

B physics and CP violation in the Standard Model and beyond

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coffee beans icon Introduction

coffee beans icon B physics and the Unitarity Triangle

coffee beans icon The Unitarity Triangle beyond the SM

coffee beans icon Minimal Flavour Violation

coffee beans icon Beyond MFV: general SUSY models

coffee beans icon Conclusions & Outlook

see www.utfit.org for
details & updates

INTRODUCTION

- In the SM, Yukawa couplings are the only source of flavour and CP violation in weak processes. Everything can be written in terms of quark masses and the CKM matrix.
- No tree-level FCNC (GIM mechanism)
 - ⇒ quantum corrections computable and sensitive to higher-dim operators ⇒ powerful probe of NP
- Flavour SU(3) strongly broken, 3rd generation has large coupling to EW breaking sector
 - ⇒ expect NP effects to show up in B physics

4 QUESTIONS FOR THIS TALK

- 1) How good is our knowledge of the SM UT?
- 2) How severe are the constraints on NP from the UT analysis?
- 3) What have we learned on the structure of NP from B physics and the UT?
- 4) Can we expect to learn more in the near future?

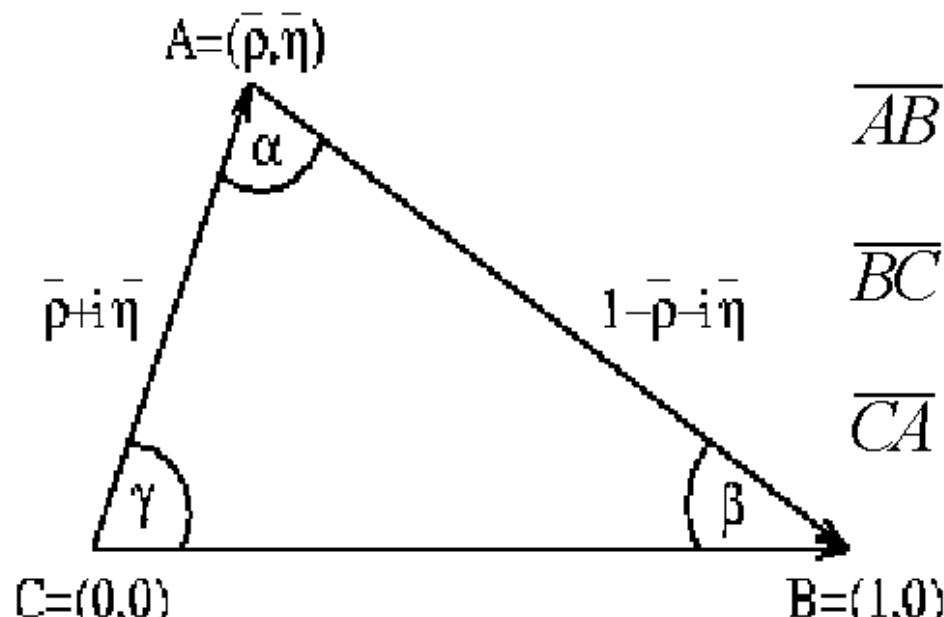
THE UNITARITY TRIANGLE

Wolfenstein-Buras
parameterization:

A useful unitarity relation:

$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

Defines a triangle in
terms of $\bar{\rho}$ and $\bar{\eta}$:
The Unitarity Triangle



$$\overline{AB} = \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*}$$

$$\overline{BC} = 1$$

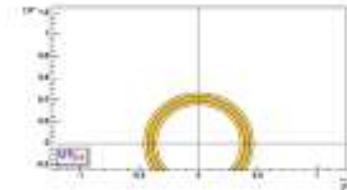
$$\overline{CA} = \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

B physics summarized on the UT

Most of B physics measurements can be translated on the UT:

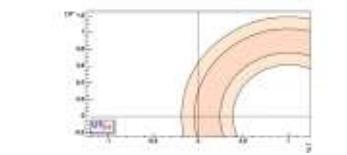
$\text{BR}(b \rightarrow c l \bar{\nu})$, $\text{BR}(B \rightarrow D^{(*)} l \bar{\nu})$

$$|V_{cb}|$$



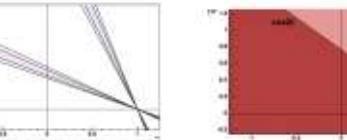
$\text{BR}(b \rightarrow u l \bar{\nu})$, $\text{BR}(B \rightarrow \pi l \bar{\nu})$

$$|V_{ub}|$$



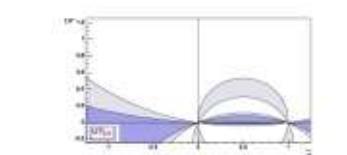
Δm_d ($B_d - \bar{B}_d$ mass diff.)

$$|V_{td}|^2$$



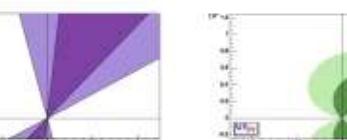
$A_{CP}(b \rightarrow c \bar{c} s)$ ($J/\psi K, \dots$)

$$\sin 2\beta, \cos 2\beta$$



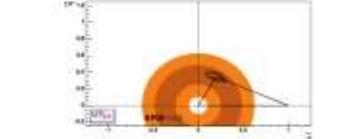
$A_{CP}(b \rightarrow s \bar{s} s, d \bar{d} s)$ ($\phi K, \pi K, \dots$)

$$\sin 2\beta$$



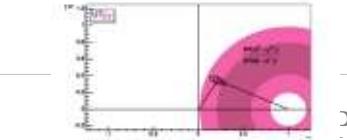
$A_{CP}(b \rightarrow d \bar{d} d, u \bar{u} d)$ ($\pi\pi, \rho\rho, \dots$)

$$\sin 2\alpha$$



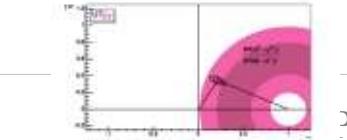
$\text{BR}(b \rightarrow c u d, c u s)$ ($D K, \dots$)

$$\gamma, \sin(2\beta + \gamma)$$



$\text{BR}(B \rightarrow \tau \nu)$

$$|V_{ub}|$$

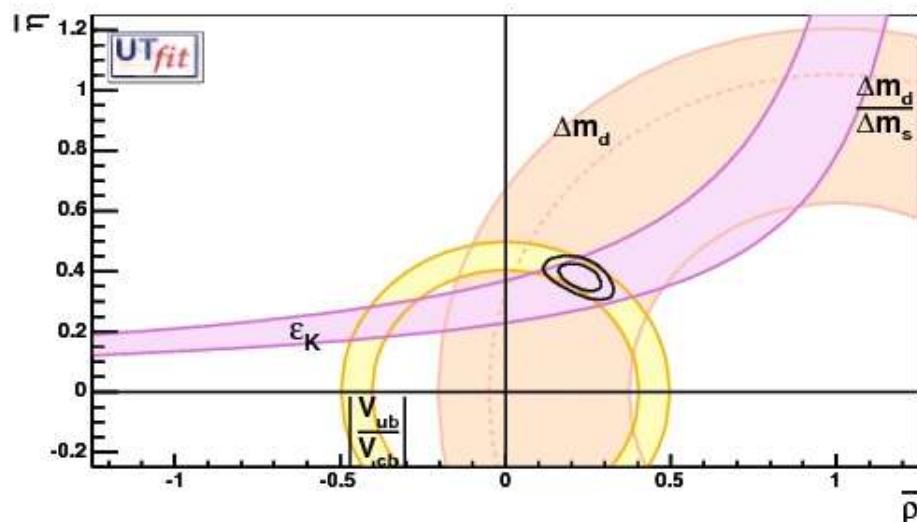


$\text{BR}(B \rightarrow \rho \gamma)/\text{BR}(B \rightarrow K^* \gamma)$

$$|V_{td}|$$

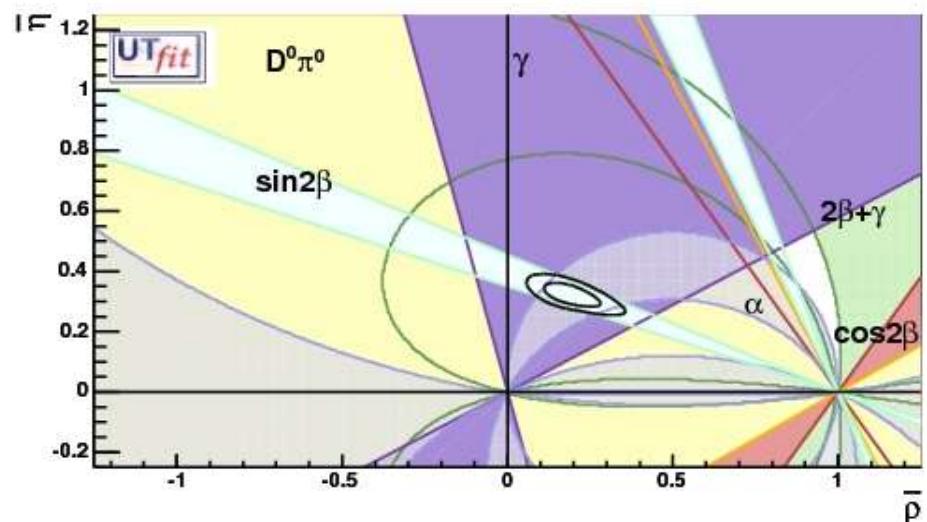
Progress of the UT analysis

End of parameter determination era, begin of precision test era:
redundant determination of the triangle with new measurements
from B-factories and test of new physics.



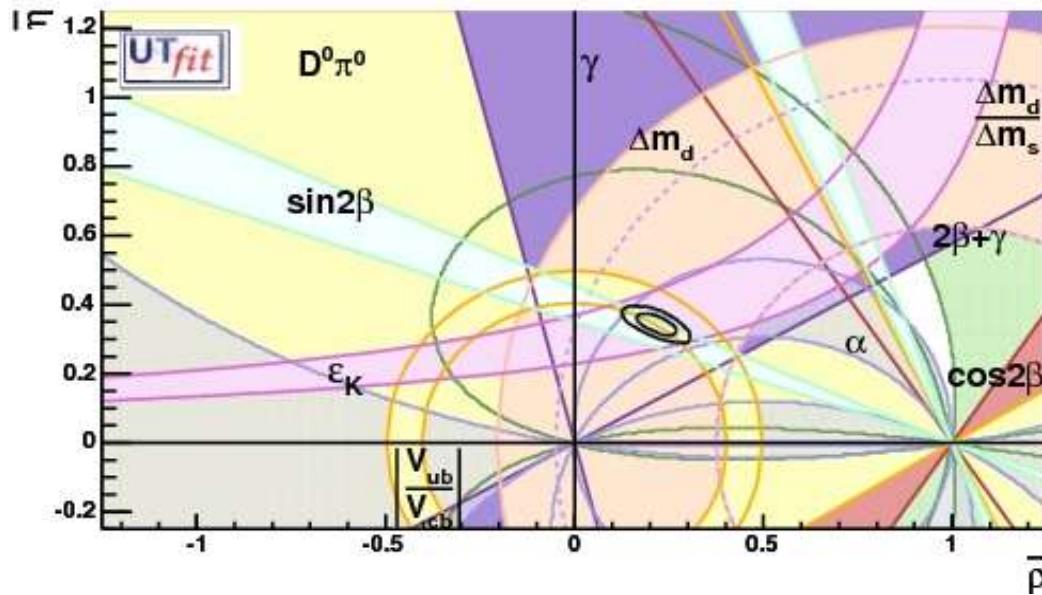
No angles:

$$|V_{ub}/V_{cb}|, \Delta m_d, \Delta M_s, \epsilon_K$$



Angles only: $\sin 2\beta, \cos 2\beta,$
 $\sin 2\alpha, \gamma$

ANSWER TO QUESTION 1) - THE SM UT

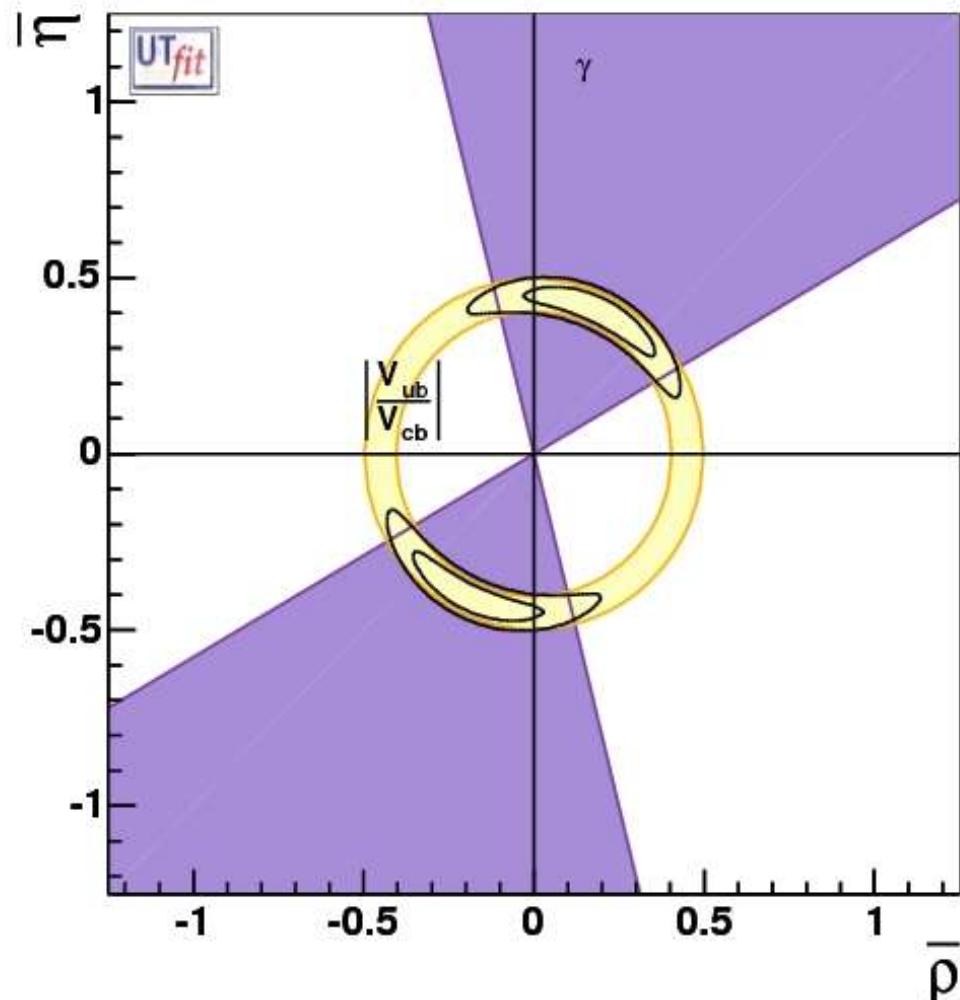


Slight disagreement
between V_{ub} and $\sin 2\beta$
after summer conferences

Parameter	value	95% prob.
ρ	0.216 ± 0.036	[0.143,0.288]
η	0.342 ± 0.022	[0.300,0.385]
$\alpha(^{\circ})$	98.5 ± 5.7	[87.1,109.8]
$\beta(^{\circ})$	23.8 ± 1.5	[21.3,26.2]
$\gamma(^{\circ})$	57.6 ± 5.5	[46.8,68.7]
$\sin 2\alpha$	-0.29 ± 0.19	[-0.64,0.09]
$\sin 2\beta$	0.735 ± 0.024	[0.688,0.781]
$\sin(2\beta+\gamma)$	0.959 ± 0.028	[0.890,0.996]
$\Delta(m_s)$ (ps^{-1})	20.0 ± 1.8	[15.5,24.2]

BEYOND THE SM I: THE REFERENCE UT

Assumptions: (1) 3-generations unitarity
(2) no new physics in tree-level processes



$$\bar{\rho} = \pm 0.18 \pm 0.12$$

$$\bar{\eta} = \pm 0.41 \pm 0.05$$

$$\begin{aligned} \sin 2\beta &= 0.782 \pm 0.065 \\ &\quad -0.641 \pm 0.087 \end{aligned}$$

$$\gamma = (65 \pm 18)^\circ \cup (-115 \pm 18)^\circ$$

$$\alpha = (87 \pm 15)^\circ \cup (-46 \pm 15)^\circ$$

Any model of new physics must satisfy these constraints

UTfit coll., hep-ph/0501199;
Botella et al., hep-ph/0502133

A more ambitious strategy:

1. Add most general NP to all sectors
2. Use all available info
3. Constrain simultaneously ρ , η and NP contributions

Botella et al., hep-ph/0502133;
Agashe et al., hep-ph/0509117;
UTfit coll., hep-ph/0509xxx.

Previous attempts:
Ciuchini et al., hep-ph/0307195;
CKMfitter group, hep-ph/0406184;
Ligeti, hep-ph/0408267.

Only possible thanks to the new measurements of CKM angles!!!
Will become the standard fit in the near future...

General parametrization of the mixing amplitudes

$$B_q - \bar{B}_q \text{ mixing: } A_{B_q} = C_q e^{2i\phi_q} A_{B_q}^{\text{SM}}$$

$$K - \bar{K} \text{ mixing: } \text{Im } A_K = C_\varepsilon \text{Im } A_K^{\text{SM}}$$

Soares, Wolfenstein PRD47;
 Deshpande,Dutta, Oh PRL77;
 Silva, Wolfenstein PRD55;
 Cohen et al. PRL78;
 Grossman, Nir, Worah PLB407;
 Ciuchini et al. @ CKM Durham

$$(\Delta M_q) = C_q (\Delta M_q)^{\text{SM}}$$

$$\varepsilon_K = C_\varepsilon \varepsilon_K^{\text{SM}}$$

$$A_{CP}(J/\Psi K_S) = \sin 2(\beta + \phi_d)$$

$$\alpha^{\text{exp}} = \alpha - \phi_d$$

$$A_{\text{SL}} \equiv \frac{\Gamma(\bar{B}^0 \rightarrow \ell^+ X) - \Gamma(B^0 \rightarrow \ell^- X)}{\Gamma(\bar{B}^0 \rightarrow \ell^+ X) + \Gamma(B^0 \rightarrow \ell^- X)}$$

$$A_{SL} = -\text{Re} \left(\frac{\Gamma_{12}}{M_{12}} \right)^{\text{SM}} \frac{\sin 2\phi_d}{C_d} + \text{Im} \left(\frac{\Gamma_{12}}{M_{12}} \right)^{\text{SM}} \frac{\cos 2\phi_d}{C_d}$$

Laplace et al., PRD65

	ρ, η	C_d	ϕ_d	C_s	ϕ_s	C_ε	NP in $\Delta F=1$
γ	X						
$ V_{ub}/V_{cb} $	X						
ΔM_d	X	X					
ΔM_s	(X)			X			
ϵ_K	X					X	
$A_{CP}(B \rightarrow J/\Psi K_s)$	X		X				
$A_{CP}(B \rightarrow J/\Psi K^*)$	X		X				
$\alpha (\rho\rho, \rho\pi, \pi\pi)$	X		X				X
A_{SL}	X	X	X				X
$A_{CP}(B_s \rightarrow J/\Psi \Phi)$	(X)				X		

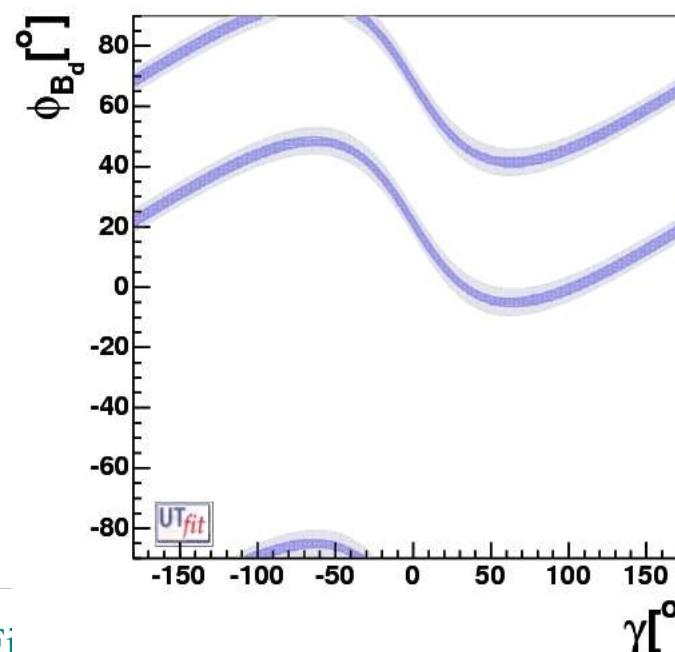
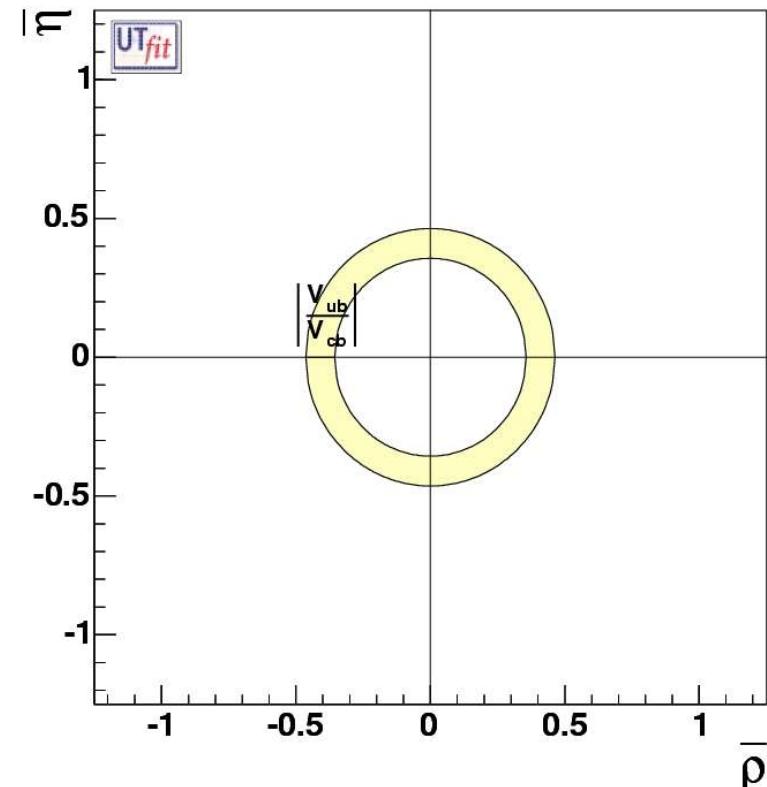
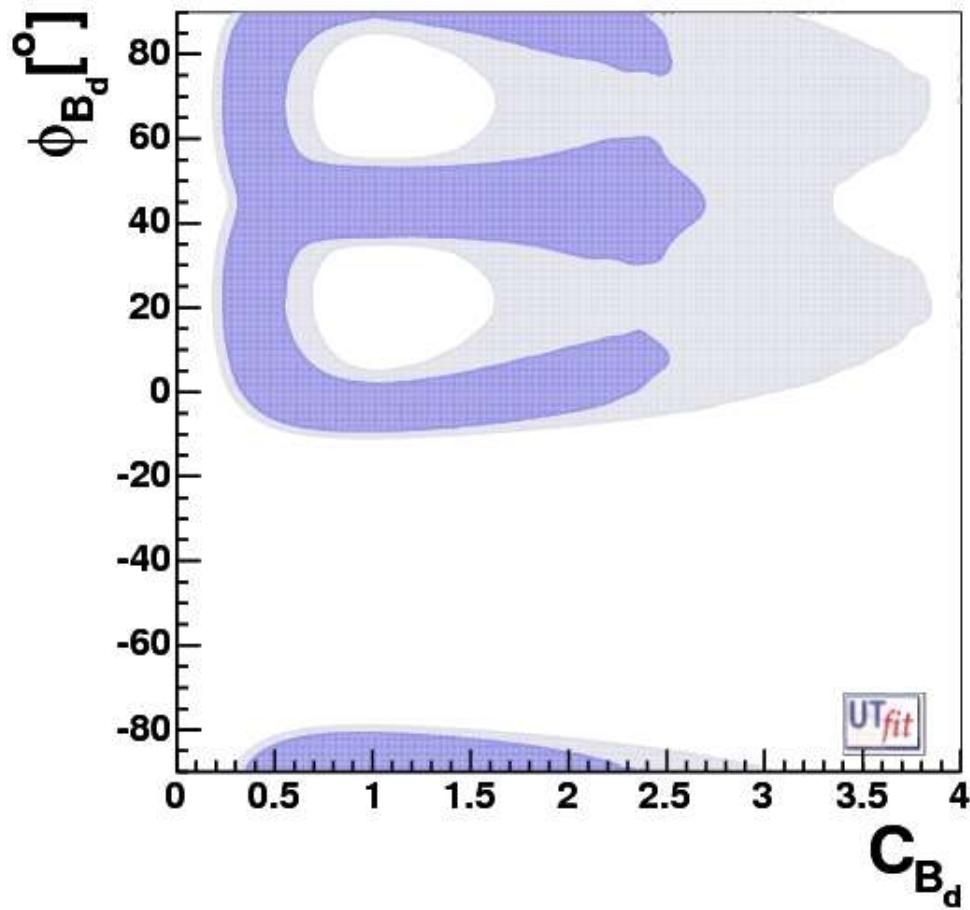
(3) assume NP in $b \rightarrow d$ decays is $SU(2)$ invariant

Use: $|V_{ub}/V_{cb}|$, γ , ΔM_d , ΔM_s , α , $\sin 2\beta$, $\cos 2\beta$ and A_{SL}

constrain simultaneously $\rho, \eta, C_d, \phi_d, C_s$ and C_ε
 (no handle at present on ϕ_s - wait for LHCb)

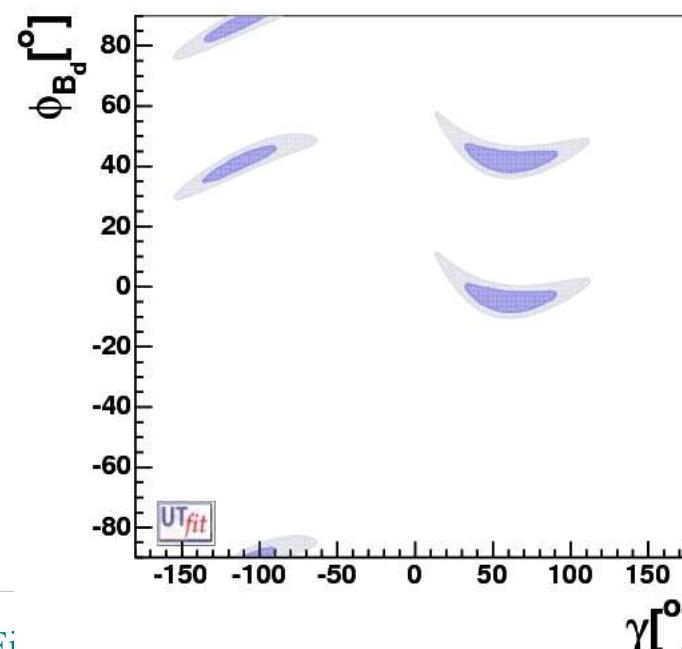
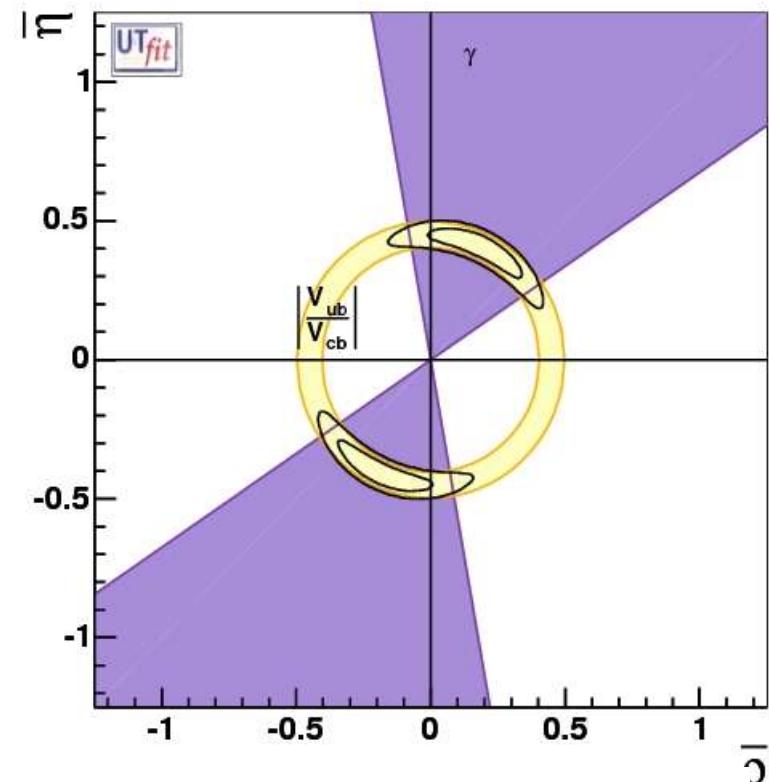
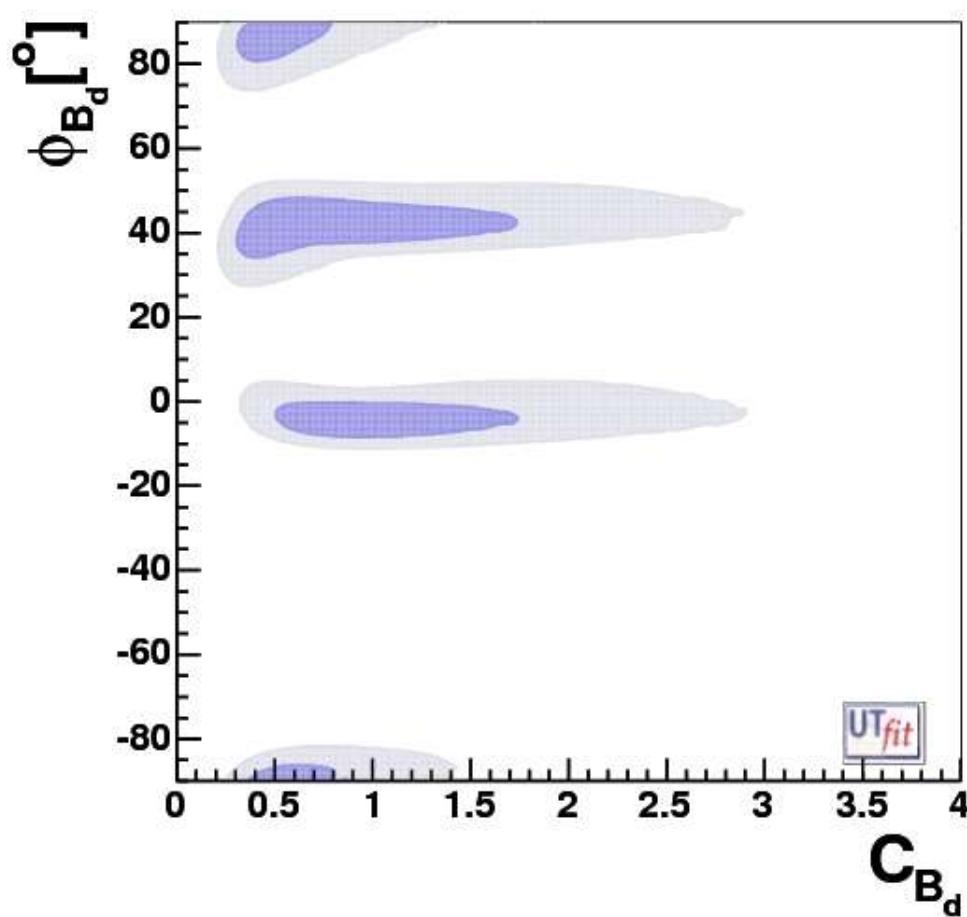
Using:

- $\varepsilon, \Delta m_d, \sin 2\beta$



Using:

- $\varepsilon, \Delta m_d, \sin 2\beta$
- γ



4 solutions for ρ , η , C_d and ϕ_d :

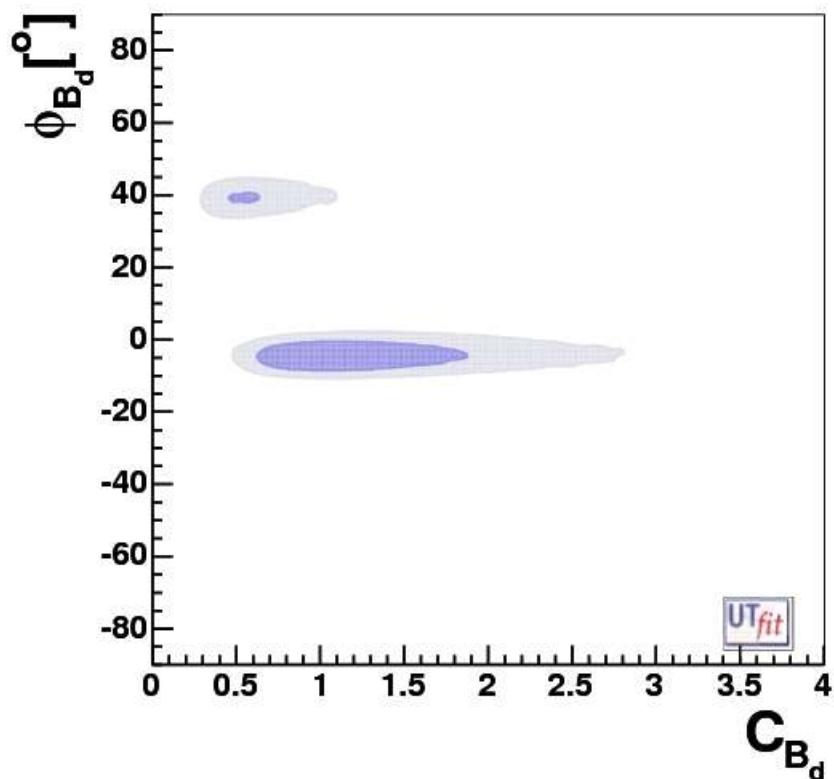
	γ	C_d	ϕ_d	$\cos 2(\beta + \phi_d)$	$\sin 2(\alpha - \phi_d)$	$\sin(2(\beta + \phi_d) + \gamma)$	A_{SL}
SM-LIKE	60°	1	0°	0,68	-0,23	0,96	OK
NP 1	60°	1	43°	-0,68	0,96	-0,23	OK
NP 2	120°	0,4	40°	0,68	-0,23	-0,96	$O(10^{-2})$
NP 3	120°	0,4	83°	-0,68	0,96	0,23	OK

NP 1 & 3 solutions can be eliminated using angle measurements (α most effective at present)

NP 2 solution can be suppressed using $A_{SL} = (-3 \pm 7) \cdot 10^{-3}$
⇒ the SM-like solution is strongly favoured!

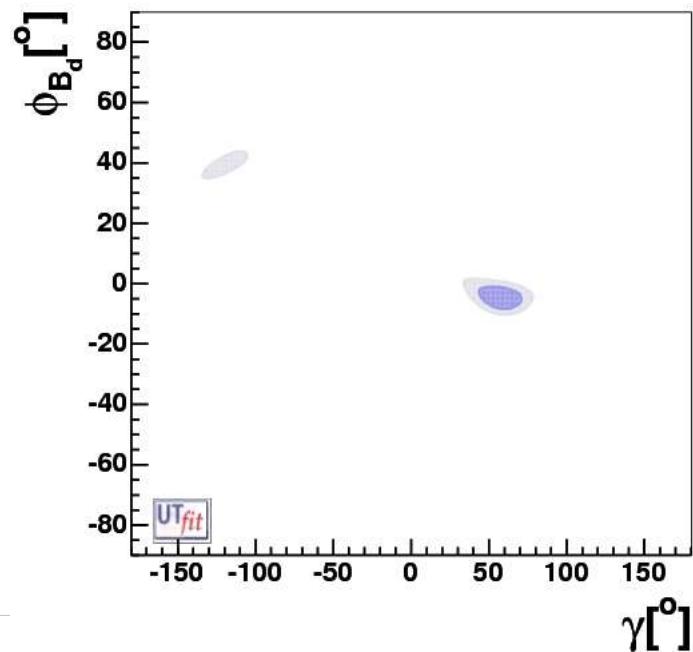
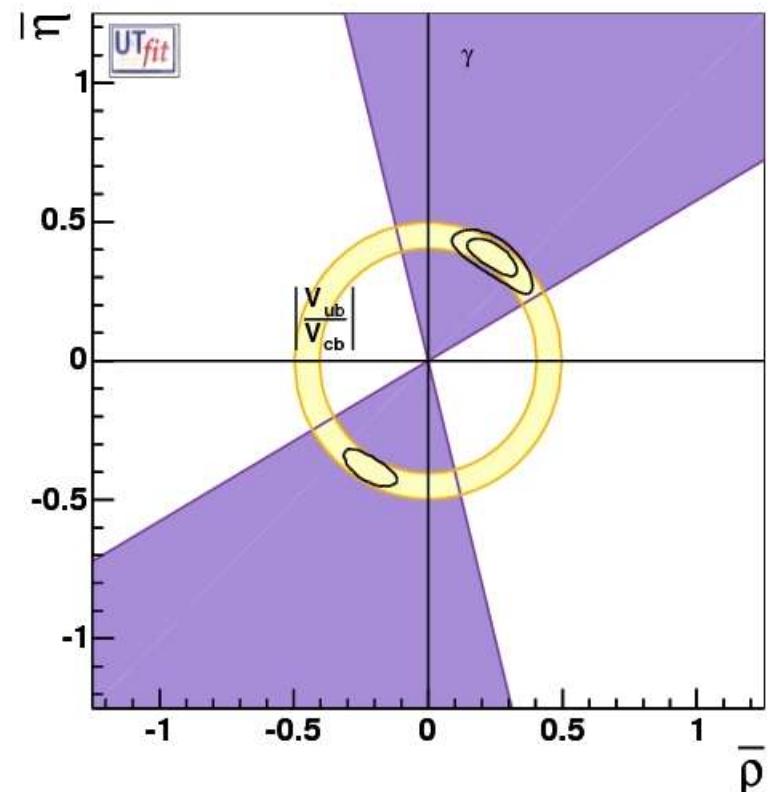
Using:

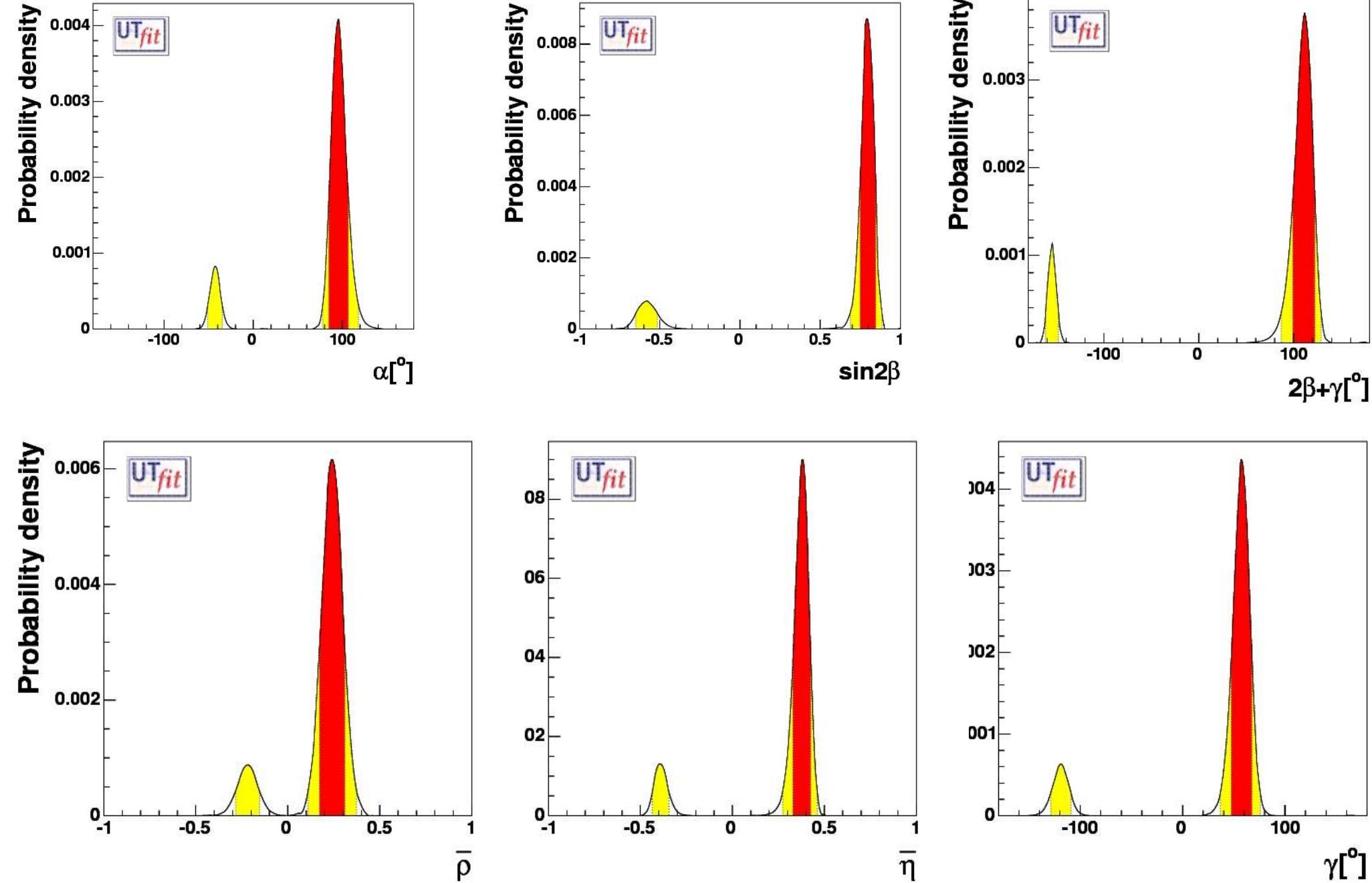
- $\varepsilon, \Delta m_d, \sin 2\beta$
- γ
- $\alpha, \cos 2\beta$ & A_{SL}



SM solution @ 88% prob.

NP solution @ 12% prob.



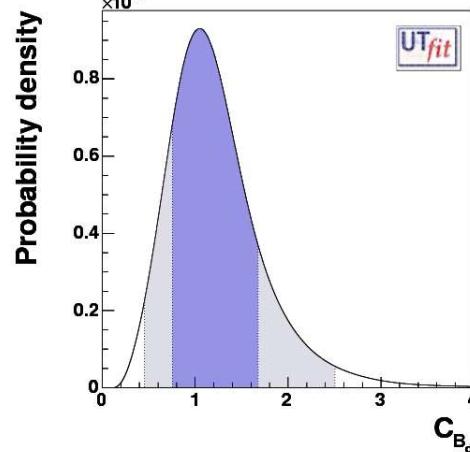


Question 2) - How large is the NP contribution?

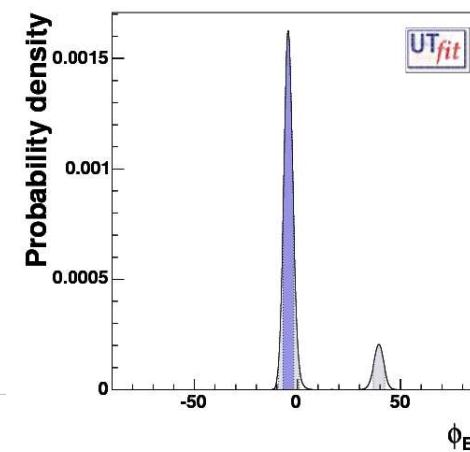
Define

$$C_{B_d} e^{2i\phi_{B_d}} = \frac{A_{\text{SM}} e^{2i\beta} + A_{\text{NP}} e^{2i(\beta+\phi_{\text{NP}})}}{A_{\text{SM}} e^{2i\beta}}$$

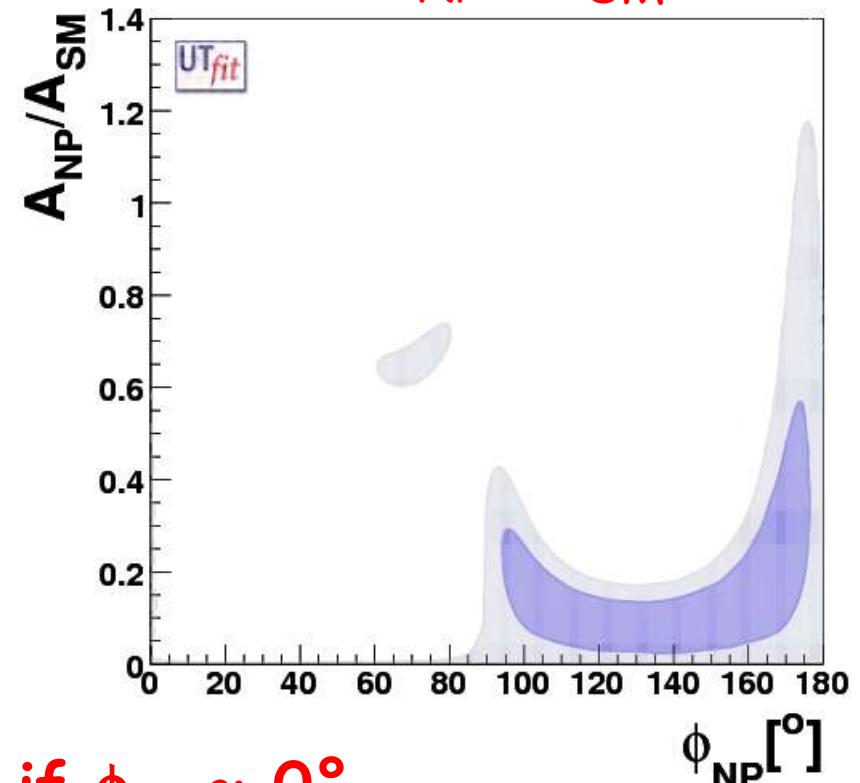
The UT analysis strongly constrains $A_{\text{NP}}/A_{\text{SM}}$:



$$C_{B_d} = 1.21 \pm 0.46$$



$$\phi_{B_d} = (-4.5 \pm 2.6)^\circ$$



$A_{\text{NP}}/A_{\text{SM}} \sim 1$ only if $\phi_{\text{NP}} \sim 0^\circ$,
otherwise $A_{\text{NP}}/A_{\text{SM}} \sim 0\text{-}20\%$ @ 95% prob.

QUESTION 3) - WHAT HAVE WE LEARNED ON NP?

- ▶ New sources of CPV in $s \rightarrow d$ and/or $b \rightarrow d$ transitions are:
 - strongly constrained by the UT fit
 - “unnecessary”, given the great success of the fit
- ▶ New sources of CPV in $b \rightarrow s$ transitions are
 - much less (un-) constrained by the UT fit
 - Possibly constrained by rare decays & $b \rightarrow s$ penguins (model-dependent)

QUESTION 3) - CONTINUED

Two classes of NP models still allowed by data:

1. Models with no new source of flavour & CP violation (**Minimal Flavour Violation**)

2. Models with new sources of CPV in $b \rightarrow s$ transitions

- natural in many flavour models, given the strong breaking of family SU(3)

Pomarol, Tommasini; Barbieri, Dvali, Hall; Barbieri, Hall; Barbieri, Hall, Romanino; Berezhiani, Rossi; Masiero et al; ...

- hinted at by v's in SUSY-GUTs

Baek et al.; Moroi; Akama et al.; Chang, Masiero, Murayama; Hisano, Shimizu; Goto et al.; ...

MINIMAL FLAVOUR VIOLATION

Gabrielli, Giudice, NPB433; Buras et al., PLB500;
D'Ambrosio et al., NPB 645; Bobeth et al., hep-ph/0505110

1) No new source of flavour and CP violation

NP contributions also governed by Yukawas

NP only modifies SM top contribution to FCNC & CPV

2a) One Higgs or small/moderate $\tan\beta$

No new operators, full correlations among K & B decays

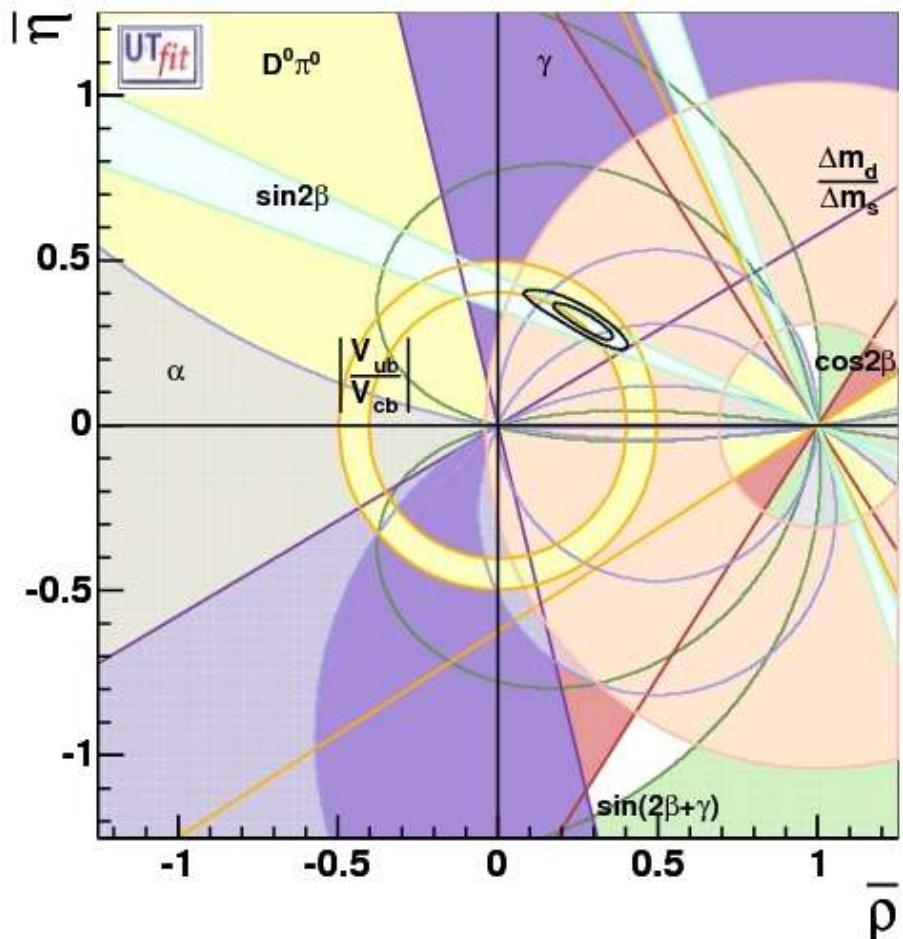
2b) Large $\tan\beta$

New operators, less correlations among K & B decays

The Universal Unitarity Triangle

Buras et al., PLB500

Angle measurements + $\Delta M_d / \Delta M_s$ unaffected by NP in MFV



$\bar{\rho}$	0.258 ± 0.066	[0.107, 0.373]
$\bar{\eta}$	0.319 ± 0.039	[0.249, 0.398]
$\sin 2\beta$	0.726 ± 0.028	[0.668, 0.778]
$\alpha [^\circ]$	105 ± 11	[81, 123]
$\gamma [^\circ]$	51 ± 10	[34, 74]
$(2\beta + \gamma) [^\circ]$	98 ± 12	[78, 122]

valid in any MFV model
for any value of $\tan\beta$

UTfit Coll., hep-ph/0509xxx

UUT starting point for MFV studies of rare decays

Bobeth, Bona, Buras, Ewerth, Pierini, L.S., Weiler, hep-ph/0505110

Identify leading NP contributions:

1) dimension 4 operators: FCNC effective Z vertex

$$\Rightarrow C = C_{SM} + \Delta C$$

2) dimension 5 operators: (chromo)magnetic penguin

$$\Rightarrow C_7^{\text{eff}} = (C_7^{\text{eff}})_{SM} + \Delta C_7^{\text{eff}}$$

3) dimension 6 operators: penguins, boxes

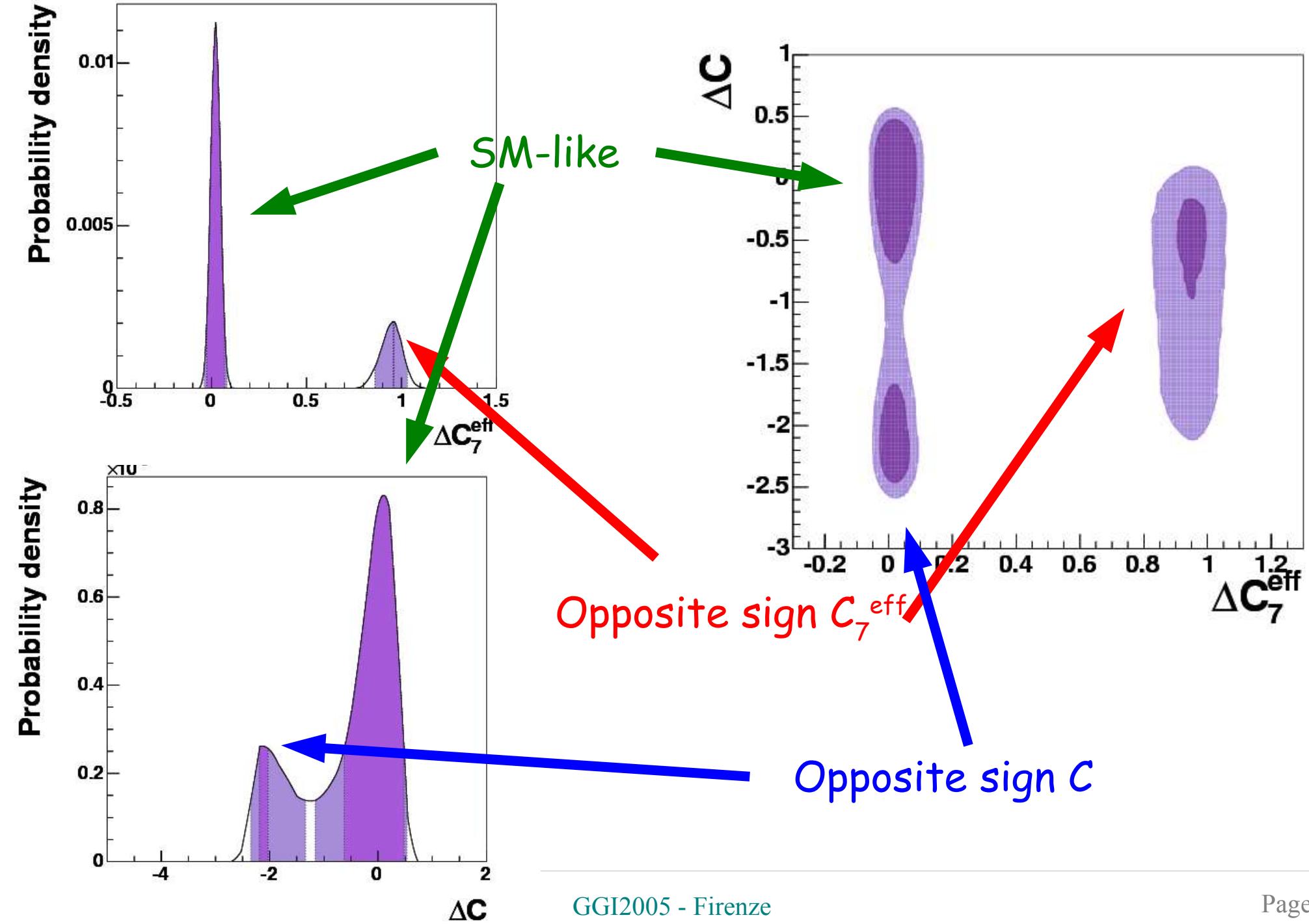
\Rightarrow subleading NP contributions to rare decays

Rare decays \Leftrightarrow SM functions + $\Delta C, \Delta C_7^{\text{eff}}$

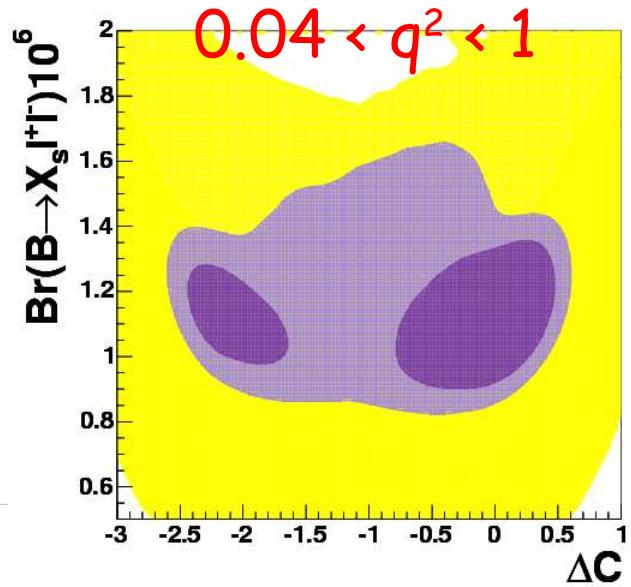
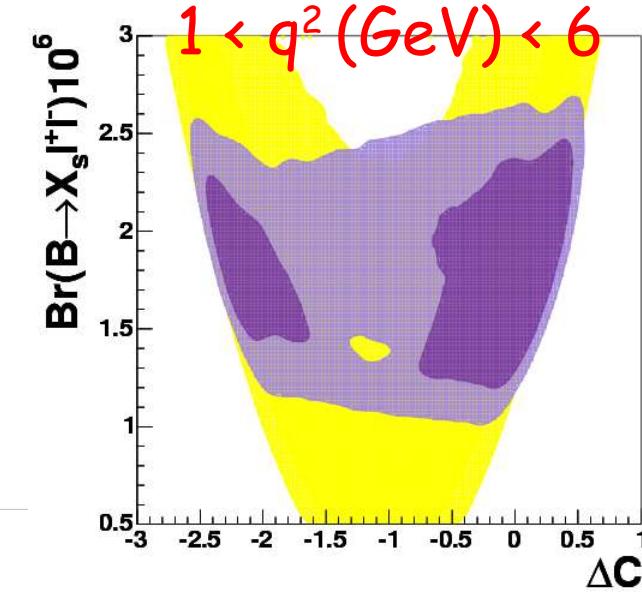
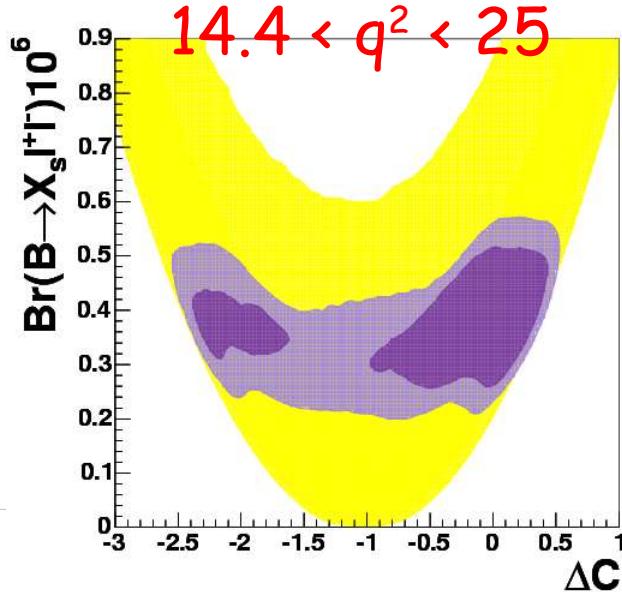
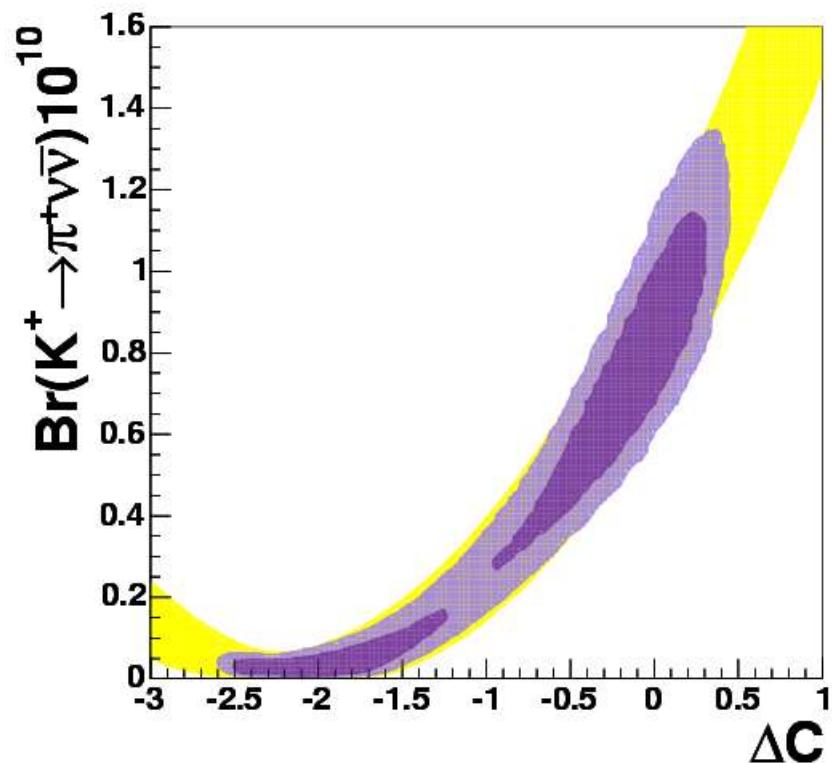
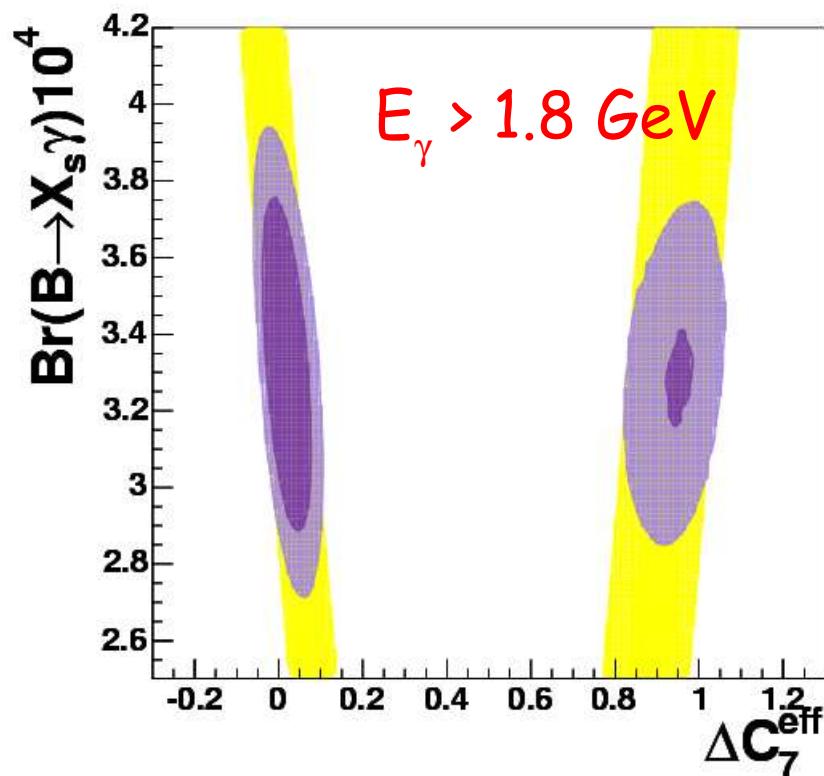
RARE DECAYS IN MFV

- ρ, η from the UUT analysis
- ΔC_7^{eff} can be constrained using $\text{BR}(B \rightarrow X_s \gamma)$
- ΔC can be constrained using $\text{BR}(B \rightarrow X_s l^+ l^-)$ and $\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$
- Get predictions for all other rare decays

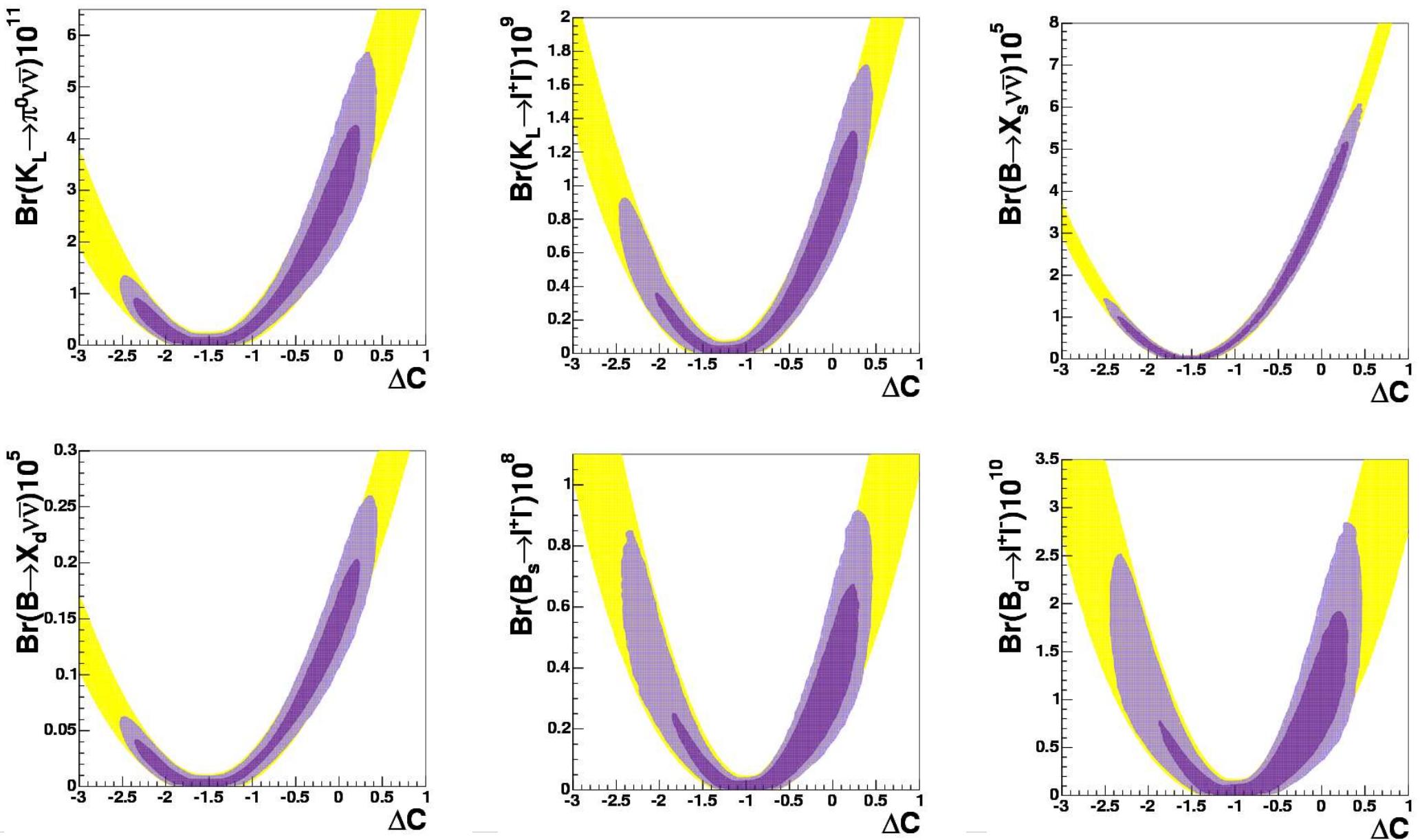
CONSTRAINTS ON NP



NP CONTRIBUTIONS vs EXP CONSTRAINTS



ANSWER TO QUESTION 4) - PREDICTIONS FOR RARE DECAYS

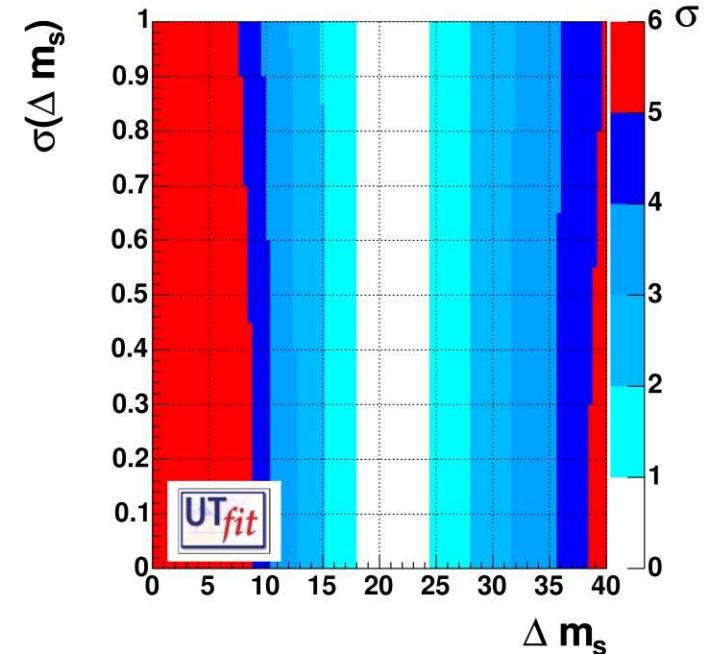
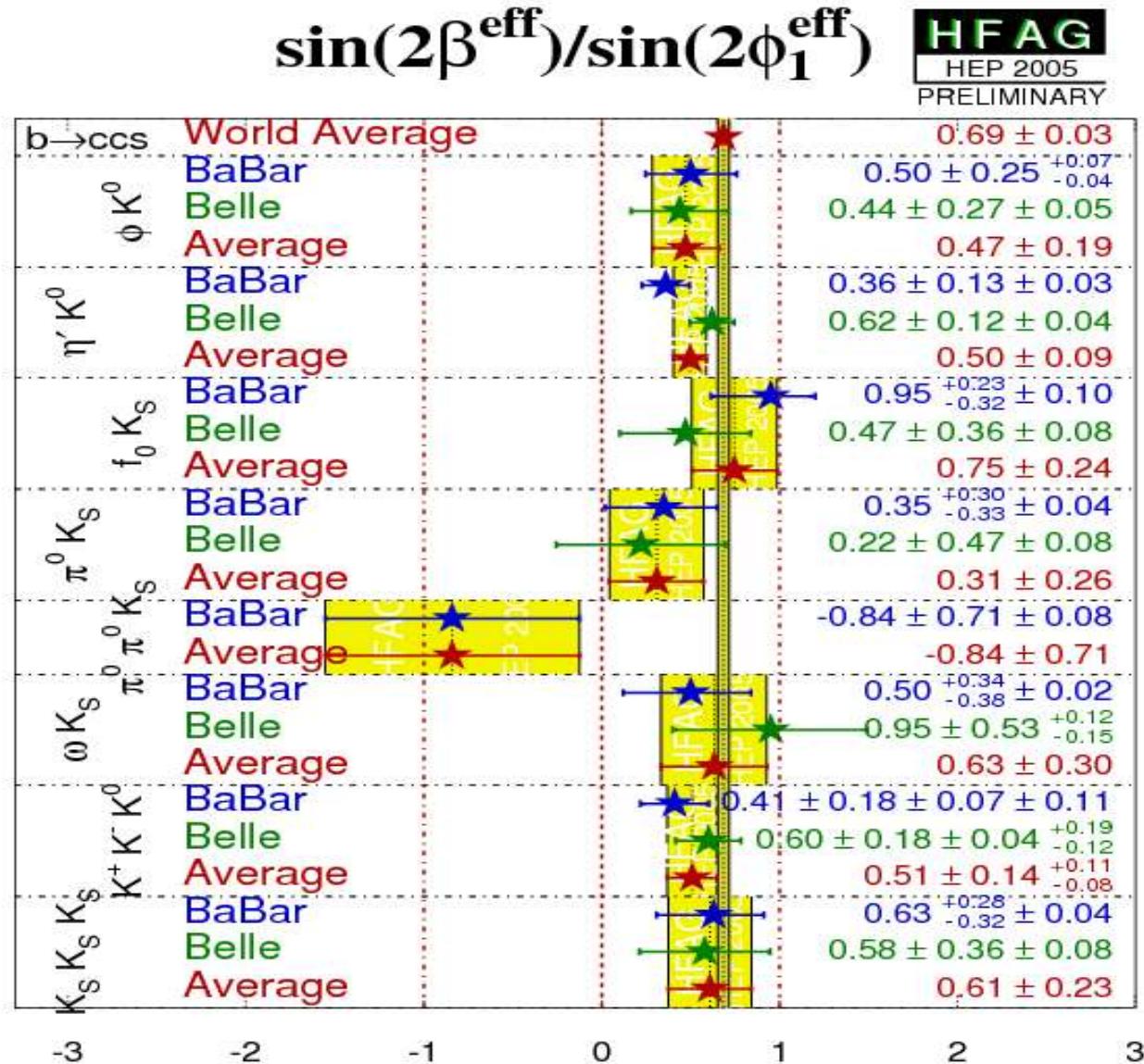


UPPER BOUNDS ON RARE DECAYS:

Branching Ratios	MFV (95%)	SM (68%)	SM (95%)	exp
$Br(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \times 10^{11}$	< 11.9	8.3 ± 1.2	$[6.1, 10.9]$	$(14.7_{-8.9}^{+13.0})$ [19]
$Br(K_L \rightarrow \pi^0 \nu \bar{\nu}) \times 10^{11}$	< 4.59	3.08 ± 0.56	$[2.03, 4.26]$	$< 5.9 \cdot 10^4$ [37]
$Br(K_L \rightarrow \mu^+ \mu^-)_{\text{SD}} \times 10^9$	< 1.36	0.87 ± 0.13	$[0.63, 1.15]$	-
$Br(B \rightarrow X_s \nu \bar{\nu}) \times 10^5$	< 5.17	3.66 ± 0.21	$[3.25, 4.09]$	< 64 [38]
$Br(B \rightarrow X_d \nu \bar{\nu}) \times 10^6$	< 2.17	1.50 ± 0.19	$[1.12, 1.91]$	-
$Br(B_s \rightarrow \mu^+ \mu^-) \times 10^9$	< 7.42	3.67 ± 1.01	$[1.91, 5.91]$	$< 2.7 \cdot 10^2$ [39]
$Br(B_d \rightarrow \mu^+ \mu^-) \times 10^{10}$	< 2.20	1.04 ± 0.34	$[0.47, 1.81]$	$< 1.5 \cdot 10^3$ [39]

In MFV models (at low/moderate $\tan \beta$) rare decays can be only slightly enhanced w.r.t the SM. Strong suppressions still possible at present.

The last resort: NP in $b \rightarrow s$ modes



$\Delta m_s > 31(38) \text{ ps}^{-1}$
 is new physics @ $3(5)\sigma$

The SUSY option

Bertolini, Borzumati, Masiero, NPB294; Ciuchini et al., PRL79; Barbieri, Strumia, NPB508; Kagan, Neubert, PRD58; Abel, Cottingham, Wittingham PRD58; Borzumati et al., PRD62; Besmer, Greub, Hurth NPB609; Lunghi, Wyler, PLB521; Causse; Hiller, PRD66; Khalil, Kou PRD67; Kane et al., PRL90; Harnik et al.; Ciuchini et al., PRD67; Baek, PRD67; Hisano, Shimizu, PLB581; Gabrielli et al., NPB710; Khalil, hep-ph/0505151;...

- Well-motivated extension of the SM
- SUSY flavour models, SUSY-GUTS & neutrino oscillations point towards possibly large b-s mixing in the squark sector

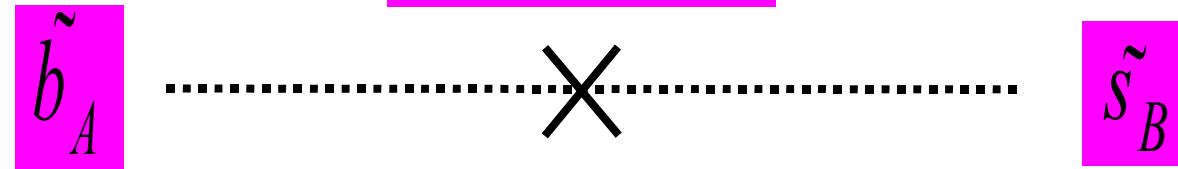
A Model-Independent Analysis

Ciuchini et al., in progress - Preliminary!!

- We consider a MSSM with generic soft SUSY-breaking terms, but
 - dominant gluino contributions only
 - mass insertion approximation

$$\left(\delta^d_{23}\right)_{AB}$$

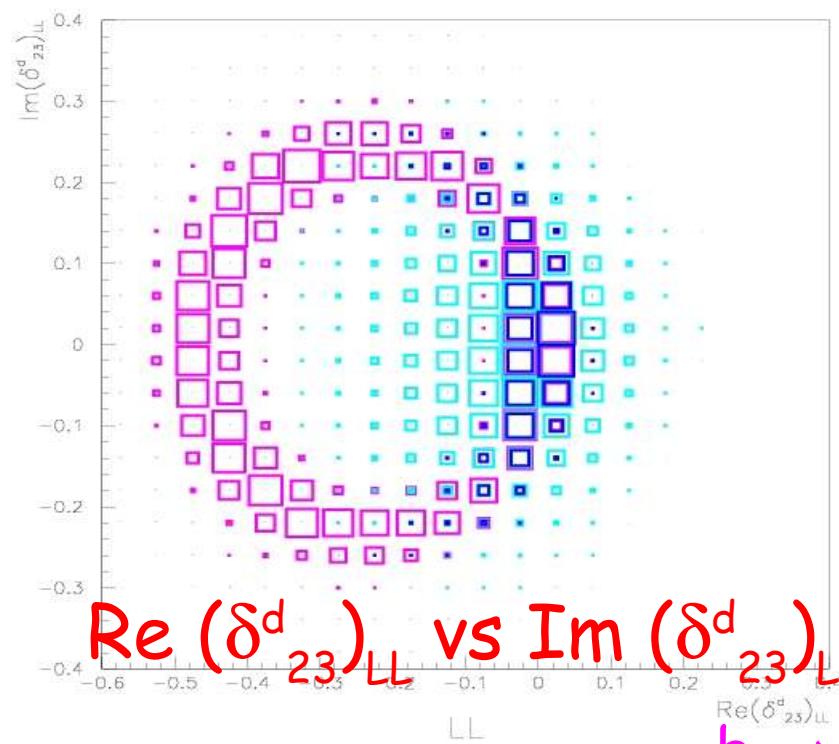
Think of δ 's as SUSY equivalent of CKM mixing



four insertions AB=LL, LR, RL, RR

CONSTRAINTS ON δ 's

- gluinos contribute to rare decays only through (chromo)magnetic penguins - (electro)penguin operators suppressed
Bertolini et al., NPB353; Gabbiani et al., NPB477; Buras, Romanino, L.S., NPB520
- very strong constraints from combination of $b \rightarrow s \gamma$ and $b \rightarrow s l^+ l^-$ (both dominated by C_7^{eff})
Ciuchini et al, PRD67; Hiller, PRD69; Gambino, Haisch, Misiak, PRL94
- Use $m_{gl} = m_{sq} = -\mu = 350 \text{ GeV}$, $\tan \beta = 10$

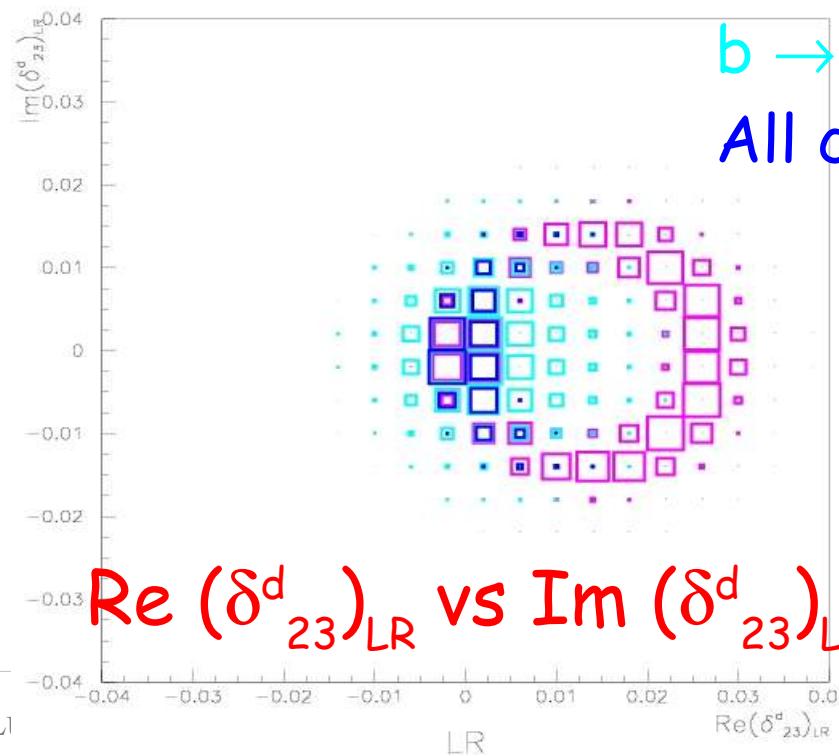


$\text{Re}(\delta_{23}^d)_{\text{LL}} \text{ vs } \text{Im}(\delta_{23}^d)_{\text{LL}}$

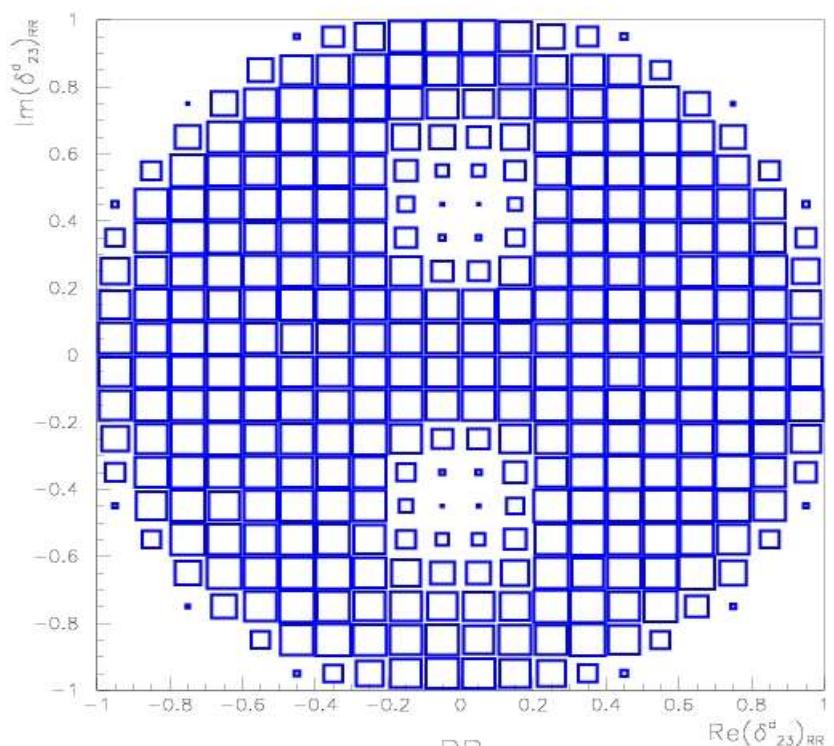
$b \rightarrow s \gamma \text{ only}$

$b \rightarrow s \parallel \text{ only}$

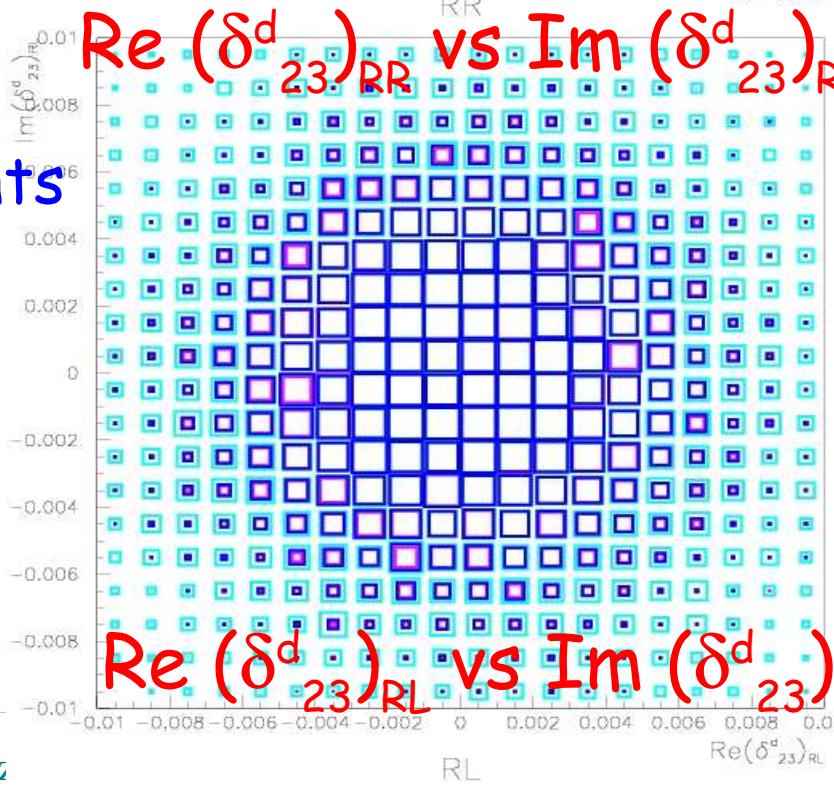
All constraints



$\text{Re}(\delta_{23}^d)_{\text{LR}} \text{ vs } \text{Im}(\delta_{23}^d)_{\text{LR}}$



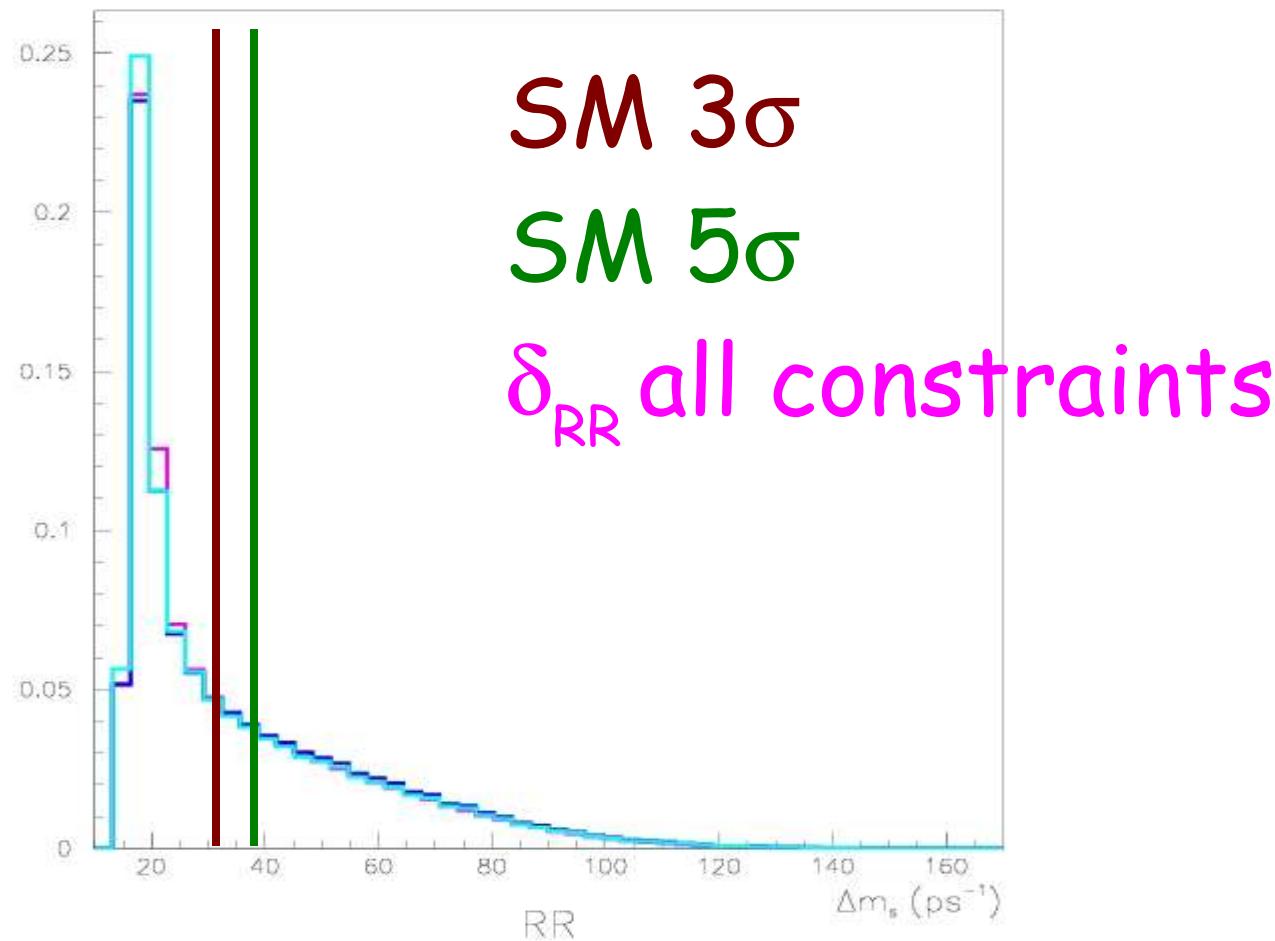
$\text{Re}(\delta_{23}^d)_{\text{RR}} \text{ vs } \text{Im}(\delta_{23}^d)_{\text{RR}}$



$\text{Re}(\delta_{23}^d)_{\text{RL}} \text{ vs } \text{Im}(\delta_{23}^d)_{\text{RL}}$

ANSWER TO QUESTION 4) - THE ΔM_s EXAMPLE

ΔM_s :

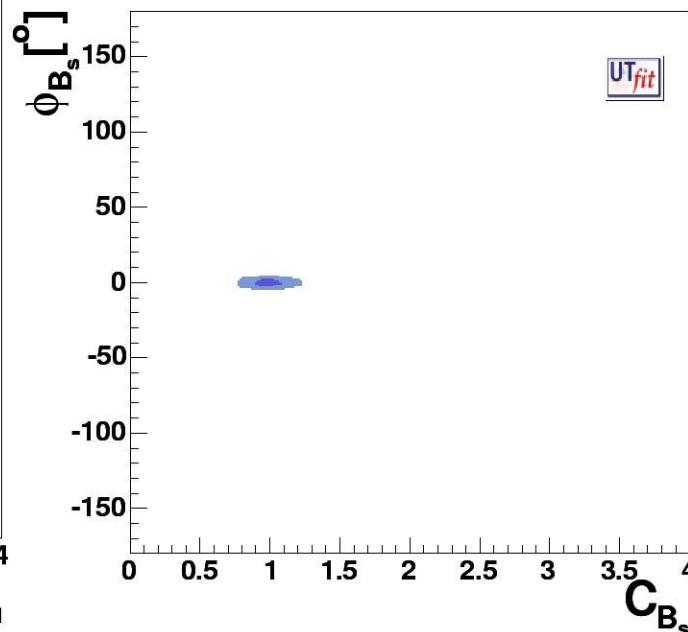
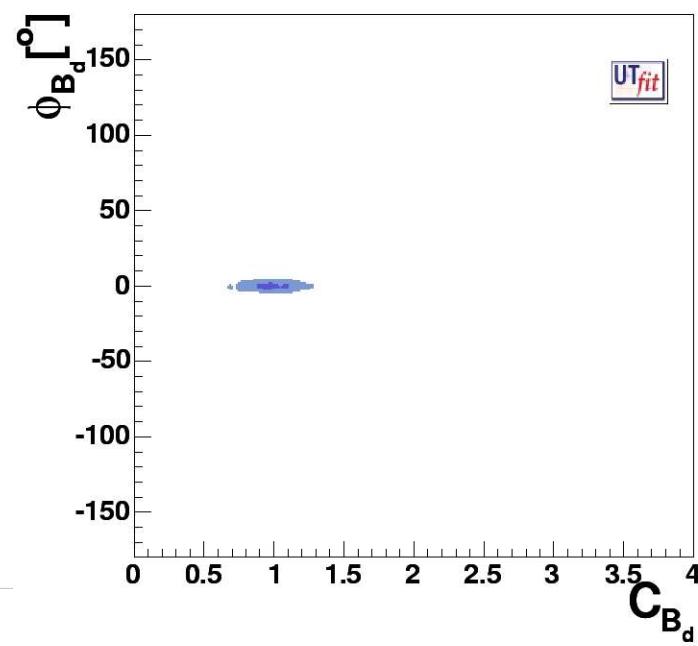
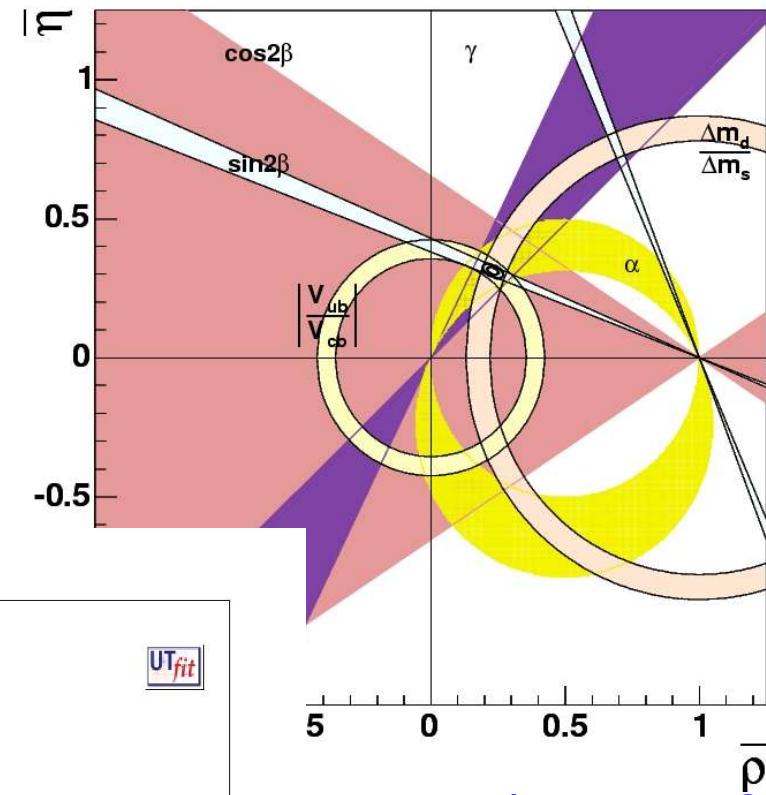
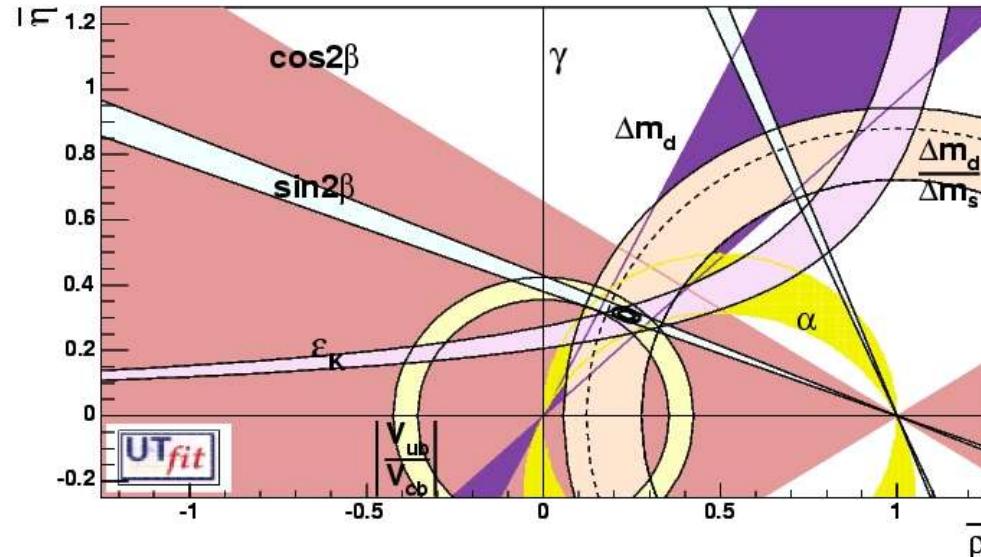


Large values of ΔM_s possible for RR
(and LL @ low $\tan \beta$), with large values
of mixing phase \Leftrightarrow CPV in $B_s \rightarrow \psi\phi, D_s^+D_s^-$

Conclusions

- The SM is (surprisingly enough) extremely successful in reproducing all available data
- Thanks to the recent progress, NP in $\Delta B=2$ and $\Delta S=2$ transitions is strongly constrained, pointing towards MFV
- Surprises (from SUSY) still possible in $b \rightarrow s$ transitions, though rare decays are getting tighter and tighter
- Hadron colliders will tell us whether SM, MFV or New Flavour & CPV in $b \rightarrow s \dots$

OUTLOOK: 2010



Or, hopefully,
something
different...

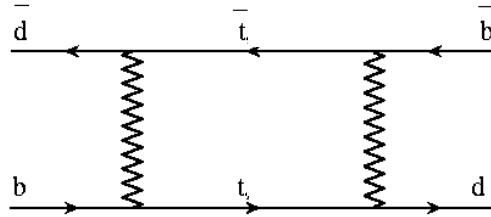
BACKUP SLIDES

MFV: an effective theory approach

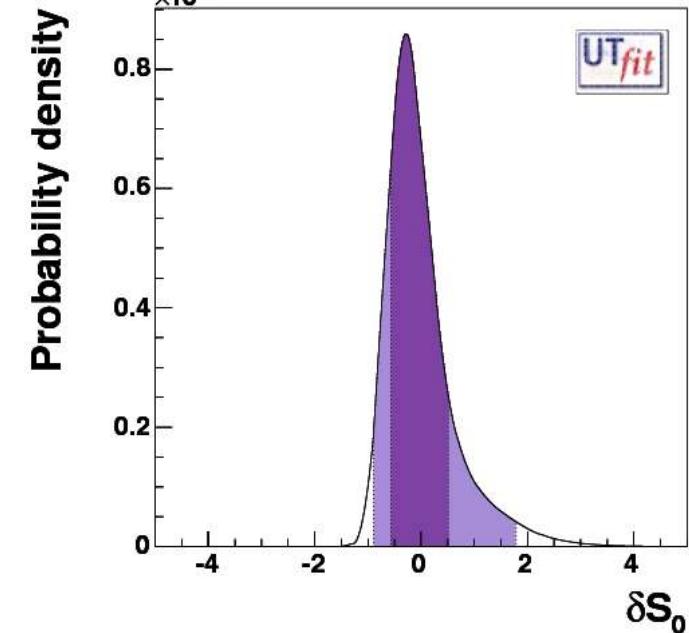
D'Ambrosio et al., hep-ph/0207036

- ▶ classification of the dim-6 operators built with the SM fields and 1 or 2 Higgs doublets under the assumption that the flavour violation dynamics is determined by ordinary Yukawa couplings

1H: Universal NP effect in the $\Delta F=2$ Inami-lim function of the top



$$S_0(x_t) \rightarrow S_0(x_t) + \delta S_0, \quad |\delta S_0| = O\left(4 \frac{\Lambda_0^2}{\Lambda^2}\right), \quad \Lambda_0 \sim 2.4 \text{ TeV}$$



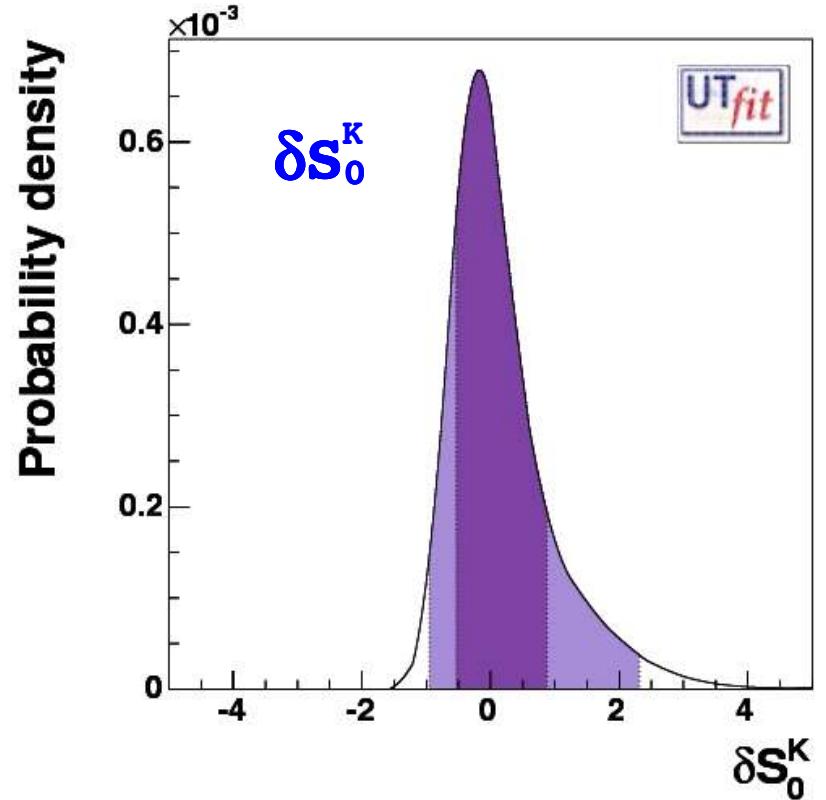
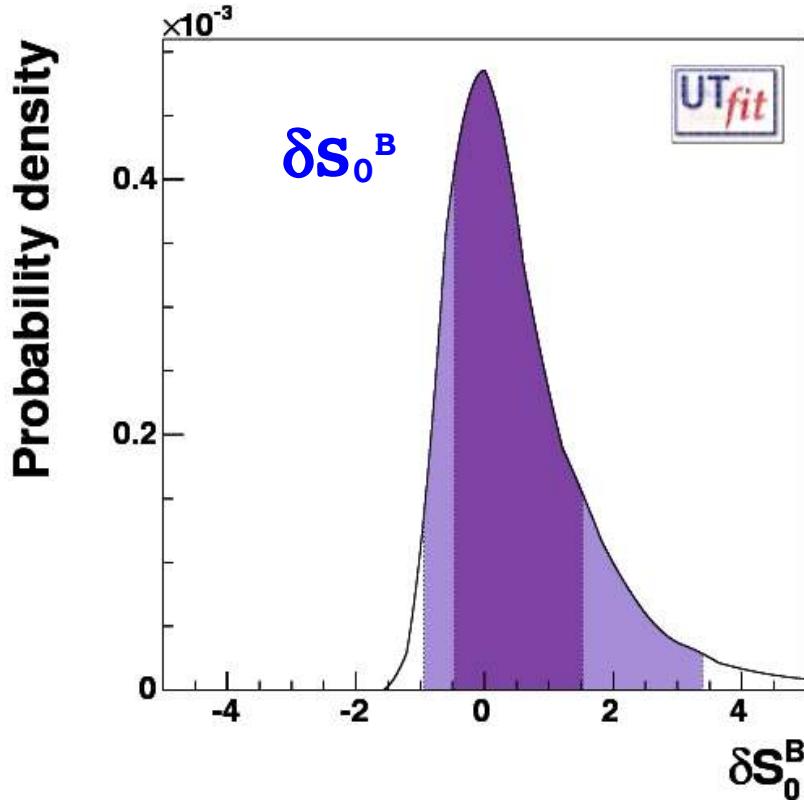
We can bound the NP scale Λ :

$\Lambda > 5.1 \text{ TeV} @ 95\% \text{ prob. for positive } \delta S_0$

$\Lambda > 3.6 \text{ TeV} @ 95\% \text{ prob. for negative } \delta S_0$

2H + large $\tan\beta$: terms proportional to the bottom Yukawa coupling are enhanced and cannot be neglected any more

$$\delta S_0^B \neq \delta S_0^K$$

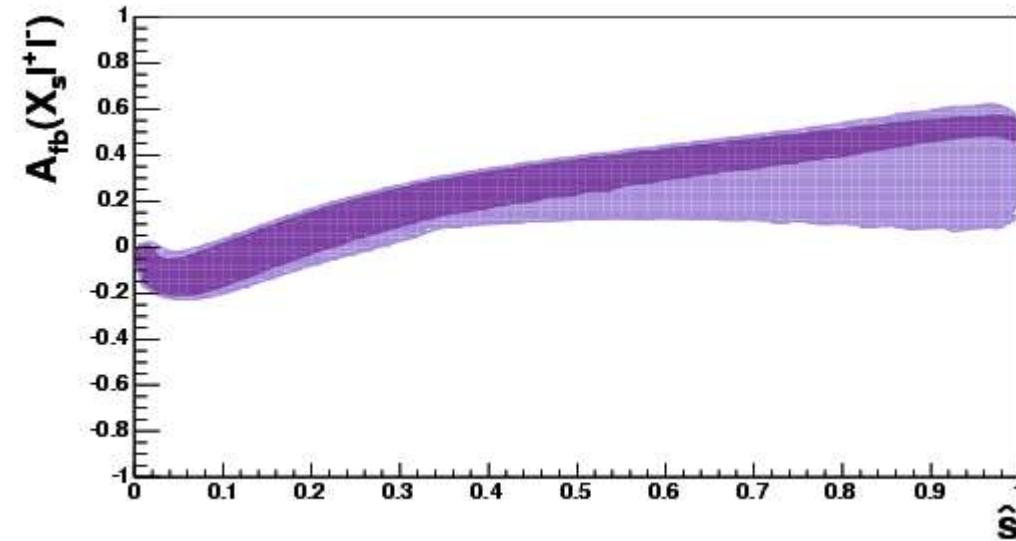


$\Lambda > 2.6 \text{ TeV} @ 95\% \text{ prob. for } \delta S_0 > 0$
 $\Lambda > 4.9 \text{ TeV} @ 95\% \text{ prob. for } \delta S_0 < 0$

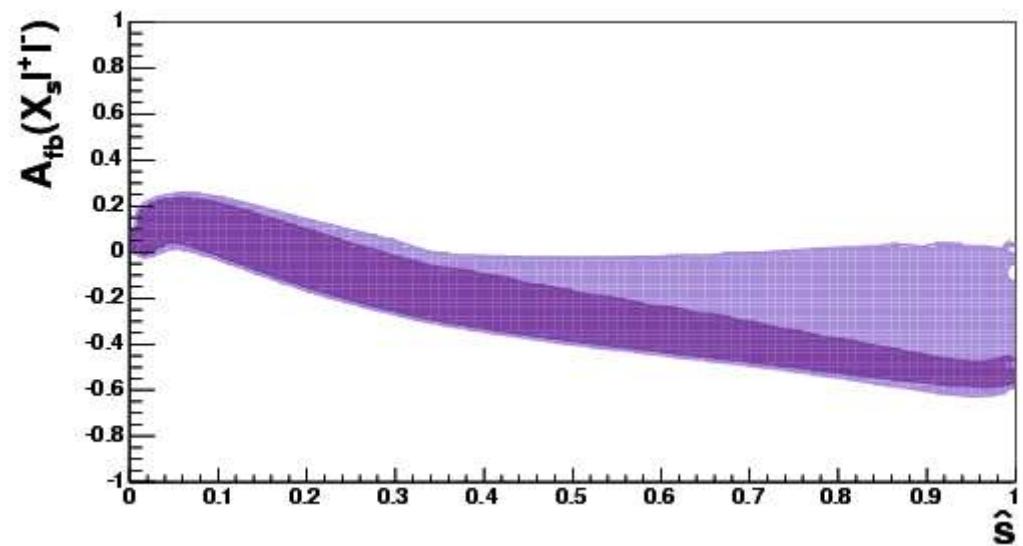
$\Lambda > 3.2 \text{ TeV} @ 95\% \text{ prob. for } \delta S_0 > 0$
 $\Lambda > 4.9 \text{ TeV} @ 95\% \text{ prob. for } \delta S_0 < 0$

FORWARD-BACKWARD ASYMMETRY IN $B \rightarrow X_s l^+ l^-$

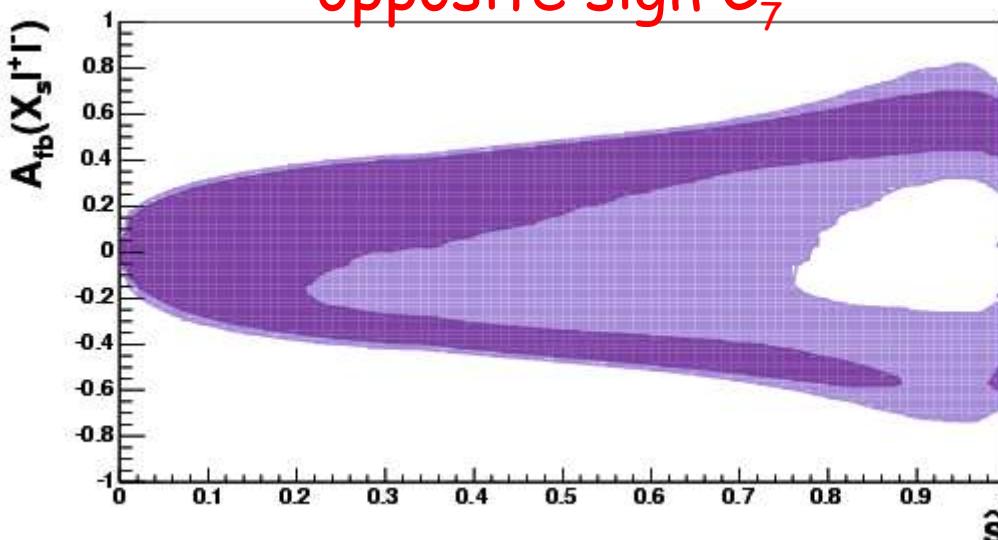
C_7^{eff}, C SM-like



opposite sign C



opposite sign C_7^{eff}



Can we estimate NP contributions to $B \rightarrow (\phi, \eta, \omega, \pi) K_s$?

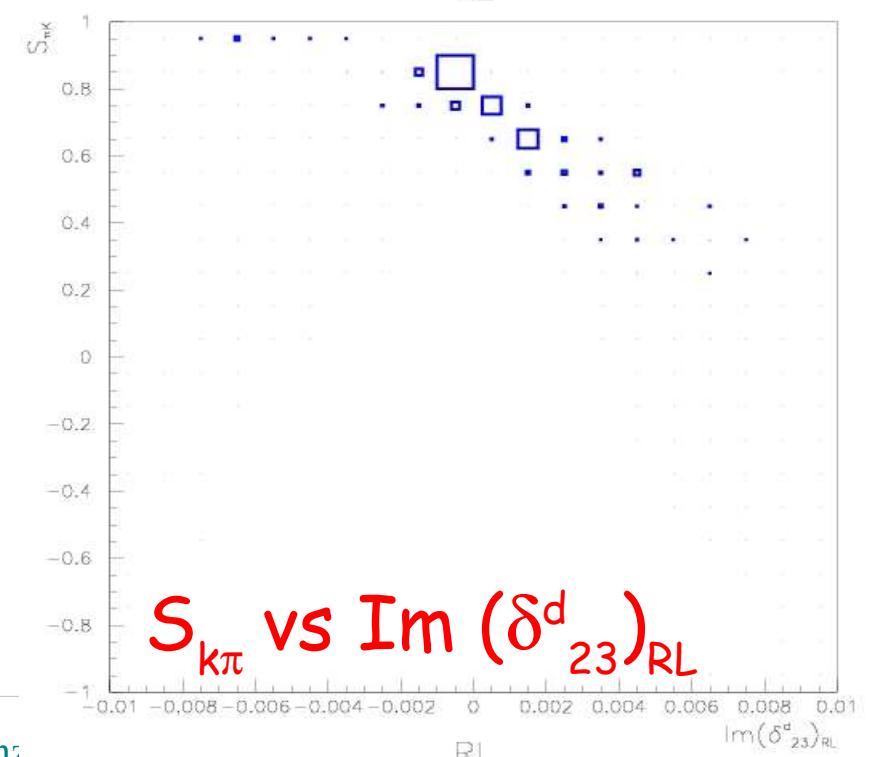
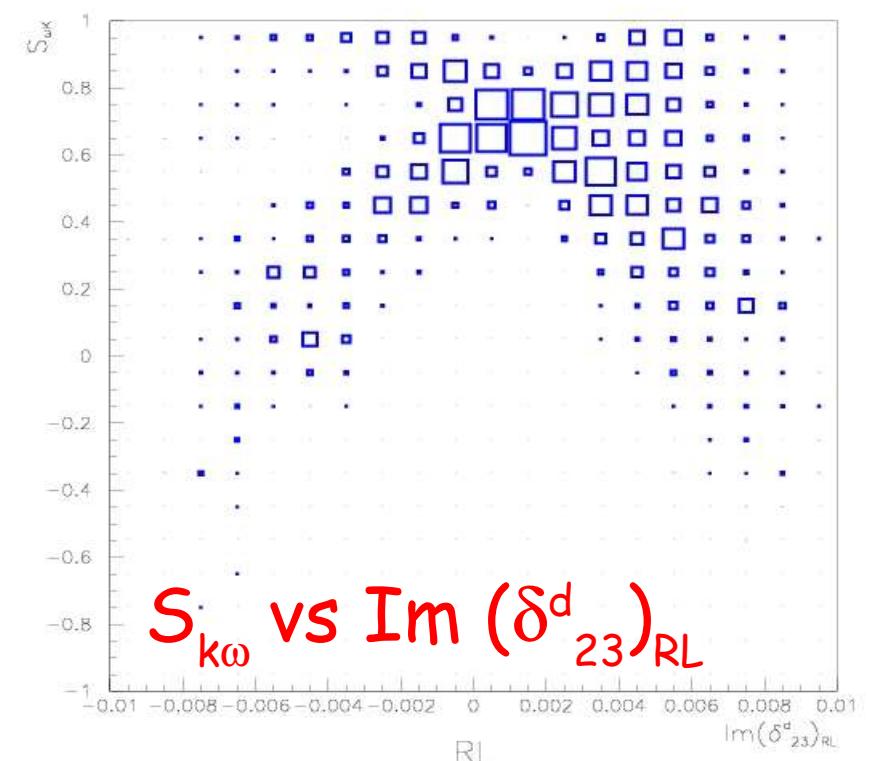
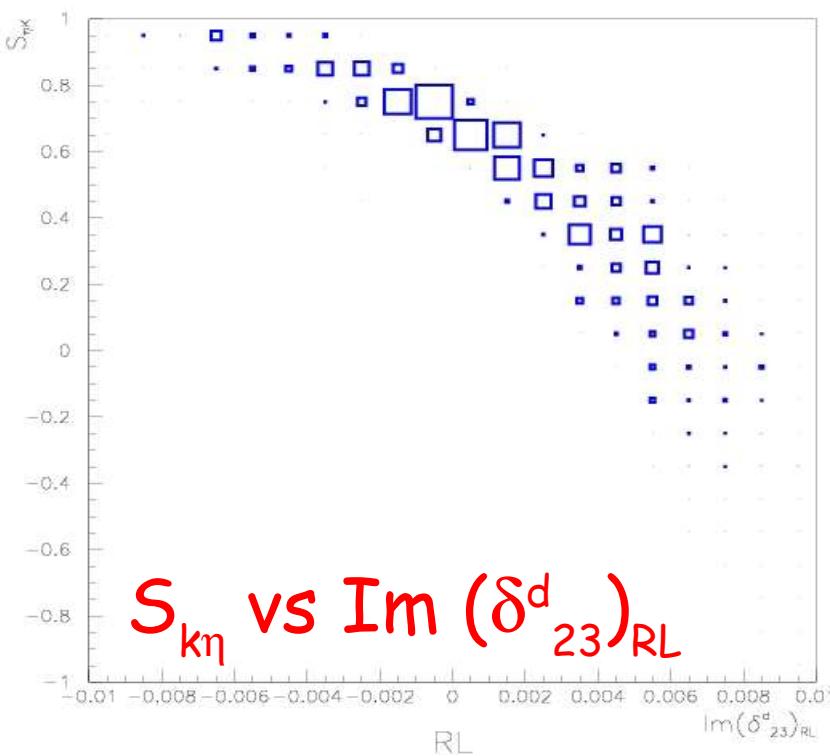
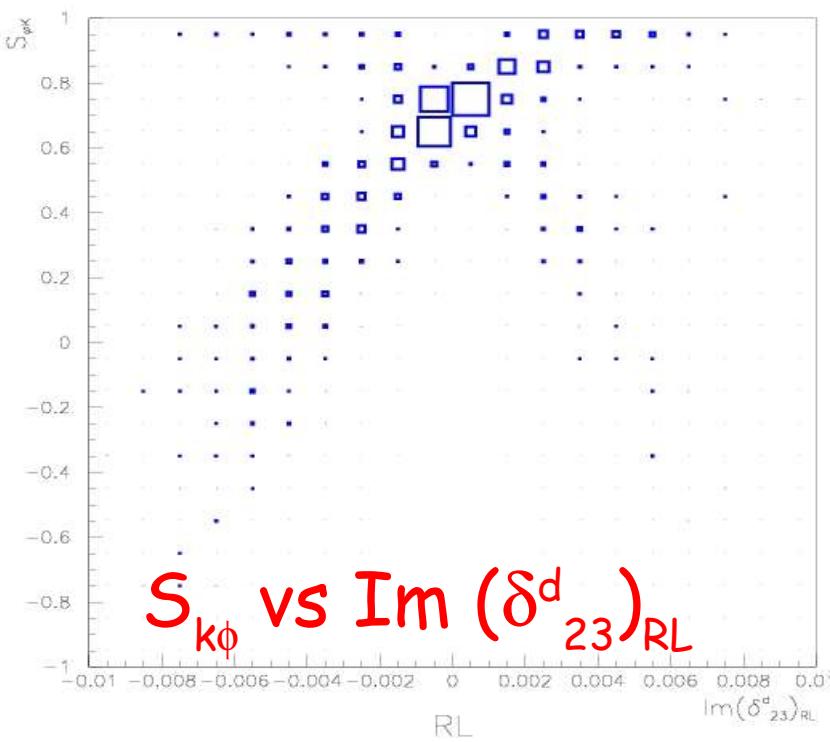
- Realistic studies of NP effects in these modes should take into account:
 - Hadronic uncertainties in computation of decay amplitudes → model dependent
 - Correlation with other $b \rightarrow s$ observables:
 $b \rightarrow s \gamma$, $b \rightarrow s l^+ l^-$, $B \rightarrow K\pi$, ΔM_s , etc.
→ very stringent by now

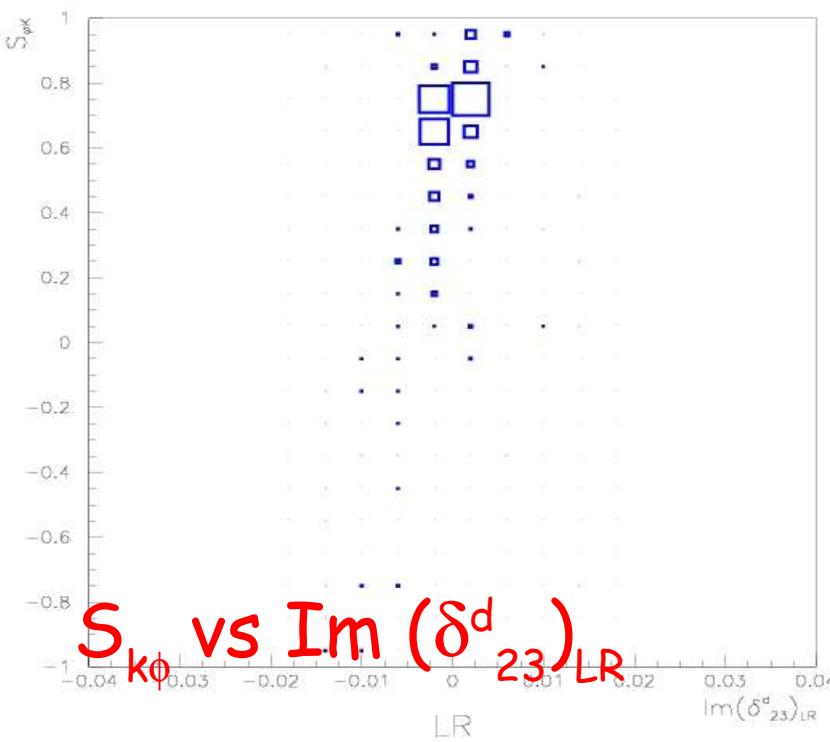
PREDICTIONS FOR $\sin^2\beta^{\text{eff}}$

- To be generous with SUSY, use QCD factorization with enlarged range for power-suppressed corrections - **Model dependent, large uncertainties**

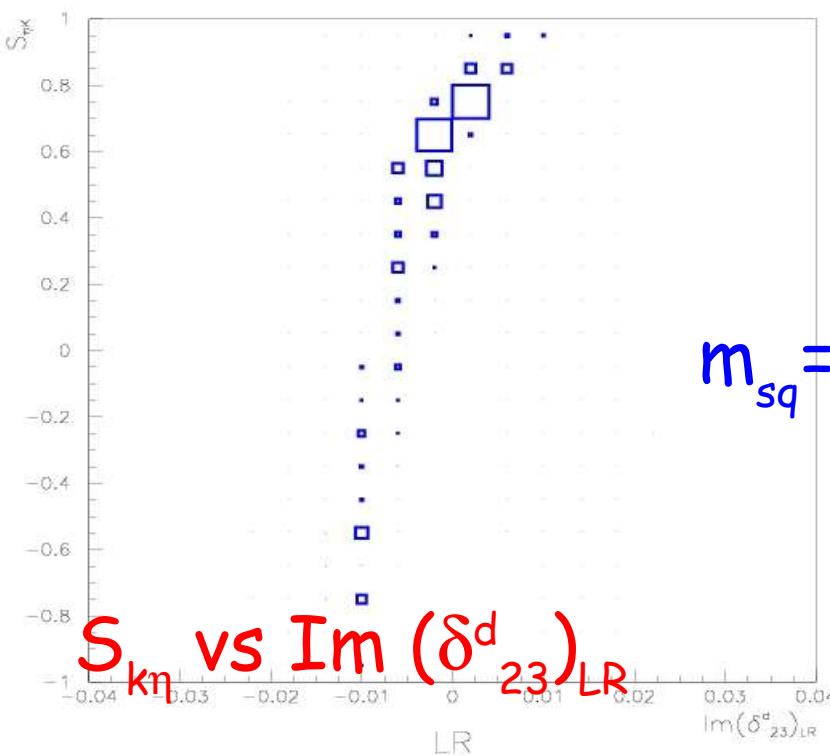
Beneke et al., PRL83, NPB606, NPB675; Ciuchini et al., PLB515, PRD67.

- impose agreement with BR's and direct CP violation
- As an example, results in the RL case

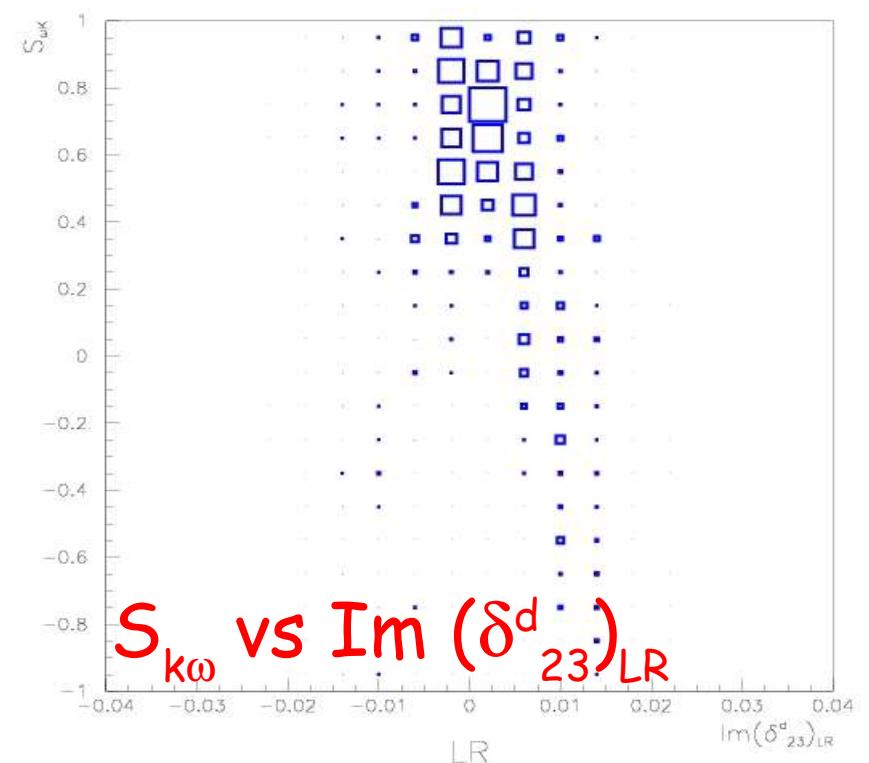




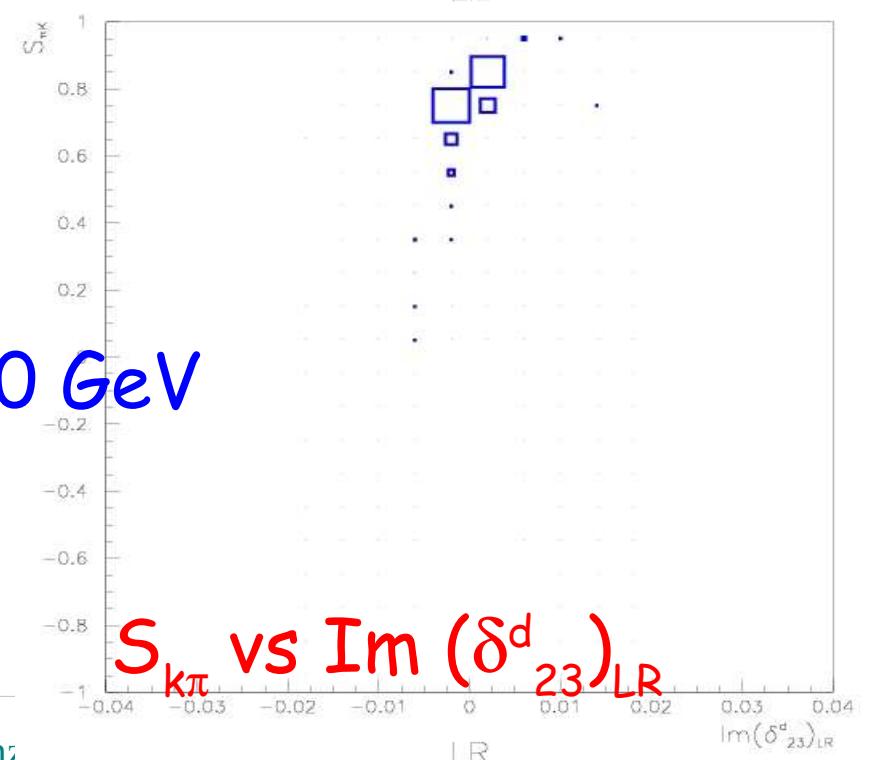
$S_{k\phi}$ vs $\text{Im}(\delta_{23}^d)_{\text{LR}}$



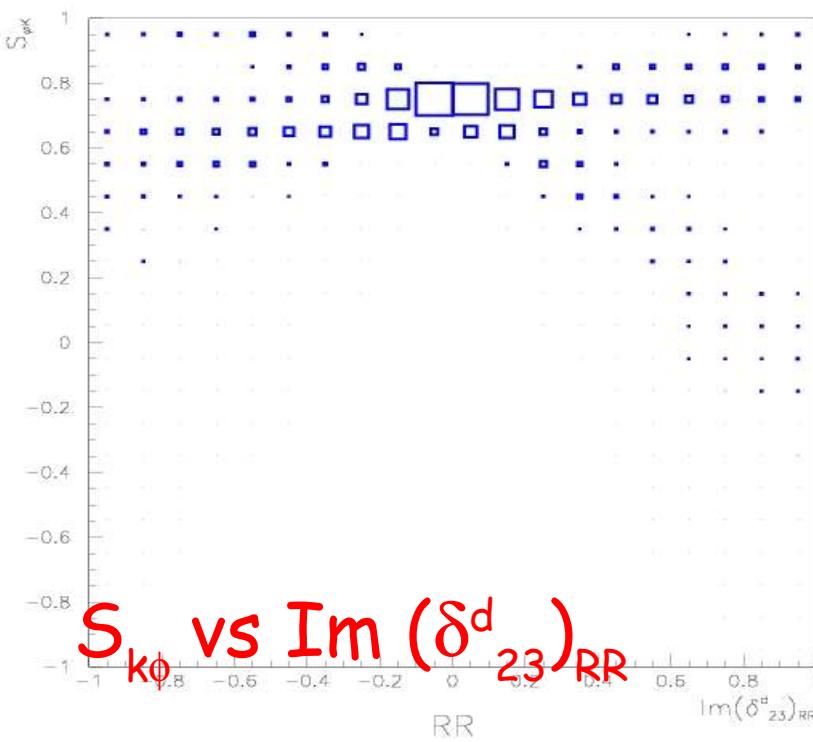
S_{kn} vs $\text{Im}(\delta_{23}^d)_{\text{LR}}$



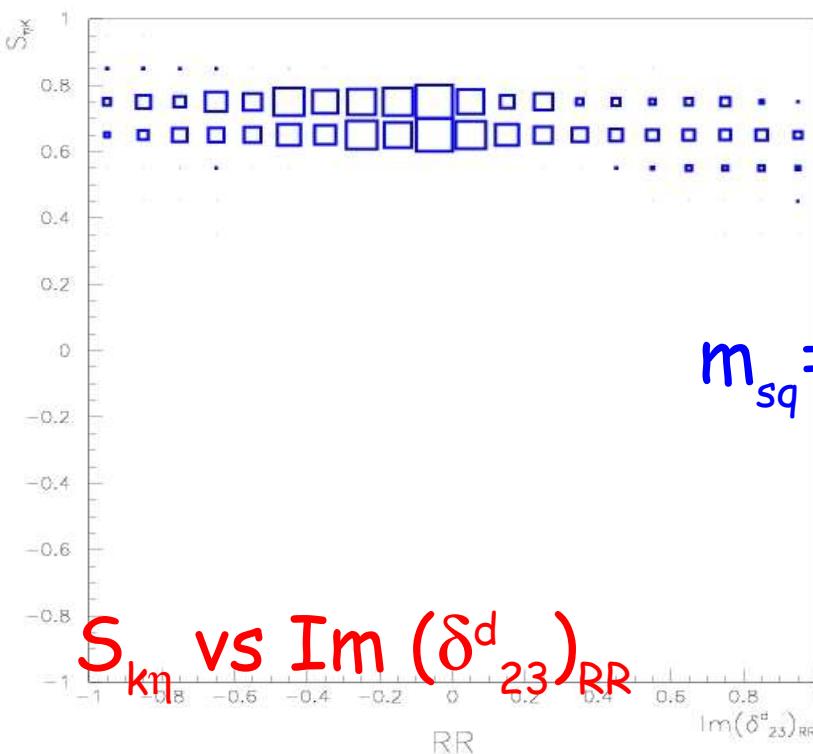
$S_{k\omega}$ vs $\text{Im}(\delta_{23}^d)_{\text{LR}}$



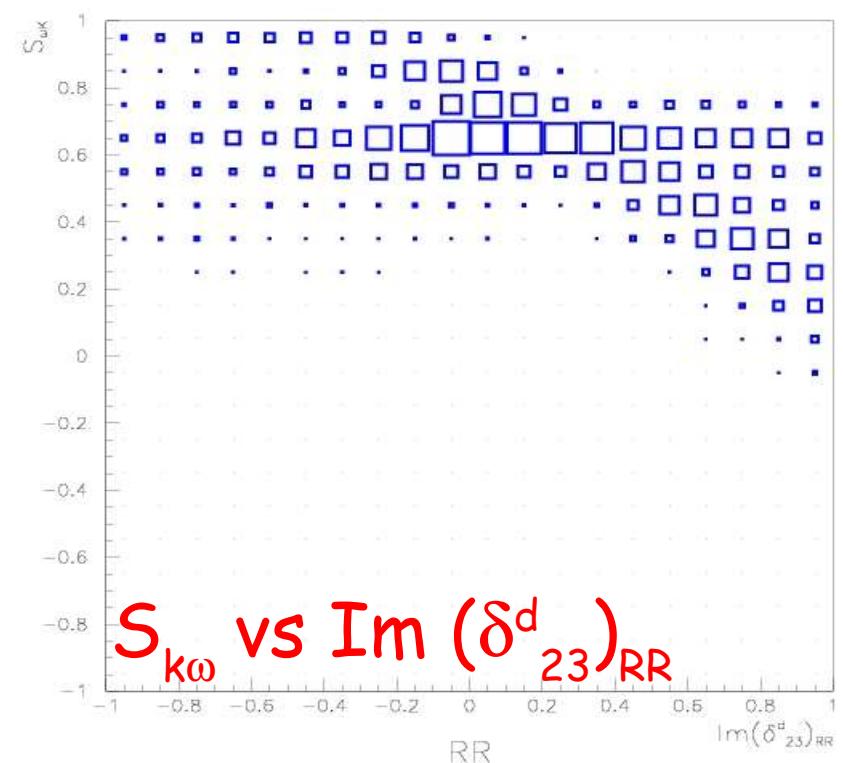
$S_{k\pi}$ vs $\text{Im}(\delta_{23}^d)_{\text{LR}}$



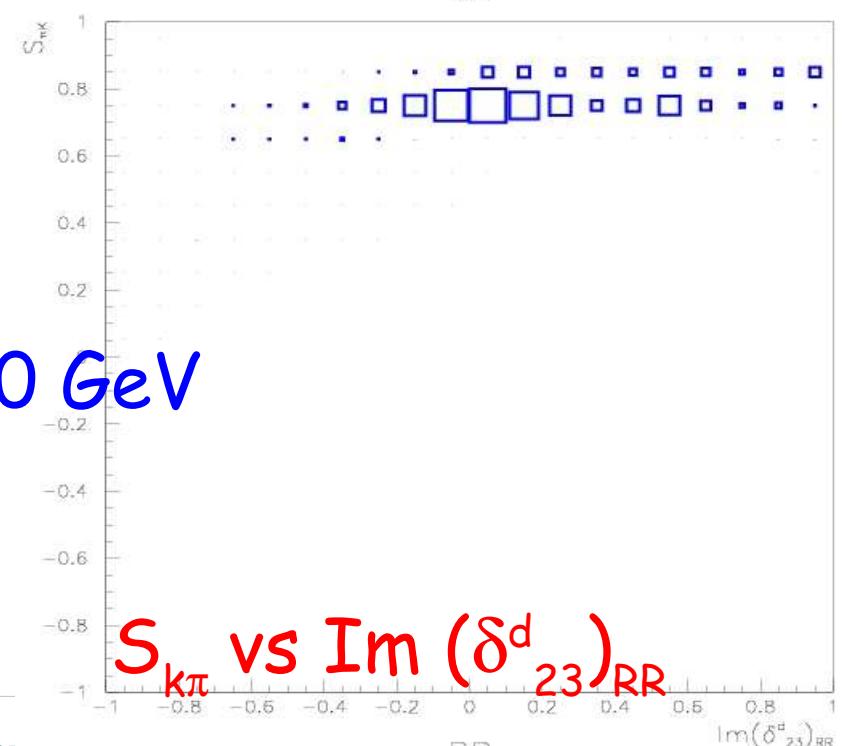
$S_{k\phi}$ vs $\text{Im}(\delta_{23}^d)_{RR}$



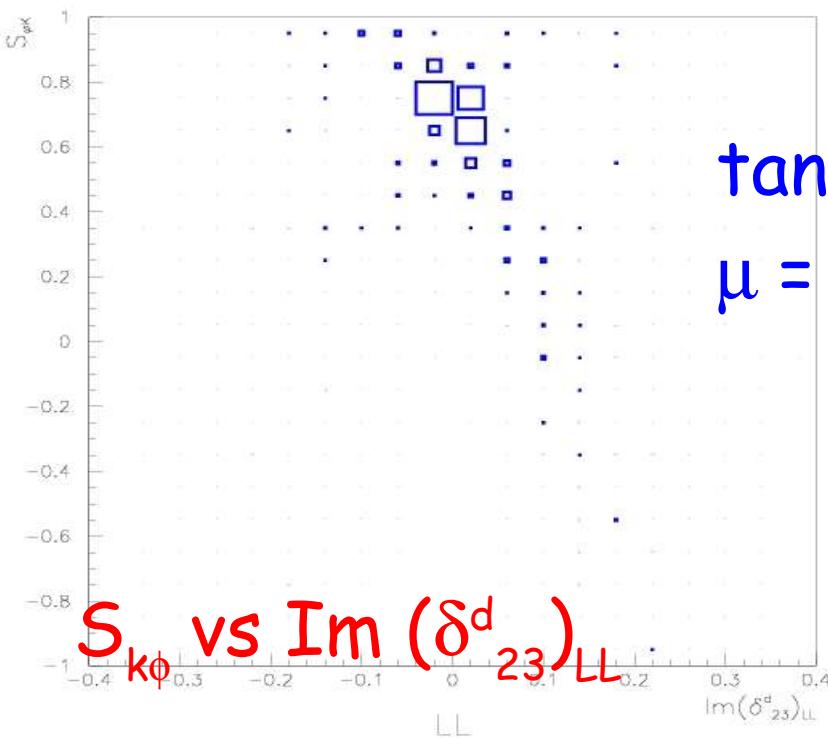
S_{kn} vs $\text{Im}(\delta_{23}^d)_{RR}$



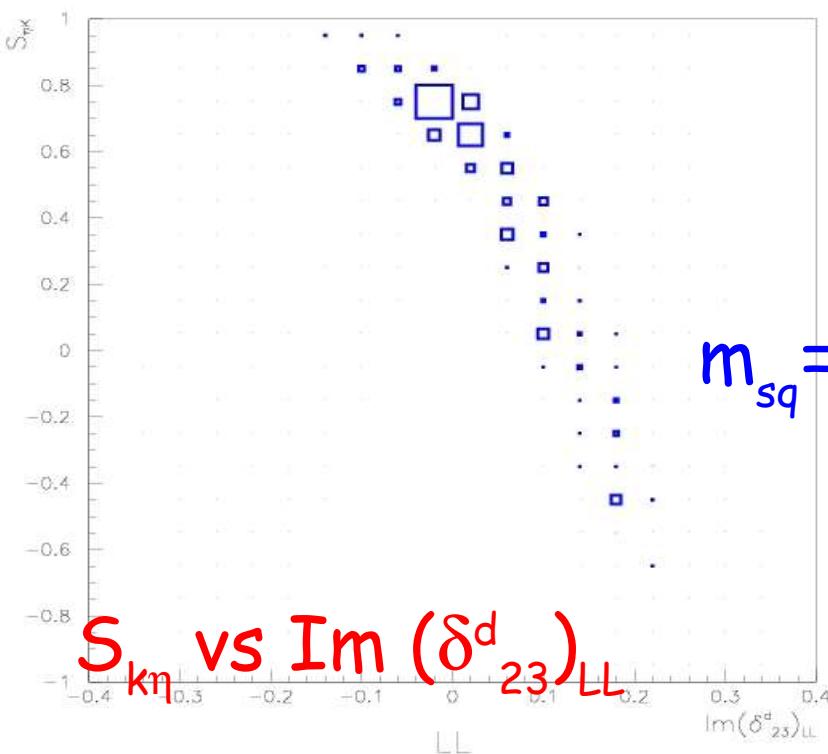
$S_{k\omega}$ vs $\text{Im}(\delta_{23}^d)_{RR}$



$S_{k\pi}$ vs $\text{Im}(\delta_{23}^d)_{RR}$



$\tan \beta = 10,$
 $\mu = -350 \text{ GeV}$



$m_{sq} = m_{gl} = 350 \text{ GeV}$

