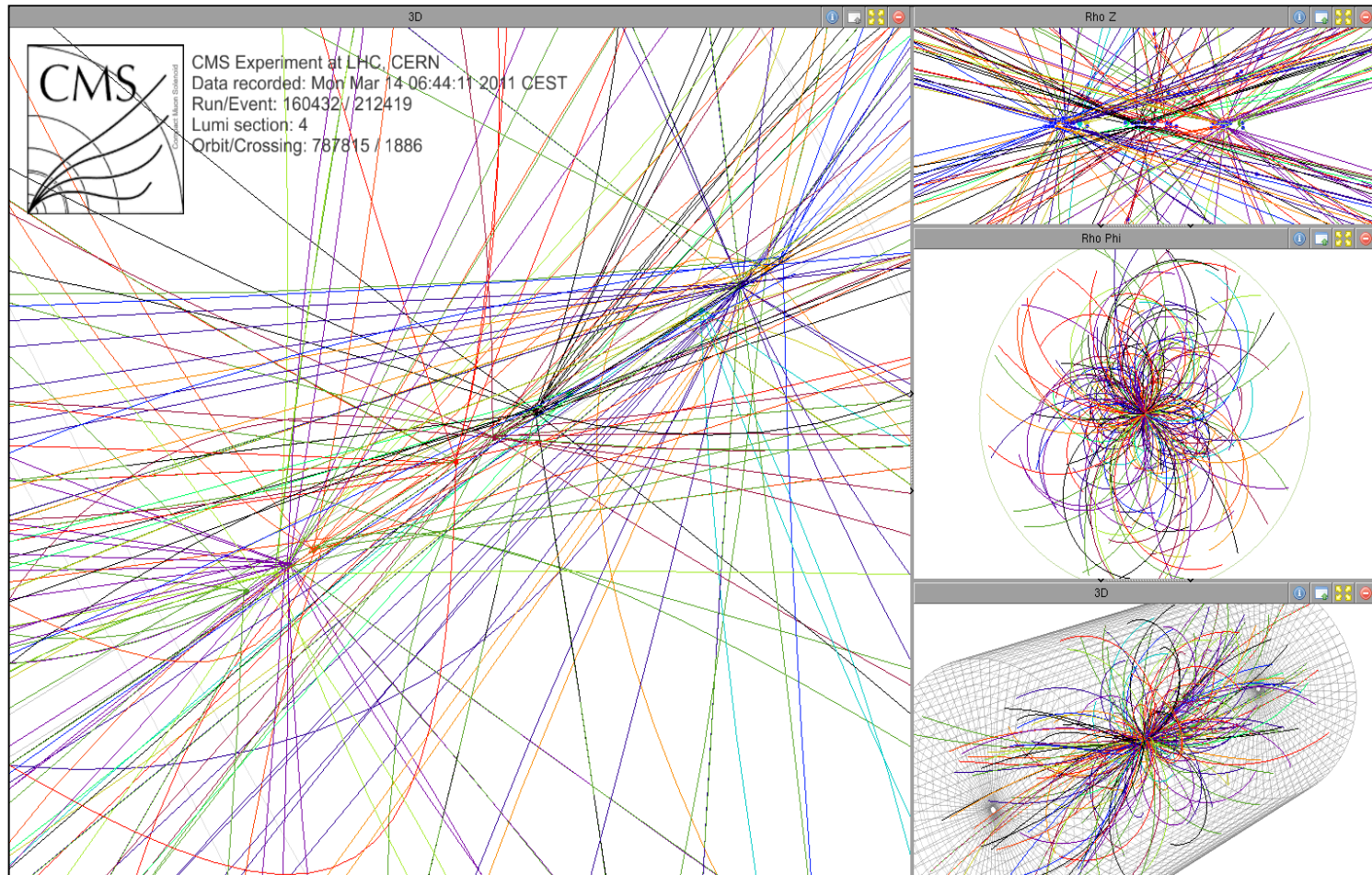
Max luminosity  
 $L = 3.5 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$

**Rapid increase in instantaneous luminosity:**

April ( $L=2 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ ) – October ( $3.5 \times 10^{33}$ )

**We have been collecting per day more data than 4 x (entire 2010 run)**

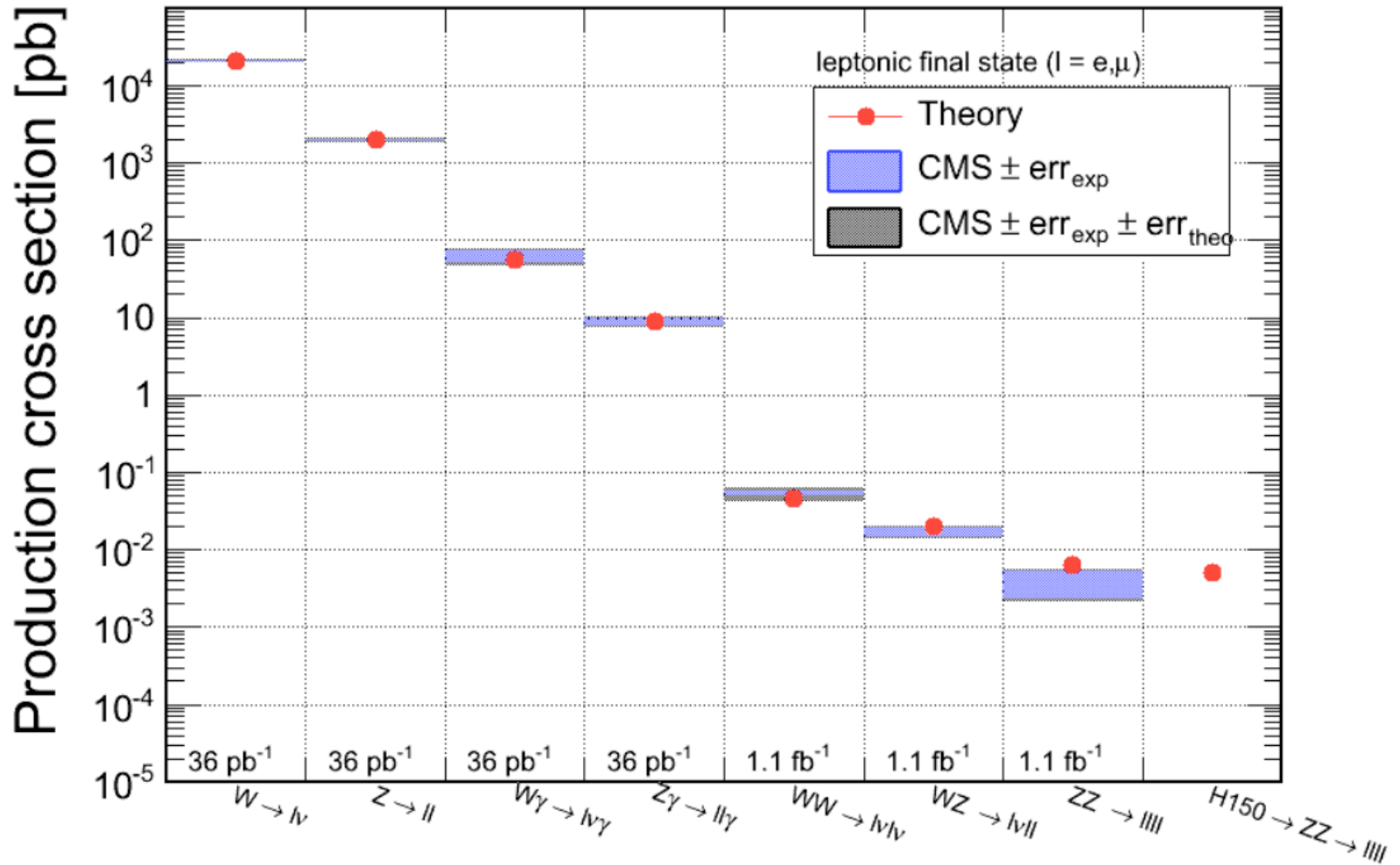
# Pile-up



**On average, 2011 data have 6 pile-up events per BX**

**Shown event has 13 reconstructed vertices**

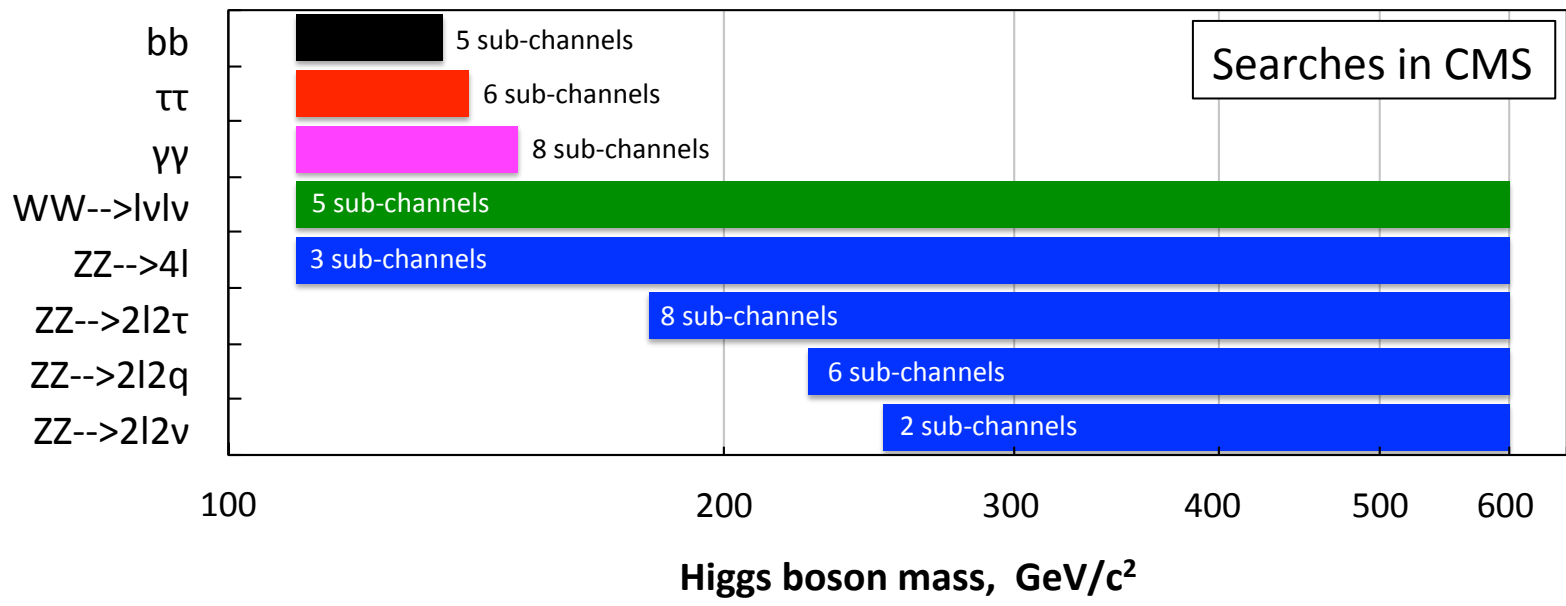
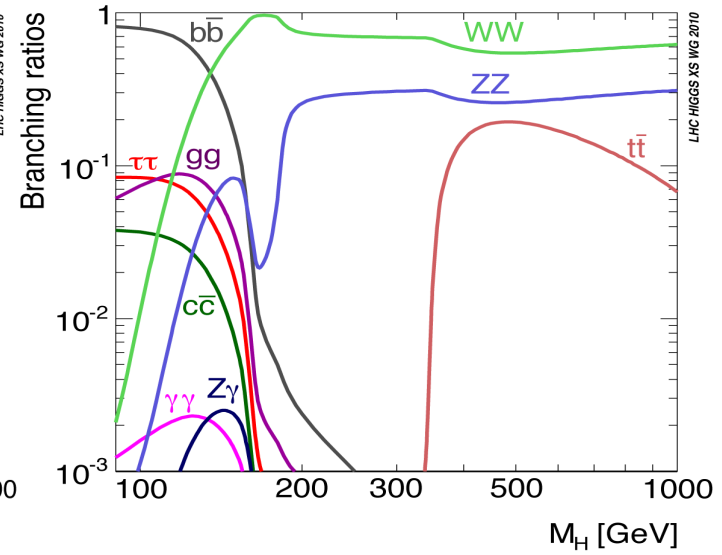
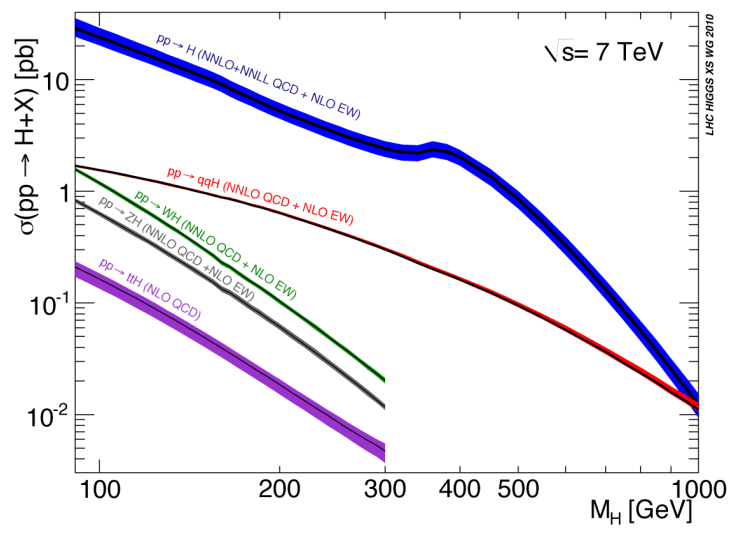
# CMS performance



QCD cross section  $> 10^{10}$  pb

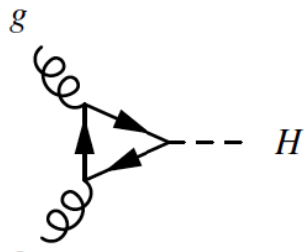
# SM Higgs searches

# SM Higgs: production, decays, searches

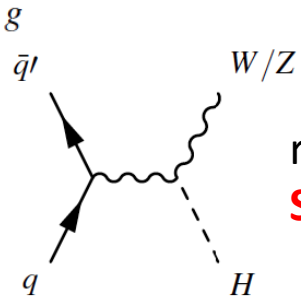


**H -> bb**

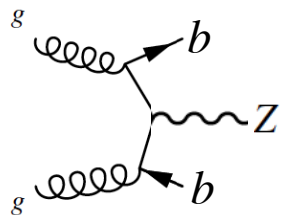
# H→bb: why is it so hard at LHC?



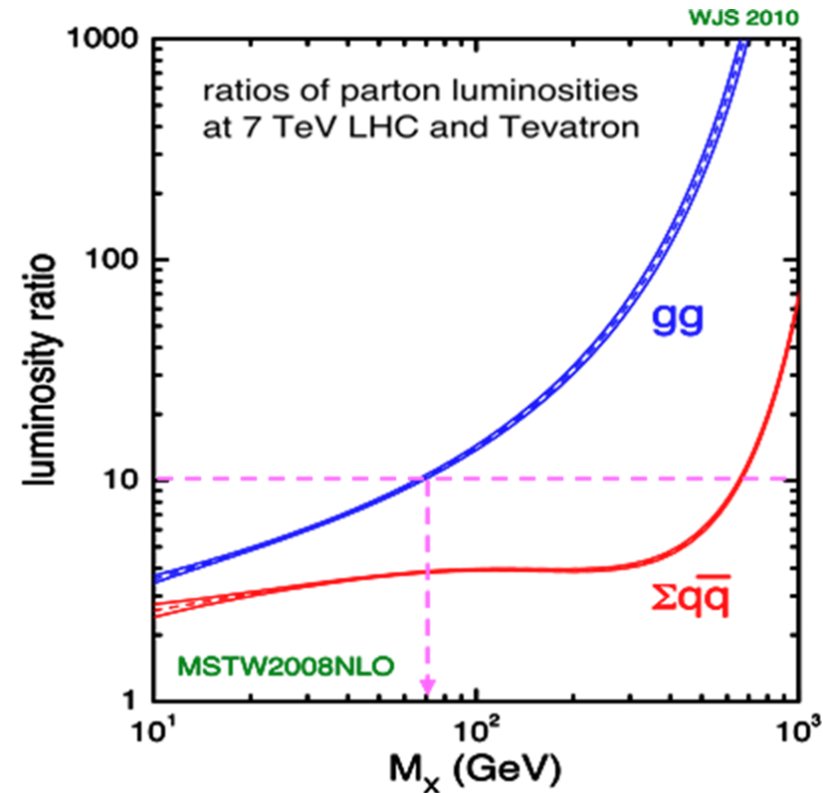
**gg-production:**  
too large bkgd



reduce bkgd by adding W/Z tags;  
**Signal: qqbar-production**

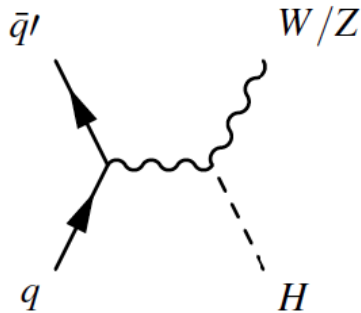


**Bkgd: gluon-enriched production**



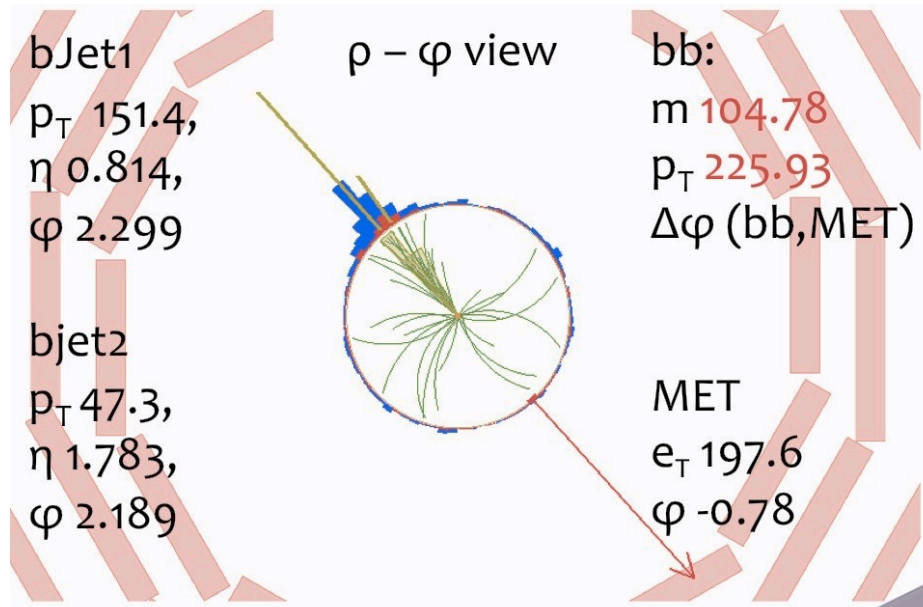
- **W/Z+H(bb)** is the main channel for low mass Higgs at Tevatron
- **At LHC (pp-collisions), S/B is 3-4 times worse than at Tevatron**

# V+H(bb) signature



## Selection:

- 5 channels:  $W \rightarrow l\nu$ ,  $Z \rightarrow ll$ ,  $Z \rightarrow \nu\nu$
- high MET quality for  $W(l\nu)$  and  $Z(\nu\nu)$
- two jets with tight b-tags
- V+H(bb) topology: back-to-back,  $\Delta\phi(V,H) > 3$
- $p_T(bb) > 100-160$  GeV (but not super boosted)
- cut-and-count on MVA output (BDT)



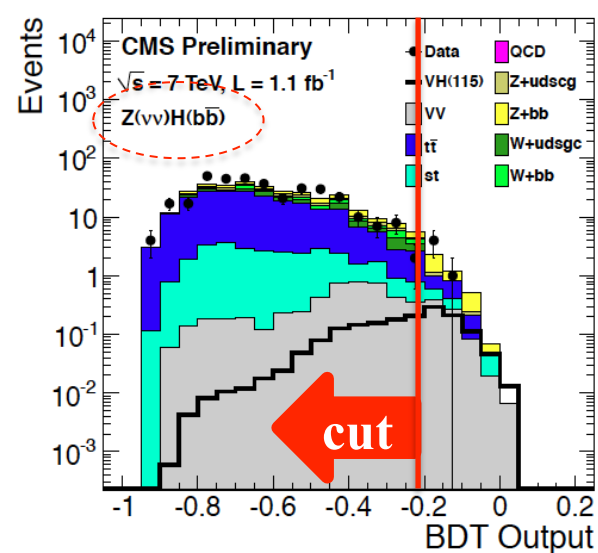
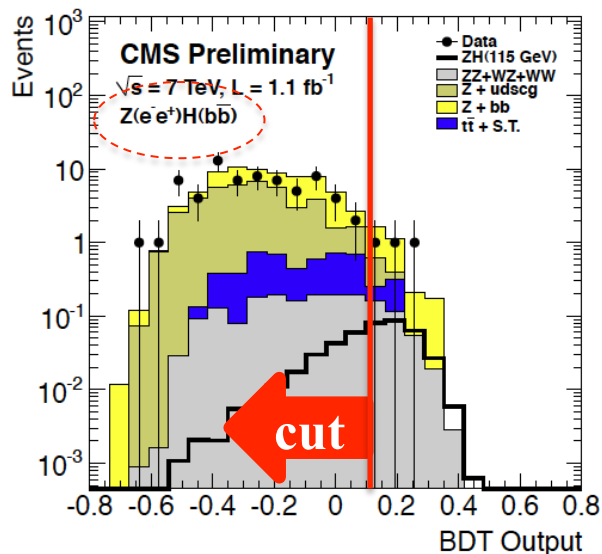
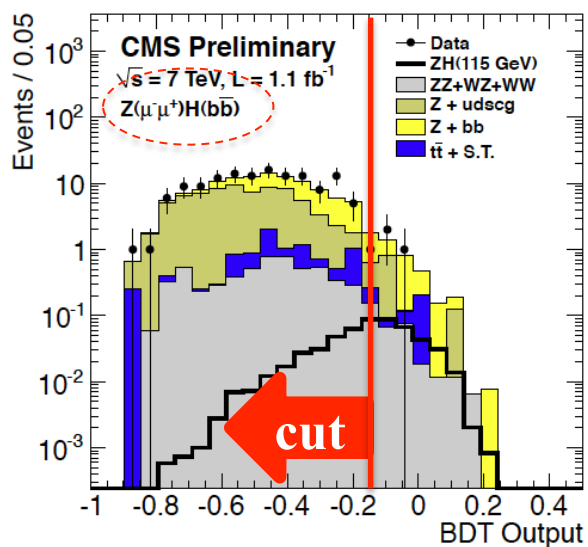
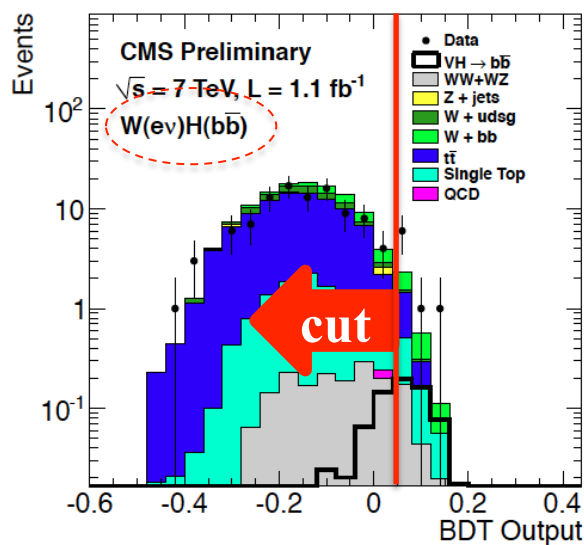
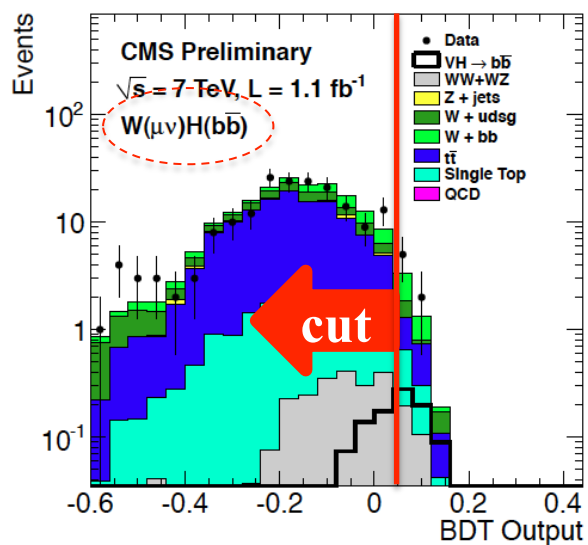
**bb mass resolution: 10%**  
 (aided by the bb-system boost)

## Main backgrounds:

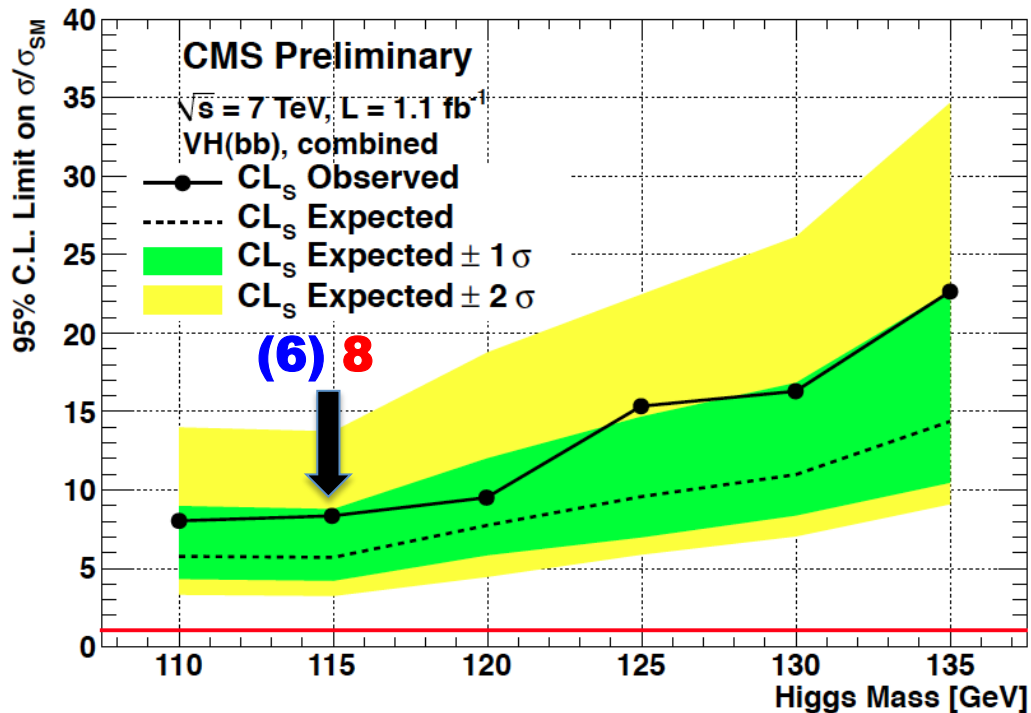
- **Vbb**: from data (invert  $p_T(bb)$  boost)
- **V+jets**: from data (invert b-tag)
- **tt**: from data (require extra jet)
- **QCD**: from data (require small  $\Delta\phi(MET, jet)$ , ...)
- **W+Z(bb) and Z+Z(bb)**: from MC



# H→bb distributions ( $m_H=115$ GeV)



# H->bb results



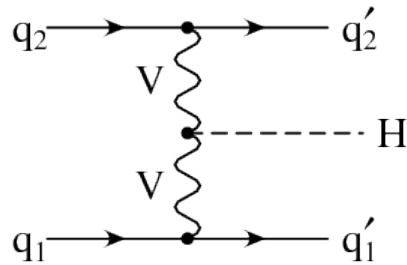
$m_H = 115 \text{ GeV}$

- Sensitivity 5.7
- Observed 8.3

Ratio of limits with/without systematic errors  $\sim 1.3$

**H ->  $\tau\tau$**

# H- $\rightarrow$ $\tau\tau$ signature



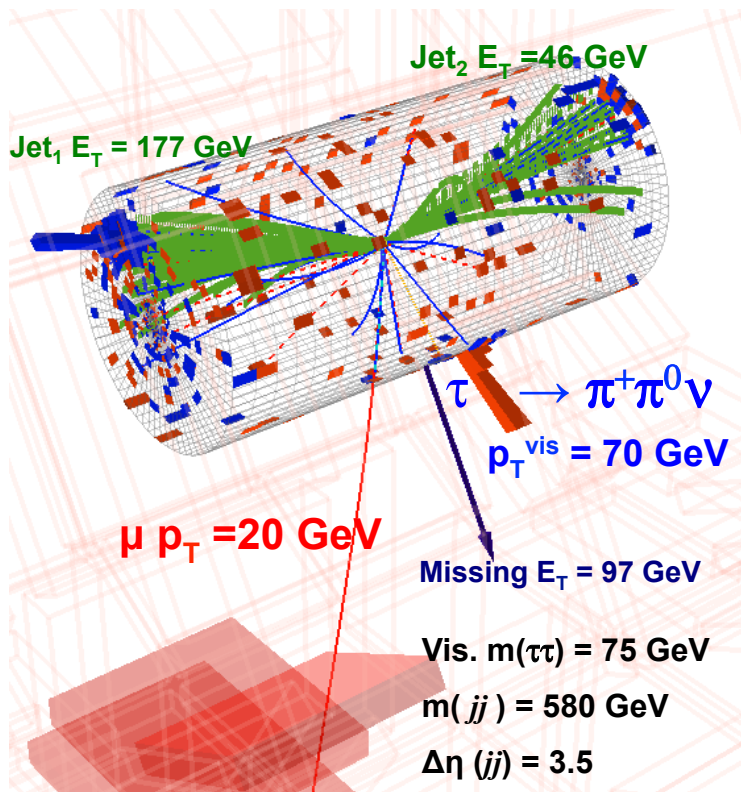
## Selection:

- 6 channels:  $\tau_e\tau_{had}$ ,  $\tau_\mu\tau_{had}$ ,  $\tau_e\tau_\mu$  (VBF, non-VBF)
- main sensitivity from VBF production: two forward jets with no jets in between
- isolated leptons
- CDF topological cut ( $p_{T1}$ ,  $p_{T2}$ , MET)
- final discriminant:  $\tau\tau$ -mass distribution

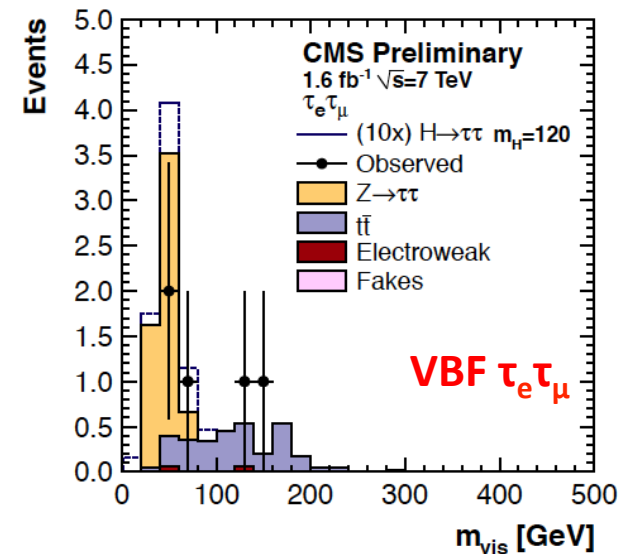
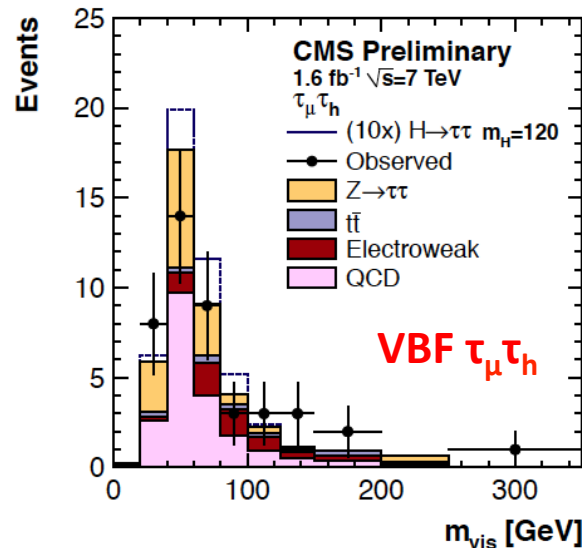
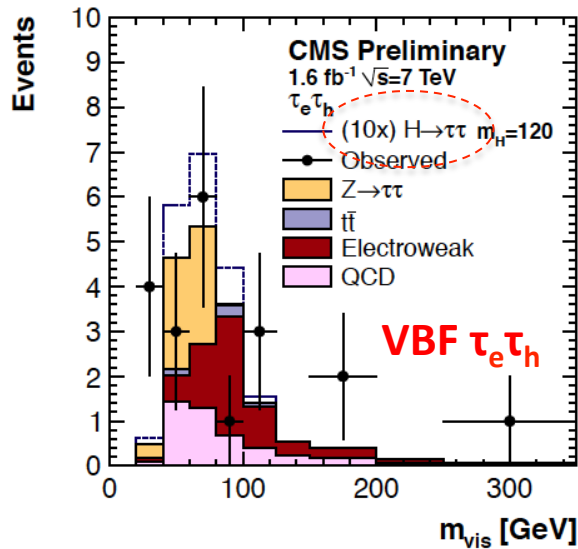
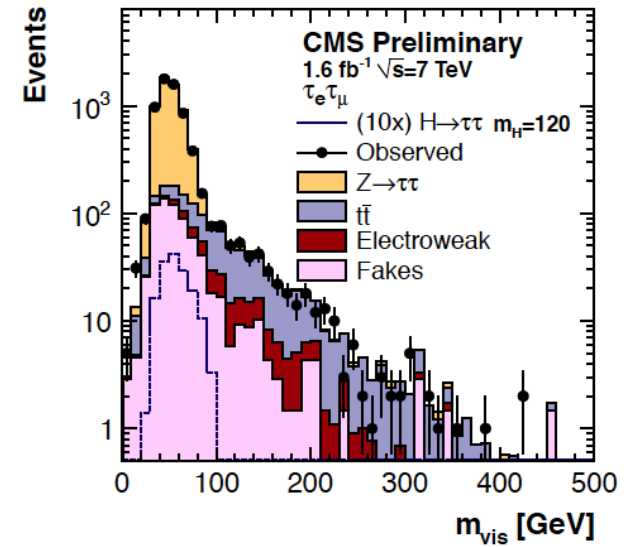
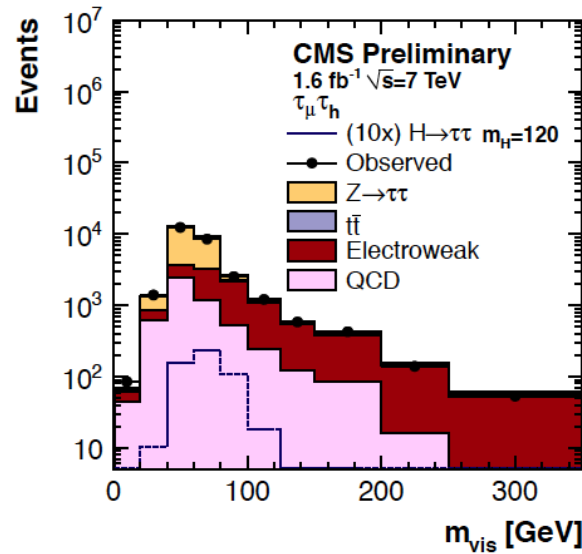
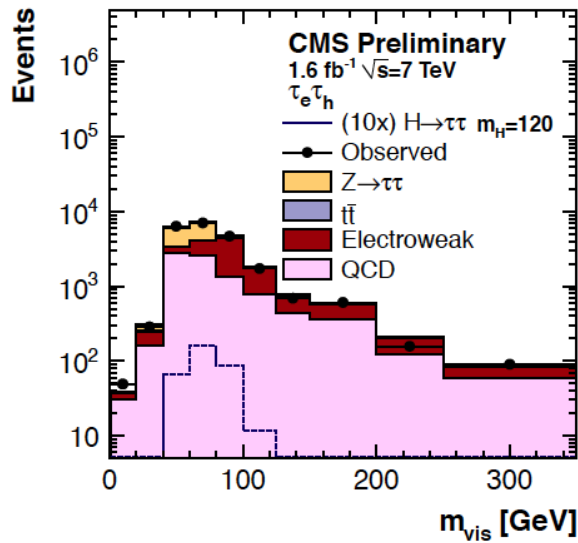
$\tau\tau$  mass resolution: 20%

## Main backgrounds:

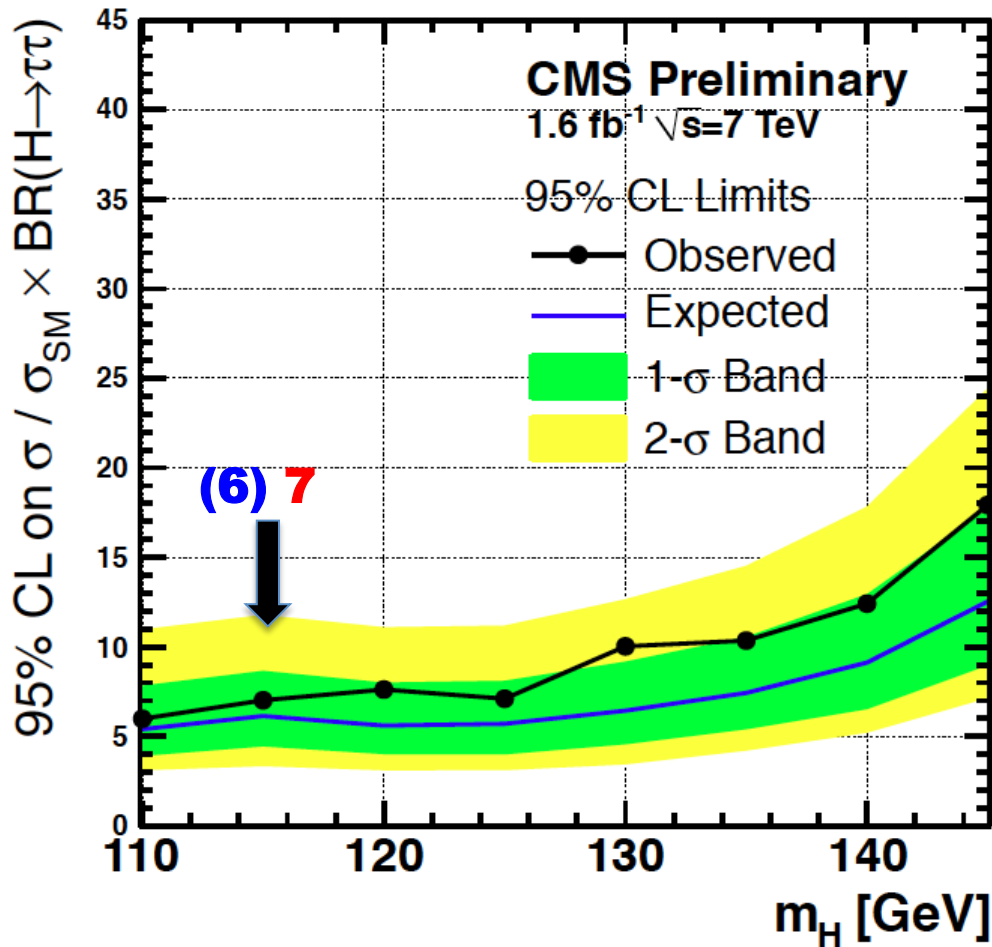
- $Z\rightarrow\tau\tau$ : from data (mass distr. fit with MC shape)
- $W$ +jets: from data (invert topological cut)
- QCD: from data (same sign)
- $t\bar{t}$ , di-bosons: from data (II events)



# H → ττ distributions



# H $\rightarrow\tau\tau$ results

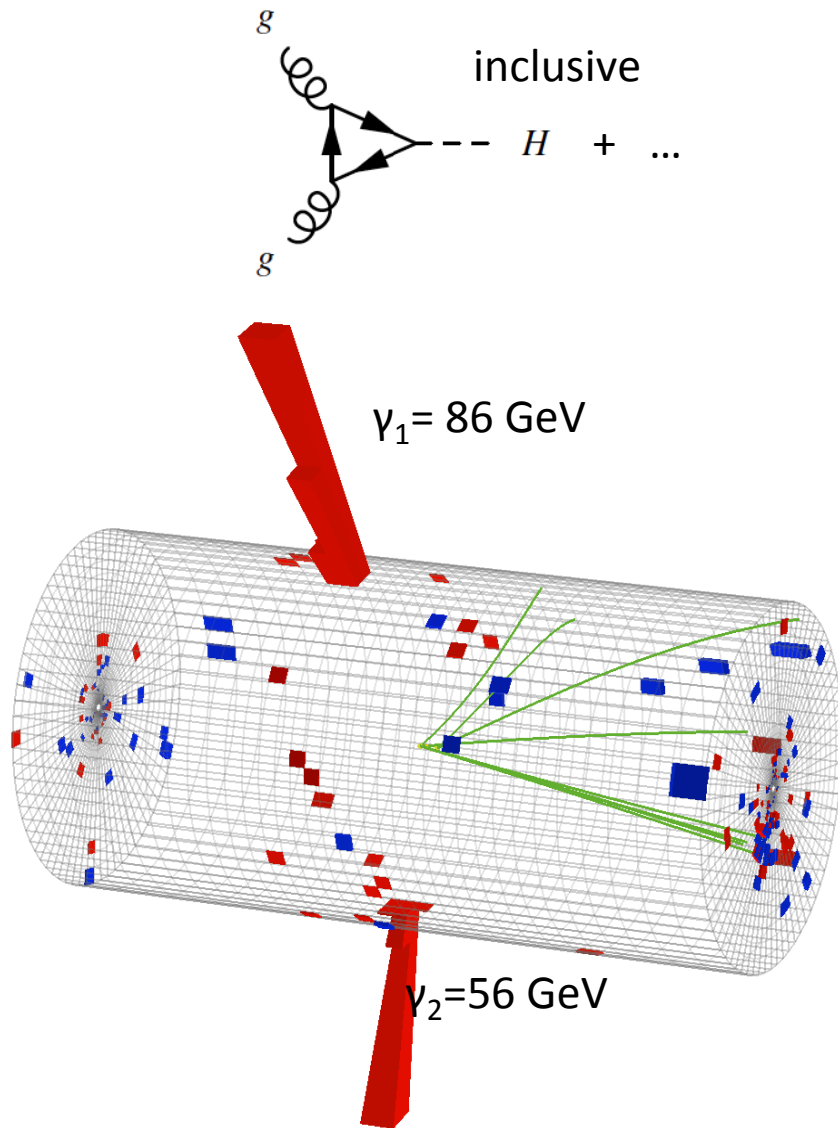


$m_H=115$  GeV

- Sensitivity 6.1
- Observed 7.0

$$H \rightarrow \gamma\gamma$$

# H- $\rightarrow\gamma\gamma$ signature

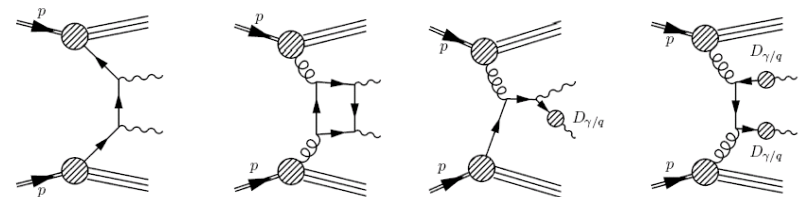


## Selection:

- inclusive production
- two isolated photons
- 4 event categories based on quality of photons and, hence, expected  $m_{\gamma\gamma}$  resolution
- Events are also split based on  $p_T(\gamma\gamma)$ , but this helps only for fermiophobic higgs
- final discriminant:  $\gamma\gamma$ -mass distributions

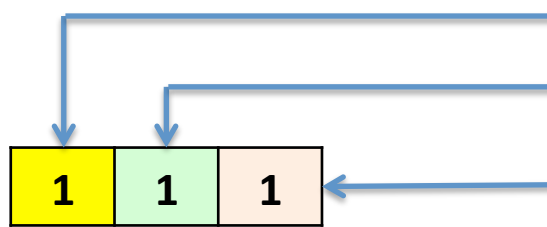
Best category  $m_{\gamma\gamma}$  resolution:  $\sim 1\%$

Main backgrounds: from sidebands





# H- $\rightarrow\gamma\gamma$ distributions

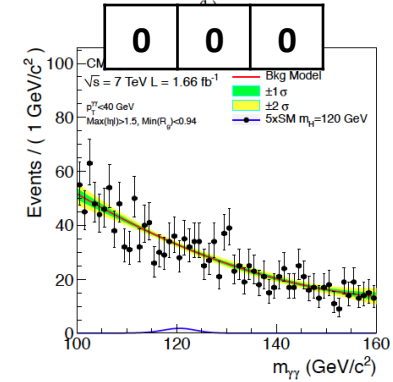
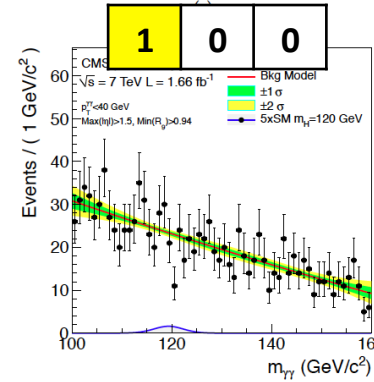
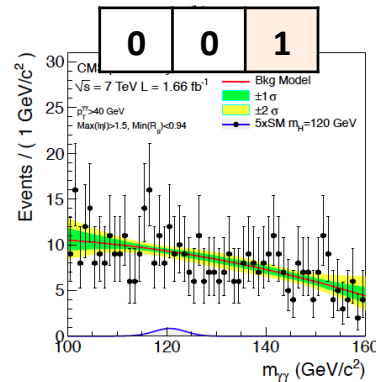
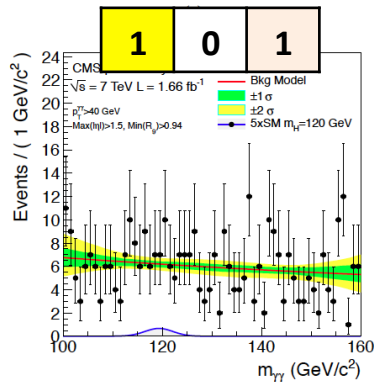
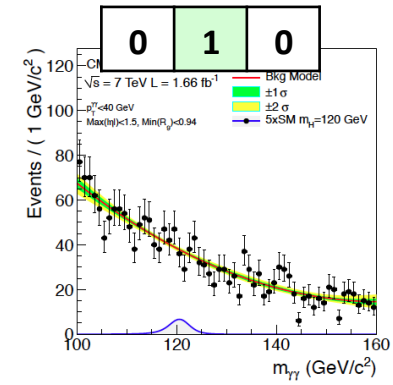
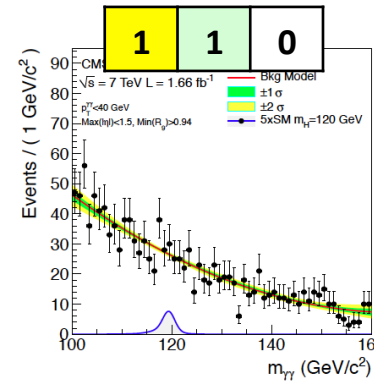
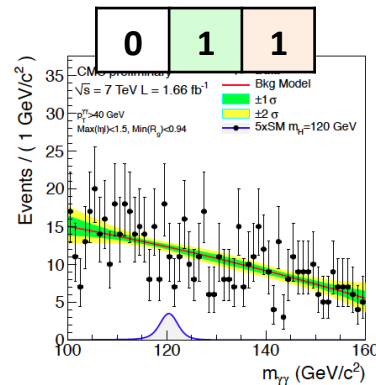
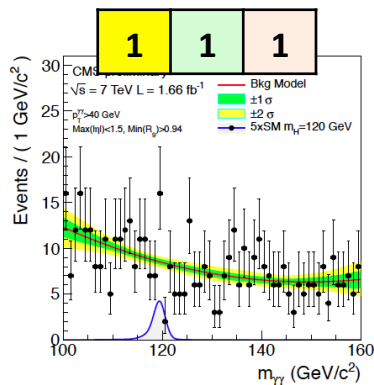


Both photons of high quality?

Both photons in barrel?

Di-photon  $p_T > 40$  GeV?

(this bit is useful for fermiophobic Higgs only)



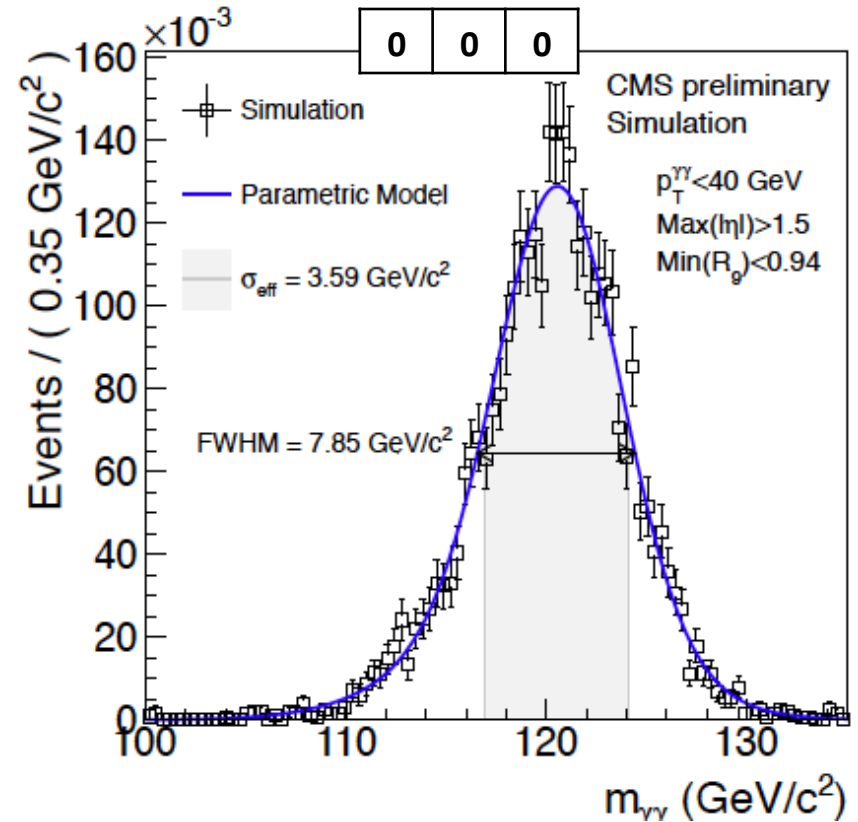
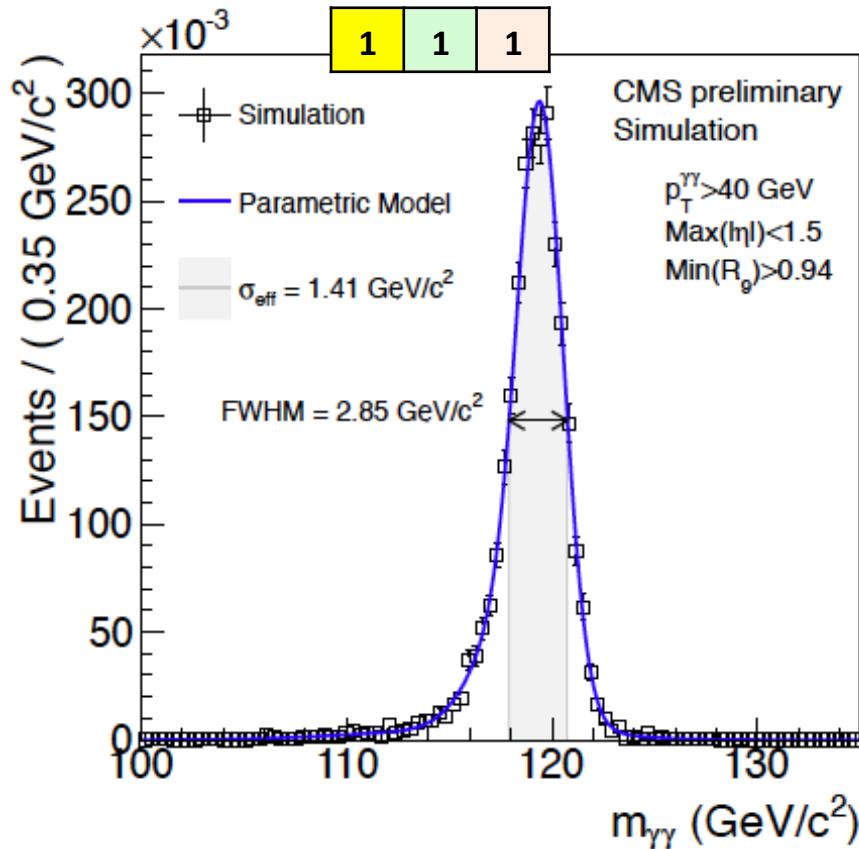
(c)

(d)

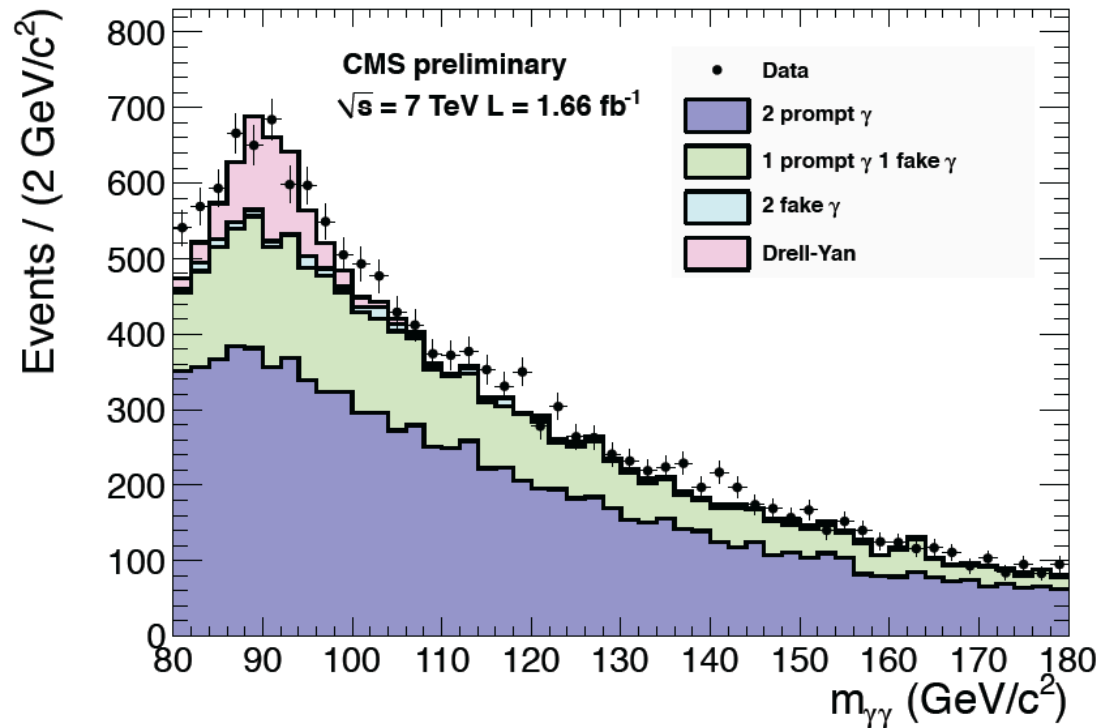
(c)

(d)

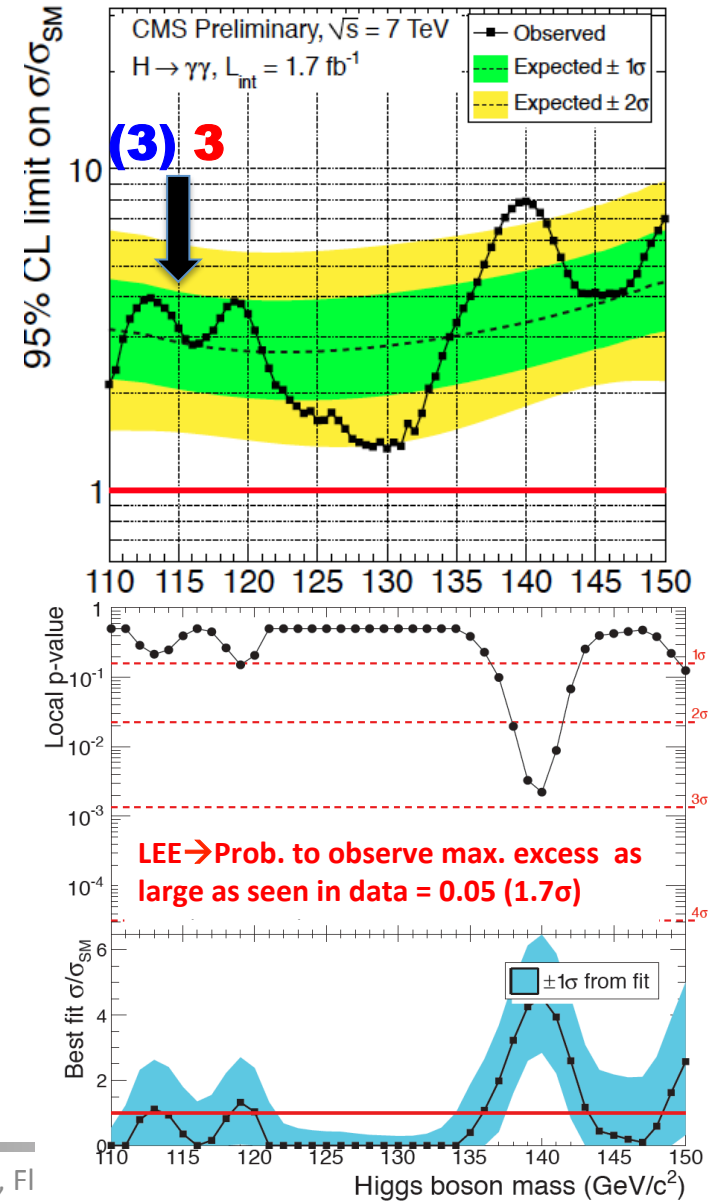
# H- $\rightarrow\gamma\gamma$ mass resolutions



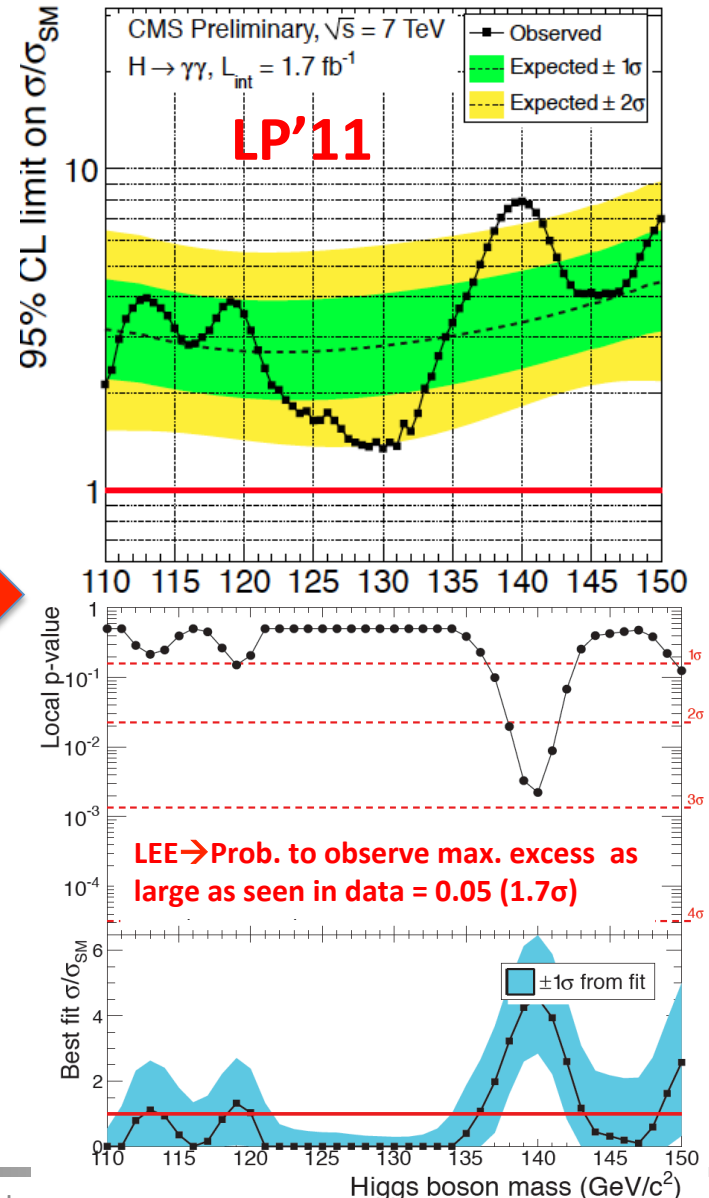
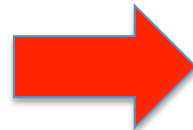
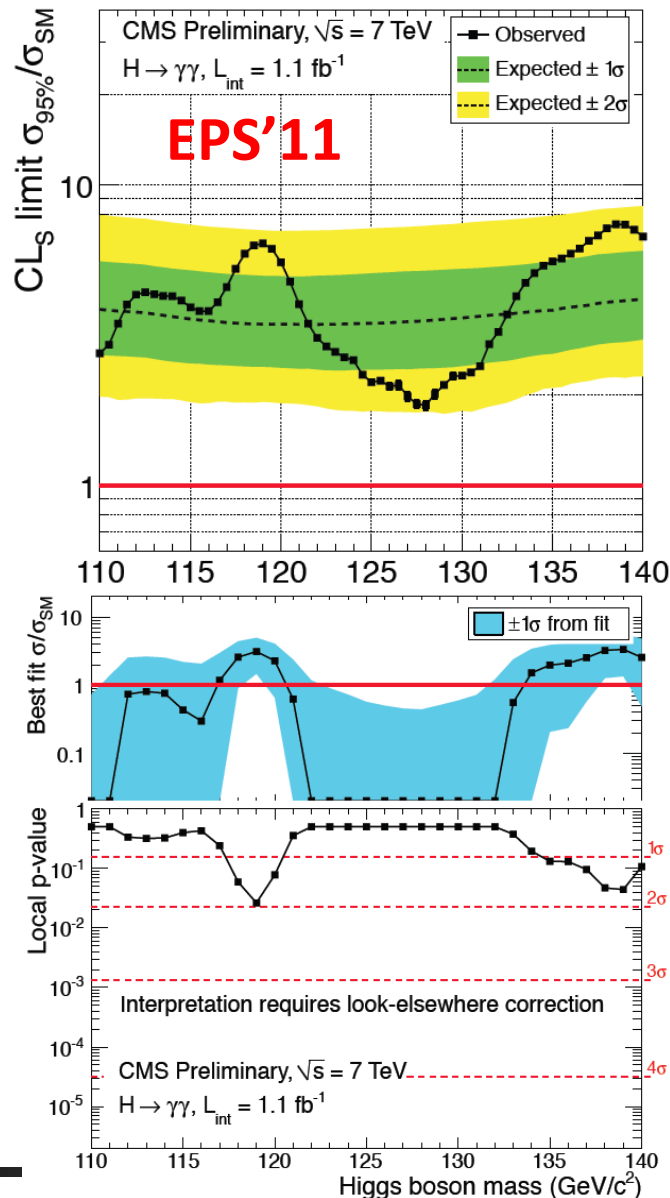
# H $\rightarrow\gamma\gamma$ results



- Bkgd MC predictions are not used in the analysis
- Mass distributions actually analyzed in 8 event categories

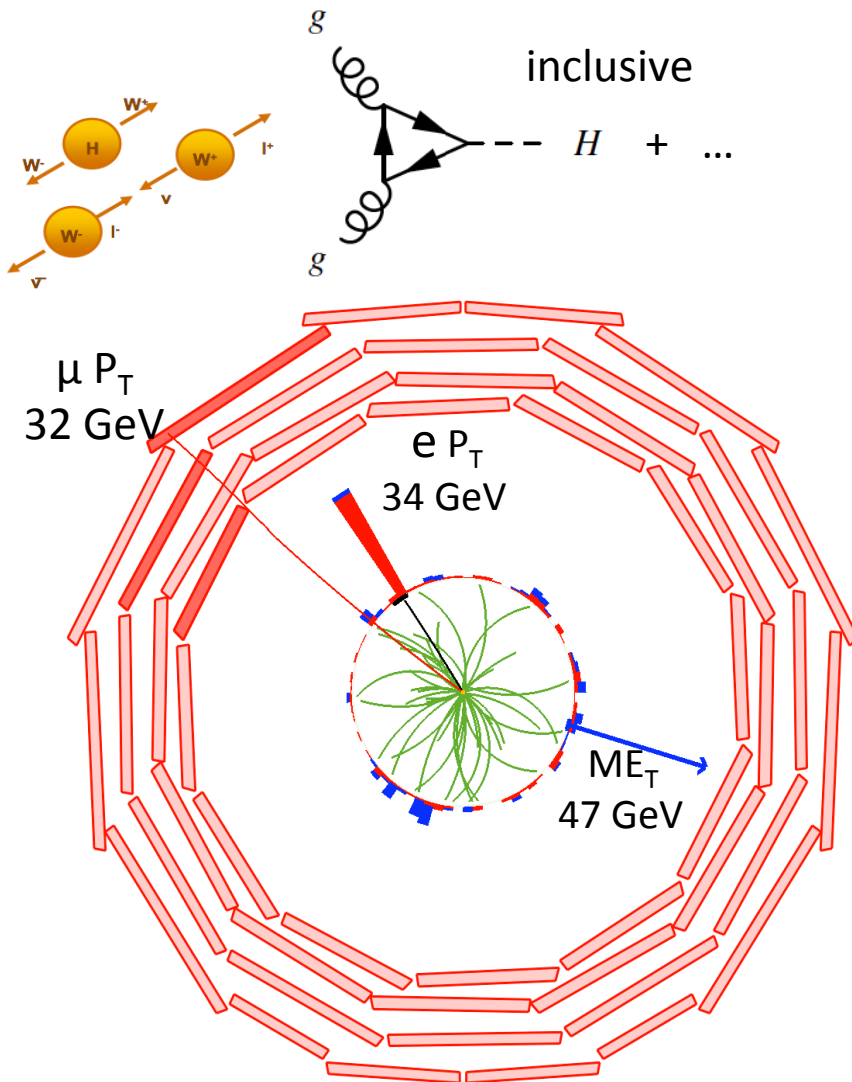


# H $\rightarrow\gamma\gamma$ results: from EPS and LP



**H -> WW**

# H- $\rightarrow$ WW- $\rightarrow$ l $\nu$ l $\nu$ signature



## Selection:

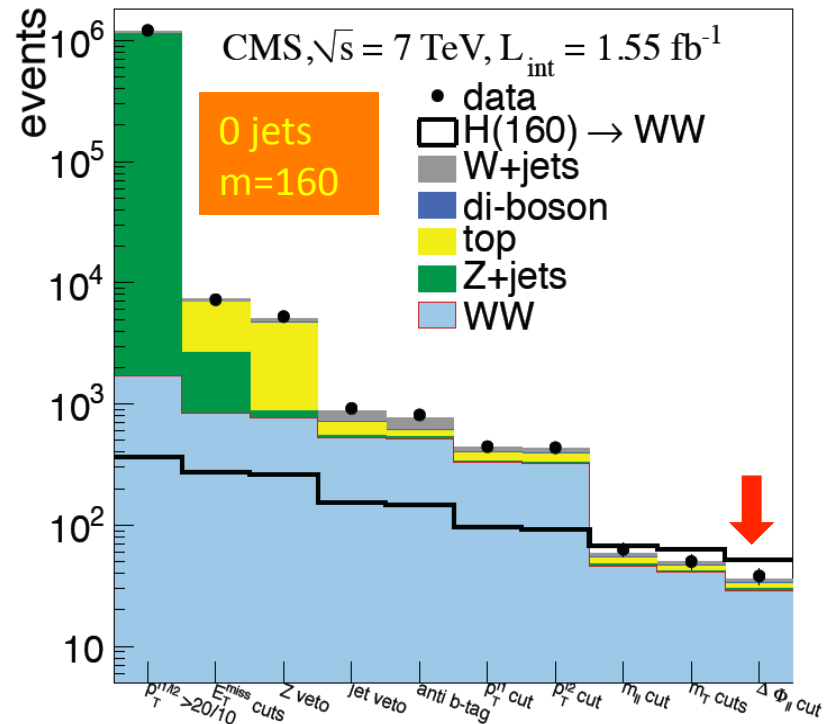
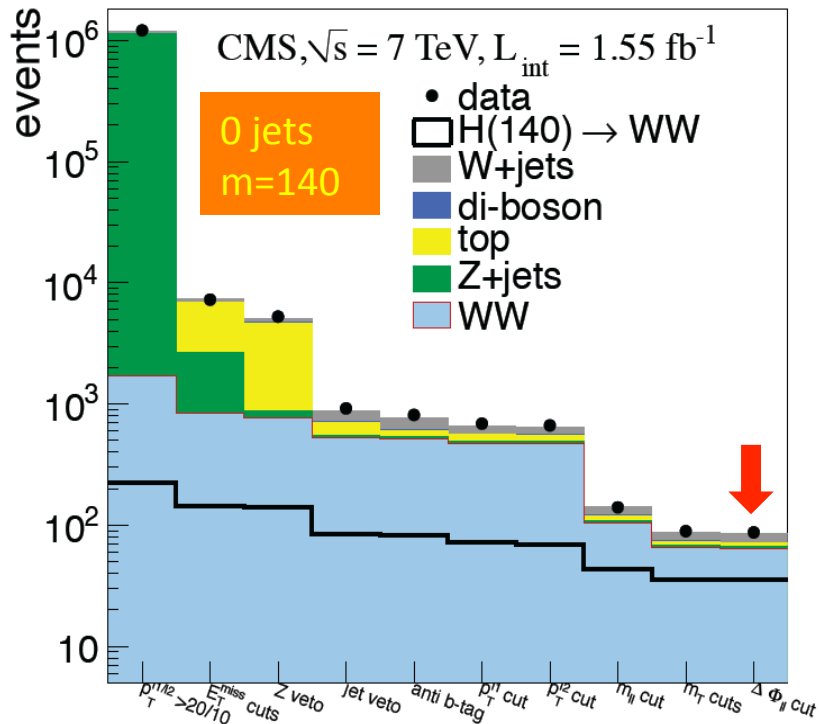
- two isolated leptons, small  $\Delta\phi$ , small  $m_{ll}$
- MET
- Transverse mass  $m_T$
- cut-and-count in 5 categories:
  - Same-Flavor di-leptons + 0 jets
  - Opposite-Flavor di-leptons + 0 jets
  - Same-Flavor di-leptons + 1 jet
  - Opposite-Flavor di-leptons + 1 jet
  - SF/OF di-leptons + 2 VBF-like jets

## Mass resolution: 20%

## Main backgrounds:

- WW( $m_H < 200$ ): from data (small di-lepton mass)
- WW( $m_H > 200$ ): from MC
- tt: from data (inverted b-tag)
- W: from data (tight-to-loose fake rate)
- Drell-Yan: from data (on-shell Z)
- WZ, ZZ: from MC

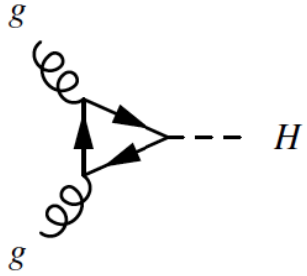
# H- $\rightarrow$ WW- $\rightarrow$ lvlv: cut flow



- **Observations:**

- remarkable agreement of data and bkgd predictions cut by cut
- for m=160, SM Higgs would give many more events than observed

# H $\rightarrow$ WW $\rightarrow$ l $\nu$ l $\nu$ distributions

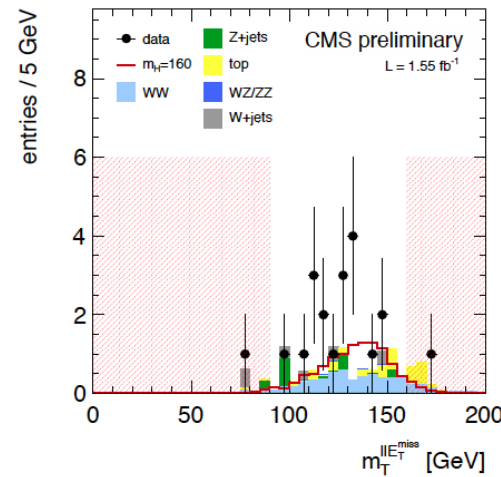
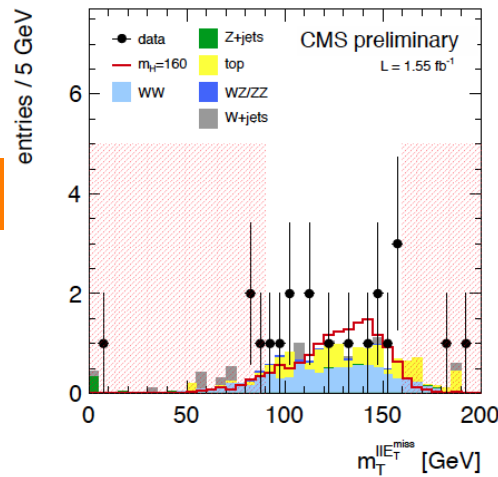
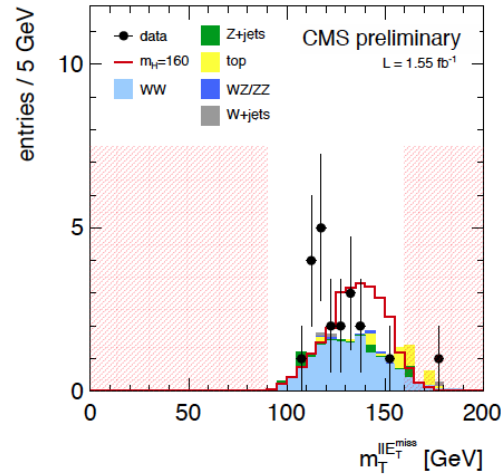
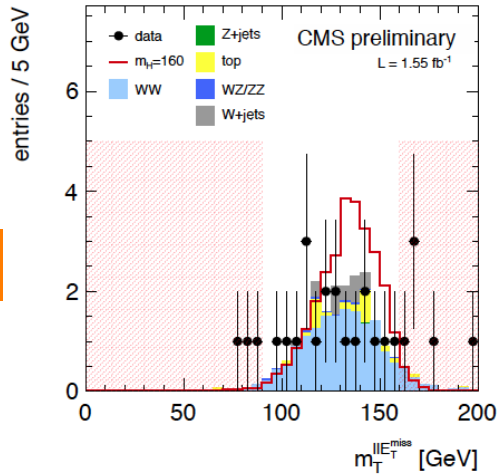


0 jets

1 jet

$e\mu$

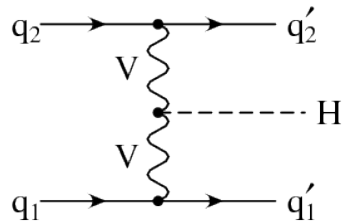
$ee + \mu\mu$



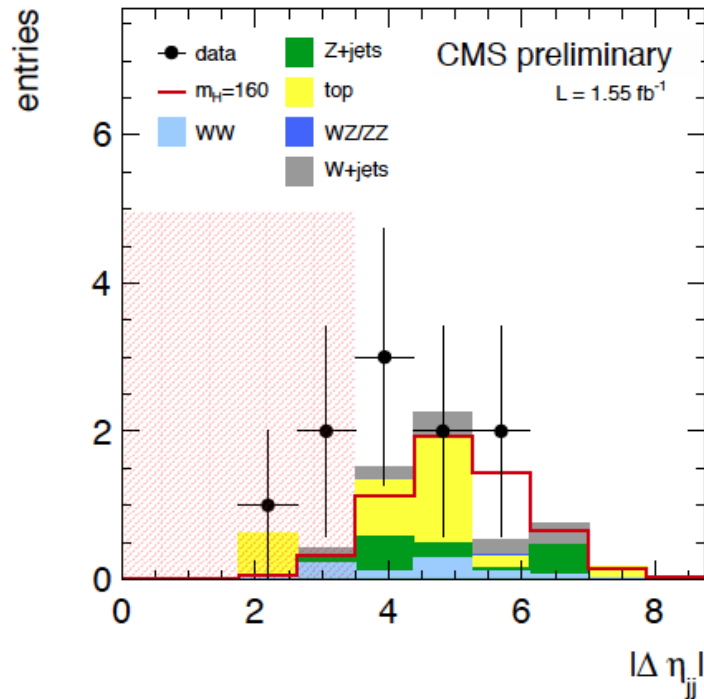
HWW signal  
is not stacked



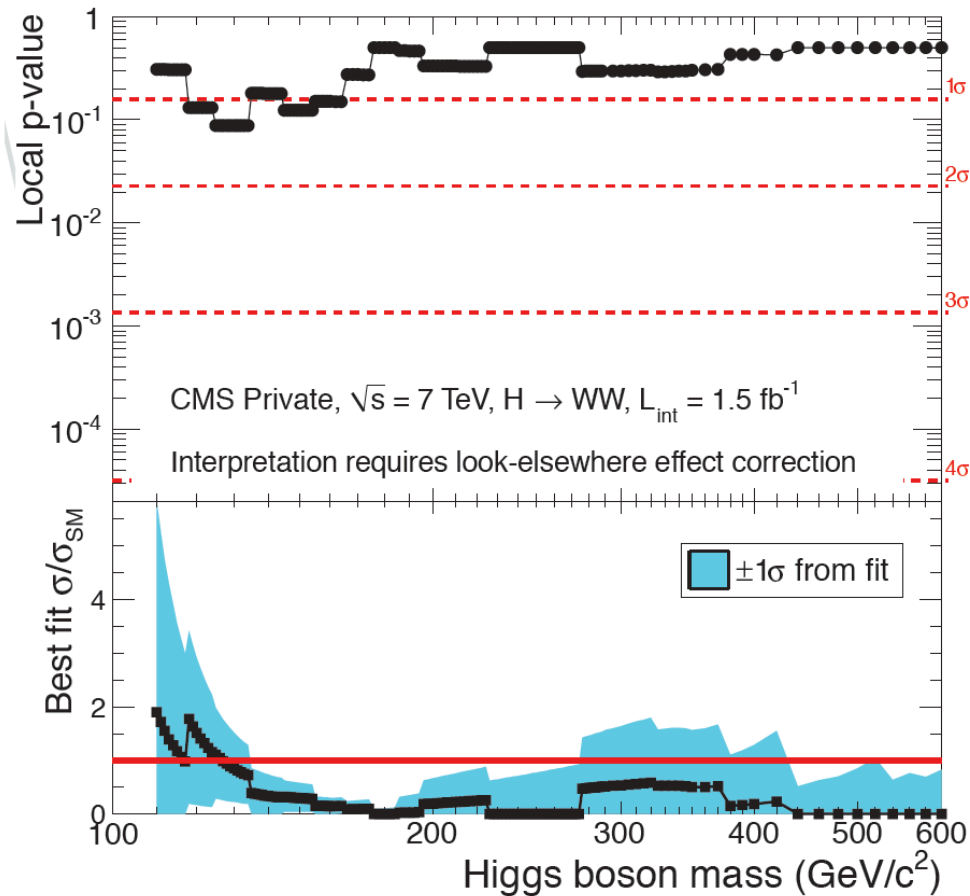
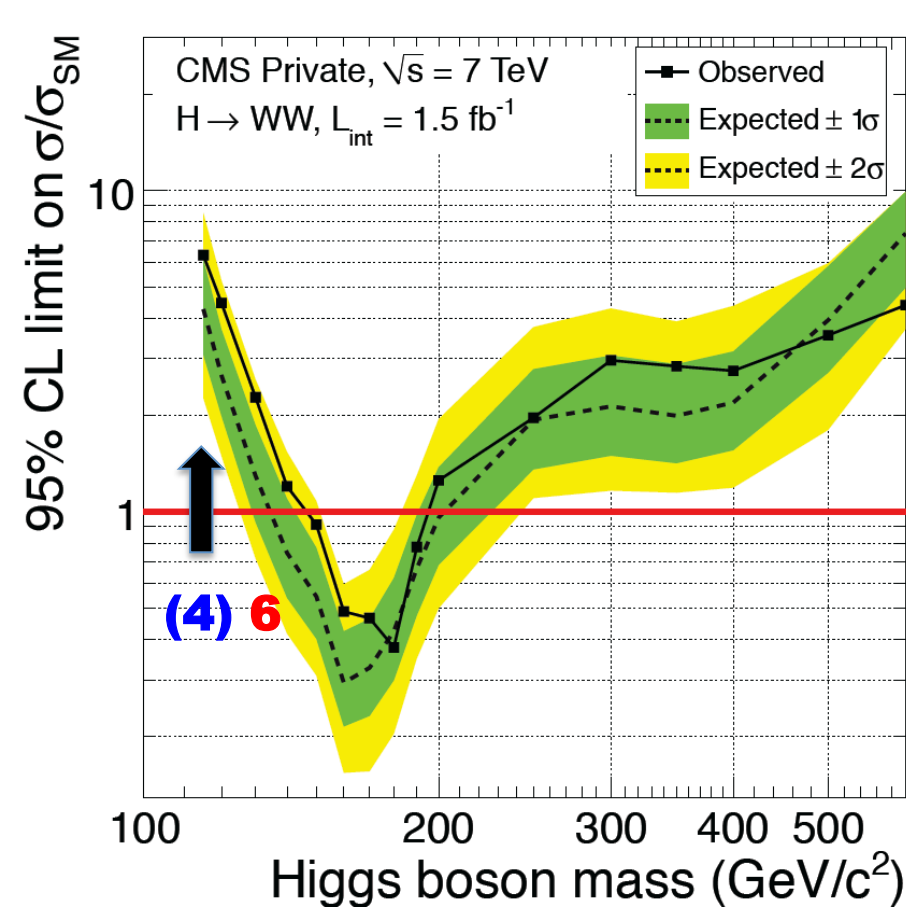
# H $\rightarrow$ WW $\rightarrow$ l $\nu$ l $\nu$ distributions



2 jets

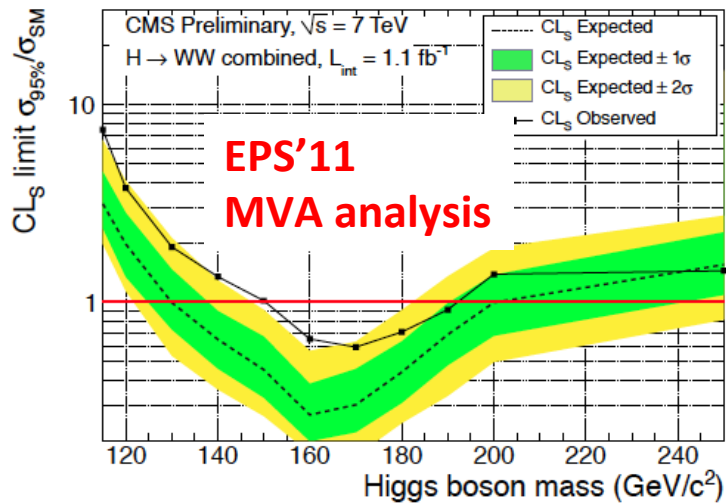


# H → WW → lνlν results

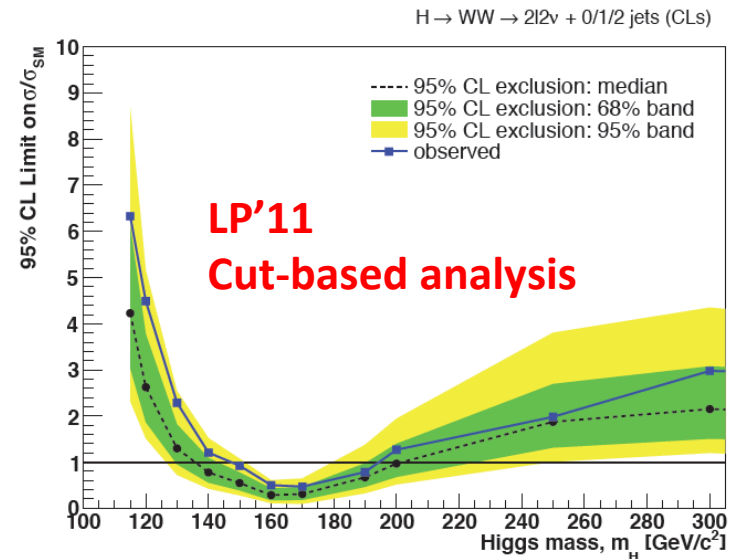
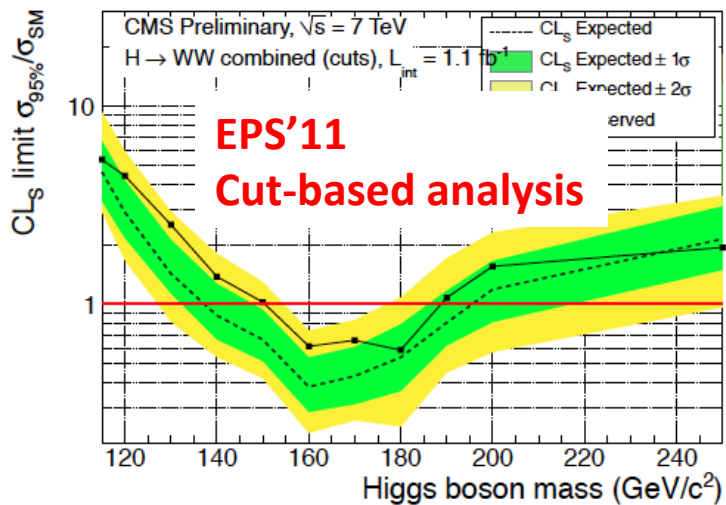
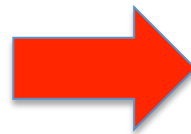


- SM Higgs boson with mass  $147 < M_H < 194 \text{ GeV}$  ruled out at 95% CL
- SM Higgs boson expected sensitivity  $136 < M_H < 200 \text{ GeV}$
- Ratio of limits at  $m_H = 130$  with/without systematic errors  $\sim 1.5$

# H → WW → lνlν results: from EPS and LP

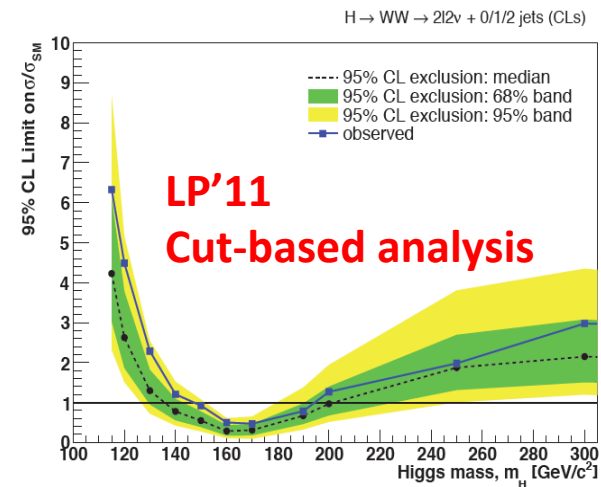
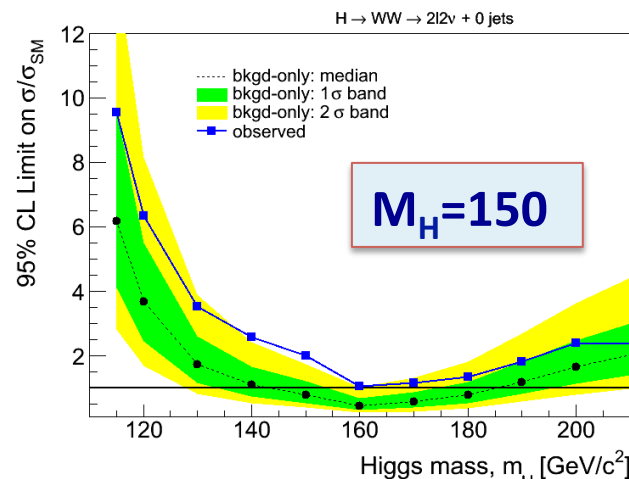
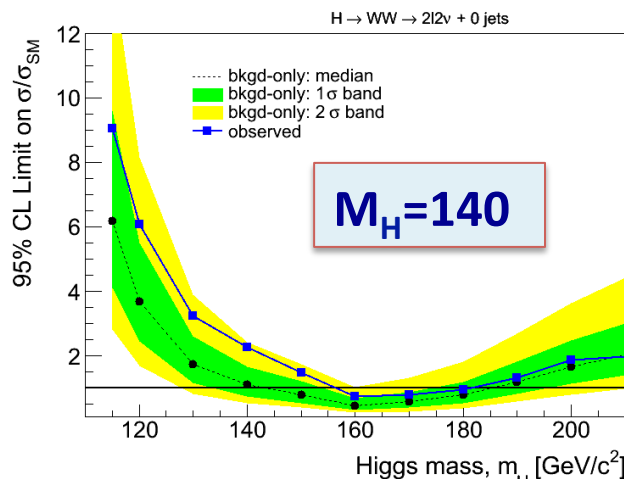
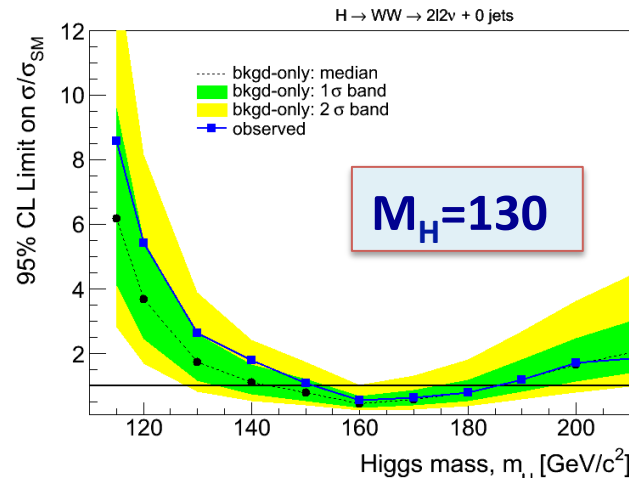
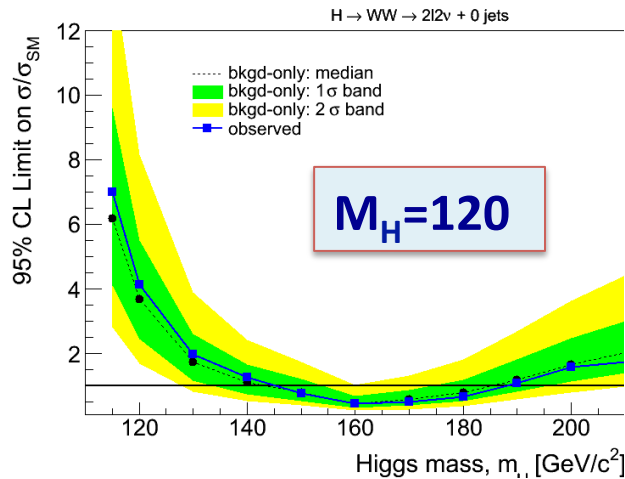


**LP'11  
MVA analysis not available**



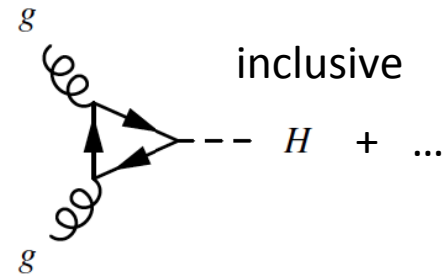
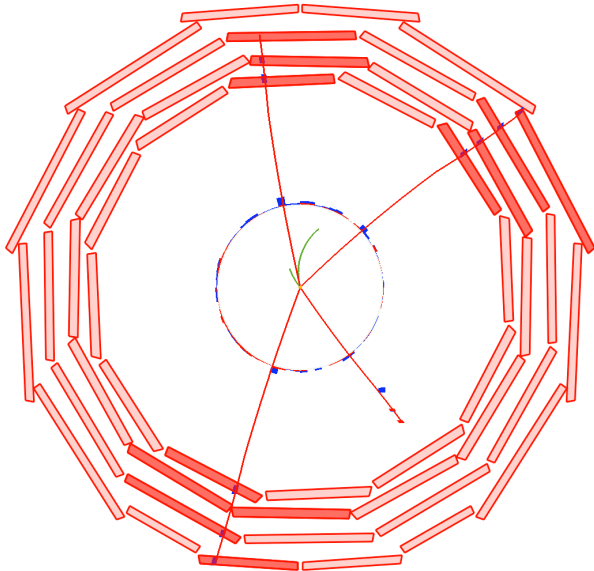
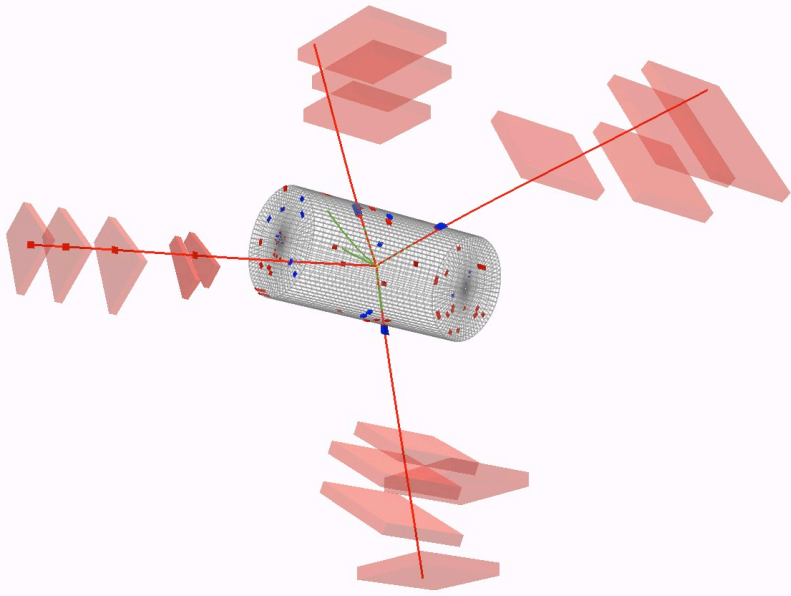
# H → WW → 2l2v: what to expect?

Injecting signal (Azimov dataset):  
 1.1 fb<sup>-1</sup> exercise for cut-and-count analysis



**H -> ZZ**

# H $\rightarrow$ ZZ $\rightarrow$ 4l signature



## Selection:

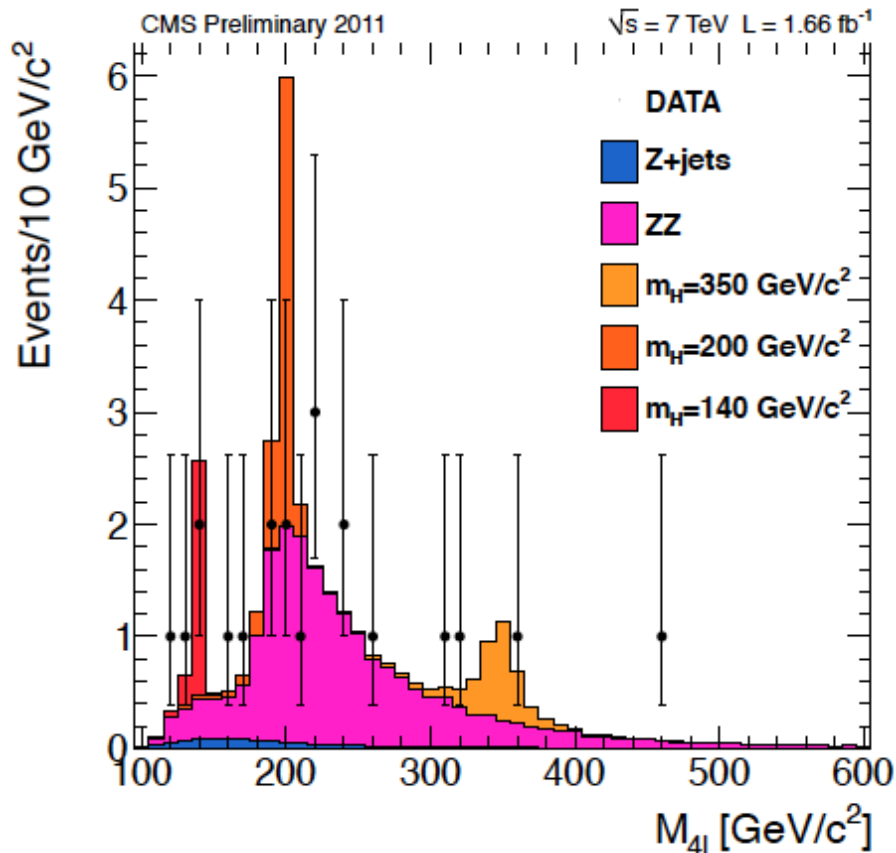
- 4 isolated leptons: 4e, 4 $\mu$ , 2e2 $\mu$
- no impact parameter
- Final discriminant: m(4l) mass distribution

**Mass resolution: 1%**

## Main backgrounds:

- ZZ: from MC ZZ/Z and measured Z
- tt and Z+jets: from data (4l with loose leptons), shape and extrapolation from MC

# H→ZZ→4l: mass distributions

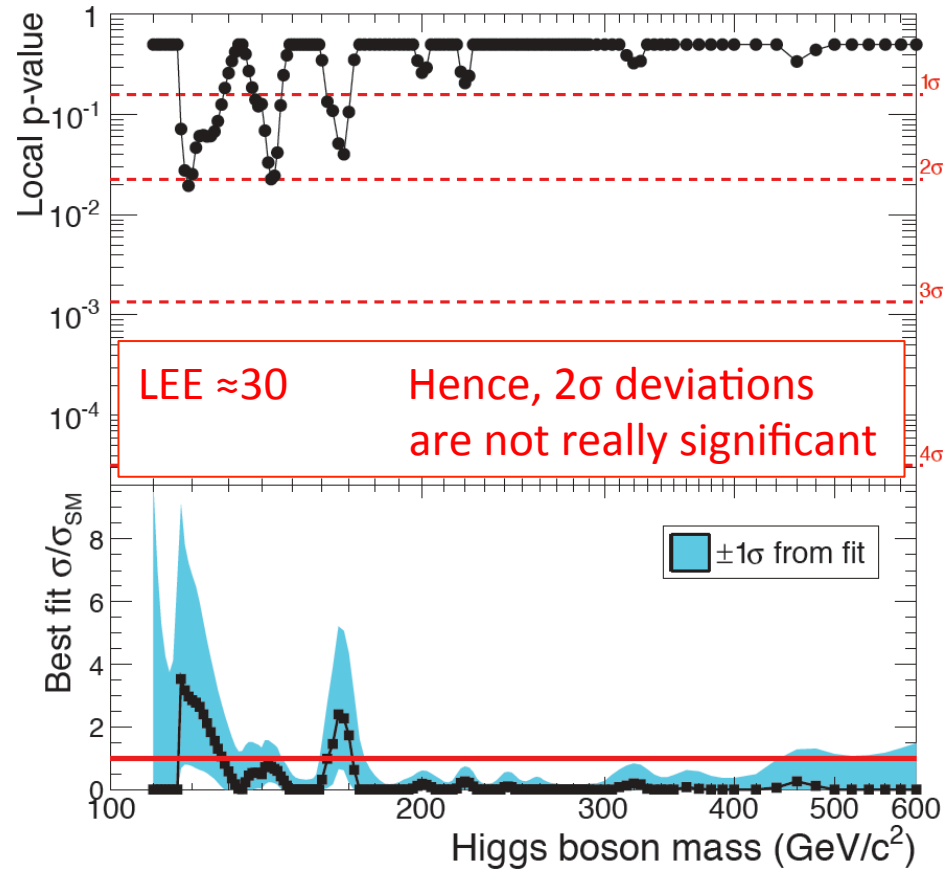
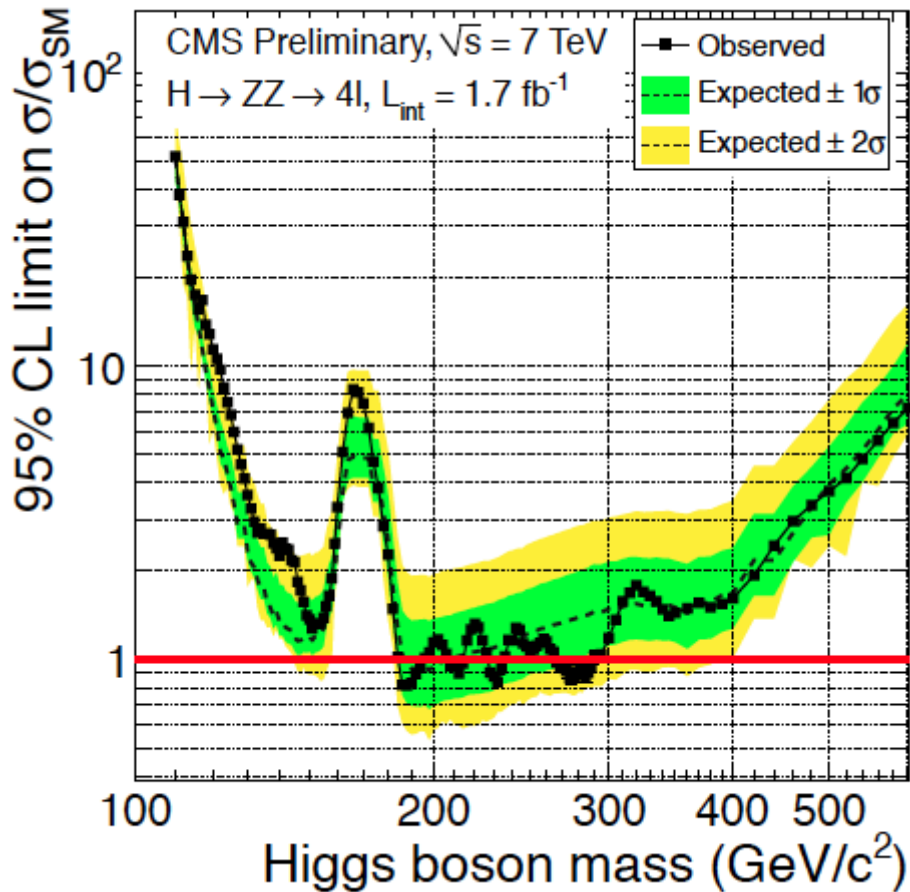


- **Observed 21 events**
- **Expected  $21.2 \pm 0.8$**

## Note:

- each event with low  $m(4l)$  will appear very significant (low bkgd and narrow peak)
- update from EPS ( $1.1 \text{ fb}^{-1}$ ) to LP ( $1.7 \text{ fb}^{-1}$ ) did not bring new low mass events

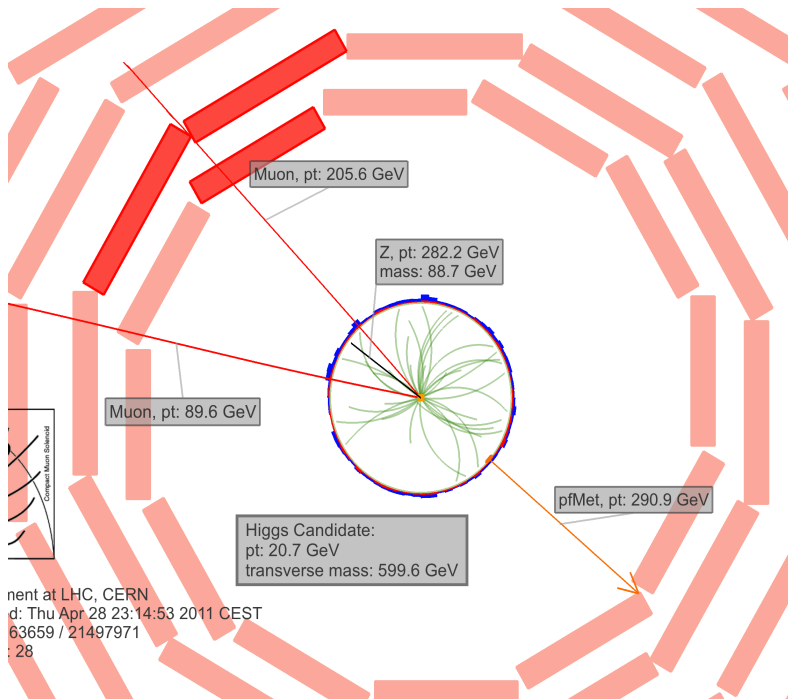
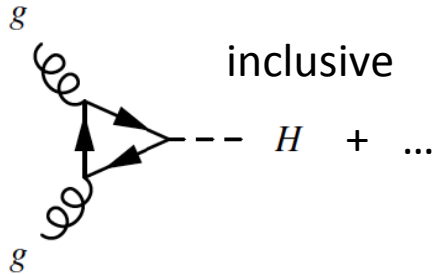
# H $\rightarrow$ ZZ $\rightarrow$ 4l results



Ratio of limits with/without system errors  $\sim 1.06$



# H->ZZ->2l2v signature



## Selection:

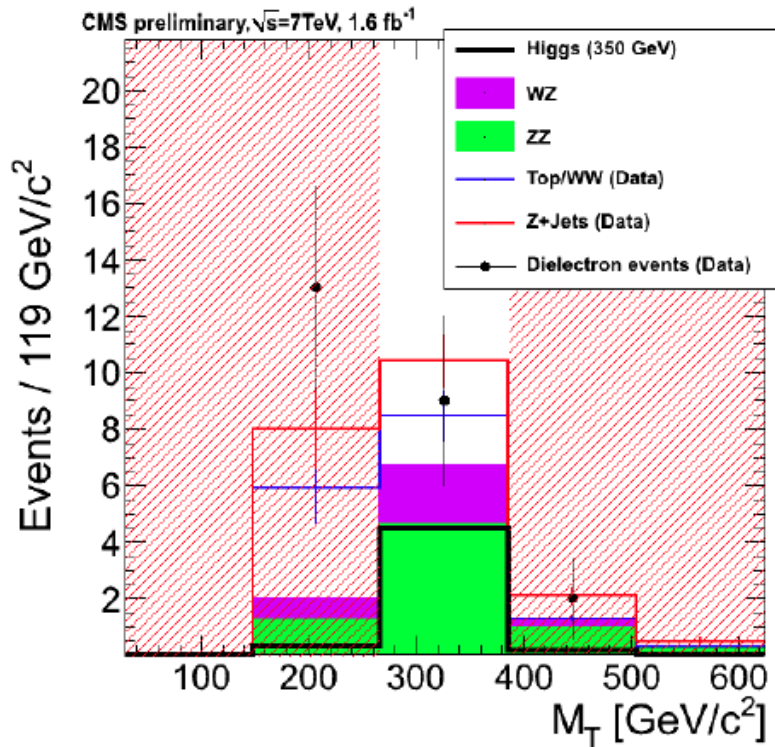
- 2 channels: 2 isolated leptons: Z(2e), Z(2 $\mu$ )
- no impact parameter
- large  $p_T(\text{ll})$
- large MET, not aligned with jets or leptons
- $m_T$  (sensitive to mass)
- cut-and-count

Mass resolution: 10%

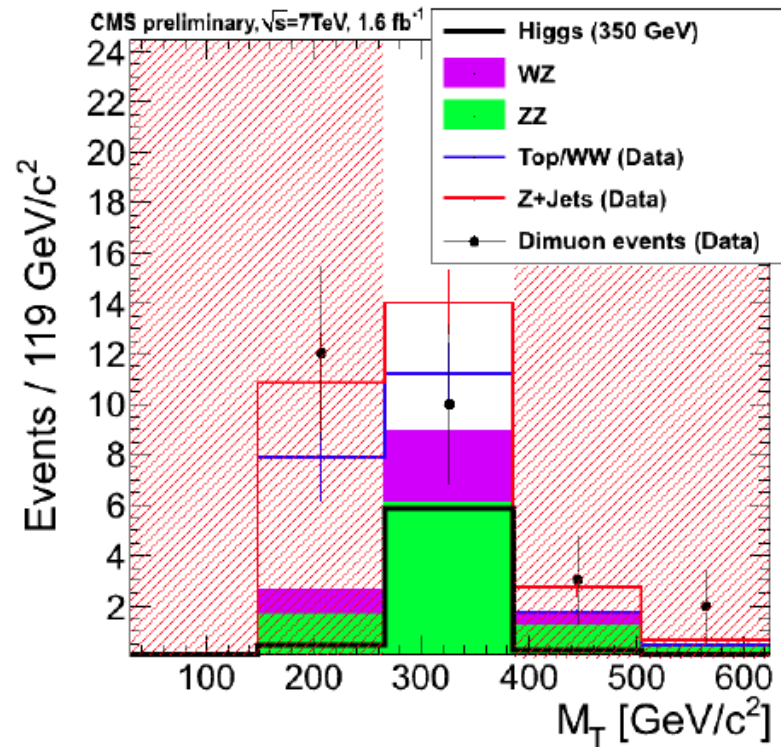
## Main backgrounds:

- Z+jets ( sig:bkgd = 1:10<sup>5</sup> ): from data ( $\gamma$ +jets)
- tt, WW, Wjets: from data (off Z-peak)
- ZZ, WZ: from MC

# H- $\rightarrow$ ZZ- $\rightarrow$ 2l2v distributions

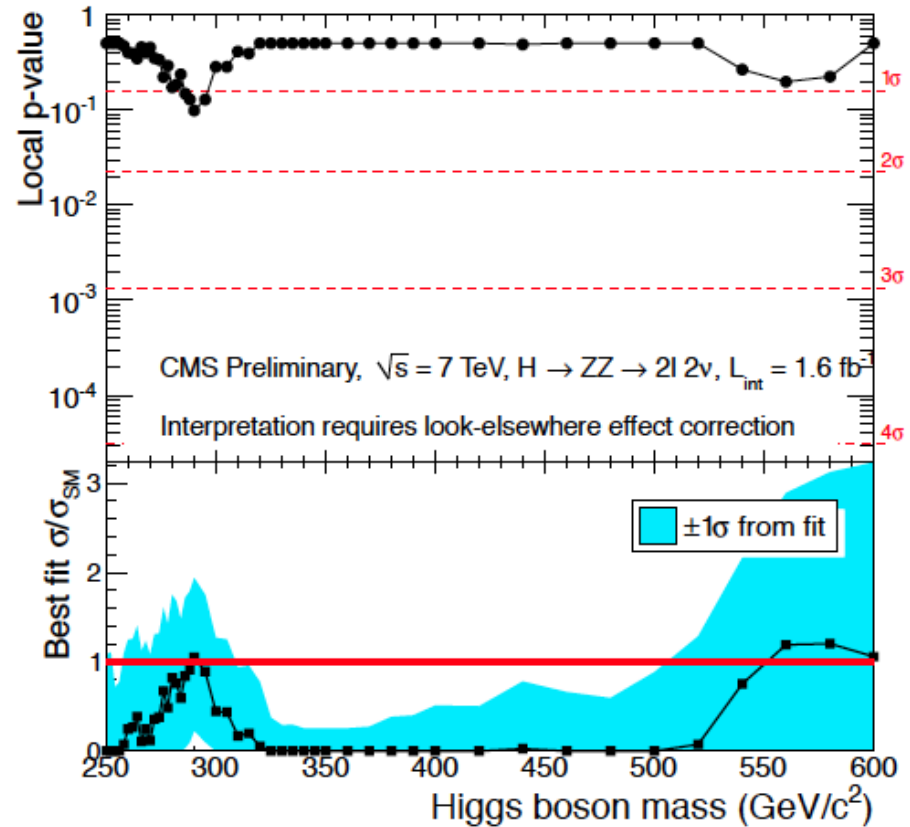
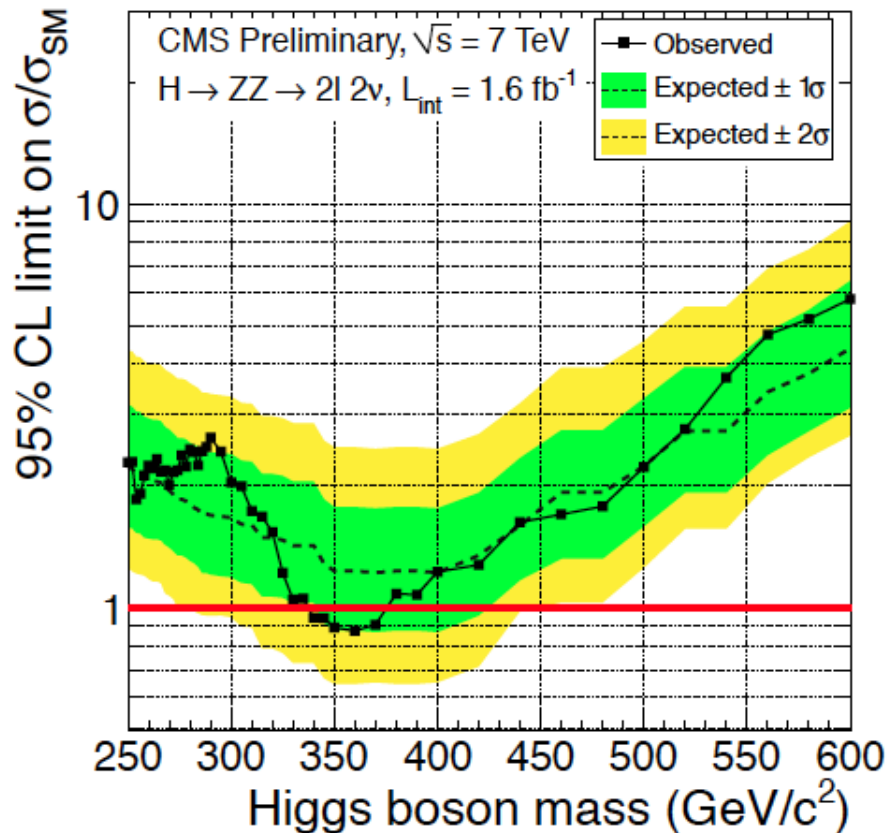


$ee$

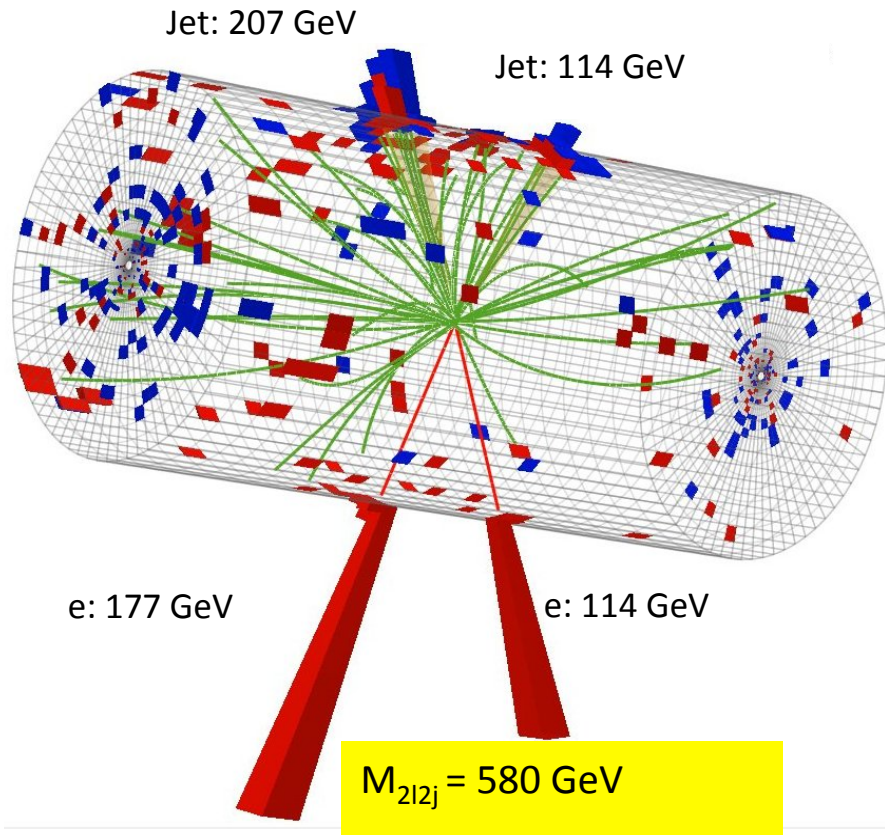


$\mu\mu$

# H $\rightarrow$ ZZ $\rightarrow$ 2l 2v results



# H->ZZ->2l2q signature



## Selection:

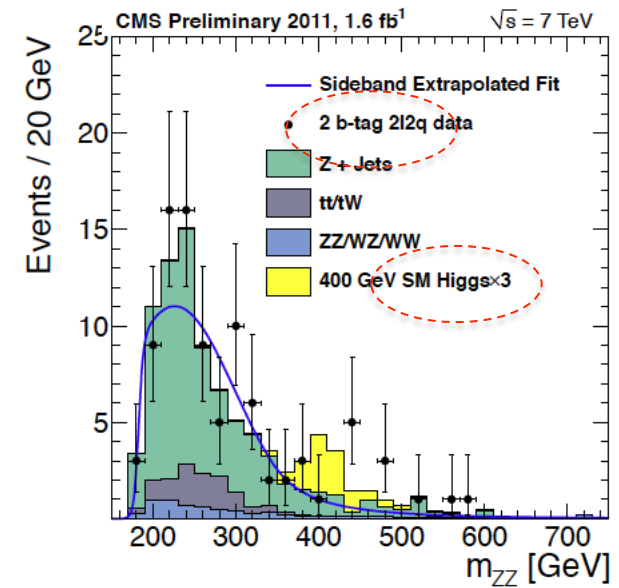
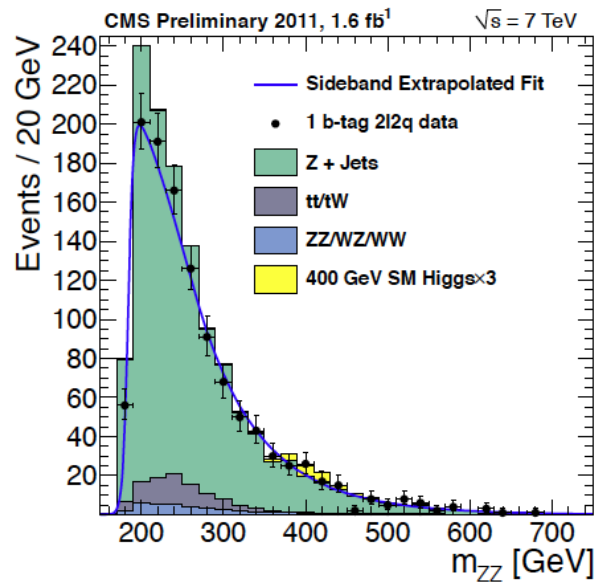
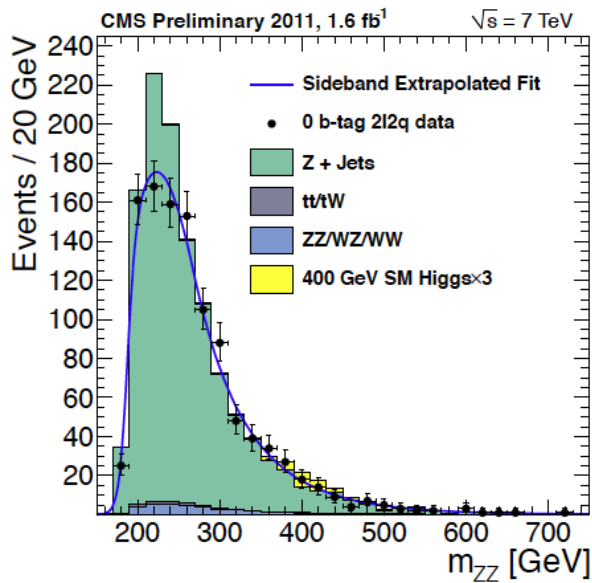
- 2 isolated leptons,  $Z(2e)$ ,  $Z(2\mu)$ , with no impact parameter
- two jets:  $Z(jj)$  with 0, 1, 2 b-tags
- most of sensitivity from 2 b-tag category
- no MET
- cut on angular topology (ME-based)
- $m_{ljj}$  mass distribution

**Mass resolution: 3%**

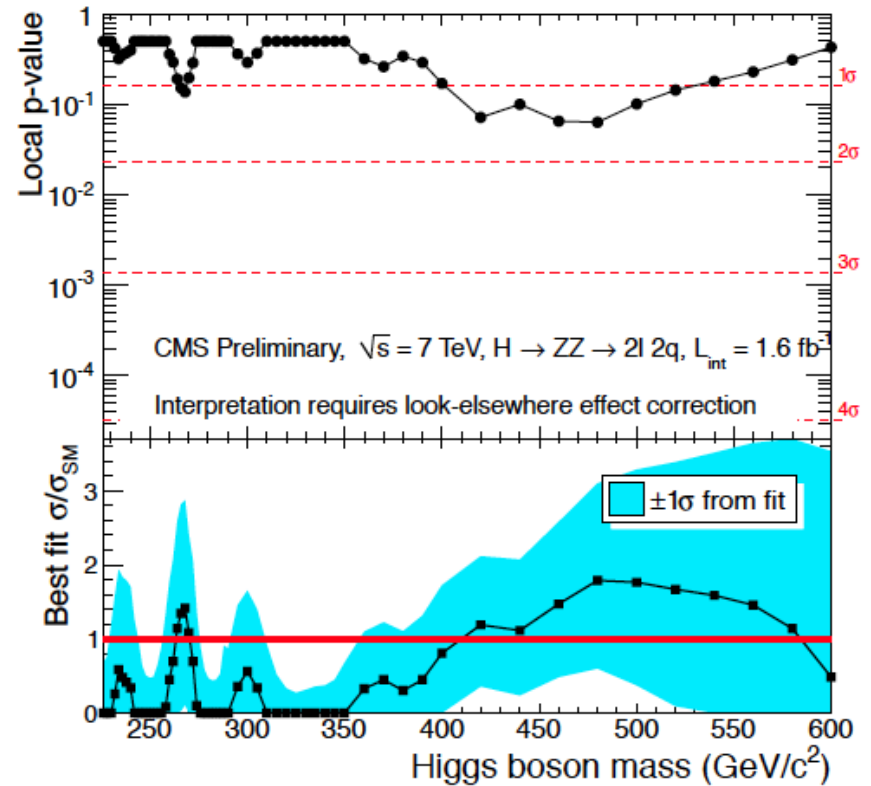
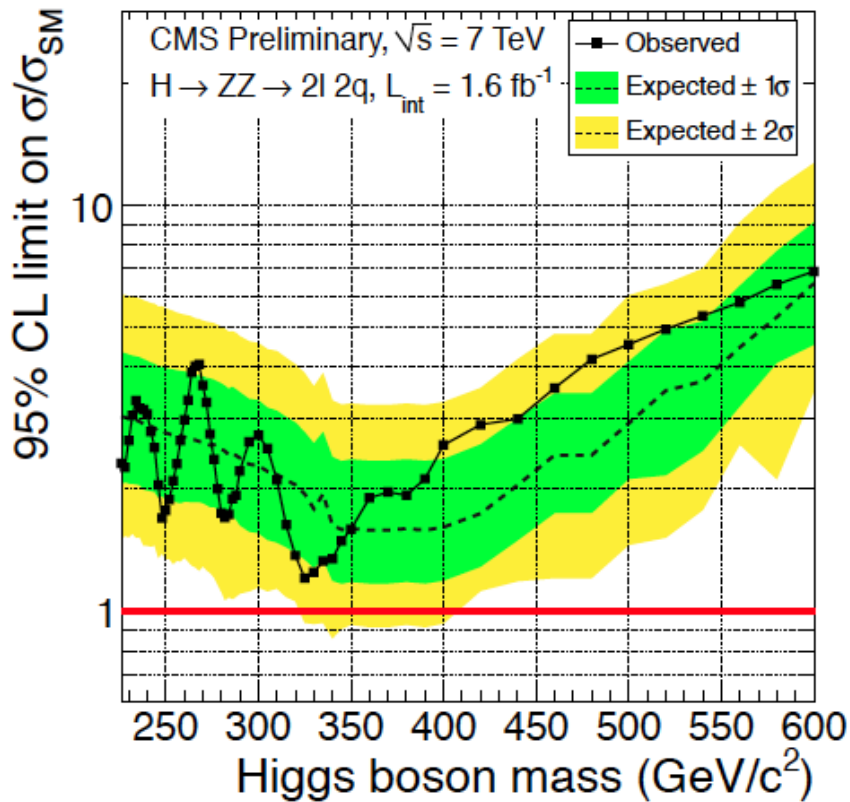
## Main backgrounds: from sidebands

- Z+jets ( including heavy flavor jets )
- WZ, ZZ
- tt, WW

# H $\rightarrow$ ZZ $\rightarrow$ 2l2q distributions



# H $\rightarrow$ ZZ $\rightarrow$ 2l 2q results



# Combination of searches



# Combination scope

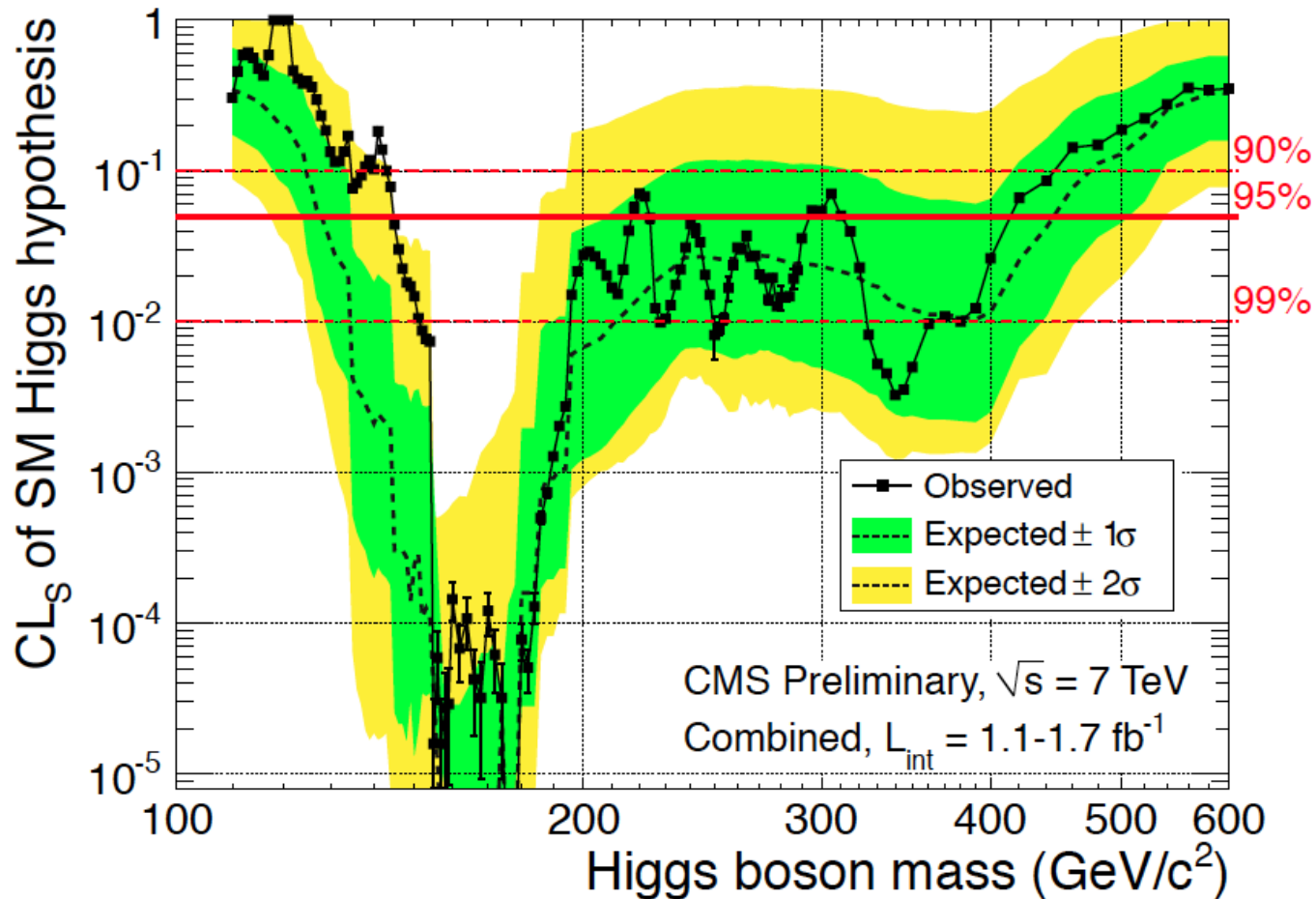
channel	mass range (GeV/ $c^2$ )	luminosity (fb $^{-1}$ )	number of sub-channels	type of analysis	number of nuisances
$H \rightarrow \gamma\gamma$	110-150	1.7	8	mass shape (unbinned)	3+40=43
$H \rightarrow \tau\tau$	110-140	1.1	6	mass shape (binned)	10+25=35
$H \rightarrow bb$	110-135	1.1	5	cut&count	10+59 = 69
$H \rightarrow WW \rightarrow 2\ell 2\nu$	110-600	1.5	5	cut&count	15 +79 =94
$H \rightarrow ZZ \rightarrow 4\ell$	110-600	1.7	3	mass shape (unbinned)	14+20=34
$H \rightarrow ZZ \rightarrow 2\ell 2\tau$	180-600	1.1	8	mass shape (unbinned)	13+10=23
$H \rightarrow ZZ \rightarrow 2\ell 2\nu$	250-600	1.6	2	cut&count	14+4=18
$H \rightarrow ZZ \rightarrow 2\ell 2q$	226-600	1.6	6	mass shape (unbinned)	12+15=27
TOTAL (8)	110-600	1.1-1.7	27 for low $m_H$ 24 for high $m_H$		241 for low $m_H$ 146 for high $m_H$



# Uncertainties common to many channels

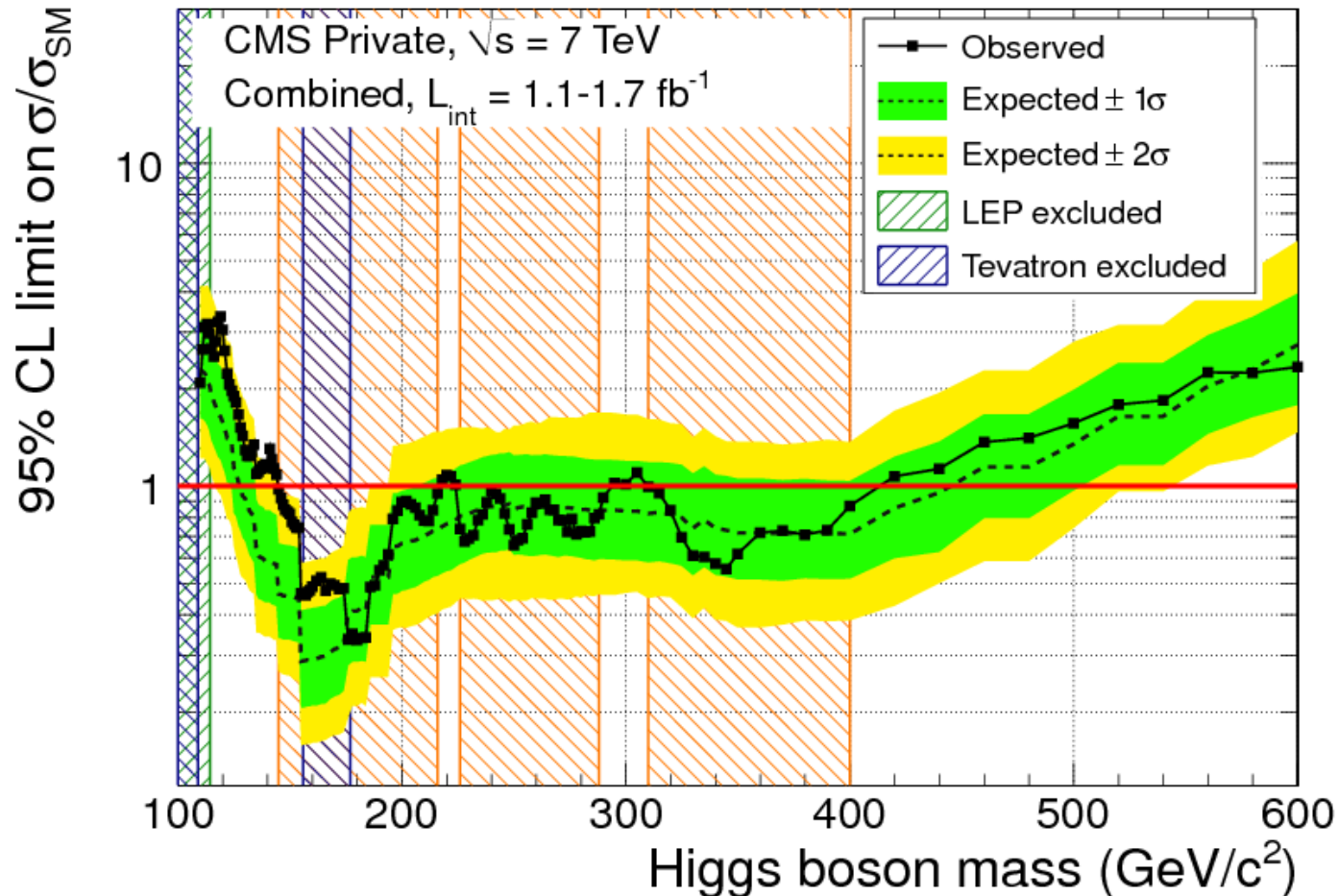
group	nuisance	comments
cross section ( <i>pdf</i> )	gg qqbar	$gg \rightarrow H, t\bar{t}H, VQQ, t\bar{t}, tW, tb$ (s-channel), $gg \rightarrow VV$ VBF $H, VH, V, VV, \gamma\gamma$
cross section (QCD scales)	ggH ggH1in ggH2in qqH VH ttH VV ggVV	total inclusive $gg \rightarrow H$ inclusive $gg/qg \rightarrow H + \geq 1$ jets inclusive $gg/qg \rightarrow H + \geq 2$ jets VBF $H$ associate $VH$ $t\bar{t}H$ WW, WZ, and ZZ up to NLO $gg \rightarrow WW$ and $gg \rightarrow ZZ$
Higgs BR	ZZ	Branching ratio $BR(H \rightarrow ZZ)$
phenomenology	UE & PS	modeling of underlying event (UE) and parton showering (PS)
luminosity	lumi	uncertainties in integrated luminosity
efficiencies	muon electron tau b-tag	prompt muon efficiency (includes reconstruction, isolation) prompt electron efficiency (includes reconstruction, isolation) reconstruction efficiency of prompt hadronically decaying tau b-tag efficiency for b-jets (anti-correlated with b-jet veto)
$p_T$ scales	muon electron tau jets	prompt muon $p_T$ -scale prompt electron $p_T$ -scale $p_T$ scale for prompt hadronically decaying tau jet energy scale
$p_T$ resolutions	electron	prompt electron $p_T$ -resolution
fake rates	lepton	determination of fake lepton rates in data
trigger efficiencies	muon electron	prompt muon efficiency (includes trigger, reconstruction, isolation) prompt electron efficiency (includes trigger, reconstruction, isolation)

# Exclusion CL for SM Higgs



**SM Higgs boson: expected exclusion mass range: 130 – 440 GeV**  
**Observed exclusion mass range: 145-216, 226-288, 310-400 GeV**

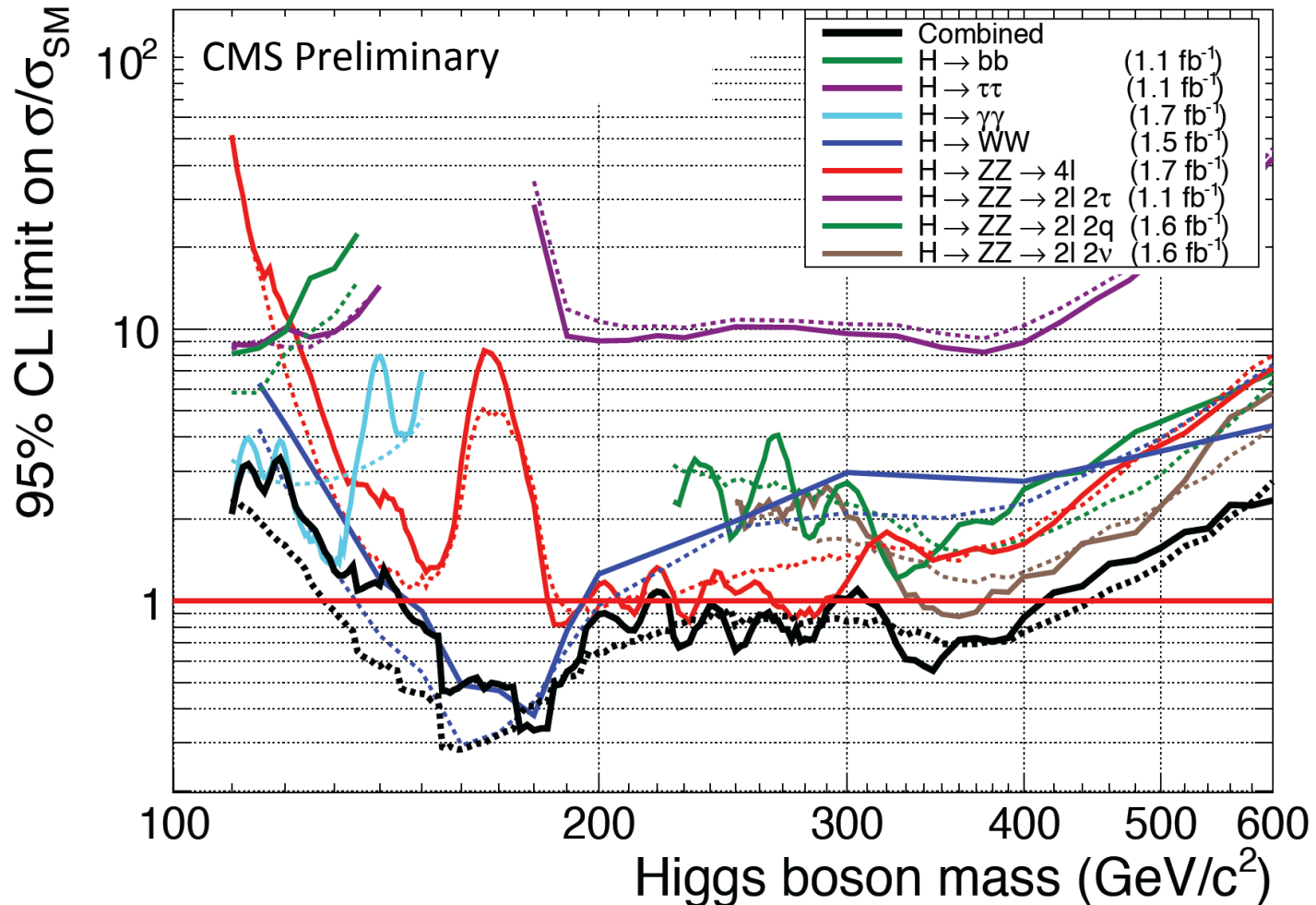
# Exclusion limits on $\mu$



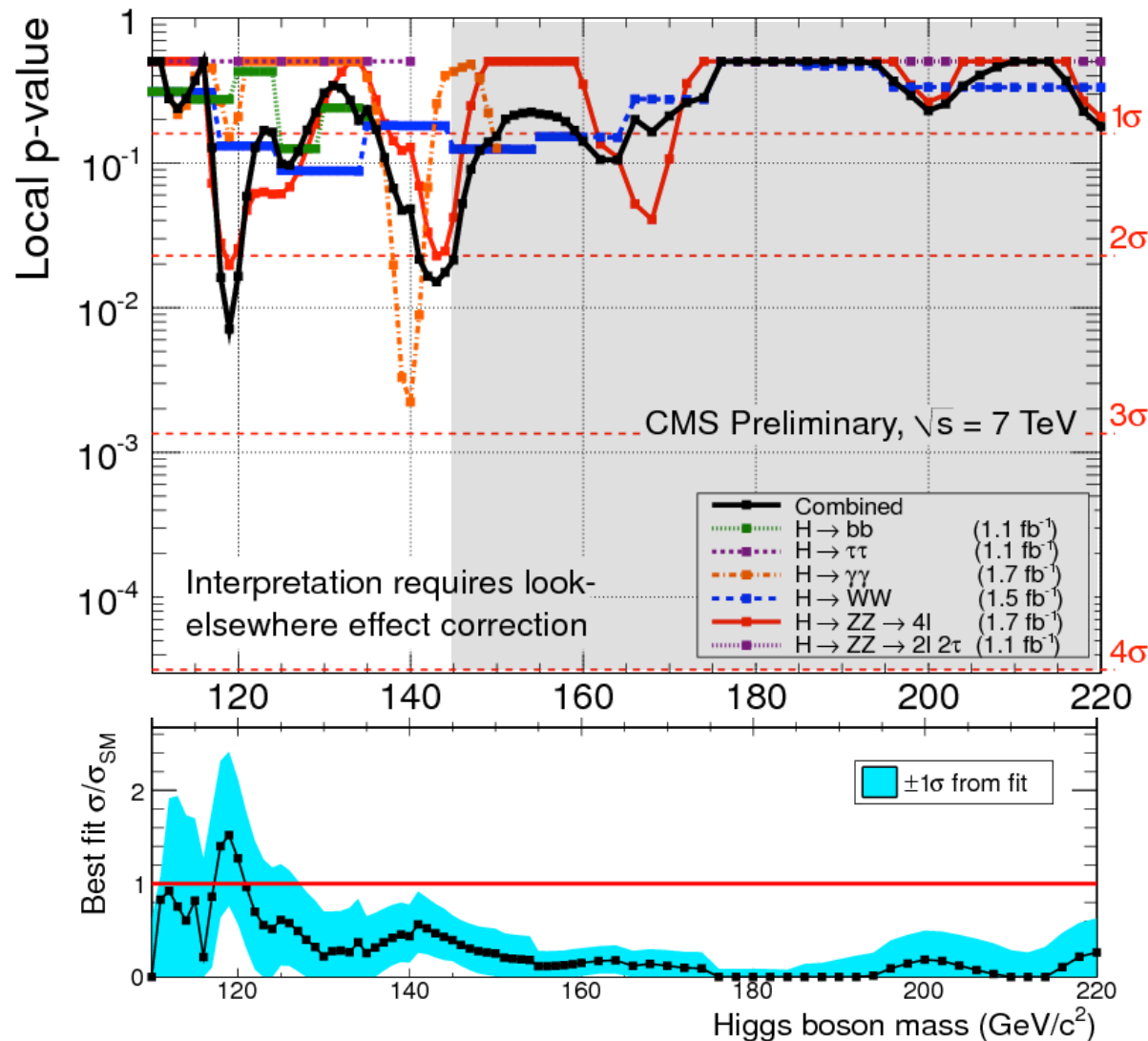
**SM Higgs boson: expected exclusion mass range: 130 – 440 GeV**  
**Observed exclusion mass range: 145-216, 226-288, 310-400 GeV**

# Interplay of channels

Solid line – observed limit  
Dashed line – median expected

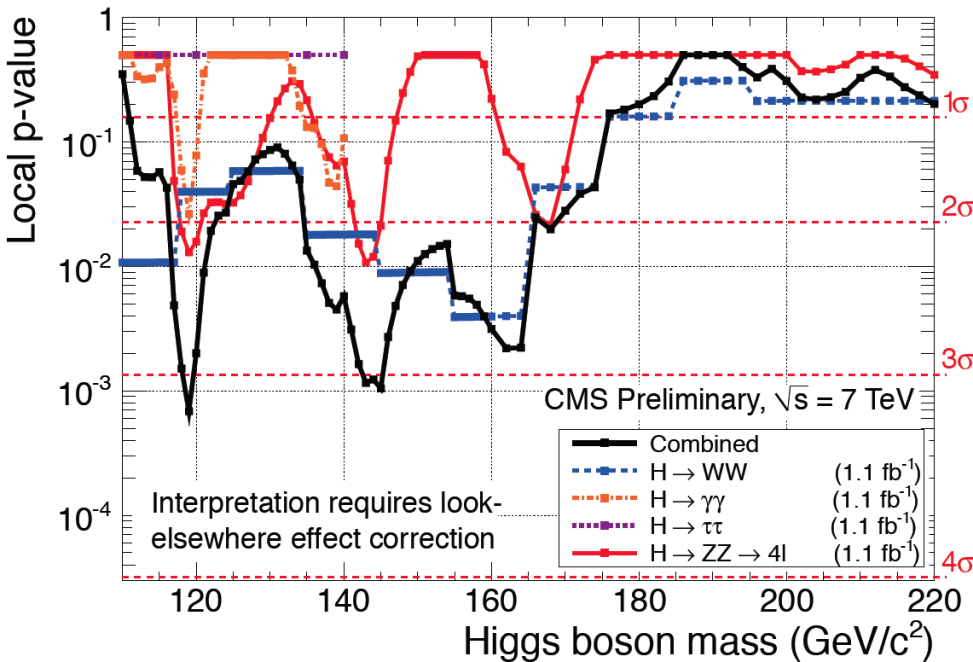


# Quantifying excesses seen by CMS

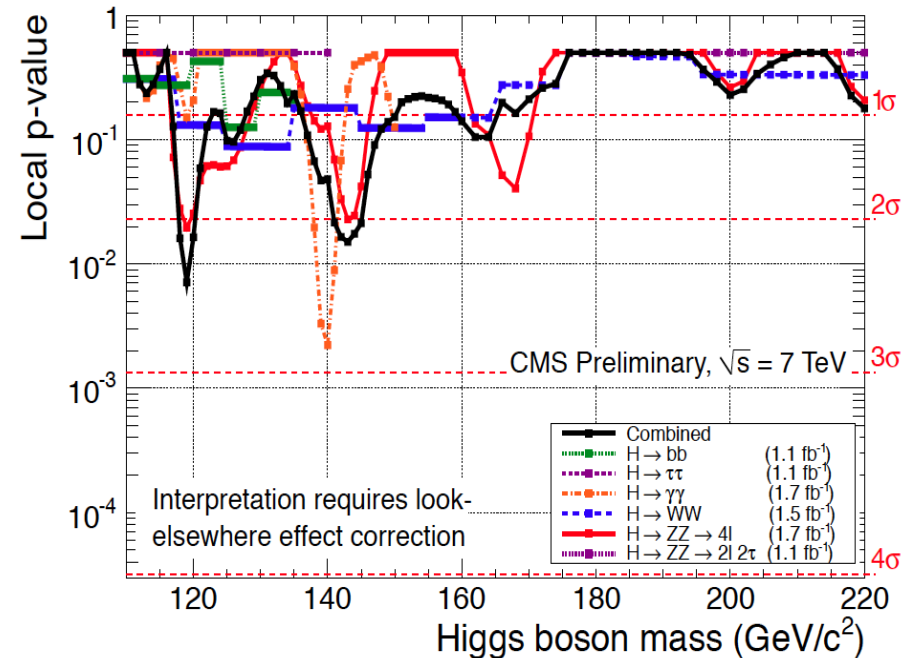


# CMS excess: from EPS to LP

## EPS results

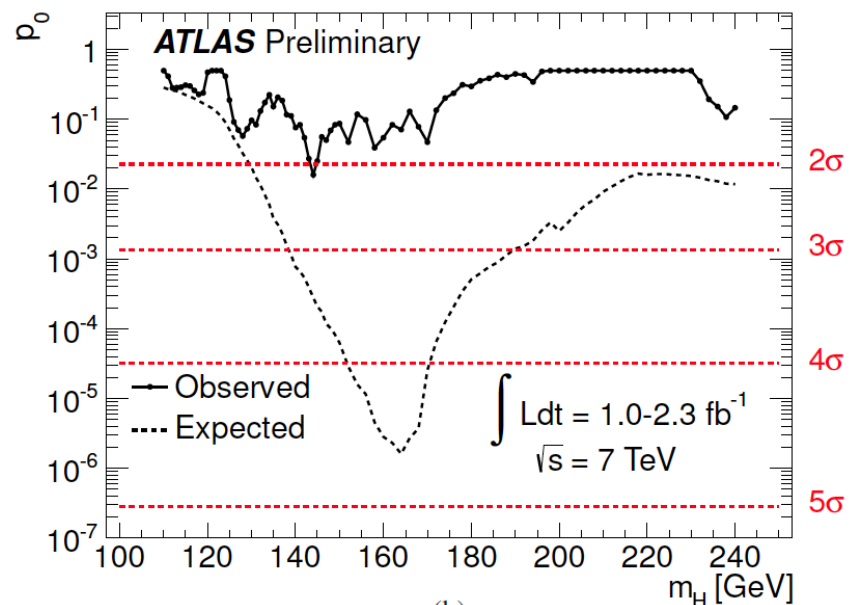
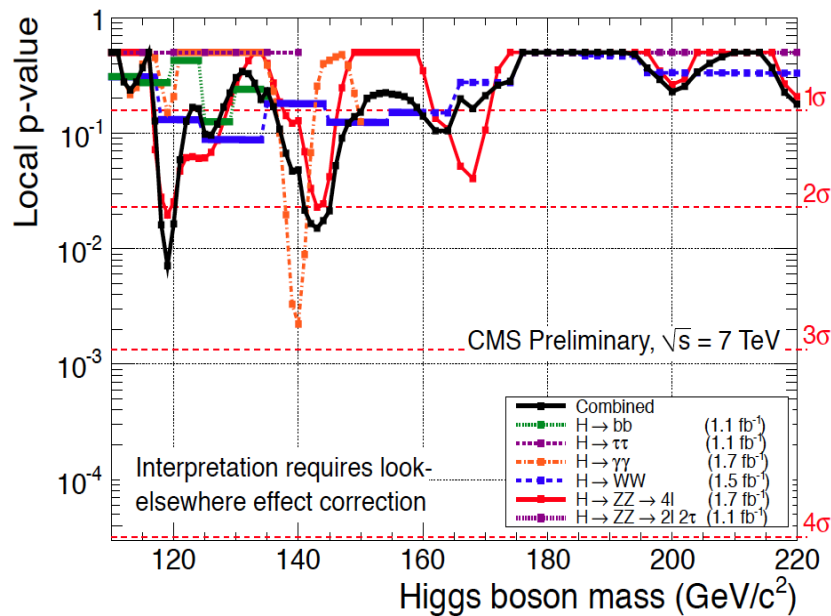
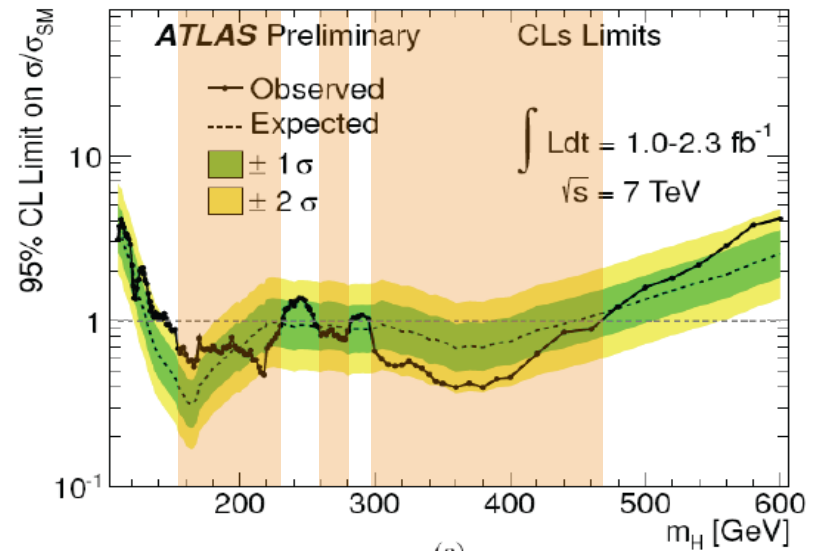
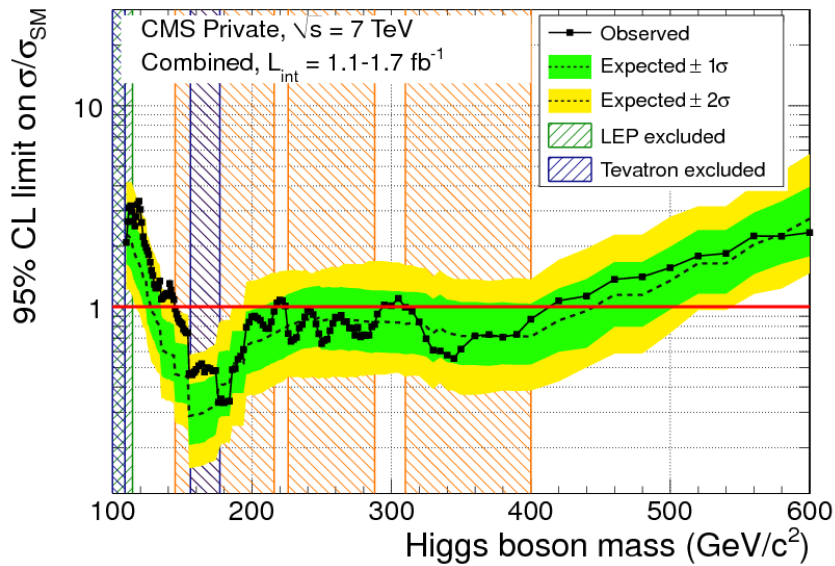


## LP results

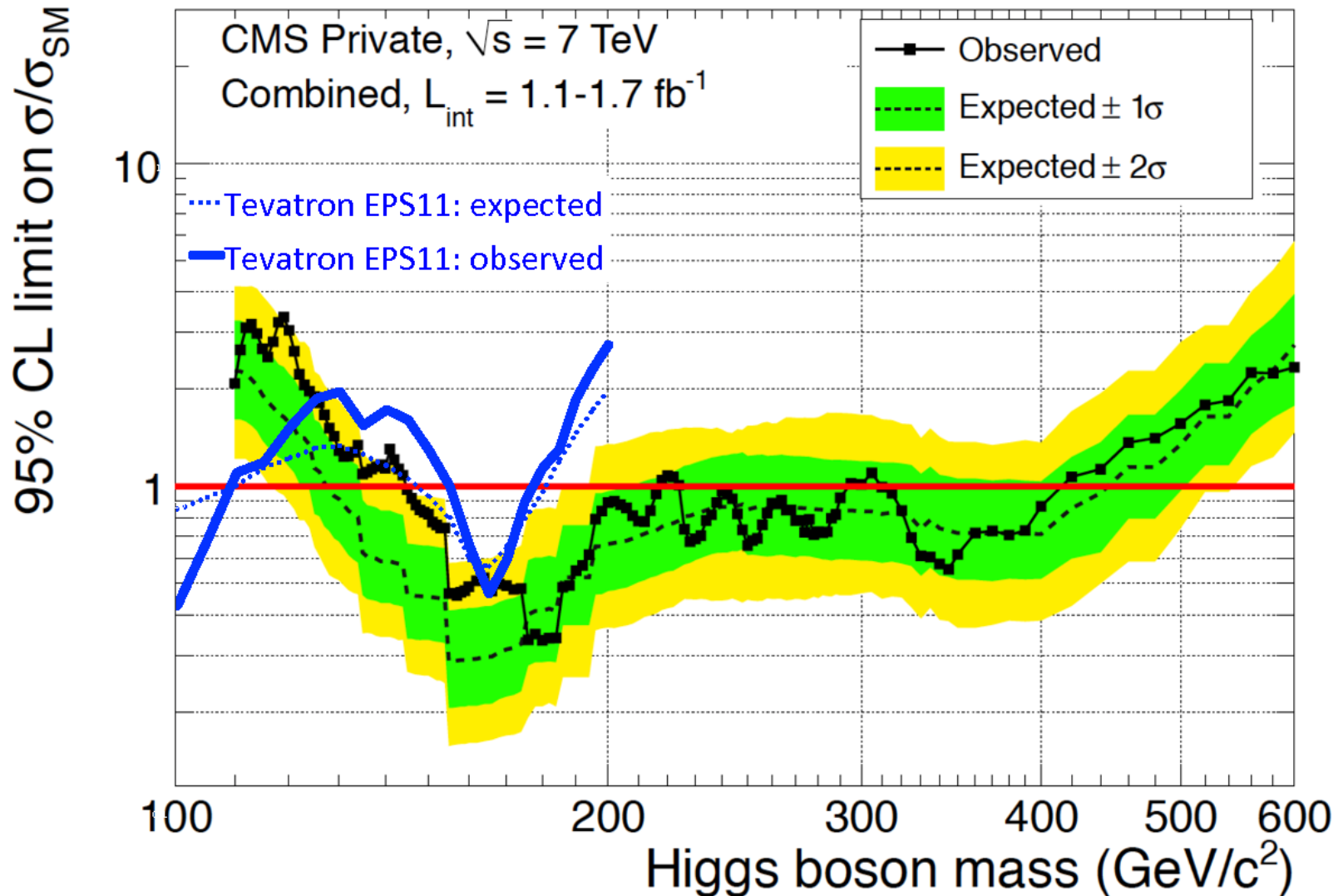


- $H \rightarrow WW \rightarrow l\nu l\nu$  recessed: now more conservative analyses, new data has smaller excess
- $H \rightarrow ZZ \rightarrow 4l$ : no new low mass events (this is perfectly OK as we expected to add  $<1$  event)
- $H \rightarrow \gamma\gamma$ :  $m=120$  excess recessed,  $m=140$  excess grew

# CMS – ATLAS



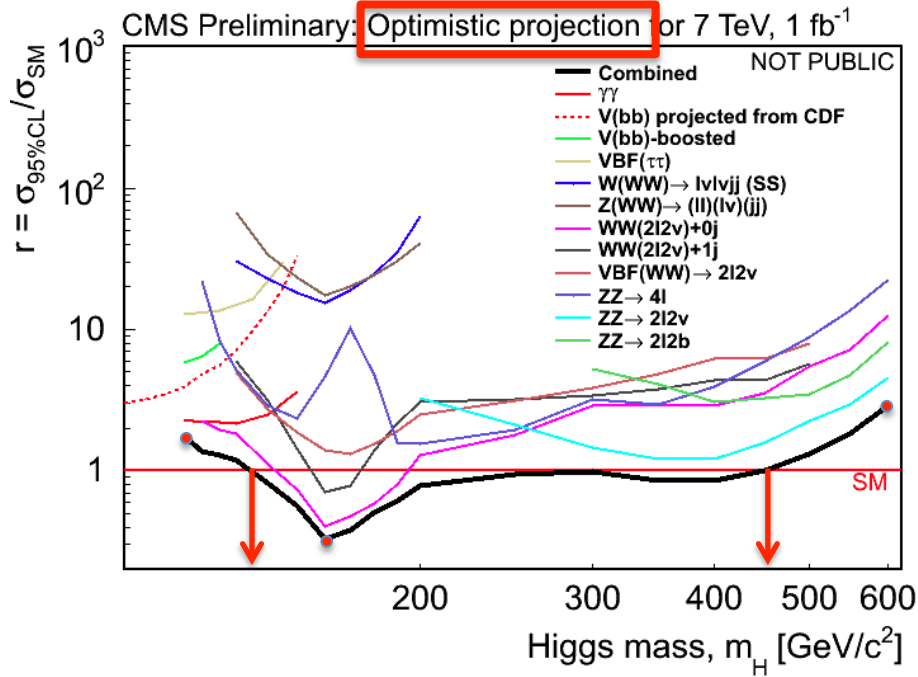
# CMS – Tevatron



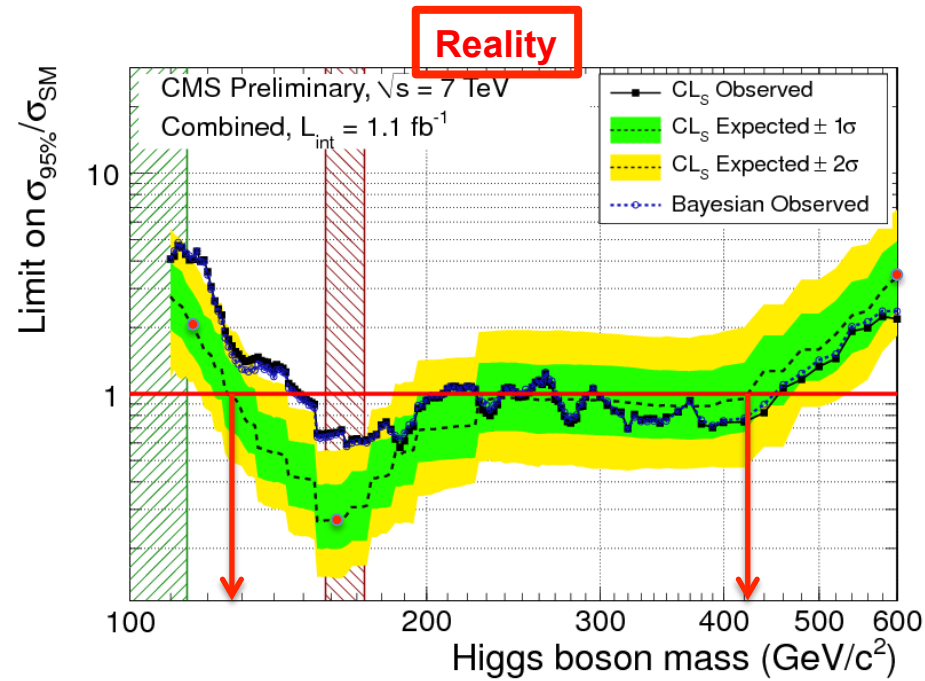


# Outlook

# How did we do so far?

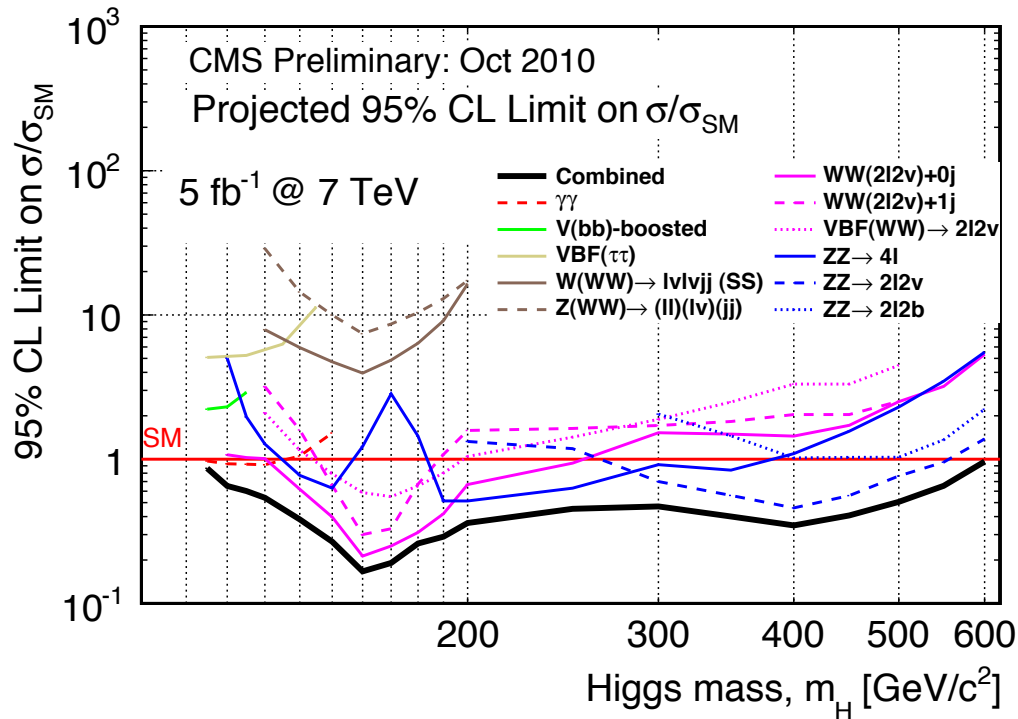


September 28, 2010 Projection: **135-450 GeV**



Sensitivity reported at EPS: **127-420 GeV**

# Prospects for 2011



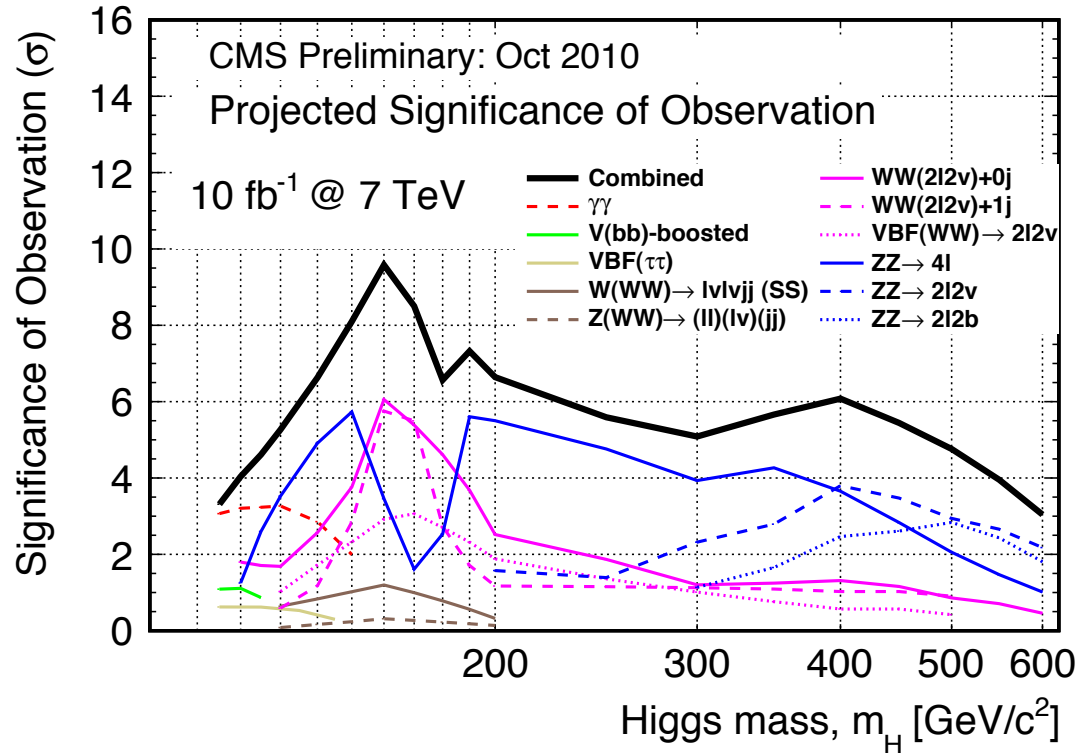
Full 2011 run integrated lumi (good data) = 4.7 fb<sup>-1</sup>

If SM Higgs is not there at all,

one might expect to know that by the end of the year...

but, given we have an excess, it will now take a bit longer...

# Prospects for 2012



2012 run integrated lumi being discussed is 30 fb<sup>-1</sup>

If SM Higgs is there,

discovery is very likely next year

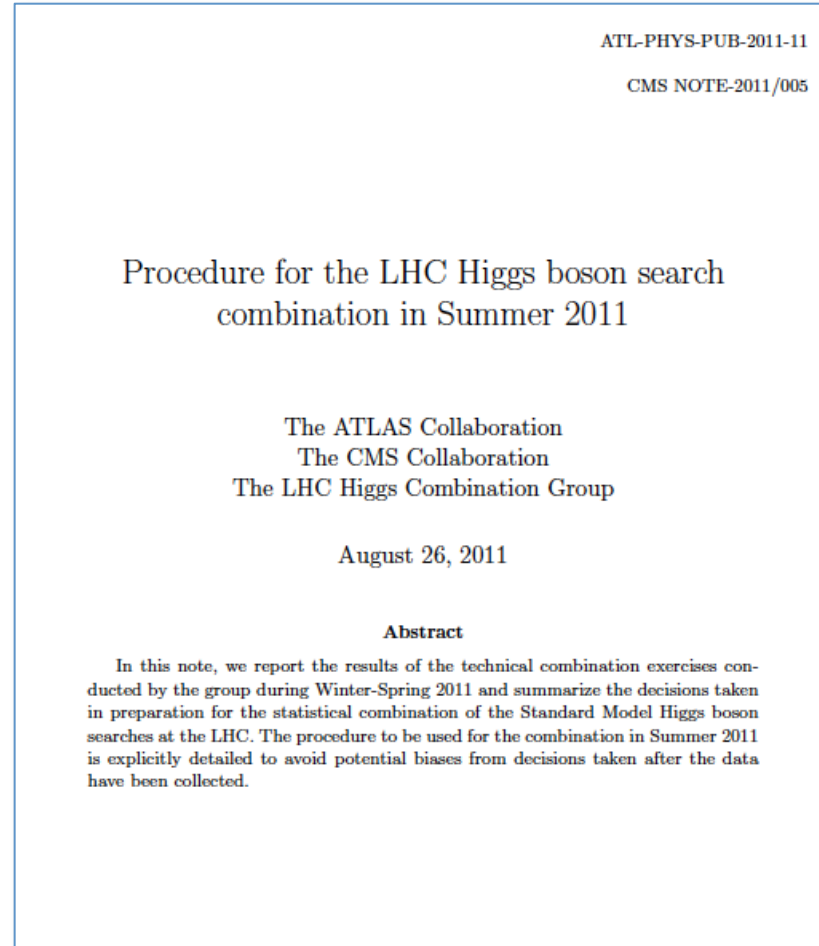
# Summary

- **SM Higgs boson excluded at 95% CL in the mass range from 145-400 GeV with two narrow gaps (gaps excluded at 90% CL)**
- **The excess at low masses remains. It is not inconsistent with SM Higgs, but its significance is way too low for any speculations.**
- **2011: with 5 fb<sup>-1</sup> per experiment this year, we expect to reach exclusion sensitivity in the mass range from 115-600 GeV**
- **2012: with 30 fb<sup>-1</sup> per experiment next year, we expect to reach discovery sensitivity in the mass range from 115-600 GeV**

# Backup

# Stat methods used

- **50-page document (6 months of the joint effort)**
  - explicit formulation of the methods to be used
  - record of ATLAS & CMS “handshakes” on toy combinations
- **RooStats – the engine for ATLAS+CMS combination\***



\* CMS-only combination is always validated by requiring the agreement between RooStats and L&S results

# Stat methods used: main terms

- SM Higgs signal  $s$
- background  $b$
- nuisance parameters  $\theta$
- signal strength modifier  $\mu = \sigma / \sigma_{SM}$
- best-fit signal strength modifier  $\mu\text{-hat}$
- test statistic  $q$
- p-value =  $P(q \geq q^{obs})$
- significance  $Z$
- $CL_s = P(q \geq q^{obs} | b + \mu s) / P(q \geq q^{obs} | b)$



# Stat methods used: uncertainties (1)

- **uncertainties are modeled by introducing independent nuisance parameter**
- **correlated uncertainties in different channels are associated with the same nuisance parameter**
- **pdf types for uncertainties:**
  - **unconstrained: flat prior**
  - **generic case for observables that can take  $\pm$  values: normal**
  - **generic for positive definite observables: lognormal (normal in log space)**
  - **statistical: gamma distribution**

# Stat methods used: uncertainties (2)

**uncertainty** --> nuisance parameter  $\theta$ , whose best estimate is  $\tilde{\theta}$

**Bayesian** declares his degree of believe on the true value of nuisance  $\theta$ :  $\rho(\theta|\tilde{\theta})$

**Frequentist** wants to know pdf of “measuring”  $\tilde{\theta}$ , should nuisance be  $\theta$ :  $p(\tilde{\theta}|\theta)$

Two paradigms can be connected via Bayes’ theorem:

$$\rho(\theta|\tilde{\theta}) \sim p(\tilde{\theta}|\theta) \cdot \pi_{\theta}(\theta)$$

posterior  
as a prior for  
Bayesian  
analysis

“measurement”  
PDF for  
frequentist  
analysis

“primordial”  
hyper prior

Type of syst. error	posterior $\rho(\theta \tilde{\theta})$	frequentist $p(\tilde{\theta} \theta)$	prior $\pi_{\theta}(\theta)$
Unconstrained	flat	flat	flat
Gaussian, Lognormal	$\rho(\theta \tilde{\theta}) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{(\theta-\tilde{\theta})^2}{2}\right)$	$p(\tilde{\theta} \theta) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{(\tilde{\theta}-\theta)^2}{2}\right)$	flat
Statistical	$\rho(\theta N) = \frac{\theta^N}{N!} \exp(-\theta)$	$p(N \theta) = \frac{\theta^N}{N!} \exp(-\theta)$	flat

## Typical examples

**Gaussian:**  $b = b_0 (1 + \varepsilon\theta)$

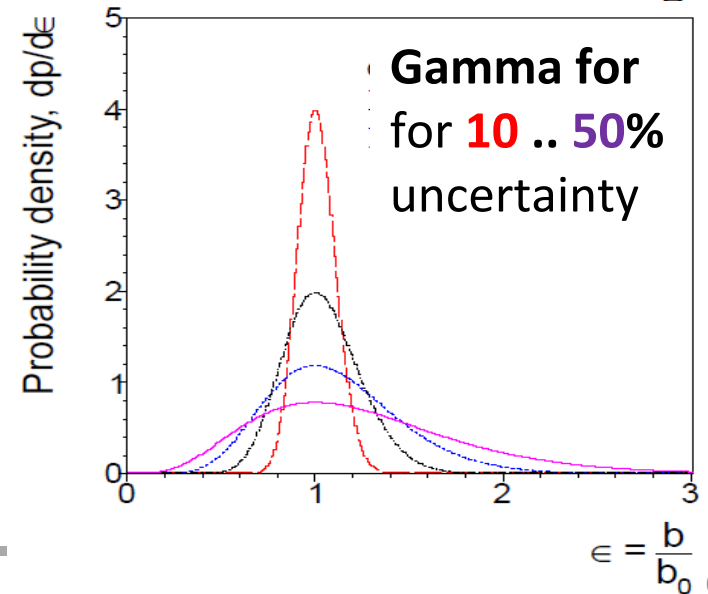
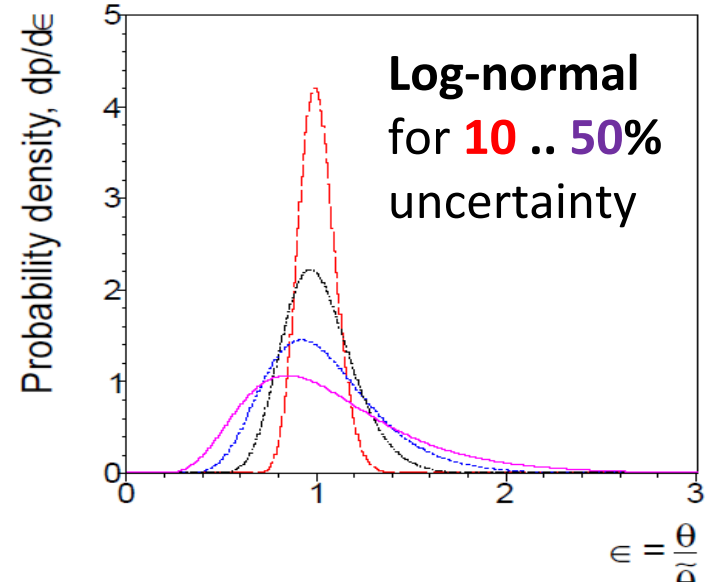
**Lognormal:**  $b = b_0 \kappa^{\theta}$

**Statistical:**  $b = \alpha \times \theta$

# Statistical analysis: modelling

## PDFs for nuisance parameters:

- For yields measured from a control sample with stat. uncertainties: **Gamma**
- Other uncertainties on yields: **log-normal** (remains “regular” for large uncertainties)
- Parameters with no prior knowledge, e.g. the  $\gamma\gamma$  background: **uniform distrib.**
- Other parameters, usually affecting shapes: **Gaussians**



# Statistical choices for setting limits

- **Two main paradigms**

- **Frequentist**

- classical
    - Feldman-Cousins
    - modified frequentist (a.k.a.  $CL_s$ )

- **Bayesian**

- which prior?

- **How do we deal with systematic uncertainties?**

- this brings even more sub-sub-flavors for each of the above...

# Stat methods used: limits

Pursue both frequentist and Bayesian paradigms,  
which allows us to validate robustness of results...

1.  $CL_s$  (exact formulation as agreed with ATLAS)
  - (a) assess probabilities using pseudo-experiments
  - (b) also, from asymptotic properties of the test statistic
2. Bayesian (with flat prior on signal strength)

# Limits: Bayesian paradigm

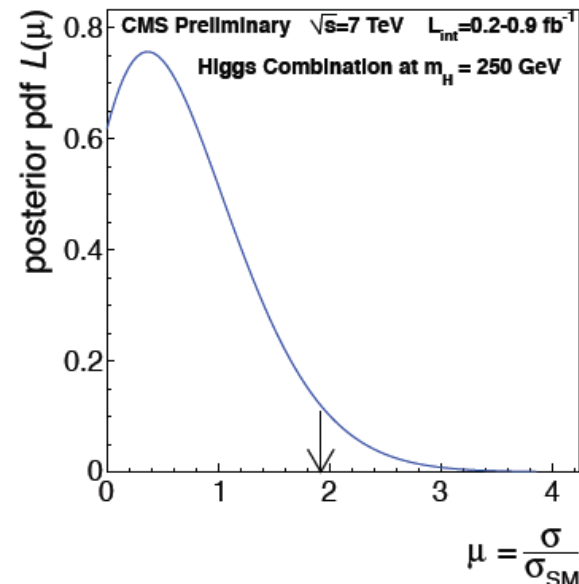
## Posterior on signal strength $\mu$

- using flat prior
- marginalization of nuisance parameters

$$p(\mu | \text{data}) = \frac{1}{C} \int_{\theta} p(\text{data} | \underline{\mu s(\theta)} + b(\theta)) \rho_{\theta}(\theta) \underline{\pi_{\mu}(\mu)} \underline{d\theta}.$$

## Deriving limit on $\mu$

$$\int_0^{\mu_{95\%CL}} p(\mu | \text{data}) d\mu = 0.95$$



# Limits: modified frequentist $CL_s$

**Pure frequentist.** *Aided by Bayes' theorem, all systematic errors are "measurements"*

## Likelihood

$$\mathcal{L}(\text{data} | \mu, \theta) = \text{Poisson}(\text{data} | \mu \cdot s(\theta) + b(\theta)) \cdot p(\tilde{\theta} | \theta)$$

## Test statistic

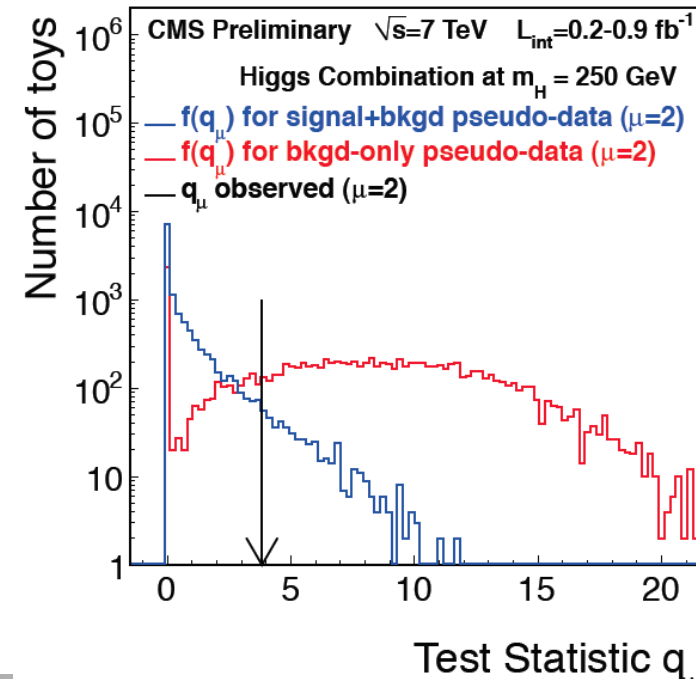
$$\tilde{q}_\mu = -2 \ln \frac{\mathcal{L}(\text{data} | \mu, \hat{\theta}_\mu)}{\mathcal{L}(\text{data} | \hat{\mu}, \hat{\theta})}, \quad \text{with a constraint } 0 \leq \hat{\mu} \leq \mu$$

## Pseudo-data (toys)

- fit data to find two best sets of nuisances  $\hat{\theta}_0^{obs}$  and  $\hat{\theta}_\mu^{obs}$
- prepare sampling distributions of test statistics
  - bkgd-only pseudo-data: (data,  $\tilde{\theta}$ ) for  $b(\hat{\theta}_0^{obs})$
  - signal+bkgd pseudo-data: (data,  $\tilde{\theta}$ ) for  $\mu s(\hat{\theta}_\mu^{obs}) + b(\hat{\theta}_\mu^{obs})$

## Define

$$CL_s = \frac{P(q_\mu \geq q_\mu^{obs} | \mu s(\hat{\theta}_\mu^{obs}) + b(\hat{\theta}_\mu^{obs}))}{P(q_\mu \geq q_\mu^{obs} | b(\hat{\theta}_0^{obs}))}$$



# Limits: modified frequentist $CL_s$

## Likelihood

$$\mathcal{L}(\text{data} | \mu, \theta) = \text{Poisson}(\text{data} | \mu \cdot s(\theta) + b(\theta)) \cdot p(\tilde{\theta} | \theta)$$

LEP did not use syst. error pdf's in Likelihood

TEV puts in  $\rho(\theta | \tilde{\theta}) = p(\tilde{\theta} | \theta)$  for pdf's we use

## Test statistics

$$\tilde{q}_\mu = -2 \ln \frac{\mathcal{L}(\text{data} | \mu, \hat{\theta}_\mu)}{\mathcal{L}(\text{data} | \hat{\mu}, \hat{\theta})}, \quad \text{with a constraint } 0 \leq \hat{\mu} \leq \mu$$

LEP and TEV, fix  $\mu=0$  in the denominator

LEP does not profile nuisance (there aren't any)

TEV does profile for nuisances

## Pseudo-data (toys)

- fit data to find two best sets of nuisances  $\hat{\theta}_0^{obs}$  and  $\hat{\theta}_\mu^{obs}$
- prepare sampling distributions of test statistics
  - bkgd-only pseudo-data:  $(\text{data}, \tilde{\theta})$  for  $b(\hat{\theta}_0^{obs})$
  - signal+bkgd pseudo-data:  $(\text{data}, \tilde{\theta})$  for  $\mu s(\hat{\theta}_\mu^{obs}) + b(\hat{\theta}_\mu^{obs})$

TEV/LEP use  $\tilde{\theta}$  to generate  $\theta$  and then generate pseudo-data using new  $s(\theta)$  and  $b(\theta)$ , which is explicitly Bayesian

Define  $CL_s = \frac{P(q_\mu \geq q_\mu^{obs} | \mu s(\hat{\theta}_\mu^{obs}) + b(\hat{\theta}_\mu^{obs}))}{P(q_\mu \geq q_\mu^{obs} | b(\hat{\theta}_0^{obs}))}$



# Stat methods used: excess (p-value)

**test statistic** – profile likelihood

$$q_0 = -2 \ln \frac{\mathcal{L}(\text{data}|0, \hat{\theta}_0)}{\mathcal{L}(\text{data}|\hat{\mu}, \hat{\theta})} \quad \text{and } \hat{\mu} \geq 0$$

**“local” p-values** – from asymptotic approximation

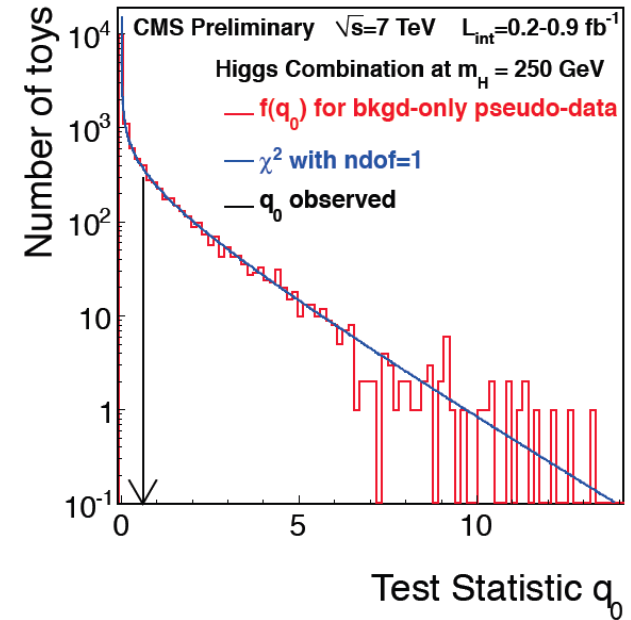
$$p_0 = P(q_0 \geq q_0^{obs}) = \frac{1}{2} \left[ 1 - \text{erf} \left( \sqrt{q_0^{obs}/2} \right) \right]$$

**significance Z** – “one-sided Gaussian tail” convention

$$Z = \sqrt{q_0^{obs}}$$

**IMPORTANT:**

- small “local” p-value means one has a “local” excess w.r.t. bkgd-only expectations
- it does not tell us whether the excess is due to a signal or not
- nor does it tell us whether the excess is consistent with THE expected signal
  - overall rate?
  - relative contributions of different channels?
- moreover, one must be ware of a potentially large **look-elsewhere effect (LEE)**



# Stat methods used: excess (LEE)

**“local” p-value and Z:** chance to fluctuate at least as high as the observed Z at a given  $m_H$

**“global” p-value and Z:** chance to fluctuate at least as high as the observed  $Z_{\max}$  anywhere in the full search range

**trials factor:**  $K = (\text{global p-value for } Z_{\max}) / (\text{local p-value of } Z_{\max})$

## MORE THAN ONE WAY TO ESTIMATE LEE

- if bkgd model for a search in the full mass range is available, one can toss toys
- if MC sample is much larger than data, one can use MC fragments as pseudo-data
- one can assess trials factor from a number of observed low-Z up-crossings
- use a plain bound: K cannot be larger than the number of tested mass points

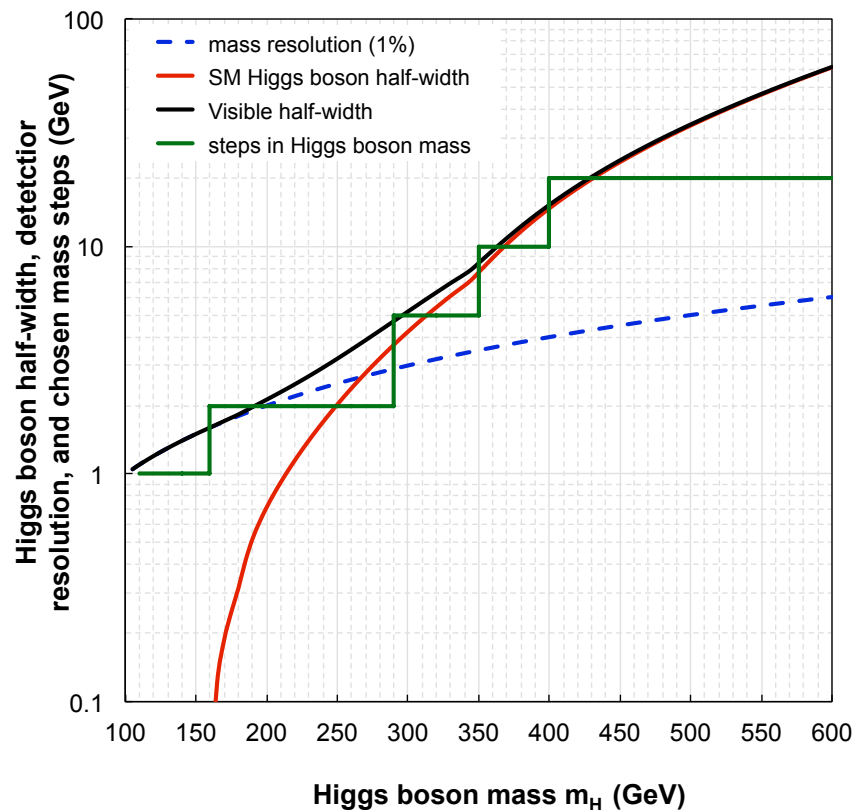
The last two have been used in the current combination

# Test Higgs boson mass points

**step  $\approx 1\sigma$  mass resolution**

- Loss of sensitivity for a Higgs boson with  $m_H$  right between the chosen grid points  $<5\%$
- With twice larger step, we loose up to 20% in sensitivity

**138 mass points  
in the current combination**



# Treatment of theory uncertainties

- **LHC Higgs Cross Section group:**
  - Higgs “QCD scale” errors provided
  - Higgs PDF+ $\alpha_s$  errors provided
  - The two are stated to be independent
  - **Recommendations**
    - use flat pdf for QCD scale uncertainties
    - use normal (or lognormal) pdf for PDF+ $\alpha_s$  uncertainties
    - QCD scale PDF+ $\alpha_s$  uncertainties are to be added linearly
- **LHC Higgs Combination group**
  - takes all this input as is,  
except for the two underlined recommendations

# Treatment of theory uncertainties

## Why not flat pdf for QCD scale uncertainties?

- errors are assessed by varying QCD scales up and down by a factor of  $n$  (typically 2, e.g.  $\mu = \mu_0 \times 2$ )
- it appears unphysical to set pdf=0 (exact!) for CS variations corresponding to  $\mu = \mu_0 \times 2.000001$ , while assign equal pdf density for  $\mu_0$  and  $\mu_0 \times 2.000000$
- we opted to use lognormal errors for all positive-definite quantities (cross sections belong to this class)
  - tests with toy models show that the difference between using flat and lognormal pdf's is small and its sign is not unique (depends on stat method)
  - Tevatron did such tests too with the same conclusion: the effect is small

# Treatment of theory uncertainties

## Why not add errors linearly?

- Adding QCD scale and PDF+ $\alpha_s$  uncertainties linearly would imply 100% positive correlation between them, contrary to the statement that they are independent
- Note that we also need to worry about correlations of systematics between different processes, not just between QCD scale and PDF+ $\alpha_s$  uncertainties for Higgs
- For example:  $gg \rightarrow H \rightarrow WW$  and  $gg \rightarrow WW$ 
  - QCD scale errors for these two are not correlated (so we are told)
  - PDF+ $\alpha_s$  uncertainties for these two are strongly correlated (both of gg-origin; also, explicitly demonstrated by CTEQ folks)
  - Keeping QCD scale and PDF+ $\alpha_s$  uncertainties independent allows to accommodate both requirements