

# Two-dimensional Fermi gases

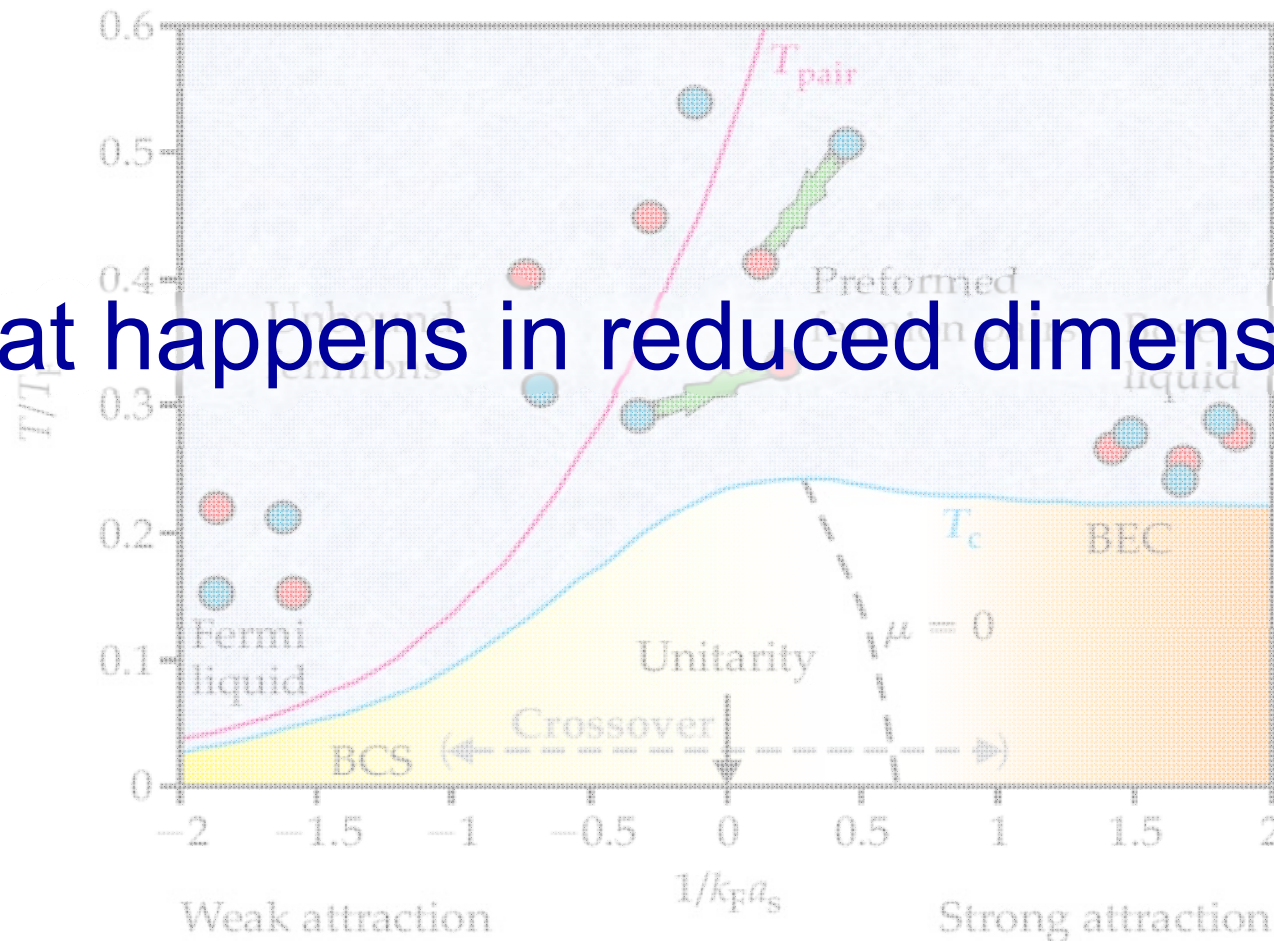
*Michael Köhl*



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# BEC-BCS crossover

What happens in reduced dimensions?

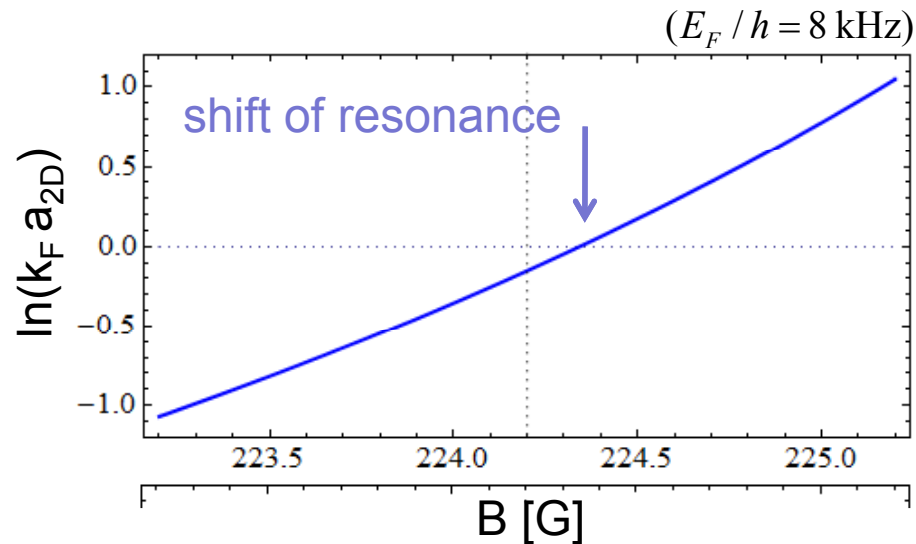


Sa de Melo, Physics Today (2008)



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# A very short theory overview for 2D



Mean-field coupling in 2D

(Bloom 1975)

$$g_{2D} = -\frac{2\pi\hbar^2}{m} \frac{1}{\ln(k_F a_{2D})}$$

$$\left( g_{3D} = \frac{4\pi\hbar^2}{m} a_{3D} \right)$$



Bose gas  
of dimers

strongly interacting  
2D Fermi gas

Fermi  
liquid ?

non-interacting  
2D Fermi gas

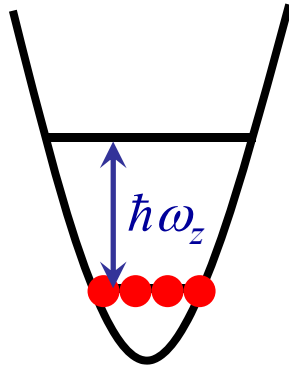
- BKT transition at  $T_{\text{BKT}} \approx 0.1 T_F$  in the strongly interacting regime
- $T_{\text{BKT}}$  decays exponentially towards weak attractive interactions (as in 3D)

*Theory:* Bloom, P.W. Anderson, Randeria, Shlyapnikov, Petrov, Devreese, Julienne, Duan, Zwerger, Giorgini, Sa de Melo, ...



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# Quasi-2D geometry



## Conditions for 2D

$$E_F, k_B T \ll \hbar\omega_z$$

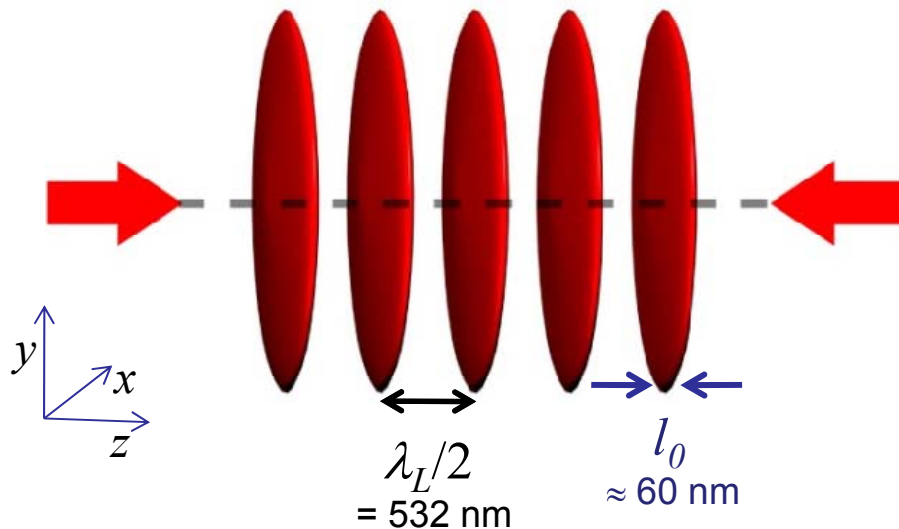
Strong axial confinement required

$$E_F \approx h \times 8 \text{ kHz}$$

$$\omega_z \approx 2\pi \times 80 \text{ kHz}$$

$$\omega_{\perp} \approx 2\pi \times 130 \text{ Hz}$$

## Optical lattice: array of 2D quantum gases



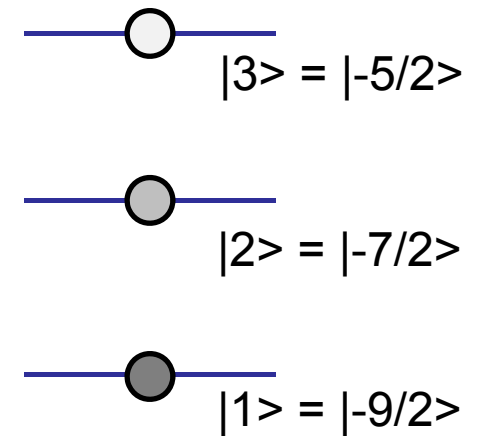
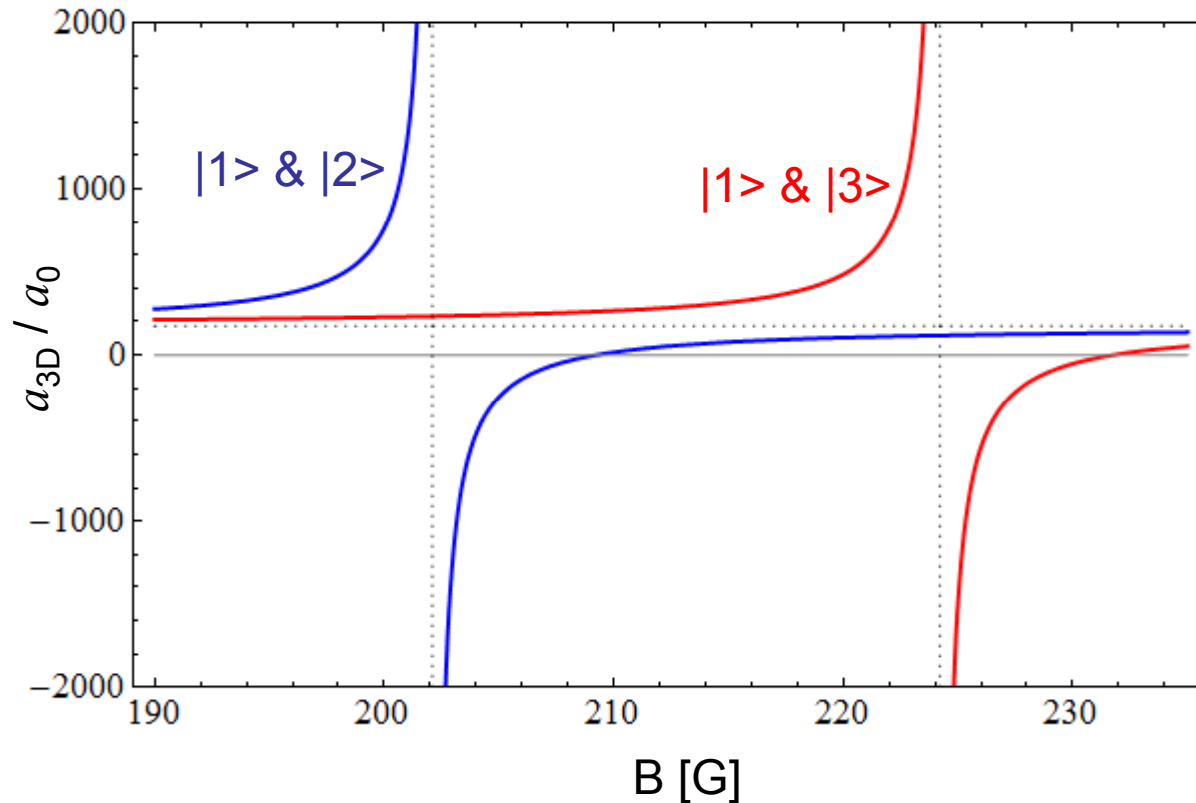
- lattice depth  $83 E_{\text{rec}}$
- hopping rate  $0.002 \text{ Hz}$
- $\sim 2000$  Fermions per spin state
- $\sim 30$  "pancakes" / layers

B. Fröhlich, M. Feld, E. Vogt, M. Koschorreck, W. Zwerger, MK, PRL 106, 105301 (2011)  
other 2D Fermi gases: Inguscio, Grimm, Esslinger, Turlapov, Vale, Zwierlein



# Preparing strongly interacting 2D systems

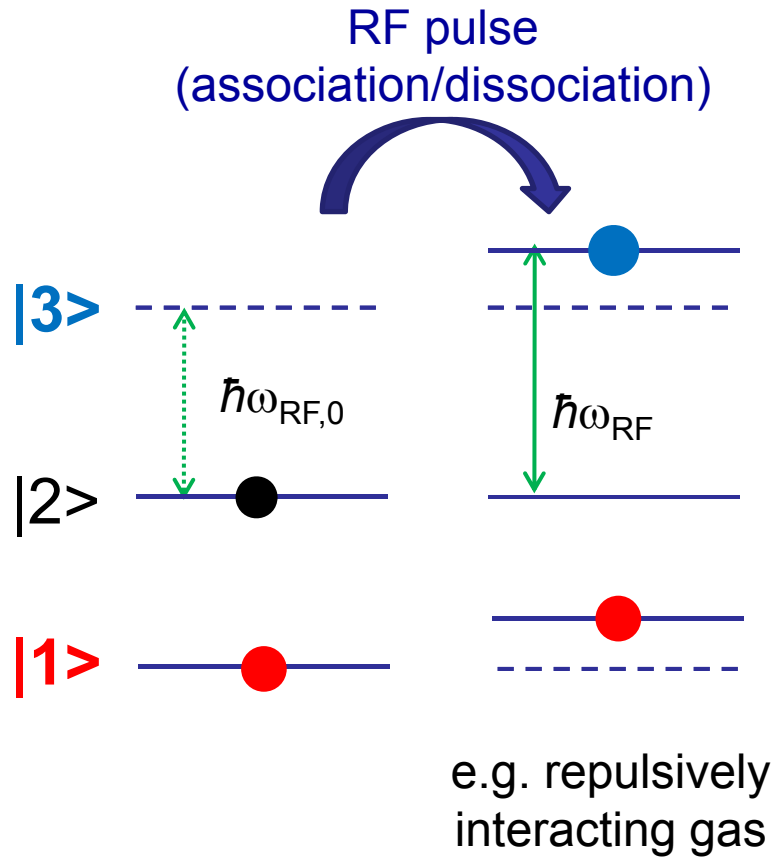
Feshbach resonances in  $^{40}\text{K}$



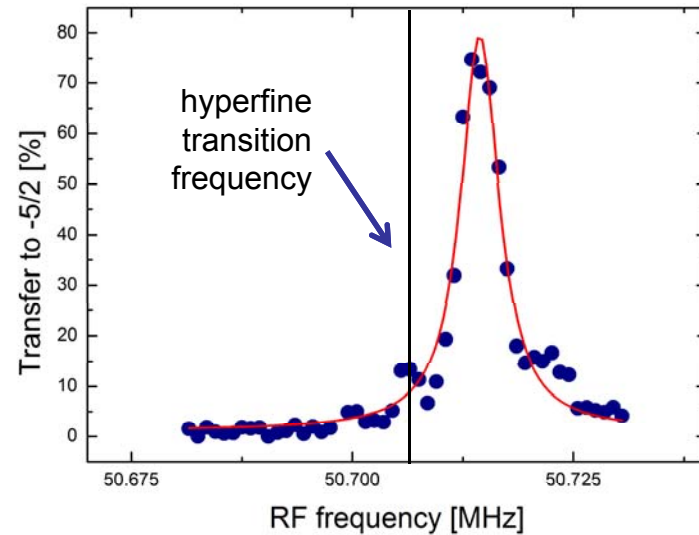
$|2\rangle$  &  $|3\rangle$

$$a_{BG} = 174a_0$$

# Radio-frequency spectroscopy



$|1\rangle$  &  $|3\rangle$   
224G FB res.

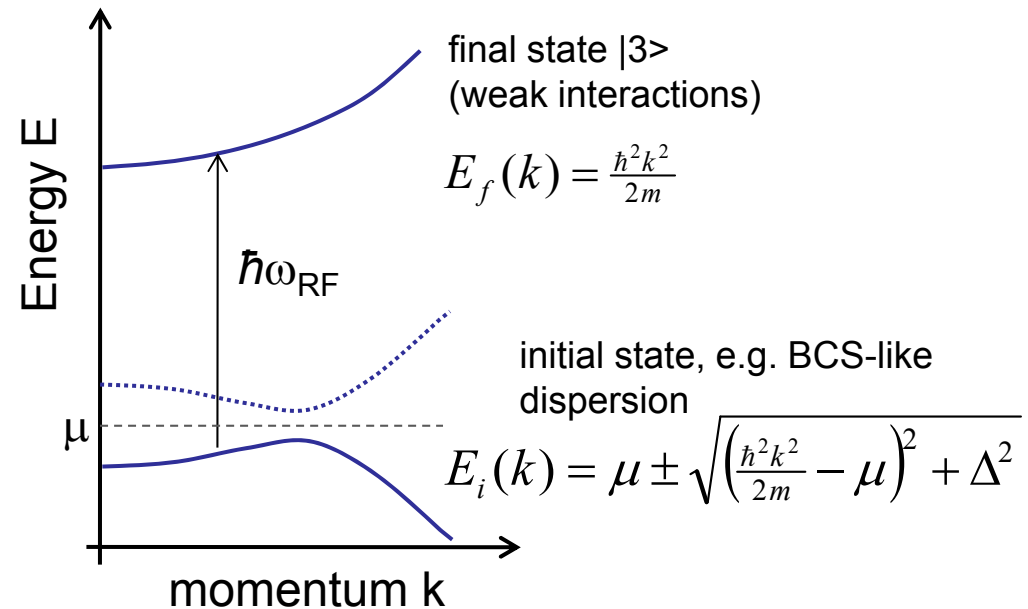
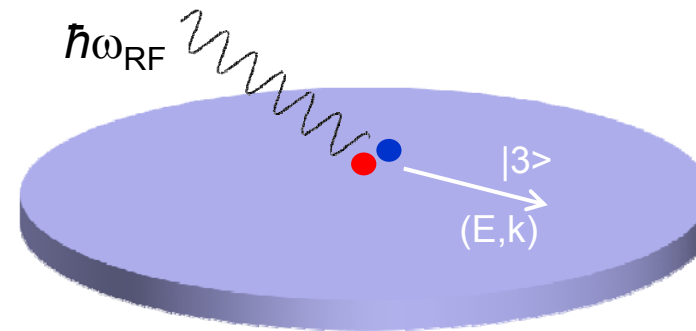
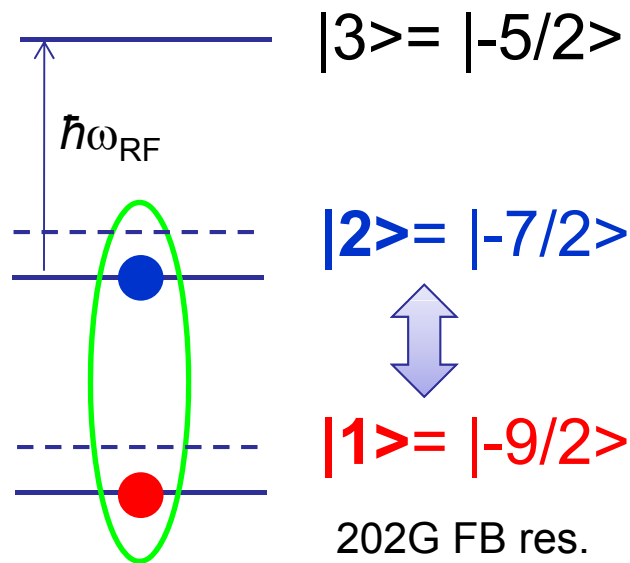


3D: Regal et al., Nature (2003)  
2D: B. Fröhlich, M. Feld, E. Vogt, M. Koschorreck, W. Zwerger, MK, PRL 106, 105301 (2011)



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# Momentum-resolved RF spectroscopy ("ARPES")



ARPES in 3D Experiment: Jin

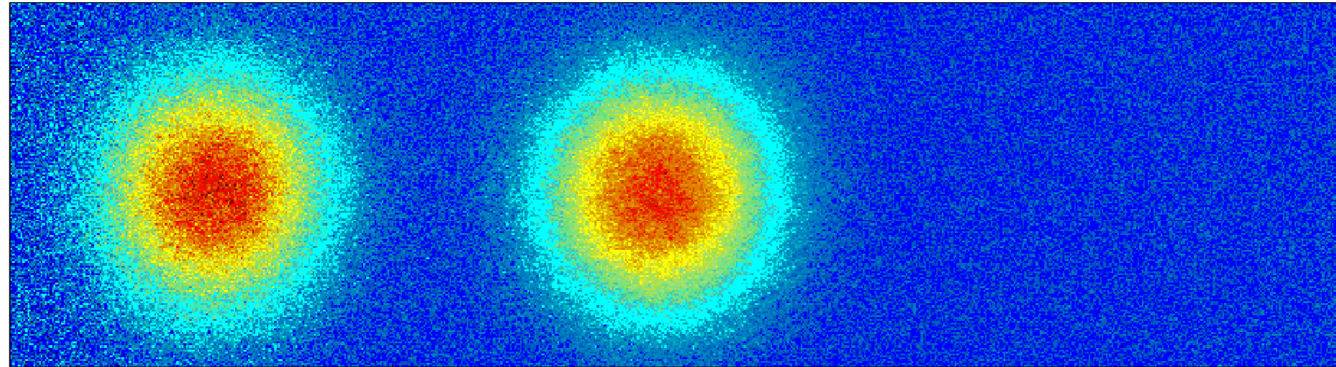
Theory: Georges, Strinati, Levin, Ohashi, Zwerger, Drummond, ...

# Population of the spin states

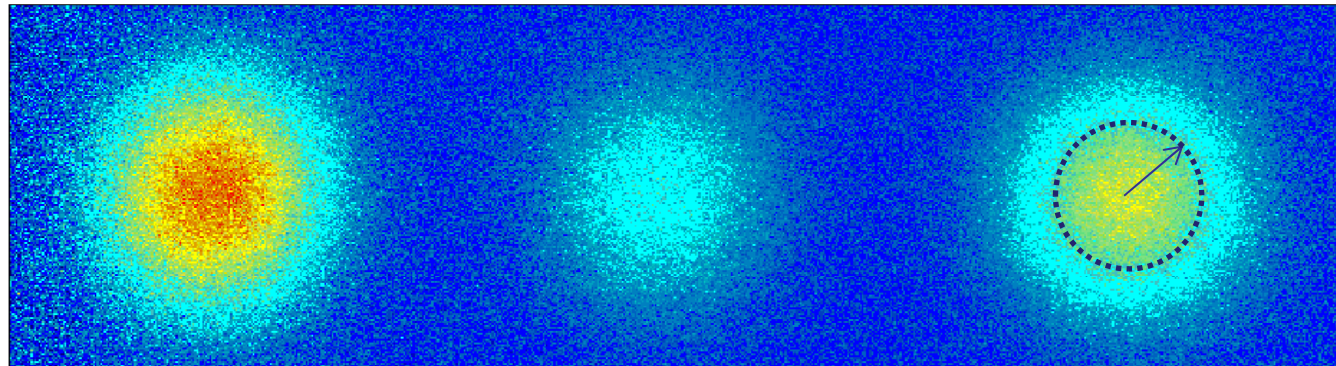
$|-9/2\rangle$

$|-7/2\rangle$

$|-5/2\rangle$



RF pulse

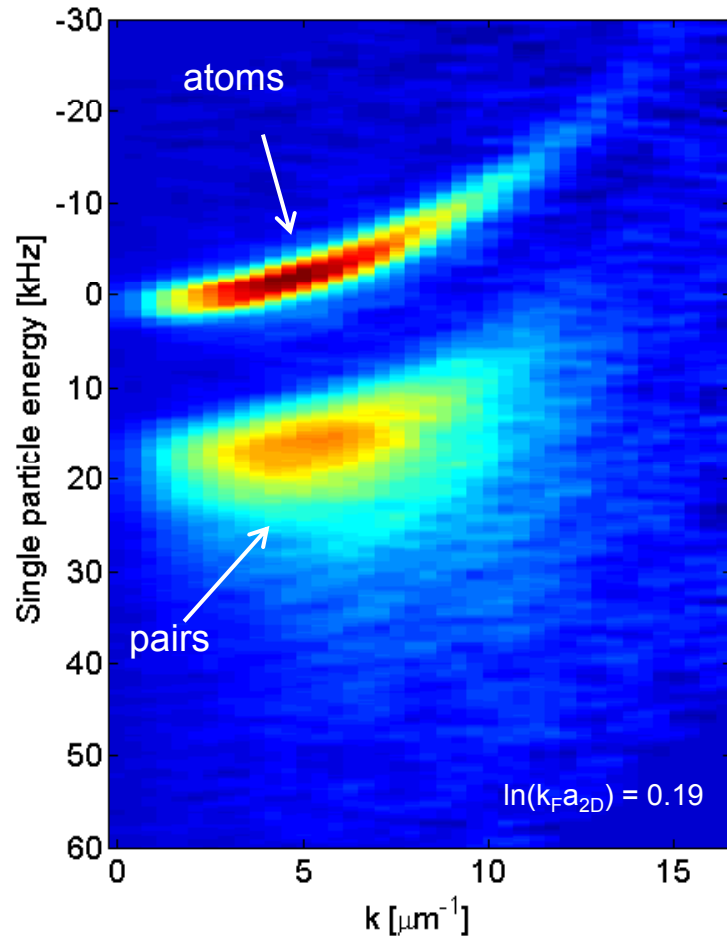


$$k = \sqrt{k_x^2 + k_y^2}$$





# Single-particle spectral function



“BCS” side

$$\ln(k_F a_{2D}) > 0, \quad E_B < E_F$$

no isolated dimers, attractive interactions, pairs are huge compared to inter-particle spacing

“Condensation energy” of Cooper pairs  
(MF theory, T=0, Randeria 1989)

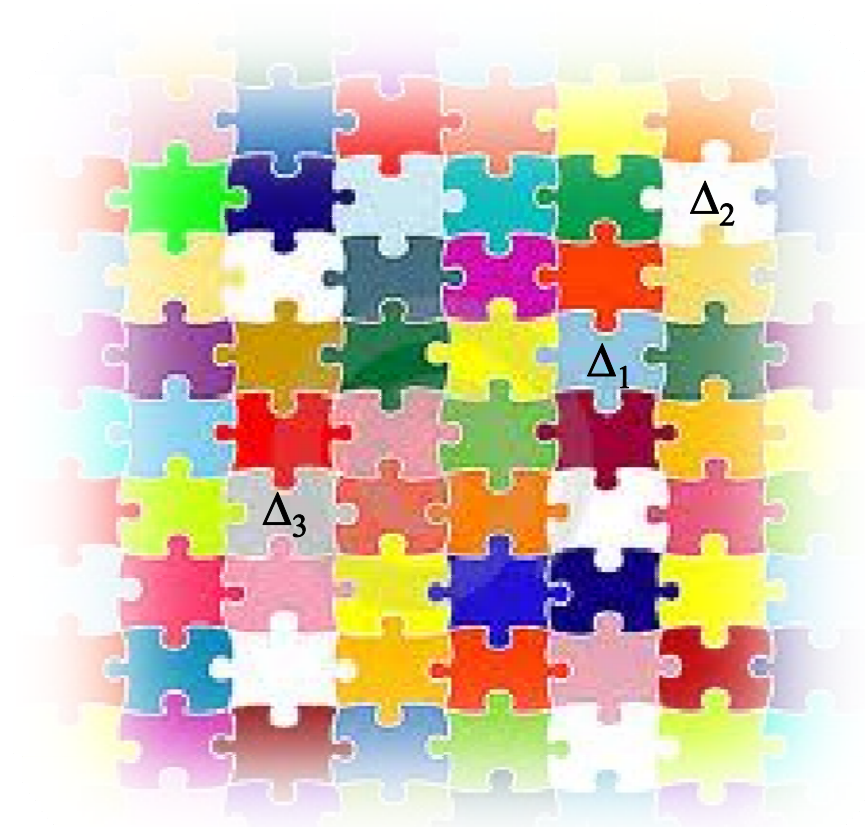
$$E_{th}(k=0) = \frac{\Delta^2}{2E_F} = E_B$$

↑

Only the case in 2D  
(in 3D:  $E_B=0$  on the BCS side)

# Pairing pseudogap phenomenon

complex order parameter  $\Delta(T, x) = |\Delta(T, x)|e^{i\theta(T, x)}$



spatial average

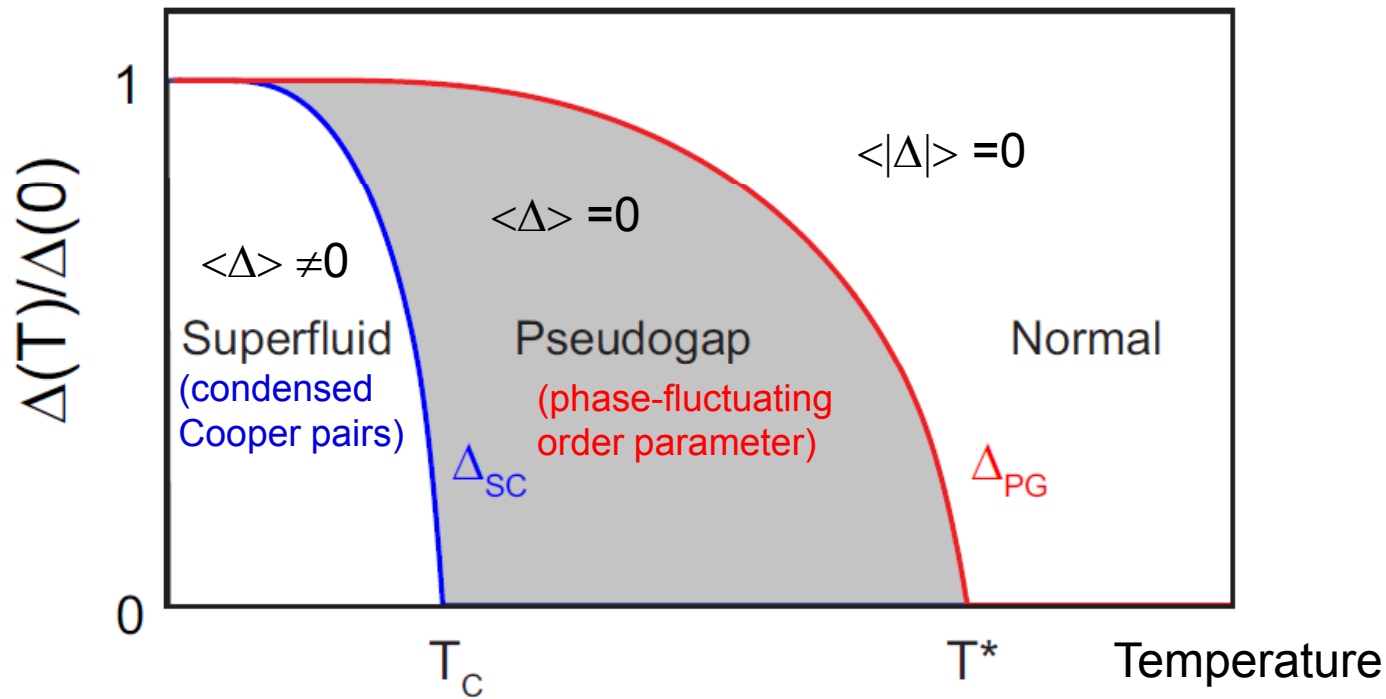
$$\langle \Delta \rangle = 0$$

but  $\langle |\Delta| \rangle > 0$



# Pairing pseudogap phenomenon

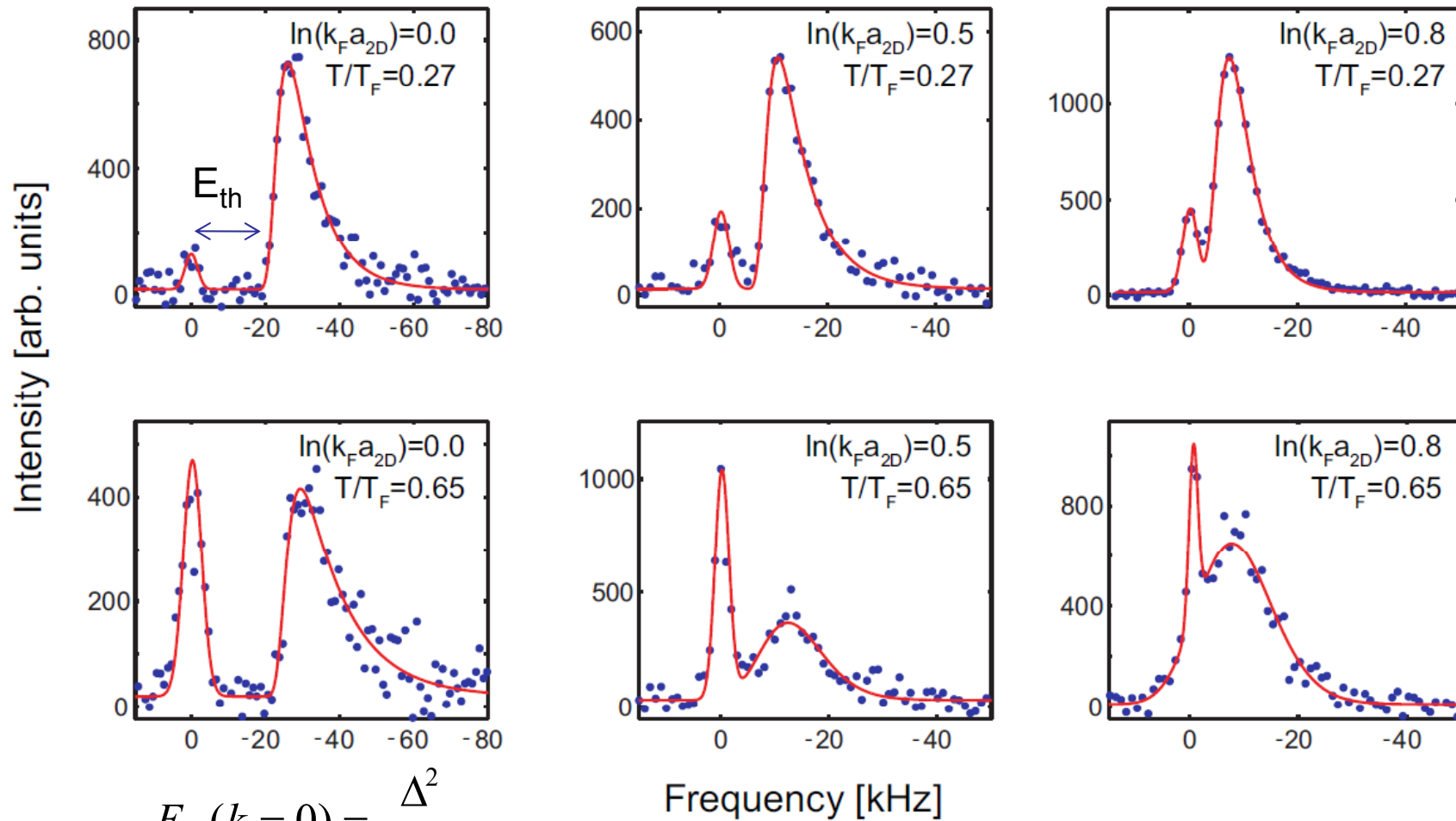
complex order parameter  $\Delta(T, x) = |\Delta(T, x)|e^{i\theta(T, x)}$



In 3D weak coupling BCS:  $T_c \approx T^*$  (pairs condense as they form)

Theory: Randeria, Levin, Sa De Melo, Kleinert, ...

# Spectra at $k=0$ : Determining the pseudogap

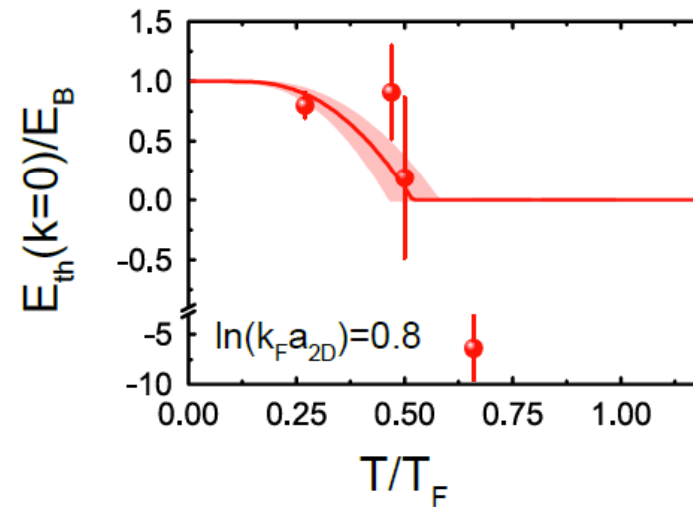
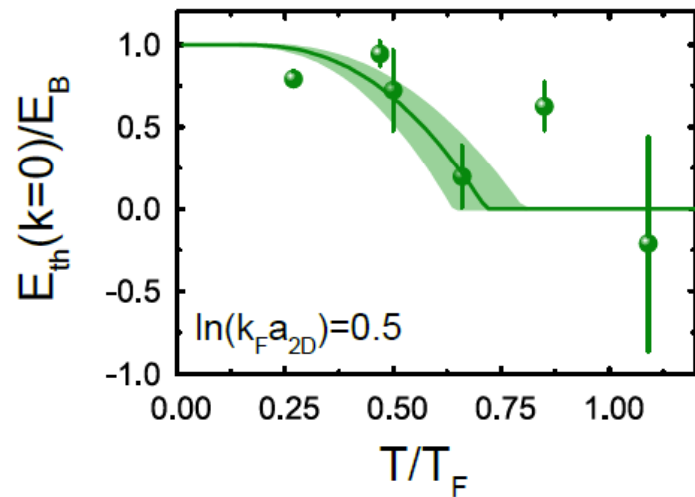
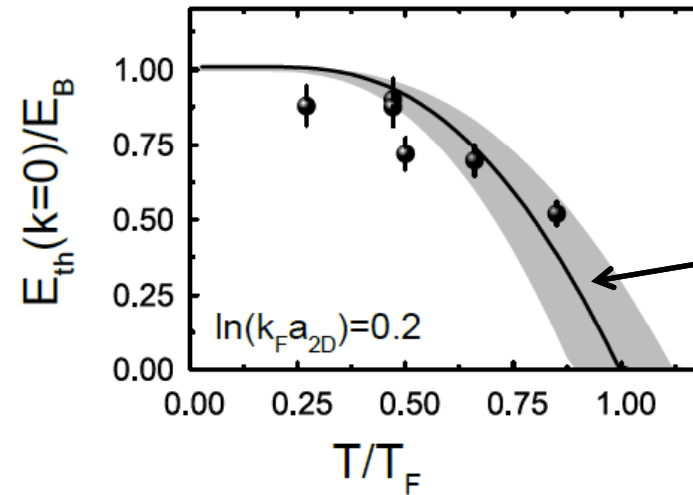
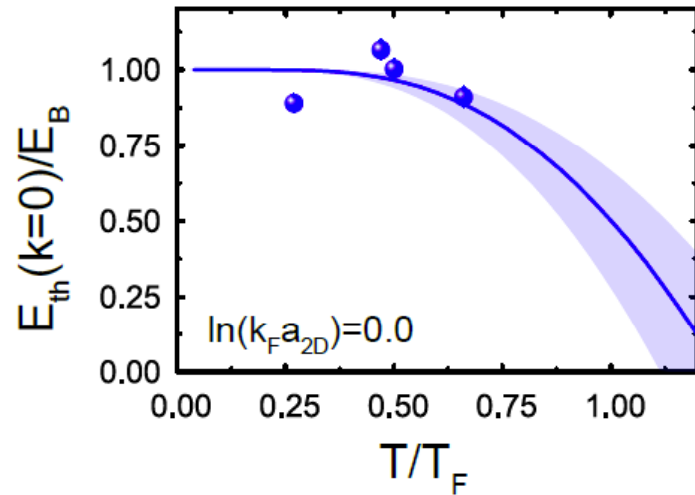


$$E_{th}(k=0) = \frac{\Delta^2}{2E_F}$$

M. Feld et al., Nature 480, 75 (2011)



# Temperature dependence

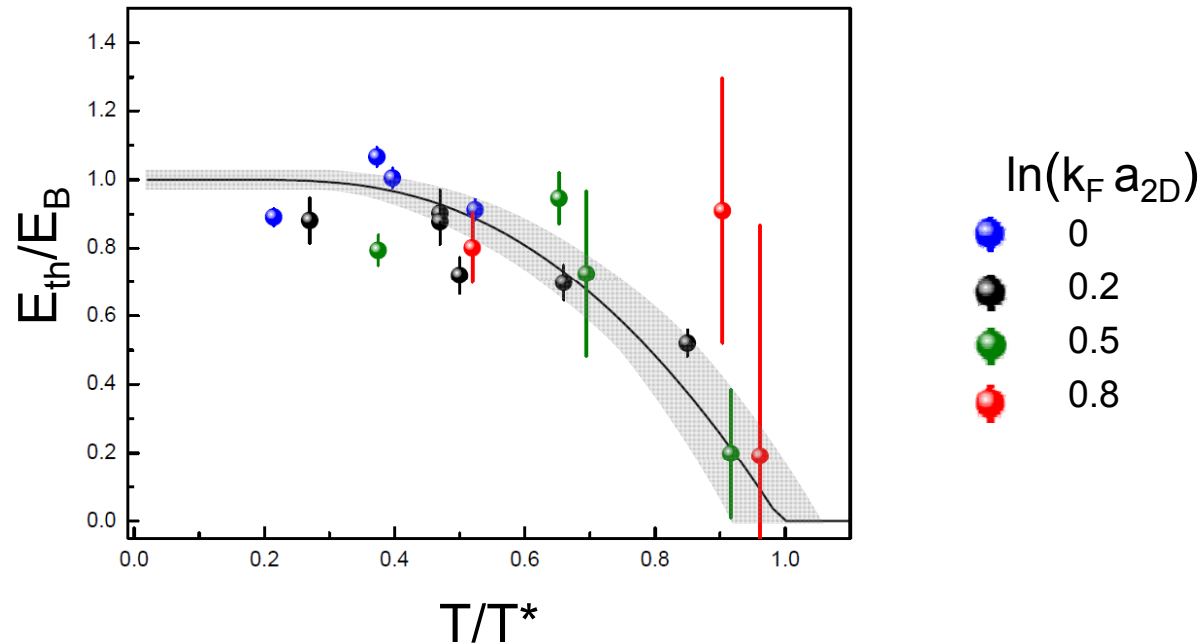


M. Feld et al., Nature 480, 75 (2011)



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# Pairing pseudogap

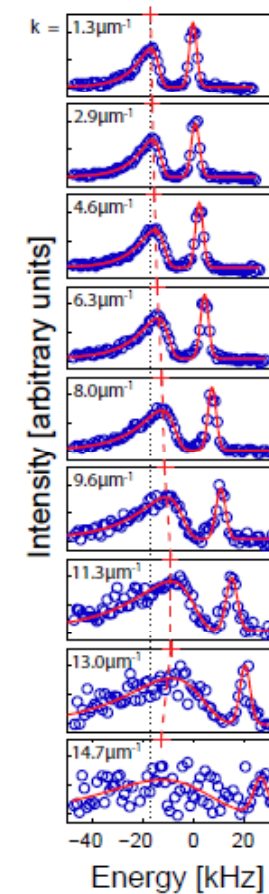
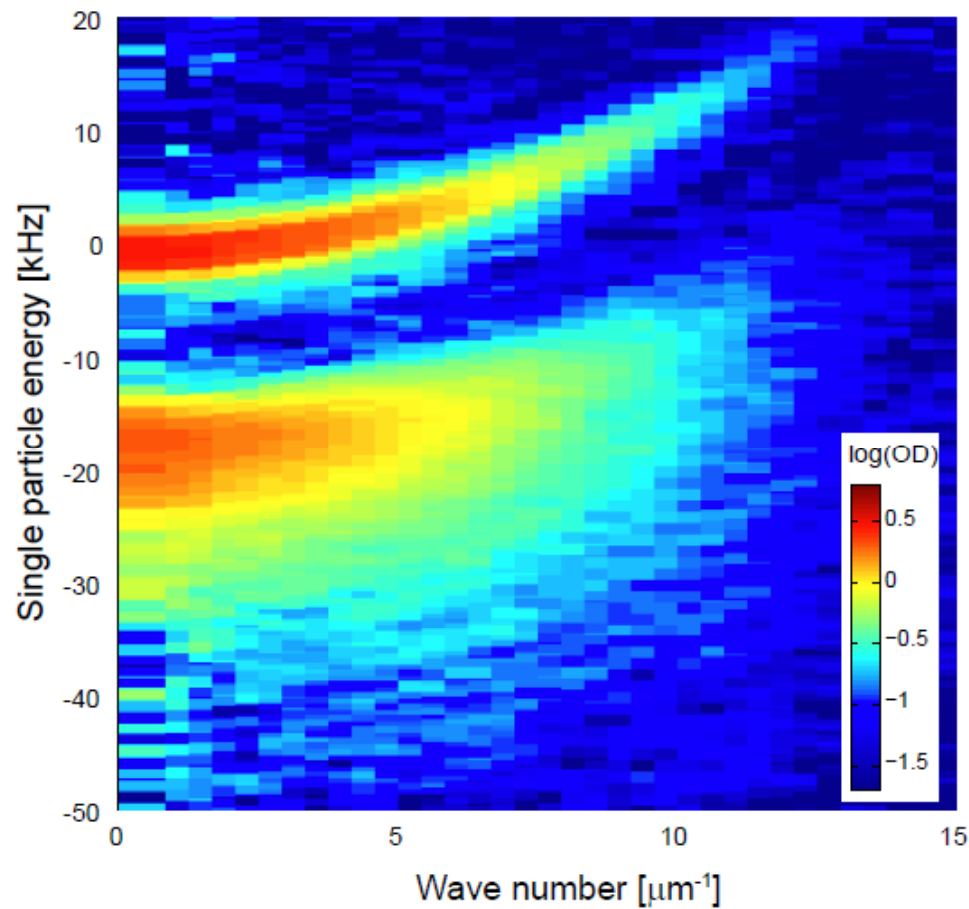


In 3D: Observation of Fermion condensates below  $T/T_F \approx 0.15$   
[by projection onto molecules]

In 2D: No condensation observed.



# Back-bending of dispersion relation

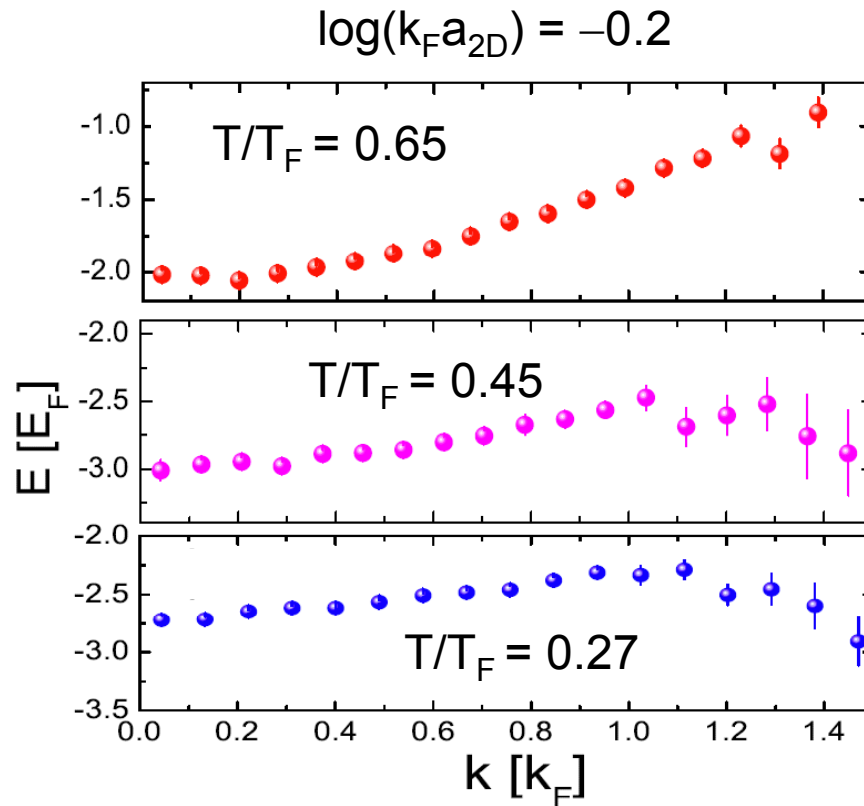


M. Feld et al., Nature 480, 75 (2011)



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# Back-bending of dispersion relation



BCS-like dispersion  
at low T

M. Feld et al., Nature 480, 75 (2011)

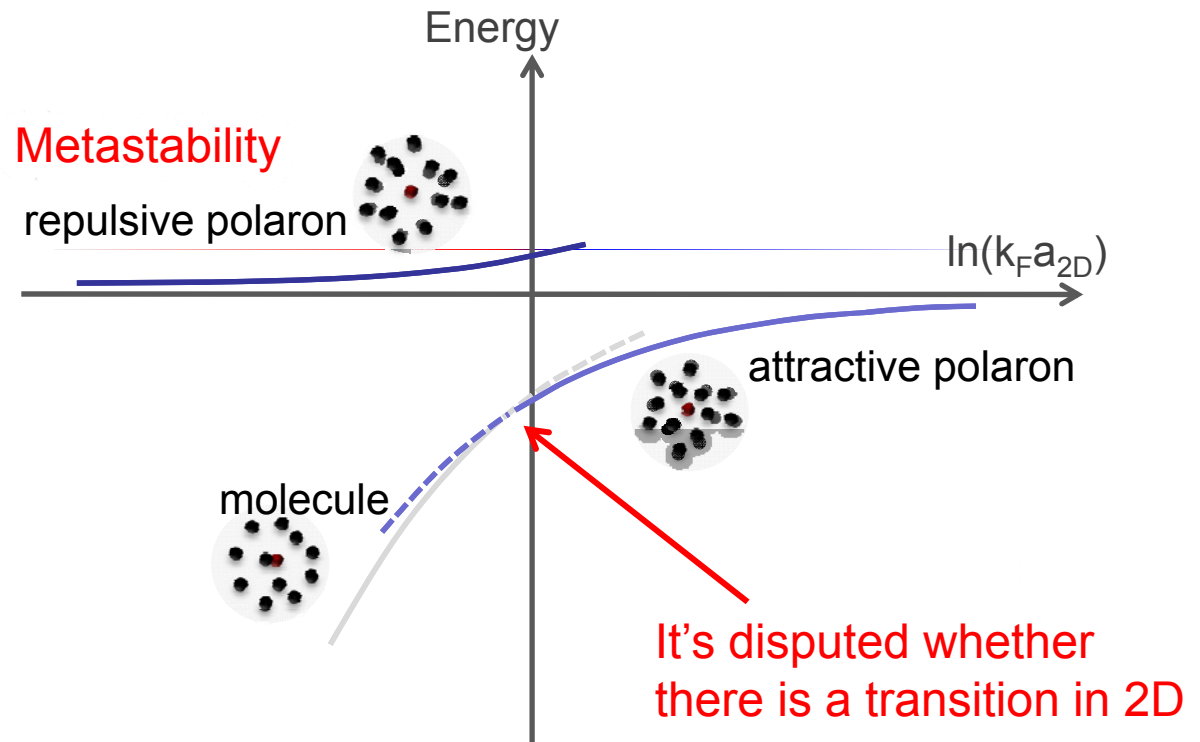


# Strongly imbalanced Fermi gases in 2D

The “N+1” problem: one  $|\downarrow\rangle$  impurity in a large  $|\uparrow\rangle$  Fermi sea

$$|P\rangle = \alpha_0 c_{0\downarrow}^\dagger |N\rangle + \frac{1}{\Omega} \sum_{\mathbf{k}, \mathbf{q}} \alpha_{\mathbf{k}\mathbf{q}} c_{\mathbf{q}-\mathbf{k}\downarrow}^\dagger c_{\mathbf{k}\uparrow}^\dagger c_{\mathbf{q}\uparrow} |N\rangle,$$

- Mobile impurity interacting with a Fermi sea of atoms
- Tunable interactions
- Polaron properties determine phase diagram of imbalanced Fermi mixtures

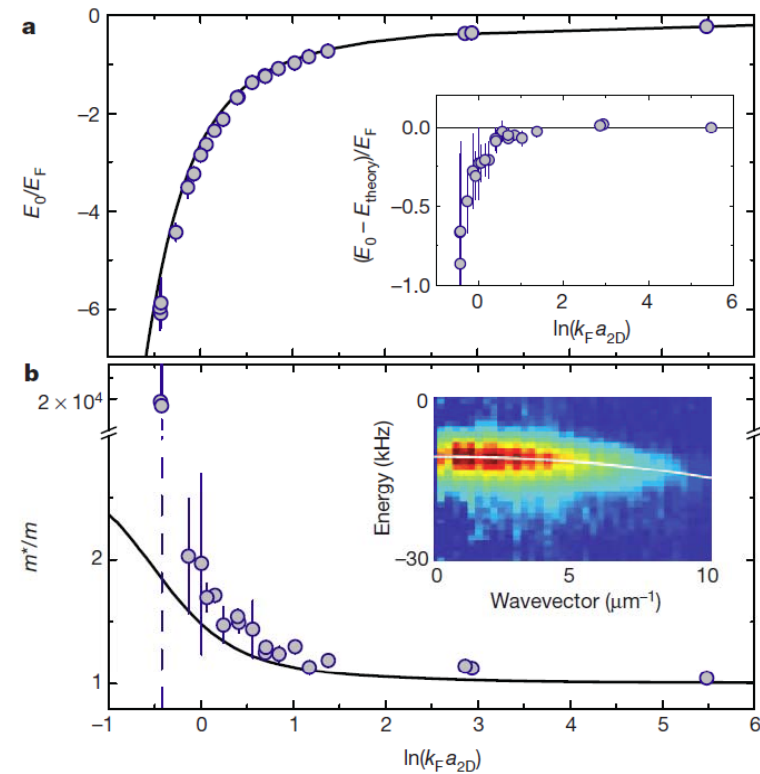
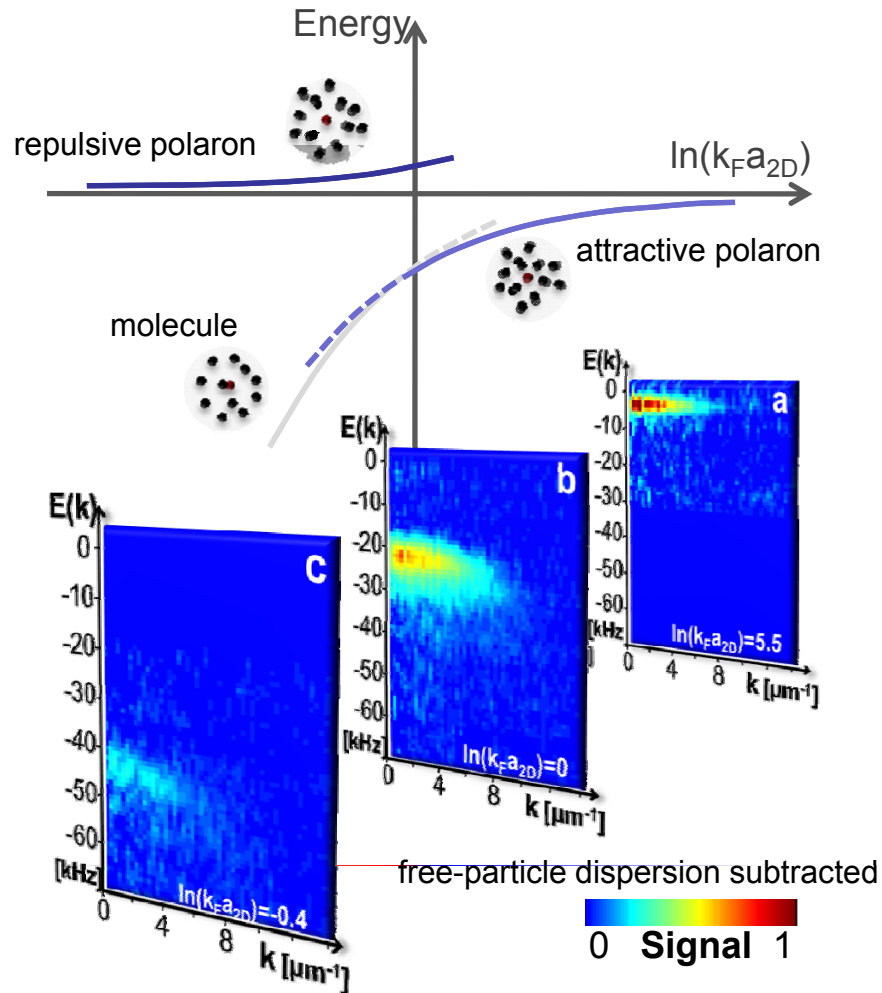


3D Theory: Bruun, Bulgac, Chevy, Giorgini, Lobo, Prokofiev, Stringari, Svistunov, ...

3D Expt: Zwierlein, Salomon, Grimm

2D Theory: Bruun, Demler, Enss, Parish, Pethick, Recati, ...

# Characterizing the attractive polaron

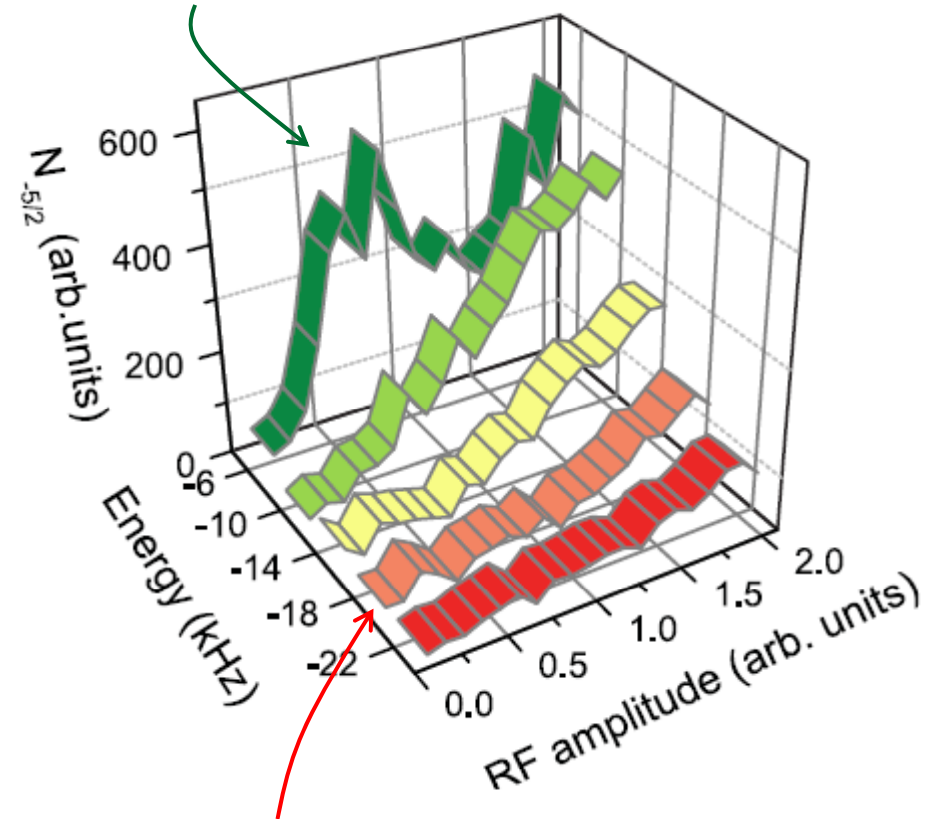
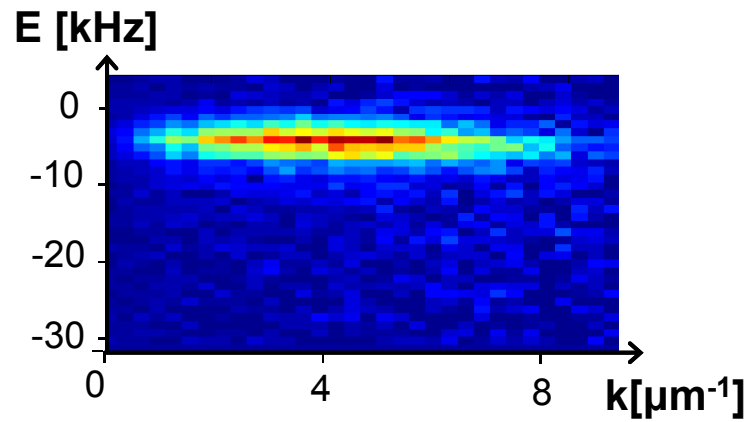


Theory from: R. Schmidt, T. Enss,  
V. Pietilä, E. Demler, PRA 85, 021602 (2012)

M. Koschorreck et al., Nature (2012), Advanced Online Publication 23/5/2012

# Coherence of the polaron

Rabi oscillations between polaron and free particle

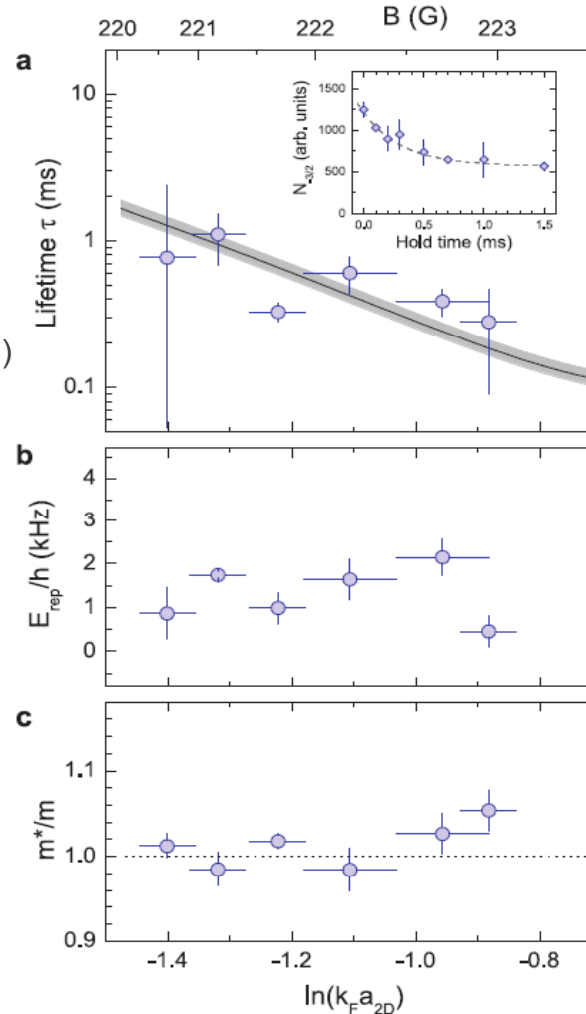
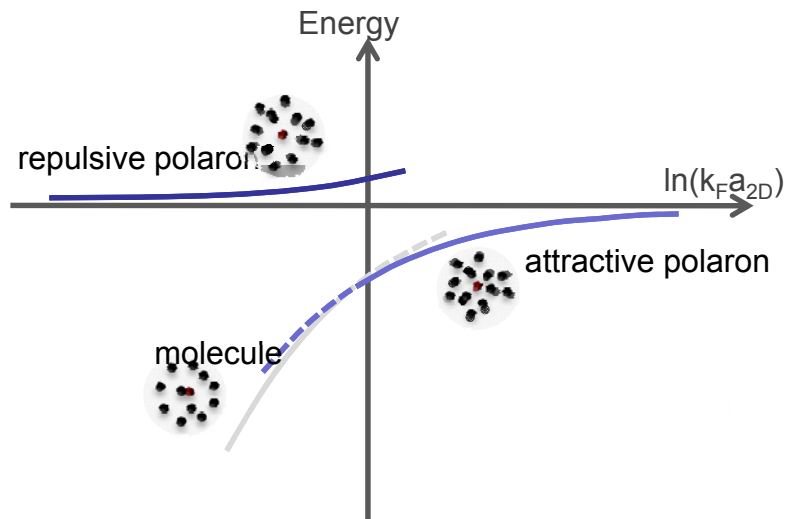


Incoherent transfer: rate  $\sim$  amplitude

M. Koschorreck et al., Nature (2012), Advanced Online Publication 23/5/2012



# Repulsive polaron

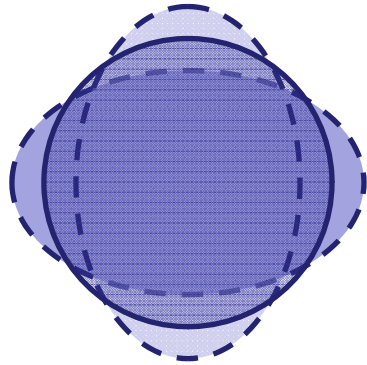


Theory:  
V. Ngampruetikorn et al.,  
EPL 98 30005 (2012).

Energies comparable to:  
R. Schmidt, T. Enss,  
V. Pietilä, E. Demler,  
PRA 85, 021602 (2012)

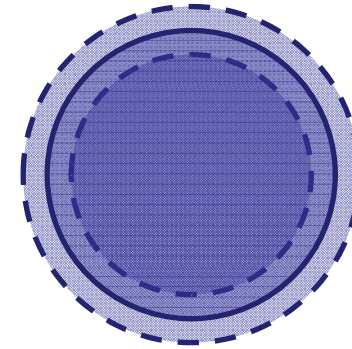
Similar experiments in 3D: Ketterle & Grimm groups M. Koschorreck et al., Nature (2012), Advanced Online Publication 23/5/2012

# Scale invariance and viscosity of a 2D Fermi gas



Quadrupole mode

- insensitive to EoS
- measures shear viscosity



Breathing mode

- measures compressibility
- measures bulk viscosity



# Equation of state and scale invariance

- Scale invariance in a homogeneous system:  $H(\lambda x) = H(x)/\lambda^2$   
→ Simple equation of state  $P = 2\varepsilon/D$
- In cylindrically symmetric trap: scale invariance is replaced by a  $SO(2,1)$  Lorentz symmetry (Pitaevskii/Rosch, 1997)

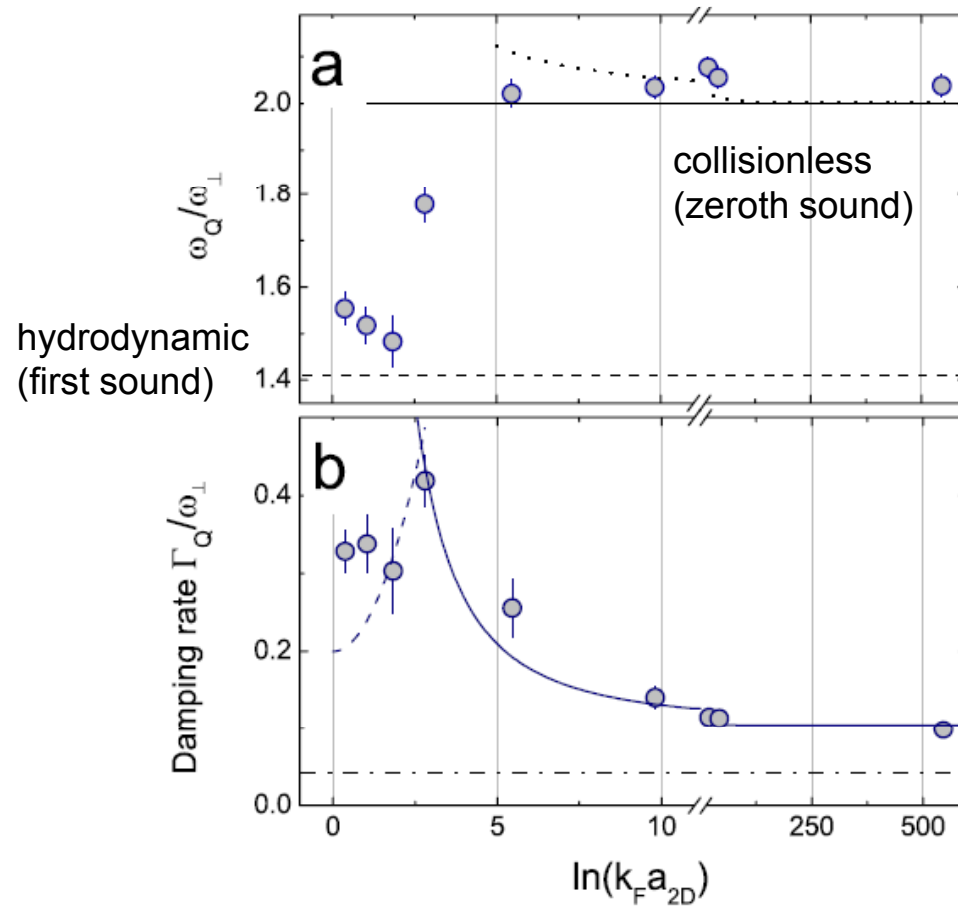
## Two remarkable predictions:

1. Breathing mode:  $\omega_B = 2\omega_{\perp}$  (independent of interaction strength!)
  2. bulk viscosity is zero
- Quantum anomaly due to log-dependence of coupling strength?  
(Olshanii 2010)

For bosons: Pitaevskii/Rosch, Perrin/Olshanii, Chin, Dalibard; for fermions: Schaefer, Hofmann, Randeria/Taylor, Bruun,...

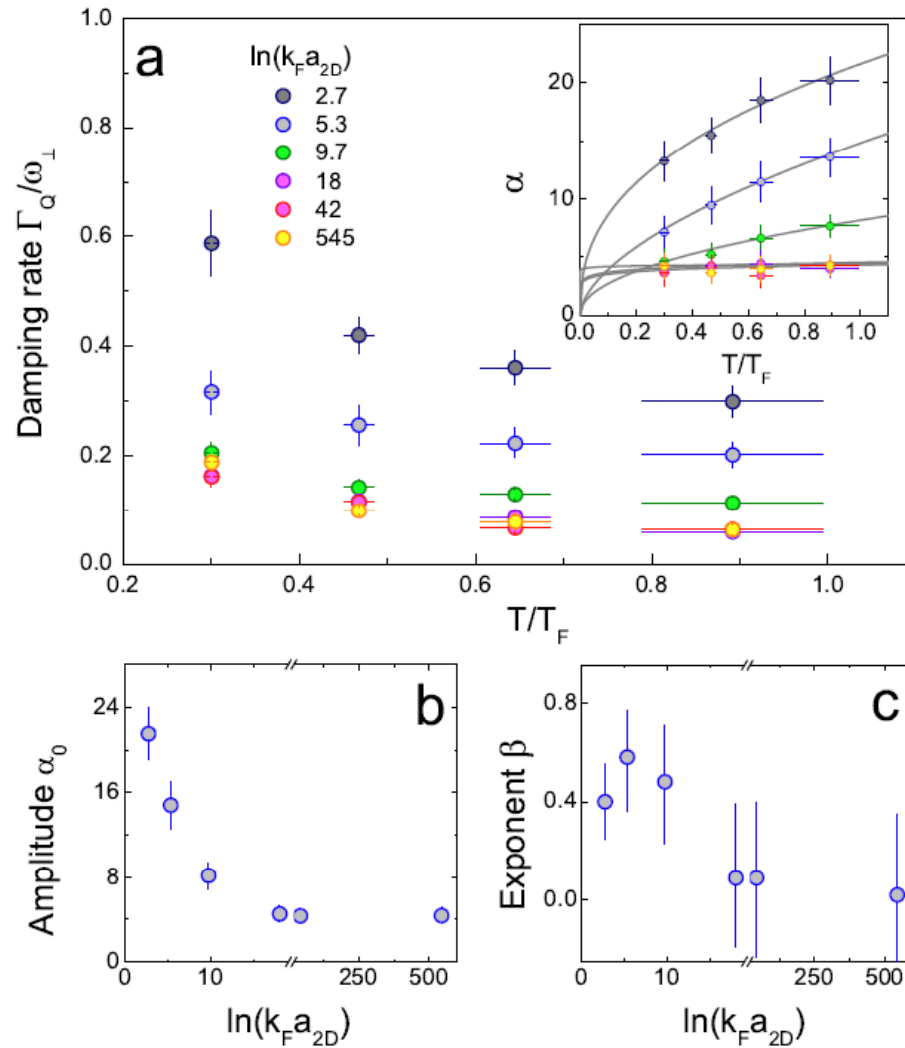
# Collective modes

## Quadrupole mode



E. Vogt et al, PRL 108, 070404 (2012).

# Temperature dependent damping



Shear viscosity

$$\eta = \hbar n \alpha(T/T_F)$$

dimensionless  
function

$$\alpha(T/T_F) = \alpha_0 \times (T/T_F)^\beta$$

E. Vogt et al, PRL 108, 070404 (2012).



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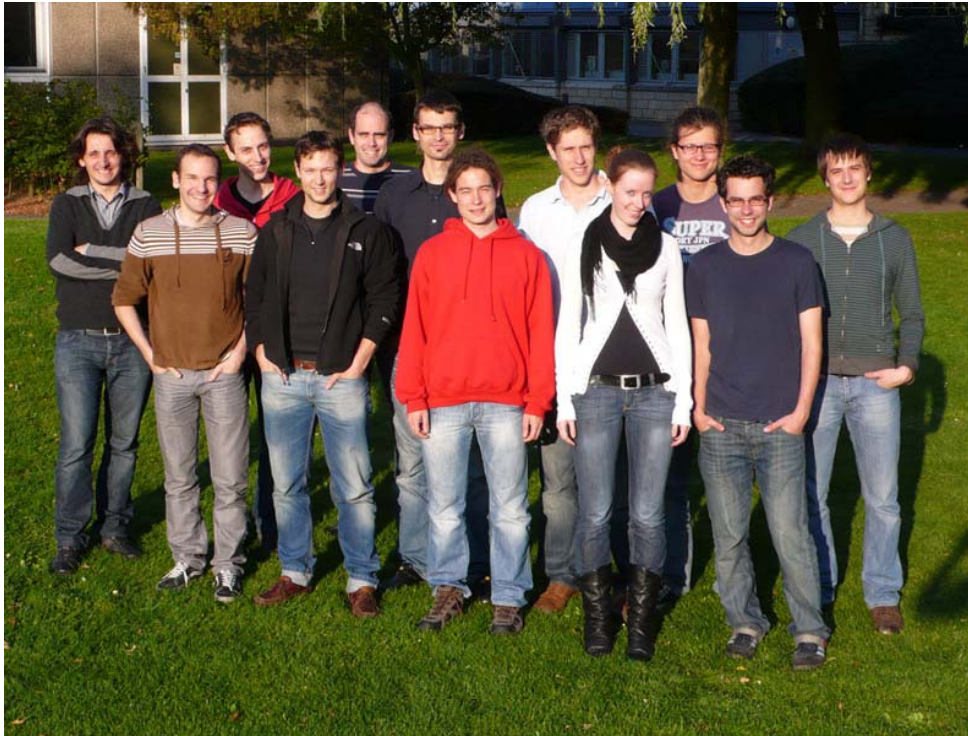


# Summary

- ARPES measurements in 2D
- Pairing pseudogap
- 2D Fermi polaron
- Collective modes to determine equation of state



# Thanks



Fermi gases  
Ion & BEC  
Ion trap QIP

E. Vogt, M. Koschorreck, D. Pertot, L. Miller, E. Cocchi, J. Bohn  
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[www.quantumoptics.eu](http://www.quantumoptics.eu)

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