

Electroweak Precision Physics from LEP to ILC

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ILC PHYSICS IN FLORENCE

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Outline

- Electroweak precision observables – Standard Model
- Theory versus data
- Perspectives
- Extensions of the SM – Supersymmetry
- Outlook

Standard Model

- the symmetry group $SU(2) \times U(1) \times SU(3)_C$
- the principle of local gauge invariance
 - fermion – vector boson interaction
 - vector boson self-interaction
- Higgs mechanism and Yukawa interactions
 - masses $M_W, M_Z, m_{\text{fermion}}$

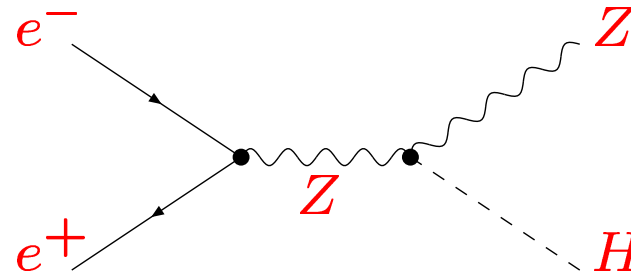
renormalizable quantum field theory

accurate theoretical predictions

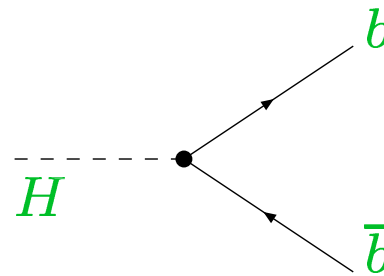
- detect deviations → “new physics” ?

Search for the Standard Model Higgs at LEP

Dominant production process: $e^+e^- \rightarrow ZH$



Dominant decay process: $H \rightarrow b\bar{b}$

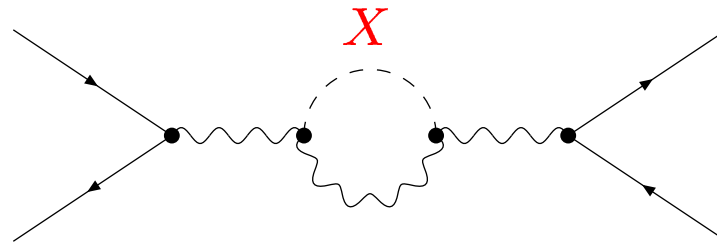


exclusion limit (95% C.L.): $M_H > 114.4 \text{ GeV}$

Precision observables – SM

Test of theory at quantum level:

Sensitivity to loop corrections

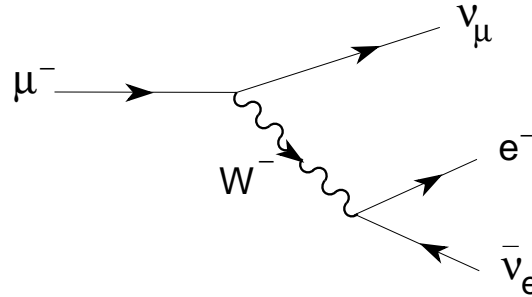


- μ lifetime: $M_W, \Delta r, G_F$
- Z observables: $g_V, g_A, \sin^2 \theta_{\text{eff}}, \Gamma_Z, \dots$

sensitivity to heavy internal particles (X)

Standard Model: $X = \text{Higgs, top}$

$M_W - M_Z$ correlation



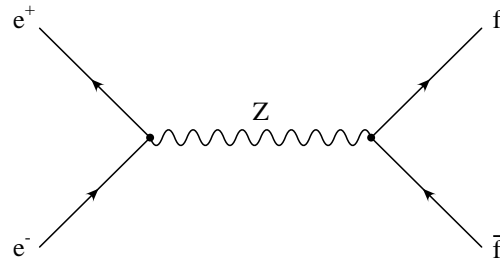
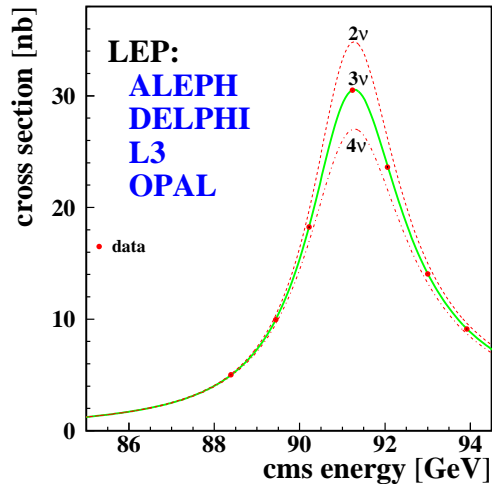
$$\frac{G_F}{\sqrt{2}} = \frac{\pi\alpha}{M_W^2 (1 - M_W^2/M_Z^2)} (1 + \Delta r)$$

Δr : quantum correction, $\Delta r = \Delta r(m_t, M_H)$

$\rightarrow M_W = M_W(\alpha, G_F, M_Z, m_t, M_H)$

complete two-loop calculation available

Z resonance



- effective Z boson couplings with higher-order $\Delta g_{V,A}$

$$g_V^f \rightarrow g_V^f + \Delta g_V^f, \quad g_A^f \rightarrow g_A^f + \Delta g_A^f$$

- effective ew mixing angle (for $f = e$):

$$\sin^2 \theta_{\text{eff}} = \frac{1}{4} \left(1 - \text{Re} \frac{g_V^e}{g_A^e} \right) = \kappa \cdot \left(1 - \frac{M_W^2}{M_Z^2} \right)$$

EW 2-loop calculations for Δr

Freitas, Hollik, Walter, Weiglein

Awramik, Czakon

Onishchenko, Veretin

EW 2-loop calculations for $\sin^2 \theta_{\text{eff}}$

Awramik, Czakon, Freitas, Weiglein

Awramik, Czakon, Freitas

Hollik, Meier, Uccirati

universal terms beyond 2-loop order (EW and QCD)

van der Bij, Chetyrkin, Faisst, Jikia, Seidensticker

Faisst, Kühn Seidensticker, Veretin

Boughezal, Tausk, van der Bij

Schröder, Steinhauser

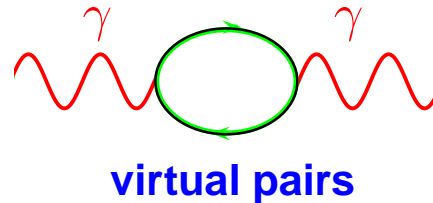
Chetyrkin, Faisst, Kühn

Chetyrkin, Faisst, Kühn, Maierhofer, Sturm

Boughezal, Czakon

charge renormalization $e + \delta e$ involves

photon vacuum polarization



$$\Pi^\gamma(M_Z^2) - \Pi^\gamma(0) \equiv \Delta\alpha \quad \rightarrow \quad \alpha(M_Z) = \frac{\alpha}{1 - \Delta\alpha}$$

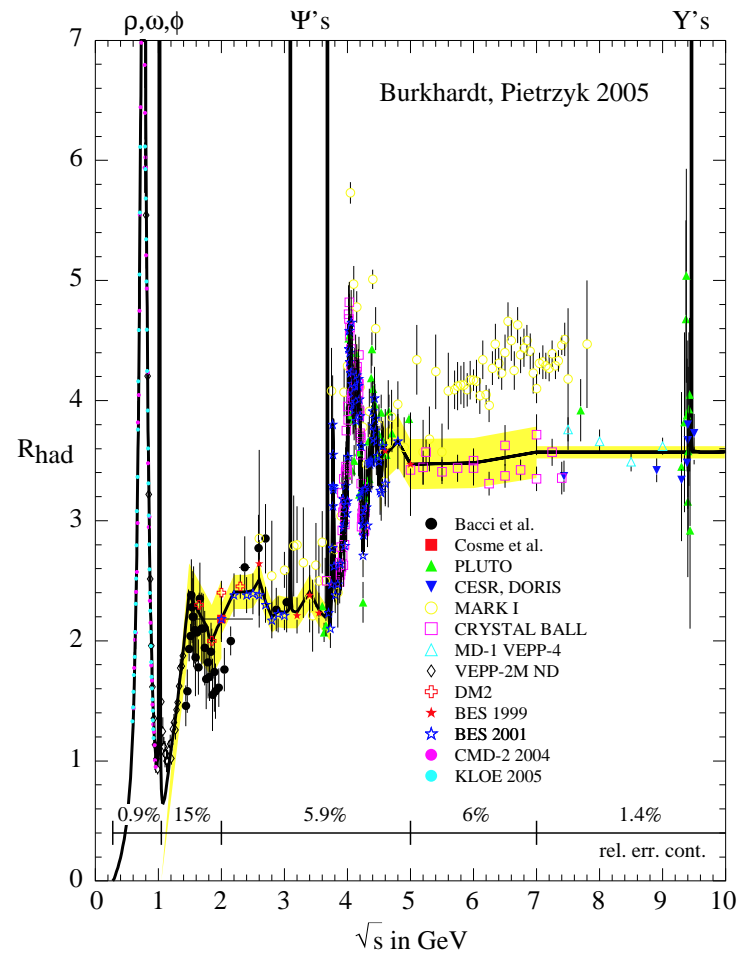
$$\Delta\alpha = \Delta\alpha_{\text{lept}} + \Delta\alpha_{\text{had}},$$

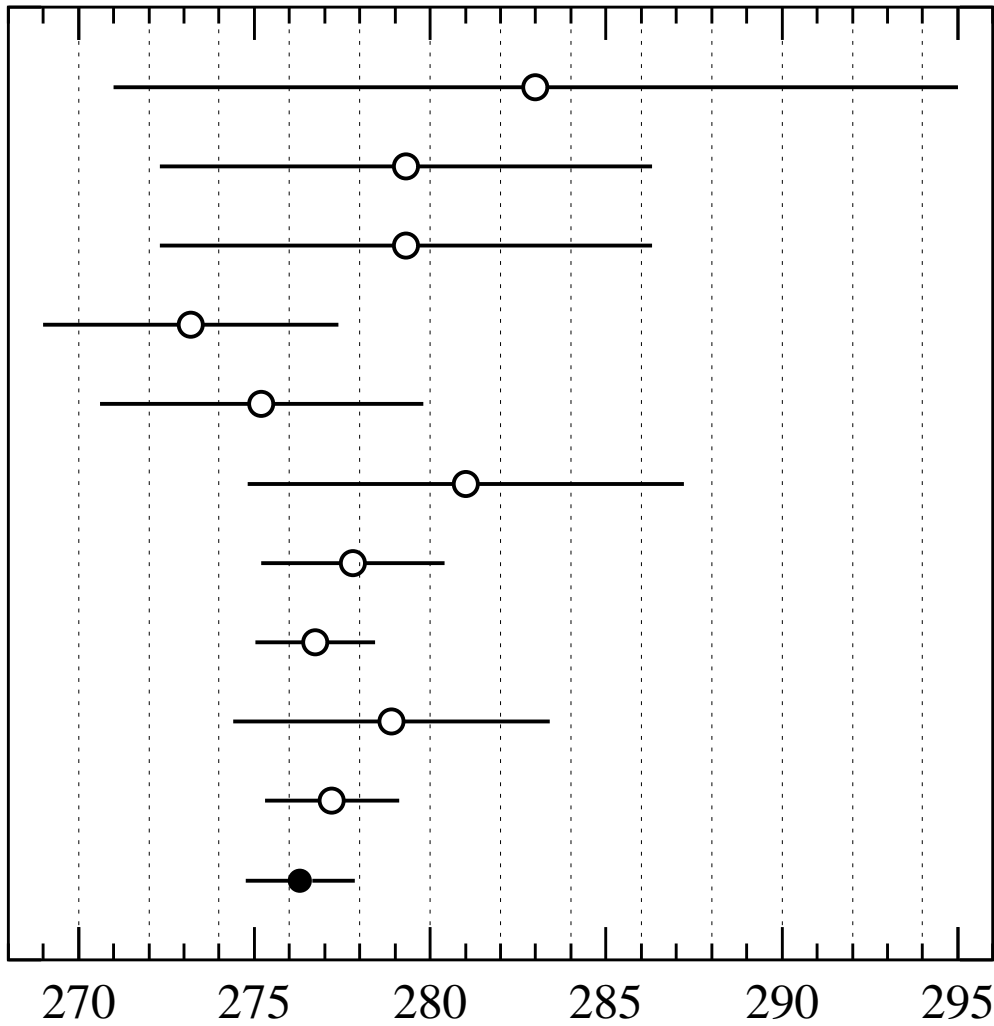
$$\Delta\alpha_{\text{lept}} = 0.031498 \quad (3 - \text{loop})$$

$$\Delta\alpha_{\text{had}} = 0.02758 \pm 0.00035$$

significant source of parametric uncertainty

$$\Delta\alpha_{\text{had}} = -\frac{\alpha}{3\pi} M_Z^2 \operatorname{Re} \int_{4m_\pi^2}^{\infty} ds' \frac{R_{\text{had}}(s')}{s'(s' - M_Z^2 - i\epsilon)}$$





Lynn, Penso, Verzegnassi, '87

Eidelman, Jegerlehner '95

Burkhardt, Pietrzyk '95

Martin, Zeppenfeld '95

Swartz '96

Aleman, Davier, Höcker '97

Davier, Höcker '97

Kühn, Steinhauser '98

Groote et al. '98

Erlar '98

Davier, Höcker '98

$$\Delta\alpha_{\text{had}}(M_Z^2) \quad (\times 10^{-4})$$

input from experiments

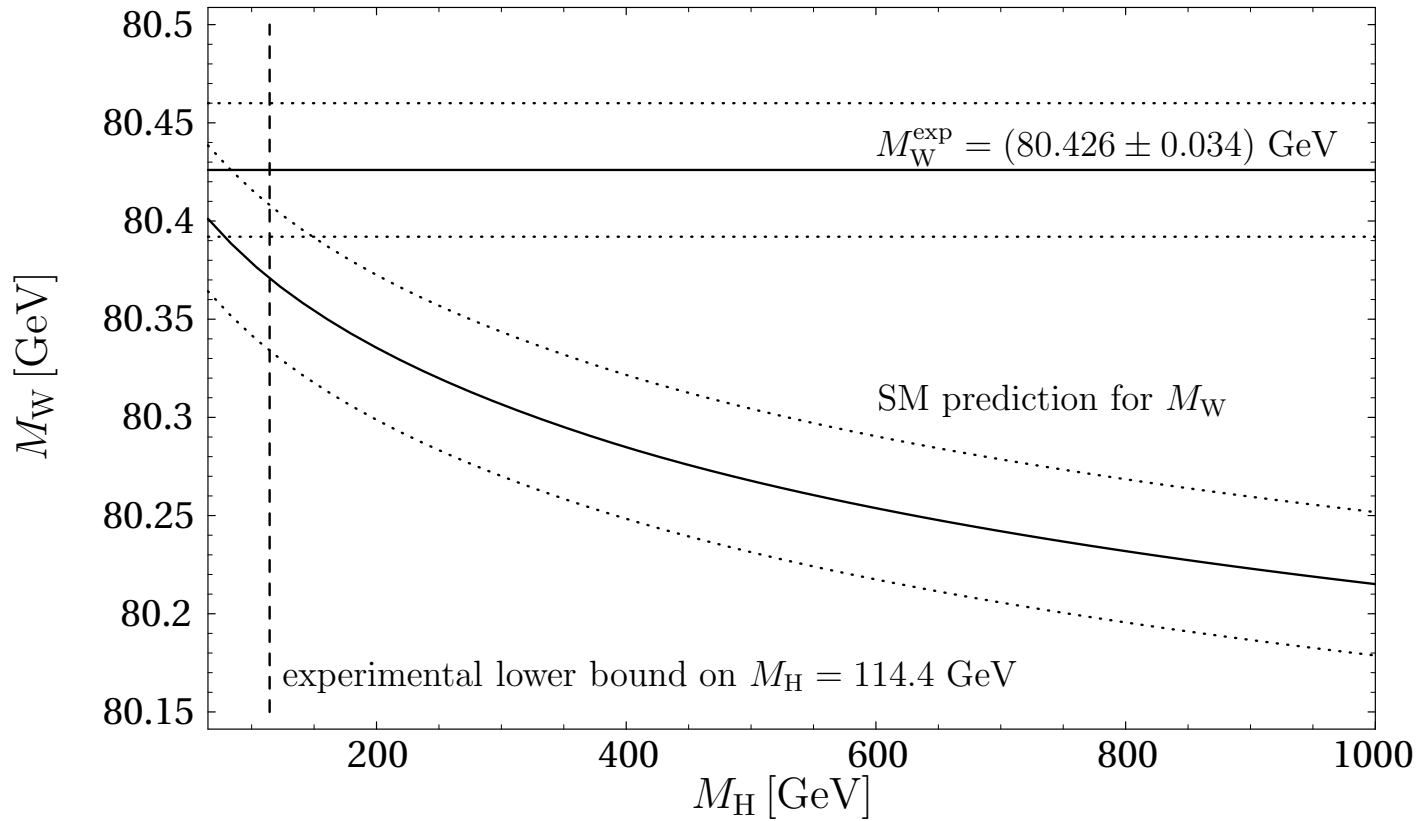
- **LEP1/SLC:** $e^+e^- \rightarrow Z \rightarrow f\bar{f}$
LEP1: $\sim 4 \times 10^6$ events/experiment
4 experiments (1989 – 1995)
- **LEP2:** $e^+e^- \rightarrow W^+W^-$
 $\mathcal{O}(10^4)$ W pairs (1996 – 2000)
- **Tevatron:** $q\bar{q}' \rightarrow W \rightarrow l\nu, q\bar{q}'$
($p\bar{p}$) $q\bar{q}' \rightarrow t\bar{t}, t \rightarrow W^+b \rightarrow \dots$
- **low-energy experiments** (μ decay, νN scattering, νe scattering, atomic parity violation, ...)

Theory versus Data

experimental results (selection)

M_Z [GeV]	$= 91.1875 \pm 0.0021$	0.002%
Γ_Z [GeV]	$= 2.4952 \pm 0.0023$	0.09%
$\sin^2 \theta_{\text{eff}}^{\text{lept}}$	$= 0.23148 \pm 0.00017$	0.07%
M_W [GeV]	$= 80.392 \pm 0.029$	0.04%
m_t [GeV]	$= 170.9 \pm 1.8$	1.05%
G_F [GeV ⁻²]	$= 1.16637(1)10^{-5}$	0.001%

quantum effects at least one order of magnitude larger than experimental uncertainties



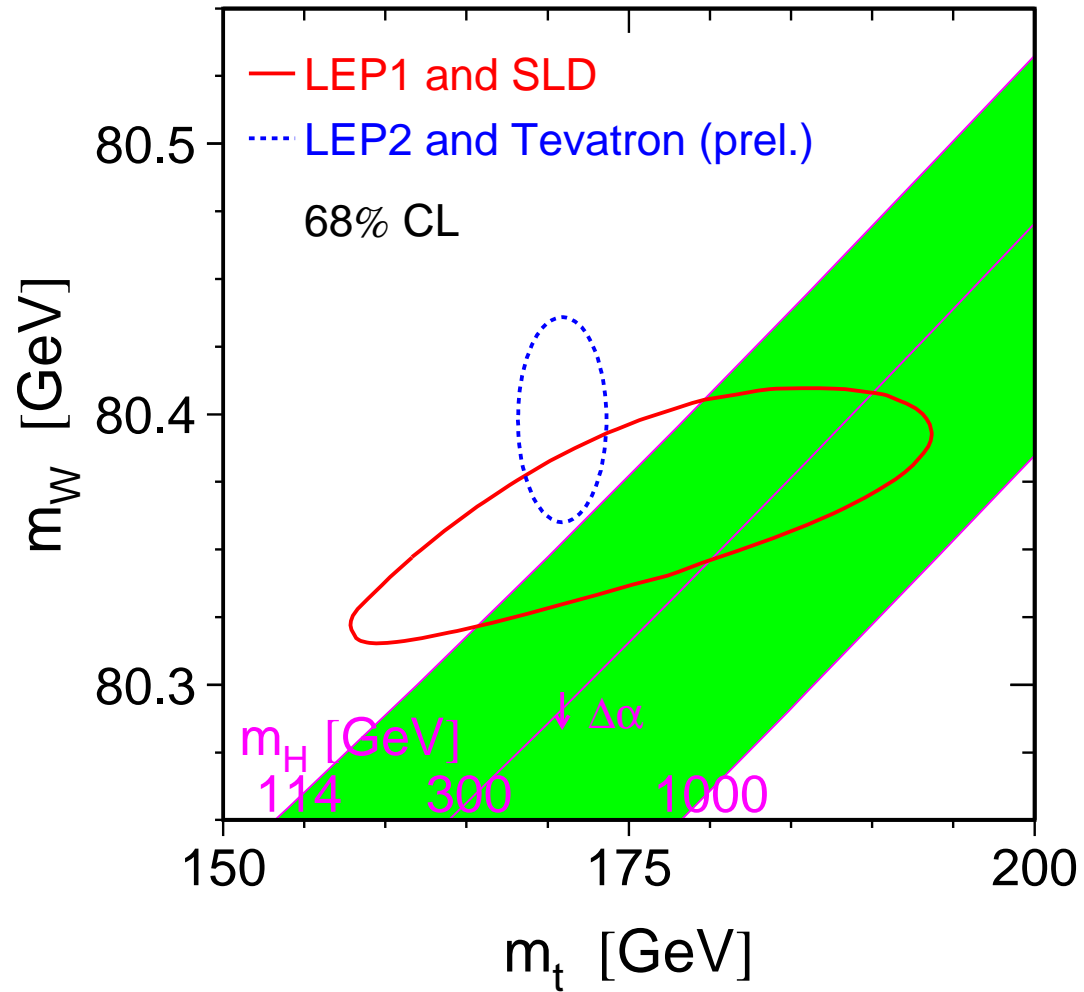
[Awramik, Czakon, Freitas, Weiglein]

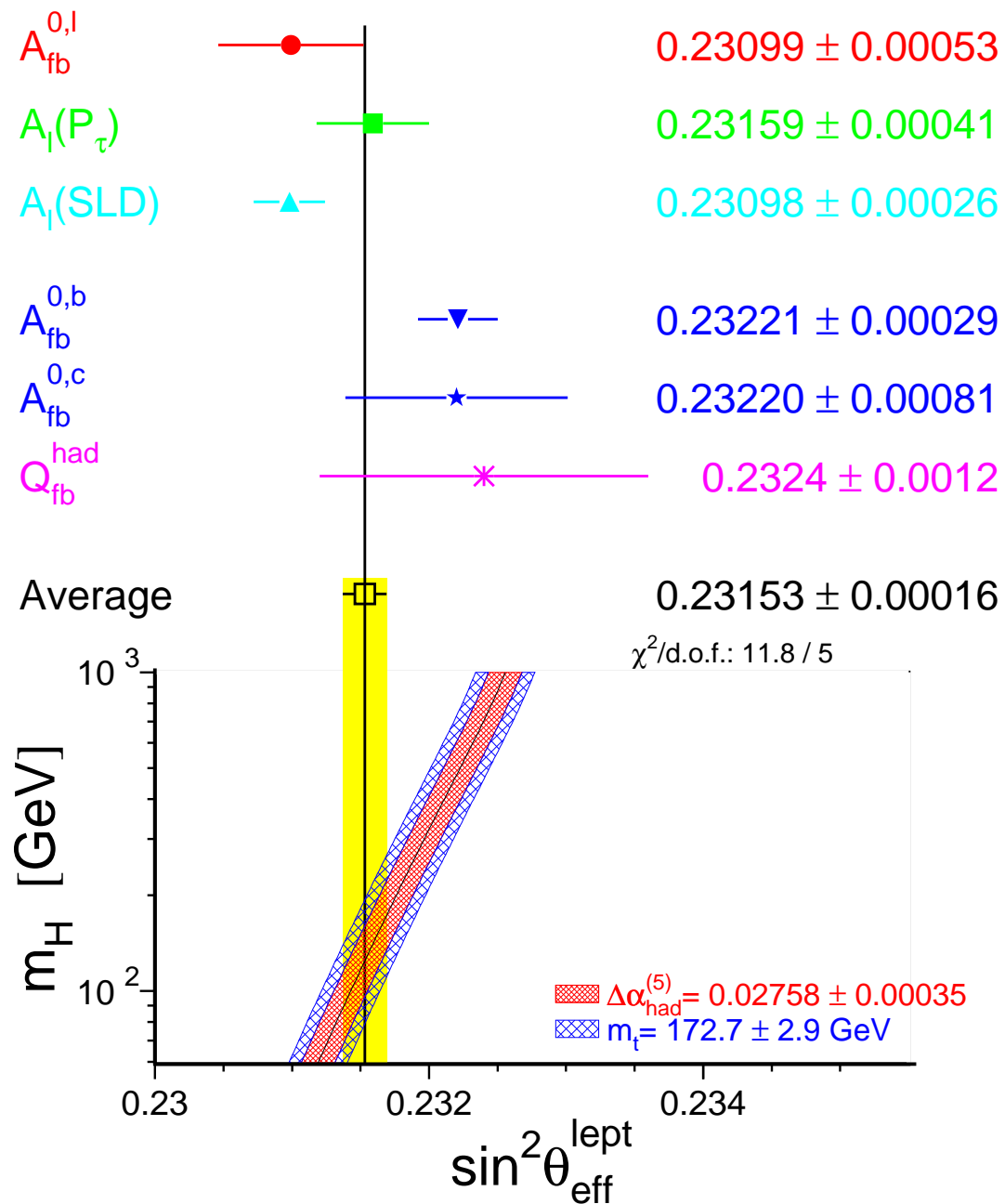
$$m_t = 174.3 \pm 5.1 \text{ GeV}$$

$$\delta M_W^{\text{theo}} \simeq 4 \text{ MeV}$$

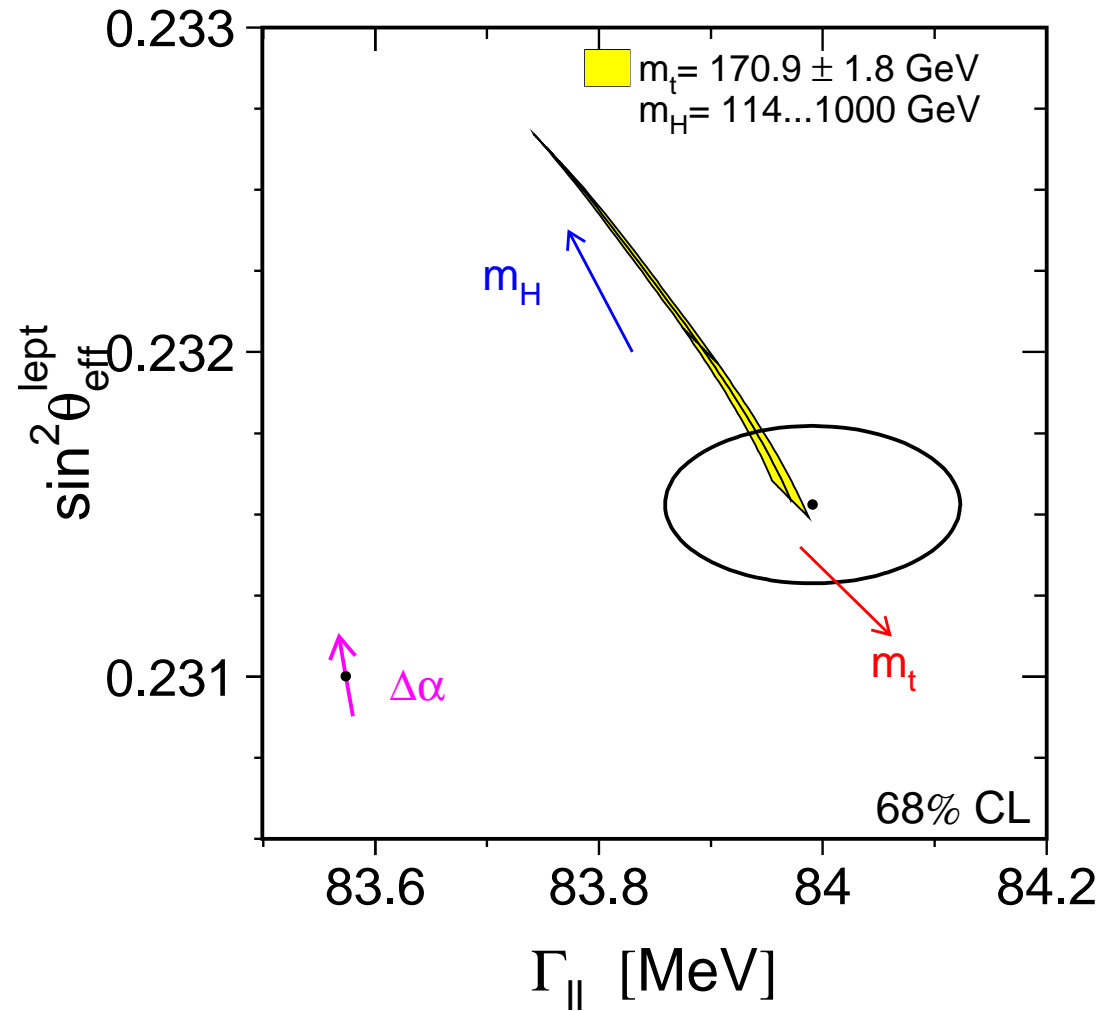
$$\delta \sin^2 \theta_{\text{eff}}^{\text{theo}} \simeq 5 \cdot 10^{-5}$$

LEP Electroweak Working Group





LEP Electroweak Working Group



ORGANISATION EUROPÉENNE POUR LA RECHERCHE NUCLÉAIRE
CERN EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

Z PHYSICS AT LEP 1

Edited by
Guido Altarelli, Ronald Kleiss and Claudio Verzegnassi

Volume 1: STANDARD PHYSICS

Co-ordinated and supervised by G. Altarelli

GENEVA
1989

development of precision

1990-1992

91.1904 ± 0.0065

1993-1994

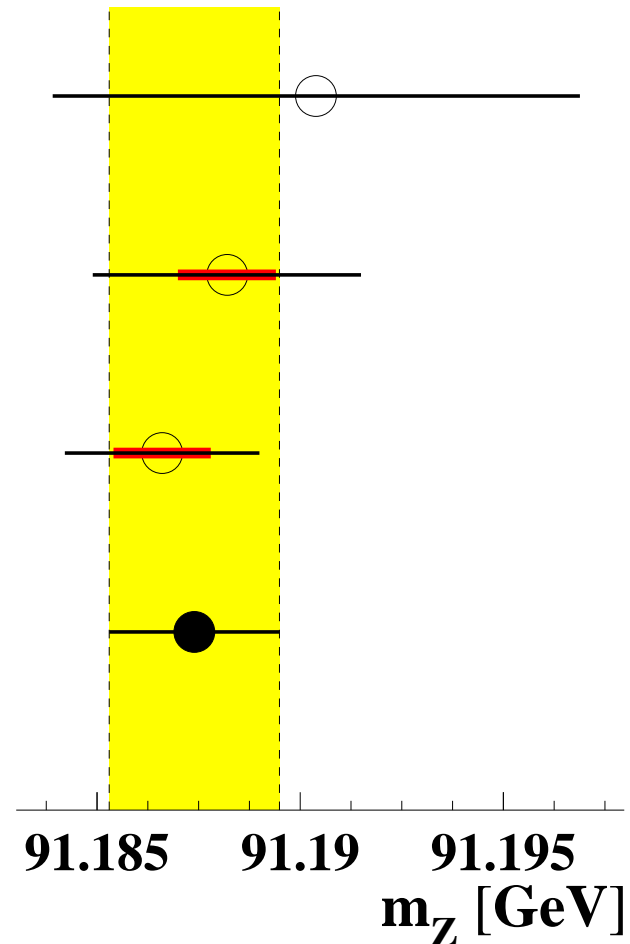
91.1882 ± 0.0033

1995

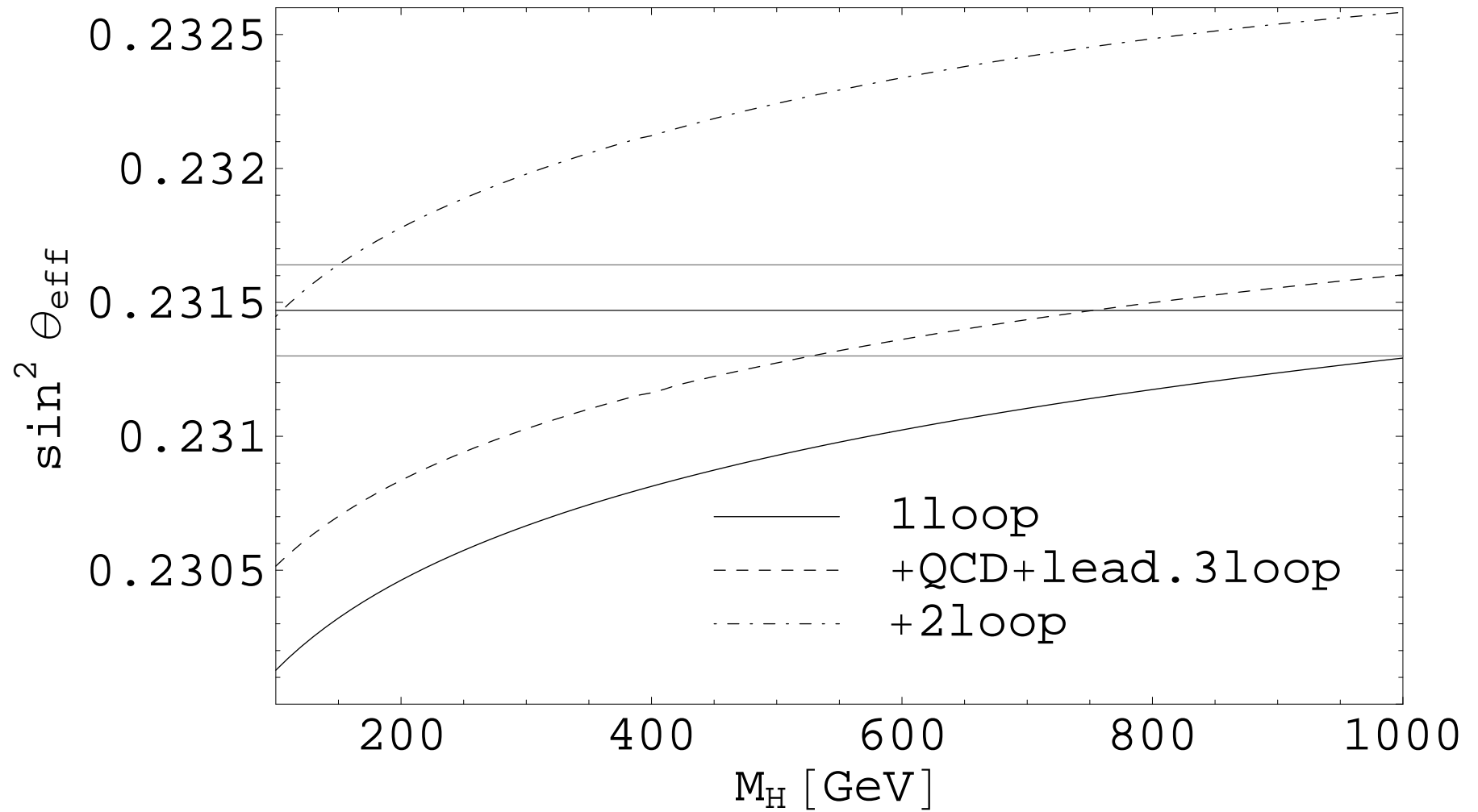
91.1866 ± 0.0024

average

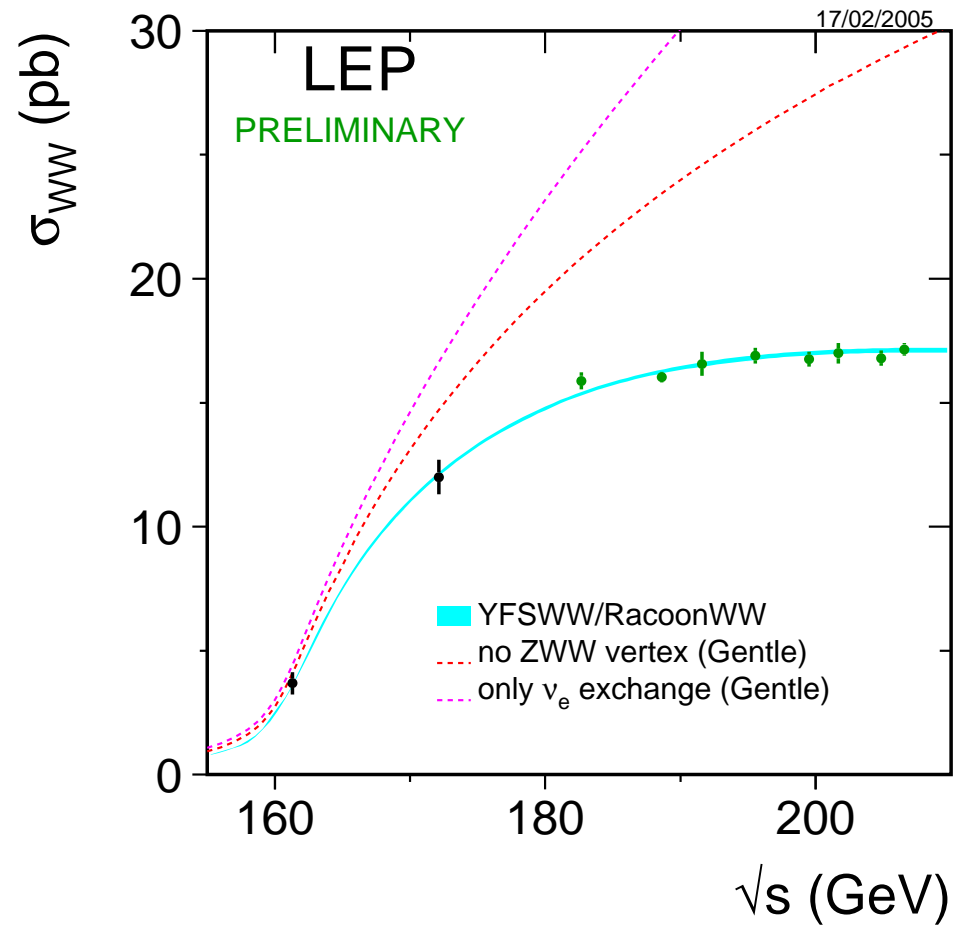
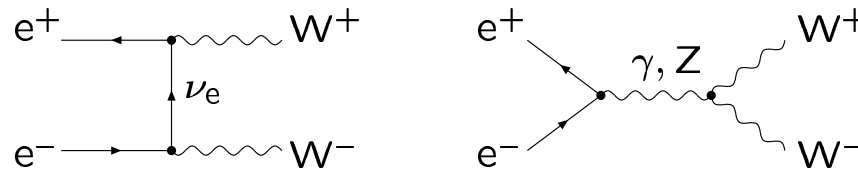
91.1874 ± 0.0021

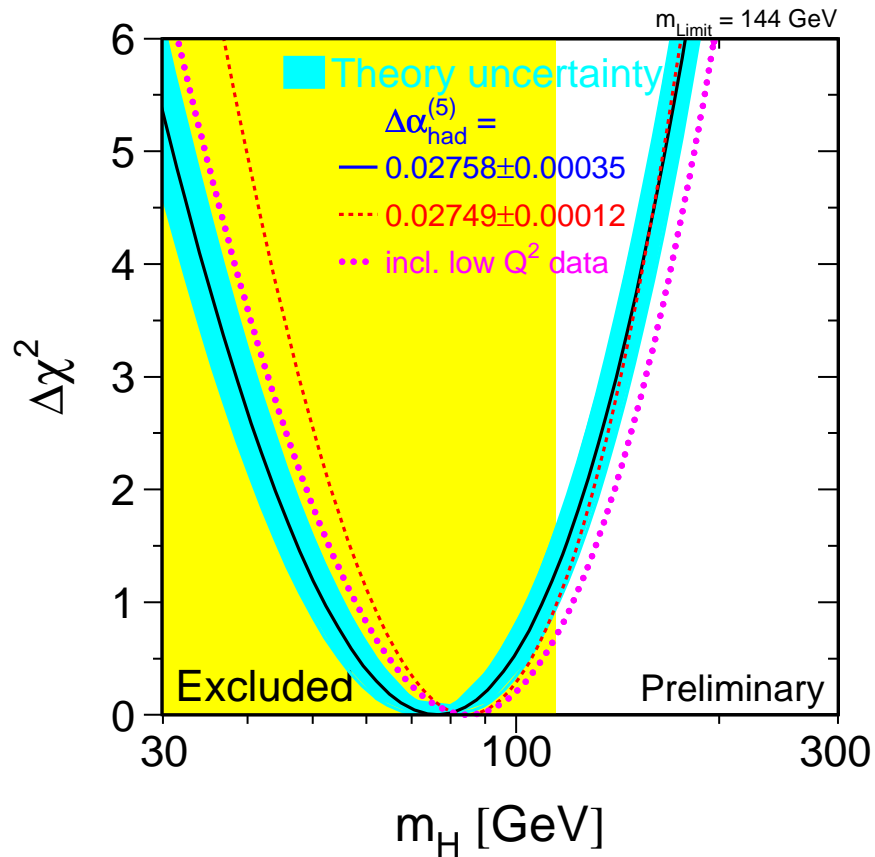


importance of two-loop calculations



W-pair production





blueband: theory uncertainty

“Precision Calculations
at the Z Resonance”

CERN 95-03

[Bardin, Hollik, Passarino (eds.)]

$$M_H < 144 \text{ GeV} \quad (95\% \text{C.L.})$$

with renormalized probability for $M_H > 114 \text{ GeV}$:

$$M_H < 182 \text{ GeV} \quad (95\% \text{C.L.})$$

Future perspectives

error for	LEP/Tev	Tev/LHC	LC	LC/GigaZ
M_W [MeV]	29	15	15	7
$\sin^2 \theta_{\text{eff}}$	0.00017	0.00021		0.000013
m_{top} [GeV]	1.8	1 - 1.5	0.2	0.13
M_{Higgs} [GeV]	–	0.1	0.05	0.05

$$\delta M_Z = 2.1 \text{ MeV} \quad (\text{LEP})$$

$$\delta G_F / G_F = 1 \cdot 10^{-5} \quad (\mu \text{ lifetime})$$

GigaZ $\sim 10^9$ Z bosons

MegaW $\sim 10^6$ W bosons

M_W from Drell-Yan at the LHC

$$q\bar{q}' \rightarrow W^+ \rightarrow \ell^+ \nu_\ell$$

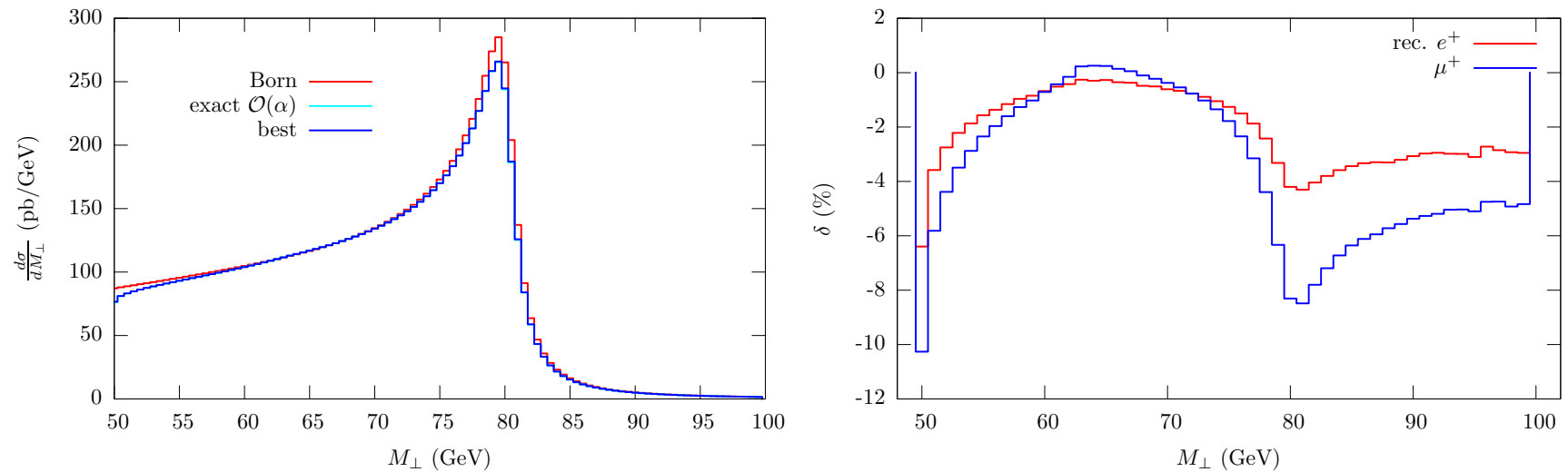


Fig. 1. Transverse mass distribution and $\mathcal{O}(\alpha)$ relative correction.

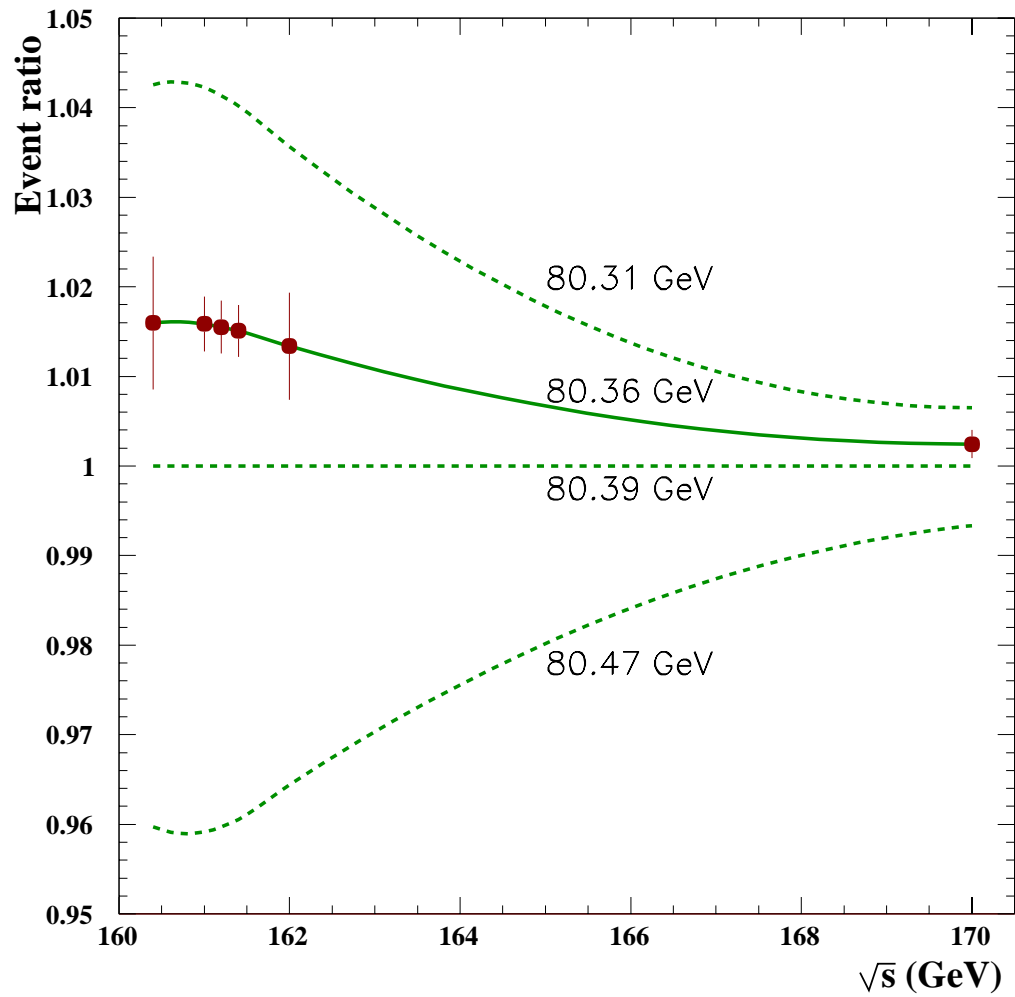
[Carloni Calame et al.]

[Baur, Wackerath]

[Dittmaier, Krämer]

[Arbuzov et al.]

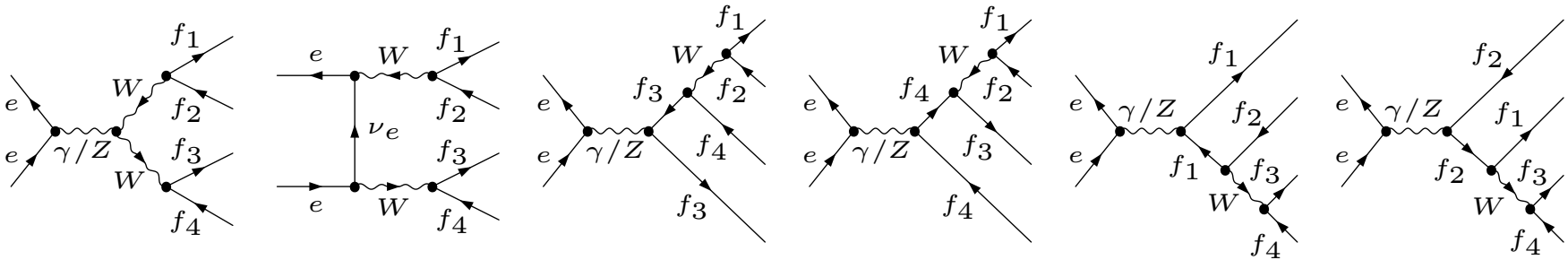
M_W from threshold scan in e^+e^- annihilation



M_W from threshold $e^+e^- \rightarrow WW \rightarrow 4f$

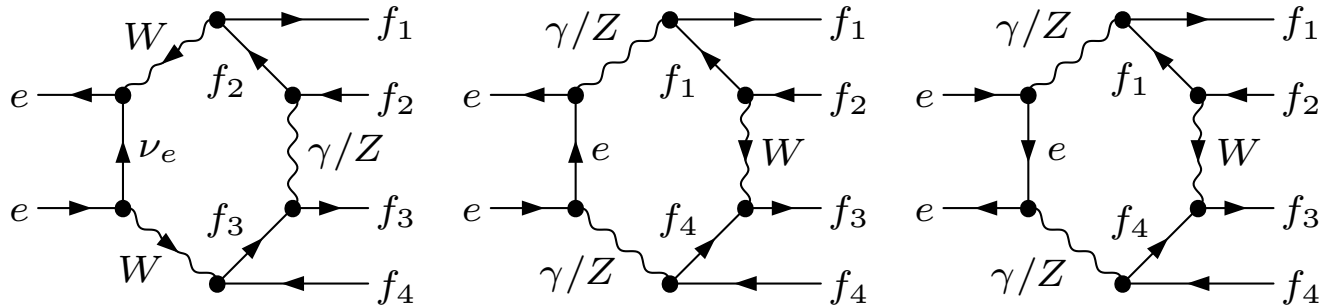
Some Feynman diagrams...

...for LO:



...for NLO: total number = $\mathcal{O}(1200)$

40 hexagons



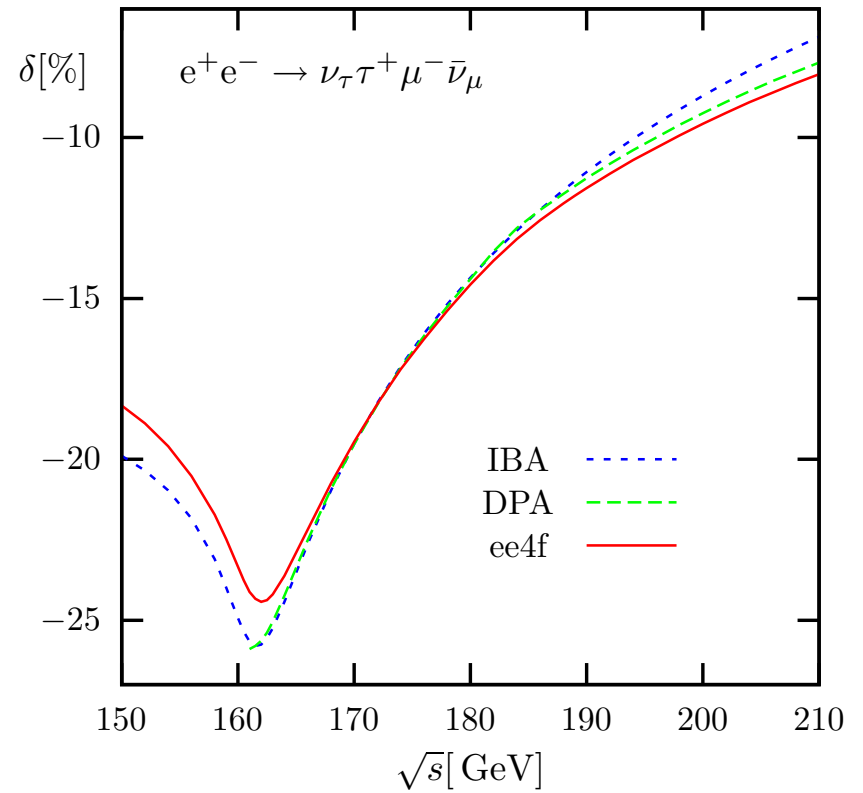
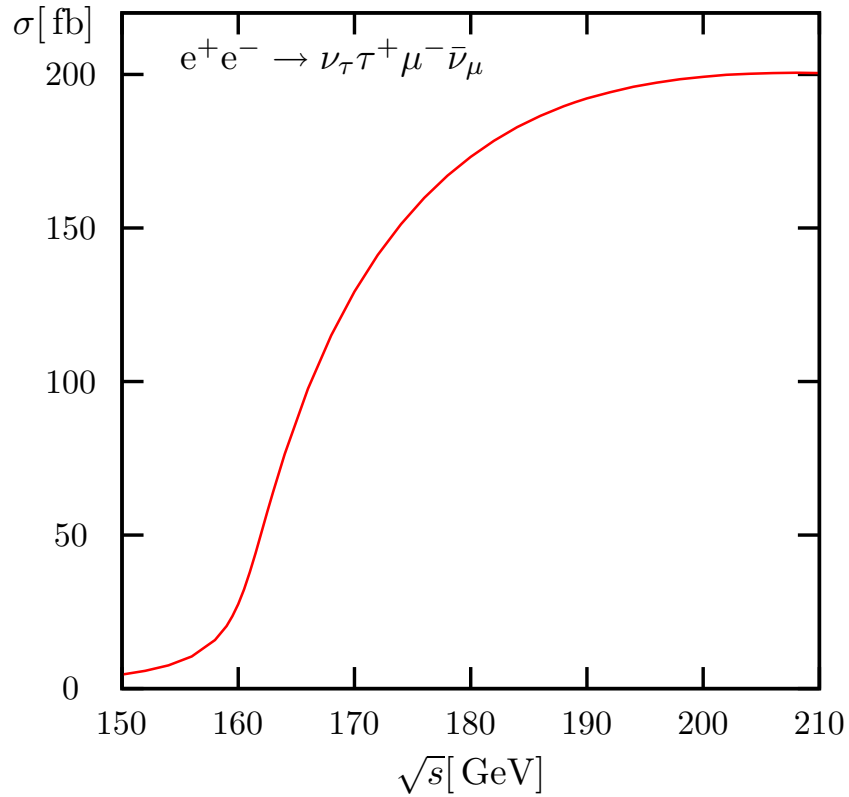
+ graphs with reversed fermion-number flow in final state

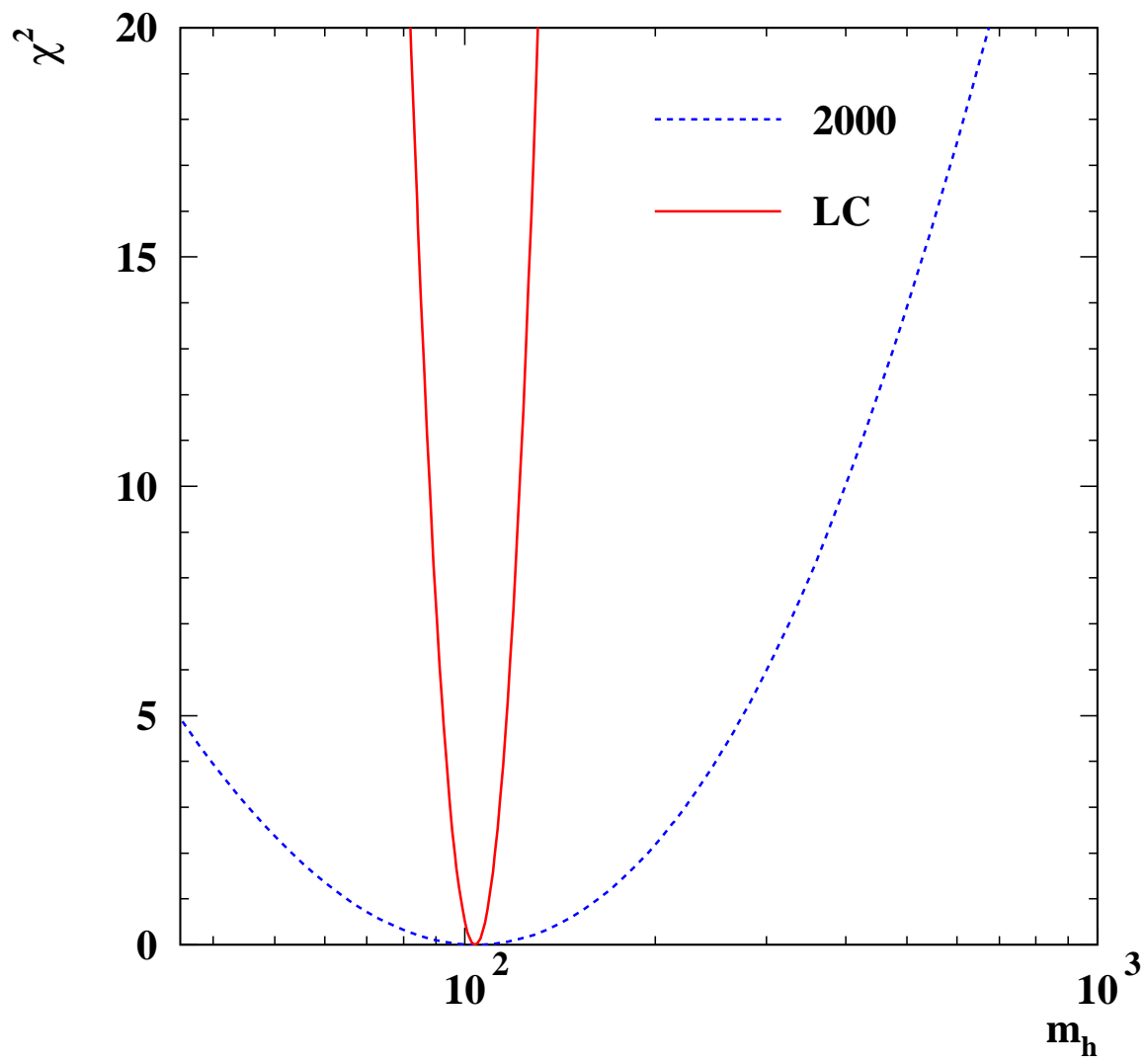
+ 112 pentagons

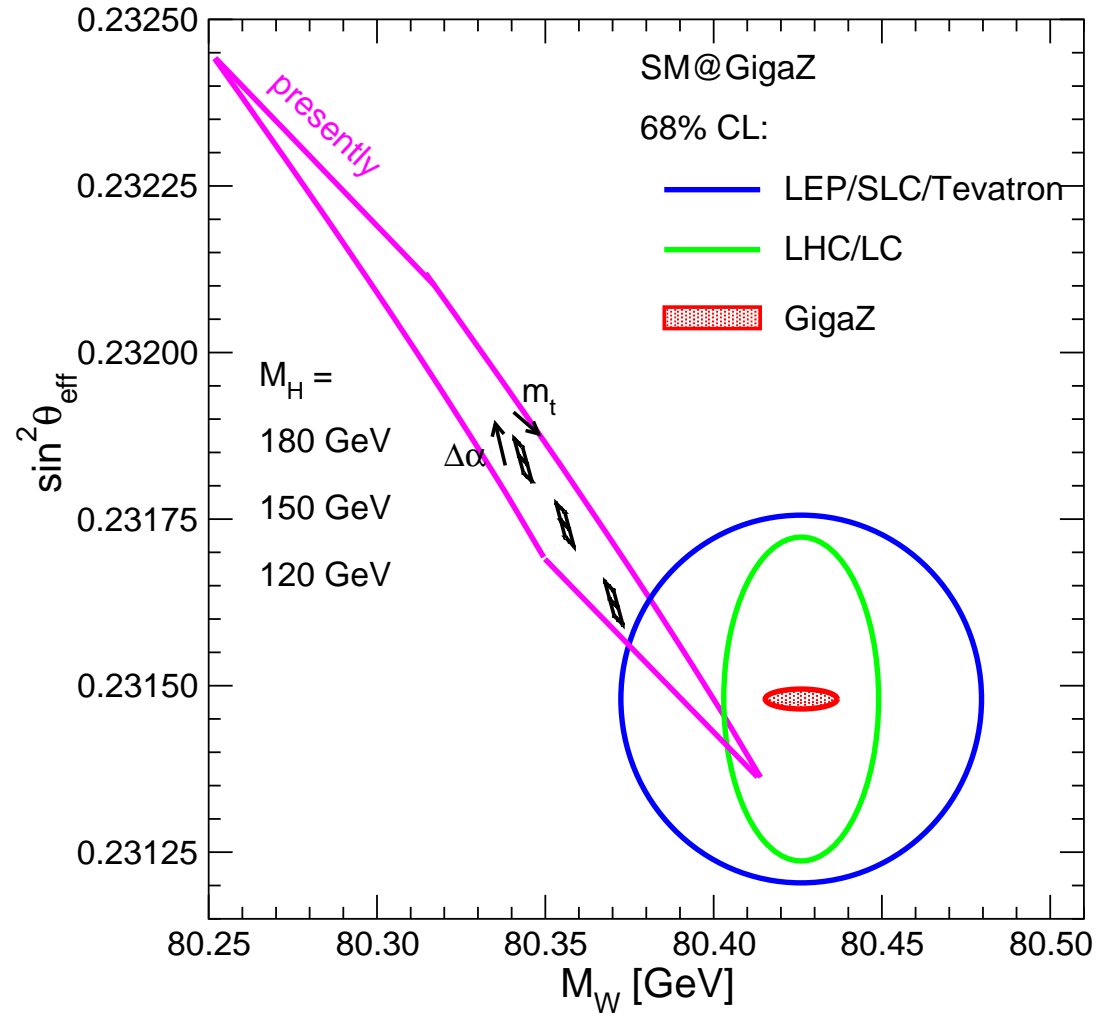
+ 227 boxes ('tHF gauge) + many vertex and self-energy corrections

M_W from threshold $e^+e^- \rightarrow WW \rightarrow 4f$

Denner, Dittmaier, Roth, Wieders '05





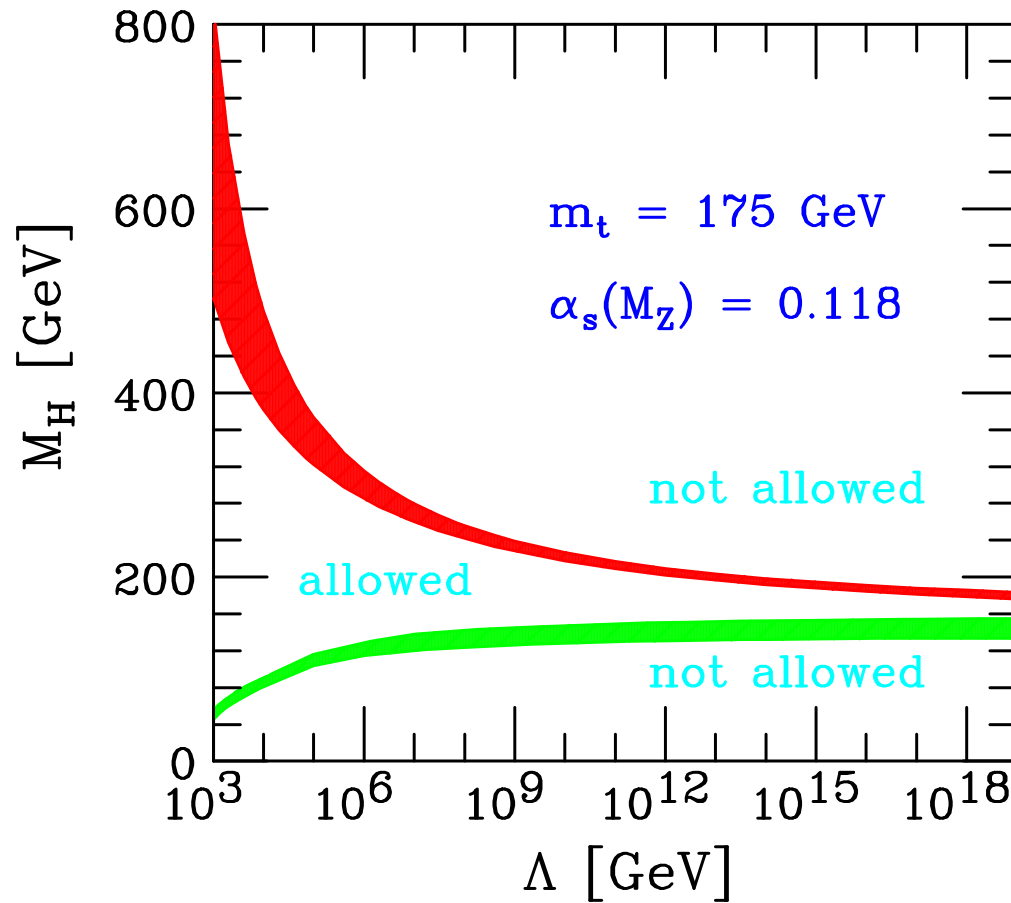


Theoretical bounds on Higgs boson mass from

- perturbativity \rightarrow upper bound
- unitarity \rightarrow upper bound
- triviality (Landau pole) \rightarrow upper bound
- vacuum stability \rightarrow lower bound

combined effects, RGE in two-loop order:

$$\frac{d\lambda}{dt} = \frac{1}{16\pi^2} (12\lambda^2 - 3g_t^4 + 6\lambda g_t^2 + \dots)$$



SM Higgs:

- λH^4 term ad hoc
- Higgs boson mass: free parameter $\sim \sqrt{\lambda}$
- no a-priori reason for a light Higgs boson

SUSY Standard Model avoids these questions

$$H_2 = \begin{pmatrix} H_2^+ \\ v_2 + H_2^0 \end{pmatrix}, \quad H_1 = \begin{pmatrix} v_1 + H_1^0 \\ H_1^- \end{pmatrix}$$

couples to u

couples to d

- SUSY gauge interaction $\rightarrow H^4$ terms
- self coupling remains weak

Minimal Supersymmetric SM

Superpartners for Standard Model particles:

$$[u, d, c, s, t, b]_{L,R} \quad [e, \mu, \tau]_{L,R} \quad [\nu_{e,\mu,\tau}]_L \quad \text{Spin } \frac{1}{2}$$

$$[\tilde{u}, \tilde{d}, \tilde{c}, \tilde{s}, \tilde{t}, \tilde{b}]_{L,R} \quad [\tilde{e}, \tilde{\mu}, \tilde{\tau}]_{L,R} \quad [\tilde{\nu}_{e,\mu,\tau}]_L \quad \text{Spin } 0$$

$$g \quad \underbrace{W^\pm, H^\pm}_{\text{Spin } 1} \quad \underbrace{\gamma, Z, H_1^0, H_2^0}_{\text{Spin } 0}$$

$$\tilde{g} \quad \tilde{\chi}_{1,2}^\pm \quad \tilde{\chi}_{1,2,3,4}^0 \quad \text{Spin } \frac{1}{2}$$

Enlarged Higgs sector: two Higgs doublets, physical states:

$$h^0, H^0, A^0, H^\pm$$

masses and mixing of SUSY particles through soft-breaking

model parameters

- gaugino masses: M_1, M_2, M_3
- sfermion masses: $M_L, M_{\tilde{u}_R}, M_{\tilde{d}_R}$
for each doublet of squarks and sleptons
- trilinear coupling: $A_{\tilde{f}}$ for each \tilde{f}
→ L - R sfermion mixing
- supersymmetric Higgsino mass parameter: μ
- Higgs sector parameters: $M_A, \tan \beta = v_2/v_1$

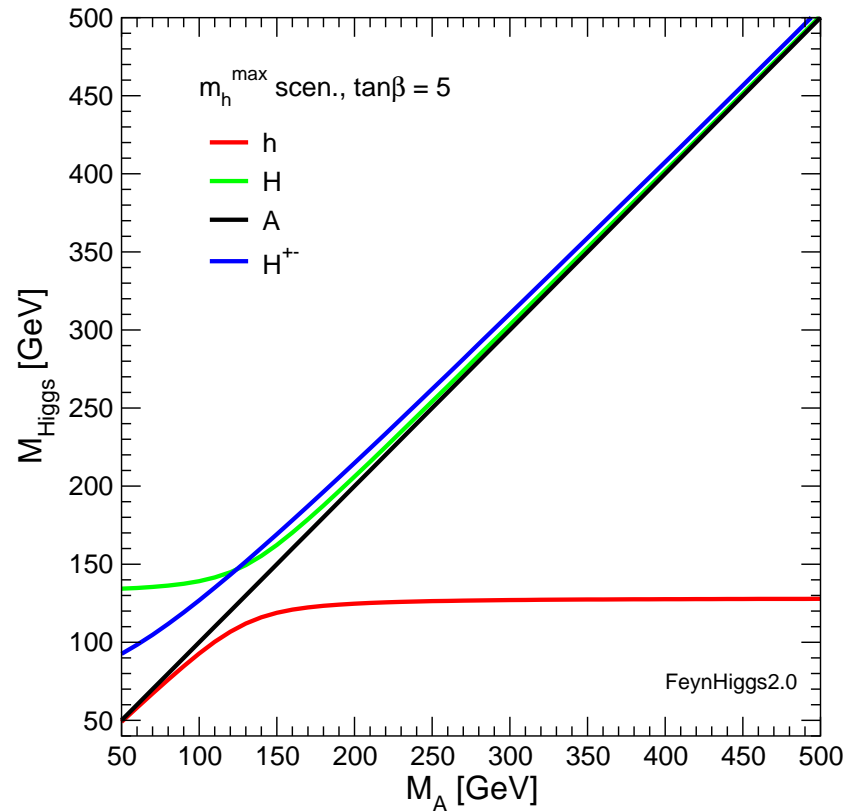
Benchmark scenarios

“Snowmass points and slopes” (SPS),
hep-ph/0202233

examples (mSUGRA):

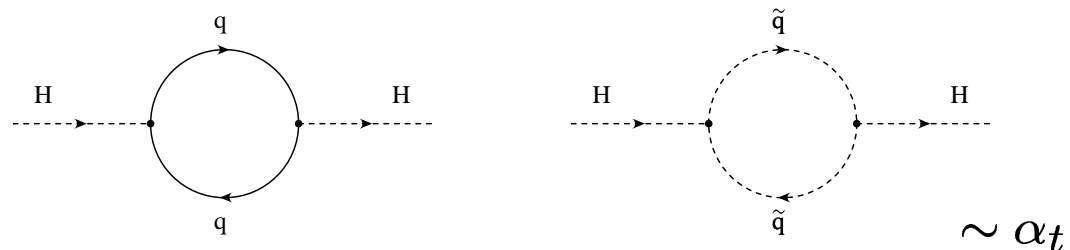
- **SPS1a:** $m_0 = 100 \text{ GeV}$, $m_{1/2} = 250 \text{ GeV}$, $A_0 = -100$,
 $\tan \beta = 10$, $\mu > 0$.
- **SPS1b:** $m_0 = 200 \text{ GeV}$, $m_{1/2} = 400 \text{ GeV}$, $A_0 = 0$,
 $\tan \beta = 30$, $\mu > 0$.

Spectrum of Higgs bosons in the MSSM (example)



large M_A : h^0 like SM Higgs boson \sim decoupling regime

m_h^0 strongly influenced by quantum effects, e.g.



1-loop: complete

2-loop:

– QCD corrections $\sim \alpha_s \alpha_t, \alpha_s \alpha_b$

– Yukawa corrections $\sim \alpha_t^2$

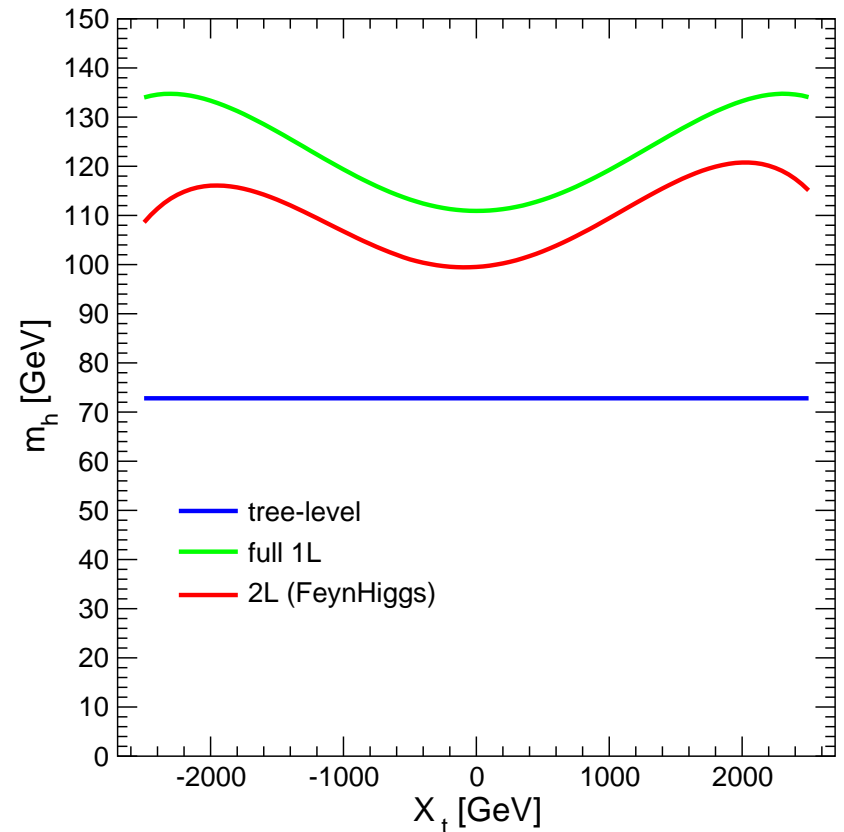
present theoretical uncertainty:

$$\delta m_h \simeq 3\text{-}4 \text{ GeV}$$

[Degrassi, Heinemeyer, WH, Slavich,

Weiglein]

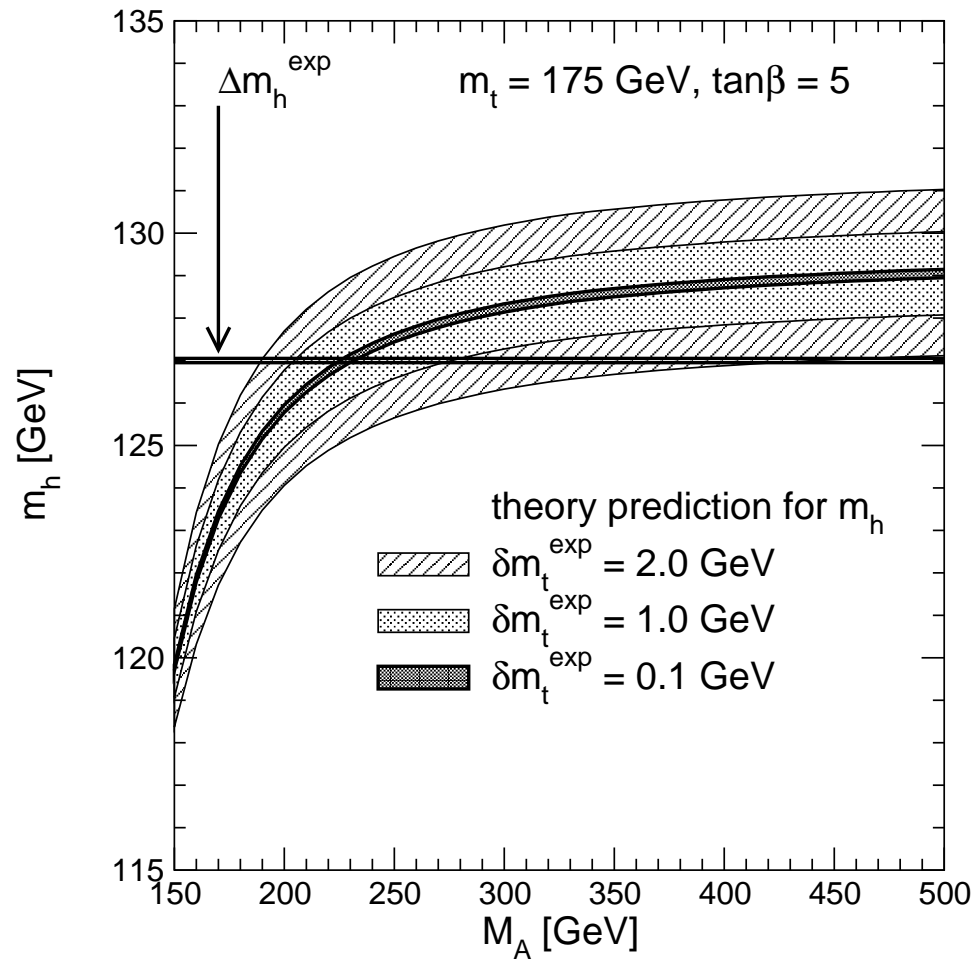
m_{h^0} prediction at different levels of accuracy:



$\tan \beta = 3, \quad M_{\tilde{Q}} = M_A = 1 \text{ TeV}, \quad m_{\tilde{g}} = 800 \text{ GeV}$

X_t : top-squark mixing parameter

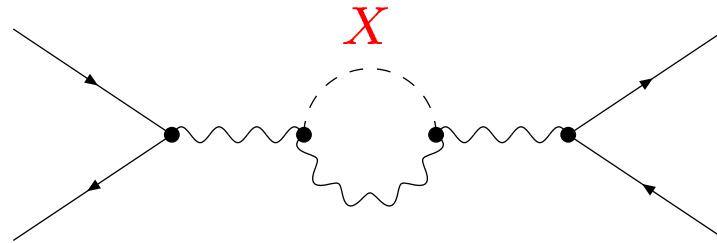
$$X_t = A_t - \mu \cot \beta$$



dependent on all SUSY particles and masses/mixings through Higgs self-energies

Test of theory at quantum level:

Sensitivity to loop corrections



$X =$ Higgs bosons, SUSY particles

- μ lifetime: $M_W, \Delta r, G_F$
- Z observables: $g_V, g_A, \sin^2 \theta_{\text{eff}}, \Gamma_Z, \dots$

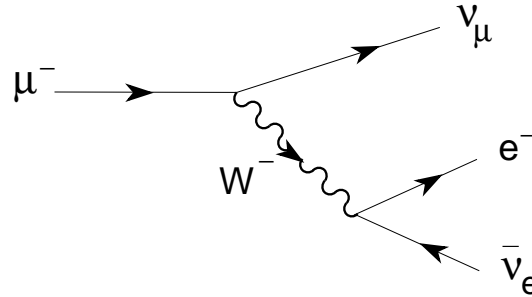
[Heinemeyer, WH, Weiglein, Phys. Rep. 425 (2006) 265]

new: 2-loop improvements $\mathcal{O}(\alpha\alpha_s, \alpha_t^2, \alpha_b^2, \alpha_t\alpha_b)$
and complex parameters

[Heinemeyer, WH, Stöckinger, A. Weber, Weiglein 06]

[Heinemeyer, WH, A. Weber, Weiglein 07]

$M_W - M_Z$ correlation



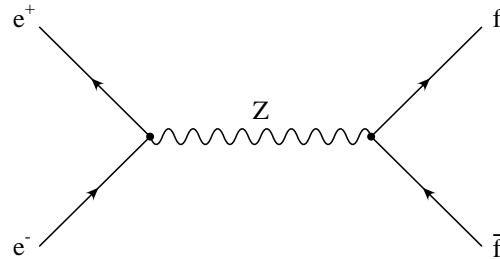
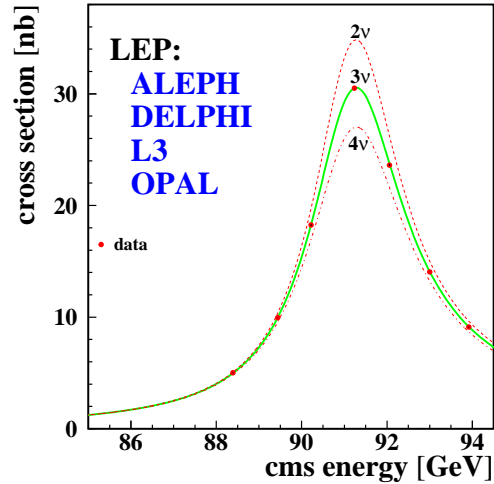
$$\frac{G_F}{\sqrt{2}} = \frac{\pi\alpha}{M_W^2 (1 - M_W^2/M_Z^2)} (1 + \Delta r)$$

Δr : quantum correction, $\Delta r = \Delta r(m_t, X_{\text{SUSY}})$

$\rightarrow M_W = M_W(\alpha, G_F, M_Z, m_t, X_{\text{SUSY}})$

X_{SUSY} = set of non-standard model parameters

Z resonance



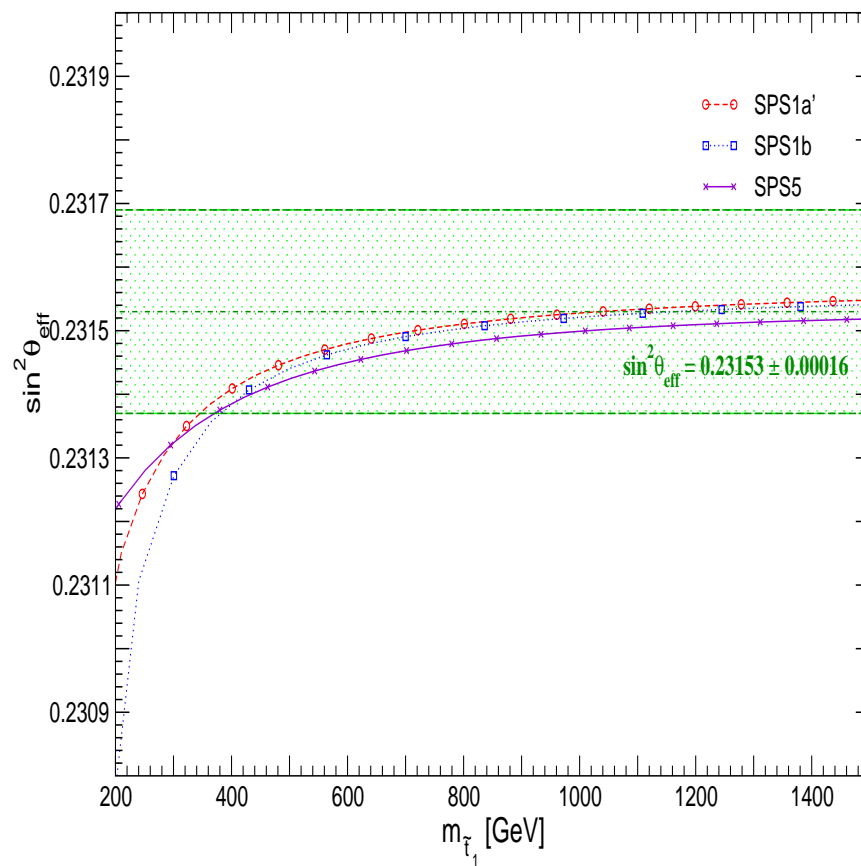
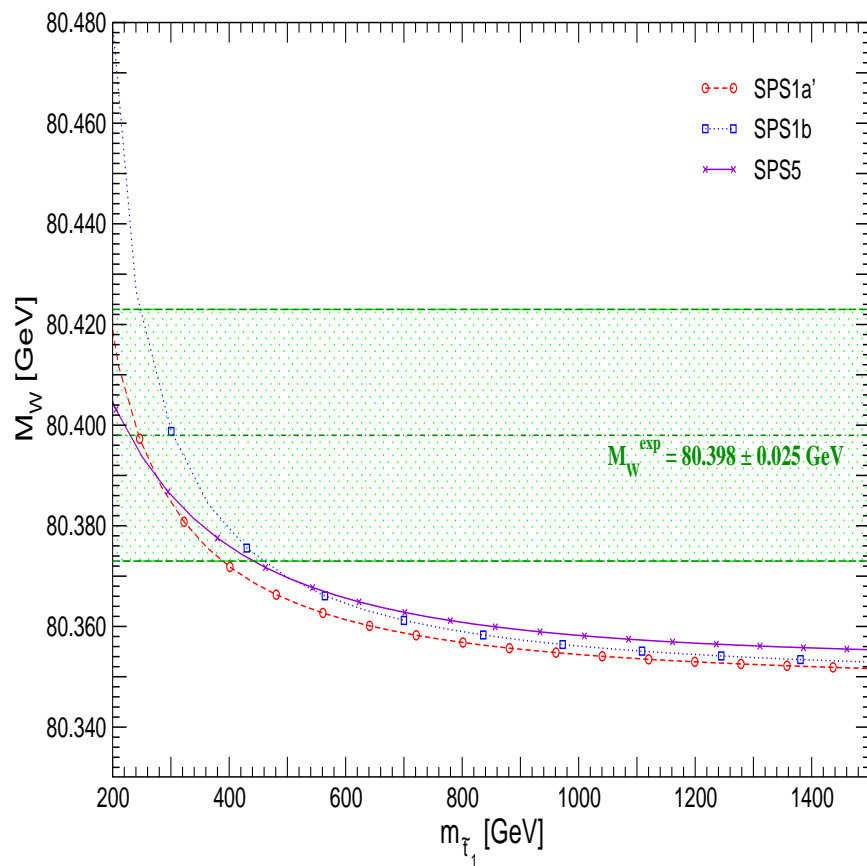
effective Z boson couplings

$$g_V^f \rightarrow g_V^f + \Delta g_V^f, \quad g_A^f \rightarrow g_A^f + \Delta g_A^f$$

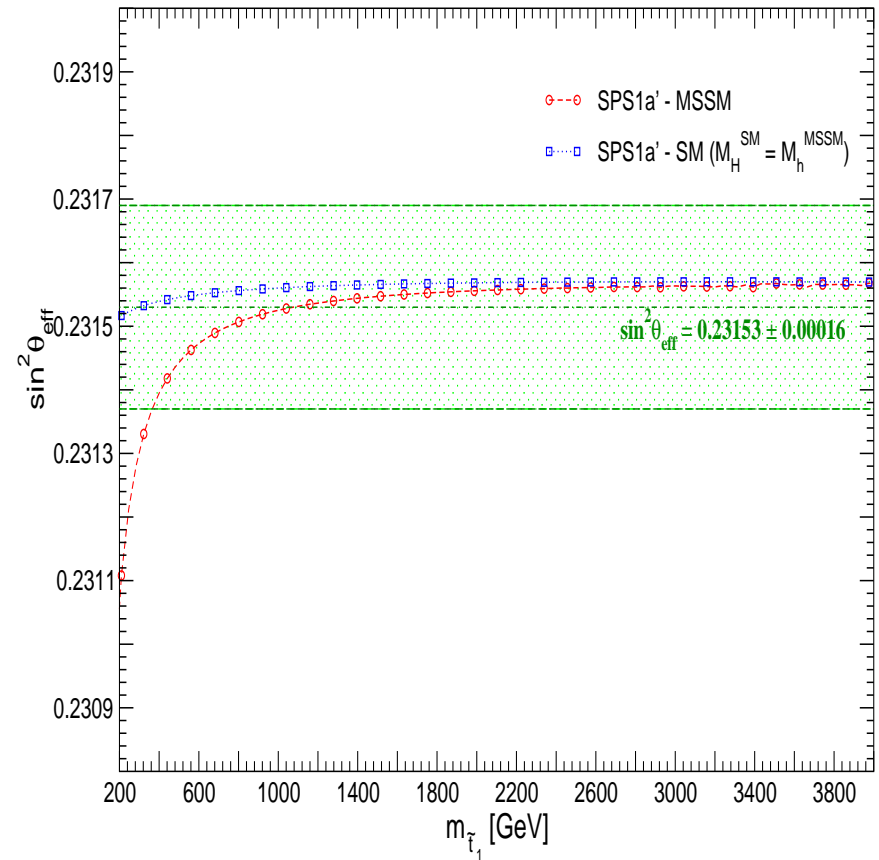
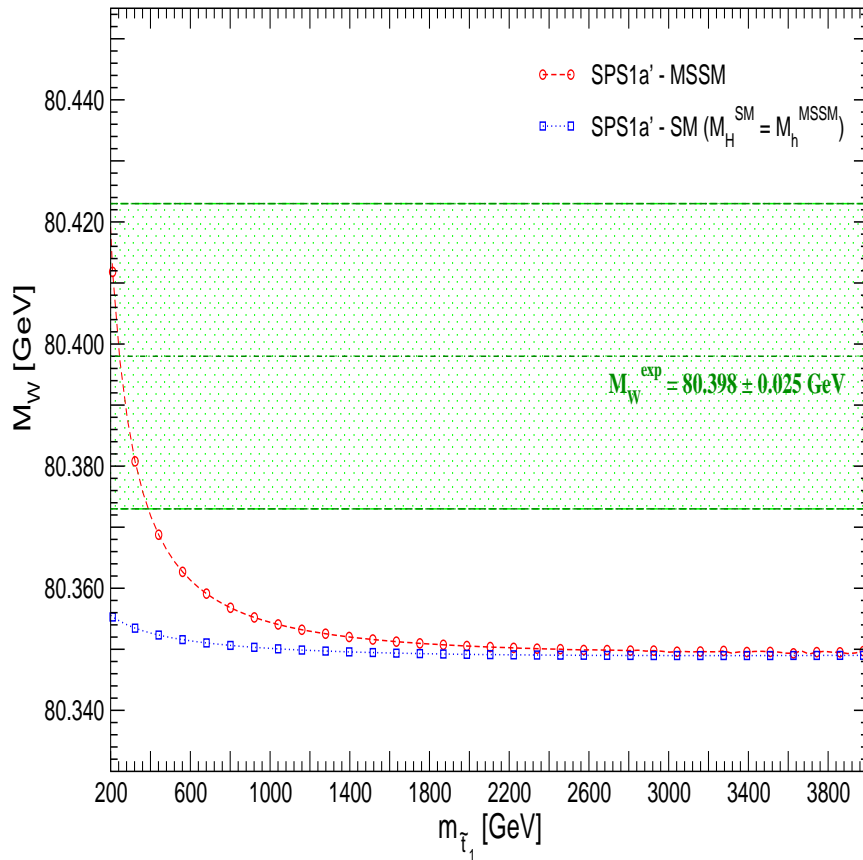
with higher order contributions $\Delta g_{V,A}^f (m_t, X_{\text{SUSY}})$

$$\sin^2 \theta_{\text{eff}} = \frac{1}{4} \left(1 - \text{Re} \frac{g_V^e}{g_A^e} \right) = \kappa \cdot \left(1 - \frac{M_W^2}{M_Z^2} \right)$$

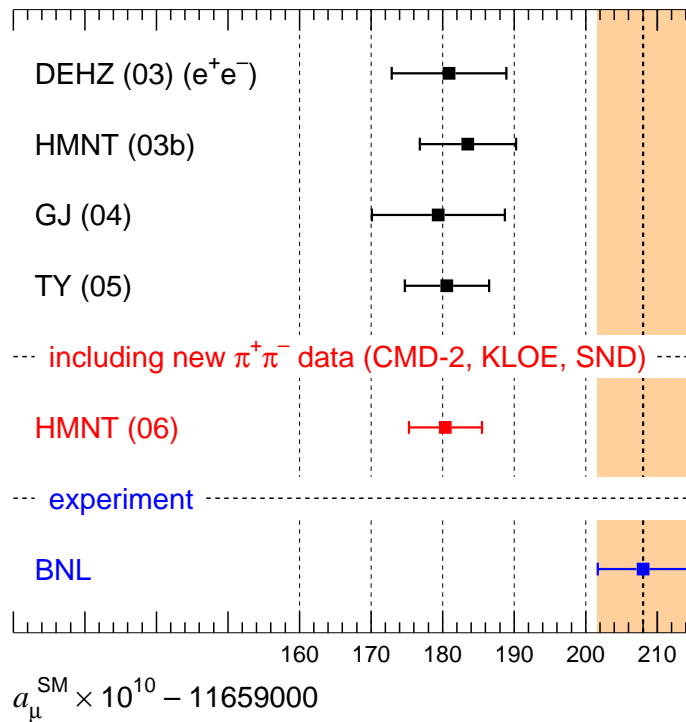
M_W and $\sin^2 \theta_{\text{eff}}$ for varied SUSY-scale



M_W and $\sin^2 \theta_{\text{eff}}$ for varied SUSY-scale



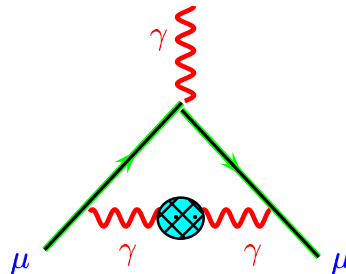
Anomalous g-factor of the muon



Hagiwara, Martin, Nomura, Teubner

e^+e^- data based SM prediction: 3.4σ below exp. value

theory uncertainty from hadronic vacuum polarization



$g - 2$ with supersymmetry

new contributions from virtual SUSY partners of μ , ν_μ and of W^\pm , Z



extra terms

$$+ \frac{\alpha}{\pi} \frac{m_\mu^2}{M_{\text{SUSY}}^2} \cdot \frac{v_2}{v_1}$$

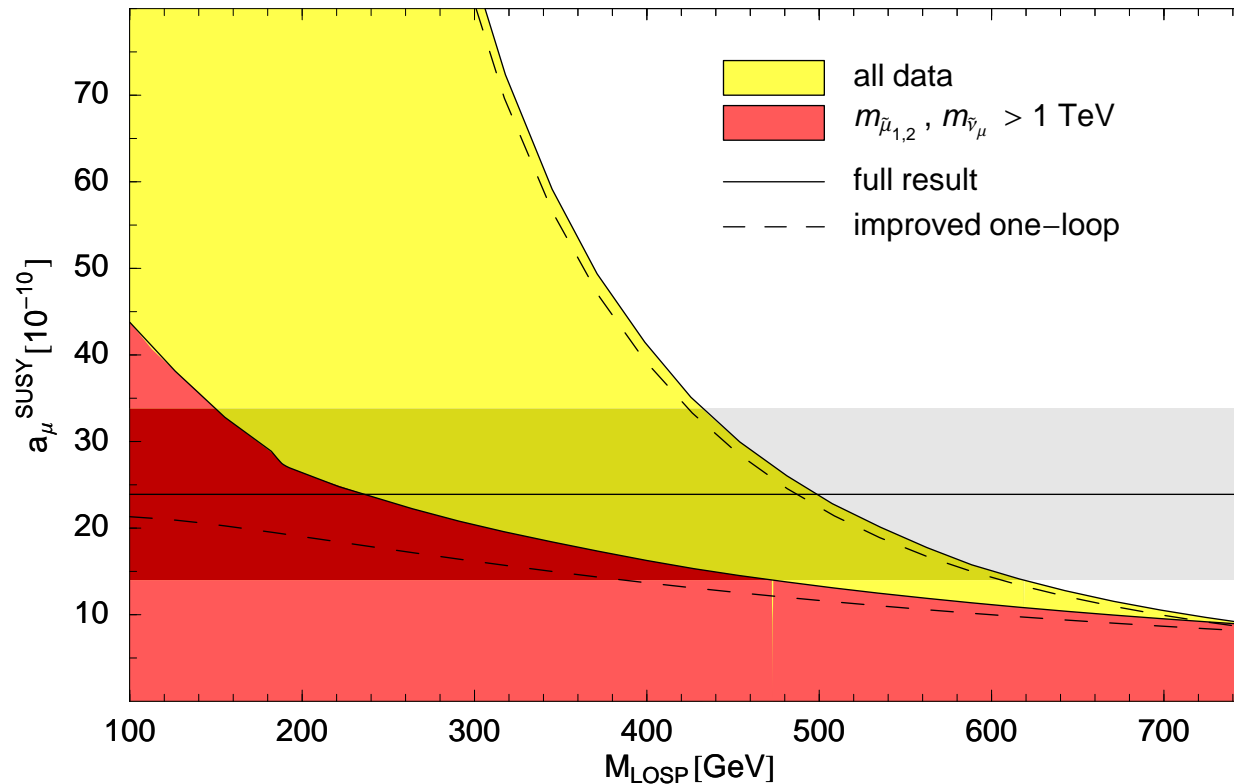
can provide missing contribution for

$$M_{\text{SUSY}} = 200 - 600 \text{ GeV}$$

2-loop calculation [*Heinemeyer, Stöckinger, ...*]

scan over SUSY parameters compatible with
EW and $b \rightarrow s\gamma$ constraints $(\tan \beta = 50)$

[Stöckinger]



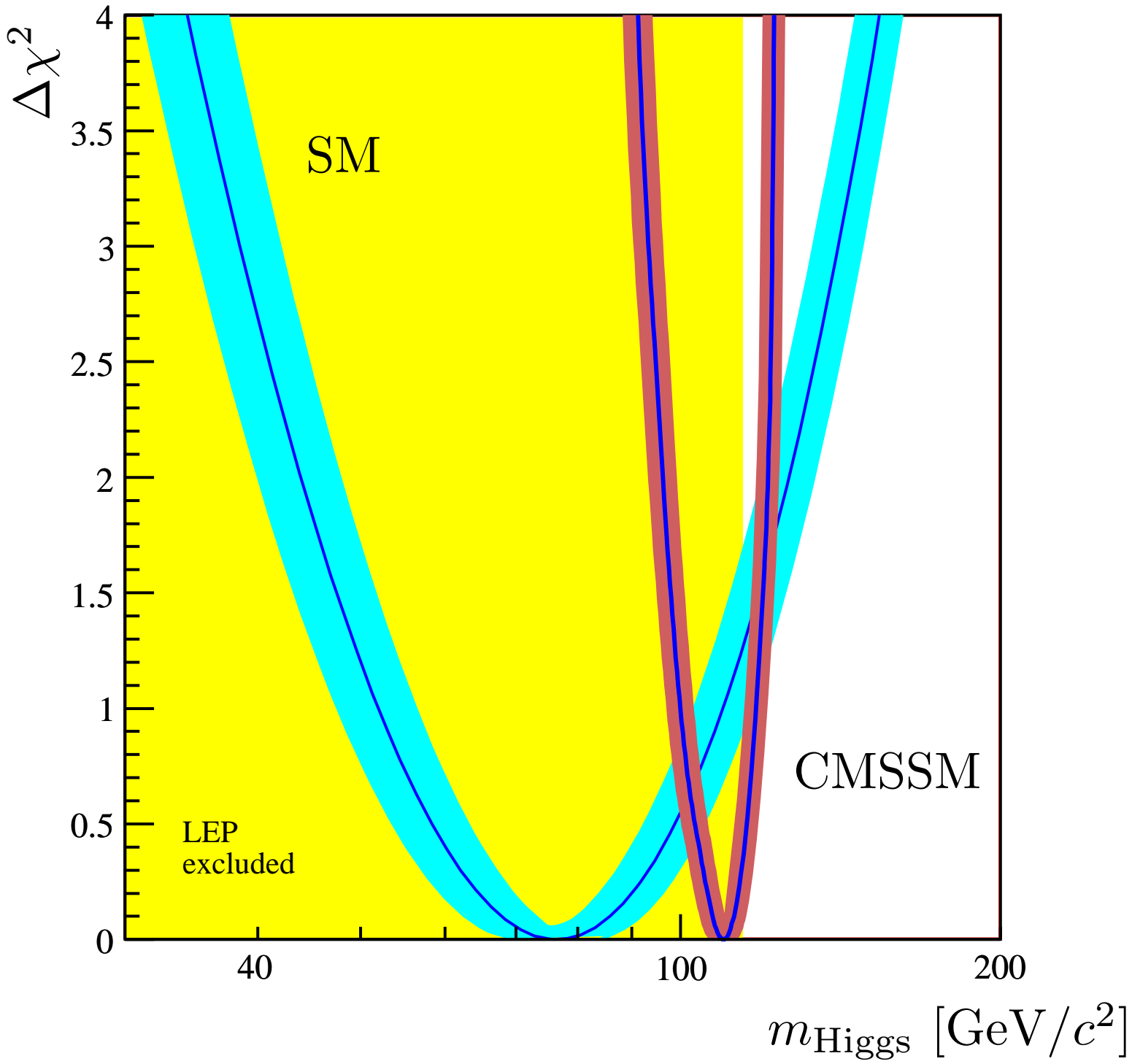
LOSP = lightest observable SUSY particle ($\chi_1^\pm, \chi_2^0, \dots$)

CMSSM			$ \sigma^{\text{meas}} - \sigma^{\text{fit}} / \sigma^{\text{meas}}$			
Variable	Measurement	Fit	0	1	2	3
$\Delta\alpha_{\text{had}}^{(5)}(m_Z)$	0.02758 ± 0.00035	0.02774	█			
m_Z [GeV]	91.1875 ± 0.0021	91.1873	█			
Γ_Z [GeV]	2.4952 ± 0.0023	2.4952	█			
σ_{had}^0 [nb]	41.540 ± 0.037	41.486	█	█		
R_l	20.767 ± 0.025	20.744	█	█		
$A_{\text{fb}}^{0,l}$	0.01714 ± 0.00095	0.01641	█	█		
$A_l(P_\tau)$	0.1465 ± 0.0032	0.1479	█	█		
R_b	0.21629 ± 0.00066	0.21613	█			
R_c	0.1721 ± 0.0030	0.1722	█			
$A_{\text{fb}}^{0,b}$	0.0992 ± 0.0016	0.1037	█	█	█	
$A_{\text{fb}}^{0,c}$	0.0707 ± 0.0035	0.0741	█	█		
A_b	0.923 ± 0.020	0.935	█	█		
A_c	0.670 ± 0.027	0.668	█			
$A_l(\text{SLD})$	0.1513 ± 0.0021	0.1479	█	█		
$\sin^2\theta_{\text{eff}}^{\text{lept}}(Q_{\text{fb}})$	0.2324 ± 0.0012	0.2314	█	█		
m_W [GeV]	80.398 ± 0.025	80.382	█	█		
m_t [GeV]	170.9 ± 1.8	170.8	█			
$R(b \rightarrow s\gamma)$	1.13 ± 0.12	1.12	█			
$B_s \rightarrow \mu\mu$ [$\times 10^{-8}$]	< 8.00	0.33				
Δa_μ [$\times 10^{-9}$]	2.95 ± 0.87	2.95				
Ωh^2	0.113 ± 0.009	0.113				

Standard Model			$ \sigma^{\text{meas}} - \sigma^{\text{fit}} / \sigma^{\text{meas}}$			
Variable	Measurement	Fit	0	1	2	3
$\Delta\alpha_{\text{had}}^{(5)}(m_Z)$	0.02758 ± 0.00035	0.02768	█			
m_Z [GeV]	91.1875 ± 0.0021	91.1875	█			
Γ_Z [GeV]	2.4952 ± 0.0023	2.4957	█			
σ_{had}^0 [nb]	41.540 ± 0.037	41.477	█	█		
R_l	20.767 ± 0.025	20.744	█	█		
$A_{\text{fb}}^{0,l}$	0.01714 ± 0.00095	0.01645	█	█		
$A_l(P_\tau)$	0.1465 ± 0.0032	0.1481	█	█		
R_b	0.21629 ± 0.00066	0.21586	█			
R_c	0.1721 ± 0.0030	0.1722	█			
$A_{\text{fb}}^{0,b}$	0.0992 ± 0.0016	0.1038	█	█	█	
$A_{\text{fb}}^{0,c}$	0.0707 ± 0.0035	0.0742	█	█		
A_b	0.923 ± 0.020	0.935	█	█		
A_c	0.670 ± 0.027	0.668	█			
$A_l(\text{SLD})$	0.1513 ± 0.0021	0.1481	█	█		
$\sin^2\theta_{\text{eff}}^{\text{lept}}(Q_{\text{fb}})$	0.2324 ± 0.0012	0.2314	█	█		
m_W [GeV]	80.398 ± 0.025	80.374	█	█		
m_t [GeV]	170.9 ± 1.8	171.3	█			
Γ_W [GeV]	2.140 ± 0.060	2.091	█			

global fit in the constrained MSSM including data from $g - 2$, B physics, and cosmic relic density

[O. Buchmueller et al., arXiv:0707.3447]



Scatter plots for M_W & $\sin^2 \theta_{\text{eff}}$

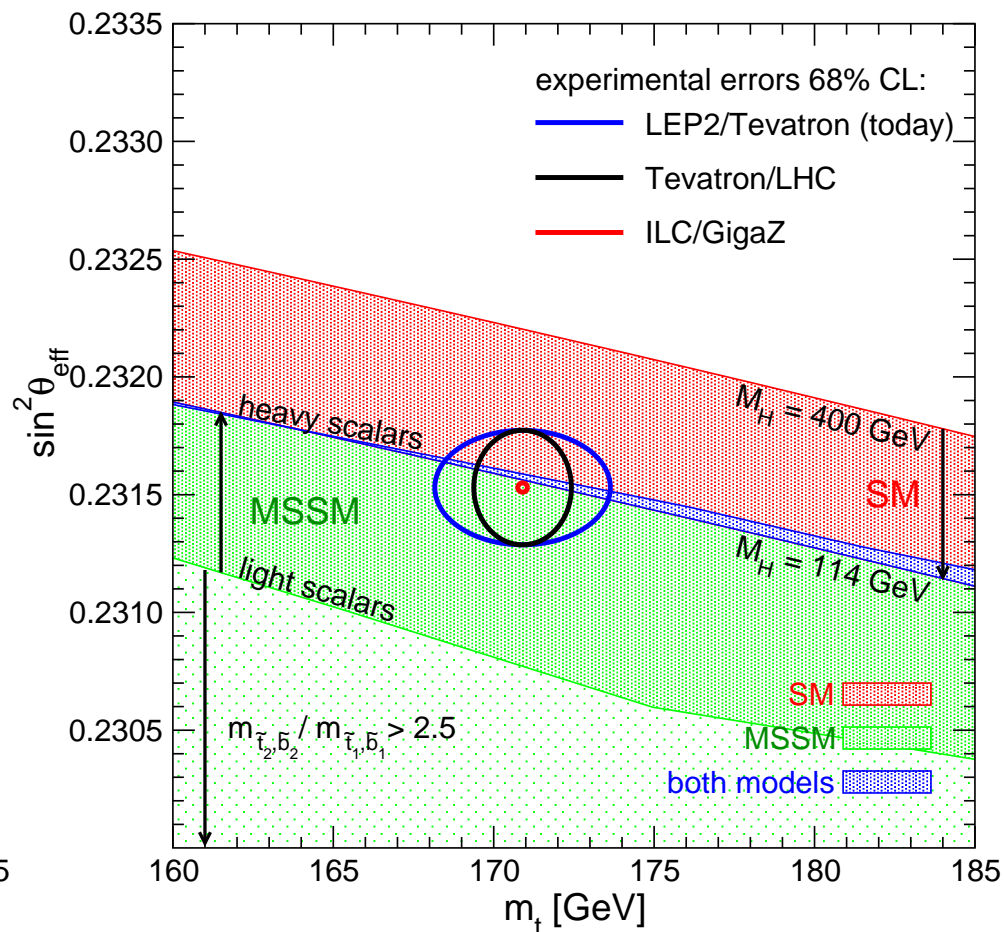
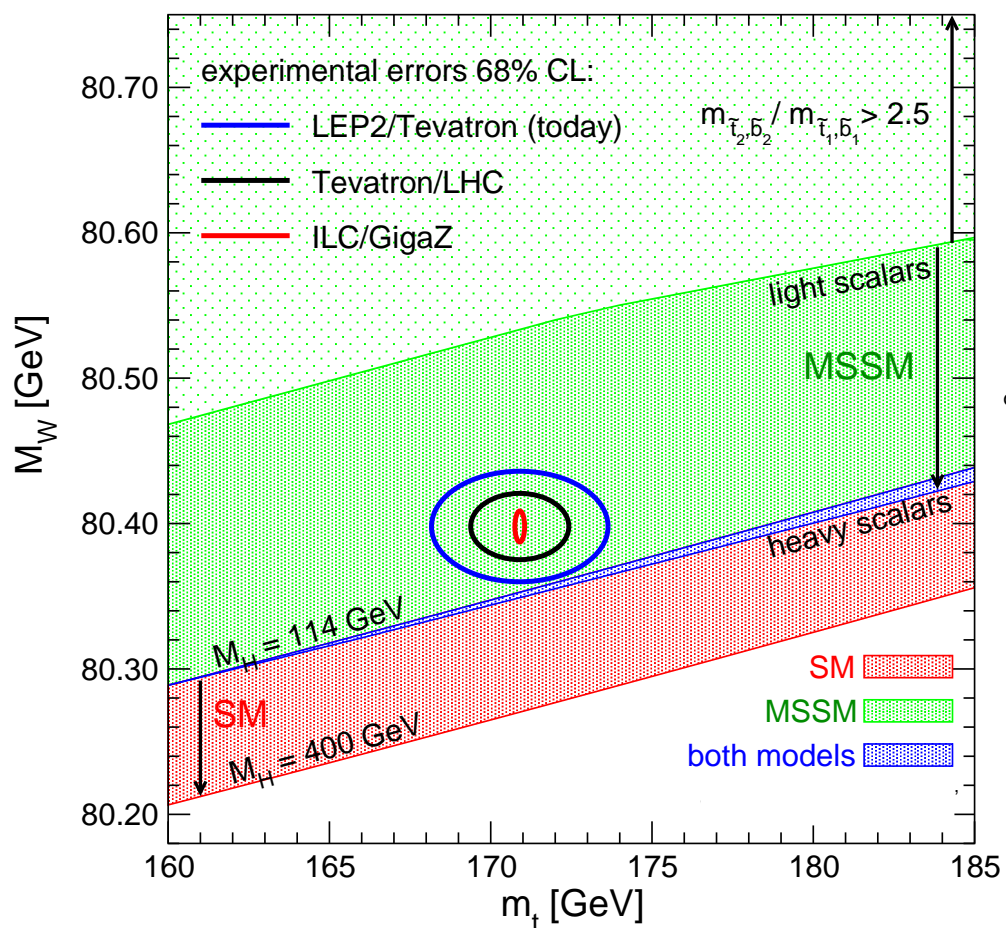
■ SUSY parameters:

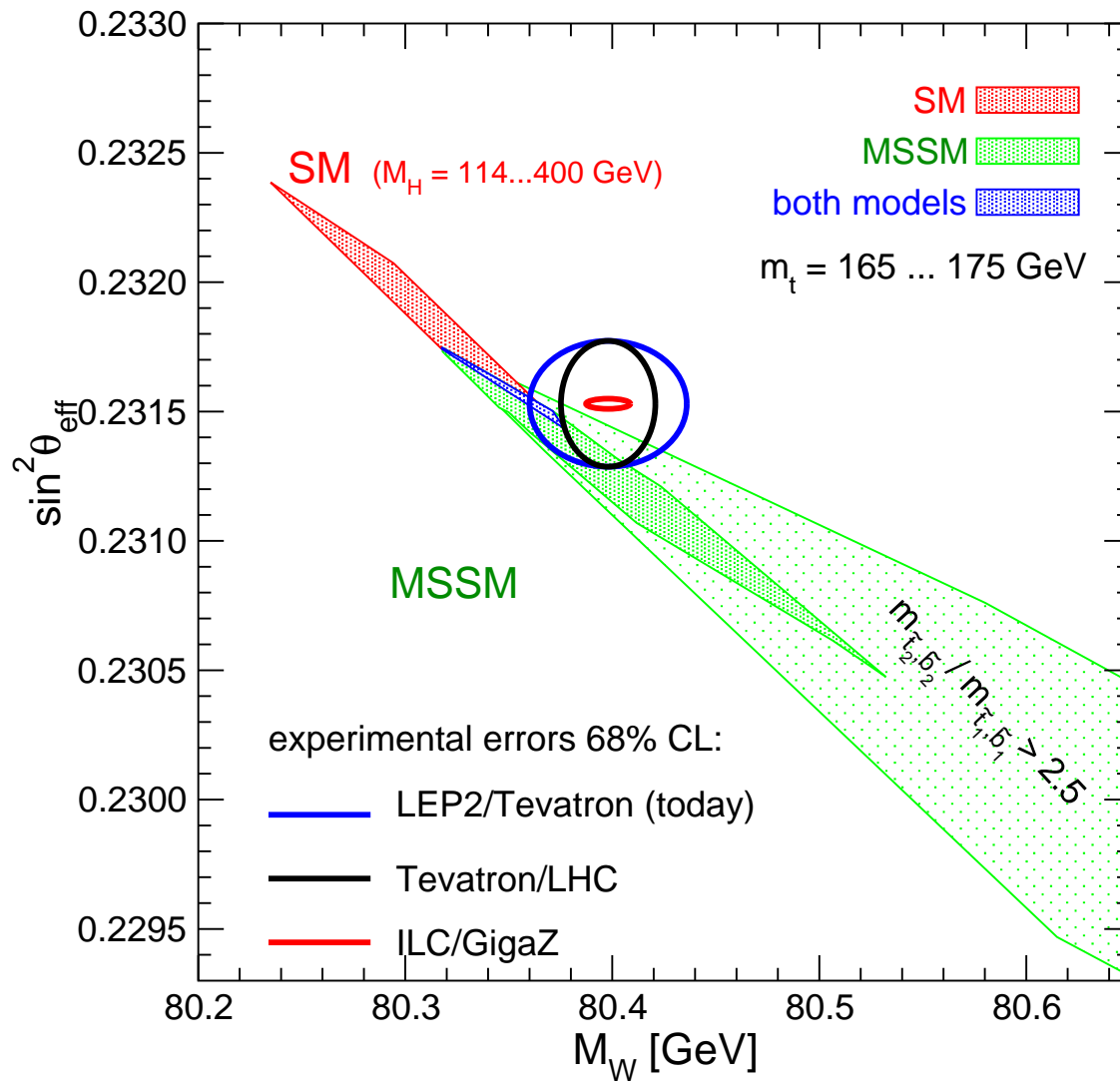
$$\begin{aligned} \text{sleptons} & : M_{\tilde{F}, \tilde{F}'} = 100 \dots 2000 \text{ GeV} \\ \text{light squarks} & : M_{\tilde{F}, \tilde{F}'_{\text{up/down}}} = 100 \dots 2000 \text{ GeV} \\ \tilde{t}/\tilde{b} \text{ doublet} & : M_{\tilde{F}, \tilde{F}'_{\text{up/down}}} = 100 \dots 2000 \text{ GeV} \\ & A_{t,b} = -2000 \dots 2000 \text{ GeV} \\ \text{gauginos} & : M_{1,2} = 100 \dots 2000 \text{ GeV} \\ & m_{\tilde{g}} = 195 \dots 1500 \text{ GeV} \\ & \mu = -2000 \dots 2000 \text{ GeV} \\ \text{Higgs} & : M_A = 90 - 1000 \text{ GeV} \\ & \tan \beta = 1.1 \dots 60 \end{aligned}$$

- Unconstrained scan, only Higgs mass required to be in agreement with LEP data.

[Heinemeyer, Hollik, Stöckinger, Weber, Weiglein]

$M_W(m_t)$ and $\sin^2 \theta_{\text{eff}}(m_t)$ in the MSSM





Outlook – Possible scenarios

- a single light Higgs boson
 - SM Higgs boson?
 - SUSY light Higgs boson?
 H, A, H^\pm heavy (decoupling scenario) $h \sim H_{\text{SM}}$
- a light Higgs boson + more (H, A, H^\pm)
 - SUSY Higgs?
 - non-SUSY 2-Higgs-Doublet model?
- a single heavy Higgs boson ($\gg 200$ GeV)
 - SUSY ruled out
 - SM + (?) strong interaction?
- no Higgs boson
 - strongly interacting weak interaction
new strong force \sim TeV scale

Conclusions

- **Electroweak precision physics**
 - sensitive to quantum structure
 - constraints on unknown parameters
- **precision tests of the Standard Model have established the SM as a quantum field theory**
- **MSSM is competitive to the SM**
 - global fits of similar quality (even better)
 - natural: light Higgs boson h^0
- **future experiments at colliders**
 - discovery of Higgs and SUSY at LHC (?)
 - precision studies at e^+e^- Linear Collider