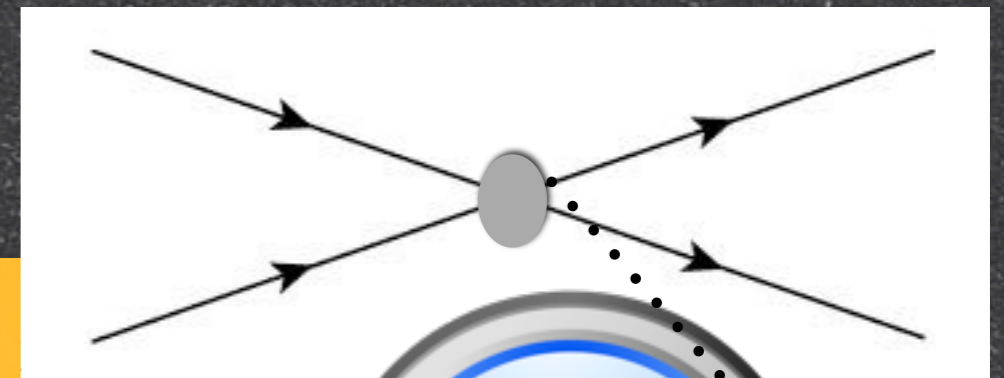


Adam Falkowski (LPT Orsay)

Model Independent Constraints

on

Physics Beyond the Standard Model



Florence, 17 September 2015

Based on my [1505.00046](#), [1503.07872](#) with Aielet Efrati and Yotam Soreq, [1411.0669](#) with Francesco Riva, and [1508.00581](#) with Martín Gonzalez-Alonso, Admir Greljo, and David Marzocca

Plan

- Effective field theory approach to physics beyond the standard model
- Current precision constraints:
 - from LEP-1 pole observables
 - from LHC Higgs data and LEP-2 WW production
 - from LEP-2 $ee \rightarrow ll$ scattering (preview)

Effective Field Theory

approach to BSM physics

Premise

- SM is probably a correct theory the weak scale, at least as the lowest order term in an **effective theory** expansion
- If new particles are heavy, their effects can be parametrized by higher-dimensional operators added to the SM Lagrangian
- EFT framework offers a systematic expansion around the SM organized in terms of operator dimensions, with higher dimensional operator suppressed by the mass scale Λ of new physics

Effective Theory Approach to BSM

Basic assumptions

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} \dots \\ v + h + \dots \end{pmatrix}$$

- New physics scale Λ separated from EW scale v , $\Lambda \gg v$
- **Linearly** realized $SU(3) \times SU(2) \times U(1)$ local symmetry spontaneously broken by VEV of Higgs doublet field

EFT Lagrangian beyond the SM expanded in operator dimension D

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}^{D=5} + \frac{1}{\Lambda^2} \mathcal{L}^{D=6} + \frac{1}{\Lambda^3} \mathcal{L}^{D=7} + \frac{1}{\Lambda^4} \mathcal{L}^{D=8} + \dots$$

*Alternatively,
non-linear Lagrangians
with derivative expansion*

Effective Theory Approach to BSM

Basic assumptions

- New physics scale Λ separated from EW scale v , $\Lambda \gg v$
- **Linearly** realized $SU(3) \times SU(2) \times U(1)$ local symmetry spontaneously broken by VEV of Higgs doublet field

EFT Lagrangian beyond the SM expanded in operator dimension D

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}^{D=5} + \frac{1}{\Lambda^2} \mathcal{L}^{D=6} + \frac{1}{\Lambda^3} \mathcal{L}^{D=7} + \frac{1}{\Lambda^4} \mathcal{L}^{D=8} + \dots$$

Lepton number violating,
hence too small to probe at LHC

By assumption,
subleading
to $D=6$

EFT approach to BSM

- First attempts to classify dimension-6 operators back in 1986
- First complete and non-redundant set of operators explicitly written down only in 2010
- Operators can be traded for other operators using integration by parts, field redefinition, equations of motion, Fierz transformation, etc
- Because of that, one can choose many different bases == non-redundant sets of operators

Buchmuller,Wyler
pre-arxiv (1986)

Grzadkowski et al.
[1008.4884](#)

see e.g.
Grzadkowski et al. [1008.4884](#)
Giudice et al [hep-ph/0703164](#)
Contino et al [1303.3876](#)

For D=6 Lagrangian several complete non-redundant set of operators (so-called **basis**) proposed in the literature

D=6 Basis

SILH basis

Giudice et al [hep-ph/0703164](#)
Contino et al [1303.3876](#)

HISZ basis

Hagiwara et al (1993)

h basis

LHCHSWG-INT-2015-001

$\mathcal{L}^{D=6}$

Warsaw Basis

Grzadkowski et al. [1008.4884](#)

Primary basis

Gupta et al [1405.0181](#)

- All bases are equivalent, but some may be more convenient for specific applications
- Physics description (EWPT, Higgs, RG running) in any of these bases contains the same information, provided **all** operators contributing to that process are taken into account

Example: Warsaw Basis

Grzadkowski et al.
1008.4884

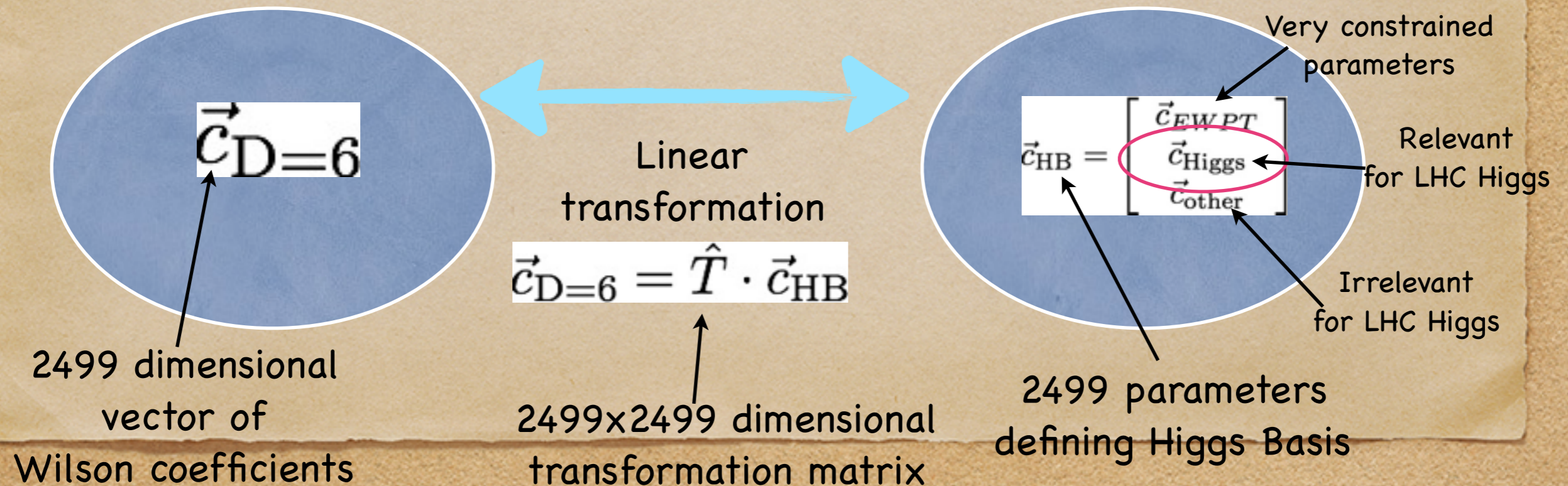
59 different
kinds of operators,
of which 17 are complex
2499 distinct operators,
including flavor structure
and CP conjugates

Alonso et al 1312.2014

$H^4 D^2$ and H^6		$f^2 H^3$		$V^3 D^3$	
O_H	$[\partial_\mu(H^\dagger H)]^2$	O_e	$-(H^\dagger H - \frac{v^2}{2})\bar{e}H^\dagger\ell$	O_{3G}	$g_s^3 f^{abc} G_{\mu\nu}^a G_{\nu\rho}^b G_{\rho\mu}^c$
O_T	$(H^\dagger \overleftrightarrow{D}_\mu H)^2$	O_u	$-(H^\dagger H - \frac{v^2}{2})\bar{u}\tilde{H}^\dagger q$	$O_{\widetilde{3G}}$	$g_s^3 f^{abc} \tilde{G}_{\mu\nu}^a G_{\nu\rho}^b G_{\rho\mu}^c$
O_{6H}	$(H^\dagger H)^3$	O_d	$-(H^\dagger H - \frac{v^2}{2})\bar{d}H^\dagger q$	O_{3W}	$g^3 \epsilon^{ijk} W_{\mu\nu}^i W_{\nu\rho}^j W_{\rho\mu}^k$
				$O_{\widetilde{3W}}$	$g^3 \epsilon^{ijk} \tilde{W}_{\mu\nu}^i W_{\nu\rho}^j W_{\rho\mu}^k$
$V^2 H^2$		$f^2 H^2 D$		$f^2 VHD$	
O_{GG}	$\frac{g_s^2}{4} H^\dagger H G_{\mu\nu}^a G_{\mu\nu}^a$	$O_{H\ell}$	$i\bar{\ell}\gamma_\mu\ell H^\dagger \overleftrightarrow{D}_\mu H$	O_{eW}	$g\bar{\ell}\sigma_{\mu\nu}e\sigma^i H W_{\mu\nu}^i$
$O_{\widetilde{GG}}$	$\frac{g_s^2}{4} H^\dagger H \tilde{G}_{\mu\nu}^a G_{\mu\nu}^a$	$O'_{H\ell}$	$i\bar{\ell}\sigma^i\gamma_\mu\ell H^\dagger \sigma^i \overleftrightarrow{D}_\mu H$	O_{eB}	$g'\bar{\ell}\sigma_{\mu\nu}eHB_{\mu\nu}$
O_{WW}	$\frac{g^2}{4} H^\dagger H W_{\mu\nu}^i W_{\mu\nu}^i$	O_{He}	$i\bar{e}\gamma_\mu\bar{e}H^\dagger \overleftrightarrow{D}_\mu H$	O_{uG}	$g_s\bar{q}\sigma_{\mu\nu}T^a u\tilde{H} G_{\mu\nu}^a$
$O_{\widetilde{WW}}$	$\frac{g^2}{4} H^\dagger H \tilde{W}_{\mu\nu}^i W_{\mu\nu}^i$	O_{Hq}	$i\bar{q}\gamma_\mu q H^\dagger \overleftrightarrow{D}_\mu H$	O_{uW}	$g\bar{q}\sigma_{\mu\nu}u\sigma^i \tilde{H} W_{\mu\nu}^i$
O_{BB}	$\frac{g'^2}{4} H^\dagger H B_{\mu\nu} B_{\mu\nu}$	O'_{Hq}	$i\bar{q}\sigma^i\gamma_\mu q H^\dagger \sigma^i \overleftrightarrow{D}_\mu H$	O_{uB}	$g'\bar{q}\sigma_{\mu\nu}u\tilde{H} B_{\mu\nu}$
$O_{\widetilde{BB}}$	$\frac{g'^2}{4} H^\dagger H \tilde{B}_{\mu\nu} B_{\mu\nu}$	O_{Hu}	$i\bar{u}\gamma_\mu u H^\dagger \overleftrightarrow{D}_\mu H$	O_{dG}	$g_s\bar{q}\sigma_{\mu\nu}T^a dH G_{\mu\nu}^a$
O_{WB}	$gg'H^\dagger\sigma^i H W_{\mu\nu}^i B_{\mu\nu}$	O_{Hd}	$i\bar{d}\gamma_\mu d H^\dagger \overleftrightarrow{D}_\mu H$	O_{dW}	$g\bar{q}\sigma_{\mu\nu}d\sigma^i H W_{\mu\nu}^i$
$O_{\widetilde{WB}}$	$gg'H^\dagger\sigma^i H \tilde{W}_{\mu\nu}^i B_{\mu\nu}$	O_{Hud}	$i\bar{u}\gamma_\mu d \tilde{H}^\dagger D_\mu H$	O_{dB}	$g'\bar{q}\sigma_{\mu\nu}dH B_{\mu\nu}$
$(\bar{L}L)(\bar{L}L)$ and $(\bar{L}R)(\bar{L}R)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$O_{\ell\ell}$	$(\bar{\ell}\gamma_\mu\ell)(\bar{\ell}\gamma_\mu\ell)$	O_{ee}	$(\bar{e}\gamma_\mu e)(\bar{e}\gamma_\mu e)$	$O_{\ell e}$	$(\bar{\ell}\gamma_\mu\ell)(\bar{e}\gamma_\mu e)$
O_{qq}	$(\bar{q}\gamma_\mu q)(\bar{q}\gamma_\mu q)$	O_{uu}	$(\bar{u}\gamma_\mu u)(\bar{u}\gamma_\mu u)$	$O_{\ell u}$	$(\bar{\ell}\gamma_\mu\ell)(\bar{u}\gamma_\mu u)$
O'_{qq}	$(\bar{q}\gamma_\mu\sigma^i q)(\bar{q}\gamma_\mu\sigma^i q)$	O_{dd}	$(\bar{d}\gamma_\mu d)(\bar{d}\gamma_\mu d)$	$O_{\ell d}$	$(\bar{\ell}\gamma_\mu\ell)(\bar{d}\gamma_\mu d)$
$O_{\ell q}$	$(\bar{\ell}\gamma_\mu\ell)(\bar{q}\gamma_\mu q)$	O_{eu}	$(\bar{e}\gamma_\mu e)(\bar{u}\gamma_\mu u)$	O_{qe}	$(\bar{q}\gamma_\mu q)(\bar{e}\gamma_\mu e)$
$O'_{\ell q}$	$(\bar{\ell}\gamma_\mu\sigma^i\ell)(\bar{q}\gamma_\mu\sigma^i q)$	O_{ed}	$(\bar{e}\gamma_\mu e)(\bar{d}\gamma_\mu d)$	O_{qu}	$(\bar{q}\gamma_\mu q)(\bar{u}\gamma_\mu u)$
O_{quqd}	$(\bar{q}^j u)\epsilon_{jk}(\bar{q}^k d)$	O_{ud}	$(\bar{u}\gamma_\mu u)(\bar{d}\gamma_\mu d)$	O'_{qu}	$(\bar{q}\gamma_\mu T^a q)(\bar{u}\gamma_\mu T^a u)$
O'_{quqd}	$(\bar{q}^j T^a u)\epsilon_{jk}(\bar{q}^k T^a d)$	O'_{ud}	$(\bar{u}\gamma_\mu T^a u)(\bar{d}\gamma_\mu T^a d)$	O_{qd}	$(\bar{q}\gamma_\mu q)(\bar{d}\gamma_\mu d)$
$O_{\ell equ}$	$(\bar{\ell}^j e)\epsilon_{jk}(\bar{q}^k u)$			O'_{qd}	$(\bar{q}\gamma_\mu T^a q)(\bar{d}\gamma_\mu T^a d)$
$O'_{\ell equ}$	$(\bar{\ell}^j\sigma_{\mu\nu}e)\epsilon_{jk}(\bar{q}^k\sigma^{\mu\nu}u)$				
$O_{\ell edq}$	$(\bar{\ell}^j e)(\bar{d}q^j)$				

h-basis

- ◆ Connection between operators and observables a bit obscured in Warsaw or SILH basis. Also, in Warsaw basis EW precision constraints look complicated
- ◆ h-basis proposed by LHCHXSWG2 to separate combinations of Wilson coefficients strongly constrained by EWPT from those relevant for LHC Higgs studies
- ◆ Rotation of any other $D=6$ basis such that one isolates linear combinations affecting Higgs observables and not constrained severely by precision tests



- h-basis is defined via effective Lagrangian of mass eigenstates after electroweak symmetry breaking (photon, W, Z, Higgs boson, top). SU(3) x SU(2) x U(1) is not manifest but hidden in relations between different couplings
- Feature #1:** In the tree-level Lagrangian, all kinetic terms are canonically normalized, and there's no kinetic mixing between mass eigenstates. In particular, all oblique corrections from new physics are zero, except for a correction to the W boson mass

$$\mathcal{L}_{\text{kin}} = -\frac{1}{2}W_{\mu\nu}^+W_{\mu\nu}^- - \frac{1}{4}Z_{\mu\nu}Z_{\mu\nu} - \frac{1}{4}A_{\mu\nu}A_{\mu\nu} + (1 + 2\delta m)m_W^2W_\mu^+W_\mu^- + \frac{m_Z^2}{2}Z_\mu Z_\mu$$

- Feature #2:** Tree-level relation between the couplings in the Lagrangian and SM input observables is the same as in the SM. In particular, photon and gluon couple as in SM, and there's no correction to Z mass term
- Features #1 and #2 can always be obtained **without any loss of generality**, via integration by parts, fields and couplings redefinition

$$m_Z = \frac{\sqrt{g_L^2 + g_Y^2}v}{2}$$

$$\alpha = \frac{g_L g_Y}{\sqrt{g_L^2 + g_Y^2}}$$

$$\tau_\mu = \frac{384\pi^3 v^4}{m_\mu^5}$$

h-Basis: Z and W couplings to fermions

- By construction, photon and gluon couplings as in the SM. Only W and Z couplings are affected

$$\mathcal{L} \supset \frac{g_L g_Y}{\sqrt{g_L^2 + g_Y^2}} Q_f A_\mu \bar{f} \gamma_\mu f + g_s G_\mu^a \bar{q} \gamma_\mu T^a q$$

- Effects of dimension-6 operators are parametrized by a set of **vertex corrections**

Independent : $\delta g_L^{Ze}, \delta g_R^{Ze}, \delta g_L^{W\ell}, \delta g_L^{Zu}, \delta g_R^{Zu}, \delta g_L^{Zd}, \delta g_R^{Zd}, \delta g_R^{Wq}$

Dependent : $\delta g_L^{Z\nu}, \delta g_L^{Wq}$

$$\mathcal{L}_{vff} = \frac{g_L}{\sqrt{2}} \left(W_\mu^+ \bar{u} \bar{\sigma}_\mu (V_{CKM} + \delta g_L^{Wq}) d + W_\mu^+ u^c \sigma_\mu \delta g_R^{Wq} \bar{d}^c + W_\mu^+ \bar{\nu} \bar{\sigma}_\mu (I + \delta g_L^{W\ell}) e + \text{h.c.} \right) + \sqrt{g_L^2 + g_Y^2} Z_\mu \left[\sum_{f \in u, d, e, \nu} \bar{f} \bar{\sigma}_\mu (T_f^3 - s_\theta^2 Q_f + \delta g_L^{Zf}) f + \sum_{f^c \in u^c, d^c, e^c} f^c \sigma_\mu (-s_\theta^2 Q_f + \delta g_R^{Zf}) \bar{f}^c \right]$$

Dependent Couplings:

Relations enforced by linearly realized SU(3) x SU(2) x U(1) symmetry at the level of dimension-6 operators

$$\delta g_L^{Z\nu} = \delta g_L^{Ze} + \delta g_L^{W\ell}$$

$$\delta g_L^{Wq} = \delta g_L^{Zu} V_{CKM} - V_{CKM} \delta g_L^{Zd}$$

h-Basis: Higgs couplings to matter

In HB, Higgs couplings to gauge bosons described by 6 CP even and 4 CP odd parameters that are unconstrained by LEP-1

D=6 EFT with linearly realized SU(3)xSU(2)xU(1) enforces relations between Higgs couplings to gauge bosons (otherwise, more parameters)

Corrections to Higgs Yukawa couplings to fermions are also unconstrained by EWPT

Apart from δm and δg , additional 6+3x3x3 CP-even and 4+3x3x3 CP-odd parameters to parametrize LHC Higgs physics

CP even : δc_z $c_{z\Box}$ c_{zz} $c_{z\gamma}$ $c_{\gamma\gamma}$ c_{gg}
 CP odd : \tilde{c}_{zz} $\tilde{c}_{z\gamma}$ $\tilde{c}_{\gamma\gamma}$ \tilde{c}_{gg}

$$\mathcal{L}_{\text{hvv}} = \frac{h}{v} [2(1 + \delta c_w) m_W^2 W_\mu^+ W_\mu^- + (1 + \delta c_z) m_Z^2 Z_\mu Z_\mu + c_{ww} \frac{g_L^2}{2} W_{\mu\nu}^+ W_{\mu\nu}^- + \tilde{c}_{ww} \frac{g_L^2}{2} W_{\mu\nu}^+ \tilde{W}_{\mu\nu}^- + c_{w\Box} g_L^2 (W_\mu^- \partial_\nu W_{\mu\nu}^+ + \text{h.c.}) + c_{gg} \frac{g_s^2}{4} G_{\mu\nu}^a G_{\mu\nu}^a + c_{\gamma\gamma} \frac{e^2}{4} A_{\mu\nu} A_{\mu\nu} + c_{z\gamma} \frac{eg_L}{2c_\theta} Z_{\mu\nu} A_{\mu\nu} + c_{zz} \frac{g_L^2}{4c_\theta^2} Z_{\mu\nu} Z_{\mu\nu} + c_{z\Box} g_L^2 Z_\mu \partial_\nu Z_{\mu\nu} + c_{\gamma\Box} g_L g_Y Z_\mu \partial_\nu A_{\mu\nu} + \tilde{c}_{gg} \frac{g_s^2}{4} G_{\mu\nu}^a \tilde{G}_{\mu\nu}^a + \tilde{c}_{\gamma\gamma} \frac{e^2}{4} A_{\mu\nu} \tilde{A}_{\mu\nu} + \tilde{c}_{z\gamma} \frac{eg_L}{2c_\theta} Z_{\mu\nu} \tilde{A}_{\mu\nu} + \tilde{c}_{zz} \frac{g_L^2}{4c_\theta^2} Z_{\mu\nu} \tilde{Z}_{\mu\nu}]$$

$\delta c_w = \delta c_z + 4\delta m$ ← relative correction to W mass

$$c_{ww} = c_{zz} + 2s_\theta^2 c_{z\gamma} + s_\theta^4 c_{\gamma\gamma}$$

$$\tilde{c}_{ww} = \tilde{c}_{zz} + 2s_\theta^2 \tilde{c}_{z\gamma} + s_\theta^4 \tilde{c}_{\gamma\gamma}$$

$$c_{w\Box} = \frac{1}{g_L^2 - g_Y^2} [g_L^2 c_{z\Box} + g_Y^2 c_{zz} - e^2 s_\theta^2 c_{\gamma\gamma} - (g_L^2 - g_Y^2) s_\theta^2 c_{z\gamma}]$$

$$c_{\gamma\Box} = \frac{1}{g_L^2 - g_Y^2} [2g_L^2 c_{z\Box} + (g_L^2 + g_Y^2) c_{zz} - e^2 c_{\gamma\gamma} - (g_L^2 - g_Y^2) c_{z\gamma}]$$

LHCHXSWG-INT-2015-001

CP even : δy_u δy_d δy_e
 CP odd : ϕ_u ϕ_d ϕ_e

$$\mathcal{L}_{\text{hff}} = - \sum_{f=u,d,e} m_f f^c (I + \delta y_f e^{i\phi_f}) f + \text{h.c.}$$

h-basis: Triple Gauge Couplings

SM predicts TGCs in terms of gauge couplings
as consequence of SM gauge symmetry and renormalizability:

$$\mathcal{L}_{\text{TGC}}^{\text{SM}} = ie \left[A_{\mu\nu} W_{\mu}^{+} W_{\nu}^{-} + (W_{\mu\nu}^{+} W_{\mu}^{-} - W_{\mu\nu}^{-} W_{\mu}^{+}) A_{\nu} \right] \\ + ig_L c_{\theta} \left[(W_{\mu\nu}^{+} W_{\mu}^{-} - W_{\mu\nu}^{-} W_{\mu}^{+}) Z_{\nu} + Z_{\mu\nu} W_{\mu}^{+} W_{\nu}^{-} \right]$$

In EFT with D=6 operators, new "anomalous" contributions to TGCs arise

$$\mathcal{L}_{\text{tgc}}^{D=6} = ie \left[\delta\kappa_{\gamma} A_{\mu\nu} W_{\mu}^{+} W_{\nu}^{-} + \tilde{\kappa}_{\gamma} \tilde{A}_{\mu\nu} W_{\mu}^{+} W_{\nu}^{-} \right] \\ + ig_L c_{\theta} \left[\delta g_{1,z} (W_{\mu\nu}^{+} W_{\mu}^{-} - W_{\mu\nu}^{-} W_{\mu}^{+}) Z_{\nu} + \delta\kappa_z Z_{\mu\nu} W_{\mu}^{+} W_{\nu}^{-} + \tilde{\kappa}_z \tilde{Z}_{\mu\nu} W_{\mu}^{+} W_{\nu}^{-} \right] \\ + i \frac{e}{m_W^2} \left[\lambda_{\gamma} W_{\mu\nu}^{+} W_{\nu\rho}^{-} A_{\rho\mu} + \tilde{\lambda}_{\gamma} W_{\mu\nu}^{+} W_{\nu\rho}^{-} \tilde{A}_{\rho\mu} \right] + i \frac{g_L c_{\theta}}{m_W^2} \left[\lambda_z W_{\mu\nu}^{+} W_{\nu\rho}^{-} Z_{\rho\mu} + \tilde{\lambda}_z W_{\mu\nu}^{+} W_{\nu\rho}^{-} \tilde{Z}_{\rho\mu} \right]$$

These depend on previously introduced h-basis
parameters describing Higgs couplings to
electroweak gauge bosons, and on 2 new parameters

CP – even : λ_z
CP – odd : $\tilde{\lambda}_z$

$$\delta g_{1,z} = \frac{1}{2(g_L^2 - g_Y^2)} \left[c_{\gamma\gamma} e^2 g_Y^2 + c_{z\gamma} (g_L^2 - g_Y^2) g_Y^2 - c_{zz} (g_L^2 + g_Y^2) g_Y^2 - c_{z\Box} (g_L^2 + g_Y^2) g_L^2 \right] \\ \delta\kappa_{\gamma} = - \frac{g_L^2}{2} \left(c_{\gamma\gamma} \frac{e^2}{g_L^2 + g_Y^2} + c_{z\gamma} \frac{g_L^2 - g_Y^2}{g_L^2 + g_Y^2} - c_{zz} \right), \quad \delta\kappa_z = \delta g_{1,z} - t_{\theta}^2 \delta\kappa_{\gamma} \\ \tilde{\kappa}_{\gamma} = - \frac{g_L^2}{2} \left(\tilde{c}_{\gamma\gamma} \frac{e^2}{g_L^2 + g_Y^2} + \tilde{c}_{z\gamma} \frac{g_L^2 - g_Y^2}{g_L^2 + g_Y^2} - \tilde{c}_{zz} \right), \quad \tilde{\kappa}_z = - t_{\theta}^2 \tilde{\kappa}_{\gamma} \\ \lambda_{\gamma} = \lambda_z \\ \tilde{\lambda}_{\gamma} = \tilde{\lambda}_z$$

For more details and the rest of the Lagrangian, see [LHCHXSWG-INT-2015-001](#)

In the rest of the talk I will discuss constraints on the parameters in the h -basis

Model-independent
precision constraints
on dimension 6 operators

Analysis Assumptions

- Working **at order $1/\Lambda^2$** in EFT expansion. Taking into account corrections from D=6 operators, and neglecting D=8 and higher operators. (Only taking into account corrections to observables that are linear in h-basis parameters, that is to say, only interference terms between SM and new physics. Quadratic corrections are formally of order $1/\Lambda^4$, much as D=8 operators that are neglected.)
- Working at **tree-level** in EFT parameters (SM predictions taken at NLO or NNLO, but only interference of tree-level BSM corrections with tree-level SM amplitude taken into account)
- Except on las slide, restrict to observables that **do not depend on 4-fermion operators** (they are **not** neglected – just do not contribute at tree-level; constraints on 4-fermion operators left for future work)
- Allowing **all dimension-6 operators to be present** simultaneously with arbitrary coefficients (within EFT validity range). Constraints are obtained on all parameters affecting EWPT and Higgs at tree level, and correlations matrix is computed.
- Unless otherwise noted, dimension-6 operators are allowed with arbitrary flavor structure

Han, Skiba
hep-ph/0412166

Efrati, AA, Soreq
1503.07782

Constraints on Vertex Corrections from Pole Observables

Pole observables (LEP-1 et al)

- For observables with Z or W bosons on-shell, interference between SM amplitudes and 4-fermion operators is suppressed by Γ/m and can be neglected
- Corrections from dimension-6 Lagrangian to pole observables can be expressed just by vertex corrections δg and W mass correction δm
- I will not assume anything about δg : they are allowed to be arbitrary, flavor dependent, and all can be simultaneously present

$$\mathcal{L}_{vff} = \frac{g_L}{\sqrt{2}} \left(W_\mu^+ \bar{u} \bar{\sigma}_\mu (V_{CKM} + \delta g_L^{Wq}) d + W_\mu^+ u^c \sigma_\mu \delta g_R^{Wq} \bar{d}^c + W_\mu^+ \bar{\nu} \bar{\sigma}_\mu (I + \delta g_L^{W\ell}) e + \text{h.c.} \right)$$

$$+ \sqrt{g_L^2 + g_Y^2} Z_\mu \left[\sum_{f \in u, d, e, \nu} \bar{f} \bar{\sigma}_\mu (T_f^3 - s_\theta^2 Q_f + \delta g_L^{Zf}) f + \sum_{f^c \in u^c, d^c, e^c} f^c \sigma_\mu (-s_\theta^2 Q_f + \delta g_R^{Zf}) \bar{f}^c \right]$$

On-shell Z decays: nuts and bolts

Lowest order:

$$\Gamma(Z \rightarrow f\bar{f}) = \frac{N_f m_Z}{24\pi} g_{fZ}^2 \quad g_{fZ} = \sqrt{g_L^2 + g_Y^2} (T_f^3 - s_\theta^2 Q_f)$$

$$\Gamma(W \rightarrow f\bar{f}') = \frac{N_f m_W}{48\pi} g_{fW,L}^2 \quad g_{fW,L} = g_L$$

w/ new physics:

$$\Gamma(Z \rightarrow f\bar{f}) = \frac{N_f m_Z}{24\pi} g_{fZ;\text{eff}}^2 \quad \Gamma(W \rightarrow f\bar{f}') = \frac{N_f m_W}{48\pi} g_{fW,L;\text{eff}}^2$$

- Including leading order new physics corrections amount to replacing Z coupling to fermions with effective couplings
- These effective couplings encode the effect of **vertex** and **oblique** corrections
- Shift of the effective couplings in the presence of dimension-6 operators allows one to read off the dependence of observables on dimension-6 operators
- In general, pole observables constrain complicated combinations of coefficients of dimension-6 operators
- However, in h-basis, oblique corrections are absent (except for δm) thus δg directly constrained

$$g_{fW,L;\text{eff}} = \frac{g_{L0}}{\sqrt{1 - \delta\Pi'_{WW}(m_W^2)}} (1 + \delta g_L^{Wf})$$

$$g_{fZ;\text{eff}} = \frac{\sqrt{g_{L0}^2 + g_{Y0}^2}}{\sqrt{1 - \delta\Pi'_{ZZ}(m_Z^2)}} (T_f^3 - s_{\text{eff}}^2 Q_f + \delta g^{Zf})$$

$$s_{\text{eff}}^2 = \frac{g_{Y0}^2}{g_{L0}^2 + g_{Y0}^2} \left(1 - \frac{g_L}{g_Y} \frac{\delta\Pi_{\gamma Z}(m_Z^2)}{m_Z^2} \right)$$

$$g_{fW,L;\text{eff}} = g_L (1 + \delta g_L^{Wf})$$

$$g_{fZ;\text{eff}} = \sqrt{g_L^2 + g_Y^2} (T_f^3 - s_\theta^2 Q_f + \delta g^{Zf})$$

Z-pole observables

Observable	Experimental value	Ref.	SM prediction	Definition
Γ_Z [GeV]	2.4952 ± 0.0023	[21]	2.4950	$\sum_f \Gamma(Z \rightarrow ff)$
σ_{had} [nb]	41.541 ± 0.037	[21]	41.484	$\frac{12\pi}{m_Z^2} \frac{\Gamma(Z \rightarrow e^+e^-)\Gamma(Z \rightarrow q\bar{q})}{\Gamma_Z^2}$
R_e	20.804 ± 0.050	[21]	20.743	$\frac{\sum_q \Gamma(Z \rightarrow q\bar{q})}{\Gamma(Z \rightarrow e^+e^-)}$
R_μ	20.785 ± 0.033	[21]	20.743	$\frac{\sum_q \Gamma(Z \rightarrow q\bar{q})}{\Gamma(Z \rightarrow \mu^+\mu^-)}$
R_τ	20.764 ± 0.045	[21]	20.743	$\frac{\sum_q \Gamma(Z \rightarrow q\bar{q})}{\Gamma(Z \rightarrow \tau^+\tau^-)}$
$A_{\text{FB}}^{0,e}$	0.0145 ± 0.0025	[21]	0.0163	$\frac{3}{4} A_e^2$
$A_{\text{FB}}^{0,\mu}$	0.0169 ± 0.0013	[21]	0.0163	$\frac{3}{4} A_e A_\mu$
$A_{\text{FB}}^{0,\tau}$	0.0188 ± 0.0017	[21]	0.0163	$\frac{3}{4} A_e A_\tau$
R_b	0.21629 ± 0.00066	[21]	0.21578	$\frac{\Gamma(Z \rightarrow b\bar{b})}{\sum_q \Gamma(Z \rightarrow q\bar{q})}$
R_c	0.1721 ± 0.0030	[21]	0.17226	$\frac{\Gamma(Z \rightarrow c\bar{c})}{\sum_q \Gamma(Z \rightarrow q\bar{q})}$
A_b^{FB}	0.0992 ± 0.0016	[21]	0.1032	$\frac{3}{4} A_e A_b$
A_c^{FB}	0.0707 ± 0.0035	[21]	0.0738	$\frac{3}{4} A_e A_c$
A_e	0.1516 ± 0.0021	[21]	0.1472	$\frac{\Gamma(Z \rightarrow e_L^+e_L^-) - \Gamma(Z \rightarrow e_R^+e_R^-)}{\Gamma(Z \rightarrow e^+e^-)}$
A_μ	0.142 ± 0.015	[21]	0.1472	$\frac{\Gamma(Z \rightarrow \mu_L^+\mu_L^-) - \Gamma(Z \rightarrow \mu_R^+\mu_R^-)}{\Gamma(Z \rightarrow \mu^+\mu^-)}$
A_τ	0.136 ± 0.015	[21]	0.1472	$\frac{\Gamma(Z \rightarrow \tau_L^+\tau_L^-) - \Gamma(Z \rightarrow \tau_R^+\tau_R^-)}{\Gamma(Z \rightarrow \tau^+\tau^-)}$
A_b	0.923 ± 0.020	[21]	0.935	$\frac{\Gamma(Z \rightarrow b_L b_L) - \Gamma(Z \rightarrow b_R b_R)}{\Gamma(Z \rightarrow b\bar{b})}$
A_c	0.670 ± 0.027	[21]	0.668	$\frac{\Gamma(Z \rightarrow c_L \bar{c}_L) - \Gamma(Z \rightarrow c_R \bar{c}_R)}{\Gamma(Z \rightarrow c\bar{c})}$
A_s	0.895 ± 0.091	[22]	0.935	$\frac{\Gamma(Z \rightarrow s_L \bar{s}_L) - \Gamma(Z \rightarrow s_R \bar{s}_R)}{\Gamma(Z \rightarrow s\bar{s})}$
R_{uc}	0.166 ± 0.009	[23]	0.1724	$\frac{\Gamma(Z \rightarrow u\bar{u}) + \Gamma(Z \rightarrow c\bar{c})}{2 \sum_q \Gamma(Z \rightarrow q\bar{q})}$

Table 1: **Z boson pole observables.** The experimental errors of the observables between the double lines are correlated, which is taken into account in the fit. The results for $A_{e,\mu,\tau}$ listed above come from the combination of leptonic polarization and left-right asymmetry measurements at the SLD; we also include the results $A_\tau = 0.1439 \pm 0.0043$, $A_e = 0.1498 \pm 0.0049$ from tau polarization measurements at LEP-1 [21]. For the theoretical predictions we use the best fit SM values from GFitter [20]. We also include the model-independent measurement of on-shell Z boson couplings to light quarks in D0 [26].

W-pole observables

Observable	Experimental value	Ref.	SM prediction	Definition
m_W [GeV]	80.385 ± 0.015	[27]	80.364	$\frac{g_L v}{2} (1 + \delta m)$
Γ_W [GeV]	2.085 ± 0.042	[23]	2.091	$\sum_f \Gamma(W \rightarrow f f')$
$\text{Br}(W \rightarrow e\nu)$	0.1071 ± 0.0016	[28]	0.1083	$\frac{\Gamma(W \rightarrow e\nu)}{\sum_f \Gamma(W \rightarrow f f')}$
$\text{Br}(W \rightarrow \mu\nu)$	0.1063 ± 0.0015	[28]	0.1083	$\frac{\Gamma(W \rightarrow \mu\nu)}{\sum_f \Gamma(W \rightarrow f f')}$
$\text{Br}(W \rightarrow \tau\nu)$	0.1138 ± 0.0021	[28]	0.1083	$\frac{\Gamma(W \rightarrow \tau\nu)}{\sum_f \Gamma(W \rightarrow f f')}$
R_{Wc}	0.49 ± 0.04	[23]	0.50	$\frac{\Gamma(W \rightarrow cs)}{\Gamma(W \rightarrow ud) + \Gamma(W \rightarrow cs)}$
R_σ	0.998 ± 0.041	[29]	1.000	$g_L^{Wq3} / g_{L,SM}^{Wq3}$

Table 2: **W-boson pole observables.** Measurements of the 3 leptonic branching fractions are correlated. For the theoretical predictions of m_W and Γ_W , we use the best fit SM values from GFitter [20], while for the leptonic branching fractions we take the value quoted in [28].

Pole observables - constraints

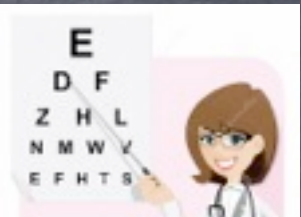
Efrati,AA,Soreq
1503.07872

All diagonal vertex corrections except for δg_{WqR} and δg_{ZtR} simultaneously constrained in a completely model-independent way

$$\begin{aligned} [\delta g_L^{We}]_{ii} &= \begin{pmatrix} -1.00 \pm 0.64 \\ -1.36 \pm 0.59 \\ 1.95 \pm 0.79 \end{pmatrix} \times 10^{-2}, \\ [\delta g_L^{Ze}]_{ii} &= \begin{pmatrix} -0.26 \pm 0.28 \\ 0.1 \pm 1.1 \\ 0.16 \pm 0.58 \end{pmatrix} \times 10^{-3}, & [\delta g_R^{Ze}]_{ii} &= \begin{pmatrix} -0.37 \pm 0.27 \\ 0.0 \pm 1.3 \\ 0.39 \pm 0.62 \end{pmatrix} \times 10^{-3}, \\ [\delta g_L^{Zu}]_{ii} &= \begin{pmatrix} -0.8 \pm 3.1 \\ -0.16 \pm 0.36 \\ -0.28 \pm 3.8 \end{pmatrix} \times 10^{-2}, & [\delta g_R^{Zu}]_{ii} &= \begin{pmatrix} 1.3 \pm 5.1 \\ -0.38 \pm 0.51 \\ \times \end{pmatrix} \times 10^{-2}, \\ \delta m &= (2.6 \pm 1.9) \cdot 10^{-4}. & [\delta g_L^{Zd}]_{ii} &= \begin{pmatrix} -1.0 \pm 4.4 \\ 0.9 \pm 2.8 \\ 0.33 \pm 0.16 \end{pmatrix} \times 10^{-2}, & [\delta g_R^{Zd}]_{ii} &= \begin{pmatrix} 2.9 \pm 16 \\ 3.5 \pm 5.0 \\ 2.30 \pm 0.82 \end{pmatrix} \times 10^{-2}. \end{aligned}$$

- Z coupling to charged leptons constrained at 0.1% level
- W couplings to leptons constrained at 1% level
- Some couplings to quarks (bottom, charm) also constrained at 1% level
- Some couplings very weakly constrained in a model-independent way, in particular Z couplings to light quarks (though their combination affecting *total* hadronic Z-width is strongly constrained)
- Some off-diagonal vertex corrections can also be constrained

Pole constraints - correlations



1.	0.12	-0.63	-0.1	0.04	0.01	0.08	-0.04	-0.24	-0.02	0.	0.	-0.03	0.01	0.	-0.02	-0.03	0.02	-0.05	0.03	0.
-0.12	1.	-0.56	-0.13	0.05	0.01	0.08	-0.07	-0.24	-0.02	0.	0.	-0.03	0.01	0.	-0.02	-0.03	0.02	-0.05	0.04	0.
-0.63	-0.56	1.	-0.1	-0.04	0.01	0.07	-0.06	-0.24	0.01	-0.01	0.	0.02	-0.01	0.	0.01	0.03	0.02	0.04	0.03	0.01
-0.1	-0.13	-0.1	1.	-0.08	-0.07	0.15	-0.04	0.24	0.02	0.1	-0.02	0.03	0.09	-0.01	0.02	0.03	-0.06	0.05	0.03	-0.35
-0.04	0.05	-0.04	-0.08	1.	0.06	-0.04	0.91	-0.24	0.	-0.02	0.	0.	-0.03	0.	0.	0.01	0.07	0.01	0.	0.04
0.01	0.01	0.01	-0.07	0.06	1.	0.02	-0.03	0.41	-0.01	-0.03	0.	-0.01	0.01	0.	0.	0.	0.07	-0.01	-0.01	0.01
0.08	0.08	0.07	0.15	-0.04	0.02	1.	-0.06	-0.24	-0.01	0.09	-0.02	-0.01	0.12	-0.01	-0.01	-0.01	-0.04	-0.02	-0.01	-0.38
-0.06	-0.07	-0.06	-0.04	0.01	-0.03	-0.06	1.	0.04	0.01	0.	0.	0.01	-0.02	0.	0.01	0.01	0.01	0.02	0.02	0.03
-0.04	0.04	-0.04	0.04	-0.04	0.41	-0.04	0.04	1.	0.01	0.02	0.	0.01	-0.01	0.	0.01	0.01	-0.05	0.02	0.02	0.
-0.02	-0.02	0.01	0.02	0.	-0.01	-0.01	0.01	0.02	1.	-0.04	0.	0.73	0.05	0.	0.79	-0.06	-0.01	0.76	-0.12	0.
0.	0.	-0.01	0.1	-0.02	-0.03	0.09	0.	0.02	-0.04	1.	-0.01	0.03	0.41	0.	-0.03	0.09	-0.15	0.04	0.03	-0.18
0.	0.	0.	-0.02	0.	0.	-0.02	0.	0.	0.	-0.01	1.	0.	-0.03	0.6	0.	0.	0.04	0.	0.	0.04
-0.03	0.03	0.02	0.03	0.	-0.01	-0.01	0.01	0.01	0.73	0.03	0.	1.	0.03	0.	0.75	-0.21	-0.01	-0.02	-0.16	-0.01
0.01	0.01	-0.01	0.09	-0.01	0.01	0.12	-0.02	-0.01	0.05	0.41	-0.01	0.03	1.	0.	0.03	0.04	-0.18	0.07	0.04	-0.16
0.	0.	0.	-0.01	0.	0.	-0.01	0.	0.	0.	0.	0.	0.6	0.	0.	1.	0.	0.	0.03	0.	0.02
-0.02	-0.02	0.01	0.02	0.	0.	-0.01	0.01	0.01	0.79	-0.03	0.	0.71	0.03	0.	1.	-0.62	-0.01	0.67	0.01	0.
-0.03	0.03	0.03	0.03	0.01	0.	-0.01	0.01	0.01	-0.06	0.09	0.	-0.21	0.04	0.	-0.62	1.	-0.02	-0.03	-0.03	-0.02
0.02	0.02	0.02	-0.16	0.07	0.07	-0.14	0.01	-0.05	-0.01	-0.15	0.04	-0.01	-0.18	0.03	-0.01	-0.02	1.	-0.02	-0.02	0.01
-0.05	-0.05	0.04	0.05	0.01	-0.01	-0.02	0.02	0.02	0.76	0.04	0.	0.92	0.07	0.	0.67	-0.03	-0.02	1.	-0.32	-0.02
-0.03	-0.04	0.03	0.03	0.	-0.01	-0.01	0.02	0.02	-0.12	0.03	0.	-0.15	0.04	0.	0.01	-0.03	-0.02	-0.32	1.	-0.01
0.	0.	0.01	-0.15	0.04	0.01	-0.18	0.03	0.	0.	-0.18	0.04	0.01	-0.16	0.02	0.	0.02	0.01	-0.02	0.01	1.

- Full correlation matrix is also derived
- From that, one can reproduce **full likelihood function** as function of 21 parameters δg and δm
- If dictionary from h-basis to other bases exists, results can be easily recast to another form
- Similarly, when mapping to d=6 basis from (fewer) parameters of particular BSM models is given, results can be easily recast as constraints on that model

$$\chi_{\text{pole}}^2 = \sum_{ij} (\delta g_i - \delta g_i^0) \Delta_{ij}^{-1} (\delta g_j - \delta g_j^0),$$

$$\Delta_{ij} = \delta g_i^{\text{err}} \rho_{ij} \delta g_j^{\text{err}}$$

Correlation Matrix

1 σ Errors

Central Values

Pole constraints - recast to Warsaw basis

Results

$$[\hat{c}'_{H\ell}]_{ii} = \begin{pmatrix} -1.09 \pm 0.64 \\ -1.45 \pm 0.59 \\ 1.87 \pm 0.79 \end{pmatrix} \times 10^{-2}, \quad [\hat{c}_{H\ell}]_{ii} = \begin{pmatrix} 1.03 \pm 0.63 \\ 1.32 \pm 0.62 \\ -2.01 \pm 0.80 \end{pmatrix} \times 10^{-2},$$

$$[\hat{c}_{He}]_{ii} = \begin{pmatrix} 0.22 \pm 0.66 \\ -0.6 \pm 2.6 \\ -1.4 \pm 1.3 \end{pmatrix} \times 10^{-3}, \quad c'_{\ell\ell} = (-1.21 \pm 0.41) \times 10^{-2},$$

$$[\hat{c}'_{Hq}]_{ii} = \begin{pmatrix} 0.1 \pm 2.7 \\ -1.2 \pm 2.8 \\ -0.7 \pm 3.8 \end{pmatrix} \times 10^{-2}, \quad [\hat{c}_{Hq}]_{ii} = \begin{pmatrix} 1.8 \pm 7.0 \\ -0.8 \pm 2.9 \\ 0.0 \pm 3.8 \end{pmatrix} \times 10^{-2},$$

$$[\hat{c}_{Hu}]_{ii} = \begin{pmatrix} -3 \pm 10 \\ 0.8 \pm 1.0 \\ \times \end{pmatrix} \times 10^{-2}, \quad [\hat{c}_{Hd}]_{ii} = \begin{pmatrix} -6 \pm 32 \\ -7 \pm 10 \\ -4.6 \pm 1.6 \end{pmatrix} \times 10^{-2}.$$

$$[\hat{c}'_{H\ell}]_{ij} = [c'_{HL}]_{ij} + \left(g_L^2 c_{WB} - \frac{g_L^2}{g_Y^2} c_T \right) \delta_{ij},$$

$$[\hat{c}_{H\ell}]_{ij} = [c_{HL}]_{ij} - c_T \delta_{ij},$$

$$[\hat{c}_{He}]_{ij} = [c_{HE}]_{ij} - 2c_T \delta_{ij},$$

$$[\hat{c}'_{Hq}]_{ij} = [c'_{HQ}]_{ij} + \left(g_L^2 c_{WB} - \frac{g_L^2}{g_Y^2} c_T \right) \delta_{ij},$$

$$[\hat{c}_{Hq}]_{ij} = [c_{HQ}]_{ij} + \frac{1}{3} c_T \delta_{ij},$$

$$[\hat{c}_{Hu}]_{ij} = [c_{HU}]_{ij} + \frac{4}{3} c_T \delta_{ij},$$

$$[\hat{c}_{Hd}]_{ij} = [c_{HD}]_{ij} - \frac{2}{3} c_T \delta_{ij}.$$

Dictionary

$$\delta g_L^{W\ell} = c'_{H\ell} + f(1/2, 0) - f(-1/2, -1),$$

$$\delta g_L^{Z\nu} = \frac{1}{2} (c'_{H\ell} - c_{H\ell}) + f(1/2, 0),$$

$$\delta g_L^{Ze} = -\frac{1}{2} (c'_{H\ell} + c_{H\ell}) + f(-1/2, -1),$$

$$\delta g_R^{Ze} = -\frac{1}{2} c_{He} + f(0, -1),$$

$$f(T^3, Q) = \mathbb{I} \left[-Q c_{WB} \frac{g_L^2 g_Y^2}{g_L^2 - g_Y^2} + (c_T - \delta v) \left(T^3 + Q \frac{g_Y^2}{g_L^2 - g_Y^2} \right) \right].$$

$$\delta g_L^{Wq} = c'_{Hq} V + f(1/2, 2/3) V - f(-1/2, -1/3) V,$$

$$\delta g_R^{Wq} = c_{Hud},$$

$$\delta g_L^{Zu} = \frac{1}{2} (c'_{Hq} - c_{Hq}) + f(1/2, 2/3),$$

$$\delta g_L^{Zd} = -\frac{1}{2} V^\dagger (c'_{Hq} + c_{Hq}) V + f(-1/2, -1/3),$$

$$\delta g_R^{Zu} = -\frac{1}{2} c_{Hu} + f(0, 2/3),$$

$$\delta g_R^{Zd} = -\frac{1}{2} c_{Hd} + f(0, -1/3).$$

Note in Warsaw basis only combinations of Wilson coefficients are constrained by pole observables

Pole constraints - recast to SILH' basis

Results

$$[s_{\ell\ell}]_{1221} = (4.8 \pm 1.6) \times 10^{-2}, \quad \frac{s_W + s_B}{2} = -0.43 \pm 0.26, \quad s_T = (-1.03 \pm 0.63) \times 10^{-2},$$

$$[s'_{H\ell}]_{ii} = \begin{pmatrix} 0 \\ -0.36 \pm 0.92 \\ 3.0 \pm 1.3 \end{pmatrix} \times 10^{-2}, \quad [s_{H\ell}]_{ii} = \begin{pmatrix} 0 \\ 0.29 \pm 0.95 \\ -3.0 \pm 1.3 \end{pmatrix} \times 10^{-2},$$

$$[s_{He}]_{ii} = \begin{pmatrix} -2.0 \pm 1.3 \\ -2.1 \pm 1.3 \\ -2.2 \pm 1.3 \end{pmatrix} \times 10^{-2},$$

$$[s'_{Hq}]_{ii} = \begin{pmatrix} 1.2 \pm 2.8 \\ -0.1 \pm 2.9 \\ 0.4 \pm 3.8 \end{pmatrix} \times 10^{-2}, \quad [s_{Hq}]_{ii} = \begin{pmatrix} 2.1 \pm 7.1 \\ -0.4 \pm 2.9 \\ 0.3 \pm 3.8 \end{pmatrix} \times 10^{-2},$$

$$[s_{Hu}]_{ii} = \begin{pmatrix} -1 \pm 10 \\ 2.2 \pm 1.3 \\ \times \end{pmatrix} \times 10^{-2}, \quad [s_{Hd}]_{ii} = \begin{pmatrix} -6 \pm 32 \\ -7 \pm 10 \\ -5.3 \pm 1.7 \end{pmatrix} \times 10^{-2}, \quad ($$

In SILH basis pole constraints look simpler,
though important correlations remain, notably between c_W+c_B and leptonic couplings

Pole constraints - flavor blind

$$[\delta g^{Vf}]_{ij} = \delta g^{Vf} \delta_{ij}$$

$$\begin{pmatrix} \delta g_L^{W\ell} \\ \delta g_L^{Ze} \\ \delta g_R^{Ze} \\ \delta g_L^{Zu} \\ \delta g_R^{Zu} \\ \delta g_L^{Zd} \\ \delta g_R^{Zd} \end{pmatrix} = \begin{pmatrix} -0.89 \pm 0.84 \\ -0.20 \pm 0.23 \\ -0.20 \pm 0.24 \\ -1.7 \pm 2.1 \\ -2.3 \pm 4.6 \\ 2.8 \pm 1.5 \\ 19.9 \pm 7.7 \end{pmatrix} \times 10^{-3}$$

- All leptonic couplings constrained at per-mille level, all quark couplings constrained at 1% level or better

Pole constraints - universal theories

Oblique corrections: $\delta\mathcal{M}(V_{1,\mu} \rightarrow V_{2,\nu}) = \eta_{\mu\nu} \left(\delta\Pi_{V_1 V_2}^{(0)} + \delta\Pi_{V_1 V_2}^{(2)} p^2 + \delta\Pi_{V_1 V_2}^{(4)} p^4 + \dots \right) + p_\mu p_\nu (\dots)$

$$\alpha S = -4 \frac{g_L g_Y}{g_L^2 + g_Y^2} \delta\Pi_{3B}^{(2)}$$

$$\alpha T = \frac{\delta\Pi_{11}^{(0)} - \delta\Pi_{33}^{(0)}}{m_W^2}$$

$$\alpha U = \frac{4g_Y^2}{g_L^2 + g_Y^2} \left(\delta\Pi_{11}^{(2)} - \delta\Pi_{33}^{(2)} \right)$$

$$\alpha V = m_W^2 \left(\delta\Pi_{11}^{(4)} - \delta\Pi_{33}^{(4)} \right)$$

$$\alpha W = -m_W^2 \delta\Pi_{33}^{(4)}$$

$$\alpha X = -m_W^2 \delta\Pi_{3B}^{(4)}$$

$$\alpha Y = -m_W^2 \delta\Pi_{BB}^{(4)}$$

Peskin Takeuchi
pre-arxiv

Barbieri et al
hep-ph/0405040

Equivalent to restricted form of flavor-diagonal vertex corrections, W-mass corrections, and 4-fermion operators:

$$[\delta g^{Zf}]_{ij} = \delta_{ij} \alpha \left\{ T_f^3 \frac{2T - W - \frac{g_Y^2}{g_L^2} Y}{4} + Q_f \frac{2g_Y^2 T - (g_L^2 + g_Y^2)S + g_Y^2 W + \frac{g_Y^2(2g_L^2 - g_Y^2)}{g_L^2} Y}{4(g_L^2 - g_Y^2)} \right\}$$

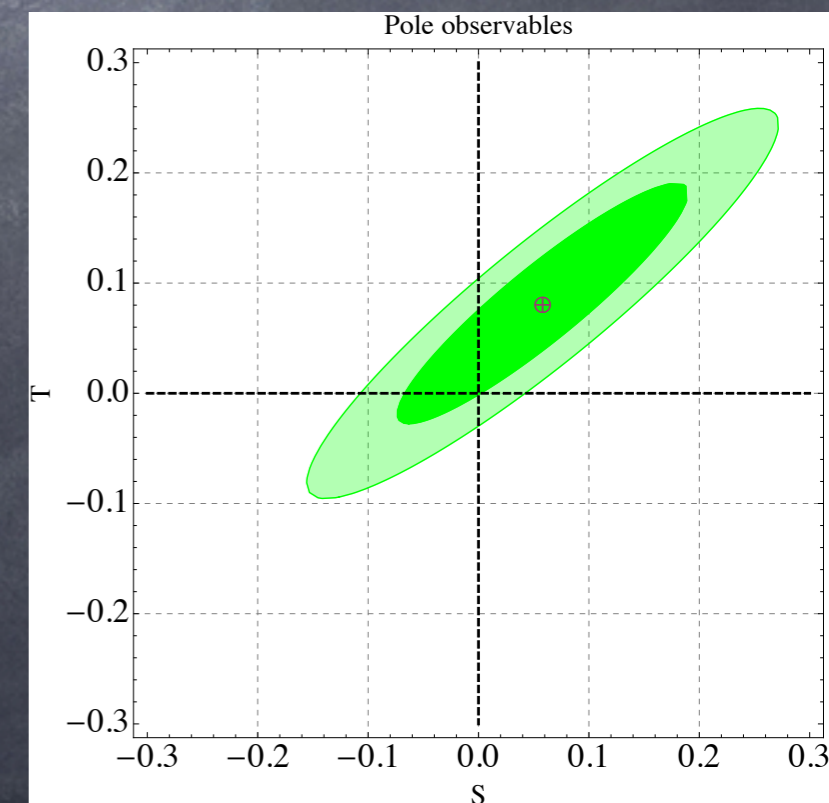
$$\delta m = \frac{\alpha}{4(g_L^2 - g_Y^2)} [2g_L^2 T - (g_L^2 + g_Y^2)S + g_Y^2 W + g_Y^2 Y]$$

$$[c_{\ell\ell}]_{iiii} = -\frac{\alpha}{4} \left[W + \frac{g_Y^2}{g_L^2} Y \right]$$

$$[c_{\ell\ell}]_{iijj} = \frac{\alpha}{2} \left[W - \frac{g_Y^2}{g_L^2} Y \right] \quad i < j$$

$$[c_{\ell\ell}]_{ijji} = -\alpha W \quad i < j$$

Same likelihood for pole observables can be used to constrain up to 3 oblique params



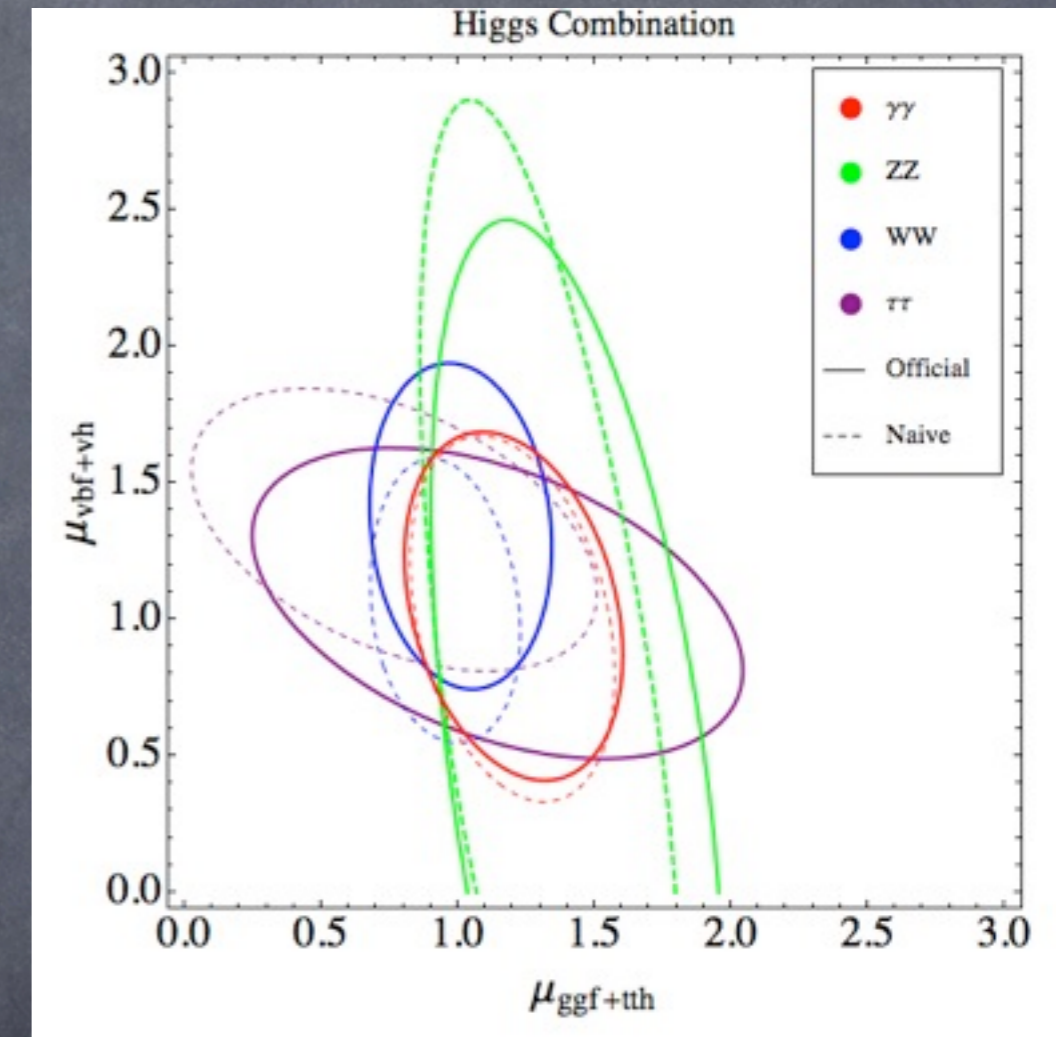
Constraints from LHC Higgs data

Higgs signal strength observables

Channel	μ	Production	Ref.
$\gamma\gamma$	$1.16^{+0.20}_{-0.18}$	2D	[31]
	$1.0^{+1.6}_{-1.6}$	Wh	[34]
	$0.1^{+3.7}_{-0.1}$	Zh	[34]
	$0.58^{+0.93}_{-0.81}$	Vh	[33]
	$1.30^{+2.62}_{-1.75}$ & $2.7^{+2.4}_{-1.7}$	tth	[33, 34]
$Z\gamma$	$2.7^{+4.5}_{-4.3}$ & $-0.2^{+4.9}_{-4.9}$	total	[34, 35]
ZZ^*	$1.31^{+0.27}_{-0.14}$	2D	[31]
WW^*	$1.11^{+0.18}_{-0.17}$	2D	[31]
	$2.1^{+1.9}_{-1.6}$	Wh	[36]
	$5.1^{+4.3}_{-3.1}$	Zh	[36]
	$0.80^{+1.09}_{-0.93}$	Vh	[33]
$\tau\tau$	$1.12^{+0.25}_{-0.23}$	2D	[31]
	$0.87^{+1.00}_{-0.88}$	Vh	[33]
bb	$1.11^{+0.65}_{-0.61}$	Wh	[32]
	$0.05^{+0.52}_{-0.49}$	Zh	[32]
	$0.89^{+0.47}_{-0.44}$	Vh	[33]
	$2.8^{+1.6}_{-1.4}$	VBF	[37]
	$1.5^{+1.1}_{-1.1}$ & $1.2^{+1.6}_{-1.5}$	tth	[38, 39]
$\mu\mu$	$-0.7^{+3.7}_{-3.7}$ & $0.8^{+3.5}_{-3.4}$	total	[34, 40]
multi- ℓ	$2.1^{+1.4}_{-1.2}$ & $3.8^{+1.4}_{-1.4}$	tth	[41, 42]

Including 2D likelihoods from recent ATLAS+CMS combination

ATLAS-CONF-2015-044
CMS-PAS-HIG-15-002



Higgs Basis: Higgs couplings to gauge bosons

$$\begin{array}{l} \text{CP even : } \delta c_z \quad c_{z\Box} \quad c_{zz} \quad c_{z\gamma} \quad c_{\gamma\gamma} \quad c_{gg} \\ \text{CP odd : } \tilde{c}_{zz} \quad \tilde{c}_{z\gamma} \quad \tilde{c}_{\gamma\gamma} \quad \tilde{c}_{gg} \end{array}$$

In Higgs basis, Higgs couplings to gauge bosons are described by 10 parameters

These parameters are observables probed by multiple Higgs production (ggF, VBF, VH) and Higgs decay ($\gamma\gamma$, $Z\gamma$, $VV^* \rightarrow 4f$) processes

Linearly realized $SU(3) \times SU(2) \times U(1)$ with D=6 operators enforces relations between Higgs couplings to gauge bosons (otherwise, 5 more parameters)

$$\begin{aligned} \mathcal{L}_{\text{hvv}} = & \frac{h}{v} [2(1 + \delta c_w) m_W^2 W_\mu^+ W_\mu^- + (1 + \delta c_z) m_Z^2 Z_\mu Z_\mu \\ & + c_{ww} \frac{g_L^2}{2} W_{\mu\nu}^+ W_{\mu\nu}^- + \tilde{c}_{ww} \frac{g_L^2}{2} W_{\mu\nu}^+ \tilde{W}_{\mu\nu}^- + c_{w\Box} g_L^2 (W_\mu^- \partial_\nu W_{\mu\nu}^+ + \text{h.c.}) \\ & + c_{gg} \frac{g_s^2}{4} G_{\mu\nu}^a G_{\mu\nu}^a + c_{\gamma\gamma} \frac{e^2}{4} A_{\mu\nu} A_{\mu\nu} + c_{z\gamma} \frac{eg_L}{2c_\theta} Z_{\mu\nu} A_{\mu\nu} + c_{zz} \frac{g_L^2}{4c_\theta^2} Z_{\mu\nu} Z_{\mu\nu} \\ & + c_{z\Box} g_L^2 Z_\mu \partial_\nu Z_{\mu\nu} + c_{\gamma\Box} g_L g_Y Z_\mu \partial_\nu A_{\mu\nu} \\ & + \tilde{c}_{gg} \frac{g_s^2}{4} G_{\mu\nu}^a \tilde{G}_{\mu\nu}^a + \tilde{c}_{\gamma\gamma} \frac{e^2}{4} A_{\mu\nu} \tilde{A}_{\mu\nu} + \tilde{c}_{z\gamma} \frac{eg_L}{2c_\theta} Z_{\mu\nu} \tilde{A}_{\mu\nu} + \tilde{c}_{zz} \frac{g_L^2}{4c_\theta^2} Z_{\mu\nu} \tilde{Z}_{\mu\nu}] \end{aligned}$$

$$\delta c_w = \delta c_z + 4\delta m,$$

$$c_{ww} = c_{zz} + 2s_\theta^2 c_{z\gamma} + s_\theta^4 c_{\gamma\gamma},$$

$$\tilde{c}_{ww} = \tilde{c}_{zz} + 2s_\theta^2 \tilde{c}_{z\gamma} + s_\theta^4 \tilde{c}_{\gamma\gamma},$$

$$c_{w\Box} = \frac{1}{g_L^2 - g_Y^2} [g_L^2 c_{z\Box} + g_Y^2 c_{zz} - e^2 s_\theta^2 c_{\gamma\gamma} - (g_L^2 - g_Y^2) s_\theta^2 c_{z\gamma}],$$

$$c_{\gamma\Box} = \frac{1}{g_L^2 - g_Y^2} [2g_L^2 c_{z\Box} + (g_L^2 + g_Y^2) c_{zz} - e^2 c_{\gamma\gamma} - (g_L^2 - g_Y^2) c_{z\gamma}]$$

Higgs Basis: Higgs couplings to fermions

- In Higgs basis, Higgs couplings to fermions are described by 3 general complex 3x3 matrices
- Here I will assume MFV couplings, thus reducing number of parameters to 2x3
- Without that assumption, couplings to light fermions are unconstrained, leading to flat directions; their effect on other parameters is similar to adding additional invisible width

$$\begin{array}{l} \text{CP even : } \delta y_u \quad \delta y_d \quad \delta y_e \\ \text{CP odd : } \phi_u \quad \phi_d \quad \phi_e \end{array}$$

$$\Delta \mathcal{L}_{\text{hff}}^{D=6} = -\frac{h}{v} \sum_{f \in u, d, e} \delta y_f e^{i\phi_f} m_f f^c f + \text{h.c.}$$

Other Higgs couplings to fermions (vertex-like, or dipole-like) are constrained to be small by precision observables and cannot affect LHC Higgs observables given the current level of precision

Higgs observables in the Higgs basis

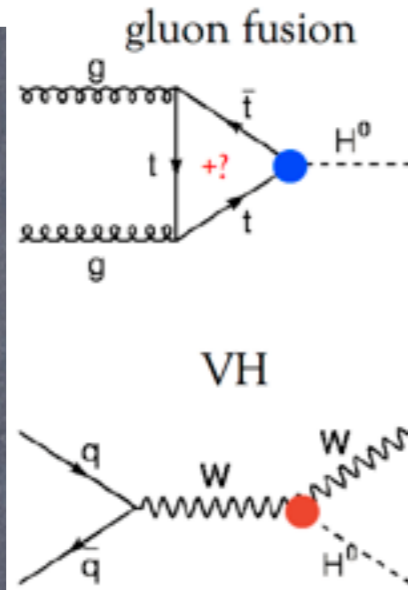
- Higgs signal strength observables at linear level are only sensitive to CP even parameter (CP odd enter only quadratically and are ignored)
- Only couplings unconstrained by precision tests can be relevant at the LHC
- Thus, assuming MFV couplings to fermions, only 9 EFT parameter affect Higgs signal strength measured at LHC

δC_z $C_z \square$ C_{zz} $C_{z\gamma}$ $C_{\gamma\gamma}$ C_{gg} δy_u δy_d δy_e

Higgs production in the Higgs basis

$$\frac{\sigma_{ggh}}{\sigma_{ggh}^{\text{SM}}} \simeq 1 + 237c_{gg} + 2.06\delta y_u - 0.06\delta y_d.$$

$$\begin{aligned} \frac{\sigma_{VBF}}{\sigma_{VBF}^{\text{SM}}} &\simeq 1 + 1.49\delta c_w + 0.51\delta c_z - \begin{pmatrix} 1.08 \\ 1.11 \\ 1.23 \end{pmatrix} c_{w\Box} - 0.10c_{ww} - \begin{pmatrix} 0.35 \\ 0.35 \\ 0.40 \end{pmatrix} c_{z\Box} \\ &\quad - 0.04c_{zz} - 0.10c_{\gamma\Box} - 0.02c_{z\gamma} \\ &\rightarrow 1 + 2\delta c_z - 2.25c_{z\Box} - 0.83c_{zz} + 0.30c_{z\gamma} + 0.12c_{\gamma\gamma}. \end{aligned}$$



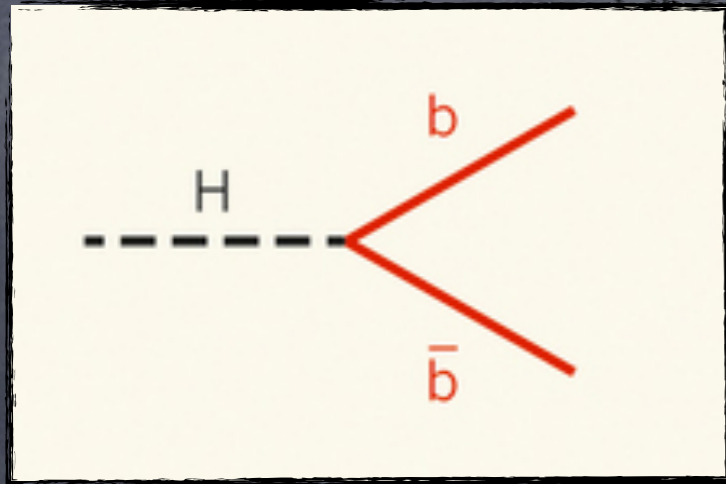
$$\frac{\sigma_{tth}}{\sigma_{tth}^{\text{SM}}} \simeq 1 + 2\delta y_u.$$

$$\begin{aligned} \frac{\sigma_{Wh}}{\sigma_{Wh}^{\text{SM}}} &\simeq 1 + 2\delta c_w + \begin{pmatrix} 6.39 \\ 6.51 \\ 6.96 \end{pmatrix} c_{w\Box} + \begin{pmatrix} 1.49 \\ 1.49 \\ 1.50 \end{pmatrix} c_{ww} \\ &\rightarrow 1 + 2\delta c_z + \begin{pmatrix} 9.26 \\ 9.43 \\ 10.08 \end{pmatrix} c_{z\Box} + \begin{pmatrix} 4.35 \\ 4.41 \\ 4.63 \end{pmatrix} c_{zz} - \begin{pmatrix} 0.81 \\ 0.84 \\ 0.93 \end{pmatrix} c_{z\gamma} - \begin{pmatrix} 0.43 \\ 0.44 \\ 0.48 \end{pmatrix} c_{\gamma\gamma} \\ \frac{\sigma_{Zh}}{\sigma_{Zh}^{\text{SM}}} &\simeq 1 + 2\delta c_z + \begin{pmatrix} 5.30 \\ 5.40 \\ 5.72 \end{pmatrix} c_{z\Box} + \begin{pmatrix} 1.79 \\ 1.80 \\ 1.82 \end{pmatrix} c_{zz} + \begin{pmatrix} 0.80 \\ 0.82 \\ 0.87 \end{pmatrix} c_{\gamma\Box} + \begin{pmatrix} 0.22 \\ 0.22 \\ 0.22 \end{pmatrix} c_{z\gamma}, \\ &\rightarrow 1 + 2\delta c_z + \begin{pmatrix} 7.61 \\ 7.77 \\ 8.24 \end{pmatrix} c_{z\Box} + \begin{pmatrix} 3.31 \\ 3.35 \\ 3.47 \end{pmatrix} c_{zz} - \begin{pmatrix} 0.58 \\ 0.60 \\ 0.65 \end{pmatrix} c_{z\gamma} + \begin{pmatrix} 0.27 \\ 0.28 \\ 0.30 \end{pmatrix} c_{\gamma\gamma}. \end{aligned}$$

$\begin{pmatrix} 7 \\ 8 \\ 13 \end{pmatrix}$ TeV

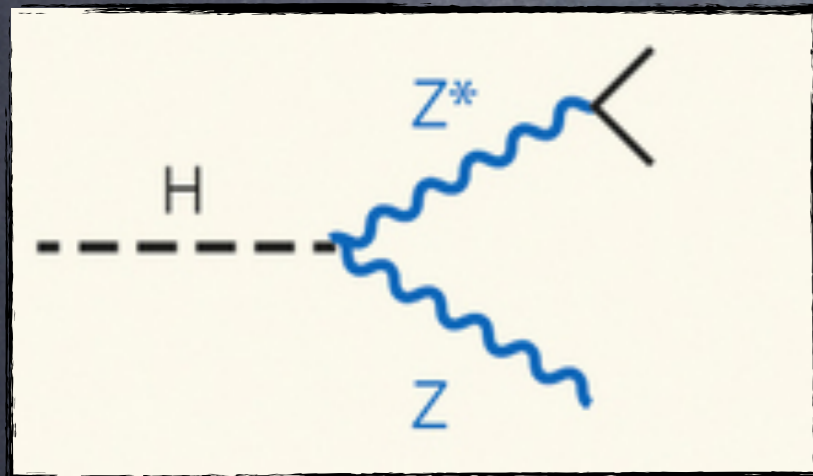
Higgs decay in the Higgs basis

Decays to 2 fermions



$$\frac{\Gamma_{cc}}{\Gamma_{cc}^{\text{SM}}} \simeq 1 + 2\delta y_u, \quad \frac{\Gamma_{bb}}{\Gamma_{bb}^{\text{SM}}} \simeq 1 + 2\delta y_d, \quad \frac{\Gamma_{\tau\tau}}{\Gamma_{\tau\tau}^{\text{SM}}} \simeq 1 + 2\delta y_e,$$

Decays to 4 fermions



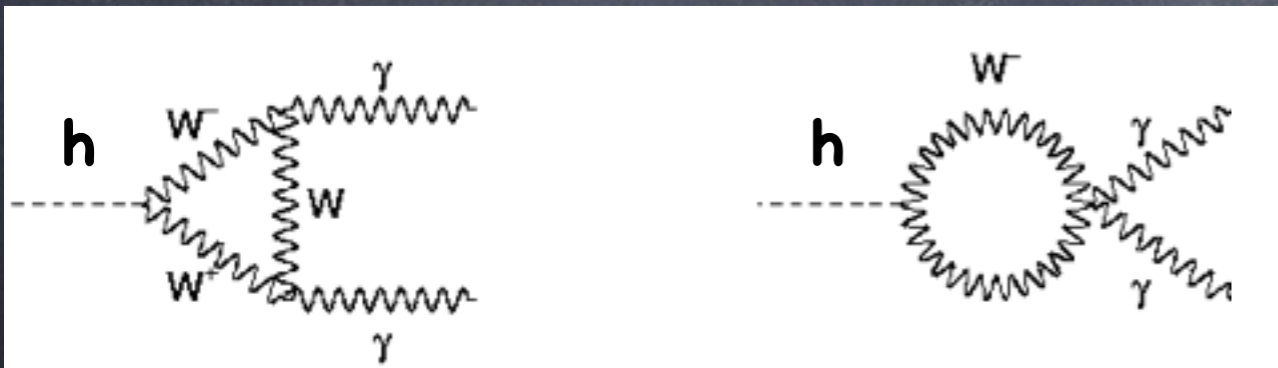
$$\frac{\Gamma_{2\ell 2\nu}}{\Gamma_{2\ell 2\nu}^{\text{SM}}} \simeq 1 + 2\delta c_w + 0.46c_{w\Box} - 0.15c_{ww}$$

$$\rightarrow 1 + 2\delta c_z + 0.67c_{z\Box} + 0.05c_{zz} - 0.17c_{z\gamma} - 0.05c_{\gamma\gamma}$$

$$\left(\begin{array}{c} 2e2\mu \\ 4e \end{array} \right)$$

$$\begin{aligned} \frac{\bar{\Gamma}_{4\ell}}{\bar{\Gamma}_{4\ell}^{\text{SM}}} &\simeq 1 + 2\delta c_z + \begin{pmatrix} 0.41 \\ 0.39 \end{pmatrix} c_{z\Box} - \begin{pmatrix} 0.15 \\ 0.14 \end{pmatrix} c_{zz} + \begin{pmatrix} 0.07 \\ 0.05 \end{pmatrix} c_{z\gamma} - \begin{pmatrix} 0.02 \\ 0.02 \end{pmatrix} c_{\gamma\Box} + \begin{pmatrix} < 0.01 \\ 0.03 \end{pmatrix} c_{\gamma\gamma} \\ &\rightarrow 1 + 2\delta c_z + \begin{pmatrix} 0.35 \\ 0.32 \end{pmatrix} c_{z\Box} - \begin{pmatrix} 0.19 \\ 0.19 \end{pmatrix} c_{zz} + \begin{pmatrix} 0.09 \\ 0.08 \end{pmatrix} c_{z\gamma} + \begin{pmatrix} 0.01 \\ 0.02 \end{pmatrix} c_{\gamma\gamma}. \end{aligned} \quad (4.13)$$

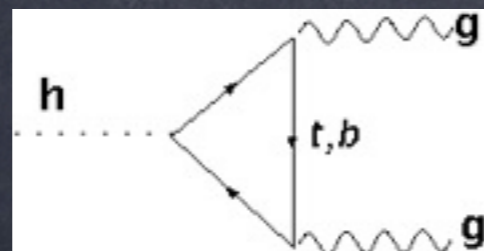
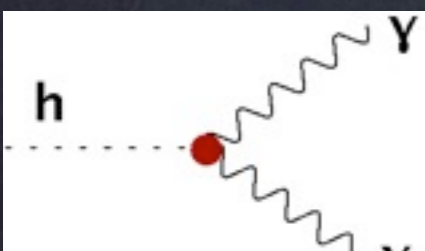
Decays to 2 gauge bosons



$$\frac{\Gamma_{VV}}{\Gamma_{VV}^{\text{SM}}} \simeq \left| 1 + \frac{\hat{c}_{vv}}{c_{vv}^{\text{SM}}} \right|^2, \quad vv \in \{gg, \gamma\gamma, z\gamma\},$$

$$\hat{c}_{\gamma\gamma} = c_{\gamma\gamma}, \quad c_{\gamma\gamma}^{\text{SM}} \simeq -8.3 \times 10^{-2},$$

$$\hat{c}_{z\gamma} = c_{z\gamma}, \quad c_{z\gamma}^{\text{SM}} \simeq -5.9 \times 10^{-2},$$



Higgs observables in the Higgs basis

Signal strength

$$\mu_{X;Y} = \frac{\sigma(pp \rightarrow X)}{\sigma(pp \rightarrow X)_{\text{SM}}} \frac{\Gamma(h \rightarrow Y)}{\Gamma(h \rightarrow Y)_{\text{SM}}} \frac{\Gamma(h \rightarrow \text{all})_{\text{SM}}}{\Gamma(h \rightarrow \text{all})}$$

In EFT, assuming no other degrees of freedom,
so total width is just sum of partial width into SM particle
no invisible width in this analysis

- One can express all measured signal strength in terms of the 9 EFT parameters

δc_z $c_z \square$ c_{zz} $c_{z\gamma}$ $c_{\gamma\gamma}$ c_{gg} δy_u δy_d δy_e

- Using available LHC signal strength data one can obtain constraints on **most** of these parameters

Higgs constraints on EFT

	$\mathbf{L} (x_0 \pm 1 \sigma)$
δc_z	-0.12 ± 0.20
c_{zz}	0.6 ± 1.9
$c_{z\Box}$	-0.25 ± 0.83
$c_{\gamma\gamma}$	0.015 ± 0.029
$c_{z\gamma}$	0.01 ± 0.10
c_{gg}	-0.0056 ± 0.0028
δy_u	0.55 ± 0.30
δy_d	-0.42 ± 0.45
δy_e	-0.18 ± 0.36

AA
1505.00046

Flat direction

$$c_{zz} \approx -2.3c_{z\Box}$$

Needs more data
on differential distributions
in $h \rightarrow 4f$ decays

- Not all parameters yet constrained enough that EFT approach is valid
- Results sensitive to including corrections to Higgs observables quadratic in EFT parameters which are formally $O(1/\Lambda^4)$. Thus, in general, results may be sensitive to including dimension-8 operators

Combined Constraints from LEP-2 WW and LHC Higgs

Previously

Corbett et al 1304.1151
Dumont et al 1304.3369
Pomarol Riva 1308.2803
Masso 1406.6377
Ellis et al 1410.7703

Now

AA, Gonzalez-Alonso, Greljo, Marzocca 1508.00581

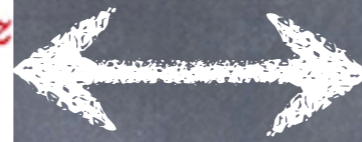
Consistent EFT analysis
at $O(1/\Lambda^2)$

TGC - Higgs Synergy

TGC

Higgs

CP even : $\delta\kappa_\gamma$ $\delta g_{1,z}$ λ_z
 CP odd : $\tilde{\kappa}_\gamma$ $\tilde{\lambda}_z$



CP even : δc_z $c_{z\Box}$ c_{zz} $c_{z\gamma}$ $c_{\gamma\gamma}$ c_{gg}
 CP odd : \tilde{c}_{zz} $\tilde{c}_{z\gamma}$ $\tilde{c}_{\gamma\gamma}$ \tilde{c}_{gg}

Linearly realized $SU(3)\times SU(2)\times U(1)$ at D=6 level enforces relations between TGC and Higgs couplings in the Higgs basis

$$\delta g_{1,z} = \frac{1}{2(g_L^2 - g_Y^2)} [c_{\gamma\gamma} e^2 g_Y^2 + c_{z\gamma} (g_L^2 - g_Y^2) g'^2 - c_{zz} (g_L^2 + g_Y^2) g_Y^2 - c_{z\Box} (g_L^2 + g_Y^2) g_L^2]$$

$$\delta\kappa_\gamma = -\frac{g_L^2}{2} \left(c_{\gamma\gamma} \frac{e^2}{g_L^2 + g_Y^2} + c_{z\gamma} \frac{g_L^2 - g_Y^2}{g_L^2 + g_Y^2} - c_{zz} \right),$$

$$\tilde{\kappa}_\gamma = -\frac{g_L^2}{2} \left(\tilde{c}_{\gamma\gamma} \frac{e^2}{g_L^2 + g_Y^2} + \tilde{c}_{z\gamma} \frac{g_L^2 - g_Y^2}{g_L^2 + g_Y^2} - \tilde{c}_{zz} \right),$$

- In Higgs basis formalism, all but 2 TGCs are dependent couplings and can be expressed by Higgs couplings to gauge bosons
- Therefore constraints on δg_{1z} and $\delta\kappa_\gamma$ imply constraints on Higgs couplings
- But for that, all TGCs have to be **simultaneously** constrained in multi-dimensional fit, and correlation matrix should be given
- Note that $c_{z\gamma}$ c_{zz} and $c_{z\Box}$ are difficult to access experimentally in Higgs physics
- Important to combine Higgs and TGC data!

Higgs constraints on EFT

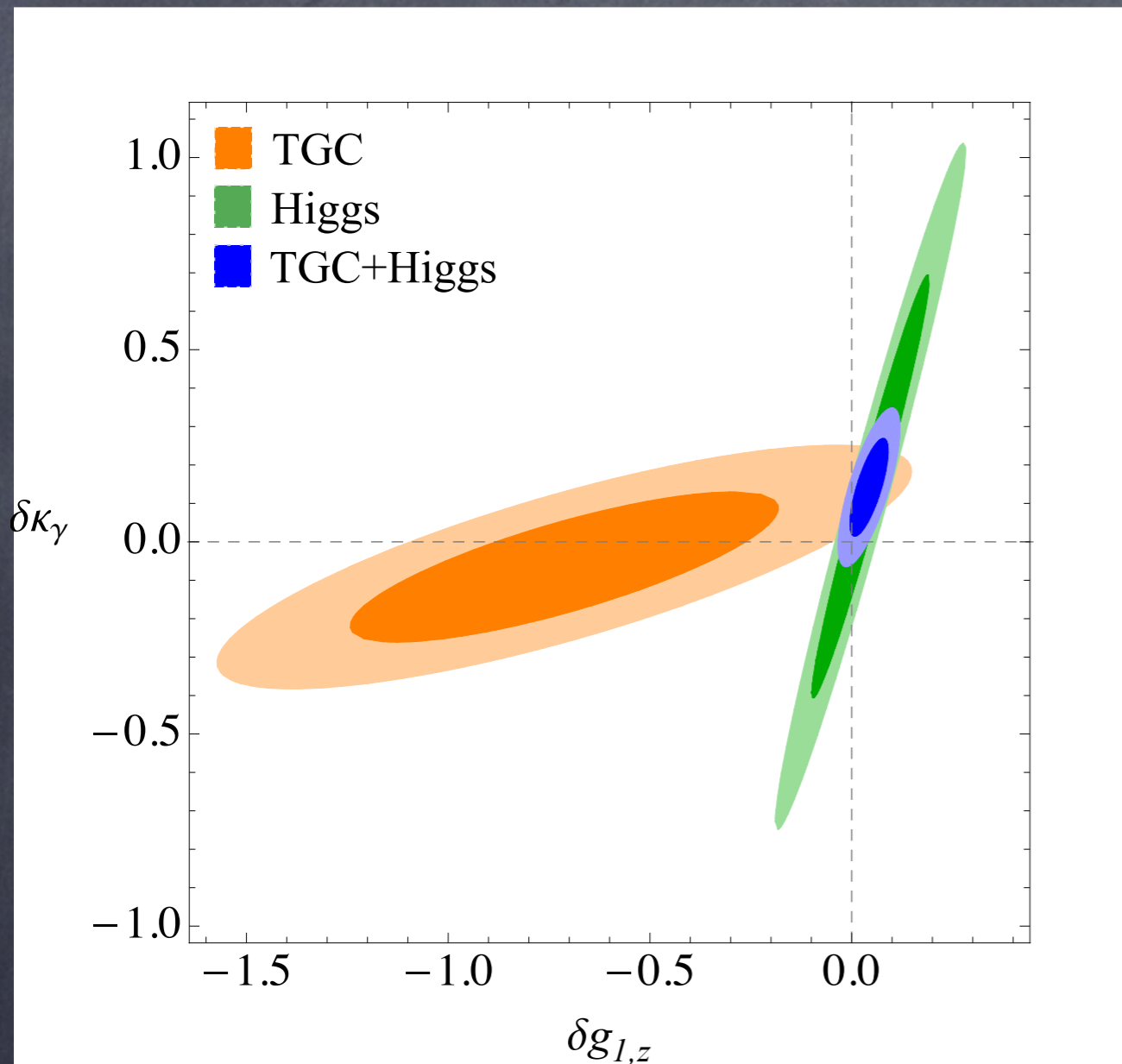
$$\begin{pmatrix} \delta c_z \\ c_{zz} \\ c_{z\Box} \\ c_{\gamma\gamma} \\ c_{z\gamma} \\ c_{gg} \\ \delta y_u \\ \delta y_d \\ \delta y_e \\ \lambda_z \end{pmatrix} = \begin{pmatrix} -0.07 \pm 0.14 \\ 0.65 \pm 0.42 \\ -0.29 \pm 0.21 \\ -0.005 \pm 0.014 \\ -0.005 \pm 0.095 \\ -0.0053 \pm 0.0027 \\ 0.55 \pm 0.30 \\ -0.44 \pm 0.24 \\ -0.22 \pm 0.18 \\ -0.152 \pm 0.080 \end{pmatrix}$$

Correlation matrix

1.	-0.07	-0.23	0.4	-0.05	-0.05	0.03	0.56	0.49	-0.24
-0.07	1.	-0.92	0.34	0.18	0.	0.02	-0.3	-0.38	-0.85
-0.23	-0.92	1.	-0.43	-0.12	0.03	0.	0.21	0.21	0.94
0.4	0.34	-0.43	1.	0.09	0.4	-0.47	-0.11	-0.12	-0.42
-0.05	0.18	-0.12	0.09	1.	0.01	-0.01	-0.1	-0.13	-0.12
-0.05	0.	0.03	0.4	0.01	1.	-0.89	0.18	0.06	0.03
0.03	0.02	0.	-0.47	-0.01	-0.89	1.	0.1	0.04	0.01
0.56	-0.3	0.21	-0.11	-0.1	0.18	0.1	1.	0.66	0.19
0.49	-0.38	0.21	-0.12	-0.13	0.06	0.04	0.66	1.	0.18
-0.24	-0.85	0.94	-0.42	-0.12	0.03	0.01	0.19	0.18	1.

- Flat direction between c_{zz} and $c_{z\Box}$ lifted to large extent by WW data!
- Much better constraints on some parameters.
Most parameters (marginally) within the EFT regime
- Lower sensitivity to the quadratic terms (though still not completely negligible, especially for δc_z and δy_d)

Corollary: constraints on TGCs

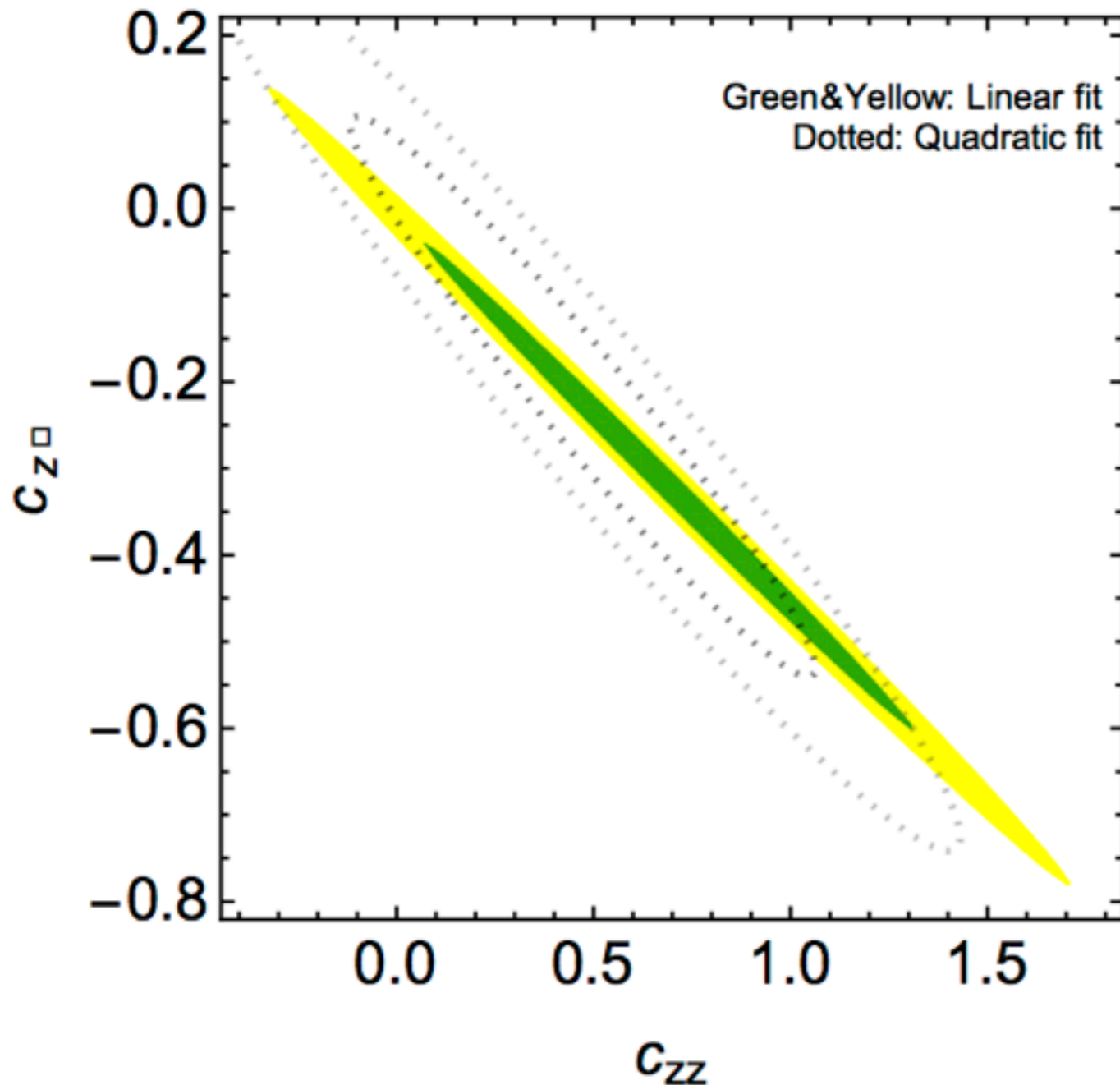


- LHC Higgs and LEP-2 WW data by itself do not constrain TGCs robustly due to each suffering from 1 flat direction in space of 3 TGCs
- However, the flat directions are orthogonal and combined constraints lead to robust $O(0.1)$ limits on aTGCs

$$\begin{pmatrix} \delta g_{1,z} \\ \delta \kappa_\gamma \\ \lambda_z \end{pmatrix} = \begin{pmatrix} 0.037 \pm 0.041 \\ 0.133 \pm 0.087 \\ -0.152 \pm 0.080 \end{pmatrix},$$

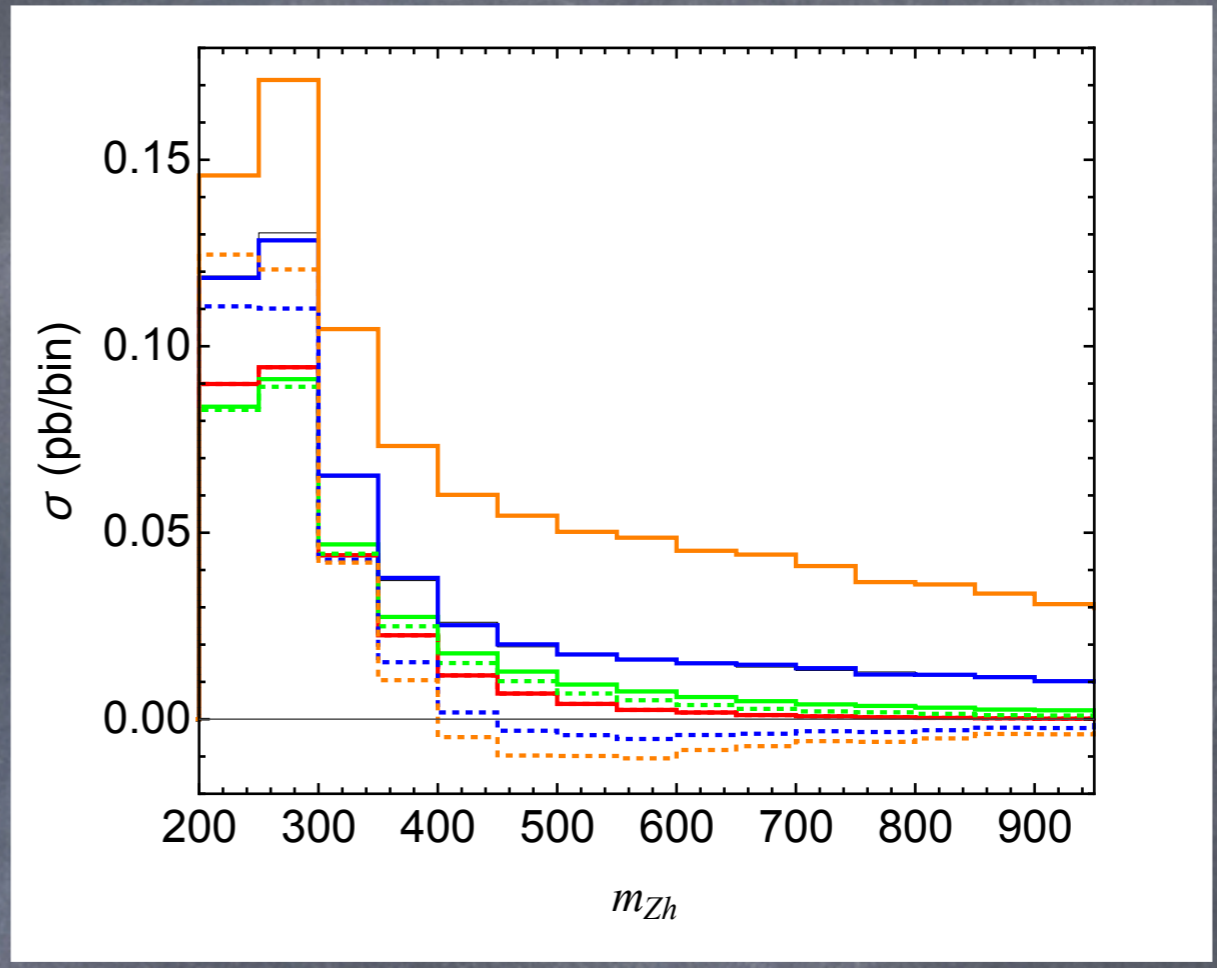
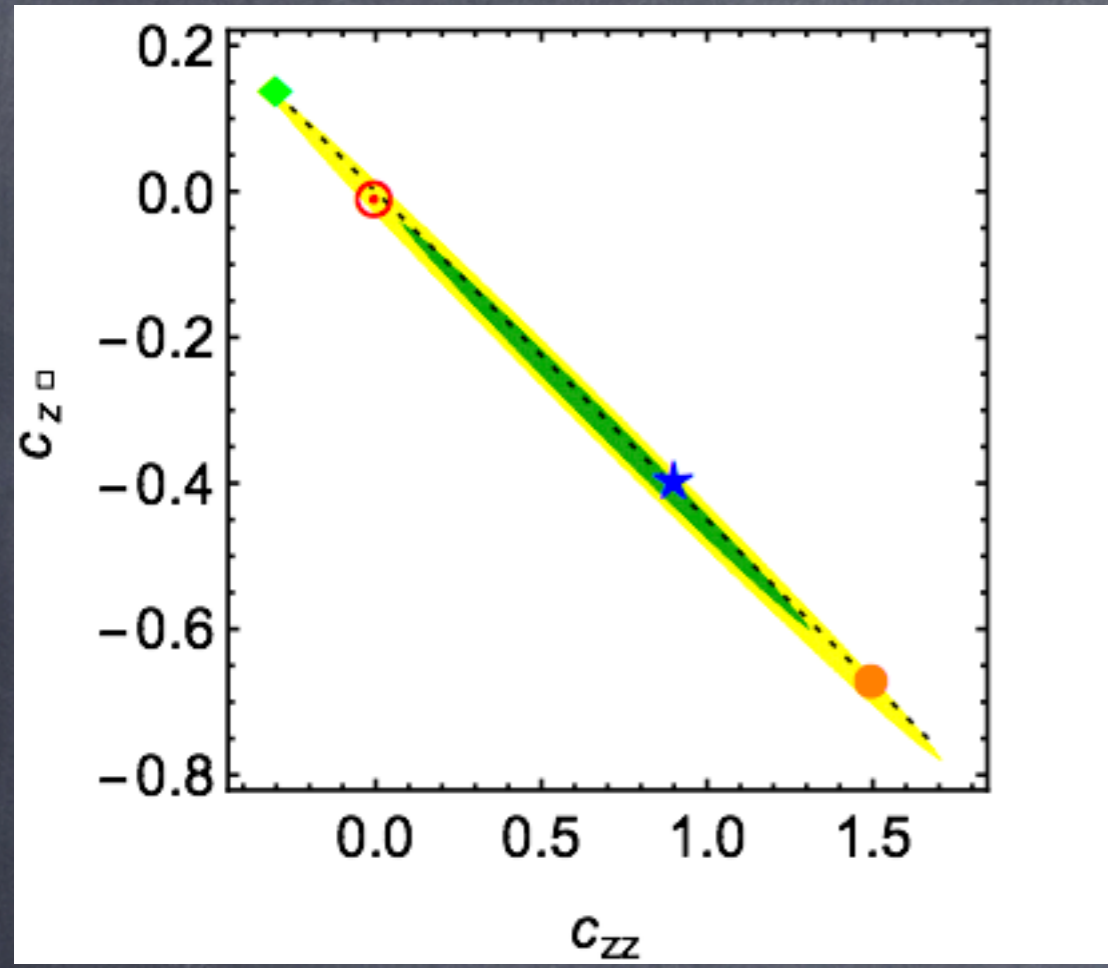
$$\rho = \begin{pmatrix} 1 & 0.62 & -0.84 \\ 0.62 & 1 & -0.85 \\ -0.84 & -0.85 & 1 \end{pmatrix}$$

Combined WW+Higgs: robustness



- Non-trivial constraints at linear ($1/\Lambda^2$) level
- Quadratic ($1/\Lambda^4$) terms not completely negligible yet, but they do not change fit qualitatively

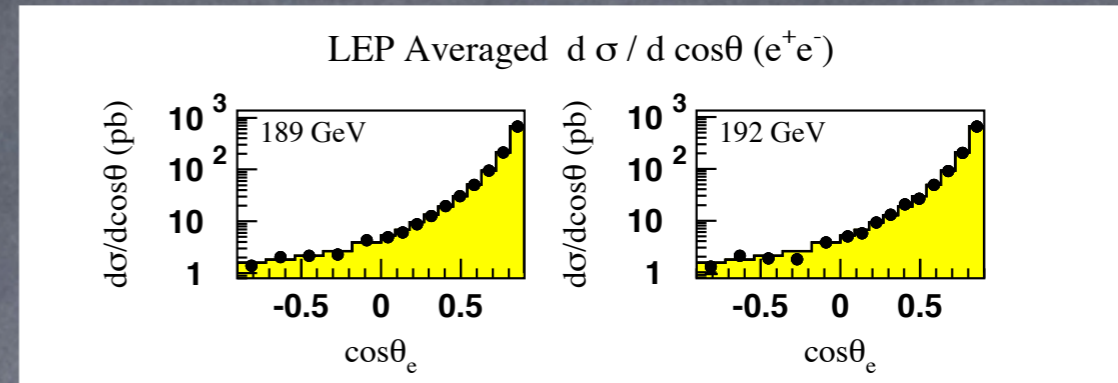
Combined WW+Higgs: robustness



- For VH production, quadratic ($1/\Lambda^4$) contributions are comparable to linear ($1/\Lambda^2$) ones
- They are numerically important but don't change fit significantly because they constrain similar direction in parameter space as linear ones
- Sensitivity to $1/\Lambda^4$ terms greatly reduced if VH signal strength with cut $m_{VH} < 400$ GeV was quoted

Constraints on 4 fermion operators

$$\begin{aligned}
 [O_{\ell\ell}]_{1111} &= (\bar{\ell}_1 \bar{\sigma}_\mu \ell_1)(\bar{\ell}_1 \bar{\sigma}_\mu \ell_1), \\
 [O_{\ell e}]_{1111} &= (\bar{\ell}_1 \bar{\sigma}_\mu \ell_1)(e_1^c \sigma_\mu \bar{e}_1^c), \\
 [O_{ee}]_{1111} &= (e_1^c \sigma_\mu \bar{e}_1^c)(e_1^c \sigma_\mu \bar{e}_1^c).
 \end{aligned}$$

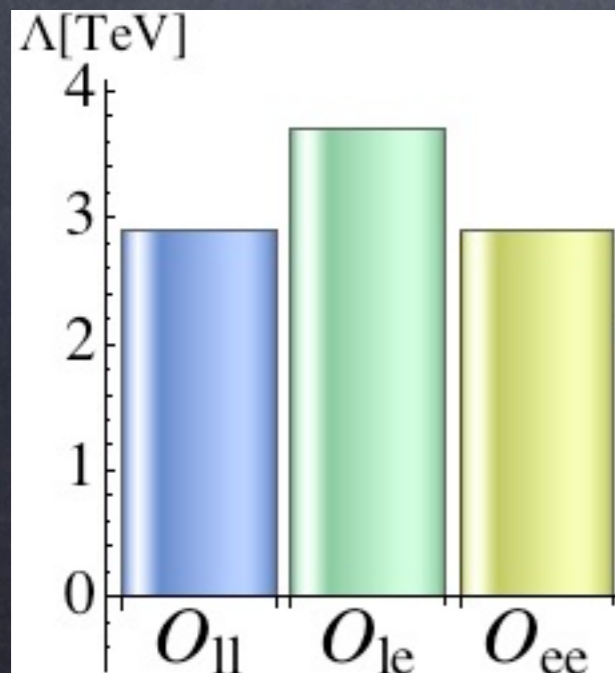


1-by-1

Simultaneous

$$\begin{aligned}
 [c_{\ell\ell}]_{1111} &= (4.0 \pm 1.6) \times 10^{-3} \\
 [c_{\ell e}]_{1111} &= (1.7 \pm 1.5) \times 10^{-3} \\
 [c_{ee}]_{1111} &= (4.0 \pm 1.7) \times 10^{-3}
 \end{aligned}$$

$$\begin{aligned}
 [c_{\ell\ell}]_{1111} &= -0.35 \pm 0.39 \\
 [c_{\ell e}]_{1111} &= (-3.7 \pm 2.7) \times 10^{-3} \\
 [c_{ee}]_{1111} &= 0.37 \pm 0.40
 \end{aligned}$$



$$\rho = \begin{pmatrix} 1 & 0.57 & \approx -1 \\ 0.57 & 1 & -0.57 \\ \approx -1 & -0.57 & 1 \end{pmatrix}$$

Take away

- There are strong constraints on certain combinations of dimension-6 operators from the pole observables measured at LEP-1 and other colliders. These can be conveniently presented as correlated constraints on vertex corrections and W mass corrections.
- Assuming MFV, these constraints allow one to describe LO EFT deformations of single Higgs signal strength LHC observables by just 9 parameters
- There are non-trivial constraints on all of these 9 parameters from Higgs and WW data
- Synergy of TGC and Higgs coupling measurements is crucial for deriving meaningful bounds