

Fluctuation studies in Phobos

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for the  collaboration

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Workshop on “Correlations and fluctuations ”
Florence, Italy, July 8, 2006

PHOBOS collaboration (July 2006)

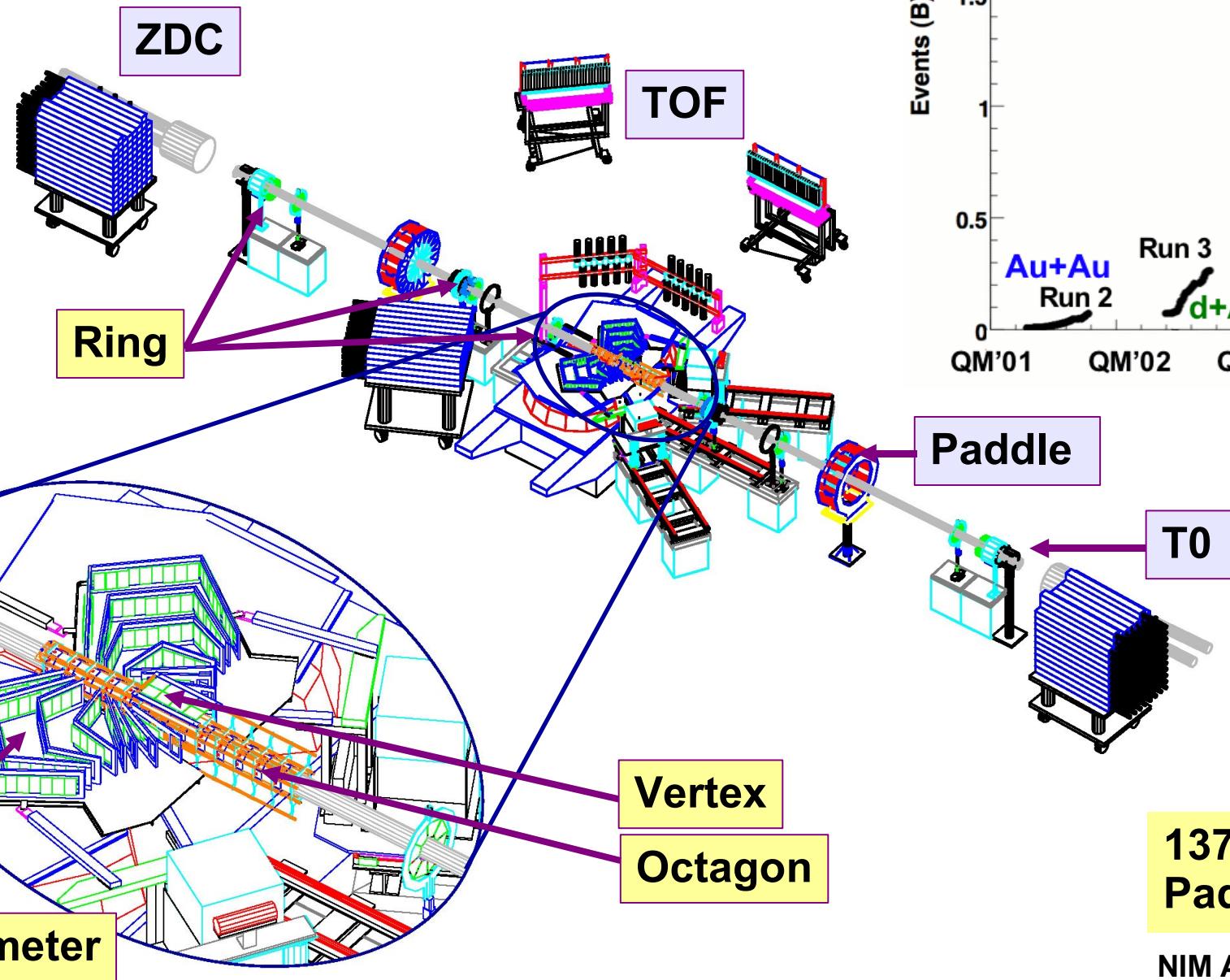


Burak Alver, Birger Back, Mark Baker, Maarten Ballintijn, Donald Barton, Russell Betts, Richard Bindel, Wit Busza (Spokesperson), Zhengwei Chai, Vasundhara Chetluru, Edmundo García, Tomasz Gburek, Kristjan Gulbrandsen, Clive Halliwell, Joshua Hamblen, Ian Harnarine, Conor Henderson, David Hofman, Richard Hollis, Roman Hołyński, Burt Holzman, Aneta Iordanova, Jay Kane, Piotr Kulinich, Chia Ming Kuo, Wei Li, Willis Lin, Constantin Loizides, Steven Manly, Alice Mignerey, Gerrit van Nieuwenhuizen, Rachid Nouicer, Andrzej Olszewski, Robert Pak, Corey Reed, Eric Richardson, Christof Roland, Gunther Roland, Joe Sagerer, Iouri Sedykh, Chadd Smith, Maciej Stankiewicz, Peter Steinberg, George Stephans, Andrei Sukhanov, Artur Szostak, Marguerite Belt Tonjes, Adam Trzupek, Sergei Vaurynovich, Robin Verdier, Gábor Veres, Peter Walters, Edward Wenger, Donald Willhelm, Frank Wolfs, Barbara Wosiek, Krzysztof Woźniak, Shaun Wyngaardt, Bolek Wysłouch

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PHOBOS experiment (Run5)



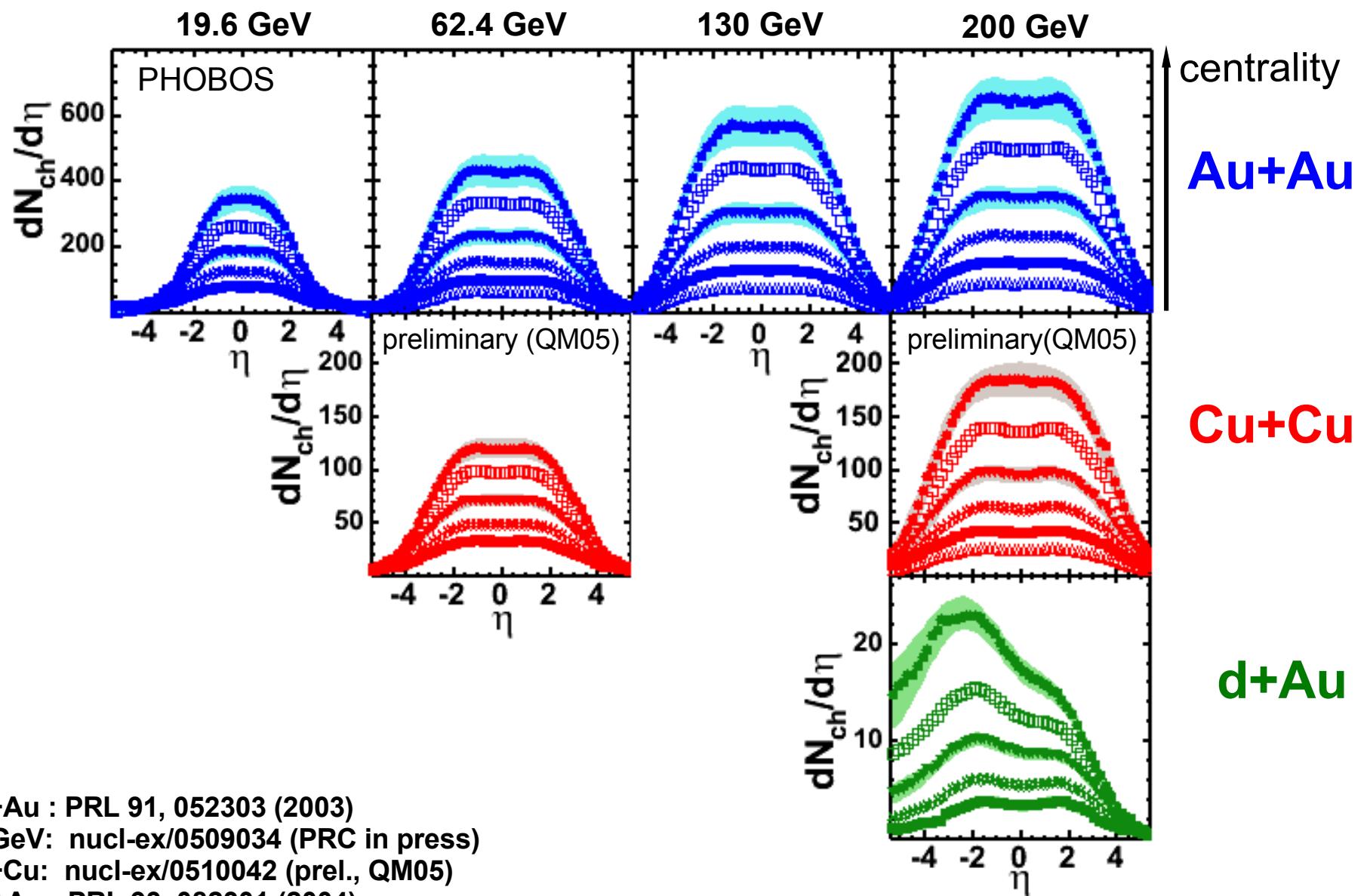
137000 Silicon
Pad Channels

NIM A499, 603-23 (2003)

Outline

- 1) Single-particle distributions
- 2) Unusual event search
- 3) Forward/backward multiplicity correlations
- 4) Two-particle angular correlations
- 5) Eccentricity fluctuations
- 6) Elliptic flow fluctuations

Charged hadron $dN/d\eta$ -distributions (1)



Charged hadron $dN/d\eta$ -distributions (2)

- Rich data set of p+p, p+A and A+A
- Scaling features of charged hadron multiplicities
 - Npart scaling
 - Extended longitudinal scaling (aka Limiting Fragmentation)
 - Factorization of energy/centrality dependence
 - Universality of total multiplicity in A+A, p+p and e^+e^-
- Seen over a wide range of collision energy

Charged hadron $dN/d\eta$ -distributions (2)

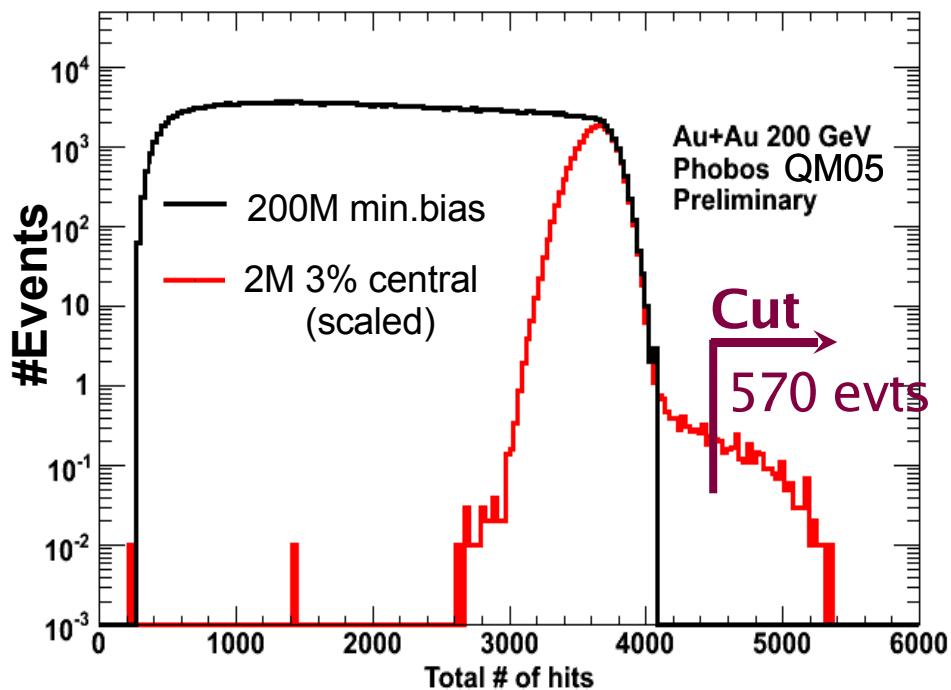
- Rich data set of $p+p$, $p+A$ and $A+A$
- Scaling features of charged hadron multiplicities
 - Npart scaling
 - Limiting Fragmentation
 - Factorization of energy/centrality dependence
 - Universality of total multiplicity in $A+A$, $p+p$ and e^+e^-
- Seen over a wide range of collision energy

In all of the above, $dN/d\eta$ is
single-particle event average

2) Unusual event search

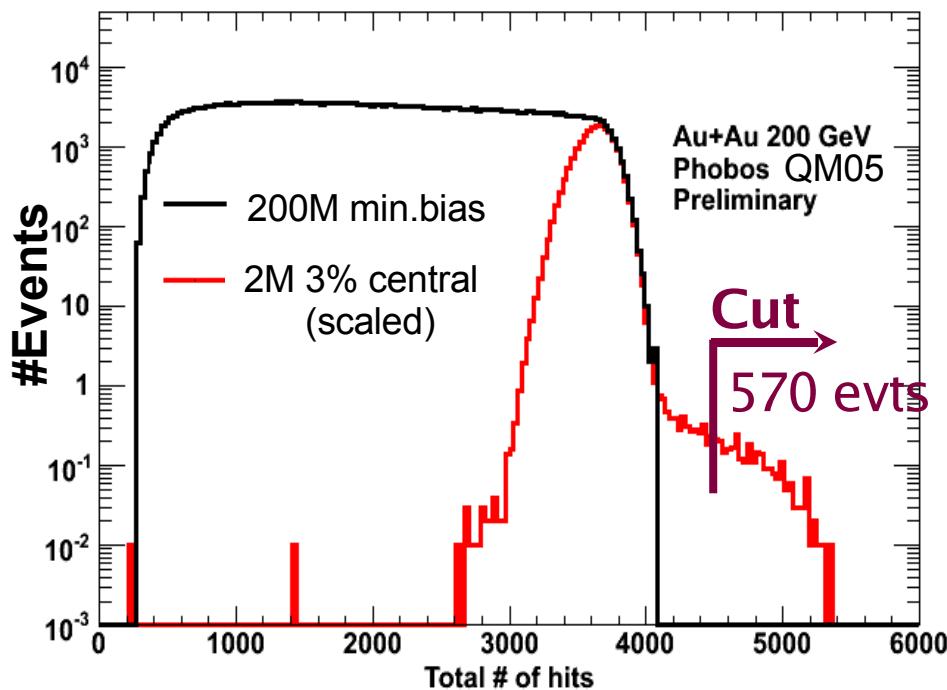
- Beyond the average dN/dn
 - Are there events with very large multiplicity?
 - Does the $dN/d\eta$ shape vary from event to event?

Unusual events: Large total multiplicity

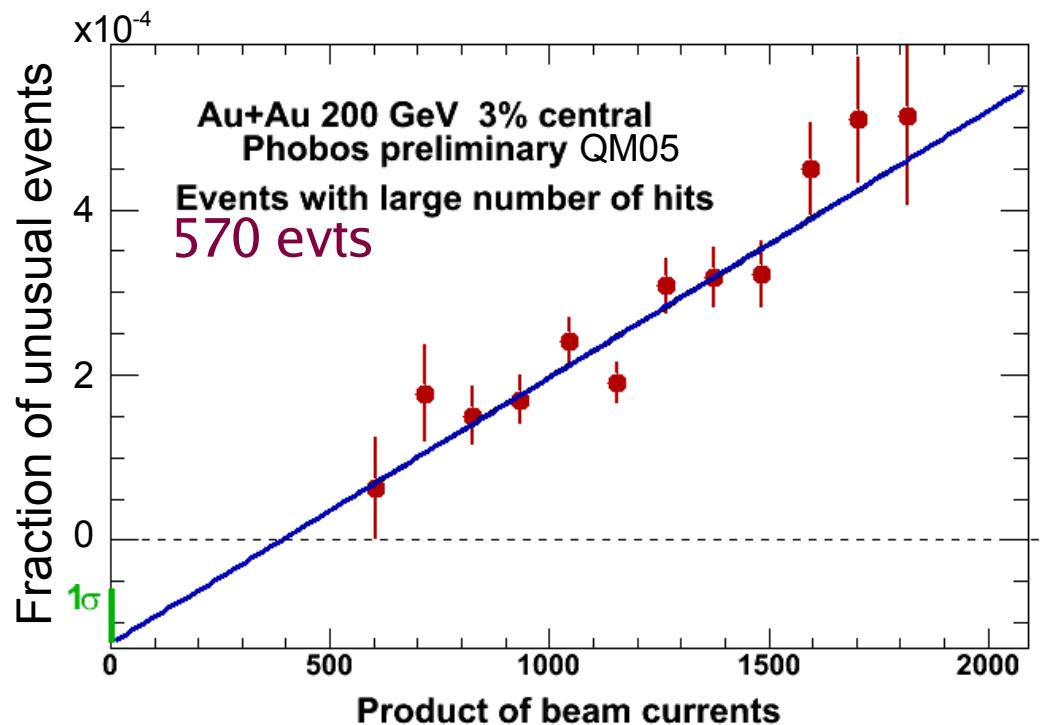


- Use high-statistics Run-4 AuAu data and select 3% central data (with loose data-quality cuts)
- Look at events with a large number of hits: $\sim 10^4$ (570/2M) events

Unusual events: Large total multiplicity

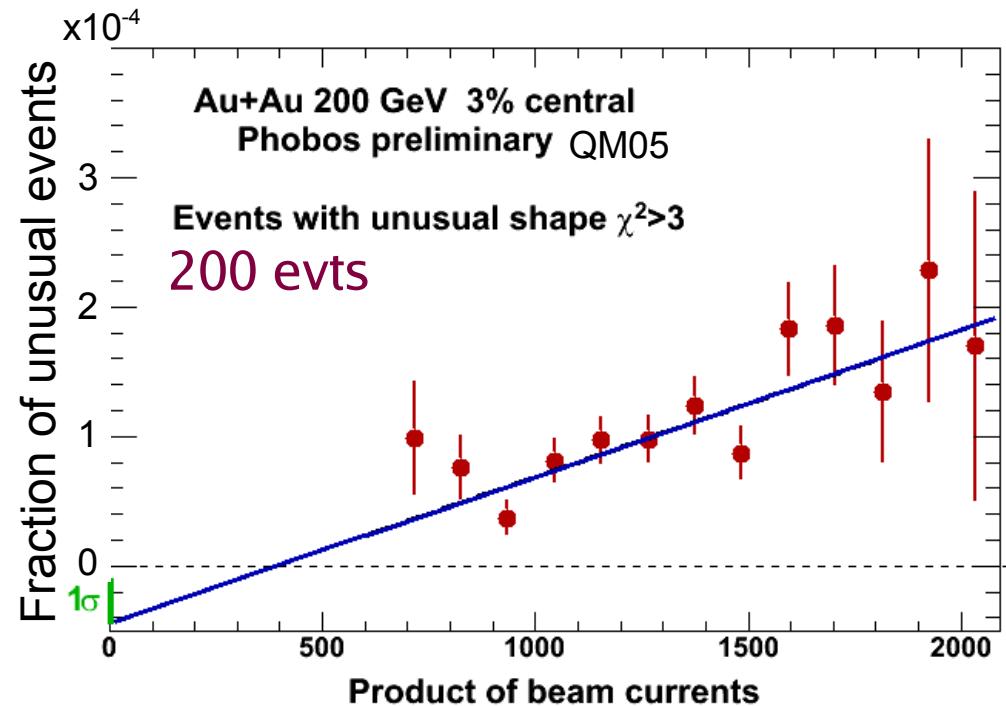
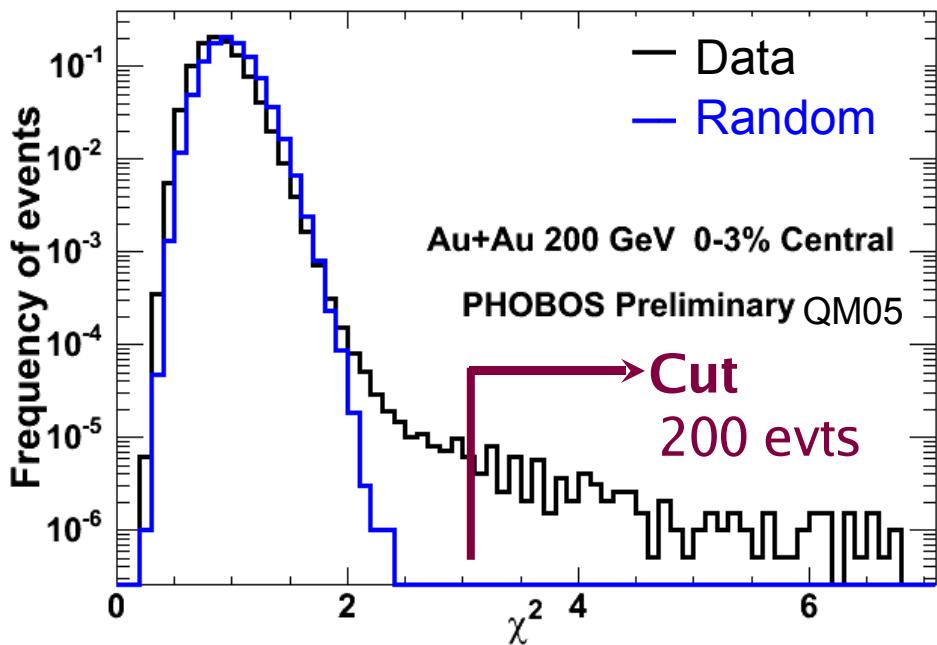


- Use high-statistics Run-4 AuAu data and select 3% central data (with loose data-quality cuts)
- Look at events with a large number of hits: $\sim 10^4$ ($570/2M$) events



- Events with large number of hits are strongly correlated with beam rate
- Rate of “unusual” events extrapolated to low luminosity is consistent with zero

Unusual events: $dN/d\eta$ -shape



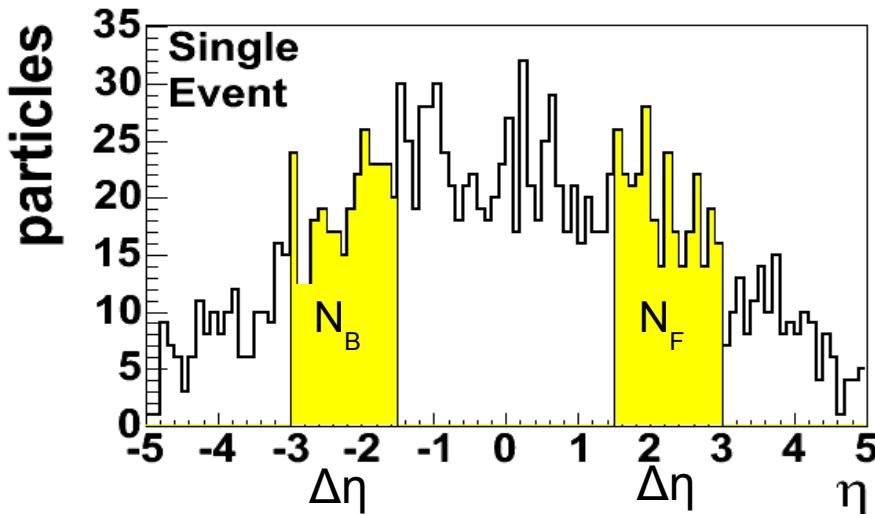
- Devide $dN/d\eta$ into individual bins (η , vertex) to get the average and its variance
- Calculate χ^2 for each event
- Compare to “random” events: distinct tail $\sim 10^{-4}$ (200/2M) events

- Events with large χ^2 are again strongly correlated with beam rate
- Rate of “unusual” events extrapolated to low luminosity is again consistent with zero

3) Forward/backward multiplicity fluctuations

- Beyond the average dN/dn
 - Quantify E-by-E correlations in particle-production over regions in η

Forward/backward multiplicity fluctuations



$$C(\eta, \Delta\eta) = \frac{N_F - N_B}{\sqrt{N_F + N_B}}$$

Use variance σ^2_C

- Independent particle production

$$\sigma^2_C = 1$$

- Correlated particle production

- Long range $\sigma^2_C \rightarrow 0$

- Short range $\sigma^2_C > 1$

- Clusters of size k within $\Delta\eta$

$$C \rightarrow \sqrt{k} C$$

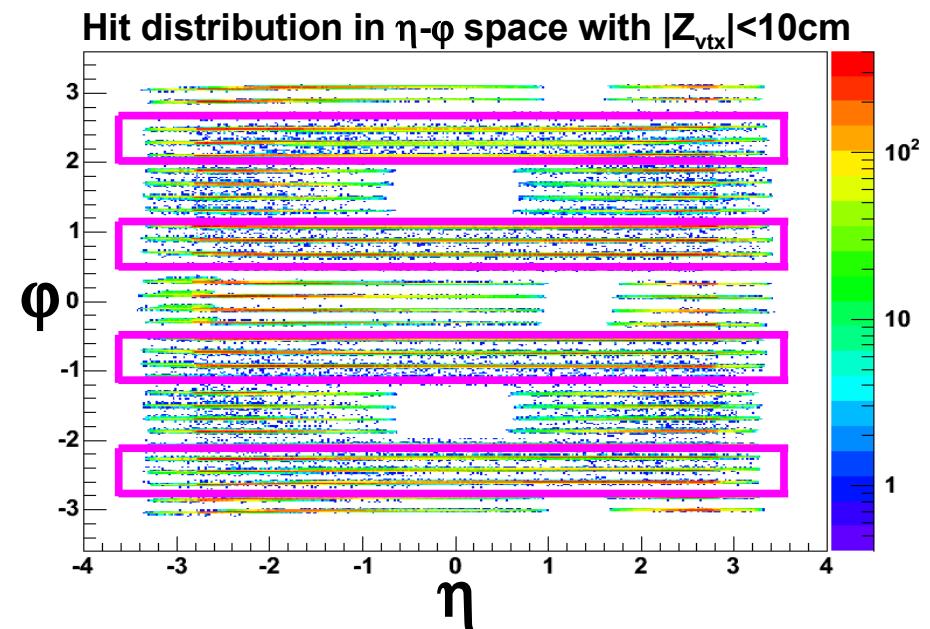
$$\sigma^2_C \rightarrow k \sigma^2_C$$

- If limited rapidity window ($\Delta\eta$)

$$k \rightarrow k_{\text{eff}}$$

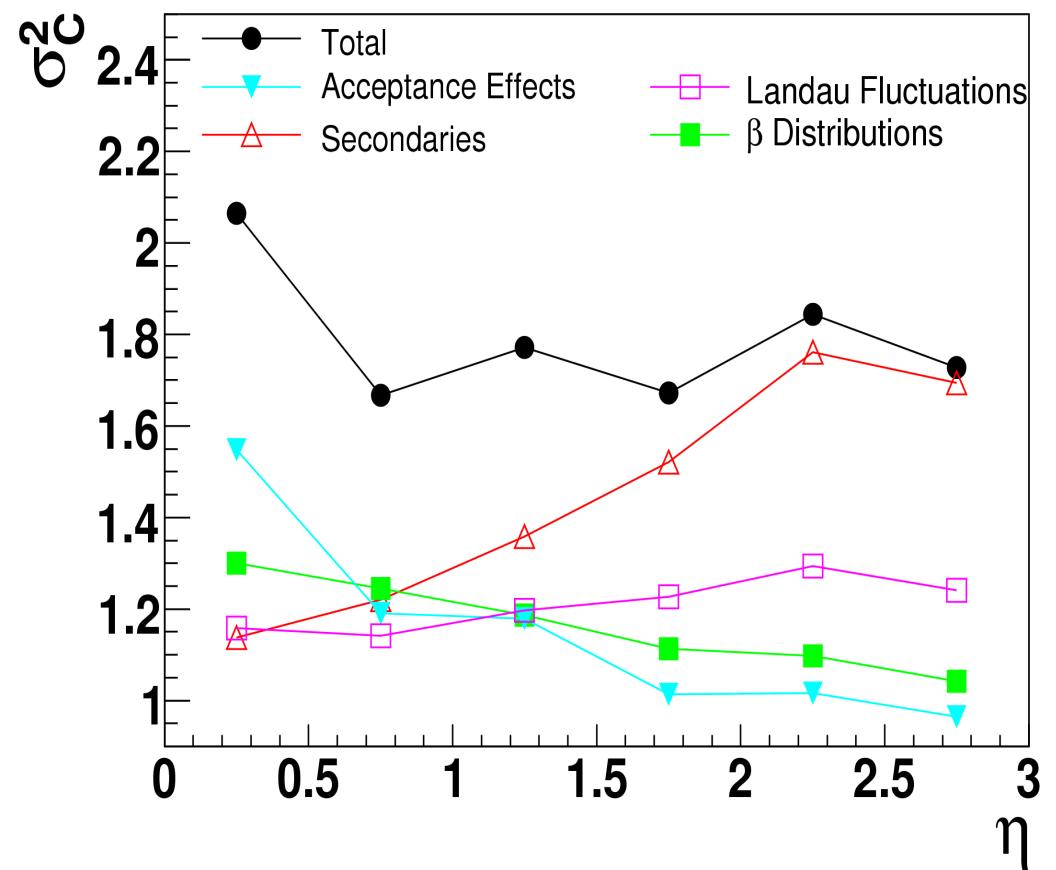
Extraction of σ^2_c

- Deal with large occupancy in the octagon
 - Use η -bin-dependent lower and upper dE/dx cuts on hits to suppress contribution from secondaries
- Deal with limited acceptance
 - Correct gap effects E-by-E with z-vertex dependent offset
 - Avoiding holes in octagon
 - Only **half** acceptance in ϕ
 - Correction ~ 2 , found with MC
- Deal with contribution of detector effect (see next slides)



Contributing sources of detector effects

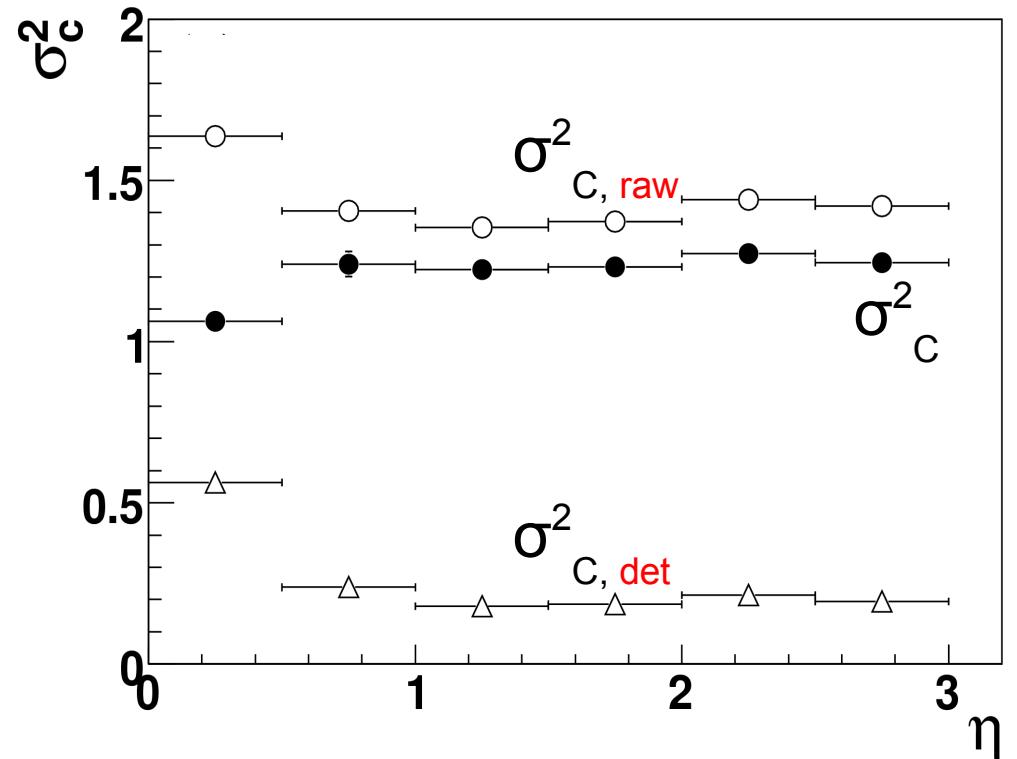
- Acceptance effects
- Secondaries
- dE/dx fluctuations
 - Landau fluctuation
 - Velocity (β) variation



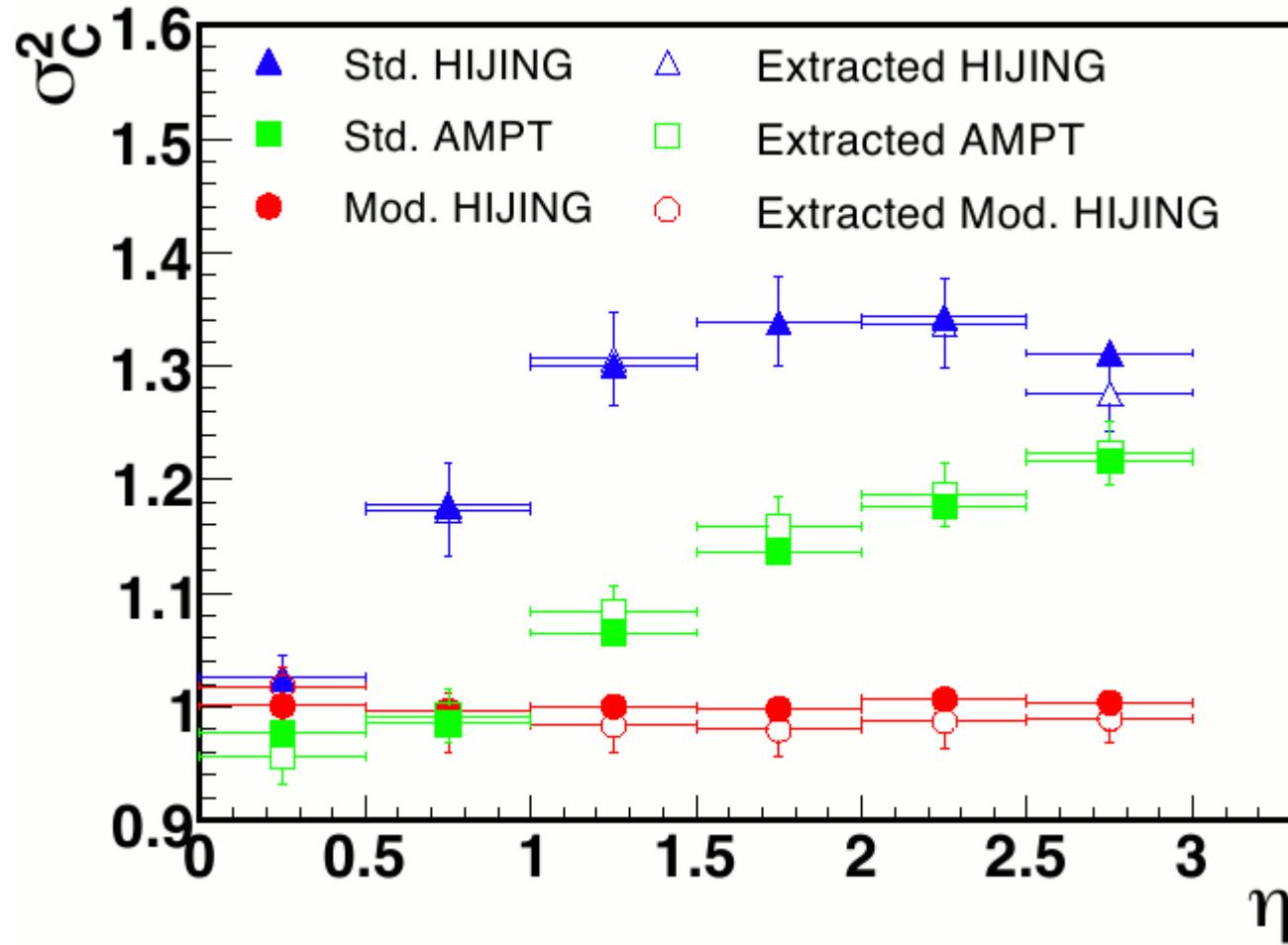
Different contributions add in quadrature
and resulting detector effects are flat in η

Removing detector effects

- Assuming $\sigma_{c, \text{raw}}^2 = \sigma_c^2 + \sigma_{c, \text{det}}^2$
- Modified HIJING with randomized sign of particle η to force $\sigma_c^2 = 1$
 - Direct access to $\sigma_{c, \text{det}}^2$
- Correction slightly depends on size of signal
 - Cure residual correlation
$$\sigma_{c, \text{det}}^2 \rightarrow \sigma_{c, \text{det}}^2 - \alpha (\sigma_c^2 - 1)$$
 - $\alpha = \text{constant}(\eta, \Delta\eta, \text{cent})$
- Systematic errors estimated to $\Delta\sigma_c^2 = 0.1$ (averaged over η)

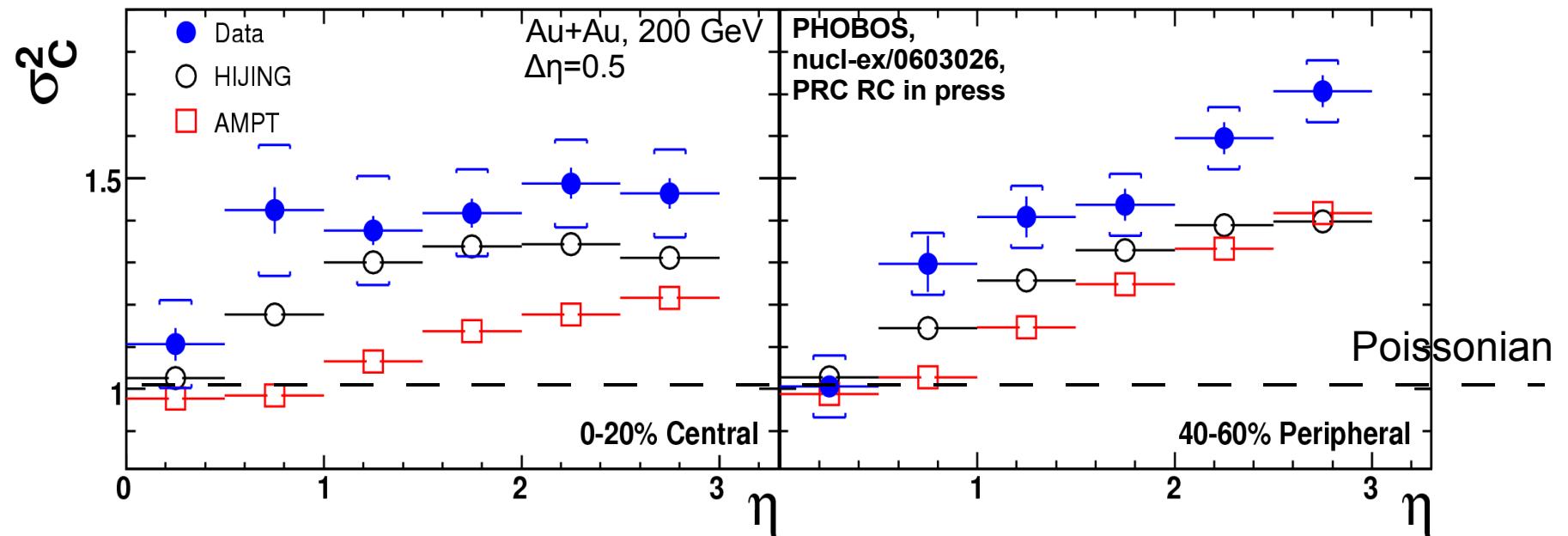


Verification with various MC

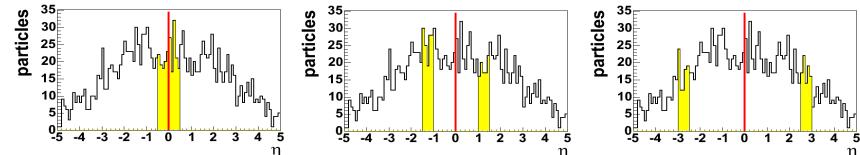


For the same tuning, the reconstructed σ_c^2 agrees with raw σ_c^2 within the errors in all tested models

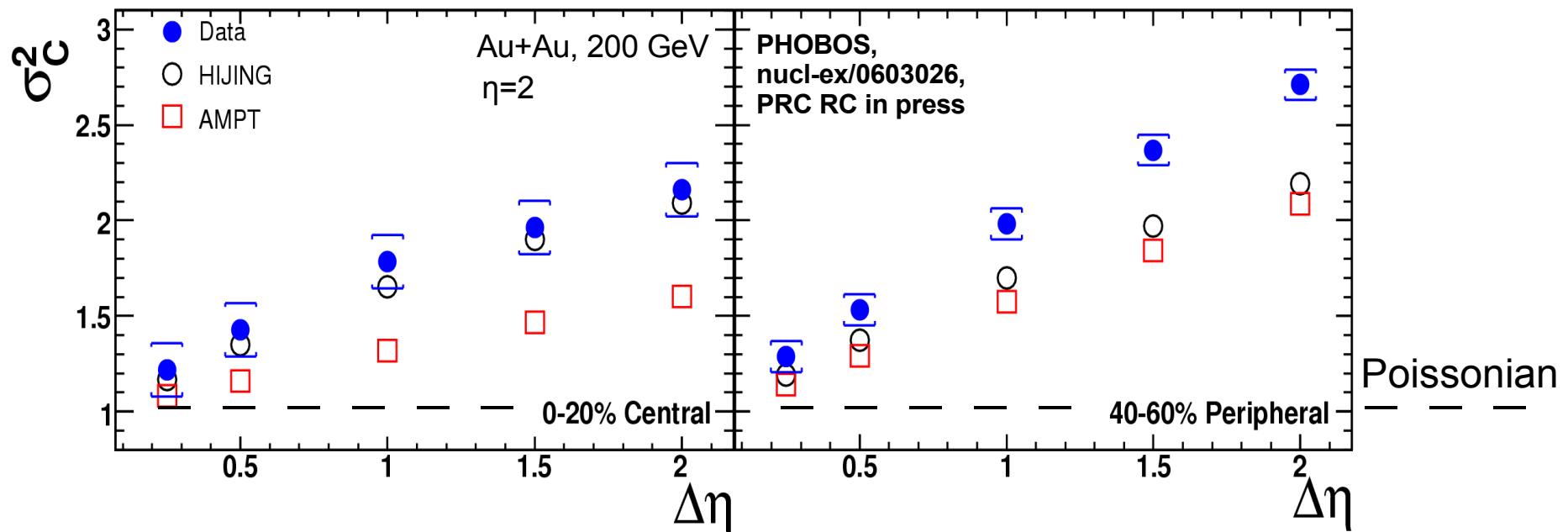
F/B results: σ_c^2 vs. η for fixed $\Delta\eta$



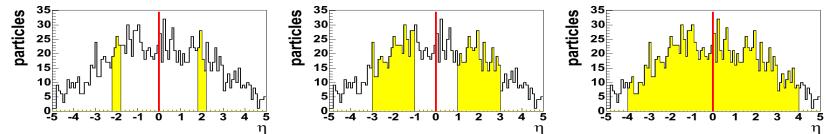
- Centrality dependence in slope observed
 - Models systematically lower (partially within errors)
- HIJING & AMPT agree in peripheral, but diverge in central events
- At $\eta=0$, models and data yield $\sigma_c^2 = 1$
 - Induced “intrinsic” long-range correlations?



F/B results: σ_c^2 vs. $\Delta\eta$ at fixed $\eta=2$



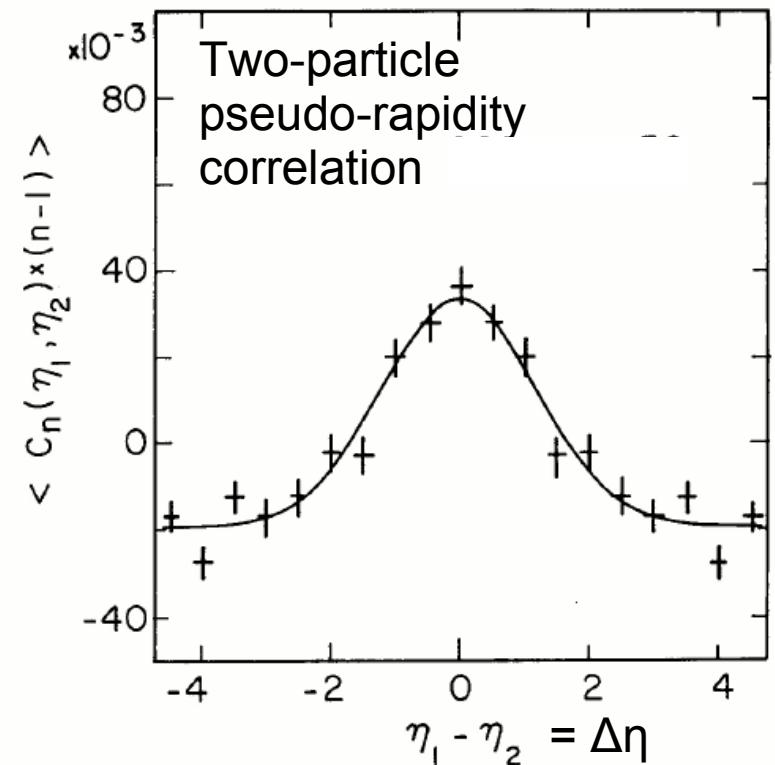
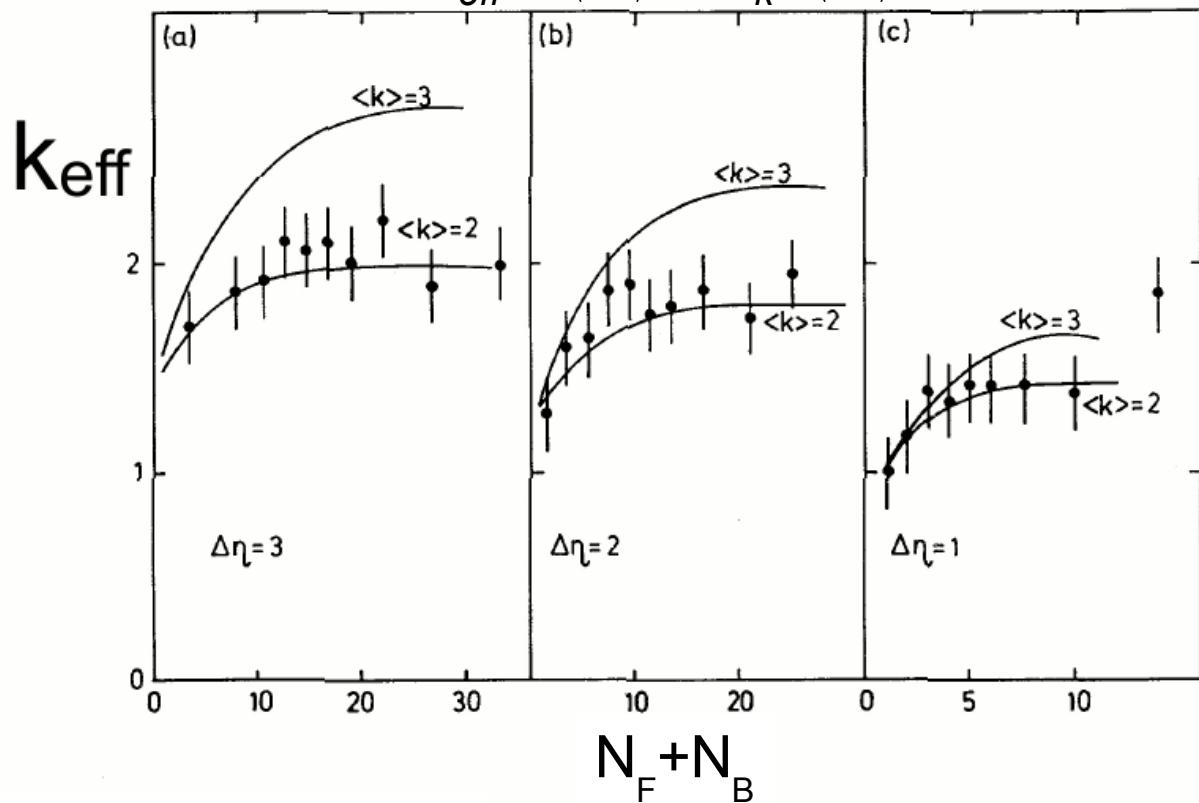
- Monotonic rise with increasing $\Delta\eta$ -bin width
- Particles produced in effective cluster size
 - Central: $k_{\text{eff}} = 2-2.3$
 - Peripheral: $k_{\text{eff}} = 2.6-2.8$
- Models do not simultaneously describe centrality and $\Delta\eta$ dependence



Clusters in elementary collisions

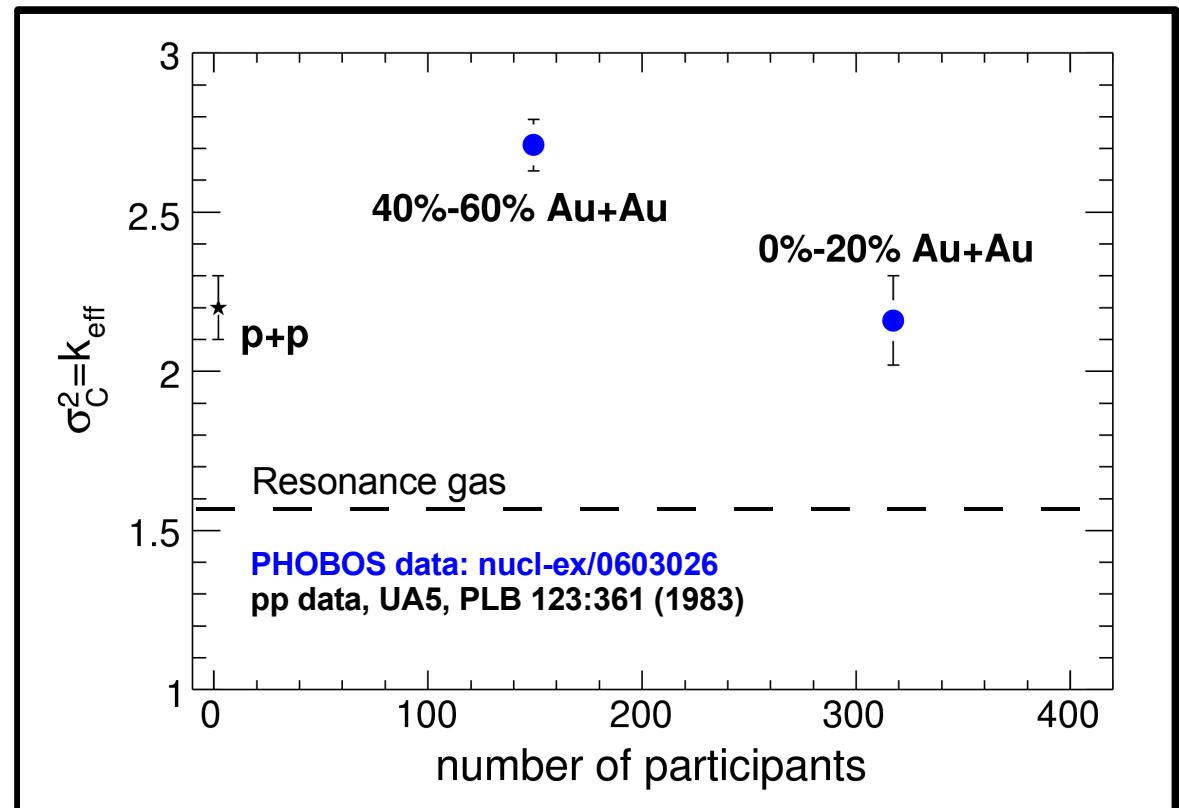
UA5: Phys.Lett.B123:361,1983

$$k_{\text{eff}} = \langle k \rangle + \sigma_k^2 / \langle k \rangle$$



Clusters in Au+Au are reminiscent
of results from p+ \bar{p}

Centrality dependence of σ_C^2



Centrality dependence of σ_c^2

- Model short and long range contribution

$$\sigma_c^2 = f \sigma_{SR}^2 + (1-f) \sigma_{LR}^2$$

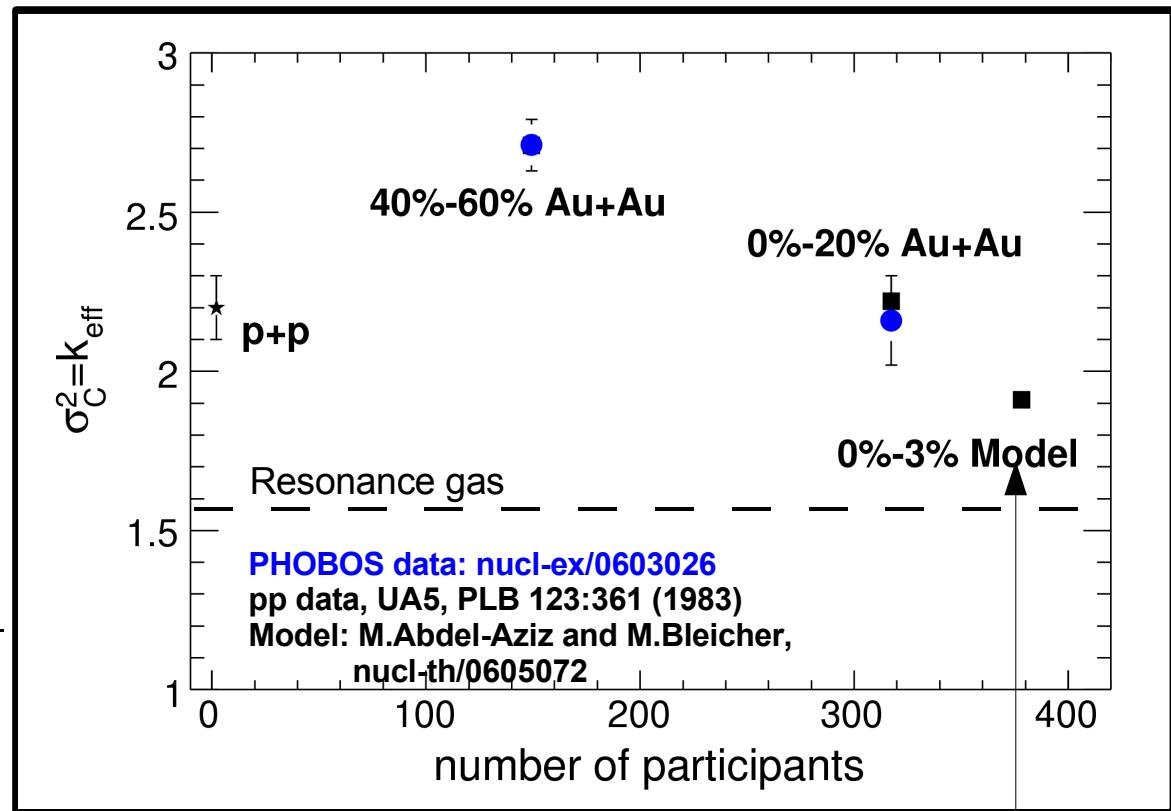
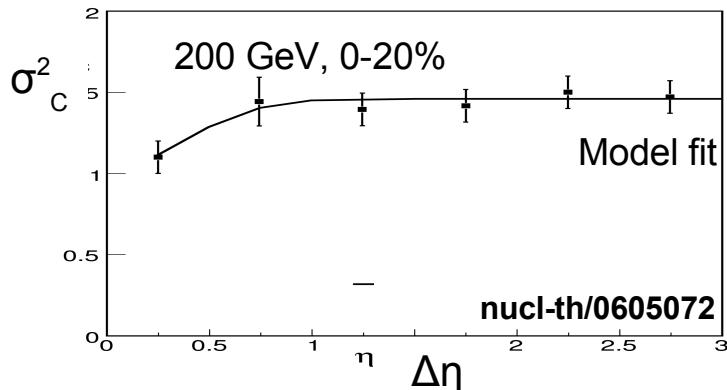
where **short range**

$$\sigma_{SR}^2 = k [1 - \exp(-\Delta\eta/\lambda_{short})]$$

and **long range**

$$\sigma_{LR}^2 = 1 - \frac{\xi}{f} \int d\eta_1 d\eta_2 \exp \frac{-(\eta_1 - \eta_2)^2}{2\lambda_{long}^2}$$

- Constrain parameters



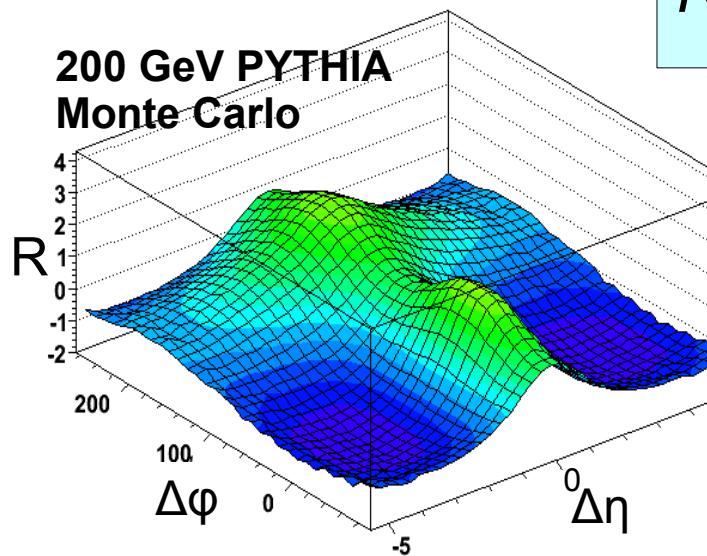
Cent.
Extra-
polation

data	f	ξ	λ_{short}	λ_{long}
Au+Au 0% – 20%	0.88	1.8	0.4	0.7
Au+Au 40% – 60%	0.99	2.5	0.6	0.9

4) Two-particle angular correlations

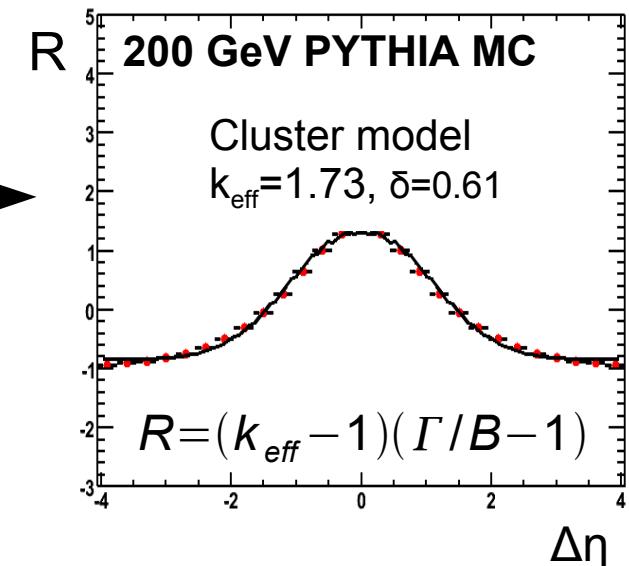
- Extend correlations from regions in $dN/d\eta$
 - **Two-particle angular correlations**

Two-particle angular correlations



$$R = \langle (n-1)(\frac{F}{B}-1) \rangle$$

Projection onto η
(altern. onto ϕ)



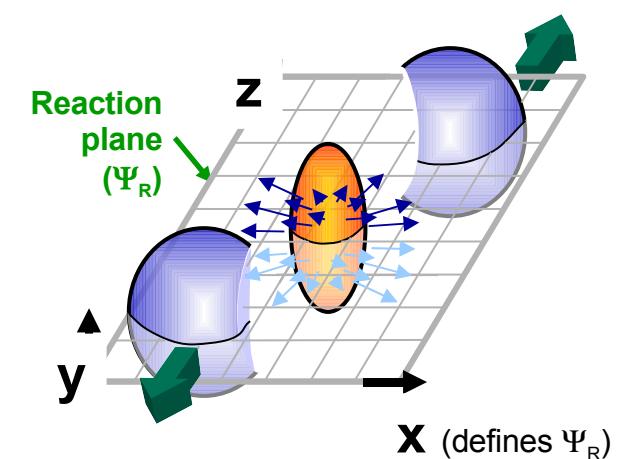
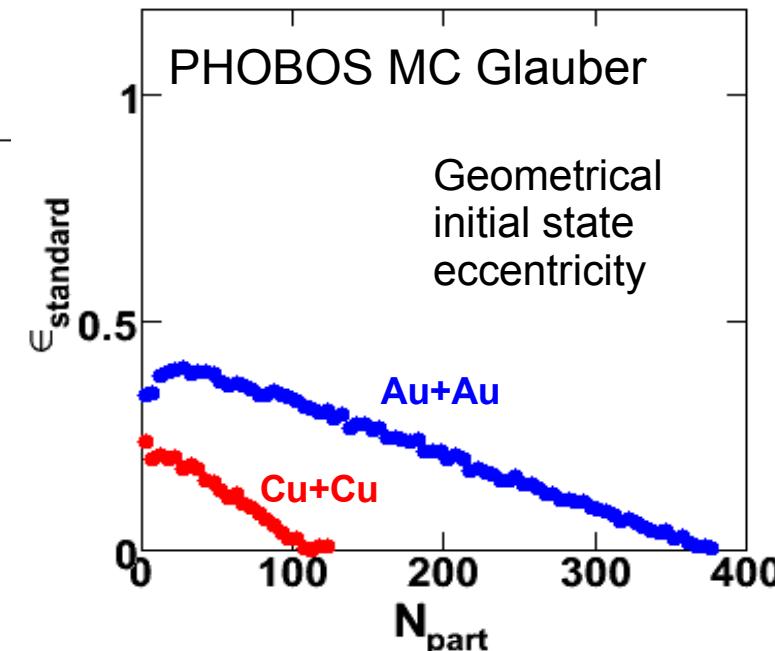
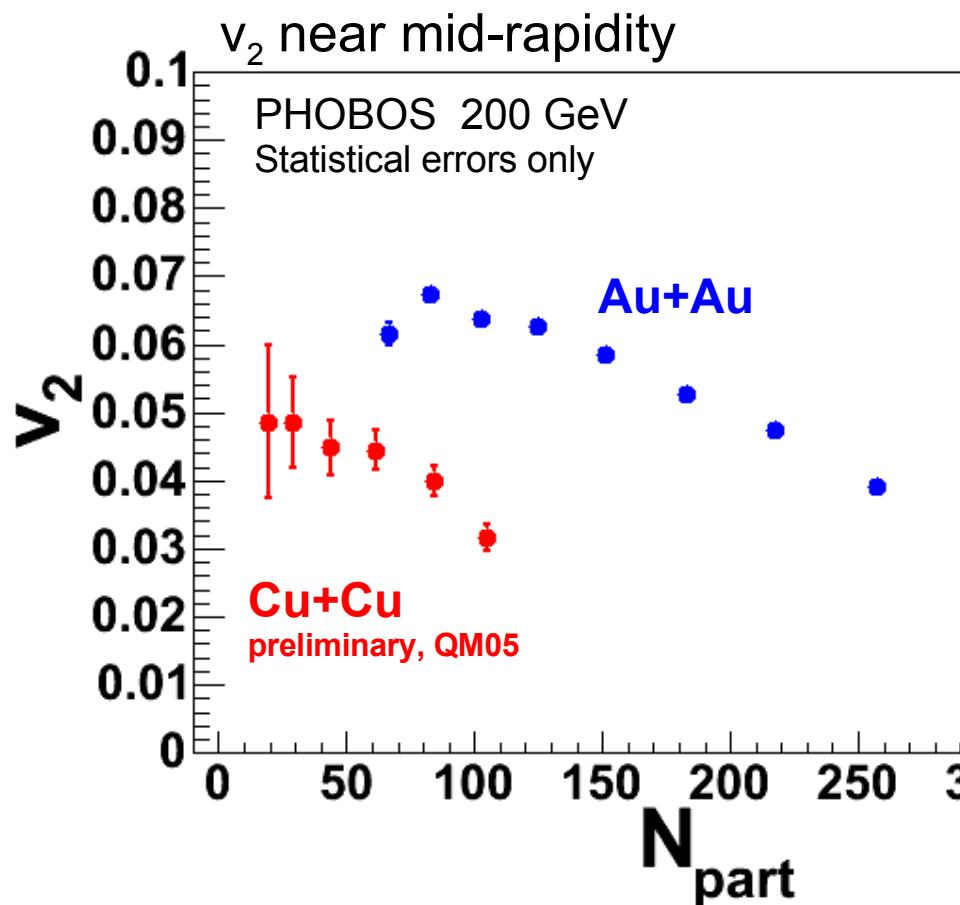
See Wei Li's talk

- Construction of R , event-by-event, weighted by event multiplicity
 - Full ϕ and large $|\eta| \leq 3$ coverage ($|\eta| \leq 5$ for future studies)
 - Single hit in silicon layer instead of particle information
 - Need special strategy for secondaries
 - No trigger particle
 - Study soft physics (fragmentation and hadronization processes)
 - Relative to trigger particle under investigation

5) Eccentricity fluctuations

- From two-particle angular correlations (clusters at hadronization times)
 - To fluctuations in the initial-state geometry and its connection to elliptic flow

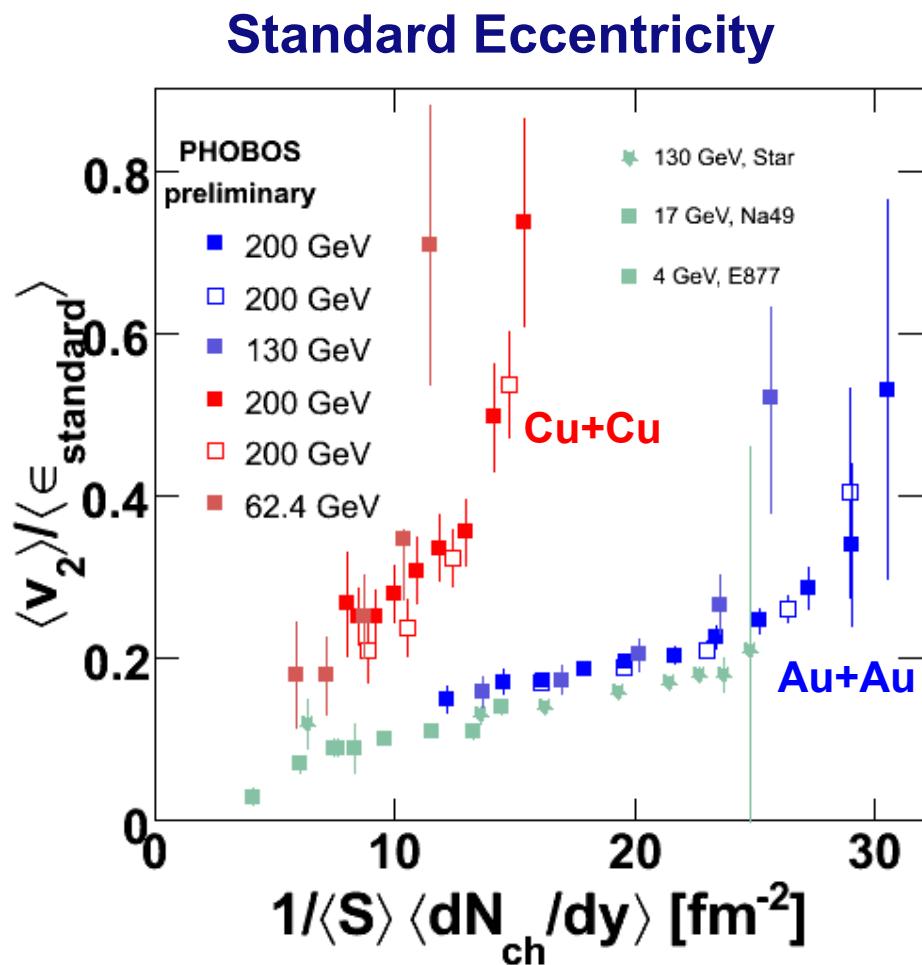
Elliptic flow in Cu+Cu and Au+Au



Au+Au: PRL 94, 122303 (2005)
Cu+Cu: prel. QM05, nucl-ex/0510042

$$dN/d(\phi - \Psi_R) = N[1 + 2v_1 \cos(\phi - \Psi_R) + 2v_2 \cos(2\phi - 2\Psi_R) + \dots]$$

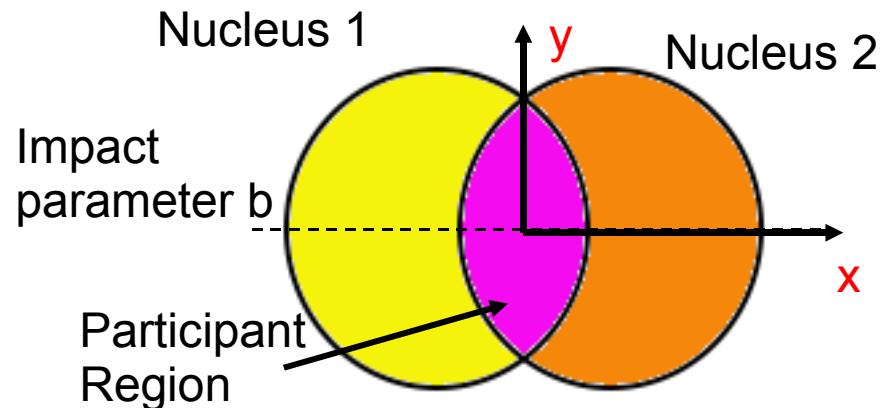
Standard eccentricity scaling



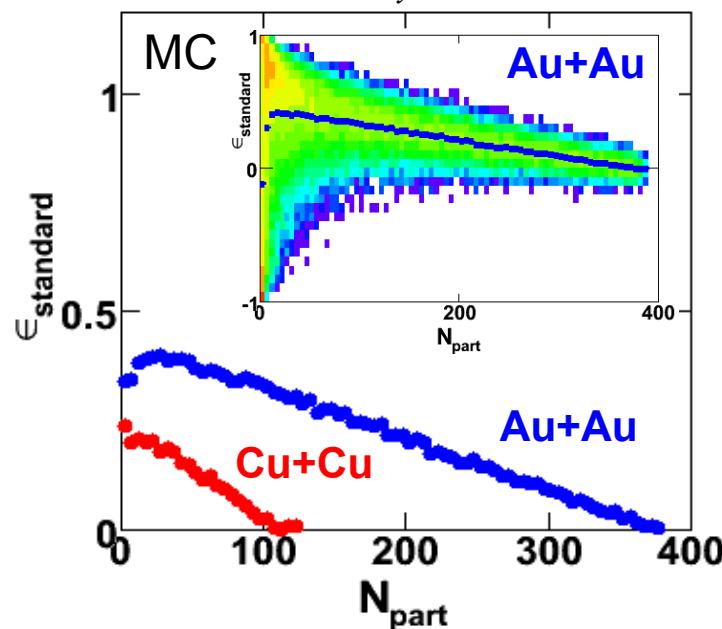
STAR, PRC 66 034904 (2002)
Voloshin, Poskanzer, PLB 474 27 (2000)
Heiselberg, Levy, PRC 59 2716, (1999)

Standard eccentricity calculation

Standard Eccentricity

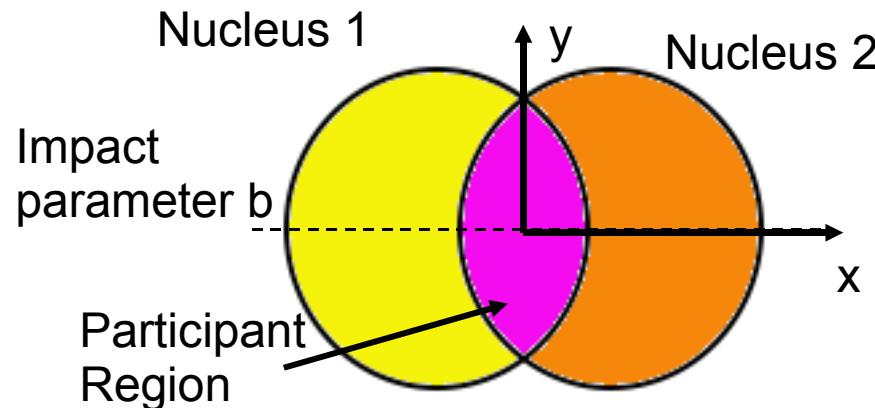


$$\epsilon_{std} = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2}$$

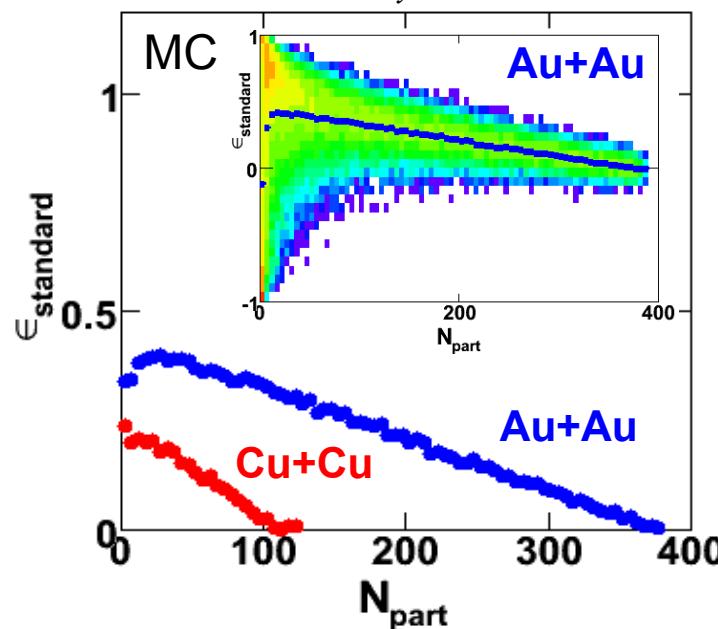


Participant eccentricity calculation

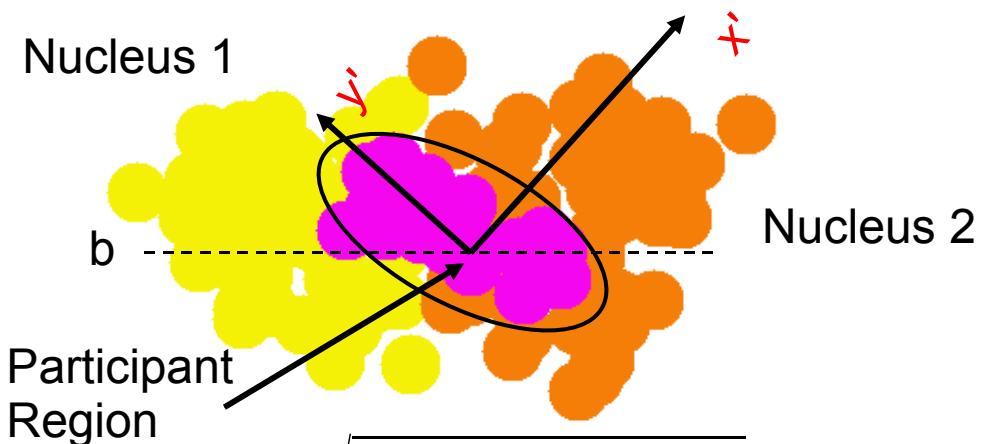
Standard Eccentricity



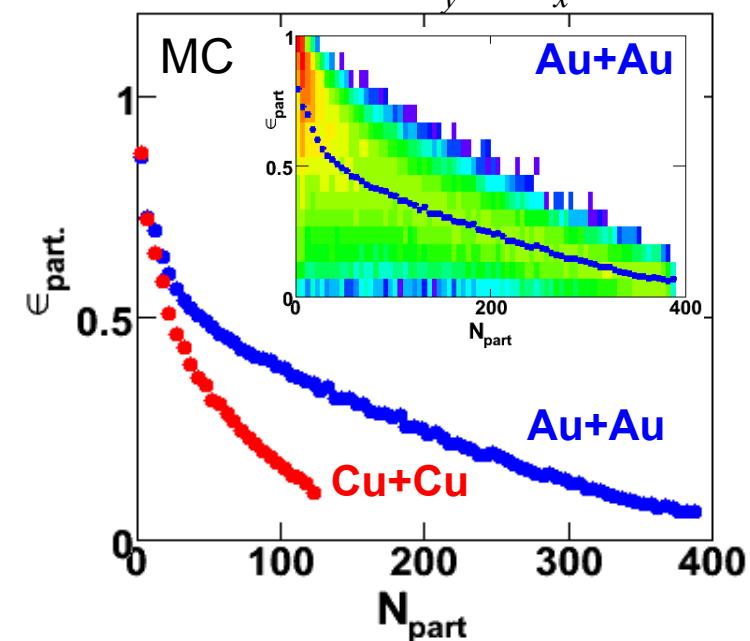
$$\epsilon_{std} = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2}$$



Participant Eccentricity

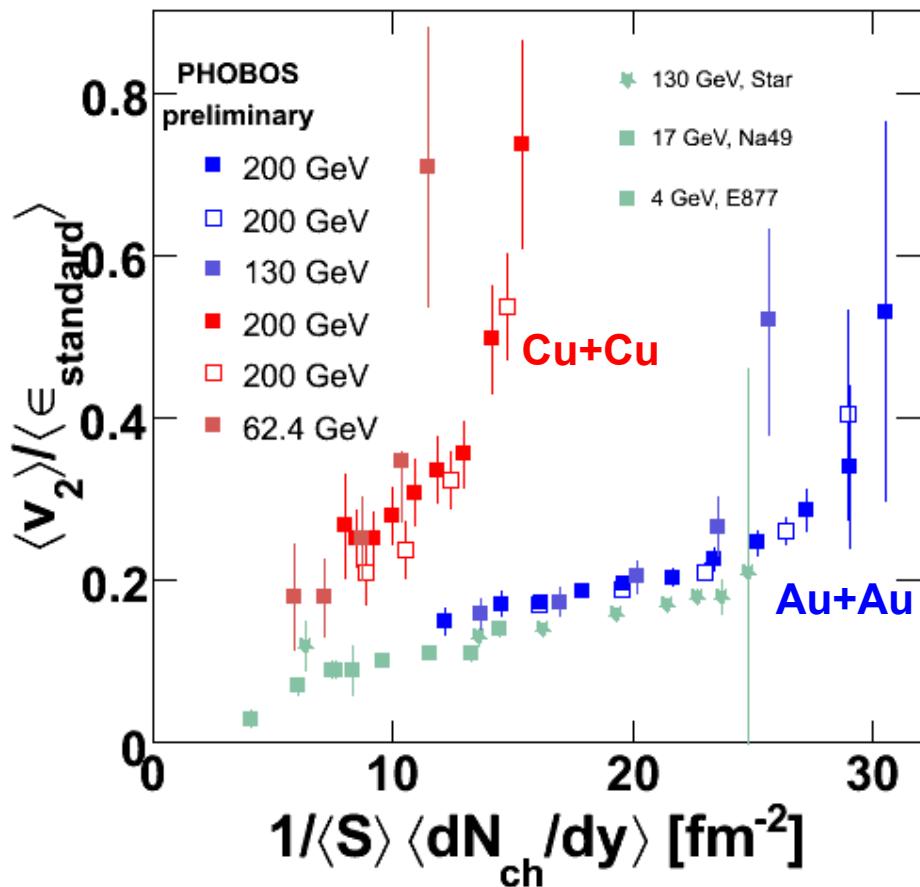


$$\epsilon_{part} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 - 4\sigma_{xy}^2}}{\sigma_y^2 + \sigma_x^2}$$

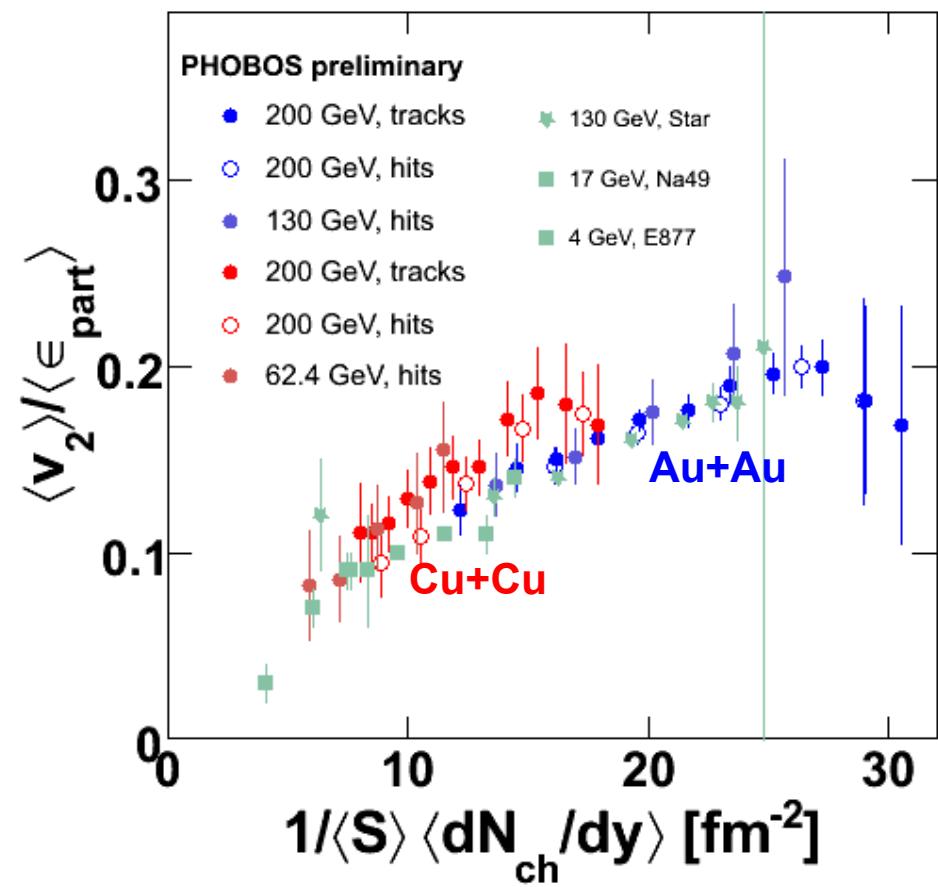


Participant eccentricity scaling

Standard Eccentricity



Participant Eccentricity



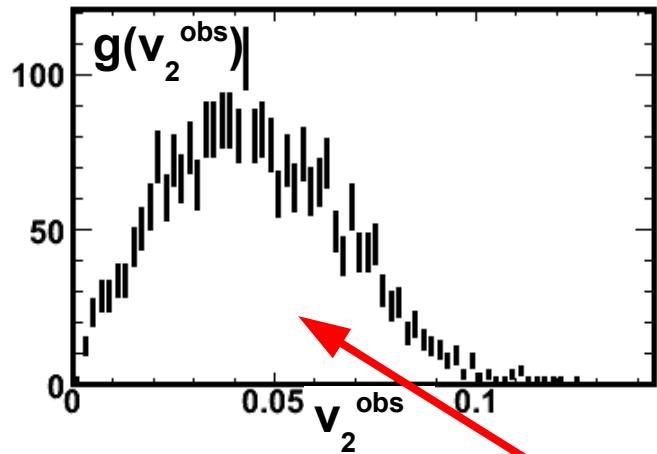
STAR, PRC 66 034904 (2002)
 Voloshin, Poskanzer, PLB 474 27 (2000)
 Heiselberg, Levy, PRC 59 2716, (1999)

6) Event-by-event elliptic fluctuations

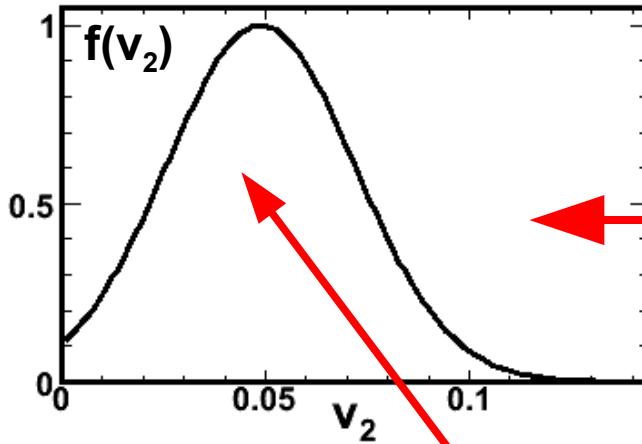
- From eccentricity fluctuations
 - To E-by-E fluctuations of the elliptic flow

Event-by-event elliptic flow fluctuations

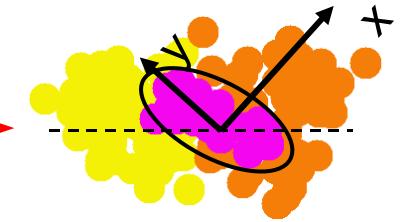
Observed v_2 distribution



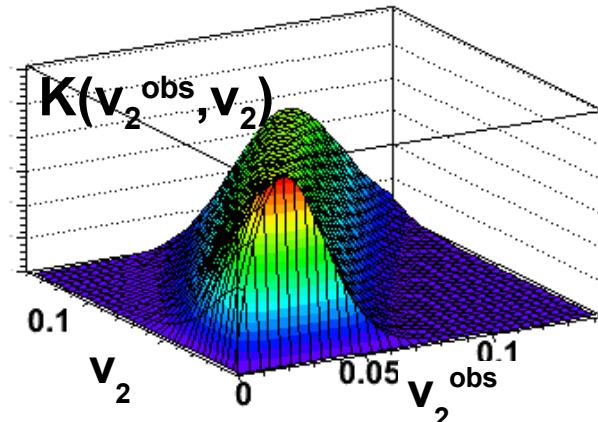
True v_2 distribution



Participant eccentricity

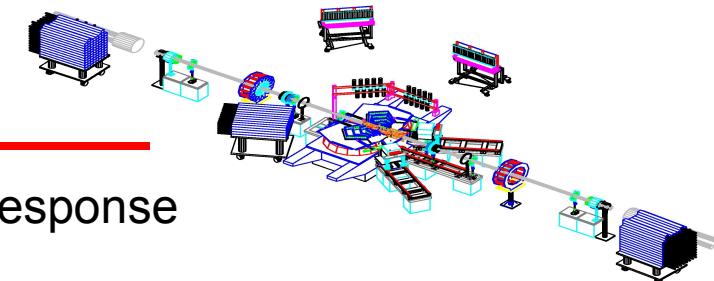


$$g(v_2^{obs}) = \int_0^\infty K(v_2^{obs}, v_2) f(v_2) dv_2$$



See Burak Alver's talk tomorrow

Detector response

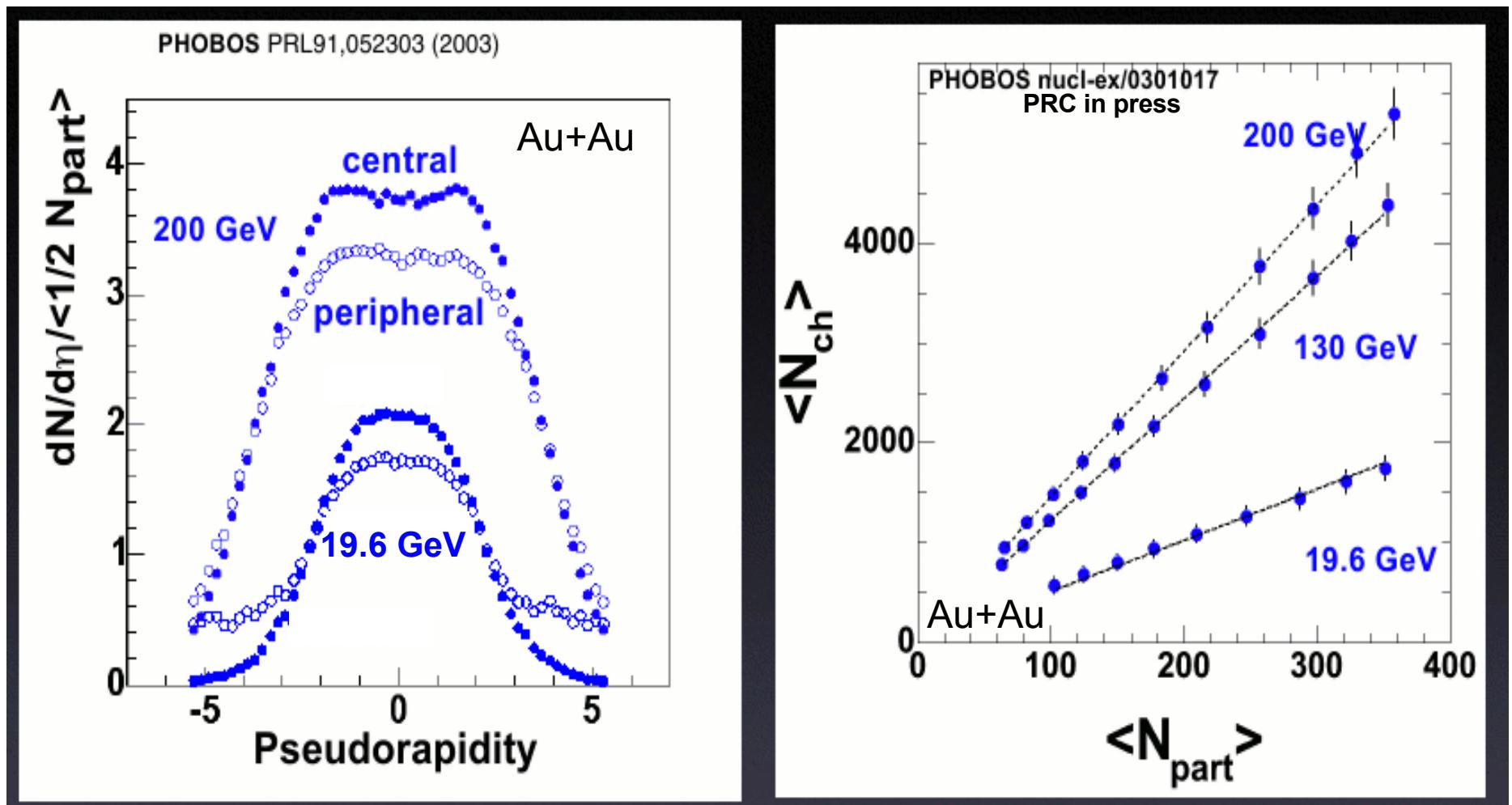


Summary and Perspectives

- Unusual event search
 - To the level of $\approx 10^{-4}$ (potentially lower) all events are “the same”
 - Refine this upper limit
- Forward-Backward multiplicity correlations
 - Connection of multiplicity fluctuations and hadron clusters
 - Interesting centrality dependence
- Two-particle angular correlation (see Wei Li's talk, 07/07/2006)
 - Comprehensive study of angular correlations in pp, dA and AA systems
- Eccentricity fluctuations
 - Participant vs standard eccentricity
 - Elliptic flow in small system connected to initial geometry fluctuations
- Elliptic flow fluctuations (see Burak Alver's talk, 07/09/2006)

Backup

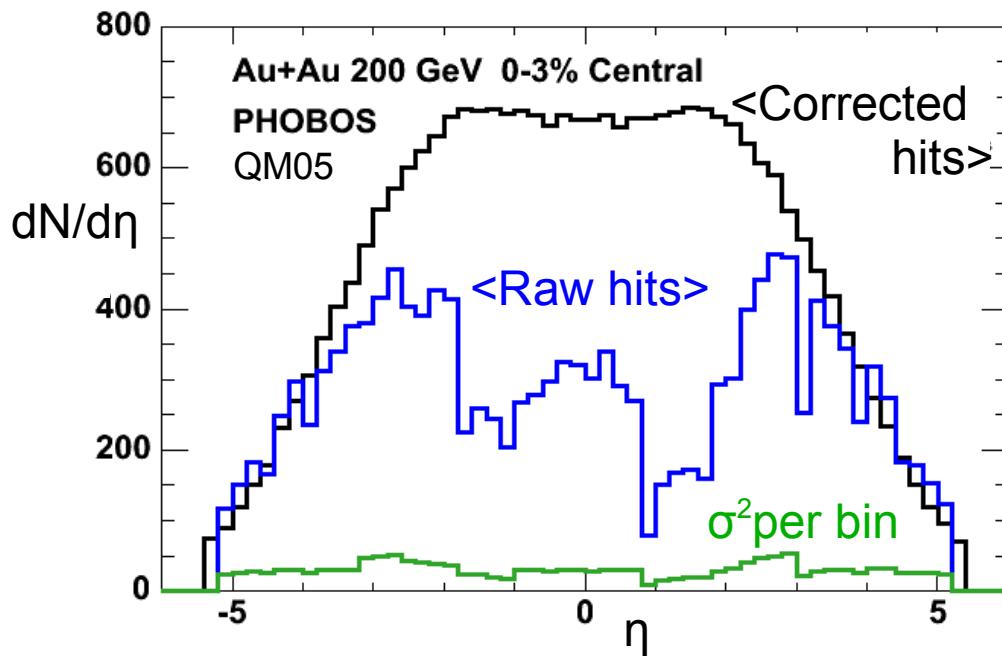
Global properties of $dN/d\eta$ -distributions



- Centrality dependence of $dN/d\eta$ **shape**
- N_{part} scaling of integrated (4π) **multiplicity**

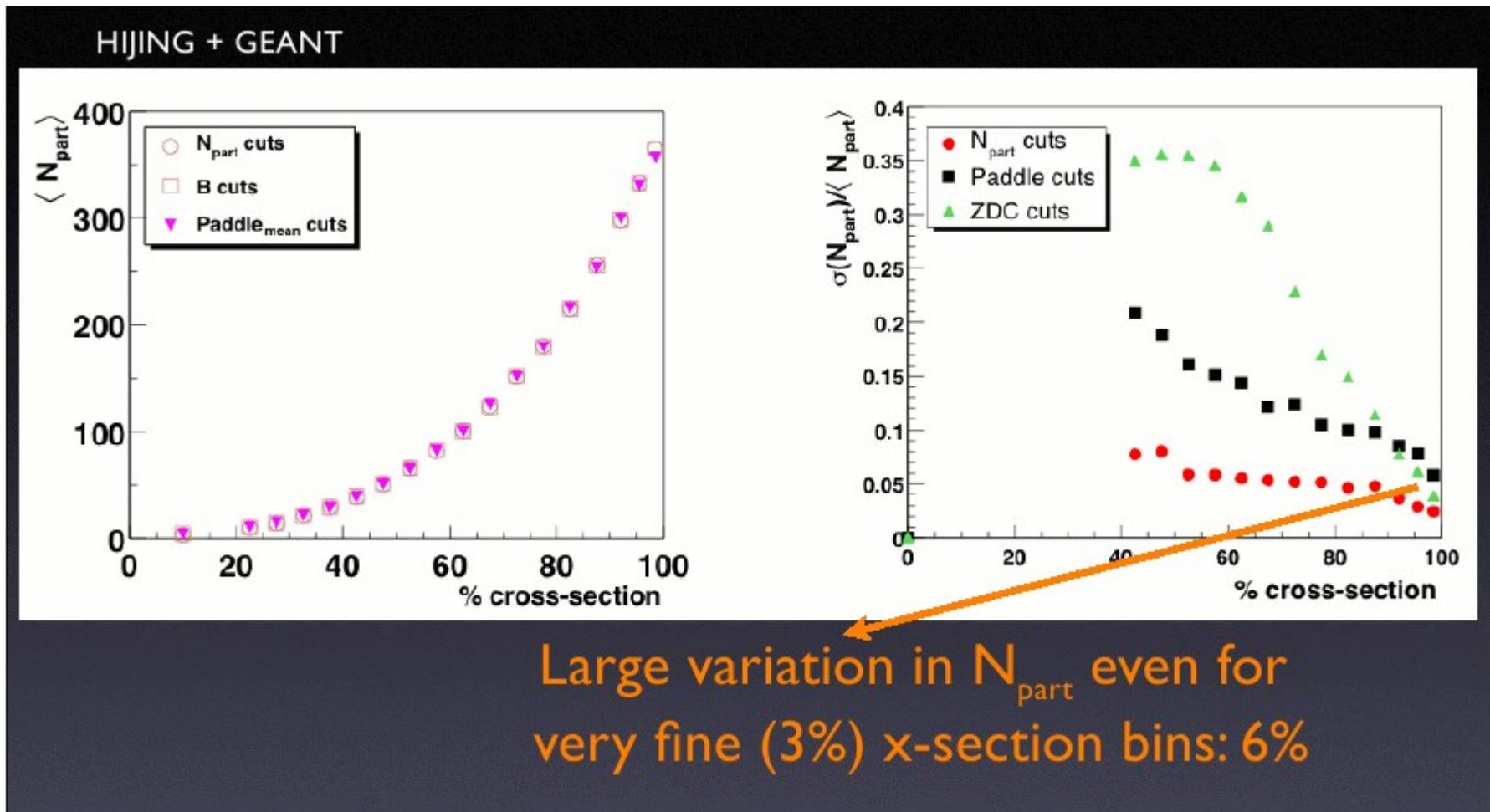
Beyond average $dN/d\eta$ -distributions

- Quantify event-by-event variation of large scale structure
 - Are there events with very large multiplicity?
 - Does the $dN/d\eta$ shape vary from event to event?

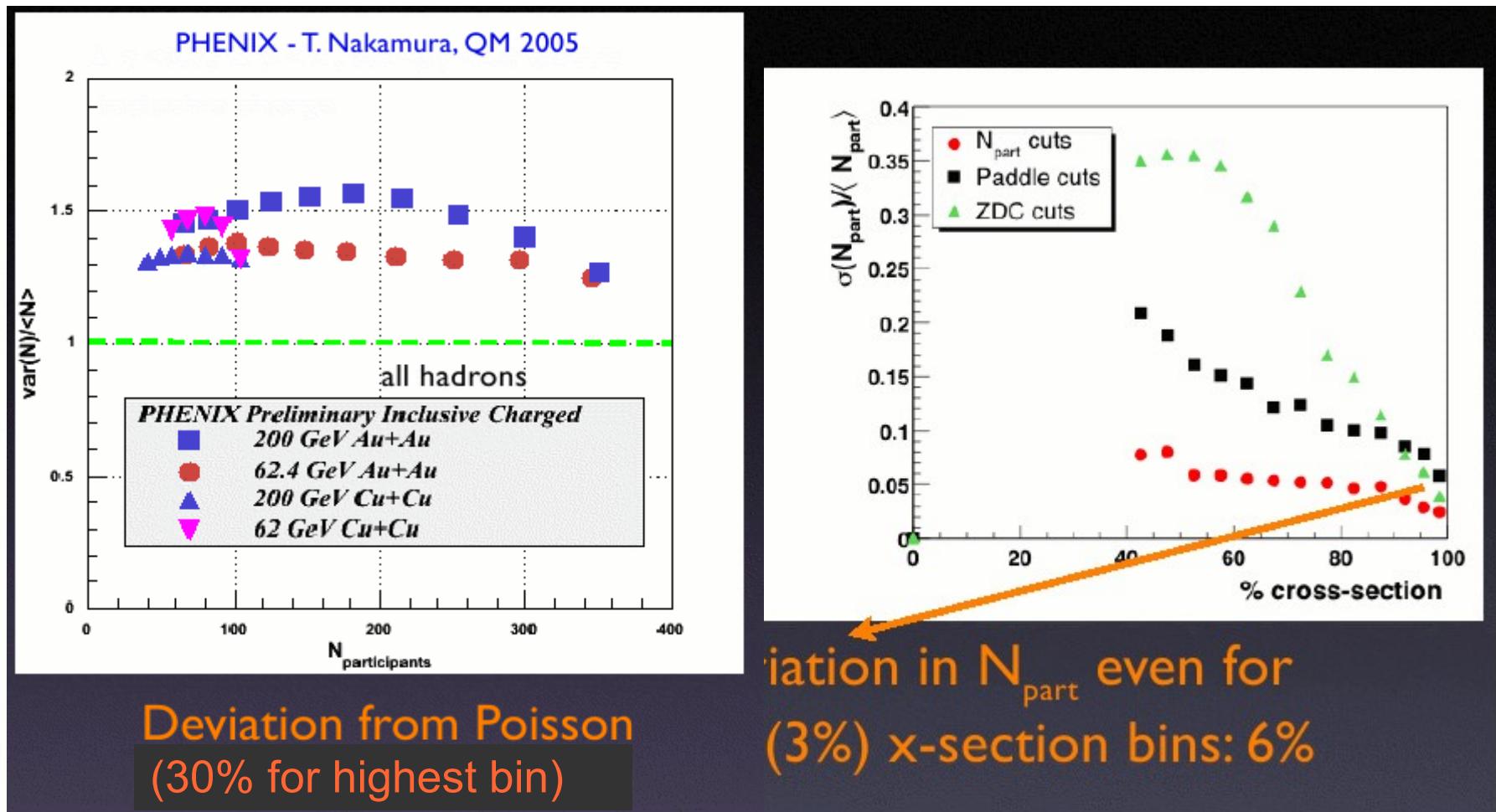


- Multiplicity fluctuations
 - Integral of raw $dN/d\eta$
- Shape fluctuations
 - χ^2 of single event vs raw (average) $dN/d\eta$

Multiplicity vs. participant fluctuations



Multiplicity vs. participant fluctuations



To do: Conclusion

Extracting number of particles per bin

- Octagon silicon sensors
 - Number of hits, N_{hit}
 - Sum of angle-corrected dE for charged particles, $E = \sum dE$

- Poissonian ansatz

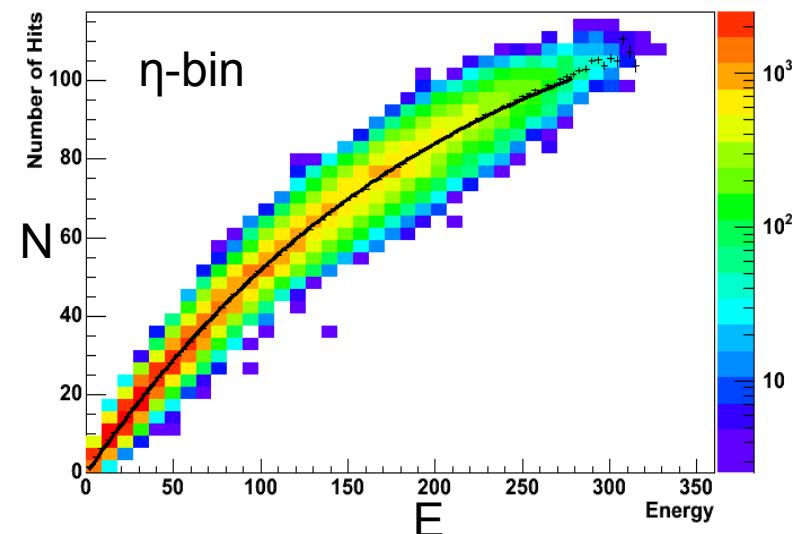
- $N_{\text{hit}} = N_{\text{max}}(1 - \exp(-E/E_{\text{max}}))$

- Average $\langle dE \rangle$ in η -bin given by $E_{\text{max}}/N_{\text{max}}$

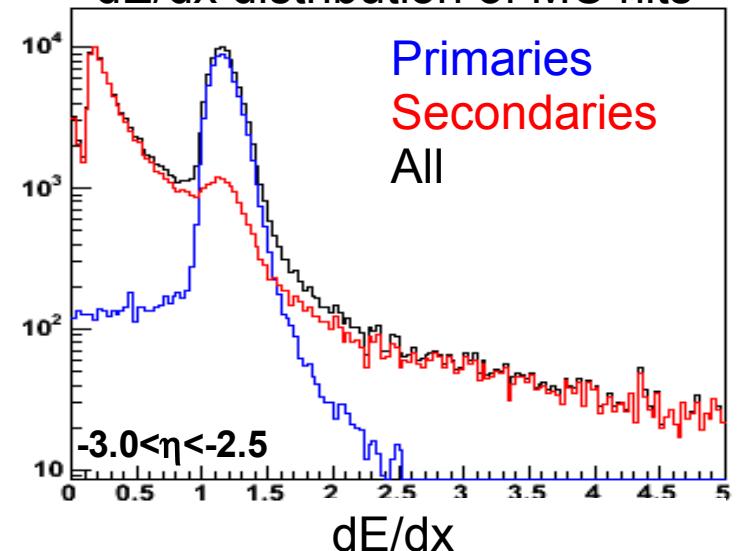
- Estimated multiplicity in η -bin

$$N = E/(E_{\text{max}}/N_{\text{max}})$$

- Use η -bin-dependent lower and upper dE/dx cuts on hits to suppress contribution from secondaries

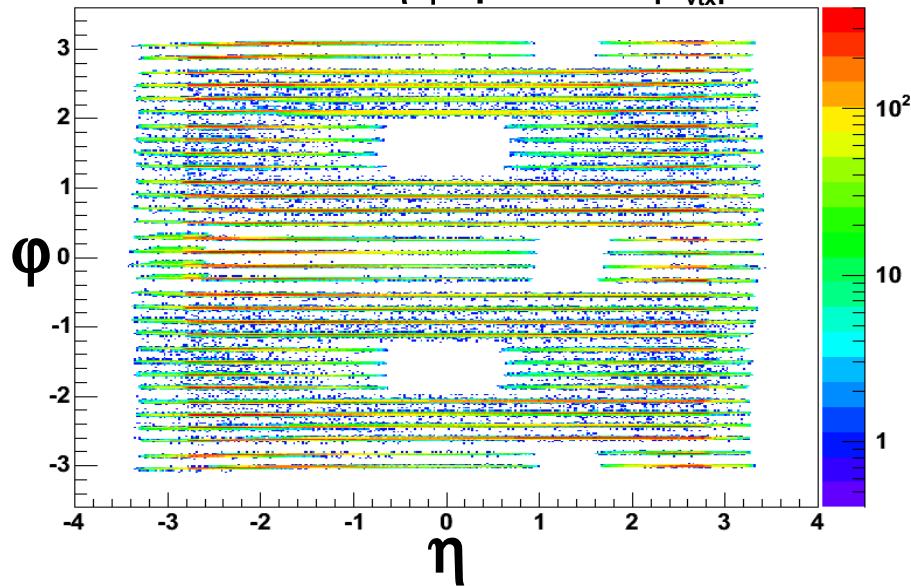


dE/dx distribution of MC hits



Acceptance correction

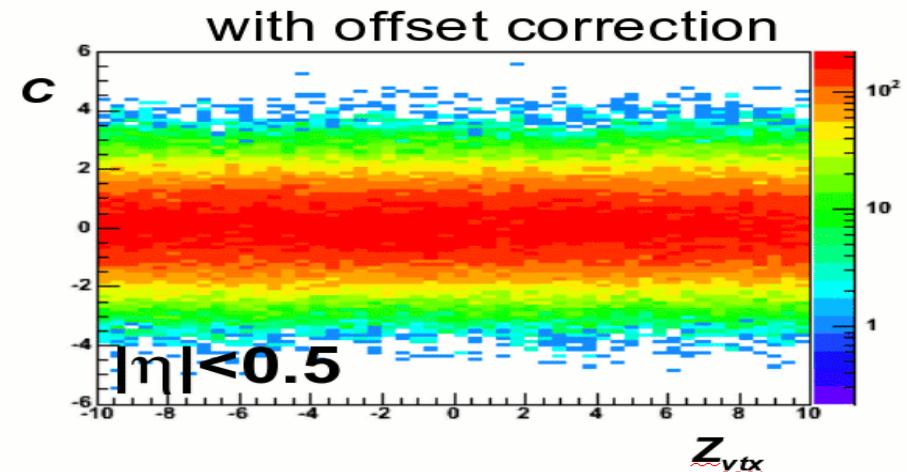
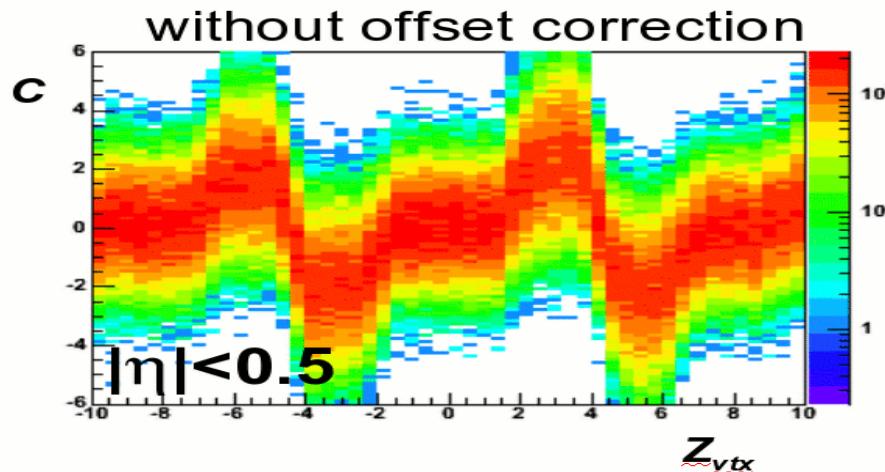
Hit distribution in η - ϕ space with $|Z_{\text{vtx}}|<10\text{cm}$



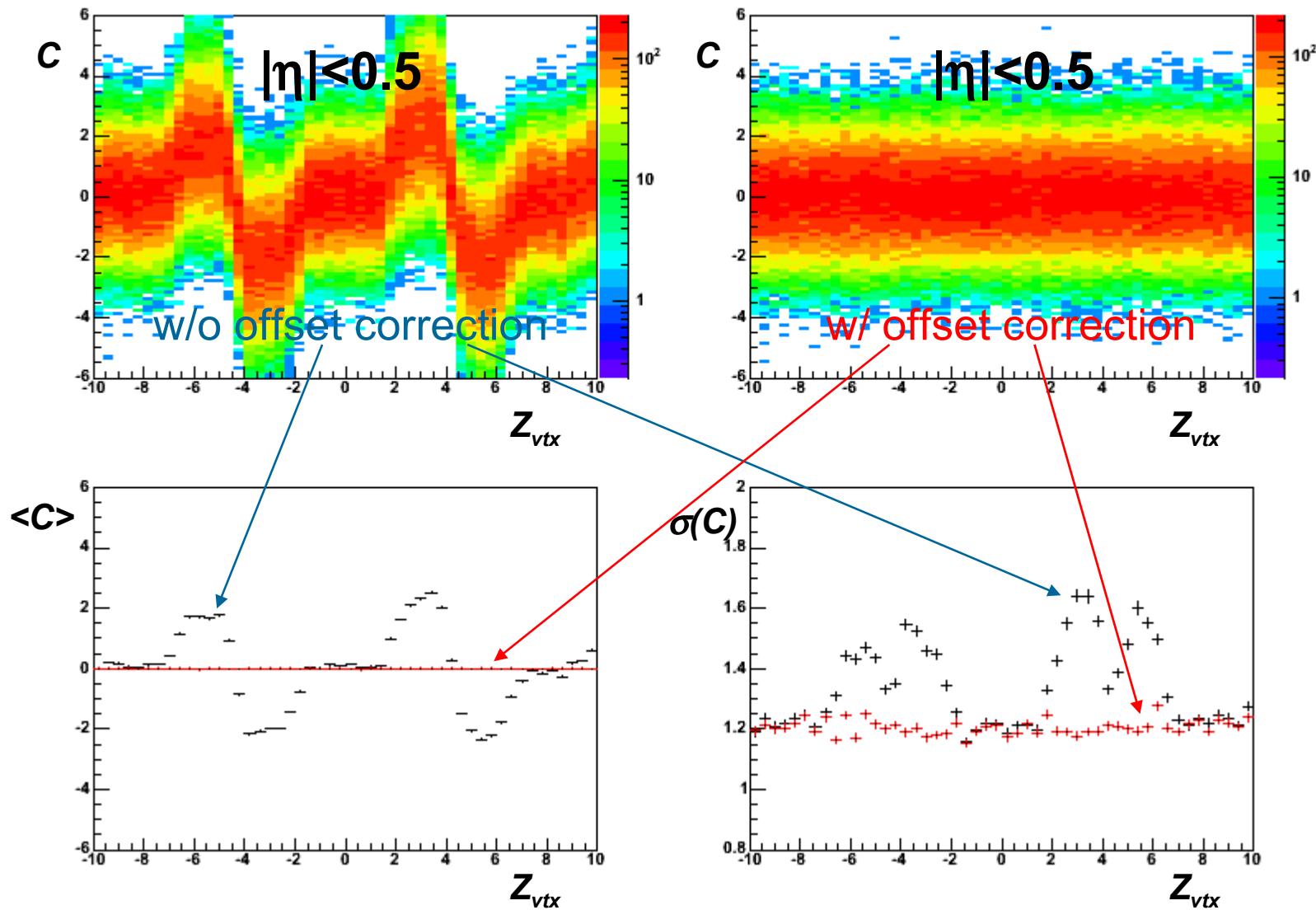
- Calculate average C per η , vertex and centrality bin

$$\Delta C = \frac{\langle N_1 - N_2 \rangle}{\sqrt{N_1 + N_2}}$$

- Subtract it event-by-event from C (according to simulations this leaves fluctuations unaffected)

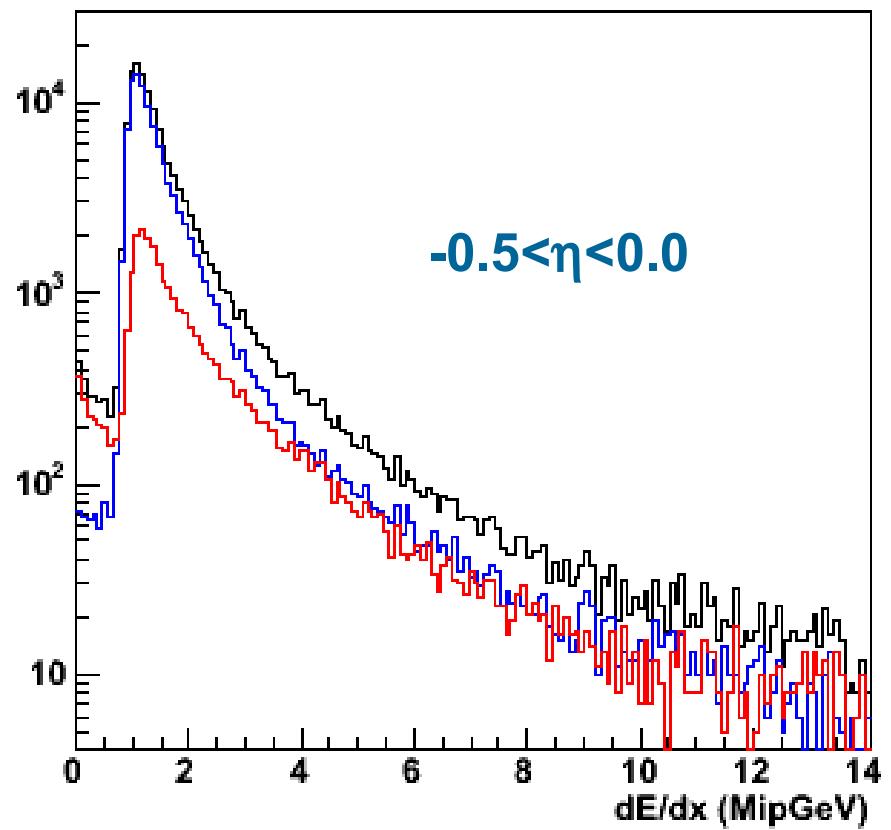
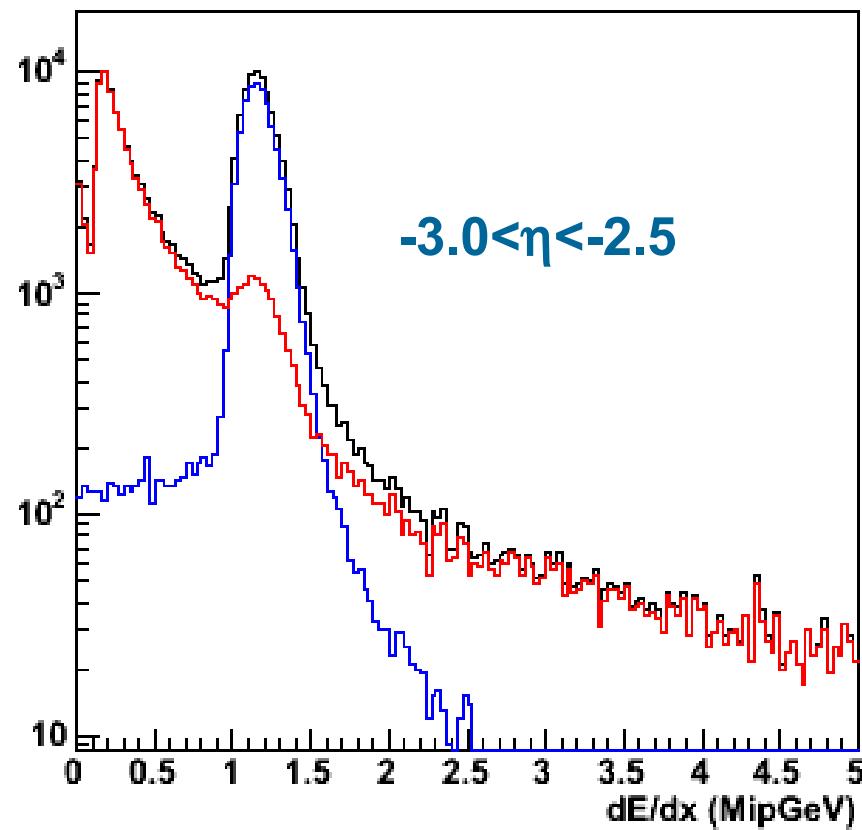


F/B: Acceptance correction

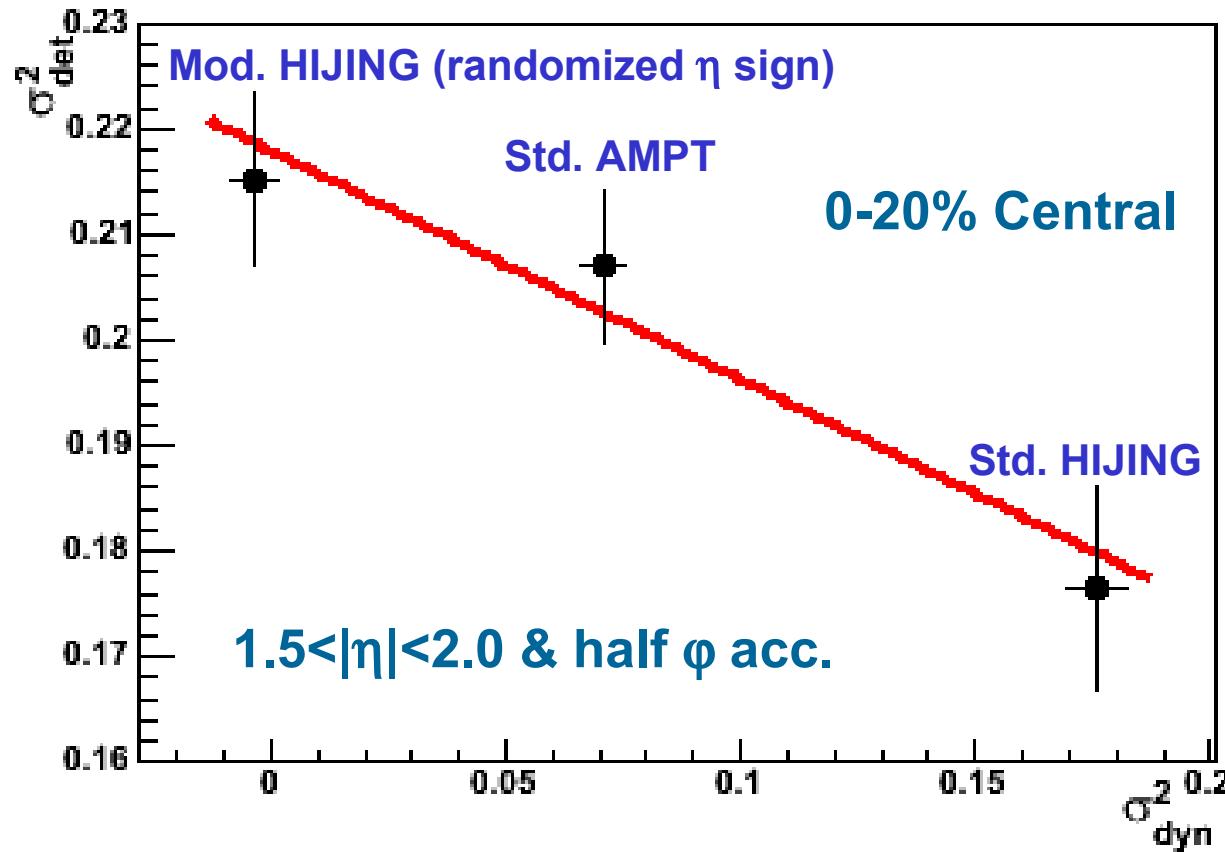


F/B: dE/dx distributions of MC hits

Black: Primaries + Secondaries, Red: Secondaries, Blue: Primaries



F/B: 1st order detector effects



Charge fluctuation

Studies by Jeon, et al

nucl-th/0503085

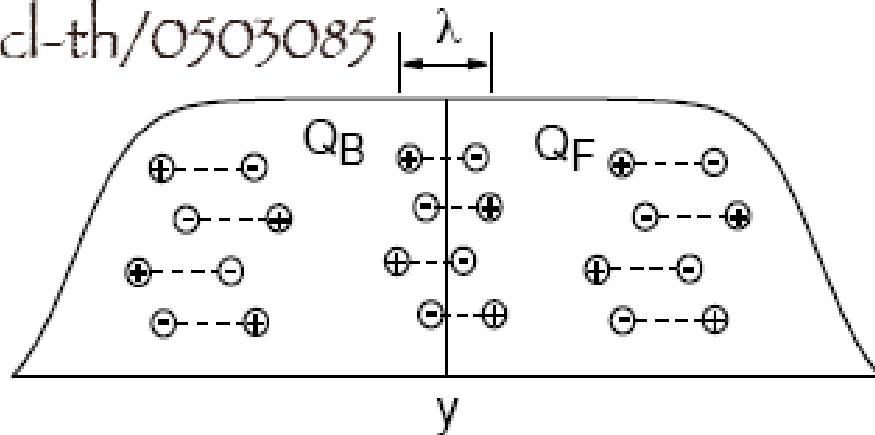
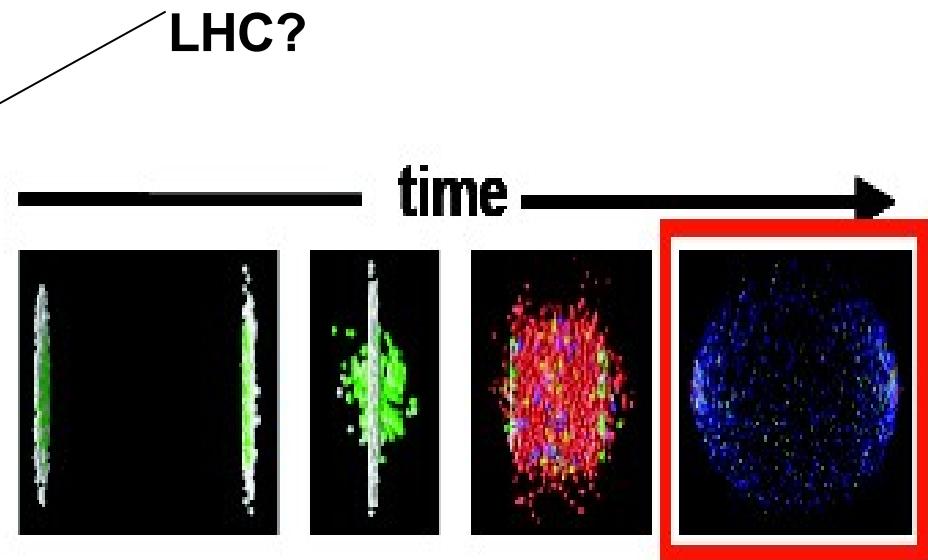
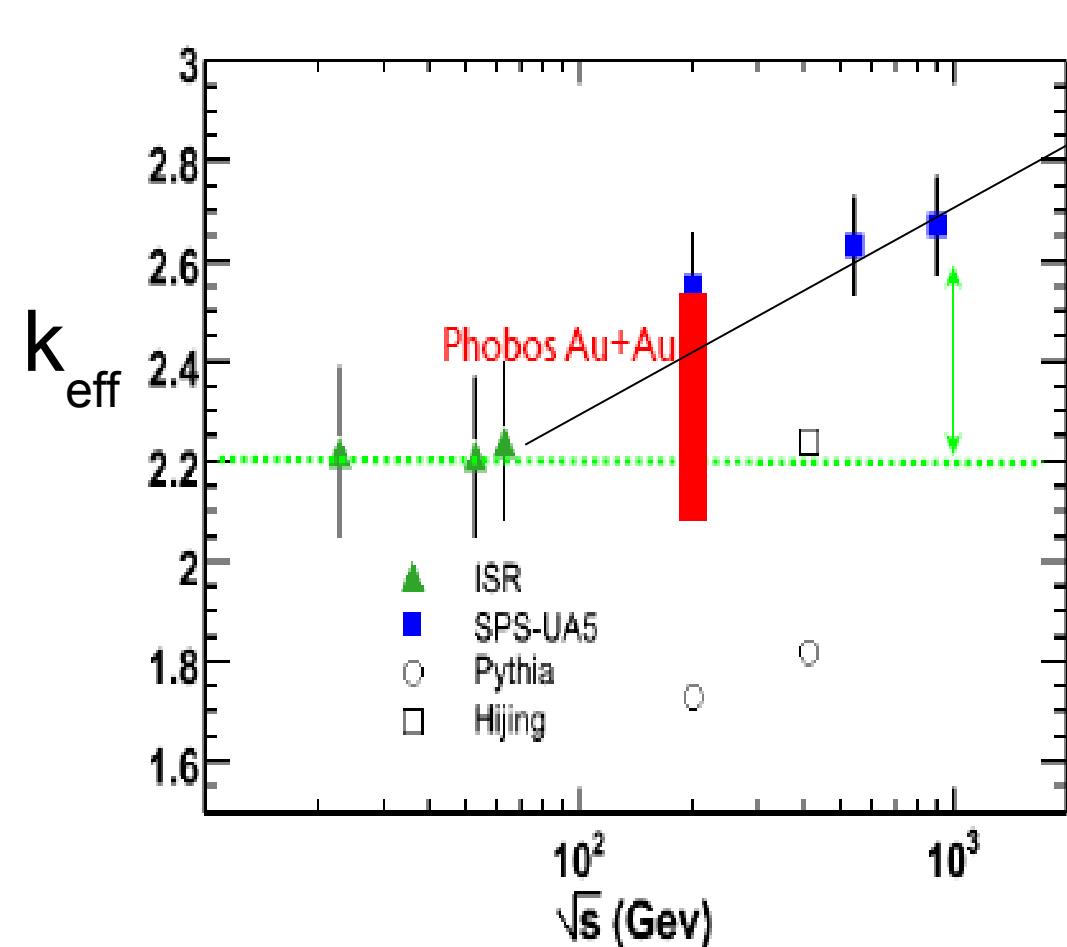


FIG. 1: A schematic illustration of the charge transfer fluctuations in the rapidity space. Only the pairs within $\lambda/2$ of y can contribute to the charge transfer fluctuation $D_u(y)$. Here λ is the rapidity correlation length, or the rapidity distance of the decay particles from a single cluster. If λ is a function of y , then $D_u(y)$ also changes with y .

- Model predicts at central region, QGP will decrease the cluster size.
- F&B method is restricted by the overlapping of F and B region near mid-rapidity.
- PHOBOS angular correlation analysis can be a useful tool to test the model.

Clusters in pp and AA



Cluster in AA is very similar to pp:

- Effects of Hadronization?
- Have to understand centrality dependence in AA
- Energy dependence: mini-jets?

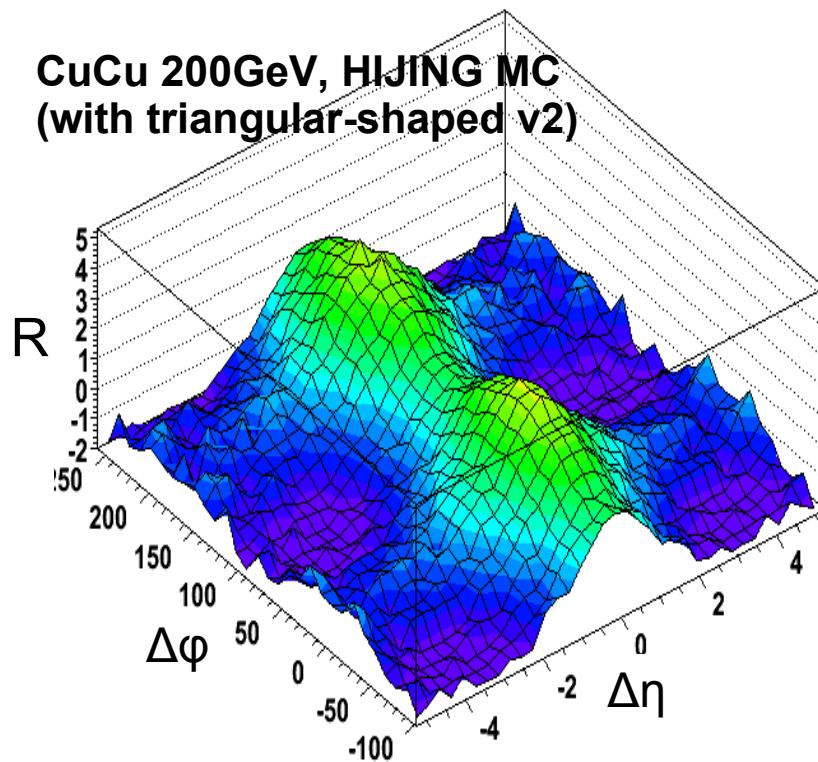
Nucl. Phys. B 86, 201 (1975)

Nucl. Phys. B 155, 269 (1979)

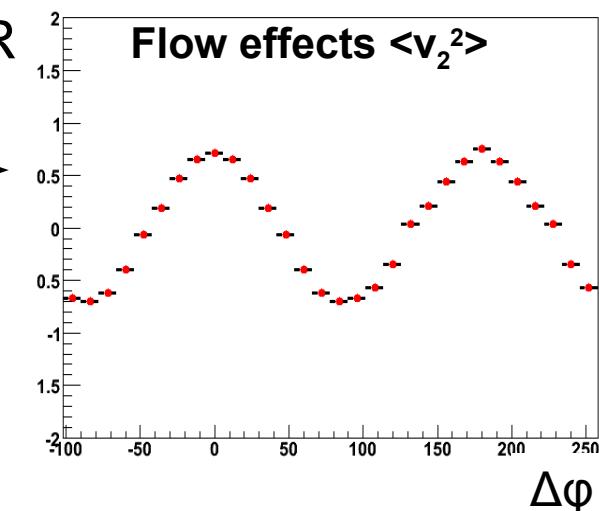
Z. Phys. - Particle and Fields C 37, 191 (1988)

Two-particle angular correlations in A+A

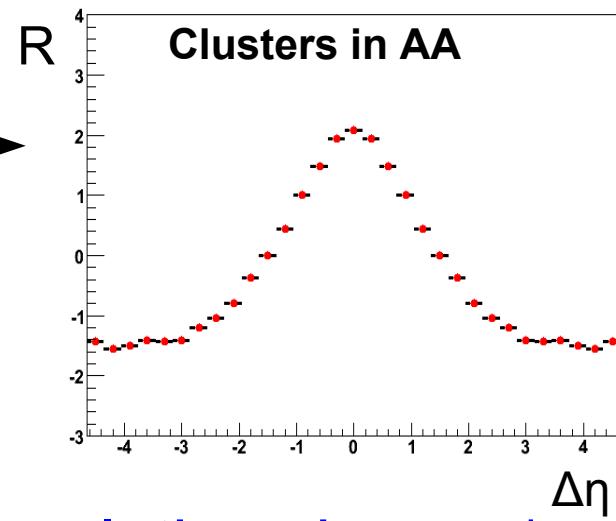
See Wei Li's talk



Projecting onto ϕ
from $0 < |\Delta\phi| < 180$

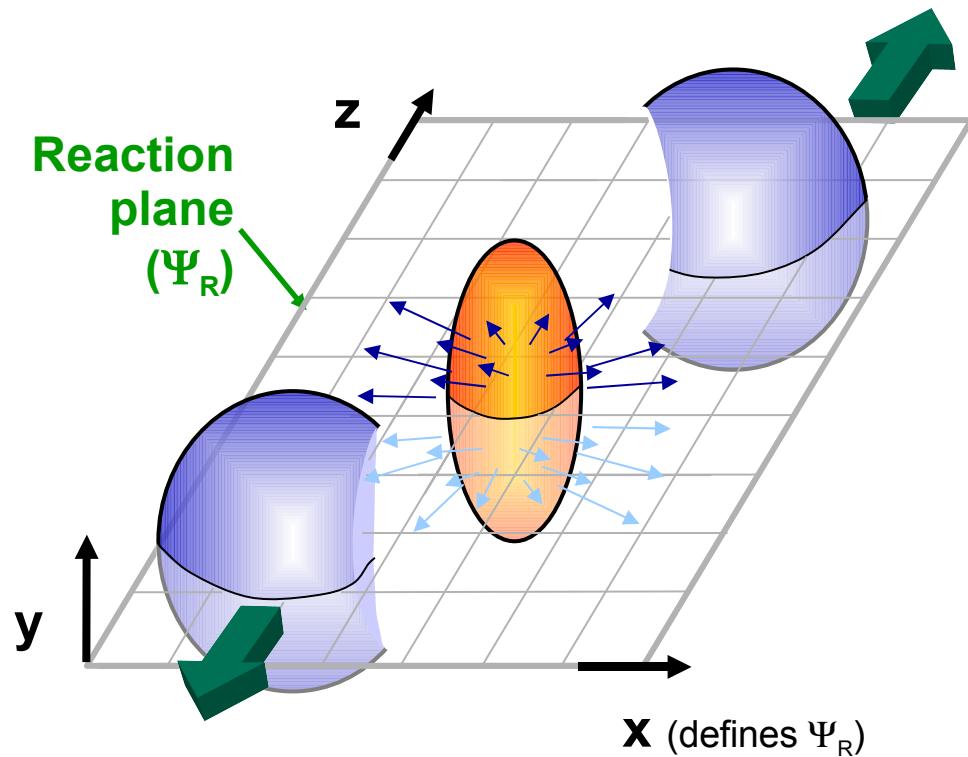


Projecting onto η
from $0 < |\Delta\eta| < 6$



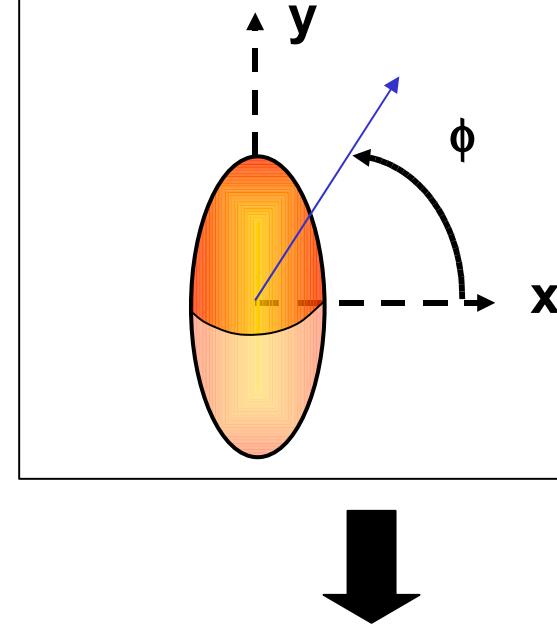
Comprehensive study of two-particle correlations in pp, dA and AA will help disentangle different effects in HI systems

Direct (v_1) and elliptic (v_2) flow

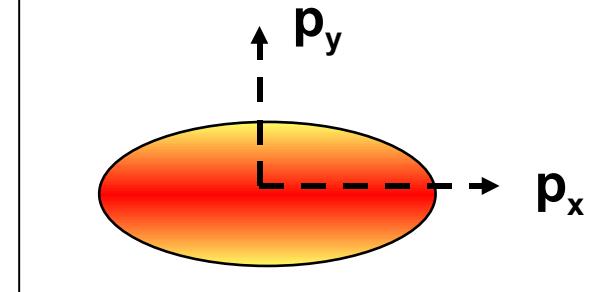


$$\frac{dN}{d(\phi - \Psi_R)} = N_0 (1 + 2v_1 \cos(\phi - \Psi_R) + 2v_2 \cos(2(\phi - \Psi_R)) + \dots)$$

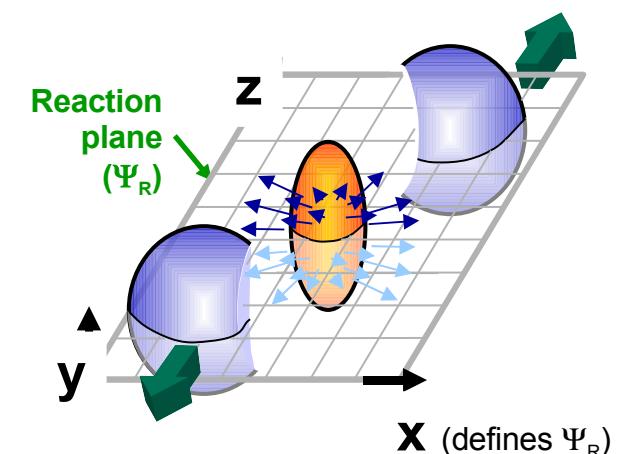
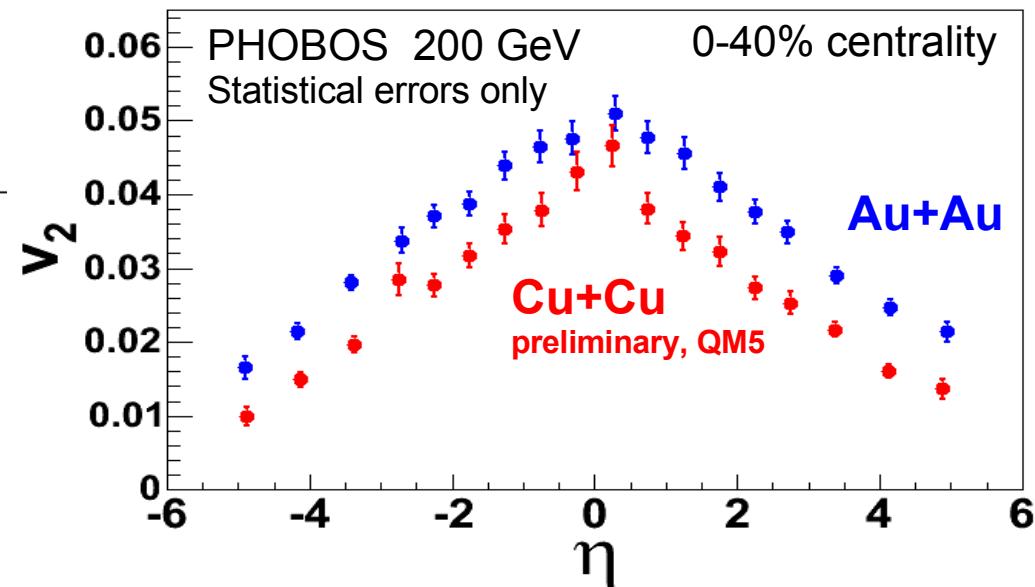
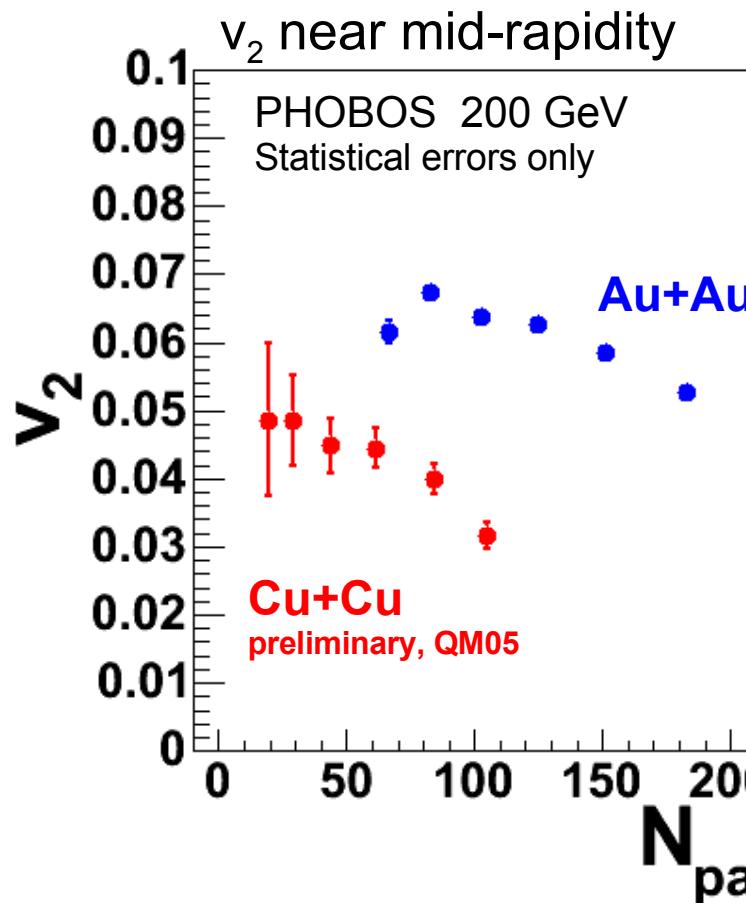
Initial spatial anisotropy



Final momentum anisotropy



Elliptic flow in Cu+Cu and Au+Au

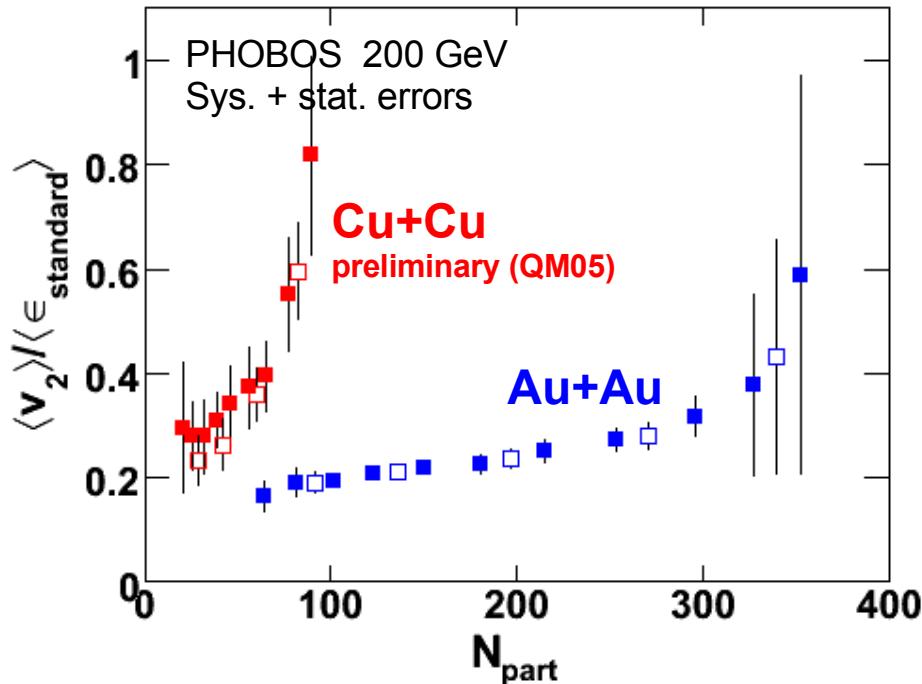


Au+Au: PRL 94, 122303 (2005)
Cu+Cu: prel. QM05, nucl-ex/0510042

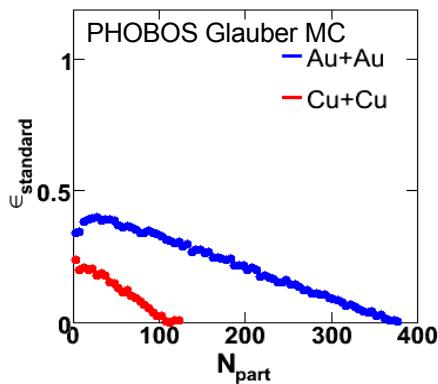
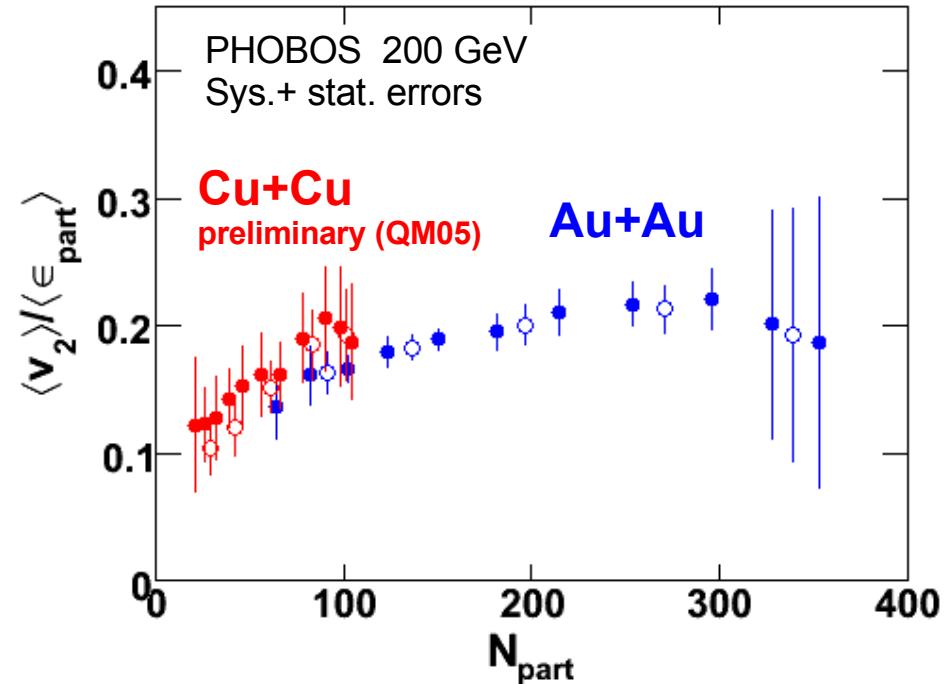
$$dN/d(\phi - \Psi_R) = N[1 + 2v_1 \cos(\phi - \Psi_R) + 2v_2 \cos(2\phi - 2\Psi_R) + \dots]$$

Scaled elliptic flow vs N_{part}

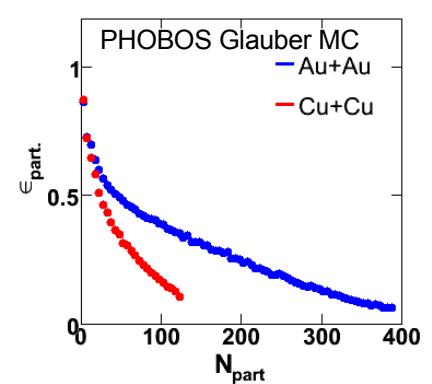
Standard Eccentricity



Participant Eccentricity

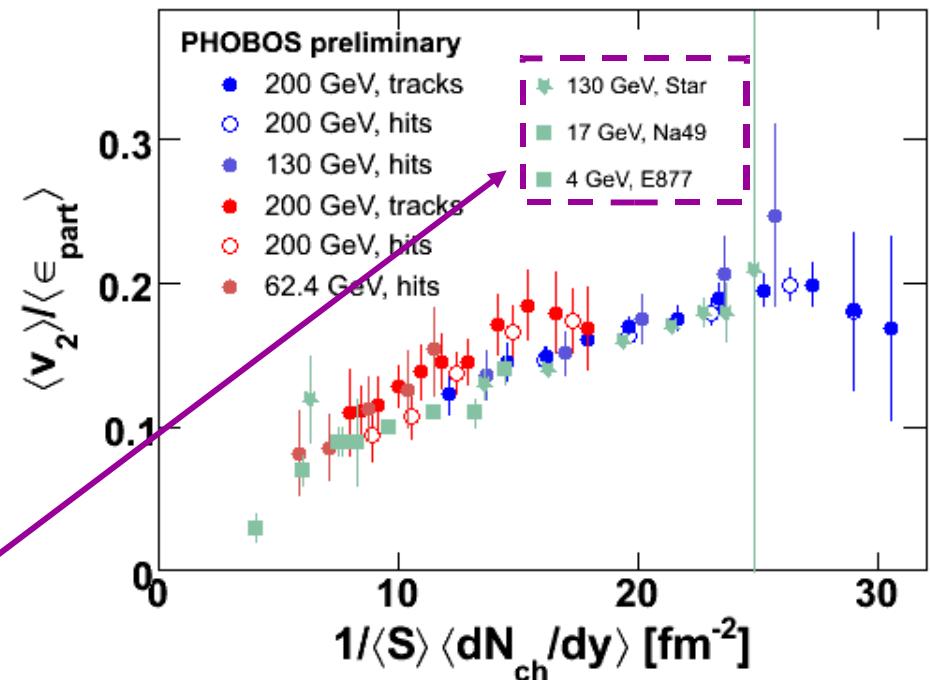


“Participant Eccentricity”
allows v_2 -scaling from
Cu+Cu to Au+Au



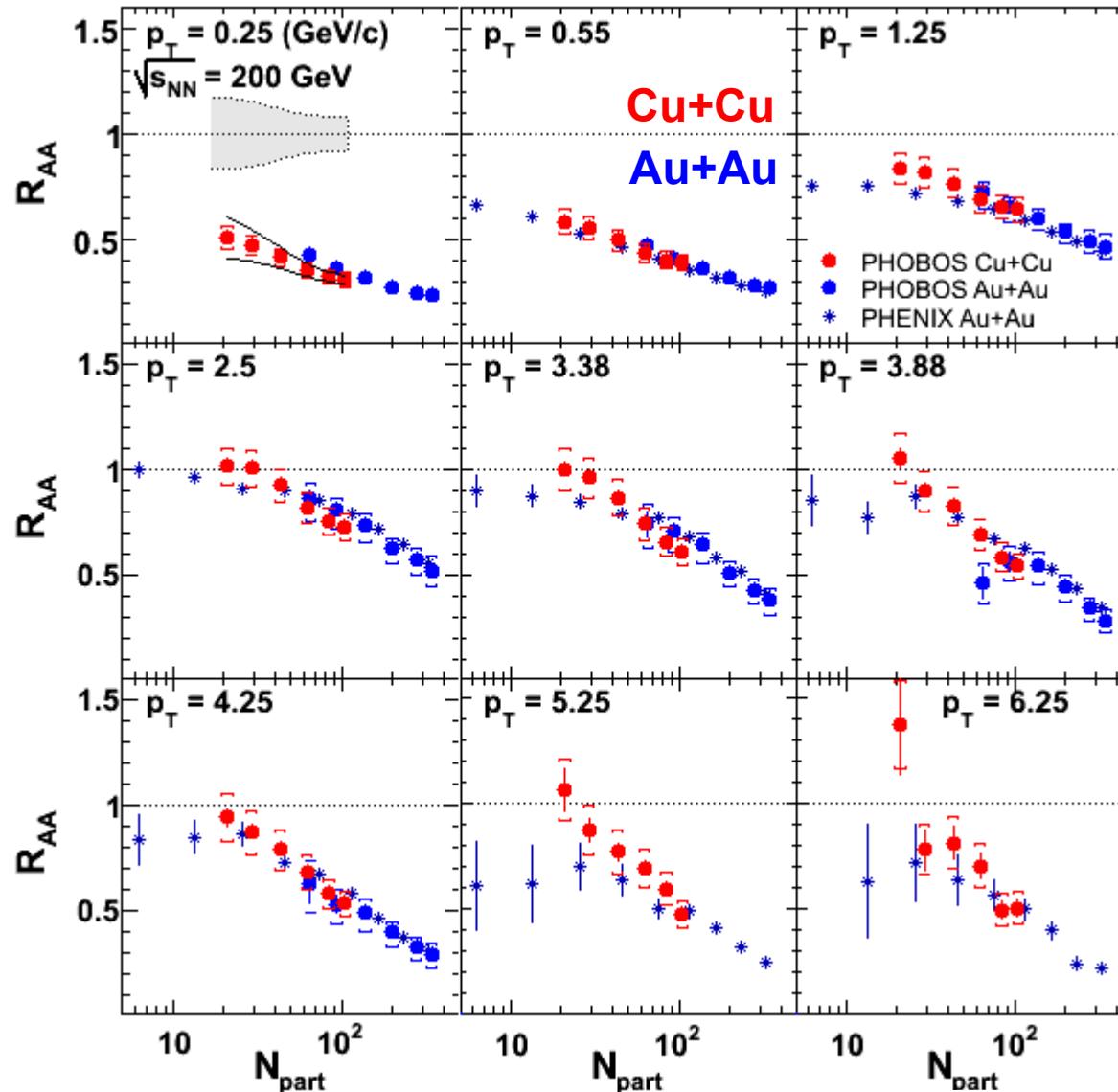
Low-density limit scaling (some details)

- **Caution:** we used ϵ_{part} for PHOBOS data. Important for Cu-Cu, less critical for Au-Au.
- Scale $v_2(\eta)$ to $\sim v_2(y)$ (10% lower)
- Scale $dN/d\eta$ to be $\sim dN/dy$ (15% higher)



Points for STAR, NA49 and E877 data taken from STAR Collaboration, Phys.Rev. C66 (2002) 034904 with no adjustments

Yields vs N_{part} at 200 GeV



$0.2 < \eta < 1.4$

System-size scaling observed!

Au+Au: PRL 94, 082304 (2005), PLB 578, 297 (2004)

Phenix: PLB 561, 82 (2003), PRC 69, 034910 (2004)

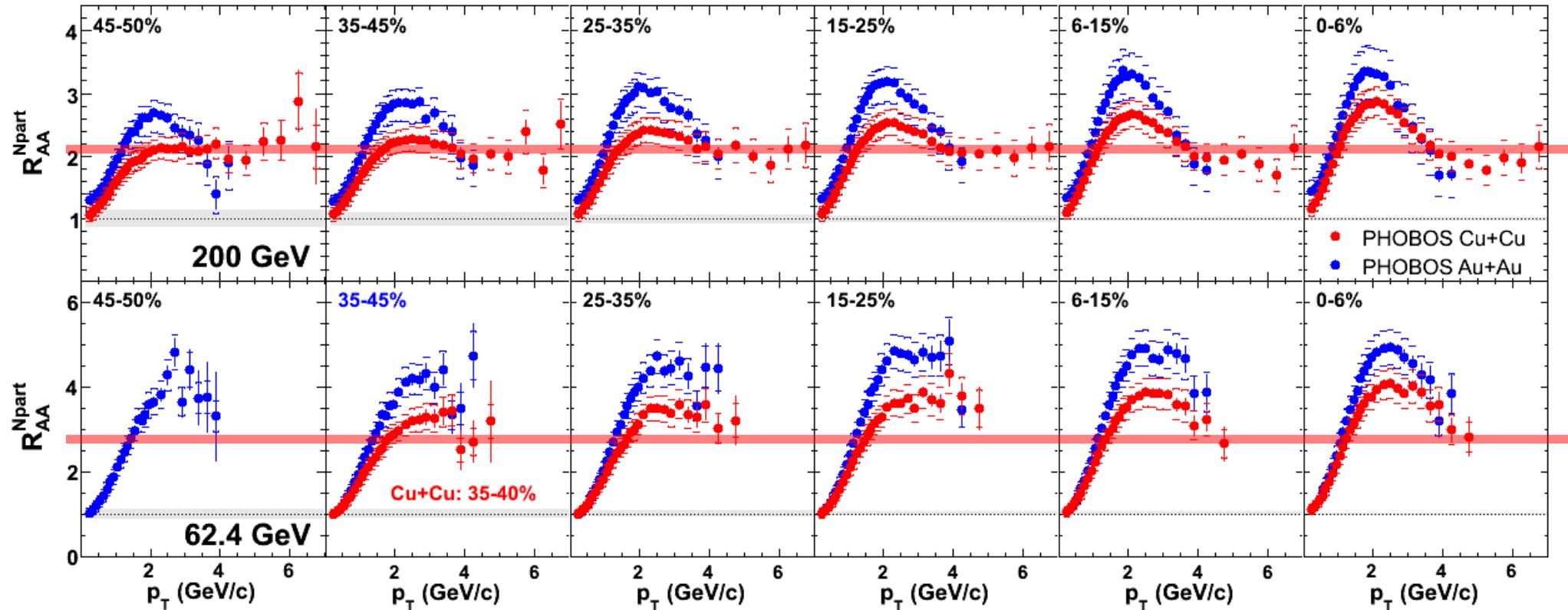
Cu+Cu: PRL 96, 212301 (2006)

p+p̄: UA1 -2.5 < η < 2.5 (acc. correction with PYTHIA)

$$R_{AA} = \frac{\sigma_{p\bar{p}}^{\text{inel}}}{\langle N_{\text{coll}} \rangle} \frac{d^2 N_{AA}/dp_T d\eta}{d^2 \sigma_{p\bar{p}}/dp_T d\eta}$$

$R_{AA}^{N_{part}}$ in Au+Au and Cu+Cu at 200 GeV

$0.2 < \eta < 1.4$



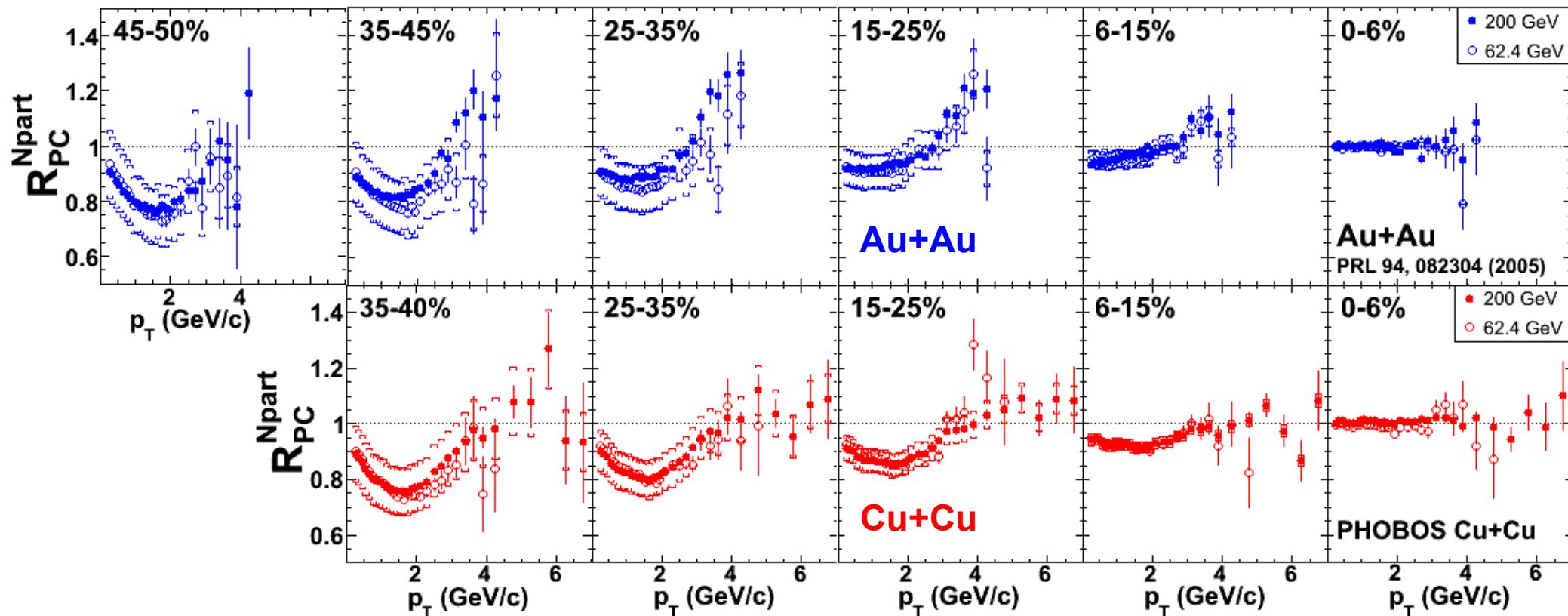
Yields normalized by N_{part} less centrality-dependent

Au+Au: PRL 94, 082304 (2005)
 Cu+Cu: PRL 96, 212301 (2006)

$$R_{AA}^{N_{part}} = \frac{\sigma_{pp}^{inel}}{\langle N_{part}/2 \rangle} \frac{d^2 N_{AA}/dp_T d\eta}{d^2 \sigma_{pp}/dp_T d\eta}$$

Factorization in bins of p_T

Normalized for central events



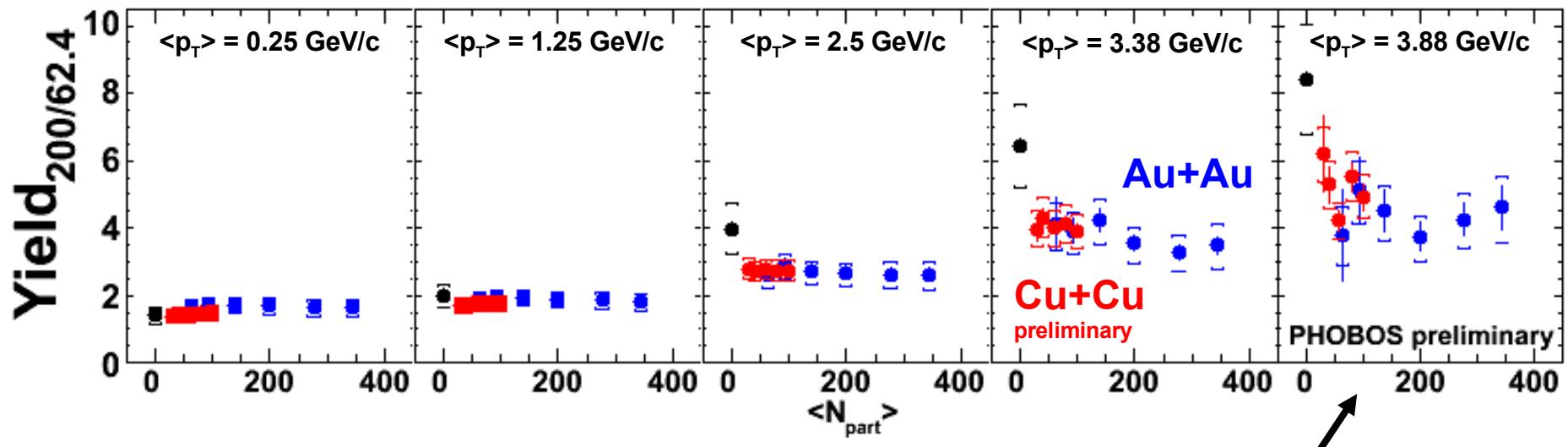
Same shape evolution from central
to peripheral at 200 GeV and 62 GeV

Au+Au: PRL 94, 082304 (2005)
Cu+Cu: PRL 96, 212301 (2006)

$$R_{PC}^{N_{part}} = \frac{\langle N_{part}^{0-6\%} \rangle}{\langle N_{part} \rangle} \frac{d^2 N_{AA}/dp_T d\eta}{d^2 N_{AA}^{0-6\%}/dp_T d\eta}$$

Factorization in bins of p_T (2)

Ratio of charged hadron yields in 200 GeV to 62 GeV

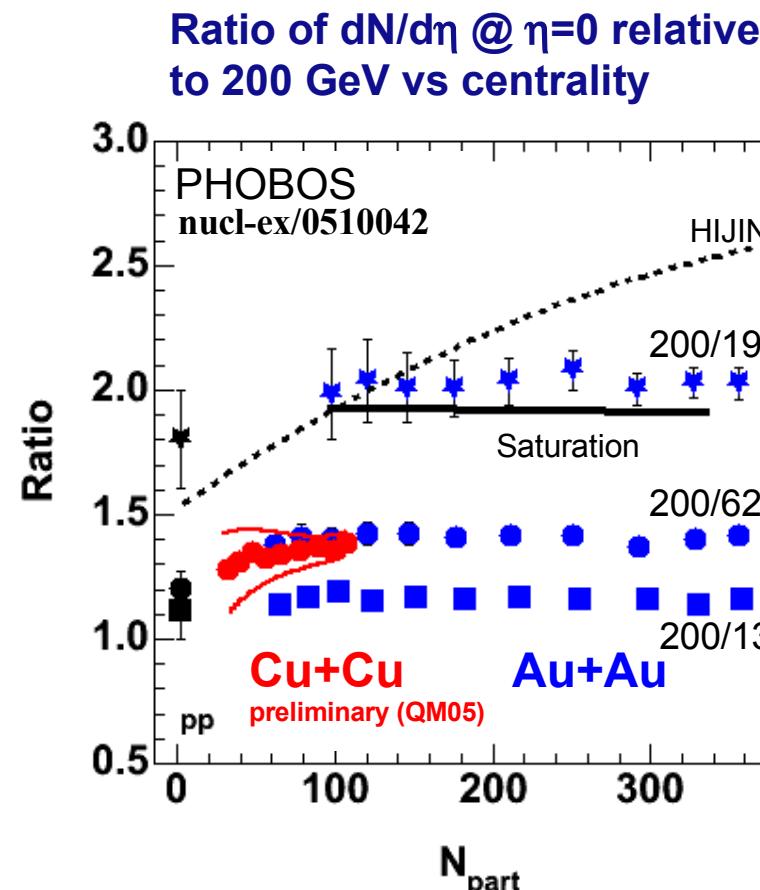
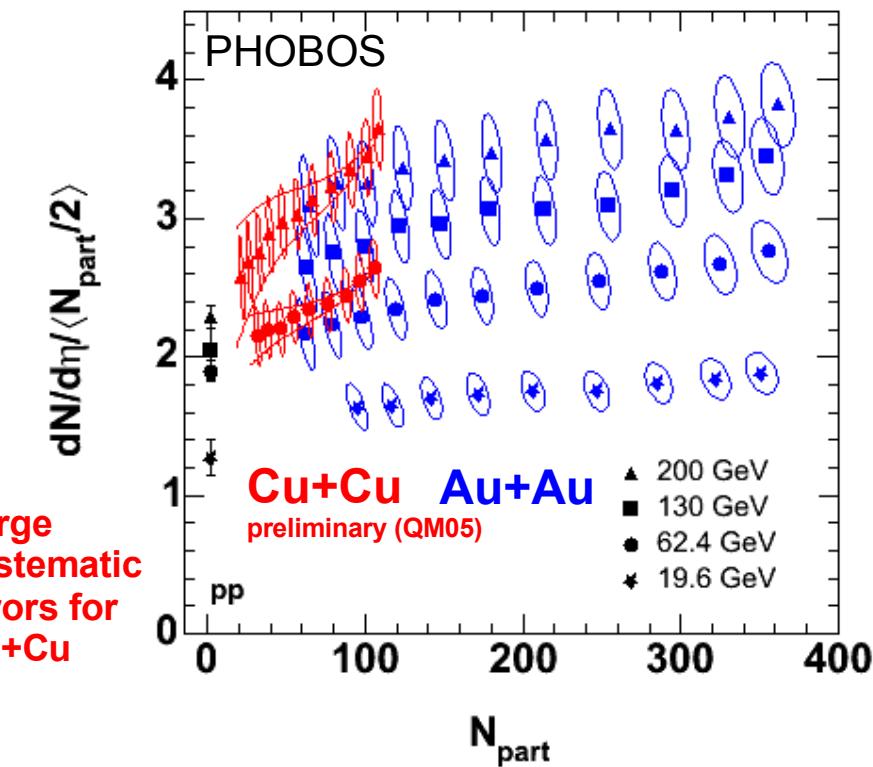


Energy/centrality factorization
up to $p_T \approx 4 \text{ GeV}/c$ for $N_{\text{part}} > 40$

Au+Au: PRL 94, 082304 (2005)

Cu+Cu: PRL 96, 212301 (2006)

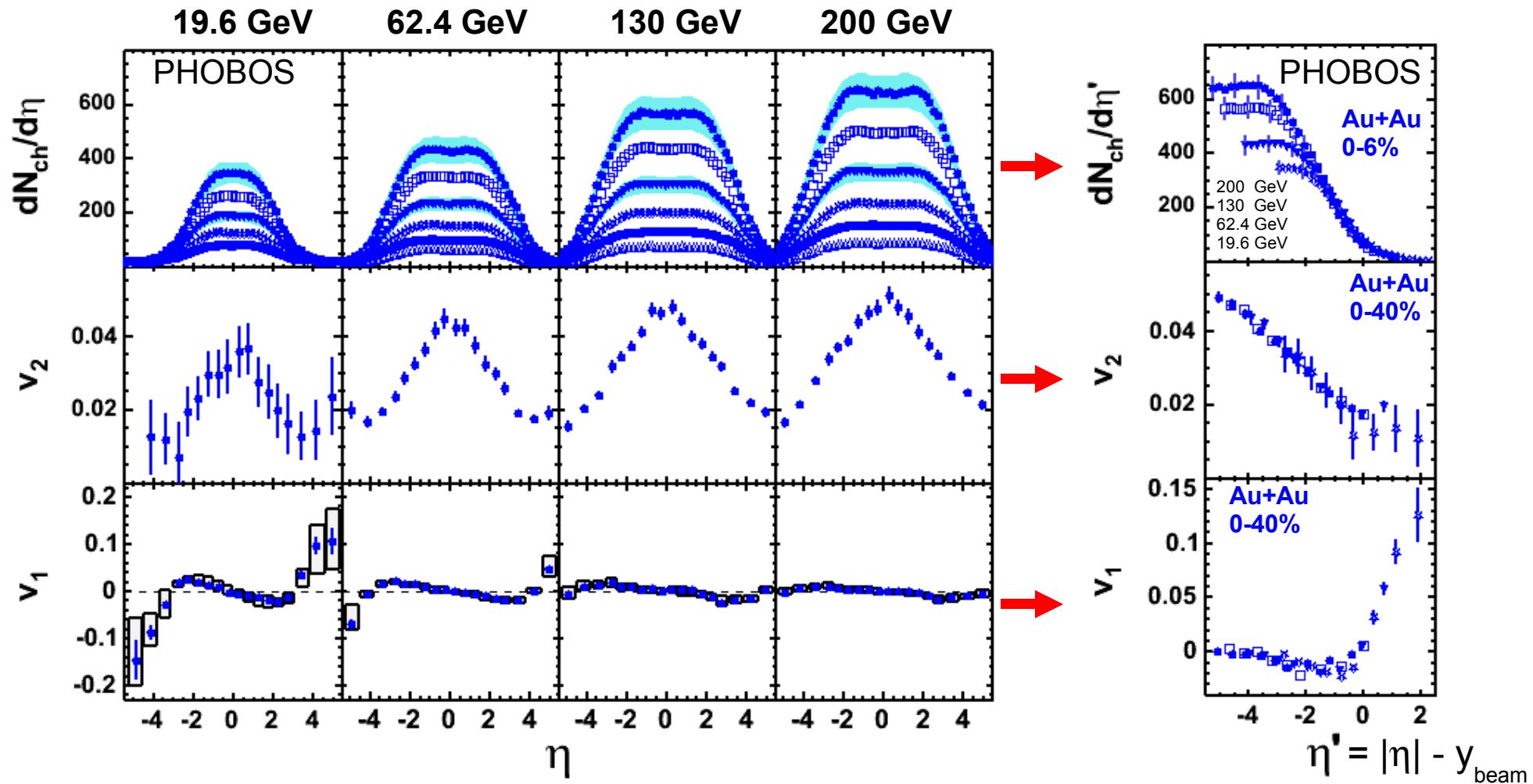
Factorization of energy and centrality



Factorization of energy and
centrality due to initial state effect?

Au+Au: Phys. Rev. C70, 021902(R) (2004)
62.4 GeV Au+Au: nucl-ex/0509034 (sub.to PRC)
Cu+Cu (preliminary): QM05, nucl-ex/0510042

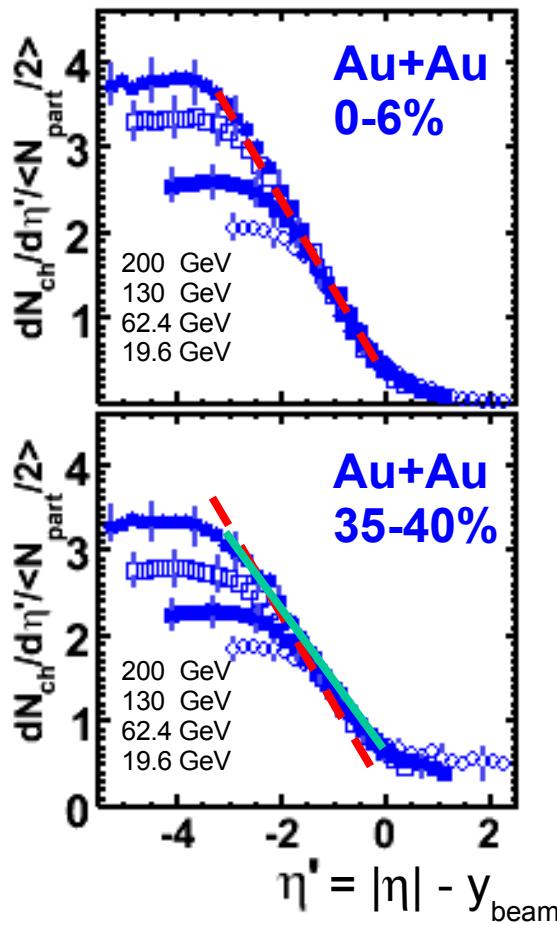
Limiting fragmentation (Au+Au)



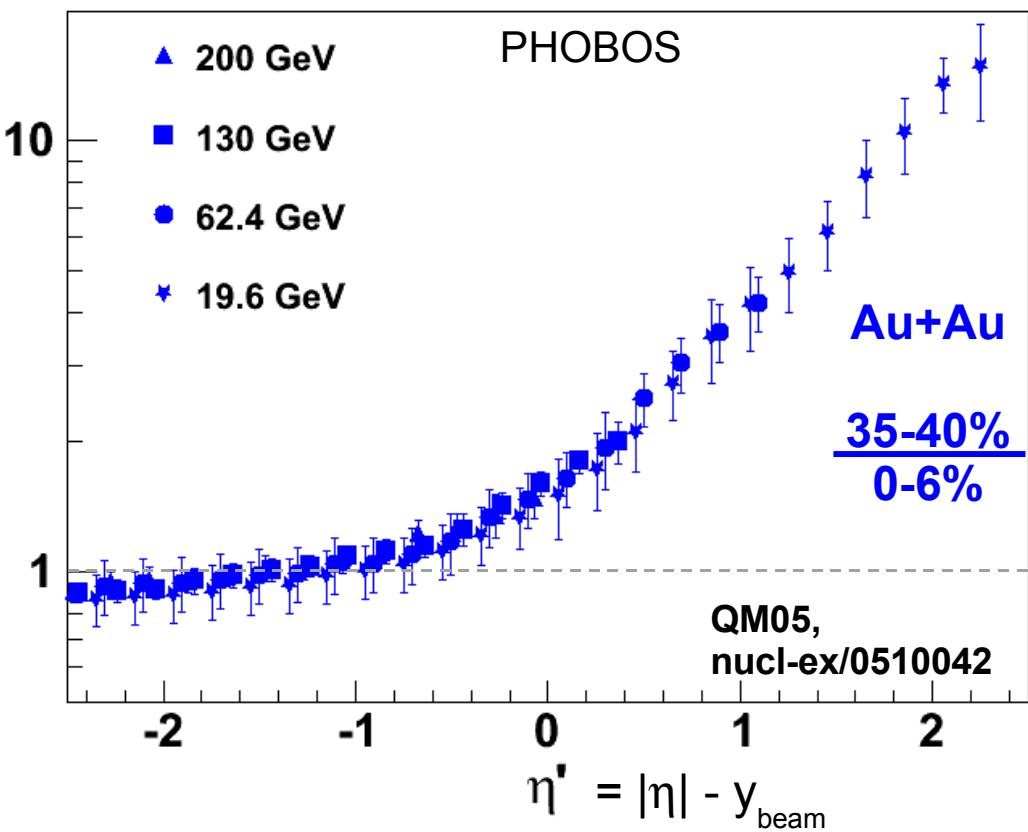
“Extended Longitudinal Scaling” of all longitudinal distributions
(same for Cu+Cu collisions)

QM05, nucl-ex/0510042

Factorization of longitudinal dynamics

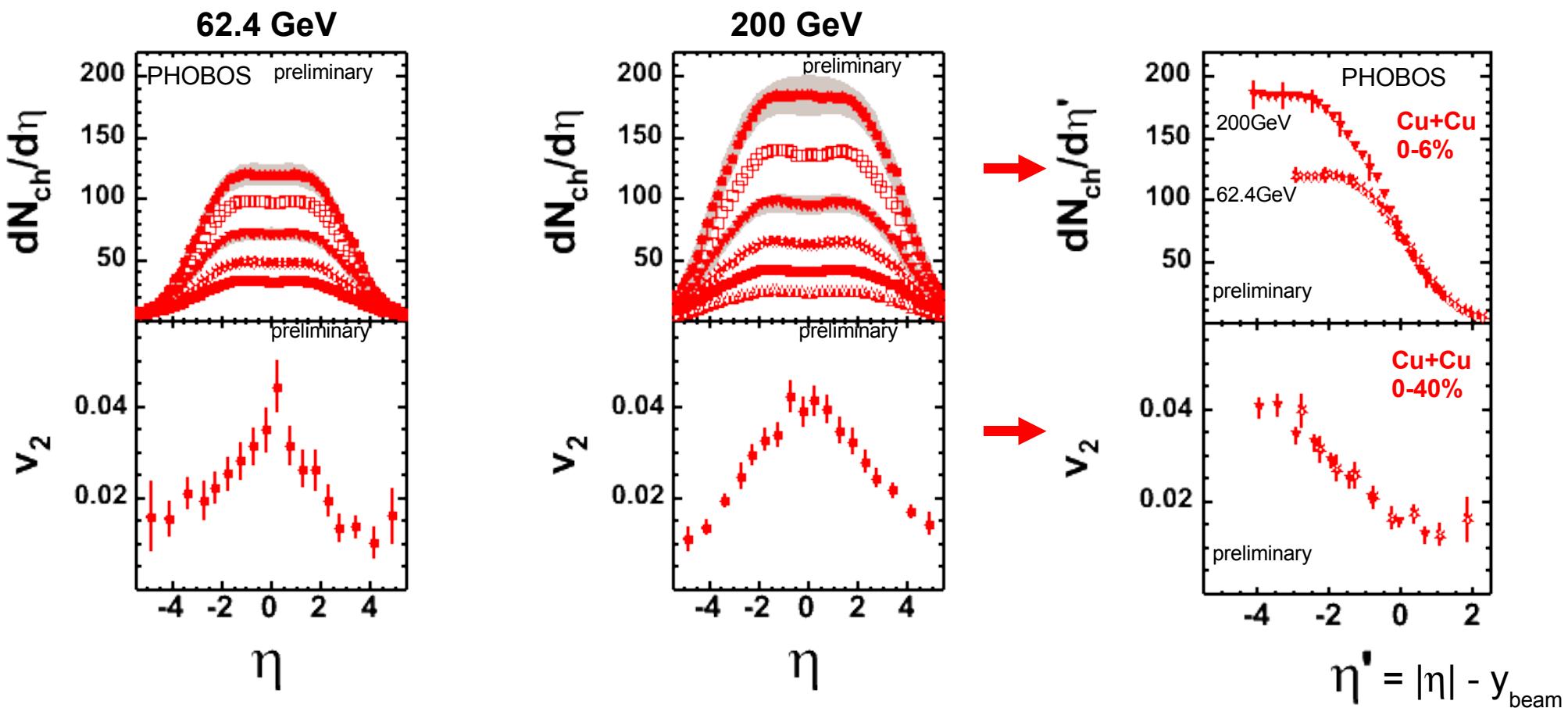


Ratio of 0-6% and 35-40% centrality
bins, each normalized by N_{part}



$R_{PC}^{N_{part}}$ is energy independent!

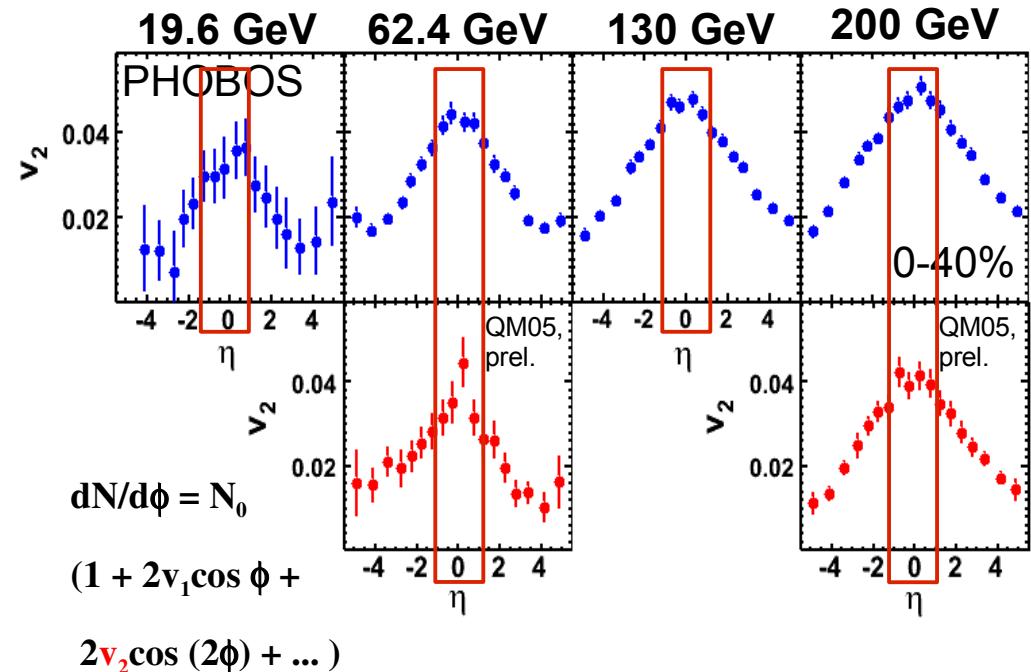
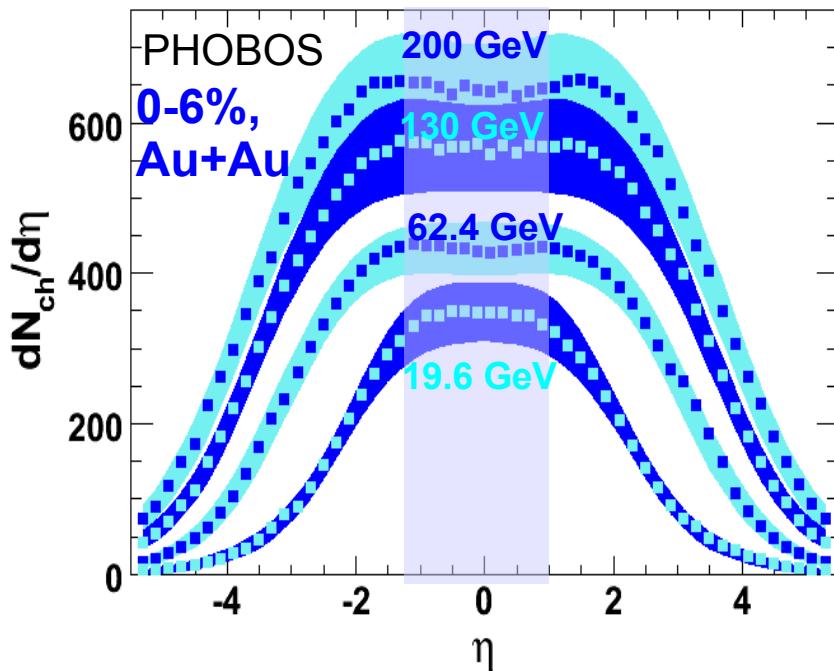
Limiting fragmentation (Cu+Cu)



**'Extended Longitudinal Scaling' also seen in Cu+Cu
Persists from p+p to Au+Au over large range in η '**

QM05, nucl-ex/0510042

Properties of the medium (2)



At 200 GeV:

$$\epsilon > 3 \text{ GeV/fm}^3$$

$$\epsilon = \frac{\langle E \rangle \times dN/d\eta \times \text{corr}}{\pi R^2 \times (0.1 - \text{few}) \text{ fm}}$$

PHOBOS WhitePaper
Strongly interacting medium
with extremely high energy density

WhitePaper: NPA, 757 28 (2005)
 v_2 Au+Au: PRL 94, 122303 (2005)
 v_2 Cu+Cu (prel.): QM05, nucl-ex/0510042