



Precision measurement with ultracold atoms & molecules

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Advances in Precision tests and Experimental Gravitation in Space
Firenze, September 28, 2006

\$ Funding \$

NIST, ONR, NSF,
AFOSR, NASA, DOE



First, let there be light

Continuous wave laser: < 1 Hz stability and accuracy

Ultrafast pulse: < 1 fs generation and control

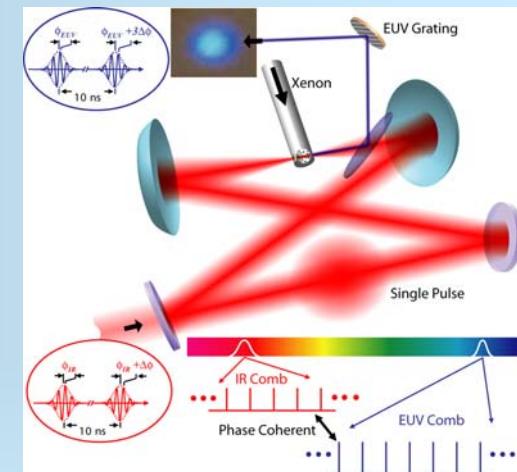
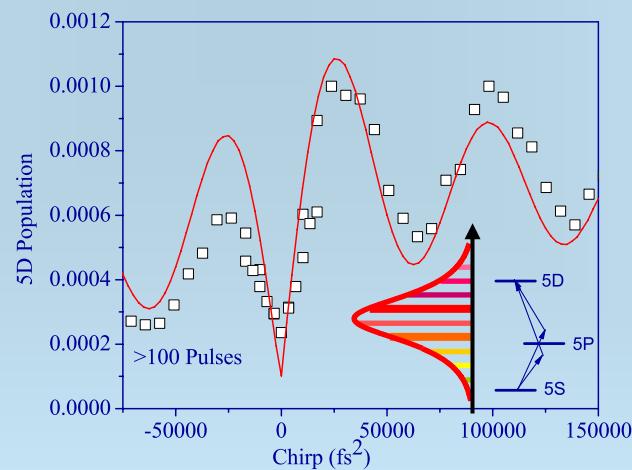
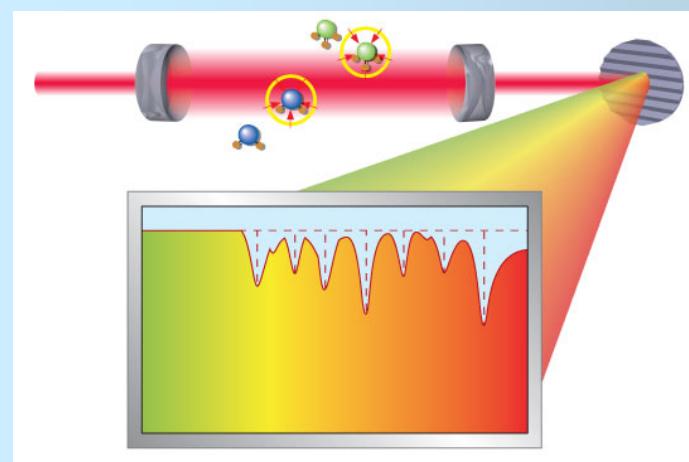
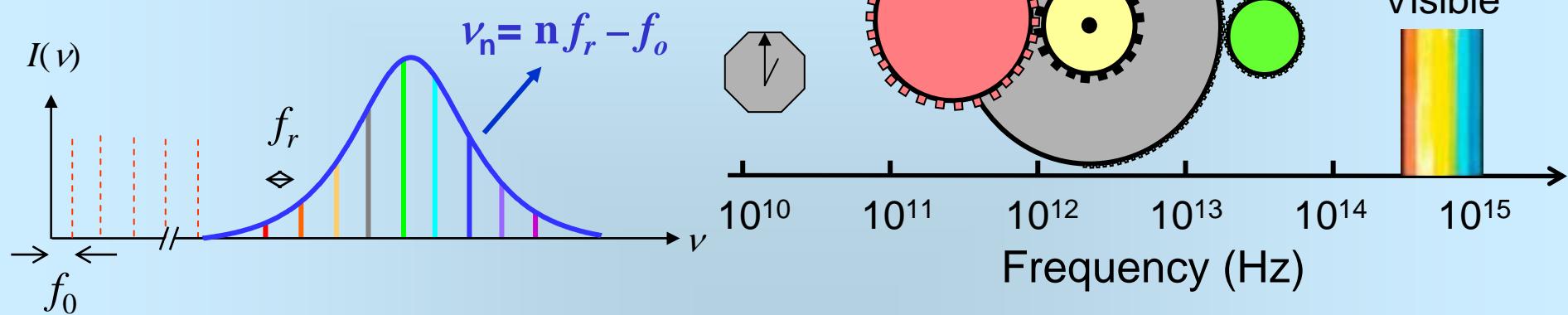
Figure of merit: 10^{-15}

Phase coherence after 10^{15} optical cycles

*Precision spectroscopy and quantum control
at highest resolution over widest optical bandwidth*

Frequency comb: state-of-the-art

- Optical Synthesizer



Quantum control

Stowe *et al.*,
PRL 96, 153001(2006).

XUV comb

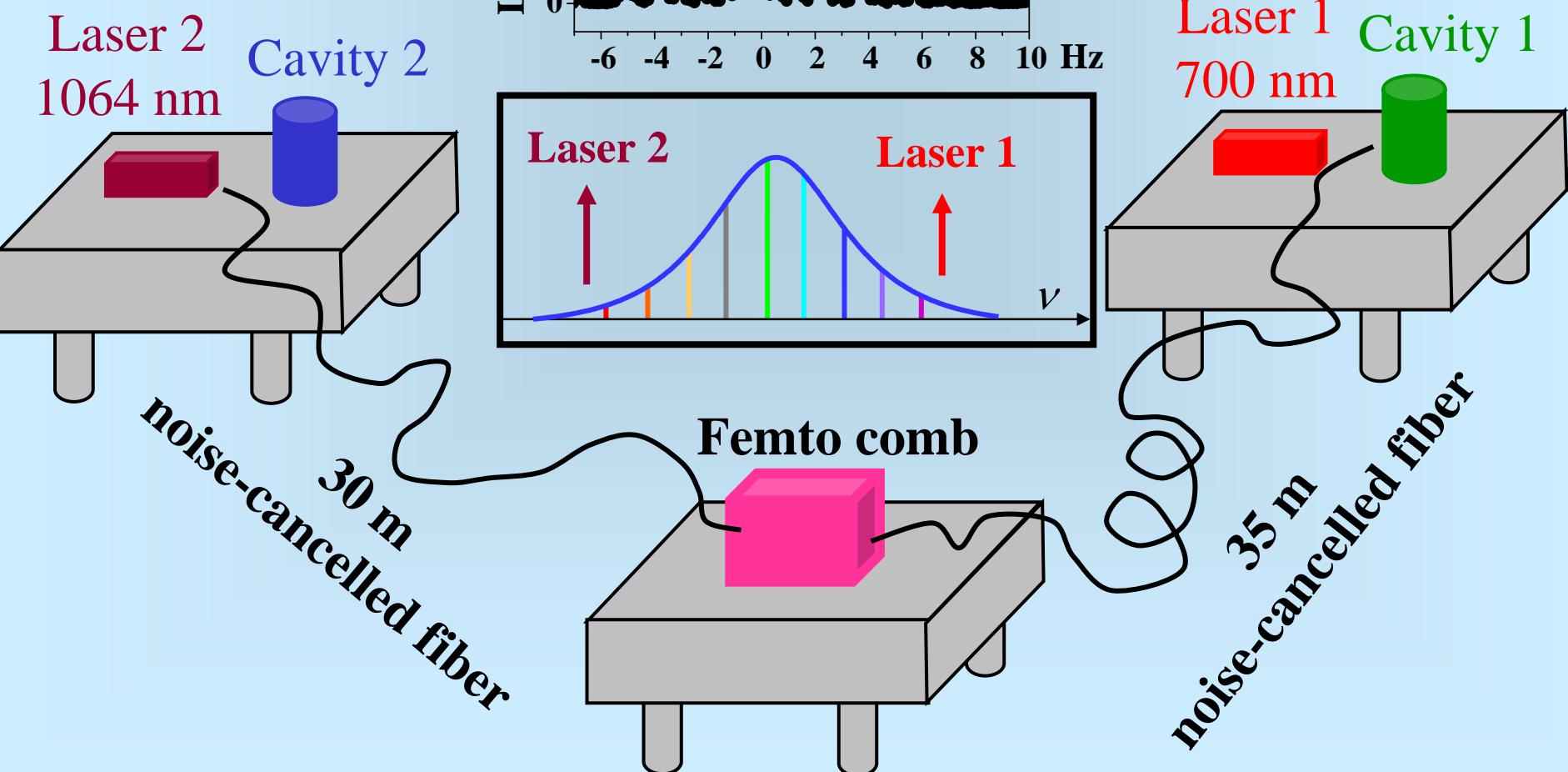
Jones *et al.*,
PRL 94, 193201 (2005).
C. Gohle *et al.*,
Nature 436, 234 (2005).

Molecular spectroscopy

Thorpe *et al.*,
Science 311, 1595 (2006).

Optical coherence > 1 s, across entire visible

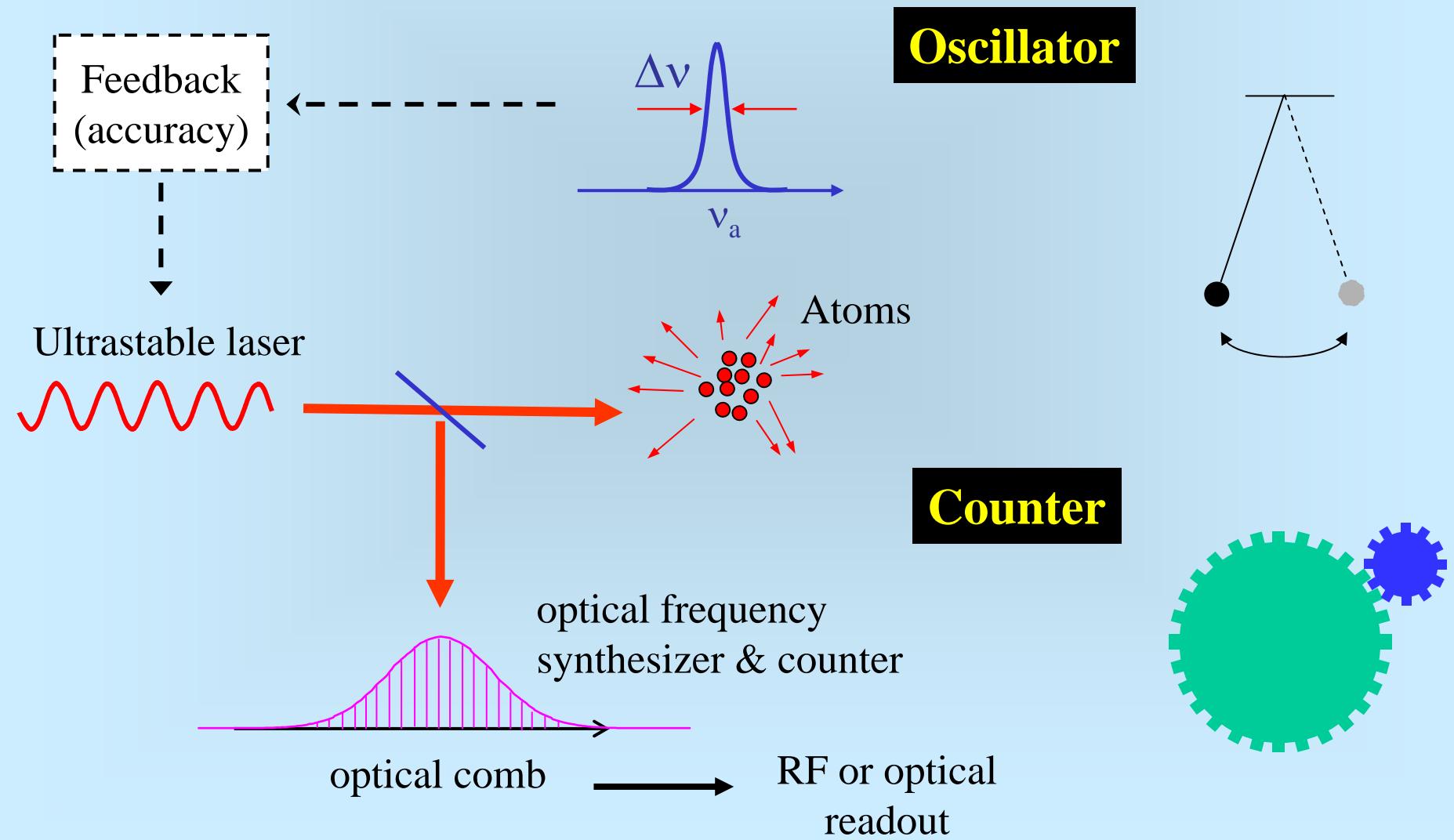
Ludlow *et al.*, PRL **96**, 033003(2006).



New era for optical atomic clocks

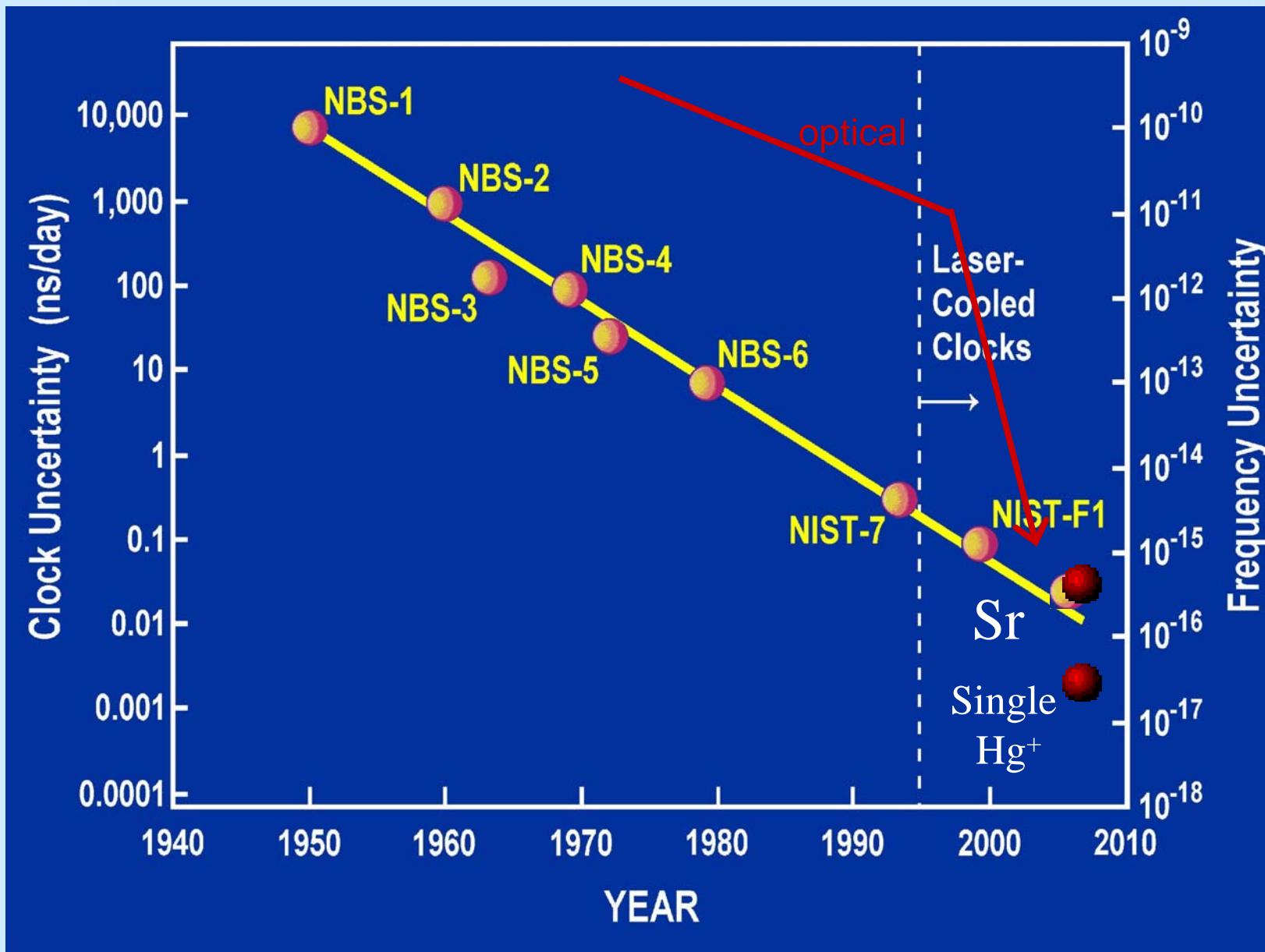
Diddams *et al.*, Science 293, 825 (2001).

Ye *et al.*, Phys. Rev. Lett. 87, 270801 (2001).



Accurate atomic clocks

Cs fountain: SYRTE, NIST, PTB, ...



Yb⁺,
Sr⁺,
Al⁺

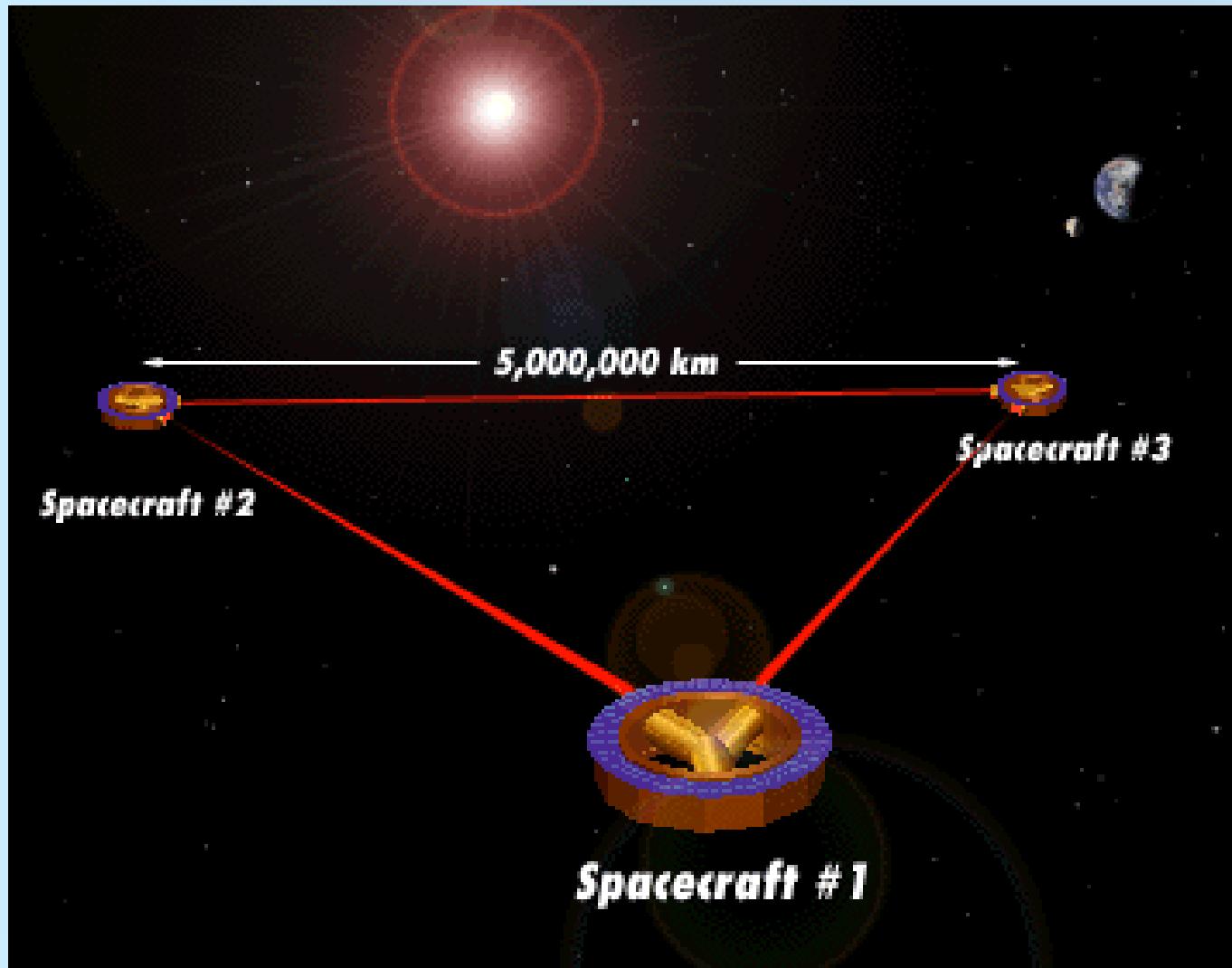
...

All in one – Space Clock and Laser Ranging

Time meets length

Ye, Opt. Lett. 29, 1153 (2004).

Space based interferometer Courtesy of P. Bender



+

Inertial
Sensor

Prof. G. Tino
PRL 2006

Control of matter

- Learning from ion trappers

Long - term quantum coherence:

Clean separation between internal & external degrees of freedom

Both in well defined quantum states

Magic wavelength dipole trap

Trapping of Single Atoms in Cavity QED

Ye, Vernooy & Kimble, Phys. Rev. Lett. 83, 4987 (1999).

that a judicious choice of λ_{FORT} can eliminate both of these problems by making $\Delta_{\text{FORT}}^e(\vec{r}) = \Delta_{\text{FORT}}^g(\vec{r}) < 0$, and hence $\Delta_{\text{FORT}}(\vec{r}) = 0$ [24]. Alternatively, even for the

the capabilities presented in this Letter should allow us to achieve atomic confinement in the Lamb-Dicke regime (i.e., $\eta_x \equiv 2\pi\Delta x/\lambda \ll 1$) in a setting for which the trapping potential for the atomic center-of-mass motion is independent of internal atomic state, as has been so powerfully exploited with trapped ions [25]. Generally

For clocks:

Katori *et al.*, Katori et al., J. Phys. Soc. Jpn 68, 2429 (1999)

6th Symp. Freq. Standards & Metrology (2002);
Phys. Rev. Lett. 91, 173005 (2003).

Cool Alkaline Earth – Strontium

JILA work: Phys.Rev.Lett. 90, 193002 (2003); Phys.Rev.Lett. 93, 073003 (2004);

Phys.Rev.Lett. 94, 153001 (2005); Phys.Rev.Lett. 94, 173002 (2005);

Phys.Rev.Lett. 96, 033003 (2006); Phys.Rev.Lett. 96, 203201 (2006).

$T \sim 0.5$ photon recoil
 ~ 220 nK

$\Delta\nu$ $\delta\nu/\nu_0$ at 1s

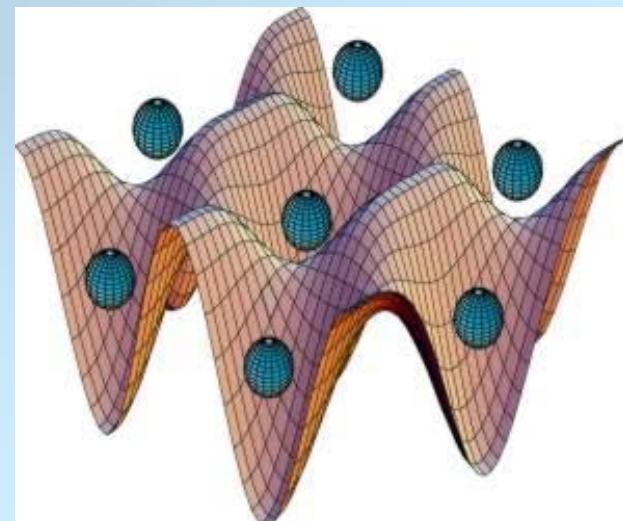
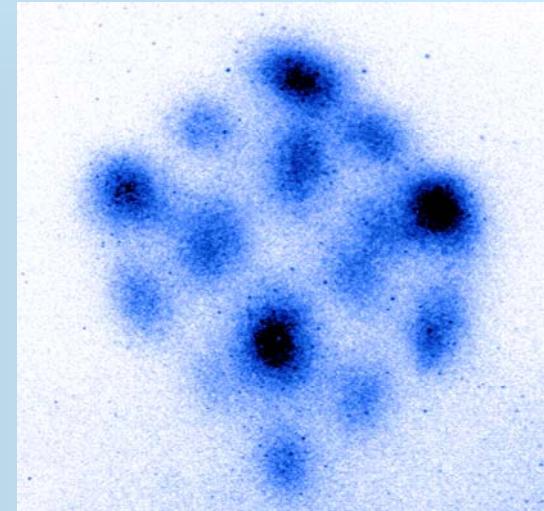
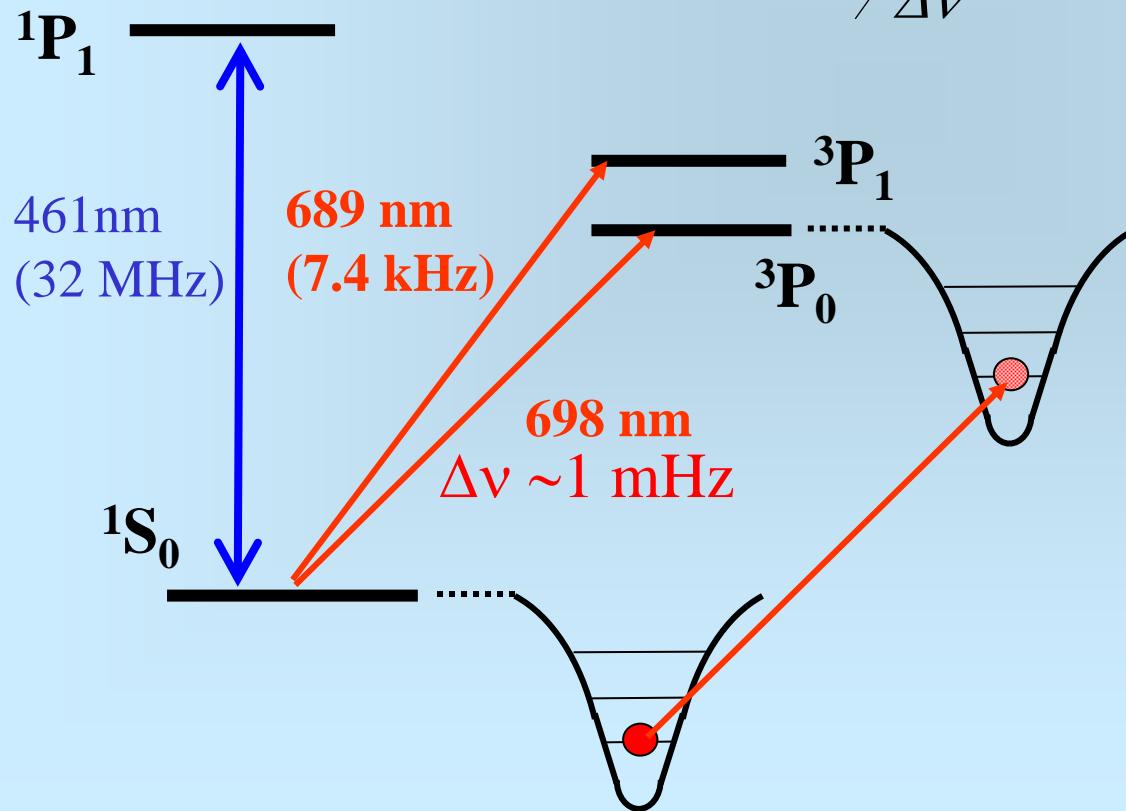
^{87}Sr $^1\text{S}_0$ - $^3\text{P}_0$

~ 1 mHz

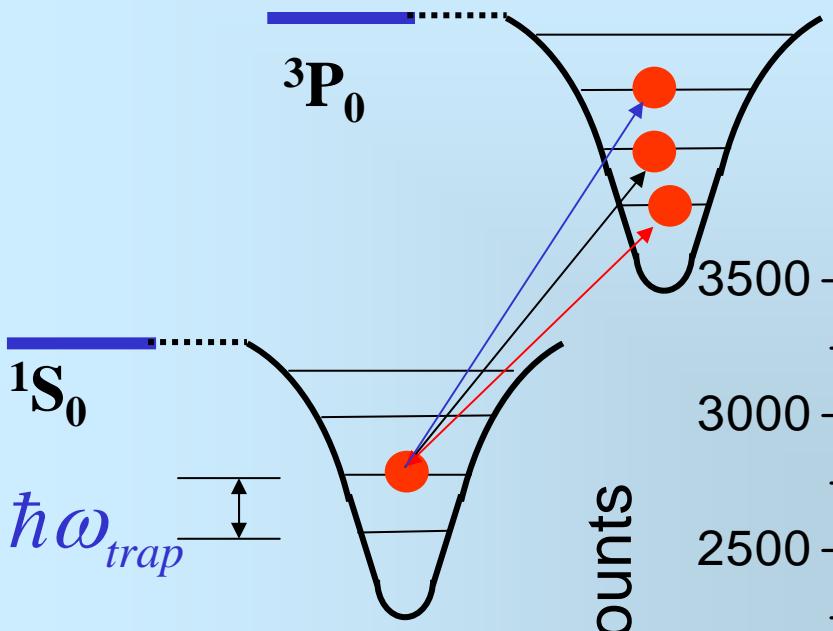
$\sim 10^{-18}$

$$\frac{\delta\nu_{noise}}{\nu_0} \approx \frac{1}{Q} \cdot \frac{1}{S/N} \cdot \frac{1}{\sqrt{\tau}}$$

$$Q \approx \nu_0 / \Delta\nu$$



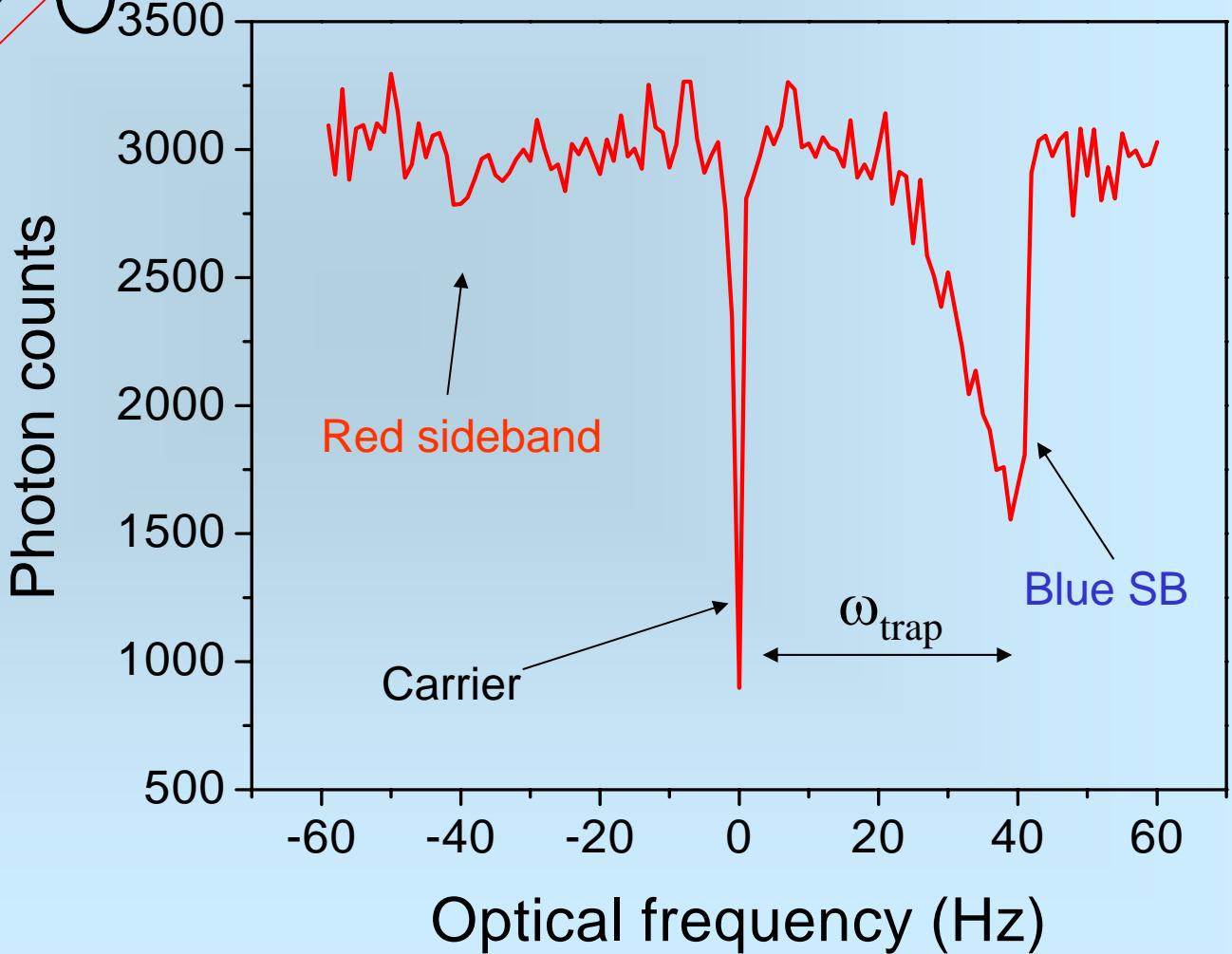
Spectroscopy at the magic wavelength



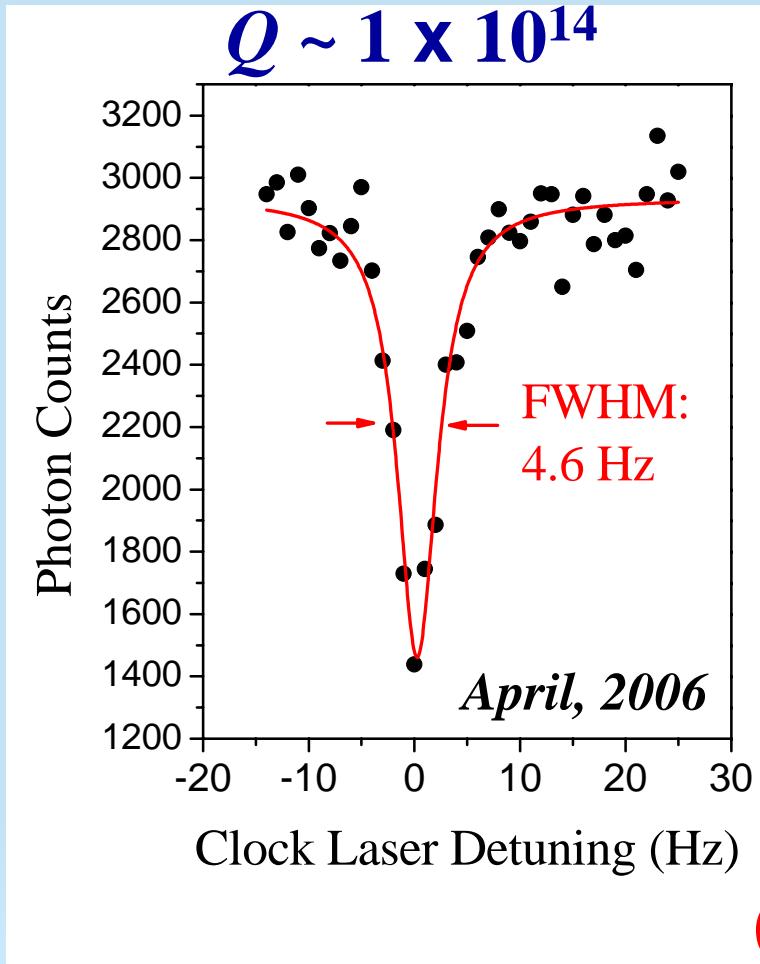
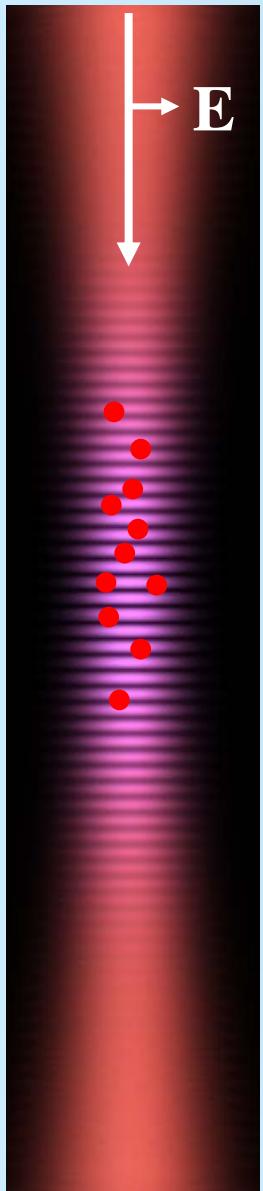
$$\omega_{recoil} \ll \omega_{trap}$$

$$\Gamma_{clock} \ll \omega_{trap}$$

1-D Lamb-Dicke Regime
 $\eta = kx_0 = (\omega_{recoil} / \omega_z)^{0.5} \sim 0.23$



Zoom into the carrier of ^{87}Sr ${}^1\text{S}_0 - {}^3\text{P}_0$

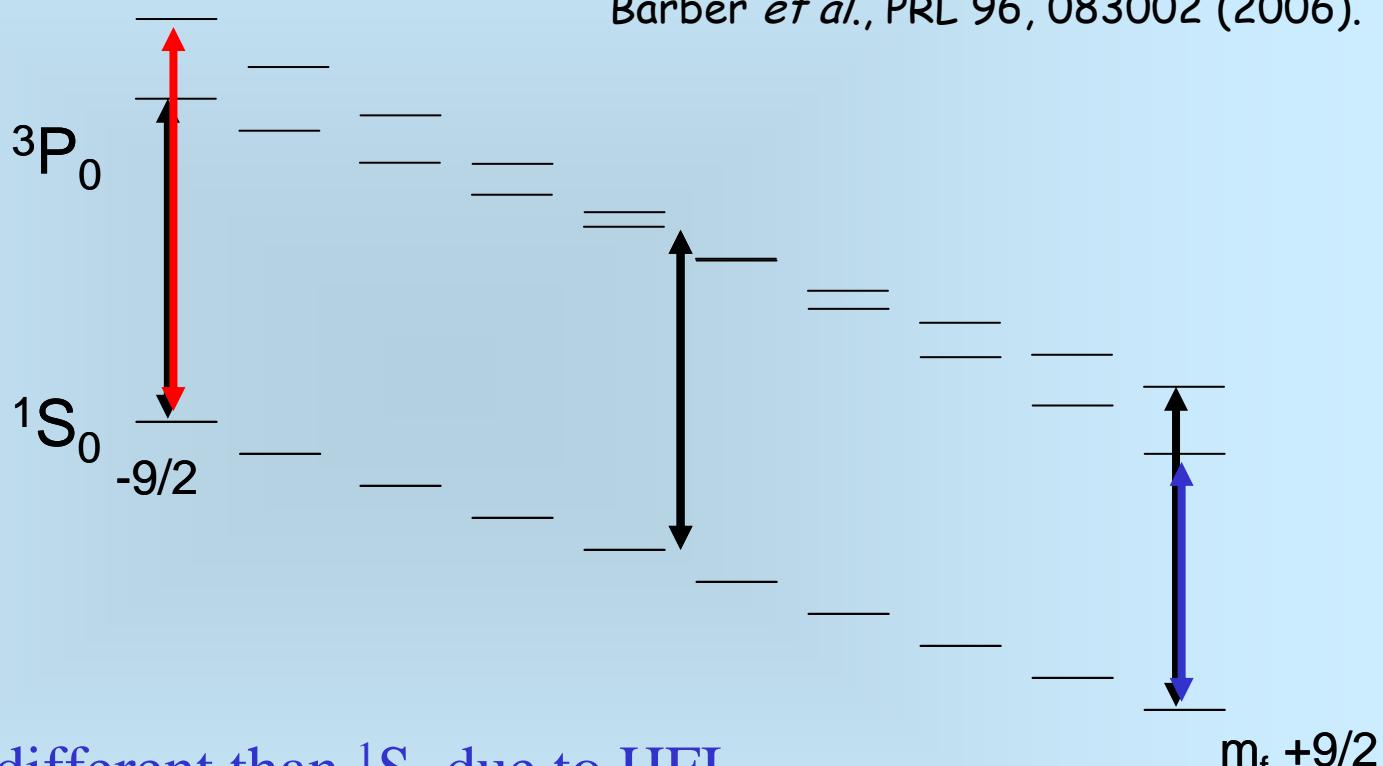
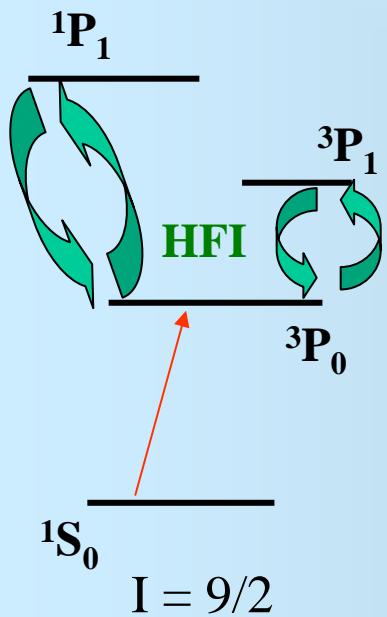


Single trace without averaging

Projected stability
 $< 1 \times 10^{-15}$ at 1 s

Reproducibility
 $\sim 6 \times 10^{-16}$
(March – September,
2006)

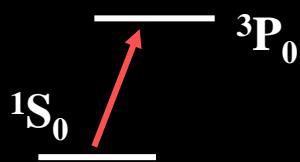
Differential g-factor – Tensor polarizability



Proposals based on Bosons:
Santra *et al.*, PRL 94, 173002 (2005).
Hong *et al.*, PRL 94, 050801 (2005).
Barber *et al.*, PRL 96, 083002 (2006).

- 3P_0 g-factor different than 1S_0 due to HFI
- Shift of $\sim 110 \times m_F$ Hz/Gauss for $\Delta m_F = 0$
- State preparation, field control
- HF structure introduces slight lattice polarization sensitivity

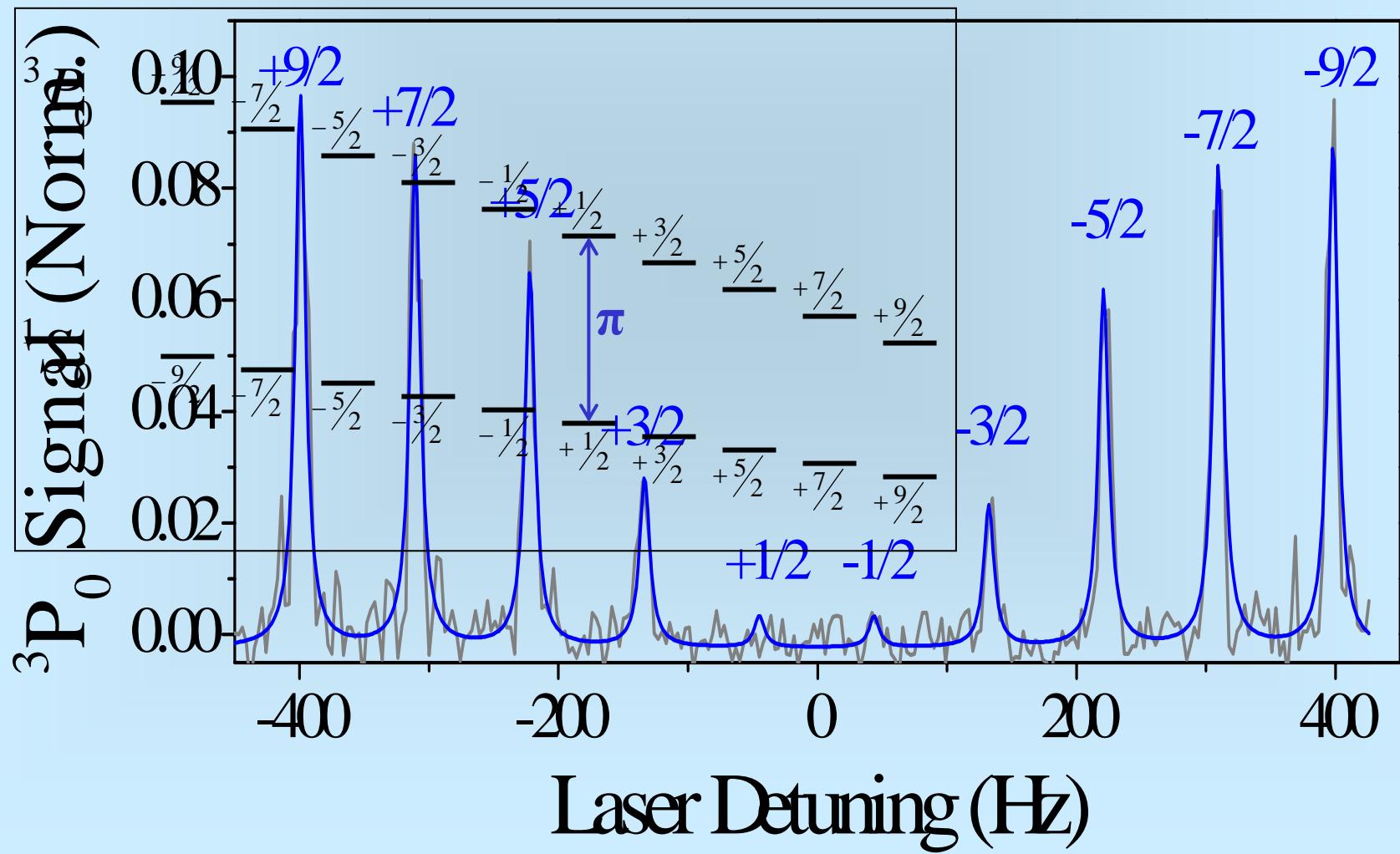
Optical Measurement of Nuclear g-factor



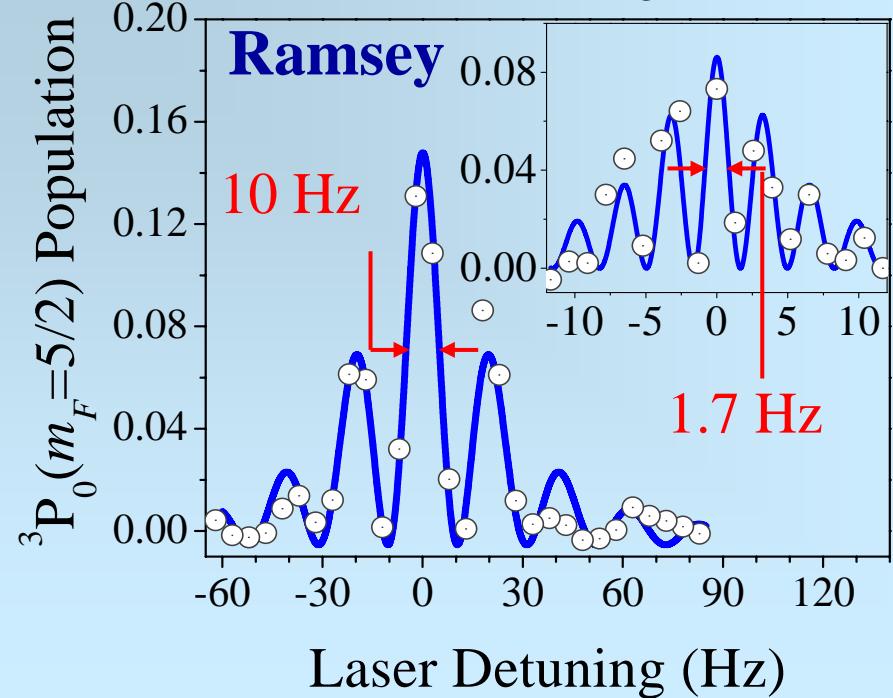
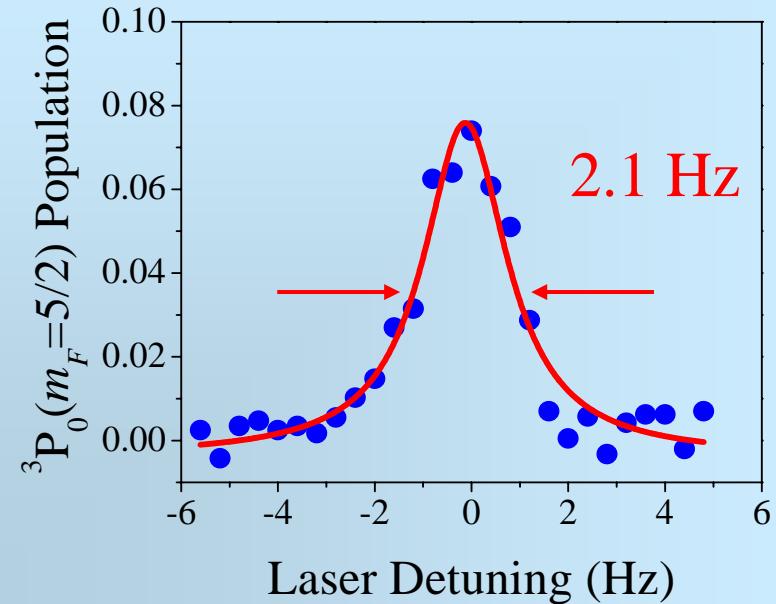
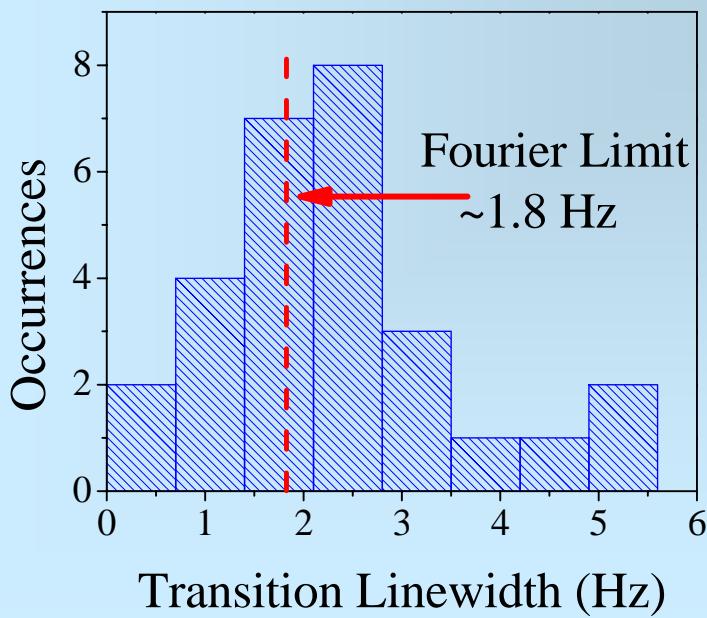
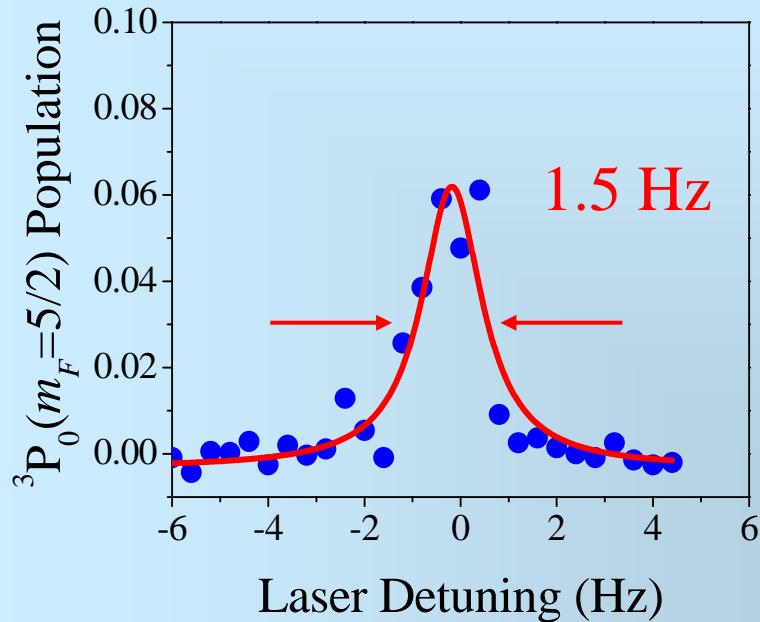
No net electronic angular momentum

$$\Delta g = -108.5(4) \text{ Hz/(G m}_\text{E}\text{)}$$

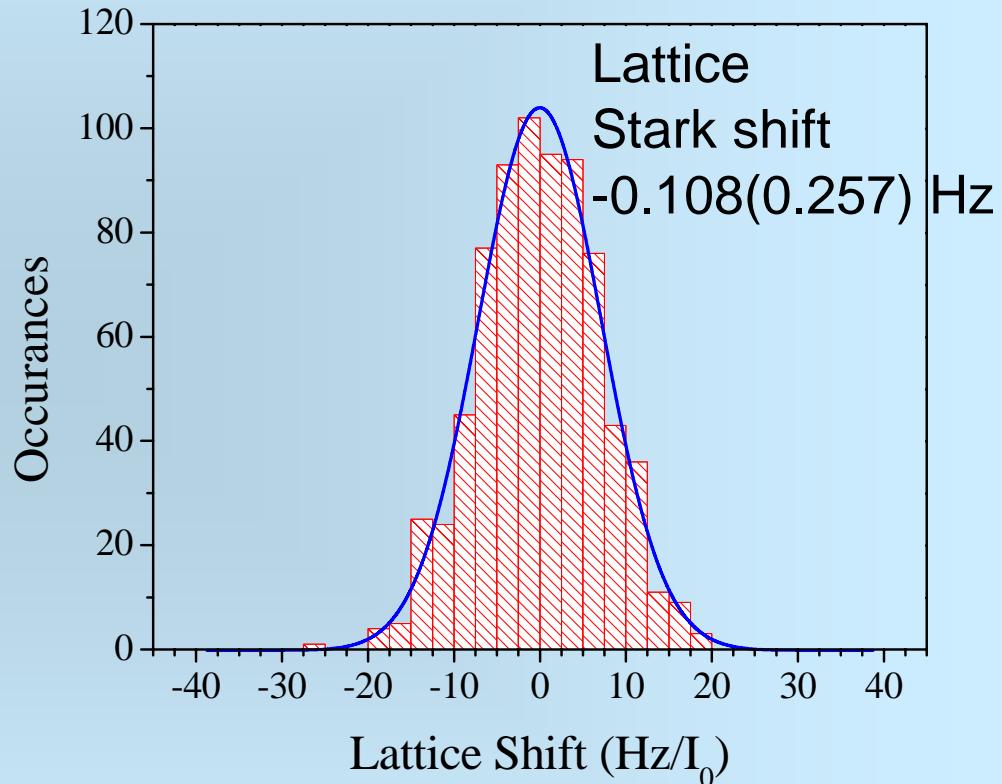
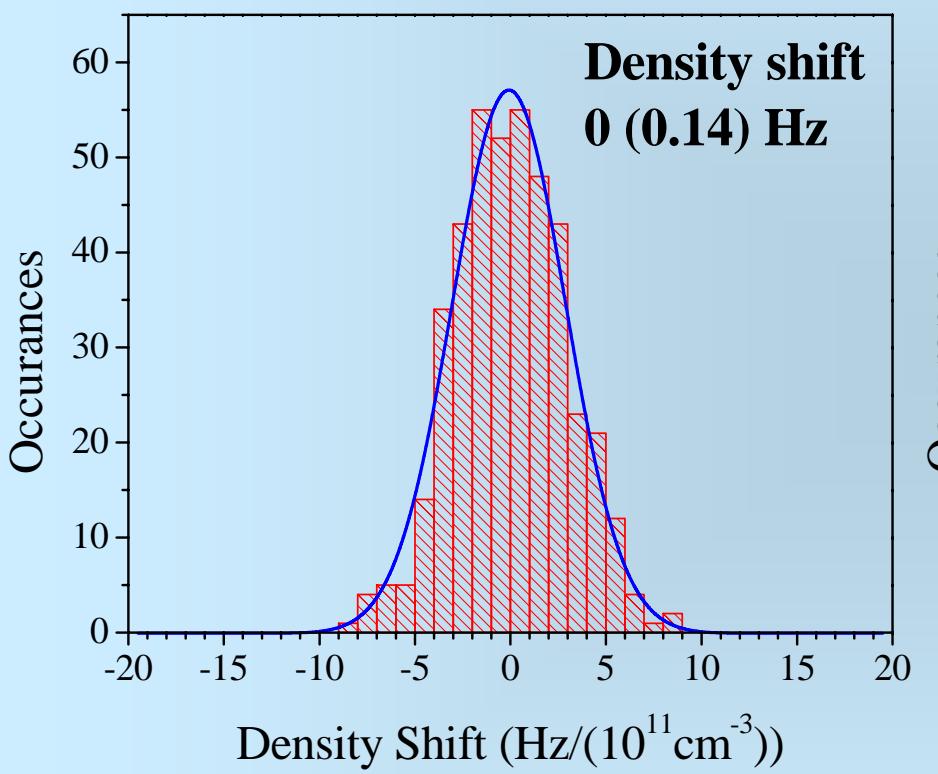
3P_0 lifetime 140(40) s



Coherent spectroscopy $Q \sim 3 \times 10^{14}$



Understanding systematics: Collision shift and Lattice AC Stark shift



Total uncertainty 0.29 Hz → 6.7 × 10⁻¹⁶

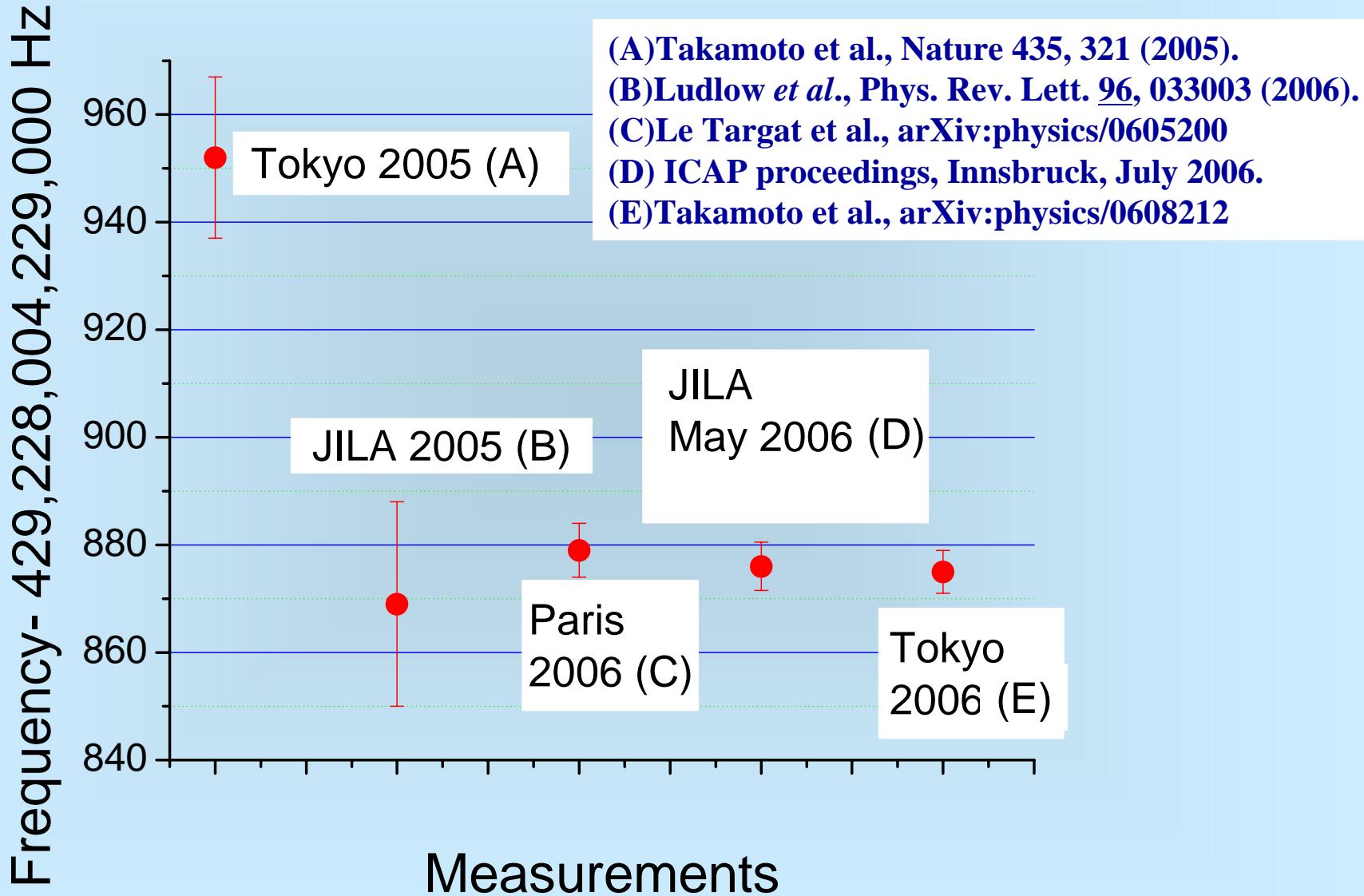
Systematic uncertainty evaluations

Zeeman shift,	0.10 Hz,	2.3 E-16
Lattice AC Stark,	0.26 Hz,	6.0 E-16
Atom density shift,	0.14 Hz,	3.3 E-16
Probe AC Stark,	0.05 Hz,	1.0 E-16
Blackbody	0.03 Hz	0.7 E-16
<i>Systematic Total</i>	<i>0.39 Hz</i>	<i>7.3 E-16</i>

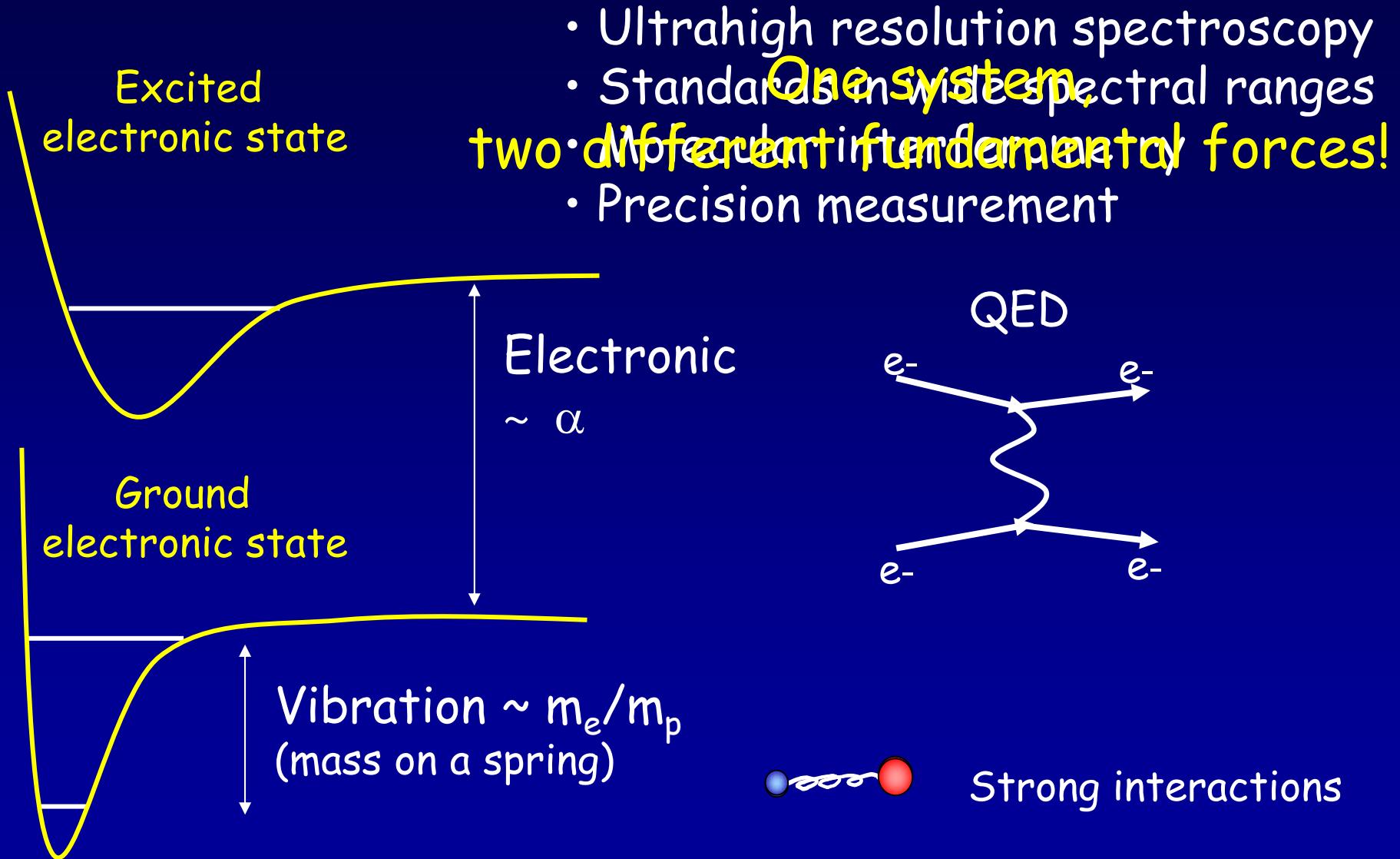
For Absolute frequency measurement against Cs:

Gravitational shift	3.0 E-16
Counting statistics	6.0 E-16
NIST Maser calibration	2.0 E-15 
<i>Measurement uncertainty Total</i>	<i>2.2 E-15</i>

Agreement among Boulder, Paris, and Tokyo



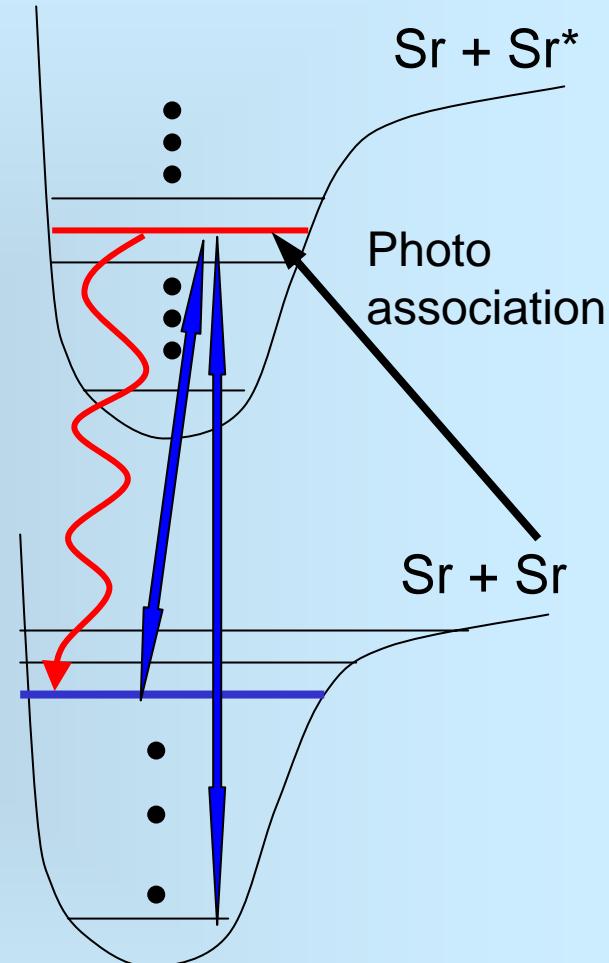
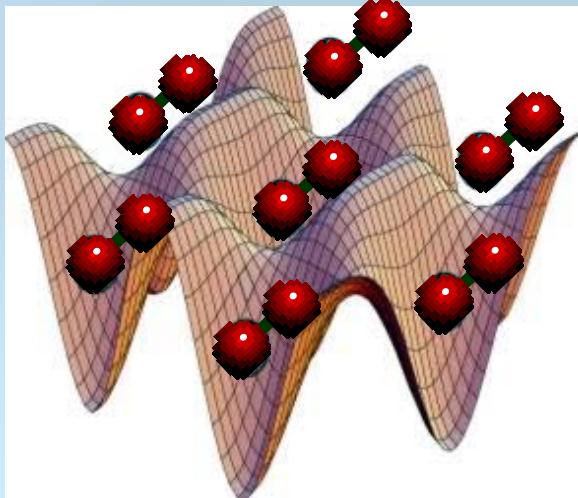
Ultracold molecules: Test fundamental principles



Ultracold Sr_2 Molecules in Lattice

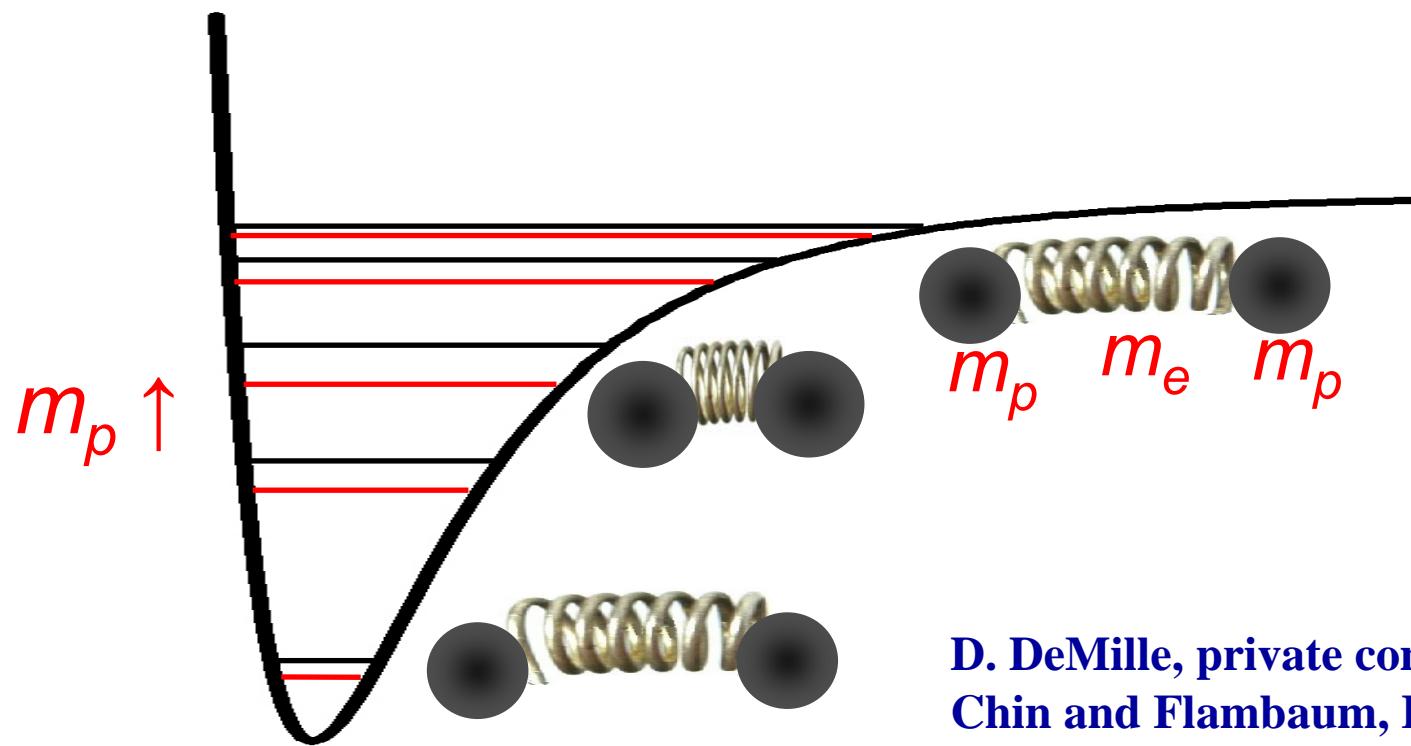
- Narrow lines
 - Favorable decay to electronic ground state
- Structureless ground state
 - Small branching ratio losses

Raman transition for ground state production



Molecular Clock – Sensitivity to Mass Ratio

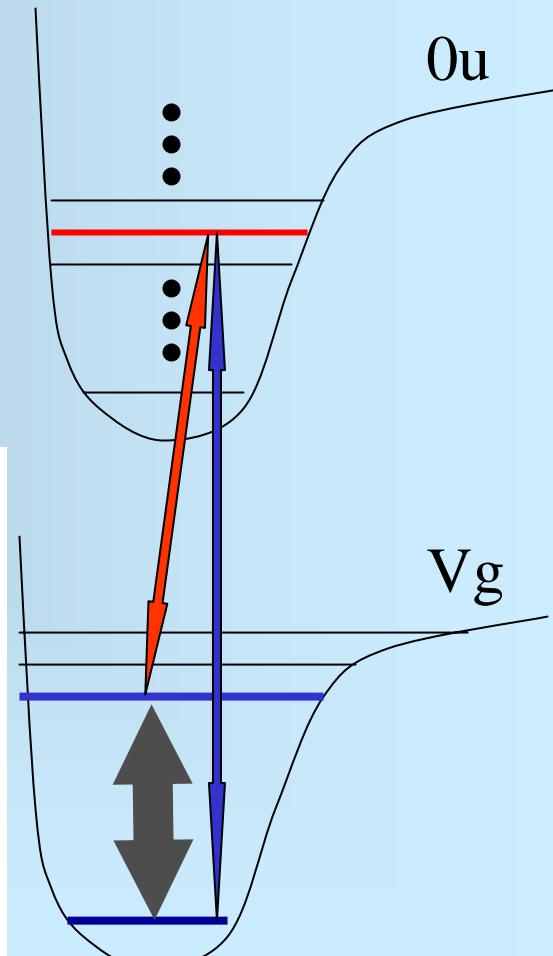
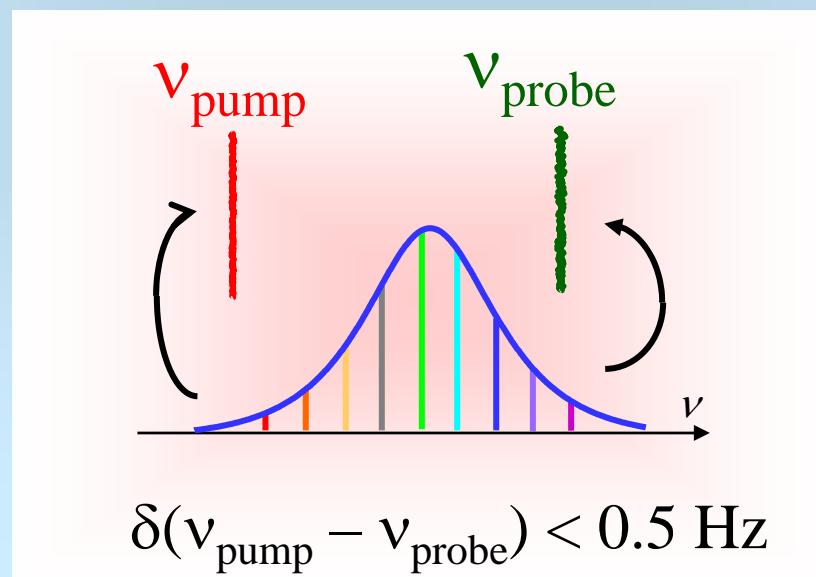
- Molecular potentials depend on electron mass, m_e
 - Kinetic energy depends on proton mass, m_p
 - Vibrational spacings depend on m_p / m_e
- Precision tests of time variation of m_p / m_e ?



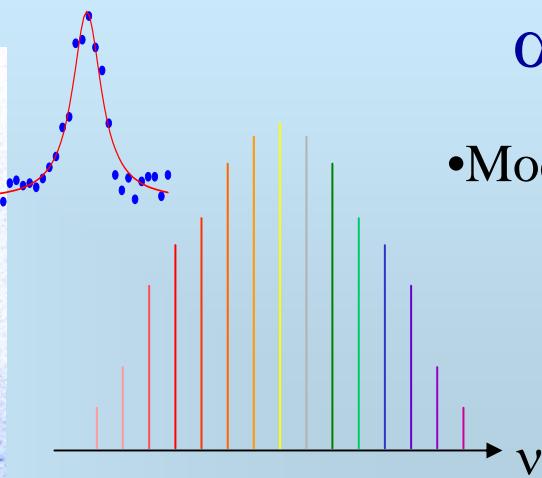
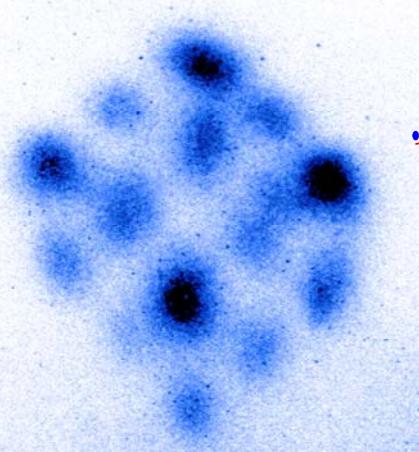
D. DeMille, private communications (2005).
Chin and Flambaum, PRL 96, 230801 (2006).
S. Schiller, molecular ions

Mass ratio tests

- Homonuclear molecules are best
- Relative Raman frequency measurement 0.3 Hz (fs comb), potential depth 3×10^{13} Hz $\rightarrow 1 \times 10^{-14}$
- Atomic clocks:
 6×10^{-15} / year, but model-dependent,
mainly QED effects

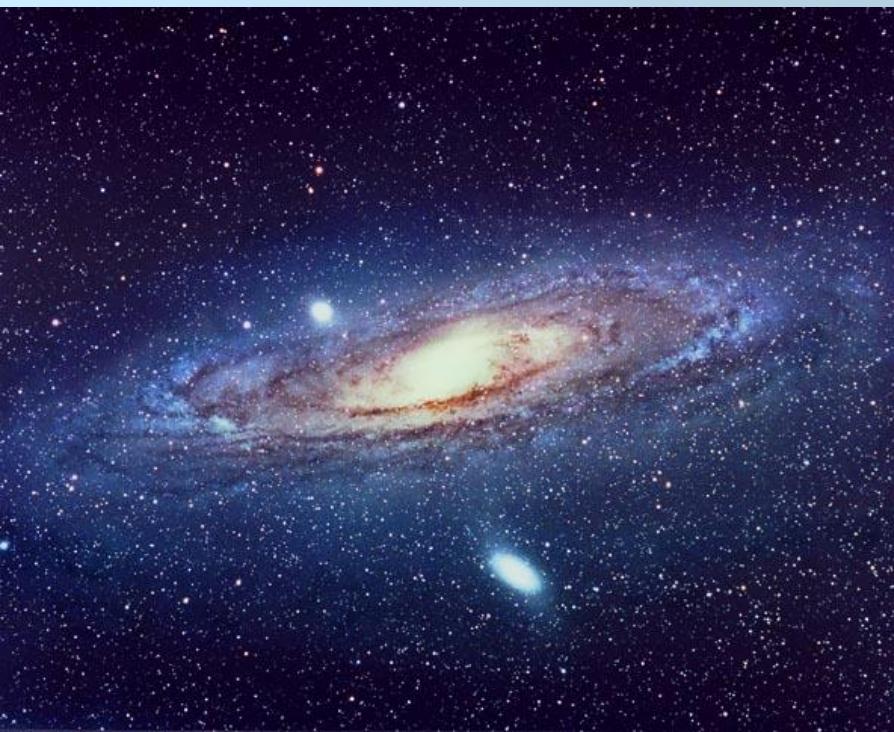


Test of fundamental constants

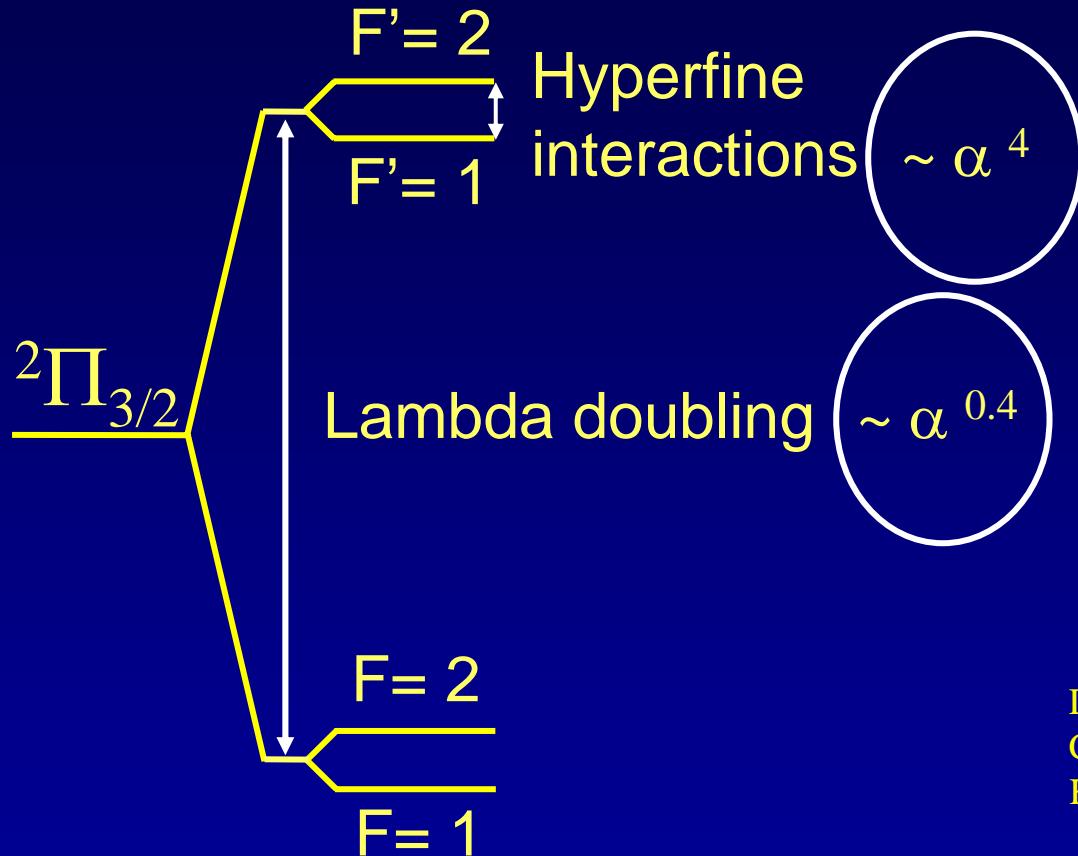


α : fine structure constant

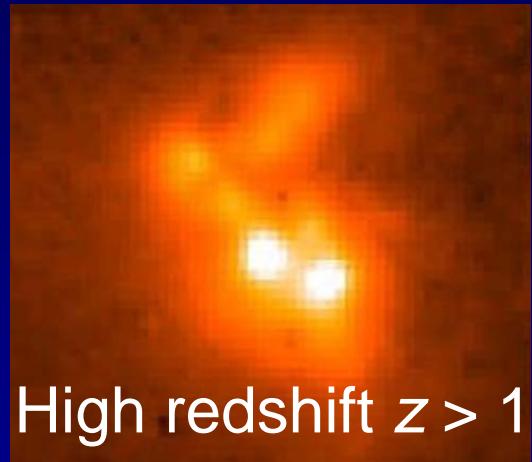
- Modern epoch
 - Atomic clock measurements are consistent with zero
 $\Delta\alpha/\alpha < 10^{-15}/\text{yr}$
- Early universe
 - Not so clear...
Webb *et al.*, PRL 87, 091301 (2001).
Astron. Astrophys. 415, L7 (2004).
– Conflicting results



Cold OH molecules to constrain $\dot{\alpha}$



OH megamasers



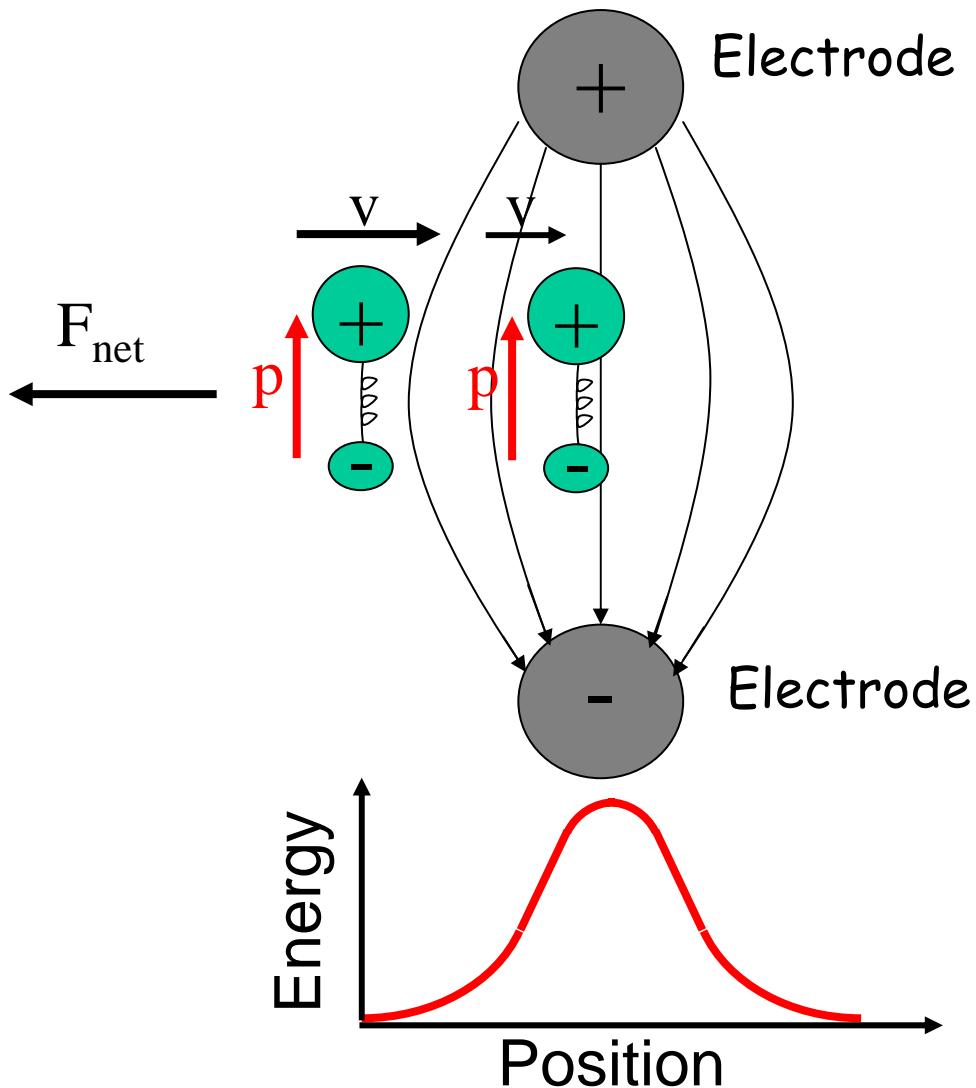
Darling, Phys. Rev. Lett **91**, 011301 (2003).
Chengalur *et al.*, Phys. Rev. Lett. **91**, 241302 (2003).
Kanekar *et al.*, Phys. Rev. Lett. **93**, 051302 (2004).

Multiple transitions from the same gas cloud (different dependences on α)
(Self check on systematics)

Current uncertainty in laboratory based experiments is 100 Hz,
leading to $\Delta\alpha/\alpha \sim 10^{-5}$

Stark deceleration

Direct manipulation of ground state molecules



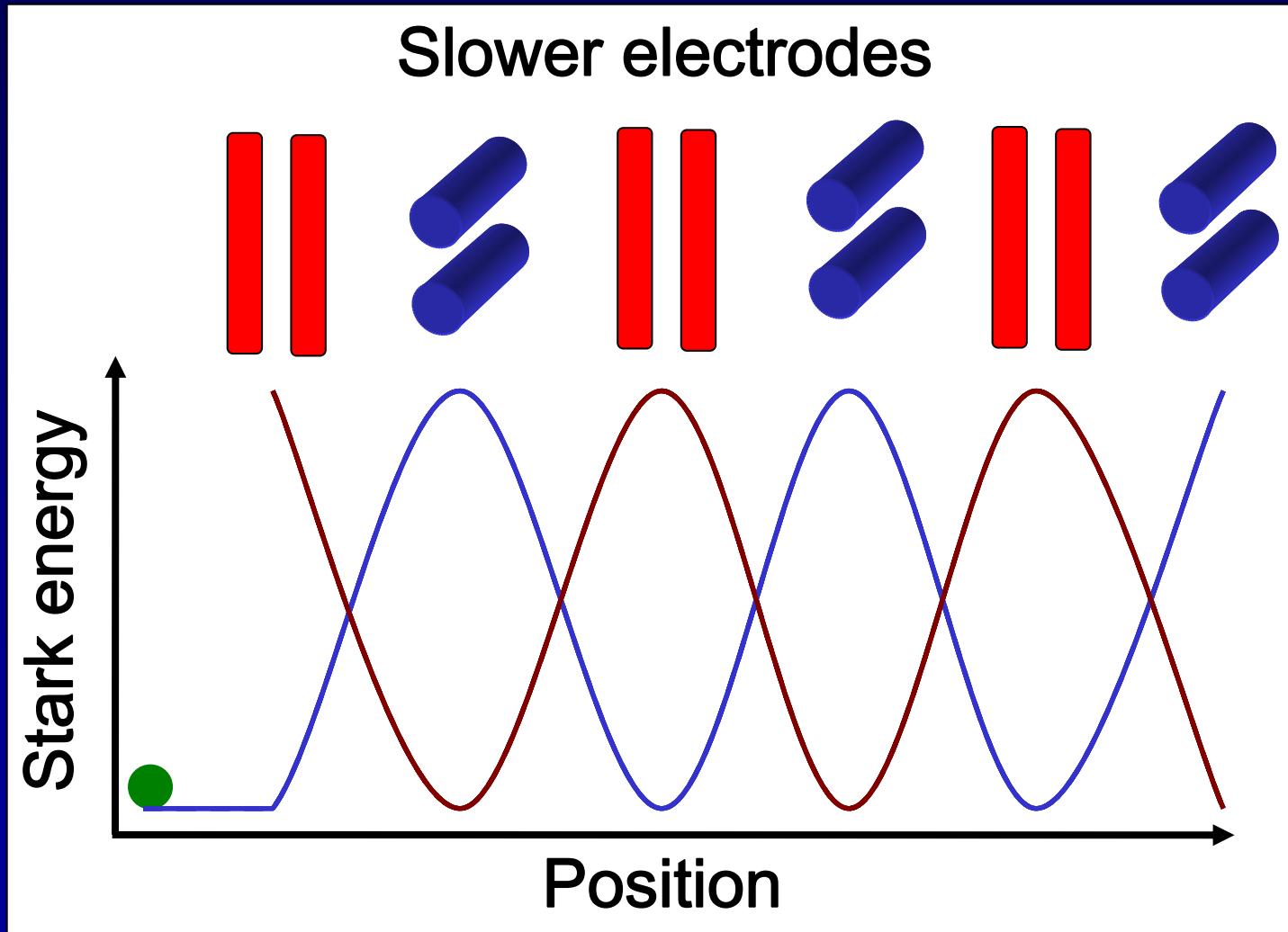
Initial cooling important
(supersonic jets: single internal quantum state; external temp. ~ 1 K in a moving frame)

Phase space selection (~ 10 mK)

Applicable to a large variety
of polar molecules

Bethlem, Berden, Meijer,
Phys. Rev. Lett. 83 1558 (1999).

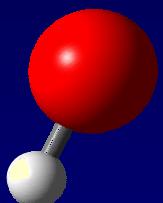
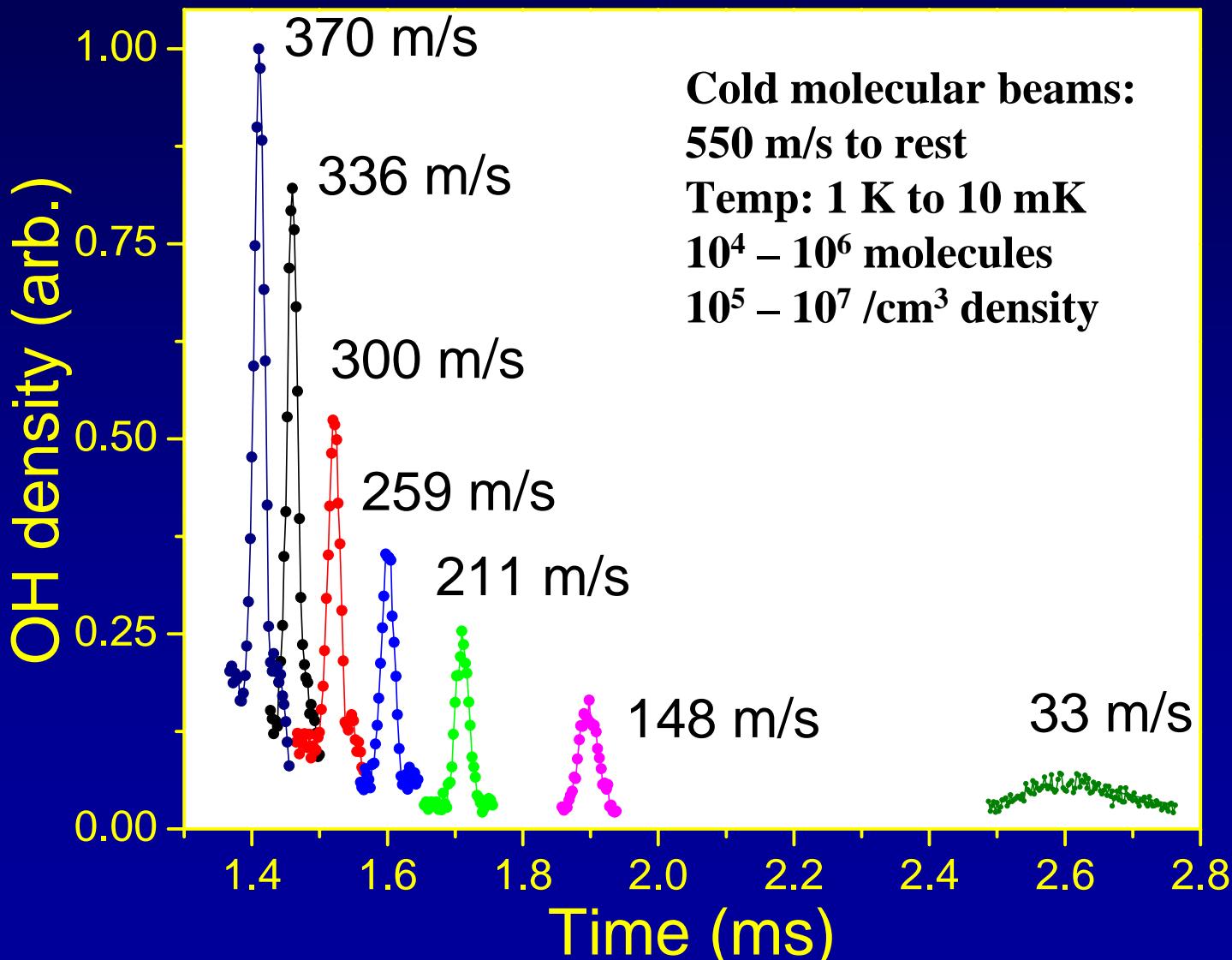
Stark Decelerator



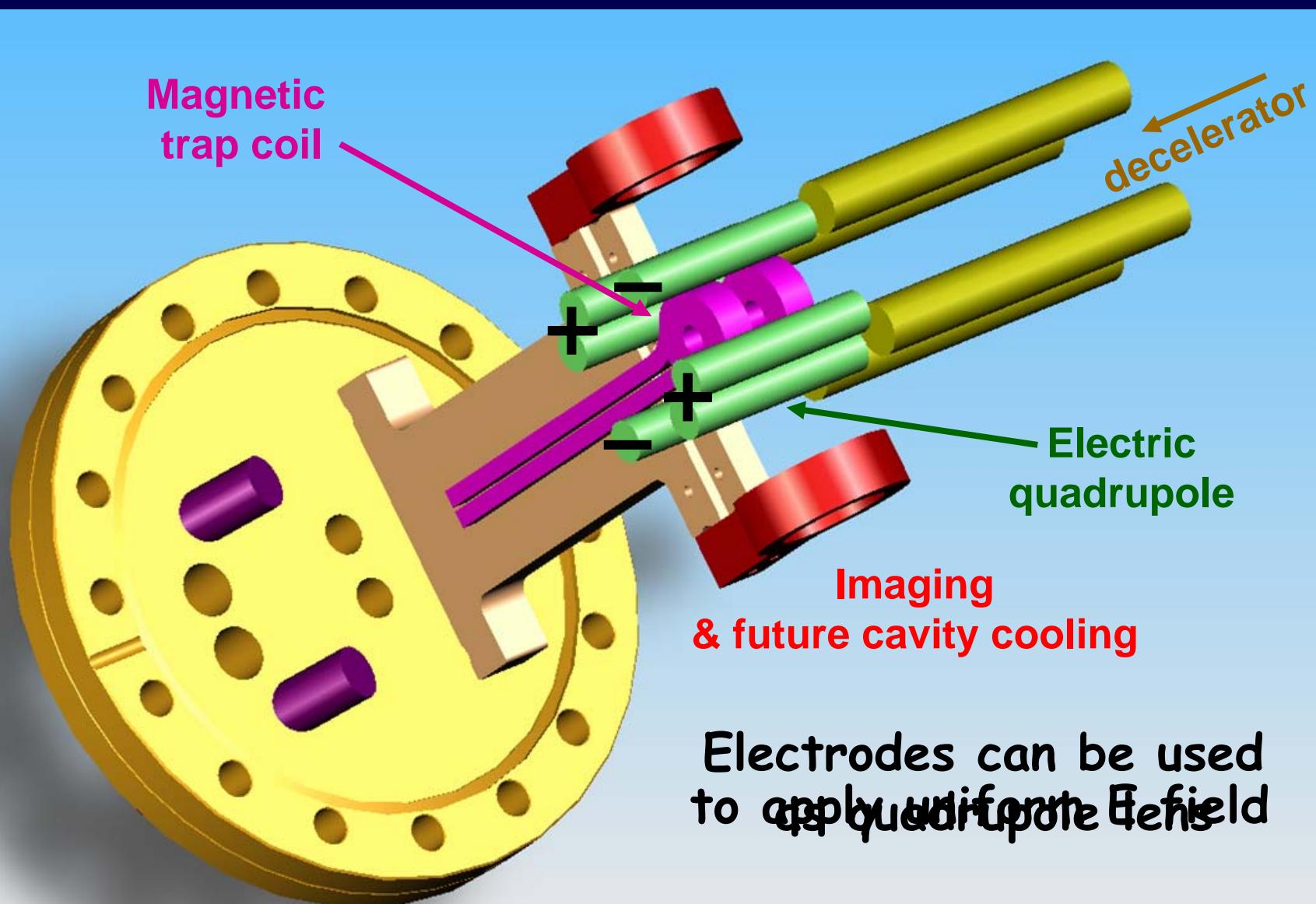
Cold OH molecules

Bochinski *et al.*, Phys. Rev. Lett. **91**, 243001 (2003).

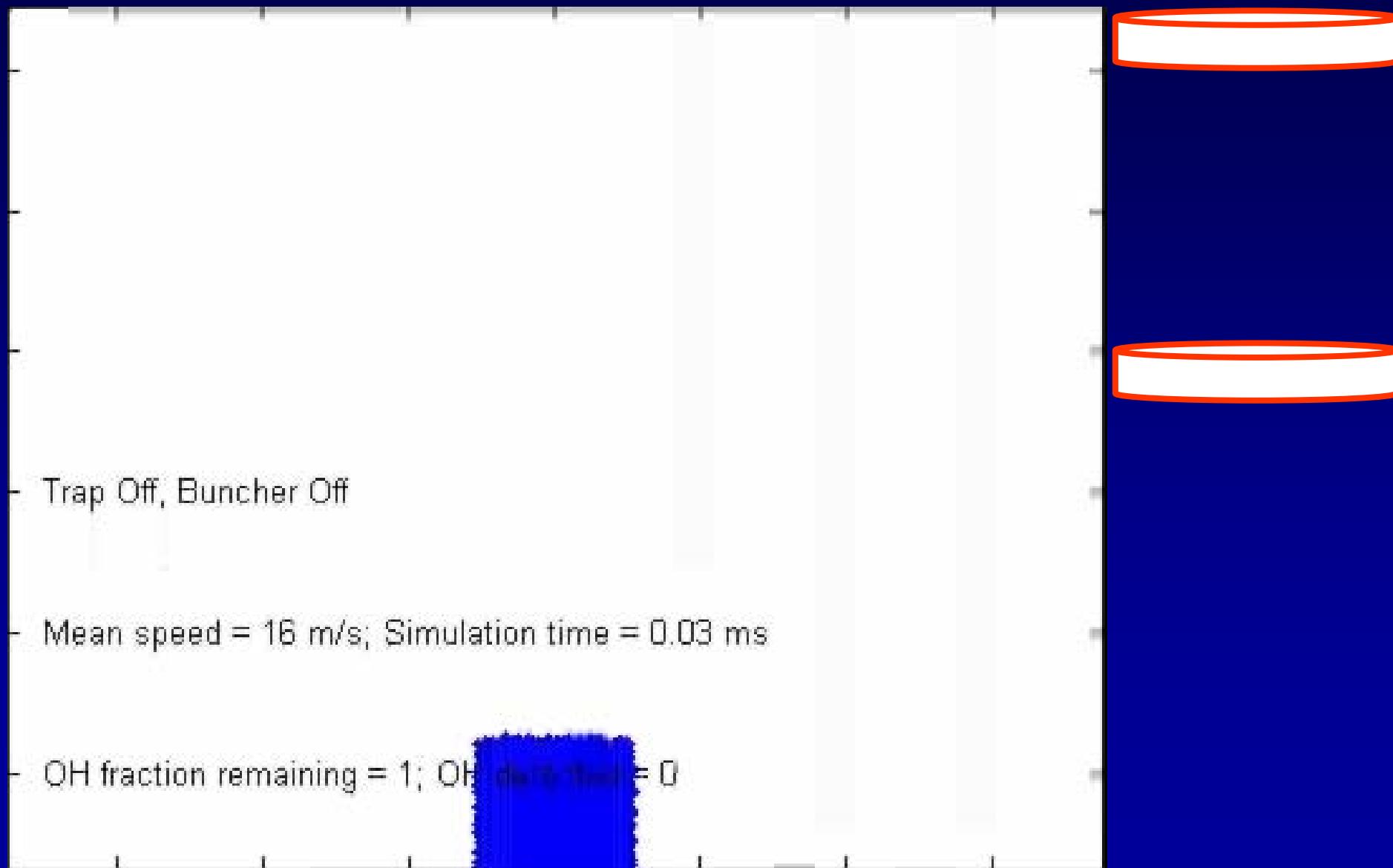
Bochinski *et al.*, Phys. Rev. A **70**, 043410 (2004).



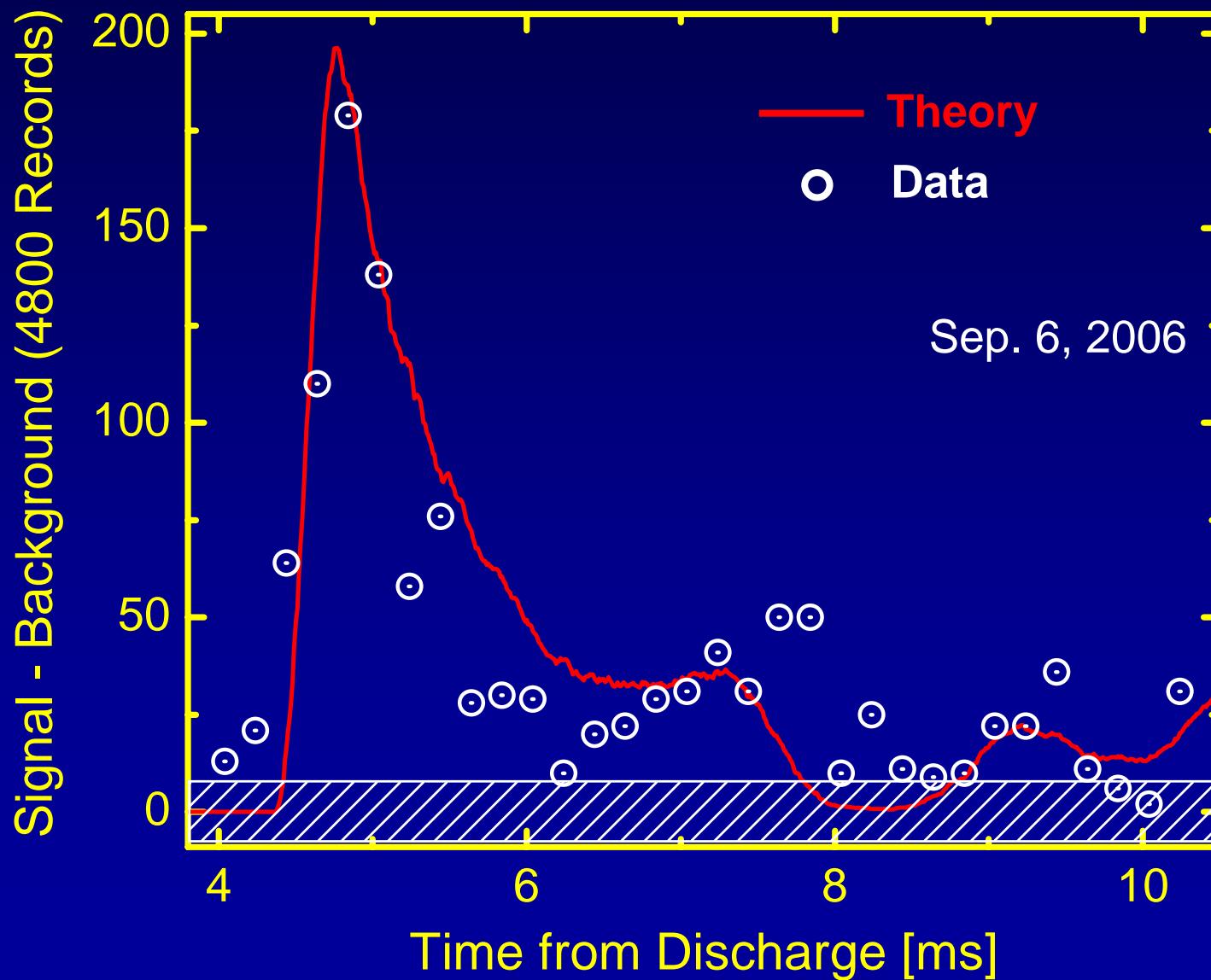
Magnetic trapping of OH



Magnetic trapping of OH



Magnetic trapping of OH



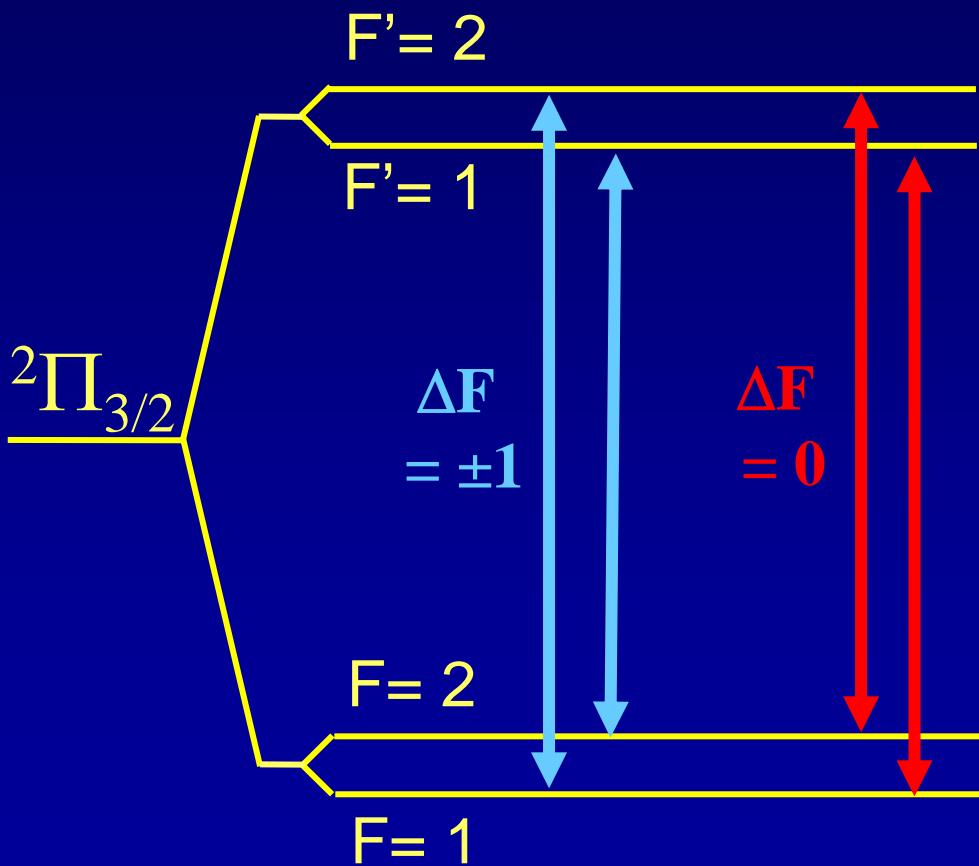
Precision measurement of OH ground structure

Measurement accuracy for all four lines: 4 - 10 Hz ($\times 10$ improvement)

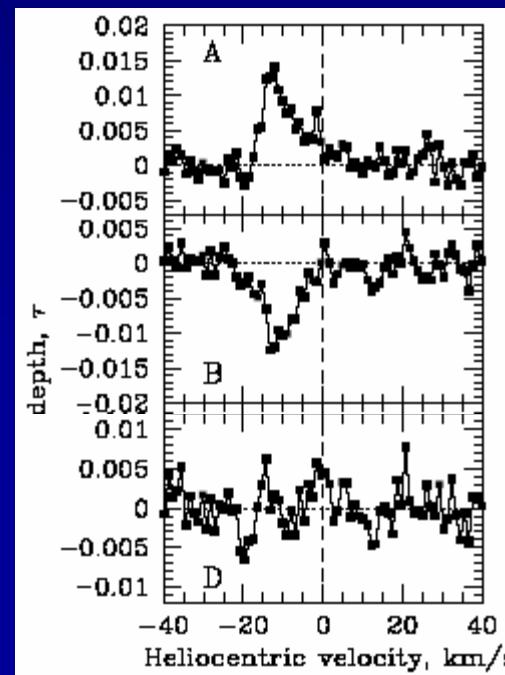
Hudson *et al.*, Phys. Rev. Lett. 96, 143004 (2006).

Lev *et al.*, arXiv:physics/0608194, August 2006.

- SUM (2 satellites)
= SUM (2 main lines)
- Satellites calibrate B
- Observed satellites conjugate



Kanekar *et al.*,
PRL 93, 051302
(2004).



What about space?

Possible sources of error: Solutions:

- EM fields in space **Main lines versus satellite lines**
- Varying Doppler effects for different lines **Emission and conjugate absorption**
OH sum rule

Astrophysical measurements coming under 100 Hz accuracy.

Deep surveys of OH megamasers are active from the local Universe to red shift $z \sim 4$.

Tests on $\Delta\alpha / \alpha$ and $\Delta\beta / \beta$ ($\beta = m_e/m_p$) at 1 ppm over 10^{10} yr.

Special thanks

<http://jilawww.colorado.edu/YeLabs>

Ultracold Sr & Sr₂

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M. Stowe
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