



FLUCTUATIONS IN NUCLEAR COLLISIONS AT 158 GEV/NUCLEON

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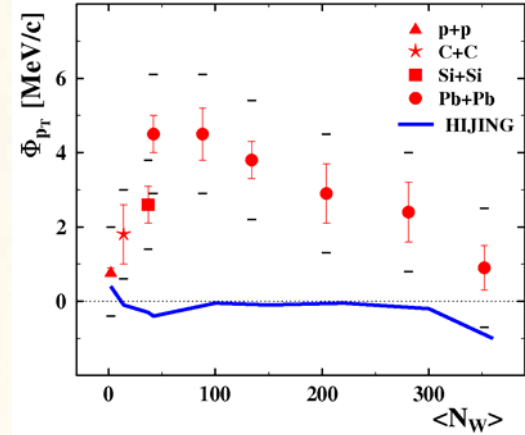
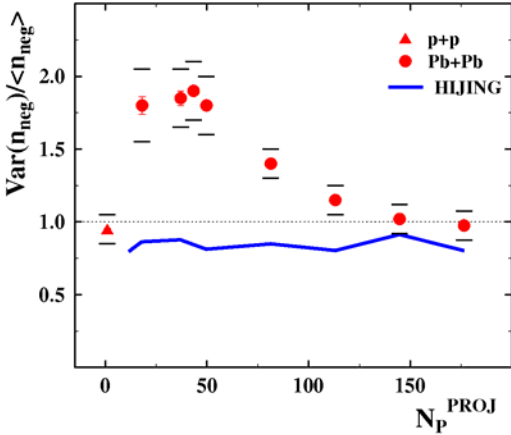
Institute of Physics, Swietokrzyska Academy
Kielce, Poland

for NA49 Collaboration

Florence, July 3 - 9 2006



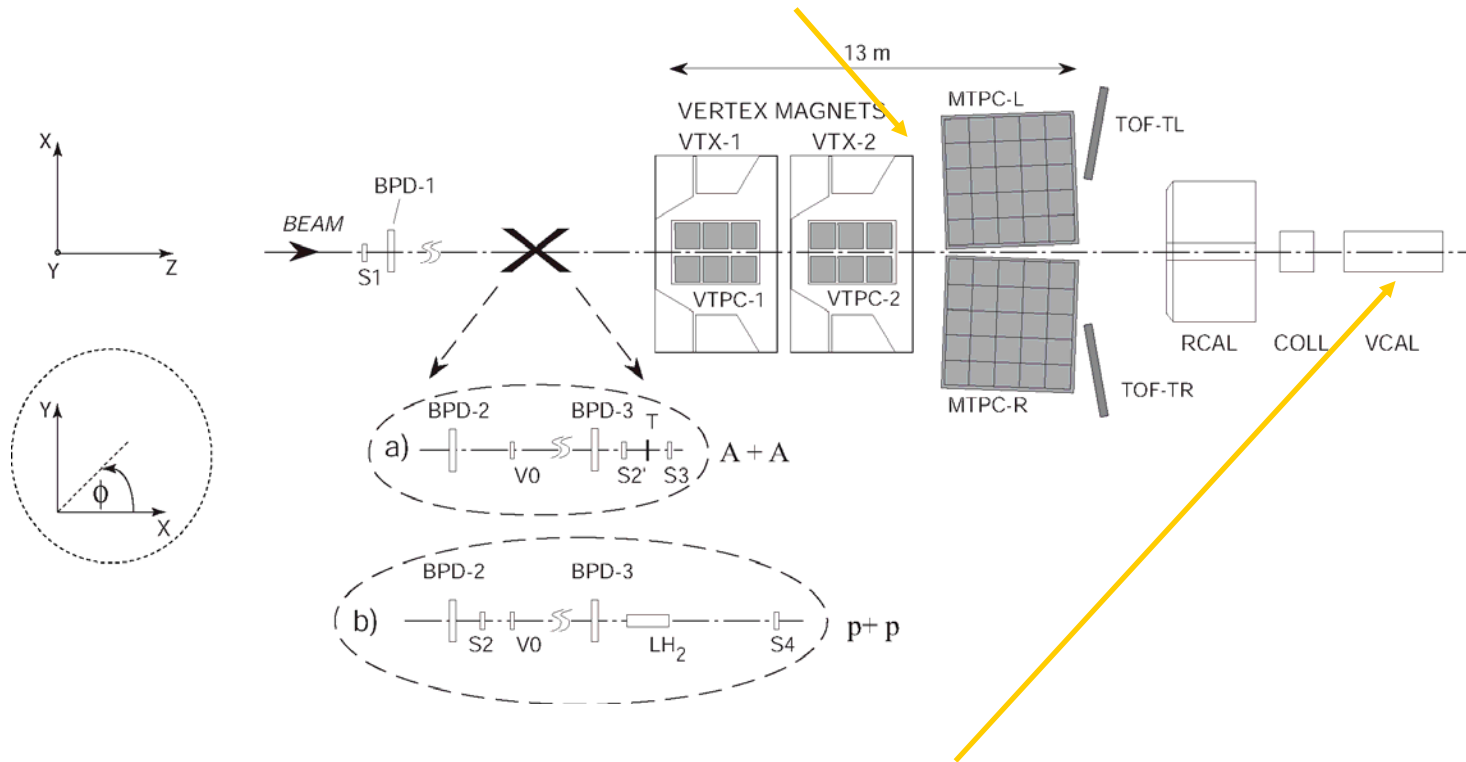
OUTLINE



- Introduction
- Results on multiplicity fluctuations
- Connection between multiplicity fluctuations and Φ_{p_T} measure
- Summary

NA49 EXPERIMENT

Charged particle multiplicity is measured by the large TPC's



Veto Calorimeter measures energy carried by PROJECTILE SPECTATORS

THE ACCEPTANCE

The acceptance used for analysis

$$4 < y < 5.5$$

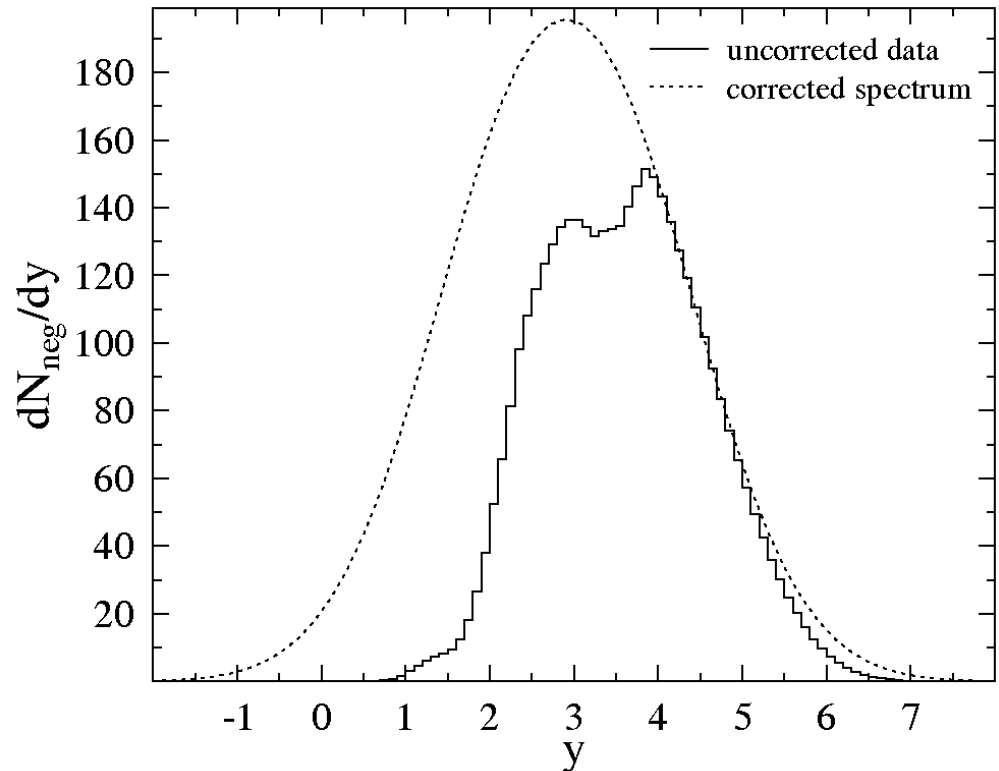
(center of mass rapidity at $y=2.9$)

$$0.005 < p_T < 1.5 \text{ GeV}/c$$

$$\phi(p_T, y)$$

Given in:

Phys. Rev. C **70** (2004) 034902



OBSERVABLES

$$\langle N \rangle = \sum N \cdot P(N)$$

$$\text{Var}(N) = \langle N^2 \rangle - \langle N \rangle^2$$

$$\frac{\text{Var}(N)}{\langle N \rangle}$$

- scaled variance

For Poisson distribution:

$$P(N) = \frac{\langle N \rangle^N}{N!} \cdot e^{-\langle N \rangle} \quad \Rightarrow \quad \frac{\text{Var}(N)}{\langle N \rangle} = 1$$

MULTIPLICITY FLUCTUATIONS IN SUPERPOSITION MODEL

ASSUMPTION:
$$N = \sum_{i=1}^{N_P} m_i$$

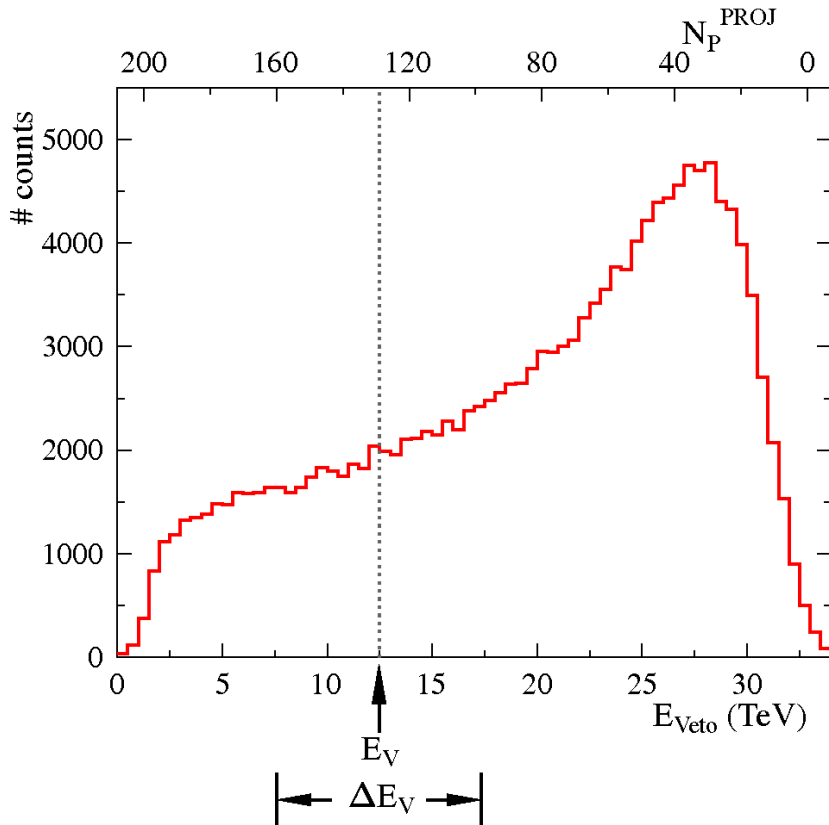
$$\langle N \rangle = \langle N_P \rangle \cdot \langle m \rangle$$

$$\text{Var}(N) = \langle N_P \rangle \cdot \text{Var}(m) + \langle m \rangle^2 \cdot \text{Var}(N_P)$$

$$\frac{\text{Var}(N)}{\langle N \rangle} = \frac{\text{Var}(m)}{\langle m \rangle} + \langle m \rangle \frac{\text{Var}(N_P)}{\langle N_P \rangle}$$

CENTRALITY SELECTION

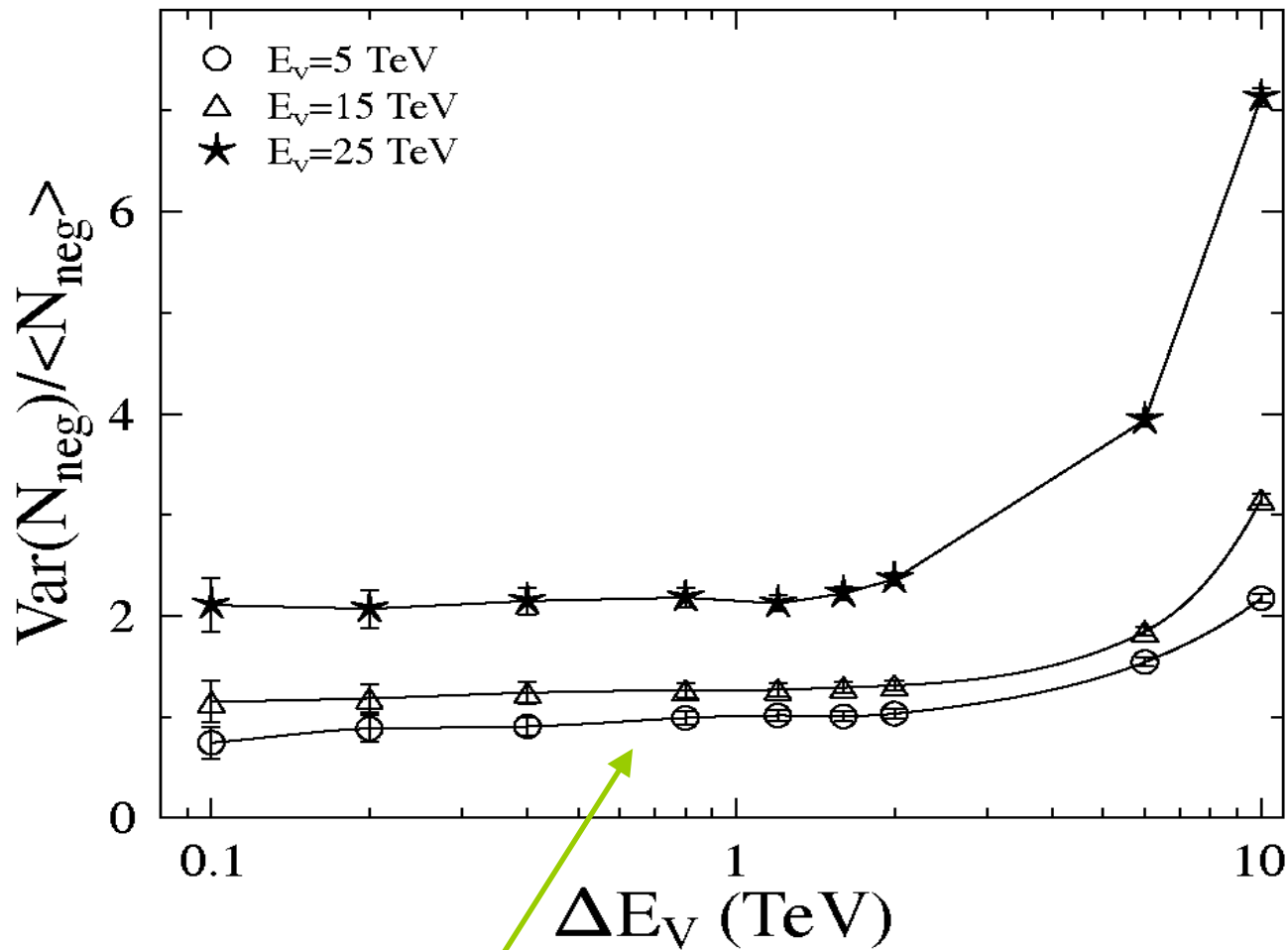
Distribution of energy E_{Veto} of the projectile spectators registered by the NA49 Veto Calorimeter



Events are selected within narrow ΔE_V intervals in E_{Veto} centered at various positions E_V

The number of projectile participants can be estimated as:

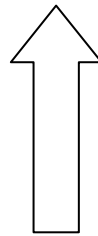
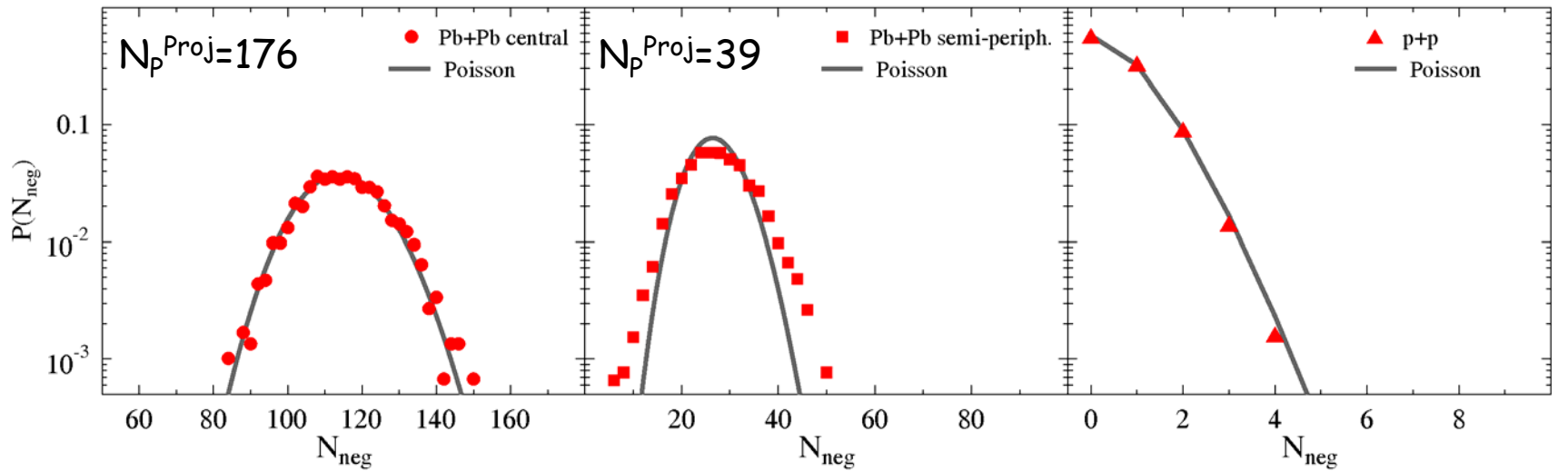
$$N_P^{PROJ} = A - \frac{E_{Veto}}{E_{LAB}}$$



Saturation for $\Delta E_V < 1 \text{ TeV}$

EXAMPLES OF MULTIPLICITY DISTRIBUTIONS

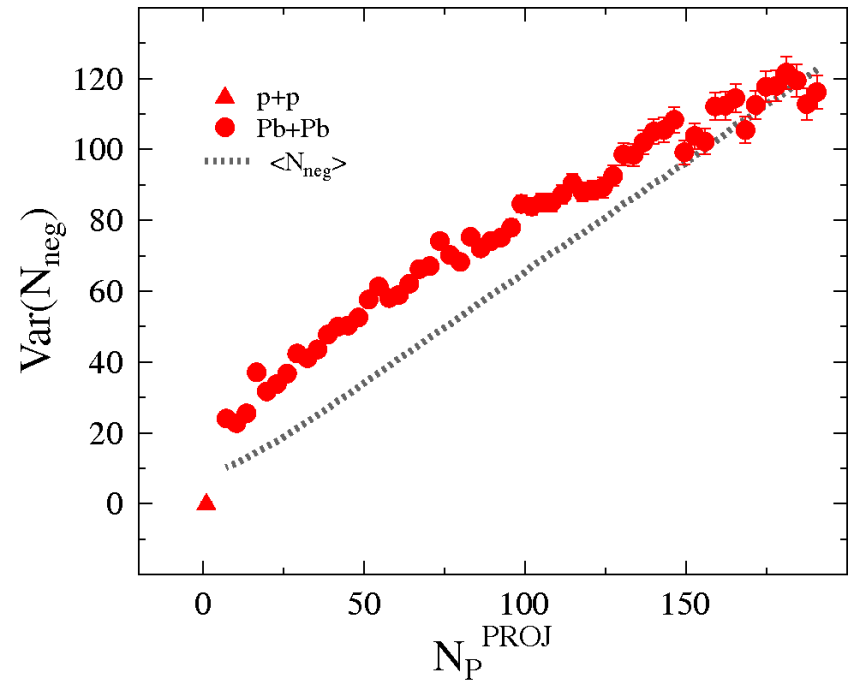
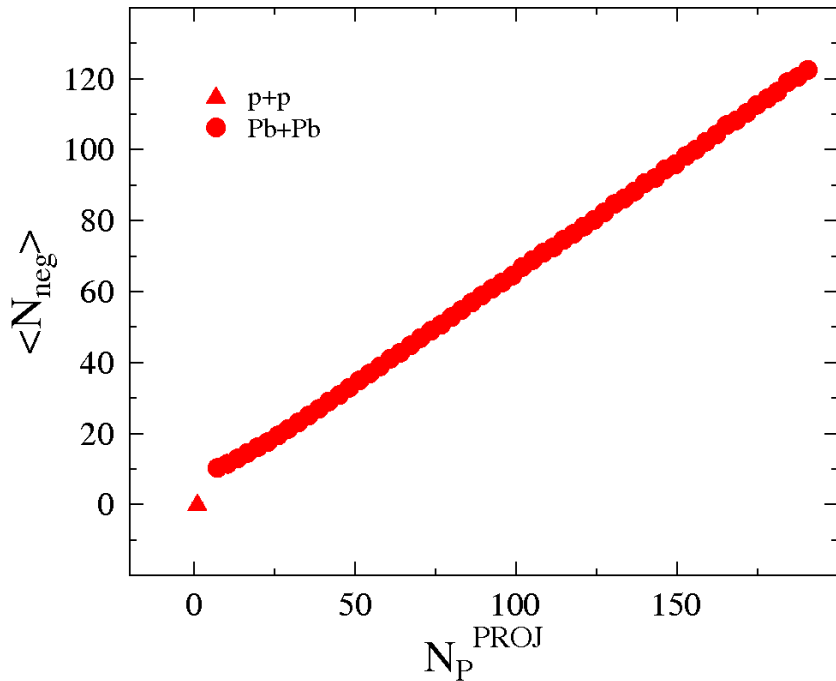
$$\Delta E_V = 500 \text{ GeV}$$



Large fluctuations for semi-peripheral Pb+Pb collisions

MEASURED MEAN VALUE AND VARIANCE OF MULTIPLICITY DISTRIBUTION VS N_P^{PROJ}

$$N_P^{PROJ} = A - \frac{E_{Veto}}{E_{LAB}} \quad \Delta E_V = 500 \text{ GeV}$$



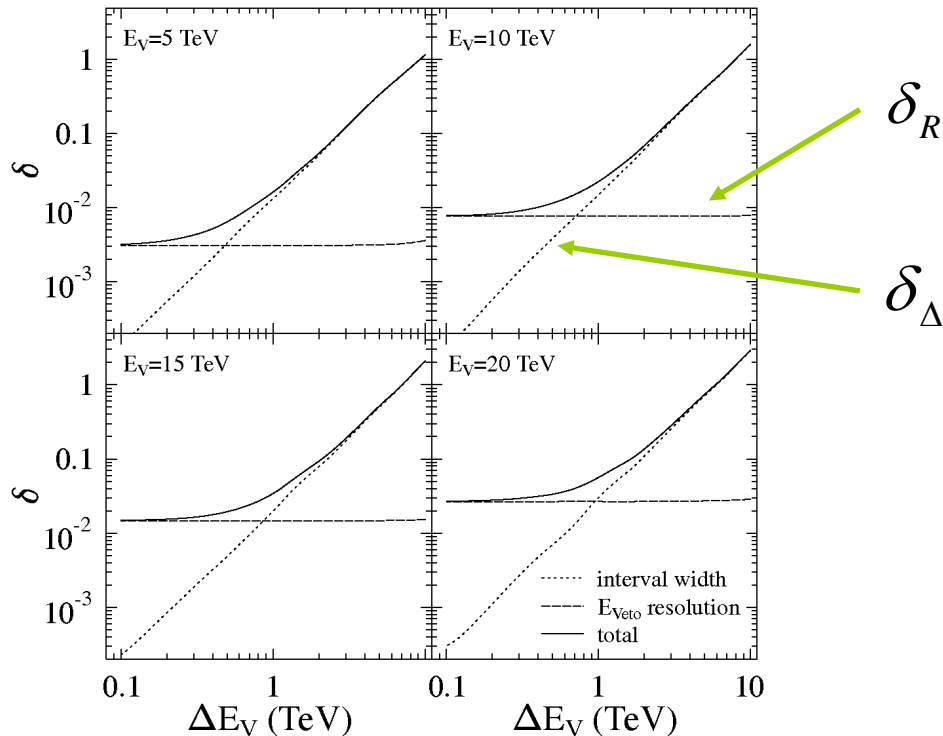
The scaled variance is corrected for:

δ_{Δ} - the finite width of E_{Veto} bin

δ_R - the finite Veto calorimeter resolution

Total correction is calculated as:

$$\delta = \delta_{\Delta} + \delta_R$$



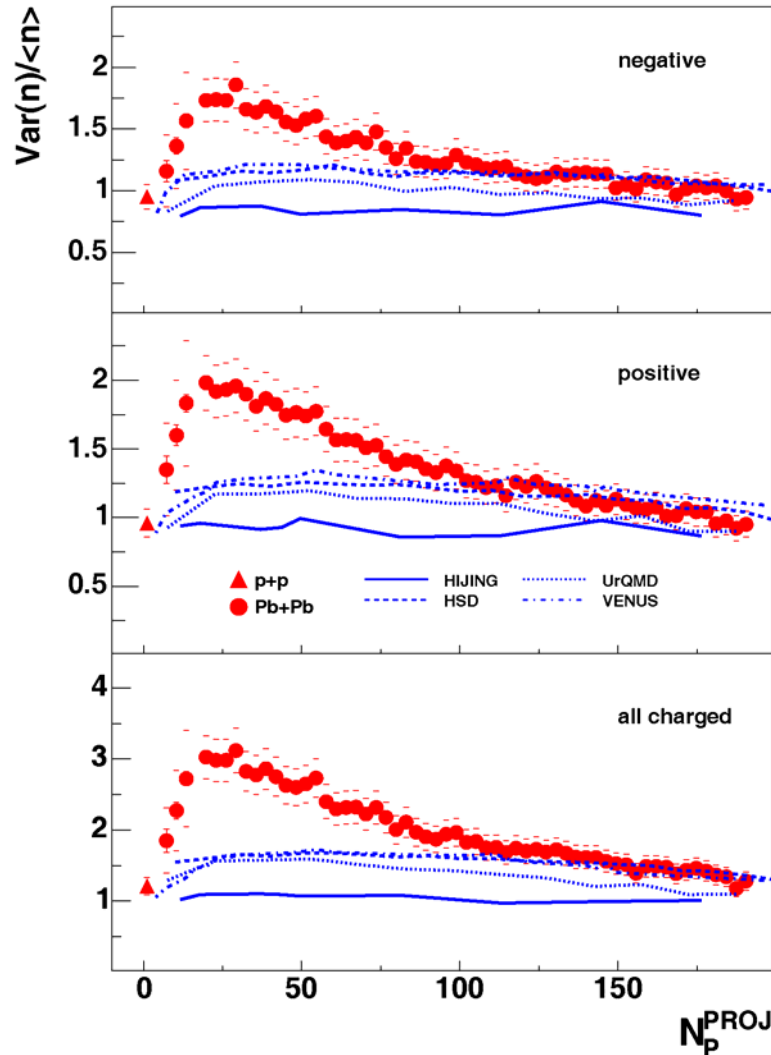
Corrections are small!

Corrected scaled variance:

$$\frac{\text{Var}(n)}{\langle n \rangle} = \frac{\text{Var}(N)}{\langle N \rangle} - \delta$$

Systematic error is lower than 10% for $N_P^{\text{PROJ}} > 20$

MULTIPLICITY FLUCTUATIONS IN Pb+Pb COLLISIONS AT 158A GeV

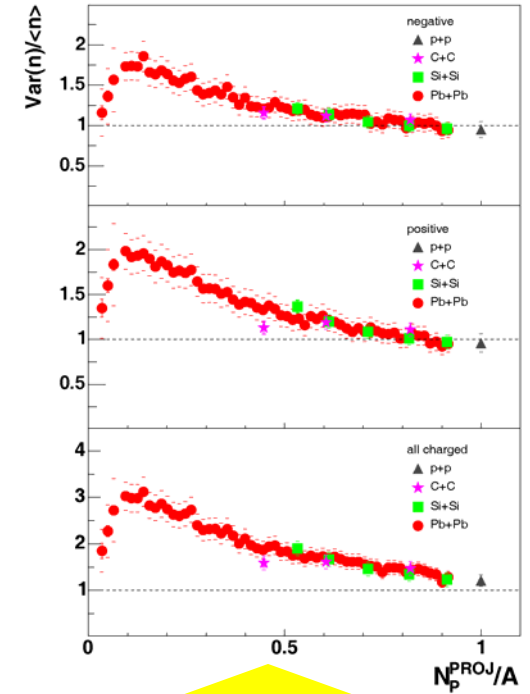
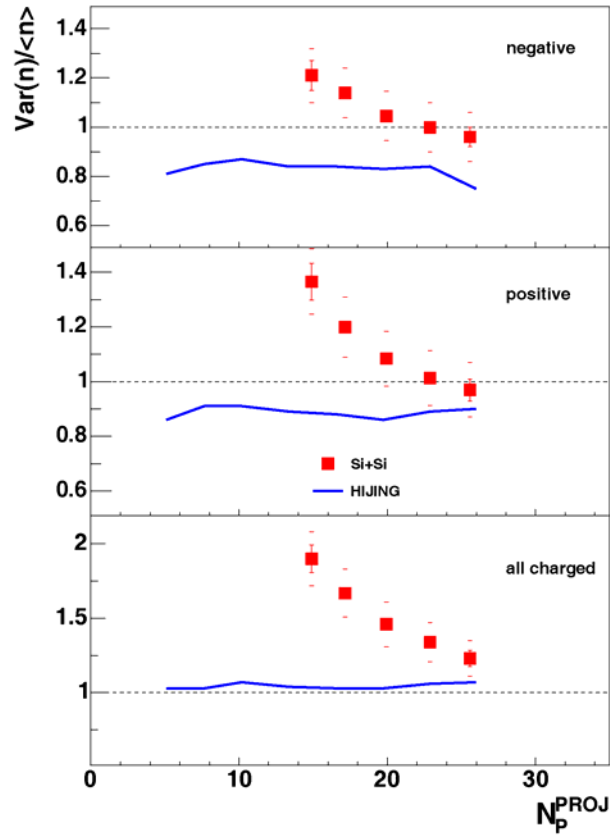
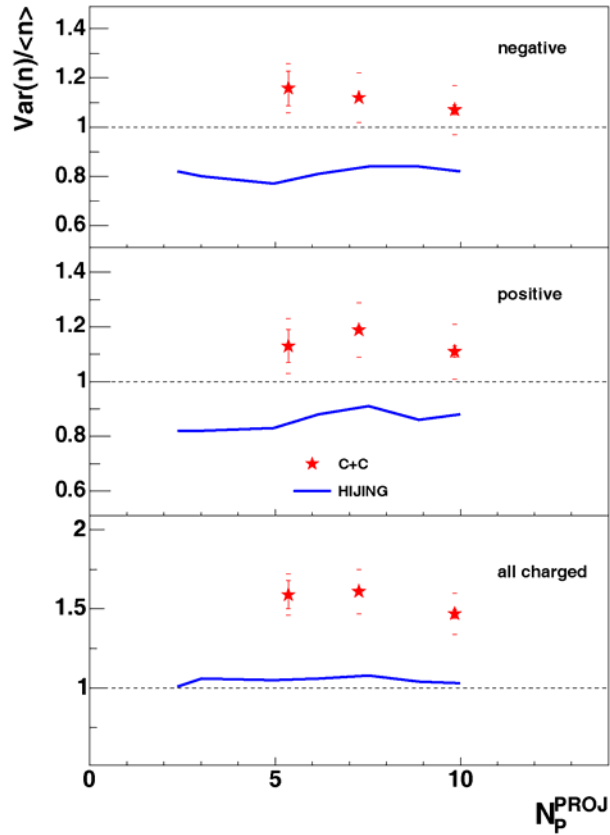


LARGE

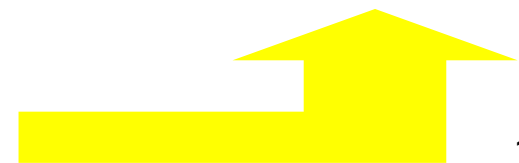
fluctuations for
semi-peripheral
Pb+Pb collisions

String-hadronic models
do not reproduce the data

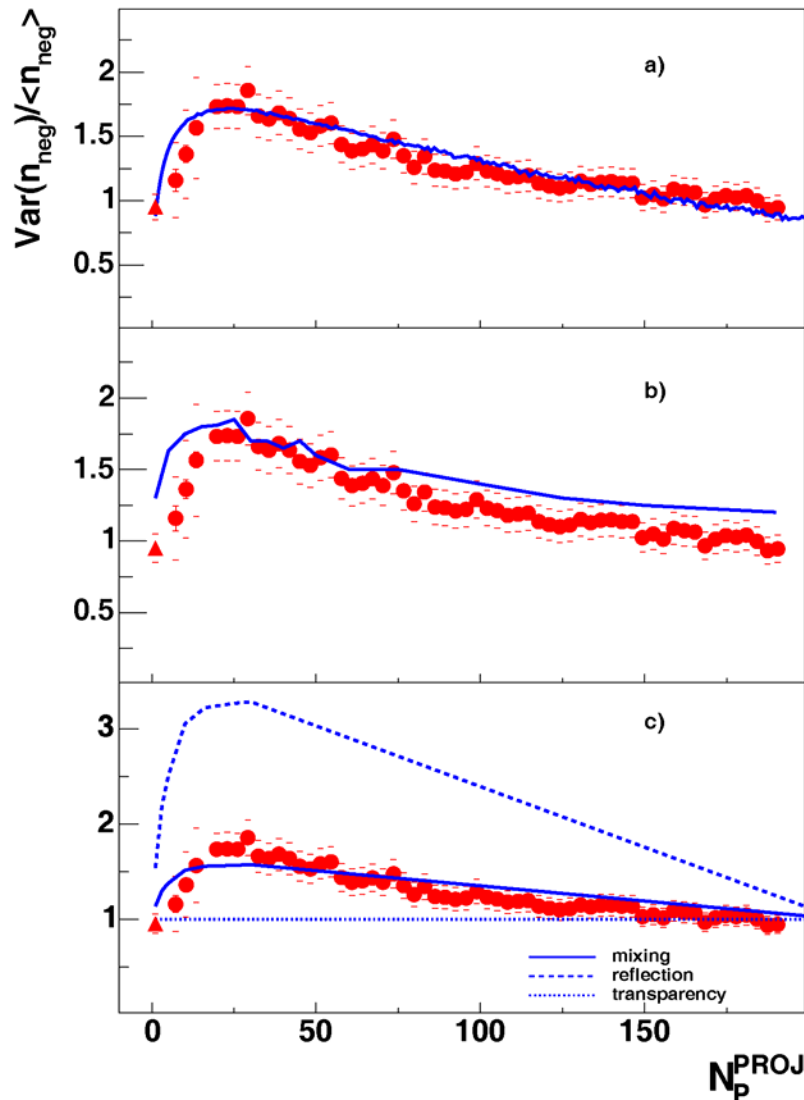
MULTIPLICITY FLUCTUATIONS IN C+C AND Si+Si COLLISIONS AT 158A GeV



SCALING!



ATTEMPTS TO EXPLAIN OBSERVED FLUCTUATIONS



**TWO-PARTICLE
CORRELATIONS**

J. Phys.:Conf. Series 5 (2005) 238

PERCOLATION

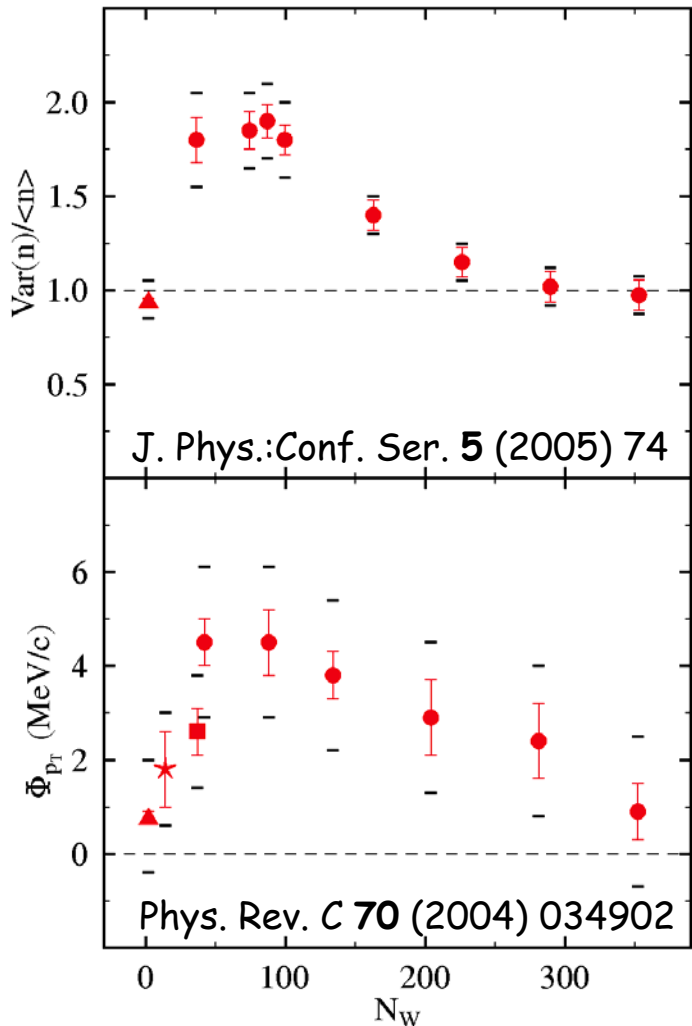
Phys. Rev. C 72 (2005) 044903

**MIXING, REFLECTION
AND TRANSPARENCY**

hep-ph/0511058

CONNECTION BETWEEN MULTIPLICITY FLUCTUATIONS AND Φ_{p_T} MEASURE

158A GeV, all negatives, acceptance: $4 < \eta < 5.5$ and $0.005 < p_T < 1.5$ GeV/c



$$P(p_T) \sim p_T \exp\left(-\frac{\sqrt{m^2 + p_T^2}}{T_N}\right)$$

$$T_N = T + \delta T \left(1 - \frac{N}{\langle N \rangle}\right)$$

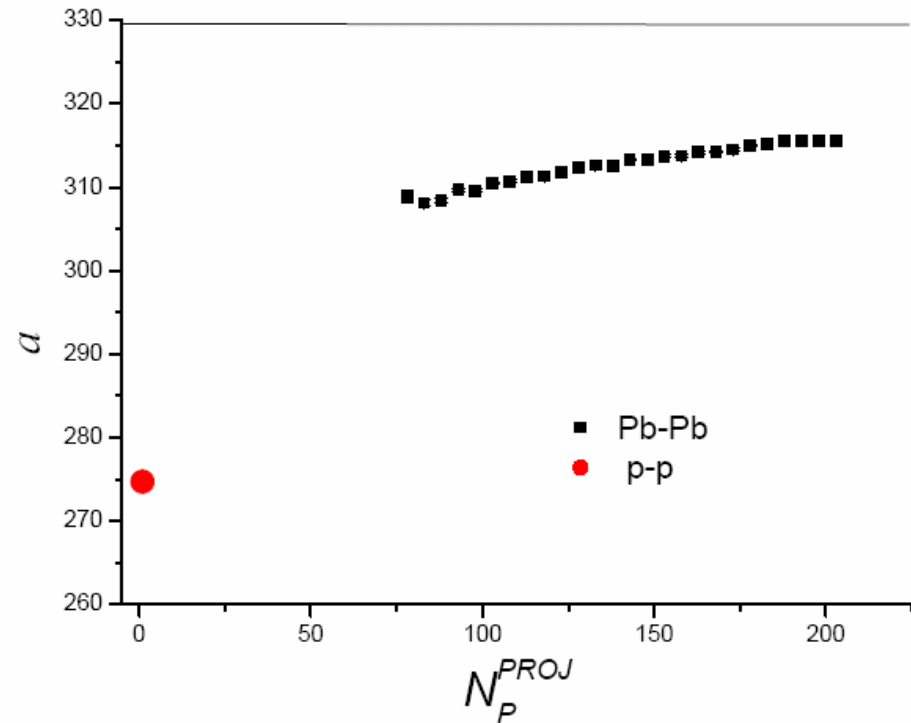
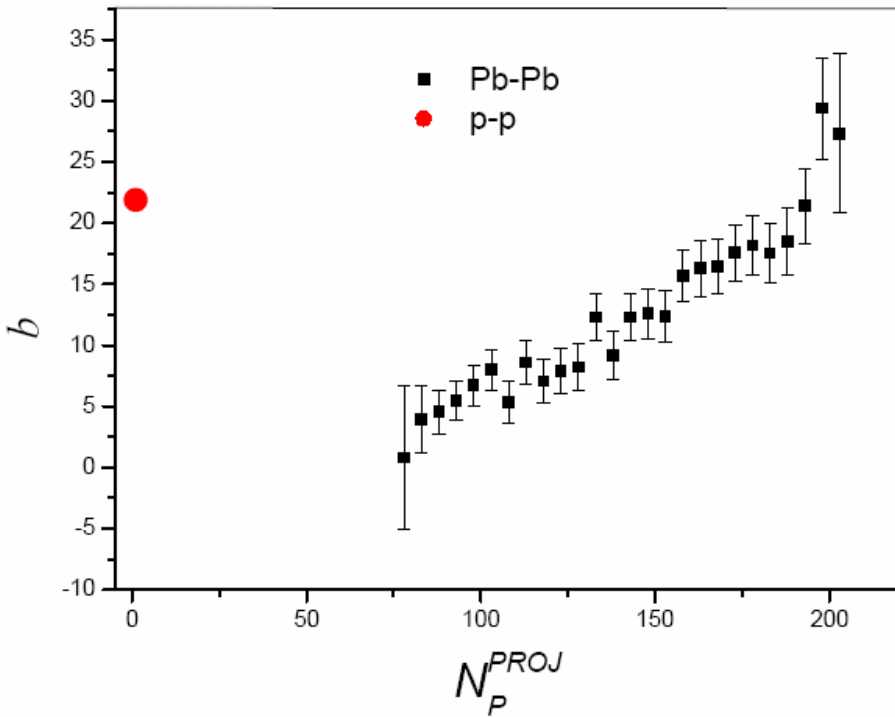
$$\Phi_{p_T} = \sqrt{2} \frac{(\delta T)^2}{T} \frac{\text{Var}(N)}{\langle N \rangle}$$

Details in:

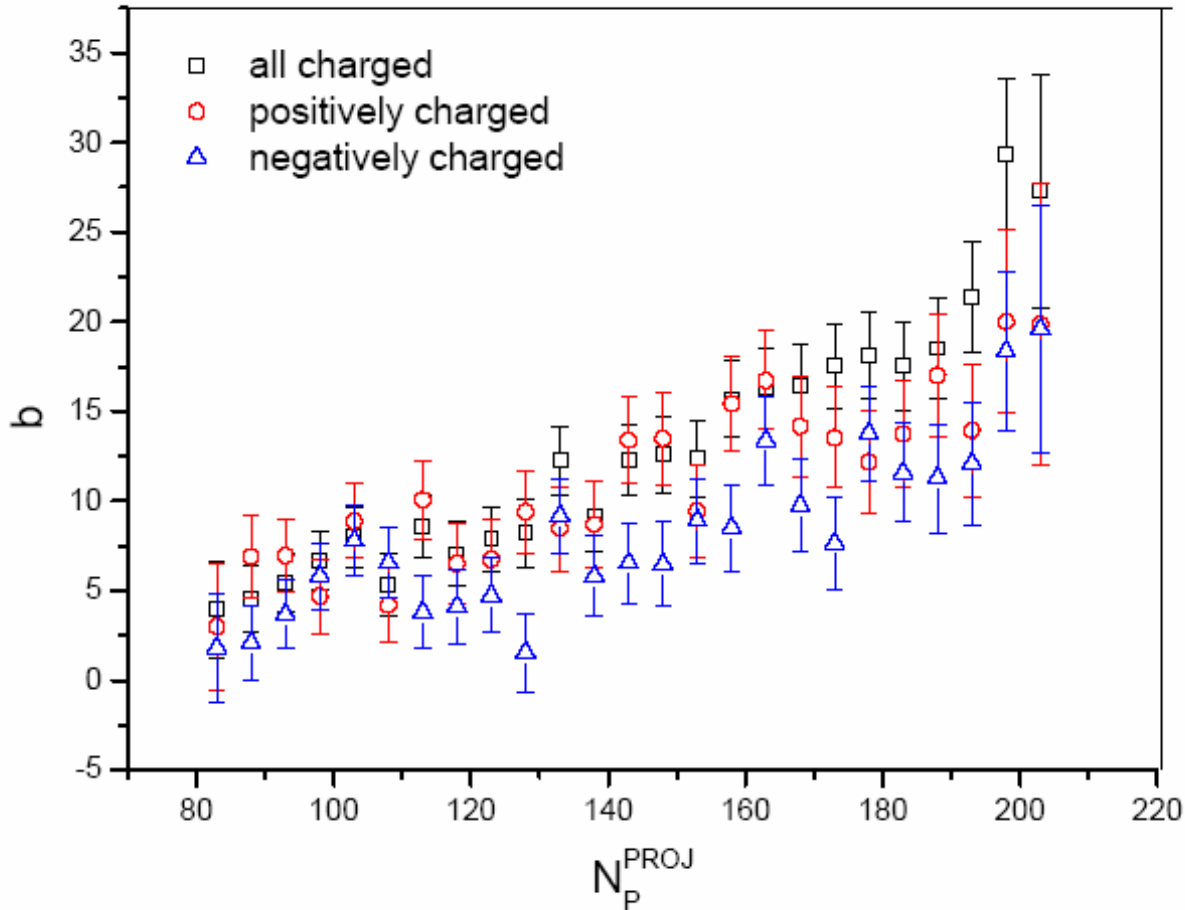
Phys. Rev. C 70 (2004) 054906

$\langle p_T \rangle$ - N CORRELATIONS

$$\langle p_T \rangle = a + b \left(1 - \frac{N}{\langle N \rangle} \right)$$



RESULTS FOR h^+ , h^- AND h^\pm



$$\langle p_T \rangle = a + b \left(1 - \frac{N}{\langle N \rangle} \right)$$

$\langle p_T \rangle$ - N CORRELATION IN SUPERPOSITION MODEL

(St. Mrówczyński Phys.Rev. C74 (2006) 044907)

1) single source

$$\langle p_T \rangle = a + b \left(1 - \frac{N}{\langle N \rangle_1} \right)$$

2) k - sources

$$\langle p_T \rangle \approx a + b \left(1 - \frac{N}{\langle N \rangle_k} \right)$$

$$\langle N \rangle_k = k \langle N \rangle_1$$

3) Varying number of sources

$$\langle p_T \rangle \approx a + b' \left(1 - \frac{N}{\langle N \rangle_k} \right)$$

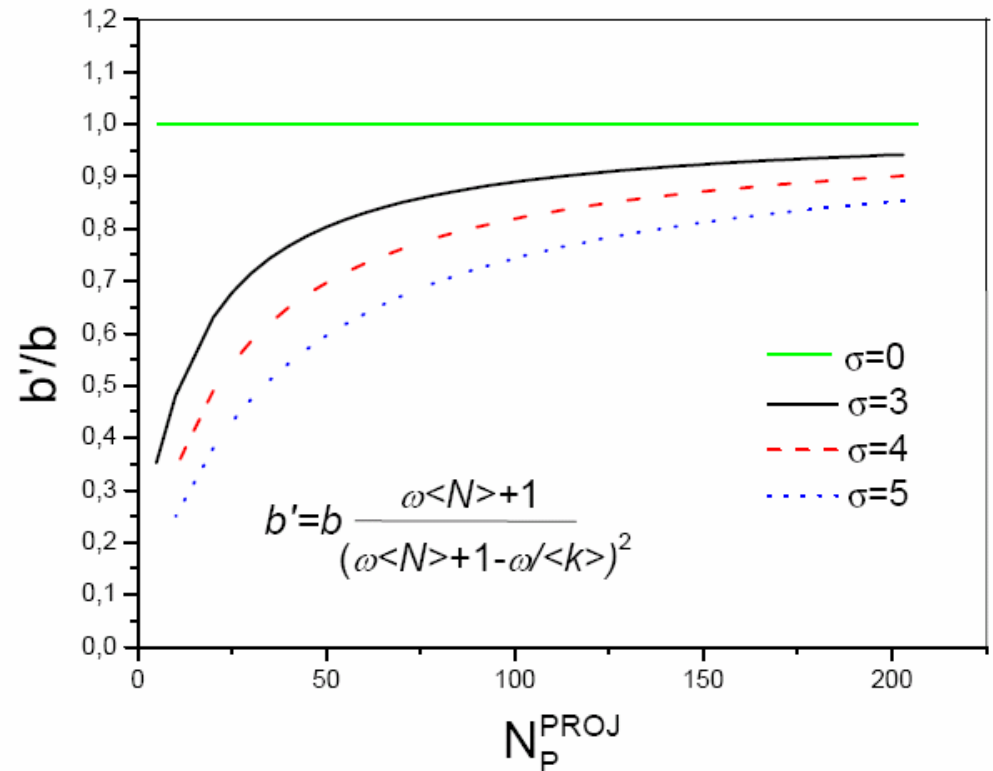
$\langle p_T \rangle$ - N CORRELATION IN SUPERPOSITION MODEL

$$b' = b \frac{\sigma^2 \langle N \rangle \langle k \rangle^3 + \langle k \rangle^4}{\left(\sigma^2 \langle N \rangle \langle k \rangle + \langle k \rangle^2 - \sigma^2 \right)^2}$$

$\sigma^2 \rightarrow 0$, then $b' \rightarrow b$

$\sigma^2 \rightarrow \infty$, then $b' \rightarrow 0$

$$\omega = \frac{\sigma^2}{\langle k \rangle}$$



EFFECT OF VETO CALORIMETER RESOLUTION

Parameterization of the energy resolution of the veto calorimeter:

$$\frac{\sigma(E_{Veto})}{E_{Veto}} = \frac{9.3}{\sqrt{E_{Veto}}} - \frac{44.4}{E_{Veto}} - 0.032$$

Given in:

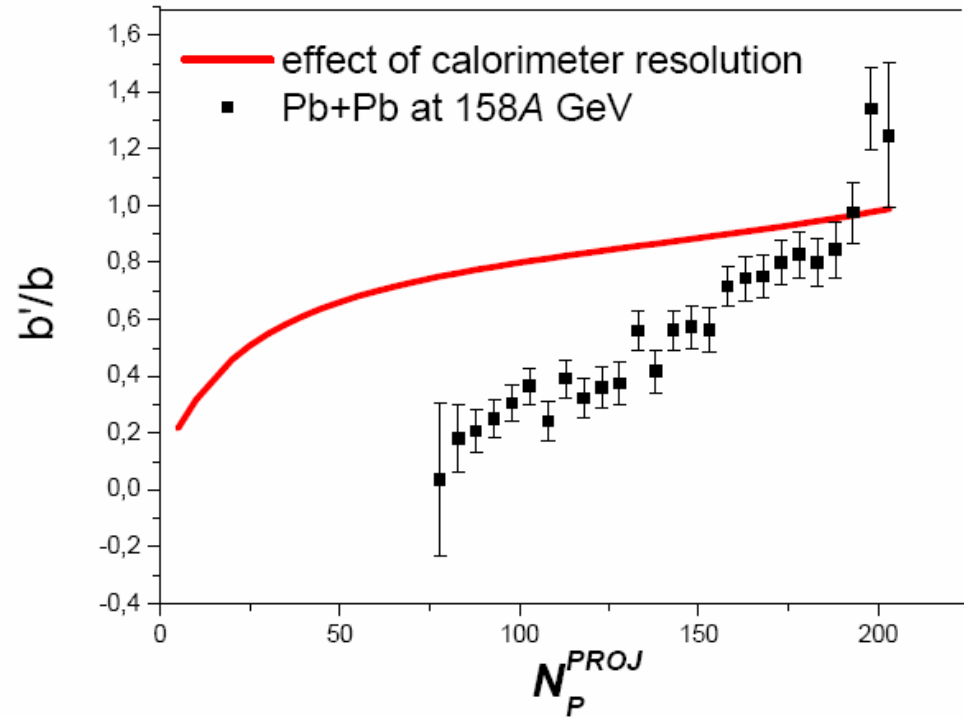
M. Rybczyński, PhD Dissertation, Kielce 2005

and

$$N_P^{PROJ} = A - \frac{E_{Veto}}{E_{LAB}}$$

then:

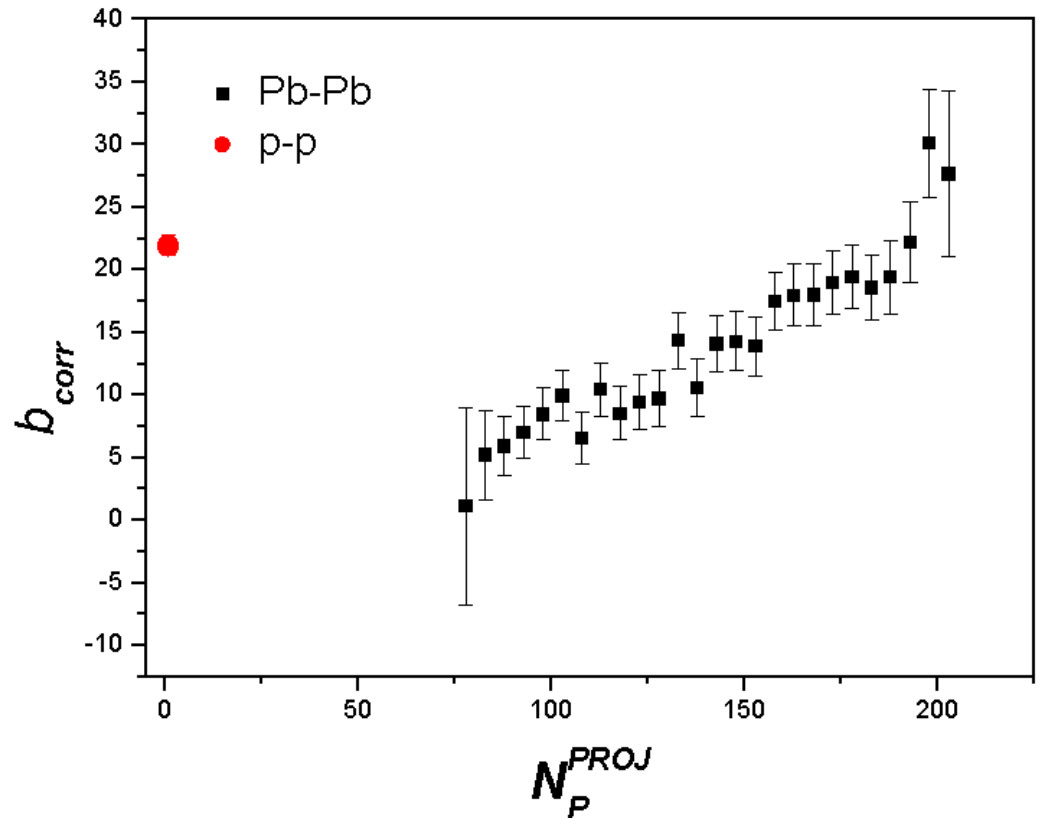
$$\sigma(\langle N_P^{PROJ} \rangle) = 0.77 \sqrt{A - \langle N_P^{PROJ} \rangle} - 0.28 - (A - \langle N_P^{PROJ} \rangle)$$



$\langle p_T \rangle$ - N CORRELATIONS

AFTER CORRECTION FOR VETO CALORIMETER RESOLUTION

$$\langle p_T \rangle = a + b_{corr} \left(1 - \frac{N}{\langle N \rangle} \right)$$



SUMMARY

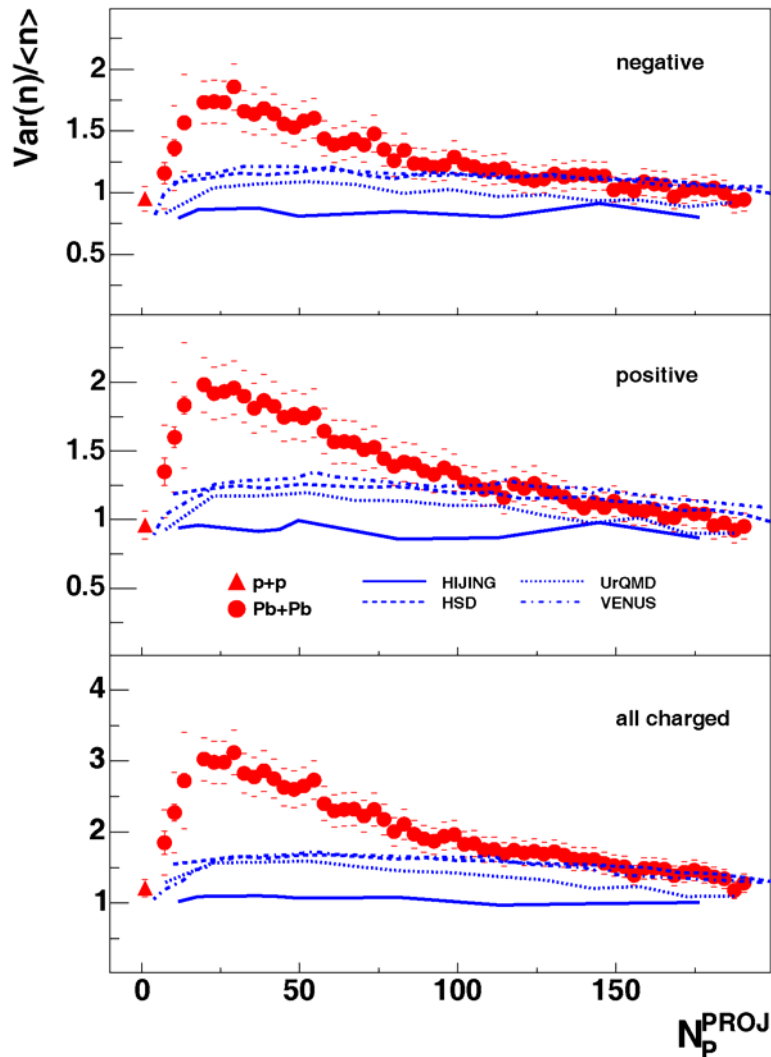
- Multiplicity fluctuations and $\langle p_T \rangle$ - N correlations in nuclear collisions at 158 GeV/nucleon were studied;
- The results in the projectile hemisphere at fixed number of projectile participants show:
 - an increase of the scaled variance of N - fluctuations with decreasing centrality
 - a decrease of the $\langle p_T \rangle$ - N correlations with decreasing centrality

OUTLOOK:

- Quantitative predictions of p_T - fluctuations from the measured N - fluctuations and $\langle p_T \rangle$ - N correlation.

BACKUP SLIDES...

MULTIPLICITY FLUCTUATIONS IN Pb+Pb COLLISIONS

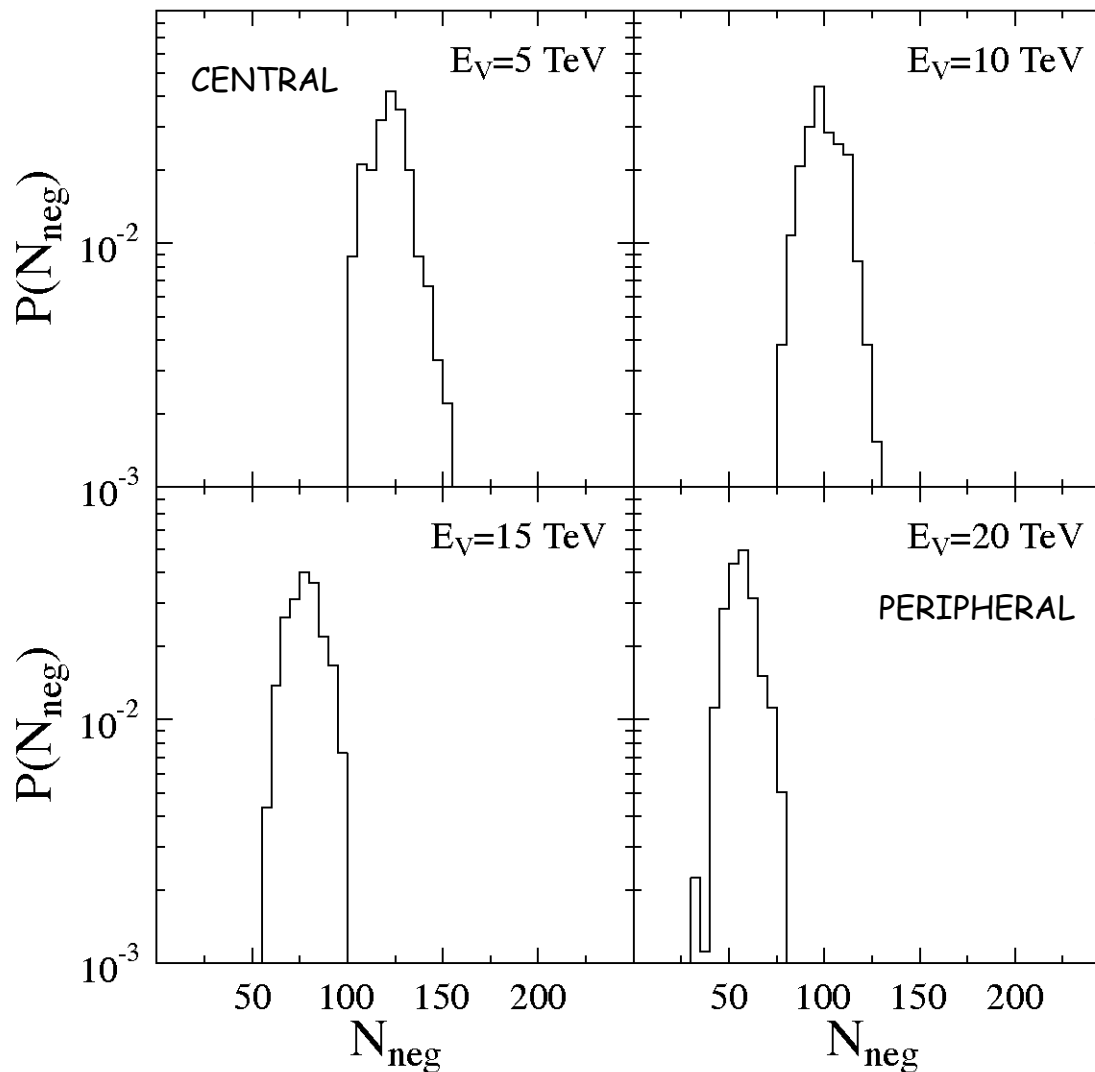


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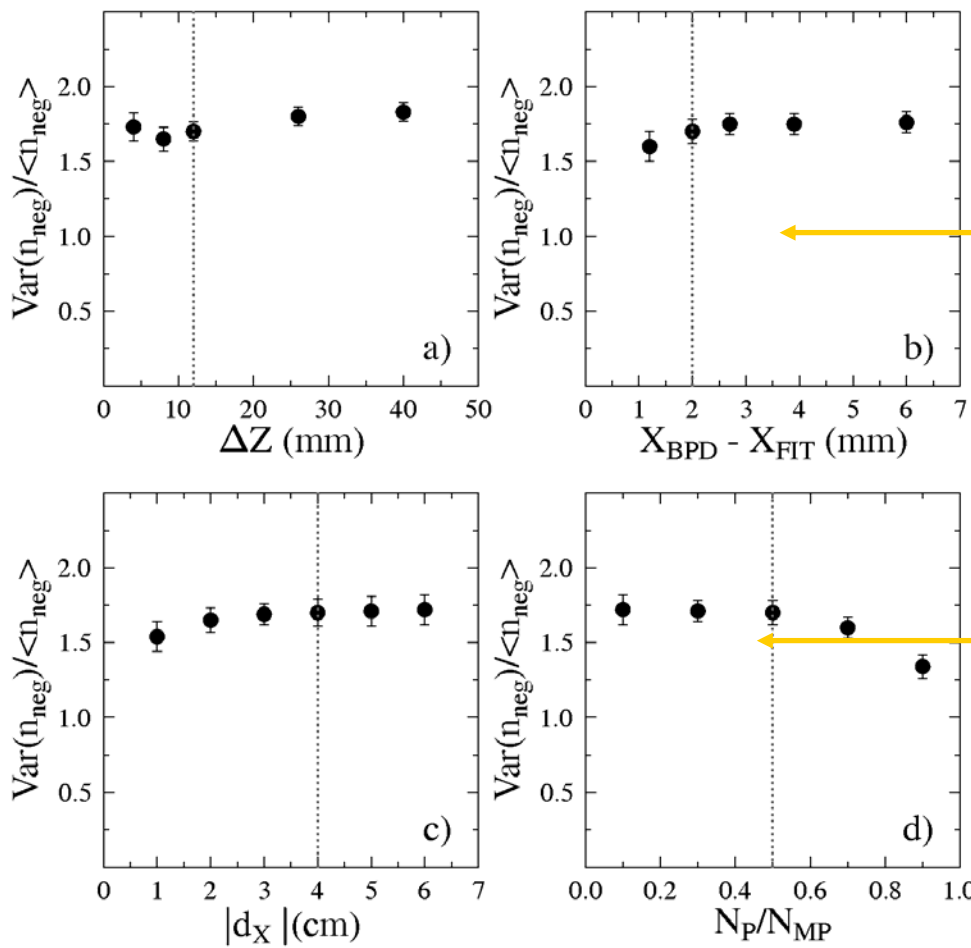
fluctuations for
semi-peripheral
Pb+Pb collisions

UNCORRECTED MULTIPLICITY DISTRIBUTIONS OF NEGATIVELY CHARGED PARTICLES

Pb+Pb at 158 GeV/nucleon; $\Delta E_V = 500$ GeV



STABILITY OF THE RESULTS WITH RESPECT TO THE ANALYSIS CUTS

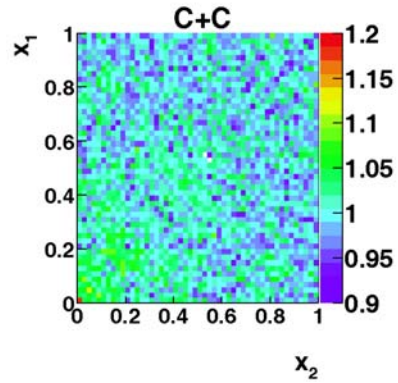
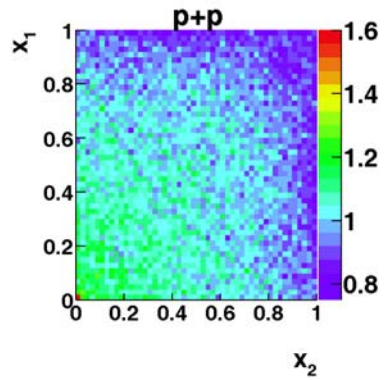


All checks done for $N_P^{\text{PROJ}} = 39$

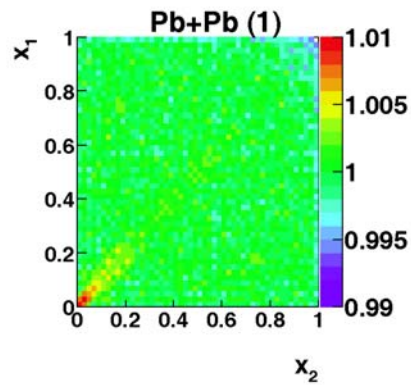
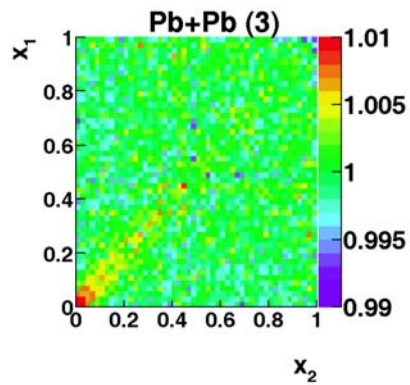
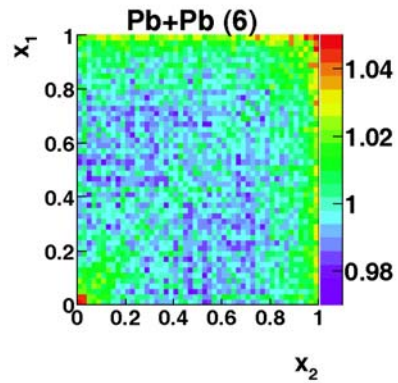
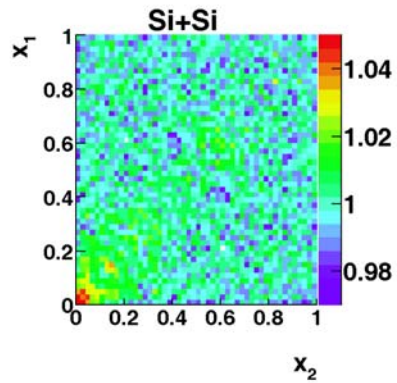
Event selection cuts

Track selection cuts

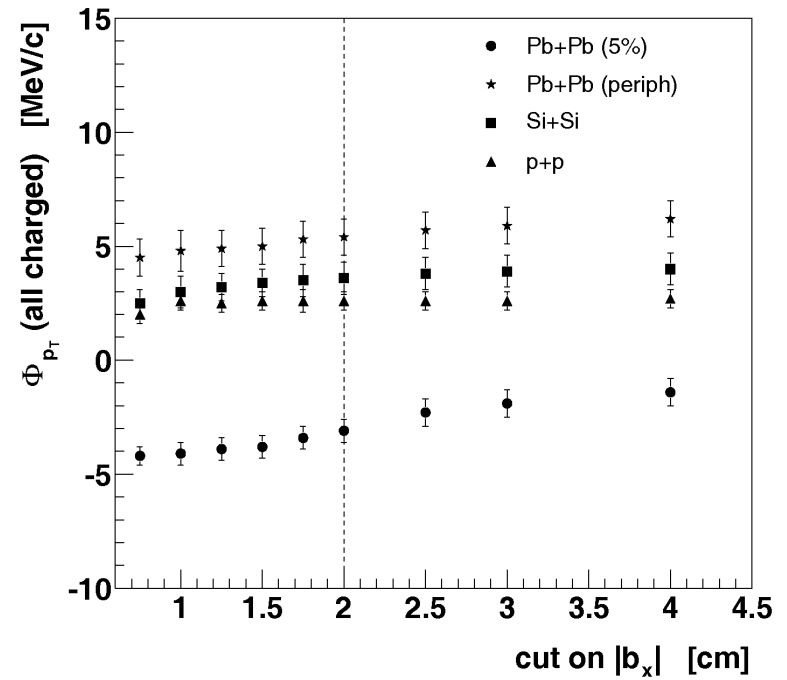
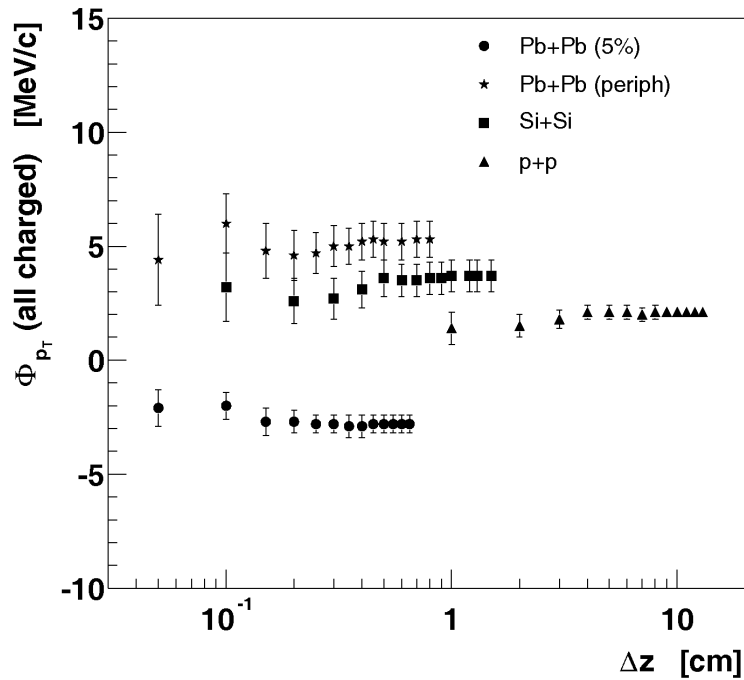
Scaled variance changes by less than 15 %



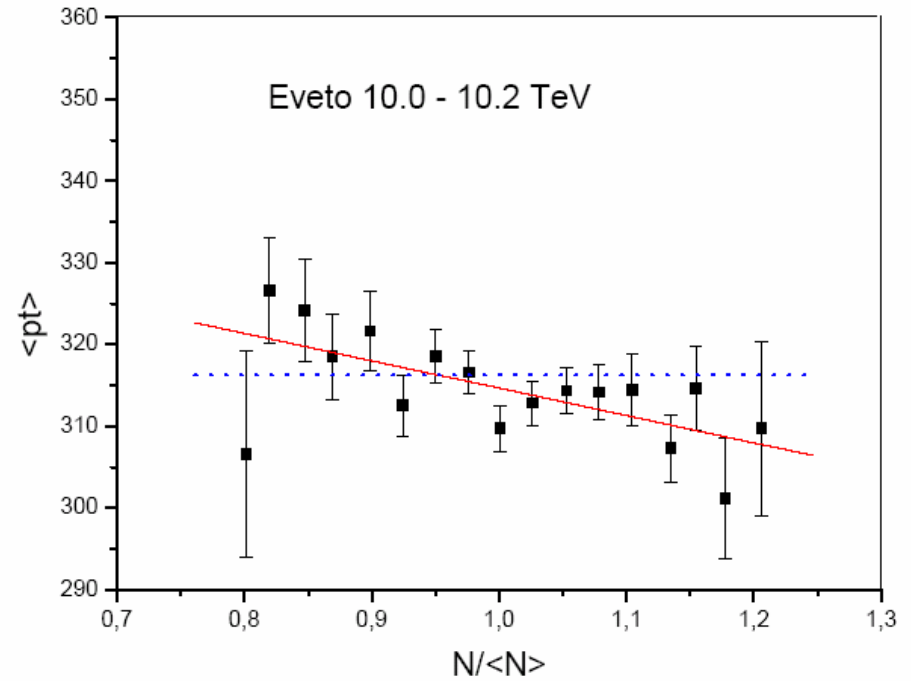
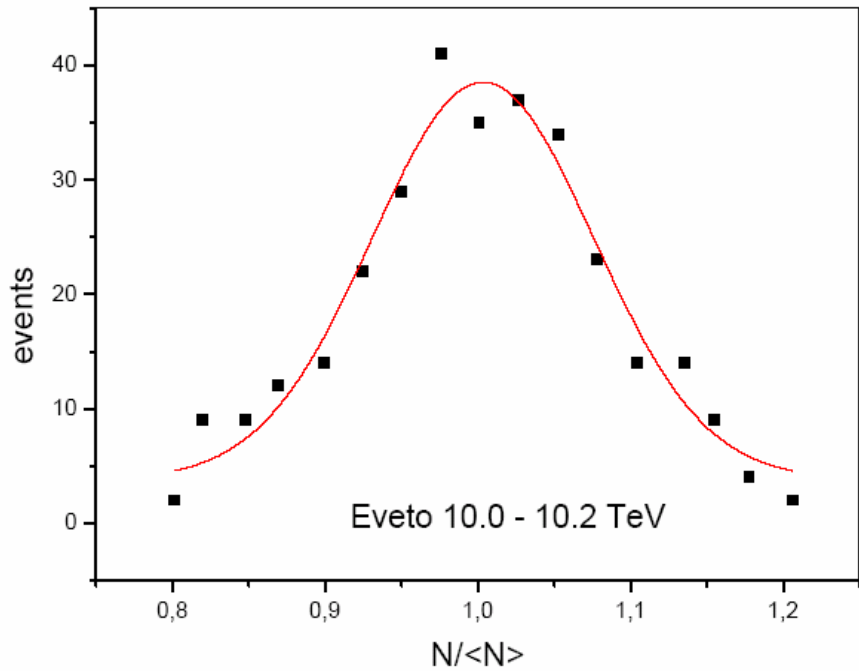
$$x(p_T) = \int_0^{p_T} \rho(p_{T'}) dp_{T'}$$



STABILITY OF THE RESULTS WITH RESPECT TO THE ANALYSIS CUTS



EXAMPLE OF p_T - N CORRELATIONS



CALCULATIONS WITHIN MIXING MODEL

Fluctuations of the target participant are calculated at:

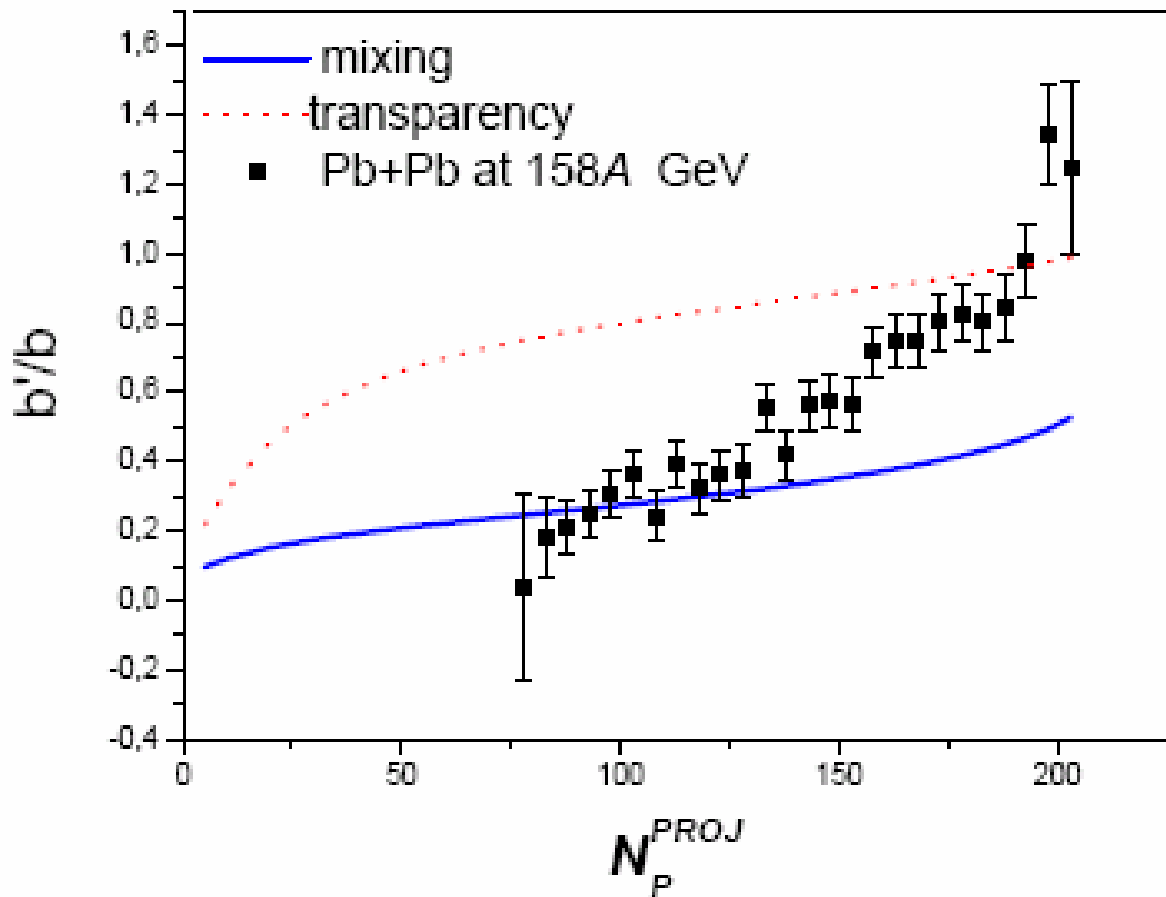
$$\sigma_{TARG}^2 = 3.28N_P^{PROJ} - 0.0158(N_P^{PROJ})^2$$

Taken from: V.P.Konchakovski Phys.Rev. C 73 (2006) 034902

The variance of the number of particle sources in mixing model is:

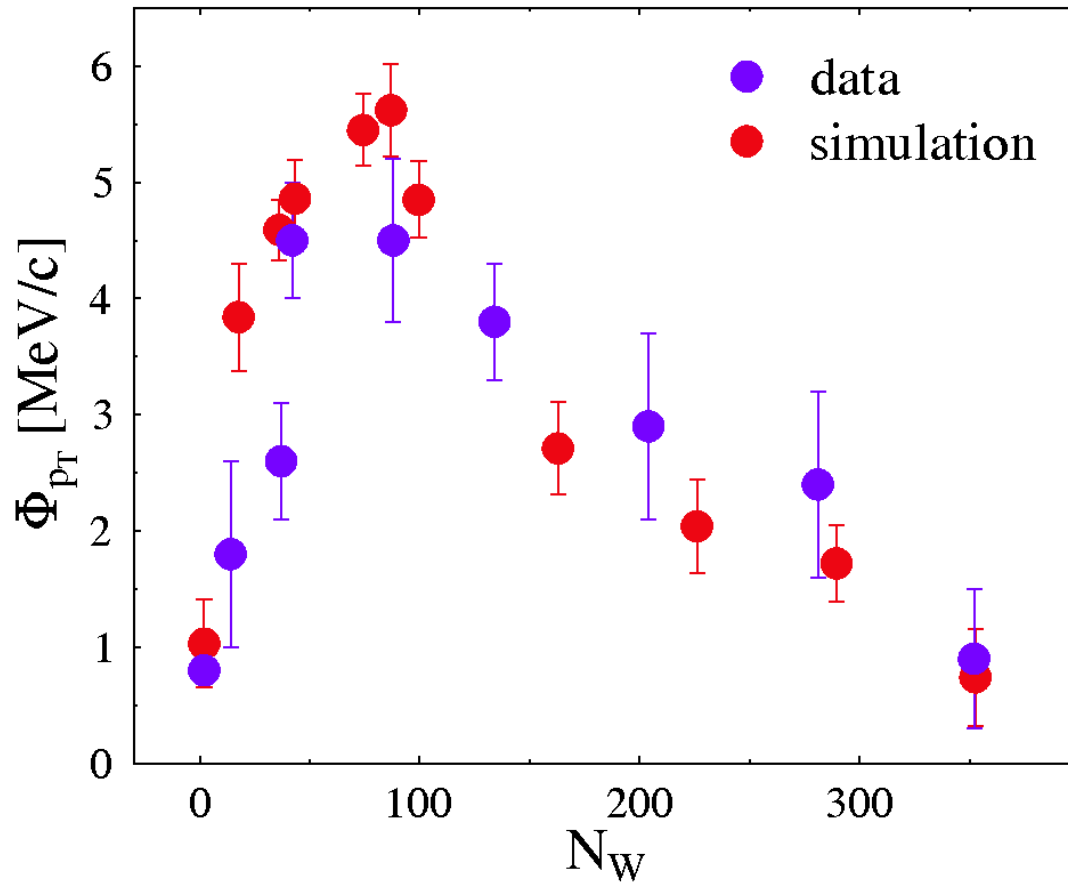
$$\sigma^2(N_P^{PROJ}) = 1.32N_P^{PROJ} - 0.004(N_P^{PROJ})^2$$

MIXING IN SUPERPOSITION MODEL



Effect of E_{veto} resolution was taken into account in model calculations

Φ_{p_T} as a function of number of wounded nucleons.



Simulation:

- $\text{Var}(N)/\langle N \rangle$ from the data
- $\langle p_T \rangle$ vs $N/\langle N \rangle$ as in p+p