MODIFIED COUPLINGS FOR A LIGHT COMPOSITE HIGGS

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Effective Lagrangians for a light Higgs

- The explicit form of the Lagrangian depends on the assumptions one makes
- If new particles are discovered they can be included in the Lagrangian in a bottom-up approach

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I WILL ASSUME:

- 1) $SU(2)_L x U(1)_Y$ is linearly realized at high energies
- 2) h(x) is a scalar (CP even) and is part of an SU(2)_L doublet H(x)
- 3) The EWSB dynamics has an (approximate) custodial symmetry global symmetry includes: $SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$

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- each extra derivative costs a factor $1/\Lambda$
- each extra power of H(x) costs a factor $g_*/\Lambda \equiv 1/f$

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For a strongly-interacting Higgs:

$$\frac{1}{f} \gg \frac{1}{\Lambda}$$

Buchmuller and Wyler, NPB 268 (1986) 621

In the following I will follow the SILH parametrization proposed in:

$$\begin{split} \mathcal{L}_{\text{SILH}} &= \frac{c_H}{2f^2} \partial^{\mu} \left(H^{\dagger} H \right) \partial_{\mu} \left(H^{\dagger} H \right) + \frac{c_T}{2f^2} \left(H^{\dagger} \overleftrightarrow{D^{\mu}} H \right) \left(H^{\dagger} \overleftrightarrow{D}_{\mu} H \right) \\ &- \frac{c_6 \lambda}{f^2} \left(H^{\dagger} H \right)^3 + \left(\frac{c_y y_f}{f^2} H^{\dagger} H \bar{f}_L H f_R + \text{h.c.} \right) \\ &+ \frac{i c_W g}{2m_{\rho}^2} \left(H^{\dagger} \sigma^i \overleftrightarrow{D^{\mu}} H \right) \left(D^{\nu} W_{\mu\nu} \right)^i + \frac{i c_B g'}{2m_{\rho}^2} \left(H^{\dagger} \overleftrightarrow{D^{\mu}} H \right) \left(\partial^{\nu} B_{\mu\nu} \right) \\ &+ \frac{i c_H W g}{m_{\rho}^2} \frac{g_{\rho}^2}{16\pi^2} \left(D^{\mu} H \right)^{\dagger} \sigma^i (D^{\nu} H) W_{\mu\nu}^i + \frac{i c_H B g'}{m_{\rho}^2} \frac{g_{\rho}^2}{16\pi^2} \left(D^{\mu} H \right)^{\dagger} (D^{\nu} H) B_{\mu\nu} \\ &+ \frac{c_{\gamma} g'^2}{m_{\rho}^2} \frac{g_{\rho}^2}{16\pi^2} \frac{g_{\rho}^2}{g_{\rho}^2} H^{\dagger} H B_{\mu\nu} B^{\mu\nu} + \frac{c_g g_S^2}{m_{\rho}^2} \frac{g_{\rho}^2}{16\pi^2} \frac{y_t^2}{g_{\rho}^2} H^{\dagger} H G_{\mu\nu}^a G^{a\mu\nu} \end{split}$$

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Giudice, Grojean, Pomarol, Rattazzi JHEP 0706 (2007) 045

 $\mathcal{L}_{\text{SILH}} = \begin{bmatrix} \frac{c_H}{2f^2} \partial^{\mu} \left(H^{\dagger} H \right) \partial_{\mu} \left(H^{\dagger} H \right) + \frac{c_T}{2f^2} \left(H^{\dagger} \overrightarrow{D^{\mu}} H \right) \left(H^{\dagger} \overrightarrow{D}_{\mu} H \right) \\ - \frac{c_6 \lambda}{f^2} \left(H^{\dagger} H \right)^3 + \left(\frac{c_y y_f}{f^2} H^{\dagger} H \overline{f}_L H f_R + \text{h.c.} \right) \\ + \frac{i c_W g}{2m_{\rho}^2} \left(H^{\dagger} \sigma^i \overrightarrow{D^{\mu}} H \right) \left(D^{\nu} W_{\mu\nu} \right)^i + \frac{i c_B g'}{2m_{\rho}^2} \left(H^{\dagger} \overrightarrow{D^{\mu}} H \right) \left(\partial^{\nu} B_{\mu\nu} \right) \\ + \frac{i c_{HW} g}{m_{\rho}^2} \frac{g_{\rho}^2}{16\pi^2} \left(D^{\mu} H \right)^{\dagger} \sigma^i (D^{\nu} H) W_{\mu\nu}^i + \frac{i c_{HB} g'}{m_{\rho}^2} \frac{g_{\rho}^2}{16\pi^2} \left(D^{\mu} H \right)^{\dagger} (D^{\nu} H) B_{\mu\nu} \\ + \frac{c_{\gamma} g'^2}{m_{\rho}^2} \frac{g_{\rho}^2}{16\pi^2} \frac{g_{\rho}^2}{g_{\rho}^2} H^{\dagger} H B_{\mu\nu} B^{\mu\nu} + \frac{c_g g_S^2}{m_{\rho}^2} \frac{g_{\rho}^2}{16\pi^2} \frac{y_t^2}{g_{\rho}^2} H^{\dagger} H G_{\mu\nu}^a G^{a\mu\nu} \end{bmatrix}$

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Probes of Higgs strong interaction

$$\frac{c_H}{2f^2} \partial^{\mu} (H^{\dagger} H) \partial_{\mu} (H^{\dagger} H)$$
$$\frac{c_y y_{\psi}}{f^2} H^{\dagger} H \bar{\psi}_L H \psi_R + h.c.$$
$$\frac{c_6 \lambda_4}{f^2} (H^{\dagger} H)^3$$

Parametrize corrections to tree-level Higgs couplings:

$$\frac{\Delta c}{c_{SM}} \sim \frac{v^2}{f^2} = \left(\frac{g_* v}{\Lambda}\right)^2$$

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6

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Use equations of motions:

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contact correction to three-body decays



inclusive WW,ZZ observables

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exclusive WW,ZZ observables and Z $\!\gamma$

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Use equations of motions:

$$D_{\mu}V_{\mu\nu}V_{\nu}h = (m_V^2V_{\nu} + \bar{\psi}\gamma_{\nu}\psi)V_{\nu}h$$

Notice: LEP already puts strong bounds on these operators

$$\hat{S} = (c_W + c_B) \, \frac{m_W^2}{\Lambda^2} \lesssim 10^{-3}$$

effects expected to be small

$$\frac{i c_{HW} g}{\Lambda^2} (D^{\mu} H)^{\dagger} \sigma^a (D^{\mu} H) W^a_{\mu\nu}$$
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 $G_{\mu\nu}G_{\mu\nu}h$

These operators imply couplings of photon and gluons to neutral particles and give corrections to the gyromagnetic ratios

$$c_{\gamma Zh} \propto (c_{HW} - c_{HB})$$

 $(g - 2)_W \propto (c_{HW} + c_{HB})$

$$\frac{g_*^2}{16\pi^2} \times \frac{i c_{HW}g}{\Lambda^2} (D^{\mu}H)^{\dagger} \sigma^a (D^{\mu}H) W^a_{\mu\nu}$$
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They cannot be generated by integrating out heavy states at tree-level in a minimally coupled gauge theory

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Corrections to $h \rightarrow WW$, ZZ rates:

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one linear combination starts at dim=8

 $G_{\mu\nu}G_{\mu\nu}h$

Corrections to $h \rightarrow WW$, ZZ rates:

'Form factor'

Corrections to $h \rightarrow WW$, ZZ angular distributions and $h \rightarrow \gamma Z$ rate:

 $\frac{\delta \mathcal{A}}{\mathcal{A}_{SM}} \sim \left(\frac{v^2}{f^2}\right)$

test Higgs strong interactions

$$\frac{g_*^2}{16\pi^2} \times \frac{i c_{HW}g}{\Lambda^2} \left(D^{\mu}H\right)^{\dagger} \sigma^a \left(D^{\mu}H\right) W^a_{\mu\nu}$$
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In principle $h \rightarrow \gamma \gamma$, *gg* rates also probe strong dynamics ...

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$$\frac{\delta \mathcal{A}}{\mathcal{A}_{SM}} \sim \left(\frac{v^2}{f^2}\right) \times \frac{\lambda^2}{g_*^2}$$

'Form factor'

For a pNG boson Higgs additional suppression follows from breaking the shift symmetry

$$\begin{aligned} \mathcal{L} &= \frac{1}{2} \partial_{\mu} h \, \partial^{\mu} h - \frac{1}{2} m_{h}^{2} h^{2} + d_{3} \, \frac{1}{6} \left(\frac{3m_{h}^{2}}{v} \right) h^{3} + \dots \\ &- \left(m_{W}^{2} \, W_{\mu} W^{\mu} + \frac{1}{2} m_{Z}^{2} \, Z_{\mu} Z^{\mu} \right) \left(1 + 2c_{V} \, \frac{h}{v} + \dots \right) - \sum_{\psi=u,d,l} m_{\psi^{(i)}} \, \bar{\psi}^{(i)} \psi^{(i)} \left(1 + c_{\psi} \, \frac{h}{v} + \dots \right) \\ &+ \frac{\alpha_{em}}{8\pi} \left(2 \, c_{WW} \, W_{\mu\nu}^{+} W^{-\mu\nu} + c_{ZZ} \, Z_{\mu\nu} Z^{\mu\nu} + 2 \, c_{Z\gamma} \, Z_{\mu\nu} \gamma^{\mu\nu} + c_{\gamma\gamma} \, \gamma_{\mu\nu} \gamma^{\mu\nu} \right) \frac{h}{v} \\ &+ \frac{\alpha_{s}}{8\pi} \, c_{gg} \, G_{\mu\nu}^{a} G^{a \, \mu\nu} \, \frac{h}{v} + c_{W} \left(W_{\nu}^{-} D_{\mu} W^{+ \, \mu\nu} + h.c. \right) \frac{h}{v} + c_{Z} \, Z_{\nu} \partial_{\mu} Z^{\mu\nu} \, \frac{h}{v} \\ &+ \left(\frac{c_{W}}{\sin \theta_{W} \cos \theta_{W}} - \frac{c_{Z}}{\tan \theta_{W}} \right) Z_{\nu} \partial_{\mu} \gamma^{\mu\nu} \, \frac{h}{v} + \dots \end{aligned}$$

$$\mathcal{L} = \frac{1}{2} \partial_{\mu} h \, \partial^{\mu} h - \frac{1}{2} m_{h}^{2} h^{2} + d_{3} \frac{1}{6} \left(\frac{3m_{h}^{2}}{v} \right) h^{3} + \dots$$

$$- \left(m_{W}^{2} W_{\mu} W^{\mu} + \frac{1}{2} m_{Z}^{2} Z_{\mu} Z^{\mu} \right) \left(1 + 2c_{V} \frac{h}{v} + \dots \right) - \sum_{\psi=u,d,l} m_{\psi^{(i)}} \bar{\psi}^{(i)} \psi^{(i)} \left(1 + c_{\psi} \frac{h}{v} + \dots \right) \right)$$

$$+ \frac{\alpha_{em}}{8\pi} \left(2 c_{WW} W_{\mu\nu}^{+} W^{-\mu\nu} + c_{ZZ} Z_{\mu\nu} Z^{\mu\nu} + 2 c_{Z\gamma} Z_{\mu\nu} \gamma^{\mu\nu} + c_{\gamma\gamma} \gamma_{\mu\nu} \gamma^{\mu\nu} \right) \frac{h}{v}$$

$$+ \frac{\alpha_{s}}{8\pi} c_{gg} G_{\mu\nu}^{a} G^{a\,\mu\nu} \frac{h}{v} + c_{W} \left(W_{\nu}^{-} D_{\mu} W^{+\mu\nu} + h.c. \right) \frac{h}{v} + c_{Z} Z_{\nu} \partial_{\mu} Z^{\mu\nu} \frac{h}{v}$$

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The same effective Lagrangian describes a generic scalar h (custodial singlet) with SU(2)_LxU(1)_Y non-linearly realized

Each term can be dressed up with Nambu-Goldstone bosons and made manifestly $SU(2)_L x U(1)_Y$ invariant

$$\mathcal{L} = \frac{1}{2} \partial_{\mu} h \, \partial^{\mu} h - \frac{1}{2} m_{h}^{2} h^{2} + d_{3} \frac{1}{6} \left(\frac{3m_{h}^{2}}{v} \right) h^{3} + \dots$$

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$$+ \left(\frac{c_{W}}{\sin \theta_{W} \cos \theta_{W}} - \frac{c_{Z}}{\tan \theta_{W}} \right) Z_{\nu} \partial_{\mu} \gamma^{\mu\nu} \frac{h}{v} + \dots$$

- The only predictions of SILH (for single Higgs processes) are:
 - (1) The deviation of each coupling from its SM value must be small

ex:
$$c_V = 1 + \frac{c_H}{2} \frac{v^2}{f^2}$$

(2) The following relation holds: $c_{Z\gamma} = \frac{c_{WW}}{\sin(2\theta_W)} - \frac{c_{ZZ}}{2}\cot(\theta_W) - \frac{c_{\gamma\gamma}}{2}\tan(\theta_W)$

$$\mathcal{L} = \frac{1}{2} \partial_{\mu} h \, \partial^{\mu} h - \frac{1}{2} m_{h}^{2} h^{2} + d_{3} \frac{1}{6} \left(\frac{3m_{h}^{2}}{v} \right) h^{3} + \dots$$

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$$+ \frac{\alpha_{em}}{8\pi} \left(2 c_{WW} W_{\mu\nu}^{+} W^{-\mu\nu} + c_{ZZ} Z_{\mu\nu} Z^{\mu\nu} + 2 c_{Z\gamma} Z_{\mu\nu} \gamma^{\mu\nu} + c_{\gamma\gamma} \gamma_{\mu\nu} \gamma^{\mu\nu} \right) \frac{h}{v}$$

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 Large deviations from SM couplings do not necessarily disprove a Higgs doublet (e.g. non-linearities can be large)

In that case a test of doublet/pNGB Higgs can come from double (and triple) Higgs processes

RC, Grojean, Moretti, Piccinini, Rattazzi, JHEP 1005 (2010) 089

RC, Grojean, Pappadopulo, Rattazzi, Thamm, work in progress

Enlarge SO(4)/SO(3) to SO(5)/SO(4):

[Agashe, RC, Pomarol, NPB 719 (2005) 165]

- four NG bosons form an SU(2)_L doublet H(x): the Higgs is the fourth NG boson
- resums powers of H/f (Higgs non-linearities), while still assuming expansion in ∂/Λ

Validity: $E \ll \Lambda \leq 4\pi f$

RULES:

Dress up all operators with NG bosons and build the most general Lagrangian invariant under *local* SO(4) transformations

Building blocks: CCWZ variables

$$U(\pi) = e^{i\pi(x)/f} \qquad -i U(\pi)^{\dagger} D_{\mu} U(\pi) \equiv d_{\mu}^{\hat{a}} T^{\hat{a}} + E_{\mu}^{a} T^{a}$$
$$d_{\mu} \sim \frac{D_{\mu}\pi}{f} + \dots \qquad E_{\mu} \sim A_{\mu} + \frac{1}{f^{2}} \pi \overleftrightarrow{D}_{\mu}\pi + \dots$$
$$d_{\mu} \rightarrow h(\pi, g) d_{\mu} h^{-1}(\pi, g)$$

$$E_{\mu} \to h(\pi, g) E_{\mu} h^{-1}(\pi, g) + i [\partial_{\mu} h(\pi, g)] h^{-1}(\pi, g)$$
$$h \in SO(4)$$

O(p ⁴) Lagrangian	SILH Lagrangian
$f^2 \operatorname{Tr}(d_{\mu} d^{\mu})$	O_H
$O_1^+ = [\text{Tr}(d_{\mu}d^{\mu})]^2$ $O_2^+ = [\text{Tr}(d_{\mu}d_{\nu})]^2$	dim=8
$O_3^{\pm} = \text{Tr} \left[(E_{\mu\nu}^L)^2 \pm (E_{\mu\nu}^R)^2 \right]$	O_W, O_B
$O_4^{\pm} = \operatorname{Tr}\left[\left(E_{\mu\nu}^L \pm E_{\mu\nu}^R \right) i [d^{\mu}, d^{\nu}] \right]$	O_{HW}, O_{HB}
$= \left[\text{Tr}(T^{a_L}[d_{\mu}, d_{\nu}]) \right]^2 - \left[\text{Tr}(T^{a_R}[d_{\mu}, d_{\nu}]) \right]^2$	dim=8

 O_5^-

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$$O_{1}^{+} = [\operatorname{Tr}(d_{\mu}d^{\mu})]^{2}$$

$$O_{2}^{+} = [\operatorname{Tr}(d_{\mu}d_{\nu})]^{2}$$

$$O_{3}^{\pm} = \operatorname{Tr}[(E_{\mu\nu}^{L})^{2} \pm (E_{\mu\nu}^{R})^{2}]$$

$$O_{4}^{\pm} = \operatorname{Tr}[(E_{\mu\nu}^{L} \pm E_{\mu\nu}^{R})i[d^{\mu}, d^{\nu}]]$$

$$O_{5}^{-} = [\operatorname{Tr}(T^{a_{L}}[d_{\mu}, d_{\nu}])]^{2} - [\operatorname{Tr}(T^{a_{R}}[d_{\mu}, d_{\nu}])]^{2}$$
Operators with +(-)
Superscript are even (odd
under a LR parity)
$$O_{5}^{-} = [\operatorname{Tr}(T^{a_{L}}[d_{\mu}, d_{\nu}])]^{2} - [\operatorname{Tr}(T^{a_{R}}[d_{\mu}, d_{\nu}])]^{2}$$

)

$$\begin{array}{cccc} \pi^{\hat{i}} \to -\pi^{\hat{i}} & d_{\mu} \to P_{RL} \, d_{\mu} \, P_{LR} & \\ \pi^{\hat{4}} \to +\pi^{\hat{4}} & E_{\mu}^{L} \leftrightarrow P_{RL} \, E_{\mu}^{R} \, P_{RL} & P_{LR} = \begin{pmatrix} -1 & & \\ & -1 & & \\ & & -1 & \\ & & & +1 & \\ & & & & +1 \end{pmatrix} \\ \hat{i} = 1, 2, 3 & & & & \\ \end{array}$$

$$O_{1}^{+} = [\operatorname{Tr}(d_{\mu}d^{\mu})]^{2}$$

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Notice: P_{LR} : is an <u>accidental</u> invariance at $O(p^2)$

$$\mathcal{L}^{(2)} = \frac{f^2}{4} \operatorname{Tr}(d_{\mu}d^{\mu})$$



The decay $h \rightarrow Z\gamma$ in composite Higgs models

[Based on: Azatov, RC, Di lura, Galloway, work in progress]

Mediated by two operators of the SILH Lagrangian:

$$O_{HW} = \frac{i c_{HW} g}{16\pi^2 f^2} (D^{\mu} H)^{\dagger} \sigma^a (D^{\mu} H) W^a_{\mu\nu}$$

$$O_{HB} = \frac{i c_{HB} g'}{16\pi^2 f^2} (D^{\mu} H)^{\dagger} (D^{\mu} H) B_{\mu\nu}$$

$$O_{BB} = \frac{c_{BB} g'^2}{16\pi^2 f^2} B_{\mu\nu} B^{\mu\nu} H^{\dagger} H$$

$$c_{Z\gamma} \left(\frac{\alpha_{em}}{2\pi}\right) \gamma_{\mu\nu} Z^{\mu\nu} \frac{h}{v}$$

$$c_{Z\gamma} = \frac{c_{HB} - c_{HW}}{4\sin(2\theta_W)} - 2\tan\theta_W c_{BB}$$

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only one breaks
the Higgs shift
$$O_{BB} = \frac{c_{BB}g'^2}{16\pi^2 f^2} B_{\mu\nu}B^{\mu\nu}H^{\dagger}H$$

$$c_{Z\gamma} \left(\frac{\alpha_{em}}{2\pi}\right) \gamma_{\mu\nu}Z^{\mu\nu}\frac{h}{v}$$

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symmetry

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only one breaks
the Higgs shift or $O_{BB} = \frac{c_{BB} g'^2}{16\pi^2 f^2} B_{\mu\nu} B^{\mu\nu} H^{\dagger} H$

$$C_{Z\gamma} \left(\frac{\alpha_{em}}{2\pi}\right) \gamma_{\mu\nu} Z^{\mu\nu} \frac{h}{v}$$

$$c_{Z\gamma} = \frac{c_{HB} - c_{HW}}{4\sin(2\theta_W)} - 2\tan\theta_W c_{BB}$$

Unlike $h \rightarrow \gamma \gamma$, gg, the rate $h \rightarrow \gamma Z$ does not carry the extra spurion suppression:

$$\frac{\Gamma(h \to Z\gamma)}{\Gamma(h \to Z\gamma)_{SM}} = 1 + O\left(\frac{v^2}{f^2}\right)$$

tests Higgs strong interactions

Mediated by two operators of the SILH Lagrangian:

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$$O_{BB} = \frac{c_{BB} g'^2}{16\pi^2 f^2} B_{\mu\nu} B^{\mu\nu} H^{\dagger} H$$

In the SO(5)/SO(4) Lagrangian there is one operator at $O(p^4)$:

$$O_{HW} - O_{HB} \longrightarrow O_4^- = \operatorname{Tr}\left[\left(E_{\mu\nu}^L - E_{\mu\nu}^R\right)i[d^{\mu}, d^{\nu}]\right]$$

$$c_{Z\gamma} = g^2 c_4^- \left(\frac{v}{f}\right)^2$$

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$$\underbrace{\gamma_{\mu\nu}} \widetilde{Z_{\mu}(v/f)}$$

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at 1-loop: $\sim \frac{1}{16\pi^{2}}$ IR running due
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Naively the IR contribution would dominate over the UV one

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<u>However</u>: $O_4^- = \text{Tr}\left[\left(E_{\mu\nu}^L - E_{\mu\nu}^R\right)i[d^{\mu}, d^{\nu}]\right]$ is odd under P_{LR}

Accidental P_{LR} invariance of the $O(p^2)$ Lagrangian forbids any running due NG bosons

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Accidental P_{LR} invariance of the $O(p^2)$ Lagrangian forbids any running due NG bosons

 c_4^- entirely comes from UV threshold contributions

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If P_{LR} is an exact invariance of the strong dynamics, generating O_4^- costs an additional weak spurion factor:

$$c_4^- \sim rac{1}{16\pi^2} imes rac{\lambda^2}{g_*^2} \qquad \mbox{back to the estimate of $\gamma\gamma$, gg}$$

Consider the case of one spin-1 (3,1) of $SU(2)_L x SU(2)_R$ lighter than the other resonances

$$\rho_{\mu} \to h(\pi, g) \rho_{\mu} h^{-1}(\pi, g) + [\partial_{\mu} h(\pi, g)] h^{-1}(\pi, g)$$



 $----- m_h, m_W$

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Assumption: the derivative expansion of the Lagrangian is controlled by (∂/Λ):

$$\mathcal{L} = \frac{f^2}{4} d^{\hat{a}}_{\mu} d^{\hat{a}\,\mu} - \frac{1}{4g^2_{\rho_L}} \rho^{a_L}_{\mu\nu} \rho^{a_L\,\mu\nu} + \frac{m^2_{\rho}}{2g^2_{\rho_L}} \left(\rho^{a_L}_{\mu} - E^{a_L}_{\mu}\right)^2 + \sum_i \alpha_i \, Q_i + \cdots$$

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 ρ can be integrated out by solving the e.o.m at lowest order

$$\rho_{\mu} = E_{\mu} + O(\partial^2 / m_{\rho}^2)$$

$$\mathcal{L}_{eff} = \left(-\frac{1}{g_{\rho}^2} + \alpha_2\right) \operatorname{Tr}\left[\left(E_{\mu\nu}^L\right)^2\right] + \left(\alpha_1 - \alpha_2\right) \operatorname{Tr}\left[E_{\mu\nu}^L i[d_{\mu}, d_{\nu}]\right]$$

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the strength of any interactions of the resonance does not exceed g_* up to the cutoff scale

[Partial UV completion]

RC, Marzocca, Pappadopulo, Rattazzi JHEP 1110 (2011) 081

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Ex:

$$\mathcal{A}(\pi\pi\rho^{(T)}) \sim g_{\rho} \left[a_{\rho}^{2} + \alpha_{1} \frac{E^{2}}{f^{2}} \right]$$

$$\mathcal{A} \leq g_{*} \text{ for } E \leq \Lambda \longrightarrow \alpha_{1} \lesssim \frac{1}{g_{*}g_{\rho}} < \frac{1}{g_{\rho}^{2}}$$

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By saturating the bound:
$$\alpha_{1,2} \sim \frac{1}{g_{
ho}^2} \times \frac{g_{
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In general:
$$c_4^- = (\alpha_1^L - \alpha_1^R) - (\alpha_2^L - \alpha_2^R) \sim \frac{1}{16\pi^2}$$

Let us neglect the mixings with elementary fields and work in the CCWZ basis:

$$\mathcal{L} = \bar{\chi} \left(\gamma^{\mu} \, i \nabla_{\mu} - m \right) \chi + \zeta \, \bar{\chi} \, \gamma^{\mu} i d_{\mu} \, \chi$$

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$$\downarrow$$

$$\partial_{\mu} + i (E^{L}_{\mu} + E^{R}_{\mu})$$
LR symmetric

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Only one diagram generates O_4^- :

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LR symmetric

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MODEL 1 [MCHM5]:

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MODEL 2 [MCHM10]:

$$\chi = (2,2) \oplus (3,1) \oplus (1,3) \qquad \qquad \mathcal{L} = \sum_{i=4,3L,3R} \bar{\chi}_i \left(\gamma^{\mu} i \nabla_{\mu} - m_i\right) \chi_i \\ = \{\chi_4, \chi_{3L}, \chi_{3R}\} \qquad \qquad \qquad + \zeta_L \ \bar{\chi}_4 \ \gamma^{\mu} i d_{\mu} \ \chi_{3L} + \zeta_R \ \bar{\chi}_4 \ \gamma^{\mu} i d_{\mu} \ \chi_{3R} + h.c.$$

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In general:

$$\begin{split} c_4^- &\sim \frac{1}{16\pi^2} \bigg\{ (\zeta_L^2 - \zeta_R^2) \log \left(\frac{\Lambda^2}{m_{3L} m_{3R}} \right) \\ &+ (\zeta_L^2 + \zeta_R^2) \log \frac{m_{3R}^2}{m_{3L}^2} + \frac{\zeta_L^2 m_{3L}^2 - \zeta_R^2 m_{3R}^2}{m_4^2} \bigg\} \end{split}$$



for $\zeta_L = \zeta_R = 1$ varying m_4, m_{3L}, m_{3R} between [2f, 10f]

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- Yet scenarios with O(1) enhancements in h→Zγ exist, and an experimental measurement would be important