

NNLOPS predictions for Higgs boson production

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GGI

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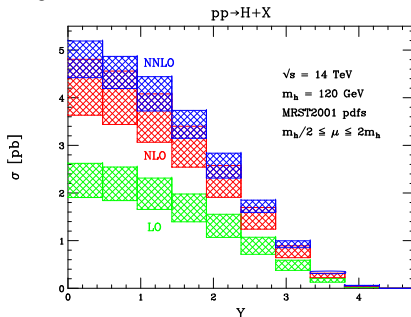
Outline

- ▶ brief motivation
- ▶ method used
- ▶ results
- ▶ conclusion, discussion, ...lunch!

NNLO Higgs production

NLO not always enough: NNLO needed when

1. large NLO/LO “K-factor”
[as in Higgs Physics]
 2. very high precision needed
[e.g. Drell-Yan]
- last couple of years:
huge progress in NNLO

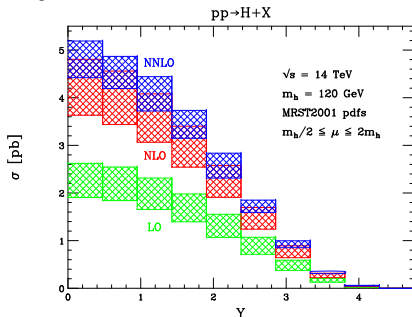


[Anastasiou et al., '04-'05]

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Q: can we merge NNLO and PS?

[Anastasiou et al., '04-'05]

☞ Realistic event generation with state-of-the-art perturbative accuracy !
☞ could be important for precision studies in Higgs physics

▶ method presented here was used so far for

- Higgs production

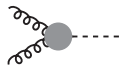
[Hamilton,Nason,ER,Zanderighi, 1309.0017]

- neutral & charged Drell-Yan

[Karlberg,ER,Zanderighi, 1407.2940]

Summary of the talk

Higgs at NNLO:



loops: 0 1 2



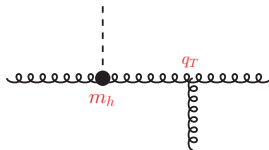
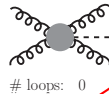
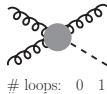
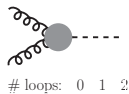
loops: 0 1



loops: 0

Summary of the talk

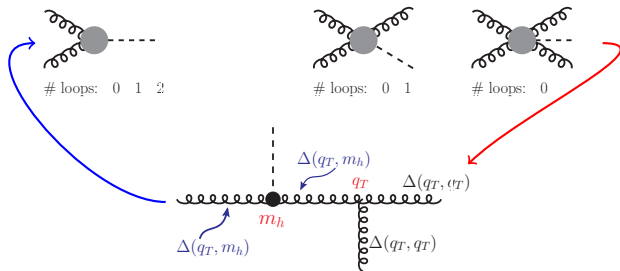
Higgs at NNLO:



(a) 1 and 2 jets: POWHEG H+1j

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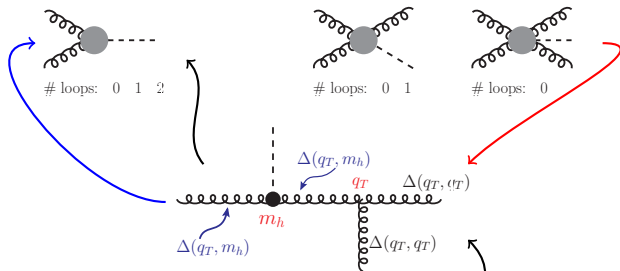
Higgs at NNLO:



- (b) - integrate down to $q_T = 0$ with MiNLO
 - "Improved MiNLO" allows to build a H-HJ @ NLOPS generator
- (a) 1 and 2 jets: POWHEG H+1j

Summary of the talk

Higgs at NNLO:



(c) 2 loops missing: from exact fixed-order NNLO

$$W(y) = \frac{d\sigma(y)_{\text{NNLO}}}{d\sigma(y)_{\text{MINLO}}}$$

(b) - integrate down to $q_T = 0$ with MiNLO

- "Improved MiNLO" allows to build a H-HJ @ NLOPS generator

(a) 1 and 2 jets: POWHEG H+1j

- ▶ what do we need and what do we already have?

	H (inclusive)	H+j (inclusive)	H+2j (inclusive)
H @ NLOPS	NLO	LO	shower
HJ @ NLOPS	/	NLO	LO
H-HJ @ NLOPS	NLO	NLO	LO
H @ NNLOPS	NNLO	NLO	LO

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H @ NNLOPS	NNLO	NLO	LO

👉 a merged H-HJ generator is almost OK

- ▶ many of the multijet NLO+PS merging approaches work by combining 2 (or more) NLO+PS generators, introducing a merging scale
- ▶ POWHEG + MiNLO: **no need of merging scale**: it extends the validity of an NLO computation with jets in the final state in regions where jets become unresolved

Multiscale Improved NLO

[Hamilton,Nason,Zanderighi, 1206.3572]

- ▶ original goal: method to **a-priori** choose scales in **multijet** NLO computation
- ▶ non-trivial task: hierarchy among scales can spoil accuracy (large logs can appear, without being resummed)
- ▶ how: correct weights of different NLO terms with CKKW-inspired approach (**without spoiling formal NLO accuracy**)

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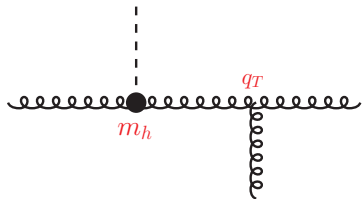
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 - for each point sampled, build the “more-likely” shower history that would have produced that kinematics (can be done by clustering kinematics with k_T -algo, then, by undoing the clustering, build “skeleton”)
 - correct original NLO: α_S evaluated at **nodal scales** and **Sudakov FFs**
 - has been used in V/H + up to 2 jets and in VH + up to 1 jet

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$$\bar{B}_{\text{NLO}} = \alpha_S^3(\mu_R) \left[B + \alpha_S^{(\text{NLO})} V(\mu_R) + \alpha_S^{(\text{NLO})} \int d\Phi_{\text{r}} R \right]$$



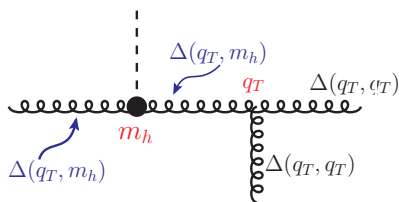
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$$\bar{B}_{\text{MiNLO}} = \alpha_S^2(m_h) \alpha_S(q_T) \Delta_g^2(q_T, m_h) \left[B \left(1 - 2\Delta_g^{(1)}(q_T, m_h) \right) + \alpha_S^{(\text{NLO})} V(\bar{\mu}_R) + \alpha_S^{(\text{NLO})} \int d\Phi_T R \right]$$



$$\cdot \bar{\mu}_R = (m_h^2 q_T^2)^{1/3}$$

$$\cdot \log \Delta_f(q_T, m_h) = - \int_{q_T^2}^{m_h^2} \frac{dq^2}{q^2} \frac{\alpha_S(q^2)}{2\pi} \left[A_f \log \frac{m_h^2}{q^2} + B_f \right]$$

$$\cdot \Delta_f^{(1)}(q_T, m_h) = - \frac{\alpha_S^{(\text{NLO})}}{2\pi} \left[\frac{1}{2} A_{1,f} \log^2 \frac{m_h^2}{q_T^2} + B_{1,f} \log \frac{m_h^2}{q_T^2} \right]$$

$$\cdot \mu_F = q_T$$

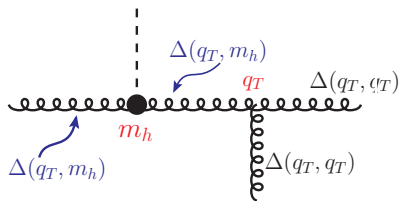
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☞ Sudakov FF included on $H+j$
Born kinematics

- ▶ with MiNLO, **finite results** from HJ also when 1st jet is **unresolved** ($q_T \rightarrow 0$)
- ▶ \bar{B}_{MiNLO} ideal to extend validity of HJ-POWHEG [called "HJ-MiNLO" hereafter]

“Improved” MiNLO & NLOPS merging

- ▶ formal accuracy of HJ-MiNLO for inclusive observables carefully investigated

[Hamilton et al., 1212.4504]

- ▶ HJ-MiNLO describes inclusive observables at order $\alpha_S^2 + \alpha_S^3$
- ▶ to reach genuine NLO when fully inclusive ($\text{NLO}^{(0)}$), “spurious” terms must be of relative order α_S^2 , *i.e.*

$$O_{\text{HJ-MiNLO}} = O_{\text{H@NLO}} + \mathcal{O}(\alpha_S^4) \quad \text{if } O \text{ is inclusive}$$

- ▶ “Original MiNLO ” contains **ambiguous “ $\mathcal{O}(\alpha_S^{2+1.5})$ ” terms**
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- ▶ Possible to improve $HJ\text{-MiNLO}$ such that inclusive NLO is recovered ($NLO^{(0)}$), without spoiling NLO accuracy of $H+j$ ($NLO^{(1)}$).

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- proof based on careful comparisons of MiNLO with general resummation formula

$$\sim \sigma_0 \frac{1}{q_T^2} [\alpha_S, \alpha_S^2, \alpha_S^3, \alpha_S^4, \alpha_S L, \alpha_S^2 L, \alpha_S^3 L, \alpha_S^4 L] \exp S(q_T, Q) + R_f \quad L = \log(Q^2/q_T^2)$$

- need to include B_2 coefficient in MiNLO-Sudakovs:
 - **highlighted terms** are needed to reach NLO⁽⁰⁾:

$$\int^{Q^2} \frac{dq_T^2}{q_T^2} L^m \alpha_S^n(q_T) \exp S \sim (\alpha_S(Q^2))^{n-(m+1)/2}$$

(scaling in low- p_T region is $\alpha_S L^2 \sim 1!$)

- if I don't include B_2 in MiNLO Δ_g , I miss a term $(1/q_T^2) \alpha_S^2 B_2 \exp S$
- upon integration, violate NLO⁽⁰⁾ by a term of relative $\mathcal{O}(\alpha_S^{3/2})$
- need to evaluate $\alpha_S^{(\text{NLO})}$ in HJ-MiNLO at scale q_T , and $\mu_F = q_T$

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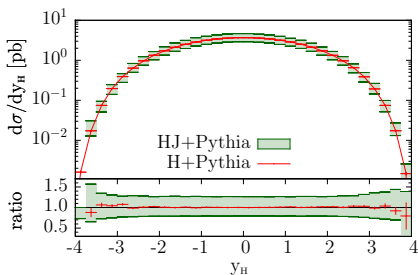
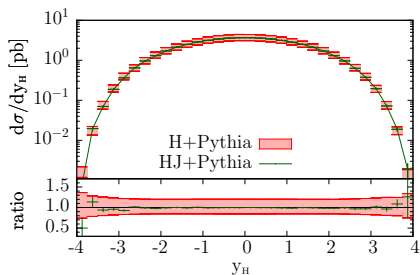
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- ▶ Possible to improve HJ-MiNLO such that inclusive NLO is recovered ($\text{NLO}^{(0)}$), without spoiling NLO accuracy of $H+j$ ($\text{NLO}^{(1)}$).

Effectively as if we merged $\text{NLO}^{(0)}$ and $\text{NLO}^{(1)}$ samples, **without merging** different samples (no merging scale used: there is just one sample).



- ▶ “H+Pythia”: standalone POWHEG ($gg \rightarrow H$) + PYTHIA (PS level) [7pts band, $\mu = m_H$]
- ▶ “HJ+Pythia”: HJ-MiNLO + PYTHIA (PS level) [7pts band, μ from MiNLO]
- ✓ very good agreement (both value and band)

Notice: band is $\sim 20 - 30\%$

- ▶ HJ-MiNLO+POWHEG generator gives H-HJ @ NLOPS

	H (inclusive)	H+j (inclusive)	H+2j (inclusive)
✓ H-HJ @ NLOPS	NLO	NLO	LO
H @ NNLOPS	NNLO	NLO	LO

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- ▶ reweighting (differential on y_H) of “MiNLO-generated” events:

$$W(y_H) = \frac{\left(\frac{d\sigma}{dy_H}\right)_{\text{NNLO}}}{\left(\frac{d\sigma}{dy_H}\right)_{\text{HJ-MiNLO}}}$$

- ▶ by construction NNLO accuracy on fully inclusive observables (σ_{tot}, y_H) [✓]
- ▶ to reach NNLOPS accuracy, need to be sure that the reweighting doesn't spoil the NLO accuracy of HJ-MiNLO in 1-jet region []

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- ▶ by construction NNLO accuracy on fully inclusive observables (σ_{tot}, y_H) [✓]
- ▶ to reach NNLOPS accuracy, need to be sure that the reweighting doesn't spoil the NLO accuracy of HJ-MiNLO in 1-jet region [✓]
- ▶ notice: formally works because no spurious $\mathcal{O}(\alpha_S^{2+1.5})$ terms in H-HJ @ NLOPS

Higgs at NNLO+PS II

- ▶ Variants for reweighting ($W(y_H)$) are also possible:

$$W(y, p_T) = h(p_T) \frac{\int d\sigma_A^{\text{NNLO}} \delta(y - y(\Phi))}{\int d\sigma_A^{\text{MiNLO}} \delta(y - y(\Phi))} + (1 - h(p_T))$$

$$d\sigma_A = d\sigma h(p_T), \quad d\sigma_B = d\sigma (1 - h(p_T)), \quad h = \frac{(\beta m_H)^2}{(\beta m_H)^2 + p_T^2}$$

- . $h(p_T)$ controls where the NNLO/NLO K-factor is distributed (in the high- p_T region, there is no improvement in including it)
- . β cannot be too small, otherwise resummation spoiled: for Higgs, chosen $\beta = 1/2$

-
- ▶ for Higgs (and for Drell-Yan) we used

$$W(y, p_T) = h(p_T) \frac{\int d\sigma^{\text{NNLO}} \delta(y - y(\Phi)) - \int d\sigma_B^{\text{MiNLO}} \delta(y - y(\Phi))}{\int d\sigma_A^{\text{MiNLO}} \delta(y - y(\Phi))} + (1 - h(p_T))$$

- . one gets exactly $(d\sigma/dy)_{\text{NNLOPS}} = (d\sigma/dy)_{\text{NNLO}}$ (no α_S^5 terms)
- . we used $h(p_T^{j1})$

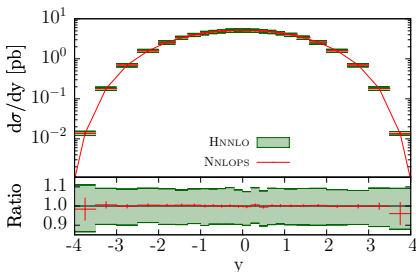
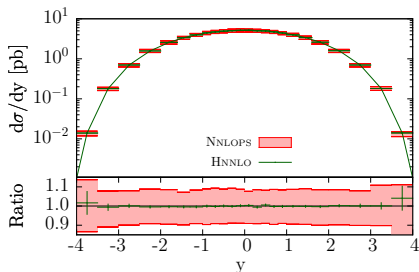
inputs for following plots:

- results are for 8 TeV LHC
- scale choices: NNLO input with $\mu = m_H/2$, HJ-MiNLO “core scale” m_H (other powers are at q_T)
- PDF: everywhere MSTW2008 NNLO
- NNLO always from HNNLO
- 6M events reweighted at the LH level
- plots after k_T -ordered PYTHIA 6 at the PS level (hadronization and MPI switched off)

NNLO+PS (fully incl.)

- ▶ NNLO with $\mu = m_H/2$, HJ-MiNLO “core scale” m_H
- ▶ ($7_{\text{Mi}} \times 3_{\text{NN}}$) pts scale var. in NNLOPS, 7pts in NNLO

[NNLO from HNNLO, Catani, Grazzini]

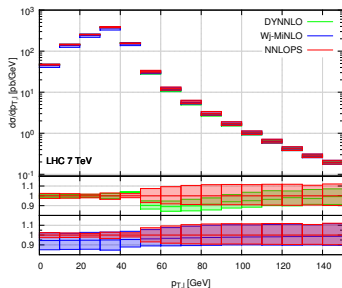


☞ Notice: band is 10% (at NLO would be $\sim 20\text{-}30\%$)

[Until and including $\mathcal{O}(\alpha_S^4)$, PS effects don't affect y_H (first 2 emissions controlled properly at $\mathcal{O}(\alpha_S^4)$ by MiNLO+POWHEG)]

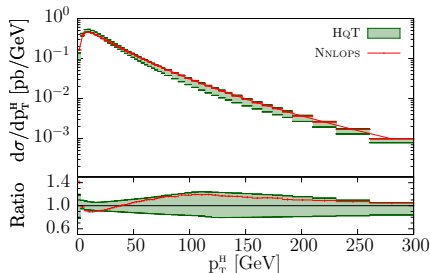
NNLO+PS: multi-dim reweighting

- ▶ for Higgs: 1-dim NNLOPS reweighting ($W(y; p_T)$), so y_H will be obviously OK
- ▶ does it work if Φ_B is multi-dim (as in Drell-Yan)?

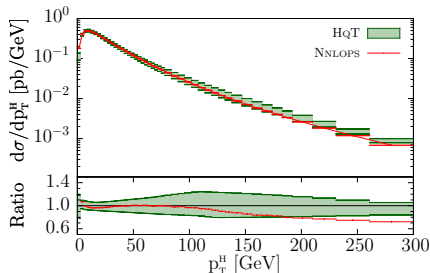


- ▶ $p_{T,\ell}$ is **not** the observable we are using to do the NNLO reweighting
- ✓ we see exactly what we expect: $p_{T,\ell}$ has NNLO uncertainty if $p_{T,\ell} < M_W/2$, and NLO if $p_{T,\ell} > M_W/2$
- ▶ [just above peak, DYNNLO uses M_W , WJ-MINLO uses $p_{T,W}$ and here $0 \lesssim p_{T,W} \lesssim M_W$]

$\beta = \infty$ (W indep. of p_T)

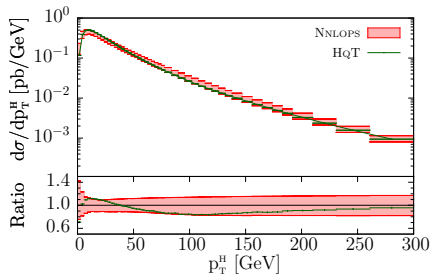


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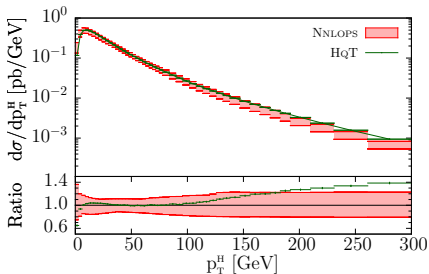


- ▶ HqT: NNLL+NNLO, $\mu_R = \mu_F = m_H/2$ [7pts], $Q_{\text{res}} \equiv m_H/2$ [HqT, Bozzi et al.]
- ✓ $\beta = 1/2$ & ∞ : uncertainty bands of HqT contain NNLOPS at low-/moderate p_T
- ▶ $\beta = 1/2$: HqT tail harder than NNLOPS tail ($\mu_{\text{HqT}} < \mu_{\text{MiNLO}}$)
HJ @ NNLO will allow to say more for large $p_{T,H}$
- ▶ $\beta = 1/2$: very good agreement with HqT resummation
[" \sim expected", since $Q_{\text{res}} \equiv m_H/2$]

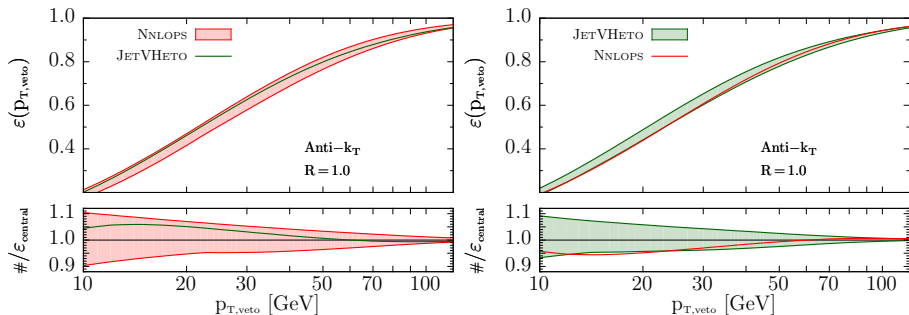
$\beta = \infty$ (W indep. of p_T)



$\beta = 1/2$



- ▶ HqT: NNLL+NNLO, $\mu_R = \mu_F = m_H/2$ [7pts], $Q_{\text{res}} \equiv m_H/2$
- ▶ $\beta = 1/2$: NNLOPS tail \rightarrow NLOPS tail [$W(y, p_T \gg m_H) \rightarrow 1$]
larger band (affected just marginally by NNLO, so it's \sim genuine NLO band)



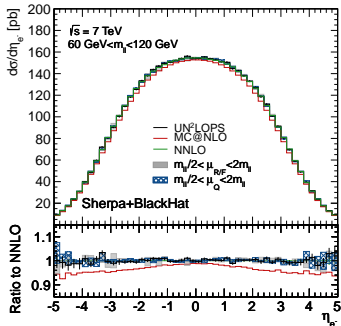
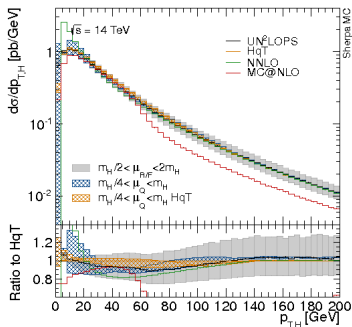
$$\varepsilon(p_{T,\text{veto}}) = \frac{\Sigma(p_{T,\text{veto}})}{\sigma^{\text{tot}}} = \frac{1}{\sigma^{\text{tot}}} \int d\sigma \theta(p_{T,\text{veto}} - p_T^{j1})$$

- ▶ JetVHeto: NNLL resum, $\mu_R = \mu_F = m_H/2$ [7pts], $Q_{\text{res}} \equiv m_H/2$, (a)-scheme only
[JetVHeto, Banfi et al.]
- ▶ nice agreement, differences never more than 5-6 %

☞ Separation of $H \rightarrow WW$ from $t\bar{t}$ bkg: x-sec binned in N_{jet}
0-jet bin \Leftrightarrow jet-veto accurate predictions needed !

► UNNLOPS

[Hoeche, Li, Prestel '14]



► formalism worked out also within the Geneva framework:

[Alioli, Bauer, et al, '13]

- work in progress, preliminary results for DY shown at “PSR2014”

conclusions

- ▶ `MINLO`-improved `POWHEG` generator allows to reach NNLOPS accuracy for simple processes
- ▶ shown results for Higgs at NNLOPS
- ▶ predictions and theoretical uncertainties match NNLO where they have to
- ▶ typically, quite good agreement with analytic resummation (but for Drell-Yan slightly worse...)
 - good news, but not yet really studied/understood formally
- ▶ other approaches appeared: will be interesting to compare
- ▶ mass effects in Higgs @ NNLOPS
- ▶ ... phenomenology ...

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Thank you for your attention!