

Communication to thermal dark matter with large self-interactions

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Based on M.-S. Seo, Phys. Lett. B748, 316;
S.-M. Choi, JHEP1509, 063 & To appear.

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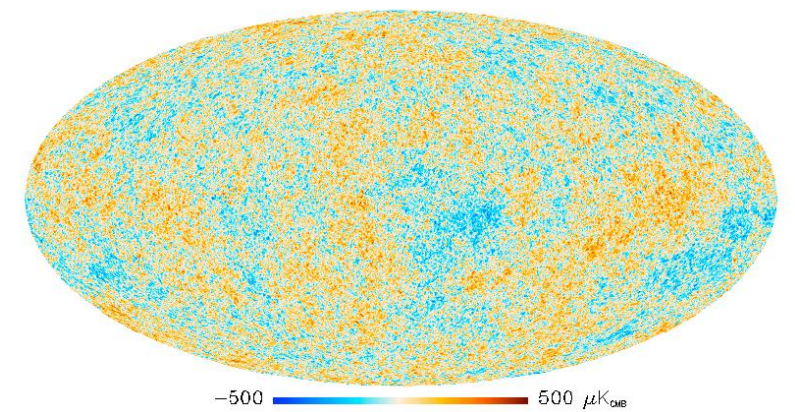
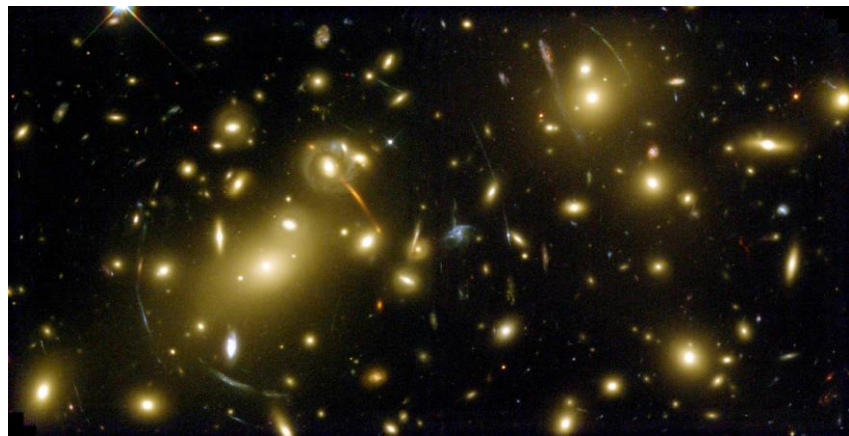
Outline

- Motivation
- SIMP DM from hidden QCD
- SIMP DM from discrete symmetries
- Conclusions

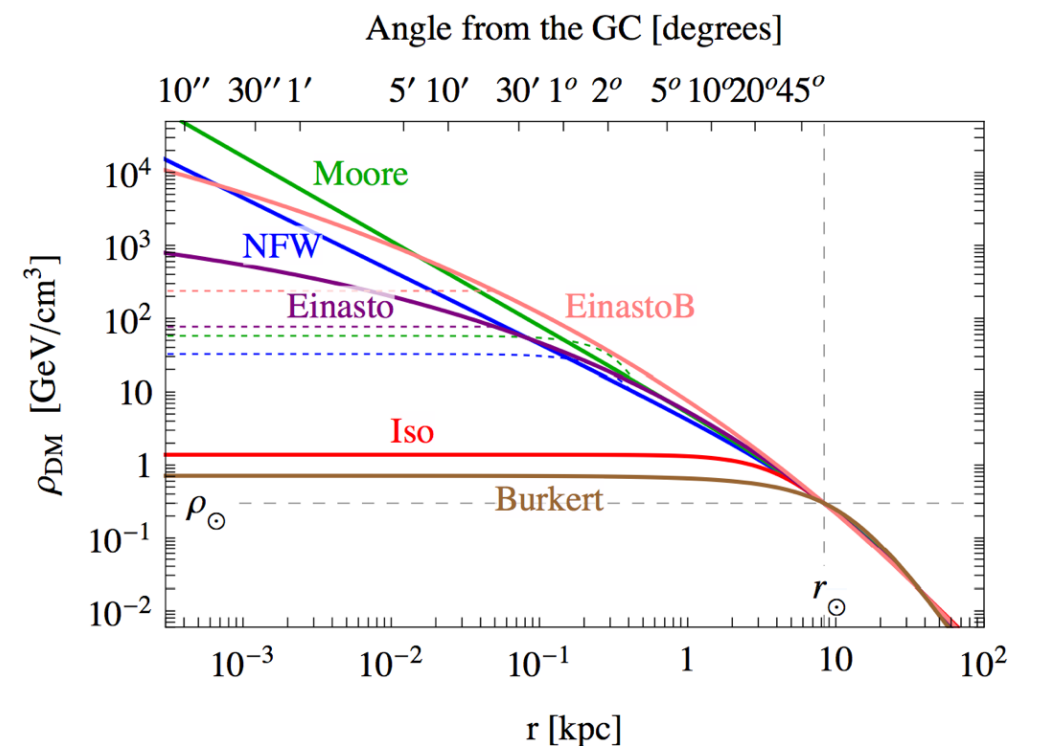
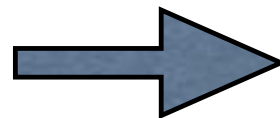
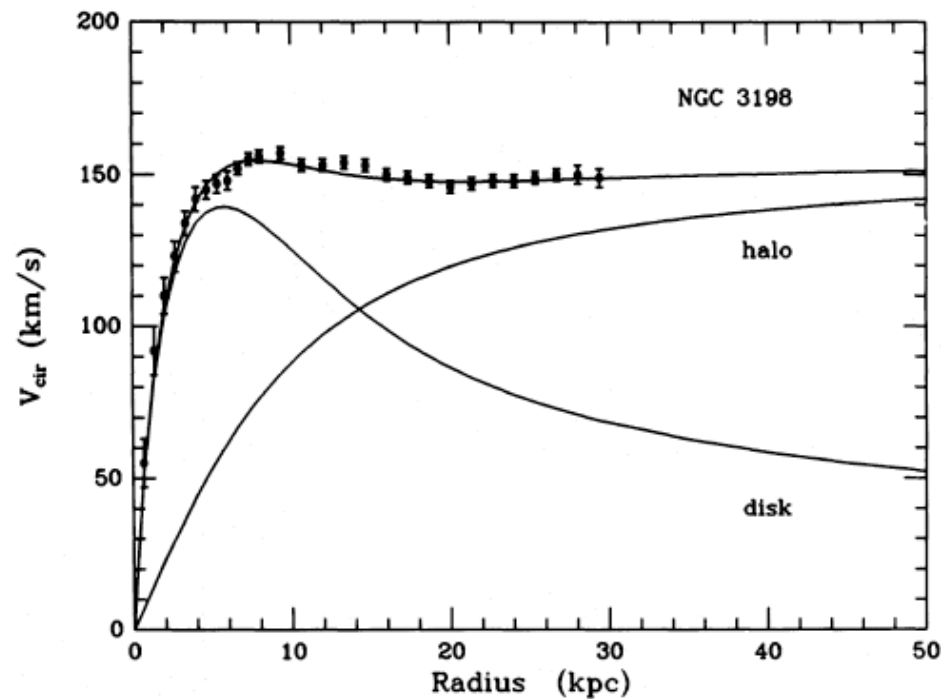
Motivation

Dark matter everywhere!

Large-scale evidences

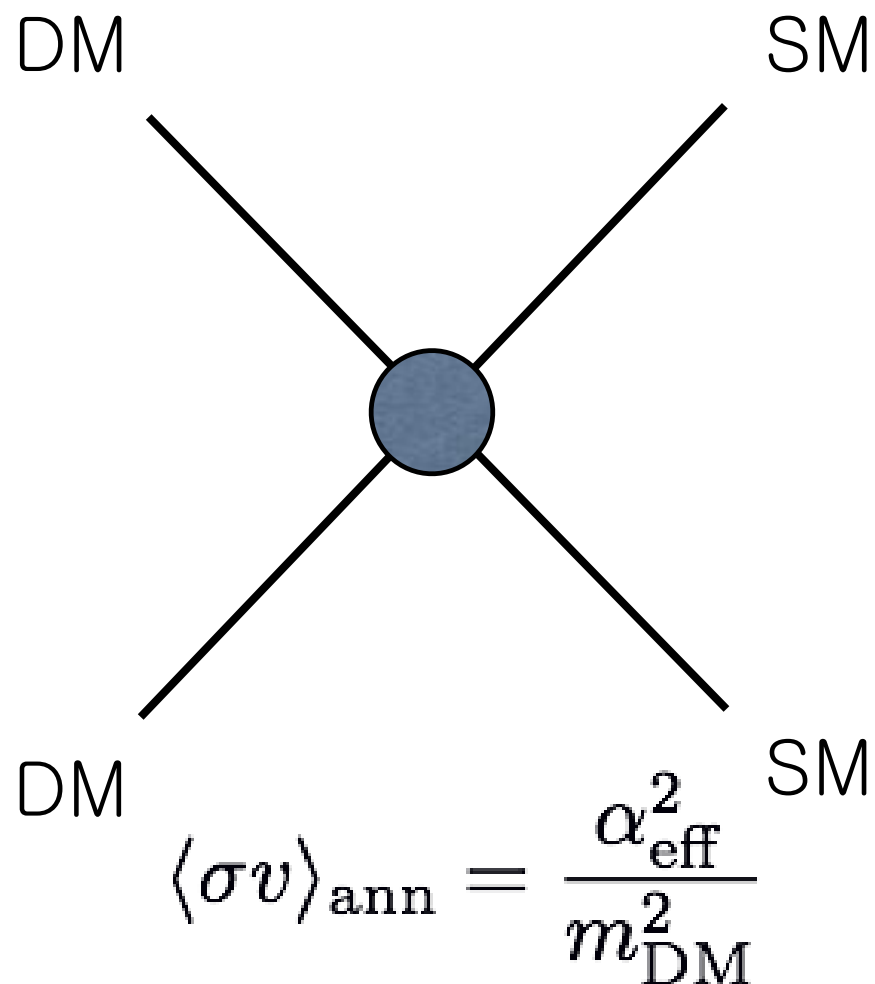


Galaxies (including our Milky Way)



WIMP paradigm

- WIMP DM density relies on $2 \rightarrow 2$ annihilation processes with weak interactions.



$$\frac{dn}{dt} + 3Hn = -\langle \sigma v \rangle (n^2 - n_{\text{eq}}^2)$$

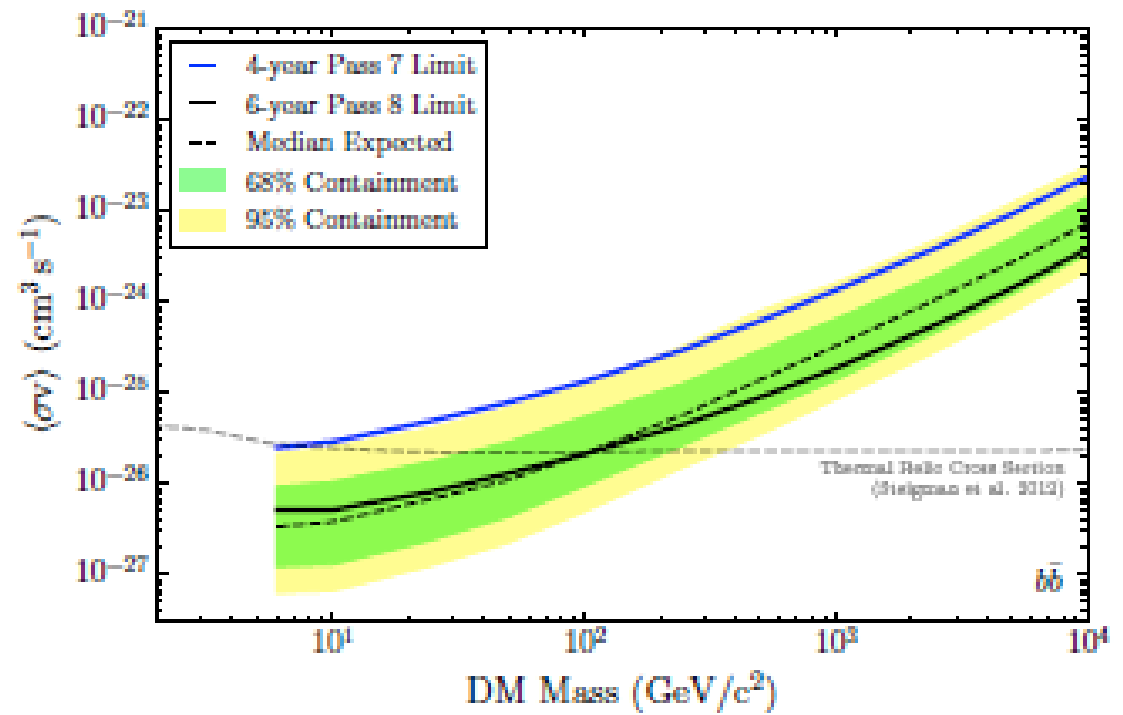
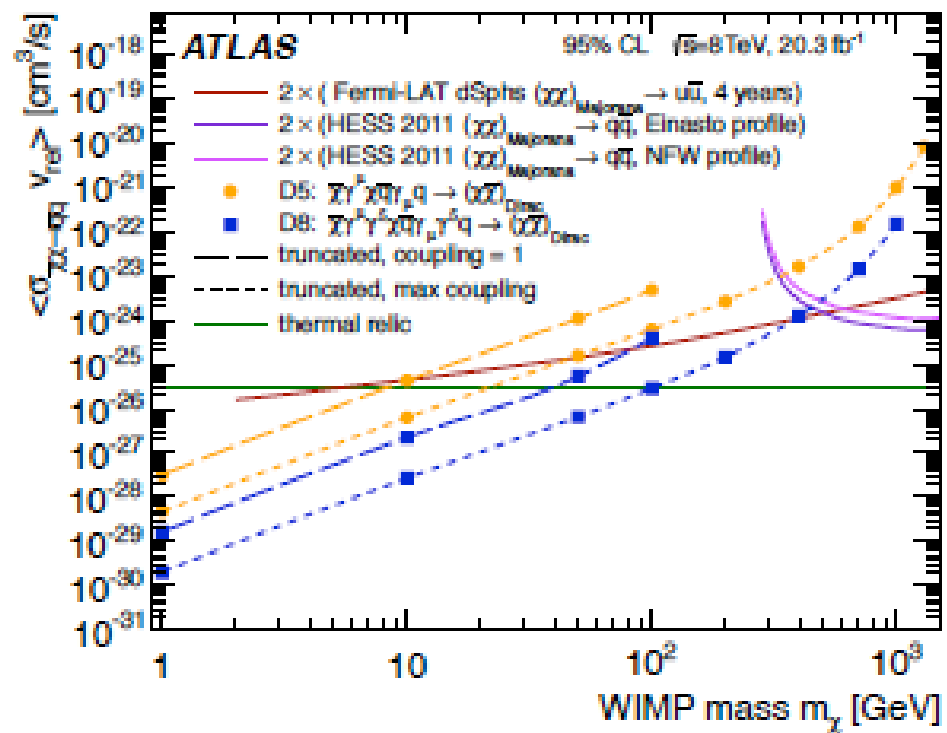
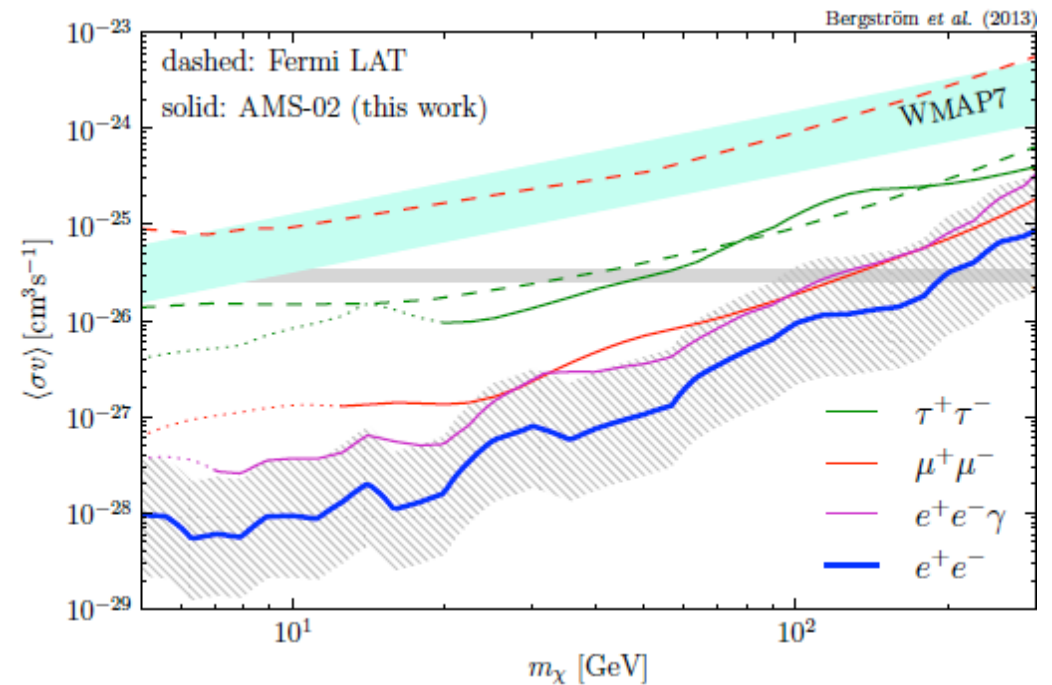
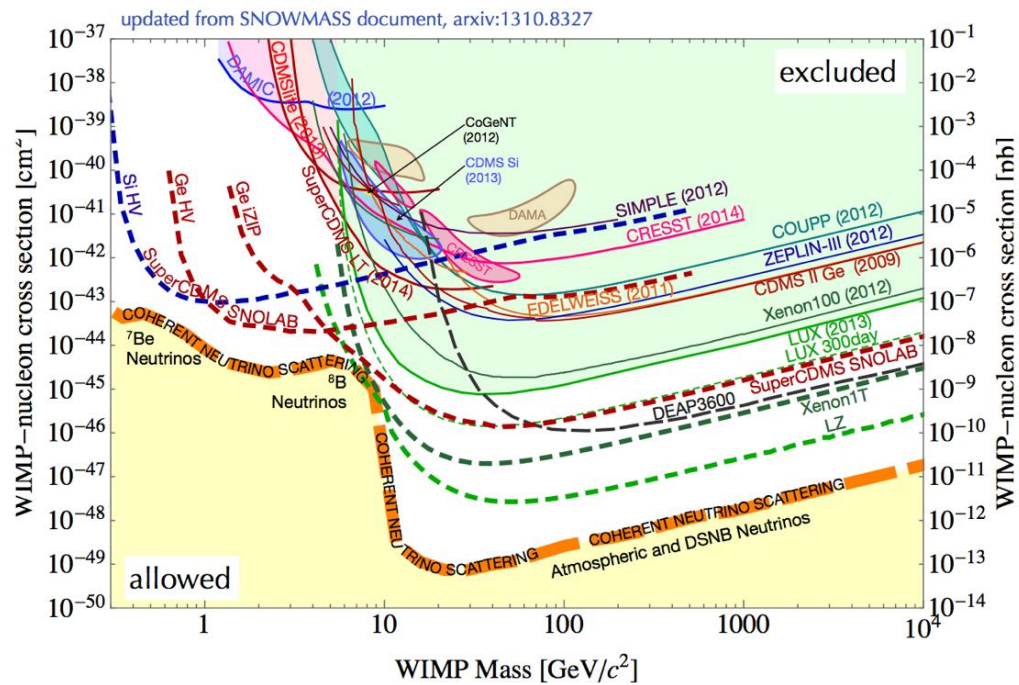
WIMP freeze-out:

$$\Gamma_{\text{ann}} = n_{\text{DM}} \langle \sigma v \rangle_{\text{ann}} \sim H = 0.33 g_*^{1/2} \frac{T_F^2}{M_P}$$

$$m_{\text{DM}} = \alpha_{\text{eff}} \left(\frac{5.35 \kappa}{x_F g_*^{1/2}} T_{\text{eq}} M_P \right)^{1/2} \quad \kappa \simeq 10.8$$

$$\alpha_{\text{eff}} \sim 0.1 \quad \longrightarrow \quad m_{\text{DM}} \sim 100 \text{ GeV.}$$

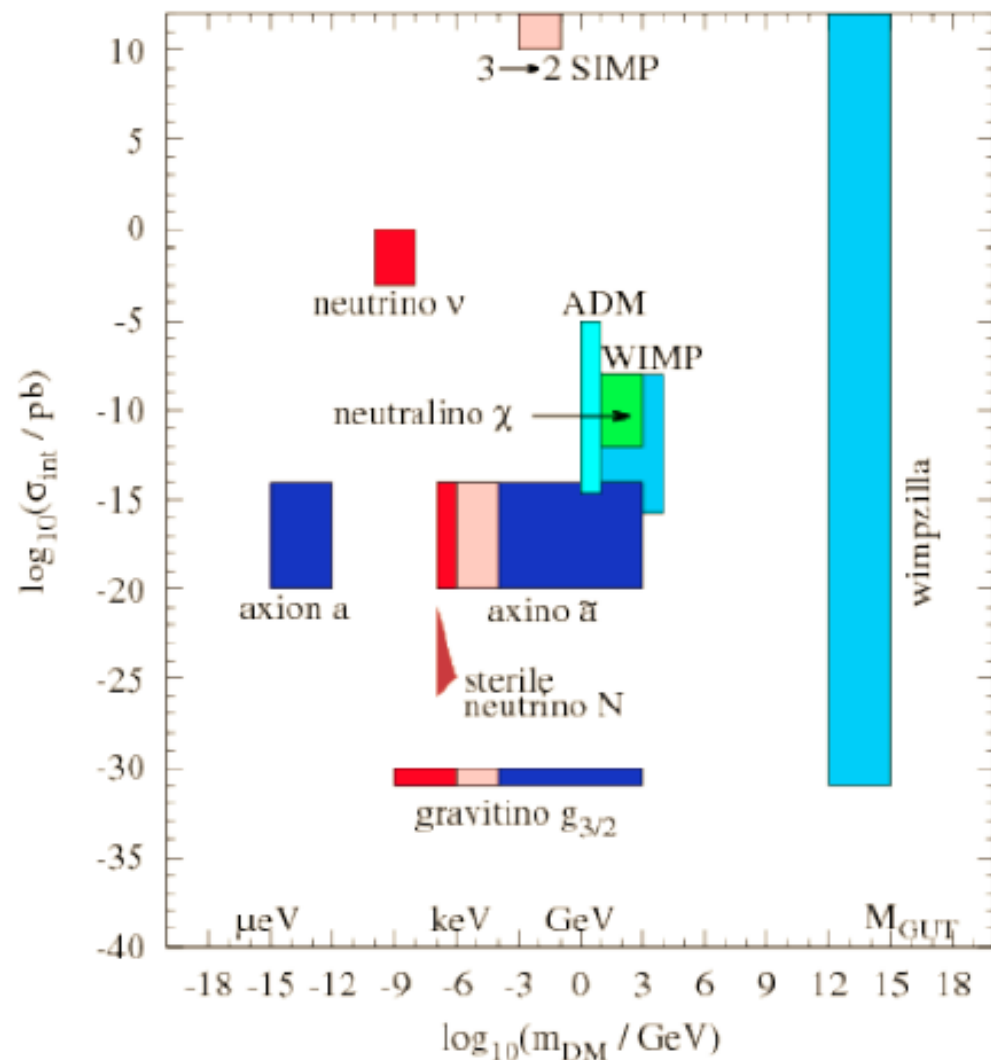
WIMP around the corner?



- Direct/indirect/collider searches rule out a wide range of WIMP dark matter.

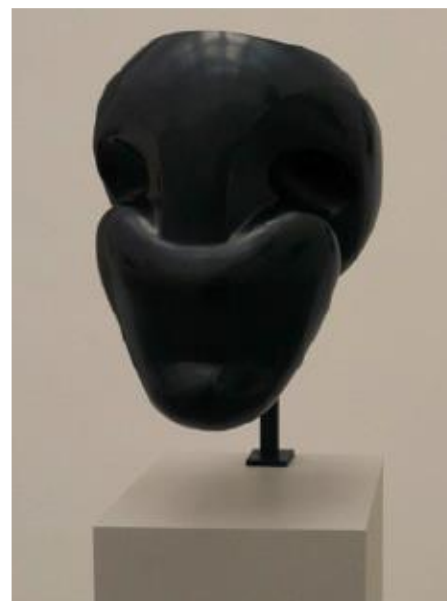
Non-WIMP?

- WIMP paradigm is based mostly on the assumption that DM is related to weak-scale physics solving the hierarchy problem.



[Choi, Kim, Roszkowski, 1407.0017]

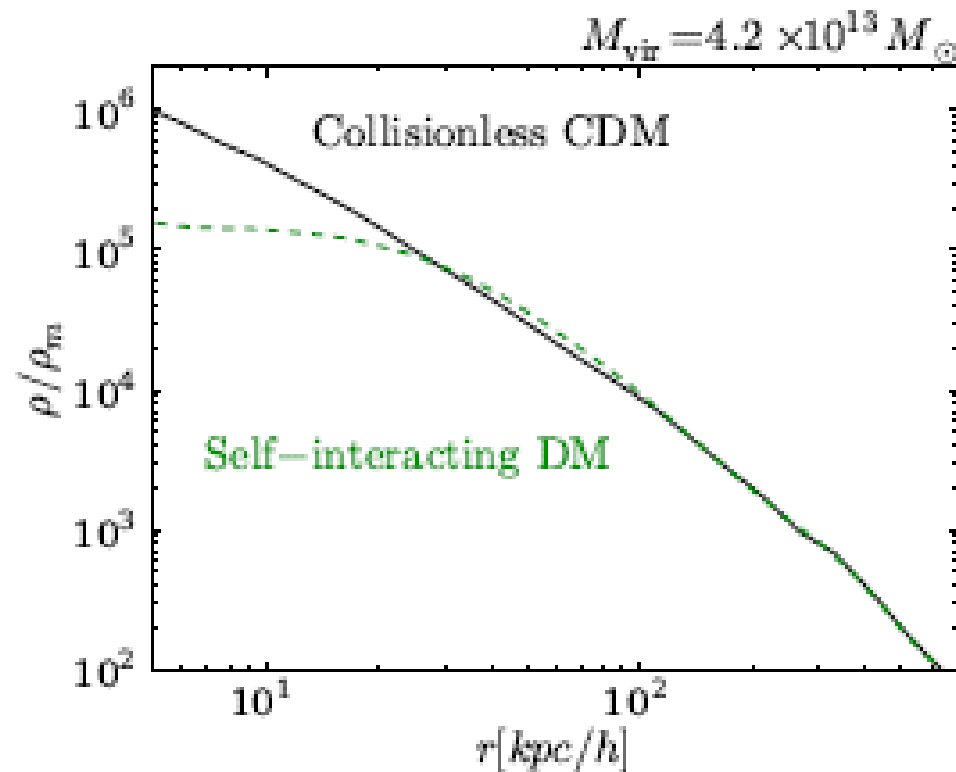
- But, dark matter might be related to different problems such as QCD axion or some unknown hidden sector.



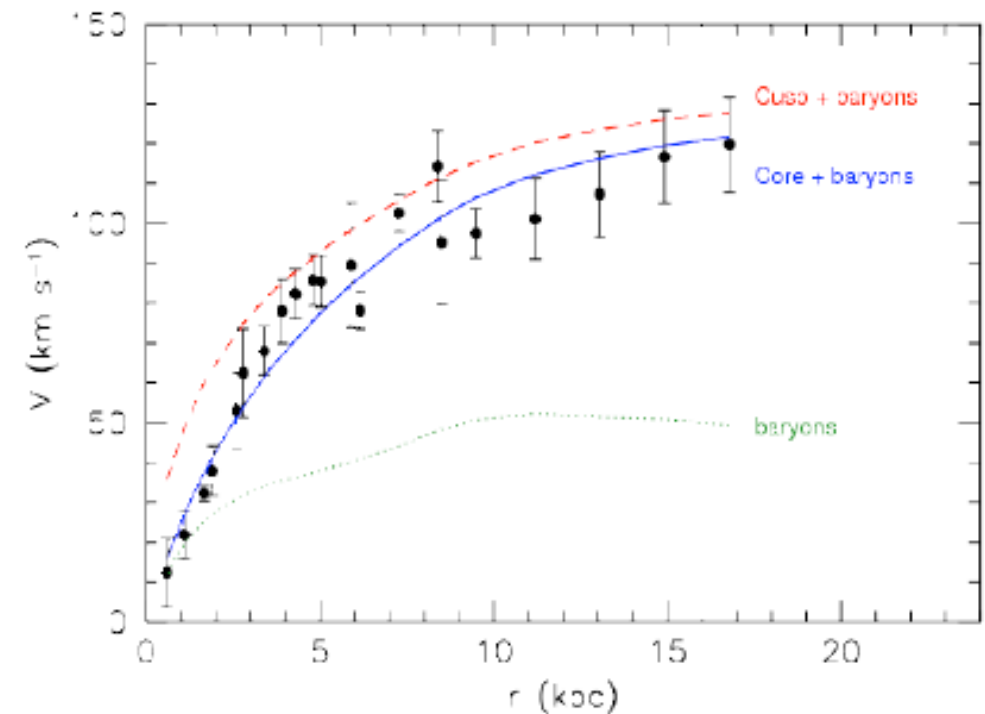
more than this?

DM self-interactions

- Solve small-scale problems in galaxies: core-cusp, too-big-to-fail, missing satellites, etc.



[D.H. Weinberg et al(2013)]



NFW overshoots data!

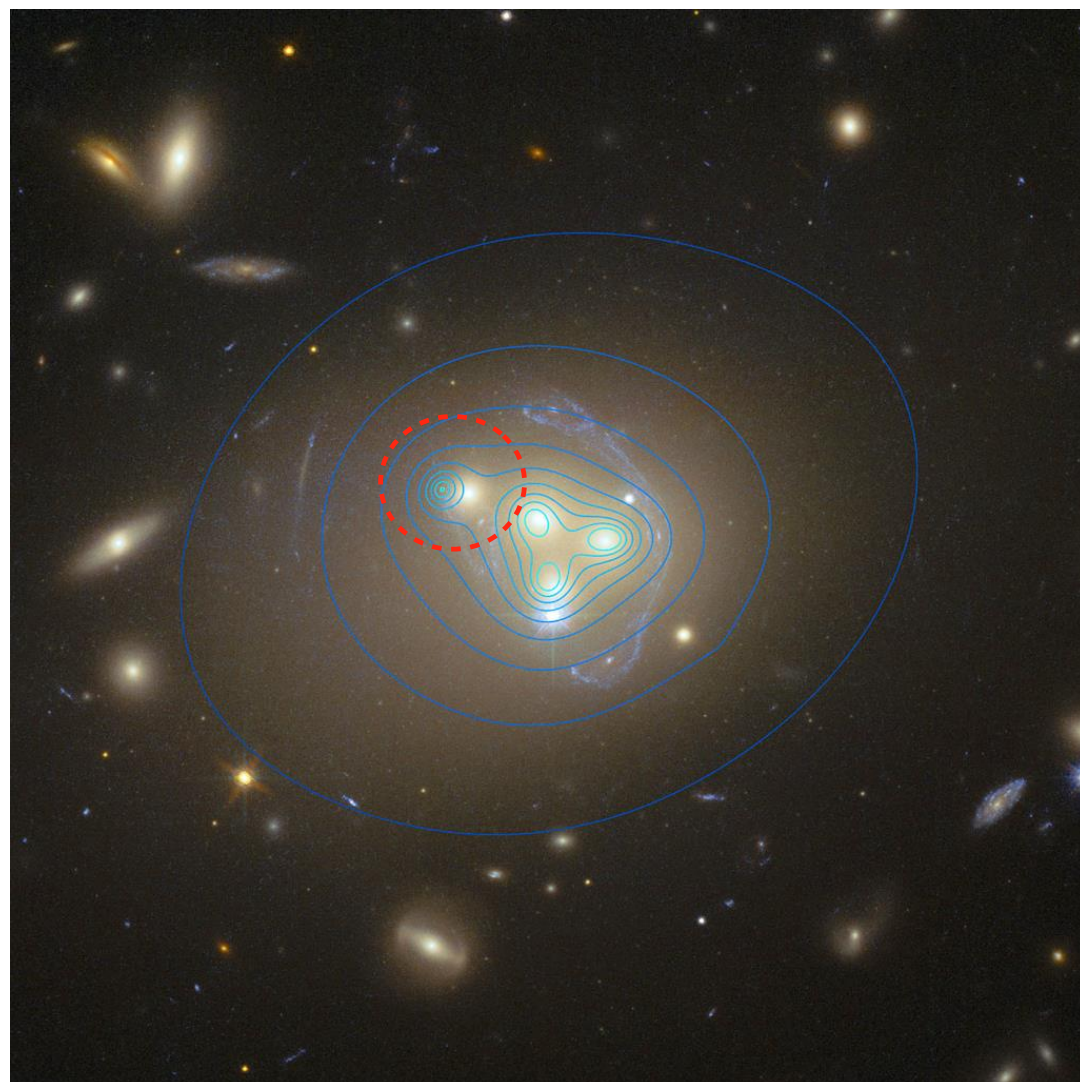
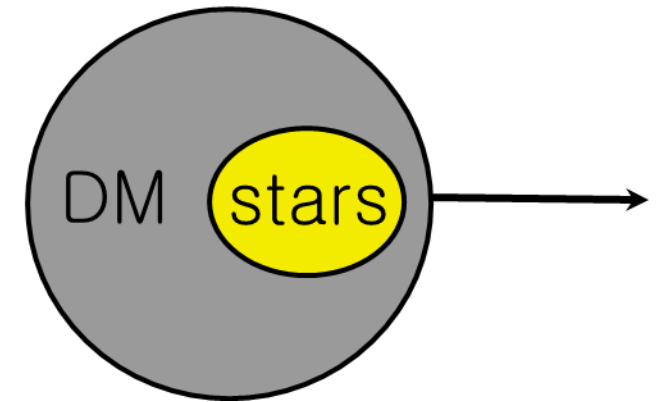
➔ $\sigma_{\text{self}}/m_{\text{DM}} = 0.1 - 10 \text{ cm}^2/\text{g}$

cf. WIMP DM: $\sigma_{\text{self}}/m_{\text{WIMP}} \sim 10^{-11} \text{ GeV}^{-3} \sim 10^{-14} \text{ cm}^2/\text{g}$.

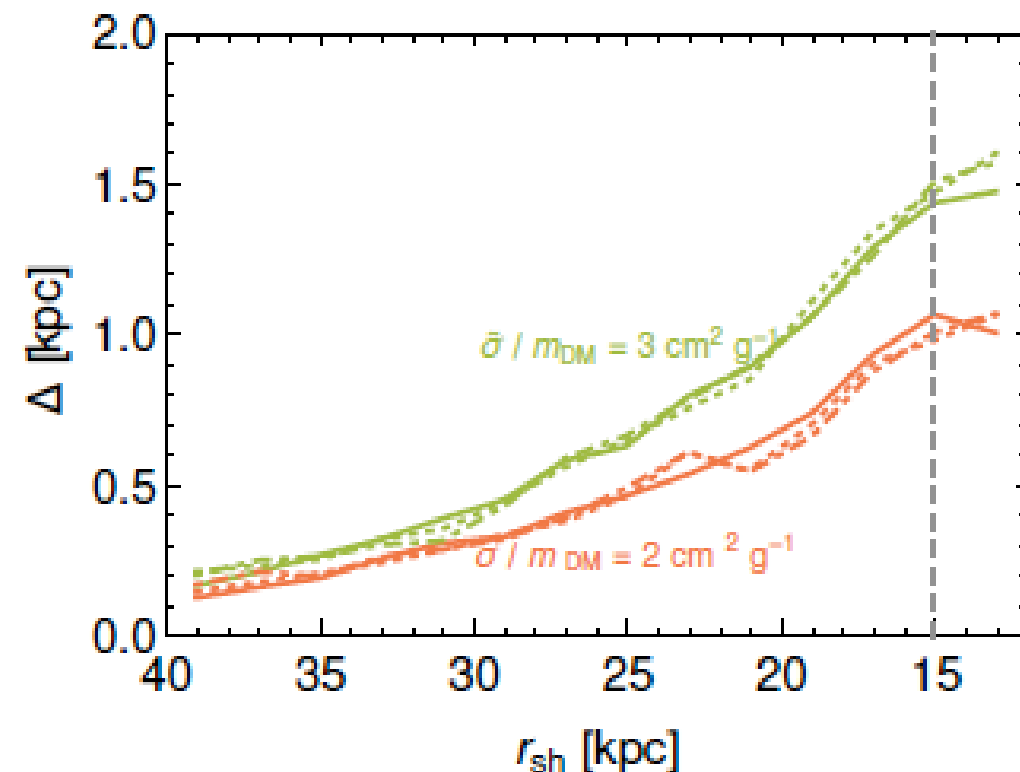
Bullet cluster & halo shape: $\sigma_{\text{self}}/m_{\text{DM}} < 1 \text{ cm}^2/\text{g}$

Abell 3827

- Lead to an observable effect the lag of DM subhalos from their stars.
- Among four colliding galaxies observed by Hubble Telescope, one of subhalo lags behind the galaxy.



DM subhalo separation $\Delta = 1.62^{+0.47}_{-0.49}$ kpc
[Massey et al(2015)]

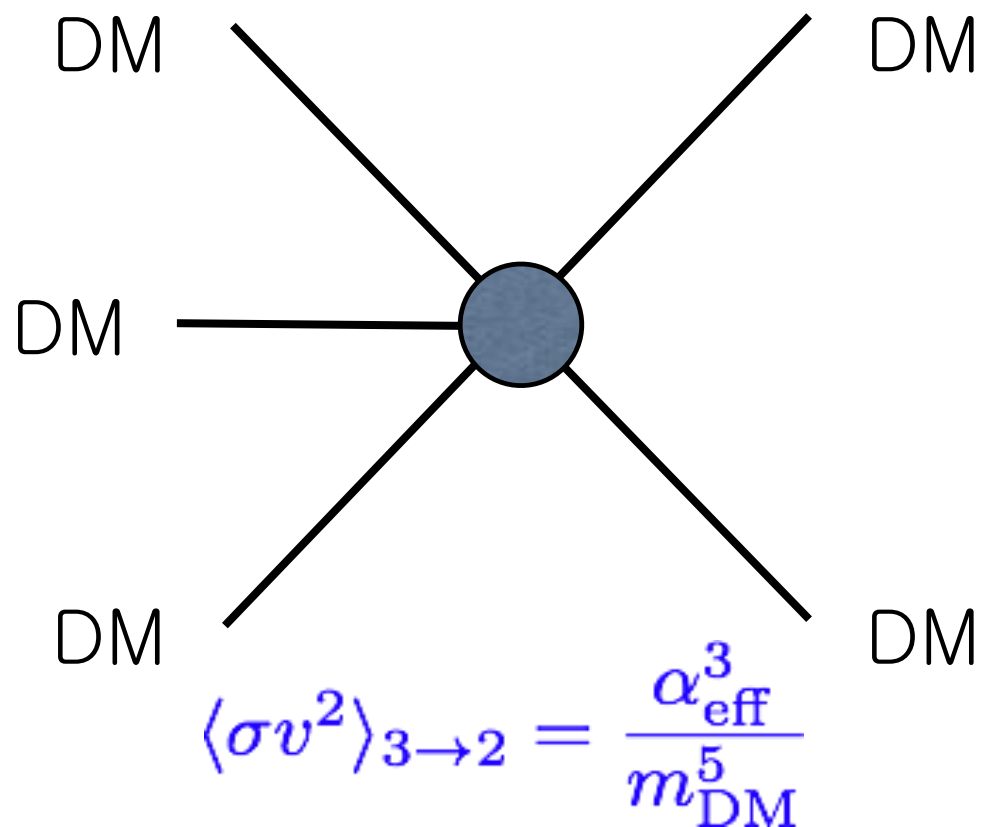


[Kahlhoefer et al (2015)]

SIMP paradigm

- Strong Interacting Massive Particle(SIMP) is a thermal DM, due to $3 \rightarrow 2$ self-annihilation.

[Hochberg et al, 2014]



$$\frac{dn}{dt} + 3Hn = -\langle \sigma v \rangle_{3 \rightarrow 2} (n^2 - n_{\text{eq}}^2)$$

Freeze-out:

$$\Gamma_{3 \rightarrow 2} = n_{\text{DM}}^2 \langle \sigma v^2 \rangle_{3 \rightarrow 2} \sim H(T_F)$$

$$m_{\text{DM}} = \alpha_{\text{eff}} \left(\frac{5.35 \kappa^2}{x_F^4 g_*^{1/2}} T_{\text{eq}}^2 M_P \right)^{1/3} \quad (\kappa \simeq 2.55)$$

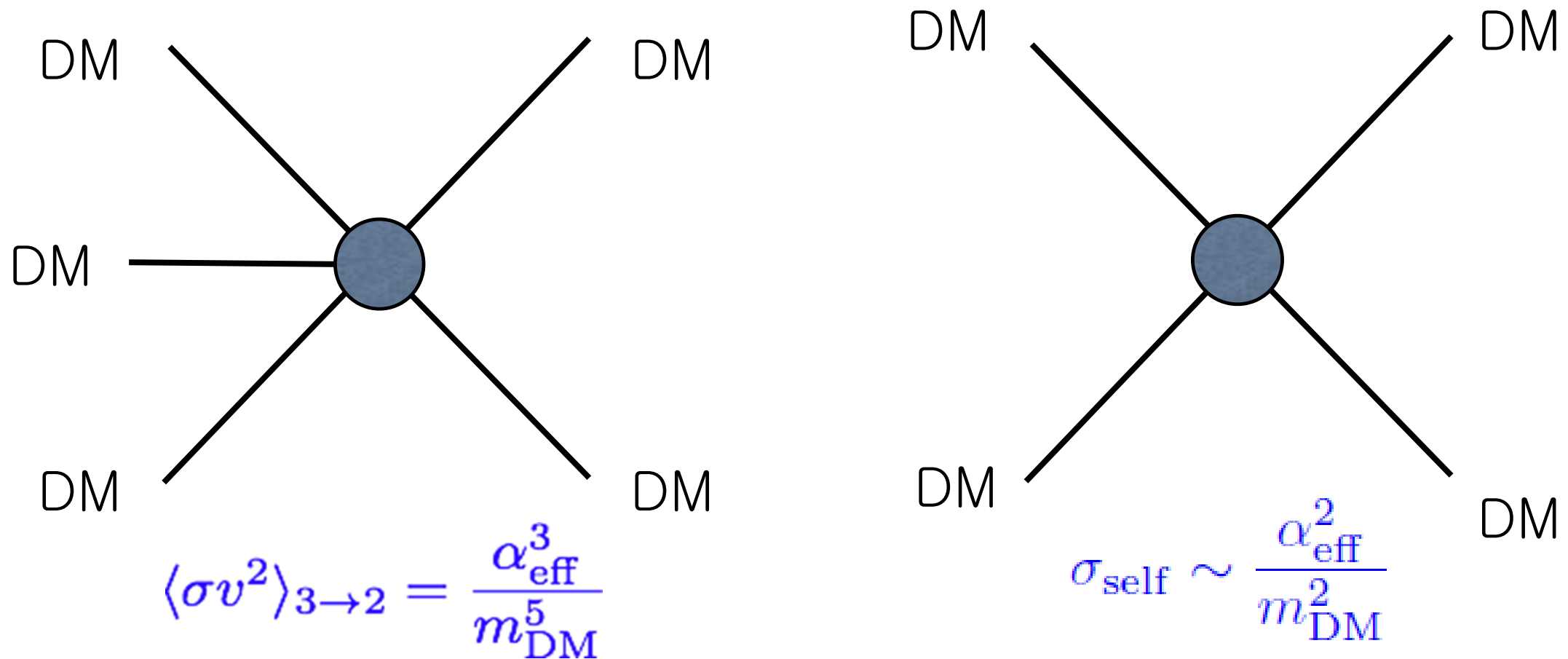
cf. WIMP:

$$m_{\text{DM}} = \alpha_{\text{eff}} \left(\frac{5.35 \kappa}{x_F g_*^{1/2}} T_{\text{eq}} M_P \right)^{1/2}$$

$$\alpha_{\text{eff}} = 1 - 30 \quad \longrightarrow \quad m_{\text{DM}} \sim 10 \text{ MeV} - 1 \text{ GeV}$$

Large SIMP self-interaction

- SIMP DM predicts typically large DM self-interactions.

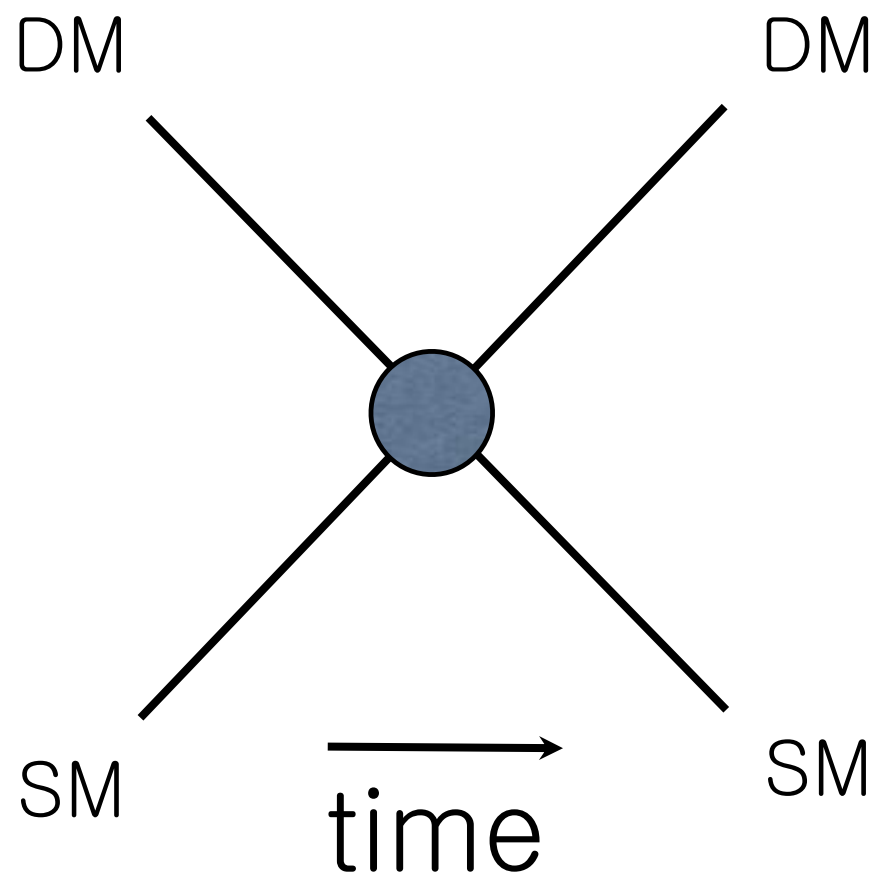


$\Rightarrow \frac{\sigma_{\text{self}}}{m_{\text{DM}}} = 4 \times 10^3 \text{ GeV}^{-3} \left(\frac{100 \text{ MeV}}{m_{\text{DM}}} \right)^3 \left(\frac{\alpha_{\text{eff}}}{2} \right)^2$

Bullet cluster & spherical halo shapes.

$\frac{\sigma_{\text{self}}}{m_{\text{DM}}} < 1 \text{ cm}^2/\text{g} = 4.6 \times 10^3 \text{ GeV}^{-3}$

SIMP conditions



- Equilibration of heat from SIMP: kinetic equilibrium with SM bath.

$$\langle \sigma v \rangle_{\text{kin}} = \frac{\epsilon_1^2}{m_{\text{DM}}^2}; \quad n_{\text{SM}} \langle \sigma v \rangle_{\text{kin}} > H(T_F)$$

$$\epsilon_1 \gtrsim 0.9 \times 10^{-9} \alpha_{\text{eff}}^{1/2}$$

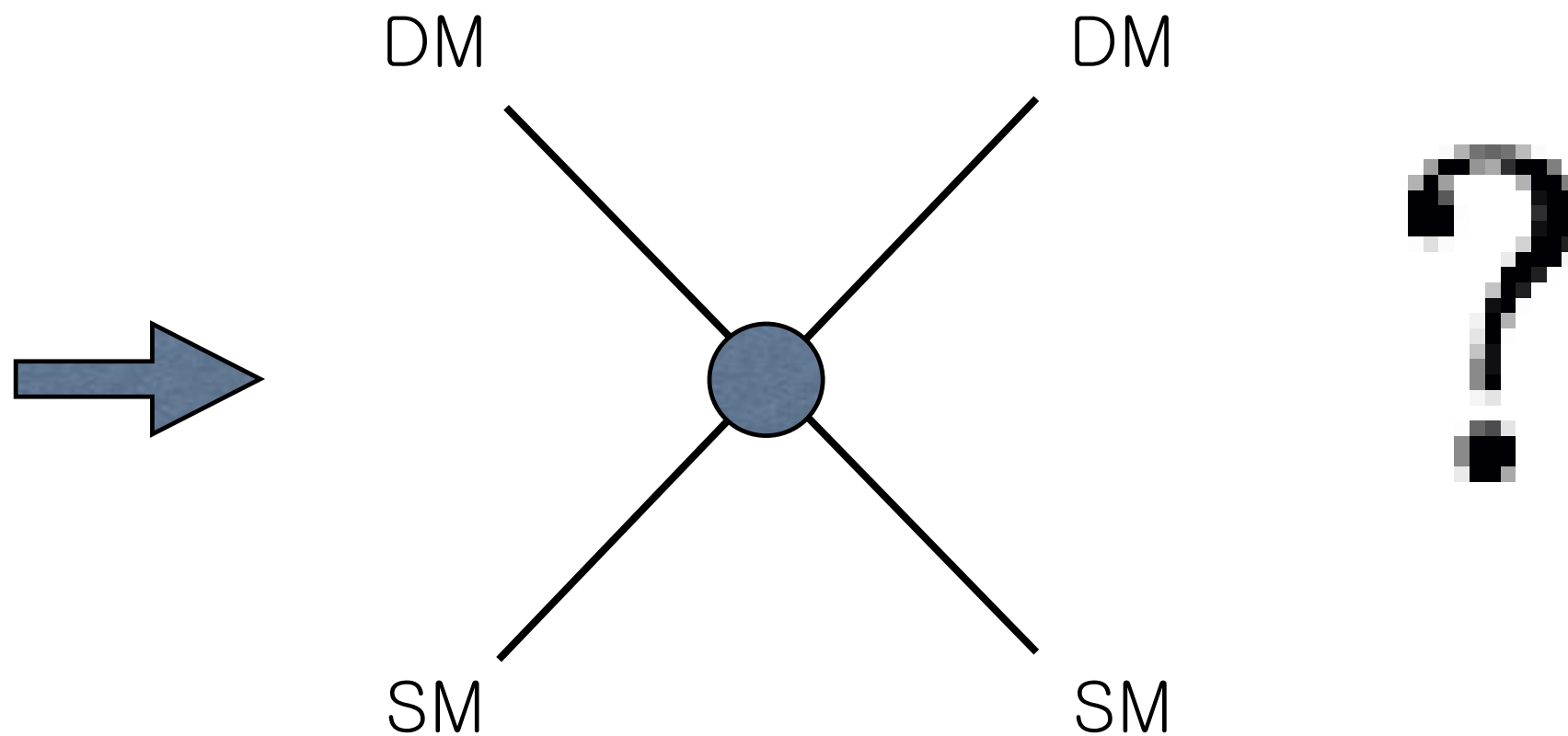
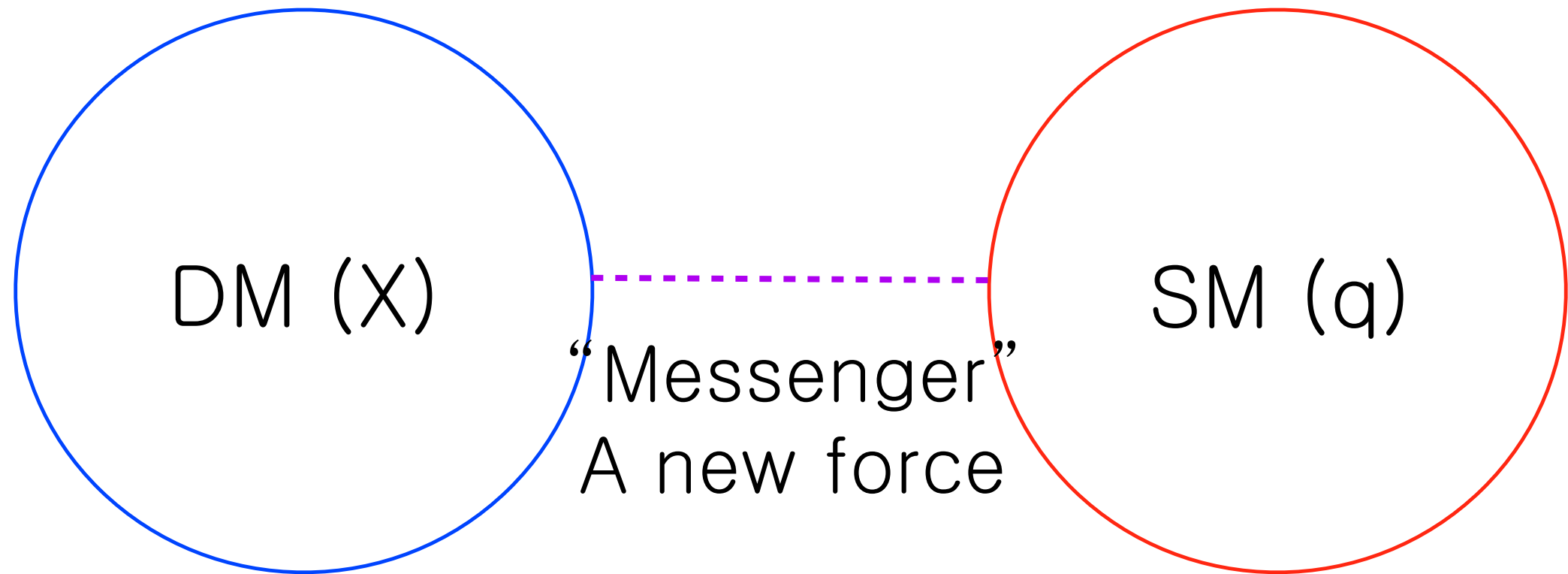
- The same coupling leads to $2 \rightarrow 2$ DM annihilation, which is subdominant when

$$\langle \sigma v \rangle_{\text{ann}} = \frac{\epsilon_2^2}{m_{\text{DM}}^2}; \quad n_{\text{SM}} \langle \sigma v \rangle_{\text{kin}} < n_{\text{DM}} \langle \sigma v^2 \rangle_{3 \rightarrow 2}$$

$$\epsilon_2 \sim \epsilon_1$$

$$\epsilon_1 \lesssim 2.4 \times 10^{-6} \alpha_{\text{eff}}$$

DM messengers



SIMP DM from
hidden QCD

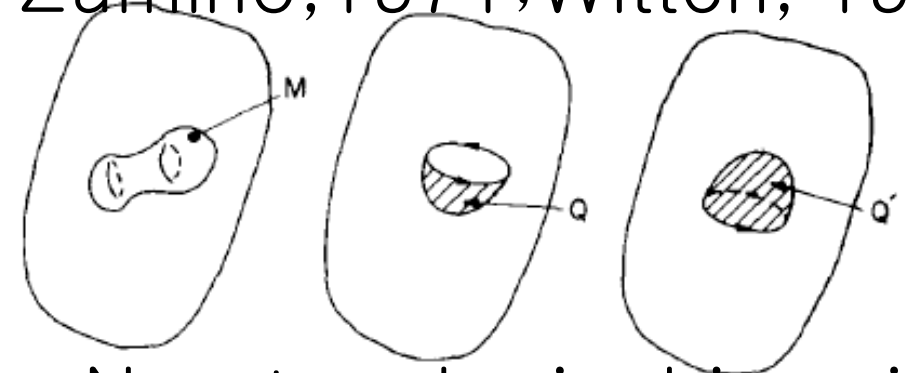
Hidden QCD with WZW term

- Dark flavor symmetry $G = \text{SU}(N_f) \times \text{SU}(N_f)$ is broken down to $H = \text{SU}(N_f)$ by $\text{SU}(N_c)$ QCD-like condensation.
- Effective action for Goldstone bosons contains a 5-point self-interaction from **Wess-Zumino-Witten term** for $\pi_5(G/H) = \mathbb{Z}$ (i.e. $N_f \geq 3$).

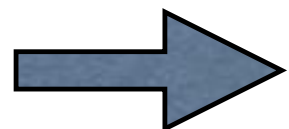
$$U = e^{2i\pi/F}, \quad \pi \equiv \pi^a T^a \quad [\text{Wess, Zumino, 1971; Witten, 1983}]$$

$$\mathcal{L}_{WZW} = \frac{2N_c}{15\pi^2} \epsilon^{\mu\nu\rho\sigma} \text{Tr}[\pi \partial_\mu \pi \partial_\nu \pi \partial_\rho \pi \partial_\sigma \pi]$$

$$N_f = 3 : \pi = \frac{\sqrt{2}}{F} \begin{bmatrix} \frac{1}{\sqrt{2}}\tilde{\pi}_0 + \frac{1}{\sqrt{6}}\tilde{\eta}^0 & \tilde{\pi}^+ & \tilde{K}^+ \\ \tilde{\pi}^- & -\frac{1}{\sqrt{2}}\tilde{\pi}_0 + \frac{1}{\sqrt{6}}\tilde{\eta}^0 & \tilde{K}^0 \\ \tilde{K}^- & \tilde{K}^0 & -\sqrt{\frac{2}{3}}\tilde{\eta}^0 \end{bmatrix}$$



N_c : topological invariant of 5-sphere ($Q+Q'$) in $\text{SU}(3)$



Flavor symmetry ensures stability of dark SIMP mesons.

SIMP dark mesons

- “Large color group” leads to **strong 5-point interactions** while satisfying bounds on self-interactions.

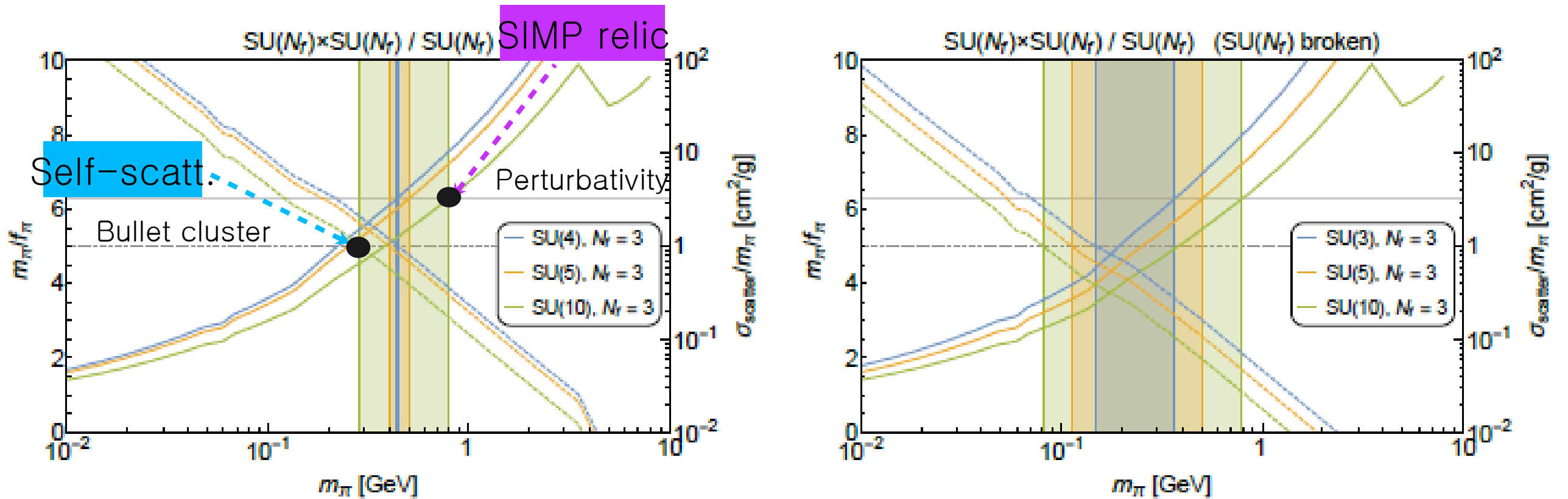
[Hochberg et al, 2014]

$$\langle \sigma v^2 \rangle_{3 \rightarrow 2} = \frac{5\sqrt{5}N_c^2 m_\pi^5 t^2}{2\pi^5 F^{10}} \frac{1}{N_\pi^3} \left(\frac{T_F}{m_\pi} \right)^2 \sim \text{const}$$

$$\sigma_{\text{self}} = \frac{m_\pi^2}{32\pi F^4} \frac{a^2}{N_\pi^2} \sim \text{const}$$

G_e	G_f/H	N_π	t^2	$N_f^2 a^2$
$SU(N_c)$	$\frac{SU(N_f) \times SU(N_f)}{SU(N_f)}$ ($N_f \geq 3$)	$N_f^2 - 1$	$\frac{4}{3} N_f (N_f^2 - 1)(N_f^2 - 4)$	$8(N_f - 1)(N_f + 1)(3N_f^4 - 2N_f^2 + 6)$
$SO(N_c)$	$SU(N_f)/SO(N_f)$ ($N_f \geq 3$)	$\frac{1}{2}(N_f + 2)(N_f - 1)$	$\frac{1}{12} N_f (N_f^2 - 1)(N_f^2 - 4)$	$(N_f - 1)(N_f + 2)(3N_f^4 + 7N_f^3 - 2N_f^2 - 12N_f + 24)$
$Sp(N_c)$	$SU(2N_f)/Sp(2N_f)$ ($N_f \geq 2$)	$(2N_f + 1)(N_f - 1)$	$\frac{2}{3} N_f (N_f^2 - 1)(4N_f^2 - 1)$	$4(N_f - 1)(2N_f + 1)(6N_f^4 - 7N_f^3 - N_f^2 + 3N_f + 3)$

SIMP parameter space



[Hochberg, Kuflik, Murayama, Volansky, Wacker, 2014]

Bullet cluster, Halo shape

Perturbativity

$$\sigma_{\text{self}}/m_{\text{DM}} < 1 \text{ cm}^2/\text{g}$$

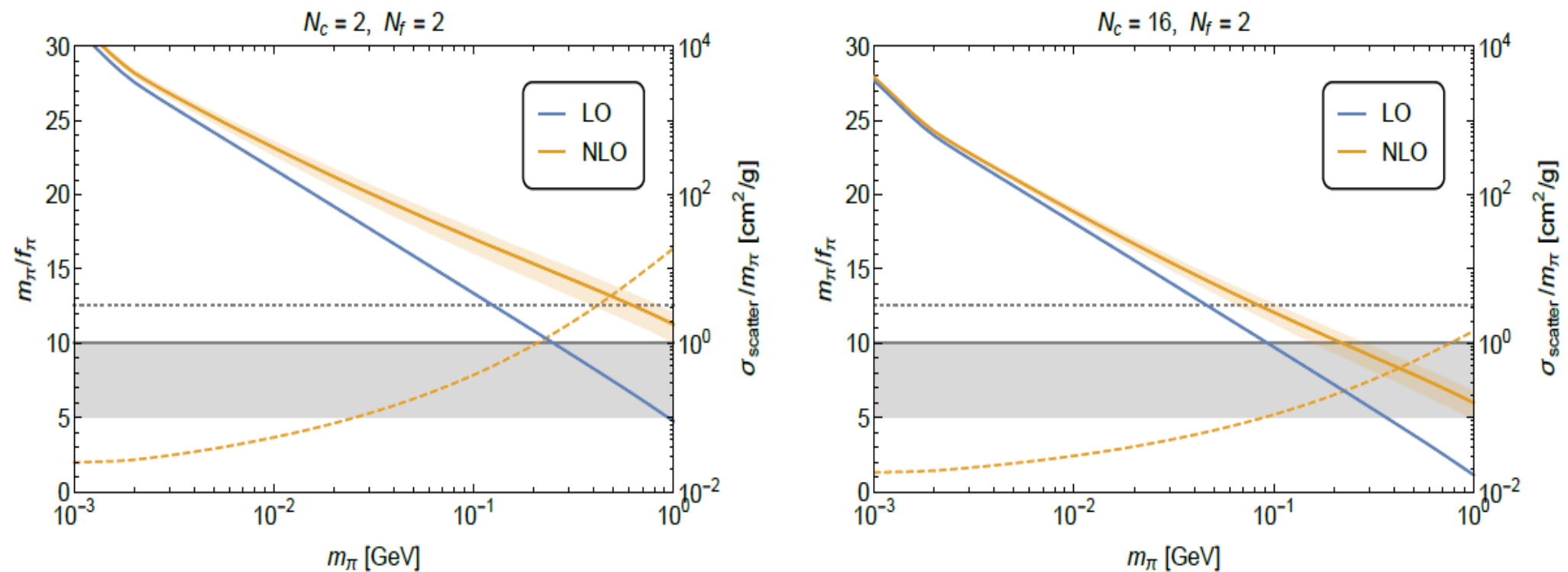
$$m_\pi/f_\pi < 2\pi$$

$N_c > 3$ is required due to bounds on self-scattering.

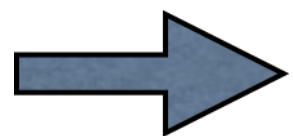
Similar results for $SU(N_f)/SO(N_f)$ or $SU(2N_f)/Sp(2N_f)$.

NLO corrections

- $2 \rightarrow 2$: LO, $3 \rightarrow 2$: NLO [Hansen et al, 2015]



NLO corrections enhance $2 \rightarrow 2$ scattering cross sections, making the self-interaction bound stronger.



Need a large color or large meson decay constant: additional annihilation channel ?

Twin Higgs & mirror symmetry

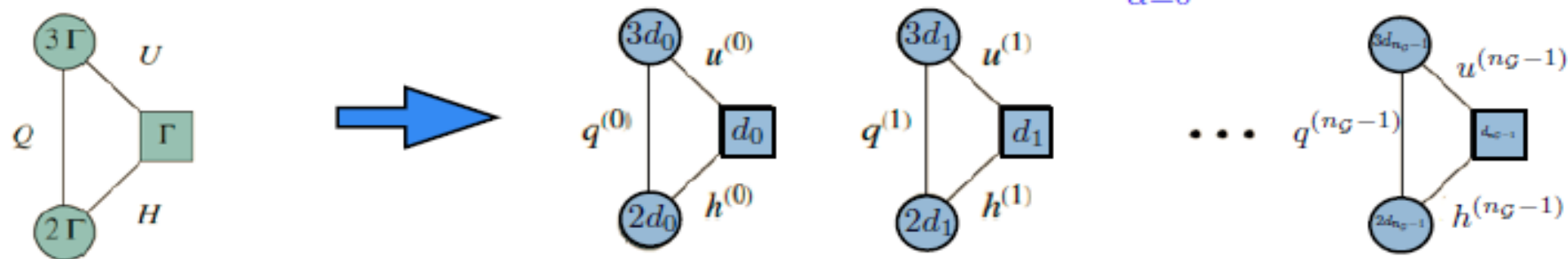
- **Twin Higgs:** $[SU(3)_A \times SU(2)_A] \times [SU(3)_B \times SU(2)_B] \times Z_2$
[Chacko, Goh, Harnik, 2005]

$$\mathcal{L}_Y = -y_A H_A q_A u_A^c - y_B H_B q_B u_B^c, \quad y_A = y_B;$$

$$\Rightarrow \delta m_h^2 = \frac{3}{4\pi^2} (y_A^2 - y_B^2) \Lambda^2 = 0 : \text{ no quadratic divergence.}$$

- **Two-point function on orbifolds inherits the full symmetry.**
[Craig, Knapen, Longhi, 2014]

$$[SU(3\Gamma) \times SU(2\Gamma)]_{\text{local}} \times SU(\Gamma)_{\text{global}} / \mathcal{G} \quad (\Gamma = |\mathcal{G}| = \sum_{\alpha=0}^{n_{\mathcal{G}}-1} (d_{\alpha})^2, \quad d_{\alpha} : \text{dim of irrep } r_{\alpha})$$



$$V^{(1)} \supset -\frac{3}{8\pi^2} \Lambda^2 \sum_{\alpha=0}^{n_{\mathcal{G}}-1} (y^{(\alpha)})^2 |h^{(\alpha)}|^2 \sim y^2 \Lambda^2 \sum_{\alpha} |h^{(\alpha)}|^2.$$

$$y^{(\alpha)} = \frac{y}{\sqrt{d_{\alpha}}}$$

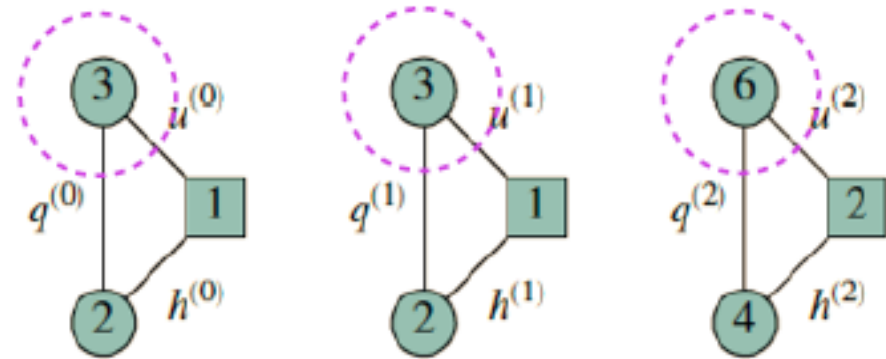
Twin Higgs: $SU(6) \times SU(4) / Z_2.$

Mirror QCD

- S_3 orbifolds: $SU(3)_A \times SU(3)_B \times SU(6)_B$ QCD

$$SU(18) \times SU(12) \times SU(6)_f / S_3$$

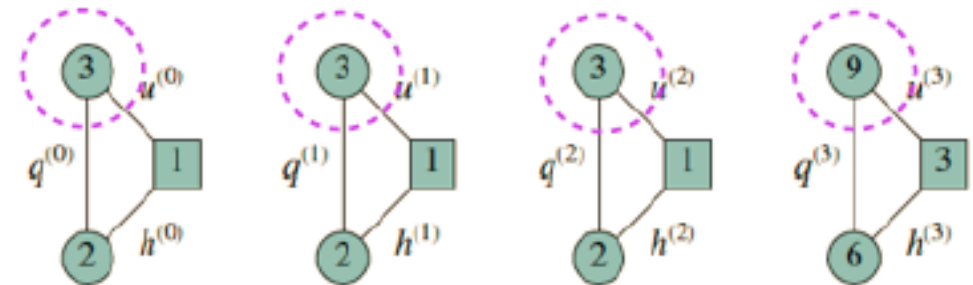
$$S_3 : d_0 = 1, d_1 = 1, d_2 = 2$$



- A_4 orbifolds: $SU(3)_A \times SU(3)_B \times SU(3')_B \times SU(9)_B$ QCD

$$SU(36) \times SU(24) \times SU(12)_f / A_4$$

$$A_4 : d_0 = 1, d_1 = 1, d_2 = 1, d_3 = 3$$



- Gauge loops on S_3 or A_4 lead to quadratic divergence.

$$V^{(1)} \supset \frac{3}{16\pi^2} \Lambda^2 \sum_{\alpha=1}^{n_G} C_2(h^{(\alpha)}) (g^{(\alpha)})^2 |h^{(\alpha)}|^2 \longrightarrow \delta m_h^2 \sim \frac{g^2}{N} \Lambda^2 (1 - 1/d_{n_Q}^2)$$

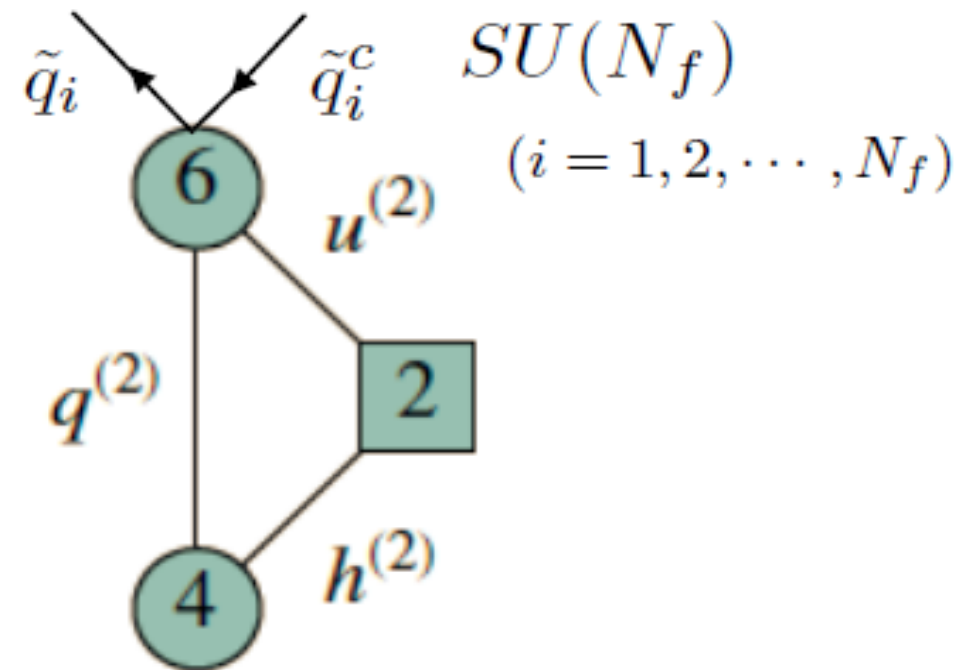
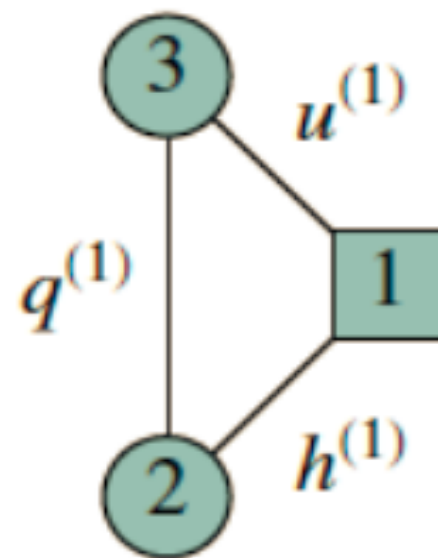
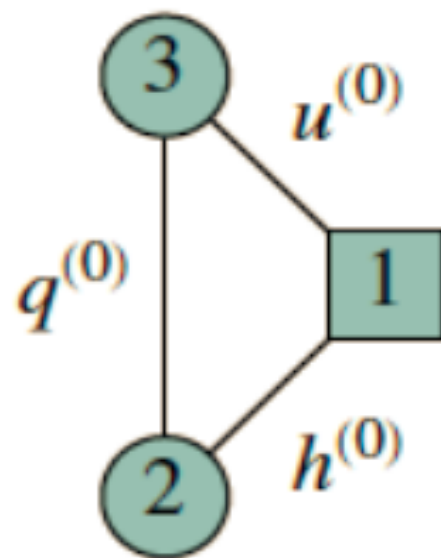
$$g^{(\alpha)} = \frac{g}{\sqrt{d_\alpha}} \quad (d_{n_Q} : \text{irrep of largest dim.})$$

But, they are parametrically small!

SIMP mesons on orbifolds

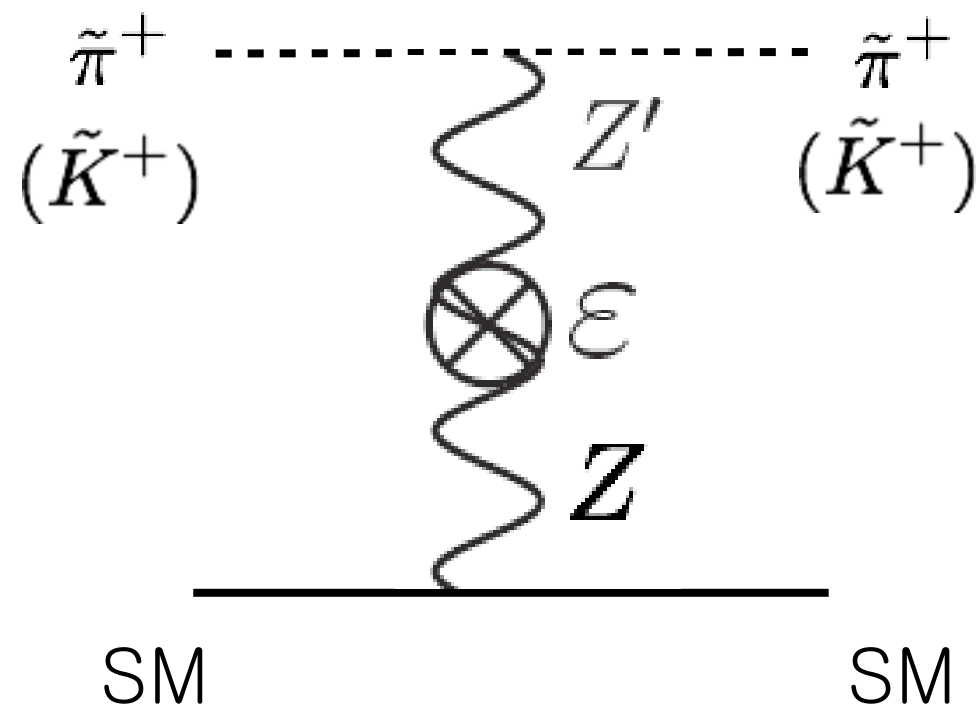
- Light dark quarks, that are vector-like under QCD partner group, can be introduced as split multiplets, without spoiling naturalness.
- Z' (part of the full gauge symmetry) mediates between the SM and dark mesons.

e.g. $SU(18) \times SU(12) \times SU(6)_f / S_3$



Dark mesons & Z' -portal

- Dark meson can be in kinetic equilibrium with the SM particles via Z' - Z kinetic mixing.



$$\mathcal{L}_{\text{mix}} = -\frac{\epsilon}{2 \cos \theta_W} F'_{\mu\nu} F^{\mu\nu}$$

$$\Rightarrow \langle \sigma v \rangle_{\text{kin}} \approx \frac{768 \alpha \alpha_D \epsilon^2}{\pi N_\pi} \frac{m_\pi^2}{m_{Z'}^4} \left(\frac{T_F}{m_\pi} \right).$$

cf. Higgs-portal coupling does not work, because leptons in thermal bath have small Yukawa couplings.

- $2 \rightarrow 2$ annihilation with Z' -portal could be suppressed (or be as large as $3 \rightarrow 2$ ann).

\Rightarrow $3 \rightarrow 2$ dominance: SIMP conditions

WZW with Z'

[Witten, 1983]

- Dark quarks are vector-like under broken $U(1)'$.
- Modified WZW with $U(1)'$:

$$S = S_0(D_\mu U, D_\mu U^{-1}) + S_{\text{WZW}}(U, U^{-1}) - eN_c \int d^4x A'_\mu J^\mu$$

$$+ \frac{ie^2 N_c}{24\pi^2} \int d^4x \epsilon^{\mu\nu\rho\sigma} \partial_\mu A'^\nu A'_\rho \text{Tr}[Q^2 \partial_\sigma U U^{-1} + Q^2 U^{-1} \partial_\sigma U + Q U Q U^{-1} \partial_\sigma U U^{-1}],$$

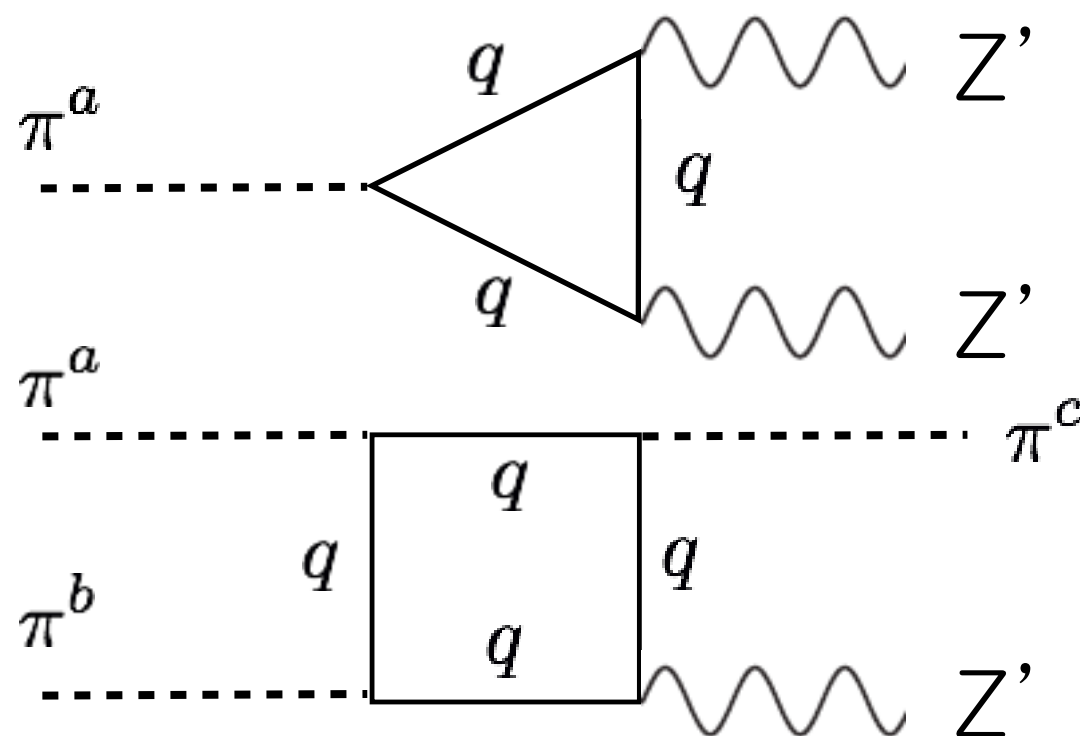
$$J^\mu = \frac{1}{48\pi^2} \epsilon^{\mu\nu\rho\sigma} \text{Tr}[Q \partial_\nu U U^{-1} \partial_\rho U U^{-1} \partial_\sigma U U^{-1} + Q U^{-1} \partial_\nu U U^{-1} \partial_\rho U U^{-1} \partial_\sigma U].$$

AVV anomalies.

➔ DM decay

AAAV anomalies.

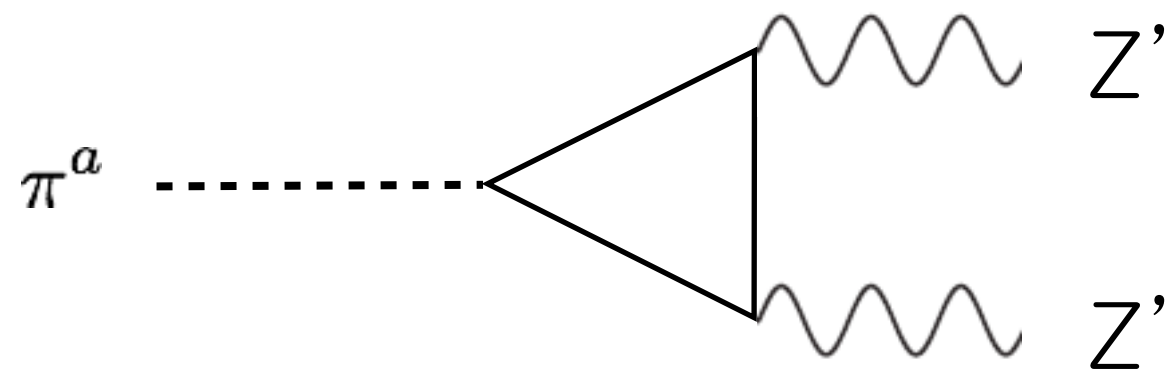
➔ $2 \rightarrow 2$ ann



Stability of dark mesons

[HML, Seo, 2015]

- Stability of dark neutral mesons requires the **cancellation of AVV anomalies**.



$$\propto \text{Tr}(Q_D^2 T^a) = 0$$

$$\text{if } Q_D^2 = I.$$

$$\rightarrow Q_D = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$$

: flavor non-universal charges

cf. QCD: $Q = \text{diag}(2/3, -1/3, -1/3)$

$$D_\mu U = \partial_\mu U + ig_D [Q_D, U] Z'_\mu; \quad \tilde{\pi}^\pm, \tilde{K}^\pm : \pm 2 \text{ charges.}$$

- $\pi \pi \rightarrow \pi Z'$ is forbidden for $m_{Z'} > m_\pi$.

Dark flavor violation

- Flavor non-universal U(1) charges breaks flavor symmetry leads to meson mass splitting:

$$\mathcal{L}_{\text{mass}} = -\frac{1}{2}\Lambda^3 \text{Tr}[M_q(U + U^{-1})] - c\alpha_D \Lambda^4 \text{Tr}[QUQU^{-1}].$$

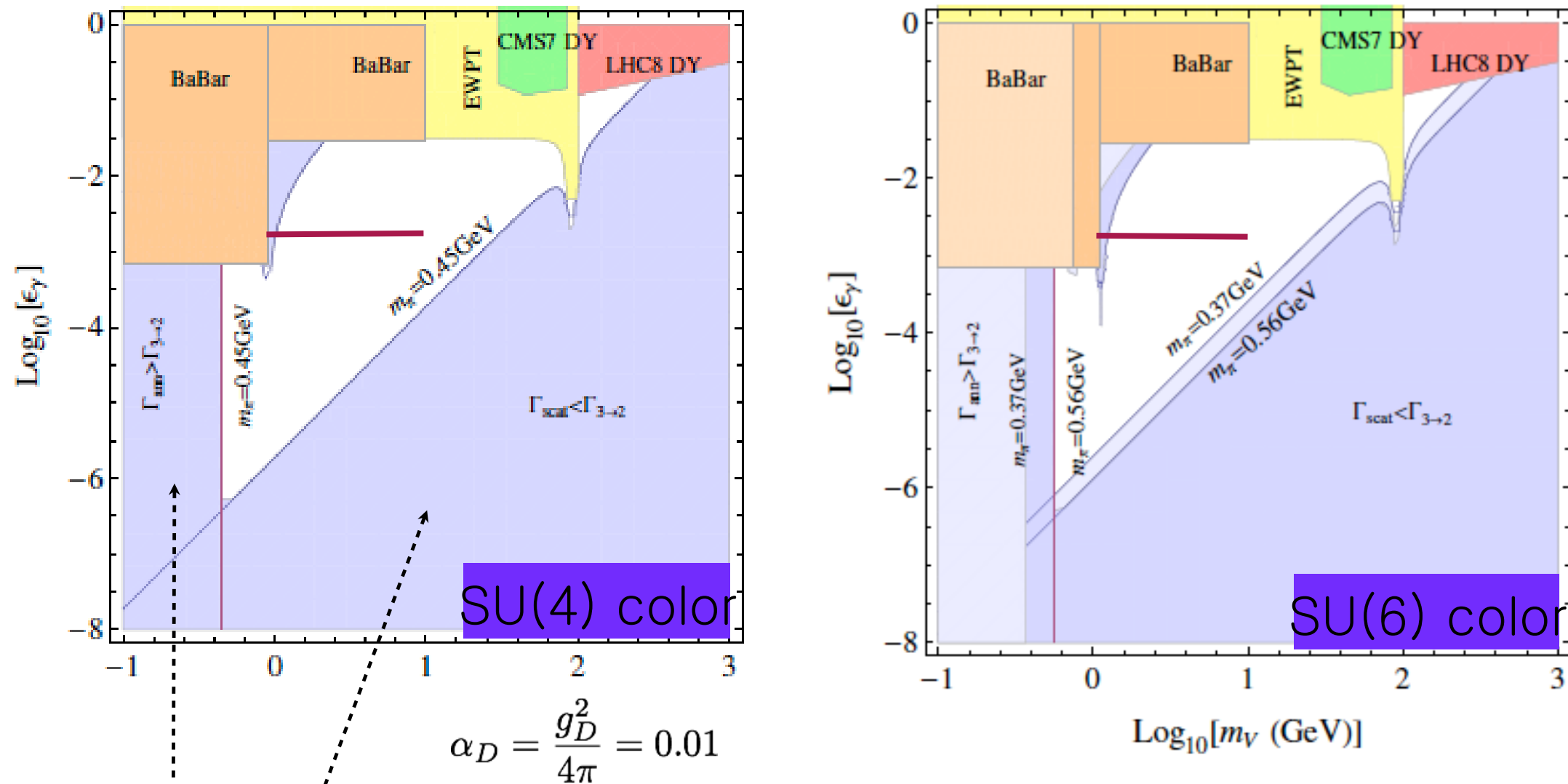
→ $\Delta m_\pi^2 \sim \frac{\alpha_D \Lambda^4}{F^2} \sim \alpha_D F^2 \lesssim 0.01 m_\pi^2 : \alpha_D \lesssim 0.01$

- Higher dimensional operators must be suppressed by high cutoff or small coupling:

$$\mathcal{L}_{hdo} = \frac{1}{M^2} (\bar{q} \gamma_\mu \gamma^5 T^a q) (\bar{l} \gamma^\mu l) \sim \frac{F}{M^2} \partial_\mu \pi^a (\bar{l} \gamma^\mu l)$$

→ $\Gamma_\pi \simeq \frac{F^2 m_\pi m_l^2}{8\pi M^4}, \quad \text{DM stability: } M > 10^9 \text{ GeV.}$

Z' at colliders



SIMP conditions

$e^+e^- \rightarrow \gamma Z' \rightarrow \gamma(l^+l^-)$, $e^+e^- \rightarrow \gamma + \text{MET}$ (BaBar),
 $h \rightarrow ZZ'$ (CMS 8TeV), Drell-Yan, dileptons.

- SIMP conditions are complementary in constraining Z' parameters to direct Z' searches.

SIMP DM from
discrete symmmetries

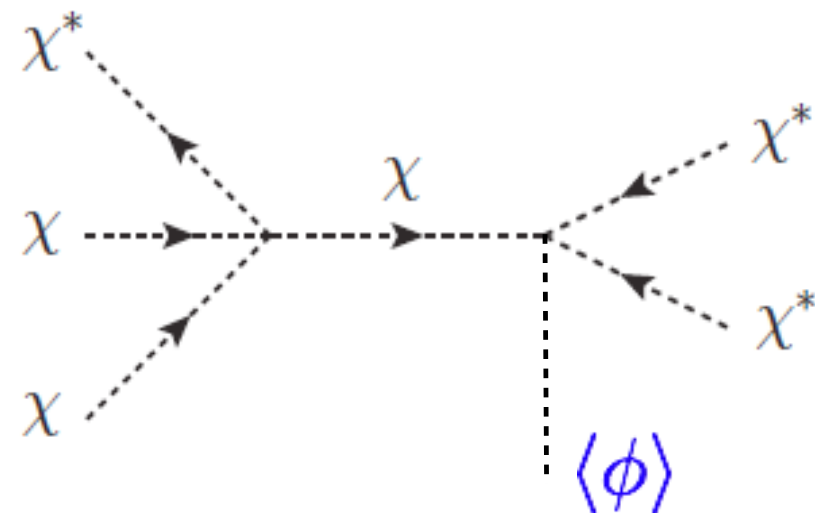
Gauged Z_3 and SIMP

- 5-point SIMP interaction is inconsistent with Z_2 and flavor symmetry is broken.
- Z_3 is the minimal symmetry for stabilizing SIMP, a remnant of a local $U(1)$.
- Built-in Z' gauge boson communicates with the SM via the kinetic mixing.

	ϕ	χ
$U(1)_V$	+3	+1

Table 1: $U(1)_V$ charges.

$$\langle \phi \rangle = \frac{1}{\sqrt{2}} v' \quad \longrightarrow \quad U(1)_V \rightarrow Z_3.$$



A Z_3 Model

[Belanger et al(2012); Ko, Tang(2014);
S.M. Choi, HML, 2015]

- χ : Dark Matter, ϕ : Dark Higgs, V : Dark photon.

$$\mathcal{L} = -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} - \frac{1}{2}\sin\xi V_{\mu\nu}B^{\mu\nu} + |D_\mu\phi|^2 + |D_\mu\chi|^2 + |D_\mu H|^2 - V(\phi, \chi, H)$$

$$D_\mu\chi = (\partial_\mu - iq_\chi g_D V_\mu)\chi$$

$V(\phi, \chi, H) = V_{\text{DM}} + V_{\text{SM}}$ with

$$V_{\text{DM}} = -m_\phi^2|\phi|^2 + m_\chi^2|\chi|^2 + \lambda_\phi|\phi|^4 + \lambda_\chi|\chi|^4 + \lambda_{\phi\chi}|\phi|^2|\chi|^2 \\ + \left(\frac{\sqrt{2}}{3!}\kappa\phi^\dagger\chi^3 + \text{h.c.}\right) + \lambda_{\phi H}|\phi|^2|H|^2 + \lambda_{\chi H}|\chi|^2|H|^2,$$

$$V_{\text{SM}} = -m_H^2|H|^2 + \lambda_H|H|^4.$$

Scalar SIMP DM

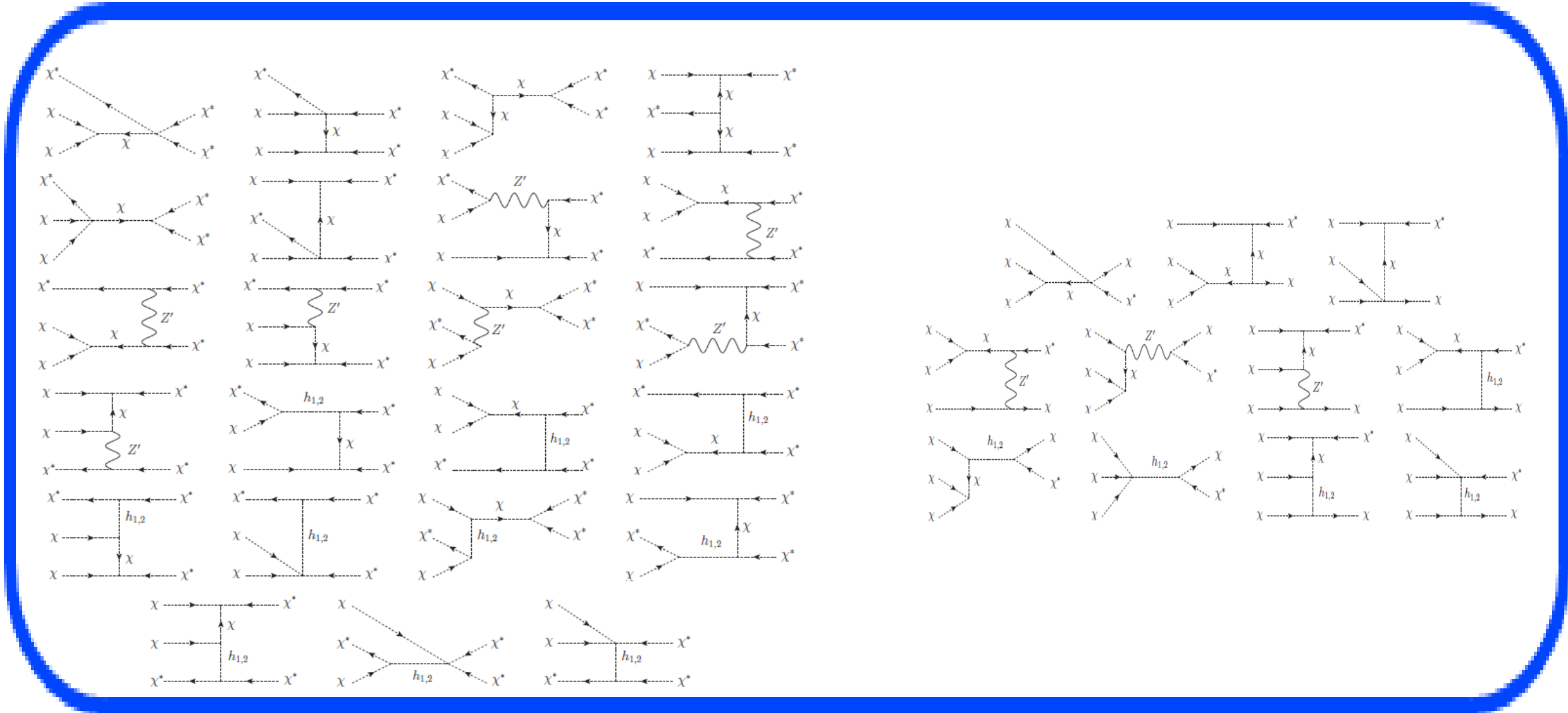
- $2 \rightarrow 2$ annihilation channels are forbidden for heavy dark Higgs and Z' .
- $3 \rightarrow 2$ annihilation channels are through Higgs + Z' exchanges:

$$\begin{aligned} \langle \sigma v_{\text{rel}}^2 \rangle_{3 \rightarrow 2} &= \frac{1}{4} (\langle \sigma v_{\text{rel}}^2 \rangle_{\chi\chi\chi^* \rightarrow \chi^*\chi^*} + \langle \sigma v_{\text{rel}}^2 \rangle_{\chi\chi\chi \rightarrow \chi\chi^*}) \\ &= \frac{\sqrt{5}}{1536\pi m_\chi^3} (|\mathcal{M}_{\chi\chi\chi^* \rightarrow \chi^*\chi^*}|^2 + |\mathcal{M}_{\chi\chi\chi \rightarrow \chi\chi^*}|^2) \equiv \frac{a_{\text{eff}}^3}{m_\chi^5}. \end{aligned}$$

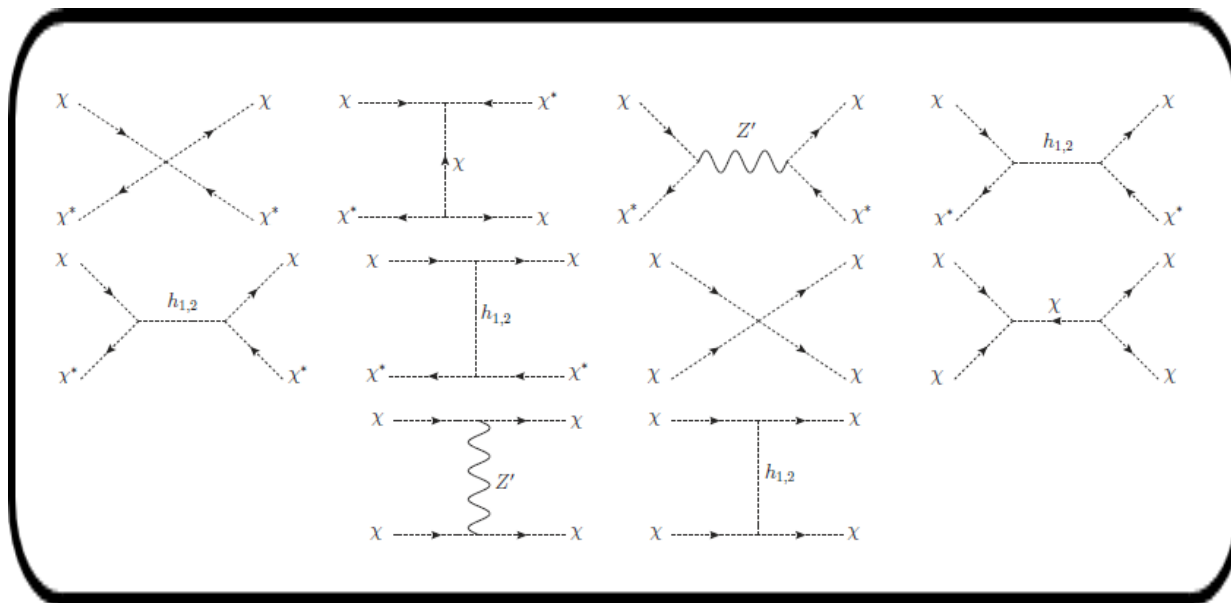
$$|\mathcal{M}_{\chi\chi\chi^* \rightarrow \chi^*\chi^*}|^2 = \frac{R^2}{16m_\chi^2} \left(74\lambda_\chi - 117R^2 - \frac{200g_D^2 m_\chi^2}{m_\chi^2 + m_{Z'}^2} + \frac{24\lambda_{\phi\chi} m_\chi^2 (3m_\chi^2 - 2m_{h_1}^2) - \lambda_{\phi\chi}^2 (43m_\chi^2 - 37m_{h_1}^2) m_{Z'}^2 / (9g_D^2)}{(4m_\chi^2 - m_{h_1}^2)(m_\chi^2 + m_{h_1}^2)} \right)^2$$

$$|\mathcal{M}_{\chi\chi\chi \rightarrow \chi\chi^*}|^2 = \frac{3R^2}{m_\chi^2} \left(2\lambda_\chi + 9R^2 + \frac{25g_D^2 m_\chi^2}{m_\chi^2 + m_{Z'}^2} + \frac{2\lambda_{\phi\chi} m_\chi^2 (13m_\chi^2 - 2m_{h_1}^2) - \lambda_{\phi\chi}^2 (19m_\chi^2 - m_{h_1}^2) m_{Z'}^2 / (9g_D^2)}{(9m_\chi^2 - m_{h_1}^2)(m_\chi^2 + m_{h_1}^2)} \right)^2 \quad R \equiv \sqrt{2}\kappa v' / (6m_\chi).$$

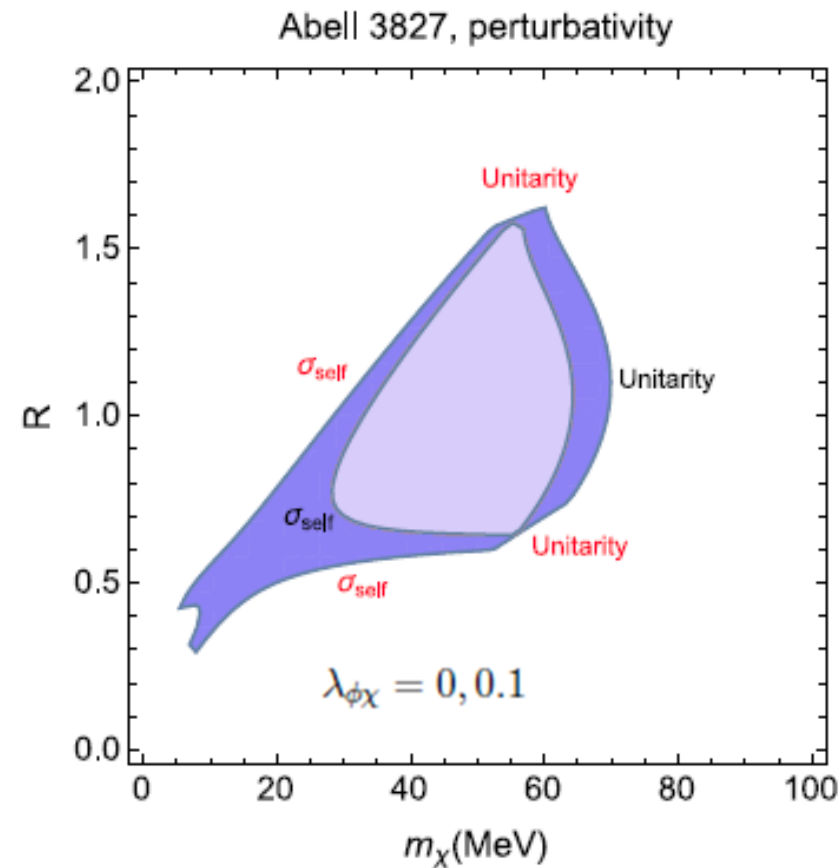
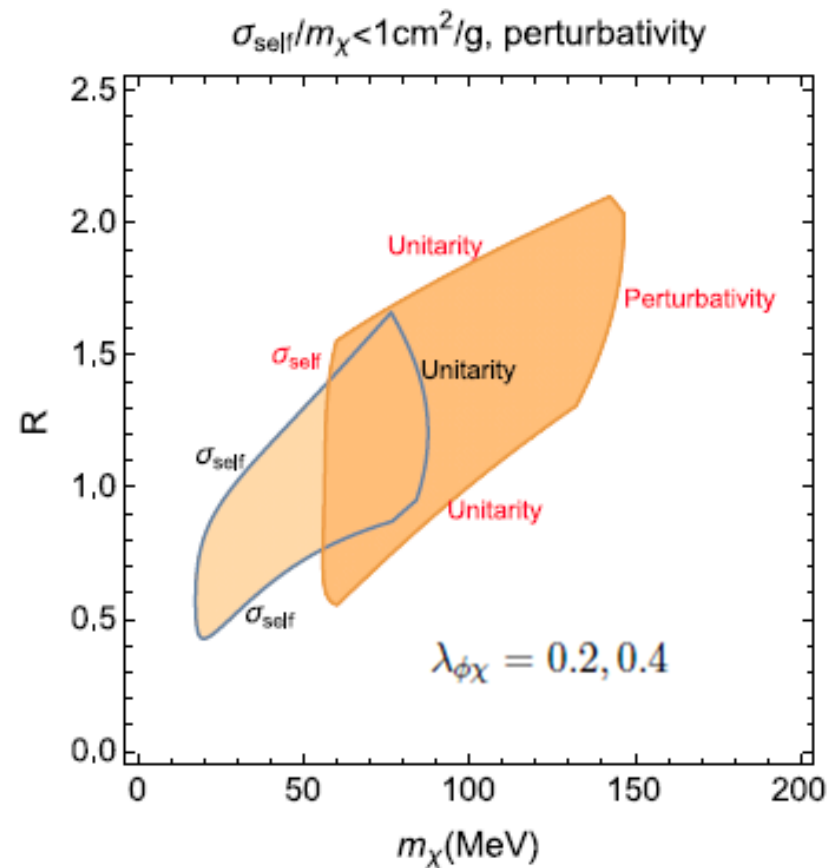
3 → 2



2 → 2



Bounds on self-interaction



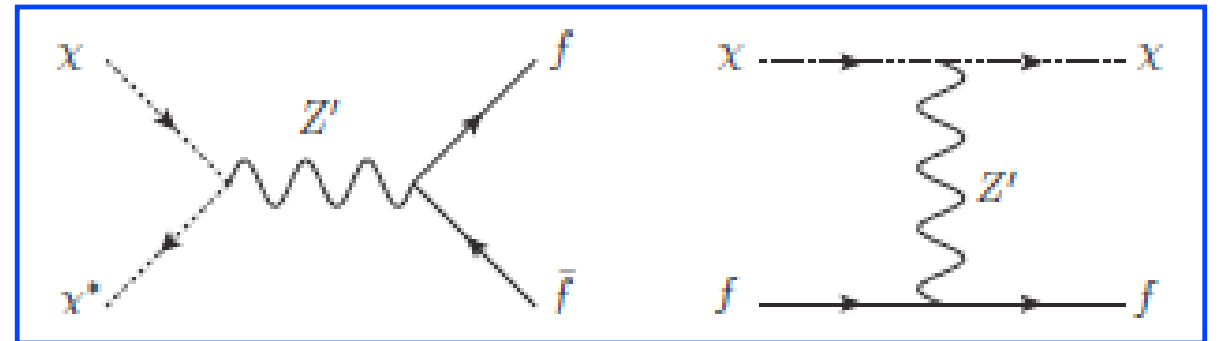
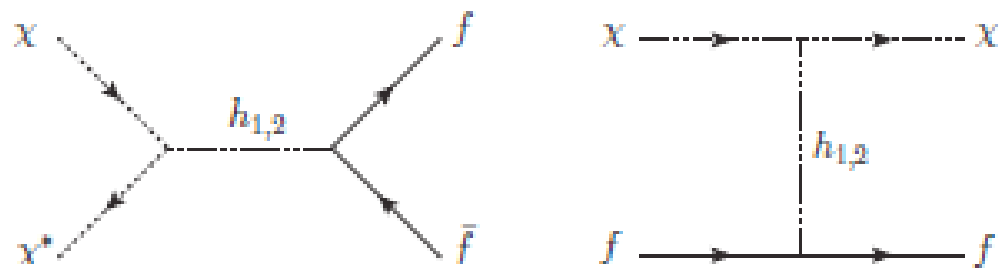
Abell 3827

$$\sigma_{\text{self}}/m_\chi = 1 - 3 \text{ cm}^2/\text{g}$$

$$m_{Z'} = 5m_\chi, g_D = 0.1 \text{ and } m_{h_1} = 1.5m_\chi.$$

- SIMP relic density: $m_\chi = 0.03 \alpha_{\text{eff}} (T_{\text{eq}}^2 M_P)^{1/3}$
- Bullet cluster & halo shape: $\sigma_{\text{self}}/m_\chi \lesssim 1 \text{ cm}^2/\text{g}$
- Unitarity, perturbativity: $\lambda_\chi < 4\pi, |\mathcal{M}_{\chi\chi} + \mathcal{M}_{\chi\chi^*}| < 8\pi.$

Kinetic equil. condition



Higgs-portal:

negligible for kinetic scatt.,
safe for Higgs (invisible) signals & indirect detections

Z'-portal:

works for kinetic scatt.,
bounded by collider searches,
safe for indirect detections.

- SIMP conditions: $n_{\text{DM}} \langle \sigma v_{\text{rel}} \rangle_{\text{ann}} < n_{\text{DM}}^2 \langle \sigma v_{\text{rel}}^2 \rangle_{3 \rightarrow 2} < n_{\text{SM}} \langle \sigma v_{\text{rel}} \rangle_{\text{kin}}$

$$\langle \sigma v_{\text{rel}} \rangle_{\text{ann}} = \frac{2\varepsilon^2 e^2 g_D^2 m_\chi^2}{\pi[(4m_\chi^2 - m_{Z'}^2)^2 + m_{Z'}^2 \Gamma_{Z'}^2]} \left(\frac{T}{m_\chi} \right) \equiv \frac{\delta_1^2}{m_\chi^2}$$

$$\langle \sigma v_{\text{rel}} \rangle_{\text{scatt}} = \frac{3\varepsilon^2 e^2 g_D^2 m_\chi^2}{2\pi m_{Z'}^4} \left(\frac{T}{m_\chi} \right) \equiv \frac{\delta_2^2}{m_\chi^2}$$

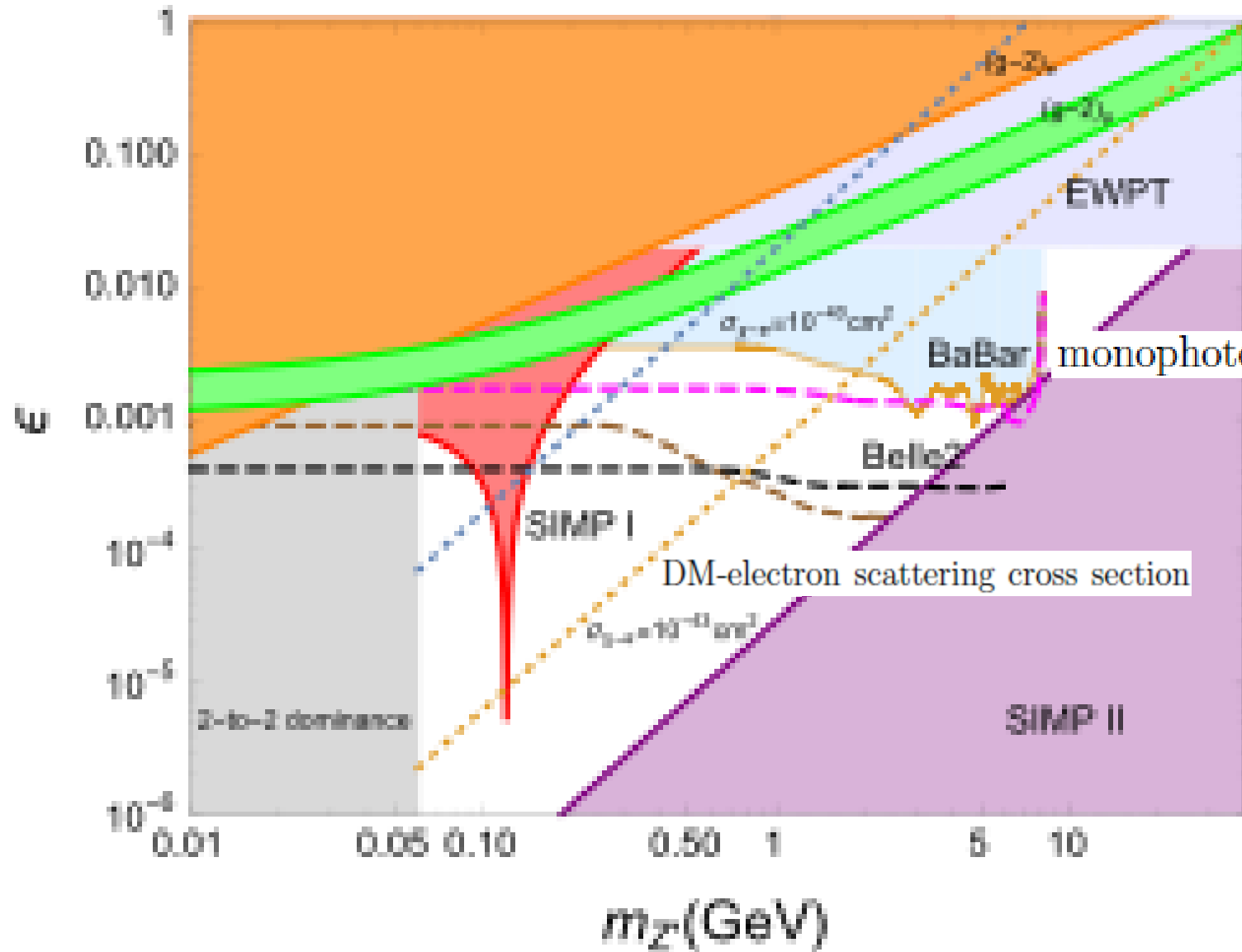
$$\varepsilon \simeq \cos \theta_W \xi$$

$$\delta_1 \lesssim 2.4 \times 10^{-6} \alpha_{\text{eff}},$$

$$\delta_2 \gtrsim 10^{-9} \alpha_{\text{eff}}^{1/2}.$$

SIMP & Z' searches

$$m_\chi = 60 \text{ MeV}, g_D = 0.3$$



monophoton + MET at BaBar

BaBar
monophoton + dilepton
 $10^{-4} - 10^{-3}$ ($\text{BR}(l\bar{l}) = 1$)
for $m_{Z'} = 0.02 - 10.2$ GeV

beam dump (E137)
 10^{-3} below $m_{Z'} = 0.1$ GeV.

- SIMP conditions are complementary for Z' searches at colliders.

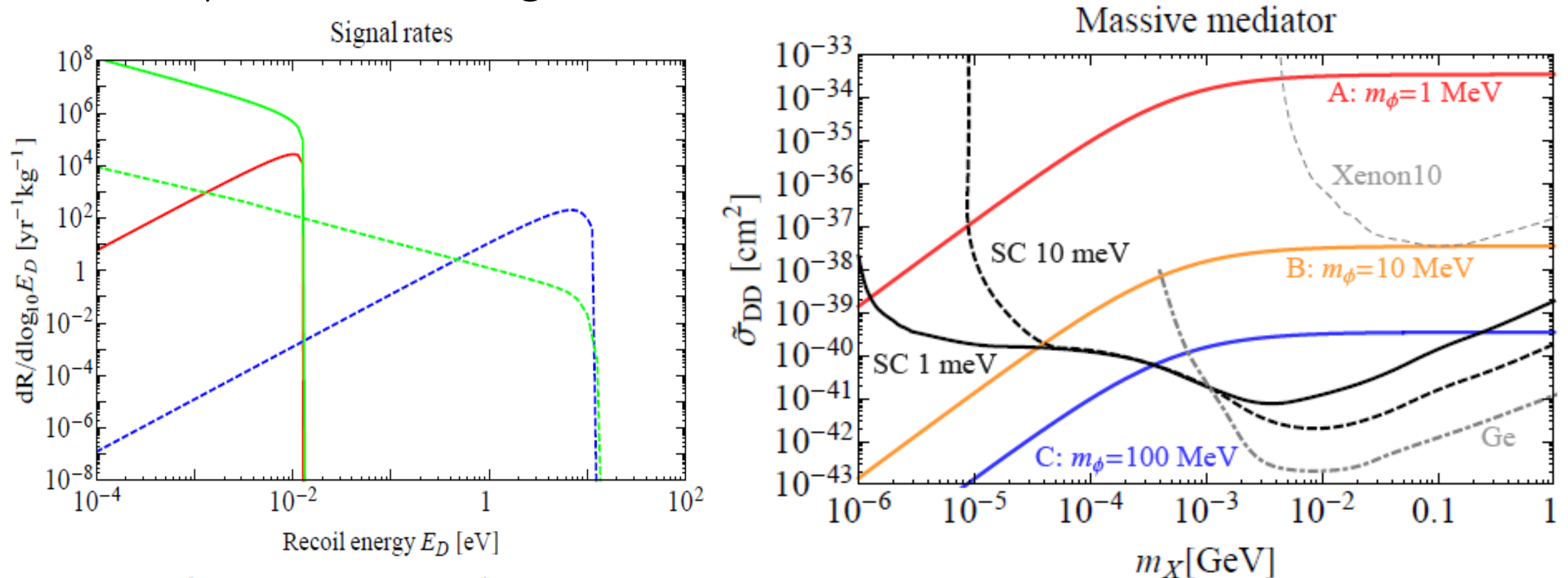
Direct detection

- SIMP dark matter scatters off electrons, leading to small recoil energy: $E = \frac{q^2}{2m_e} \lesssim 20 \text{ eV}$.

$$\sigma_{\text{DD}} = \frac{\epsilon^2 e^2 g_D^2 \mu^2}{\pi m_{Z'}^4} \quad (q = \mu v_{\text{DM}}, \mu = m_e m_\chi / (m_e + m_\chi))$$

$$\text{XENON10: } \sigma_{\text{DD}} < 2 \times 10^{-36} \text{ cm}^2, \quad m_\chi = 30 \text{ MeV}.$$

Superconducting detectors? [Hochberg et al (2015)]



Blue: $(m_\phi, m_\chi, \alpha_X, g_e) = (100 \text{ MeV}, 100 \text{ MeV}, 0.1, 3 \times 10^{-5})$

A Z_5 model

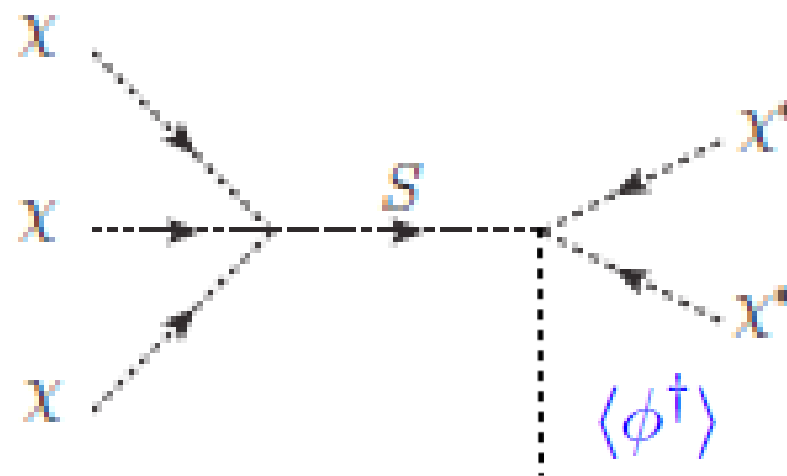
[S.M.Choi, HML, to appear]

- 5-point interaction is picked up by Z_5 , mediated by a heavy singlet scalar S (cf. no cubic coupling for DM).

	ϕ	χ	S
$U(1)_V$	+5	+1	+3

Table 1: $U(1)_V$ charges.

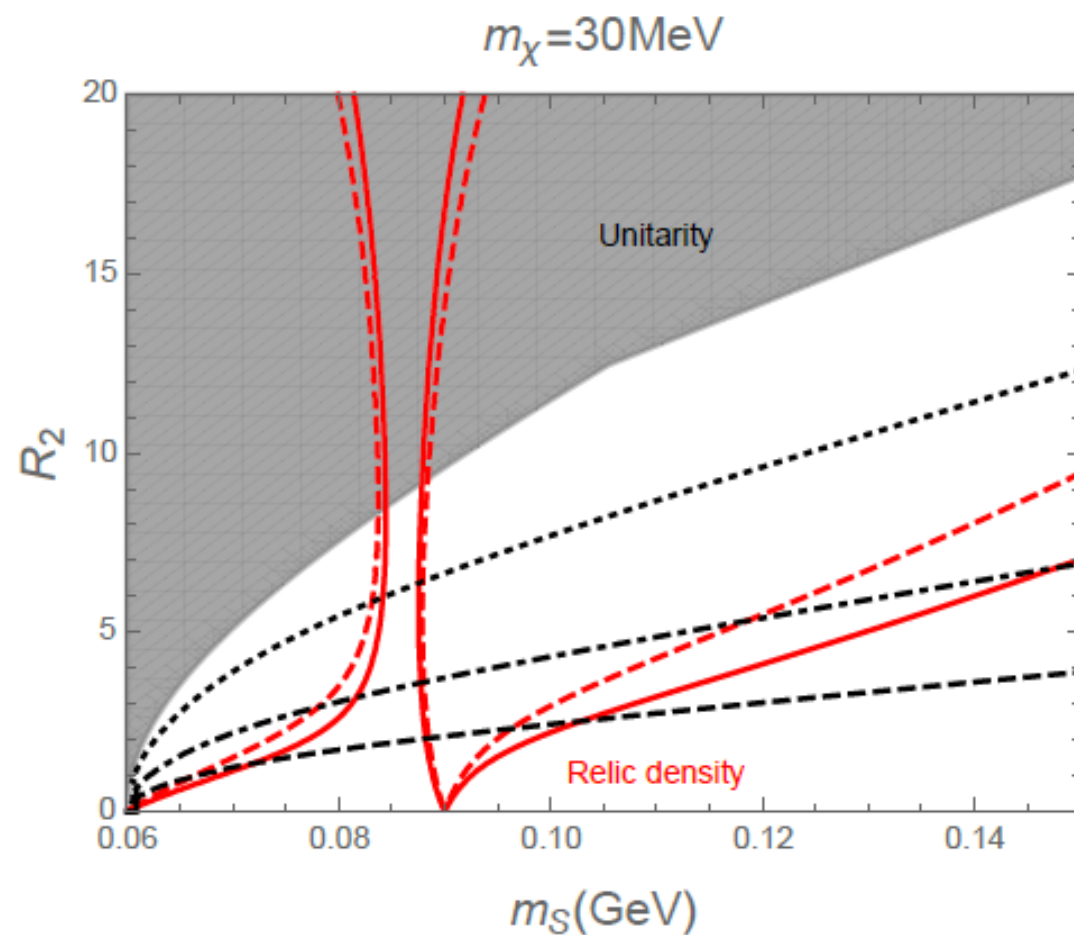
$$\mathcal{L}_{\text{int}} \supset \frac{1}{\sqrt{2}}\lambda_1\phi^\dagger S^2\chi^\dagger + \frac{1}{\sqrt{2}}\lambda_2\phi^\dagger S\chi^2 + \frac{1}{6}\lambda_3 S^\dagger\chi^3 + \text{h.c.}$$



- Z' again makes SIMP DM in kinetic equilibrium.
- Singlet scalar S can be stable too.

Resonant $3 \rightarrow 2$ in Z_5

- 5-point interaction in Z_5 can be enhanced near resonance.



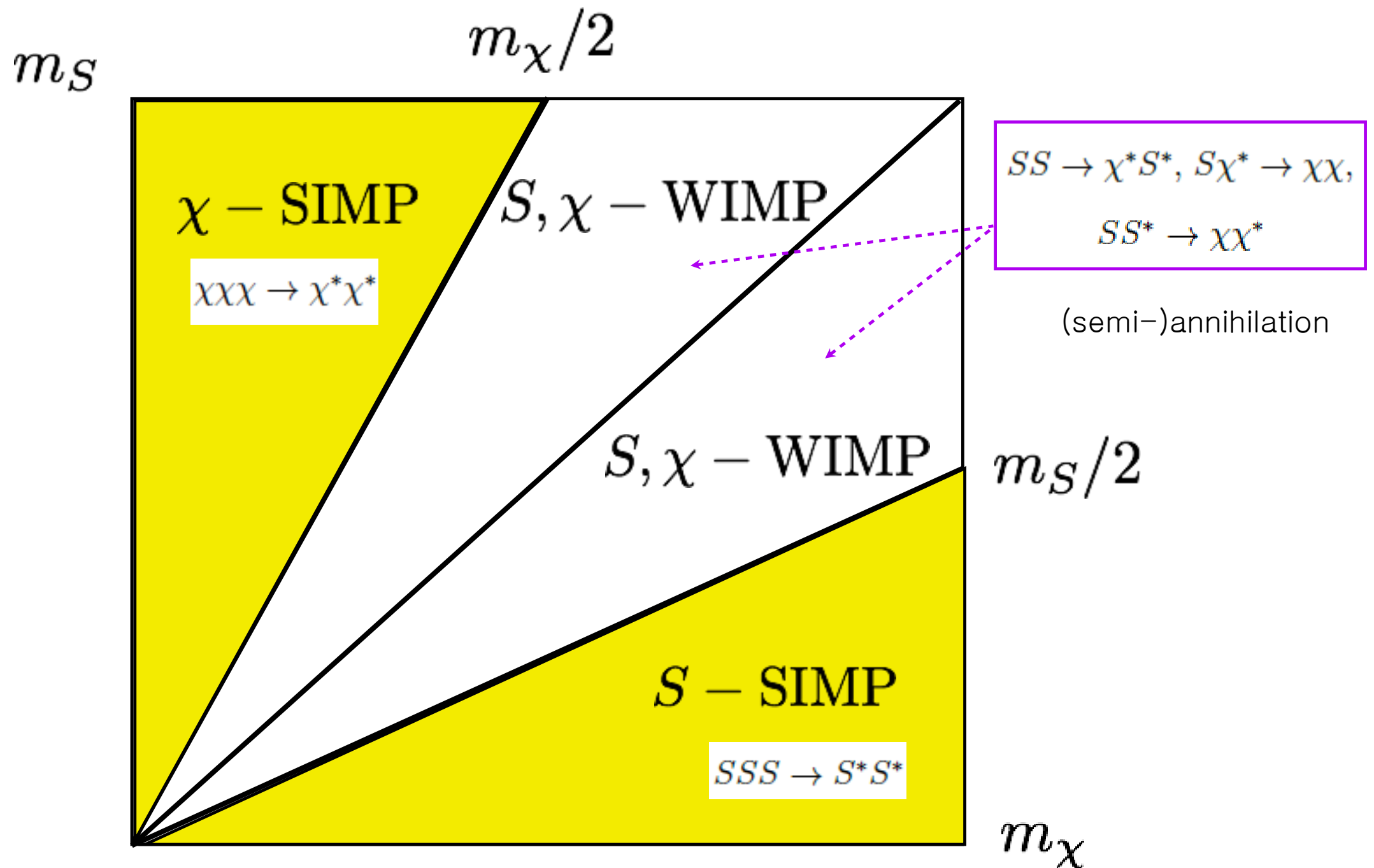
$$\langle \sigma v^2 \rangle_{3 \rightarrow 2} \propto \frac{1}{(9m_\chi^2 - m_S^2)^2 + \Gamma_S^2 m_S^2}$$

$$\lambda_1 = 0; \quad R_2 \equiv \lambda_2 v' / (\sqrt{2} m_\chi)$$

$$\lambda_3 = 8\pi \quad \text{and} \quad \lambda_3 = 6\pi$$

safe from the bounds from self-interactions (with potentially large NLO).

Phase diagram of DM



WIMP phases need a sizable annihilation into the SM, e.g. Z' portal.

Conclusions

- SIMP paradigm leads to testable scenarios via DM self-interactions as well as possibly, messengers particles.
- SIMP dark mesons can be in kinetic equilibrium with Z' portal and remain stable.
- Scalar SIMP dark matter with discrete gauge symmetries has a built-in Z' -portal.
- For discrete symmetries of high degree, we need a scalar mediator for 5-point interactions, which can be enhanced near resonance.